□ The Co-dfns Compiler

A High-performance, Parallel APL Compiler

```
    ○ Copyright © 2011-2017 Aaron W. Hsu arcfide@sacrideo.us
    ○ This program is free software: you can redistribute it and/or modify it under the terms of the GNU Affero
    ○ General Public License as published by the Free Software Foundation, either version 3 of the License, or (at your
    ○ option) any later version.
    ○ This program is distributed in the hope that it will be useful, but WITHOUT ANY WARRANTY; without even the
    ○ implied warranty of MERCHANTABILITY or FITNESS FOR A PARTICULAR PURPOSE. See the GNU Affero
```

Nou should have received a copy of the GNU Affero General Public License along with this program.

○ If not, see http://www.gnu.org/licenses/

© General Public License for more details.

:Namespace CODFNS

```
\leftarrow 0.13
           VERSION
                                       \leftarrow 2017 12 0
     AF\Delta PREFIX
                                       ← '/usr/local'
              AF\Delta LIB
                 VS\Delta PS \leftarrow '\setminus 2017\setminus \circ, '' Enterprise' 'Professional' 'Community', '' \subset' \setminus VC\setminus Auxiliary\setminus Build'
                 VS\Delta PS , \leftarrow C' 14.0\VC'
                 VS\Delta PS, "\approx \leftarrow C'\Program Files (x86)\Microsoft Visual Studio'
                 VS\Delta PS ,"\(\sigma\) cvarsall.bat'
    Cmp \leftarrow \{\_ \leftarrow 1 \mid DELETE \mid \alpha, soext \mid \theta \}
                       \_\leftarrow ($$ opsys'vsc''gcc''clang') $$ $$ $\alpha\dashv(\alpha,'.cpp')$ put$$$ $$ $$ gctt $\supset a$ $n\leftarrow ps$ $$ $$ $$
                       \_ \leftarrow \square NEXISTS \alpha, soext \theta \diamond \_ : n
                                   'COMPILE ERROR'□SIGNAL22}
 MkNS \leftarrow \{NS \dashv \alpha \circ \{NS. \pm \alpha \ mkf \omega\} : (1 = 1 \mid \Delta \omega) \neq 0 \mid \Delta \omega \dashv NS \leftarrow \#. \square NS \theta\}
       Fix \leftarrow \{\alpha MkNS \alpha Cmp \omega\}
     Xml \leftarrow \{ \boxed{\mathsf{XML}} \ (0 \ \boxed{\ } \boxtimes \omega), (, \circ \overline{\Phi} \neq 2 \uparrow 1 \downarrow \boxtimes \omega), (\subset''), \overline{\neg} (\subset (\overline{\ } 3 + \not\equiv \boxtimes \omega) \uparrow, \overline{\ } '\mathsf{nrsgvyel'}), \circ \overline{\neg} ' \downarrow \overline{\Phi} \circ, \overline{\ } \boxtimes 3 \downarrow \boxtimes \omega \}
   MKA \leftarrow \{mka \subset \omega \dashv \text{'mka'} \exists NA'P', (\alpha, soext \theta), \text{'} | mkarray < PP'\}
    EXA \leftarrow \{exa \ \theta \ \omega \ \exists \ 'exa' \ \square NA \ (\alpha, soext \ \theta), \ '| \ exarray \ >PP \ P'\}
 FREA \leftarrow \{frea \ \cup \ | \ frea' \ | \ \mathsf{NA}(\alpha, soext \ \theta), \ | \ \mathsf{frea} \ \mathsf{P}'\}
opsys ← {ω ⊃ \approx 'Win' 'Lin' 'Mac' ι ⊂ 3 ↑ ⊃ '.' \squareWG 'APLVersion'}
soext \leftarrow \{opsys'.dll''.so''.dylib'\}
     tie \leftarrow \{0 :: \square SIGNAL \square EN \diamond 22 :: \omega \square NCREATE 0 \diamond 0 \square NRESIZE \omega \square NTIE 0\}
   put \leftarrow \{s \leftarrow (^{-}128 + 256 \mid 128 + 'UTF - 8' \mid UCS \alpha) \mid NAPPEND (t \leftarrow tie \omega) 83 \diamond 1 : r \leftarrow s \dashv \mid NUNTIE t\}
 mkf \leftarrow \{fn \leftarrow (\alpha, soext \, \theta), ' \mid ', ('\Delta' \, \square R' \, \_' \mid \vdash \omega), ' \, \_dwa ' \\ f \leftarrow \omega, ' \leftarrow \{\_\leftarrow' \mid dya' \mid \square NA' \mid ', fn, ' > PP \mid PP' \mid \diamond ' \\ f, \leftarrow '\_\leftarrow' \mid mon' \mid \square NA' \mid ', fn, ' > PP \mid P \mid PP' \mid \diamond ' \\ f, '0 = \square NC' \mid \alpha' \mid :mon \mid 0 \mid 0 \mid \omega \mid \diamond dya \mid 0 \mid \alpha \mid \omega \} \mid \diamond 0'\}
```

```
cco \leftarrow \text{'-std=c++11} -Ofast -g -Wall -fPIC -shared'
     ucc \leftarrow \{\omega\omega (\Box SH \alpha\alpha, ' ', cco, cci, ccf) \omega\}
     gcc \leftarrow 'g++'ucc'so'
 clang \leftarrow 'clang++'ucc'dylib'
    vsco \leftarrow \{z \leftarrow '/ \text{W3 /wd4102 /wd4275 /Gm- /O2 /Zc:inline /Zi /Fd"', <math>\omega, '.pdb" '
                      z,← '/errorReport:prompt /WX- /MD /EHsc /nologo
                                   z,'/I"%AF_PATH%\include" /D "NOMINMAX" /D "AF_DEBUG"'}
    vslo \leftarrow \{z \leftarrow ' / \text{link /DLL /OPT:REF /INCREMENTAL:NO /SUBSYSTEM:WINDOWS '}\}
                      z ,\leftarrow '/LIBPATH:"%AF_PATH%\lib" /DYNAMICBASE "af',AF\Delta LIB,'.lib" '
                                   z,'/OPT:ICF /ERRORREPORT:PROMPT /TLBID:1 '}
     vsc_o \leftarrow \{ \sim \lor \neq b \leftarrow \square NEXISTS^" VS\Delta PS : 'MISSING VISUAL C++' \square SIGNAL 99 \diamond '" "', '" amd64', " \supset b \neq VS\Delta PS \}
    vsc \leftarrow \{\Box CMD ('\%comspec\% /C', vsc_0, vsc_1, vsc_2) \omega\}
    get \leftarrow \{\alpha\alpha \mid \Diamond\omega\}
wrap \leftarrow 50 (\lozenge (1+1 \uparrow \lozenge) 51 \downarrow \lozenge)
bind \leftarrow \{n \_ e \leftarrow \omega \diamond (0 \ n\_ \square e) \leftarrow \subset n \diamond e\}
      at \leftarrow \{\alpha \leftarrow \vdash \diamond A \dashv ((B) \neq (rA) \land A) \leftarrow \alpha \alpha \alpha (B) \neq ((r \leftarrow (\not\equiv \rho B \leftarrow \omega \omega \omega) ((x/\uparrow), \downarrow) \land A) \land (A \leftarrow \omega)\}
d_t _k n_r s_g v_y e_l \leftarrow 17 + f\Delta \leftarrow 4
d \leftarrow d_get \diamond t \leftarrow t_get \diamond k \leftarrow k_get \diamond n \leftarrow n_get \diamond r \leftarrow r_get \diamond s \leftarrow s_get
g \leftarrow g get \diamond v \leftarrow v get \diamond y \leftarrow y get \diamond e \leftarrow e get \diamond l \leftarrow l get
                                                                                                     \diamond msk \leftarrow \{(t \omega) \in \subset \alpha\alpha\} \diamond sel \leftarrow \{(\alpha\alpha msk \omega) \neq \omega\}
 new \leftarrow \{ \nabla_{7} f\Delta \uparrow 0 \alpha, \omega \}
      A \leftarrow \{(\mathsf{'A'} \ new \ \alpha\alpha) \ wrap \supset 5/\omega\}
                                                                                                     \diamond A_m \leftarrow 'A' msk
                                                                                                                                                A_s \leftarrow 'A' sel
                                                                                                                                                     \diamond E_s \leftarrow 'E' sel
                                                                                                    \Leftrightarrow E_m \leftarrow 'E' msk
       E \leftarrow \{(\mathsf{E'} \ new \ \alpha\alpha) \ wrap \supset 5/\omega\}
       F \leftarrow \{(\mathsf{F'} \ new \ \alpha\alpha) \ wrap \supset \bar{\gamma}/\ (\subset 0 \ f\Delta \ \rho \ \theta), \omega\} \diamond F_m \leftarrow \mathsf{F'} \ msk
                                                                                                  \begin{array}{lll} \{\} \Leftrightarrow F_m \leftarrow \text{'F'} msk & \Leftrightarrow F_s \leftarrow \text{'F'} sel \\ \Leftrightarrow G_m \leftarrow \text{'G'} msk & \Leftrightarrow G_s \leftarrow \text{'G'} sel \\ \Leftrightarrow L_m \leftarrow \text{'L'} msk & \Leftrightarrow L_s \leftarrow \text{'L'} sel \\ \} \Leftrightarrow M_m \leftarrow \text{'M'} msk & \Leftrightarrow M_s \leftarrow \text{'M'} sel \\ \Leftrightarrow N_m \leftarrow \text{'N'} msk & \Leftrightarrow N_s \leftarrow \text{'N'} sel \\ \Leftrightarrow O_m \leftarrow \text{'O'} msk & \Leftrightarrow O_s \leftarrow \text{'O'} sel \\ \Leftrightarrow P_m \leftarrow \text{'P'} msk & \Leftrightarrow P_s \leftarrow \text{'P'} sel \\ \Leftrightarrow S_m \leftarrow \text{'S'} msk & \Leftrightarrow S_s \leftarrow \text{'S'} sel \\ \Leftrightarrow V_m \leftarrow \text{'V'} msk & \Leftrightarrow V_s \leftarrow \text{'V'} sel \\ \Leftrightarrow V_m \leftarrow \text{'Y'} msk & \Leftrightarrow V_s \leftarrow \text{'Y'} sel \\ \Leftrightarrow Z_m \leftarrow \text{'Z'} msk & \Leftrightarrow Z_s \leftarrow \text{'Z'} sel \\ \end{array}
                                                                                                                                                 \Leftrightarrow F_s \leftarrow 'F' sel
      G \leftarrow \{(\mathsf{'G'} \ new \ 0) \ wrap \supset 5/\omega\}
       L \leftarrow \{(\mathsf{'L'} \ new \ 0) \ wrap \supset 5/\omega\}
      M \leftarrow \{(\mathsf{'M'} \ new \ 0 \ ") \ wrap \supset 5/(\subset 0 \ f\Delta \ \rho \ \theta), \omega\} \diamond M_m \leftarrow \mathsf{'M'} \ msk
      N \leftarrow \{ 'N' \ new \ 0 \ ( \Phi \omega ) \}
      O \leftarrow \{('0' \ new \ \alpha\alpha) \ wrap \supset 5/\omega\}
       P \leftarrow \{'P' \ new \ 0 \ \omega\}
       S \leftarrow \{ \mathsf{'S'} \ new \ 0 \ \omega \}
       V \leftarrow \{ 'V' \text{ new } \alpha\alpha \omega \}
      Y \leftarrow \{'Y' \text{ new } 0 \omega\}
       Z \leftarrow \{'\mathsf{Z}' \ new \ 1 \ \omega\}
```

```
-c \leftarrow \{0 \ge \exists c \ a \ e \ r \leftarrow p \leftarrow \alpha \ \alpha \alpha \ \omega : p \diamond 0 \ge \exists c \ a \ e \ r, \leftarrow p \leftarrow \alpha \ \omega \omega \ \omega : p \diamond c \ a \ e \ (r \uparrow \sim -|/ \not\equiv r \ r, \rangle\}
        \_s \leftarrow \{0 < \exists c \ a \ e \ r \leftarrow p \leftarrow \alpha \ \alpha \alpha \ \omega : p \diamond 0 < \exists c, a, e \ r \leftarrow p \leftarrow e \ \omega \omega \ r : p \diamond (c \ [c](a, a)) \ e \ r \}
\_noenv \leftarrow \{0 < \supset c \ a \ e \ r \leftarrow p \leftarrow \alpha \ \alpha\alpha \ \omega : p \diamond c \ a \ \alpha \ r\}
    \_env \leftarrow \{0 < \supset c \ a \ e \ r \leftarrow p \leftarrow \alpha \ \alpha\alpha \ \omega : p \diamond c \ a \ (e \ \omega\omega \ a) \ r\}
  \_then \leftarrow \{0 < \supset c \ a \ e \ r \leftarrow p \leftarrow \alpha \ \alpha \alpha \ \omega : p \diamond 0 < \supset c \ a \ e \_ \leftarrow p \leftarrow e \ (\omega \omega \_s \ eot) \ a : p \diamond c \ a \ e \ r\}
    \_not \leftarrow \{0 < \supset c \ a \ e \ r \leftarrow \alpha \ \alpha\alpha \ \omega : 0 \ a \ \alpha \ \omega \diamond 2 \ a \ \alpha \ \omega \}
      as \leftarrow \{0 < \supset c \ a \ e \ r \leftarrow \alpha \ \alpha\alpha \ \omega : c \ a \ e \ r \diamond c \ (, \subset \omega\omega \ a) \ e \ r\}
         t \leftarrow \{0 < \exists c \ a \ e \ r \leftarrow \alpha \ \alpha \alpha \ \omega : c \ a \ e \ r \diamond e \ \omega \omega \ a : c \ a \ e \ r \diamond 2 \ \theta \ \alpha \ \omega\}
    \_ign \leftarrow \{c \ a \ e \ r \leftarrow \alpha \ \alpha\alpha \ \omega \diamond c \ \theta \ e \ r\}
  \_peek \leftarrow \{0 
     _yes \leftarrow \{0 \theta \alpha \omega\}
    \_opt \leftarrow \{\alpha (\alpha \alpha \_o \_yes) \omega\}
    \_any \leftarrow \{\alpha (\alpha \alpha \_s \nabla \_o \_yes) \omega\}
 \_some \leftarrow \{\alpha (\alpha \alpha \_s (\alpha \alpha \_any)) \omega\}
     \_set \leftarrow \{(0 \neq \not\equiv \omega) \land (\supset \omega) \in \alpha\alpha : 0 (,\supset \omega) \alpha (1 \downarrow \omega) \diamond 2 \theta \alpha \omega\}
      \_tk \leftarrow \{((\not\equiv,\alpha\alpha) \uparrow \omega) \equiv,\alpha\alpha : 0 (\subset,\alpha\alpha) \alpha ((\not\equiv,\alpha\alpha) \downarrow \omega) \diamond 2 \theta \alpha \omega\}
    \_eat \leftarrow \{0 = \not\equiv \omega : 2 \theta \alpha \omega \diamond 0 (\alpha \alpha \uparrow \omega) \alpha (\alpha \alpha \downarrow \omega)\}
     ws \leftarrow ('', \square UCS 9)_set
    aws \leftarrow ws \quad anv \quad ign
 awslf \leftarrow (\square UCS 10 13) \_set \_o ws \_any \_ign
    gets \leftarrow aws\_s('\leftarrow'\_tk)\_s aws\_ign
   \tilde{h}im \leftarrow '-'_set
    dot \leftarrow ' \cdot ' \_set
     jot ← '∘' _set
    lbrc \leftarrow aws\_s('\{'\_set\}\_s aws
   rbrc \leftarrow aws\_s(')'\_set)\_s aws
   lpar \leftarrow aws\_s('('\_tk)\_s aws\_ign
  rpar \leftarrow aws\_s(')'\_tk)\_s aws\_ign

lbrk \leftarrow aws\_s('['\_tk)\_s aws\_ign
   rbrk \leftarrow aws_s(']'_tk)_s aws_ign
  semi \leftarrow aws\_s(';'\_tk\_as('a'V\circ,\circ\supset))\_s \ aws \ grd \leftarrow aws\_s(':'\_tk)\_s \ aws\_ign
   egrd \leftarrow aws\_s('::'\_tk)\_s aws\_ign
alpha \leftarrow {}^{\prime}\mathsf{ABCDEFGHIJKLMNOPQRSTUVWXYZabcdefghijklmnopqrstuvwxyz\Delta'\_set
 digits \leftarrow '0123456789' set
  mop \leftarrow '"/+ \" set
   dop_i \leftarrow ' \cdot * \circ ' \_set
  dop_2 \leftarrow ' \circ * \circ ' \_set
   dop_3 \leftarrow ' \circ ' \_set
     eot \leftarrow aws\_s \{" \equiv \omega : 0 \theta \alpha " \diamond 2 \theta \alpha \omega\}_{ign}
   digs \leftarrow digits \_some
 odigs \leftarrow digits\_any
     int \leftarrow aws\_s digs\_s (him\_opt)\_s aws
  float \leftarrow aws\_s (odigs\_s dot\_s int\_o (digs\_s dot))\_s aws
name \leftarrow aws \_s (alpha \_o (digits \_some \_s alpha) \_some) \_s aws
     aw \leftarrow aws \_s ('\alpha\omega' \_set) \_s aws
aaww \leftarrow aws\_s(('aa'\_tk)\_o('\omega\omega'\_tk))\_saws
    sep \leftarrow aws\_s(('\diamond', \square UCS 10 13)\_set\_ign)\_s aws
    nss \leftarrow awslf\_s (': Namespace' _tk) _s aws _s (name _opt) _s awslf_ign
    nse \leftarrow awslf\_s (': EndNamespace'_tk)_s awslf\_ign
```

```
Sfn \leftarrow aws\_s(('\mathsf{TFF}\square'\_tk)\_o('\mathsf{TFFI}\square'\_tk))\_s aws\_as\{P \oplus \in \omega\}
   Prim \leftarrow prim \_as P
        Vt \leftarrow \{((0 \mid \Diamond \alpha) \iota \omega) 1 \mid \alpha ; " \mid 1\}
     Var \leftarrow \{\alpha (aaww o aw o (name as \oplus) t (\alpha \alpha = Vt) as (\omega \omega V \circ, \circ \supset)) \omega \}
  Num \leftarrow float\_oint\_as(N \circ \oplus)
Strand \leftarrow 0 \ Var'a' \ \_s \ (0 \ Var'a' \ \_some) \ \_as \ ('s' \ A \circ \oplus)
     Pex \leftarrow \{\alpha (rpar \_s Ex \_s lpar) \omega\}
  Atom \leftarrow Strand \ o \ (0 \ Var' \ a' \ as \ ('v'A)) \ o \ (Num \ some \ as \ ('n' \ A \circ \Phi)) \ o \ Pex
     Brk \leftarrow rbrk\_s\{\alpha(Ex\_opt\_s(semi\_s(Ex\_opt)\_any))\omega\}\_s(brk\_as('i'E\circ\Phi)
     Idx \leftarrow Brk\_s(\_ves\_as\{P,'[']\})\_sAtom\_as(2E\circ \bigoplus)
    Blrp \leftarrow \{\alpha (\alpha \alpha \_s (\omega \omega Slrp \nabla)) \omega\}
    Slrp \leftarrow \{\alpha (\alpha \alpha \_o (\omega \omega \_s \nabla) \_o ((1 \_eat) \_s \nabla)) \omega\}
                                                        e \leftarrow ('\omega\omega''\alpha\alpha', '\alpha\omega'), \circ 5 \circ 1 \otimes 1 + 3 \cdot 3 \cdot 2 \cdot 2 \cdot T \cdot (6 \cdot 4 \cdot 4 + 1 \cdot 5 \cdot 9) + 2 \times 1 \cdot 14
       Fa \leftarrow \{
                                                        a \leftarrow e (\alpha \{ \omega \text{ Gex \_o Ex \_o Fex Stmts \_then Fn} = \alpha \alpha ; \alpha \}) \circ 2 1 \vdash \omega
                                                       m \leftarrow (0 = 0 \mid \nabla a) \land \land \neq (\lor \uparrow \circ .= \approx \iota 14) \lor \circ .\neq \approx 1 \mid \nabla a
                                             \sim \vee \neq m : ([\neq 0 \mid \nabla a) \theta \alpha \omega
              (1 = + \neq m) \land 2 > m \wr 1 : 0 (, \subset (F' \text{ new } 1) \text{ wrap } \supset m \neq 1 \mid \boxtimes a) \alpha \omega
                                                        z \leftarrow (\text{'F' new 'a'}) wrap \supset (m \neq \text{'F' new" } 1 + \iota 14) \bar{\iota}.(wrap \circ \supset) m \neq 1 \prod \Diamond a
                                                                 0 (, \subset z) \alpha \omega
      Fn \leftarrow \{
                                                      ns \leftarrow nz \neq m \leftarrow \{(F_m \omega) \land 1 \in k \omega\} z \leftarrow \supset (\omega \diamond 0) = \not\equiv ns : 0 (, \subset z) \alpha
                                                        p \leftarrow \alpha \circ Fa 'ns \diamond 0 < c \leftarrow [/ \supset p : c \theta \alpha \omega]
                                                                 0 (\sqrt[5]{(c 0 4 \rho \theta)}, \approx p \{\omega ((d + \circ \supset \dashv), 1 \downarrow \circ 1 \vdash) \supset \sqrt[5]{1 \supset \alpha} \text{ at}\{m\} \downarrow z) \alpha''\}
      Pfe \leftarrow \{\alpha (rpar \ s \ Fex \ s \ lpar) \ \omega\}
     Bfn \leftarrow rbrc \ Blrp \ lbrc \ \_as \ ('F' \ new \ ^1, \circ \subset \circ \oplus 1 \downarrow \ ^1 \downarrow \vdash)
     Fnp \leftarrow Prim\_o(1 \ Var'f')\_o \ Sfn\_o \ Bfn\_o \ Pfe
    Mop \leftarrow \{\alpha ((mop \ as P) \ s Afx \ as (1 O)) \omega\}
   Dop_1 \leftarrow \{\alpha ((dop_1 \_as P) \_s Afx \_as (2 O \circ \oplus)) \omega\}
   Dop_{\alpha} \leftarrow \{\alpha (Atom \ s(dop_{\alpha} \ as P) \ sAfx \ as (2 O \circ \oplus)) \omega\}
   Dop_3 \leftarrow (dop_3 \_as\ P) \_s\ Atom\ \_as\ (2\ O\circ \bigoplus)\ \_o\ (dot\ \_s\ jot\ \_as\ (P\circ \bigoplus)\ \_as\ (1\ O))
     Bop \leftarrow \{\alpha (rbrk\_s Ex\_s lbrk\_s (\_yes\_as \{P, '[']\})\_s Afx\_as (2 O \circ \oplus)) \omega\}
     Afx \leftarrow Mop\_o(Fnp\_s(Dop,\_oDop,\_opt)\_as(\supset wrap/\circ \oplus))\_oDop,\_oBop
     Trn \leftarrow \{\alpha (Afx \ s((Afx \ o Idx \ o Atom) \ s(\nabla \ opt) \ opt)) \omega\} \ as('t' F \circ \Phi)
   Bind \leftarrow \{\alpha (gets\_s (name\_as \oplus)\_env (\alpha\alpha\{(\supset \oplus \omega) \alpha\alpha \overline{\varsigma} \alpha\})\_as (\omega\omega new'b', \vdash)) \omega\}
   Asgn \leftarrow gets\_s \ Brk\_s \ (name\_as \ \bigcirc \ t \ (0 = Vt) \ \_as \ ('a' \ V \circ, \circ \supset)) \ \_as \ ('a' \ E \circ \bigcirc)
     Fex \leftarrow Afx \_s (Trn \_opt) \_s (1 Bind 'F' \_any) \_as (\supset wrap / \circ \oplus)
    App \leftarrow Afx\_s(Idx\_oAtom\_s(dop2\_not)\_opt)\_as\{(\not\equiv\omega)E\oplus\omega\}
       Ex \leftarrow Idx\_oAtom\_s\{\alpha(0Bind'E'\_oAsgn\_oApp\_s\nabla\_opt)\omega\}\_as(\supset wrap/\circ \Phi)
     Gex \leftarrow Ex\_s \ grd\_s \ Ex\_as \ (G \circ \Phi)
   Nlrp \leftarrow sep \ o \ eot \ Slrp \ (lbrc \ Blrp \ rbrc)
  Stmts \leftarrow \{\alpha (sep\_any\_s (Nlrp\_then (\alpha\alpha\_s eot \circ \Phi))\_any\_s eot) \omega\}
       Ns \leftarrow nss Blrp nse then (Ex o Fex Stmts then Fn) s eot as M
        ps \leftarrow \{0 \neq \supset c \ a \ e \ r \leftarrow (0 \ 2 \ \rho \ \theta) \ Ns \in \{\omega \ / \sim \land \setminus \ ' \land ' \neq \omega \} \ \omega \ , \ \Box UCS \ 10 : \Box SIGNAL \ c \diamond (\supset a) \ e\}
```

```
scp \leftarrow (+ \downarrow F_m) \vdash \circ \subset \sqsubseteq \vdash
    prf \leftarrow ((\not\equiv \uparrow \ 1 \downarrow \vdash (\not\vdash \ddot{\sim}) \ 0 \not= \vdash) \ddot{\circ} \ 1 \uparrow \circ r) \vdash
    enc \leftarrow \subset \dashv, \circ \supset ((\dashv, '\_', \vdash) / (\subset''), (\overline{\Phi}'' \vdash (/\tilde{\sim}) \ 0 \neq \vdash))
   veo \leftarrow \cup ((\subset'\%u'), (, "prims), \dashv) \sim "\circ \{\supset, / \{\subset "(1 \equiv \exists \omega) \vdash \omega\}" \omega\} = 1 \downarrow \vdash (/") (\land / "0 \neq ((\supset 0 \rho \vdash) "\vdash)))
 ndo \leftarrow \{\alpha \leftarrow \vdash \diamond m \supset \circ(\subset, \vdash) \text{``} \alpha \circ \alpha \alpha \text{````} \omega \supset \circ(, \circ \subset \sim \subset) \text{```} m \leftarrow 1 \geq \equiv \text{``} \omega \}
    n2f \leftarrow (\supset,/) ((1 = \equiv) \supset, \circ \subset \sim \circ \subset)
              rn \leftarrow \vdash, \circ \downarrow (1+d) \uparrow \circ \bar{} 1 (+ \uparrow d \circ .= \circ 1 + ([/0,d))
               rd \leftarrow \vdash, (+/\uparrow \circ r \land . (= \lor 0 = \vdash) \circ \Diamond \circ \uparrow \circ r \vdash (\not \vdash \ddot{\sim}) F_m \land 1 \in \ddot{\sim} k)
                 df \leftarrow \vdash (\not \dashv \ddot{\sim}) \ (+ \setminus 1 = d) \ (\sim \dashv \in \dashv (/\ddot{\sim}) \ (1 = d) \ \land \ (\sim \ '\mathsf{b}' \in \ddot{\sim} \ k) \ \land \ O_{\scriptscriptstyle m} \lor F_{\scriptscriptstyle m}) \ \vdash
      dua \leftarrow ((\sim G_m) \land F_m \lor \downarrow \circ prf \in r \circ F_\circ) (\dashv (\downarrow \circ \vdash) (d (\not = ) \dashv) (0, 1 \downarrow (\bar{} 1 \oplus \vdash) \land \dashv = \bar{} 1 \oplus \dashv) \dashv (\not = \circ \vdash) 0 \in \bar{} n) \vdash (\downarrow \circ \vdash) 0 \vdash (\downarrow \circ \vdash) 0 \in \bar{} n) \vdash (\downarrow \circ \vdash) 0 \vdash (\downarrow \lor) 0 \vdash (\downarrow \circ \vdash) 0 
             du \leftarrow \vdash (\neq \sim \sim) dua \lor \circ (\lor /) (prf \land . (= \lor 0 = \vdash) \circ \lozenge prf (\neq \sim) dua) \land \uparrow \circ r \land . \geq \circ \lozenge dua (\neq \circ \vdash) \uparrow \circ r \times 0 = prf
            lfn \leftarrow (d, \mathsf{'Of'}, 3 \downarrow \vdash) \circ 1 \ at (F_m \land \mathsf{'b'} \in \stackrel{\sim}{\sim} k) (d, \mathsf{'Vf'}, (\mathsf{'fn'} \ enc \circ \supset r), 4 \downarrow \vdash) \circ 1 \ at (F_m \land 1 \in \stackrel{\sim}{\sim} k)
                     lf \leftarrow (\supset 5/) (1, 1 \downarrow F_m \land 1 \in k) blg (\uparrow r) (\subset lfh \circlearrowleft ((\vdash -(\supset -2 \mid \supset)) d), 1 \downarrow \circlearrowleft \vdash) lfn) \boxminus 1 \downarrow \vdash
            dn \leftarrow ((0 \in \stackrel{\sim}{\sim} n) \land (A_m \land \mathsf{v}' \in \stackrel{\sim}{\sim} k) \lor O_m \land \mathsf{f}' \in \stackrel{\sim}{\sim} k) ((\sim \dashv) (\not \to \vdash) (d - ^{-1} \oplus \dashv), 1 \downarrow_{\scriptscriptstyle{[1]}} \vdash) \vdash
mrep \leftarrow (1 + \supset), P' \circ (\ddot{,}'\vdash), (\subset''), \ddot{\sim} 1 \downarrow 4 \downarrow \circ, 1 \uparrow \vdash
mreu \leftarrow \supset, 'E' 'u', (\subset"), \stackrel{\sim}{\sim} \stackrel{\sim}{\sim} 1 \( \psi \) 3 \( \lor, 1 \\ \rac{\racksq}{\rightarrow} \)
      mre \leftarrow (\supset 5/) (-\circ \supset V_m \lor A_m) \circ \supset \circ \bigoplus (\downarrow, (((\vdash \rho = (\not\equiv \bigotimes), = \not\equiv \times 2 < \not\equiv) mreu ; mrep ; (1+d), 1 \downarrow = 1 \vdash) "\uparrow)) \vdash (\downarrow, (((\vdash p = (\not\equiv \bigotimes), = \not\equiv \times 2 < \not\equiv) mreu ; mrep ; (1+d), 1 \downarrow = 1 \vdash) "\uparrow)) \vdash (\downarrow, (((\vdash p = (\not\equiv \bigotimes), = (\not\equiv \bigotimes), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, ((\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\downarrow, (\vdash p = (\downarrow \bowtie), = (\downarrow, (\vdash p = (\vdash p = (\downarrow, (\vdash p = (\vdash p = (\downarrow, (\vdash p = (\downarrow, (\vdash p = (\vdash
      mrs \leftarrow \vdash \subset_{[0]} \stackrel{\sim}{\sim} 1, 1 \downarrow d = 1 + \circ \supset d
    mrk \leftarrow (-\circ(+/\wedge \setminus) \circ \bigoplus L_m) (\uparrow \neg \sim \circ (mre (mre mrs) \circ at (G_m \circ (\supset \neg /) 1 \uparrow \sim \vdash) \circ mrs) \downarrow) \vdash
           mr \leftarrow (\supset 5/) ((1 \uparrow \vdash), (mrk" 1 \downarrow \vdash)) \circ scp
              ur \leftarrow ((2 \uparrow \vdash), 1, ('um' enc \circ \supset r), 4 \downarrow \vdash) \circ 1 \ at (E_m \land 'u' \in \approx k)
                   rt \leftarrow \vdash, (\lor \lor F_m) + (+ \neq prf \land . (= \lor 0 = \dashv) \circ \lozenge \stackrel{\sim}{\sim} \circ \uparrow \circ r M_s = G_s) - F_m
         nm \leftarrow ((3 \uparrow \vdash), ('fe' enc \circ \supset r), 4 \downarrow \vdash) \circ 1 \ at ((0 \in \approx n) \land E_m \lor O_m \lor A_m)
            lgg \leftarrow (5/1\downarrow \vdash) 50\supset \stackrel{\sim}{\sim} \dashv (((^{-}1+d),2,\stackrel{\sim}{\sim}t,k,n,r,05,s); \stackrel{\sim}{\rightarrow} 53,\stackrel{\mathsf{'V'}}{,} \stackrel{\mathsf{'a'}}{,} 3(\downarrow \stackrel{\circ}{\circ}1)1\uparrow \vdash) 0\supset 1\uparrow \vdash 1)
              fe \leftarrow (\supset \bar{}) (+ + d \leq g) (\subset (\vdash \uparrow \approx 1 = \circ \not\equiv \vdash) \bar{} \circ \supset \circ fee \vdash) \models \vdash
       can \leftarrow (+ \setminus A_m \lor O_m) ((, 1 \uparrow \vdash), \circ (\subset ( \vdash 1 + 2 \mid \not\equiv) \supset (\subset \circ \subset \supset), \subset) \circ n \mid \downarrow \vdash) \mid \vdash \mid \vdash
         cas \leftarrow (\bar{\ }1 \oplus (A_m \vee O_m) \wedge '\mathbf{v} \mathbf{f}' \in \bar{\ }k) \vee (\downarrow prf) \in \bar{\ }r \vdash (\neq \bar{\ }) A_m \wedge '\mathbf{n}' \in \bar{\ }k
              ca \leftarrow (can \vdash (+\ddot{\sim}) cas \lor A_m \lor O_m \land 'f' \in \ddot{\sim} k) \dashv at (A_m \lor O_m \land 'f' \in \ddot{\sim} k) \vartheta, \circ \subset \ddot{\sim} \vdash (+\ddot{\sim} \circ \sim) cas
                     lj \leftarrow (\supset 5/) (1 \uparrow scp), ((\vdash 5 2 ' \vdash 0 0, 2 ", = 72 \downarrow 4 \downarrow 0, 1 \uparrow \vdash) " 1 \downarrow scp)
               sd \leftarrow (\supset 5/) (1 \uparrow scp), (n F) (d, \forall f', (\subset \dashv), 4 \downarrow \vdash) \circ 1 at ((\subset, \forall f') \in n) \circ 1 \downarrow scp
     inp \leftarrow (E_m \land \dashv) \lor 1, 2 \neq / \dashv
    inza \leftarrow (1 \uparrow 1 \downarrow \dashv) ( \not \vdash \sim \circ \not\equiv) at ((\subset, '\alpha') \in \sim n) ( \uparrow 1 \uparrow \dashv) ( \not \vdash \sim \circ \not\equiv) at ((\subset, '\omega') \in \sim n) \vdash
          inz \leftarrow (1 \uparrow \neg) (d, t, k, 3 \downarrow \ddot{\circ} 1 (\not \neg \circ \not\equiv)) at (0, \ddot{\sim} 2 \not=/\circ \bigoplus (\lor \lor \circ \bigoplus E_m)) inza
