# The Co-dfns Compiler

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### 1 Introduction

### 2 User's Guide

## 3 Co-dfns Architecture

This section describes the "big picture" parts of the Co-dfns compiler. The intent here is to try to show how all of the various moving parts of the compiler fit together, to provide a sort of road map that will give you a precise plan for understanding how the various components affect one another. One of the most important things to understand in any compiler is the net effect a local change in the code can have on the rest of the system, so I hope that this section will help to clarify this.

The design of the Co-dfns compiler is one of austerity and minimalism. My intent is, was, and hopefully shall remain that of producing an exceptionally clear design that avoids or eliminates unnecessary code and complexity within the design. I attack this problem in many ways, but I primarily attempt to do this by both reducing the size of the code surface in total, that is, write less code, as well as reducing the number of entry points and paths through that code. In other words, my ideal design is one in which you enter the compiler in some limited, but well defined and useful set of entry points, and then proceed in a linear fashion through the code as the execution path, resulting finally in your result. This is the "ultimate" in data flow, functionally oriented programming.

The ramifications of this design choice implies a few important things. Firstly, it implies that I reduce and eliminate any code that represents boilerplate or that does not actively contribute to the "big picture" of the code. This is required in an extreme degree if I am to reduce the overall complexity of the design. This also implies that there is very little intentional redundancy in the shape and style of the source, making it very terse and compact. Since there are intentionally very few entry and exit points through the control flow of the code, this reduces the number of dependencies for me to be aware of when dealing with a single piece of code, but this also comes at the cost of not being able to see many examples of the interfaces with that code. Often, there will be one, and only one place, in which a given piece of code is used, and I do not want the code to needlessly store excess information in its source that doesn't need to be there.

This all culminates in something that can be quite shocking at first: making a change to the source is almost always a big deal. If all the source code is meaningful and carefully constructed, this also means that making changes to this code are almost always non-trivial,

because if the code represented something trivial, I would have tried to remove it from the code so that only the "big things" were in the code itself. Thus, anyone who wishes to view and read the compiler code should take it upon themselves to appreciate the way in which the code flows together, and how the flow of the program runs, as doing so will be essential to understanding how to make changes to the source without breaking something. Fortunately, this does come with the intended benefits of a very short and simple codebase that has clear flow through the system, it just means that if you want to change something, make sure you realize that you are almost always likely to be working at the "architectural" level, rather than at the small and trivial level of details.

The compiler is designed to fit into a single Dyalog APL namespace, and importantly, we do not define additional nested namespaces or other forms of name hiding. I intentionally want to restrict the namespace to a single global one. This single global namespace should therefore contain the carefully curated names that matter, and any that do not matter should, ideally, not be defined or used. The namespace itself can be divided into three main groupings: the public facing entry-points into the system, the compiler logic itself, and the utilities or other elements that serve to support the others. This gives use the following code outline.

```
(*5)=
:Namespace codfns

(Global Settings 8a)
(The Fix API 11)
(User-command API 13a)

(Parser 15)
(Compiler 30)
(Code Generator 31)
(Interface to the backend C compiler 36)
(Linking with Dyalog 37a)

(Must Have APL Utilities 38c)
(AST Record Structure 13b)
(Converters between parent and depth vectors 13c)
(XML Rendering 42b)
(Pretty-printing AST trees 39)
```

#### :EndNamespace

5

Root chunk (not used in this document). Defines: codfns, used in chunks 6, 14b, 31, 36, 41b, and 43–49.

This (\* 5) chunk is meant to be stored to a file. We have a build system for doing this that depends on the contents of the (*Tangle Commands* 6) chunk. Thus, we follow the convention here of updating the contents of the (*Tangle Commands* 6) chunk each time that we initially define a new chunk that is intended to be output to a file during the tangling process. See more about the build infrastructure later in this document.

6 ⟨Tangle Commands 6⟩≡
echo "Tangling codfns.apln..."
notangle codfns.nw > src/codfns.apln
This definition is continued in chunks 14b, 41b, 44, 46, and 47c.
This code is used in chunk 43.
Defines:
codfns.apln, never used.
Uses codfns 5 and src 48.

The primary user-facing interfaces into the compiler are (*The Fix API* 11) and the (*User-command API* 13a). These are the ways that you primarily drive the entire compiler. I intentionally expose the rest of the compiler interfaces without hiding them so that people who wish to leverage these other parts of the system without using the "entire" compiler pipeline are able to do so, but I do not consider this a public interface.

This distinction matters because of our testing philosophy and our version numbering. Generally speaking, our version numbering scheme only tracks a major or minor change in the compiler when the externally facing interfaces receive some fundamental changes. Changes to the internal changes are *not* considered for this versioning scheme. Moreover, since I intend for there to be great freedom in changing and altering the behavior of these internal pipeline interfaces, these interfaces are not directly tested, and the test suite should *not* include testing against these internal interfaces. We philosophically only test against the external interfaces, and eschew internal unit tests.<sup>1</sup>

The utility functions defined below the core compiler pipeline represent functionality that is tangential to the main compiler operation. However, these utilities also tend to represent some specific insight into the design of the compiler. Understanding the core AST structure and design as well as getting a grip on how to manipulate the core tree manipulation structures are vital to understanding the rest of the code. Therefore, this section spends more time on discussing these topics before the upcoming sections dealing with a more detailed exposition of the compiler itself. However, there are utilities that we consider more advanced, such as the pretty-printing functions and XML rendering that are topics of interest to advanced users of the compiler, but which are not part of the main compiler pipeline. Even though these functions have intentionally general application and are likely to be useful not only to those working on the compiler itself but also to those who are using more advanced compiler features, these utilities are not critical to a deep understanding of the compiler, so these are not discussed in this section. Instead, we discuss those topics in the section on developer tooling and infrastructure concerns.

The remaining parts of this section will describe the external facing interfaces to the compiler as well as the core underlying data structures and idioms that form the underlying skeleton and foundation for writing and working with any aspect of the compiler. These are all feature and component agnostic elements of the system that do not belong solely to only a single part, but that impact all other

<sup>&</sup>lt;sup>1</sup>You can read more of my opinions on this matter in my article, "The Fallacy of Unit Testing".

elements of the compiler source code, and so it pays especially well to pay attention and understand this code to a high degree.

### 3.1 Global Settings

There are some global options that we assume to exist throughout the compiler. These set the standard behaviors as well as serve as knobs that can be tweaked in some cases to identify what behaviors we want from the rest of the compiler.

First, we have a set of read-only global constants that are defined to configure our APL environment. These are the typical ones, and we try to stick to the defaults, except that we are sane, and thus we use  $\Pi$ IO set to 0.

```
8a ⟨Global Settings 8a⟩≡

□IO □ML □WX+O 1 3

This definition is continued in chunks 8-10.
This code is used in chunk 5.

Defines:
□IO, used in chunk 40.
□ML, used in chunk 40.
□WX, never used.
```

Additionally, we set a VERSION constant to track changes to the system through the distributions. We use semantic versioning<sup>2</sup> as our versioning scheme. That being said, we also do not have particular qualms about changing the public API at a rapid pace, provided that we document this.

```
8b (Global Settings 8a)+≡
VERSION←4 1 0
This code is used in chunk 5.
Defines:
VERSION, never used.
```

<sup>&</sup>lt;sup>2</sup>https://semver.org/

We depend on ArrayFire<sup>3</sup> for much of our GPU backend functionality. This means we need to know two things, where ArrayFire is installed and which ArrayFire backend we should use when compiling. We only really need to know where ArrayFire is installed on UNIX style systems, as these systems seem to be much more variable in this regard, and there is an environment variable that we can use in Windows to find out where ArrayFire is installed more conveniently on that platform. We default to using 'cuda' as our main option, but we also support the following options for AFALIB:

#### cuda opencl cpu

Using ' ' for AFALIB will use ArrayFire's unified backend, but we don't default to this because we have seen some issues on some platforms with reliability problems. To avoid this, we choose to use cuda as the default, which tends to either work or fail explicitly, which allows the user to respond rather than crashing ungracefully in the case of the unified backend.

The least reliable backend we have seen is the openct one, which seems to be more hit or miss depending on the underlying stability of the OpenCL drivers that are installed on the user's system. In particular, some Linux OpenCL installations seem to be particularly fragile. In such cases, always make sure that a good, solid OpenCL library is being used.

9 (Global Settings 8a)+≡

AFΔPREFIX+'/opt/arrayfire'

AFΔLIB+' cuda'

This code is used in chunk 5.

Defines:

AFΔLIB, used in chunks 13a, 36, and 49a.

AFΔPREFIX, used in chunk 36.

<sup>&</sup>lt;sup>3</sup>https://arrayfire.com/

On Windows, we rely on the Visual Studio C/C++ compiler to build our runtime and user code. We have settled on trying to stay as up to date with this as possible. However, there are many different installation paths used by Visual Studio, which can make it difficult to know where to look unless we hardcode each location. Instead, we assume that Visual Studio will not be a primary interest to our users, making it likely that they will be installing Visual Studio only as a dependency for using Co-dfns. In this case, it is likely that they will be using the Community version. Thus, we default to using the latest version of Visual Studio of which we are aware and using the Community version of this, which Microsoft does not charge for.

If a different version of Visual Studio is installed, then it is important to figure out what the right path should be to locate the Visual Studio installation. The main thing we need to get from this path is access to the vcvarsall.bat batch file. This file configures the cmd.exe environment to be able to find the Visual Studio compiler and work in the right way. In the 2002 Community addition, and apparently most new versions of Visual Studio, this is located in the VC\Auxiliary\Build\ subdirectory of the main installation folder. When changing this path, we want to make sure that the following path points to the correct vcvarsall.bat file:

VSAPATH, '\VC\Auxiliary\Build\vcvarsall.bat'

Most users will simply need to alter Community to match the edition of Visual Studio 2022 that they have installed on their system.

10 ⟨Global Settings 8a⟩+≡
VSΔPATH+'\Program Files\Microsoft Visual Studio'
VSΔPATH,+'\2022\Community'
This code is used in chunk 5.
Defines:
VSΔPATH, used in chunks 36 and 49a.

#### 3.2 The Fix API

One of the core entry points into the compiler is through the Fix function. This function is designed to mimic and more or less replace the use of the DFIX function found in Dyalog APL. Its design models that behavior, and it is important as an entry-point because it exercises most of the core elements of the compiler. In particular, the design of the compiler's pipeline is demonstrated most fully in this function.

11

```
Parse \rightarrow Compile \rightarrow Generate \rightarrow Backend \rightarrow Link
```

The interfaces to the <code>DFIX</code> function and the Co-dfns <code>Fix</code> function differ in a few key ways. The left argument to <code>Fix</code> is a character vector giving the name to use when generating files and other artifacts. This does *not* affect the name of the resulting namespace, since that is defined, if at all, in the file source itself. The  $\alpha$  argument only affects the name of the files and other outputs that <code>Fix</code> generates.

We also print out which part of the compiler we are in when we enter that "phase". Doing this helps to give us an intuitive sense of how fast each phase is and whether one phase is taking an abnormally long time or not. It also helps in debugging.

The input requirements for Fix are not listed in the definition itself, because both the parser PS and the Fix function need to use the same basic checks, and since the Fix function calls the parser as its first entry point, it doesn't make much sense to duplicate that work in both places. The requirements are as follows:

- Scalar/Vector
- Character type

Uses SIGNAL 19b.

12a

12b

• Simple or Vector of Vectors

We generate a DOMAIN ERROR if the inputs are not well-formed.

⟨Verify source input ω, set IN 12a⟩≡
IN+ω

err+'PARSER EXPECTS SCALAR OR VECTOR INPUT'
1<#pIN:err □SIGNAL 11

err+'PARSER EXPECTS SIMPLE OR VECTOR OF VECTOR INPUT'
2<|≡IN:err □SIGNAL 11

⟨Normalize the input formatting 12b⟩

err+'PARSER EXPECTS CHARACTER ARRAY'
0≠10|□DR IN:err □SIGNAL 11

This code is used in chunk 15.</pre>

The input formatting that is accepted means that newlines could be denoted either with LF, CR, or CRLF sequences inside of the vectors themselves or they could be denoted by having separate vectors for the various lines, or even a mixture of both. To simplify this situation we want to normalize them so that we are always dealing with some combination of LF, CR, and CRLF sequences within the file itself, rather than dealing with the nested situation. This ensures that after verification of the input, everything will work off of the same format. We intentionally put a newline at the end of the file even if we may not require one because it is possible that we are dealing with a file that is missing its final newline. By always adding one, we ensure that every line in the input is always terminated by a line ending. Life is also simpler if we just use LF as our line ending instead of something else, this means that future code must be aware that there could be mixed line endings in the file.

(Normalize the input formatting 12b)≡
IN←∈(⊆IN), "□UCS 10
This code is used in chunk 12a.

### 3.3 The User Command API

```
\langle User\text{-}command API \mid 3a \rangle \equiv
13a
         ⊽Z←Help _
          Z+'Usage: <object> <target> [-af={cpu,opencl,cuda}]'
         ⊽r←List
          r+□NS"1p<0 ♦ r.Name+,"c'Compile' ♦ r.Group+c'CODFNS'
          r[0].Desc←'Compile an object using Co-dfns'
          r.Parse←c'2S -af=cpu opencl cuda

∇ Run(C I); Convert; in; out

         A Parameters
                  AFALIB
                                   ArrayFire backend to use
          Convert+\{\alpha(|SE.SALT.Load'[SALT]/lib/NStoScript -noname').ntgennscode <math>\omega\}
          in out←I.Arguments ♦ AF∆LIB←I.af''⊃~I.af≡0
          S←(c':Namespace ',out),2↓0 0 0 out Convert ##.THIS.±in
          →0/~'Compile' #C
          {\#\text{.THIS.} \underline{\bullet}\text{out}, '\leftarrow \omega'} out Fix S-\squareEX'##.THIS.',out
       This code is used in chunk 5.
       Uses AFALIB 9 and Fix 11.
```

### 3.4 AST Record Structure

```
13b (AST Record Structure 13b)≡

f △ + 'ptknfsrdx'

N△ + 'ABCEFGKLMNOPSVZ'

A B C E F G K L M N O P S V Z←1+115

This code is used in chunk 5.
```

## 3.5 Converters between parent and depth vectors

```
13c (Converters between parent and depth vectors 13c) \equiv
P2D \leftarrow \{z \leftarrow, \iota \neq \omega \land d \leftarrow \omega \neq, z \land \_ \leftarrow \{p \dashv d + \leftarrow \omega \neq p \leftarrow \alpha[z, \leftarrow \omega]\} \stackrel{*}{\times} \equiv \stackrel{\sim}{\sim} \omega \land d(\triangle(-1 + d) \uparrow \stackrel{\circ}{\circ} 0 \ 1 \vdash \varphi z)\}
D2P \leftarrow \{0 = \neq \omega : \theta \land p \dashv 2\{p[\omega] \leftarrow \alpha[\alpha\underline{\iota}\omega]\} \neq \vdash \circ \leftarrow \exists \omega \dashv p \leftarrow \iota \neq \omega\}
This code is used in chunk 5.
```

## 4 Testing

We use the APLUnit testing framework to facilitate our testing of the Co-dfns compiler. The test harness is designed around a testing philosophy in which we ever only write black-box tests that work on the whole compiler using inputs that could be created or are expected to be creatable by end-users. That is, we do no "unit testing" of our source code, but only whole program testing.

The testing framework is provided by the ut.apin file, which is not part of this literate program and so is not included in this document. In order to make some of the testing more convenient, we define the function TEST to run the tests that exist in the tests\ subdirectory. Each of these tests has a specific number which defines the test, and we refer to the tests by number when running them. Both of these testing functions assume that we are running inside of the tests\ directory or one configured identically to it.

The TEST function takes either 'ALL' as its input or a test number in the form of an integer. Given an integer, we call the test matching that number in the current working directory.

The 'ALL' option causes TEST to run all of the tests that are defined in the current working directory. This command is a nicety, since we can technically do all of this by iterating the TEST function over the range of test numbers, but this would not create the aggregate statistics that we would like to see at the end of the testing report. By using 'ALL' we get to see a complete summary of the results of testing all the code, rather than just the individual testing results on a per testing group/number basis.

```
14a
       ⟨TEST 14a⟩≡
         TEST←{
                   #.UT.(print_passed print_summary)←1
                    'ALL'≡ω:#.UT.run './
                   path←'./t',(1 Ο̄̄̄(4ρ10)τω),'_*_tests.dyalog'
                   #.UT.run ⊃⊃0□NINFO⊡1⊢path
       Root chunk (not used in this document).
       Defines:
         TEST, used in chunks 14b and 23.
          The TEST function is part of the utilities that exist outside of the
       codfns namespace, so we define a file for it.
       \langle Tangle\ Commands\ 6 \rangle + \equiv
14b
         echo "Tangling src/TEST.aplf..."
         notangle -R'[[TEST]]' codfns.nw > src/TEST.aplf
       This code is used in chunk 43.
       Defines:
         TEST.aplf, never used.
       Uses codfns 5, src 48, and TEST 14a.
```

## 5 Co-dfns Compiler

#### 5.1 Parser

The first, and in many ways, the most complex element of the compiler is the parser. APL has a number of unique issues when it comes to adequately parsing the language, but the most important is handling the context-sensitive nature of parsing variables: depending on the type of a variable, the parse tree can look very different. To manage this, we make use of a linear, multi-pass style of parser in which the parsing process consists of numerous small passes over the input, each time refining the input into something more like the final result. The parser should take some input that matches the input requirements of the Fix function and produce a suitable output AST.

```
PS :: Source \rightarrow AST \times ExportTypes \times SymbolTable \times Source
```

We can think of the parser as starting with a forest of trees, each of which contains a single root node that represents a single character in from the input source, with all trees arranged in the source order. During each pass of the parser, we progressively combine these trees into more complex trees until we end up at the end with a single tree per parsed module. In other words, we take a fully flat forest of single-node trees and progressively increase the depth while reducing the number of root-nodes until we have our desired AST structure.

We divide the parsing roughly into two main phases, the tokenization phase and the parsing phase. Unlike most compilers, we don't have a strict division in these two phases, so, as they say, think of them more like guidelines than actual rules<sup>4</sup>.

```
15 ⟨Parser 15⟩≡
PS+{

⟨Verify source input ω, set IN 12a⟩

⟨Parsing Constants 16a⟩
⟨Line and error reporting utilities 19b⟩

⟨Tokenize input 20⟩
⟨Parse token stream 23⟩

⟨Adjust AST for output 16b⟩
}
```

<sup>4</sup>https://www.youtube.com/watch?v=WJVBvvS57j0

This code is used in chunk 5. Defines:

PS. used in chunks 11 and 48.

When parsing, it's very helpful to have names for line endings.

16a ⟨Parsing Constants 16a⟩≡
CR LF+□UCS 13 10
This code is used in chunk 15.

### 5.1.1 Output of the Parser

After we finish all of our parsing, we need to take the resulting AST and convert that into something that is suitable for output to the rest of the system. We do this in a few ways.

When we finish parsing, we expect the following fields:

Field	Description
d	Depth vector
t	Node type
k	Node sub-class or "kind"
n	Name/value field
pos	Starting index for source position
end	Exclussive index for source end position
хn	Names of top-level exported bindings
хt	Types of top-level exported bindings
s y m	Symbol Table
IN	Canonical source code

The xn and xt fields are not part of the AST proper, but form an auxiliary analysis that is exceptionally useful, and so we include this as a part of the output of the parser. After parsing a module, we want to extract out the top-level bindings and what their types are, which we can then use to feed into things like the linker and other areas that might need to know what names are available in a given module. Top-level bindings are identified as bindings that appear as a part of an initialization function, also known as F0.

```
16b ⟨Adjust AST for output 16b⟩≡

msk+(t=B)^k[I@{t[ω]≠F}*≡~p]=0

xn+(0ρ-''),msk+n ◊ xt+msk+k

This definition is continued in chunks 17-19.

This code is used in chunk 15.

Defines:

xn, used in chunk 19a.

xt, used in chunk 19a.
```

We also want to convert the AST to an order that follows a depth-first, preorder traversal order, so that we can switch from using the parent vector to the depth vector. We use this output as our main output because it is space efficient for storage, and it works well as a canonical form to use. Because applications may want to only use the parser and not the rest of the compiler, we want to choose an output format that is suitable for external as well as internal use. This has some performance overheads, but it is probably worth it regardless, as reordering at this point to allow a depth vector enables some nice assumptions in the rest of the compiler. We use the P2D utility to reorder all of our AST columns. Note that things like the exported bindings and the symbol table are not strictly part of the AST structure, because they are of a different length and type than the other columns.

\(\langle Adjust AST for output \, 16b\rangle +\equiv \)
d i \(\dagger P2D\) p \(\digger d\) n t k pos end I \(\circ \dagger \dagger c\)
This code is used in chunk 15.

There is an inefficiency in the AST representation at this point, where the n field contains character vectors. This inefficiency was necessary while building up the AST because we were not sure what symbols would be created before we parsed them, but at this point, we know the full set of symbols that we have in the AST. This means that we can convert the n field to a symbol table representation. In this case, we want the n field to pair with a sym list that contains all the unique symbols in the source. We want old\_nssym[|new\_n] to hold for this new n field. In other words, we want the new n field to contain negative integers whose magnitudes are valid indices into the sym symbol table. This means that there is only one character vector per unique symbol or numeric literal in the source code, which can greatly reduce memory usage. Moreover, it is much faster to compare symbols that are represented by numeric index rather than character vector. Most of the work we expect to be done on the n field, so that we never have to pull in symunless we want to know the actual value of the symbol. This actually mimics the feature of symbols in other languages like Scheme, but it comes with an additional efficiency benefit in that we do not require the use of a full generalized pointer to represent a symbol if we have fewer symbols. This means that we are very likely only going to need a single byte or a couple of bytes per symbol to represent it in the n field.

The choice to make all of our symbols negative in value is somewhat strange, but we have a good reason for doing so. The n field is a single field that we use to contain general data for every node, and as such, it represents a sort of union type of all sorts of different data. In particular, we also want to be able to support using the n field to point to other nodes in the AST, which is a feature we rely heavily on in the compiler transformations. However, this feature would conflict with using the n field as an index into the sym table, rather than as an index into the AST. By making symbol pointers negative, we put them into a separate space than the positive AST node pointers, allowing us to store both pointers in the same field. This may seem like a little bit of a strange hack, but it actually makes reasoning about things a little easier, because we can tend to think of n as a name, even if that name is pointing to an AST or a symbol, and avoids needless space duplication or the need to remember to update multiple fields that are only relevant for some nodes.

We map the 0th index to be a null or empty symbol. We also want to reserve the first four symbol slots [1,4] so that they will *always* refer to the same symbols, namely,  $\omega$ ,  $\alpha$ , and  $\omega$ .

This gives us the following definitions for sym and n.

```
\langle Adjust \, AST \, for \, output \, 16b \rangle + \equiv 
sym \leftarrow \cup ('')(,'\omega')(,'\alpha')'\alpha\alpha'' \omega\omega', n
n \leftarrow - symin
```

18

This code is used in chunk 15.

Finally, we want to return our AST structure in a meaningful way. Logically, we have the AST proper, which consists of these fields:

```
d t k n pos end
```

The above fields are returned as an inverted table, where each column is a vector of the same length. We also want to return the variable environment, which gives the names of our top-level bindings and their types, also as an inverted table. Finally, we must return a canonical representation of the source code that is suitable as an indexing target for the pos and end fields, as well as the symbol table. Thus, we have a four element vector as the return value:

AST TopBindingTypes SymbolTable InputSource

Which gives us the following return value.

```
19a ⟨Adjust AST for output 16b⟩+≡
(d t k n pos end)(xn xt)sym IN
This code is used in chunk 15.
Uses xn 16b and xt 16b.
```

### 5.1.2 Handling Parsing Errors

```
\langle Line\ and\ error\ reporting\ utilities\ 19b \rangle \equiv
19b
            linestarts+(<u>1</u>1,2>/IN∈CR LF),≢IN
            mkdm + \{\alpha + 2 \diamond line + line starts \underline{\iota}\omega \diamond no + '[', (\bar{\iota} + line), ']'\}
                         i \leftarrow (\sim IN[i] \in CR \ LF) \neq i \leftarrow beg + ilinestarts[line+1] - beg \leftarrow linestarts[line]
                         ([EM α)(no, IN[i])(' ^'[iεω], ~' 'ρ~≢no)}
            quotelines←{
                         lines←∪linestartsıω
                         nos←(1 0ρ~2×≢lines)\'[',(₹,1+lines), 01⊢'] '
                         beg←linestarts[lines] ◇ end←linestarts[lines+1]
                         m←∈∘ω"i←beg+ı"end-beg
                         -1 + ∈ nos, (~ • CR LF",,(IN•I"i),, ' - '•I"m), CR}
            SIGNAL \leftarrow \{\alpha \leftarrow 2 \quad ' \quad \diamond \quad en \quad msg \leftarrow \alpha \quad \diamond \quad EN \circ \leftarrow en \quad \diamond \quad DM \circ \leftarrow en \quad mkdm \quad \neg \omega
                         dmx+('EN' en)('Category' 'Compiler')('Vendor' 'Co-dfns')
                         dmx, \leftarrow c'Message'(msg, CR, quotelines \omega)
                         □SIGNAL cdmx }
         This code is used in chunk 15.
         Defines:
            linestarts, never used.
            mkdm, never used.
            quotelines, used in chunk 20.
            SIGNAL, used in chunks 12a, 20, 23, 31, 36-38, and 42a.
```

### 5.1.3 Tokenizing the Input

```
\langle Tokenize\ input\ 20 \rangle \equiv
20
         A Group input into lines as a nested vector
                    pos←(ι≢IN)⊆~~IN∈CR LF
         A Mask strings
                    0≠≢lin←<u>ι</u>⊃∘φ"msk←≠†"''''=IN∘I"pos:{
                              EM←'SYNTAX ERROR: UNBALANCED STRING',('S'/~2≤≠lin),CR
                              EM, \leftarrowquotelines \in (msk\neq"pos)[lin]
                              EM □SIGNAL 2}0
         A Remove comments
                    pos msk+"~+c∧\"(~msk+mskv-1¢"msk)~'A'=IN∘I"pos
         A Remove leading and trailing whitespace
                    WS←□UCS 9 32 ♦ pos msk/~~←c~(∧\√∧\U\Φ)∘(WS∈~IN∘I)~pos
         A Flatten and separate lines and ♦ with Z type
                    t \leftarrow 0 \rho \subset pos \diamond t pos msk(\epsilon, \circ, \sim) \leftarrow Z(\neg pos)0 \diamond t[\underline{\imath}' \diamond' = IN[pos]] \leftarrow Z
         A Tokenize Strings
                    end+1+pos \diamond t[i+\underline{\iota}2<\neq0,msk]+C \diamond end[i]+end[\underline{\iota}2>\neqmsk,0]
                    t pos end/~←c(t≠0)∨~msk
         A Verify that all open characters are part of the valid character set
                    alp←'ABCDEFGHIJKLMNOPQRSTUVWXYZ_abcdefghijklmnopqrstuvwxyz'
                    alp,+'ÀÁÂÃÄÅÆÇÈÉÊËÌÍÎÏÐÑÒÓÔÖÖØÙÚÜÜÝßàáâãäåæçèéêëìíîïðñòóôõöøùúûüþ'
                    alp, ← ' ∆∆ABCDEFGHIJKLMNOPQRSTUVWXYZ '
                    num←□D
                    synb←'¯[]{}()'':αω◊;'
                    syna←'<del>0</del>□□#'
                    prmfs←'+-×÷|[[★®⊙!?~∧∨ã▽<≤=>≥≠≡≢ρ,-ф⊖┪↑↓⊂⊆⊃∈€∩∪ιι[]↓♥₾क⊥┰⊣⊢▽←→'
                    prmdo←'∘.*⊡0°ö@' ♦ prmmo←'~~&I目' ♦ prmfo←'//\\
                    prms←prmfs,prmdo,prmmo,prmfo
                    x\leftarrow' '@\{t\neq 0\}IN[pos] A The spaces produce nice invariants
                    v/msk←~x∈alp,num,syna,synb,prms,WS:{
                              EM←'SYNTAX ERROR: INVALID CHARACTER(S) IN SOURCE', CR
                              EM, ←quotelines <u>r</u>msk
                              EM □SIGNAL 2}0
         A Tokenize numbers
                    _←{dm[ω]←∧\dm[ω]}"(dm∨x∈alp)⊆ı≢dm←x∈num
                    dm \vee \leftarrow (','=x) \wedge (-1\phi dm) \vee 1\phi dm
                    dmv \leftarrow ('' = x) \land 1 \Phi dm
                    dmv \leftarrow (x \in 'EeJj') \land (-1\phi dm) \land 1\phi dm
```

```
v/msk←(dm=0)^x='-':2'ORPHANED -'SIGNAL pos/~msk
                         v \neq \{1 < + \neq \omega = 'j'\}"dp\leftarrow \squareC"dm\subseteq x: 'MULTIPLE J IN NUMBER'\squareSIGNAL 2
                         v \neq \{1 < + \neq \omega = e'\} "dp \leftarrow \neg = /\{\omega \leq \omega \neq j'\} "dp: MULTIPLE E IN NUMBER' SIGNAL 2
                         v/'e'=>"dp:'MISSING MANTISSA'□SIGNAL 2
                         v+'e'=>∘φ"dp:'MISSING EXPONENT'□SIGNAL 2
                         mn ex \leftarrow \downarrow \Diamond \uparrow \{2 \uparrow (\omega \subseteq \omega \neq e'), e''\} dp
                         v \neq \{1 < + \neq ' \cdot \cdot' = \omega\}"mn, ex: 'MULTIPLE . IN NUMBER' \squareSIGNAL 2
                         v∱'.'e"ex:'REAL NUMBER IN EXPONENT'□SIGNAL 2
                         v \neq \{v \neq 1 \downarrow \omega \in '^-'\}"mn, ex: 'MISPLACED -' SIGNAL 2
                         t[i+\underline{\iota}2</0,dm]+N \Leftrightarrow end[i]+end/~2>/dm,0
A Tokenize Variables
                         t[i \leftarrow 2 < \neq 0, vm \leftarrow (\sim dm) \land x \in alp, num] \leftarrow V \Leftrightarrow end[i] \leftarrow end \neq 2 > \neq vm, 0
A Tokenize \alpha, \omega formals
                          fm \leftarrow \{ mm \leftarrow \varphi \Rightarrow (> \circ \Rightarrow , \vdash) \neq \varphi m \leftarrow \alpha = ' \quad ', \omega \quad \diamond \quad 1 \downarrow " (mm \land \sim m1) (mm \land m1 \leftarrow 1 \varphi m) \} 
                         am aam←'α'fm x ◊ wm wwm←'ω'fm x
                         ((am∨wm)/t)+A ♦ ((aam∨wwm)/t)+P ♦ ((aam∨wwm)/end)+end/<sup>2-</sup>1¢aam∨wwm
A Tokenize Primitives, Atoms
                         t[\underline{\iota}(\sim dm) \land x \in prms] \leftarrow P \diamond t[\underline{\iota}x \in syna] \leftarrow A
A Compute dfns regions and type, include } as a child
                         t[<u>i</u>'{'=x]←F ◇ 0≠⊃d←¯1φ+\1 ¯1 0['{}'ix]:'UNBALANCED DFNS'[SIGNAL 2
A Check for out of context dfns formals
                      v \neq (d=0) \land (t=P) \land IN[pos] \in '\alpha \omega' : 'DFN FORMAL REFERENCED OUTSIDE DFNS' SIGNAL REFERENCED SIGNAL SIGNAL REFERENCED SIGNAL SIGNAL SIGNAL SIGNAL SIGNAL S
A Compute trad-fns regions
                   v/Z≠t/~1¢msk←(d=0)^'∀'=x:'TRAD-FNS START/END LINES MUST BEGIN WITH ∇'□SIG
NAL 2
                         O≠>tm← 1Φ≠ \ (d=0) \ '∇'=x: 'UNBALANCED TRAD-FNS' SIGNAL 2
                   √/Z≠t/~⊃1 ~1√.φ⊂(2>/tm),0:'TRAD-FNS END LINE MUST CONTAIN ∇ ALONE'□SIGNAL
A Identify Label colons versus others
                         A Tokenize Keywords
                         ki \leftarrow \underline{\iota}(t=0) \land (d=0) \land (':'=IN[pos]) \land 1 \varphi t = V
                         t[ki] \leftarrow K \diamond end[ki] \leftarrow end[ki+1] \diamond t[ki+1] \leftarrow 0
                         ERR←'EMPTY COLON IN NON-DFNS CONTEXT, EXPECTED LABEL OR KEYWORD'
                         v \neq (t=0) \land (d=0) \land ': '=IN[pos]:ERR \square SIGNAL 2
A Tokenize System Variables
                         si←<u>ı</u>('['=IN[pos])∧1¢t=V
                         t[si] \leftarrow S \diamond end[si] \leftarrow end[si+1] \diamond t[si+1] \leftarrow 0
```

```
A Delete all characters we no longer need from the tree d tm t pos end(f;)+c(t≠0)vxe'()[]{}:;'

A Tokenize Labels

ERR←'LABEL MUST CONSIST OF A SINGLE NAME'

v≠(Z≠t[li-1])v(V≠t[li+11φmsk+t=L]):ERR [SIGNAL 2 t[li]+L ♦ end[li]+end[li+1]

d tm t pos end(f;)+c~msk

This code is used in chunk 15.
Uses quotelines 19b and SIGNAL 19b.
```

