

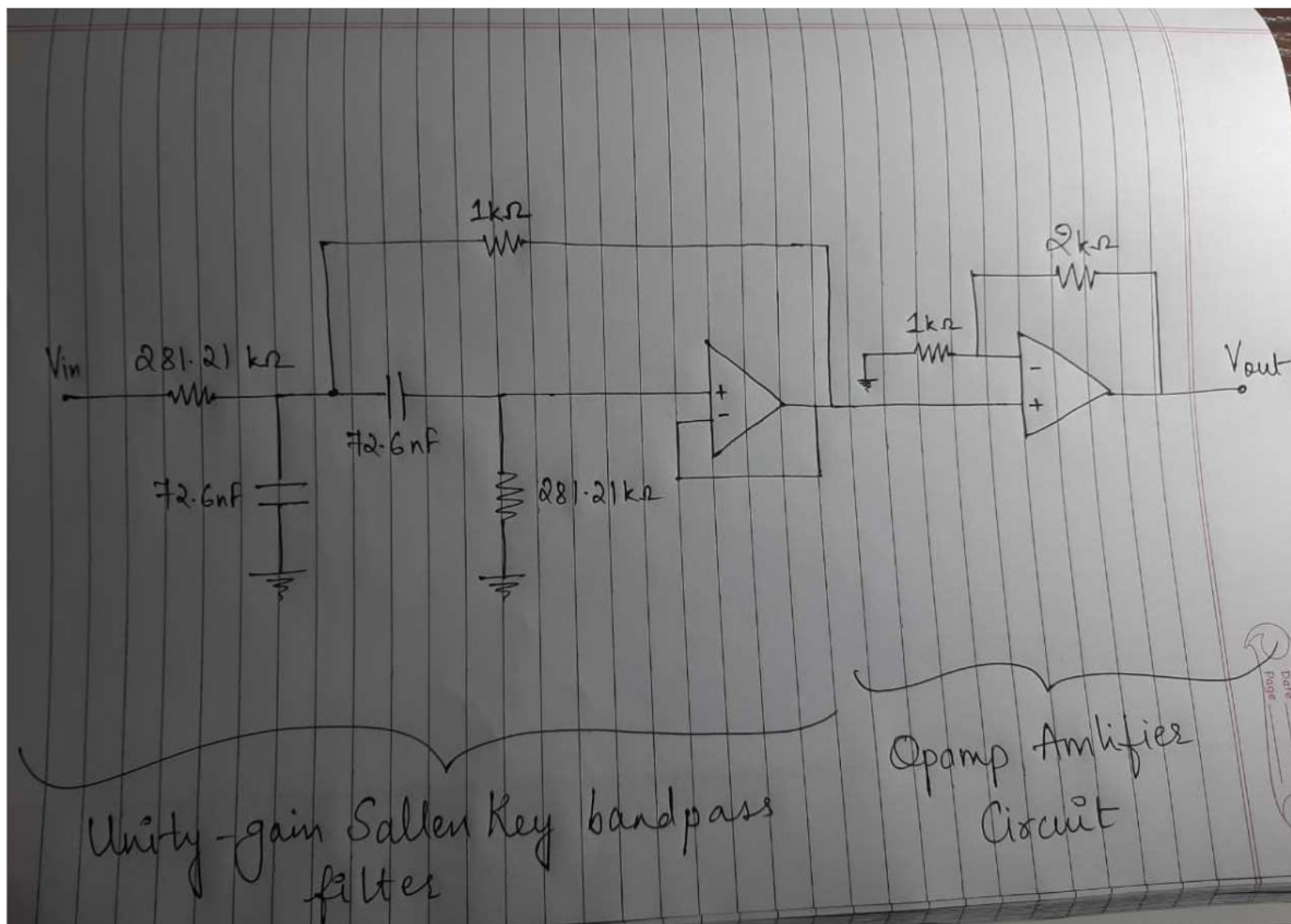
Name: JAHANVI AGRAWAL  
Roll No: IMT2019506  
Email: [Jahanvi.Agrawal@iiitb.org](mailto:Jahanvi.Agrawal@iiitb.org)

## BE-PROJECT: NARROW BAND AUDIO FILTER CIRCUIT

After studying, a few types of 2<sup>nd</sup> order bandpass filters, I concluded that Sallen-Key works the best as it's giving the best narrow-band response according to my frequency values.

I have used a **unity-gain Sallen Key topology** to create the required narrow-bandpass filter circuit. After this, in the Bode plot of this filter, at peak I didn't have  $V_{out}/V_{in}=1V$ . Thus, to solve this, I have used an **opamp amplifier** (non-inverting) circuit to amplify the final output voltage (because  $V_{out}/V_{in}$  at peak was less than 1V) so as to get  $V_{out}/V_{in}=1V$  at the peak.

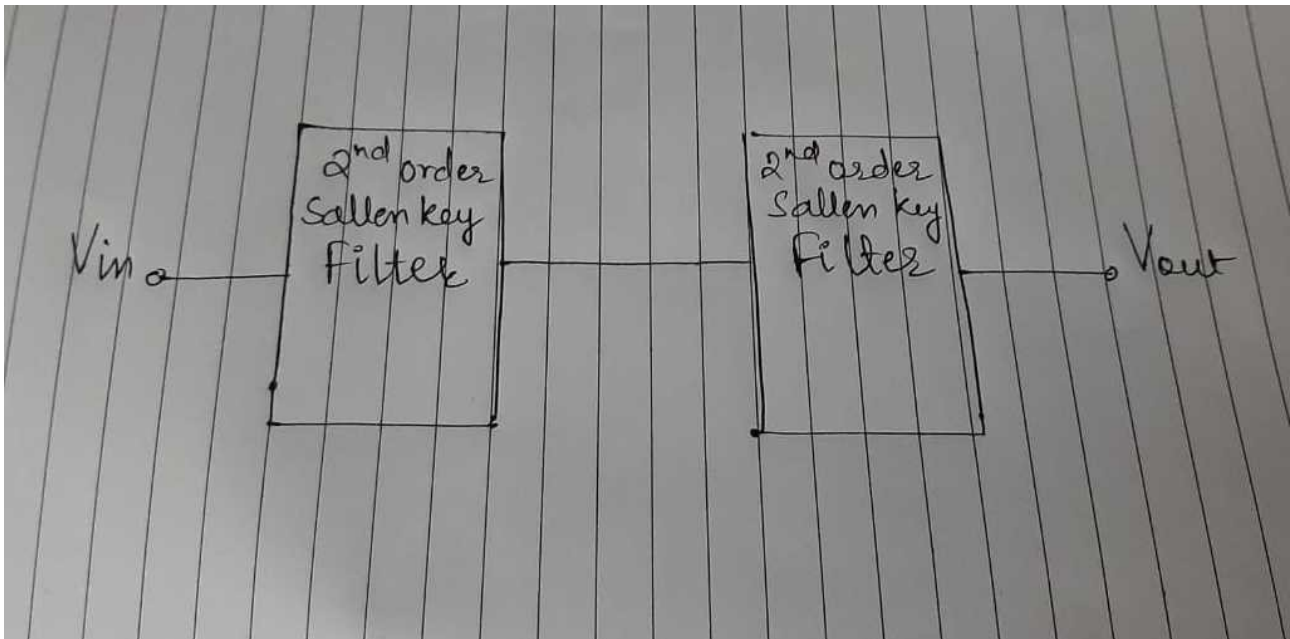
Below is the filter circuit with the component values.



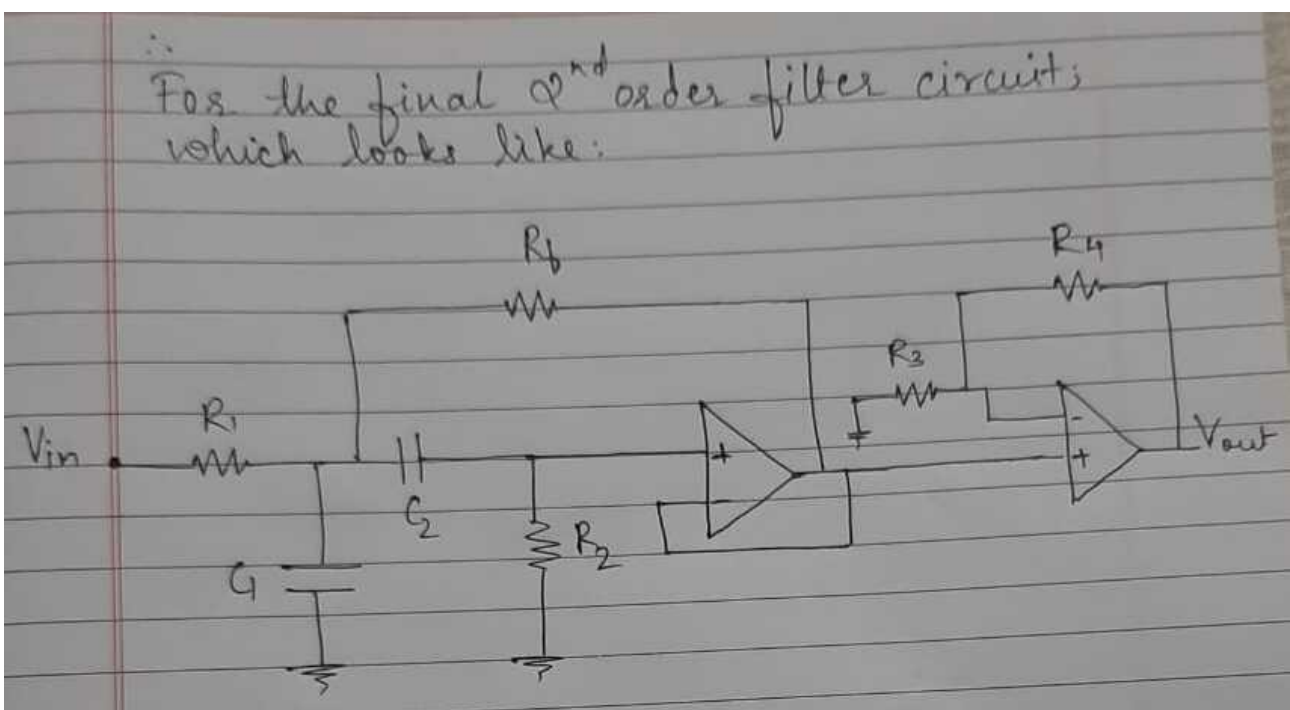
I plotted the Bode plot for the above circuit, I got the peak at  $f_4$  (as required) and amplitude of the output at  $f_5$  was less than 0.75V (as required) but the ratio of amplitudes at frequencies  $f_3$  and  $f_4$  (i.e.  $v_3/v_4$ ) was still greater than 0.75.

Thus to reduce it, I have cascaded the above 2<sup>nd</sup> order filter circuit with the same circuit again to get a final 4<sup>th</sup> order filter circuit to meet all the specifications ( $v_3 < 0.75V$ ,  $v_5 < 0.75V$  and peak of 1V at  $f_4$ ).

