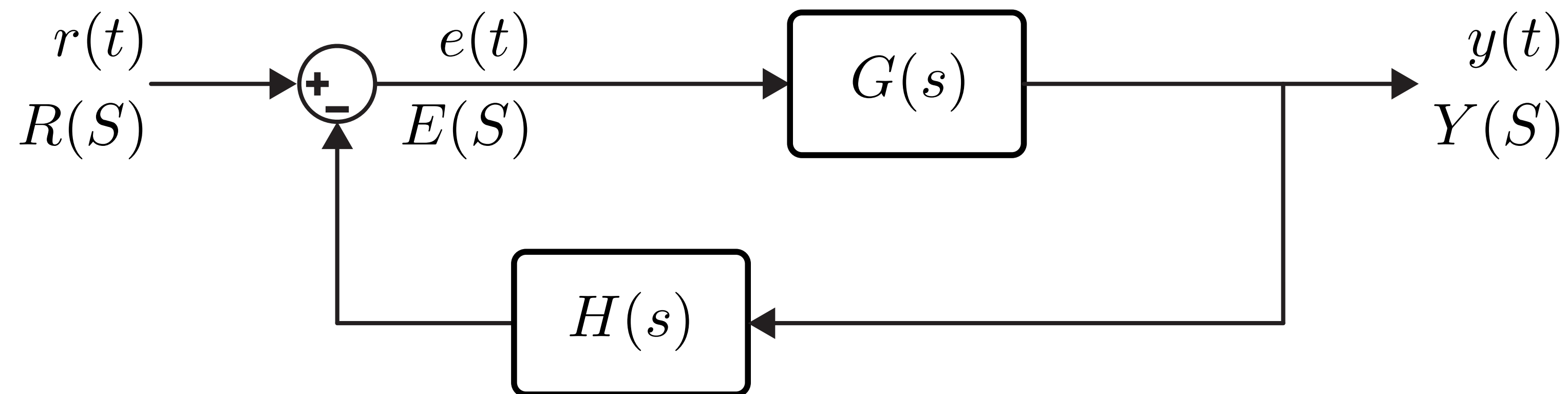
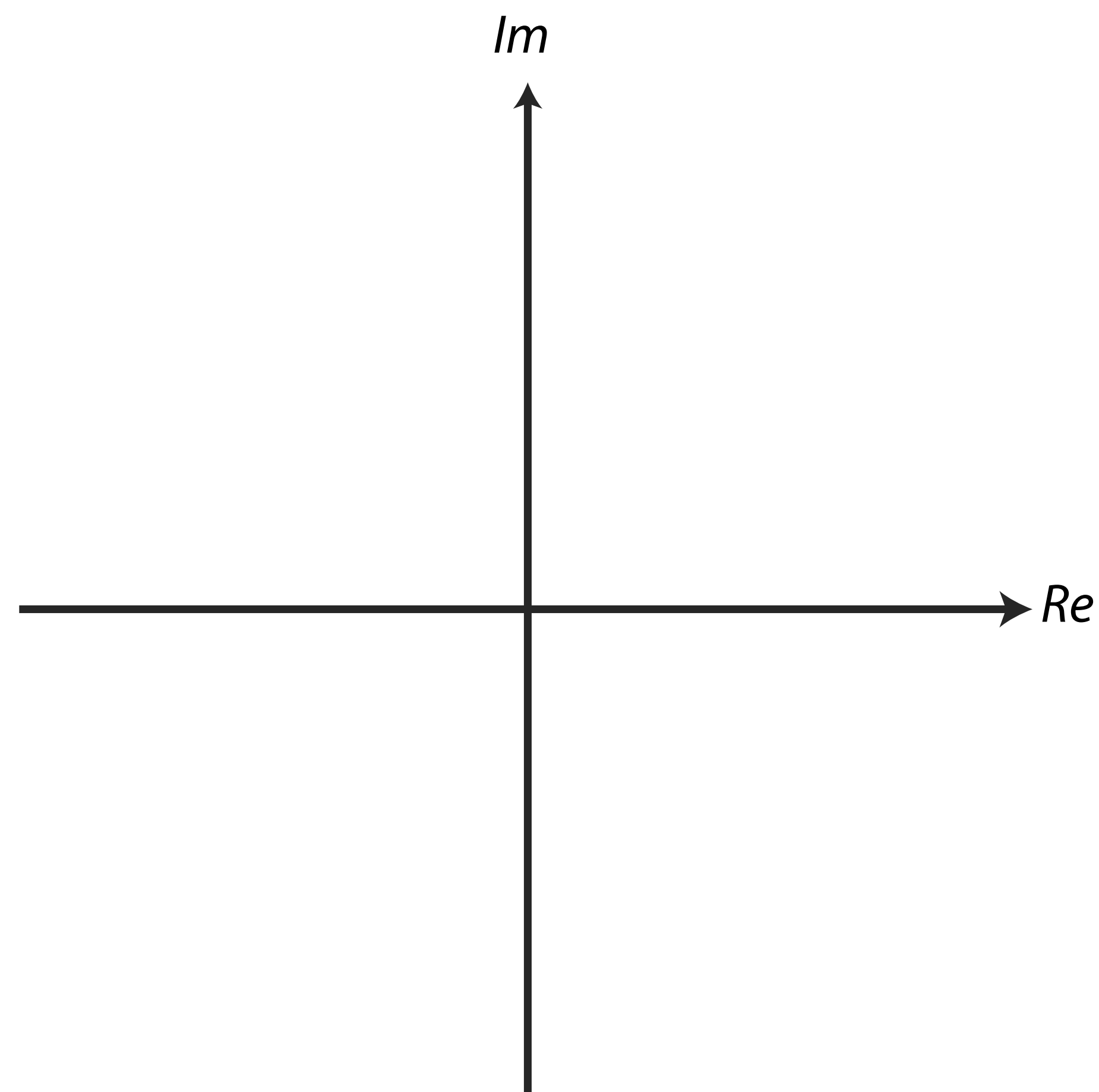
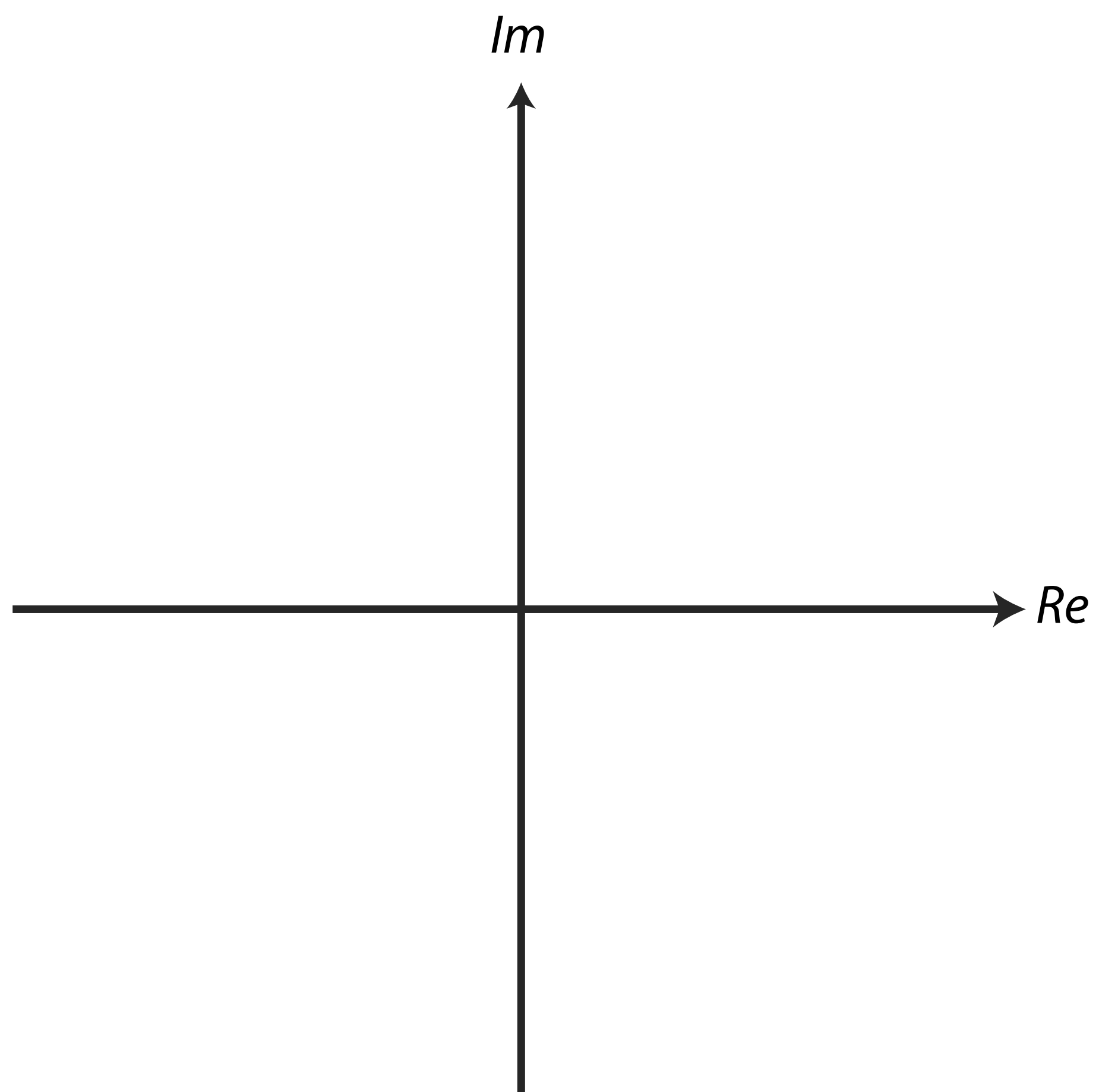


# Stability Margins: Gain & Phase Margins

<https://github.com/mertankarali/Lecture-Notes/tree/master/METU-EE302/Lecture%2017>