### 5.1.4 Parsing Token Stream

```
23
     \langle Parse\ token\ stream\ 23 \rangle \equiv
       A Now that all compound data is tokenized, reify n field before tree-building
                 A Verify that keywords are defined and scoped correctly
                KW+'NAMESPACE' 'ENDNAMESPACE' 'END' 'IF' 'ELSEIF' 'ANDIF' 'ORIF' 'ENDIF
               KW, ←'WHILE' 'ENDWHILE' 'UNTIL' 'REPEAT' 'ENDREPEAT' 'LEAVE' 'FOR' 'ENDFOR
                 KW.+'IN' 'INEACH' 'SELECT' 'ENDSELECT' 'CASE' 'CASELIST' 'ELSE' 'WITH
               KW, ←'ENDWITH' 'HOLD' 'ENDHOLD' 'TRAP' 'ENDTRAP' 'GOTO' 'RETURN' 'CONTINUE
                 KW, ←'SECTION' 'ENDSECTION' 'DISPOSABLE' 'ENDDISPOSABLE'
                 KW,"~←':'
                 msk←~KW∈~kws←n/~km←t=K
                 v/msk:('UNRECOGNIZED KEYWORD ',kws>~> msk) ☐SIGNAL 2
                 msk+kws€':NAMESPACE' ':ENDNAMESPACE'
                 v/msk∧km/tm:'NAMESPACE SCRIPTS MUST APPEAR AT THE TOP LEVEL'□SIGNAL 2
                 msk+kwseKW~':NAMESPACE' ':ENDNAMESPACE' ':SECTION' ':ENDSECTION'
               v/msk←msk∧~km/tm:{msq←2'STRUCTURED STATEMENTS MUST APPEAR WITHIN TRAD-FNS
                         msg SIGNAL \epsilon \{x+iend[\omega]-x+pos[\omega]\}"\underline{i}km+msk\}\theta
       A Verify system variables are valid
                SYSV←,"'Á' 'A' 'AI' 'AN' 'AV' 'AVU' 'BASE' 'CT' 'D' 'DCT' 'DIV' 'DM'
SYSV,←,"'DMX' 'EXCEPTION' 'FAVAIL' 'FNAMES' 'FNUMS' 'FR' 'IO' 'LC' 'LX
                 SYSV.←."'ML' 'NNAMES' 'NNUMS' 'NSI' 'NULL' 'PATH' 'PP' 'PW' 'RL' 'RSI
               SYSV, ←, "'RTL' 'SD' 'SE' 'SI' 'SM' 'STACK' 'TC' 'THIS' 'TID' 'TNAME' 'TNUMS
                 SYSV. ←. "'TPOOL' 'TRACE' 'TRAP' 'TS' 'USING' 'WA' 'WSID' 'WX' 'XSI'
              SYSF+, "'ARBIN' 'ARBOUT' 'AT' 'C' 'CLASS' 'CLEAR' 'CMD' 'CONV' 'CR' 'CS' 'CSV
                 SYSF, +, "'CY' 'DF' 'DL' 'DQ' 'DR' 'DT' 'ED' 'EM' 'EN' 'EX' 'EXPORT'
                        "'FAPPEND' 'FCHK' 'FCOPY' 'FCREATE' 'FDROP' 'FERASE' 'FFT' 'IFFT
              SYSF, +, "'FHIST' 'FHOLD' 'FIX' 'FLIB' 'FMT' 'FPROPS' 'FRDAC' 'FRDCI' 'FREAD
                 SYSF,←,"'FRENAME' 'FREPLACE' 'FRESIZE' 'FSIZE' 'FSTAC' 'FSTIE' 'FTIE'
                        ''FUNTIE' 'FX' 'INSTANCES' 'JSON' 'KL' 'LOAD' 'LOCK' 'MAP' 'MKDIR
                      "'MONITOR' 'NA' 'NAPPEND' 'NC' 'NCOPY' 'NCREATE' 'NDELETE' 'NERASE
                 SYSF, +, "'NEW' 'NEXISTS' 'NGET' 'NINFO' 'NL' 'NLOCK' 'NMOVE' 'NPARTS'
                         ''NPUT' 'NQ' 'NR' 'NREAD' 'NRENAME' 'NREPLACE' 'NRESIZE' 'NS'
                 SYSF, +, "'NSIZE' 'NTIE' 'NUNTIE' 'NXLATE' 'OFF' 'OR' 'PFKEY' 'PROFILE'
                 SYSF, +, "'REFS' 'SAVE' 'SH' 'SHADOW' 'SIGNAL' 'SIZE' 'SR' 'SRC' 'STATE
              SYSF, +, "'STOP' 'SVC' 'SVO' 'SVQ' 'SVR' 'SVS' 'TCNUMS' 'TGET' 'TKILL' 'TPUT
                 SYSF, +, "'TREQ' 'TSYNC' 'UCS' 'VR' 'VFI' 'WC' 'WG' 'WN' 'WS' 'XML' 'XT
                 SYSD←,"'OPT' 'R' 'S'
                 v/msk+(t=S)^~n∈'□', "SYSV, SYSF, SYSD:{
                         ERR+2'INVALID SYSTEM VARIABLE, FUNCTION, OR OPERATOR'
                         ERR SIGNAL \epsilonpos [\omega] \{\alpha + \iota \omega - \alpha\} "end [\omega]
                 }<u>ւ</u>msk
```

```
A Compute parent vector from d
             p←D2P d
A Compute nameclass of dfns
              k+2\times t\in F \diamond k[\neg p/\sim (t=P)\land n\in \neg \alpha'] \leftarrow 3 \diamond k[\neg p/\sim (t=P)\land n\in \neg \omega'] \leftarrow 4
A We will often wrap a set of nodes as children under a Z node
              gz \leftarrow \{z \leftarrow \omega \uparrow \sim -0 \neq \neq \omega \Leftrightarrow ks \leftarrow -1 \downarrow \omega
                          t[z] \leftarrow Z \diamond p[ks] \leftarrow z \diamond pos[z] \leftarrow pos[\neg \omega] \diamond end[z] \leftarrow end[\neg \phi z, ks] \diamond z
A Nest top-level root lines as Z nodes
              _←(gz 1φ⊢)¨(t[i]=Z)⊂i←<u>ı</u>d=0
              'Non-Z top-level node'assert t[<u>r</u>p=r≢p]=Z:
A Nest all dfns expression bodies as Z nodes
              _←p[i]{end[α]←end[⊃φω] ♦ gz¨ωc~1,<sup>-</sup>1↓t[ω]=Z}目i←<u>ι</u>t[p]=F
'Non-Z dfns body node'assert t[<u>ι</u>t[p]=F]=Z:
A Drop/eliminate any Z nodes that are empty or blank
              _←p[i]{msk[α,ω]←~^/IN[pos[ω]]∈WS}目i←ı(t[p]=Z)^p≠ι≢p⊣msk←t≠Z
              tm n t k pos end(/\sim) \leftarrow cmsk \diamond p\leftarrow(\underline{\iota} ~msk)(\vdash -1+\underline{\iota})msk/p
A Parse Keyword structures
              nss+n∈c':NAMESPACE' ♦ nse+n∈c':ENDNAMESPACE'
              ERR←':NAMESPACE KEYWORD MAY ONLY APPEAR AT BEGINNING OF A LINE'
              Z∨.≠t/~1φnss:ERR □SIGNAL 2
              ERR←'NAMESPACE DECLARATION MAY HAVE ONLY A NAME OR BE EMPTY'
              \sqrt{(Z \neq t/^{2}-1\phi_{nss})} \sqrt{(V \neq t/^{2}-1\phi_{nss})} \sqrt{Z \neq t/^{2}-2\phi_{nss}} : ERR \square SIGNAL 2
              ERR←': ENDNAMESPACE KEYWORD MUST APPEAR ALONE ON A LINE'
              v/Z≠t/~⊃1 ~1v. φ⊂nse:ERR □SIGNAL 2
              t[nsi+11onss]+M ♦ t[nei+11onse]+-M
              n[i] \leftarrow n[1+i \leftarrow \underline{\iota}(t=M) \land V=1 \Leftrightarrow end[nsi] \leftarrow end[nei]
              x \leftarrow ip = i \neq p \diamond d \leftarrow + \uparrow (t[x] = M) + -t[x] = -M
              O≠⊃φd:':NAMESPACE KEYWORD MISSING :ENDNAMESPACE PAIR'□SIGNAL 2
              p[x] \leftarrow x[D2P - 1\phi d]
A Delete unnecessary namespace nodes from the tree, leave only M's
             msk \leftarrow nssv((^{-1}\varphi nss) \land t = V) \lor nse \lor 1 \varphi nse
              t k n pos endf \sim \leftarrow cmsk \diamond p \leftarrow (\underline{\iota} \sim msk)(\vdash -1 + \underline{\iota})msk \neq p
A PARSE LABELS ...
A Map guard statements to (G (Z ...) (Z ...))
             _<del>←</del>p[i]{
                          0=+\neq m \leftarrow ': '=IN[pos[\omega]]:\theta
                          >m: 'EMPTY GUARD TEST EXPRESSION'∏SIGNAL 2
```

```
1<+/m: 'TOO MANY GUARDS'□SIGNAL 2
                                                                                                                             t[\alpha] \leftarrow G \diamond p[ti \leftarrow gz \Rightarrow tx cq \leftarrow 2\uparrow(c\theta), \forall \omega \subset 1, \neg 1 \downarrow m] \leftarrow \alpha \diamond k[ti] \leftarrow 1
                                                                                                                              ci \leftarrow \neq p \diamond p, \leftarrow \alpha \diamond t k pos end, \leftarrow 0 \diamond n, \leftarrow <'' \diamond k[gz cq, ci] \leftarrow 1
                                                                  0\}\exists i \leftarrow \underline{\iota} t[p[p]] = F
A Parse brackets and parentheses into <sup>-</sup>1 and <sup>Z</sup> nodes
                                                                                                         x+IN[pos[\omega]] \diamond bd++bm+(bo+'['=x)+-bc+']'=x \diamond pd++pm+(po+'('=x)+bd+bm+(bo+')'=x)
pc←')'=x
                                                                                                                                                                                                    O≠⊃φbd:2'UNBALANCED BRACKETS'SIGNAL pos[ω]{x+ι([+ω)
x \leftarrow [+\alpha]\ddot{o}\{\omega \neq \sim 0 \neq bd\} \text{ end } [\omega]
                                                                                                                                                                                 O≠>φpd:2'UNBALANCED PARENTHESES'SIGNAL pos[ω]{x+ι([+ω)
x \leftarrow [+\alpha] \ddot{\circ} \{\omega \neq \sim 0 \neq pd\} end[\omega]
                                                                                                                       (po/bd)∨.≠φpc/bd:'OVERLAPPING BRACKETS AND PARENTHESES'□SIGNAL
                                                                                                                            p[\omega] \leftarrow (\alpha, \omega)[1 + 10\{\omega = i \neq \omega\}D2P + \uparrow^{-1}\phibm + pm] \diamond t[bo \neq \omega] \leftarrow^{-1} \diamond t[po \neq \omega] \leftarrow^{
                                                                                                                             end[po+\omega] \leftarrow end[\phipc+\omega] \diamond end[\phibc+\omega] \leftarrow end[\phibc+\omega]
                                                                   0}目i←<u>ι</u>(t[p]=Z)^p≠ι≢p
                                                                   t k n pos endf = -msk + N[pos] \epsilon')' \diamond p + (\underline{\iota} - msk) (+-1 + \underline{\iota}) msk \neq p
A Convert semi-colon indexing into Z nodes in the -1 nodes
                                                     _+p[i]{k[z+>, fgz"g+ω<~-1φIN[pos[ω]]ε';]']+1 ◊ t[z]+Z P[1=≢"g]}∃i+ιt[p]=-
A Mark bindable nodes
                                                                   bm \leftarrow (t=V) \lor (t=A) \land n \in , "' \square \square'
                                                                   bm+\{bm-p[i]\{bm[\alpha]+(V^{-1}\equiv t[\omega])\vee \wedge \neq bm[\omega]\}\exists i+\underline{\iota}(\sim bm[p])\wedge t[p]=Z\} \forall \equiv bm
A Binding nodes
                                                                 _←p[i]{
                                                                                                                             t[\omega/\sim(n[\omega]\epsilon c, '+') \wedge 0, ^-1 \downarrow bm[\omega]] \leftarrow B
                                                                                                                             b v \leftarrow \{(\neg x)(1 \downarrow x \leftarrow \omega \neq \{t[\neg \omega] = B\} \omega)\}^{-1} \downarrow \omega \subset \{1, \neg 1 \downarrow t[\omega] \in P \mid B\}
                                                                                                                             v/~bm[∈v]: 'CANNOT BIND ASSIGNMENT VALUE' ☐SIGNAL 2
                                                                                                                             p[\omega] \leftarrow (\alpha,b)[0,-1 \downarrow + \uparrow t[\omega] = B]
                                                                                                                              n[b] \leftarrow n[\epsilon v] \diamond t[\epsilon v] \leftarrow 7 \diamond pos[b] \leftarrow pos[\epsilon v] \diamond end[b] \leftarrow end[\neg \phi \omega]
                                                                   0}目i←<u>ı</u>(t[p]=Z)^p≠ı≢p
                                                                   t k n pos endf = -msk + t \neq -7 \diamond p + (\underline{\iota} - msk) (\vdash -1 + \underline{\iota}) msk \neq p
A Mark unambiguous primitive kinds
                                            k[\underline{\iota}(t=S)\land n\epsilon' \square', "SYSV] + 1 \diamond k[\underline{\iota}(t=S)\land n\epsilon' \square', "SYSF] + 2 \diamond k[\underline{\iota}(t=S)\land n\epsilon' \square', "SYSD] + 1
                                                                    t[it=S]←P
                                                                    k[\underline{\iota}t\in A \ C \ N] \leftarrow 1 \ \diamond \ k[\underline{\iota}n\in , "prmfs] \leftarrow 2 \ \diamond \ k[\underline{\iota}n\in , "prmmo] \leftarrow 3 \ \diamond \ k[\underline{\iota}n\in , "prmdo] \leftarrow 4
                                                                    k[<u>ı</u>n∈,"prmfo]←5
                                                                    k[i+\underline{\imath}msk+(n\epsilon c, '\circ') \land 1 \phi n\epsilon c, '.'] + 3 \diamond end[i] + end[i+1] \diamond n[i] + c, '\circ.'
                                                                    t k n pos endf = -\infty + -1 \phi_{msk} + \rho + (\underline{\iota} = -1 + \underline{\iota}) + (\underline{\iota} = -1
A Anchor variables to earliest binding in matching frame
                                                                    rf \leftarrow 10 \{ \sim t[\omega] \in F G M \} p[rz \leftarrow 10 \{ \sim (t[\omega] = Z) \land (t[p[\omega]] \in F G M) \lor p[\omega] = \omega \} \stackrel{*}{\times} = \stackrel{\sim}{\sim} p]
```

```
rf[i]+p[i+\underline{\iota}t=G] \diamond rz[i]+i \diamond rf+rf I@\{rzep[i]+\circ\neg\exists i+\underline{\iota}t[p]=G\}rf
                mk \leftarrow \{\alpha[\omega], \neg n[\omega]\}
                 fr←rf mk⊢fb←fb[ı~rf mk⊢fb+fb I∘(ı~)U⊖rz mk⊢fb←ıt=B] ♦ fb,←-1
                 vb←fb[frirf mk i]@(i←<u>i</u>t=V)⊢<sup>-</sup>1ρ~≢p
                 vb[i/~(rz[i]<rz[b])∨(rz[i]=rz[b])∧i≥b←vb[i←i/~vb[i]≠-1]]←-1
                 _←{z/~¯1=vb[1[z]←fb[frι&n I@1⊢z←rf I@0⊢ω]}*≡&{rf[ω],-ω}ι(t=V)∧vb=¯1
                 v \neq msk \leftarrow (t=V) \wedge vb = -1 : \{
                      6'ALL VARIABLES MUST REFERENCE A BINDING'SIGNALεpos[ω]{α+ιω-α}¨end[α
                 <u>լ</u>msk
A \alpha/\omega \rightarrow V; M \rightarrow FO; \alpha\alpha/\omega\omega \rightarrow P2
                 t \leftarrow V@(i \leftarrow \underline{\iota}(t=A) \land n \in , "'\alpha\omega') \vdash F@\{t=M\}t \diamond vb[i] \leftarrow i \diamond k[\underline{\iota}(t=P) \land n \in '\alpha\alpha' '\omega\omega'] \leftarrow 2
A Infer types of bindings, groups, and variables
                 z \times \psi p[i] \{\alpha \omega\} = i + \underline{\iota}(t[p] \in B \ Z) \wedge p \neq \iota \neq p
                x \leftarrow \{\omega \neq \sim \land t [\omega] = 1\} \cup \phi \sim x
               O∨.=≢"x:'BRACKET SYNTAX REQUIRES FUNCTION OR ARRAY TO ITS LEFT'□SIGNAL
                _+{
                                k[msk \neq z] \leftarrow k[x \neq msk \leftarrow (k[\neg x] \neq 0) \land 1 = \neq x] \diamond z x \neq msk
                                k[z/\sim msk \leftarrow k[\supset x]=4] \leftarrow 3 \diamond z x/\sim \leftarrow c \sim msk
                     k[z/\overline{w}sk+\{(2 \ 3 \ 5 \in k[\neg \omega]) \lor =(\omega, \neq k)[0: \lambda k[\omega]=1][k,0\} \circ \varphi x]+2 \diamond z x/\overline{w}+c
                               k[z/\overline{m}sk+k[\neg \circ \varphi x]=1]+1 \diamond z x/\overline{n}+c\sim msk
                                k[i] \leftarrow k[vb[i \leftarrow \underline{\iota}t = V]]
                 ≢z}*(=∨0=⊣)≢z
                 'FAILED TO INFER ALL BINDING TYPES'assert 0=≢z:
A Strand arrays into atoms
                 i \leftarrow |i \rightarrow km \leftarrow 0 < i \leftarrow i[A|(i, \sim \leftarrow - \cup p[i]), p[i \leftarrow \underline{t}[p] \in B Z]]
                msk \leftarrow (t[i] \in C \ N) \lor msk \land \supseteq 1 \ \lnot 1 \lor . \varphi \lor msk \leftarrow km \land (t[i] \in A \ C \ N \ V \ Z) \land k[i] = 1
                np+(\not\equiv p)+\iota\not\equiv ai+i\not\vdash am+2>\not+msk,0 \diamond p+(np@ai\iota\not\equiv p)[p] \diamond p,+ai \diamond km+2<\not+0,msk
                 t k n pos end(\dashv,I)\leftarrowcai \diamond k[ai]\leftarrow1 6[\lor\not"msk\subseteqt[i]\neqN]
                 t n pos(\neg \otimes ai \sim + A(c'')(pos[km \neq i]) \diamond p[msk \neq i] + ai[(msk + msk \wedge \sim am) \neq -1 + + km]
                 i \leftarrow \underline{\iota}(t[p] = A) \wedge (k[p] = 6) \wedge t = N
                p, \leftarrow i \diamond t k n pos end(\neg, I) \leftarrow c i \diamond t k n(\neg @ i \sim) \leftarrow A 1(c'')
A PARSE B←D...
A PARSE B←...D
A Rationalize F[X]
                _←p[i]{
                                >m←t[ω]=-1:'SYNTAX ERROR:NOTHING TO INDEX'□SIGNAL 2
                               k[\omega/\sim m^{-1}\phi(k[\omega] \in 2 \ 3 \ 5) \vee (1 + \omega) = 4 + 4
                0}目i\leftarrow<u>i</u>(t[p]\inB Z)\wedge(p\neqi\neqp)\wedgek[p]\in1 2
                 i \leftarrow \underline{\iota}(t=1) \land k=4 \diamond j \leftarrow \underline{\iota}(t[p]=1) \land k[p]=4
                 (≢i)≠≢j:{
                      2'AXIS REQUIRES SINGLE AXIS EXPRESSION'SIGNAL εpos[ω]+ι¨end[ω]-pos[ω
```

```
}¬¬+{<α/~1<≠ω}目p[j]
                                    v/msk+t[j]≠Z:{
                                                           2'AXIS REQUIRES NON-EMPTY AXIS EXPRESSION'SIGNAL ext{cons}[\omega] + i 	ilde{} end[\omega]
pos[ω]
                                    }msk/p[j]
                                    p[j] \leftarrow p[i] \diamond t[i] \leftarrow P \diamond end[i] \leftarrow 1 + pos[i]
A Group function and value expressions
                                    i km\leftarrow, \neqp[i]{(\alpha, \omega)(0,1\vee\omega)}目i\leftarrow1(t[p]\inB Z)\wedge(p\neq1\neqp)\wedgek[p]\in1 2
A Mask and verify dyadic operator right operands
                                     (dm \leftarrow 1 \phi(k[i]=4) \land t[i] \in F P V Z) \lor . \land (\sim km) \lor k[i] \in O 3 4:{
                                                                      'MISSING RIGHT OPERAND'∏SIGNAL 2
                                    }0
A Refine schizophrenic types
                                     k[i/^{\sim}(k[i]=5)\wedge dmv^{-1}\phi(\sim km)v(\sim dm)\wedge k[i]\in 1 \ 6]+2 \diamond k[i/^{\sim}k[i]=5]+3
A Rationalize ..
                                     jm \leftarrow (t[i]=P) \land n[i] \in \subset, ' \circ . '
                                     jmv.∧1φ(~km)vk[i]∈3 4: 'MISSING OPERAND TO ∘.'□SIGNAL 2
                             p \leftarrow ((ji \leftarrow jm \neq i) \otimes (jj \leftarrow i \neq i \neq i \neq i \neq j = j \neq k[ji,jj] \leftarrow k[
                                     n[ji,jj]+n[jj,ji] < pos[ji,jj]+pos[ji,ji] < end[ji,jj]+end[jj,jj]
A Mask and verify monadic and dyadic operator left operands
                                     v \neq msk \leftarrow (dm \wedge 2\phi \sim km) \vee (1\phi \sim km) \wedge mm \leftarrow (k[i]=3) \wedge t[i] \in F P V Z:
                                                                     2'MISSING LEFT OPERAND'SIGNAL \epsilon pos[\omega] + i"end[\omega]-pos[\omega]
                                     }i≠~msk
                                    msk←dm∨mm
A Parse function expressions
                                  np \leftarrow (\not\equiv p) + ixc \leftarrow \not\equiv oi \leftarrow msk \neq i \diamond p \leftarrow (np@oii\not\equiv p)[p] \diamond p, \leftarrow oi \diamond t k n pos end(\neg, I) \leftarrow co
                                    p[g \neq i] \leftarrow oi[(g \leftarrow (\sim msk) \land (1 \phi msk) \lor 2 \phi dm) \neq xc - \phi + \gamma \phi msk]
                                    p[g \neq oi] \leftarrow (g \leftarrow msk \neq (1 \phi mm) \vee 2 \phi dm) \neq 1 \phi oi \Leftrightarrow t[oi] \leftarrow 0 \Leftrightarrow n[oi] \leftarrow c''
                                    pos[oi]+pos[g/i][msk/-1+++g+(~msk)\wedge(1\phi mm) \vee 2\phi dm]
                                    ol+1+(k[i/~(2\phi mm) \vee 3\phi dm]=4) \vee k[i/~(1\phi mm) \vee 2\phi dm] \in 2 3
                                    or \leftarrow (msk \neq dm) + 1 + k[dm \neq i] = 2
                                    k[oi]+3 3⊥tor ol
A Wrap all assignment values as Z nodes
                                    i \hspace{0.1cm} km \leftarrow_{\tau} \neq_{p}[i]\{(\alpha, \omega)(0, 1 \vee \omega)\} \exists i \leftarrow_{\underline{\iota}} (t[p] \in_{B} \mathbb{Z}) \wedge (p \neq_{\iota} \neq_{p}) \wedge k[p] \in_{A} \mathbb{Z}
                                     j \leftarrow i \not \sim msk \leftarrow (t[i] = P) \land n[i] \in \subset, ' \leftarrow ' \diamond nz \leftarrow (\not \equiv p) + \iota zc \leftarrow + \not - msk
                                    zm\leftarrow^{-1}\phi msk \diamond p[km\neq i]\leftarrow(zpm\neq(i\times\sim km)+zm\nmid nz)[km\neq^{-1}++\nmid zpm\leftarrow zm\vee\sim km]
A This is the definition of a function value at this point
```

```
isfn \leftarrow \{(t[\omega] \in O \ F) \lor (t[\omega] \in B \ P \ V \ Z) \land k[\omega] = 2\}
A Parse modified assignment to E4(V, F, Z)
                j \leftarrow i \neq m \leftarrow m \leq k \wedge (-1 \phi i \leq n i) \wedge (-2 \phi (t[i] = V) \wedge k[i] = 1 \diamond p[zi \leftarrow nz \neq m \leq k \neq m] \leftarrow j
             p[i/^{\sim}(1\phi m) \vee 2\phi m] + 2/j \diamond t k(\neg @j^{\sim}) + E + \diamond pos end n\{\alpha[\omega]@j + \alpha\} + vi zi, < vi + i/^{\sim} 2\phi
A Parse bracket modified assignment to E4(E6, O2(F, P3(\leftarrow)), Z)
                j \leftarrow i \not \sim m \leftarrow m \leq k \wedge (-1 \varphi i \leq f n - i) \wedge (-2 \varphi t [i] = -1) \wedge -3 \varphi (t [i] = V) \wedge k [i] = 1
                p[zi \leftarrow nz \neq msk \neq m] \leftarrow ei \leftarrow i \neq msk \neq m] \leftarrow t k end(\neg @ei = msk \neq m] \leftarrow E + (end[zi])
                p t k n(¬@(i/~2φm)~)←ei E 6(c'')
                p,+j \diamond t,+Pp^{\sim} \neq j \diamond k,+3p^{\sim} \neq j \diamond n,+(\neq j)p^{c},'+' \diamond pos,+pos[j] \diamond end,+end[j]
                p t k n pos(\neg @j \sim) \leftarrowei O 2(c'')(pos[fi\leftarrowi\neq~1\phim]) \diamond p[fi]\leftarrowj
A Parse bracket assignment to E4(E6, P2(\leftarrow), Z)
                j←i≁m←msk∧(~1φt[i]=~1)∧~2φ(t[i]=V)∧k[i]=1 ◊ p[zi←nz+~msk+m]←ei←i+~2φ
                t k end(\neg @ei \sim) \leftarrowE 4(end[zi]) \diamond p t k n(\neg @(i \neq \sim 1 \phi_m) \sim) \leftarrowei E 6(\subset'')
                p t k(¬@j~)←ei P 2
A Parse modified strand assignment
A Parse strand assignment
A SELECTIVE MODIFIED ASSIGNMENT
A SELECTIVE ASSIGNMENT
A Enclose V[X;...] for expression parsing
                i \leftarrow i [Ap[i \leftarrow \iota(t[p] \in B \ Z) \land (k[p] = 1) \land p \neq \iota \neq p]] \diamond j \leftarrow i \neq \iota \neq \iota = 1
                t[j] \leftarrow A \diamond k[j] \leftarrow 1 \diamond p[i \neq 1 \phi jm] \leftarrow j
A TRAINS
A Parse expression sequences
                i km←¬\neqp[i]{(\alpha¬\omega)(0,(2≤\neq\omega)\wedge1\vee\omega)}目i\leftarrow\underline{\iota}(t[p]\inB Z)\wedge(k[p]=1)\wedgep\neqι\neqp
                msk+m2\sqrt{fm}^{-1}\phi m2+km\sqrt{1}\phi km\sqrt{fm}+(t[i]=0)\sqrt{(t[i]}\neq A)\sqrt{k[i]}=2
                t,←Ep~xc←+/msk ♦ k,←msk/msk+m2 ♦ n,←xcp⊂''
                pos, +pos[msk/i] > end, +end[p[msk/i]]
                p, \leftarrow msk \neq -1 \varphi(i \times \sim km) + km \times x \leftarrow -1 + (\not \equiv p) + + \ \ \ \ \ \ p[km \neq i] \leftarrow km \neq x
A Rationalize V[X;...]
                i \leftarrow i \left[ \frac{1}{4} p \left[ i \leftarrow \underline{\iota} \left( t \left[ p \right] = A \right) \land k \left[ p \right] = 1 \right] \right] \diamond msk \leftarrow 2 \neq \neq^{-1}, ip \leftarrow p \left[ i \right] \diamond ip \leftarrow uip \diamond nc \leftarrow 2 \times \neq ip
                t[ip] \leftarrow E \diamond k[ip] \leftarrow 2 \diamond n[ip] \leftarrow c'' \diamond p[msk \neq i] \leftarrow msk \neq (\not\equiv p) + 1 + 2 \times -1 + + \uparrow \sim msk
                p,+2/ip ◊ t,+ncpP E ◊ k,+ncp2 6 ◊ n,+ncp,"'['
                pos,+2/pos[ip] \diamond end, +\epsilon(1+pos[ip]), -end[ip] \diamond pos[ip]+pos[i/~msk]
A Sanity check
                ERR←'INVARIANT ERROR: Z node with multiple children'
                ERR assert(+/(t[p]=Z)^p≠i≠p)=+/t=Z:
```

```
A Count parentheses in source information

ip+p[i+1(t[p]=Z)∧n[p]∈c,'('] ◊ pos[i]+pos[ip] ◊ end[i]+end[ip]

A VERIFY Z/B NODE TYPES MATCH ACTUAL TYPE

A Eliminate Z nodes from the tree

zi+p I@{t[p[ω]]=Z}*=ki+1msk+(t[p]=Z)∧t≠Z

p+(zi@ki₁≠p)[p] ◊ t k n pos end(¬@zi¬)+t k n pos end I¬cki

t k n pos end+¬+cmsk+~msk∨t=Z ◊ p+(1~msk)(+-1+1)msk+p

This code is used in chunk 15.

Uses assert 38c, SIGNAL 19b, and TEST 14a.
```