         inn \leftarrow (3 \uparrow \circ 1 \vdash), ((\dashv \rho \stackrel{\sim}{\sim} 1 + 0 \mid ([/ \circ n G)) (('fe' \equiv 2 \uparrow \vdash) \supset ( \subset \vdash), \circ \subset 'fe', ( \lnot \dashv), 2 \downarrow \vdash) \stackrel{\sim}{\sim} n), (4 \downarrow \circ 1 \vdash)
          ins \leftarrow \exists (d, t, k, ((1000 \times 1 + \exists) + 1 + n + ([/n)), 4 \downarrow \circ 1 \vdash) at (L_m \vee G_m) inn
           inr \leftarrow 1, \circ_{7} \vdash inz^{"}(\iota \circ_{7} \vdash) ins^{"}((\supset \circ n^{"} \dashv) \iota((\supset n (\not \vdash :) V_{m} \land 'f' \in : k)^{"} \vdash)) \supset "(\subset 1 \downarrow " \dashv), \circ \subset "\vdash
               in \leftarrow (\supset 5/) \circ (\vdash /) (1 \downarrow scp) inr \circ ((0 \rho \subset 0 \otimes \rho 0), \vdash /) at (\dashv /) inm ((\supset "inp \subset E_m \land \dashv), \circ 5 inp \subset_{[0]} \vdash) \vdash (\downarrow \land \land \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1) \circ 5 inp \subset_{[0]} \vdash (\downarrow \land) = (1 + 1)
```

```
pcc \leftarrow (\subset \vdash (\not \vdash \ddot{\sim}) A_m \lor O_m \land '\mathbf{f}' \in \ddot{\sim} k) \circ ((\iota \circ \cup \ddot{\sim} n) [ ] \ddot{\circ} 0 \ 2 \ (1 \ [ \not \equiv ) \uparrow \vdash) \circ (\supset_{7} \not +) \circ \oplus (\not + \circ \vdash)
pcb \leftarrow ((, \land . (= \lor 0 = \dashv) \circ \bar{\imath}) \circ 2 \ 1 \approx \circ \uparrow \circ r M_s \bar{\imath} F_s) pcc \circ 1 ((\vdash (\not+ \approx) (d = g) \land A_m \lor E_m \lor O_m) \circ scp)
 pcv \leftarrow (d, \forall V', (\exists f' \supset \circ \subset \sim O_m), (\supset v), r, s, (\subset \Theta), \sim g) at(O_m \lor A_m \land \forall v' \in \sim k)
     pc \leftarrow (\supset 5/) pcb \{ (pcv d (\dashv, 1 \downarrow \ddot{\circ} 1 \vdash) (\alpha \uparrow \ddot{\sim} 1 [\not\equiv \alpha) | \ddot{\circ} 0 2 \ddot{\sim} (n \alpha) \iota n) at (V_m \land (n \alpha) \in \tilde{\sim} n) \omega \} scp
   da \leftarrow \vdash (\neq \stackrel{\sim}{\sim} \circ \sim) (A_m \land d = g) \lor (0, \stackrel{\sim}{\sim} 2 \land / L_m) \lor (L_m \land \stackrel{\sim}{\sim} 1 \bigoplus A_m \land d = g) \lor O_m \land ('f' \in \stackrel{\sim}{\sim} k) \land 1 \neq d
   fce \leftarrow (\supset \circ n P_s) \{ \subset \Phi ' \omega', \ddot{\sim} (\not\equiv \omega) \supset "(\alpha, '\neg') ('\neg', \alpha, '\not/') \} (v A_s)
fcm \leftarrow (\land / E_m \lor A_m \lor P_m) \land \circ \sim 'ui' \in \sim \circ \supset \circ \supset k
       fc \leftarrow ((\supset 5/)^m (((d, ``An', `3 \downarrow \ ^1 \downarrow ,) \ 1 \uparrow \vdash), fce)`` at (fcm")) ('MFOEL' \in ~t) \subset_{[0]} \vdash
      ce \leftarrow (+ \ F_m \lor G_m \lor E_m \lor O_m \lor L_m) ((\ 1 \downarrow \circ, 1 \uparrow \vdash), \circ \subset (\supset \circ v \ 1 \uparrow \vdash), \circ (A_m \supset \circ \downarrow n, \circ 5 \circ n 2 f v) \ 1 \downarrow \vdash) 
         ll \leftarrow (\vdash (\not \vdash \ddot{\sim}) \ 1 \ \oplus \ L_{\scriptscriptstyle m}) \ (((\subset \subset \ \complement') \ , \circ \subset \ \ \ \circ \ n \ \dashv) \ , \ddot{\sim} \ \ 1 \ \downarrow \ddot{\circ} \ 1 \ \vdash) \ at \ L_{\scriptscriptstyle m} \ \vdash
       fv \leftarrow (\supset \bar{\gamma})(((1 \downarrow \vdash) \bar{\gamma} = (, 17 \uparrow \vdash), \circ \subset n^{-1} \uparrow \vdash) = scp)
    nv \leftarrow (\bar{\phantom{a}}1\downarrow \bar{\phantom{a}}1 \vdash), (\bar{\phantom{a}}1 \ominus \not\equiv \supset \vdash, \circ \subset \bar{\phantom{a}} (C'''' ''' f' '''' u'), (C'''' ''' i', \vdash), (C'(C'''' u'), \vdash)) \bar{\phantom{a}} v
         lt \leftarrow (\subset \theta), = \vdash
  val \leftarrow (n \bowtie n), \vdash (\vdash + (\not\equiv \dashv) \times 0 = \vdash) (\lceil / (\downarrow\not\equiv) \times \circlearrowleft 1 ( \cup n) \circ .((\subset \dashv) \in \vdash) (n2f \cdot v))
vag \leftarrow \land \circ \sim \circ (\circ . = \stackrel{\sim}{\sim} \circ 1 \not\equiv) \stackrel{\sim}{\sim} (\circ . (((1 \sqcap \vdash) > 0 \sqcap \dashv) \land (0 \sqcap \vdash) < 1 \sqcap \dashv) \stackrel{\sim}{\sim} val)
 vae \leftarrow (\cup n) (\exists, 0 \exists (\exists 0) ) \bigcirc ((\vdash, 0) (o \not\equiv \exists) \sim \vdash (\not\vdash () (\not\equiv \vdash) \uparrow \exists) (\circ ( \ominus \theta), 0 \downarrow \vdash)) vag
 vac \leftarrow (((0 \mid 0 \triangleleft \forall) \mid 0 \triangleleft \vdash) ) ) (1 \mid 0 \triangleleft \forall), 0 \triangleleft \vdash) ndo
    va \leftarrow ((\supset 5/) (1 \uparrow \vdash), (((vae E) (d, t, k, (\dashv vac n), r, s, g, y, \circ 5 \stackrel{\sim}{\sim} (\subset \dashv) vac \stackrel{\sim}{\circ} )) \vdash (1 \uparrow \vdash)) scp
avb \leftarrow \{(((, \ \ '' \alpha \omega') \uparrow \ \ 1 \downarrow \rho) \not \vdash) \alpha \ \ \square \ \ \ \circ \ 2 \ 0 \vdash \alpha \alpha \ \ 1 \ \alpha \alpha \cap \ \ (\downarrow (\bigoplus 1 + \circ 1 \ 0 \ 1 \ \ \vdash) ((\not \equiv \vdash) \uparrow \uparrow) \circ 0 \ 1 \vdash) \supset r \ \omega\}
  avi \leftarrow 10 + (\rho \dashv) T (, \dashv) \iota (C \vdash)
avh \leftarrow \{ \subset \omega, (n\omega) ((\alpha\alpha (\omega\omega avb) \omega) \{ \alpha\alpha avi ndo (\subset \alpha), \omega \}) "v \omega \}
     av \leftarrow (\supset^{\tau}) (+\backslash F_{w}) \{\alpha((\alpha((\cup \circ \oplus (0 \rho \subset "), n) E_{v}) \boxminus \omega) avh (r(1 \uparrow \omega), F_{v} \omega)) \boxminus \omega\} \vdash
     rlf \leftarrow (\bigoplus \downarrow (((1 \supset \dashv) \cup \vdash \sim 0 \sqcap \dashv) \land \ominus (\subseteq \theta), \uparrow) \circ 0 \ 1 = 1 + \circ 1 \not\equiv ) (\bigoplus 1 \ominus n, \circ 0 (\subseteq \dashv) \ veo = v)
       rl \leftarrow \vdash, \circ(\supset, /) (\subset \circ n \ O_s \ \overline{}, F_s) \ rlf \ scp
      vc \leftarrow (\supset 7)(((1 \downarrow \vdash) 7 \stackrel{\sim}{\rightarrow} (17 \uparrow \vdash), (\not\equiv \circ \cup \circ n E), 1^{-3} \uparrow \vdash) \stackrel{\sim}{\rightarrow} scp)
    eff \leftarrow (\supset 5/) \vdash (((\subset \circ \boxtimes \circ 5 d, Fe', 3 \downarrow ,) 1 \uparrow \dashv), 1 \downarrow \vdash) (d = \circ \supset d) \subset_{\omega} \vdash
       ef \leftarrow (F_m \land \overline{1} = \circ \times \circ \supset y) ((\supset \overline{5}/) (\subset \vdash (\not - \overline{a}) \circ \sim (\lor \lor \dashv)), (eff \subset (0))) \vdash (\downarrow - \overline{a}) \circ \sim (\lor \lor \dashv)
    ifn \leftarrow 1 'F' 0 'Init' \theta 0 1, (4 \rho 0) \theta \theta ,\approx \vdash
         if \leftarrow (1 \uparrow \vdash) \lnot (\vdash (\not \vdash \ddot{\sim}) O_m \land 1 = d) \lnot ((\vdash wrap \ddot{\sim} \circ ifn \circ \not\equiv \circ \cup n) \vdash (\not \vdash \ddot{\sim}) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ \vdash) \vdash (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ ) E_m \land 1 = d) \lnot (\lor \lor F_m) (\not\rightarrow \circ ) E_m \land 1 = d) (\not\rightarrow \circ ) E_m \land 1 = d) (\not\rightarrow \lor F_m) (\not\rightarrow \lor F
   fgz \leftarrow (1 \uparrow \vdash) ; (((\bar{\phantom{a}}1 + d), \bar{1} \downarrow \bar{\circ} 1 \vdash) 1 \downarrow \vdash) ; 2, 'G', 1, 3 \downarrow \bar{\circ} 1 (\bar{\phantom{a}}1 \uparrow \bar{\phantom{a}}1 \downarrow \bar{\circ} 1 \vdash) , \circ n 1 \uparrow \vdash
      fg \leftarrow (\supset \bar{\gamma}) (fgz\ddot{} at (G_m \circ (\supset \bar{\gamma})) \uparrow \ddot{} ) \vdash \subset_{iol} \ddot{} d = 2 \mid g)
     fft \leftarrow (, 1 \uparrow \vdash) (1 'Z', (2 \downarrow \lnot 5 \downarrow \dashv), (v \dashv), n, y, (\subset 2 \uparrow \circ, \circ \supset \circ \supset e), l) (\lnot 1 \uparrow E)
         ff \leftarrow ((\supset 7/) (1 \uparrow \vdash), (((1 \uparrow \vdash) 7 (((-1 + d), 1 \downarrow \circ 1 \vdash) 1 \downarrow \vdash) 7 fft) \downarrow \vdash)) scp
  fzh \leftarrow ((\cup n) \cap (\supset \circ l \dashv)) (\lnot 1 \oplus (\subset \dashv), ((\not\equiv \vdash) \lnot 1 + (\oplus n) \iota \dashv) ((\subset \dashv \supset \lnot \circ \subset (\supset \lnot e)), (\subset \dashv \supset \lnot \circ \subset (\supset \lnot y)), \circ \subset \dashv) \vdash) \vdash
    fzf \leftarrow 0 \neq (\not\equiv \circ \rho "\circ \supset \circ v \dashv)
  fzb \leftarrow (((\supset \circ v \dashv) (\not -\ddot{\sim}) fzf), n), \circ \overline{} (f' \circ, \circ \overline{\Phi}" \circ \iota (+/fzf)), (s' \circ, \circ \overline{\Phi}" \circ \iota \circ \not= \vdash)
   f_{ZV} \leftarrow (( \subset \dashv) ( \ominus \uparrow) \ddot{\sim} (\not\equiv \dashv) ( - + \circ \iota \vdash) (\not\equiv \vdash)) (( \vdash, \ddot{\sim} 1 \sqcap \circ \lozenge \dashv) \sqcap \ddot{\sim} (0 \sqcap \circ \lozenge \dashv) \iota \vdash) \ddot{\circ} 2 0 \ddot{\sim} V
   fze \leftarrow (\bar{1} + d), t, k, fzb ((\vdash/(-\circ \not\equiv \vdash) \uparrow \dashv), r, s, g, fzv, y, e, \circ, l) \vdash
   fzs \leftarrow (, 1 \uparrow \vdash) (1 \ominus (\dashv ((1 'Y', (2 \sqcap \dashv), \vdash) ; \circ \lozenge \circ ; (3 \uparrow \dashv), \vdash) 1 \oplus fzh, \lnot 1 \downarrow 6 \downarrow \dashv) ; fze) ( \not \vdash \circ \vdash)
      fz \leftarrow ((\supset \bar{\gamma}) (1 \uparrow \vdash), (((2 = d) (fzs \bar{\gamma} (1 \downarrow \circ \sim \dashv) (\not \rightarrow \vdash) 1 \downarrow \vdash) \vdash) "1 \downarrow \vdash)) (1, 1 \downarrow S_m) \subset_{(0)} \vdash
      fd \leftarrow (1 \uparrow \vdash) ; ((1, \vdash \mathsf{d}', 3 \downarrow \vdash) \circ 1 F) ; 1 \downarrow \vdash
tta \leftarrow (fc \circ da \circ (pc : \equiv) \circ mr : \equiv) \circ in : 3 \circ sdolj \circ ca \circ fe \circ lg \circ nm \circ rt \circ mr \circ dn \circ lf \circ du \circ df \circ rd \circ rn
     tt \leftarrow fd \circ fz \circ ff \circ fg \circ if \circ ef \circ vc \circ rl \circ av \circ va \circ lt \circ nv \circ fv \circ ll \circ ce \circ ur \circ tt a
```

```
E_i \leftarrow \{ \text{fn'gcl}((\subset n, \circ \supset v), e, y) \omega \}
   E_2 \leftarrow \{ \text{f n' } gcl ((\subset n, \circ \supset v), e, y) \omega \}
   E_i \leftarrow \{r \ l \ f \leftarrow \supset v \ \omega \diamond ((\supset n \ \omega) \ ('f \ n' \ var) \supset \supset e \ \omega), '=', ((\supset \supset v \ \omega) \ ('f \ n' \ var) \ 1 \supset \supset e \ \omega), ';', nl\}
   O_{\cdot} \leftarrow \{\text{'op' gcl}((\subset n, \circ \supset v), e, y) \omega\}
   O_2 \leftarrow \{\text{'op'} gcl ((\subset n, \circ \supset v), e, y) \omega\}
   O_0 \leftarrow \{"\}
   O_r \leftarrow \{ '\mathsf{EF}(', ('\Delta' \square \mathsf{R}'\_' \supset n \omega), ', ', (\supset v \omega), ') ; ', nl \}
   F_{d} \leftarrow \{\text{'FP(', (\neq n \, \omega), ');', nl}\}
F_{o} \leftarrow \{\text{'DF(', (\neq n \, \omega), ');', nl}\}
F_{l} \leftarrow \{\text{'DF(', (\neq n \, \omega), '_f )}\}, ', nl, 'A * env[] = \{\text{tenv}\};', nl\}
F_{l} \leftarrow \{\text{'DF(', (\neq n \, \omega), '_{l} f)}\}, ', nl, '(\text{env0'} dnv \, \omega), (fnv \, \omega)\}
   G_0 \leftarrow \{v \leftarrow (\supset v \omega) \ (\overline{var}) \ 1 \supset \supset e \omega \}
                           'if(1!=cnt(',v,'))err(5);if(',v,'.v.as(s32).scalar<I>()){', nl}
   G_{l} \leftarrow \{ z = ', ((\supset n \omega) ("var) \supset \supset e \omega), '; goto L', (\overline{\Phi} \supset l \omega), '; \}', nl \}
   L_0 \leftarrow \{ \exists z = ', a, '; L', (\overline{\Phi} \supset n \omega), ' : ', (a \leftarrow (1 \supset ) v \omega) ("var) 1 \supset (e \omega), ' = z; ', nl \} 
   Z_0^{\circ} \leftarrow \{'\}', nl, nl\}

Z_1 \leftarrow \{'\}', nl, nl\}
   Z_a \leftarrow \{'\}', nl, nl\}
  M_0 \leftarrow \{(rth \ \theta), (\text{'tenv'} \ dnv \ \omega), nl, \ 'A \star \text{env} [\ ] = \{', ((0 \equiv \supset \omega) \supset \text{'tenv'} \ 'NULL'), \ '\};', nl, nl\}
   S_0 \leftarrow \{(('\{', rk0, srk, 'DO(i, prk)cnt*=sp[i];', spp, sfv, slp)\omega)\}\}
   Y_0 \leftarrow \{ \supset / ((1 \not\equiv \supset n \omega) (( \dashv sts^{"}(\supset 1), "\circ \supset s), ' \}', nl, \dashv ste^{"}(\supset n) var^{"} \circ \supset r) \omega), ' \}', nl \}
gc \leftarrow \{ \supset, /\{0 = \supset t \omega : \subset 5 \rho \theta \diamond \subset ( ( \supset t \omega), \overline{\Phi} \supset k \omega) \omega \} \ddot{\circ} 1 \vdash \omega \}
                                     '-'
                                                   '×'
                                                                '÷'
                                                                                                                                            Ľ
                                                                                                                                                         ۲۲,
                                                                                                                                                                      '!'