## Lecture #17





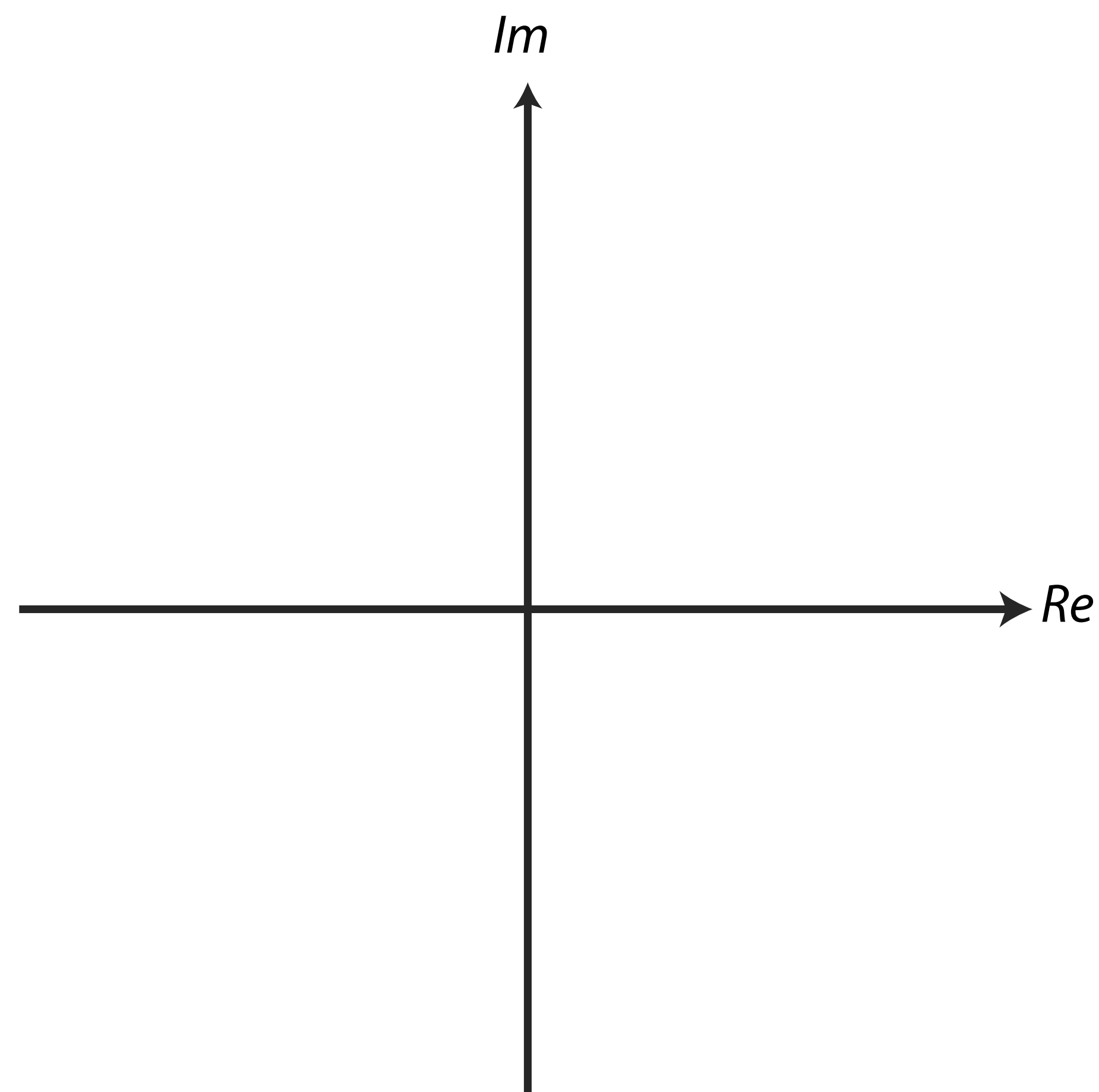
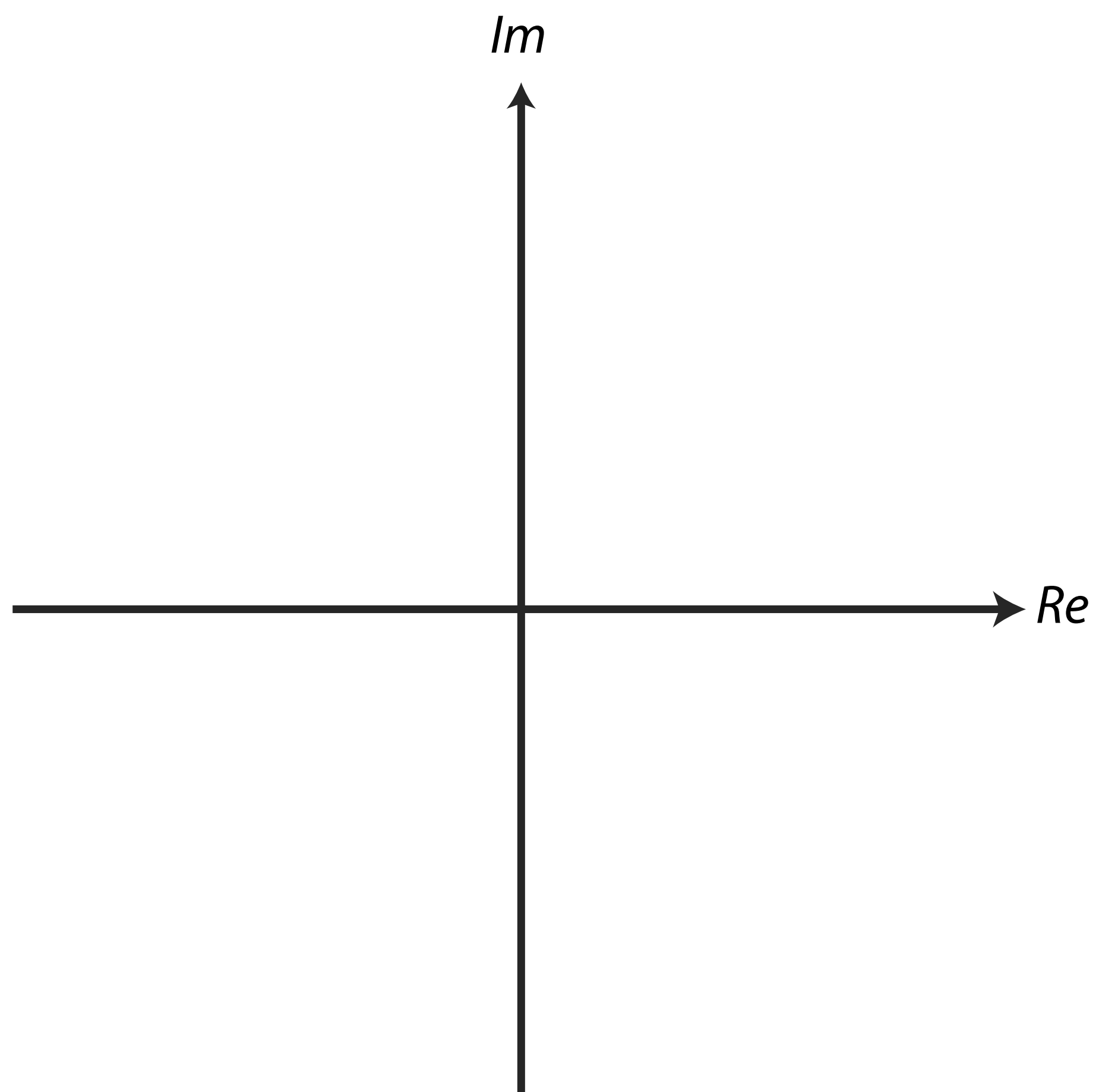
# Assumptions

- $G_{OL}(s)$  is a *minimum-phase* system, i.e.
  - No poles/zeros in the Open Right Half Plane
  - $\lim_{\omega \rightarrow \infty} \left[ \frac{G_{OL}(s)}{s} \right]_{s=j\omega} = 0$
- The feed-back system is Type 0 – 2
- Polar plot of  $G_{OL}(j\omega)$  crosses the negative real-axis at most once.

# Assumptions

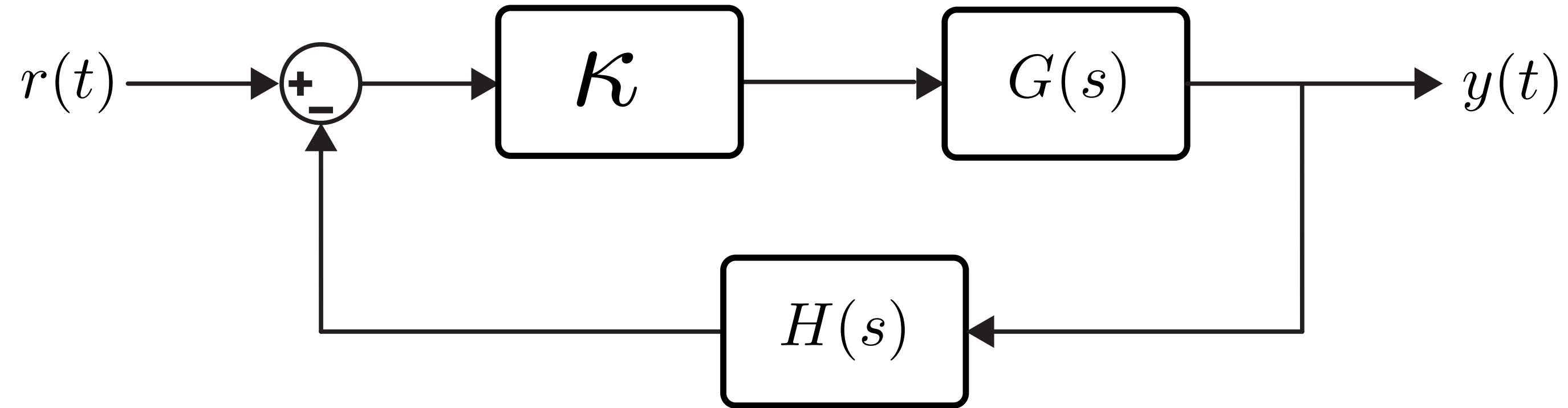
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- Polar plot of  $G_{OL}(j\omega)$  crosses the negative real-axis at most once.

