

1. Let $y(t)$ be a band-limited signal to $W = 1$ kHz, signal $y(t)$ is sampled at a rate 30% higher than the Nyquist rate to provide a guard band.
 - 1) What is the sample rate for $y(t)$?
 - 2) Please use diagrams to explain what aliasing is and why in general sampling has to meet the Nyquist sampling theorem.
 - 3) Please use diagrams to explain why the oversampling is easier to design a simple filter.
2. The maximum acceptable error for signal $x(t)$ in the sample amplitude (the maximum quantization error) is 1% of the peak-to-peak voltage, where $x(t)$ is with amplitude $0 \leq x(t) \leq 2$.
 - 1) How many quantization levels are required? How many bits per sample are required?
 - 2) Assuming the sampling rate of this system is 8kHz, what is the maximum bit rate (digital bandwidth) of this system?
 - 3) Calculated the bit rate required to transmit $x(t)$ as a linearly quantised PCM signal maintaining an SQNR of 55 dB. (Assume that the signal's peak to mean ratio is 20dB).
3. If $x(t)$ is quantised by a non-uniform quantiser Q and power $P = 100$. The quantiser Q is defined by the following four quantisation regions: $R_0 = [0,1]$, $R_1 = [1,3]$, $R_2 = [3, 7]$ and $R_3 = [7,15]$. Symbols a_i , $i = 1, 2, 3$ and 4, correspond to the amplitudes produced by each quantisation region R_i and the probabilities p_i that the amplitude of $x(t)$ is in each region R_i are as follows

p_0	p_1	p_2	p_3
0.17	0.49	0.25	0.09

- 1) What are the quantisation noise power in each region assuming that the noise is distributed uniformly, the average quantisation noise power, and the SQNR in dB.
 - 2) Obtain the information content of each symbol and entropy of the information source under the probabilities in 1).
4. Consider a source having an $M=4$ symbol alphabet where $P(x_1) = 1/2$; $P(x_2) = 1/4$ $P(x_3) = P(x_4) = 1/8$ and symbols are statistically independent.
 - 1) Calculate the information conveyed by the receipt of the symbol x_1, x_2, x_3 . and x_4 .
 - 2) What is the source entropy and the redundancy?