一、实验目的

理解逻辑回归模型,掌握逻辑回归的参数估计算法。测试一下满足和不满足朴素贝叶斯的情况下逻辑回归的效果,并找一组 UCI 上的数据集观测效果。

二、实验要求及实验环境

2.1 实验要求

- 1. 使用梯度下降,牛顿法,共轭梯度法一种或多种方法求解;
- 2. 手动生成符合多元高斯分布的数据,要求有满足和不满足朴素贝叶斯两种;
- 3. 在 UCI 网站上找一组数据集观测效果;
- 4. 使用正则项防止过拟合;

2.2 实验环境

- 硬件: Intel i5-8265U、512G SSD、8G RAM;
- 系统: Windows 11;
- IDE: Pycharm.

三、设计思想

3.1 算法原理

对某一个样本 $\langle x, y \rangle$, 其标记为 1 的概率为

$$\begin{split} P(y=1|\pmb{x}) &= \frac{P(y=1)P(\pmb{x}|y=1)}{P(y=1)P(\pmb{x}|y=1) + P(y=0)P(\pmb{x}|y=0)} \\ &= \frac{1}{1 + \frac{P(y=0)P(\pmb{x}|y=0)}{P(y=1)P(\pmb{x}|y=1)}} \\ &= \frac{1}{1 + \exp(\ln\frac{P(y=0)}{P(y=1)} + \ln\frac{P(\pmb{x}|y=0)}{P(\pmb{x}|y=1)})}. \end{split}$$

令 $P(y=1)=\pi$,假设此时样本各维度间互相独立。则有

$$P(y=1|\mathbf{x}) = \frac{1}{1 + \exp(\ln\frac{1-\pi}{\pi} + \sum_{i=1}^{m} \ln\frac{P(x_i|y=0)}{P(x_i|y=1)})},$$
 (1)

其中m为样本x的属性个数。

不妨设
$$P(x_i|y=1) \sim N(\mu_{i1}, \sigma_i)$$
, $P(x_i|y=0) \sim N(\mu_{i0}, \sigma_i)$, 则:

$$P(x_i|y=1) = \frac{1}{\sqrt{2\pi}\sigma_i}e^{-\frac{(x_i-\mu_{i1})^2}{2\mu_i^2}},$$

$$P(x_i|y=0) = \frac{1}{\sqrt{2\pi}\sigma_i} e^{-\frac{(x_i - \mu_{i0})^2}{2\mu_i^2}},$$

$$\ln \frac{P(x_i|y=0)}{P(x_i|y=1)} = -\frac{(x_i-\mu_{i0})^2}{2\mu_i^2} + \frac{(x_i-\mu_{i1})^2}{2\mu_i^2} = \frac{2(\mu_{i0}-\mu_{i1})x_i + \mu_{i1}^2 - \mu_{i0}^2}{2\sigma_i^2}.$$

对式(1)进一步化简可得

$$P(y = 1 | \mathbf{x}) = \frac{1}{1 + \exp(\ln \frac{1 - \pi}{\pi} + \sum_{i=1}^{m} (\frac{2(\mu_{i0} - \mu_{i1})}{2\sigma_i^2} x_i + \frac{\mu_{i1}^2 - \mu_{i0}^2}{2\sigma_i^2}))}$$
$$= \frac{1}{1 + \exp(w_0 + \sum_{i=1}^{m} w_i x_i)}.$$

构造

$$\mathbf{w}' = \begin{pmatrix} w_0 & w_1 & \cdots & w_m \end{pmatrix},$$

 $\mathbf{x}' = \begin{pmatrix} 1 & x_1 & \cdots & x_m \end{pmatrix},$

则式(1)可进一步简化为

$$P(y=1|\boldsymbol{x}) = \frac{1}{1 + \exp(\boldsymbol{w}'\boldsymbol{x})}.$$

由上易得

$$P(y = 0|\mathbf{x}) = \frac{\exp(\mathbf{w}'\mathbf{x})}{1 + \exp(\mathbf{w}'\mathbf{x})},$$
$$\frac{P(y = 0|\mathbf{x})}{P(y = 1|\mathbf{x})} = \exp(\mathbf{w}'\mathbf{x}),$$
$$\ln \frac{P(y = 0|\mathbf{x})}{P(y = 1|\mathbf{x})} = \mathbf{w}'\mathbf{x}.$$

现在有一组样本点 $\{\langle x_1, y_1 \rangle, \langle x_2, y_2 \rangle \cdots \langle x_n, y_n \rangle \}$,应找到一组 w 使得上面这一组数据出现的概率最大,即

$$W_{MLE} = \arg \max P(\langle \boldsymbol{x_1}, y \rangle, \langle \boldsymbol{x_2}, y \rangle \cdots \langle \boldsymbol{x_n}, y \rangle | \boldsymbol{w})$$

$$= \arg \max \prod_{i=1}^{n} P(\langle \boldsymbol{x_i}, y_i \rangle | \boldsymbol{w})$$
(2)

但之前仅推出 $P(y_i|x_i)$, 因此将式 (2) 变化为

$$W_{MCLE} = \arg \max \prod_{i=1}^{n} P(y_i | \boldsymbol{x_i}, \boldsymbol{w}).$$

而加入先验概率,采用贝叶斯估计之后

$$W_{MCAP} = \arg \max \prod_{i=1}^{n} P(\boldsymbol{w}) P(y_i | \boldsymbol{x_i}, \boldsymbol{w}).$$

具体表现为损失函数则为

$$L(\boldsymbol{w})_{MCLE} = \sum_{i=1}^{n} y_i \ln P(y_i = 1 | \boldsymbol{x_i}) + (1 - y_i) \ln P(y_i = 0 | \boldsymbol{x_i})$$
$$= \sum_{i=1}^{n} (1 - y_i) \boldsymbol{w'x_i} - \ln[1 + \exp(\boldsymbol{w'x_i})].$$

对其求导有

$$\frac{\partial L(\boldsymbol{w})}{\partial \boldsymbol{w}} = \sum_{i=1}^{n} \left[\frac{1}{1 + \exp(\boldsymbol{w}'\boldsymbol{x}_{i})} - y_{i} \right] \boldsymbol{x}_{i}$$

$$= \sum_{i=1}^{n} \left[sigmoid(-\boldsymbol{w}'\boldsymbol{x}_{i}) - y_{i} \right] \boldsymbol{x}_{i}.$$
(3)

为后续编程方便,现将其改写为矩阵乘法的方式。首先构造

$$\boldsymbol{X} = \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1(m+1)} \\ x_{21} & x_{22} & \cdots & x_{2(m+1)} \\ \vdots & \vdots & & \vdots \\ x_{n1} & x_{n2} & \cdots & x_{n(m+1)} \end{bmatrix} \in \boldsymbol{R}^{n*(m+1)},$$

$$\mathbf{y}' = \begin{pmatrix} y_1 & y_2 & \cdots & y_n \end{pmatrix},$$

X,y 中每一行表示一个样本, $x_{i0}=1$,一个样本有 m 个属性,一个标记,一共有 n 个样本。

则式(3)可以改写为

$$\frac{\partial L(\boldsymbol{w})}{\partial \boldsymbol{w}} = k_1 \boldsymbol{x_1} + k_2 \boldsymbol{x_2} + \dots + k_n \boldsymbol{x_n} = \boldsymbol{X'K},$$

$$oldsymbol{X'} = egin{pmatrix} oldsymbol{x_1} & oldsymbol{x_2} & \cdots & oldsymbol{x_n} \end{pmatrix},$$

$$\boldsymbol{K} = \begin{pmatrix} k_1 \\ k_2 \\ \vdots \\ k_n \end{pmatrix},$$

$$k_i = \frac{1}{1 + \exp(\boldsymbol{w'x_i})} - y_i = sigmoid(-\boldsymbol{w'x_i}) - y_i.$$

即

$$\frac{\partial L(\boldsymbol{w})}{\partial \boldsymbol{w}} = \boldsymbol{X'}[sigmoid(-\boldsymbol{X}\boldsymbol{w}) - \boldsymbol{Y}].$$

其二阶导数为

$$\frac{\partial^2 L(\boldsymbol{w})}{\partial \boldsymbol{w} \partial \boldsymbol{w'}} = \boldsymbol{X'} \frac{\partial sigmoid(-\boldsymbol{X}\boldsymbol{w})}{\partial \boldsymbol{w'}}.$$

其中

$$sigmoid(-\boldsymbol{X}\boldsymbol{w}) = \begin{pmatrix} sigmoid(-\boldsymbol{x_1'w}) \\ sigmoid(-\boldsymbol{x_2'w}) \\ \vdots \\ sigmoid(-\boldsymbol{x_n'w}) \end{pmatrix} = \begin{pmatrix} z_1 \\ z_2 \\ \vdots \\ z_n \end{pmatrix}$$

$$\boldsymbol{w'} = \begin{pmatrix} w_1 & w_2 & \cdots & w_{m+1} \end{pmatrix}$$

列向量对行向量求导有

$$\frac{\partial sigmoid(-\boldsymbol{X}\boldsymbol{w})}{\partial \boldsymbol{w'}} = \begin{bmatrix}
\frac{\partial z_1}{\partial w_1} & \frac{\partial z_1}{\partial w_2} & \cdots & \frac{\partial z_1}{\partial w_{m+1}} \\
\frac{\partial z_2}{\partial w_1} & \frac{\partial z_2}{\partial w_2} & \cdots & \frac{\partial z_2}{\partial w_{m+1}} \\
\vdots & \vdots & & \vdots \\
\frac{\partial z_n}{\partial w_1} & \frac{\partial z_n}{\partial w_2} & \cdots & \frac{\partial z_n}{\partial w_{m+1}}
\end{bmatrix}$$
(4)

而

$$\frac{\partial z_i}{\partial w_j} = \frac{\partial sigmoid(-\boldsymbol{x_1'w})}{\partial w_j} = z_i(1-z_i)x_{ij}$$

则式(4)求解得

$$\frac{\partial sigmoid(-\boldsymbol{X}\boldsymbol{w})}{\partial \boldsymbol{w'}} = \begin{bmatrix} z_1(1-z_1)x_{11} & z_1(1-z_1)x_{12} & \cdots & z_1(1-z_1)x_{1(m+1)} \\ z_2(1-z_2)x_{21} & z_2(1-z_2)x_{22} & \cdots & z_2(1-z_2)x_{2(m+1)} \\ \vdots & \vdots & & \vdots \\ z_n(1-z_n)x_{n1} & z_n(1-z_n)x_{n2} & \cdots & z_n(1-z_n)x_{n(m+1)} \end{bmatrix}$$

构造

$$\boldsymbol{Z} = \begin{pmatrix} sigmoid(-\boldsymbol{x_1'w})(1 - sigmoid(-\boldsymbol{x_1'w})) \\ sigmoid(-\boldsymbol{x_2'w})(1 - sigmoid(-\boldsymbol{x_2'w})) \\ \vdots \\ sigmoid(-\boldsymbol{x_n'w})(1 - sigmoid(-\boldsymbol{x_n'w})) \end{pmatrix}$$

则二阶导数可写作

$$\frac{\partial^2 L(\boldsymbol{w})}{\partial \boldsymbol{w} \partial \boldsymbol{w'}} = \boldsymbol{X'} (\boldsymbol{Z} \bullet \boldsymbol{X})$$

3.2 梯度下降

参数更新的方法为

$$w + = \eta \frac{\partial L(w)}{\partial w} - \lambda w$$

3.3 牛顿法

参数更新的方法为

$$\mathbf{w} + = (\frac{\partial^2 L(\mathbf{w})}{\partial \mathbf{w} \partial \mathbf{w}'})^{-1} \frac{\partial L\mathbf{w}}{\partial \mathbf{w}} - \lambda \mathbf{w}$$

3.4 数据结构

使用 ndarray 作为主要的数据结构,运用 pandas 库处理 UCI 数据集。

四、实验结果与分析

4.1 梯度下降

表 1 梯度下降分类准确率

正则项系数	混合高斯分布		iris 数据集	adult 数据集
	独立	不独立	110 30,711	addit 3X Will /K
0	0.97	0.98	1.0	0.8069
e^{-10}	0.99	1.0	1.0	0.8069
e^{-8}	0.96	1.0	1.0	0.8080
e^{-6}	0.99	0.97	1.0	0.8069
e^{-4}	0.99	1.0	1.0	0.8080

梯度下降此时分类效果较好,在 adult 数据集上准确率均在 0.80 左右,符合数据集附带文件上提到的错误率。

4.2 牛顿法

表 2 牛顿法分类准确率

正则项系数 _	混合高	iris 数据集	
	独立	不独立	1113 奴加来
0	0.99	0.93	1.0
e^{-6}	0.99	0.99	1.0
e^{-4}	1.0	0.96	1.0
e^{-3}	0.97	0.96	1.0
e^{-2}	0.99	0.98	1.0