Assumptions  $\Rightarrow$  Gain & Phase Margin from Polar Plot



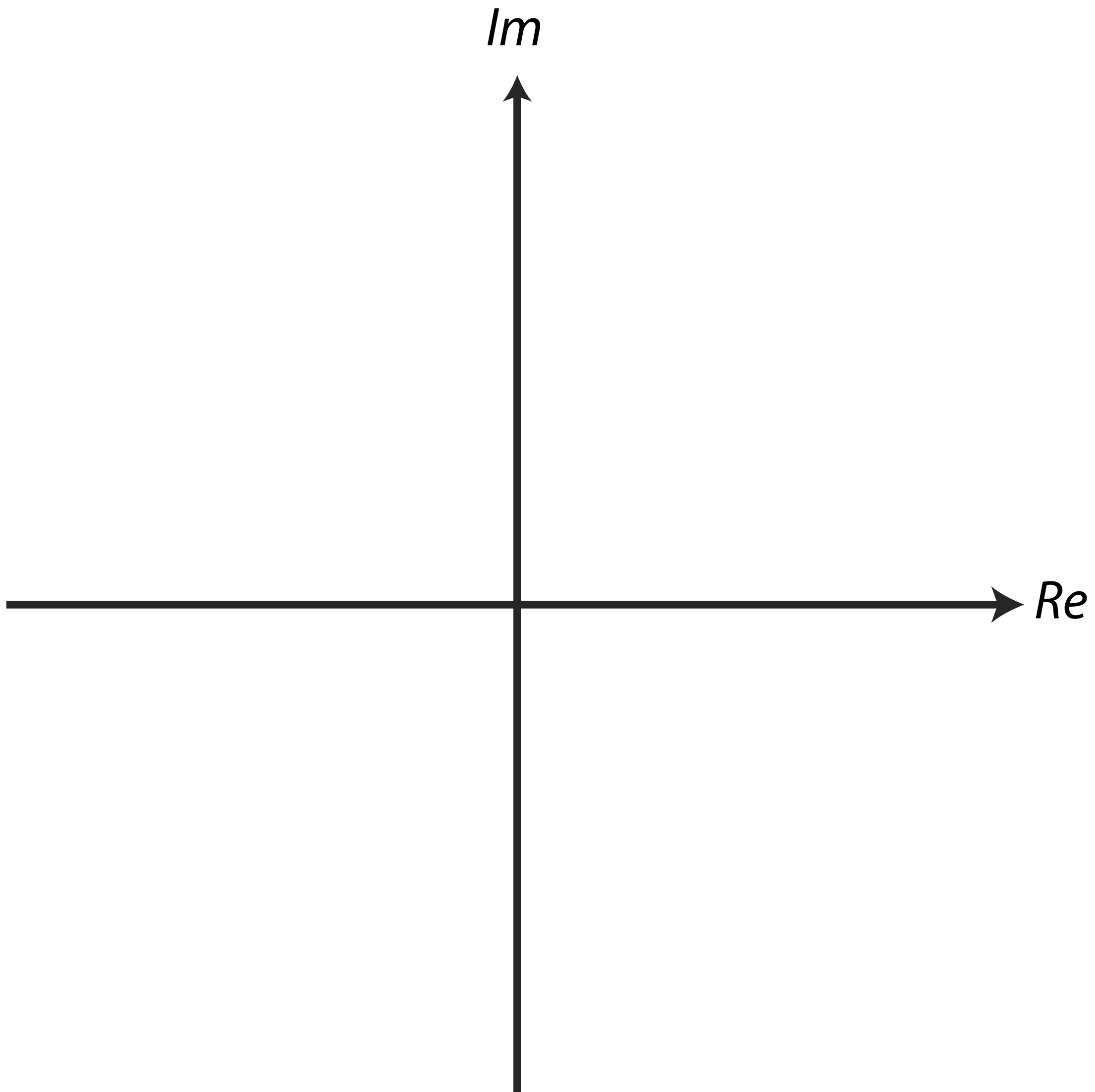
# Gain Margin, $g_m$

$g_m$  : the change in open-loop gain required to reach the Nyquist stability limit



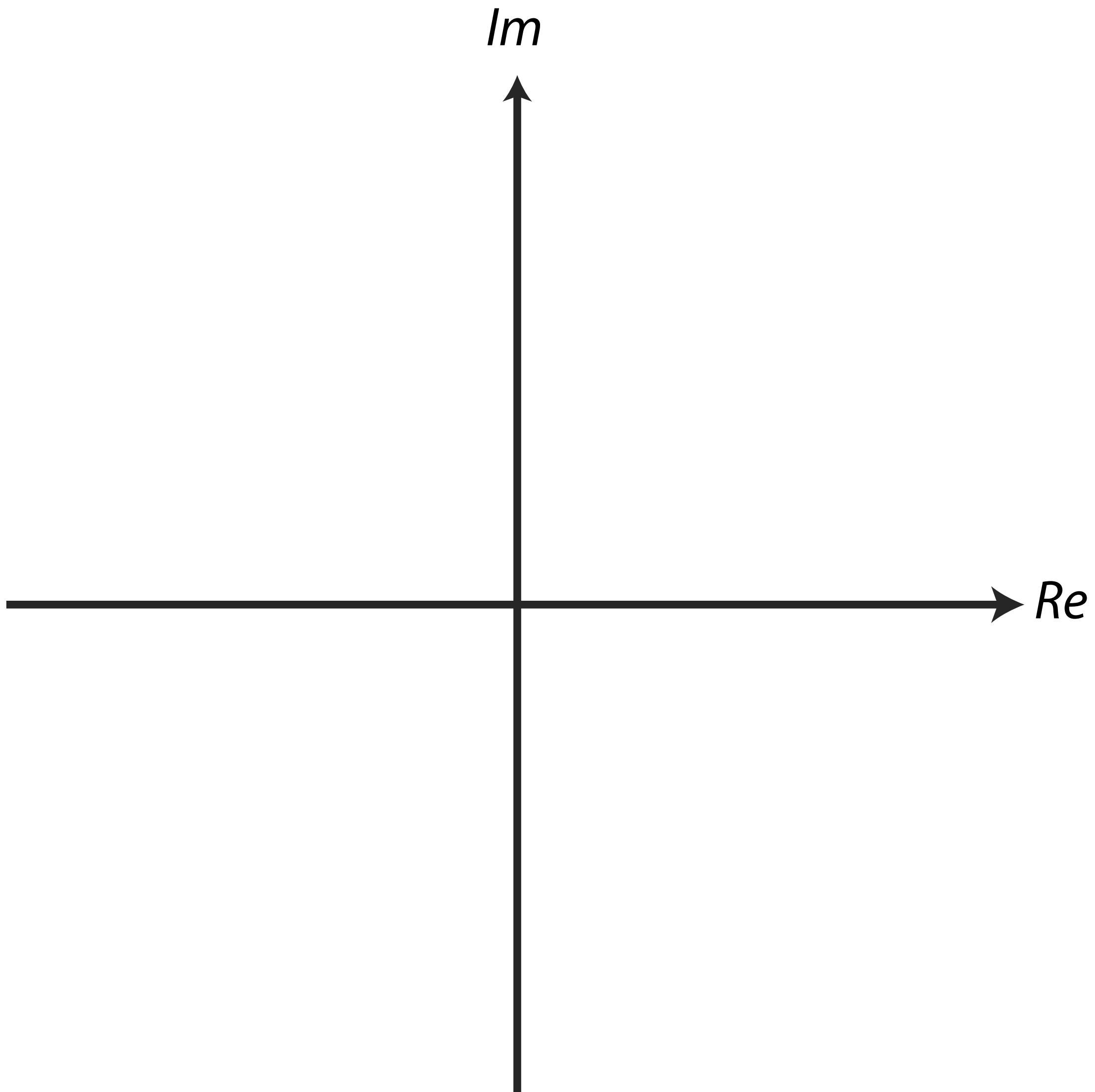
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# Gain Margin, $g_m$

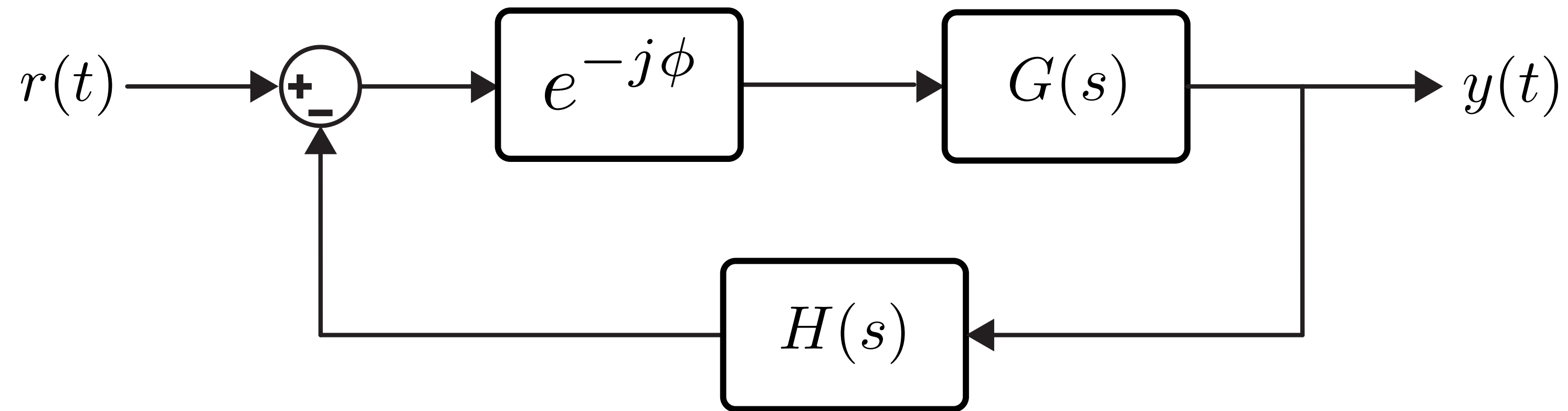
$g_m$  : the change in open-loop gain required to reach the Nyquist stability limit