                                                                                                                         'o'
                        'add' 'sub' 'mul'
                                                                                                                                            'min' 'max'
                                                               'div'
                                                                            'exp'
                                                                                          'log'
                                                                                                        'res'
                                                                                                                         'cir'
                                                                                                                                                                      'fac'
nams ←
 syms ,← ," '<'
                                                   '='
                                                                ′≥′
                                                                              '>'
                                                                                           '≠'
                                                                                                                         '^'
                                                                                                                                            'v'
                                                                                                                                                          '⊼'
                                                                                                                                                                       '∼'
                                     ′≤′
nams,← 'lth' 'lte' 'eql' 'gte'
                                                                            'gth' 'neq'
                                                                                                                          'and'
                                                                                                                                            'lor' 'nan'
                                                                                                                                                                      'nor'
 syms ,← ,¨ '[]'
                                     Έ,
                                                   'ι'
                                                                                                         'ф'
                                                                                                                         'φ'
                                                                                                                                                                       'ɔ'
                                                                'ρ'
                                                                                                                                            'Θ'
                                                                                                                                                         '∈'
                        'sqd' 'brk'
                                                                                          'ctf
                                                 'iot'
                                                                                                        'rot'
                                                                                                                         'trn'
                                                                                                                                            'rtf' 'mem' 'dis'
                                                               'rho'
                                                                             'cat'
 syms ,\leftarrow ," '\equiv'
                                      '≢'
                                                   ′⊢′
                                                                ′⊣′
                                                                              'т'
                                                                                           '⊥'
                                                                                                        '/'
                                                                                                                         '†'
                                                                                                                                                         Ή'
                                                                                                                                                                       '?'
                                                                                                                                            '\'
                                                              'lft'
nams, \leftarrow 'eqv'
                                    'nqv' 'rgt'
                                                                                          'dec'
                                                                                                       'red'
                                                                                                                                            'scn' 'scf' 'rol'
                                                                             'enc'
                                                                                                                         'rdf'
syms ,← ," '†'
nams ,← 'tke'
                                                                '∷'
                                                                                           ';'
                                                                                                        ′∵′
                                                                                                                                            ′υ′
                                      '↓'
                                                                                                                         'o'
                                                                                                                                                          'n
                                                  'map' 'com'
                                     'drp'
                                                                            'dot' 'rnk'
                                                                                                      'pow'
                                                                                                                         'jot'
                                                                                                                                            'unq' 'int'
 syms ,← , " '\'
                                                                             'c'
                                                  'o .'
                                                             '∈'
                                                                                           '⊟'
                                     'ቑ'
                                                                                                        '□FFT'
                                                                                                                         ′∐IFFT′′%u′
nams ,← 'gdu' 'gdd' 'oup' 'fnd' 'par' 'mdv' 'fft'
   nl \leftarrow \square UCS \ 13 \ 10 \diamond fvs \leftarrow , "0 \ (\neq ") \ 0 \neq (\not\equiv \circ \rho" \dashv) \diamond cln \leftarrow " \square R' - " \diamond cnm \leftarrow (syms \ \iota \subset) \supset (nams, \subset)
 lits \leftarrow \{ A (0, eshp, constant (', (cln \Phi \omega), ', eshp, ', ('f64' 's32' \supset \omega = [\omega), ') )' \}
 litv \leftarrow \{\text{'std::vector<'}, (\text{DI'} \supset \sim \land / \omega = \lfloor \omega \}, \text{'>}\{\text{'}, (cln \supset \{\alpha, ', ', \omega \} / \Phi^{\text{''}} \omega \}, '\} . \text{data()'}\}
 lit \leftarrow \{' \mid = 0 \text{ } \rho \text{ } \omega \text{ } : (cnm \text{ } \omega), \alpha \diamond 1 = \not\equiv \omega \text{ } : lits \text{ } \omega \diamond \text{ } lita \text{ } \omega\}
 var \leftarrow \{\alpha \equiv , \mathbf{\alpha}' : , \mathbf{l}' \diamond \alpha \equiv , \mathbf{\omega}' : , \mathbf{r}' \diamond \mathbf{1} \geq \supset \omega : \alpha \alpha \ lit , \alpha \diamond \mathbf{env}[', (\overline{\Phi} \supset \omega), '][', (\overline{\Phi} \supset \omega), ']'\}
dnv \leftarrow \{(0 \equiv z) \supset (A', \alpha, [', (\overline{\phi} z \leftarrow ) v \omega), '];') (A*', \alpha, '=NULL;')\}
 fnv \leftarrow \{z \leftarrow 'A \times env[', (\bar{\uparrow} 1 + \supset s \omega), '] = \{', (\supset, /(\subset 'env0'), \{', p[', (\bar{\uparrow} \omega), ']'\}" \mid \supset s \omega), '\};', nl\}
 gcl \leftarrow \{zrln \leftarrow ((3 \rho \subset fn'), \subset \alpha)\} \supset \alpha var/\omega\} \cup (\supset \omega), \forall l \supset \omega \land n, '(', (\supset \{\alpha, ', ', \omega\}/zlr \sim \subset fn'), ', env); ', nl\}
```

```
\nabla Z \leftarrow Gfx\Delta Init S
                     DNA'P', (BSOS), '| w_new <C[]'</pre>
   'w new'
   'w_close' □NA'I ', (BSOS), | w_close P'
                     \square NA(BSOS),' | w del P'
   'w del'
                     \square NA (BSOS), ' | w_{img} < PP P'
   'w_img'
   'w_plot' □NA(BSOS),'|w_plot <PP P'
   \mathsf{w\_hist'} \ \ \square \mathsf{NA} \ (BSOS), \ \mathsf{w\_hist} \ \mathsf{<PP} \ \mathsf{F8} \ \mathsf{F8} \ \mathsf{P'}
   'loadimg' \square NA (BSOS), '| loadimg >PP <C[] I'
   'saveimg' \square NA(BSOS), '| saveimg <PP <C[]'
   Z \leftarrow 0.0 \, \bar{\rho} \, \theta
     Display \leftarrow \{\alpha \leftarrow 'Co-dfns' \diamond W \leftarrow w\_new \subset \alpha \diamond 777 :: w\_del W
                                 w \det W \dashv W \alpha \alpha \{w \in Close \alpha : \Phi' \subseteq SIGNAL 777' \diamond \alpha \alpha \alpha \omega \} \# \omega \omega \vdash \omega \}
LoadImage \leftarrow \{\alpha \leftarrow 1 \diamond \bigotimes loadimg \vartheta \omega \alpha\}
SaveImage \leftarrow \{\alpha \leftarrow 'image.png' \diamond saveimg(\Diamond \omega) \alpha\}