表 3 牛顿法分类 adult 数据集

正则项系数	0	e^{-12}	e^{-10}	e^{-8}
正确率	0.7519	0.7519	0.7519	0.7519

牛顿法在处理 adult 数据集时,在求逆矩阵的过程中若正则项系数较大会在求逆过程中出现错误。

五、结论

混合高斯分布中,即使不满足朴素贝叶斯的条件,但只要各属性间的相关性适当,仍然可以保证模型的效果。iris 数据集,两个类别非常容易区分,符合数据集附带文件的说明。adult 数据集,数据维数多,训练用时长,数据噪声大,根据附带文件的说明,使用朴素贝叶斯的思想分类,误差大约为 0.16,上述训练数据较为合理。

参考文献

[1] CSDN, https://blog.csdn.net/alanwalker1/article/details/112688367, last accessed 2021/10/24

A主程序

```
import copy
import numpy as np
from data_guass import get_data_guass
from data_uci import get_data_uci
gradient_regulation_radio = 0
newton_regulation_radio = 0
def sigmoid_trick(m):
   for i in range(len(m)):
      a = m[i]
      if a >= 0:
         m[i] = 1 / (1 + np.exp(-1 * a))
      else:
          temp = np.exp(a)
         m[i] = temp / (1 + temp)
   return m
def gradient_descent(train_X, train_Y, validation_X, validation_Y, regulation_radio=0.0):
   dimension_num = len(train_X[0])
   # adam中的超参数,一般使用以下值
   adam_beta_1 = 0.9
   adam_beta_2 = 0.99
   inf_small = 1e-8
   learning_rate = 0.01
   # 计算过程中的累计值
   m = np.zeros(dimension_num)
   v = np.zeros(dimension_num)
   accumulative_adam_beta_1 = adam_beta_1
   accumulative_adam_beta_2 = adam_beta_2
   w = np.array([0.1 for _ in range(dimension_num)])
   temp_w = copy.deepcopy(w)
   accuracy = test(validation_X, w, validation_Y)
   accuracy_list = [accuracy]
   iteration_times = 0
   while True:
      for i in range(10000):
          gradient = np.dot(train_X.T, sigmoid_trick(-1 * np.dot(train_X, w)) - train_Y) -
              regulation_radio * w
          m = adam_beta_1 * m + (1 - adam_beta_1) * gradient
          v = adam_beta_2 * v + (1 - adam_beta_2) * (gradient ** 2)
          M = m / (1 - accumulative_adam_beta_1)
          V = v / (1 - accumulative_adam_beta_2)
```

```
accumulative_adam_beta_1 *= adam_beta_1
          accumulative_adam_beta_2 *= adam_beta_2
          w += learning_rate * M / (V ** (1 / 2) + inf_small)
       iteration_times += 1
       accuracy = test(validation_X, w, validation_Y)
       if accuracy < accuracy_list[-1] or iteration_times >= 15:
          break
       else:
          temp_w = copy.deepcopy(w)
          accuracy_list.append(accuracy)
   return temp_w, iteration_times
def Newton_method(train_X, train_Y, validation_X, validation_Y, regulation_radio=0.0):
   dimension_num = len(train_X[0])
   w = np.array([0.1 for _ in range(dimension_num)])
   temp_w = copy.deepcopy(w)
   accuracy = test(validation_X, w, validation_Y)
   accuracy_list = [accuracy]
   iteration_times = 0
   while True:
      for i in range(10000):
          sigmoid = sigmoid_trick(-1 * np.dot(train_X, w))
          a = np.dot(train_X.T, sigmoid - train_Y)
          b = train_X.T @ (np.reshape(sigmoid * (1 - sigmoid), (len(sigmoid), 1)) * train_X)
          delta_w = np.dot(np.linalg.pinv(b), a) - w * regulation_radio
          w += delta_w
      iteration_times += 1
      accuracy = test(validation_X, w, validation_Y)
       if iteration_times >= 15 or accuracy < accuracy_list[-1]:</pre>
          break
       else:
          temp_w = copy.deepcopy(w)
          accuracy_list.append(accuracy)
   return temp_w, iteration_times
def test(X, w, Y):
   X = np.array(X)
   Y = np.array(Y)
   predict_result = np.dot(X, w)
   right_num = 0
   for i in range(len(X)):
       if (predict_result[i] >= 0 and Y[i] == 0) or (predict_result[i] < 0 and Y[i] == 1):</pre>
          right_num += 1
```

```
return float(right_num) / len(X)
if __name__ == '__main__':
   train_X_list, train_Y_list, validation_X_list, validation_Y_list, test_X_list, test_Y_list
       = get_data_guass(100, 20, 100, 0.7, False)
   # train_X_list, train_Y_list, validation_X_list, validation_Y_list, test_X_list,
       test_Y_list = get_data_uci("iris")
   # train_X_list, train_Y_list, validation_X_list, validation_Y_list, test_X_list,
       test_Y_list = get_data_uci("adult")
   train_X = np.array(train_X_list)
   train_Y = np.array(train_Y_list)
   validation_X = np.array(validation_X_list)
   validation_Y = np.array(validation_Y_list)
   test_X = np.array(test_X_list)
   test_Y = np.array(test_Y_list)
   w1, iteration_times_1 = gradient_descent(train_X, train_Y, validation_X, validation_Y,
       gradient_regulation_radio)
   print((test(test_X_list, w1, test_Y_list)), w1, iteration_times_1)
   w2, iteration_times_1 = Newton_method(train_X, train_Y, validation_X, validation_Y,
       newton_regulation_radio)
   print(test(test_X, w2, test_Y), w2, iteration_times_1)
```

