The Co-dfns Compiler

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 ${\tt codfns.nw}$ 2

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1 Introduction

2 User's Guide

VERSION, never used.

□IO, used in chunk 33. □ML, used in chunk 33. □WX, never used.

VSAPATH, used in chunks 21 and 30a.

3 Co-dfns Architecture

```
(* 3a)≡
3a
        :Namespace codfns
           (Global Settings 3b)
           (The Fix API 4a)
           (User-command API 4b)
           (AST Record Structure 4c)
           ⟨Parser 6⟩
           (Compiler 15)
           (Code Generator 16)
           (Interface to the backend C compiler 21)
           (Linking with Dyalog 22a)
           (Converters between parent and depth vectors 5)
           (XML Rendering 31b)
           (Pretty-printing AST trees 32a)
        :EndNamespace
      Root chunk (not used in this document).
      Defines:
        codfns, used in chunks 16, 21, 24, 26, 29, and 30.
      3.1 Global Settings
      ⟨Global Settings 3b⟩≡
3b
        □IO □ML □WX←0 1 3
        VERSION←4 1 0
        AF∆PREFIX←'/opt/arrayfire'
        AF∆LIB+'cuda'
        VS∆PATH←'\Program Files\Microsoft Visual Studio\2022\Community'
      This code is used in chunk 3a.
      Defines:
        AFALIB, used in chunks 4b, 21, and 30a.
        AFAPREFIX, used in chunk 21.
```

3.2 The Fix API

```
4a \langle The\ Fix\ API\ 4a\rangle\equiv Fix+{n NS{\omega-|\(\text{\psi}\cdot\) CC{\omega-|\(\text{\psi}\cdot\) GC{\omega-|\(\text{\psi}\cdot\) TT{\omega-|\(\text{\psi}\cdot\) a n s src+PS \omega-|\(\text{\psi}\cdot\) This code is used in chunk 3a. Uses src 29c.
```

3.3 The user-command API

```
4b
      \langle User\text{-}command API 4b \rangle \equiv
       ⊽Z←Help _
         Z+'Usage: <object> <target> [-af={cpu,opencl,cuda}]'

∇ r←List

         r+□NS"1pc0 ♦ r.Name+,"c'Compile' ♦ r.Group+c'CODFNS'
         r[0].Desc←'Compile an object using Co-dfns'
         r.Parse←c'2S -af=cpu opencl cuda

∇ Run(C I); Convert; in; out

        A Parameters
        A AFΔLIB ArrayFire backend to use
         Convert+\{\alpha(|SE.SALT.Load'[SALT]/lib/NStoScript -noname').ntgennscode <math>\omega\}
         in out←I.Arguments ◊ AF∆LIB←I.af''⊃~I.af≡0
         S←(c':Namespace ',out),2↓0 0 0 out Convert ##.THIS.±in
         →0/~'Compile' #C
         {##.THIS. ±out, '←ω'}out Fix S¬□EX'##.THIS.',out
      This code is used in chunk 3a.
```

This code is used in chunk 3a. Uses AFALIB 3b.

4 Co-dfns Compiler

4.1 AST Record Structure

```
4c (AST Record Structure 4c)≡
f Δ+'ptknfsrdx'
NΔ+'ABCEFGKLMNOPSVZ'
This code is used in chunk 3a.
```

4.2 Converters between parent and depth vectors

4.3 Parser

```
6
      \langle Parser 6 \rangle \equiv
          PS \leftarrow \{IN \leftarrow \omega \land A B C E F G K L M N O P S V Z \leftarrow 1 + i 15\}
              I \leftarrow \{(\neg \omega) [\alpha] \land U \leftarrow \{0 = [NC'\alpha' : \omega\omega \overset{*}{\star}^{-1} \ \alpha\alpha \ \omega\omega \ \omega \ \land \ \omega\omega \overset{*}{\star}^{-1} \vdash (\omega\omega \ \alpha) \ \alpha\alpha \ \omega\omega \ \omega\}
              assert \leftarrow {\alpha \leftarrow 'assertion failure' \diamond 0 \in \omega: _{\alpha} □SIGNAL 8' \diamond shy \leftarrow 0}
              1<≢pIN: 'PARSER REQUIRES A SCALAR/VECTOR INPUT'□SIGNAL 11
              2<|≡IN:'PARSER REQUIRES A SIMPLE OR VECTOR OF VECTOR INPUT'□SIGNAL 11
              IN \leftarrow \epsilon (\subseteq IN), \square UCS 10
              O≠10|□DR IN: 'PARSER REQUIRES A CHARACTER ARRAY'□SIGNAL 11
         A Line and error reporting utilities
              CR LF←□UCS 13 10
              linestarts+(<u>1</u>1,2>/IN∈CR LF),≢IN
              mkdm + \{\alpha + 2 \diamond line + line starts \underline{\iota}\omega \diamond no + '[', (\bar{\iota} + line), ']'
                 i÷(~IN[i]∈CR LF)/i÷beg+:linestarts[line+1]-beg+linestarts[line]
                 ([EM α)(no,IN[i])(' ^'[i∈ω],~' 'ρ~≢no)}
              quotelines←{
                 lines←∪linestartsıω
                 nos←(1 0ρ~2×≢lines)\'[',(₹-1+lines), 01-'] '
                 beg+linestarts[lines] ♦ end+linestarts[lines+1]
                 m←∈∘ω"i←beg+ı"end-beg
                 -1+∈nos,(~•CR LF",,(IN•I"i),,' -'•I"m),CR}
              SIGNAL \leftarrow \{\alpha \leftarrow 2 ' ' \diamond en msg \leftarrow \alpha \diamond EN \circ \leftarrow en \diamond DM \circ \leftarrow en mkdm \supset \omega
                 dmx+('EN' en)('Category' 'Compiler')('Vendor' 'Co-dfns')
                 dmx, \leftarrow c'Message'(msg, CR, quotelines \omega)
                 □SIGNAL < dmx }</pre>
         A Group input into lines as a nested vector
              pos←(ι≢IN)⊆~~IN∈CR LF
         A Mask strings
              O≠≢lin←<u>ι</u>⊃∘φ"msk←≠\"''''=IN∘I"pos:{
                 EM←'SYNTAX ERROR: UNBALANCED STRING',('S'/~2≤≢lin),CR
                 EM, \leftarrowquotelines \epsilon (msk\neq"pos)[lin]
                 EM \PiSIGNAL 2}\theta
         A Remove comments
              pos msk/~~←c∧\~(~msk+mskv~1¢~msk)~'A'=IN∘I~pos
         A Remove leading and trailing whitespace
              WS+□UCS 9 32 ♦ pos msk/~~+c~(\\tau\tau\tau\dot)\o(WS\equiv IN\oI)\"pos
         A Flatten and separate lines and ♦ with Z type
              t \leftarrow 0 \rho \subset pos \diamond t pos msk(\epsilon, \circ, \sim) \leftarrow Z(\neg pos)0 \diamond t[\underline{\iota}' \diamond' = IN[pos]] \leftarrow Z
```

```
A Tokenize Strings
    end\leftarrow 1 + pos \diamond t[i \leftarrow 2 < \neq 0, msk] \leftarrow C \diamond end[i] \leftarrow end[i \geq \neq msk, 0]
    t pos end/~←c(t≠0)∨~msk
A Verify that all open characters are part of the valid character set
    alp←'ABCDEFGHIJKLMNOPQRSTUVWXYZ_abcdefghijklmnopqrstuvwxyz'
    alp,+'ÀÁÂÃÄÅÆÇÈÉÊËÌÍÎÏÐÑÒÓÔÖÖØÙÚÛÜÝßàáâãäåæçèéêëììíîïðñòóôõöøùúûüþ'
    alp, ←' ΔΔABCDEFGHIJKLMNOPQRSTUVWXYZ'
    num←□D
    synb \leftarrow '^{-}[]{}()'':\alpha\omega\diamond;'
    syna←'<del>0</del>□□#'
    prmfs←'+-×÷|[[**0!?~∧νÃν̄<≤=>≥≠≡≢ρ,,φθΦ↑↓⊂⊆⊃€€∩∪ι<u>ι</u>[]Δ♥±▼⊥Τ⊣⊢⊞∇←→'
    prmdo←'∘.*⊡0°0@' ♦ prmmo←'~~&I目' ♦ prmfo←'//\\
    prms←prmfs,prmdo,prmmo,prmfo
    x←' '@{t≠0}IN[pos] A The spaces produce nice invariants
    v∱msk←~x∈alp,num,syna,synb,prms,WS:{
       EM←'SYNTAX ERROR: INVALID CHARACTER(S) IN SOURCE', CR
       EM, ←quotelines <u>ı</u>msk
       EM □SIGNAL 2}0
A Tokenize numbers
    _←{dm[ω]←∧\dm[ω]}"(dm∨x∈alp)⊆ι≢dm←x∈num
    dm \vee \leftarrow ('.' = x) \wedge (-1 \varphi dm) \vee 1 \varphi dm
    dmv \leftarrow ('' = x) \land 1 \phi dm
    dmv \leftarrow (x \in 'EeJj') \land (^{-1}\phi dm) \land 1\phi dm
    v∱msk←(dm=0)^x='-':2'ORPHANED -'SIGNAL pos/~msk
    v+{1<++ω='j'}"dp←□C"dm∈x:'MULTIPLE J IN NUMBER'□SIGNAL 2
    v \neq \{1 < + \neq \omega = e'\} "dp \leftarrow \neg = /\{\omega \leq \omega \neq j'\} "dp: MULTIPLE E IN NUMBER' SIGNAL 2
    v/'e'=>"dp:'MISSING MANTISSA'□SIGNAL 2
    v+'e'=>∘¢"dp:'MISSING EXPONENT'□SIGNAL 2
    mn ex \leftarrow \downarrow \Diamond \uparrow \{2 \uparrow (\omega \subseteq \omega \neq e'), e''\} dp
    v \neq \{1 < + \neq ' . ' = \omega\}"mn, ex: 'MULTIPLE . IN NUMBER' SIGNAL 2
    v∱'.'ϵ"ex:'REAL NUMBER IN EXPONENT'□SIGNAL 2
    v \neq \{v \neq 1 \downarrow \omega \in '^-'\}"mn,ex:'MISPLACED -'\squareSIGNAL 2
    t[i \leftarrow 12 < \neq 0, dm] \leftarrow N \Leftrightarrow end[i] \leftarrow end \neq 2 > \neq dm, 0
A Tokenize Variables
    t[i+\underline{\imath}2</0,vm+(\sim dm)\land x\in alp,num]+V \Leftrightarrow end[i]+end/~2>/vm,0
A Tokenize \alpha, \omega formals
    fm \leftarrow \{mm \leftarrow \phi \supset (> \circ \supset, \vdash) \neq \phi m \leftarrow \alpha = ' ', \omega \diamond 1 \downarrow "(mm \land \sim m1)(mm \land m1 \leftarrow 1 \phi m)\}
    am aam←'α'fm x ◊ wm wwm←'ω'fm x
    ((am \lor wm) / t) + A \diamond ((aam \lor wwm) / t) + P \diamond ((aam \lor wwm) / end) + end / = 1 / eam \lor wwm
```

A Tokenize Primitives, Atoms

```
t[\underline{\iota}(\sim dm) \land x \in prms] \leftarrow P \diamond t[\underline{\iota}x \in syna] \leftarrow A
A Compute dfns regions and type, include } as a child
    t[\underline{\iota}' {'=x}] \leftarrow 0 \neq 0 \neq 0 \neq 1 + 1 = 1 = 0 = 1 = 0 = 1 = 0
A Check for out of context dfns formals
    v \neq (d=0) \land (t=P) \land IN[pos] \in \alpha \omega' : 'DFN FORMAL REFERENCED OUTSIDE DFNS' SIGNAL 2
A Compute trad-fns regions
   v/Z≠t/~1¢msk←(d=0)∧'∀'=x:'TRAD-FNS START/END LINES MUST BEGIN WITH ∀'□SIGNAL
    √/Z≠t/~⊃1 T1v.φc(2>/tm);0:'TRAD-FNS END LINE MUST CONTAIN ▼ ALONE'□SIGNAL 2
A Identify Label colons versus others
    t[\underline{\iota}tm\wedge(d=0)\wedge\epsilon((\sim)\wedge(<\downarrow\vee\downarrow))"':'=(t=Z)\subset IN[pos]]\leftarrow L
A Tokenize Keywords
    ki \leftarrow \underline{\iota}(t=0) \land (d=0) \land (':'=IN[pos]) \land 1 \varphi t = V
    t[ki] \leftarrow K \diamond end[ki] \leftarrow end[ki+1] \diamond t[ki+1] \leftarrow 0
    ERR+'EMPTY COLON IN NON-DFNS CONTEXT, EXPECTED LABEL OR KEYWORD'
    v \neq (t=0) \land (d=0) \land ':'=IN[pos]:ERR \square SIGNAL 2
A Tokenize System Variables
    si←<u>ı</u>('□'=IN[pos])∧1φt=V
    t[si] \leftarrow S \diamond end[si] \leftarrow end[si+1] \diamond t[si+1] \leftarrow 0
A Delete all characters we no longer need from the tree
    d tm t pos end(f^{\sim}) \leftarrow c(t \neq 0) \lor x \in '()[]{}:;'
A Tokenize Labels
    ERR+'LABEL MUST CONSIST OF A SINGLE NAME'
    \vee \neq (Z \neq t[li-1]) \vee (V \neq t[li \leftarrow \iota 1 \varphi_{msk} \leftarrow t = L]) : ERR \square SIGNAL 2
    t[li]←L ♦ end[li]←end[li+1]
    d tm t pos end(/~)←c~msk
A Now that all compound data is tokenized, reify n field before tree-building
    n \leftarrow \{1 \neq \omega'' \mid 0', \omega\} \otimes \{t = N\} (c'') \otimes \{t \in Z \}  \square C \otimes \{t \in K \} \mid N \circ I'' pos + \iota'' end - pos \}
A Verify that keywords are defined and scoped correctly
    KW÷'NAMESPACE' 'ENDNAMESPACE' 'END' 'IF' 'ELSEIF' 'ANDIF' 'ORIF' 'ENDIF'
    KW,←'WHILE' 'ENDWHILE' 'UNTIL' 'REPEAT' 'ENDREPEAT' 'LEAVE' 'FOR' 'ENDFOR'
    KW, ←'IN' 'INEACH' 'SELECT' 'ENDSELECT' 'CASE' 'CASELIST' 'ELSE' 'WITH'
    KW, ←'ENDWITH' 'HOLD' 'ENDHOLD' 'TRAP' 'ENDTRAP' 'GOTO' 'RETURN' 'CONTINUE'
    KW, ←'SECTION' 'ENDSECTION' 'DISPOSABLE' 'ENDDISPOSABLE'
   KW,"~←':'
    msk \leftarrow \sim KW \in \sim kws \leftarrow n \neq \sim km \leftarrow t = K
```

```
v/msk:('UNRECOGNIZED KEYWORD ', kws>~> 1msk) □SIGNAL 2
    msk+kwse':NAMESPACE' ':ENDNAMESPACE'
    v≠msk∧km≠tm:'NAMESPACE SCRIPTS MUST APPEAR AT THE TOP LEVEL'□SIGNAL 2
    msk+kws∈KW~':NAMESPACE' ':ENDNAMESPACE' ':SECTION' ':ENDSECTION'
    √/msk←msk∧~km/tm:{msg+2'STRUCTURED STATEMENTS MUST APPEAR WITHIN TRAD-FNS'
       msg SIGNAL \epsilon \{x+iend[\omega]-x+pos[\omega]\}"\underline{i}km+msk\}\theta
A Verify system variables are valid
    SYSV←,"'Á' 'A' 'AI' 'AN' 'AV' 'AVU' 'BASE' 'CT' 'D' 'DCT' 'DIV' 'DM'
SYSV,←,"'DMX' 'EXCEPTION' 'FAVAIL' 'FNAMES' 'FNUMS' 'FR' 'IO' 'LC' 'LX'
    SYSV, \( \dagger, \quad \text{DMX' 'EXCEPTION' 'FAVAIL' 'FNAMES' 'FNUMS' 'FR' 'IO' 'LC' 'LX'

SYSV, \( \dagger, \quad \text{"ML' 'NNAMES' 'NNUMS' 'NSI' 'NULL' 'PATH' 'PP' 'PW' 'RL' 'RSI'

SYSV, \( \dagger, \quad \text{"RTL' 'SD' 'SE' 'SI' 'SM' 'STACK' 'TC' 'THIS' 'TID' 'TNAME' 'TNUMS'

SYSV, \( \dagger, \quad \text{"TPOOL' 'TRACE' 'TRAP' 'TS' 'USING' 'WA' 'WSID' 'WX' 'XSI'
    SYSF+,"'ARBIN' 'ARBOUT' 'AT' 'C' 'CLASS' 'CLEAR' 'CMD' 'CONV' 'CR' 'CS' 'CSV SYSF,+,"'CY' 'DF' 'DL' 'DQ' 'DR' 'DT' 'ED' 'EM' 'EN' 'EX' 'EXPORT'
               "'FAPPEND' 'FCHK' 'FCOPY' 'FCREATE' 'FDROP' 'FERASE' 'FFT' 'IFFT'
               "'FHIST' 'FHOLD' 'FIX' 'FLIB' 'FMT' 'FPROPS' 'FRDAC' 'FRDCI' 'FREAD'
               "'FRENAME' 'FREPLACE' 'FRESIZE' 'FSIZE' 'FSTAC' 'FSTIE' 'FTIE'
    SYSF, +, "'FUNTIE' 'FX' 'INSTANCES' 'JSON' 'KL' 'LOAD' 'LOCK' 'MAP' 'MKDIR'
SYSF, +, "'MONITOR' 'NA' 'NAPPEND' 'NC' 'NCOPY' 'NCREATE' 'NDELETE' 'NERASE'
SYSF, +, "'NEW' 'NEXISTS' 'NGET' 'NINFO' 'NL' 'NLOCK' 'NMOVE' 'NPARTS'
SYSF, +, "'NPUT' 'NQ' 'NR' 'NREAD' 'NRENAME' 'NREPLACE' 'NRESIZE' 'NS'
SYSF, +, "'NSIZE' 'NTIE' 'NUNTIE' 'NXLATE' 'OFF' 'OR' 'PFKEY' 'PROFILE'
    "'STOP' 'SVC' 'SVO' 'SVQ' 'SVR' 'SVS' 'TCNUMS' 'TGET' 'TKILL' 'TPUT'
    SYSD+,"'OPT' 'R' 'S'
    v/msk←(t=S)^~ne'[]',"SYSV,SYSF,SYSD:{
       ERR←2'INVALID SYSTEM VARIABLE, FUNCTION, OR OPERATOR'
       ERR SIGNAL \epsilonpos [\omega] \{\alpha + \iota \omega - \alpha\} "end [\omega]
    }ımsk
A Compute parent vector from d
    p←D2P d
A Compute nameclass of dfns
    k+2\times t\in F \diamond k[\upsilon p/~(t=P)\land n\in c'\alpha\alpha'] \leftarrow 3 \diamond k[\upsilon p/~(t=P)\land n\in c'\omega\omega'] \leftarrow 4
A We will often wrap a set of nodes as children under a Z node
    gz \leftarrow \{z \leftarrow \omega \uparrow \sim -0 \neq \neq \omega \land ks \leftarrow -1 \downarrow \omega
       t[z]+Z \diamond p[ks]+\neg z \diamond pos[z]+pos[\neg \omega] \diamond end[z]+end[\neg \phi z, ks] \diamond z
A Nest top-level root lines as Z nodes
     _+(gz 1∳⊢)"(t[i]=Z)<i+<u>ı</u>d=0
    'Non-Z top-level node'assert t[<u>i</u>p=i≠p]=Z:
```

```
A Nest all dfns expression bodies as Z nodes
            \_ \leftarrow p[i] \{ end[\alpha] \leftarrow end[\neg \phi\omega] \land gz ``\omega \subset 1, ^1 \downarrow t[\omega] = Z \} \exists i \leftarrow \underline{\iota} t[p] = F
              'Non-Z dfns body node'assert t[<u>r</u>t[p]=F]=Z:
A Drop/eliminate any Z nodes that are empty or blank
            \_ \leftarrow p[i] \{ msk[\alpha, \omega] \leftarrow \land \ne IN[pos[\omega]] \in WS \} \exists i \leftarrow \underline{\iota}(t[p] = Z) \land p \ne \iota \not\equiv p \neg msk \leftarrow t \ne Z
            tm n t k pos end(f^{\sim}) + cmsk \diamond p+(\underline{\iota} - msk)(\vdash -1+\underline{\iota}) mskfp
A Parse Keyword structures
            nss+n∈c':NAMESPACE' ♦ nse+n∈c':ENDNAMESPACE'
            ERR←':NAMESPACE KEYWORD MAY ONLY APPEAR AT BEGINNING OF A LINE'
            Zv.≠t/~1¢nss:ERR □SIGNAL 2
            ERR←'NAMESPACE DECLARATION MAY HAVE ONLY A NAME OR BE EMPTY'
            v+(Z≠t+~1$nss)^(V≠t+~1$nss)vZ≠t+~2$nss:ERR ☐SIGNAL 2
            ERR←': ENDNAMESPACE KEYWORD MUST APPEAR ALONE ON A LINE'
            v/Z≠t/~⊃1 ~1v.¢cnse:ERR □SIGNAL 2
            t[nsi+<u>1</u>1¢nss]+M ♦ t[nei+<u>1</u>1¢nse]+-M
            n[i] \leftarrow n[1+i \leftarrow \underline{\iota}(t=M) \land V=1 \Leftrightarrow end[nsi] \leftarrow end[nei]
            x \leftarrow \underline{\iota} p = \iota \not\equiv p \diamond d \leftarrow + \uparrow (t[x] = M) + -t[x] = -M
            O≠⊃¢d:':NAMESPACE KEYWORD MISSING :ENDNAMESPACE PAIR'□SIGNAL 2
            p[x] \leftarrow x[D2P^{-1}\phi d]
A Delete unnecessary namespace nodes from the tree, leave only M's
            msk \leftarrow nssv((-1\phi nss) \land t = V) \lor nse \lor 1\phi nse
            t k n pos endf \sim c msk \diamond p \leftarrow (\underline{\iota} \sim msk) (\vdash -1 + \underline{\iota}) msk \neq p
A PARSE LABELS ...
A Map guard statements to (G (Z ...) (Z ...))
                     0=+\neq m \leftarrow ':'=IN[pos[\omega]]:\theta
                     >m: 'EMPTY GUARD TEST EXPRESSION' ☐ SIGNAL 2
                     1<+/m: 'TOO MANY GUARDS' ☐ SIGNAL 2
                     t[\alpha] \leftarrow G \diamond p[ti \leftarrow gz \Rightarrow tx cq \leftarrow 2\uparrow(c\theta), \forall \omega \subset 1, \neg 1 \downarrow m] \leftarrow \alpha \diamond k[ti] \leftarrow 1
                     ci \leftarrow \neq p \land p, \leftarrow \alpha \land t \land pos \ end, \leftarrow 0 \land n, \leftarrow c'' \land k[gz \ cq, ci] \leftarrow 1
            0}目i←<u>ı</u>t[p[p]]=F
A Parse brackets and parentheses into <sup>-1</sup> and <sup>Z</sup> nodes
            _←p[i]{
                     x \leftarrow IN[pos[\omega]] \diamond bd \leftarrow tbm \leftarrow (bo \leftarrow '['=x) + -bc \leftarrow ']' = x \diamond pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + -pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow pd \leftarrow tbm \leftarrow (po \leftarrow '('=x) + pc \leftarrow ')' = x \leftrightarrow
                     0 \neq \neg \Phi d : 2 \cup BALANCED BRACKETS \cup SIGNAL pos[\omega] \{x + \iota(\lceil \neq \omega) - x \leftarrow \lfloor \neq \alpha\} \circ \{\omega \neq \neg 0 \neq bd\} = nd[\omega] 
              0 \neq \neg \phi pd: 2 \cup NBALANCED PARENTHESES \cup SIGNAL pos[\omega] \{x + \iota(\lceil + \omega) - x + \lfloor + \alpha \} \ddot{o} \{\omega + \ddot{\sim} 0 \neq pd \} end[\omega] \}
                      (po∱bd)∨.≠¢pc∱bd:'OVERLAPPING BRACKETS AND PARENTHESES'∐SIGNAL 2
                     p[\omega] \leftarrow (\alpha, \omega)[1 + ^{-1}Q\{\omega = i \neq \omega\}D2P + + ^{-1}\varphi bm + pm] \diamond t[bo \neq \omega] \leftarrow ^{-1} \diamond t[po \neq \omega] \leftarrow Z
                     end[po+\omega] \(\def \text{end}[\phi pc+\omega] \(\def \text{end}[\text{bo}\text{\alpha}] \(+\text{end}[\phi bc\text{\alpha}]
            0}目i←<u>ı</u>(t[p]=Z)^p≠ι≢p
```

```
t k n pos end\neq = cmsk \leftarrow IN[pos]\epsilon')' \diamond p \leftarrow (\underline{\iota} \sim msk)(\vdash -1 + \underline{\iota})msk \neq p
A Convert semi-colon indexing into Z nodes in the -1 nodes
           _+p[i]{k[z+>-,/qz"q+ω<~-1φIN[pos[ω]]ε';]']+1 φ t[z]+Z P[1=#"q]}目i+<u>ι</u>t[p]=-1
A Mark bindable nodes
           bm \leftarrow (t=V) \vee (t=A) \wedge n \in , "' \square \square'
           bm+\{bm-p[i]\{bm[\alpha]+(V^{-1}\equiv t[\omega])\vee \wedge \neq bm[\omega]\}\{i+\underline{\iota}(\sim bm[p])\wedge t[p]=Z\} \stackrel{\cdot}{\times}\equiv bm
A Binding nodes
           _<del>←</del>p[i]{
                   t[\omega/\sim(n[\omega]\in\subset, '\leftarrow')\land 0, -1\downarrow bm[\omega]]\leftarrow B
                   b\ v \leftarrow \{(\neg``x)(1\downarrow``x \leftarrow \omega \not \vdash \ddot{} \{t[\neg \omega] = B\}``\omega)\}^{-1} \varphi``\omega \subset \ddot{} 1, \neg 1 \downarrow t[\omega] \in P\ B
                   v/~bm[∈v]: 'CANNOT BIND ASSIGNMENT VALUE' SIGNAL 2
                   p[\omega] \leftarrow (\alpha, b)[0, -1 \downarrow + \uparrow t[\omega] = B]
                   n[b]+n[\epsilon v] \diamond t[\epsilon v]+^{-7} \diamond pos[b]+pos[\epsilon v] \diamond end[b]+end[\Rightarrow \phi\omega]
           0}目i←<u>ı</u>(t[p]=Z)^p≠ı≢p
           t k n pos end\neq \leftarrow cmsk + t \neq = 7 \Leftrightarrow p + (\underline{\iota} - msk) (\vdash -1 + \underline{\iota}) msk \neq p
A Mark unambiguous primitive kinds
           k[\underline{\iota}(t=S)\land ne']', "SYSV]+1 \diamond k[\underline{\iota}(t=S)\land ne']', "SYSF]+2 \diamond k[\underline{\iota}(t=S)\land ne']', "SYSD]+4
           t[\underline{\imath}t=S]+P
           k[\underline{\iota}t\in A \ C \ N]+1 \diamond k[\underline{\iota}n\in ,"prmfs]+2 \diamond k[\underline{\iota}n\in ,"prmmo]+3 \diamond k[\underline{\iota}n\in ,"prmdo]+4
           k[\underline{\iota}n\epsilon, "prmfo] \leftarrow 5
           k[i\leftarrow_{lms}k\leftarrow(n\in c, '\circ')\land 1\phi n\in c, '.']\leftarrow 3 \diamond end[i]\leftarrow end[i+1] \diamond n[i]\leftarrow c, '\circ.'
           t k n pos endf = -\infty + \infty + \infty
A Anchor variables to earliest binding in matching frame
           \mathsf{rf}^{-1} @ \{ \mathsf{rt}[\omega] \in \mathsf{F} \ \mathsf{G} \ \mathsf{M} \} \mathsf{p}[\mathsf{rz}^{+1} @ \{ \mathsf{r}(\mathsf{t}[\omega] = \mathsf{Z}) \land (\mathsf{t}[\mathsf{p}[\omega]] \in \mathsf{F} \ \mathsf{G} \ \mathsf{M}) \lor \mathsf{p}[\omega] = \omega \} \stackrel{\mathsf{*}}{=} \stackrel{\mathsf{*}}{=} \stackrel{\mathsf{*}}{=} )
           rf[i] \leftarrow p[i \leftarrow \underline{t} = G] \diamond rz[i] \leftarrow i \diamond rf \leftarrow rf I@\{rz \in p[i] \vdash \circ \neg \exists i \leftarrow \underline{t}[p] = G\}rf
           mk \leftarrow \{\alpha[\omega], \neg n[\omega]\}
           fr←rf mk⊢fb←fb[ı~rf mk⊢fb+fb I∘(ı~)U⊖rz mk⊢fb←ıt=B] ♦ fb,←1
           vb←fb[frirf mk i]@(i←it=V)⊢<sup>-</sup>1p~≢p
           vb[i/\sim(rz[i]<rz[b])v(rz[i]=rz[b])\wedge i \ge b \leftarrow vb[i+i/\sim vb[i] \ne 1]] \leftarrow 1
            _+{z/~¯1=vb[1[z]+fb[frι\n I@1⊢z+rf I@0⊢ω]}*≡\{rf[ω],-ω}<u>ι</u>(t=V)∧vb=¯1
           \sqrt{msk} \leftarrow (t=V) \wedge vb = -1:{
                   6'ALL VARIABLES MUST REFERENCE A BINDING'SIGNAL\epsilonpos[\omega]\{\alpha+\iota\omega-\alpha\}"end[\omega]
           }<u>ı</u>msk
A \alpha/\omega \rightarrow V; A \rightarrow B; A \rightarrow B; A \rightarrow B
           t \leftarrow V@(i \leftarrow \underline{\iota}(t=A) \land n \in , "'\alpha\omega') \vdash F@\{t=M\}t \ \diamond \ vb[i] \leftarrow i \ \diamond \ k[\underline{\iota}(t=P) \land n \in '\alpha\alpha' \ '\omega\omega'] \leftarrow 2
A Infer types of bindings, groups, and variables
           z \times \downarrow p[i]{\alpha\omega} = i + \underline{\iota}(t[p] \in B \ Z) \wedge p \neq \iota \neq p
           x \leftarrow \{\omega \neq \sim \sim \uparrow t [\omega] = 1\} \cup \phi \sim x
           O∨.=≢"x:'BRACKET SYNTAX REQUIRES FUNCTION OR ARRAY TO ITS LEFT'□SIGNAL 2
```

```
_←{
         k[msk \neq z] \leftarrow k[x \neq msk \leftarrow (k[\neg x] \neq 0) \land 1 = \neq x] \diamond z x \neq msk
         k[z \neq \text{msk} + k[\text{s"x}] = 4] + 3 \diamond z x \neq \text{msk}
         k[z\not\vdash^{\sim}msk\leftarrow\{(2\ 3\ 5\in^{\sim}k[\supset\omega])\lor=(\omega,\not\equiv k)[0\iota^{\sim}\land k[\omega]=1][k,0\}\circ \phi^{\circ}x]\leftarrow2 \diamond z x\not\vdash^{\sim}\leftarrow c\sim msk
         k[z/\sim msk \leftarrow k[\supset \circ \varphi "x]=1] \leftarrow 1 \diamond z x/\sim \leftarrow c \sim msk
         k[i] \leftarrow k[vb[i \leftarrow \underline{\iota}t = V]]
     ≢z}*(=∨0=⊣)≢z
      'FAILED TO INFER ALL BINDING TYPES'assert O=≢z:
A Strand arrays into atoms
     i \leftarrow |i \rightarrow km \leftarrow 0 < i \leftarrow i[A|(i, \sim \leftarrow - \cup p[i]), p[i \leftarrow \underline{\iota}t[p] \in B Z]]
     msk+(t[i] \in C \ N) \lor msk \land \supset 1 \ \lnot 1 \lor . \varphi \lor msk+km \land (t[i] \in A \ C \ N \ V \ Z) \land k[i]=1
     np+(\not\equiv p)+\iota\not\equiv ai+i\not\vdash am+2>\not=msk,0 \diamond p+(np@ai\iota\not\equiv p)[p] \diamond p,+ai \diamond km+2<\not=0,msk
     t k n pos end(\neg, I) + cai \diamond k[ai] + 1 6[\lor + msk\subseteqt[i] \neqN]
     t n pos(\neg \otimes ai \sim + A(c'')(pos[km \neq i]) \diamond p[msk \neq i] + ai[(msk + msk \wedge \sim am) \neq -1 + + km]
     i \leftarrow \underline{\iota}(t[p]=A) \wedge (k[p]=6) \wedge t=N
     p, \leftarrow i \diamond t k n pos end(\neg, I) \leftarrow c i \diamond t k n(\neg @ i \sim) \leftarrow A 1(c'')
A PARSE B←D...
A PARSE B←...D
A Rationalize F[X]
     _←p[i]{
         >m←t[ω]=-1:'SYNTAX ERROR:NOTHING TO INDEX'□SIGNAL 2
         k[\omega/\sim m^{-1}\phi(k[\omega] \in 2 \ 3 \ 5) \vee (\omega) = 4] \leftarrow 4
     0}\exists i \leftarrow \underline{\iota}(t[p] \in B \ Z) \land (p \neq \iota \neq p) \land k[p] \in 1 \ 2
     i \leftarrow \underline{\iota}(t=1) \land k=4 \diamond j \leftarrow \underline{\iota}(t[p]=1) \land k[p]=4
      (≢i)≠≢j:{
         2'AXIS REQUIRES SINGLE AXIS EXPRESSION'SIGNAL epos[\omega]+i"end[\omega]-pos[\omega]
     }¬¬+{cα+~1<≠ω}目p[j]
     v/msk+t[j]≠Z:{
         2'AXIS REQUIRES NON-EMPTY AXIS EXPRESSION'SIGNAL \epsilonpos[\omega]+\iota"end[\omega]-pos[\omega]
     }msk/p[j]
     p[j]+p[i] \diamond t[i]+P \diamond end[i]+1+pos[i]
A Group function and value expressions
     i km\leftarrow, \neqp[i]{(\alpha,\omega)(0,1\vee\omega)}\existsi \leftarrow \iota(t[p]\inB Z)\wedge(p\neqι\neqp)\wedgek[p]\in1 2
A Mask and verify dyadic operator right operands
      (dm \leftarrow 1\phi(k[i]=4) \land t[i] \in F P V Z) \lor . \land (\sim km) \lor k[i] \in O 3 4:{
          'MISSING RIGHT OPERAND'□SIGNAL 2
     }0
A Refine schizophrenic types
     k[i/(k[i]=5)\wedge dmv^{-1}\phi(\sim km)\vee(\sim dm)\wedge k[i]\in 1 6]\leftarrow 2 \diamond k[i/(k[i]=5)\leftarrow 3
```

```
A Rationalize o.
         jm \leftarrow (t[i]=P) \land n[i] \in \subset, ' \circ . '
         imv.∧1φ(~km)vk[i]∈3 4: 'MISSING OPERAND TO ∘.'□SIGNAL 2
         p \leftarrow ((ji \leftarrow jm \neq i) @ (jj \leftarrow i \neq i \neq i = 1 + i \neq j = 1
         n[ji,jj]+n[jj,ji] ops[ji,jj]+pos[ji,ji] end[ji,jj]+end[jj,jj]
A Mask and verify monadic and dyadic operator left operands
         v \neq msk \leftarrow (dm \wedge 2 \varphi \sim km) \vee (1 \varphi \sim km) \wedge mm \leftarrow (k[i]=3) \wedge t[i] \in F P V Z: {
               2'MISSING LEFT OPERAND'SIGNAL \epsilon pos[\omega] + \iota"end[\omega]-pos[\omega]
         }i ≠~msk
         msk←dm∨mm
A Parse function expressions
         np+(\not\equiv p)+ixc+\not\equiv oi+msk\neq i \diamond p+(np@oii\not\equiv p)[p] \diamond p,+oi \diamond t k n pos end(\neg,I)+coi
         p[g \neq i] \leftarrow oi[(g \leftarrow (\sim msk) \land (1 \phi msk) \lor 2 \phi dm) \neq xc - \phi + \gamma \phi msk]
         p[q/oi] \leftarrow (q \leftarrow msk/(1 \phi mm) \vee 2 \phi dm) / 1 \phi oi \diamond t[oi] \leftarrow 0 \diamond n[oi] \leftarrow c''
         pos[oi] \leftarrow pos[g \neq i][msk \neq -1++ g \leftarrow (\sim msk) \land (1 \phi mm) \lor 2 \phi dm]
         ol+1+(k[i+\sim (2\phi mm) \times 3\phi dm]=4) \times k[i+\sim (1\phi mm) \times 2\phi dm] \in 2 3
         or \leftarrow (msk/dm) + 1 + k[dm/i] = 2
         k[oi]←3 3⊥tor ol
A Wrap all assignment values as I nodes
         i km\leftarrow,\neqp[i]{(\alpha,\omega)(0,1\vee\omega)}目i\leftarrow\underline{\iota}(t[p]\inB Z)\wedge(p\neqι\neqp)\wedgek[p]\in1
         j \leftarrow i \not\sim msk \leftarrow (t[i]=P) \land n[i] \in \subset, ' \leftarrow ' \diamond nz \leftarrow (\not \equiv p) + izc \leftarrow + \not \sim msk
         zm\leftarrow^{-1}\phi msk \diamond p[km/i]\leftarrow(zpm/(i\times\sim km)+zm\nz)[km/^{-1}++\zpm\leftarrow zm\vee\sim km]
A This is the definition of a function value at this point
         isfn \leftarrow \{(t[\omega] \in O \ F) \lor (t[\omega] \in B \ P \ V \ Z) \land k[\omega] = 2\}
A Parse modified assignment to E4(V, F, Z)
          j \leftarrow i \neq \text{m} \leftarrow \text{msk} \land (\text{-1}\phi i \text{sfn} i) \land \text{-2}\phi(t[i]=V) \land k[i]=1 \diamond p[zi \leftarrow nz \neq \text{msk} \neq m] \leftarrow j
         A Parse bracket modified assignment to E4(E6, O2(F, P3(\leftarrow)), Z)
         j \leftarrow i \neq m \leftarrow msk \wedge (-1\phi isfn i) \wedge (-2\phi t[i] = -1) \wedge -3\phi (t[i] = V) \wedge k[i] = 1
         p[zi \leftarrow nz \neq msk \neq m] \leftarrow ei \leftarrow i \neq 3 \neq m \diamond t k end(\neg @ei = ) \leftarrow E + (end[zi])
         p t k n(¬@(i/~2φm)~)←ei E 6(⊂'')
         p, +j \diamond t, +Pp \stackrel{\sim}{=} j \diamond k, +3p \stackrel{\sim}{=} j \diamond n, +(\neq j)p < j < pos, +pos[j] \diamond end, +end[j]
         p t k n pos(\neg @j \sim) +ei O 2(c'')(pos[fi+i \neq \sim1\phim]) \Diamond p[fi]+j
A Parse bracket assignment to E4(E6, P2(\leftarrow), Z)
         j \leftarrow i \neq m \leftarrow m \leq k \wedge (-1 \varphi t[i] = -1) \wedge -2 \varphi (t[i] = V) \wedge k[i] = 1 \Leftrightarrow p[zi \leftarrow nz \neq m \leq k \neq m] \leftarrow ei \leftarrow i \neq 2 \varphi m
         t k end(\neg @ei \sim ) \leftarrow E + (end[zi]) \diamond p t k n(<math>\neg @(i \neq \sim 1 \phi_m) \sim ) \leftarrow ei E 6(<'')
         p t k(¬@j~) ←ei P 2
```

```
A Parse modified strand assignment
      A Parse strand assignment
     A SELECTIVE MODIFIED ASSIGNMENT
      A SELECTIVE ASSIGNMENT
      A Enclose V[X;...] for expression parsing
                 i \leftarrow i [Ap[i \leftarrow \underline{\iota}(t[p] \in B \ Z) \land (k[p] = 1) \land p \neq \iota \neq p]] \diamond j \leftarrow i \neq \widetilde{\iota} jm \leftarrow t[i] = 1
                 t[j] \leftarrow A \diamond k[j] \leftarrow 1 \diamond p[i \neq 1 \phi jm] \leftarrow j
      A TRAINS
      A Parse expression sequences
                 i km\leftarrow,\neqp[i]{(\alpha,\omega)(0,(2≤\neq\omega)\wedge1\vee\omega)}目i\leftarrow1(t[p]\inB Z)\wedge(k[p]=1)\wedgep\neq1\neqp
                 msk+m2 \lor fm \land \sim^{-1} dm2 + km \land (1 dkm) \land \sim fm + (t[i]=0) \lor (t[i] \neq A) \land k[i]=2
                 t, ←Ep~xc++/msk ♦ k, ←msk/msk+m2 ♦ n, ←xcp<''
                 pos, ←pos[msk/i] ◇ end, ←end[p[msk/i]]
                 p, \leftarrow msk \neq -1 \varphi(i \times \sim km) + km \times x \leftarrow -1 + (\not \equiv p) + + \ \ \ \ \ \ p[km \neq i] \leftarrow km \neq x
      A Rationalize V[X;...]
                 i \leftarrow i [Ap[i \leftarrow \iota(t[p]=A) \land k[p]=-1]] \diamond msk \leftarrow 2 \neq f^{-1}, ip \leftarrow p[i] \diamond ip \leftarrow \iota ip \diamond nc \leftarrow 2 \times \neq ip
                 t[ip] \leftarrow E \diamond k[ip] \leftarrow 2 \diamond n[ip] \leftarrow c'' \diamond p[msk \neq i] \leftarrow msk \neq (\not\equiv p) + 1 + 2 \times (ip) 
                 p, +2/ip ◊ t, +ncpP E ◊ k, +ncp2 6 ◊ n, +ncp, "'[' ''
                 pos, +2/pos[ip] \diamond end, +\epsilon(1+pos[ip]), -end[ip] \diamond pos[ip]+pos[i/~msk]
      A Sanity check
                 ERR←'INVARIANT ERROR: I node with multiple children'
                 ERR assert(+/(t[p]=Z) \land p \neq i \neq p)=+/t=Z:
      A Count parentheses in source information
                 ip+p[i+\underline{\iota}(t[p]=Z)\wedge n[p]\in c,'('] \diamond pos[i]+pos[ip] \diamond end[i]+end[ip]
      A VERIFY Z/B NODE TYPES MATCH ACTUAL TYPE
      A Eliminate Z nodes from the tree
                 zi \leftarrow p I@\{t[p[\omega]] = Z\} \stackrel{*}{\times} = ki \leftarrow \underline{\iota} msk \leftarrow (t[p] = Z) \land t \neq Z
                 p+(zi@kiı≢p)[p] ♦ t k n pos end(⊣@zi~)+t k n pos end I~cki
                 t k n pos endf \sim \text{-cmsk} + \text{-msk} \times t = Z \Leftrightarrow p + (\underline{\iota} \sim \text{msk}) (\vdash -1 + \underline{\iota}) \text{msk} \neq p
      A Compute Exports
                 msk \leftarrow (t=B) \land k[I@\{t[\omega] \neq F\} \stackrel{*}{=} \stackrel{\sim}{p}] = 0
                 xn←(0p⊂''),msk/n ◊ xt←msk/k
                 d i\leftarrowP2D p \diamond d n t k pos end I\circ+\leftarrowci \diamond sym\leftarrowU('')(,'\omega')(,'\alpha')'\alpha\alpha' '\omega\omega',n
                  (d t k(-symin)pos end)(xn xt)sym IN}
This code is used in chunk 3a.
```

Uses TEST 31a.

4.4 Compiler Transformations

```
15
           \langle Compiler 15 \rangle \equiv
                 TT \leftarrow \{((d \ t \ k \ n \ ss \ se) \ exp \ sym \ src) \leftarrow \omega \diamond \ I \leftarrow \{((\neg \omega)) \ \alpha\}
                      ABCEFGKLMNOPSVZ+1+115
               A Compute parent vector and reference scope
                      r \leftarrow I@\{t[\omega] \neq F\} \stackrel{\sim}{*} \equiv \stackrel{\sim}{p} \rightarrow 2\{p[\omega] \leftarrow \alpha[\alpha\underline{\iota}\omega]\} \neq r \circ c = d \rightarrow p \leftarrow \iota \neq d
               A Lift Functions to top-level
                      p, \leftarrow n[i] \leftarrow (\neq p) + i \neq i \leftarrow \underline{i}(t = F) \land p \neq i \neq p \diamond t k n r(\neg, I) \leftarrow ci \diamond p r I \leftarrow \leftarrow cn[i] @ i \vdash i \neq p
                      t[i]←C
               A Wrap expressions as binding or return statements
                      i \leftarrow (\iota(\neg t \in F G) \land t[p] = F), \{\omega \neq 2 \mid \iota \neq \omega\}_{\iota t[p] = G} \diamond p t k n r \neq \leftarrow cm \leftarrow 2@i \vdash 1p \neq p
                      pri I \sim \leftarrow j \leftarrow (+ + m) - 1 \diamond n \leftarrow j \quad I@(0 \leq \vdash) n \diamond p[i] \leftarrow j \leftarrow i - 1
                      k[j] \leftarrow (k[r[j]] = 0) \lor 0@({ \Rightarrow \phi} \exists p[j]) \vdash (t[j] = B) \lor (t[j] = E) \land k[j] = 4 \diamond t[j] \leftarrow E
               A Lift guard tests
                      p[i]+p[x+^{-1}+i+\{\omega/^{\sim}-2|i\neq\omega\}_{\underline{i}}t[p]=G] \diamond t[i,x]+t[x,i] \diamond k[i,x]+k[x,i]
                      n[x] \leftarrow n[i] \diamond p \leftarrow ((x,i)@(i,x) \vdash i \neq p)[p]
               A Count strand and indexing children
                      n[\underline{\iota}(t \in A \in E) \land k = 6] \leftarrow 0 \diamond n[p \neq (t[p] \in A \in E) \land k[p] = 6] + \leftarrow 1
               A Lift and flatten expressions
                      p[i] \leftarrow p[x \leftarrow p \ I@{\sim t[p[\omega]] \in F \ G} \times = i \leftarrow i t \in G \ A \ B \ C \ E \ O \ P \ V] \diamond i \leftarrow (\phi i)[\Delta \phi x]
                      p t k n r{\alpha[\omega]@i+\alpha}\leftarrowcj \diamond p\leftarrow(i@j+\iota$p)[p]
               A Compute slots for each frame
                      s \leftarrow 1, \forall \in i \quad n[ \cup x] \leftarrow \emptyset \neq [x \leftarrow 0] \forall e \leftarrow \cup [ \emptyset \downarrow \neg n \leftarrow r[b], \neg n[b \leftarrow t = B]
               A Compute frame depths
                      d \leftarrow (\not\equiv p) \uparrow d \diamond d[i \leftarrow \iota t = F] \leftarrow 0 \diamond \leftarrow \{z \rightarrow d[i] + \leftarrow \omega \neq z \leftarrow r[\omega]\} \stackrel{\checkmark}{=} i \diamond f \leftarrow d[0] \stackrel{\lozenge}{\lozenge} e], \stackrel{\frown}{=} 1
               A Record exported top-level bindings
                      xi \leftarrow \underline{\iota}(t=B) \wedge k[r]=0
                      ptknfsrdxi sym}
           This code is used in chunk 3a.
           Uses src 29c.
```