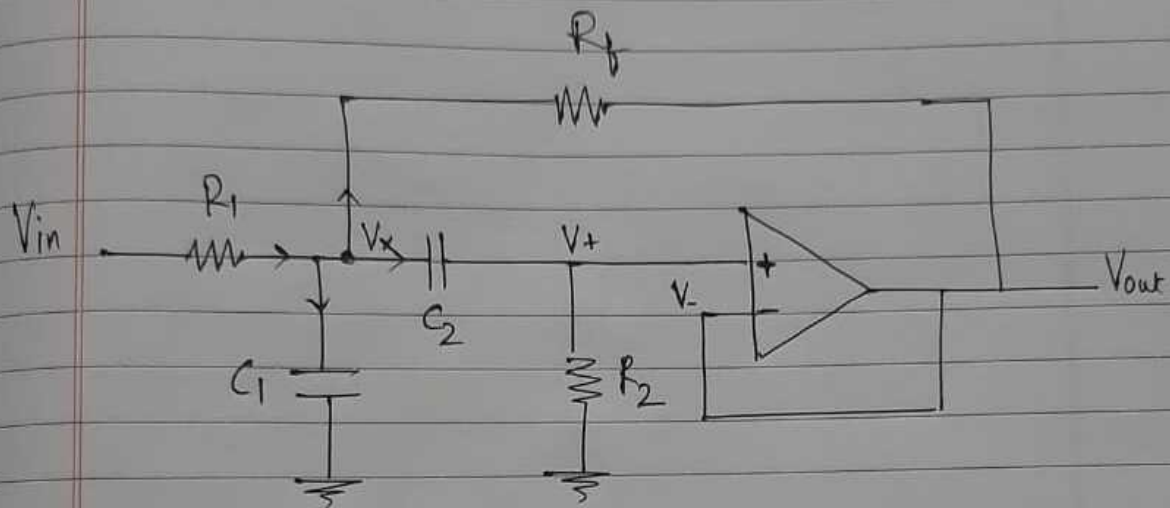
The block diagram of the final cascaded 4<sup>th</sup> order filter circuit:



### Transfer-Function Detailed Derivation:



## Transfer function for a unity-gain Sallen Key Bandpass Filter.



This is an ideal opamp

$$\therefore V_+ = V_- = V_{out} \quad \text{--- (1)}$$

Writing KCL at  $V_x$  node:

$$\boxed{\frac{V_{in} - V_x}{R_1} = \frac{V_x}{Z_{C_1}} + \frac{V_x - V_{out}}{R_f} + \frac{V_{out}}{R_2}} \quad \text{--- (2)}$$

$$\text{Here } Z_{C_1} = \frac{1}{j\omega C_1} = \frac{1}{s C_1}$$

$$[\because s = j\omega]$$

Applying KCL at  $V_+$  nodes

$$\frac{V_x - V_+}{Z_{C_2}} = \frac{V_+}{R_2}$$

[By eqn (1) ;  $V_+ = V_{out}$ ]

$\therefore$

$$\frac{V_x - V_{out}}{Z_{C_2}} = \frac{V_{out}}{R_2}$$

$$\therefore V_x = V_{out} \left( 1 + \frac{Z_{C_2}}{R_2} \right)$$

$$\left[ \text{And } Z_{C_2} = \frac{1}{j\omega C_2} = \frac{1}{sC_2} \right]$$

$$\therefore \left[ V_x = V_{out} \left( 1 + \frac{1}{sC_2 R_2} \right) \right] \text{ --- (3)}$$

Putting eqn (3) in eqn (2) ;

$$\frac{V_{in}}{R_1} = V_x \left( \frac{1}{R_1} + sC_1 + \frac{1}{R_f} \right) + V_{out} \left( \frac{1}{R_2} - \frac{1}{R_f} \right)$$

$$\frac{V_{in}}{R_1} = V_{out} \left( \frac{1}{R_1} + sC_1 + \frac{1}{R_f} + \frac{R_1 + R_f}{sC_2 R_2 R_1 R_f} + \frac{sC_1}{sC_2 R_2} \right) + V_{out} \left( \frac{1}{R_2} - \frac{1}{R_f} \right)$$



$$\frac{V_{in}}{R_1} = V_{out} \left( \frac{1}{R_1} + \frac{1}{R_2} + sC_1 + \frac{C_1}{C_2 R_2} + \frac{R_1 + R_f}{sC_2 R_1 R_2 R_f} \right)$$