## 5.2 Compiler Transformations

```
\langle Compiler 30 \rangle \equiv
30
                TT \leftarrow \{((d \ t \ k \ n \ ss \ se) exp \ sym \ src) \leftarrow \omega \diamond \ I \leftarrow \{(\subset \omega) [\alpha] \}
                                 A B C E F G K L M N O P S V Z+1+115
              A Compute parent vector and reference scope
                                 r \leftarrow I@\{t[\omega] \neq F\} \stackrel{\text{``}}{=} \stackrel{\text{``}}{=} p \rightarrow 2\{p[\omega] \leftarrow \alpha[\alpha\underline{\iota}\omega]\} \neq - \circ c = d \rightarrow p \leftarrow \iota \neq d
              A Lift Functions to top-level
                                 p, \leftarrow n[i] \leftarrow (\neq p) + i \neq i \leftarrow \underline{i}(t = F) \land p \neq i \neq p \land t \land n \land r(\neg, I) \leftarrow ci \land p \land I \sim \leftarrow cn[i]@i \vdash i \neq p
                                 t[i]←C
              A Wrap expressions as binding or return statements
                                 i \leftarrow (\underline{\iota}(\neg t \in F G) \land t[p] = F), \{\omega \neq 2 \mid \iota \neq \omega\} \underline{\iota} t[p] = G \diamond p t k n r \neq \neg \leftarrow 2@i \vdash 1p \neq p
                                 p r i I \sim (+ + m) - 1 \diamond n + j \quad I@(0 \leq +) n \diamond p[i] + j + i - 1
                                 k[j] \leftarrow (k[r[j]] = 0) \lor 0@({\neg \phi \omega} \exists p[j]) \vdash (t[j] = B) \lor (t[j] = E) \land k[j] = 4 \diamond t[j] \leftarrow E
              A Lift guard tests
                                 p[i]+p[x+^{-1}+i+\{\omega/\tilde{\sim}-2|i\neq\omega\}\underline{i}t[p]=G] \diamond t[i,x]+t[x,i] \diamond k[i,x]+k[x,i]
                                n[x] \leftarrow n[i] \diamond p \leftarrow ((x,i)@(i,x) \vdash i \neq p)[p]
              A Count strand and indexing children
                                n[\underline{\iota}(t \in A \ E) \land k = 6] \leftarrow 0 \diamond n[p \neq (t[p] \in A \ E) \land k[p] = 6] + \leftarrow 1
              A Lift and flatten expressions
                                 p[i] + p[x + p I@{-t[p[\omega]] \in F G} \stackrel{\times}{=} i + \underline{\iota}t \in G A B C E O P V] \diamond j + (\phi i)[A\phi x]
                                 p t k n r{\alpha[\omega]@i+\alpha}\leftarrowcj \diamond p\leftarrow(i@j+\iota\neqp)[p]
              A Compute slots for each frame
                                 s+<sup>-</sup>1,~ει"n[∪x]++∘≢[x+0[|\qe+∪I∘¼~rn+r[b],,n[b+<u>ι</u>t=B]
              A Compute frame depths
                                 d\leftarrow (\neq p) \uparrow d \diamond d[i\leftarrow t=F] \leftarrow 0 \diamond \leftarrow \{z\dashv d[i] + \leftarrow \omega \neq z \leftarrow r[\omega]\} = i \diamond f\leftarrow d[0] \neq e], -1
              A Record exported top-level bindings
                                xi \leftarrow \underline{\iota}(t=B) \wedge k[r]=0
                                 ptknfsrdxisym}
           This code is used in chunk 5.
           Uses src 48.
```