4.5 Code Generator

```
\langle Code\ Generator\ 16 \rangle \equiv
16
         GC←{
            p t k n fr sl rf fd xi sym←ω ◇ A B C E F G K L M N O P S V Z←1+:15
            I \leftarrow \{( \subset \omega) [\alpha] \land com \leftarrow \{ \supset \{\alpha, ', ', \omega\} / \omega \}
            ks \leftarrow \{\omega \subset [0] \sim (\neg \omega) = \omega[;0]\} \diamond nam \leftarrow \{'\Delta' \square R' \_ ' \circ \sigma \sim sym[|\omega]\}
           syms ←,"'+'
                                                                                                         '['
                                          '×'
                                                  ' <u>+</u> '
                                                          ۱*۱
                                                                  '⊛'
                                                                          '1'
                                                                                    '0'
                                                                                               '['
           nams ← 'add'
                                         'mul' 'div' 'exp' 'log' 'res'
                                                                                                       'max' 'fac
                                'sub'
                                                                                   'cir'
                                                                                              'min'
           syms,←,"'<'
                                '≤'
                                          ' = '
                                                  '≥'
                                                          ' > <sup>i</sup>
                                                                  '≠'
                                                                                    ' ^ '
                                                                                               ' v '
                                                                                                         ' ~ '
           nams,← 'lth'
                                'lte'
                                                 'gte'
                                                         'gth'
                                         'eql'
                                                                  'neq'
                                                                          'not'
                                                                                              'lor'
                                                                                   'and'
                                                                                                       'nan'
                                                   ρ'
            syms, ←, "'[]'
                                '['
                                          'ι'
                                                                           'φ'
                                                                                    'p'
                                                                                               '⊖'
                                                                                                        ' ∈ '
           nams,← 'sqd'
                                                         'cat'
                                                                 'ctf'
                                                                                   'trn'
                                'brk'
                                         'iot'
                                                 'rho'
                                                                         'rot'
                                                                                              'rtf'
                                                                                                       'mem'
           syms,←,"'≡
                                '≢'
                                          '⊢'
                                                  '⊣'
                                                          'т'
                                                                  '1'
                                                                           '/'
                                                                                    '†'
                                                                                               '\'
                                                                                                         '+'
                                                 'lft' 'enc' 'dec' 'red'
           nams,← 'eqv'
                                         'rgt'
                                'nqv'
                                                                                   'rdf'
                                                                                              'scn'
                                                                                                       'scf' 'rol
                                ' ↓ '
                                                                                    ' 0 '
                                                                                                        ' n '
            syms,←,"'↑'
                                                  ' ∷ '
                                                                                               ' u '
           nams,← 'tke'
                                'drp'
                                                'com' 'dot' 'rnk' 'pow'
                                                                                             'unq'
                                                                                                       'int' 'get
                                         'map'
                                                                                   'jot'
           syms,←,"'↓'
                                                '<u>€</u>'
                                'ቑ'
                                        ' • . '
                                                        ' c '
                                                                '∄'
                                                                       'DFFT'
                                                                                 '[]IFFT'
                                                                                            '%s'
                                                                                                    '<u>⊆</u>'
                                                                 'mdv' 'fft'
                                                                                                     'nst' 'conv
           nams, ← 'gdu'
                                gdd'
                                         'oup' 'fnd' 'par'
                                                                                  'ift'
                                                                                             'scl'
            syms,←,"'∇'
                                          'α'
                                                  'ω'
                                                                          '%u'
                                                           'αα'
                                                                   'ωω'
                                                                          1.1
                                                          'aa'
            nams,← 'this' 'span' 'l'
                                                  'r'
                                                                  'ww'
            gck \leftarrow (A 1)(A 6)
           gcv← 'Aa' 'As'
            gck, \leftarrow (B \ 1)(B \ 2)(B \ 3)(B \ 4)
           gcv,←'Bv' 'Bf' 'Bo' 'Bo'
            gck, \leftarrow (C 1)(C 2)
           gcv, ←'Ca' 'Cf'
            gck, +(E -2)(E -1)(E 0)(E 1)(E 2)(E 4)(E 6)
            gcv, ←'Ec' 'Ek' 'Er' 'Em' 'Ed' 'Eb' 'Ei'
            gck, \leftarrow (F \ 0)(F \ 2)(F \ 3)(F \ 4)
            gcv, ←'Fz' 'Fn' 'Fm' 'Fd'
            gck, \leftarrow (G \ 0)(N \ 1)
           gcv,←'Gd' 'Na'
            qck, \leftarrow (0\ 1)(0\ 2)(0\ 4)\ (0\ 5)\ (0\ 7)\ (0\ 8)
            gcv, ←'Ov' 'Of' 'Ovv' 'Ofv' 'Ovf' 'Off'
            qck, \leftarrow (P \ 0)(P \ 1)(P \ 2)(P \ 3)(P \ 4)
            gcv, ←'Pv' 'Pv' 'Pf' 'Po' 'Po'
            gck, \leftarrow (V \ 0)(V \ 1)(V \ 2)(V \ 3)(V \ 4)
            gcv, ←'Va' 'Va' 'Vf' 'Vo' 'Vo'
            gcv,←c'{''/* Unhandled '',(⊽α),'' */'',NL}'
           NL← UCS 13 10
            pref <c '#include "codfns.h"'
            pref, ←c''
```

'!

' ~

'nor

'dis

۰,

'?

۰+

'□CONV

```
pref,←c'EXPORT int'
pref, ←c'DyalogGetInterpreterFunctions(void *p)'
pref, ←c'{'
pref, +c' return set_dwafns(p);'
pref,←c'}'
pref, ←c''
Bf+{id+sym>~|4>α
  z <cid,' = retain_cell(stkhd[-1]);'</pre>
z }
Cf←{id←φ4⊃α
  z +c'mk_closure((struct closure **)stkhd++, fn',id,', 0);'
z }
Ek+{
  z +c'release_cell(*--stkhd);'
  z,←c''
z }
Em+{
  z ←c'c = *--stkhd;'
  z, ←c'w = *--stkhd;'
  z, <-c'(c->fn)((struct array **)stkhd++, NULL, w, c->fv);'
 z,←c'release_cell(c);'
  z,←c'release_cell(w);'
z }
Er←{
  z ←c'*z = *--stkhd;'
  z,←c'goto cleanup;'
  z, ←c ' i
z }
Fn \leftarrow \{id \leftarrow \sqrt{5} > \alpha \land x \leftarrow \sqrt{5} = \sqrt{4} \land t \leftarrow 2[x \land k \leftarrow 3]x\}
  hsw \leftarrow (t=0) \lor (t=E) \land k \in 1 \ 2 \ \diamond \ hsa \leftarrow ((t=E) \land k=2) \lor (t=0) \land k \in 4 \ 5 \ 7 \ 8
  z ←c'int'
 z,←c'fn',id,'(struct array **z, struct array *l, struct array *r, void *fv[])
  z,←c'{'
  z,←c'
                      *stk[128];'
           void
  z,←c' void
                   **stkhd;'
                             *w;'
  z,←hsw/c'
                   void
  z,←hsa/c'
                              *a;'
                    void
  z,←hsw/c'
                    struct closure *c;'
  z, ←c''
  z, \leftarrow c' stkhd = &stk[0];'
```

```
z,←c''
  z,← '
            ',"⊃,∱dis"ω
  z,←c'
           *z = NULL; '
  z,←c''
  z,←⊂'cleanup:'
  z,←c'
          return 0;'
  z, +c'}'
  z,←c''
z }
Fz\leftarrow \{id\leftarrow 5>\alpha \land awc\leftarrow v\neq (3[x)\{(w\in A\ O)\lor(w=E)\land\alpha>0\}2[x\leftarrow b>-,\neq w\}\}
  z +c'int init',id,' = 0;'
  z,←c''
  z,←c'EXPORT int'
  z,←c'init(void)'
  z,←c'{'
  z,←c'
          return fn',id,'(NULL, NULL, NULL, NULL);'
  z, <c'}'
  z,←c''
  z,←c'int'
 z,←c'fn',id,'(struct array **z, struct array *l, struct array *r, void *fv[])
  z, +c'{'
  z,←c'
           void
                     *stk[128];'
  z,←c'
           void
                     **stkhd;'
  z,←awc/⊂'
                            *a, *w;'
                  void
  z,←awc/⊂'
                  struct closure *c;'
  z,←c''
  z,←c'
           if (init',id,')'
  z,←c'
                     return 0;'
  z,←c''
  z,←c'
           stkhd = &stk[0];'
  z,←c'
           init',id,' = 1;'
  z,←c'
           cdf_init();'
  z,←c''
  z,← '
             ',"⊃,∱dis"ω
  z,←c'
          return 0;'
  z, +c'}'
  z, ←c''
z }
Pf+{id+(symsisym[|4>α])>nams
 z +c'*stkhd++ = retain_cell(',id,');'
z }
Va \leftarrow \{id \leftarrow (|4 \Rightarrow \alpha) \Rightarrow '' 'r' 'l' 'aa' 'ww', 5 \downarrow sym
  z +c'*stkhd++ = retain_cell(',id,');'
```

```
z}
Zp+{n+'fn', φω
  k[ω]∈0 2:{
    z ←c'int'
    z, +cn, '(struct array **z, struct array *l, struct array *r, void *fv[]);
    z, ←c''
  z}ω
  'UNKNOWN FUNCTION TYPE'□SIGNAL 16
}
Zx \leftarrow \{n \leftarrow sym \Rightarrow \sim |n[\omega] \diamond rid \leftarrow \sigma rf[\omega]
  k[ω]=0:c''
  k[\omega]=1:{}
    z +c'struct array *',n,';'
  k[\omega] = 2:{
    z +c'struct closure *',n,';'
    z,←c''
    z,←c'EXPORT int'
    z, \leftarrow cn, '\_dwa(struct\ localp\ *zp,\ struct\ localp\ *lp,\ struct\ localp\ *rp)'
    z,←c' struct array *z, *l, *r;'
    z,←c' int err;'
    z,←c''
    z, <- c' l = NULL; '
    z, <c' r = NULL;'
    z,←c''
    z,←c' fn',rid,'(NULL, NULL, NULL, NULL);'
    z,←c''
    z,←c' err = 0;'
    z,←c''
    z,←c' if (lp)'
    z,←c'
                    err = dwa2array(&l, lp->pocket);'
    z,←c''
    z,←c' if (err)'
    z,←c'
                     dwa_error(err);;'
    z,←c''
    z, ←c' if (rp)'
    z,←c'
                     dwa2array(&r, rp->pocket);'
    z,←c''
    z,←c' if (err) {'
    z,←c'
                     release_array(l);'
    z,←c'
                     dwa_error(err);'
    z,←c'}'
    z,←c''
```

```
z, +c' err = (',n,'->fn)(&z, l, r, ',n,'->fv);'
      z,←c''
      z,←c' release_array(l);'
      z,←c' release_array(r);'
      z,←c''
      z,←c' if (err)'
      z,←c'
                          dwa_error(err);'
      z,←c''
      z, +c' err = array2dwa(NULL, z, zp);'
      z,←c' release_array(z);'
      z,←c''
      z,←c' if (err)'
     z,←c'
                          dwa_error(err);'
     z,←c''
      z,←c' return 0;'
     z, +c'}'
     z, ←c''
   z}ω
   ±'''UNKNOWN EXPORT TYPE''□SIGNAL 16'
d i+P2D p ◊ ast+(\q\d p t k n(\i\d p)\fr sl fd)[i;]
NOTFOUND+\{('[GC] \text{ UNSUPPORTED NODE TYPE }',N\Delta[\supset\omega],$$\pi\supset$$\phi\omega)[SIGNAL 16}
 dis \leftarrow \{0 = 2 \Rightarrow h \leftarrow, 1 \uparrow \omega: ' ' \diamond (\not\equiv gck) = i \leftarrow gck \ i \leftarrow h[2\ 3]: NOTFOUND\ h[2\ 3] \diamond h(\not\equiv i \rightarrow gcv) \ ks \ 1 \downarrow \omega \} 
z \leftarrow \epsilon, \circ NL"pref, \Rightarrow, \neq(, \neqZp"\underline{\iota}t=F), (, \neqZx"xi), (\subset c'), dis"ks ast
```

