The Co-dfns Compiler

Aaron W. Hsu June 8, 2022

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1 Introduction

2 User's Guide

3 Co-dfns Architecture

This section describes the "big picture" parts of the Co-dfns compiler. The intent here is to try to show how all of the various moving parts of the compiler fit together, to provide a sort of road map that will give you a precise plan for understanding how the various components affect one another. One of the most important things to understand in any compiler is the net effect a local change in the code can have on the rest of the system, so I hope that this section will help to clarify this.

The design of the Co-dfns compiler is one of austerity and minimalism. My intent is, was, and hopefully shall remain that of producing an exceptionally clear design that avoids or eliminates unnecessary code and complexity within the design. I attack this problem in many ways, but I primarily attempt to do this by both reducing the size of the code surface in total, that is, write less code, as well as reducing the number of entry points and paths through that code. In other words, my ideal design is one in which you enter the compiler in some limited, but well defined and useful set of entry points, and then proceed in a linear fashion through the code as the execution path, resulting finally in your result. This is the "ultimate" in data flow, functionally oriented programming.

The ramifications of this design choice implies a few important things. Firstly, it implies that I reduce and eliminate any code that represents boilerplate or that does not actively contribute to the "big picture" of the code. This is required in an extreme degree if I am to reduce the overall complexity of the design. This also implies that there is very little intentional redundancy in the shape and style of the source, making it very terse and compact. Since there are intentionally very few entry and exit points through the control flow of the code, this reduces the number of dependencies for me to be aware of when dealing with a single piece of code, but this also comes at the cost of not being able to see many examples of the interfaces with that code. Often, there will be one, and only one place, in which a given piece of code is used, and I do not want the code to needlessly store excess information in its source that doesn't need to be there.

This all culminates in something that can be quite shocking at first: making a change to the source is almost always a big deal. If all the source code is meaningful and carefully constructed, this also means that making changes to this code are almost always non-trivial,

because if the code represented something trivial, I would have tried to remove it from the code so that only the "big things" were in the code itself. Thus, anyone who wishes to view and read the compiler code should take it upon themselves to appreciate the way in which the code flows together, and how the flow of the program runs, as doing so will be essential to understanding how to make changes to the source without breaking something. Fortunately, this does come with the intended benefits of a very short and simple codebase that has clear flow through the system, it just means that if you want to change something, make sure you realize that you are almost always likely to be working at the "architectural" level, rather than at the small and trivial level of details.

The compiler is designed to fit into a single Dyalog APL namespace, and importantly, we do not define additional nested namespaces or other forms of name hiding. I intentionally want to restrict the namespace to a single global one. This single global namespace should therefore contain the carefully curated names that matter, and any that do not matter should, ideally, not be defined or used. The namespace itself can be divided into three main groupings: the public facing entry-points into the system, the compiler logic itself, and the utilities or other elements that serve to support the others. This gives use the following code outline.

```
(*4)=
:Namespace codfns

(Global Settings 6)
(The Fix API 7)
(User-command API 9a)

(Parser 22)
(Compiler 32)
(Code Generator 33)
(Interface to the backend C compiler 38)
(Linking with Dyalog 39a)

(AST Record Structure 9b)
(Converters between parent and depth vectors 9c)
(XML Rendering 18a)
(Pretty-printing AST trees 18b)
```

:EndNamespace

Root chunk (not used in this document). Defines: codfns, used in chunks 10, 13, 16, 17, 33, and 38.

The primary user-facing interfaces into the compiler are (*The Fix API 7*) and the (*User-command API 9a*). These are the ways that you primarily drive the entire compiler. I intentionally expose the rest of the compiler interfaces without hiding them so that people who wish to leverage these other parts of the system without using the "entire" compiler pipeline are able to do so, but I do not consider this a public interface.

This distinction matters because of our testing philosophy and our version numbering. Generally speaking, our version numbering scheme only tracks a major or minor change in the compiler when the externally facing interfaces receive some fundamental changes. Changes to the internal changes are *not* considered for this versioning scheme. Moreover, since I intend for there to be great freedom in changing and altering the behavior of these internal pipeline interfaces, these interfaces are not directly tested, and the test suite should *not* include testing against these internal interfaces. We philosophically only test against the external interfaces, and eschew internal unit tests.¹

The utility functions defined below the core compiler pipeline represent functionality that is tangential to the main compiler operation. However, these utilities also tend to represent some specific insight into the design of the compiler. Understanding the core AST structure and design as well as getting a grip on how to manipulate the core tree manipulation structures are vital to understanding the rest of the code. Therefore, this section spends more time on discussing these topics before the upcoming sections dealing with a more detailed exposition of the compiler itself. However, there are utilities that we consider more advanced, such as the pretty-printing functions and XML rendering that are topics of interest to advanced users of the compiler, but which are not part of the main compiler pipeline. Even though these functions have intentionally general application and are likely to be useful not only to those working on the compiler itself but also to those who are using more advanced compiler features, these utilities are not critical to a deep understanding of the compiler, so these are not discussed in this section. Instead, we discuss those topics in the section on developer tooling and infrastructure concerns.

The remaining parts of this section will describe the external facing interfaces to the compiler as well as the core underlying data structures and idioms that form the underlying skeleton and foundation for writing and working with any aspect of the compiler. These are all feature and component agnostic elements of the system that do not belong solely to only a single part, but that impact all other

¹You can read more of my opinions on this matter in my article, "The Fallacy of Unit Testing".

elements of the compiler source code, and so it pays especially well to pay attention and understand this code to a high degree.

3.1 Global Settings

```
\langle Global\ Settings\ 6 \rangle \equiv
6
        □IO □ML □WX←0 1 3
        VERSION←4 1 0
        AF∆PREFIX←'/opt/arrayfire'
        AF∆LIB←'cuda'
        VS∆PATH←'\Program Files\Microsoft Visual Studio\2022\Community'
      This code is used in chunk 4.
      Defines:
        AFALIB, used in chunks 9a, 17a, and 38.
        AFAPREFIX, used in chunk 38.
        VERSION, never used.
        VSAPATH, used in chunks 17a and 38.
        □IO, used in chunk 19.
        □ML, used in chunk 19.
        □wx, never used.
```

3.2 The Fix API

One of the core entry points into the compiler is through the Fix function. This function is designed to mimic and more or less replace the use of the DFIX function found in Dyalog APL. Its design models that behavior, and it is important as an entry-point because it exercises most of the core elements of the compiler. In particular, the design of the compiler's pipeline is demonstrated most fully in this function.

```
Parse \rightarrow Compile \rightarrow Generate \rightarrow Backend \rightarrow Link
```

The interfaces to the <code>DFIX</code> function and the Co-dfns <code>Fix</code> function differ in a few key ways. The left argument to <code>Fix</code> is a character vector giving the name to use when generating files and other artifacts. This does *not* affect the name of the resulting namespace, since that is defined, if at all, in the file source itself. The α argument only affects the name of the files and other outputs that <code>Fix</code> generates.

We also print out which part of the compiler we are in when we enter that "phase". Doing this helps to give us an intuitive sense of how fast each phase is and whether one phase is taking an abnormally long time or not. It also helps in debugging.

The input requirements for Fix are not listed in the definition itself, because both the parser PS and the Fix function need to use the same basic checks, and since the Fix function calls the parser as its first entry point, it doesn't make much sense to duplicate that work in both places. The requirements are as follows:

- Scalar/Vector
- Character type
- Simple or Vector of Vectors

We generate a DOMAIN ERROR if the inputs are not well-formed.

```
8a (Verify input from IN 8a)≡
err+'PARSER EXPECTS SCALAR OR VECTOR INPUT'
1<#pIN:err □SIGNAL 11

err+'PARSER EXPECTS SIMPLE OR VECTOR OF VECTOR INPUT'
2<|≡IN:err □SIGNAL 11

⟨Normalize the input formatting 8b⟩

err+'PARSER EXPECTS CHARACTER ARRAY'
0≠10|□DR IN:err □SIGNAL 11

This code is used in chunk 22.
```

The input formatting that is accepted means that newlines could be denoted either with LF, CR, or CRLF sequences inside of the vectors themselves or they could be denoted by having separate vectors for the various lines, or even a mixture of both. To simplify this situation we want to normalize them so that we are always dealing with some combination of LF, CR, and CRLF sequences within the file itself, rather than dealing with the nested situation. This ensures that after verification of the input, everything will work off of the same format. We intentionally put a newline at the end of the file even if we may not require one because it is possible that we are dealing with a file that is missing its final newline. By always adding one, we ensure that every line in the input is always terminated by a line ending. Life is also simpler if we just use LF as our line ending instead of something else, this means that future code must be aware that there could be mixed line endings in the file.

```
(Normalize the input formatting 8b) = IN←∈(⊆IN), "☐UCS 10
This code is used in chunk 8a.
```

8b

3.3 The User Command API

```
\langle User\text{-}command API 9a \rangle \equiv
9a
       ⊽Z←Help _
        Z+'Usage: <object> <target> [-af={cpu,opencl,cuda}]'
       ⊽r←List
        r+□NS"1p<0 ♦ r.Name+,"c'Compile' ♦ r.Group+c'CODFNS'
        r[0].Desc+'Compile an object using Co-dfns'
        r.Parse←c'2S -af=cpu opencl cuda

∇ Run(C I); Convert; in; out

       A Parameters
               AFALIB
                               ArrayFire backend to use
        Convert+\{\alpha([SE.SALT.Load'[SALT]/lib/NStoScript -noname').ntgennscode <math>\omega\}
        in out←I.Arguments ♦ AF∆LIB←I.af''⊃~I.af≡0
        S←(c':Namespace ',out),2↓0 0 0 out Convert ##.THIS.±in
        →0/~'Compile' #C
        {##.THIS. ±out, '←ω'}out Fix S¬□EX'##.THIS.',out
     This code is used in chunk 4.
     Uses AFALIB 6 and Fix 7.
```

3.4 AST Record Structure

```
9b (AST Record Structure 9b)≡
f∆←'ptknfsrdx'
N∆←'ABCEFGKLMNOPSVZ'
This code is used in chunk 4.
```

3.5 Converters between parent and depth vectors

```
9c (Converters between parent and depth vectors 9c) =
P2D \leftarrow \{z \leftarrow, \iota \neq \omega \land d \leftarrow \omega \neq, z \land \_ \leftarrow \{p \dashv d + \leftarrow \omega \neq p \leftarrow \alpha[z, \leftarrow \omega]\} \stackrel{\checkmark}{=} \stackrel{\sim}{=} \omega \land d(A(-1+d) \uparrow \stackrel{\circ}{=} 0 1 \vdash \varphi z)\}
D2P \leftarrow \{0 = \neq \omega : \varphi \land p \dashv 2\{p[\omega] \leftarrow \alpha[\alpha\underline{\iota}\omega]\} \neq \vdash \circ c = \omega \dashv p \leftarrow \iota \neq \omega\}
This code is used in chunk 4.
```

4 Developer Infrastructure

4.1 Building the Compiler

4.1.1 Tangling and Weaving the Literate Source

The Co-dfns compiler is written, developed, and distributed as a literate program. For more information about literate programming, see the resources available at http://literateprogramming.com/. We use noweb as our preferred literate programming tool because it is eminently simple, while still handling the majority of our needs and producing high quality output in LATEX format with all the important elements of literate programming, including live hyperlinking and cross-references. We intend codfns.nw to tangle into the following files based on specific chunks that have been provided in this document.

Chunk	File Output
	src\codfns.apln
(C Runtime Support 40a)	rtm\runtime.c
(C Runtime Header 40b)	rtm\codfns.h
(Implementation of APL Primitives 39b)	rtm\prim.apln
(DISPLAY <i>Utility</i> 19)	<pre>src\DISPLAY.aplf</pre>
(ΜΚΔRTM <i>Command</i> 16b)	src\MK∆RTM.aplf
(PP <i>Utility</i> 20a)	src\PP.aplf
(TANGLE Command 12)	src\TANGLE.aplf
(TEST Function 21)	src\TEST.aplf
(WEAVE Command 14)	src\WEAVE.aplf
(Tangle Script 10)	TANGLE.sh
(Weave Script 13)	WEAVE.sh

The following bash script will create these files.

```
(Tangle Script 10)=
#!/bin/bash
echo "Tangling src/codfns.apln..."
notangle codfns.nw > src/codfns.apln

echo "Tangling src/DISPLAY.aplf..."
notangle -R'[[DISPLAY]] Utility' codfns.nw > src/DISPLAY.aplf

echo "Tangling src/MKΔRTM.aplf..."
notangle -R'[[MKΔRTM]] Command' codfns.nw > src/MKΔRTM.aplf

echo "Tangling src/PP.aplf..."
notangle -R'[[PP]] Utility' codfns.nw > src/PP.aplf
```

```
echo "Tangling src/TANGLE.aplf..."
notangle -R'[[TANGLE]] Command' codfns.nw > src/TANGLE.aplf
echo "Tangling src/TEST.aplf..."
notangle -R'[[TEST]] Function' codfns.nw > src/TEST.aplf
echo "Tangling src/WEAVE.aplf..."
notangle -R'[[WEAVE]] Command' codfns.nw > src/WEAVE.aplf
echo "Tangling TANGLE.sh..."
notangle -R'Tangle Script' codfns.nw > TANGLE.sh
echo "Tangling WEAVE.sh..."
notangle -R'Weave Script' codfns.nw > WEAVE.sh
Root chunk (not used in this document).
Uses codfns 4, DISPLAY 19, MKARTM 16b, PP 20a, src 16c, TANGLE 12, TEST 21, and WEAVE 14.
```

On Windows, the best way that we have found to do this is via the Cygwin project. This document assumes that you have already successfully built and installed via Cygwin a working Icon-driven noweb installation.

Users who prefer to work in a UNIX fashion via Cygwin or some other subsystem on Windows can follow the build scripts directly. For developers who prefer to work in a primarily Windows environment, the following build scripts assist in handling the calls into Cygwin so that you do not need to have a Cygwin terminal open all the time.

When tangled to the TANGLE.aplf file, this script will enable the user simply type TANGLE to update the code tree from within a Dyalog APL Session. This is much more convenient than keeping a Cygwin Terminal session open along with a Dyalog APL session while programming. At the moment, this file is only designed to work on Windows with Cygwin, but we should in principle extend this to work on Linux and Mac OS X style machines as well.

Note: this command expects to be run from within the root of the repository, not from, say, within the testing directory.

```
12 (TANGLE Command 12)≡

TANGLE; SH; CWD; CD

SH←'C:\cygwin64\bin\bash.exe -l -c '

CWD←⇒□CMD'C:\cygwin64\bin\bash.exe -c pwd'

CD←'cd ''', CWD, ''''

□CMD SH, '"', CD, '&& ./TANGLE.sh"'

Root chunk (not used in this document).

Defines:

TANGLE, used in chunk 10.
```

Weaving is the process by which we produce the final printed output of this document, intended for reading and general human consumption. We rely on the LATEX typesetting system to do this. Moreover, because we make heavy use of UTF-8 and prefer to have our own fonts installed and used, it is necessary to use the xelatex system instead of the typical LATEX engine. In order to get the indexing right, we must run the engine twice. The first run will update the indexing files that will be picked up on the second run and incorporated into the final document. Note, we have tried to use the lualatex engine, which in theory should work just as well as the xelatex engine, but we get a strange error relating to noweb's style file, so we stick with xelatex for now.

Running this script also depends on having the appropriate fonts installed. In this case, please ensure that the following fonts are installed in your Windows font system so that they can be picked up by the TEX engine.

- Libre Baskerville (Regular, Italic, Bold)
- APL385 Unicode
- Lucida Sans Unicode
- Cambria Math

Uses codfns 4.

If you do not wish to use these fonts, then see the top of the codfns.nw file and edit the font specifications to the fonts that you do wish to use.

Note the use of -delay -index for options. We want to generate indexing, but we also need to make sure that we can use some of our own packages in the system,

Note: this command expects to be run from within the root of the repository, not from, say, within the testing directory.

Like the (TANGLE Command 12), the following command, when tangled to the WEAVE.aplf file permits the Windows programmer to simply execute WEAVE in a the Dyalog APL session and weave the documents together.

4.2 Loading the Compiler

In order to load the compiler into an APL session as well as all the development utilities, we assume that you have first managed to either load up a session with a bootstrapped version of the TANGLE command or that you already have a tangled <code>src\</code> directory. If the <code>src\</code> directory has not yet been created by running the TANGLE command, then this must be done before loading the compiler system. After tangling, the compiler can be loaded using the provided <code>LOAD</code> shortcut. This shortcut is meant to use the Dyalog Link system for hotloading the files in <code>src\</code> into the root namespace. We do so through the following link command:

Link.Create # src -source=dir -watch=dir

This means that we want to link the src\ directory into the # namespace, but we also want to make sure that we only pull changes that come from the filesystem. This is because we are editing the code via the WEB document, and we do not want to risk having some intermediate representation that isn't accurate and that doesn't flow the right way; we want all appropriate changes to begin in the WEB document and then, and only then, flow into the session. This also allows us to make some modifications to the code for testing and experimentation inside of the session without consideration for the code outside of the session, and such changes will be removed or forgotten on the next TANGLE command.

To set this up, we also ensure that we begin our work within the root Co-dfns repository directory, as this is where we expect to run the TANGLE and WEAVE commands.

There is unfortunately only a limited range of possibilities for linking in a new directory as we wish to do. The method we choose to use is launching a fresh Dyalog APL session and then using an LX expression from the command line to do the actual linking using the DSE.UCMD functionality. I personally find this to be rather hackish, and I hope that an alternative approach to doing this will show up in the near future. Nonetheless, the arguments that we pass to dyalog.exe look something like this:

LX="[SE.UCMD'Link.Create # src -source=dir -watch=dir'"

If you do not use the LOAD shortcut, you can use the above command to do the linking manually.

4.3 Building the Runtime

One of our goals with the Co-dfns runtime is to write as much of it as possible in APL. This means that we want to have at minimum a

very small kernel that has been written in C, while most of the rest of the code is implemented in some APL files. This leads to a three part breakdown of the process to build the runtime.

```
16a ⟨Build the runtime 16a⟩≡
⟨Compile the primitives in prim.apln 16c⟩
⟨Build codfns.dll DLL 17a⟩
⟨Copy the runtime files into tests\ 17b⟩
This code is used in chunk 16b.
```

We define the command MKARTM to build the runtime. This command takes a path to the root directory of the Co-dfns repository; this is to allow us to rebuild the runtime from anywhere in the system if we so choose.

```
(MKΔRTM Command 16b)≡
    MKΔRTM path;prim;put;src;tie;vsbat;vsc;wsd

⟨Basic tie and put utilities 20b⟩
    ⟨Build the runtime 16a⟩
Root chunk (not used in this document).
Defines:
    MKΔRTM, used in chunk 10.
Uses put 20b, src 16c, tie 20b, vsbat 17a, and wsd 17a.
```

The first step we must take is producing an appropriate C file that contains the primitives that we have defined in prim.apln. This means that we want to only compile the code in prim.apln as far as producing the C code. Since we do not have a full blown runtime yet, we will be compiling the prim.c file along with the rest of the runtime code, instead of the normal build process, which assumes that we already have a working runtime. This means that we only invoke the GC TT PS passes of the compiler pipeline, while avoiding the CC pass. We use the SALT system to load the source from prim.apln and then run the compiler passes that we want before storing the resulting code in the rtm\prim.c file.

```
16c  ⟨Compile the primitives in prim.apln 16c⟩≡
    src+□SRC □SE.SALT.Load path, '\rtm\prim.apln'
        (path, '\rtm\prim.c')put codfns.{GC TT PS ω}src
    This code is used in chunk 16a.
    Defines:
        src, used in chunks 7, 10, 16b, and 32.
    Uses codfns 4 and put 20b.
```

Once we have the rtm\prim.c file written appropriately, we can run the main compiler process. For simplicity, we just compile all of the .c files that are found in the rtm\ subdirectory. We must ensure that we are appropriatelly invoking our ArrayFire dependencies as well as producing the appropriate debugging symbols most of the time.

```
\langle Build \text{ codfns.dll } DLL \text{ 17a} \rangle \equiv
17a
        vsbat+#.codfns.VSΔPATH,'\VC\Auxiliary\Build\vcvarsall.bat'
        wsd←path,'\'
        vsc←'%comspec% /C ""',vsbat,'" amd64'
        vsc, ←' && cd "', wsd, '\rtm"'
        vsc,←' && cl /MP /W3 /wd4102 /wd4275 /Od /Zc:inline /Zi /FS'
                        /Fo".\\" /Fd"codfns.pdb"'
        vsc,←'
        vsc,←'
                        /WX /MD /EHsc /nologo /I"%AF_PATH%\include"'
                        /D "NOMINMAX" /D "AF_DEBUG" /D "EXPORTING" '
        vsc,←'
                        "*.c" /link /DLL /OPT:REF'
        vsc,←'
                         /INCREMENTAL:NO /SUBSYSTEM:WINDOWS'
                        /LIBPATH: "%AF_PATH%\lib"'
        vsc,←'
                        /DYNAMICBASE "af',codfns.AFΔLIB,'.lib"'
        vsc,←'
                        /OPT:ICF /ERRORREPORT:PROMPT'
        vsc,←'
        vsc,←'
                         /TLBID:1 /OUT: "codfns.dll"" '
      This code is used in chunk 16a.
      Defines:
        vsbat, used in chunks 16b and 38.
        wsd, used in chunks 16b and 17b.
      Uses AFALIB 6, codfns 4, and VSAPATH 6.
```

Finally, in order to write up the test harness to work right, we must copy the appropriate runtime files into the tests\ directory so that we can find them when we finally start running our code there.

4.4 XML Rendering

This code is used in chunk 4.

4.5 AST Pretty-printing

```
⟨Pretty-printing AST trees 18b⟩≡
18b
                {\tt dlk} \leftarrow \{((x[]\rho\omega)\uparrow[x\leftarrow2\,|\,1+\omega\omega]\alpha),[\omega\omega]\alpha\alpha@(<0\ 0) \\ \div (\,'\,_{\Gamma}{}'=>\omega)\vdash\omega\}
               dwh \leftarrow \{\omega('\top'dlk\ 1)'\ | + \Gamma''(0]\emptyset)dct, \Rightarrow \pi/((\not\equiv \alpha), "\subset \lceil/\not\equiv \circ \emptyset "\alpha) \uparrow "\alpha\}
               \mathsf{dwv} \leftarrow \{\omega(' \mid \mathsf{-'dlk} \mid 0)' \mid \neg \neg \neg \mid \mathsf{-'(0)} \vdash ) \mathsf{dct}(\neg \neg \neg 1 \downarrow \vdash) \neg \{\alpha, \mathsf{-'}, \omega\} / (1 + \lceil / \not\equiv ``\alpha) \{\alpha \uparrow \omega, \neg `` \mid \mathsf{-'} \uparrow \neg \not\equiv \Diamond \omega\} \ ``\alpha\}
                |yr \leftarrow \{i \leftarrow \underline{1}\alpha = d \diamond k \ v \leftarrow \downarrow \Diamond \omega \omega[i], \circ \subset \exists i \diamond (\omega \circ \{\alpha[\omega]\} \ v) \alpha \alpha \ \omega \in \omega \} \omega 
                                 (ω=ι≠ω)/>αα lyr/(1+ι[/d), co, o τ lbl}
                lb3+{a+ı≢⊃w
                                 '(',"')',"~{α,';',ω}/*"(ΝΔ{α[ω]}@2⊢(2¬ω){α[|ω]}@{0>ω}@4↑¬ω)[α;]}
            This code is used in chunk 4.
            Defines:
                dct, never used.
               dlk, never used.
               dwh, never used.
               dwv, never used.
               163, never used.
               pp3, never used.
```

4.6 Debugging utilities

The following utilities help to improve quality of life when working with the Co-dfns source code.

The DISPLAY function is taken from https://dfns.dyalog.com and helps to make debugging easier by allowing us to thread DISPLAY calls into expressions. I prefer to do something like this:

```
... \{\omega \neg \Box \leftarrow \#.DISPLAY \omega\} ...
```

{

cursively box arrays:

The function itself returns the character rendering of the code, so the above little expression is one that I use to insert and do debugging within an expression.

```
⟨DISPLAY Utility 19⟩≡
19
          DISPLAY+{□IO □ML+0
                                                                                                                             А Вс
          play of array.
                   α+1 ♦ chars+α>'..'''|-' '□□|-'
                                                                                                A α: O-clunky, 1-smooth
                  tl tr bl br vt hz←chars
                                                                                                                   A Top left
                  box←{
                          vrt hrz←(-1+ρω)ρ"vt hz
                                                                                                                    A Vert. ar
                            top \leftarrow (hz, '\theta \rightarrow ')[-1 \uparrow \alpha], hrz
                                                                                                                            A Up
          per border with axis.
                          bot \leftarrow (\neg \alpha), hrz
          der with type.
                          rgt←tr,vt,vrt,br
                          lax+(vt, '\phi\downarrow')[-1\downarrow1\downarrow\alpha], "cvrt
                                                                                                         A Left side(s) wi
                          lft←\tl,(↑lax),bl
                          lft,(top,\omega,bot),rgt
                      }
                    deco \leftarrow \{\alpha \leftarrow type \text{ open } \omega \diamond \alpha, axes \omega\}
                                                                                                  A Type and axes vector
                   axes \leftarrow \{(-2\lceil \rho \rho \omega) \uparrow 1 + \times \rho \omega\}
                                                                                                                            A Ar
          ray axis types.
                  open\leftarrow{(1[ρω)ρω}
          pose null axes.
                   trim\leftarrow \{(\sim 1 \ 1 \le \wedge \ne \omega = ' ')/\omega\}
                                                                                                                            A Re
          move extra blank cols.
                   type←{{(1=ρω)⊃'+'ω}∪,char"ω}
                                                                                                       A Simple array type
                      char←{θ≡ρω:hz ◊ (⊃ωε'¯',□D)⊃'#~'}∘₹
                                                                                           A Simple scalar type.
                      line\{(6 \neq 10 | \Box DR' '\omega) \Rightarrow '-'\}
                                                                                                                            A ur
          derline for atom.
```

A Simple scalar

A Object rep: □OR

A Simple array.

A Nested array.

```
0=\equiv\omega: '; (open \squareFMT \omega); line \omega
                                  1 \Theta \equiv (\equiv \omega)(\rho \omega): '\nabla' 0 0 box \square FMT \omega
                                       1=\equiv\omega:(\text{deco }\omega)\text{box open }\square\text{FMT open }\omega
                                       ('ϵ'deco ω)box trim □FMT ∇"open ω
                          }ω
          Root chunk (not used in this document).
            DISPLAY, used in chunks 10 and 20a.
          Uses ☐10 6 and ☐ML 6.
              I also define a function PP that encapsulates the above usage pat-
          tern that I like to use, making the whole thing less verbose and a little
          more convenient.
          ⟨PP Utility 20a⟩≡
20a
            PP \leftarrow \{\omega \dashv \Box \leftarrow \#.DISPLAY \omega\}
          Root chunk (not used in this document).
          Defines:
            PP, used in chunks 10 and 39a.
```

4.7 Reading and Writing Files

Uses DISPLAY 19.

It is helpful to be able to easily write files to disk, and the following put and tie utilities help us to do so when we want to. These are pretty standard, but they could maybe be replaced by <code>INPUT</code> or something like that.

```
20b (Basic tie and put utilities 20b)≡

tie←{

0::□SIGNAL □EN

22::ω□NCREATE 0

0□NRESIZE ω□NTIE 0

}

put←{

s←(-128+256|128+'UTF-8'□UCS ω)□NAPPEND(t←tie α)83

1:r←s→□NUNTIE t

}

This code is used in chunk 16b.
Defines:
put, used in chunks 16 and 38.
tie, used in chunks 16b and 38.
```

4.8 Testing Harness

We use the APLUnit testing framework to facilitate our testing of the Co-dfns compiler. The test harness is designed around a testing philosophy in which we ever only write black-box tests that work on the whole compiler using inputs that could be created or are expected to be creatable by end-users. That is, we do no "unit testing" of our source code, but only whole program testing.

The testing framework is provided by the ut.aptn file, which is not part of this literate program and so is not included in this document. In order to make some of the testing more convenient, we define the function TEST to run the tests that exist in the tests\ subdirectory. Each of these tests has a specific number which defines the test, and we refer to the tests by number when running them. Both of these testing functions assume that we are running inside of the tests\ directory or one configured identically to it.

The TEST function takes either 'ALL' as its input or a test number in the form of an integer. Given an integer, we call the test matching that number in the current working directory.

The 'ALL' option causes TEST to run all of the tests that are defined in the current working directory. This command is a nicety, since we can technically do all of this by iterating the TEST function over the range of test numbers, but this would not create the aggregate statistics that we would like to see at the end of the testing report. By using 'ALL' we get to see a complete summary of the results of testing all the code, rather than just the individual testing results on a per testing group/number basis.

```
21 ⟨TEST Function 21⟩≡

TEST+{

#.UT.(print_passed print_summary)+1

'ALL'≡ω:#.UT.run './'

path+'./t',(1 0₹(4ρ10)τω),'_*_tests.dyalog'

#.UT.run >>0□NINFO⊡1⊢path
}

Root chunk (not used in this document).
Defines:

TEST, used in chunks 10 and 22.
```

5 Co-dfns Compiler

5.1 Parser

```
22
        \langle Parser\ 22 \rangle \equiv
            PS \leftarrow \{IN \leftarrow \omega \land A B C E F G K L M N O P S V Z \leftarrow 1 + i 15
                          I \leftarrow \{(\neg \omega) [\alpha] \land U \leftarrow \{0 = [NC'\alpha' : \omega\omega \ddot{*}^{-1} \ \alpha\alpha \ \omega\omega \ \omega \ \land \ \omega\omega \ddot{*}^{-1} \vdash (\omega\omega \ \alpha) \ \alpha\alpha \ \omega\omega \ \omega\}
                          assert\leftarrow \{\alpha \leftarrow \text{'assertion failure'} \diamond 0 \in \omega : \pm \alpha \square SIGNAL 8' \diamond shy \leftarrow 0\}
                         (Verify input from IN 8a)
           A Line and error reporting utilities
                         CR LF←□UCS 13 10
                          linestarts ← (11,2> /IN ∈ CR LF), ≢IN
                         mkdm + \{\alpha + 2 \diamond line + line starts \underline{\iota}\omega \diamond no + '[', (\bar{\iota} + line), ']'
                                      i \leftarrow (\sim IN[i] \in CR \ LF) \neq i \leftarrow beg + ilinestarts[line+1] - beg \leftarrow linestarts[line+1]
                                       ([EM α)(no,IN[i])(' ^'[i∈ω],~' 'ρ~≢no)}
                          quotelines←{
                                       lines←∪linestarts<u>ι</u>ω
                                       nos←(1 0ρ~2×≢lines)\'[',(▼-1+lines),°1⊢'] '
                                       beg+linestarts[lines] ♦ end+linestarts[lines+1]
                                       m←∈∘ω"i←beg+ı"end-beg
                                       -1 + ∈ nos, (~ • CR LF", (IN•I"i), , ' - '•I"m), CR}
                          SIGNAL \leftarrow \{\alpha \leftarrow 2 \mid ' \Rightarrow en msg \leftarrow \alpha \Rightarrow EN \circ \leftarrow en \Rightarrow DM \circ \leftarrow en mkdm \Rightarrow \omega
                                       dmx+('EN' en)('Category' 'Compiler')('Vendor' 'Co-dfns')
                                       dmx, \leftarrow c'Message'(msg, CR, quotelines \omega)
                                       □SIGNAL cdmx}
           A Group input into lines as a nested vector
                         pos←(ι≢IN)⊆~~IN∈CR LF
           A Mask strings
                          0≠≢lin←<u>ι</u>⊃∘φ"msk←≠\"'''=IN∘I"pos:{
                                       EM←'SYNTAX ERROR: UNBALANCED STRING',('S'/~2≤≸lin),CR
                                       EM, \leftarrowquotelines \epsilon (msk\neq"pos)[lin]
                                       EM □SIGNAL 2}0
           A Remove comments
                          pos msk/~~~c^\takemskv-1\phimsk)\alpha'a'=IN\left I"pos
           A Remove leading and trailing whitespace
                         WS←□UCS 9 32 ♦ pos mskf~~←c~(∧\v∧\UΦ)∘(WSe~IN∘I)~pos
           A Flatten and separate lines and ♦ with Z type
                          t \leftarrow 0 \rho c pos \diamond t pos msk(\epsilon, \circ, \tilde{c}) \leftarrow Z(\tilde{c} pos) 0 \diamond t[\underline{\iota}' \diamond' = IN[pos]] \leftarrow Z
```

```
A Tokenize Strings
             end+1+pos \diamond t[i+\underline{\iota}2<\neq0,msk]+C \diamond end[i]+end[\underline{\iota}2>\neqmsk,0]
             t pos end/~←c(t≠0)v~msk
A Verify that all open characters are part of the valid character set
             alp←'ABCDEFGHIJKLMNOPQRSTUVWXYZ_abcdefghijklmnopqrstuvwxyz'
             alp,+'ÀÁÂÃÄÅÆÇÈÉÊËÌÍÎÏÐÑÒÓÔÕÖØÙÚÛÜÝßàáâãäåæçèéêëìíîïðñòóôõöøùúûüþ'
             alp, ←' ΔΔABCDEFGHIJKLMNOPQRSTUVWXYZ'
             num←□D
             synb←'¯[]{}()'':αω◊;'
             syna←'&□□#'
             prmfs+'+-×÷|[[*®0!?~∧∨ñヾ<≤=>≥≠≡≢p,;φΘq↑↓⊂⊆⊃∈<u>∈</u>n∪ι<u>ι</u>[|↓♥±ਙ⊥⊤⊣⊢믱▽←→'
             prmdo←'∘.*⊡0°0@' ♦ prmmo←'~~&エ目' ♦ prmfo←'//\\
             prms+prmfs, prmdo, prmmo, prmfo
             x+' '@{t\neq 0}IN[pos] A The spaces produce nice invariants
             v∱msk←~x∈alp,num,syna,synb,prms,WS:{
                        EM←'SYNTAX ERROR: INVALID CHARACTER(S) IN SOURCE', CR
                        EM, ←quotelines <u>ı</u>msk
                        EM □SIGNAL 2}0
A Tokenize numbers
             _←{dm[ω]+∧+dm[ω]}"(dm∨x∈alp)⊆ı≢dm←x∈num
             dmv \leftarrow ('.'=x) \wedge (-1\phi dm) \vee 1\phi dm
             dm∨+('-'=x)∧1¢dm
             dmv \leftarrow (x \in 'EeJj') \wedge (^{-}1\phi dm) \wedge 1\phi dm
             v∱msk←(dm=0)^x='-':2'ORPHANED -'SIGNAL pos/~msk
             v \neq \{1 < + \neq \omega = 'j'\}"dp\leftarrow \squareC"dm\leq x: 'MULTIPLE J IN NUMBER'\squareSIGNAL 2
             v/{1<+/ω='e'}"dp←⊃-,/{ω⊆~ω≠'j'}"dp:'MULTIPLE E IN NUMBER'∐SIGNAL 2
             v∱'e'=¬"dp:'MISSING MANTISSA'□SIGNAL 2
             v+'e'=>∘φ"dp:'MISSING EXPONENT'□SIGNAL 2
             mn ex \leftarrow \downarrow \Diamond \uparrow \{2 \uparrow (\omega \subseteq \omega \neq e'), e''\} dp
             v \neq \{1 < + \neq ' \cdot ' = \omega\}"mn, ex: 'MULTIPLE . IN NUMBER' \squareSIGNAL 2
             v∱'.'ϵ"ex:'REAL NUMBER IN EXPONENT'□SIGNAL 2
             \vee + \{ \vee + 1 \downarrow \omega \in '^{-} \}"mn, ex: 'MISPLACED - '\[ SIGNAL 2
             t[i \leftarrow 12 < \neq 0, dm] \leftarrow N \Leftrightarrow end[i] \leftarrow end \neq 2 > \neq dm, 0
A Tokenize Variables
             t[i \leftarrow \underline{1}2 < \neq 0, vm \leftarrow (\sim dm) \land x \in alp, num] \leftarrow V \Leftrightarrow end[i] \leftarrow end \neq \sim 2 > \neq vm, 0
A Tokenize \alpha, \omega formals
             fm \leftarrow \{mm \leftarrow \phi \supset (> \circ \supset, \vdash) \neq \phi m \leftarrow \alpha = ' ', \omega \diamond 1 \downarrow "(mm \land \sim m1)(mm \land m1 \leftarrow 1 \phi m)\}
             am aam←'α'fm x ◊ wm wwm←'ω'fm x
             ((am∨wm)/t)+A ♦ ((aam∨wwm)/t)+P ♦ ((aam∨wwm)/end)+end/<sup>2-</sup>1¢aam∨wwm
A Tokenize Primitives, Atoms
```

```
t[\underline{\iota}(\sim dm) \land x \in prms] \leftarrow P \diamond t[\underline{\iota}x \in syna] \leftarrow A
A Compute dfns regions and type, include } as a child
           t[i'{'=x]+F ◊ 0≠>d←-1++1 -1 0['{}'ix]:'UNBALANCED DFNS' SIGNAL 2
A Check for out of context dfns formals
          \vee \neq (d=0) \land (t=P) \land IN[pos] \in \alpha\omega': 'DFN FORMAL REFERENCED OUTSIDE DFNS' SIGNAL
A Compute trad-fns regions
         v/Z≠t/~1¢msk←(d=0)∧'∀'=x:'TRAD-FNS START/END LINES MUST BEGIN WITH ∀'□SIG
NAL 2
           O≠>tm←<sup>-</sup>1φ≠\(d=0)^'∀'=x:'UNBALANCED TRAD-FNS'□SIGNAL 2
        v≁Z≠t≁~⊃1 ¯1v.¢⊂(2>/tm);0:'TRAD-FNS END LINE MUST CONTAIN ⊽ ALONE'□SIGNAL
A Identify Label colons versus others
           t[\underline{\iota}tm\wedge(d=0)\wedge\epsilon((\sim)\wedge(<\uparrow\vee\uparrow))"':'=(t=Z)cIN[pos]]\leftarrow L
A Tokenize Keywords
           ki \leftarrow \underline{\iota}(t=0) \land (d=0) \land (':'=IN[pos]) \land 1 \varphi t = V
           t[ki] \leftarrow K \diamond end[ki] \leftarrow end[ki+1] \diamond t[ki+1] \leftarrow 0
           ERR←'EMPTY COLON IN NON-DFNS CONTEXT, EXPECTED LABEL OR KEYWORD'
           v \neq (t=0) \land (d=0) \land ':'=IN[pos]:ERR \square SIGNAL 2
A Tokenize System Variables
           si \leftarrow \underline{\iota}(' \square' = IN[pos]) \land 1 \varphi t = V
           t[si] \leftarrow S \diamond end[si] \leftarrow end[si+1] \diamond t[si+1] \leftarrow 0
A Delete all characters we no longer need from the tree
           d tm t pos end(f^{\sim}) \leftarrow c(t \neq 0) \lor x \in '()[]{}:;'
A Tokenize Labels
           ERR←'LABEL MUST CONSIST OF A SINGLE NAME'
           v\neq(Z\neq t[li-1])v(V\neq t[li\leftarrow \underline{\iota}1\phi_{msk}\leftarrow t=L]):ERR \square SIGNAL 2
           t[li]+L > end[li]+end[li+1]
           d tm t pos end(/~)←c~msk
A Now that all compound data is tokenized, reify n field before tree-building
           A Verify that keywords are defined and scoped correctly
          KW+'NAMESPACE' 'ENDNAMESPACE' 'END' 'IF' 'ELSEIF' 'ANDIF' 'ORIF' 'ENDIF
         KW, ←'WHILE' 'ENDWHILE' 'UNTIL' 'REPEAT' 'ENDREPEAT' 'LEAVE' 'FOR' 'ENDFOR
           KW, ←'IN' 'INEACH' 'SELECT' 'ENDSELECT' 'CASE' 'CASELIST' 'ELSE' 'WITH
         KW, ← 'ENDWITH' 'HOLD' 'ENDHOLD' 'TRAP' 'ENDTRAP' 'GOTO' 'RETURN' 'CONTINUE
           KW, ←'SECTION' 'ENDSECTION' 'DISPOSABLE' 'ENDDISPOSABLE'
           KW,"~←':'
```

```
msk \leftarrow \sim KW \in \sim kws \leftarrow n \neq \sim km \leftarrow t = K
           v/msk:('UNRECOGNIZED KEYWORD ', kws>~> 1msk) □SIGNAL 2
           msk+kws€':NAMESPACE' ':ENDNAMESPACE'
           v/msk∧km/tm:'NAMESPACE SCRIPTS MUST APPEAR AT THE TOP LEVEL'□SIGNAL 2
           msk+kws∈KW~':NAMESPACE' ':ENDNAMESPACE' ':SECTION' ':ENDSECTION'
        v∱msk←msk∧~km/tm:{msg←2'STRUCTURED STATEMENTS MUST APPEAR WITHIN TRAD-FNS
                     msg SIGNAL \epsilon \{x+iend[\omega]-x+pos[\omega]\}"\underline{i}km+msk\}\theta
A Verify system variables are valid
           SYSV←,"'Á' 'A' 'AI' 'AN' 'AV' 'AVU' 'BASE' 'CT' 'D' 'DCT' 'DIV' 'DM'
           SYSV, +, "'DMX' 'EXCEPTION' 'FAVAIL' 'FNAMES' 'FNUMS' 'FR' 'IO' 'LC' 'L>
           SYSV,←,"'ML' 'NNAMES' 'NNUMS' 'NSI' 'NULL' 'PATH' 'PP' 'PW' 'RL' 'RSI
        SYSV, +, "'RTL' 'SD' 'SE' 'SI' 'SM' 'STACK' 'TC' 'THIS' 'TID' 'TNAME' 'TNUMS
           SYSV, +, "'TPOOL' 'TRACE' 'TRAP' 'TS' 'USING' 'WA' 'WSID' 'WX' 'XSI'
       SYSF+."'ARBIN' 'ARBOUT' 'AT' 'C' 'CLASS' 'CLEAR' 'CMD' 'CONV' 'CR' 'CS' 'CSN
           SYSF,←,"'CY' 'DF' 'DL' 'DQ' 'DR' 'DT' 'ED' 'EM' 'EN' 'EX' 'EXPORT'
SYSF,←,"'FAPPEND' 'FCHK' 'FCOPY' 'FCREATE' 'FDROP' 'FERASE' 'FFT' 'IFFT
        SYSF, ←, "'FHIST' 'FHOLD' 'FIX' 'FLIB' 'FMT' 'FPROPS' 'FRDAC' 'FRDCI' 'FREAC
           SYSF,←,"'FRENAME' 'FREPLACE' 'FRESIZE' 'FSIZE' 'FSTAC' 'FSTIE' 'FTIE'
                   "'FUNTIE' 'FX' 'INSTANCES' 'JSON' 'KL' 'LOAD' 'LOCK' 'MAP' 'MKDIR
        SYSF, +, "'MONITOR' 'NA' 'NAPPEND' 'NC' 'NCOPY' 'NCREATE' 'NDELETE' 'NERASE
           SYSF, +, "'NEW' 'NEXISTS' 'NGET' 'NINFO' 'NL' 'NLOCK' 'NMOVE' 'NPARTS'
                    "'NPUT' 'NQ' 'NR' 'NREAD' 'NRENAME' 'NREPLACE' 'NRESIZE' 'NS'
                    "'NSIZE' 'NTIE' 'NUNTIE' 'NXLATE' 'OFF' 'OR' 'PFKEY' 'PROFILE'
                   "'REFS' 'SAVE' 'SH' 'SHADOW' 'SIGNAL' 'SIZE' 'SR' 'SRC' 'STATE
        SYSF, +, "'STOP' 'SVC' 'SVO' 'SVQ' 'SVR' 'SVS' 'TCNUMS' 'TGET' 'TKILL' 'TPUT
           SYSF, \leftarrow, "'TREQ' 'TSYNC' 'UCS' 'VR' 'VFI' 'WC' 'WG' 'WN' 'WS' 'XML' 'XT SYSD\leftarrow, "'OPT' 'R' 'S'
           v/msk+(t=S)^~n∈'□', "SYSV, SYSF, SYSD:{
                     ERR+2'INVALID SYSTEM VARIABLE, FUNCTION, OR OPERATOR'
                     ERR SIGNAL \epsilonpos [\omega] \{\alpha + \iota \omega - \alpha\} "end [\omega]
           }<u>ւ</u>msk
A Compute parent vector from d
           p←D2P d
A Compute nameclass of dfns
           k+2\times t\in F \diamond k[\neg p/\sim (t=P)\land n\in \neg \alpha'] \leftarrow 3 \diamond k[\neg p/\sim (t=P)\land n\in \neg \omega'] \leftarrow 4
A We will often wrap a set of nodes as children under a Z node
           gz \leftarrow \{z \leftarrow \omega \uparrow \sim -0 \neq \neq \omega \diamond ks \leftarrow -1 \downarrow \omega
                     t[z]+Z \diamond p[ks]+\neg z \diamond pos[z]+pos[\neg \omega] \diamond end[z]+end[\neg \phi z, ks] \diamond z
A Nest top-level root lines as Z nodes
           _←(gz 1φ⊢)"(t[i]=Z)<i←<u>ı</u>d=0
           'Non-Z top-level node'assert t[<u>r</u>p=r≢p]=Z:
```

```
A Nest all dfns expression bodies as Z nodes
                                      _+p[i]{end[α]+end[>φω] < gz"ω<~1, -1+t[ω]=Z}目i+<u>ι</u>t[p]=F
                                     'Non-Z dfns body node'assert t[\underline{\imath}t[p]=F]=Z:
A Drop/eliminate any Z nodes that are empty or blank
                                      _←p[i]{msk[α,ω]←~∧/IN[pos[ω]]∈WS}目i←<u>ι</u>(t[p]=Z)∧p≠ι≢p⊣msk←t≠Z
                                     tm n t k pos end(/\sim) \leftarrow cmsk \diamond p\leftarrow(\underline{\iota} ~msk)(\vdash -1+\underline{\iota})msk/p
A Parse Keyword structures
                                    nss←n∈c':NAMESPACE' ♦ nse←n∈c':ENDNAMESPACE'
                                     ERR+':NAMESPACE KEYWORD MAY ONLY APPEAR AT BEGINNING OF A LINE'
                                     Zv.≠t/~1¢nss:ERR □SIGNAL 2
                                     ERR←'NAMESPACE DECLARATION MAY HAVE ONLY A NAME OR BE EMPTY'
                                     \sqrt{(Z \neq t \neq -1 \phi_{nss})} \sqrt{(V \neq t \neq -1 \phi_{nss})} \sqrt{Z \neq t \neq -2 \phi_{nss}} \cdot ERR \square SIGNAL 2
                                      ERR+': ENDNAMESPACE KEYWORD MUST APPEAR ALONE ON A LINE'
                                     v/Z≠t/~⊃1 ~1v.¢cnse:ERR □SIGNAL 2
                                     t[nsi+11qnss]+M ♦ t[nei+11qnse]+-M
                                     n[i] \leftarrow n[1+i \leftarrow \underline{\iota}(t=M) \land V=1 \Leftrightarrow end[nsi] \leftarrow end[nei]
                                     x \leftarrow \underline{i} p = i \neq p \diamond d \leftarrow + \uparrow (t[x] = M) + -t[x] = -M
                                     O≠⊃¢d:':NAMESPACE KEYWORD MISSING :ENDNAMESPACE PAIR'□SIGNAL 2
                                    p[x] \leftarrow x[D2P - 1\phi d]
A Delete unnecessary namespace nodes from the tree, leave only M's
                                    msk \leftarrow nssv((^{-1}\phi nss) \land t = V) \lor nsev1\phi nse
                                     t k n pos endf \sim -cmsk \diamond p \leftarrow (\underline{\iota} \sim msk) (\vdash -1 + \underline{\iota}) msk \neq p
A PARSE LABELS ...
A Map guard statements to (G (Z \dots) (Z \dots))
                                    _←p[i]{
                                                                      0=+\neq m \leftarrow ':'=IN[pos[\omega]]:\theta
                                                                      >m: 'EMPTY GUARD TEST EXPRESSION'□SIGNAL 2
                                                                      1<+/m: 'TOO MANY GUARDS'□SIGNAL 2
                                                                      t[\alpha] \leftarrow G \diamond p[ti \leftarrow gz \Rightarrow tx cq \leftarrow 2\uparrow(c\theta), \forall \omega \subset 1, \neg 1 \downarrow m] \leftarrow \alpha \diamond k[ti] \leftarrow 1
                                                                      ci \leftarrow \neq p \land p, \leftarrow \alpha \land t \land pos \ end, \leftarrow 0 \land n, \leftarrow c'' \land k[gz \ cq, ci] \leftarrow 1
                                     0}目i←<u>ı</u>t[p[p]]=F
A Parse brackets and parentheses into <sup>-</sup>1 and <sup>Z</sup> nodes
                                    _←p[i]{
                                                           x \leftarrow IN[pos[\omega]] \diamond bd \leftarrow + bm \leftarrow (bo \leftarrow '['=x) + -bc \leftarrow ']' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow + bm \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow '('=x) + bc \leftarrow ')' = x \diamond pd \leftarrow (po \leftarrow
pc←')'=x
                                                                                                             0 \neq \neg \phi bd: 2 \cup BRACKETS \cup SIGNAL pos[\omega] \{x + \iota (\lceil \neq \omega)\}
x \leftarrow [+\alpha]\ddot{o}\{\omega \neq \sim 0 \neq bd\} \text{ end } [\omega]
                                                                                                  O≠>φpd:2'UNBALANCED PARENTHESES'SIGNAL pos[ω]{x+ι([+ω)
x \leftarrow [+\alpha] \ddot{\circ} \{\omega \neq \sim 0 \neq pd\} end[\omega]
```

```
(po/bd) v.≠φpc/bd: 'OVERLAPPING BRACKETS AND PARENTHESES' □SIGNAL
                                                                                 p[\omega] \leftarrow (\alpha, \omega)[1 + 1@\{\omega = \iota \neq \omega\}D2P + \uparrow 1 \phi bm + pm] \diamond t[bo \neq \omega] \leftarrow 1 \diamond t[po \neq
                                                                                  end[po/\omega] \( end[\po/\omega] \( end[\po/\omega] \( end[\po/\omega] \( end[\po/\omega]
                                           0\}\exists i \leftarrow \underline{\iota}(t[p]=Z) \land p \neq \iota \neq p
                                           t k n pos end/\leftarrowcmsk\leftarrowIN[pos]\epsilon')' \diamond p\leftarrow(\underline{\iota}cmsk)(\vdash-1+\underline{\iota})msk\neqp
A Convert semi-colon indexing into Z nodes in the <sup>-1</sup> nodes
                                  _+p[i]{k[z+>, +gz"g+ωc~-1φIN[pos[ω]]ε';]']+1 ◊ t[z]+Z P[1=≢"g]}∃i+ιt[p]=-
A Mark bindable nodes
                                           bm←(t=V)∨(t=A)∧n∈,"'□□'
                                           bm \leftarrow \{bm \neg p[i] \{bm[\alpha] \leftarrow (V \neg 1 \equiv t[\omega]) \lor \land \not \neg bm[\omega] \} \exists i \leftarrow_{\underline{\iota}} (\sim bm[p]) \land t[p] = Z\} \stackrel{\checkmark}{\times} \equiv bm
A Binding nodes
                                           _<del>-</del>p[i]{
                                                                                  t[\omega/\sim(n[\omega]\epsilon c, '+') \land 0, ^-1 \downarrow bm[\omega]] \leftarrow B
                                                                                  b v \leftarrow \{(\neg x)(1 + x \leftarrow \omega \neq \{t[\neg \omega] = B\} \omega)\}^{-1} \oplus \omega \subset \{1, \neg 1 + t[\omega] \in P \mid B\}
                                                                                  v/~bm[∈v]: 'CANNOT BIND ASSIGNMENT VALUE' ☐SIGNAL 2
                                                                                  p[\omega] \leftarrow (\alpha, b)[0, -1 \downarrow + \uparrow t[\omega] = B]
                                                                                  n[b]+n[\epsilon v] \diamond t[\epsilon v]+7 \diamond pos[b]+pos[\epsilon v] \diamond end[b]+end[\Rightarrow \phi\omega]
                                           0}目i←<u>i</u>(t[p]=Z)^p≠i≢p
                                            A Mark unambiguous primitive kinds
                             k[\iota(t=S)\land ne' \square', "SYSV] + 1 \diamond k[\iota(t=S)\land ne' \square', "SYSF] + 2 \diamond k[\iota(t=S)\land ne' \square', "SYSD] 
                                            t[it=S]←P
                                            k[\underline{\iota}t\in A \ C \ N] \leftarrow 1 \ \diamond \ k[\underline{\iota}n\in , "prmfs] \leftarrow 2 \ \diamond \ k[\underline{\iota}n\in , "prmmo] \leftarrow 3 \ \diamond \ k[\underline{\iota}n\in , "prmdo] \leftarrow 4
                                           k[\underline{\iota}n\epsilon,"prmfo] \leftarrow 5
                                            k[i+<u>ı</u>msk+(n∈c,'∘')∧1¢n∈c,'.']+3 ◊ end[i]+end[i+1] ◊ n[i]+c,'∘.'
                                           t k n pos end\neq \leftarrow -1 \phi_{msk} \Leftrightarrow p + (\underline{\iota} - msk) (\vdash -1 + \underline{\iota}) msk \neq p
A Anchor variables to earliest binding in matching frame
                                            rf \leftarrow 10 \{ \sim t[\omega] \in F \ G \ M \} p[rz \leftarrow 10 \{ \sim (t[\omega] = Z) \land (t[p[\omega]] \in F \ G \ M) \lor p[\omega] = \omega \} \stackrel{*}{\times} = \stackrel{\sim}{\sim} p]
                                            rf[i]+p[i+\underline{\iota}t=G] \diamond rz[i]+i \diamond rf+rf I@\{rzep[i]+\circ\neg\exists i+\underline{\iota}t[p]=G\}rf
                                           mk \leftarrow \{\alpha[\omega], \neg n[\omega]\}
                                           fr+rf mk+fb+fb[\iota \sim rf mk+fb+fb I\circ (\iota \sim)U\thetarz mk+fb+\underline{\iota}t=B] \diamond fb,+^-1
                                           vb←fb[frirf mk i]@(i←<u>i</u>t=V)⊢<sup>-</sup>1ρ~≢p
                                           vb[i/~(rz[i]<rz[b])∨(rz[i]=rz[b])∧i≥b←vb[i←i/~vb[i]≠-1]]←-1
                                           _{\leftarrow}\{z/^{2}-1=vb[1][z]+fb[fri\n] = I@1+z+rf = I@0+\omega]\} = \n{rf[\omega], = \n} = \n(t=V)\(\dagger vb=-1)
                                           v \neq msk \leftarrow (t=V) \wedge vb = -1 : \{
                                                           6'ALL VARIABLES MUST REFERENCE A BINDING'SIGNALεpos[ω]{α+ιω-α}¨end[α
                                           }<u>ւ</u>msk
A \alpha/\omega \rightarrow V; M \rightarrow FO; \alpha\alpha/\omega\omega \rightarrow P2
                                           t \leftarrow V@(i \leftarrow \underline{\iota}(t=A) \land n \in , "'\alpha\omega') \vdash F@\{t=M\}t \diamond vb[i] \leftarrow i \diamond k[\underline{\iota}(t=P) \land n \in '\alpha\alpha' '\omega\omega'] \leftarrow 2
```

```
A Infer types of bindings, groups, and variables
                 z \times + \varphi p[i] \{\alpha \omega\} \exists i + \underline{\iota}(t[p] \in B \ Z) \land p \neq \iota \neq p
                 x \leftarrow \{\omega \neq \sim \land t [\omega] = 1\} \cup \phi \sim x
                O∨.=≢"x:'BRACKET SYNTAX REQUIRES FUNCTION OR ARRAY TO ITS LEFT'□SIGNAL
                                k[msk/z] \leftarrow k[x/\overline{m}sk \leftarrow (k[\neg x] \neq 0) \land 1 = \neq x] \Leftrightarrow z \times /\overline{m} \leftarrow c \sim msk
                                k[z/\overline{m}sk+k[\neg x]=4]+3 \diamond z x/\overline{+}+c\sim msk
                     k[z/\overline{w}sk+\{(2 \ 3 \ 5 \in k[\neg \omega])\vee +=(\omega, \neq k)[0: \lambda k[\omega]=1][k,0\}\circ \varphi x]+2 \diamond z x/\overline{w}+c
                                k[z \neq msk \leftarrow k[\neg \circ \phi x] = 1] \leftarrow 1 \diamond z x \neq c \leftarrow msk
                                k[i]←k[vb[i←<u>l</u>t=V]]
                 ≢z}*(=∨0=⊣)≢z
                 'FAILED TO INFER ALL BINDING TYPES'assert 0=≢z:
A Strand arrays into atoms
                 i \leftarrow |i \rightarrow km \leftarrow 0 < i \leftarrow i[A|(i, \sim \leftarrow - \cup p[i]), p[i \leftarrow \underline{\iota}t[p] \in B Z]]
                 msk \leftarrow (t[i] \in C \ N) \lor msk \land \supseteq 1 \ \lnot 1 \lor . \varphi \lor msk \leftarrow km \land (t[i] \in A \ C \ N \ V \ Z) \land k[i] = 1
                 np+(\not\equiv p)+i\not\equiv ai+i\not\vdash am+2>\not+msk,0 \diamond p+(np@aii\not\equiv p)[p] \diamond p,+ai \diamond km+2<\not+0,msk
                 t k n pos end(\neg,I)\leftarrow cai \diamond k[ai]\leftarrow 1 \delta[v \neq msk \le t[i] \ne N]
                 t n pos(\neg @ai \sim ) \leftarrow A(c'')(pos[km \neq i]) \diamond p[msk \neq i] \leftarrow ai[(msk \leftarrow msk \land \sim am) \neq -1 + + \km]
                 i \leftarrow \underline{\iota}(t[p] = A) \wedge (k[p] = 6) \wedge t = N
                 p, \leftarrow i \diamond t k n pos end(\neg, I) \leftarrow c i \diamond t k n(\neg @ i \sim) \leftarrow A 1(c'')
A PARSE B←D...
A PARSE B←...D
A Rationalize F[X]
                 _←p[i]{
                                \neg m \leftarrow t[\omega] = 1: SYNTAX ERROR: NOTHING TO INDEX' SIGNAL 2
                                k[\omega/\sim m^{-1}\phi(k[\omega] \in 2 \ 3 \ 5) \vee (1 + \omega) = 4 + 4
                 0}\exists i \leftarrow \underline{\iota}(t[p] \in B \ Z) \land (p \neq \iota \neq p) \land k[p] \in 1 \ 2
                 i \leftarrow \underline{\iota}(t=1) \land k=4 \diamond j \leftarrow \underline{\iota}(t[p]=1) \land k[p]=4
                 (≠i)≠≠j:{
                       2'AXIS REQUIRES SINGLE AXIS EXPRESSION'SIGNAL εpos[ω]+ι¨end[ω]-pos[ω
                 }¬¬+{<α+~1<≠ω}目p[j]
                 v/msk←t[j]≠Z:{
                            2'AXIS REQUIRES NON-EMPTY AXIS EXPRESSION'SIGNAL epos[\omega]+iend[\omega]
pos[ω]
                 }msk/p[j]
                 p[j]+p[i] \diamond t[i]+P \diamond end[i]+1+pos[i]
A Group function and value expressions
                 i \hspace{0.1cm} km \leftarrow_{5} \neq_{p}[i] \{(\alpha, \omega)(0, 1 \vee \omega)\} \exists i \leftarrow_{\underline{\iota}} (t[p] \in_{B} Z) \wedge (p \neq_{\bar{\iota}} \neq_{p}) \wedge_{k}[p] \in_{A} Z \}
A Mask and verify dyadic operator right operands
                 (dm \leftarrow 1\phi(k[i]=4) \land t[i] \in F P V Z) \lor . \land (\sim km) \lor k[i] \in O 3 4:{
                                 'MISSING RIGHT OPERAND'∏SIGNAL 2
```