### 5.3 Code Generator

```
\langle Code\ Generator\ 31 \rangle \equiv
31
         GC←{
                    p t k n fr sl rf fd xi sym←ω ◆ A B C E F G K L M N O P S V Z←1+:15
                    I \leftarrow \{(\subset \omega) [\alpha] \Leftrightarrow com \leftarrow \{\supset \{\alpha, ', ', \omega\} / \omega\}
                    ks \leftarrow \{\omega \subset [0] \sim (\neg \omega) = \omega [; 0]\} \diamond nam \leftarrow \{'\Delta' \square R' \_ ' \circ \sigma \sim sym[|\omega]\}
                syms +,"'+'
                                                                       1 <u>+</u> 1
                                                                                                      '⊛'
                                                  'mul' 'div' 'exp' 'log' 'res'
                                          'sub'
                                                                                            'cir'
                nams ←
                                'add'
                                                                                                      'min'
                                                                       '≥'
                                          '≤'
                                                      ' = '
                                                                                                     '≠'
                syms, ←,
                                                                          'neq' 'not'
                                'lth'
                                          'lte'
                                                  'eql' 'gte' 'gth'
                                                                                             'and'
                                                                                                      'lor'
                nams,←
                                                              'ι'
                                                                            'ρ'
                syms,←,
                                                  'iot' 'rho' 'cat
                                                                          'ctf' 'rot'
                                'sqd'
                                          'brk'
                                                                                                      'rtf'
                nams,←
                                               '≢'
                                                            ' <del>-</del> '
                                                                          '⊣'
                                                                                                       ' _ '
                syms,←,
                                                   'rgt' 'lft'
                                                                          'dec' 'red'
                                 eqv'
                                                                                             'rdf'
                                                                                                      'scn'
                nams,←
                                               '↓'
                                                                                                         ' ;; '
                syms,←,
                                                           'com' 'dot'
                                                                          'rnk' 'pow'
                                                                                             'jot'
                                'tke
                                                                                                      'unq'
                nams,←
                                                            '∘.' '∈'
                                                                                 ٠٠'
                                                                                                '⊞'
                syms,←,
                                           gdd' 'oup' 'fnd' 'par'
                                                                           'mdv' 'fft'
                                                                                             'ift'
                                                                                                       'scl'
                nams,←
                                 gdu'
                syms,←,¨'∇'
                                                                            'ω'
                                                                                                       'ωω'
                                                                                               'aa'
                                    'this' 'span' 'l'
                                                                            'r'
                                                                                                         'ww'
                  nams,←
                   gck← (A 1)(A 6)
                    gcv← 'Aa' 'As'
                    gck, +(B 1)(B 2)(B 3)(B 4)
                    gcv, +'Bv' 'Bf' 'Bo' 'Bo'
                    gck, +(C 1)(C 2)
                    gcv, ←'Ca' 'Cf'
                    gck, \leftarrow (E^{-2})(E^{-1})(E^{-0})(E^{-1})(E^{-0})(E^{-0})(E^{-0})
                                        'Ek' 'Er' 'Em' 'Ed' 'Eb' 'Ei'
                    gcv,←'Ec'
                    gck, ←(F 0)(F 2)(F 3)(F 4)
                    gcv, ←'Fz' 'Fn' 'Fm' 'Fd'
                    gck, ←(G 0)(N 1)
                    gcv,←'Gd' 'Na'
                    qck, \leftarrow (0\ 1)(0\ 2)(0\ 4)\ (0\ 5)\ (0\ 7)\ (0\ 8)
                    gcv, ←'0v' '0f' '0vv' '0fv' '0vf' '0ff'
                    gck, \leftarrow (P \ 0)(P \ 1)(P \ 2)(P \ 3)(P \ 4)
                    gcv, ←'Pv' 'Pv' 'Pf' 'Po' 'Po'
                    gck, \leftarrow (V \ 0)(V \ 1)(V \ 2)(V \ 3)(V \ 4)
                    gcv,←'Va' 'Va' 'Vf' 'Vo' 'Vo'
                    gcv,←c'{''/* Unhandled '',(⊽α),'' */'',NL}'
                    NL← UCS 13 10
                    pref ←c'#include "codfns.h"'
                    pref,←c''
```

'max

'nan

'mem

'scf

'int

'[FF]

'nst

```
pref, ←c'EXPORT int'
          pref, ←c'DyalogGetInterpreterFunctions(void *p)'
          pref, ←c'{'
          pref,←c'
                         return set_dwafns(p);'
          pref,←c'}'
          pref,←c''
          Bf+{id+sym>~|4>α
                     z +cid,' = retain_cell(stkhd[-1]);'
          z }
          Cf+{id+a4>a
                     z +c'mk_closure((struct closure **)stkhd++, fn',id,', 0);'
          z }
          Ek+{
                     z ←c'release_cell(*--stkhd);'
                     z,←c''
          z }
          Em←{
                     z ←c'c = *--stkhd;'
                     z, ←c'w = *--stkhd;'
                     z, <-c'(c->fn)((struct array **)stkhd++, NULL, w, c->fv);'
                     z,←c'release_cell(c);'
                     z, ←c'release_cell(w);'
          z }
          Er←{
                     z ←c'*z = *--stkhd;'
                     z,←c'goto cleanup;'
                     z, ←c'Ĩ
          z }
          Fn \leftarrow \{id \leftarrow \overline{a} = 5 \Rightarrow \alpha \land x \leftarrow \delta \Rightarrow \neg \neq \omega \land t \leftarrow 2 [x \land k \leftarrow 3 ]x\}
                     hsw \leftarrow (t=0) \lor (t=E) \land k \in 1 \ 2 \ \Diamond \ hsa \leftarrow ((t=E) \land k=2) \lor (t=0) \land k \in 4 \ 5 \ 7 \ 8
                     z ←c'int'
                         z,←c'fn',id,'(struct array **z, struct array *l, struct ar
ray *r, void *fv[])'
                     z,←c'{'
                     z,←c'
                                    void
                                               *stk[128];'
                     z,←c'
                                              **stkhd;'
                                    void
                     z,←hsw/c' void
                                            *w; '
                     z,←hsa/c' void
                                            *a;'
                     z,←hsw/c' struct closure *c;'
                     z,←c''
```

```
z,←c'
                                   stkhd = &stk[0];'
                    z,←c''
                    z,← ' ',"⊃,/dis"ω
                    z,←c'
                                   *z = NULL; '
                    z,←c''
                    z,←c'cleanup:'
                    z,←c'
                                 return 0;'
                    z, +c'}'
                    z,←c''
          z }
          Fz \leftarrow \{id \leftarrow 5 \Rightarrow \alpha \land awc \leftarrow \sqrt{(3[x)} \{(\omega \in A \ O) \lor (\omega = E) \land \alpha > 0\} 2[x \leftarrow \varphi \Rightarrow \sqrt{\omega}\}\}
                    z ←c'int init',id,' = 0;'
                    z,←c''
                    z,←c'EXPORT int'
                    z,←c'init(void)'
                    z,←c'{'
                    z,←c' return fn',id,'(NULL, NULL, NULL, NULL);'
                    z,←c''
                    z,←c'int'
                        z, +c'fn', id, '(struct array **z, struct array *l, struct ar
ray *r, void *fv[])'
                    z, ←c'{'
                    z,←c'
                                             *stk[128];'
                                   void
                    z, ←c'
                                            **stkhd;'
                                   void
                    z,← awc/c'
                                           void
                                                    *a, *w;'
                    z,← awc/c'
                                           struct closure *c;'
                    z,←c''
                    z,←c'
                                   if (init',id,')'
                    z,←c'
                                             return 0;'
                    z,←c''
                    z,←c'
                                   stkhd = &stk[0];'
                    z,←c'
                                   init',id,' = 1;'
                    z,←c'
                                   cdf_init();'
                    z,←c''
                    z,← ' ',"⊃, /dis"ω
                    z,←c'
                                  return 0;'
                    z, <c'}'
                    z,←c''
          z }
          Pf \leftarrow \{id \leftarrow (symsisym[|4 > \alpha]) > nams
                    z +c'*stkhd++ = retain_cell(',id,');'
          z }
```

```
Va←{id←(|4>α)>'' 'r' 'l' 'aa' 'ww',5↓sym
                  z +c'*stkhd++ = retain_cell(',id,');'
         z }
         Zp←{n←'fn', ⊽ω
                  k[\omega] \in 0 2:{
                            z ←c'int'
                              z, ← ⊂ n, '(struct array **z, struct array *l, struct ar
ray *r, void *fv[]);'
                            z,←c''
                   'UNKNOWN FUNCTION TYPE'□SIGNAL 16
         }
         Zx \leftarrow \{n \leftarrow sym \Rightarrow \neg [n[\omega] \land rid \leftarrow \pi rf[\omega]\}
                  k[ω]=0:c''
                  k[\omega] = 1 : {
                            z ←c'struct array *',n,';'
                  z}ω
                  k[\omega] = 2:{
                            z ←c'struct closure *',n,';'
                            z,←c''
                            z,←c'EXPORT int'
                        z, -cn, '_dwa(struct localp *zp, struct localp *lp, struct lo
calp *rp)'
                            z, ←c'{'
                            z,←c'
                                          struct array *z, *l, *r; '
                            z,←c'
                                          int err;'
                            z,←c''
                            z,←c'
                                          l = NULL;'
                            z,←c'
                                          r = NULL; '
                            z,←c''
                            z, ←c'
                                          fn',rid,'(NULL, NULL, NULL, NULL);'
                            z,←c''
                            z,←c'
                                          err = 0;'
                            z,←c''
                            z,←c'
                                          if (lp)'
                            z,←c'
                                                   err = dwa2array(&l, lp->pocket);'
                            z,←c''
                            z,←c'
                                          if (err)'
                            z,←c'
                                                   dwa_error(err);;'
                            z,←c''
                            z,←c'
                                          if (rp)'
                            z,←c'
                                                   dwa2array(&r, rp->pocket);'
                            z,←c''
                            z,←c'
                                          if (err) {'
```

```
z,←c'
                                                      release_array(l);'
                         z,←c'
                                                      dwa_error(err);'
                                           }'
                         z,←c'
                         z,←c''
                         z,←c'
                                           err = (',n,'->fn)(&z, l, r, ',n,'->fv);'
                         z,←c''
                          z,←c'
                                           release_array(l);'
                          z,←c'
                                           release_array(r);'
                         z,←c''
                         z,←c'
                                          if (err)'
                         z,←c'
                                                      dwa_error(err);'
                         z,←c''
                         z, ←c'
                                           err = array2dwa(NULL, z, zp);'
                         z, ←c'
                                           release_array(z);'
                         z,←c''
                         z,←c'
                                           if (err)'
                         z,←c'
                                                      dwa_error(err);'
                          z,←c''
                          z,←c'
                                          return 0;'
                          z, ←c'}'
                         z,←c''
              z } ω
              ±'''UNKNOWN EXPORT TYPE''□SIGNAL 16'
   }
   d i \leftarrow P2D p \diamond ast \leftarrow (\Diamond \uparrow d p t k n(\iota \not\equiv p) fr sl fd)[i;]
   NOTFOUND+{('[GC] UNSUPPORTED NODE TYPE ',N\Delta[>\omega],\pi>\phi\omega)||SIGNAL 16}
 dis \leftarrow \{0=2 \Rightarrow h \leftarrow, 1 \uparrow \omega: ' ' \diamond (\not = gck) = i \leftarrow gck \downarrow ch[2\ 3]: NOTFOUND\ h[2\ 3] \diamond h(\not = i \Rightarrow gcv) ks\ 1 \downarrow \omega \} 
   z+ε, •NL"pref, >, /(, /Zp"<u>ι</u>t=F),(, /Zx"xi),(cc''),dis"ks ast
```

This code is used in chunk 5. Uses codfns 5 and SIGNAL 19b.

## 5.4 Backend C Compiler Interface

```
(Interface to the backend C compiler 36)\equiv
36
         CC←{
                     vsbat÷VS∆PATH,'\VC\Auxiliary\Build\vcvarsall.bat'
                    tie\leftarrow{0:: \squareSIGNAL \squareEN \diamond 22::\omega \squareNCREATE 0 \diamond 0 \squareNRESIZE \omega \squareNTIE 0}
                   put+{s+(<sup>-</sup>128+256|128+'UTF-8'□UCS α)□NAPPEND(t+tie ω)83 ♦ 1:r+s-□NUNTIE t
                    \langle The \text{ opsys } utility \text{ } 42c \rangle
                     soext+{opsys'.dll' '.so' '.dylib'}
                    ccf \leftarrow \{ ( -o''', \omega, '.', \alpha, '''''', \omega, '.c'' - laf', AF\Delta LIB, ' > ', \omega, '.log 2 > &1' \}
                 cci+{'-I''', AFΔPREFIX, '/include'' -L''', AFΔPREFIX, opsys''' ''/lib64'' ''/
                    cco+'-std=c99 -Ofast -g -Wall -fPIC -shared -Wno-parentheses '
                    cco, ←'-Wno-misleading-indentation '
                    ucc \leftarrow \{\omega\omega(\Box SH \alpha\alpha, ' ', cco, cci, ccf)\omega\}
                    gcc←'gcc'ucc'so'
                    clang+'clang'ucc'dylib'
                    vsco+{z+'/W3 /wd4102 /wd4275 /O2 /Zc:inline /Zi /FS /Fd"',ω,'.pdb" '
                                z,←'/WX /MD /EHsc /nologo '
                                z,'/I"%AF PATH%\include" /D "NOMINMAX" /D "AF DEBUG" '}
                    vslo+{z+'/link /DLL /OPT:REF /INCREMENTAL:NO /SUBSYSTEM:WINDOWS '
                           z,←'/LIBPATH:"%AF_PATH%\lib" /OPT:ICF /ERRORREPORT:PROMPT /TLBID:1
                     z,'/DYNAMICBASE~"af',~AF\Delta LIB,~'.lib"~"codfns.lib"~'\} \\ vsc0 \leftarrow \{ \sim [NEXISTS~vsbat:'VISUAL~C?'] \\ SIGNAL~99~~'""',vsbat,'"~amd64'' \} 
                     vsc1+{' && cd "',(¬□CMD'echo %CD%'),'" && cl ',(vsco ω),' "',ω,'.c" '}
                    vsc2←{(vslo ω), '/OUT:"',ω,'.dll" > "',ω,'.log""'}
                    vsc \leftarrow \{ \Box CMD \ ('\%comspec\% \ /C \ ',vsc0,vsc1,vsc2) \omega \}
                      \leftarrow(\pmopsys'vsc' 'gcc' 'clang')\alpha-\forall\alpha, '.c'-1 \squareNDELETE f\leftarrow\alpha, soext\theta
                    \square \leftarrow_{\tau} \Rightarrow \square NGET(\alpha, '.log')1
                    □NEXISTS f:f ♦ 'COMPILE ERROR' □SIGNAL 22}
       This code is used in chunk 5.
       Uses AFALIB 9, AFAPREFIX 9, codfns 5, put 42a, SIGNAL 19b, tie 42a, vsbat 49a,
         vsc 49a, and VSAPATH 10.
```