Divide by  $C_1$ :

$$\frac{V_{in}}{C_1 R_1} = V_{out} \left( \frac{1}{C_1 R_1} + \frac{1}{C_1 R_2} + s + \frac{1}{C_2 R_2} + \frac{R_1 + R_f}{sC_1 C_2 R_1 R_2 R_f} \right)$$

Multiply by  $s$ :

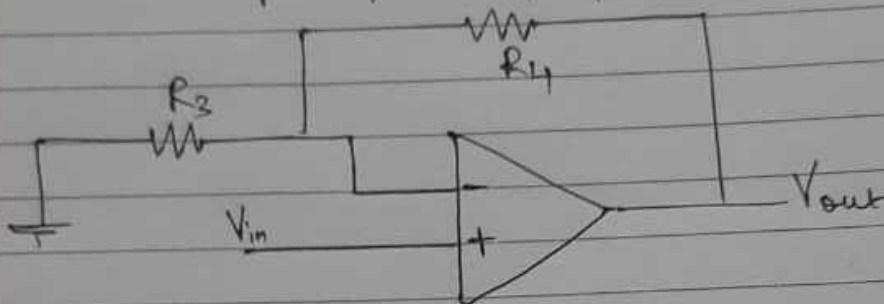
$$\frac{s V_{in}}{C_1 R_1} = V_{out} \left( s^2 + \left( \frac{1}{C_1 R_1} + \frac{1}{C_1 R_2} + \frac{1}{C_2 R_2} \right) s + \frac{R_1 + R_f}{C_1 C_2 R_1 R_2 R_f} \right)$$

$$\therefore \frac{V_{out}}{V_{in}} = \frac{s / C_1 R_1}{s^2 + \left( \frac{1}{C_1 R_1} + \frac{1}{C_1 R_2} + \frac{1}{C_2 R_2} \right) s + \frac{R_1 + R_f}{C_1 C_2 R_1 R_2 R_f}}$$

This is the transfer function for the unity-gain Sallen Key we used in the filter circuit.

Now, we have also used an opamp amplifier circuit to make the peak ~~at~~ 1V at  $f_1$  frequency, as by only using the previous Sallen key, the peak value was coming less than 1V.

$\therefore$  The opamp amplifier circuit:



$$V_{out} = V_{in} \left( 1 + \frac{R_4}{R_3} \right)$$

Therefore, the final Transfer-function of the filter used, is:

$$\frac{V_{out}}{V_{in}} = \frac{\left(1 + \frac{R_4}{R_3}\right) \frac{s}{C_1 R_1}}{s^2 + \left(\frac{1}{C_1 R_1} + \frac{1}{C_1 R_2} + \frac{1}{C_2 R_2}\right)s + \frac{R_1 + R_f}{C_1 C_2 R_1 R_2 R_f}}$$

[where  $s = j\omega$ ]

Designing the filter:

The transfer function looks like:  
for the unity gain Sallen key:

$$\frac{V_{out}}{V_{in}} = \frac{s/C_1 R_1}{s^2 + \left(\frac{1}{C_1 R_1} + \frac{1}{C_1 R_2} + \frac{1}{C_2 R_2}\right)s + \frac{R_1 + R_f}{C_1 C_2 R_1 R_2 R_f}}$$

$$\therefore f_0 = \frac{1}{2\pi} \sqrt{\frac{R_1 + R_f}{C_1 C_2 R_1 R_2 R_f}} \quad \text{--- (1)}$$

↑  
central frequency

and

$$Q = \frac{\sqrt{(R_1 + R_f) R_1 R_2 R_f C_1 C_2}}{R_1 R_f (C_1 + C_2) + R_2 C_2 R_f} \quad \text{--- (2)}$$

↑  
Quality factor

I have;  $f_4 (\text{peak}) = 130.81 \text{ Hz}$

$$\begin{aligned} BW &= f_5 - f_3 \\ &= 146.81 - 123.47 \\ &= 23.36 \text{ Hz} \end{aligned}$$

$$Q = \frac{b_4}{BW} = \frac{130.81}{23.36} = \underline{\underline{5.6}}$$

Doing the calculations:

Taking;  $C_1 = C_2 = C$   
 $R_1 = R_2 = R$   
 $R_f = 1k\Omega$

$\therefore$  In eqn (1);

$$130.81 = \frac{1}{2\pi} \left[ \frac{1000 + R}{C^2 \cdot R^2 \cdot 1000} \right] \quad \text{--- (3)}$$

In eqn (2);

$$5.6 = \frac{(R+1000) R^2 C^2 \cdot 1000}{R(1000)(2C) + R(1000)C}$$

$$5.6 = \frac{CR \cancel{C} (1000)(R+1000)}{3RC(1000)}$$

$$16800 = \cancel{C} (1000)(R+1000)$$

$$282210000 = 1000(R + 1000)$$

$$R = 281210 \Omega$$

$$\boxed{R = 281.21 \text{ k}\Omega}$$

$\therefore$  In eqn (i):

$$C = \frac{1}{2\pi(130.81)} \left[ \frac{1000 + R}{R^2 \cdot 1000} \right]$$

$$= \underline{\underline{72.6 \text{ nF}}}$$

$\therefore$   
Component values:

$$\boxed{R_1 = R_2 = 281.21 \text{ k}\Omega}$$

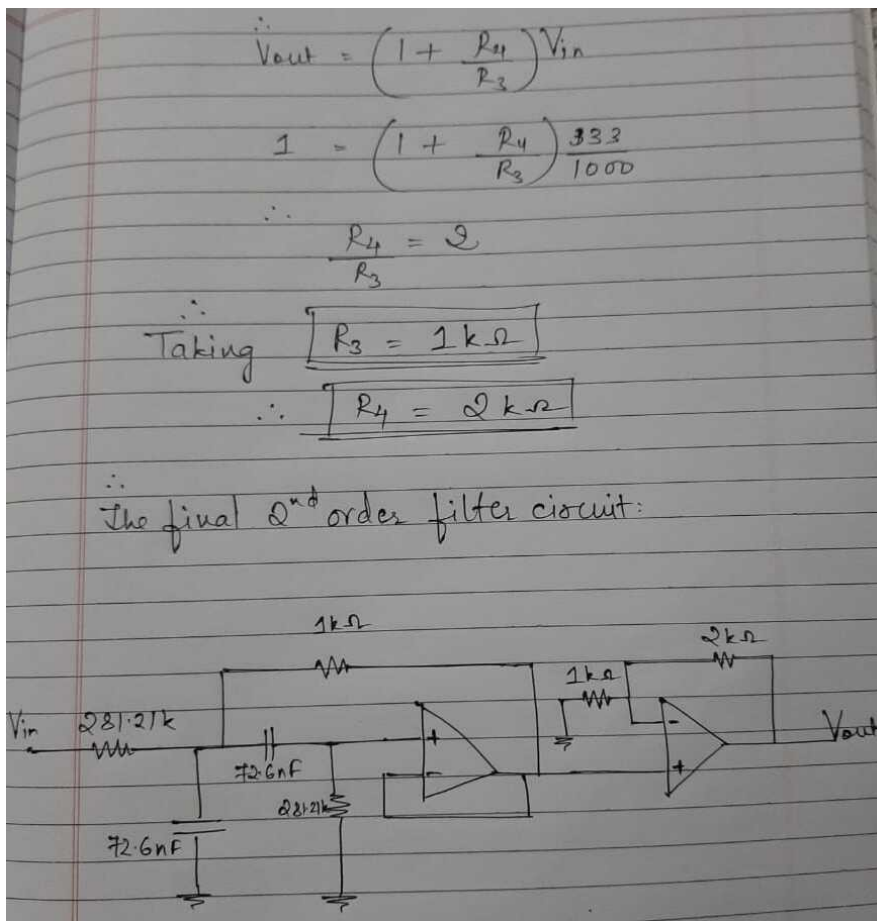
$$\boxed{C_1 = C_2 = 72.6 \text{ nF}} \quad \boxed{R_f = 1 \text{ k}\Omega}$$

Now, for the opamp amplifier circuit;

We got a peak at 333mV when we plotted the Bode plot of only the unity-gain Sallen key.