} 0 A Refine schizophrenic types $k[i/(k[i]=5)\wedge dm^{-1}\phi(\sim km)\vee(\sim dm)\wedge k[i]\in 1 \ 6]+2 \ \phi \ k[i/(k[i]=5)+3$ A Rationalize ∘. jm←(t[i]=P)^n[i]€⊂,'o.' jmv.∧1φ(~km)vk[i]∈3 4: 'MISSING OPERAND TO ∘.'□SIGNAL 2 $p \leftarrow ((ji \leftarrow jm \neq i) @ (jj \leftarrow i \neq i \neq i = 1 \\ \phi) [p] \diamond t[ji,jj] \leftarrow t[jj,ji] \diamond k[ji,jj] \leftarrow k[jj,ji]$ $n[ji,jj] + n[jj,ji] \diamond pos[ji,jj] + pos[ji,ji] \diamond end[ji,jj] + end[jj,jj]$ A Mask and verify monadic and dyadic operator left operands $v \neq msk \leftarrow (dm \wedge 2 \varphi \sim km) \vee (1 \varphi \sim km) \wedge mm \leftarrow (k[i]=3) \wedge t[i] \in F P V Z:{$ 2'MISSING LEFT OPERAND'SIGNAL $\epsilon pos[\omega] + \iota$ "end[ω]- $pos[\omega]$ }i ≠~msk msk←dm∨mm A Parse function expressions $np \leftarrow (\not\equiv p) + ixc \leftarrow \not\equiv oi \leftarrow msk \neq i \diamond p \leftarrow (np@oii\not\equiv p)[p] \diamond p, \leftarrow oi \diamond t k n pos end(¬,I) \leftarrow cos position for the position fo$ $p[g/i] \leftarrow oi[(g \leftarrow (\sim msk) \land (1 \phi msk) \lor 2 \phi dm) / xc - \phi + \gamma \phi msk]$ $p[g \neq oi] \leftarrow (g \leftarrow msk \neq (1 \phi mm) \vee 2 \phi dm) \neq 1 \phi oi \Leftrightarrow t[oi] \leftarrow O \Leftrightarrow n[oi] \leftarrow c''$ $pos[oi] \leftarrow pos[g \neq i][msk \neq -1++ g \leftarrow (\sim msk) \land (1 \phi mm) \lor 2 \phi dm]$ $ol+1+(k[i/\sim(2\phi mm) \times 3\phi dm]=4) \times k[i/\sim(1\phi mm) \times 2\phi dm] \in 2$ 3 $or \leftarrow (msk \neq dm) + 1 + k[dm \neq i] = 2$ k[oi]←3 3⊥tor ol A Wrap all assignment values as I nodes i km← $, \neq p[i]$ {(α, ω)(0,1 $\vee \omega$)} $\exists i \leftarrow \underline{\iota}(t[p] \in B Z) \land (p \neq \iota \neq p) \land k[p] \in 1$ j+i/~msk+(t[i]=P)∧n[i]∈c,'+' ♦ nz+(≠p)+zzc++/msk $zm\leftarrow 1\phi msk \diamond p[km \neq i] \leftarrow (zpm \neq (i \times \sim km) + zm + nz)[km \neq -1 + + + zpm \leftarrow zm \vee \sim km]$ A This is the definition of a function value at this point $isfn \leftarrow \{(t[\omega] \in O \ F) \lor (t[\omega] \in B \ P \ V \ Z) \land k[\omega] = 2\}$ A Parse modified assignment to E4(V, F, Z) $j \leftarrow i \neq m \leftarrow m \leq k \land (-1 \phi i \leq n i) \land -2 \phi(t[i] = V) \land k[i] = 1 \diamond p[zi \leftarrow nz \neq m \leq k \neq m] \leftarrow j$ $p[i/^{2}(1\phi m) \vee 2\phi m] + 2/j \diamond t k(\neg @j^{2}) + E + \phi pos end n(\alpha[\omega]@j + \alpha) + vi zi, cvi + i/^{2}2\phi$ A Parse bracket modified assignment to E4(E6, O2(F, P3(\leftarrow)), Z) $j \leftarrow i \neq m \leftarrow m \leq k \wedge (-1 \phi i \leq n i) \wedge (-2 \phi t[i] = -1) \wedge -3 \phi (t[i] = V) \wedge k[i] = 1$ $p[zi \leftarrow nz \neq msk \neq m] \leftarrow ei \leftarrow i \neq msk \neq m] \leftarrow t k end(\neg @ei = msk \neq m] \leftarrow E + (end[zi])$ p t k n(¬@(i/~2φm)~)←ei E 6(c'') $p, \leftarrow j \diamond t, \leftarrow Pp \stackrel{\sim}{=} j \diamond k, \leftarrow 3p \stackrel{\sim}{=} j \diamond n, \leftarrow (\neq j) p \subset , ' \leftarrow ' \diamond pos, \leftarrow pos[j] \diamond end, \leftarrow end[j]$

p t k n pos($\neg @j \sim) \leftarrow ei O 2(c'')(pos[fi \leftarrow i \neq \sim 1 \phi m]) \diamond p[fi] \leftarrow j$

```
A Parse bracket assignment to E4(E6, P2(\leftarrow), Z)
                                 j \leftarrow i \neq m \leftarrow m \leq k \wedge (-1 \varphi t[i] = -1) \wedge -2 \varphi (t[i] = V) \wedge k[i] = 1 \Leftrightarrow p[zi \leftarrow nz \neq m \leq k \neq m] \leftarrow ei \leftarrow i \neq m \leq k \neq m
                                t k end(\neg @ei = ) \leftarrow E + (end[zi]) \diamond p t k n(<math>\neg @(i \neq = 1 \phi m) = ) \leftarrow ei E 6(c'')
                                p t k(¬@j~)←ei P 2
A Parse modified strand assignment
A Parse strand assignment
A SELECTIVE MODIFIED ASSIGNMENT
A SELECTIVE ASSIGNMENT
A Enclose V[X;...] for expression parsing
                                i \leftarrow i [Ap[i \leftarrow \underline{\iota}(t[p] \in B \ Z) \land (k[p] = 1) \land p \neq \iota \neq p]] \diamond j \leftarrow i \neq \widetilde{\iota} \neq \widetilde{\iota} = 1
                                t[j] \leftarrow A \diamond k[j] \leftarrow 1 \diamond p[i \neq 1 \phi_{jm}] \leftarrow j
A TRAINS
A Parse expression sequences
                                i km←¬\neqp[i]{(\alpha¬\omega)(0,(2≤\neq\omega)\wedge1\vee\omega)}\existsi←\underline{\iota}(t[p]\inB Z)\wedge(k[p]=1)\wedgep\neqι\neqp
                                msk+m2\sqrt{fm}^{-1}\phi m2+km\sqrt{1}\phi km\sqrt{fm}+(t[i]=0)\sqrt{(t[i]}\neq A)\sqrt{k[i]}=2
                                t,←Ep~xc←+/msk ♦ k,←msk/msk+m2 ♦ n,←xcp⊂''
                                pos, ←pos[msk/i] ◇ end, ←end[p[msk/i]]
                                p, \leftarrow msk \neq (i \times km) + km \times x \leftarrow (i \neq p) + km \times k \Leftrightarrow p[km \neq i] \leftarrow km \neq x
A Rationalize V[X;...]
                                i \leftarrow i [Ap[i \leftarrow 1(t[p]=A) \land k[p]=-1]] \diamond msk \leftarrow 2 \neq f^{-1}, ip \leftarrow p[i] \diamond ip \leftarrow uip \diamond nc \leftarrow 2 \times \neq ip
                                t[ip] \leftarrow E \diamond k[ip] \leftarrow 2 \diamond n[ip] \leftarrow c'' \diamond p[msk \neq i] \leftarrow msk \neq (\not\equiv p) + 1 + 2 \times (ip) 
                                p, +2/ip ◊ t, +ncρP E ◊ k, +ncρ2 6 ◊ n, +ncρ,"'[' '
                                pos, +2/pos[ip] \diamond end, +\epsilon(1+pos[ip]), -end[ip] \diamond pos[ip] +pos[i/~msk]
A Sanity check
                                 ERR←'INVARIANT ERROR: Z node with multiple children'
                                ERR assert(+/(t[p]=Z) \land p \neq i \neq p)=+/t=Z:
A Count parentheses in source information
                                ip+p[i+\underline{\iota}(t[p]=Z)\wedge n[p] \in c, '('] \diamond pos[i]+pos[ip] \diamond end[i]+end[ip]
A VERIFY Z/B NODE TYPES MATCH ACTUAL TYPE
A Eliminate Z nodes from the tree
                                 zi \leftarrow p I@\{t[p[\omega]]=Z\} \stackrel{*}{=} ki \leftarrow \underline{\iota} msk \leftarrow (t[p]=Z) \land t \neq Z
                                p+(zi@kiı≢p)[p] ♦ t k n pos end(⊣@zi~)+t k n pos end I~<ki
                                 t k n pos endf \sim \text{cmsk} \sim \text{msk} \vee t = Z \diamond p \leftarrow (\underline{\iota} \sim \text{msk}) (\vdash -1 + \underline{\iota}) \text{msk} \neq p
A Compute Exports
                                msk \leftarrow (t=B) \land k[I@\{t[\omega] \neq F\} \stackrel{\text{``}}{=} \stackrel{\text{``}}{=} p] = 0
```

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```
 xn \leftarrow (0 \rho c''), msk \neq n \  \, xt \leftarrow msk \neq k \\ d \  \, i \leftarrow P2D \  \, p \  \, d \  \, n \  \, t \  \, k \  \, pos \  \, end \  \, I \circ \vdash \leftarrow ci \  \, \diamond \  \, sym \leftarrow \cup ('')(,'\omega')(,'\alpha')'\alpha\alpha' \  \, '\omega\omega', n \\ (d \  \, t \  \, k(-symin)pos \  \, end)(xn \  \, xt)sym \  \, IN \}  This code is used in chunk 4. Uses TEST 21.
```

5.2 Compiler Transformations

```
\langle Compiler 32 \rangle \equiv
32
                TT \leftarrow \{((d \ t \ k \ n \ ss \ se) exp \ sym \ src) \leftarrow \omega \diamond \ I \leftarrow \{(\subset \omega) [\alpha] \}
                                A B C E F G K L M N O P S V Z+1+115
              A Compute parent vector and reference scope
                                r \leftarrow I@\{t[\omega] \neq F\} \stackrel{\text{``}}{=} \stackrel{\text{``}}{=} p \rightarrow 2\{p[\omega] \leftarrow \alpha[\alpha\underline{\iota}\omega]\} \neq - \circ c = d \rightarrow p \leftarrow \iota \neq d
              A Lift Functions to top-level
                                p, \leftarrow n[i] \leftarrow (\neq p) + i \neq i \leftarrow \underline{i}(t = F) \land p \neq i \neq p \land t \land n \land r(\neg, I) \leftarrow ci \land p \land I \sim \leftarrow cn[i]@i \vdash i \neq p
                                t[i]←C
              A Wrap expressions as binding or return statements
                                i \leftarrow (\underline{\iota}(\neg t \in F G) \land t[p] = F), \{\omega \neq 2 \mid \iota \neq \omega\} \underline{\iota} t[p] = G \diamond p t k n r \neq \neg \leftarrow 2@i \vdash 1p \neq p
                                p r i I \sim (+ + m) - 1 \diamond n + j \quad I@(0 \leq +) n \diamond p[i] + j + i - 1
                                k[j] \leftarrow (k[r[j]] = 0) \lor 0@({\neg \phi \omega} \exists p[j]) \vdash (t[j] = B) \lor (t[j] = E) \land k[j] = 4 \diamond t[j] \leftarrow E
              A Lift guard tests
                                p[i]+p[x+^{-1}+i+\{\omega/\tilde{\sim}-2|i\neq\omega\}\underline{i}t[p]=G] \diamond t[i,x]+t[x,i] \diamond k[i,x]+k[x,i]
                                n[x] \leftarrow n[i] \diamond p \leftarrow ((x,i)@(i,x) \vdash i \neq p)[p]
              A Count strand and indexing children
                                n[\underline{\iota}(t \in A \ E) \land k = 6] \leftarrow 0 \diamond n[p \neq (t[p] \in A \ E) \land k[p] = 6] + \leftarrow 1
              A Lift and flatten expressions
                                p[i] + p[x + p I@{-t[p[\omega]] \in F G} \stackrel{\times}{=} i + \underline{\iota}t \in G A B C E O P V] \diamond j + (\phi i)[A\phi x]
                                p t k n r{\alpha[\omega]@i+\alpha}\leftarrowcj \diamond p\leftarrow(i@j+\iota\neqp)[p]
              A Compute slots for each frame
                                 s+<sup>-</sup>1,~ει"n[∪x]++∘≢[x+0[|\qe+∪I∘¼~rn+r[b],,n[b+<u>ι</u>t=B]
              A Compute frame depths
                                 d\leftarrow (\neq p) \uparrow d \diamond d[i\leftarrow t=F] \leftarrow 0 \diamond \leftarrow \{z\dashv d[i] + \leftarrow \omega \neq z \leftarrow r[\omega]\} = i \diamond f\leftarrow d[0] \neq e], -1
              A Record exported top-level bindings
                                xi \leftarrow \underline{\iota}(t=B) \wedge k[r]=0
                                ptknfsrdxisym}
          This code is used in chunk 4.
          Uses src 16c.
```

5.3 Code Generator

```
\langle Code\ Generator\ 33 \rangle \equiv
33
         GC←{
                    p t k n fr sl rf fd xi sym←ω ◆ A B C E F G K L M N O P S V Z←1+:15
                    I \leftarrow \{(\subset \omega) [\alpha] \Leftrightarrow com \leftarrow \{\supset \{\alpha, ', ', \omega\} / \omega\}
                    ks \leftarrow \{\omega \subset [0] \sim (\neg \omega) = \omega [; 0]\} \diamond nam \leftarrow \{'\Delta' \square R' \_ ' \circ \sigma \sim sym[|\omega]\}
                syms +,"'+'
                                                                       1 <u>+</u> 1
                                                                                                       '⊛'
                                                  'mul' 'div' 'exp' 'log' 'res'
                                          'sub'
                                                                                             'cir'
                 nams ←
                                'add'
                                                                                                      'min'
                                                                                                               'max
                                                                       '≥'
                                          '≤'
                                                       ' = '
                                                                                                      '≠'
                 syms, ←,
                                                                           'neq' 'not'
                                'lth'
                                           'lte'
                                                   'eql' 'gte' 'gth'
                                                                                             'and'
                                                                                                       'lor'
                                                                                                                'nan
                nams,←
                                                              'ι'
                                                                            'ρ'
                 syms,←,
                                                   'iot' 'rho' 'cat
                                                                           'ctf' 'rot'
                                'sqd'
                                           'brk'
                                                                                                       'rtf'
                 nams,←
                                                                                                                'mem
                                               '≢'
                                                            ' <del>-</del> '
                                                                           '⊣'
                                                                                                       ' _ '
                 syms,←,
                                                   'rgt' 'lft'
                                                                          'dec' 'red'
                                 eqv'
                                                                                             'rdf'
                                                                                                       'scn'
                                                                                                                'scf
                 nams,←
                                               '↓'
                                                                                                          ' ;; '
                 syms,←,
                                                           'com' 'dot'
                                                                           'rnk' 'pow'
                                                                                             'jot'
                                                                                                               'int
                                'tke
                                                                                                       'unq'
                                                   'map'
                 nams,←
                                                            '°.' '<u>ε</u>'
                                                                                  ٠٠'
                                                                                                '⊞'
                                                                                                               '[FF]
                 syms,←,
                                            gdd' 'oup' 'fnd' 'par'
                                                                           'mdv' 'fft'
                                                                                             'ift'
                                                                                                       'scl'
                                                                                                               'nst
                 nams,←
                                 gdu'
                syms,←,¨'∇'
                                                                            'ω'
                                                                                                        'ωω'
                                                                                               'aa'
                                    'this' 'span' 'l'
                                                                            'r'
                                                                                                          'ww'
                  nams,←
                    gck← (A 1)(A 6)
                    gcv← 'Aa' 'As'
                    gck, +(B 1)(B 2)(B 3)(B 4)
                    gcv, +'Bv' 'Bf' 'Bo' 'Bo'
                    gck, +(C 1)(C 2)
                    gcv, ←'Ca' 'Cf'
                    gck, \leftarrow (E^{-2})(E^{-1})(E^{-0})(E^{-1})(E^{-0})(E^{-0})(E^{-0})
                                        'Ek' 'Er' 'Em' 'Ed' 'Eb' 'Ei'
                    gcv,←'Ec'
                    gck, ←(F 0)(F 2)(F 3)(F 4)
                    gcv, ←'Fz' 'Fn' 'Fm' 'Fd'
                    gck, ←(G 0)(N 1)
                    gcv,←'Gd' 'Na'
                    qck, \leftarrow (0\ 1)(0\ 2)(0\ 4)\ (0\ 5)\ (0\ 7)\ (0\ 8)
                    gcv, ←'0v' '0f' '0vv' '0fv' '0vf' '0ff'
                    gck, \leftarrow (P \ 0)(P \ 1)(P \ 2)(P \ 3)(P \ 4)
                    gcv,←'Pv' 'Pv' 'Pf' 'Po' 'Po'
                    gck, \leftarrow (V \ 0)(V \ 1)(V \ 2)(V \ 3)(V \ 4)
                    gcv,←'Va' 'Va' 'Vf' 'Vo' 'Vo'
                    gcv,←c'{''/* Unhandled '',(⊽α),'' */'',NL}'
                    NL← UCS 13 10
                    pref ←c'#include "codfns.h"'
                    pref,←c''
```

```
pref, ←c'EXPORT int'
          pref, ←c'DyalogGetInterpreterFunctions(void *p)'
          pref,←c'{'
          pref,←c'
                         return set_dwafns(p);'
          pref,←c'}'
          pref,←c''
          Bf+{id+sym>~|4>α
                     z +cid,' = retain_cell(stkhd[-1]);'
          z }
          Cf←{id←す4⊃a
                     z +c'mk_closure((struct closure **)stkhd++, fn',id,', 0);'
          z }
          Ek+{
                     z +c'release_cell(*--stkhd);'
                     z,←c''
          z }
          Em←{
                     z ←c'c = *--stkhd;'
                     z, ←c'w = *--stkhd;'
                     z, <-c'(c->fn)((struct array **)stkhd++, NULL, w, c->fv);'
                     z,←c'release_cell(c);'
                     z,←c'release_cell(w);'
          z }
          Er←{
                     z ←c'*z = *--stkhd;'
                     z,←c'goto cleanup;'
                     z, ←c'Ĩ
          z }
          Fn \leftarrow \{id \leftarrow \overline{a} = 5 \Rightarrow \alpha \land x \leftarrow \delta \Rightarrow \neg \neq \omega \land t \leftarrow 2 [x \land k \leftarrow 3 ]x\}
                     hsw \leftarrow (t=0) \lor (t=E) \land k \in 1 \ 2 \ \diamond \ hsa \leftarrow ((t=E) \land k=2) \lor (t=0) \land k \in 4 \ 5 \ 7 \ 8
                     z ←c'int'
                         z,←c'fn',id,'(struct array **z, struct array *l, struct ar
ray *r, void *fv[])'
                     z,←c'{'
                     z,←c'
                                    void
                                               *stk[128];'
                     z,←c'
                                              **stkhd;'
                                    void
                    z,←hsw/c' void
                                            *w; '
                    z,←hsa/c' void
                                            *a;'
                     z,←hsw/c' struct closure *c;'
                     z,←c''
```

34

```
z,←c'
                                   stkhd = &stk[0];'
                    z,←c''
                    z,← ' ',"⊃,/dis"ω
                    z,←c'
                                   *z = NULL; '
                    z,←c''
                    z,←c'cleanup:'
                    z,←c'
                                 return 0;'
                    z, +c'}'
                    z,←c''
          z }
          Fz \leftarrow \{id \leftarrow 5 \Rightarrow \alpha \land awc \leftarrow \sqrt{(3[x)} \{(\omega \in A \ O) \lor (\omega = E) \land \alpha > 0\} 2[x \leftarrow \varphi \Rightarrow \sqrt{\omega}\}\}
                    z ←c'int init',id,' = 0;'
                    z,←c''
                    z,←c'EXPORT int'
                    z,←c'init(void)'
                    z,←c'{'
                    z,←c' return fn',id,'(NULL, NULL, NULL, NULL);'
                    z,←c''
                    z,←c'int'
                        z, +c'fn', id, '(struct array **z, struct array *l, struct ar
ray *r, void *fv[])'
                    z, ←c'{'
                    z,←c'
                                             *stk[128];'
                                   void
                    z, ←c'
                                            **stkhd;'
                                   void
                    z,← awc/c'
                                           void
                                                    *a, *w;'
                    z,← awc/c'
                                           struct closure *c;'
                    z,←c''
                    z,←c'
                                   if (init',id,')'
                    z,←c'
                                             return 0;'
                    z,←c''
                    z,←c'
                                   stkhd = &stk[0];'
                    z,←c'
                                   init',id,' = 1;'
                    z,←c'
                                   cdf_init();'
                    z,←c''
                    z,← ' ',"⊃, /dis"ω
                    z,←c'
                                  return 0;'
                    z, <c'}'
                    z,←c''
          z }
          Pf \leftarrow \{id \leftarrow (symsisym[|4 > \alpha]) > nams
                    z +c'*stkhd++ = retain_cell(',id,');'
          z }
```

```
Va←{id←(|4>α)>'' 'r' 'l' 'aa' 'ww',5↓sym
                  z +c'*stkhd++ = retain_cell(',id,');'
         z }
         Zp←{n←'fn', ⊽ω
                  k[\omega] \in 0 2:{
                            z ←c'int'
                              z, ← ⊂ n, '(struct array **z, struct array *l, struct ar
ray *r, void *fv[]);'
                            z,←c''
                   'UNKNOWN FUNCTION TYPE'□SIGNAL 16
         }
         Zx \leftarrow \{n \leftarrow sym \Rightarrow \neg [n[\omega] \land rid \leftarrow \pi rf[\omega]\}
                  k[ω]=0:c''
                  k[\omega] = 1 : {
                            z ←c'struct array *',n,';'
                  z}ω
                  k[\omega] = 2:{
                            z ←c'struct closure *',n,';'
                            z,←c''
                            z,←c'EXPORT int'
                        z, -cn, '_dwa(struct localp *zp, struct localp *lp, struct lo
calp *rp)'
                            z, ←c'{'
                            z,←c'
                                          struct array *z, *l, *r; '
                            z,←c'
                                          int err;'
                            z,←c''
                            z,←c'
                                          l = NULL;'
                            z,←c'
                                          r = NULL; '
                            z,←c''
                            z, ←c'
                                          fn',rid,'(NULL, NULL, NULL, NULL);'
                            z,←c''
                            z,←c'
                                          err = 0;'
                            z,←c''
                            z,←c'
                                          if (lp)'
                            z,←c'
                                                   err = dwa2array(&l, lp->pocket);'
                            z,←c''
                            z,←c'
                                          if (err)'
                            z,←c'
                                                   dwa_error(err);;'
                            z,←c''
                            z,←c'
                                          if (rp)'
                            z,←c'
                                                   dwa2array(&r, rp->pocket);'
                            z,←c''
                            z,←c'
                                          if (err) {'
```

```
z,←c'
                                                       release_array(l);'
                          z,←c'
                                                      dwa_error(err);'
                                           }'
                          z,←c'
                          z,←c''
                          z,←c'
                                           err = (',n,'->fn)(&z, l, r, ',n,'->fv);'
                          z,←c''
                          z,←c'
                                           release_array(l);'
                          z,←c'
                                           release_array(r);'
                          z,←c''
                          z,←c'
                                           if (err)'
                          z,←c'
                                                      dwa_error(err);'
                          z,←c''
                          z, ←c'
                                           err = array2dwa(NULL, z, zp);'
                          z, ←c'
                                           release_array(z);'
                          z,←c''
                          z,←c'
                                           if (err)'
                          z,←c'
                                                      dwa_error(err);'
                          z,←c''
                          z,←c'
                                           return 0;'
                          z, ←c'}'
                          z,←c''
              z } ω
              ±'''UNKNOWN EXPORT TYPE''□SIGNAL 16'
   }
   d i \leftarrow P2D p \diamond ast \leftarrow (\Diamond \uparrow d p t k n(\iota \not\equiv p) fr sl fd)[i;]
   NOTFOUND+{('[GC] UNSUPPORTED NODE TYPE ',N\Delta[\neg\omega],\tau \neg \phi\omega)||SIGNAL 16}
 dis \leftarrow \{0=2 \Rightarrow h \leftarrow, 1 \uparrow \omega: ' ' \diamond (\not = gck) = i \leftarrow gck \downarrow ch[2\ 3]: NOTFOUND\ h[2\ 3] \diamond h(\not = i \Rightarrow gcv) ks\ 1 \downarrow \omega \} 
   z+ε, •NL"pref, >, /(, /Zp"<u>ι</u>t=F),(, /Zx"xi),(cc''),dis"ks ast
```

This code is used in chunk 4. Uses codfns 4.

5.4 Backend C Compiler Interface

```
(Interface to the backend C compiler 38)\equiv
38
        CC←{
                  vsbat←VS∆PATH,'\VC\Auxiliary\Build\vcvarsall.bat'
                  tie\leftarrow{0:: \squareSIGNAL \squareEN \diamond 22::\omega \squareNCREATE 0 \diamond 0 \squareNRESIZE \omega \squareNTIE 0}
                 put+{s+(<sup>-</sup>128+256|128+'UTF-8'□UCS α)□NAPPEND(t+tie ω)83 ♦ 1:r+s-□NUNTIE t
                  opsys←{ω⊃~'Win' 'Lin' 'Mac'ι⊂3↑⊃'.'□WG'APLVersion'}
                  soext+{opsys'.dll' '.so' '.dylib'}
              cco+'-std=c99 -Ofast -g -Wall -fPIC -shared -Wno-parentheses '
                  cco, ←'-Wno-misleading-indentation '
                  ucc \leftarrow \{\omega\omega(\Box SH \alpha\alpha, ' ', cco, cci, ccf)\omega\}
                  gcc←'gcc'ucc'so'
                  clang+'clang'ucc'dylib'
                  vsco+{z+'/W3 /wd4102 /wd4275 /O2 /Zc:inline /Zi /FS /Fd"',ω,'.pdb" '
                            z,←'/WX /MD /EHsc /nologo '
                            z,'/I"%AF PATH%\include" /D "NOMINMAX" /D "AF DEBUG" '}
                  vslo+{z+'/link /DLL /OPT:REF /INCREMENTAL:NO /SUBSYSTEM:WINDOWS '
                       z,←'/LIBPATH:"%AF_PATH%\lib" /OPT:ICF /ERRORREPORT:PROMPT /TLBID:1
                   z,'/DYNAMICBASE~"af',~AF\Delta LIB,~'.lib"~"codfns.lib"~'\} \\ vsc0 \leftarrow \{ \sim [NEXISTS~vsbat:'VISUAL~C?'] \\ SIGNAL~99~~'""',vsbat,'"~amd64'' \} 
                  vsc1+{' && cd "',(¬□CMD'echo %CD%'),'" && cl ',(vsco ω),' "',ω,'.c" '}
                  vsc2←{(vslo ω), '/OUT:"',ω,'.dll" > "',ω,'.log""'}
                  vsc \leftarrow \{ \Box CMD \ ('\%comspec\% \ /C \ ',vsc0,vsc1,vsc2) \omega \}
                   .÷(±opsys'vsc' 'gcc' 'clang')α⊣ω put α,'.c'⊣1 □NDELETE f∻α,soextθ
                 \square \leftarrow_{\tau} \Rightarrow \square NGET(\alpha, '.log')1
                 □NEXISTS f:f ♦ 'COMPILE ERROR' □SIGNAL 22}
      This code is used in chunk 4.
```

Uses AFALIB 6, AFAPREFIX 6, codfns 4, put 20b, tie 20b, vsbat 17a, and VSAPATH 6.

5.5 Linking with Dyalog

```
\langle Linking \ with \ Dyalog \ 39a \rangle \equiv
39a
               NS←{
                            MKA \leftarrow \{mka \subset \omega\} \diamond EXA \leftarrow \{exa \theta \omega\}
                             Display←{α←'Co-dfns' ♦ W←w_new⊂α ♦ 777::w_del W
                                          w_del W¬W αα{w_close α: ±'□SIGNAL 777' ♦ α αα ω}*ωω⊢ω}
                             LoadImage \leftarrow \{\alpha \leftarrow 1 \diamond \sim \square \text{NEXISTS } \omega : \square \text{SIGNAL } 22 \diamond \text{loadimg } \theta \omega \alpha \}
                             SaveImage \leftarrow \{\alpha \leftarrow ' \text{ image.png'} \diamond \text{ saveimg } \omega \alpha \}
                             Image←{~2 3∨.=≢ρω:□SIGNAL 4 ♦ (3≠⊃ρω)∧3=≢ρω:□SIGNAL 5 ♦ ω⊣w_img ω α}
                             Plot+{2≠≢ρω: □SIGNAL 4 ◊ ~2 3∨.=1>ρω: □SIGNAL 5 ◊ ω¬ν_plot (◊ω) α}
                             Histogram←{ω¬ν_hist ω,α}
                             Rtm∆Init←{
                                          _←'w_new'
                                                                 □NA'P ',ω,'|w_new
                                                                                                                  <C[]'
                                           _←'w_close'□NA'I ',ω,'|w_close P'
                                                                                                                                             Р'
                                            ←'w_del'
                                                                 □NA
                                                                                                       ω, '|w_del
                                           _←'w_img'
                                                                                                                                             <PP F
                                                                 □NA
                                                                                                       ω, '|w_img
                                           _←'w_plot' □NA
                                                                                                       ω, '|w_plot
                                                                                                                                <PP P'
                                           _←'w_hist' □NA
                                                                                                       \omega, '|w hist
                                                                                                                               <PP F8
                                                                                                                                              F8 F
                                           _←'loadimg'□NA
                                                                                                       ω, '|loadimg >PP <C[] I'
                                           _←'saveimg'□NA
                                                                                                       ω, '|saveimg <PP <C[]'
                                           _←'exa'
                                                                               Пиа
                                                                                                                     ω, '|exarray >PP P'
                                                                               □NA'P ',ω,'|mkarray <PP'
                                            ←'mka'
                                         _←'FREA'
                                                                           □NA
                                                                                                               ω, '|frea
                                           ←'Sync'
                                                                               ΠNA
                                                                                                                     ω, '|cd_sync'
                                          0 0 ρ θ}
                             \begin{array}{l} \mathsf{mkna} + \{\alpha, ' \mid ', ('\Delta' \square R' \_ ' \vdash \omega), ' \_ \mathsf{cdf} \ P \ P \ P' \} \\ \mathsf{mkf} + \{\mathsf{fn} + \alpha, ' \mid ', ('\Delta' \square R' \_ ' \vdash \omega), ' \_ \mathsf{dwa} \ ' \diamond \ \mathsf{mon} \ \mathsf{dya} + \omega \circ, "' \_ \mathsf{mon}' \ ' \_ \mathsf{dya}' \\ \mathsf{z} + ('\mathsf{Z} + \{\mathsf{A}\}', \omega, ' \ \mathsf{W}') (' : \mathsf{If} \ \mathsf{O} = \square \mathsf{NC}' \ ' \underline{\Delta}.', \mathsf{mon}, ' ' ' ') \\ \end{array} 
                                 z, \leftarrow (mon dya\{'''', \alpha, ''' \underline{\Delta}.\squareNA''', fn, \omega, ' \precPP'''\}"'>PP P' '>PP \precPP'), \subset ': E
                                 z,':If O=□NC''A'''('Z←<u>∆</u>.',mon,' O O W')':Else'('Z←<u>∆</u>.',dya,' O A W')':
                            ns+#.\squareNS\Theta ♦ _+'\Delta\Delta'ns.\squareNS^{\sim}\Theta ♦ \Delta \Delta+ns.(\Delta \Delta) ♦ \Delta.names+(0\rhoc''),(2=1\supset\alpha)\neq0=
                        fns÷'Rtm∆Init' 'MKA' 'EXA' 'Display' 'LoadImage' 'SaveImage' 'Image' 'Plot
                             fns, + 'Histogram' 'soext' 'opsys' 'mkna'
                            _←Δ.□FX∘□CR"fns ◊ Δ.(decls←ω∘mkna"names) ◊ _←ns.□FX"(c''),ω∘mkf"Δ.name
                        _←Δ.□FX'Z←Init'('Z←RtmΔInit ''',ω,'''')'→0/~0=≠names' 'names ##.Δ.□NA¨dec
                            ns}
          This code is used in chunk 4.
```

6 Co-dfns Runtime

Uses PP 20a.

39b $\langle Implementation \ of \ APL \ Primitives \ 39b \rangle \equiv$ A TBW

Root chunk (not used in this document).

40a (C Runtime Support 40a) =
/* TBW */
Root chunk (not used in this document).
40b (C Runtime Header 40b) =
/* TBW */
Root chunk (not used in this document).

7 Index

7.1 Chunks

(*4) (DISPLAY *Utility* 19) (MK \(ARTM \) Command 16b) (PP *Utility* 20a) (TANGLE Command 12) ⟨TEST Function 21⟩ (WEAVE Command 14) ⟨AST Record Structure 9b⟩ (Basic tie and put utilities 20b) $\langle Build$ codfns.dll DLL 17a \rangle (Build the runtime 16a) (C Runtime Header 40b) (C Runtime Support 40a) (Code Generator 33) (Compile the primitives in prim.apln 16c) ⟨Compiler 32⟩ (Converters between parent and depth vectors 9c) (Copy the runtime files into tests\ 17b) (Global Settings 6) (Implementation of APL Primitives 39b) (Interface to the backend C compiler 38) (Linking with Dyalog 39a) (Normalize the input formatting 8b) (Parser 22) (Pretty-printing AST trees 18b) ⟨Tangle Script 10⟩ $\langle The \ Fix \ API \ 7 \rangle$ (User-command API 9a) (Verify input from IN 8a) (Weave Script 13) (XML Rendering 18a)

7.2 Identifiers

 \square ML: $\overline{\underline{6}}$, 19 \square WX: $\overline{\underline{6}}$

AFΔLIB: 6, 9a, 17a, 38 AFAPREFIX: $\underline{6}$, 38codfns: 4, 10, 13, 16c, 17a, 17b, 33, 38 dct: 18b DISPLAY: 10, 19, 20a dlk: <u>18b</u> dwh: $\overline{18b}$ dwv: $\overline{18b}$ Fix: <u>7,9</u>a lb3: <u>18b</u> MKΔRTM: 10, 16b PP: $10, 20a, \overline{39a}$ pp3: <u>18b</u> put: 16b, 16c, 20b, 38 src: 7, 10, 16b, 16c, 32 TANGLE: 10, 12 TEST: $10, 21, \overline{2}2$ tie: $16b, \overline{20}b, 38$ VERSION: $\overline{6}$ vsbat: 16b, <u>17a</u>, 38 VSΔPATH: <u>6</u>, <u>17a</u>, 38 WEAVE: 10, 14 wsd: $16b, 1\overline{7a}, 17b$ □IO: 6, 19

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