### 5.5 Linking with Dyalog

```
\langle Linking \ with \ Dyalog \ 37a \rangle \equiv
37a
              NS←{
                            MKA \leftarrow \{mka \subset \omega\} \diamond EXA \leftarrow \{exa \theta \omega\}
                            Display←{α←'Co-dfns' ♦ W←w_new⊂α ♦ 777::w_del W
                                          w_del W¬W αα{w_close α: ±'□SIGNAL 777' ♦ α αα ω}*ωω⊢ω}
                            LoadImage \leftarrow \{\alpha \leftarrow 1 \diamond \sim \square \text{NEXISTS } \omega : \square \text{SIGNAL } 22 \diamond \text{loading } \theta \omega \alpha \}
                             SaveImage \leftarrow \{\alpha \leftarrow ' \text{ image.png'} \diamond \text{ saveimg } \omega \alpha \}
                             Image←{~2 3∨.=≢ρω:□SIGNAL 4 ♦ (3≠⊃ρω)∧3=≢ρω:□SIGNAL 5 ♦ ω⊣w_img ω α}
                            Plot+{2≠≢ρω: □SIGNAL 4 ◊ ~2 3∨.=1>ρω: □SIGNAL 5 ◊ ω¬ν_plot (◊ω) α}
                            Histogram←{ω¬ν_hist ω,α}
                            Rtm∆Init←{
                                          _←'w_new'
                                                                □NA'P ',ω,'|w_new
                                                                                                                  <C[]'
                                           _←'w_close'□NA'I ',ω,'|w_close P'
                                                                                                                                             Р'
                                            ←'w_del'
                                                                 □NA
                                                                                                       ω, '|w_del
                                           _←'w_img'
                                                                                                                                             <PP F
                                                                □NA
                                                                                                       ω, '|w_img
                                           _←'w_plot' □NA
                                                                                                       ω, '|w_plot
                                                                                                                               <PP P'
                                          _←'w_hist' □NA
                                                                                                       \omega, '|w hist
                                                                                                                               <PP F8
                                                                                                                                              F8 F
                                          _←'loadimg'□NA
                                                                                                       ω, '|loadimg >PP <C[] I'
                                          _←'saveimg'□NA
                                                                                                       ω, '|saveimg <PP <C[]'
                                          _←'exa'
                                                                              Пиа
                                                                                                                     ω, '|exarray >PP P'
                                                                              □NA'P ',ω,'|mkarray <PP'
                                            ←'mka'
                                        _←'FREA'
                                                                           □NA
                                                                                                               ω, '|frea
                                           ←'Sync'
                                                                               ΠNA
                                                                                                                     ω, '|cd_sync'
                                          0 0 ρ θ}
                             \begin{array}{l} \mathsf{mkna} + \{\alpha, ' \mid ', ('\Delta' \square R' \_ ' \vdash \omega), ' \_ \mathsf{cdf} \ P \ P \ P' \} \\ \mathsf{mkf} + \{\mathsf{fn} + \alpha, ' \mid ', ('\Delta' \square R' \_ ' \vdash \omega), ' \_ \mathsf{dwa} \ ' \diamond \ \mathsf{mon} \ \mathsf{dya} + \omega \circ, "' \_ \mathsf{mon}' \ ' \_ \mathsf{dya}' \\ \mathsf{z} + ('\mathsf{Z} + \{\mathsf{A}\}', \omega, ' \ \mathsf{W}') (' : \mathsf{If} \ \mathsf{O} = \square \mathsf{NC}' \ ' \underline{\Delta}.', \mathsf{mon}, ' ' ' ') \\ \end{array} 
                                 z, \leftarrow (mon dya\{'''', \alpha, ''' \underline{\Delta}.\squareNA''', fn, \omega, ' \precPP'''\}"'>PP P' '>PP \precPP'), \subset ': E
                                z,':If O=□NC''A'''('Z←<u>∆</u>.',mon,' O O W')':Else'('Z←<u>∆</u>.',dya,' O A W')':
                           ns+#.\squareNS\Theta ♦ _+'\Delta\Delta'ns.\squareNS^{\sim}\Theta ♦ \Delta \Delta+ns.(\Delta \Delta) ♦ \Delta.names+(0pc''),(2=1\neg\alpha)\neq0=
                        fns÷'Rtm∆Init' 'MKA' 'EXA' 'Display' 'LoadImage' 'SaveImage' 'Image' 'Plot
                            fns, + 'Histogram' 'soext' 'opsys' 'mkna'
                            _←Δ.□FX∘□CR¨fns ◊ Δ.(decls←ω∘mkna¨names) ◊ _←ns.□FX¨(c''),ω∘mkf¨Δ.name
                       _←Δ.□FX'Z←Init'('Z←RtmΔInit ''',ω,'''')'→0/~0=≠names' 'names ##.Δ.□NA¨dec
                            ns}
```

This code is used in chunk 5. Uses PP 41a and SIGNAL 19b.

# 6 Co-dfns Runtime

37b  $\langle Implementation \ of \ APL \ Primitives \ 37b \rangle \equiv$  A TBW

Root chunk (not used in this document).

```
38a (C Runtime Support 38a)≡
/* TBW */
Root chunk (not used in this document).

38b (C Runtime Header 38b)≡
/* TBW */
Root chunk (not used in this document).
```

# 7 Utilities

### 7.1 Must haves

There are some APL functions that are so critical as to be worthy of primitive status.

- Indexing
- Under
- Assert

```
38c (Must Have APL Utilities 38c)≡

I+{(⊂ω) □α}

U+{α++ ◊ ωω*-1+α ααὂωω ω}

assert+{α+'assertion failure' ◊ 0∈ω: ½'α □SIGNAL 8' ◊ shy+0}

This code is used in chunk 5.

Defines:
 assert, used in chunk 23.

Uses SIGNAL 19b.
```

## 7.2 AST Pretty-printing

```
39
                                                                                                                              \langle Pretty-printing\ AST\ trees\ 39 \rangle \equiv
                                                                                                                                                                         \texttt{dct} \leftarrow \{\alpha \big[ (2 \times 2 \neq /n\,, 0) + (1 \uparrow \stackrel{\sim}{\neq} m) + m + n \leftarrow \varphi \lor \backslash \varphi m \leftarrow '  \  \, ' \neq \alpha \alpha \  \, \omega \big] \omega \omega \  \, \omega \}
                                                                                                                                                                       \begin{array}{l} {\rm dlk} \leftarrow \{((x[]\rho\omega)^{\dagger}[x\leftarrow2]|1+\omega\omega]\alpha), [\omega\omega]\alpha\alpha@(=0\ 0) \\ \div ((x[]\rho\omega)^{\dagger}[x\leftarrow2]|1+\omega\omega]\alpha), [\omega\omega]\alpha\alpha, [\omega]\alpha), [\omega\omega]\alpha\alpha, [\omega\omega]\alpha), [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha), [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha), [\omega\omega]\alpha, [\omega\omega]\alpha), [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha), [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha), [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha, [\omega\omega]\alpha,
                                                                                                                                                                      \mathsf{lyr} + \{\mathsf{i} \leftarrow \underline{\mathsf{i}} \alpha = \mathsf{d} \; \diamond \; \mathsf{k} \; \mathsf{v} \leftarrow \mathsf{i} \land \mathsf{u} \omega [\mathsf{i}], \circ \subset \mathsf{H} \mathsf{i} \; \diamond \; (\omega \circ \{\alpha[\omega]\} \ \ \ \ \mathsf{v}) \alpha \alpha \ \ \ \mathsf{u} \wedge \mathsf
                                                                                                                                                                                                                                                                                                                                                                          (\omega=\iota\neq\omega)\neq \neg\alpha\alpha \ \text{lyr}\neq (1+\iota\lceil/d), \neg \circ, \neg \circ, \neg \circ \text{"lbl}
                                                                                                                                                                            lb3+{a+ı≢⊃w
                                                                                                                                                                                                                                                                                                                                                                             ΄'(',"')',"~{α,';',ω}/τ"(ΝΔ{α[ω]}@2⊢(2⊃ω){α[|ω]}@{0>ω}@4↑⊃ω)[α;]}
                                                                                                                              This code is used in chunk 5.
                                                                                                                              Defines:
                                                                                                                                                                   dct, never used.
                                                                                                                                                                      dlk, never used.
                                                                                                                                                                      dwh, never used.
                                                                                                                                                                      dwv, never used.
                                                                                                                                                                      lb3, never used.
                                                                                                                                                                      pp3, never used.
```

### 7.3 Debugging utilities

The following utilities help to improve quality of life when working with the Co-dfns source code.

The DISPLAY function is taken from https://dfns.dyalog.com and helps to make debugging easier by allowing us to thread DISPLAY calls into expressions. I prefer to do something like this:

```
... \{\omega \neg \Box \leftarrow \#.DISPLAY \omega\} ...
```

{

cursively box arrays:

The function itself returns the character rendering of the code, so the above little expression is one that I use to insert and do debugging within an expression.

```
⟨DISPLAY Utility 40⟩≡
40
          DISPLAY+{□IO □ML+0
                                                                                                                           А Вс
          play of array.
                   α+1 ♦ chars+α>'..'''|-' '□□|-'
                                                                                              A α: O-clunky, 1-smooth
                  tl tr bl br vt hz←chars
                                                                                                                 A Top left
                  box←{
                          vrt hrz←(-1+ρω)ρ"vt hz
                                                                                                                  A Vert. ar
                            top \leftarrow (hz, '\theta \rightarrow ')[^{-1}\uparrow \alpha], hrz
                                                                                                                           A Up
          per border with axis.
                          bot \leftarrow (\neg \alpha), hrz
          der with type.
                          rgt←tr,vt,vrt,br
                          lax+(vt, '\phi\downarrow')[-1\downarrow1\downarrow\alpha], "cvrt
                                                                                                        A Left side(s) wi
                          lft←\tl,(↑lax),bl
                          lft,(top,\omega,bot),rgt
                      }
                    deco \leftarrow \{\alpha \leftarrow type \text{ open } \omega \diamond \alpha, axes \omega\}
                                                                                                 A Type and axes vector
                   axes←\{(-2\lceil \rho\rho\omega)\uparrow 1+\times\rho\omega\}
                                                                                                                           A Ar
          ray axis types.
                  open\leftarrow{(1[ρω)ρω}
          pose null axes.
                   trim\leftarrow \{(\sim 1 \ 1 \le \wedge \ne \omega = ' ')/\omega\}
                                                                                                                           A Re
          move extra blank cols.
                   type←{{(1=ρω)⊃'+'ω}∪,char"ω}
                                                                                                     A Simple array type
                      char←{θ≡ρω:hz ◊ (⊃ωε'¯',□D)⊃'#~'}∘₹
                                                                                          A Simple scalar type.
                      line\{(6 \neq 10 | \Box DR' '\omega) \Rightarrow '-'\}
                                                                                                                          A ur
          derline for atom.
```

A Simple scalar

```
0=\equiv\omega: '; (open \square FMT \omega); line \omega
                             1 \Theta \equiv (\equiv \omega)(\rho \omega): '\nabla' 0 0 box \square FMT \omega
                                                                                                   A Object rep: □OR
                                 1=\equiv\omega:(\text{deco }\omega)\text{box open }\square\text{FMT open }\omega
                                                                                                   A Simple array.
                                 ('ε'deco ω)box trim □FMT ∇"open ω
                                                                                                 A Nested array.
                      }ω
        Root chunk (not used in this document).
        Defines:
          DISPLAY, used in chunk 41.
        Uses □IO 8a and □ML 8a.
           I also define a function PP that encapsulates the above usage pat-
        tern that I like to use, making the whole thing less verbose and a little
        more convenient.
        ⟨PP Utility 41a⟩≡
41a
          PP \leftarrow \{\omega \dashv \Box \leftarrow \#.DISPLAY \omega\}
        Root chunk (not used in this document).
        Defines:
          PP, used in chunks 37a and 41b.
        Uses DISPLAY 40.
            Both of these function exist outside of the codfns namespace and
        so they get their own files inside of the src\ directory.
        \langle Tangle\ Commands\ 6 \rangle + \equiv
41b
          echo "Tangling src/DISPLAY.aplf..."
          notangle -R'[[DISPLAY]] Utility' codfns.nw > src/DISPLAY.aplf
          echo "Tangling src/PP.aplf..."
          notangle -R'[[PP]] Utility' codfns.nw > src/PP.aplf
        This code is used in chunk 43.
        Defines:
          DISPLAY.aplf, never used.
          PP.aplf, never used.
        Uses codfns 5, DISPLAY 40, PP 4la, and src 48.
```

### 7.4 Reading and Writing Files

It is helpful to be able to easily write files to disk, and the following put and tie utilities help us to do so when we want to. These are pretty standard, but they could maybe be replaced by <code>INPUT</code> or something like that.

```
42a ⟨Basic tie and put utilities 42a⟩≡

tie+{

0::□SIGNAL □EN

22::ω□NCREATE 0

0□NRESIZE ω□NTIE 0

}

put+{

s+(-128+256|128+'UTF-8'□UCS ω)□NAPPEND(t+tie α)83

1:r+s+□NUNTIE t

}

This code is used in chunk 47b.

Defines:

put, used in chunks 36, 47b, and 48.

tie, used in chunks 36 and 47b.

Uses SIGNAL 19b.
```

### 7.5 XML Rendering

# 7.6 Detecting the Operating System

It is quite helpful to be able to easily detect the operating system that we are on. This turns out to be helpful in more areas than just the compiler.

```
42c (The opsys utility 42c)≡
opsys←{ω¬~'Win' 'Lin' 'Mac'ι⊂3↑¬'.'□WG'APLVersion'}
This code is used in chunks 36, 44c, and 46d.
Defines:
opsys, used in chunks 44c and 46d.
```

# 8 Developer Infrastructure

### 8.1 Building the Compiler

The Co-dfns compiler is written, developed, and distributed as a literate program. For more information about literate programming, see the resources available at http://literateprogramming.com/. We use noweb as our preferred literate programming tool because it is eminently simple, while still handling the majority of our needs and producing high quality output in LATEX format with all the important elements of literate programming, including live hyperlinking and cross-references.

### 8.1.1 Tangling the Source

The process of tangling produces the executable source code for the compiler. Importantly, the tangled output is *not* meant to be used as the primary means of reading or debugging the source. Instead, it is meant primarily as the machine readable version of the code only.

With noweb, we need to invoke notangle once for each of the chunks that we wish to use to produce an output file. To make this easy, we build up a script to do this work for us.

For Linux and Mac, the following bash script creates these files. We use a separate chunk that we build up incrementally throughout the rest of this document as a record of all the chunks that we should create. Notice that we explicitly tangle the TANGLE.sh file as the last thing that we do; this helps to ensure that we are reliably executing the rest of the script before changing the contents of the file, as some systems will be affected and change execution behavior in strange ways if we change the TANGLE.sh file early on in the execution of the file.

```
43 ⟨TANGLE.sh 43⟩≡
#!/bin/bash

⟨Tangle Commands 6⟩

echo "Tangling TANGLE.sh..."
notangle -R'[[TANGLE.sh]]' codfns.nw > TANGLE.sh
Root chunk (not used in this document).
Defines:
TANGLE.sh, used in chunk 44a.
Uses codfns 5 and TANGLE 44c.
```

On Windows, the best way that we have found to do this is by installing noweb using the Cygwin project and then calling TANGLE.sh from a local TANGLE.bat file. This document assumes that you have already successfully built and installed via Cygwin a working Icondriven noweb installation.

Users who prefer to work in a UNIX fashion via Cygwin or some other subsystem on Windows can follow the build scripts directly. For developers who prefer to work in a primarily Windows environment, the following TANGLE.bat build script assists in handling the calls into Cygwin so that you do not need to have a Cygwin terminal open all the time.

When tangled to the TANGLE.aplf file, the following script enables the user to simply type TANGLE within a Dyalog APL session to update the code tree from within Dyalog itself. This is much more convenient than keeping a Cygwin Terminal session open along with a Dyalog APL session while programming.

Note: this command expects to be run from within the root of the repository, not from, say, within the testing directory.

```
⟨TANGLE 44c⟩≡
44c
          TANGLE; opsys
          (The opsys utility 42c)
          ☐CMD opsys '.\TANGLE.bat' './TANGLE.sh' './TANGLE.sh'
        Root chunk (not used in this document).
        Defines:
          TANGLE, used in chunks 43 and 44.
        Uses opsys 42c.
        \langle Tangle\ Commands\ 6 \rangle + \equiv
44d
          echo "Tangling TANGLE.aplf..."
          notangle -R'[[TANGLE]]' codfns.nw > src/TANGLE.aplf
        This code is used in chunk 43.
        Defines:
          TANGLE.aplf, never used.
        Uses codfns 5, src 48, and TANGLE 44c.
```

#### 8.1.2 Weaving the Source

Weaving is the process by which we produce the final printed output of this document, intended for reading and general human consumption. We rely on the LATEX typesetting system to do this. Moreover, because we make heavy use of UTF-8 and prefer to have our own fonts installed and used, it is necessary to use the xelatex system instead of the typical LATEX engine. In order to get the indexing right, we must run the engine twice. The first run will update the indexing files that will be picked up on the second run and incorporated into the final document. Note, we have tried to use the lualatex engine, which in theory should work just as well as the xelatex engine, but we get a strange error relating to noweb's style file, so we stick with xelatex for now.

Running this script also depends on having the appropriate fonts installed. In this case, please ensure that the following fonts are installed in your Windows font system so that they can be picked up by the TFX engine.

- Libre Baskerville (Regular, Italic, Bold)
- APL385 Unicode
- Lucida Sans Unicode
- Cambria Math

If you do not wish to use these fonts, then see the top of the codfns.nw file and edit the font specifications to the fonts that you do wish to use.

Note the use of -delay -index for options. We want to generate indexing, but we also need to make sure that we can use some of our own packages in the system,

Note: this command expects to be run from within the root of the repository, not from, say, within the testing directory.

```
45  (WEAVE.sh 45)≡
    #!/bin/bash
    mkdir -p woven
    noweave -delay -index codfns.nw > woven/codfns.tex
    cd woven
    xelatex codfns
    xelatex codfns
Root chunk (not used in this document).
Defines:
    WEAVE.sh, used in chunk 46.
Uses codfns 5.
```

```
\langle Tangle\ Commands\ 6 \rangle + \equiv
46a
          echo "Tangling WEAVE.sh..."
          notangle -R'[[WEAVE.sh]]' codfns.nw > WEAVE.sh
        This code is used in chunk 43.
        Uses codfns 5, WEAVE 46d, and WEAVE.sh 45.
        And just like the tangling code, we want to define a TANGLE.bat batch
        file to call the Cygwin environment from Windows.
46b
        \langle WEAVE.bat 46b \rangle \equiv
          set SH=C:\cygwin64\bin\bash.exe -l -c
          %SH% "cd $OLDPWD && ./WEAVE.sh"
        Root chunk (not used in this document).
        Defines:
          WEAVE.bat, used in chunk 46c.
        Uses WEAVE 46d and WEAVE. sh 45.
        \langle Tangle\ Commands\ 6 \rangle + \equiv
46c
          echo "Tangling WEAVE.bat..."
          notangle -R'[[WEAVE.bat]]' codfns.nw > WEAVE.bat
        This code is used in chunk 43.
        Uses codfns 5, WEAVE 46d, and WEAVE.bat 46b.
           Like the (TANGLE Command (never defined)), the following command,
        when tangled to the WEAVE.aplf file enables weaving in a the Dyalog
        APL session by executing the WEAVE command.
        \langle \text{WEAVE 46d} \rangle \equiv
46d
          WEAVE; opsys
          (The opsys utility 42c)
          □CMD opsys '.\WEAVE.bat' './WEAVE.sh' './WEAVE.sh'
        Root chunk (not used in this document).
        Defines:
          WEAVE, used in chunk 46.
        Uses opsys 42c.
        \langle Tangle\ Commands\ 6 \rangle + \equiv
46e
          echo "Tangling src/WEAVE.aplf..."
          notangle -R'[[WEAVE]]' codfns.nw > src/WEAVE.aplf
        This code is used in chunk 43.
        Defines:
          WEAVE.aplf, never used.
        Uses codfns 5, src 48, and WEAVE 46d.
```

### 8.2 Building the Runtime

One of our goals with the Co-dfns runtime is to write as much of it as possible in APL. This means that we want to have at minimum a very small kernel that has been written in C, while most of the rest of the code is implemented in some APL files. This leads to a three part breakdown of the process to build the runtime.

```
47a ⟨Build the runtime 47a⟩≡
⟨Compile the primitives in prim.apln 48⟩
⟨Build codfns.dll DLL 49a⟩
⟨Copy the runtime files into tests\ 49b⟩
This code is used in chunk 47b.
```

We define the command MKARTM to build the runtime. This command takes a path to the root directory of the Co-dfns repository; this is to allow us to rebuild the runtime from anywhere in the system if we so choose.

```
47b (MKΔRTM 47b)≡
MKΔRTM path; put; tie; src; vsbat; vsc; wsd

⟨Basic tie and put utilities 42a⟩
⟨Build the runtime 47a⟩
Root chunk (not used in this document).
Defines:
MKΔRTM, used in chunk 47c.
Uses put 42a, src 48, tie 42a, vsbat 49a, vsc 49a, and wsd 49a.
```

This file is another of our external utilities that exists outside of the codfns namespace, so it gets its own file in src\.

```
47c (Tangle Commands 6)+=
echo "Tangling src/MKΔRTM.aplf..."
notangle -R'[[MKΔRTM]]' codfns.nw > src/MKΔRTM.aplf
This code is used in chunk 43.
Defines:
MKΔRTM.aplf, never used.
Uses codfns 5, MKΔRTM 47b, and src 48.
```

The first step we must take is producing an appropriate C file that contains the primitives that we have defined in primapln. This means that we want to only compile the code in primapln as far as producing the C code. Since we do not have a full blown runtime yet, we will be compiling the primac file along with the rest of the runtime code, instead of the normal build process, which assumes that we already have a working runtime. This means that we only invoke the GC TT PS passes of the compiler pipeline, while avoiding the CC pass. We use the SALT system to load the source from primapln and then run the compiler passes that we want before storing the resulting code in the rtm\primac file.

48 (Compile the primitives in prim.apln 48)≡
src+□SRC □SE.SALT.Load path, '\rtm\prim.apln'
(path, '\rtm\prim.c') put codfns.{GC TT PS ω}src
This code is used in chunk 47a.
Defines:
src, used in chunks 6, 11, 14b, 30, 41b, 44d, 46, and 47.
Uses codfns 5, PS 15, and put 42a.

Once we have the rtm\prim.c file written appropriately, we can run the main compiler process. For simplicity, we just compile all of the .c files that are found in the rtm\ subdirectory. We must ensure that we are appropriatelly invoking our ArrayFire dependencies as well as producing the appropriate debugging symbols most of the time.

```
\langle Build \text{ codfns.dll } DLL \text{ 49a} \rangle \equiv
49a
         vsbat←#.codfns.VS∆PATH
         vsbat, '\VC\Auxiliary\Build\vcvarsall.bat'
        wsd←path, '\'
         vsc←'%comspec% /C ""',vsbat,'" amd64'
                  && cd "', wsd, '\rtm"'
         vsc,←'
                  && cl /MP /W3 /wd4102 /wd4275'
         vsc,←'
                    /Od /Zc:inline /Zi /FS'
         vsc,←'
                    /Fo".\\" /Fd"codfns.pdb"'
         vsc,←'
                    /WX /MD /EHsc /nologo'
         vsc,←'
                   /I"%AF_PATH%\include"'
                    /D"NOMINMAX" /D"AF_DEBUG" /D"EXPORTING" '
         vsc,←'
                    "*.c" /link /DLL /OPT:REF'
         vsc,←'
                    /INCREMENTAL:NO /SUBSYSTEM:WINDOWS'
         vsc,←'
         vsc,←'
                    /LIBPATH: "%AF PATH%\lib" '
         vsc,←'
                    /DYNAMICBASE "af',codfns.AFΔLIB,'.lib"'
         vsc,←'
                    /OPT:ICF /ERRORREPORT:PROMPT'
         vsc,←'
                    /TLBID:1 /OUT: "codfns.dll"" '
       This code is used in chunk 47a.
       Defines:
        vsbat, used in chunks 36 and 47b.
         vsc, used in chunks 36, 47b, and 49b.
        wsd, used in chunks 47b and 49b.
       Uses AFALIB 9, codfns 5, and VSAPATH 10.
```

Finally, in order to write up the test harness to work right, we must copy the appropriate runtime files into the tests\ directory so that we can find them when we finally start running our code there.

```
49b (Copy the runtime files into tests\ 49b)≡

□CMD □←'copy "',wsd,'rtm\codfns.h" "',wsd,'tests\"'
□CMD □←'copy "',wsd,'rtm\codfns.exp" "',wsd,'tests\"'
□CMD □←'copy "',wsd,'rtm\codfns.lib" "',wsd,'tests\"'
□CMD □←'copy "',wsd,'rtm\codfns.pdb" "',wsd,'tests\"'
□CMD □←'copy "',wsd,'rtm\codfns.dll" "',wsd,'tests\"'
This code is used in chunk 47a.
Uses codfns 5, vsc 49a, and wsd 49a.
```

### 8.3 Loading the Compiler

In order to load the compiler into an APL session as well as all the development utilities, we assume that you have first managed to either load up a session with a bootstrapped version of the TANGLE command or that you already have a tangled <code>src\</code> directory. If the <code>src\</code> directory has not yet been created by running the TANGLE command, then this must be done before loading the compiler system. After tangling, the compiler can be loaded using the provided <code>LOAD</code> shortcut. This shortcut is meant to use the Dyalog Link system for hotloading the files in <code>src\</code> into the root namespace. We do so through the following link command:

Link.Create # src -source=dir -watch=dir

This means that we want to link the <code>src\</code> directory into the <code>#</code> namespace, but we also want to make sure that we only pull changes that come from the filesystem. This is because we are editing the code via the WEB document, and we do not want to risk having some intermediate representation that isn't accurate and that doesn't flow the right way; we want all appropriate changes to begin in the WEB document and then, and only then, flow into the session. This also allows us to make some modifications to the code for testing and experimentation inside of the session without consideration for the code outside of the session, and such changes will be removed or forgotten on the next TANGLE command.

To set this up, we also ensure that we begin our work within the root Co-dfns repository directory, as this is where we expect to run the TANGLE and WEAVE commands.

There is unfortunately only a limited range of possibilities for linking in a new directory as we wish to do. The method we choose to use is launching a fresh Dyalog APL session and then using an LX expression from the command line to do the actual linking using the DSE.UCMD functionality. I personally find this to be rather hackish, and I hope that an alternative approach to doing this will show up in the near future. Nonetheless, the arguments that we pass to dyalog.exe look something like this:

LX="DSE.UCMD'Link.Create # src -source=dir -watch=dir'"

If you do not use the LOAD shortcut, you can use the above command to do the linking manually.

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### 9.1 Chunks

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