This code is used in chunk 3a.

Uses codfns 3a.

4.6 Backend C Compiler Interface

```
\langle Interface to the backend C compiler 21 \rangle \equiv
21
       CC←{
          vsbat←VS∆PATH,'\VC\Auxiliary\Build\vcvarsall.bat'
          tie\leftarrow{0:: \squareSIGNAL \squareEN \diamond 22::\omega \squareNCREATE 0 \diamond 0 \squareNRESIZE \omega \squareNTIE 0}
          put+{s+(^128+256|128+'UTF-8'^1UCS α)^1NAPPEND(t+tie ω)83 ♦ 1:r+s-^1NUNTIE t}
          opsys←{ω¬~'Win' 'Lin' 'Mac'ι⊂3↑¬'.'□WG'APLVersion'}
          soext+{opsys'.dll' '.so' '.dylib'}
         cco←'-std=c99 -Ofast -g -Wall -fPIC -shared -Wno-parentheses
          cco, ←'-Wno-misleading-indentation '
          ucc \leftarrow \{\omega\omega(\Box SH \alpha\alpha, ' ', cco, cci, ccf)\omega\}
          gcc←'gcc'ucc'so'
          clang+'clang'ucc'dylib'
          vsco+{z+'/W3 /wd4102 /wd4275 /O2 /Zc:inline /Zi /FS /Fd"',ω,'.pdb" '
            z,←'/WX /MD /EHsc /nologo '
            z,'/I"%AF PATH%\include" /D "NOMINMAX" /D "AF DEBUG" '}
          vslo+{z+'/link /DLL /OPT:REF /INCREMENTAL:NO /SUBSYSTEM:WINDOWS '
            z,←'/LIBPATH:"%AF PATH%\lib" /OPT:ICF /ERRORREPORT:PROMPT /TLBID:1 '
            z,'/DYNAMICBASE "af', AFΔLIB, '.lib" "codfns.lib" '}
          vscO+{~□NEXISTS vsbat:'VISUAL C?'□SIGNAL 99 ♦ '""',vsbat,'" amd64'}
          vsc1+{' && cd "',(¬□CMD'echo %CD%'),'" && cl ',(vsco ω),' "',ω,'.c" '}
          vsc2+{(vslo ω),'/OUT:"',ω,'.dll" > "',ω,'.log""'}
          vsc \leftarrow \{ \Box CMD \ ('\%comspec\% \ /C \ ', vsc0, vsc1, vsc2) \omega \}
           +(±opsys'vsc' 'gcc' 'clang')α⊣ω put α,'.c'⊣1 □NDELETE f+α,soextθ
          \square \leftarrow_{\tau} \supset \square NGET(\alpha, '.log')1
         □NEXISTS f:f ♦ 'COMPILE ERROR' □SIGNAL 22}
     This code is used in chunk 3a.
     Uses AFALIB 3b, AFAPREFIX 3b, codfns 3a, put 32b, tie 32b, vsbat 30a,
       and VSAPATH 3b.
```

4.7 Linking with Dyalog

```
\langle Linking \ with \ Dyalog \ 22a \rangle \equiv
22a
              NS←{
                  MKA \leftarrow \{mka \subset \omega\} \diamond EXA \leftarrow \{exa \theta \omega\}
                  Display←{α←'Co-dfns' ♦ W←w_new⊂α ♦ 777::w_del W
                      w\_del \  \, W \dashv W \  \, \alpha\alpha\{w\_close \  \, \alpha: \underline{*} \, ' \, \square \\ SIGNAL \  \, 777 \, ' \  \, \diamond \  \, \alpha \  \, \alpha\omega\} \\ \ddot{*} \, \omega\omega \vdash \omega\} 
                  LoadImage \leftarrow \{\alpha \leftarrow 1 \diamond \sim \square \text{NEXISTS } \omega : \square \text{SIGNAL } 22 \diamond \text{ loading } \theta \omega \alpha \}
                  SaveImage \leftarrow \{\alpha \leftarrow ' \text{ image.png'} \Rightarrow \text{ saveimg } \omega \alpha \}
                  Image←{~2 3∨.=∮ρω:□SIGNAL 4 ♦ (3≠⊃ρω)∧3=∮ρω:□SIGNAL 5 ♦ ω⊣ν_img ω α}
                  Plot+{2≠\neqρω: □SIGNAL 4 \diamond ~2 3\vee.=1>ρω: □SIGNAL 5 \diamond ω\dashvw_plot (\Diamondω) α}
                  Histogram←\{ω¬ν\_hist ω,α\}
                  Rtm∆Init←{
                                       □NA'P ',ω,'|w_new
                     _←'w_new'
                                                                          <C[]'
                     _←'w_close'□NA'I ',ω,'|w_close P'
                     _←'w_del'
                                       □NA
                                                     ω,'|w_del
                     _←'w_img'
                                                     ω,'|w_img
                                                                         <PP P'
                                       □NA
                     _←'w_plot' □NA
                                                     ω, '|w_plot <PP P'
                     \omega, '|w_hist <PP F8
                                                                                         F8 P'
                     _←'loadimg'□NA
                                                     ω,'|loadimg >PP <C[] I'
                     _←'saveimg'□NA
                                                     ω,'|saveimg <PP <C[]'
                                                     ω, '|exarray >PP P'
                     _←'exa'
                                       □NA
                                       □NA'P ',ω,'|mkarray <PP
                     _←'mka'
                     _←'FREA'
                                                     ω, '|frea
                                       □NA
                      ←'Sync'
                                       □NA
                                                     \omega, '|cd sync'
                     0 0 p <del>0</del>}
                  \begin{array}{l} mkna \leftarrow \{\alpha, ' \mid ', ('\Delta' \square R' \_ ' \vdash \omega), '\_cdf \ P \ P \ P'\} \\ mkf \leftarrow \{fn \leftarrow \alpha, ' \mid ', ('\Delta' \square R' \_ ' \vdash \omega), '\_dwa \ ' \Leftrightarrow mon \ dya \leftarrow \omega \circ, ''' \_mon' \ '\_dya' \end{array} 
                     z \leftarrow ('Z \leftarrow \{A\}', \omega, 'W')(': \text{If } O = \square NC'' \underline{\Delta}.', mon, '''')
                     z,÷(mon dya{'''',α,'''<u>Δ</u>. □NA''',fn,ω,' <PP'''}"'>PP P' '>PP <PP'),c':EndIf
                    z,':If O=□NC''A'''('Z←<u>∆</u>.',mon,' O O W')':Else'('Z←<u>∆</u>.',dya,' O A W')':EndIf'
                  ns+\#. \square NS\Theta \diamond \_+'\Delta\Delta' ns. \square NS"=\Theta \diamond \Delta \underline{\Delta}+ns. (\Delta \underline{\Delta}) \diamond \Delta. names+(0p=''), (2=1>\alpha) \neq 0>\alpha
                  fns←'Rtm∆Init' 'MKA' 'EXA' 'Display' 'LoadImage' 'SaveImage' 'Image' 'Plot'
                  fns, + 'Histogram' 'soext' 'opsys' 'mkna'
                  _+Δ.□FX∘□CR"fns ♦ Δ.(decls+ω∘mkna"names) ♦ _+ns.□FX"(<''),ω∘mkf"Δ.names
                  __←Δ.□FX'Z←Init'('Z←RtmΔInit ''',ω,'''')'→0/~0=≢names' 'names ##.Δ.□NA"decls
                 ns}
```

This code is used in chunk 3a. Uses PP 34.

5 Co-dfns Runtime

```
22b \langle Implementation \ of \ APL \ Primitives \ 22b \rangle \equiv A TBW
```

Root chunk (not used in this document).

23a $\langle CRuntime\ Support\ 23a \rangle \equiv$ /* TBW */

Root chunk (not used in this document).

23b $\langle C Runtime Header 23b \rangle \equiv$ /* TBW */

Root chunk (not used in this document).

6 Developer's Guide

6.1 Building the Compiler

6.1.1 Tangling and Weaving the Literate Source

The Co-dfns compiler is written, developed, and distributed as a literate program. For more information about literate programming, see the resources available at http://literateprogramming.com/. We use noweb as our preferred literate programming tool because it is eminently simple, while still handling the majority of our needs and producing high quality output in LATEX format with all the important elements of literate programming, including live hyperlinking and cross-references. We intend codfns.nw to tangle into the following files based on specific chunks that have been provided in this document.

