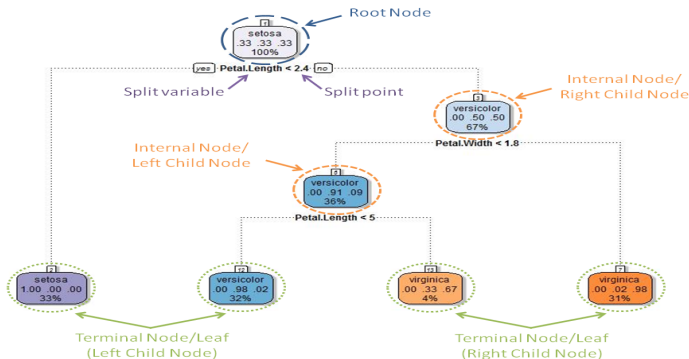


# **Introduction to Machine Learning**

## **Classification and Regression Trees (CART): Basics**

[compstat-lmu.github.io/lecture\\_i2ml](https://compstat-lmu.github.io/lecture_i2ml)

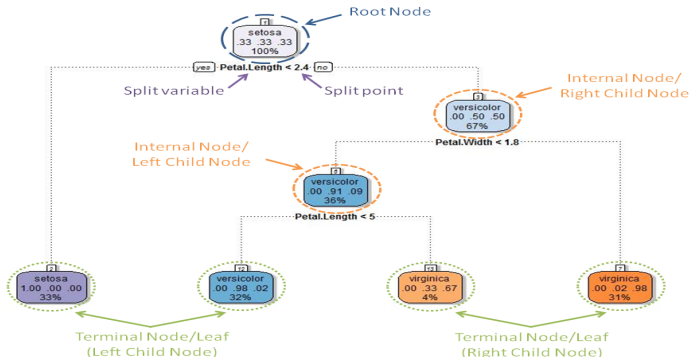
# TREE MODEL AND PREDICTION



- Classification and Regression Trees, introduced by Breiman
- Binary splits are constructed top-down
- Constant prediction in each terminal node (leaf): either a numerical value, a class label or a probability vector over class labels.

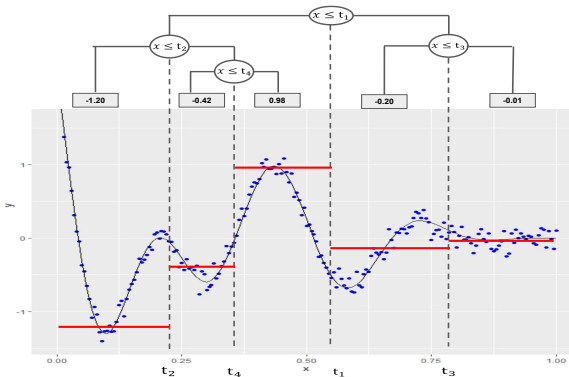
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- For predictions, observations are passed down the tree, according to the splitting rules in each node
- An observation will end up in exactly one leaf node
- All observations in a leaf node are assigned the same prediction for the target



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# TREES AS AN ADDITIVE MODEL

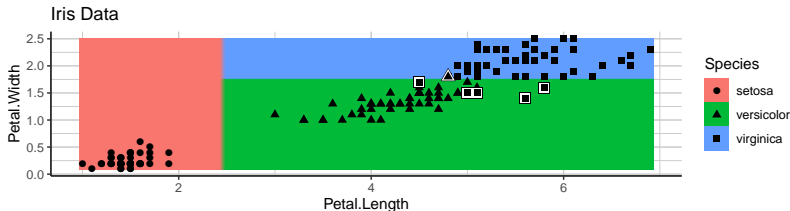
Each point in  $\mathcal{X}$  is assigned to exactly one leaf, and each leaf has a set of input points leading to it, through axis-parallel splits.

Hence, trees divide the feature space  $\mathcal{X}$  into **rectangular regions**:

$$f(\mathbf{x}) = \sum_{m=1}^M c_m \mathbb{I}(\mathbf{x} \in Q_m),$$

where a tree with  $M$  leaf nodes defines  $M$  “rectangles”  $Q_m$ .

$c_m$  is the predicted numerical response, class label or class distribution in the respective leaf node.

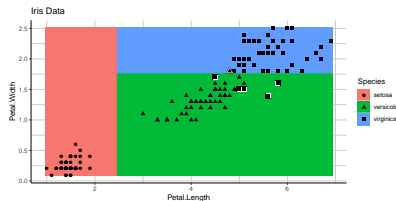


# TREES

The hypothesis space of a CART is the set of all step functions over rectangular partitions of  $\mathcal{X}$ :

$$f(\mathbf{x}) = \sum_{m=1}^M c_m \mathbb{I}(x \in Q_m),$$

Classification:



Regression:

