

upper and lower bound

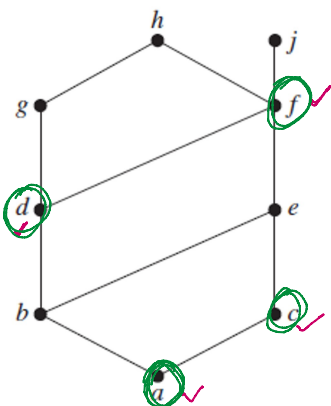
$R \leq$

Let A be the subset of the poset (S, R)

If u is the element of the set S such that aRu for all $a \in A$.
then u is called the upper bound of A .

If l is the element of the set S such that lRa for all $a \in A$.
then l is called the lower bound of A .

✓



Find the lower and upper bounds of the subsets $\{a, b, c\}$, $\{j, h\}$, and $\{a, c, d, f\}$ in the poset

① $A = \{a, b, c\}$

are $\left. \begin{matrix} aRe \\ bRe \\ cRe \end{matrix} \right\} \Rightarrow$

$\left. \begin{matrix} aRf \\ bRf \\ cRf \end{matrix} \right\} \Rightarrow fRj \\ fRh$

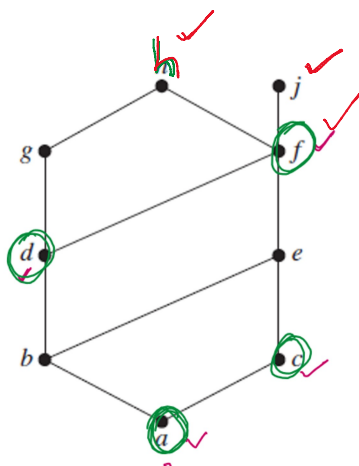
upper bounds of $\{a, b, c\} = e, f, j, h$

② $A = \{j, h\}$

no upper bound

⊗

③ $\{a, c, d, f\}$



$A = \{a, c, d, f\}$

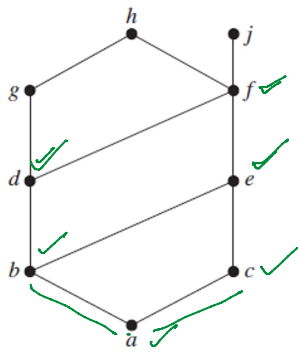
upper bound = $\{j, h, f\}$

$\left. \begin{matrix} aRx \\ cRx \\ dRx \\ fRx \end{matrix} \right\}$

$\left. \begin{matrix} aRj \\ cRj \\ dRj \\ fRj \end{matrix} \right\}$

aRf

$\left. \begin{matrix} aRf \\ cRf \\ dRf \\ fRf \end{matrix} \right\}$



$$\textcircled{1} \quad A = \{a, b, c\}$$

$$\text{Lower bond} = \{a\}$$

$$\begin{aligned} & \ell \not\sim a \\ & \ell \not\sim b \\ & \ell \not\sim c \end{aligned}$$

$$\textcircled{2} \quad A = \{j, h\}$$

$$\text{Lower bonds} = \{j, d, e, b, c, a\}$$