       Image \leftarrow \{ \sim 2 \ 3 \ \lor .= \not\equiv \rho \omega : \square SIGNAL \ 4 \ \diamond \ (3 \not= 2 \supset 3 \uparrow \rho \omega) \land 3 = \not\equiv \rho \omega : \square SIGNAL \ 5 \ \diamond \omega \dashv w img \ ( \bigcirc \omega ) \ \alpha \}
           Plot \leftarrow \{2 \neq \not\equiv \rho\omega : \square SIGNAL \ 4 \diamond \sim 2 \ 3 \lor = 1 \supset \rho\omega : \square SIGNAL \ 5 \diamond \omega \dashv w\_plot (\lozenge\omega) \ \alpha\}
Histogram \leftarrow \{\omega \dashv w\_hist \omega, \alpha\}
\nabla r
                   \leftarrow List
                   \leftarrow \square NS" \ 1 \ \rho \subset \theta \diamond r.Name \leftarrow , " \subset "Compile" \diamond r.Group \leftarrow \subset "CODFNS"
   r
   r[0].Desc \leftarrow 'Compile an object using Co-dfns'
   r.Parse \leftarrow \subset '2S -af=cpu opencl cuda '
Convert \leftarrow \{\alpha ([SE.SALT.Load'[SALT]/lib/NStoScript -noname').ntgennscode \omega\}
              \leftarrow \{CI \leftarrow \omega \diamond in \ out \leftarrow I.Arguments \diamond AF\Delta LIB \circ \leftarrow I.af'' \supset \approx I.af \equiv 0
                    S \leftarrow (\subset' : Namespace', out), 2 \downarrow 0 0 0 out Convert ##.THIS. \psi in
                    'Compile' \equiv C: \{\} \{\#\#.THIS. \oplus out, ' \leftarrow \omega'\} \text{ out } Fix S\}
Help
              ←{'Usage: <object> <target> [-af={cpu,opencl,cuda}]'}
```

```
rth \leftarrow \{ \supset, / ( \subset nl ), "\stackrel{\sim}{\sim} 2 \downarrow "\stackrel{\sim}{\sim} 2 \downarrow c \downarrow \stackrel{\sim}{\sim} 1 + ( \subset 'rth' ) \iota \stackrel{\sim}{\sim} 3 \uparrow "c \leftarrow \square SRC \square THIS \}
A #include <time.h>
A #include <stdint.h>
A #include <inttypes.h>
A #include <limits.h>
A #include <float.h>
A #include <math.h>
A #include <memory>
A #include <algorithm>
A #include <string>
A #include <cstring>
A #include <vector>
A #include <unordered_map>
A #include <arrayfire.h>
A using namespace af;
Α
A #ifdef _WIN32
  #define EXPORT extern "C" __declspec(dllexport)
А
A #elif defined(__GNUC__)
  #define EXPORT extern "C" __attribute__ ((visibility ("default")))
A #define EXPORT extern "C"
A #endif
A #ifdef _MSC_VER
A #define RSTCT __restrict
A #else
A #define RSTCT restrict
A #endif
A #define S struct
A #define Z static
A #define R return
A #define RANK(lp) ((lp)->p->r)
A #define TYPE(lp) ((lp)->p->t)
A #define SHAPE(lp) ((lp)->p->s)
A #define ETYPE(lp) ((lp)->p->e)
A #define DATA(lp) ((V*)&SHAPE(lp)[RANK(lp)])
A #define CS(n,x) case n:x;break;
A #define DO(n,x) {I i=0,_i=(n);for(;i<_i;++i){x;}}
A #define DOB(n,x) {B i=0,_i=(n);for(;i<_i;++i){x;}}
A typedef enum{APLNC=0,APLU8,APLTI,APLSI,APLI,APLD,APLP,APLU,APLV,APLW,APLZ,
  APLR, APLF, APLQ } APLTYPE;
A typedef long long L; typedef int I; typedef int16_t S16;
A typedef int8_t S8; typedef double D; typedef unsigned char U8;
A typedef dim_t B; typedef unsigned U; typedef cdouble DZ;
A typedef void V; typedef std::string STR;
A S{U f=3;U n;U x=0;wchar_t*v=L"Co-dfns";const wchar_t*e;V*c;}dmx;
A S lp{S{L l;B c;U t:4;U r:4;U e:4;U _:13;U _1:16;U _2:16;B s[1];}*p;};
A S dwa{B z;S{B z;V*(*ga)(U,U,B*,S lp*);V(*p[16])(V);V(*er)(V*);}*ws;V*p[4];};
A S dwa*dwafns; Z V derr(U n){dmx.n=n;dwafns->ws->er(&dmx);}
A EXPORT I DyalogGetInterpreterFunctions(dwa*p){
  if(p)dwafns=p;else R 0;if(dwafns->z<sizeof(S dwa))R 16;R 0;}
A Z V err(U n,wchar_t*e){dmx.e=e;throw n;}Z V err(U n){dmx.e=L"";throw n;}
A S A{I r;dim4 s;array v;A(I r,dim4 s,array v):r(r),s(s),v(v){}
  A():r(0),s(dim4()),v(array()){}};
A int isinit=0;dim4 eshp=dim4(0,(B*)NULL);std::wstring msg;
ρ
```

```
A #define NM(n,nm,sm,sd,di,mf,df,ma,da) S n##_f:FN{di;mf;df;ma;da;\
A n##_f(STR s,I m,I d):FN(s,m,d){}} n##fn(nm,sm,sd);
A #define OM(n,nm,sm,sd,mf,df) S n##_o:MOP{mf;df;\
A n## o(FN&l,A*p[]):MOP(nm,sm,sd,l,p){}};
A #define OD(n,nm,sm,sd,mf,df) S n##_o:DOP{mf;df;\
 n##_o(FN&l,FN&r,A*p[]):DOP(nm,sm,sd,l,r,p){}\
 n##_o(const A&l,FN&r,A*p[]):DOP(nm,sm,sd,l,r,p){}\
  n##_o(FN&l,const A&r,A*p[]):DOP(nm,sm,sd,l,r,p){}};
А
A #define MT
A #define DID inline array id(dim4)
A #define MFD inline V operator()(A&,const A&,A*[])
A #define MAD inline V operator()(A&,const A&,D,A*[])
A #define DFD inline V operator()(A&,const A&,const A&,A*[])
A #define DAD inline V operator()(A&,const A&,const A&,D,A*[])
A #define DI(n) inline array n::id(dim4 s)
A #define ID(n,x,t) DI(n##_f){R constant(x,s,t);}
A #define MF(n) inline V n::operator()(A&z,const A&r,A*p[])
A #define MA(n) inline V n::operator()(A&z,const A&r,D ax,A*p[])
A #define DF(n) inline V n::operator()(A&z,const A&l,const A&r,A*p[])
A #define DA(n) inline V n::operator()(A&z,const A&l,const A&r,D ax,A*p[])
A #define SF(n,x) inline V n::operator()(A&z,const A&l,const A&r,A*p[]){\
  if(l.r==r.r&&l.s==r.s){\
   z.r=l.r;z.s=l.s;const array&lv=l.v;const array&rv=r.v;x;R;}\
Α
  if(!l.r){\
   z.r=r.r;z.s=r.s;const array&rv=r.v;array lv=tile(l.v,r.s);x;R;}\
Α
  if(!r.r){\
А
    z.r=l.r;z.s=l.s;array rv=tile(r.v,l.s);const array&lv=l.v;x;R;}\
Α
   if(l.r!=r.r)err(4);if(l.s!=r.s)err(5);err(99);}
A #define FP(n) NM(n,"",0,0,MT,MFD,DFD,MT,MT);MF(n##_f){n##fn(z,A(),r,p);}
A #define EF(n,m) EXPORT V n##_dwa(lp*z,lp*l,lp*r){try{\
    A cl,cr,za;if(!isinit){Initfn(za,cl,cr,NULL);isinit=1;}\
    cpda(cr,r);if(l!=NULL)cpda(cl,l);m##fn(za,cl,cr,env);cpad(z,za);}\
Α
   catch(U n){derr(n);}\
А
   catch(exception e){msg=mkstr(e.what());dmx.e=msg.c_str();derr(500);}}\
A EXPORT V n\#_{cdf}(A*z,A*l,A*r)\{try\{m\#_{fn}(*z,*l,*r,env);\}catch(U n)\{derr(n);\}
   catch(exception x){msg=mkstr(x.what());dmx.e=msg.c_str();derr(500);}}
Α
Α
A S FN\{STR nm; I sm; I sd; FN(STR nm, I sm, I sd): nm(nm), sm(sm), sd(sd) {}
  FN():nm(""),sm(0),sd(0){}
Α
  virtual array id(dim4 s){err(16);R array();}
Α
   virtual V operator()(A&z,const A&r,A*p[]){err(99);}
Α
  virtual V operator()(A&z,const A&r,D ax,A*p[]){err(99);}
Α
  virtual V operator()(A&z,const A&l,const A&r,A*p[]){err(99);}
Α
  virtual V operator()(A&z,const A&l,const A&r,D ax,A*p[]){err(99);}};
A FN MTFN;
A S MOP:FN{FN≪ A**pp;
  MOP(STR nm, I sm, I sd, FN&ll, A*pp[]):FN(nm, sm, sd), ll(ll), pp(pp){}};
A S DOP:FN{I fl;I fr;FN≪A aa;FN&rr;A ww;A**pp;
   DOP(STR nm,I sm,I sd,FN&l,FN&r,A*p[])
Α
   :FN(nm,sm,sd),fl(1),fr(1),ll(l),aa(A()),rr(r),ww(A()),pp(p){}
Α
   DOP(STR nm,I sm,I sd,A l,FN&r,A*p[])
Α
   :FN(nm,sm,sd),fl(0),fr(1),ll(MTFN),aa(l),rr(r),ww(A()),pp(p){}
Α
   DOP(STR nm,I sm,I sd,FN&l,A r,A*p[])
Α
    :FN(nm,sm,sd),fl(1),fr(0),ll(l),aa(A()),rr(MTFN),ww(r),pp(p){}};
Α
Α
```

```
A std::wstring mkstr(const char*s){B c=std::strlen(s);std::wstring t(c,L' ');
A mbstowcs(&t[0],s,c);R t;}
A I scm(FN&f)\{R f.sm;\}I scm(const A&a)\{R 1;\}
A I scd(FN&f){R f.sd;}I scd(const A&a){R 1;}
A B cnt(dim4 s){B c=1;DO(4,c*=s[i]);R c;}
A B cnt(const A&a){B c=1;DO(a.r,c*=a.s[i]);R c;}
A B cnt(lp*d){B c=1;DO(RANK(d),c*=SHAPE(d)[i]);R c;}
A array scl(I x){R constant(x,dim4(1),s32);}
A A scl(array v) \{R \ A(0,dim + (1),v);\}
A dtype mxt(dtype at,dtype bt){if(at==c64||bt==c64)R c64;
  if(at==f64||bt==f64)R f64;
  if(at==s32||bt==s32)R s32;if(at==s16||bt==s16)R s16;
Α
  if(at==b8||bt==b8)R b8;err(16);R f64;}
A dtype mxt(const array&a,const array&b){R mxt(a.type(),b.type());}
A dtype mxt(dtype at,const A&b){R mxt(at,b.v.type());}
A Z array da16(B c,dim4 s,lp*d){std::vector<S16>b(c);
  S8*v=(S8*)DATA(d);DOB(c,b[i]=v[i]);R array(s,b.data());}
A Z array da8(B c,dim4 s,lp*d){std::vector<char>b(c);
  U8*v=(U8*)DATA(d);DOB(c,b[i]=1&(v[i/8]>>(7-(i%8))))
А
  R array(s,b.data());}
A V cpad(lp*d,A&a){I t;B c=cnt(a);
  switch(a.v.type()){CS(c64,t=APLZ);
Α
    CS(s32,t=APLI);CS(s16,t=APLSI);CS(b8,t=APLTI);CS(f64,t=APLD);
    default:if(c)err(16);t=APLI;}
А
   B s[4];DO(a.r,s[a.r-(i+1)]=a.s[i]);dwafns->ws->ga(t,a.r,s,d);
Α
   if(c)a.v.host(DATA(d));}
А
A V cpda(A&a, lp*d) { if(15!=TYPE(d))err(16); if(4<RANK(d))err(16);
   dim4 s(1);DO(RANK(d),s[RANK(d)-(i+1)]=SHAPE(d)[i]);B c=cnt(d);
   switch(ETYPE(d)){
Α
    CS(APLZ, a=A(RANK(d), s, c?array(s, (DZ*)DATA(d)):scl(0)))
А
    CS(APLI, a=A(RANK(d), s, c?array(s, (I*)DATA(d)):scl(0)))
А
    CS(APLD, a=A(RANK(d), s, c?array(s, (D*)DATA(d)):scl(0)))
Α
    CS(APLSI, a=A(RANK(d), s, c?array(s, (S16*)DATA(d)):scl(0)))
А
Α
    CS(APLTI, a=A(RANK(d), s, c?da16(c, s, d):scl(0)))
    CS(APLU8, a=A(RANK(d), s, c?da8(c, s, d):scl(0)))
Α
    default:err(16);}}
Α
Α
```

```
A NM(add, "add", 1, 1, DID, MFD, DFD, MT
                                       ,MT )NM(sub, "sub", 1, 1, DID, MFD, DFD, MT
 NM(mul, "mul", 1, 1, DID, MFD, DFD, MT
                                            )NM(div, "div", 1, 1, DID, MFD, DFD, MT
                                       , MT
 NM(max, "max", 1, 1, DID, MFD, DFD, MT
                                            ) NM(min, "min", 1, 1, DID, MFD, DFD, MT
                                                                                  , MT
                                       , MT
                                            )NM(log,"log"
 NM(exp, "exp", 1, 1, DID, MFD, DFD, MT
                                                           ,1,1,MT ,MFD,DFD,MT
                                                                                   ,MT
                                       , MT
 NM(fac, "fac", 1, 1, DID, MFD, DFD, MT
                                       ,MT
                                            )NM(res, "res", 1, 1, DID, MFD, DFD, MT
                                                                                   , MT
                                            )NM(lor, "lor", 1, 1, DID, MT, DFD, MT
 NM(and, "and", 1, 1, DID, MT, DFD, MT
                                       , MT
                                                                                   , MT
 NM(lth,"lth",1,1,DID,MT ,DFD,MT
                                       ,MT )NM(lte,"lte",1,1,DID,MT ,DFD,MT
                                                                                   , MT
 NM(gth, "gth", 1, 1, DID, MT, DFD, MT
                                            )NM(gte, "gte", 1, 1, DID, MT, DFD, MT
                                       ,MT
                                                                                   , MT
А
 NM(eql, "eql", 1, 1, DID, MT, DFD, MT
                                       , MT
                                            )NM(neq, "neq", 1, 1, DID, MT , DFD, MT
                                                                                   , MT
A NM(nan, "nan", 1, 1, MT , MT , DFD, MT
                                            )NM(nor, "nor", 1, 1, MT , MT , DFD, MT
                                       ,MT
 NM(cir, "cir", 1, 1, MT , MFD, DFD, MT
                                            ) NM(not, "not", 1, 0, MT , MFD, DFD, MT