B生成混合高斯分布

```
import numpy as np
def get_data_guass(train_size, validation_size, test_size, positive_sample_radio, naive=True):
   if naive:
      cov12 = 0.0
   else:
      cov12 = 0.2
   mean_array_positive = [1, 1]
   cov_matrix_positive = [[0.4, cov12], [cov12, 0.3]]
   mean_array_negative = [-1, -1]
   cov_matrix_negative = [[0.4, cov12], [cov12, 0.3]]
   train_X_list, train_Y_list = get_guass_distribution(train_size, int(train_size *
       positive_sample_radio), mean_array_positive, cov_matrix_positive,
                                                mean_array_negative, cov_matrix_negative)
   validation_X_list, validation_Y_list = get_guass_distribution(validation_size,
       int(validation_size * positive_sample_radio), mean_array_positive,
                                                         cov_matrix_positive,
                                                             mean_array_negative,
                                                             cov_matrix_negative)
   test_X_list, test_Y_list = get_guass_distribution(test_size, int(test_size *
```

C 读取 uci 数据集

```
import copy
import numpy as np
import pandas as pd
from data.config.adult_config import adult_config
from data.config.iris_config import iris_config
def get_data_uci(uci_data_name):
   if uci_data_name == "iris":
       data_config = iris_config
      train_nrows = 100
       test_nrows = 100
      validation_index = [25, 76]
   elif uci_data_name == "adult":
       data_config = adult_config
      train_nrows = 1000
      test nrows = 1000
       validation_index = [0, 500]
   else:
      print("尚无此数据集")
      return None
   train_filename = data_config[0]
   test_filename = data_config[1]
   field_list = data_config[2]
   discrete_field_dict = data_config[3]
   label_dict = data_config[4]
   get_log_list = data_config[5]
   train_X_list, train_Y_list = read_uci_data(train_filename, train_nrows, field_list,
       discrete_field_dict, label_dict, get_log_list)
```

```
if test_filename == train_filename:
      test_X_list, test_Y_list = train_X_list, train_Y_list
   else:
      test_X_list, test_Y_list = read_uci_data(test_filename, test_nrows, field_list,
           discrete_field_dict, label_dict, get_log_list)
   validation_X_list = test_X_list[validation_index[0]:validation_index[1]]
   validation_Y_list = test_Y_list[validation_index[0]:validation_index[1]]
   return train_X_list, train_Y_list, validation_X_list, validation_Y_list, test_X_list,
       test_Y_list
def read_uci_data(filename, nrows, field_list, discrete_field_dict, label_dict, get_log_list):
   columns = copy.deepcopy(field_list)
   columns.append("label")
   raw_data = pd.read_csv(filename, names=columns, nrows=nrows)
   processed_data = []
   processed_data_label = []
   for i in range(len(raw_data)):
      processed_sample = []
      raw_sample = raw_data.iloc[i]
      try:
          for field in field_list:
             if field in discrete_field_dict:
                 processed_sample.append(discrete_field_dict[field][raw_sample.loc[field]])
                 processed_sample.append(float(raw_sample.loc[field]))
      except KeyError:
          continue
      except ValueError:
          continue
      processed_data_label.append(label_dict[raw_sample.loc["label"]])
      processed_data.append(processed_sample)
   if len(get_log_list) != 0:
      for sample in processed_data:
          for index in get_log_list:
             if sample[index] <= 10:</pre>
                 sample[index] = 1
             else:
                 sample[index] = np.log10(sample[index])
          sample.insert(0, 1)
   else:
      for sample in processed_data:
          sample.insert(0, 1)
   return processed_data, processed_data_label
```

D 关于 iris 数据集的配置文件

```
train_filename = "./data/iris/iris.data"
test_filename = "./data/iris/iris.data"
field_list = ["sepal_length", "sepal_width", "petal_length", "petal_width"]
discrete_field_dict = {}
label_dict = {"Iris-setosa": 0, "Iris-versicolor": 1}
get_log_list = []
iris_config = [train_filename, test_filename, field_list, discrete_field_dict, label_dict, get_log_list]
```

E 关于 adult 数据集的配置文件

```
work_class_dict = {' Private': 0, ' Self-emp-not-inc': 1, ' Self-emp-inc': 2, ' Federal-gov':
   3, 'Local-gov': 4, 'State-gov': 5, 'Without-pay': 6,
              ' Never-worked': 7, }
Prof-school:: 4, 'Assoc-acdm': 5, 'Assoc-voc': 6, '9th': 7,
              ' 7th-8th': 8, ' 12th': 9, ' Masters': 10, ' 1st-4th': 11, ' 10th': 12, '
                 Doctorate': 13, ' 5th-6th': 14, ' Preschool': 15, }
marital_status_dict = {' Married-civ-spouse': 0, ' Divorced': 1, ' Never-married': 2, '
   Separated': 3, 'Widowed': 4, 'Married-spouse-absent': 5,
                 ' Married-AF-spouse': 6, }
Exec-managerial': 4, ' Prof-specialty': 5,
              ' Handlers-cleaners': 6, ' Machine-op-inspct': 7, ' Adm-clerical': 8, '
                 Farming-fishing': 9, ' Transport-moving': 10,
              ' Priv-house-serv': 11, ' Protective-serv': 12, ' Armed-Forces': 13, }
relationship_dict = {    Wife': 0, ' Own-child': 1, ' Husband': 2, ' Not-in-family': 3, '
   Other-relative': 4, 'Unmarried': 5, }
race_dict = {' White': 0, ' Asian-Pac-Islander': 1, ' Amer-Indian-Eskimo': 2, ' Other': 3, '
   Black': 4, }
sex_dict = {' Female': 0, ' Male': 1, }
' Canada': 4, ' Germany': 5,
                 ' Outlying-US(Guam-USVI-etc)': 6, ' India': 7, ' Japan': 8, ' Greece': 9, '
                     South': 10, 'China': 11, 'Cuba': 12, 'Iran': 13,
                 ' Honduras': 14, ' Philippines': 15, ' Italy': 16, ' Poland': 17, '
                     Jamaica': 18, ' Vietnam': 19, ' Mexico': 20,
                 ' Portugal': 21, ' Ireland': 22, ' France': 23, ' Dominican-Republic': 24,
                     'Laos': 25, 'Ecuador': 26, 'Taiwan': 27,
                 ' Haiti': 28, ' Columbia': 29, ' Hungary': 30, ' Guatemala': 31, '
                     Nicaragua': 32, 'Scotland': 33, 'Thailand': 34,
                 'Yugoslavia': 35, 'El-Salvador': 36, 'Trinadad&Tobago': 37, 'Peru': 38,
                     ' Hong': 39, ' Holand-Netherlands': 40, }
train_filename = "./data/adult/adult.data"
test_filename = "./data/adult/adult.test"
field_list = ['age', 'work_class', 'fnlwgt', 'education', 'education_num', 'marital_status',
    'occupation', 'relationship', 'race', 'sex',
          'capital_gain', 'capital_loss', 'hours_per_week', 'native_country']
```