Chunk	File Output
⟨* 3a⟩	src\codfns.apln
(C Runtime Support 23a)	rtm\runtime.c
$\langle C Runtime Header 23b \rangle$	rtm\codfns.h
(Implementation of APL Primitives 22b)	rtm\prim.apln
(DISPLAY <i>Utility</i> 33)	<pre>src\DISPLAY.aplf</pre>
$\langle MK \Delta RTM \ Command \ 29 b \rangle$	src\MK∆RTM.aplf
(PP <i>Utility</i> 34)	src\PP.aplf
(TANGLE $Command~25$)	src\TANGLE.aplf
(TEST Function 31a)	src\TEST.aplf
(WEAVE Command 27)	<pre>src\WEAVE.aplf</pre>
⟨Tangle Script 24⟩	TANGLE.sh
(Weave Script 26)	WEAVE.sh

The following bash script will create these files.

and WEAVE 27.

```
#!/bin/bash
notangle codfns.nw > src/codfns.apln
notangle -R'[[DISPLAY]] Utility' codfns.nw > src/DISPLAY.aplf
notangle -R'[[MKΔRTM]] Command' codfns.nw > src/MKΔRTM.aplf
notangle -R'[[PP]] Utility' codfns.nw > src/PP.aplf
notangle -R'[[TANGLE]] Command' codfns.nw > src/TANGLE.aplf
notangle -R'[[TEST]] Function' codfns.nw > src/TEST.aplf
notangle -R'[[WEAVE]] Command' codfns.nw > src/WEAVE.aplf
notangle -R'Tangle Script' codfns.nw > TANGLE.sh
notangle -R'Weave Script' codfns.nw > WEAVE.sh
Root chunk (not used in this document).
Uses codfns 3a, DISPLAY 33, MKARTM 29b, PP 34, src 29c, TANGLE 25, TEST 31a,
```

On Windows, the best way that we have found to do this is via the Cygwin project. This document assumes that you have already successfully built and installed via Cygwin a working Icon-driven noweb installation.

Users who prefer to work in a UNIX fashion via Cygwin or some other subsystem on Windows can follow the build scripts directly. For developers who prefer to work in a primarily Windows environment, the following build scripts assist in handling the calls into Cygwin so that you do not need to have a Cygwin terminal open all the time.

When tangled to the TANGLE.aplf file, this script will enable the user simply type TANGLE to update the code tree from within a Dyalog APL Session. This is much more convenient than keeping a Cygwin Terminal session open along with a Dyalog APL session while programming. At the moment, this file is only designed to work on Windows with Cygwin, but we should in principle extend this to work on Linux and Mac OS X style machines as well.

Note: this command expects to be run from within the root of the repository, not from, say, within the testing directory.

```
25 ⟨TANGLE Command 25⟩≡

TANGLE; SH; CWD; CD

SH+'C:\cygwin64\bin\bash.exe -l -c '

CWD+>□CMD'C:\cygwin64\bin\bash.exe -c pwd'

CD+'cd ''', CWD, ''''

□CMD SH, '"', CD, ' && ./TANGLE.sh"'

Root chunk (not used in this document).

Defines:

TANGLE, used in chunk 24.
```

Weaving is the process by which we produce the final printed output of this document, intended for reading and general human consumption. We rely on the LATEX typesetting system to do this. Moreover, because we make heavy use of UTF-8 and prefer to have our own fonts installed and used, it is necessary to use the xelatex system instead of the typical LATEX engine. In order to get the indexing right, we must run the engine twice. The first run will update the indexing files that will be picked up on the second run and incorporated into the final document. Note, we have tried to use the lualatex engine, which in theory should work just as well as the xelatex engine, but we get a strange error relating to noweb's style file, so we stick with xelatex for now.

Running this script also depends on having the appropriate fonts installed. In this case, please ensure that the following fonts are installed in your Windows font system so that they can be picked up by the TFX engine.

- Libre Baskerville (Regular, Italic, Bold)
- APL385 Unicode
- Lucida Sans Unicode
- Cambria Math

Uses codfns 3a.

If you do not wish to use these fonts, then see the top of the codfns.nw file and edit the font specifications to the fonts that you do wish to

Note the use of -delay -index for options. We want to generate indexing, but we also need to make sure that we can use some of our own packages in the system,

Note: this command expects to be run from within the root of the repository, not from, say, within the testing directory.

```
26  (Weave Script 26)≡
    #!/bin/bash
    mkdir woven
    noweave -delay -index codfns.nw > woven/codfns.tex
    cd woven
    xelatex codfns
    xelatex codfns
    Root chunk (not used in this document).
```

Like the (TANGLE Command 25), the following command, when tangled to the WEAVE.aplf file permits the Windows programmer to simply execute WEAVE in a the Dyalog APL session and weave the documents together.

```
27 (WEAVE Command 27)≡
WEAVE;SH;CWD;CD
SH+'C:\cygwin64\bin\bash.exe -l -c '
CWD+→□CMD'C:\cygwin64\bin\bash.exe -c pwd'
CD+'cd ''',CWD,''''

□CMD SH,'"',CD,' && ./WEAVE.sh"'
Root chunk (not used in this document).
Defines:
WEAVE, used in chunk 24.
```

6.2 Loading the Compiler

In order to load the compiler into an APL session as well as all the development utilities, we assume that you have first managed to either load up a session with a bootstrapped version of the TANGLE command or that you already have a tangled <code>src\</code> directory. If the <code>src\</code> directory has not yet been created by running the TANGLE command, then this must be done before loading the compiler system. After tangling, the compiler can be loaded using the provided <code>LOAD</code> shortcut. This shortcut is meant to use the Dyalog Link system for hotloading the files in <code>src\</code> into the root namespace. We do so through the following link command:

Link.Create # src -source=dir -watch=dir

This means that we want to link the src\ directory into the # namespace, but we also want to make sure that we only pull changes that come from the filesystem. This is because we are editing the code via the WEB document, and we do not want to risk having some intermediate representation that isn't accurate and that doesn't flow the right way; we want all appropriate changes to begin in the WEB document and then, and only then, flow into the session. This also allows us to make some modifications to the code for testing and experimentation inside of the session without consideration for the code outside of the session, and such changes will be removed or forgotten on the next TANGLE command.

To set this up, we also ensure that we begin our work within the root Co-dfns repository directory, as this is where we expect to run the TANGLE and WEAVE commands.

There is unfortunately only a limited range of possibilities for linking in a new directory as we wish to do. The method we choose to use is launching a fresh Dyalog APL session and then using an LX expression from the command line to do the actual linking using the DSE.UCMD functionality. I personally find this to be rather hackish, and I hope that an alternative approach to doing this will show up in the near future. Nonetheless, the arguments that we pass to dyalog.exe look something like this:

LX="[SE.UCMD'Link.Create # src -source=dir -watch=dir'"

If you do not use the LOAD shortcut, you can use the above command to do the linking manually.

6.3 Building the Runtime

One of our goals with the Co-dfns runtime is to write as much of it as possible in APL. This means that we want to have at minimum a

very small kernel that has been written in C, while most of the rest of the code is implemented in some APL files. This leads to a three part breakdown of the process to build the runtime.

```
29a ⟨Build the runtime 29a⟩≡
⟨Compile the primitives in prim.apln 29c⟩
⟨Build codfns.dll DLL 30a⟩
⟨Copy the runtime files into tests\30b⟩
This code is used in chunk 29b.
```

We define the command MKARTM to build the runtime. This command takes a path to the root directory of the Co-dfns repository; this is to allow us to rebuild the runtime from anywhere in the system if we so choose.

```
29b (MKΔRTM Command 29b)≡
MKΔRTM path;prim;put;src;tie;vsbat;vsc;wsd

⟨Basic tie and put utilities 32b⟩
⟨Build the runtime 29a⟩
Root chunk (not used in this document).
Defines:
MKΔRTM, used in chunk 24.
Uses put 32b, src 29c, tie 32b, vsbat 30a, and wsd 30a.
```

The first step we must take is producing an appropriate C file that contains the primitives that we have defined in prim.apln. This means that we want to only compile the code in prim.apln as far as producing the C code. Since we do not have a full blown runtime yet, we will be compiling the prim.c file along with the rest of the runtime code, instead of the normal build process, which assumes that we already have a working runtime. This means that we only invoke the GC TT PS passes of the compiler pipeline, while avoiding the CC pass. We use the SALT system to load the source from prim.apln and then run the compiler passes that we want before storing the resulting code in the rtm\prim.c file.

```
29c (Compile the primitives in prim.apln 29c)≡
src+□SRC □SE.SALT.Load path, '\rtm\prim.apln'
(path, '\rtm\prim.c')put codfns.{GC TT PS ω}src
This code is used in chunk 29a.
Defines:
src, used in chunks 4a, 15, 24, and 29b.
Uses codfns 3a and put 32b.
```

Once we have the rtm\prim.c file written appropriately, we can run the main compiler process. For simplicity, we just compile all of the .c files that are found in the rtm\ subdirectory. We must ensure that we are appropriatelly invoking our ArrayFire dependencies as well as producing the appropriate debugging symbols most of the time.

```
\langle Build \text{ codfns.dl } DLL \text{ 30a} \rangle \equiv
30a
         vsbat←#.codfns.VS∆PATH,'\VC\Auxiliary\Build\vcvarsall.bat'
        wsd←path,'\'
         vsc←'%comspec% /C ""',vsbat,'" amd64'
         vsc, ←' && cd "', wsd, '\rtm"'
         vsc,←' && cl /MP /W3 /wd4102 /wd4275 /Od /Zc:inline /Zi /FS'
         vsc,←' /Fo".\\" /Fd"codfns.pdb"'
         vsc,←' /WX /MD /EHsc /nologo /I"%AF_PATH%\include"'
         vsc,←' /D "NOMINMAX" /D "AF_DEBUG" /D "EXPORTING"'
         vsc.←' "*.c" /link /DLL /OPT:REF'
         vsc, ←' /INCREMENTAL:NO /SUBSYSTEM:WINDOWS'
         vsc, ←' /LIBPATH: "%AF_PATH%\lib"'
         vsc,←' /DYNAMICBASE "af',codfns.AF∆LIB,'.lib"'
         vsc,←'
                 /OPT:ICF /ERRORREPORT:PROMPT'
         vsc.←' /TLBID:1 /OUT:"codfns.dll""'
       This code is used in chunk 29a.
       Defines:
         vsbat, used in chunks 21 and 29b.
         wsd, used in chunks 29b and 30b.
       Uses AFALIB 3b, codfns 3a, and VSAPATH 3b.
```

Finally, in order to write up the test harness to work right, we must copy the appropriate runtime files into the tests\ directory so that we can find them when we finally start running our code there.

```
(Copy the runtime files into tests\30b) =

□CMD □+vsc
□CMD □+'copy "', wsd, 'rtm\codfns.h" "', wsd, 'tests\"'
□CMD □+'copy "', wsd, 'rtm\codfns.exp" "', wsd, 'tests\"'
□CMD □+'copy "', wsd, 'rtm\codfns.lib" "', wsd, 'tests\"'
□CMD □+'copy "', wsd, 'rtm\codfns.pdb" "', wsd, 'tests\"'
□CMD □+'copy "', wsd, 'rtm\codfns.dll" "', wsd, 'tests\"'
This code is used in chunk 29a.
Uses codfns 3a and wsd 30a.
```

6.4 Testing Harness

We use the APLUnit testing framework to facilitate our testing of the Co-dfns compiler. The test harness is designed around a testing philosophy in which we ever only write black-box tests that work on the whole compiler using inputs that could be created or are expected to be creatable by end-users. That is, we do no "unit testing" of our source code, but only whole program testing.