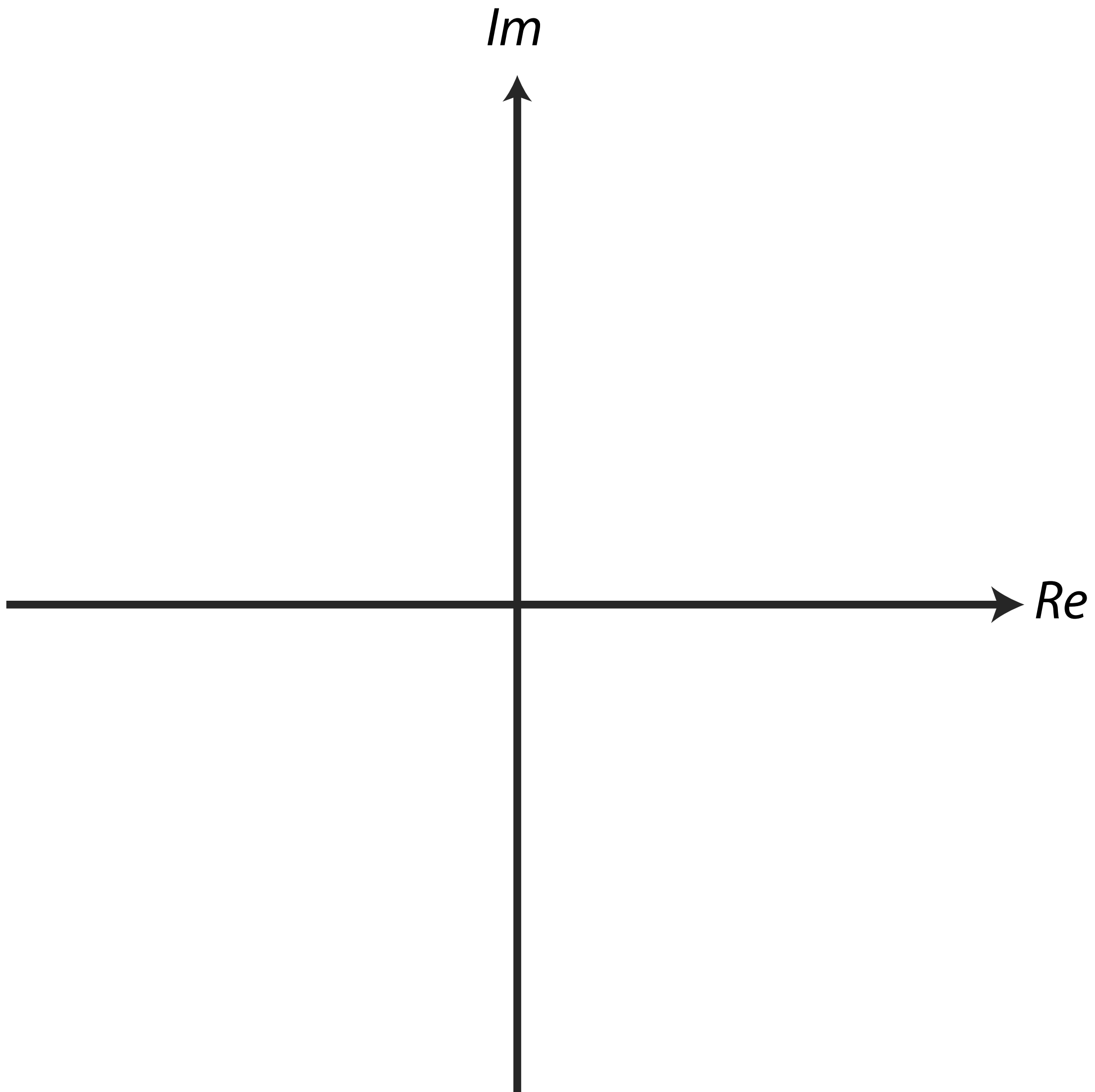
# Phase Margin, $\phi_m$

$\phi_m$  : the amount of “phase lag” required to reach the (Nyquist) stability limit



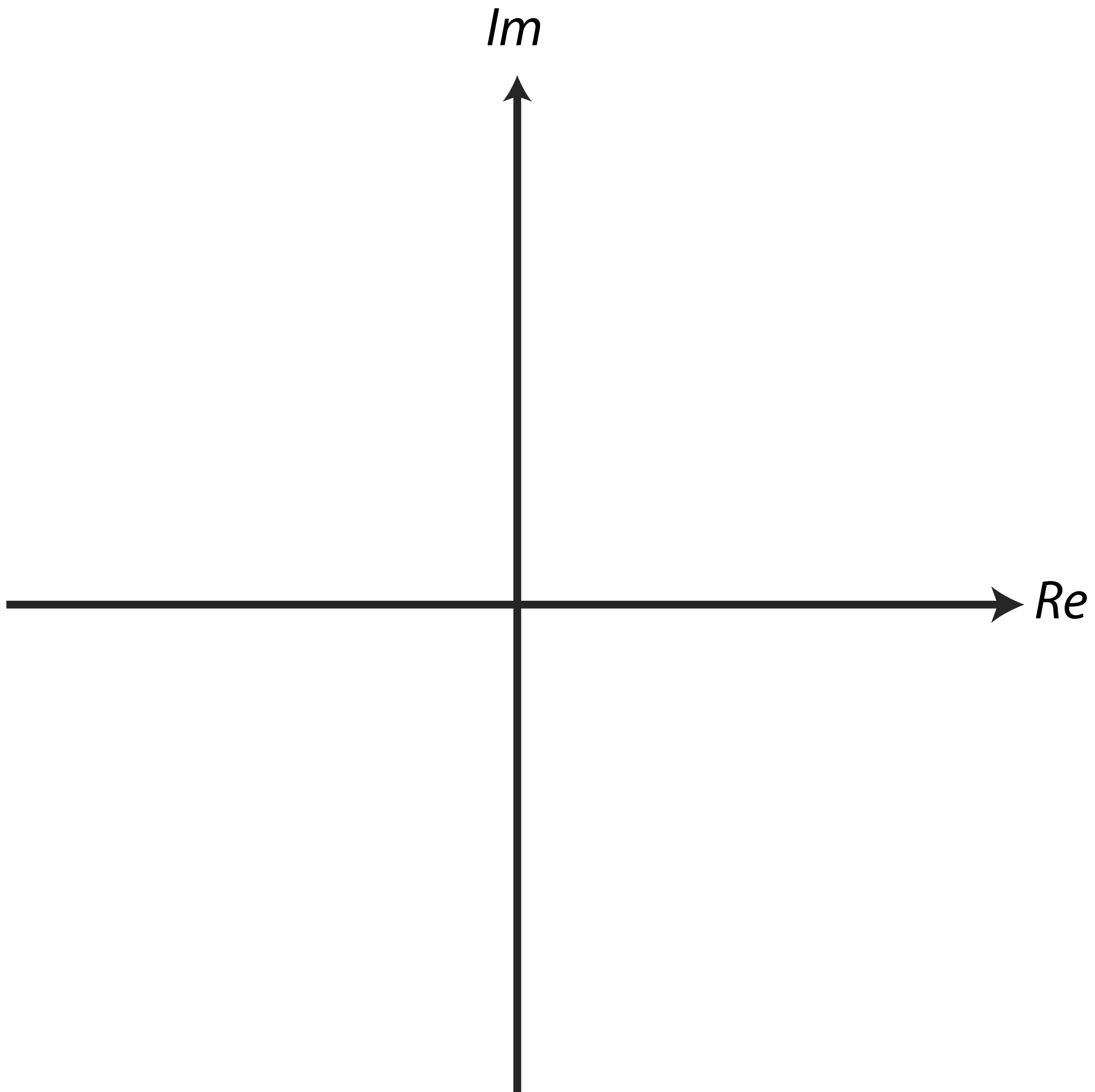
# Phase Margin, $\phi_m$

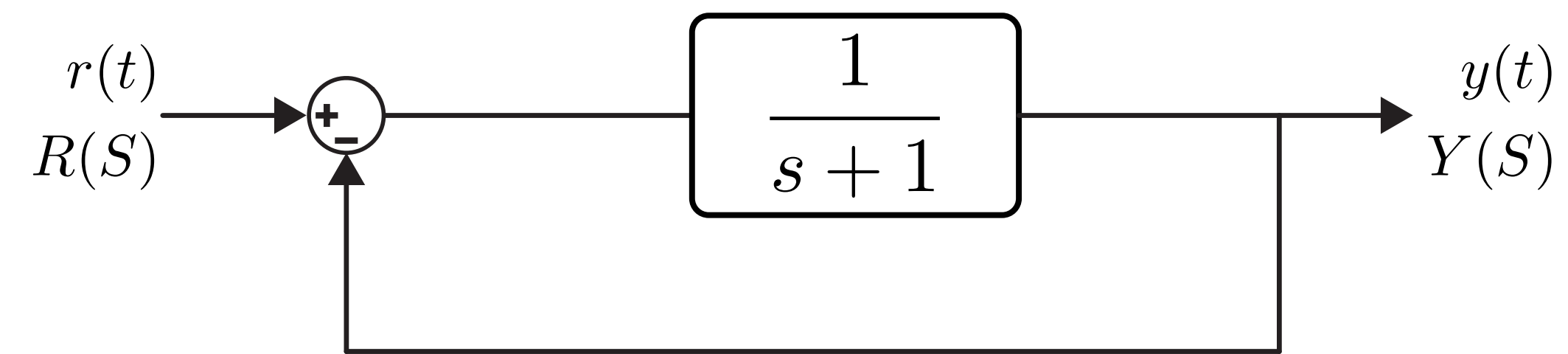
$\phi_m$  : the amount of “phase lag” required to reach the (Nyquist) stability limit



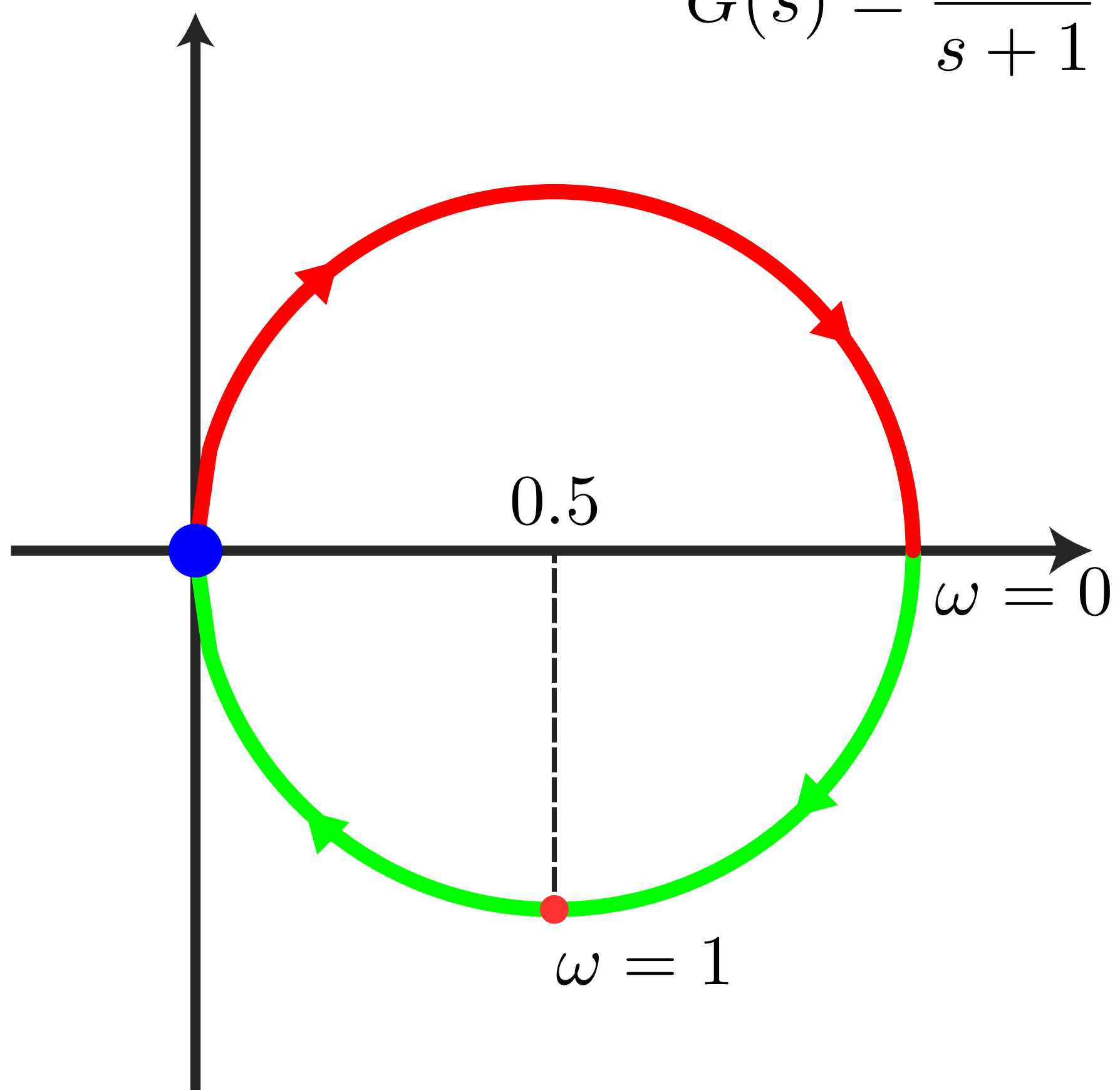
# Phase Margin, $\phi_m$

$\phi_m$  : the amount of “phase lag” required to reach the (Nyquist) stability limit

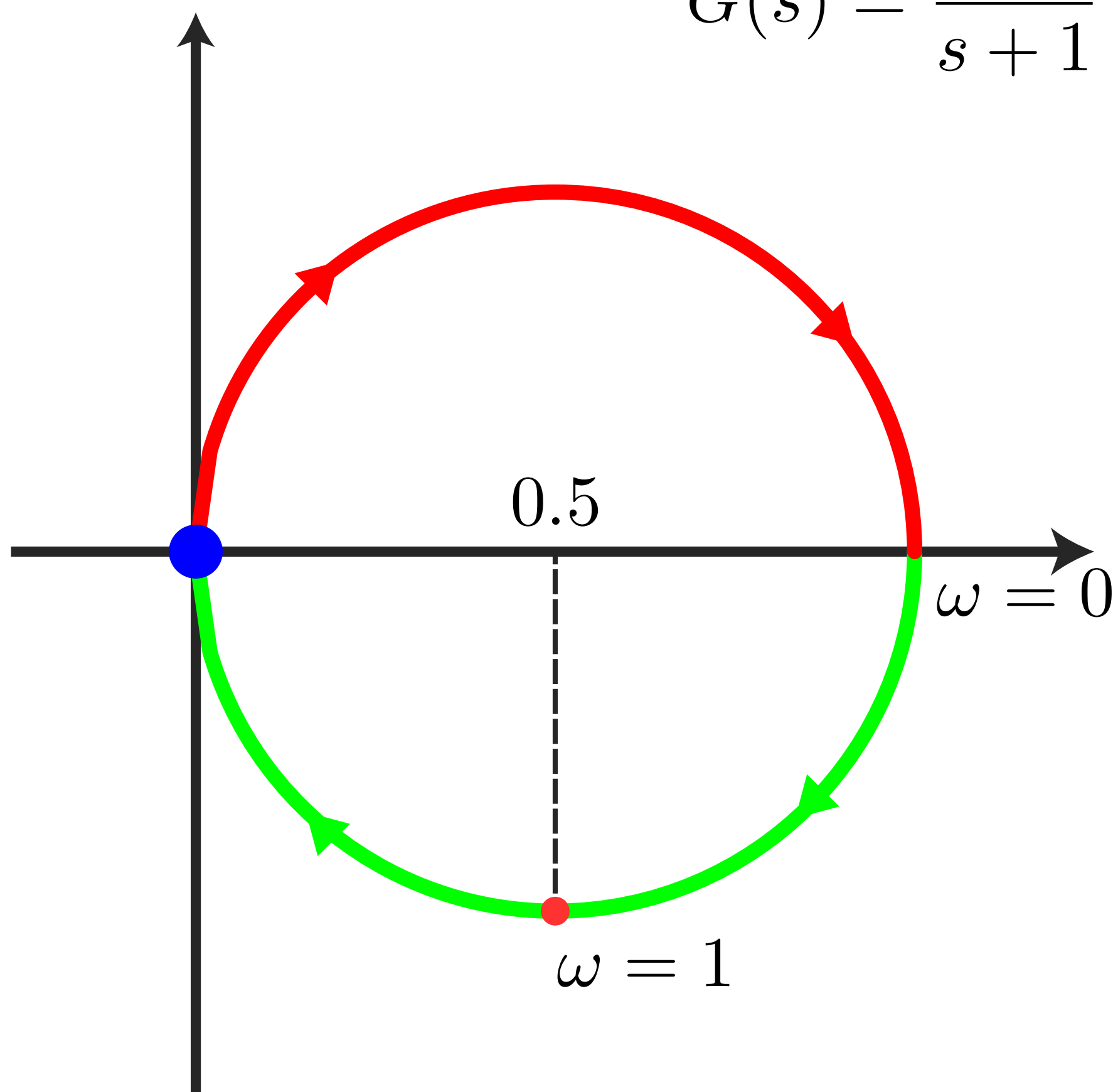




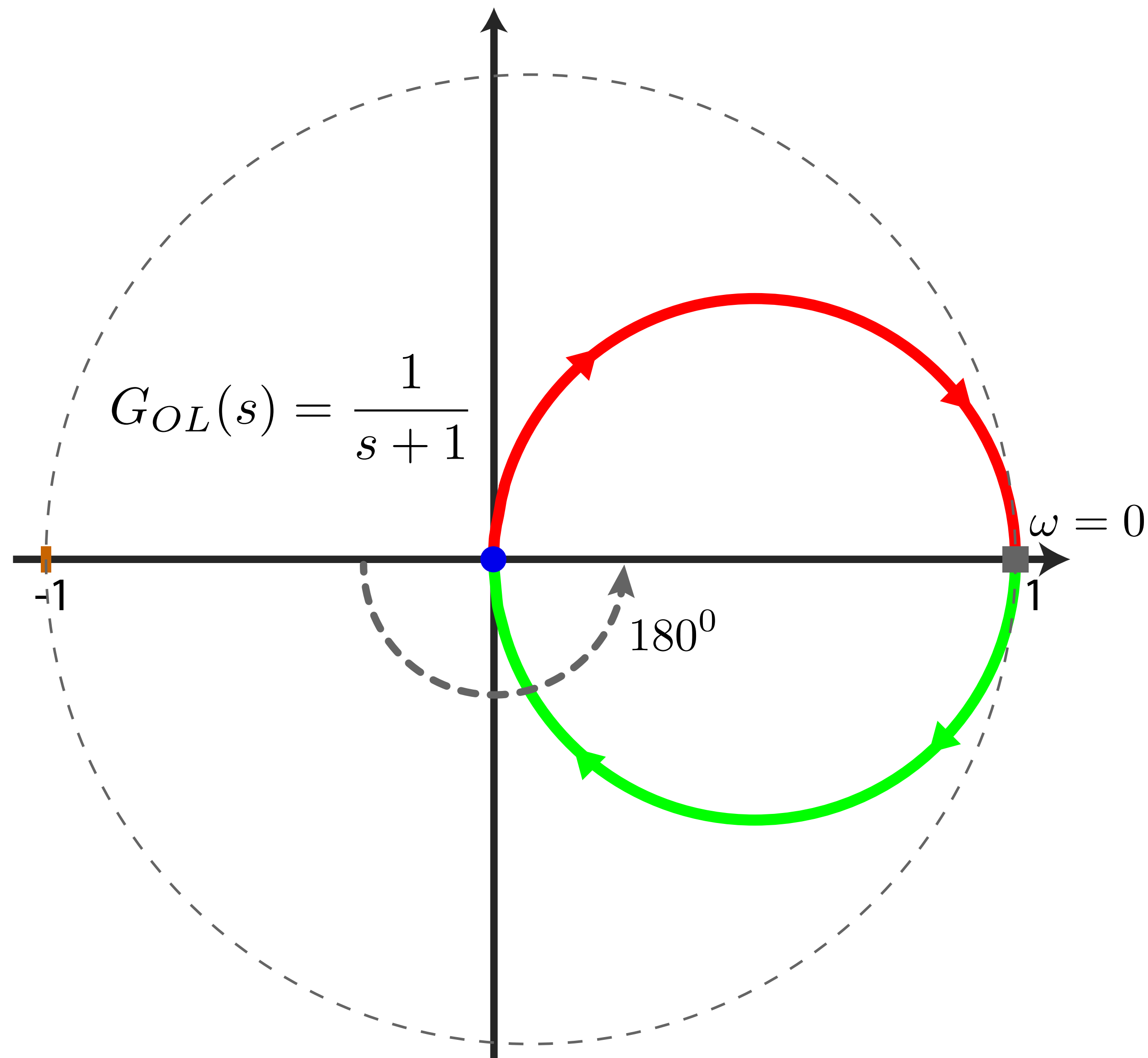
$$G(s) = \frac{1}{s + 1}$$

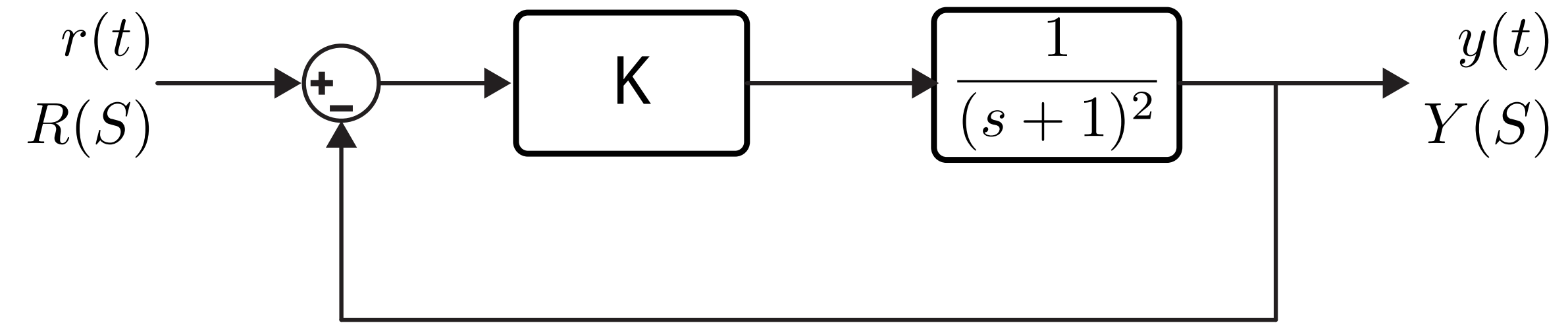


$$G(s) = \frac{1}{s + 1}$$

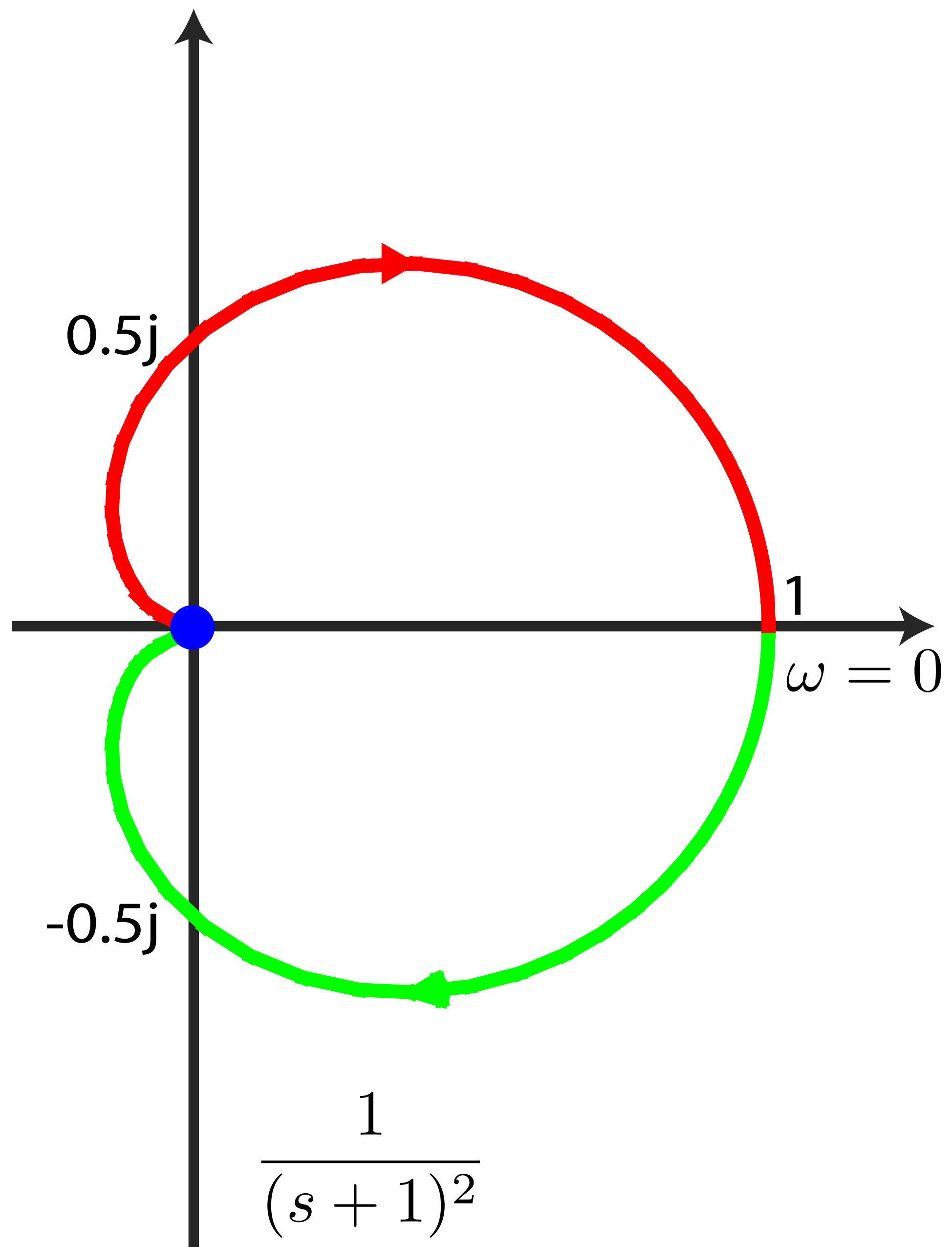


$$G_{OL}(s) = \frac{1}{s + 1}$$

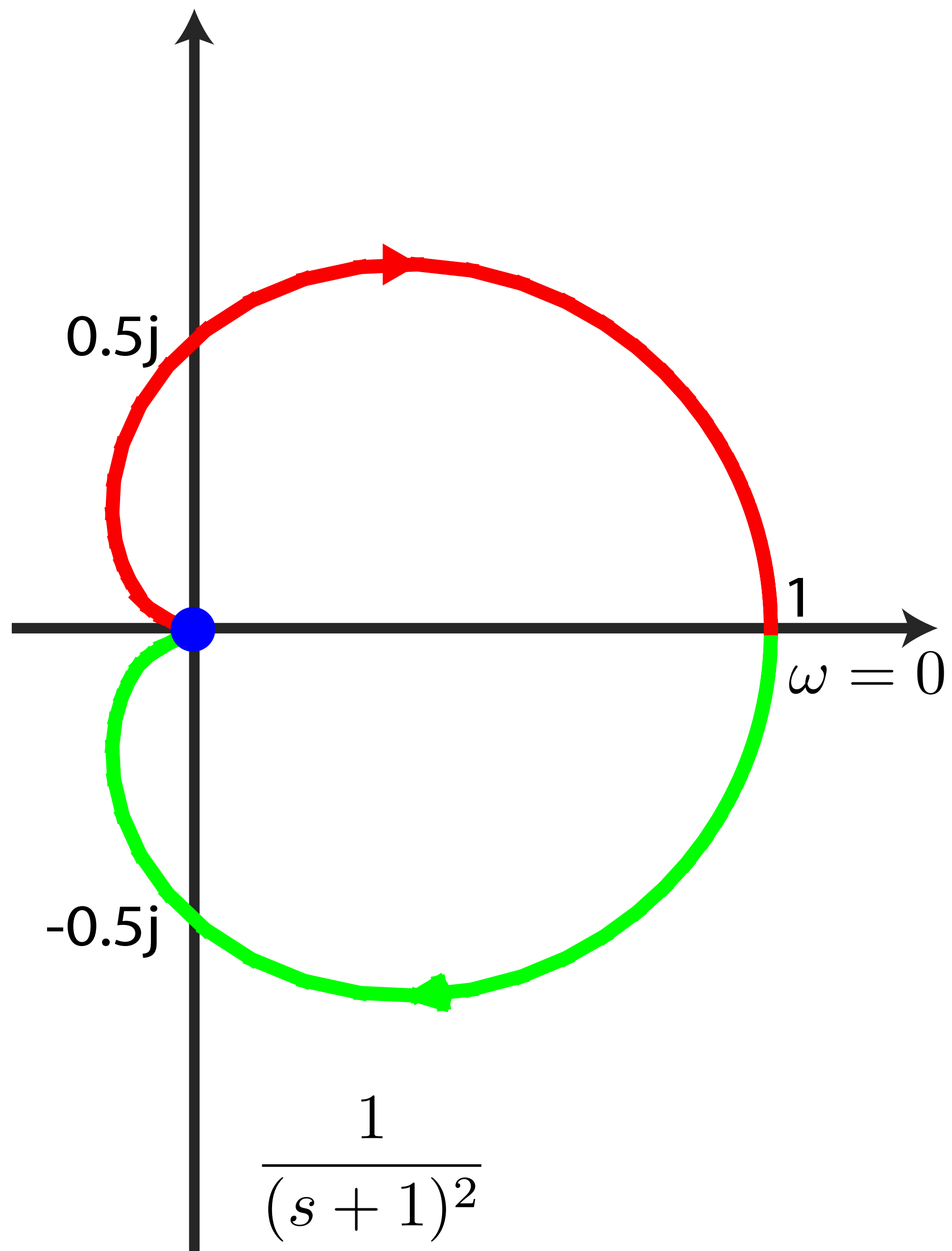


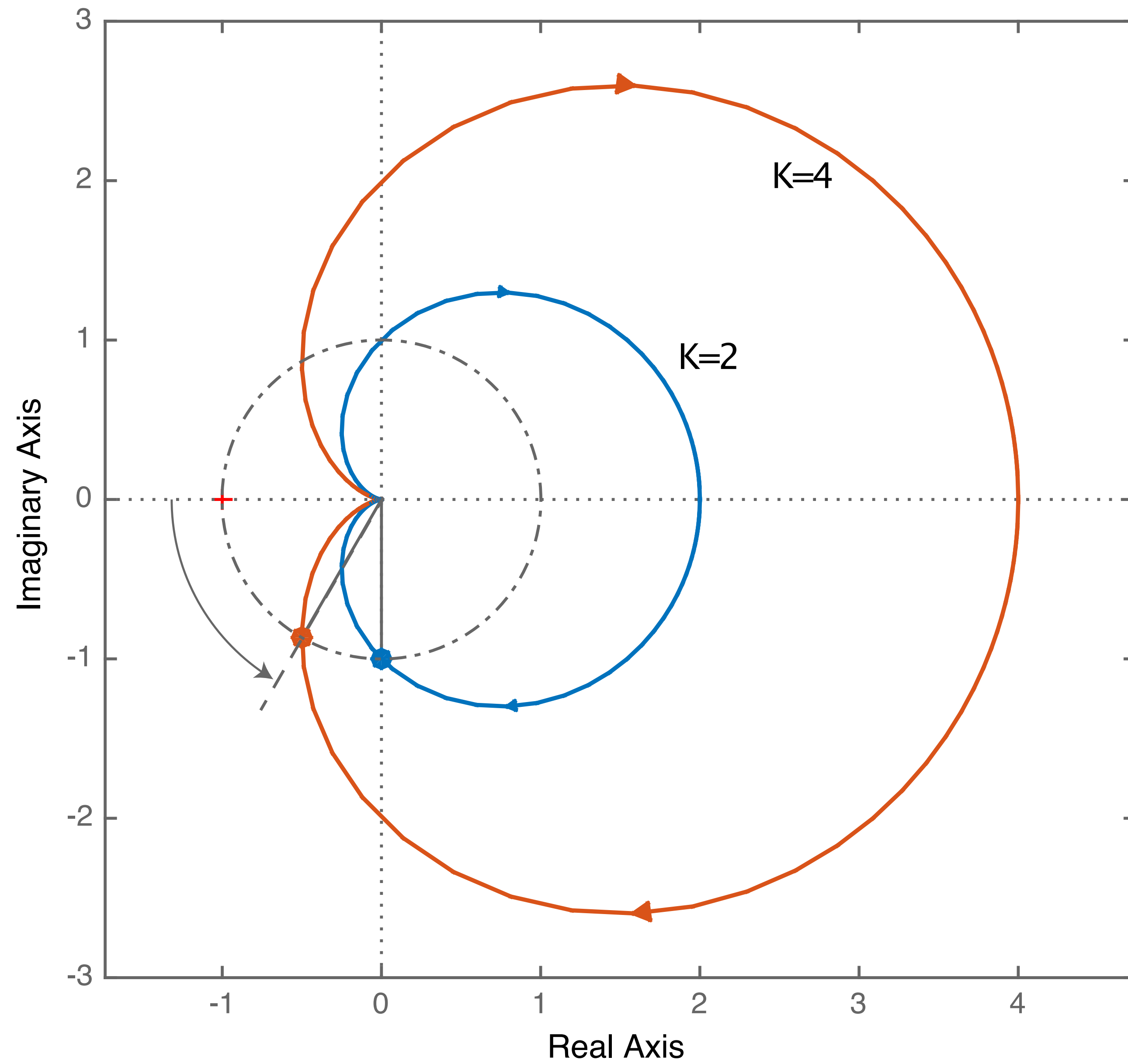


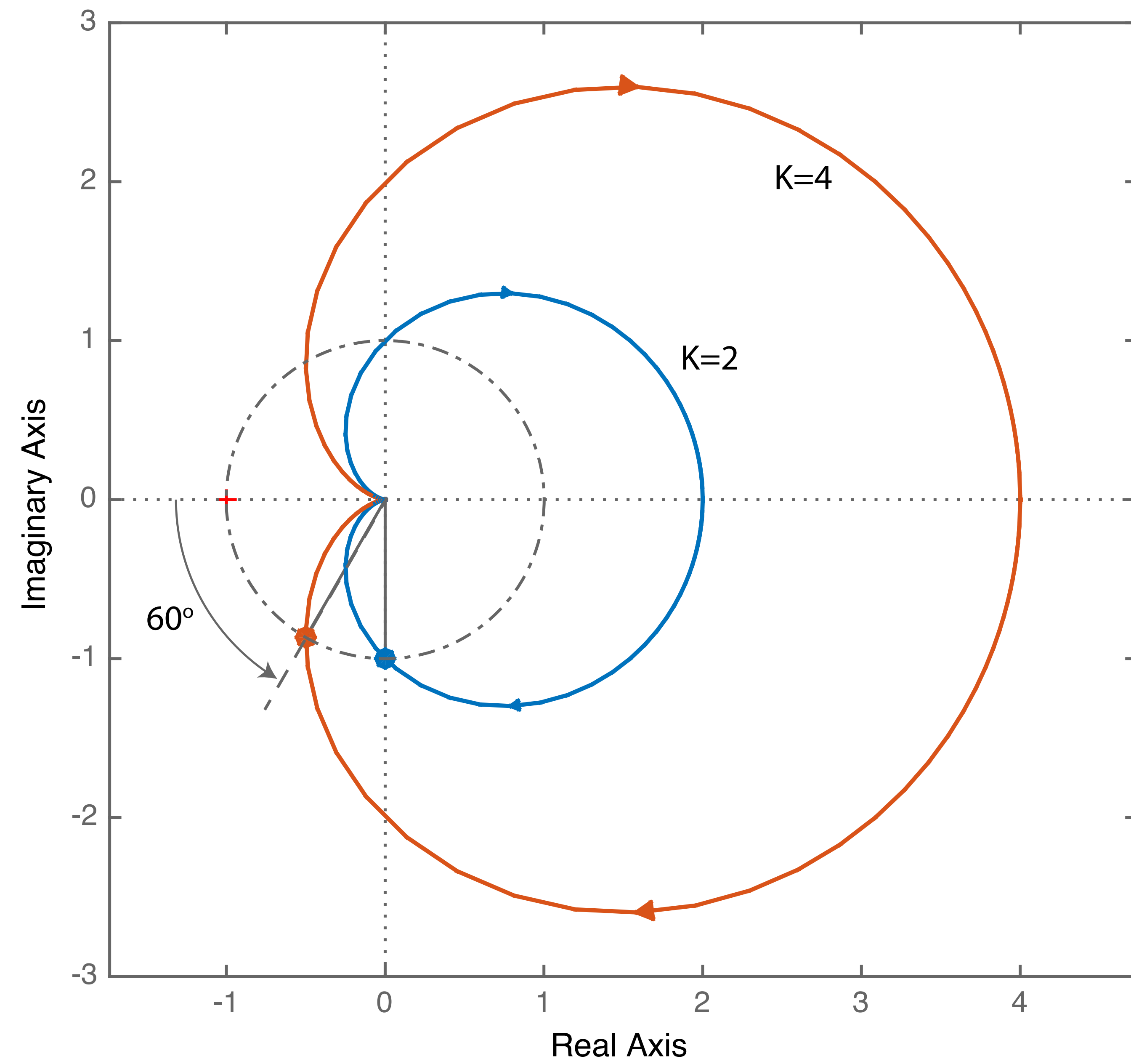
Compute the gain margin and phase margin for the following closed-loop system for  $K = 2$  and  $K = 4$

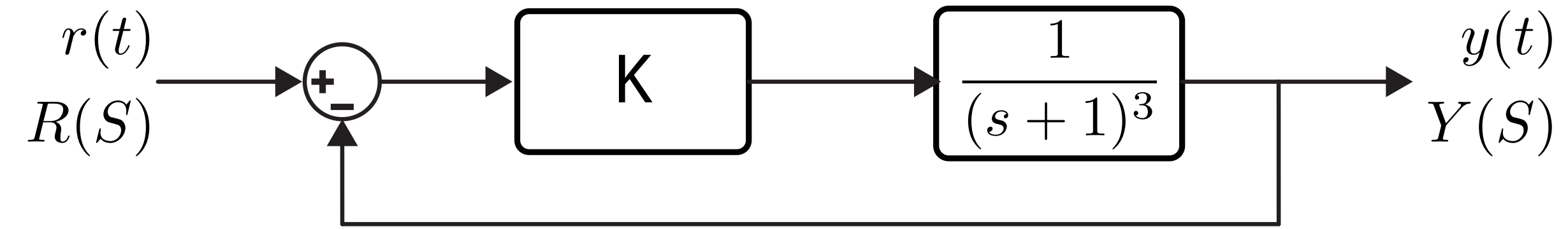




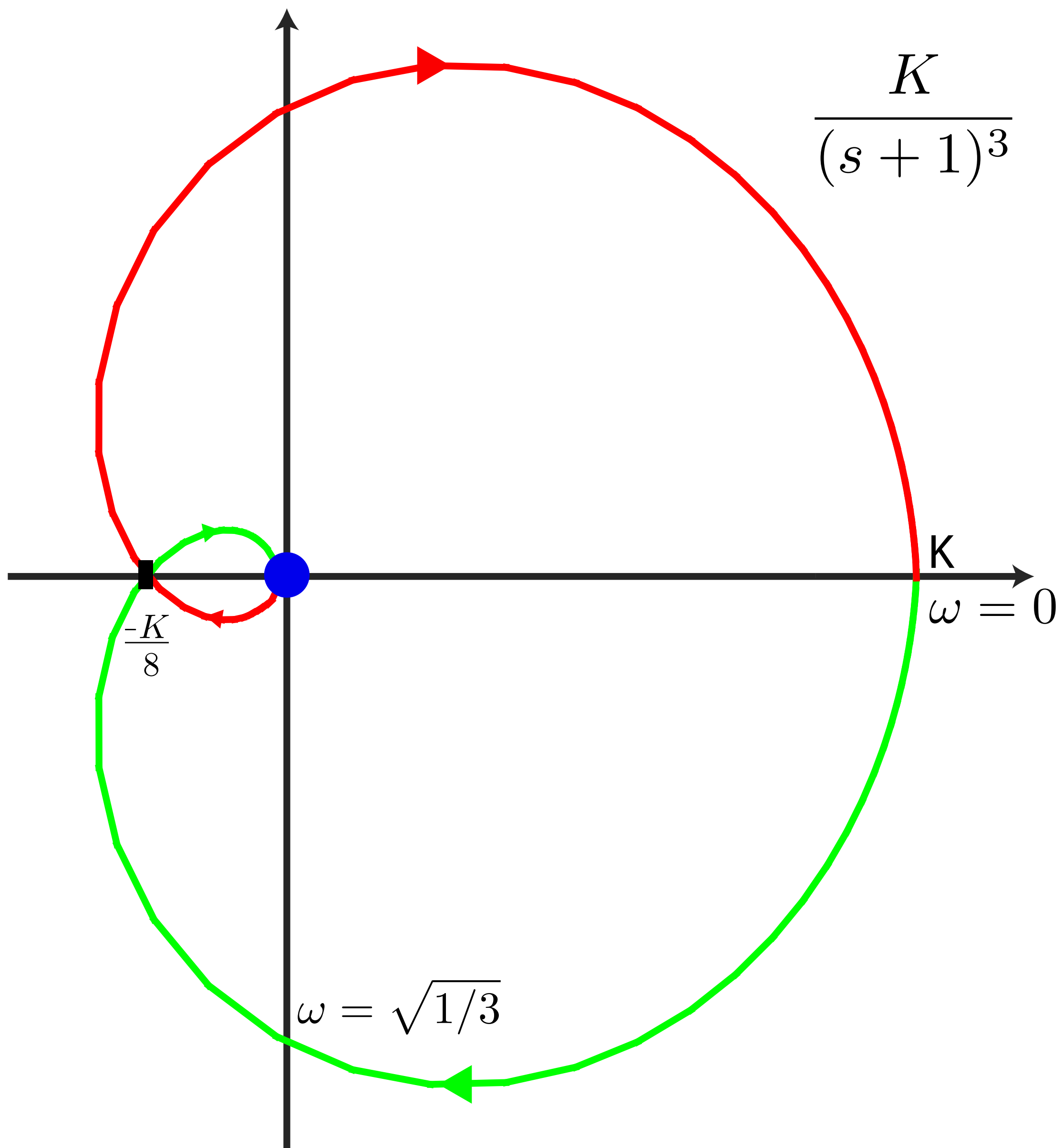


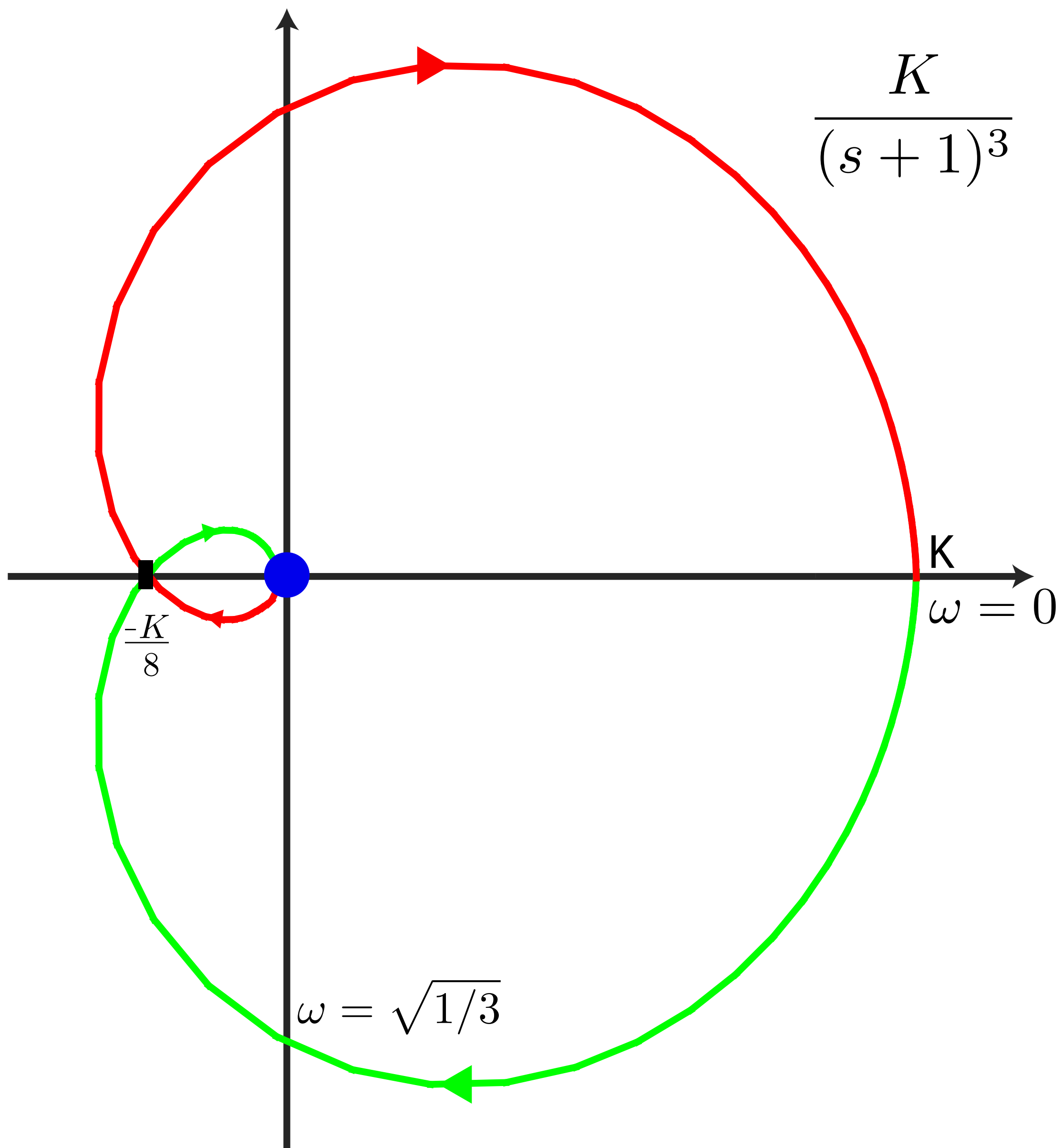




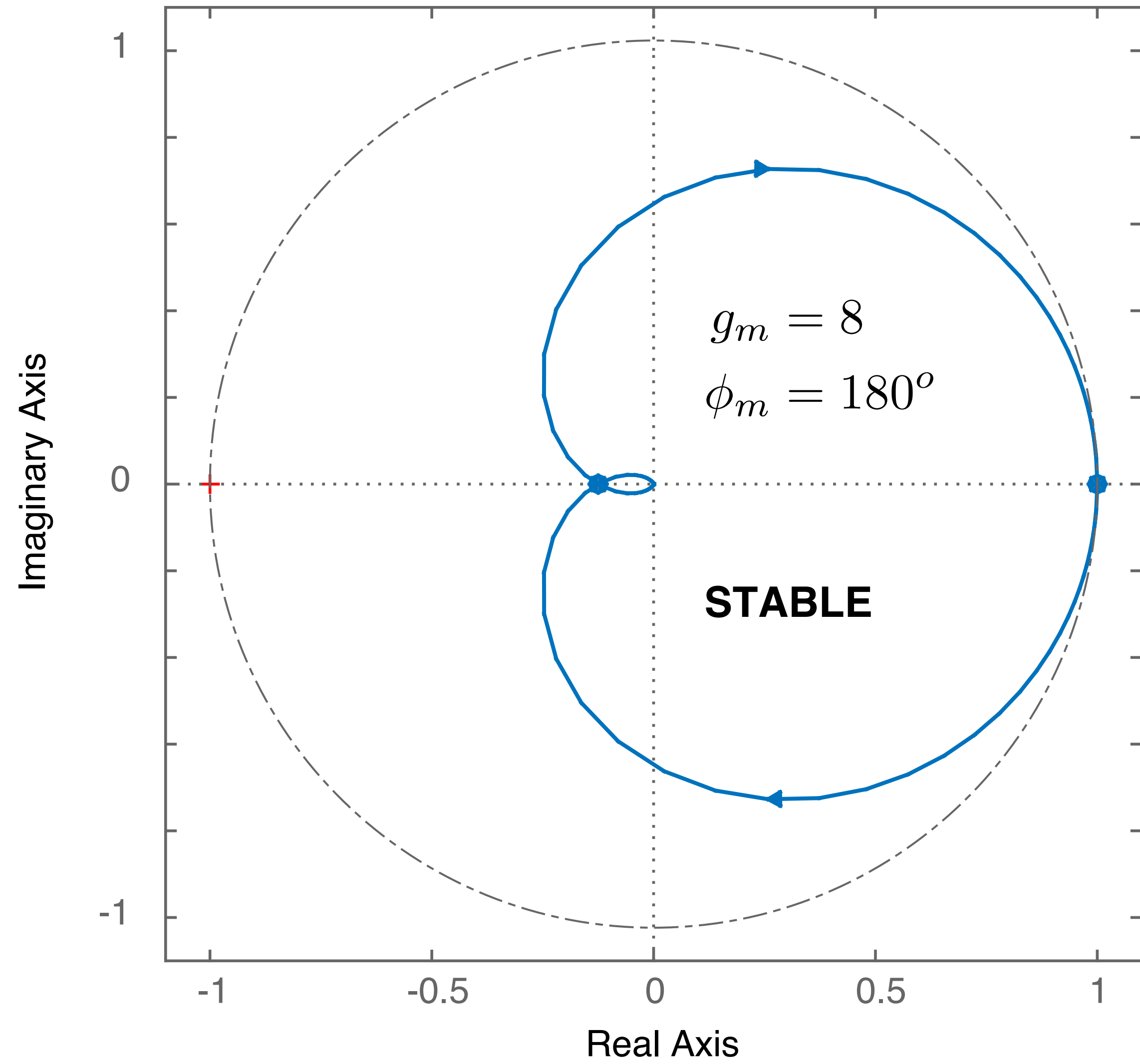


Compute the gain margin and phase margin for the following closed-loop system for  $K = 1$  and  $K = 8$





**K = 1**



**K = 8**

