

Shortest path

Weighted Graph \rightarrow A graph is s.t.b weighted Graph if a non negative no. (called the weight or length of the edge) is assigned to each and every edge of the graph

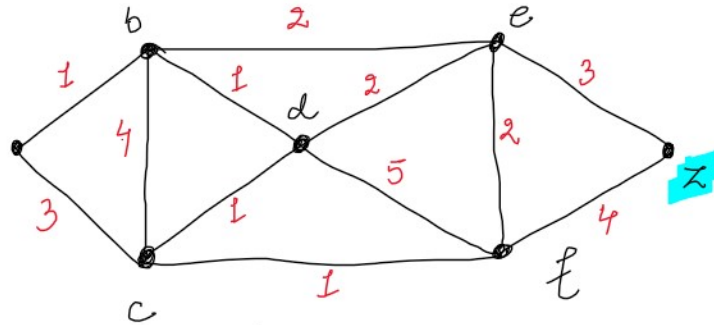
① $a \xrightarrow{1} b \xrightarrow{2} e \xrightarrow{3} z = ⑥$

② $a \xrightarrow{1} b \xrightarrow{4} c \xrightarrow{1} d \xrightarrow{2} e \xrightarrow{3} z = ⑪$

$a \xrightarrow{1} b \xrightarrow{1} d \xrightarrow{5} f \xrightarrow{4} z = ⑪$

$a \xrightarrow{3} c \xrightarrow{1} f \xrightarrow{4} z = ⑧$

$a \xrightarrow{1} b \xrightarrow{1} d \xrightarrow{5} f \xrightarrow{4} z = \dots$

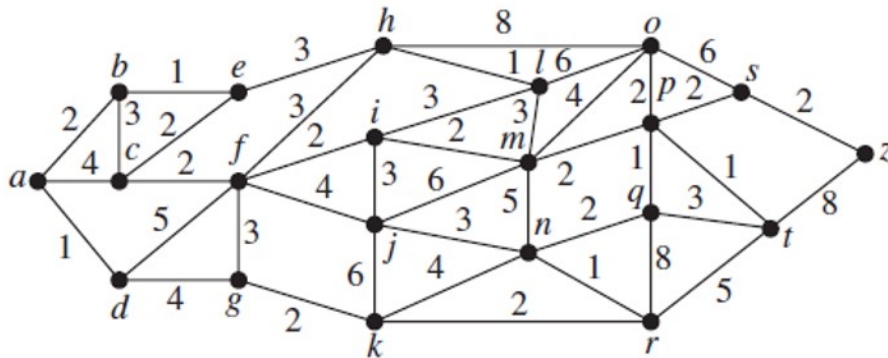


Length of the path \rightarrow

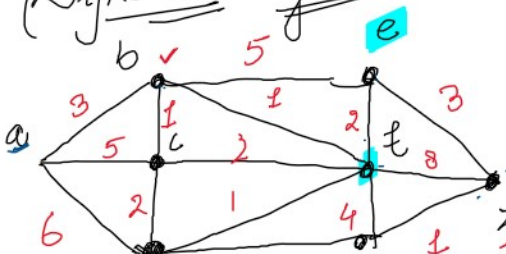
Sum of all the weights of the edges involve in that path.

Shortest path :-

the path with minimum length

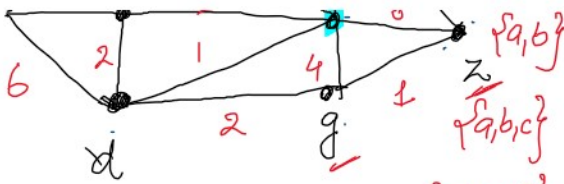


Dijkstra's Algorithm



Source vertex {a}

	b	c	d	e	f	g	z
Distance	3(a)	5(a)	6(a)	∞	∞	∞	∞
Previous	a	a	a				
Shortest path	a	a-b	a-b	a-b-e	a-b-e-f	a-b-e-f-g	a-b-e-f-g-z



$\{a, b\}$	-	$\boxed{4(a-b)}$	$6(a)$	$8(a-b)$	$4(a-b)$	∞	∞
$\{a, b, c\}$	-	-	$6(a)$	$8(a-b)$	$\boxed{4(a-b)}$	∞	∞
$\{a, b, c, f\}$	-	-	$\boxed{5(a-b-f)}$	$6(a-b-f)$	-	$8(a-b-f)$	$12(a-b-f)$
$\{a, b, c, f, d\}$	-	-	-	$\boxed{6(a-b-f)}$	-	$7(a-b-f-d)$	$12(a-b-f-d)$
$\{a, b, c, f, d, e\}$	-	-	-	-	-	$\boxed{7(a-b-f-d)}$	$9(a-b-f-d-e)$
$\{a, b, c, f, d, e, g\}$	-	-	-	-	-	-	-

$\boxed{8(a-b-f-d-g)}$

Shortest

$a-b-f-d-g-z$

length = 8