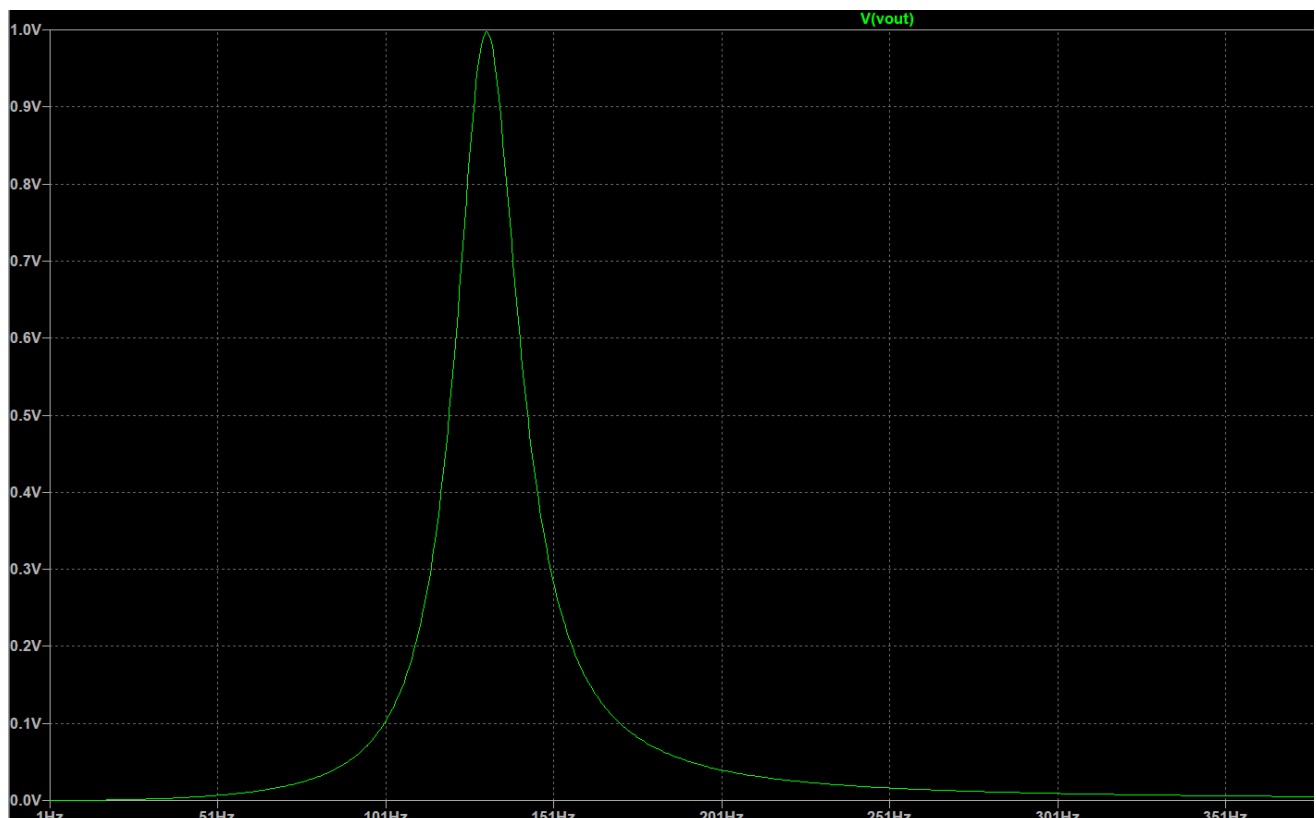
Thus, we need to amplify this to 1V to have a peak of 1V.





### My Graphs:

#### **The Bode Plot of the Designed Filter circuit:**



The final filtered response looks like:

