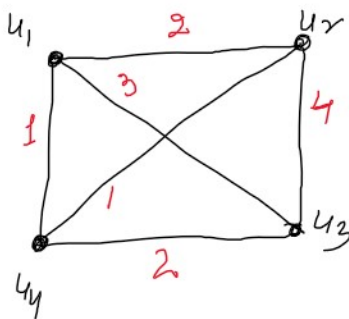


The no. of spanning tree of  $K_n$  is  $n^{n-2}$  ✓

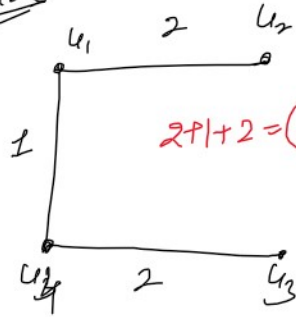
$$\begin{aligned} K_4 & 4^{4-2} = 4^2 = 16 \\ K_5 & 5^{5-2} = 5^3 = 125 \\ K_3 & 3^{3-2} = 3^1 = 3 \end{aligned}$$

\* Minimum Spanning Tree :→ A minimum spanning tree in a connected weighted graph is a spanning tree that has the smallest possible sum of weights of its edges.

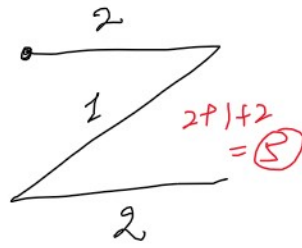


Spanning Tree

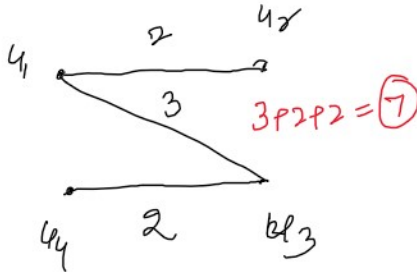
①



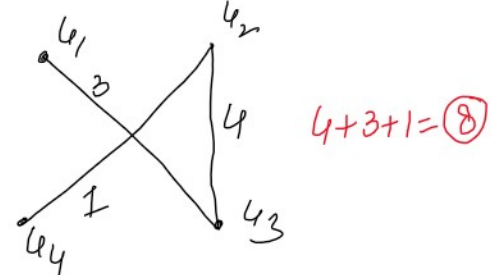
②



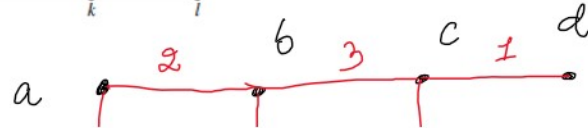
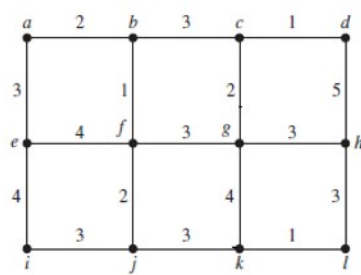
③



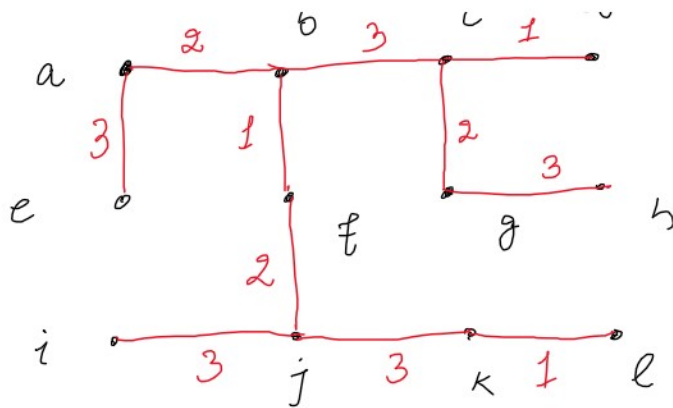
④



Kruskal Algorithm



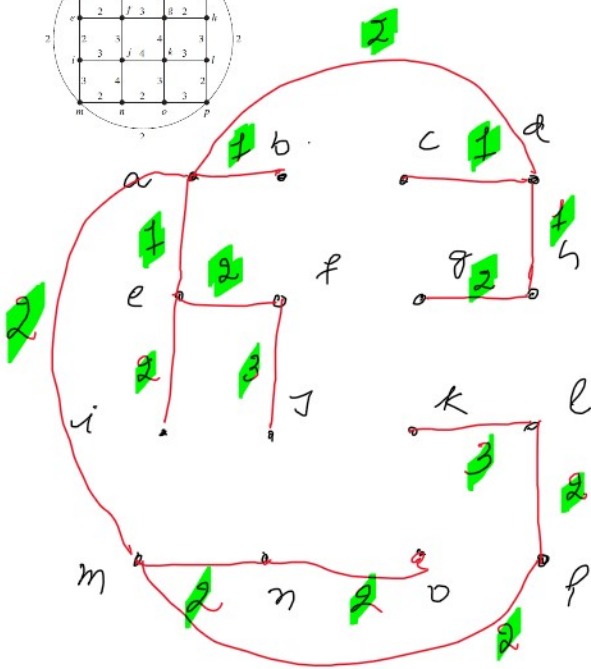
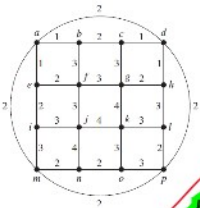
Weight	Edges	Weight	Edges
1	<a-d> ✓	5	<h-i>
1	<b-f> ✓		
1	<k-l> ✓		
2	<a-b> ✓		
2	<c-g> ✓		
2	<f-j> ✓		
3	<b-c> ✓		
3	<a-e> ✓		
3	<f-a> X Not added		



3	<a-e>	✓
3	<f-g>	✗ Not added
3	<g-h>	✓
3	<i-j>	✓
3	<j-k>	✓
<hr/>		
3	<h-l>	
4	<e-f>	
4	<e-i>	
4	<g-k>	

Height of

Minimum Spanning Tree =  $3 + 2 + 3 + 1 + 1 + 2 + 3 + 2 + 3 + 3 + 1$   
 $= 24$

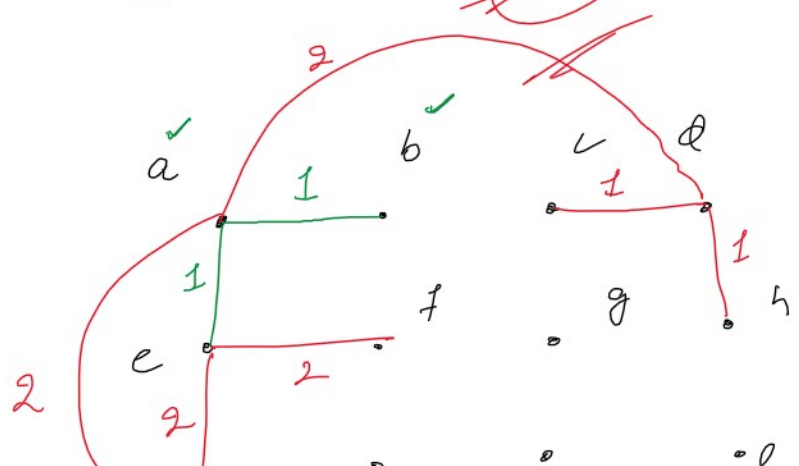
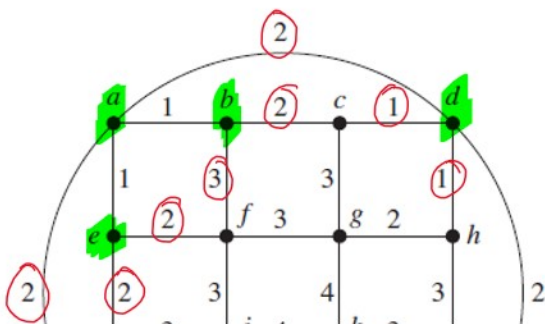


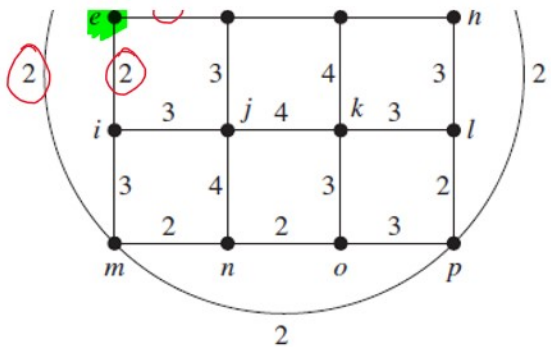
Height	Edges	
1	a-b	✓
1	c-d	✓
1	<d-h>	✓
1	<a-e>	✓
2	a-d	✓
2	<b-c>	✗
2	<e-f>	✓
2	<g-h>	✓
2	<e-l>	✓
2	<a-m>	✓
2	<m-n>	✓
2	<n-o>	✓
2	<e-p>	✓
2	<m-p>	✓
2	<p-d>	✗

Height	Edges	
3	<f-g>	✗
3	<e-g>	✗
3	<f-j>	✓
3	<i-j>	✗
3	<h-l>	✗
3	<k-l>	✓
3	<i-m>	
3	<k-o>	
3	<o-p>	
3	<b-f>	
4	<g-k>	
4	<j-k>	
4	<j-n>	

Height of Minimum Spanning Tree = 98

Prim's Algorithm





1

$\mathcal{J}$

$\mathcal{K}$

$\mathcal{L}$

$\mathcal{D}$

$\mathcal{D}$

$\mathcal{D}$

$\mathcal{L}$

$\mathcal{D}$

$\mathcal{P}$