                                                                                   ,MT
                                       ,MT
 NM(rot, "rot", 0, 0, DID, MFD, DFD, MT
                                       ,MT
                                            )NM(rtf, "rtf", 0, 0, DID, MFD, DFD, MT
                                                                                   , MT
                                            )NM(rdf, "rdf", 0, 0, DID, MT, DFD, MT
 NM(red, "red", 0, 0, DID, MT, DFD, MT
                                                                                   ,MT
                                       ,MT
                                       ,MT )NM(scf, "scf", 0, 0, DID, MT , DFD, MT
A NM(scn, "scn", 0, 0, DID, MT, DFD, MT
                                                                                   ,MT
 NM(enc, "enc", 0, 0, DID, MT, DFD, MT
                                            )NM(dec, "dec", 0, 0, MT , MT , DFD, MT
                                       , MT
                                                                                   ,MT
                                                                                   , MT
A NM(sqd, "sqd", 0, 0, MT , MFD, DFD, MT
                                       ,MT )NM(brk, "brk", 0, 0, MT , MFD, DFD, MT
                                                                                       )
A NM(iot, "iot", 0, 0, MT , MFD, DFD, MT
                                       ,MT )NM(rho, "rho", 0, 0, MT ,MFD, DFD, MT
                                                                                   , MT
 NM(cat, "cat", 0, 0, MT , MFD, DFD, MT
                                       ,DAD)NM(ctf,"ctf",0,0,MT ,MFD,DFD,MT
                                                                                       )
                                                                                   , MT
                                            )NM(rol, "rol"
 NM(trn,"trn",0,0,MT
                                       ,MT
                         ,MFD,DFD,MT
                                                           ,1,0,MT
                                                                    ,MFD,DFD,MT
                                                                                   , MT
Α
 NM(dis,"dis",0,0,MT
                         ,MFD,DFD,MT
                                            )NM(par, "par", 0, 0, MT , MFD, DFD, MT
                                                                                   , MT
                                       , MT
 NM(eqv, "eqv", 0, 0, MT , MFD, DFD, MT
                                       ,MT )NM(nqv, "nqv", 0, 0, MT ,MFD, DFD, MT
 NM(rgt, "rgt", 0, 0, MT
                                       ,MT )NM(lft,"lft",0,0,MT
                         ,MFD,DFD,MT
                                                                    ,MFD,DFD,MT
                                                                                   , MT
                                            )NM(drp, "drp", 0, 0, MT
                                                                     ,MFD,DFD,MT
                                                                                   , MT
 NM(tke,"tke",0,0,MT
                         ,MFD,DFD,MT
                                       ,MT
                                                                                       )
 NM(unq, "unq", 0, 0, MT
                         ,MFD,DFD,MT
                                       ,MT
                                           )NM(int,"int",0,0,MT
                                                                    ,MT ,DFD,MT
                                                                                   ,MT
 NM(gdu, "gdu", 0, 0, MT
                                       ,MT )NM(gdd, "gdd", 0, 0, MT , MFD, DFD, MT
                         ,MFD,DFD,MT
                                                                                  , MT
                                                                                       )
 NM(mem, "mem", 0, 0, MT
                                            )NM(fnd, "fnd", 0, 0, MT , MT , DFD, MT
                                                                                       )
                         ,MFD,DFD,MT
                                       , MT
                                                                                   , MT
 NM(fft, "fft", 1, 0, MT , MFD, MT , MT ) NM(ift, "ift", 1, 0, MT , MFD, MT , MT
 NM(mdv, "mdv", 1, 0, MT , MFD, DFD, MT , MT )
A
A ID(add,0,s32)ID(sub,0,s32)ID(mul,1,s32)ID(div,1,s32)ID(res,0,s32)
 ID(min,DBL MAX,f64)ID(max,-DBL MAX,f64)ID(exp,1,s32)ID(fac,1,s32)
A ID(and,1,s32)ID(lor,0,s32)ID(lth,0,s32)ID(lte,1,s32)ID(eql,1,s32)
 ID(gth,0,s32)ID(gte,1,s32)ID(neq,0,s32)ID(enc,0,s32)ID(red,1,s32)
 ID(rdf,1,s32)ID(scn,1,s32)ID(scf,1,s32)ID(rot,0,s32)ID(rtf,0,s32)
А
A
 OD(brk, "brk", scm(l), scd(l), MFD, DFD)
 OM(com, "com", scm(l), scd(l), MFD, DFD)
 OD(dot, "dot", 0, 0, MT, DFD)
A OD(jot, "jot", (scm(l)&&scm(r)), (scd(l)&&scd(r)), MFD, DFD)
 OM(map, "map", 1, 1, MFD, DFD)
 OM(oup, "oup", 0, 0, MT, DFD)
Α
 OD(pow, "pow", scm(l), scd(l), MFD, DFD)
 OM(red, "red", 0, 0, MFD, DFD)
 OM(rdf, "rdf", 0, 0, MFD, DFD)
A OD(rnk, "rnk", scm(l), 0, MFD, DFD)
 OM(scn, "scn", 1, 1, MFD, MT)
A OM(scf, "scf", 1, 1, MFD, MT)
```

```
A MF(add_f){z=r;}
A SF(add_f,z.v=lv+rv)
A SF(and_f,if(lv.isbool()&&rv.isbool())z.v=lv&&rv;
   else if(allTrue<I>(lv>=0&&lv<=1&&rv>0&&rv<=1))z.v=lv&&rv;
   else{A a(z.r,z.s,lv); A b(z.r,z.s,rv);
Α
    lorfn(a,a,b,p);z.v=lv*(rv/((!a.v)+a.v));})
A MF(brk_f){err(16);}
A DF(brk_f){if(l.r!=1)err(16);
   z.r=r.r;z.s=r.s;z.v=l.v(r.v.as(s32));}
A MF(cat f){z.r=1;z.s[0]=cnt(r);z.v=flat(r.v);}
A DA(cat_f){A nl=l,nr=r;I fx=(I)ceil(ax);
Α
   if(fx<0||(fx>r.r&&fx>l.r))err(4);
   if(ax!=fx){if(r.r>3||l.r>3)err(10);
Α
    if(nl.r){nl.r++;DO(3-fx,nl.s[3-i]=nl.s[3-(i+1)]);nl.s[fx]=1;}
    if(nr.r){nr.r++;DO(3-fx,nr.s[3-i]=nr.s[3-(i+1)]);nr.s[fx]=1;}
Α
    if(nl.r)nl.v=moddims(nl.v,nl.s);if(nr.r)nr.v=moddims(nr.v,nr.s);
Α
Α
    catfn(z,nl,nr,fx,p);R;}
   if(fx>=r.r&&fx>=l.r)err(4);
Α
   if(l.r&&r.r&&std::abs((I)l.r-(I)r.r)>1)err(4);
А
   z.r=(l.r>=r.r)*l.r+(r.r>l.r)*r.r+(!r.r&&!l.r);
А
   dim4 ls=l.s:dim4 rs=r.s:
Α
   if(!l.r){ls=rs;ls[fx]=1;}if(!r.r){rs=ls;rs[fx]=1;}
А
Α
   if(r.r&&l.r>r.r){DO(3-fx,rs[3-i]=rs[3-(i+1)]);rs[fx]=1;}
  if(l.r&&r.r>l.r){DO(3-fx,ls[3-i]=ls[3-(i+1)]);ls[fx]=1;}
А
   DO(4, if(i!=fx&&rs[i]!=ls[i])err(5));
Α
   DO(4,z.s[i]=(l.r>=r.r||i==fx)*ls[i]+(r.r>l.r||i==fx)*rs[i]);
А
   if(!cnt(l)){z.v=r.v;R;}if(!cnt(r)){z.v=l.v;R;}
А
А
   dtype mt=mxt(r.v,l.v);
Α
   array lv=(l.r?moddims(l.v,ls):tile(l.v,ls)).as(mt);
   array rv=(r.r?moddims(r.v,rs):tile(r.v,rs)).as(mt);
Α
   z.v=join(fx,lv,rv);}
А
A DF(cat f){if(l.r||r.r){catfn(z,l,r,0,p);R;}
   A a,b;catfn(a,l,p);catfn(b,r,p);catfn(z,a,b,0,p);}
A MF(cir_f){z.r=r.r;z.s=r.s;z.v=Pi*r.v.as(f64);}
A SF(cir_f,array fv=rv.as(f64);
   if(!l.r){I x=l.v.as(s32).scalar<I>();if(abs(x)>10)err(16);
Α
    switch(x)\{CS(0,z.v=sqrt(1-fv*fv))CS(1,z.v=sin(fv))CS(2,z.v=cos(fv))\}
Α
     CS(3,z.v=tan(fv))CS(4,z.v=sqrt(1+fv*fv))CS(5,z.v=sinh(fv))
Α
     CS(6,z.v=cosh(fv))CS(7,z.v=tanh(fv))CS(8,z.v=sqrt(fv*fv-1))CS(9,z.v=fv)
Α
     CS(10,z.v=abs(fv))CS(-1,z.v=asin(fv))CS(-2,z.v=acos(fv))
Α
     CS(-3,z.v=atan(fv))CS(-4,z.v=(fv+1)*sqrt((fv-1)/(fv+1)))
Α
     CS(-5,z.v=asinh(fv))CS(-6,z.v=acosh(fv))CS(-7,z.v=atanh(fv))
Α
Α
     CS(-8,z.v=-sqrt(fv*fv-1))CS(-9,z.v=fv)CS(-10,z.v=fv)R;
   if(anyTrue<I>(abs(lv)>10))err(16);B c=cnt(z);std::vector<I> a(c);
Α
Α
   std::vector<D> b(c);lv.as(s32).host(a.data());fv.host(b.data());
   std::vector<D> zv(c);
Α
   DOB(c,switch(a[i])\{CS(0,zv[i]=sqrt(1-b[i]*b[i]))CS(1,zv[i]=sin(b[i]))
Α
    CS(2,zv[i]=cos(b[i]))CS(3,zv[i]=tan(b[i]))CS(4,zv[i]=sqrt(1+b[i]*b[i]))
Α
    CS(5,zv[i]=sinh(b[i]))CS(6,zv[i]=cosh(b[i]))CS(7,zv[i]=tanh(b[i]))
Α
    CS(8,zv[i]=sqrt(b[i]*b[i]-1))CS(9,zv[i]=b[i])CS(10,zv[i]=abs(b[i]))
Α
    CS(-1,zv[i]=asin(b[i]))CS(-2,zv[i]=acos(b[i]))CS(-3,zv[i]=atan(b[i]))
Α
    CS(-4, zv[i] = (b[i] = -1)?0:(b[i] + 1)*sqrt((b[i] - 1)/(b[i] + 1)))
Α
    CS(-5,zv[i]=asinh(b[i]))CS(-6,zv[i]=acosh(b[i]))CS(-7,zv[i]=atanh(b[i]))
Α
    CS(-8,zv[i]=-sqrt(b[i]*b[i]-1))CS(-9,zv[i]=b[i])CS(-10,zv[i]=b[i])})
Α
   z.v=array(z.s,zv.data());)
A MF(ctf_f){dim4 sp=z.s;sp[1]=r.r?r.s[r.r-1]:1;sp[0]=sp[1]?cnt(r)/sp[1]:1;
   sp[2]=sp[3]=1;z.r=2;z.s=sp;z.v=!cnt(z)?scl(0):array(r.v,z.s);}
A DF(ctf_f){I x=l.r>r.r?l.r:r.r;if(l.r||r.r){catfn(z,l,r,x-1,p);R;}
  A a,b;catfn(a,l,p);catfn(b,r,p);catfn(z,a,b,0,p);}
```

```
A DF(dec_f){I ra=r.r?r.r-1:0;I la=l.r?l.r-1:0;z.r=ra+la;z.s=dim4(1);
   if(l.s[0]!=1&&l.s[0]!=r.s[ra]&&r.s[ra]!=1)err(5);
   DO(ra,z.s[i]=r.s[i])DO(la,z.s[i+ra]=l.s[i+1])
   if(!cnt(z)){z.v=scl(0);R;}
А
   if(!cnt(r)||!cnt(l)){z.v=constant(0,z.s,s32);R;}
А
   B lc=l.s[0];array x=l.v;if(lc==1){lc=r.s[ra];x=tile(x,(I)lc);}
А
   x=flip(scan(x,0,AF_BINARY_MUL,false),0);
А
   x=array(x,lc,x.elements()/lc).as(f64);
А
   array y=array(r.v,cnt(r)/r.s[ra],r.s[ra]).as(f64);
А
   z.v=array(matmul(r.s[ra]==1?tile(y,1,(I)l.s[0]):y,x),z.s);}
Α
A MF(dis_f){z.r=0;z.s=eshp;z.v=r.v(0);}
A DF(dis_f){if(l.v.isfloating())err(1);if(l.r>1)err(4);
   B lc=cnt(l);if(!lc){z=r;R;}if(lc!=1||r.r!=1)err(4);
  if(allTrue<char>(cnt(r)<=l.v(0)))err(3);</pre>
Α
   z.r=0;z.s=eshp;array i=l.v(0);z.v=r.v(i);}
A MF(div_f){z.r=r.r;z.s=r.s;z.v=1.0/r.v.as(f64);}
A SF(div_f,z.v=lv.as(f64)/rv.as(f64))
A MF(drp_f){if(r.r)err(16);z=r;}
A DF(drp_f){I lv[4];seq it[4];seq ix[4];B c=cnt(l);
   if(l.r>1||(c>r.r&&r.r))err(4);if(!c){z=r;R;}
Α
   U rk=r.r?r.r:(U)l.s[0];z.r=rk;z.s=r.s;l.v.as(s32).host(lv);
Α
   DO((I)c,{U j=rk-(i+1);I a=std::abs(lv[i]);
Α
    if(a>=r.s[j]){z.s[j]=0;ix[j]=seq(0);it[j]=seq(0);}
Α
    else if(lv[i]<0){
Α
     z.s[j]=r.s[j]-a;ix[j]=seq((D)z.s[j]);it[j]=ix[j];}
Α
    else{z.s[j]=r.s[j]-a;ix[j]=seq(a,(D)r.s[j]-1);it[j]=ix[j]-(D)a;}})
А
   if(!cnt(z)){z.v=scl(0);R;}z.v=array(z.s,r.v.type());z.v=0;
А
   z.v(it[0],it[1],it[2],it[3])=r.v(ix[0],ix[1],ix[2],ix[3]);}
A DF(enc_f){I rk=r.r+l.r;if(rk>4)err(16);dim4 sp=r.s;DO(l.r,sp[i+r.r]=l.s[i])
  if(!cnt(sp)){z.r=rk;z.s=sp;z.v=scl(0);R;}dim4 lt=sp,rt=sp;I k=l.r?l.r-1:0;
А
   DO(r.r,rt[i]=1)DO(l.r,lt[i+r.r]=1)array rv=tile(r.v,rt);z.r=rk;z.s=sp;
А
   array sv=flip(scan(flip(l.v,k),k,AF_BINARY_MUL),k);
Α
  array lv=tile(array(sv,rt),lt);af::index x[4];x[k]=0;
Α
Α
   array dv=sv;dv(x[0],x[1],x[2],x[3])=1;I s[]={0,0,0,0};s[k]=-1;
  dv=shift(dv,s[0],s[1],s[2],s[3]);dv=tile(array(dv,rt),lt);
  z.v=(lv!=0)*rem(rv,lv)+(lv==0)*rv;z.v=(dv!=0)*(z.v/dv).as(s32);
A SF(eql f,z.v=lv==rv)
A MF(eqv_f){z.r=0;z.s=eshp;z.v=scl(r.r!=0);}
A DF(eqv f)\{z.r=0;z.s=eshp;
  if(l.r==r.r&&l.s==r.s){z.v=allTrue(l.v==r.v);R;}z.v=scl(0);}
Α
A MF(exp_f){z.r=r.r;z.s=r.s;z.v=exp(r.v.as(f64));}
A SF(exp_f,z.v=pow(lv.as(f64),rv.as(f64)))
A MF(fac_f){z.r=r.r;z.s=r.s;z.v=factorial(r.v.as(f64));}
A SF(fac_f,array lvf=lv.as(f64);array rvf=rv.as(f64);
  z.v=exp(log(tgamma(lvf))+log(tgamma(rvf))-log(tgamma(lvf+rvf))))
Α
A MF(fft_f){z.r=r.r;z.s=r.s;z.v=dft(r.v.type()==c64?r.v:r.v.as(c64),1,r.s);}
A MF(ift_f){z.r=r.r;z.s=r.s;z.v=idft(r.v.type()==c64?r.v:r.v.as(c64),1,r.s);}
A DF(fnd_f){A t(r.r,r.s,array(r.s,b8));if(!cnt(t)){t.v=scl(0);z=t;R;}
   t.v=0;if(l.r>r.r){z=t;R;}DO(4,if(l.s[i]>r.s[i]){z=t;R;})
Α
   if(!cnt(l)){t.v=1;z=t;R;}dim4 sp;DO(4,sp[i]=1+(t.s[i]-l.s[i]))
   seq x[4];DO(4,x[i]=seq((D)sp[i]))t.v(x[0],x[1],x[2],x[3])=1;
Α
   DO((I)l.s[0],I m=i;
Α
   DO((I)l.s[1],I k=i;
Α
     DO((I)l.s[2],I j=i;
Α
      DO((I)l.s[3],t.v(x[0],x[1],x[2],x[3])=t.v(x[0],x[1],x[2],x[3])
Α
Α
       &(tile(l.v(m,k,j,i),sp)
        ==r.v(x[0]+(D)m,x[1]+(D)k,x[2]+(D)j,x[3]+(D)i)))))
Α
Α
   z=t;}
Α
```

```
A MF(gdd_f){if(r.r<1)err(4);z.r=1;z.s=dim4(r.s[r.r-1]);
  if(!cnt(r)){z.v=r.v;R;}I c=1;DO(r.r-1,c*=(I)r.s[i]);
   array mt,a=array(r.v,c,r.s[r.r-1]);z.v=iota(z.s,dim4(1),s32);
   DO(c,sort(mt,z.v,flat(a(c-(i+1),z.v)),z.v,0,false))}
A DF(gdd_f){err(16);}
A MF(qdu f){if(r.r<1)err(4);z.r=1;z.s=dim4(r.s[r.r-1]);
  if(!cnt(r)){z.v=r.v;R;}I c=1;DO(r.r-1,c*=(I)r.s[i]);
   array mt,a=array(r.v,c,r.s[r.r-1]);z.v=iota(z.s,dim4(1),s32);
А
   DO(c, sort(mt, z.v, flat(a(c-(i+1), z.v)), z.v, 0, true)))
А
A DF(gdu_f){err(16);}
A SF(gte_f,z.v=lv>=rv)
A SF(gth_f,z.v=lv>rv)
A DF(int_f){if(r.r>1||l.r>1)err(4);
  if(!cnt(r)||!cnt(l)){z.v=scl(0);z.s=dim4(0);z.r=1;R;}
  dtype mt=mxt(l.v,r.v);z.v=setIntersect(l.v.as(mt),r.v.as(mt));
Α
  z.r=1;z.s=dim4(z.v.elements());}
А
A MF(iot_f){if(r.r>1)err(4);B c=cnt(r);if(c>4)err(10);
  if(c>1)err(16);
   z.r=1;z.s=dim4(r.v.as(s32).scalar<I>());
Α
  z.v=z.s[0]?iota(z.s,dim4(1),s32):scl(0);}
A DF(iot f){z.r=r.r;z.s=r.s;B c=cnt(r);if(!c){z.v=scl(0);R;}
  B lc=cnt(l)+1;if(lc==1){z.v=scl(0);R;};if(l.r>1)err(16);
  array rf=flat(r.v).T();dtype mt=mxt(l.v,rf);
Α
  z.v=join(0,tile(l.v,1,(U)c).as(mt),rf.as(mt))==tile(rf,(U)lc,1);
  z.v=min((z.v*iota(dim4(lc),dim4(1,c),s32)+((!z.v)*lc).as(s32)),0);
  z.v=array(z.v,z.s);}
A MF(lft_f){z=r;}
A DF(lft_f){z=l;}
A MF(log_f){z.r=r.r;z.s=r.s;z.v=log(r.v.as(f64));}
A SF(log_f,z.v=log(rv.as(f64))/log(lv.as(f64)))
A SF(lor f, if(rv.isbool()&&lv.isbool())z.v=lv||rv;
   else if(lv.isbool()&&rv.isinteger())z.v=lv+(!lv)*abs(rv).as(rv.type());
   else if(rv.isbool()&&lv.isinteger())z.v=rv+(!rv)*abs(lv).as(lv.type());
   else if(lv.isinteger()&&rv.isinteger()){B c=cnt(z);
Α
    std::vector<I> a(c);abs(lv).as(s32).host(a.data());
    std::vector<I> b(c);abs(rv).as(s32).host(b.data());
Α
    DOB(c,while(b[i]){I t=b[i];b[i]=a[i]%b[i];a[i]=t;})
А
А
    z.v=array(z.s,a.data());}
   else{B c=cnt(z);
А
    std::vector<D> a(c);abs(lv).as(f64).host(a.data());
Α
    std::vector<D> b(c);abs(rv).as(f64).host(b.data());
А
    DOB(c, while(b[i]>1e-12)\{D t=b[i]; b[i]=fmod(a[i], b[i]); a[i]=t;\})
А
Α
    z.v=array(z.s,a.data());})
A SF(lte_f,z.v=lv<=rv)
A SF(lth_f,z.v=lv<rv)
A MF(max_f){z.r=r.r;z.s=r.s;z.v=ceil(r.v).as(r.v.type());}
A SF(max_f,z.v=max(lv,rv))
A MF(mem f){z.r=1;z.s=dim4(cnt(r));z.v=flat(r.v);}
 A DF(mem_f)\{z.r=l.r;z.s=l.s;I lc=(I)cnt(z);if(!lc)\{z.v=scl(0);R;\} 
  if(!cnt(r)){z.v=array(z.s,b8);z.v=0;R;}
Α
  array y=setUnique(flat(r.v));I rc=(I)y.elements();
Α
   array x=array(flat(l.v),lc,1);y=array(y,1,rc);
Α
   z.v=array(anyTrue(tile(x,1,rc)==tile(y,lc,1),1),z.s);}
А
A MF(mdv_f){if(r.r>2)err(4);if(r.r==2&&r.s[1]<r.s[0])err(5);if(!cnt(r))err(5);</pre>
   if(r.s[0]==r.s[1]){z.r=r.r;z.s=r.s;z.v=inverse(r.v);R;}
Α
   if(r.r==1){z.v=matmulNT(inverse(matmulTN(r.v,r.v)),r.v);z.r=r.r;z.s=r.s;R;}
   z.v=matmulTN(inverse(matmulNT(r.v,r.v)),r.v);z.r=r.r;z.s=r.s;
   B k=z.s[0];z.s[0]=z.s[1];z.s[1]=k;z.v=transpose(z.v);}
Α
Α
```

```
A DF(mdv f){if(r.r>2)err(4);if(l.r>2)err(4);if(r.r==2&&r.s[1]<r.s[0])err(5);</pre>
   if(!cnt(r)||!cnt(l))err(5);if(r.r&&l.r&&l.s[l.r-1]!=r.s[r.r-1])err(5);
   array rv=r.v,lv=l.v;if(r.r==1)rv=transpose(rv);if(l.r==1)lv=transpose(lv);
  z.v=transpose(matmul(inverse(matmulNT(rv,rv)),matmulNT(rv,lv)));
  z.r=(l.r-(l.r>0))+(r.r-(r.r>0));
Α
  if(l.r>1)z.s[0]=l.s[0];if(r.r>1)z.s[l.r>1]=r.s[0];}
A MF(min_f){z.r=r.r;z.s=r.s;z.v=floor(r.v).as(r.v.type());}
A SF(min_f,z.v=min(lv,rv))
A MF(mul_f){z.r=r.r;z.s=r.s;z.v=(r.v>0)-(r.v<0);}
A SF(mul f,z.v=lv*rv)
A SF(nan f,z.v=!(lv\&rv))
A SF(neq_f,z.v=lv!=rv)
A SF(nor_f,z.v=!(lv||rv))
A MF(not_f){z.r=r.r;z.s=r.s;z.v=!r.v;}
A DF(not f){err(16);}
A MF(nqv_f){z.v=scl(r.r?(I)r.s[r.r-1]:1);z.r=0;z.s=dim4(1);}
A DF(nqv f){z.r=0;z.s=eshp;I t=l.r==r.r&&l.s==r.s;
   if(t)t=allTrue<I>(l.v==r.v);z.v=scl(!t);}
A MF(par_f){err(16);}
A DF(par_f){err(16);}
A DF(red f){if(l.r>1)err(4);z.r=r.r?r.r:1;z.s=r.s;
  if(l.r!=0&&l.s[0]!=1&&r.r!=0&&r.s[0]!=1&&l.s[0]!=r.s[0])err(5);
Α
   array x=l.v;if(cnt(l)==1)x=tile(x,(I)r.s[0]);
   array y=r.v;if(r.s[0]==1)y=tile(y,(I)cnt(l));
   z.s[0]=sum<B>(abs(x));if(!cnt(z)){z.v=scl(0);R;}
Α
   array w=where(x).as(s32);
А
   if(z.s[0]==w.elements()){z.v=y(w,span);R;}
А
   array i=shift(accum(abs(x(w))),1),d=shift(w,1);i(0)=0;d(0)=0;
А
   array v=array(z.s[0],s32),u=array(z.s[0],s32);v=0;u=0;
Α
   array s=(!sign(x(w))).as(s32);array t=shift(s,1);t(0)=0;
Α
   v(i)=w-d;u(i)=s-t;z.v=y(accum(v),span);
А
   z.v*=tile(accum(u),1,(I)z.s[1],(I)z.s[2],(I)z.s[3]);}
Α
A MF(res_f){z.r=r.r;z.s=r.s;z.v=abs(r.v).as(r.v.type());}
A SF(res_f, z.v=rv-lv*floor(rv.as(f64)/(lv+(0==lv))))
A DF(rdf_f){if(l.r>1)err(4);I ra=r.r?r.r-1:0;z.r=ra+1;z.s=r.s;
  if(l.r!=0&&l.s[0]!=1&&r.r!=0&&r.s[ra]!=1&&l.s[0]!=r.s[ra])err(5);
А
   array x=l.v; array y=r.v; if(cnt(l)==1)x=tile(x,(I)r.s[ra]);
А
   if(r.s[ra]==1){dim4 s(1);s[ra]=cnt(l);y=tile(y,s);}
А
   z.s[ra]=sum<B>(abs(x));if(!cnt(z)){z.v=scl(0);R;}
А
   array w=where(x).as(s32);af::index ix[4];if(z.s[ra]==w.elements()){}
Α
   ix[ra]=w;z.v=y(ix[0],ix[1],ix[2],ix[3]);R;}
А
   array i=shift(accum(abs(x(w))),1),d=shift(w,1);i(0)=0;d(0)=0;
А
Α
   array v=array(z.s[ra],s32),u=array(z.s[ra],s32);v=0;u=0;
   array s=(!sign(x(w))).as(s32);array t=shift(s,1);t(0)=0;
Α
Α
  v(i)=w-d;u(i)=s-t;ix[ra]=accum(v);z.v=y(ix[0],ix[1],ix[2],ix[3]);
   dim4 s1(1),s2(z.s);s1[ra]=z.s[ra];s2[ra]=1;u=array(accum(u),s1);
   z.v*=tile(u,(I)s2[0],(I)s2[1],(I)s2[2],(I)s2[3]);}
Α
A MF(rgt f){z=r;}
A DF(rgt_f){z=r;}
A MF(rho_f){I sp[4]={1,1,1,1};DO(r.r,sp[r.r-(i+1)]=(I)r.s[i]);
  z.s=dim4(r.r);z.r=1;if(!cnt(z)){z.v=scl(0);R;}z.v=array(z.s,sp);}
A DF(rho_f){B cr=cnt(r);B cl=cnt(l);B s[4];if(l.r>1)err(11);if(cl>4)err(16);
  l.v.as(s64).host(s);z.r=(I)cl;DO(4,z.s[i]=i>=z.r?1:s[z.r-(i+1)])B cz=cnt(z);
  if(!cz){z.v=scl(0);R;}z.v=array(cz==cr?r.v:flat(r.v)(iota(cz)%cr),z.s);}
A MF(rol_f){z.r=r.r;z.s=r.s;if(!cnt(r)){z.v=r.v;R;}
   array rnd=randu(r.v.dims(),f64);z.v=(0==r.v)*rnd+trunc(r.v*rnd);}
Α
Α
```

```
A DF(rol_f){if(cnt(r)!=1||cnt(l)!=1)err(5);
   D lv=l.v.as(f64).scalar<D>();D rv=r.v.as(f64).scalar<D>();
  if(lv>rv||lv!=floor(lv)||rv!=floor(rv)||lv<0||rv<0)err(11);
   I = (I) | v; I = (I) | v; z.r = 1; z.s = dim + (s); if (!s) \{z.v = scl(0); R; \}
   std::vector<I> g(t);std::vector<I> d(t);
А
  ((1+range(t))*randu(t)).as(s32).host(q.data());
   DO(t,I j=g[i];if(i!=j)d[i]=d[j];d[j]=i)z.v=array(z.s,d.data());}
А
A MF(rot_f){z.r=r.r;z.s=r.s;z.v=flip(r.v,0);}
A DF(rot f){I lc=(I)cnt(l); if(lc==1){z.r=r.r;z.s=r.s;
    z.v=shift(r.v,-l.v.as(s32).scalar<I>());R;}
Α
   if(l.r!=r.r-1)err(5);DO(l.r,if(l.s[i]!=r.s[i+1])err(5))
Α
Α
   std::vector<I> x(lc);l.v.as(s32).host(x.data());
   z.v=array(r.v,r.s[0],lc);z.r=r.r;z.s=r.s;
   DO(lc,z.v(span,i)=shift(z.v(span,i),-x[i]))z.v=array(z.v,z.s);
A MF(rtf f){z.r=r.r;z.s=r.s;z.v=r.r?flip(r.v,r.r-1):r.v;}
n DF(rtf_f){I lc=(I)cnt(l);I ra=r.r?r.r-1:0;I ix[]={0,0,0,0};
   if(lc==1){z.r=r.r;z.s=r.s;ix[ra]=-l.v.as(s32).scalar<I>();
Α
    z.v=shift(r.v,ix[0],ix[1],ix[2],ix[3]);R;}
Α
   if(l.r!=r.r-1)err(5);DO(l.r,if(l.s[i]!=r.s[i])err(5))
А
   std::vector<I> x(lc);l.v.as(s32).host(x.data());
Α
   z.v=array(r.v,lc,r.s[ra]);z.r=r.r;z.s=r.s;
Α
   DO(lc,z.v(i,span)=shift(z.v(i,span),0,-x[i]))
Α
Α
   z.v=array(z.v,z.s);}
A DF(scn_f){if(r.s[0]!=1&&r.s[0]!=sum<I>(l.v>0))err(5);
   if(l.r>1)err(5);array ca=max(1,abs(l.v)).as(s32);I c=sum<I>(ca);
   if(!cnt(l))c=0;A t(r.r?r.r:1,r.s,scl(0));t.s[0]=c;
Α
   if(!cnt(t)){z=t;R;}t.v=array(t.s,r.v.type());t.v=0;
Α
А
   array pw=0<l.v;array pa=pw*l.v;I pc=sum<I>(pa);if(!pc){z=t;R;}
Α
   pw=where(pw);pa=scan(pa(pw),0,AF_BINARY_ADD,false);
   array si(pc,s32);si=0;si(pa)=1;si=accum(si)-1;
Α
   array ti(pc,s32);ti=1;ti(pa)=scan(ca,0,AF_BINARY_ADD,false)(pw);
Α
   ti=scanByKey(si,ti);t.v(ti,span)=r.v(si,span);z=t;}
A DF(scf_f){I ra=r.r?r.r-1:0;af::index sx[4];af::index tx[4];
Α
   if(r.s[ra]!=1&&r.s[ra]!=sum<I>(l.v>0))err(5);
  if(l.r>1)err(5);array ca=max(1,abs(l.v)).as(s32);I c=sum<I>(ca);
А
  if(!cnt(l))c=0;A t(ra+1,r.s,scl(0));t.s[ra]=c;
Α
   if(!cnt(t)){z=t;R;}t.v=array(t.s,r.v.type());t.v=0;
А
   array pw=0<l.v;array pa=pw*l.v;I pc=sum<I>(pa);if(!pc){z=t;R;}
А
   pw=where(pw);pa=scan(pa(pw),0,AF_BINARY_ADD,false);
Α
   array si(pc,s32);si=0;si(pa)=1;si=accum(si)-1;sx[ra]=si;
Α
   array ti(pc,s32);ti=1;ti(pa)=scan(ca,0,AF_BINARY_ADD,false)(pw);
Α
  ti=scanByKey(si,ti);tx[ra]=ti;
Α
   t.v(tx[0],tx[1],tx[2],tx[3])=r.v(sx[0],sx[1],sx[2],sx[3]);z=t;}
A MF(sqd_f){z=r;}
A DF(sqd_f){if(l.r>1)err(4);B s=!l.r?1:l.s[l.r-1];
  if(s>r.r)err(5);if(!cnt(l)){z=r;R;}
  I sv[4];af::index x[4];l.v.as(s32).host(sv);
  DO((I)s,if(sv[i]<0||sv[i]>=r.s[i])err(3));
Α
  DO((I)s,x[r.r-(i+1)]=sv[i]);z.r=r.r-(U)s;z.s=dim4(z.r,r.s.get());
   z.v=r.v(x[0],x[1],x[2],x[3]);
A MF(sub_f){z.r=r.r;z.s=r.s;z.v=-r.v;}
A SF(sub_f,z.v=lv-rv)
A MF(tke_f){z=r;}
Α
```

```
A DF(tke_f){I lv[4];seq it[4];seq ix[4];B c=cnt(l);
   if(l.r>1||(c>r.r&&r.r))err(4);if(!c){z=r;R;}
   U rk=r.r?r.r:(U)l.s[0];z.r=rk;z.s=r.s;l.v.as(s32).host(lv);
   DO((I)c,{U j=rk-(i+1);I a=std::abs(lv[i]);z.s[j]=a;
    if(a>r.s[j])ix[j]=seq((D)r.s[j]);
Α
    else if(lv[i]<0)ix[j]=seq((D)r.s[j]-a,(D)r.s[j]-1);
Α
    else ix[j]=seq(a);
Α
    it[j]=ix[j]+(lv[i]<0)*(a-(D)r.s[j]);})
Α
Α
   if(!cnt(z)){z.v=scl(0);R;}z.v=array(z.s,r.v.type());z.v=0;
   z.v(it[0],it[1],it[2],it[3])=r.v(ix[0],ix[1],ix[2],ix[3]);}
A MF(trn_f){z.r=r.r;DO(r.r,z.s[i]=r.s[r.r-(i+1)])
   switch(r.r){CS(0,z.v=r.v)CS(1,z.v=r.v)CS(2,z.v=r.v.T())}
Α
    CS(3,z.v=reorder(r.v,2,1,0))CS(4,z.v=reorder(r.v,3,2,1,0))}}
A DF(trn_f){I lv[4]; if(l.r>1||cnt(l)!=r.r)err(5);
   l.v.as(s32).host(lv);DO(r.r,if(lv[i]<0||lv[i]>=r.r)err(4))
   U8 f[]={0,0,0,0};DO(r.r,f[lv[i]]=1)
А
   U8 t=1;DO(r.r,if(t&&!f[i])t=0;else if(!t&&f[i])err(5))
А
   DO(r.r,if(!f[i])err(16))
Α
   z.r=r.r;D0(r.r,z.s[r.r-(lv[i]+1)]=r.s[r.r-(i+1)])
А
   I s[4];DO(r.r,s[r.r-(lv[i]+1)]=r.r-(i+1))
Α
   switch(r.r){CS(0,z.v=r.v)CS(1,z.v=r.v)}
Α
   CS(2,z.v=reorder(r.v,s[0],s[1]))
Α
    CS(3,z.v=reorder(r.v,s[0],s[1],s[2]))
Α
Α
    CS(4,z.v=reorder(r.v,s[0],s[1],s[2],s[3]))}}
A MF(unq_f){if(r.r>1)err(4);z.r=1;if(!cnt(r)){z.s=r.s;z.v=r.v;R;}
   array a,b;sort(a,b,r.v);z.v=a!=shift(a,1);z.v(0)=1;
   z.v=where(z.v);sort(b,z.v,b(z.v),a(z.v));
А
   z.s=dim4(z.v.elements());}
A DF(unq_f){if(r.r>1||l.r>1)err(4);z.r=1;dtype mt=mxt(l.v,r.v);
   if(!cnt(l)){z.s=r.s;z.v=r.v;R;}if(!cnt(r)){z.s=l.s;z.v=l.v;R;}
   array x=setUnique(l.v);B c=x.elements();
Α
   z.v=!anyTrue(tile(r.v,1,(U)c)==tile(array(x,1,c),(U)r.s[0],1),1);
Α
   z.v=join(0,l.v.as(mt),r.v(where(z.v)).as(mt));
Α
   z.s=dim4(z.v.elements());}
Α
```

```
A #define brkop(zz,ll,rr,pp) brk_o zz(ll,rr,pp)
A #define comop(zz,rr,pp) com_o zz(rr,pp)
A #define dotop(zz,ll,rr,pp) dot_o zz(ll,rr,pp)
A #define mapop(zz,rr,pp) map_o zz(rr,pp)
A #define redop(zz,rr,pp) red_o zz(rr,pp)
A #define jotop(zz,ll,rr,pp) jot_o zz(ll,rr,pp)
A #define oupop(zz,rr,pp) oup_o zz(rr,pp)
A #define powop(zz,ll,rr,pp) pow_o zz(ll,rr,pp)
A #define rdfop(zz,rr,pp) rdf_o zz(rr,pp)
A #define rnkop(zz,ll,rr,pp) rnk_o zz(ll,rr,pp)
A #define scnop(zz,rr,pp) scn_o zz(rr,pp)
A #define scfop(zz,rr,pp) scf_o zz(rr,pp)
A MF(brk_o){ll(z,r,(r.r?r.r-1:0)-ww.v.as(f64).scalar<D>(),p);}
A DF(brk o){D ax=l.r;if(r.r>l.r)ax=r.r;if(ax)ax--;
  ll(z,l,r,ax-ww.v.as(f64).scalar<D>(),p);}
A MF(com_o){ll(z,r,r,p);}DF(com_o){ll(z,r,l,p);}
A DF(dot_o){I ra=r.r?r.r-1:0;if(r.r&&l.r&&l.s[0]!=r.s[ra])err(5);
   I la=l.r?l.r-1:0;A t(la+ra,r.s,r.v(0));if(t.r>4)err(10);
Α
  t.s[ra]=1;DO(la,t.s[i+ra]=l.s[i+1])if(!cnt(t)){t.v=scl(0);z=t;R;}
Α
  if(!l.s[0]||!r.s[ra]){t.v=ll.id(t.s);z=t;R;}
Α
   I c=(I)(l.r?l.s[0]:r.s[ra]);
А
Α
  I rc=(I)(cnt(r)/r.s[ra]); I lc=(I)(cnt(l)/l.s[0]);
   array x=array(l.v,(I)l.s[0],lc);array y=array(r.v,rc,(I)r.s[ra]);
Α
  if(1==l.s[0]){x=tile(x,c,1);}if(1==r.s[ra]){y=tile(y,1,c);}
А
   if("add"==ll.nm&&"mul"==rr.nm){
А
   t.v=array(matmul(y.as(f64),x.as(f64)),t.s);z=t;R;}
А
А
   x=tile(array(x,c,1,lc),1,rc,1);y=tile(y.T(),1,1,lc);
  A X(3,dim+(c,rc,lc),x.as(f6+)); A Y(3,dim+(c,rc,lc),y.as(f6+));
А
   mapop(mfn,rr,p);redop(rfn,ll,p);mfn(X,X,Y,p);rfn(X,X,p);
А
   t.v=array(X.v,t.s);z=t;}
Α
A MF(jot_o){if(!fl){rr(z,aa,r,p);R;}if(!fr){ll(z,r,ww,p);R;}
Α
   rr(z,r,p); ll(z,z,p); }
A DF(jot_o){if(!fl||!fr){err(2);}rr(z,r,p);ll(z,l,z,p);}
A MF(map_o){if(scm(ll)){ll(z,r,p);R;}
  z.r=r.r;z.s=r.s;I c=(I)cnt(z);if(!c){z.v=scl(0);R;}
А
  A zs; A rs=scl(r.v(0)); ll(zs,rs,p); if(c==1)\{z.v=zs.v;R;\}
Α
  array v=array(z.s,zs.v.type());v(0)=zs.v(0);
А
А
   DO(c-1,rs.v=r.v(i+1);ll(zs,rs,p);v(i+1)=zs.v(0))z.v=v;
A DF(map_o){if(scd(ll)){ll(z,l,r,p);R;}
   if((l.r==r.r&&l.s==r.s)||!l.r){z.r=r.r;z.s=r.s;}
Α
  else if(!r.r){z.r=l.r;z.s=l.s;}else if(l.r!=r.r)err(4);
Α
Α
   else if(l.s!=r.s)err(5);else err(99);I c=(I)cnt(z);
   if(!c){z.v=scl(0);R;}A zs;A rs=scl(r.v(0));A ls=scl(l.v(0));
Α
   ll(zs,ls,rs,p);if(c==1){z.v=zs.v;R;}
Α
   array v=array(z.s,zs.v.type());v(0)=zs.v(0);
Α
   if(!r.r){rs.v=r.v;
Α
А
   DO(c-1, ls.v=l.v(i+1); ll(zs, ls, rs, p); v(i+1)=zs.v(0);)
   z.v=v;R;}
Α
Α
   if(!l.r){ls.v=l.v;
   DO(c-1,rs.v=r.v(i+1);ll(zs,ls,rs,p);v(i+1)=zs.v(0);)
Α
    z.v=v;R;}
Α
   DO(c-1, ls.v=l.v(i+1); rs.v=r.v(i+1); ll(zs, ls, rs, p);
Α
    v(i+1)=zs.v(0))z.v=v;
Α
A DF(oup_o){A t(l.r+r.r,r.s,r.v(0));if(t.r>4)err(10);
   DO(l.r,t.s[i+r.r]=l.s[i])if(!cnt(t)){t.v=scl(0);z=t;R;}
А
  array x(flat(l.v),1,cnt(l));array y(flat(r.v),cnt(r),1);
  dim4 ts(cnt(r),cnt(l));x=tile(x,(I)ts[0],1);y=tile(y,1,(I)ts[1]);
Α
  mapop(mfn,ll,p);A xa(2,ts,x);A ya(2,ts,y);mfn(xa,xa,ya,p);
Α
  t.v=array(xa.v,t.s);z=t;}
```

```
A MF(pow_o){if(fr){A t;A v=r;
    do{A u; ll(u,v,p); rr(t,u,v,p); if(t.r)err(5); v=u;}
    while(!t.v.as(s32).scalar<I>());z=v;R;}
Α
   if(ww.r)err(4);I c=ww.v.as(s32).scalar<I>();z=r;DO(c,ll(z,z,p))}
А
A DF(pow_o){if(fr){A t;A v=r;
    do{A u; ll(u,l,v,p); rr(t,u,v,p); if(t.r)err(5); v=u;}
    while(!t.v.as(s32).scalar<I>());z=v;R;}
Α
А
   if(ww.r)err(4);I c=ww.v.as(s32).scalar<I>();
   A t=r;DO(c,ll(t,l,t,p))z=t;}
Α
A MF(rdf o){A t(r.r?r.r-1:0,dim4(1),r.v(0));DO(t.r,t.s[i]=r.s[i])
   I rc=(I)r.s[t.r]; I zc=(I)cnt(t); mapop(mfn, ll, p);
Α
   if(!zc){t.v=scl(0);z=t;R;}if(!rc){t.v=ll.id(t.s);z=t;R;}
   if(1==rc){t.v=array(r.v,t.s);z=t;R;}
А
   if("add"==ll.nm){if(r.v.isbool())t.v=count(r.v,t.r).as(s32);
А
   else t.v=sum(r.v.as(f64),t.r);z=t;R;}
А
   if("mul"==ll.nm){t.v=product(r.v.as(f64),t.r);z=t;R;}
А
   if("min"==ll.nm){t.v=min(r.v,t.r);z=t;R;}
А
   if("max"==ll.nm){t.v=max(r.v,t.r);z=t;R;}
Α
   if("and"==ll.nm){t.v=allTrue(r.v,t.r);z=t;R;}
А
   if("lor"==ll.nm){t.v=anyTrue(r.v,t.r);z=t;R;}
Α
   af::index x[4];x[t.r]=rc-1;t.v=r.v(x[0],x[1],x[2],x[3]);
Α
   DO(rc-1,x[t.r]=rc-(i+2);
А
    mfn(t,A(t.r,t.s,r.v(x[0],x[1],x[2],x[3])),t,p));z=t;}
Α
A DF(rdf_o){if(l.r!=0&&(l.r!=1||l.s[0]!=1))err(5);if(!r.r)err(4);
   I lv=l.v.as(s32).scalar<I>();I ra=r.r-1;
А
    if((r.s[ra]+1)<lv)err(5); I rc=(I)((1+r.s[ra])-abs(lv));
А
   mapop(mfn,ll,p);A t(r.r,r.s,scl(0));t.s[ra]=rc;if(!cnt(t)){z=t;R;}
А
А
   if(!lv){t.v=ll.id(t.s);z=t;R;}seq rnq(rc);af::index x[4];
Α
   if(lv>=0){x[ra]=rng+((D)lv-1);t.v=r.v(x[0],x[1],x[2],x[3]);
    DO(lv-1,x[ra]=rng+((D)lv-(i+2));
Α
     mfn(t,A(t.r,t.s,r.v(x[0],x[1],x[2],x[3])),t,p))
Α
   }else{x[ra]=rng;t.v=r.v(x[0],x[1],x[2],x[3]);
Α
    DO(abs(lv)-1,x[ra]=rng+(D)(i+1);
А
Α
     mfn(t,A(t.r,t.s,r.v(x[0],x[1],x[2],x[3])),t,p))}
   z=t;}
Α
A MF(red_o){A t(r.r?r.r-1:0,dim4(1),z.v);DO(t.r,t.s[i]=r.s[i+1])
   I rc=(I)r.s[0];I zc=(I)cnt(t);if(!zc){t.v=scl(0);z=t;R;}
Α
  if(!rc){t.v=ll.id(t.s);z=t;R;}
   if(1==rc){t.v=array(r.v,t.s);z=t;R;}
А
   if("add"==ll.nm){if(r.v.isbool())t.v=count(r.v,0).as(s32);
Α
   else t.v=sum(r.v.as(f64),0);z=t;R;}
А
   if("mul"==ll.nm){t.v=product(r.v.as(f64),0);z=t;R;}
А
Α
   if("min"==ll.nm){t.v=min(r.v,0);z=t;R;}
   if("max"==ll.nm){t.v=max(r.v,0);z=t;R;}
А
   if("and"==ll.nm){t.v=allTrue(r.v,0);z=t;R;}
Α
   if("lor"==ll.nm){t.v=anyTrue(r.v,0);z=t;R;}
А
   t.v=r.v(rc-1,span);mapop(mfn,ll,p);
А
   DO(rc-1, mfn(t, A(t.r, t.s, r.v(rc-(i+2), span)), t, p))z=t;
А
A DF(red_o){if(l.r!=0&&(l.r!=1||l.s[0]!=1))err(5);if(!r.r)err(4);
   I lv=l.v.as(s32).scalar<I>();if((r.s[0]+1)<lv)err(5);</pre>
А
   I rc=(I)((1+r.s[0])-abs(lv));mapop(mfn,ll,p);
Α
   A t(r.r,r.s,scl(0));t.s[0]=rc;if(!cnt(t)){z=t;R;}
А
   if(!lv){t.v=ll.id(t.s);z=t;R;}seq rng(rc);
А
   if(lv>=0){t.v=r.v(rng+((D)lv-1),span);
Α
    DO(lv-1,mfn(t,A(t.r,t.s,r.v(rng+((D)lv-(i+2)),span)),t,p))
А
Α
   }else{t.v=r.v(rng,span);
    DO(abs(lv)-1,mfn(t,A(t.r,t.s,r.v(rng+(D)(i+1),span)),t,p))
А
Α
   z=t;}
Α
```

```
A MF(rnk_o){if(cnt(ww)!=1)err(4);I cr=ww.v.as(s32).scalar<I>();
   if(scm(ll)||cr>=r.r){ll(z,r,p);R;}
   if(cr<=-r.r||!cr){mapop(f,ll,p);f(z,r,p);R;}
Α
   if(cr<0)cr=r.r+cr;if(cr>3)err(10);I dr=r.r-cr;
А
   dim4 sp(1);DO(dr,sp[cr]*=r.s[i+cr])DO(cr,sp[i]=r.s[i])
А
   std::vector<A> tv(sp[cr]);A b(cr+1,sp,array(r.v,sp));
А
   DO((I)sp[cr], sqdfn(tv[i], scl(scl(i)), b, p); ll(tv[i], tv[i], p))
Α
   I mr=0;dim4 ms(1);dtype mt=b8;if(mr>3)err(10);
А
   DO((I)sp[cr],if(mr<tv[i].r)mr=tv[i].r;mt=mxt(mt,tv[i]);I si=i;
Α
   DO(4, if (ms[3-i] < tv[si].s[3-i]) {ms=tv[si].s;break;}))
Α
   I mc=(I)cnt(ms);array v(mc*sp[cr],mt);v=0;
А
   DO((I)sp[cr],seq ix((D)cnt(tv[i]));v(ix+(D)(i*mc))=flat(tv[i].v))
Α
   z.r=mr+dr;z.s=ms;z.s[mr]=sp[cr];z.v=array(v,z.s);}
A DF(rnk_o){I cl,cr,dl,dr;dim4 sl(1),sr(1);array wwv=ww.v.as(s32);
   if(cnt(ww)==1)cl=cr=wwv.scalar<I>();
А
   else if(cnt(ww)==2)\{cl=wwv.scalar<I>();cr=wwv(1).scalar<I>();}
А
   else err(4);
А
   if(cl>l.r)cl=l.r;if(cr>r.r)cr=r.r;if(cl<-l.r)cl=0;if(cr<-r.r)cr=0;</pre>
Α
   if(cl<0)cl=l.r+cl;if(cr<0)cr=r.r+cr;if(cr>3||cl>3)err(10);
А
   dl=l.r-cl;dr=r.r-cr;if(dl!=dr&&dl&&dr)err(4);
Α
   if(dl==dr)DO(dr,if(l.s[i+cl]!=r.s[i+cr])err(5))
Α
   DO(dl,sl[cl]*=l.s[i+cl])DO(cl,sl[i]=l.s[i])
А
   DO(dr,sr[cr]*=r.s[i+cr])DO(cr,sr[i]=r.s[i])
Α
Α
   B sz=dl>dr?sl[cl]:sr[cr];std::vector<A> tv(sz);
   A a(cl+1,sl,array(l.v,sl)); A b(cr+1,sr,array(r.v,sr));
Α
   I mr=0;dim4 ms(1);dtype mt=b8;
А
   DO((I)sz,A ta;A tb;A ai=scl(scl(i%sl[cl]));A bi=scl(scl(i%sr[cr]));
А
А
    sqdfn(ta,ai,a,p);sqdfn(tb,bi,b,p);ll(tv[i],ta,tb,p);
Α
    if(mr<tv[i].r)mr=tv[i].r;mt=mxt(mt,tv[i]);A t=tv[i];</pre>
    DO(4, if (ms[i] < t.s[i]) ms[i] = t.s[i]))
А
   B mc=cnt(ms);array v(mc*sz,mt);v=0;
Α
   DOB(sz, seq ix((D)cnt(tv[i])); v(ix+(D)(i*mc))=flat(tv[i].v))
А
   z.r=mr+(dr>dl?dr:dl);z.s=ms;z.s[mr]=sz;z.v=array(v,z.s);}
A MF(scn_o){z.r=r.r;z.s=r.s;I rc=(I)r.s[0];
   if(1==rc){z.v=r.v;R;}if(!cnt(z)){z.v=scl(0);R;}
А
   if("add"==ll.nm){z.v=scan(r.v.as(f64),0,AF_BINARY_ADD);R;}
Α
   if("mul"==ll.nm){z.v=scan(r.v.as(f64),0,AF_BINARY_MUL);R;}
А
   if("min"==ll.nm){z.v=scan(r.v.as(f64),0,AF_BINARY_MIN);R;}
А
   if(\text{"max"}==ll.nm)\{z.v=scan(r.v.as(f64),0,AF BINARY MAX);R;\}
А
   mapop(mfn,ll,p);z.v=array(z.s,f64);A t(z.r?z.r-1:0,z.s,r.v(0));
Α
   DO(t.r,t.s[i]=t.s[i+1]);t.s[t.r]=1;I tc=(I)cnt(t);
А
   DO(rc,t.v=r.v(i,span).as(f64);I c=i;
Α
    DO(c, mfn(t, A(t.r, t.s, r.v(c-(i+1), span)), t, p))
Α
    z.v(i,span)=t.v)}
Α
A MF(scf_o){z.r=r.r;z.s=r.s;I ra=r.r?r.r-1:0;I rc=(I)r.s[ra];
   if(1==rc){z.v=r.v;R;}if(!cnt(z)){z.v=scl(0);R;}
   if("add"==ll.nm){z.v=scan(r.v.as(f64),ra,AF_BINARY_ADD);R;}
Α
   if("mul"==ll.nm){z.v=scan(r.v.as(f64),ra,AF_BINARY_MUL);R;}
А
Α
   if("min"==ll.nm){z.v=scan(r.v.as(f64),ra,AF_BINARY_MIN);R;}
   if("max"==ll.nm){z.v=scan(r.v.as(f64),ra,AF BINARY MAX);R;}
А
   z.v=array(z.s,f64);A t(z.r?z.r-1:0,z.s,r.v(0));t.s[ra]=1;
Α
   I tc=(I)cnt(t);af::index x[4];mapop(mfn,ll,p);
А
   DO(rc,x[ra]=i;t.v=r.v(x[0],x[1],x[2],x[3]).as(f64);Ic=i;
Α
    DO(c,x[ra]=c-(i+1);
Α
     mfn(t,A(t.r,t.s,r.v(x[0],x[1],x[2],x[3])),t,p))
Α
Α
    x[ra]=i;z.v(x[0],x[1],x[2],x[3])=t.v)}
Α
```

```
A EXPORT A*mkarray(lp*d){A*z=new A;cpda(*z,d);R z;}
A EXPORT V frea(A*a) {delete a;}
A EXPORT V exarray(lp*d, A*a){cpad(d, *a);}
A EXPORT V afsync(V){sync();}
A EXPORT Window *w_new(char *k){R new Window(k);}
A EXPORT I w close(Window*w){R w->close();}
A EXPORT V w_del(Window*w){delete w;}
A EXPORT V w_img(lp*d,Window*w){A a;cpda(a,d);
A w->image(a.v.as(a.r==2?f32:u8));}
A EXPORT V w_plot(lp*d,Window*w){A a;cpda(a,d);w->plot(a.v.as(f32));}
A EXPORT V w_hist(lp*d,D l,D h,Window*w){A a;cpda(a,d);
A w->hist(a.v.as(u32),l,h);}
A EXPORT V loadimg(lp*z,char*p,I c){array a=loadImage(p,c);
A b(a.numdims(),a.dims(),a.as(s16));cpad(z,b);}
A EXPORT V saveimg(lp*im,char*p){A a;cpda(a,im);
A saveImageNative(p,a.v.as(a.v.type()==s32?u16:u8));}
```

:EndNamespace