The testing framework is provided by the ut.aptn file, which is not part of this literate program and so is not included in this document. In order to make some of the testing more convenient, we define the function TEST to run the tests that exist in the tests\ subdirectory. Each of these tests has a specific number which defines the test, and we refer to the tests by number when running them. Both of these testing functions assume that we are running inside of the tests\ directory or one configured identically to it.

The TEST function takes either 'ALL' as its input or a test number in the form of an integer. Given an integer, we call the test matching that number in the current working directory.

The 'ALL' option causes TEST to run all of the tests that are defined in the current working directory. This command is a nicety, since we can technically do all of this by iterating the TEST function over the range of test numbers, but this would not create the aggregate statistics that we would like to see at the end of the testing report. By using 'ALL' we get to see a complete summary of the results of testing all the code, rather than just the individual testing results on a per testing group/number basis.

```
31a ⟨TEST Function 31a⟩≡

TEST←{

#.UT.(print_passed print_summary)←1

'ALL'≡ω:#.UT.run'./'

path←'./t',(1 Ο*(4ρ10)τω),'_*_tests.dyalog'

#.UT.run >>0□NINFO⊡1⊢path

}

Root chunk (not used in this document).

Defines:

TEST, used in chunks 6 and 24.
```

6.5 XML Rendering

```
31b \langle XML\ Rendering\ 31b\rangle\equiv
Xml\leftarrow\{\alpha\leftarrow0\ \diamond\ ast\leftarrow\alpha\{d\ i\leftarrow P2D\Rightarrow\omega\ \diamond\ i\circ\{\omega[\alpha]\}``(cd),1\downarrow\alpha\downarrow\omega\}\ddot{\star}(0\neq\alpha)\vdash\omega\ \diamond\ d\ t\ k\ n\leftarrow 4\uparrow ast\ cls\leftarrow N\Delta[t],``('-..'[1+\times k]),```\alpha``|k\ \diamond\ fld\leftarrow\{((\not\equiv\omega)\uparrow3\downarrow f\Delta),\neg\omega\}``\downarrow\ \Diamond\uparrow3\downarrow ast\ [XML\ \Diamond\uparrow d\ cls(c'')fld\}
This code is used in chunk 3a.
```

6.6 AST Pretty-printing

```
\langle Pretty-printing AST trees 32a \rangle \equiv
32a
                  dct \leftarrow \{\alpha[(2 \times 2 \neq /n, 0) + (1 \uparrow \stackrel{\sim}{\neq} m) + m + n \leftarrow \phi \lor \psi \uparrow \psi \downarrow \forall \alpha \alpha \omega] \omega \omega\}
                  \mathsf{dlk} \leftarrow \{((x[\rho\omega) \uparrow [x \leftarrow 2 \mid 1 + \omega\omega]\alpha), [\omega\omega]\alpha\alpha@(<0 \ 0) \\ \div (' _{\Gamma}' = >\omega) \vdash \omega\}
                  dwh \leftarrow \{\omega('\top'dlk\ 1)'\ | \ |_{\Gamma} - '(0] \ \rangle) dct, \ \neg \neg / ((\not\equiv `\alpha), ``c[/\not\equiv \circ \lozenge ``\alpha) \uparrow ``\alpha\}
                  pp3 \leftarrow \{\alpha \leftarrow ' \circ ' \diamond d \leftarrow (\imath \neq \omega) \neq \omega \diamond \_ \leftarrow \{z \neg d + \leftarrow \omega \neq z \leftarrow \alpha[\omega]\} \\ \ddot{\ast} \equiv \ddot{\sim} \omega \diamond lbl \leftarrow \alpha \rho \\ \ddot{\sim} \neq \omega
                       lyr+{i+<u>ι</u>α=d ◊ k ν+↓φωω[i],∘-∃i ◊ (ω∘{α[ω]}"ν)αα"@k+ω}ω
                       (\omega = \iota \neq \omega) \neq \neg \alpha \alpha \quad \text{lyr} \neq (1 + \iota \lceil / d), \neg \Diamond \circ \neg \circ \circ \text{"lbl}
                  lb3←{α←ι≢⊃ω
                        \label{eq:continuity} $$ '(',''')', ```~{\alpha,';',\omega}/{\pi}"(N\Delta{\alpha[\omega]})@2+(2>\omega){\alpha[|\omega]}@{0>\omega}@4+>\omega)[\alpha;]} $$
              This code is used in chunk 3a.
              Defines:
                  dct, never used.
                  dlk, never used.
                  dwh, never used.
                  dwv, never used.
                  lb3, never used.
                  pp3, never used.
```

6.7 Reading and Writing Files

It is helpful to be able to easily write files to disk, and the following put and tie utilities help us to do so when we want to. These are pretty standard, but they could maybe be replaced by <code>INPUT</code> or something like that.

```
32b ⟨Basic tie and put utilities 32b⟩≡

tie+{
0::□SIGNAL □EN
22::ω□NCREATE 0
0□NRESIZE ω□NTIE 0
}

put+{
s+(-128+256|128+'UTF-8'□UCS ω)□NAPPEND(t+tie α)83
1:r+s+□NUNTIE t
}

This code is used in chunk 29b.
Defines:
put, used in chunks 21 and 29.
tie, used in chunks 21 and 29b.
```

6.8 Debugging utilities

The following utilities help to improve quality of life when working with the Co-dfns source code.

The DISPLAY function is taken from https://dfns.dyalog.com and helps to make debugging easier by allowing us to thread DISPLAY calls into expressions. I prefer to do something like this:

```
... \{\omega \dashv \Box \leftarrow \#.DISPLAY \omega\} ...
```

The function itself returns the character rendering of the code, so the above little expression is one that I use to insert and do debugging within an expression.

```
(DISPLAY Utility 33)≡
33
          DISPLAY←{□IO □ML←0
                                                                      A Boxed display of array.
             \alpha \leftarrow 1 \diamond \text{chars} \leftarrow \alpha \supset ' . . ' ' ' ' | - ' ' \sqcap \Box | - '
                                                                      A \alpha: 0-clunky, 1-smooth.
             tl tr bl br vt hz←chars
                                                                      A Top left, top right, ...
             box←{
                                                                      A Box with type and axes.
                vrt hrz\leftarrow(^{-}1+\rho\omega)\rho"vt hz
                                                                      A Vert. and horiz. lines.
                top \leftarrow (hz, '\theta \rightarrow ')[-1 \uparrow \alpha], hrz
                                                                      A Upper border with axis.
                bot←(⊃α),hrz
                                                                      A Lower border with type.
                rgt←tr,vt,vrt,br
                                                                      A Right side with corners.
                lax+(vt, '\phi\downarrow')[^-1\downarrow1\downarrow\alpha], "cvrt
                                                                      A Left side(s) with axes,
                lft←\tl,(↑lax),bl
                                                                      A ... and corners.
                lft,(top,ω,bot),rgt
                                                                      A Fully boxed array.
             }
             deco \leftarrow \{\alpha \leftarrow type open \omega \diamond \alpha, axes \omega\}
                                                                      A Type and axes vector.
             axes \leftarrow \{(-2\lceil \rho \rho \omega) \uparrow 1 + \times \rho \omega\}
                                                                      A Array axis types.
             open\leftarrow{(1[ρω)ρω}
                                                                      A Expose null axes.
             trim\leftarrow{(~1 1\underline{\epsilon}^/\omega=' ')/\omega}
                                                                      A Remove extra blank cols.
             type\{\{(1=\rho\omega)\supset'+'\omega\}\cup,char``\omega\}
                                                                      A Simple array type.
             char ← {θ=ρω:hz ◊ (¬ωε'-',□D)¬'#~'}∘ Φ
                                                                      A Simple scalar type.
             line \leftarrow \{(6 \neq 10 \mid \Box DR' '\omega) \Rightarrow '-'\}
                                                                      A underline for atom.
                                                                      A Recursively box arrays:
                0=\equiv\omega: '\frac{1}{2}(open \squareFMT \omega)\frac{1}{2}line \omega
                                                                      A Simple scalar.
                1 \theta \equiv (\equiv \omega)(\rho \omega): '\nabla' 0 0 box \BoxFMT \omega
                                                                      A Object rep: □OR.
                1=≡ω:(deco ω)box open □FMT open ω
                                                                      A Simple array.
                ('ε'deco ω)box trim □FMT ∇"open ω
                                                                      A Nested array.
             }ω
```

Root chunk (not used in this document).

}

Defines:

DISPLAY, used in chunks 24 and 34. Uses [IO 3b and [ML 3b.

I also define a function PP that encapsulates the above usage pattern that I like to use, making the whole thing less verbose and a little more convenient.

34 ⟨PP *Utility* 34⟩≡

 $PP \leftarrow \{\omega \neg \Box \leftarrow \#.DISPLAY \omega\}$

Root chunk (not used in this document). Defines:

PP, used in chunks 22a and 24. Uses DISPLAY 33.

7 Index

7.1 Chunks

(* 3a) (DISPLAY *Utility* 33) ⟨MK∆RTM Command 29b⟩ (PP *Utility* 34) $\langle \mathsf{TANGLE}\ Command\ 25 \rangle$ (TEST Function 31a) (WEAVE Command 27) ⟨AST Record Structure 4c⟩ (Basic tie and put utilities 32b) (Build codfns.dll DLL 30a) (Build the runtime 29a) ⟨C Runtime Header 23b⟩ (C Runtime Support 23a) (Code Generator 16) (Compile the primitives in prim.apln 29c) (Compiler 15) (Converters between parent and depth vectors 5) (Copy the runtime files into tests\ 30b) (Global Settings 3b) (Implementation of APL Primitives 22b) (Interface to the backend C compiler 21) (Linking with Dyalog 22a) (Parser 6) (Pretty-printing AST trees 32a) (Tangle Script 24) $\langle The \ Fix \ API \ 4a \rangle$ (*User-command API* 4b) (Weave Script 26) (XML Rendering 31b)

7.2 Identifiers

AFALIB: 3b, 4b, 21, 30a AFAPREFIX: 3b, 21

codfns: 3a, 16, 21, 24, 26, 29c, 30a, 30b

dct: 32a

 $\mathsf{DISPL}\overline{\mathsf{AY}}$: 24, 33, 34

 $\begin{array}{ll} \operatorname{dlk:} & \underline{32a} \\ \operatorname{dwh:} & \underline{32a} \\ \operatorname{dwv:} & \underline{32a} \\ \operatorname{lb3:} & \underline{32a} \end{array}$

 $\begin{array}{ll} \text{MK} \triangle \text{RTM: } 24, \underline{29b} \\ \text{PP: } 22a, 24, \underline{\underline{34}} \end{array}$

pp3: <u>32a</u>

put: $\overline{21}$, 29b, 29c, $\overline{32b}$ src: 4a, 15, 24, 29b, $\overline{29c}$

TANGLE: $24, \underline{25}$ TEST: $6, 24, \underline{31a}$ tie: $21, 29b, \underline{32b}$ VERSION: $\underline{3b}$ vsbat: $21, \underline{29b}, \underline{30a}$

VSAPATH: 3b, 21, 30a

WEAVE: $24,\overline{27}$ wsd: $29b,\overline{30a},30b$

 $\begin{array}{l} \square \text{Io: } \underline{3b}, 33 \\ \square \text{ML: } \underline{3b}, 33 \\ \square \text{WX: } \underline{3b} \end{array}$

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A separable portion of the object code, whose source code is excluded from the Corresponding Source as a System Library, need not be included in conveying the object code work.

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