Package 'bestsubset'

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Title Tools for best subset selection in regression

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Depends glmnet, gurobi	
Description An implementation of best subset selection in regression based on a mixed integer quadratic program formulation of the subset selection problem, and the Gurobi mixed integer program optimizer; also, tools for running simulations comparing best subset selection to other common sparse regression estimators such as the lasso and forward stepwise.	
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bestsubset-package	Simulations for best subset selection in regression
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Description

Tools for running simulations that compare best subset selection in regression to other common sparse regression estimators such as the lasso and forward stepwise.

Details

The simulation setup is based on the paper: "Best subset selection via a modern optimization lens" by Dimitris Bertsimas, Angela King, and Rahul Mazumder, Annals of Statistics, 44(2), 813-852, 2016.

bs

Best subset selection.

Description

Compute best subset selection solutions.

Usage

```
bs(x, y, k = 1:min(nrow(x), ncol(x)), intercept = TRUE,
form = ifelse(nrow(x) < ncol(x), 2, 1), time.limit = 100, nruns = 50,
maxiter = 1000, tol = 1e-04, polish = TRUE, verbose = FALSE)</pre>
```

Arguments

x	Matrix of predictors, of dimension (say) n x p.
у	Vector of responses, of length (say) n.
k	Sparsity level, i.e., number of nonzero coefficients to allow in the subset regression model; can be a vector, in which case the best subset selection problem is solved for every value of the sparsity level. Default is $1:\min(n,p)$.
intercept	Should an intercept be included in the regression model? Default is TRUE.
form	Either of 1 or 2, specifying the formulation to use for best subset solution as a mixed integer quadratic program. Formulations 1 and 2 correspond to equations (2.5) and (2.6) in Bertsimas, King, and Mazumder (2016) , see references below. Default is 1 if $n \ge p$, and 2 if $n < p$.
time.limit	The maximum amount of time (in seconds) to allow Gurobi to compute the subset selection solution at each value of k. Default is 100.
nruns	The number of runs of projected gradient descent to use, where each run begins at a random initialization for the coefficients. The best estimate over all these runs (achieving the lowest criterion value) is passed to Gurobi as a warm start. Default is 50.
maxiter	The maximum number of iterations for each run of projected gradient descent. Default is 1000.

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tol	The tolerance for the relative difference in coefficients between iterations of projected gradient descent (the algorithm terminates when the relative difference is less than the specified tolerance). Default is 1e-4.
polish	Should the project gradient descent algorithm replace the estimate at each iteration by the least squares solution on the active set? Default is TRUE.
Should	intermediate progress be printed out? Default is FALSE.

Details

This function solves best subset selection program:

$$\min_{\beta} \|Y - X\beta\|_2^2 \text{ s.t. } \|\beta\|_0 \le k$$

for a response vector Y and predictor matrix X. It follows the algorithm suggested by Bertismas, King, and Mazumder (2016) (see below for for the full reference): it first uses projected gradient descent to find an approximate solution to the above nonconvex program, and then calls Gurobi's MIO (mixed integer optimization) solver with this approximate solution as a warm start. There are two options for how to formulate best subset selection as a mixed integer quadratic program, one recommended when $n \ge p$, and the other when n < p. They correspond to equations (2.5) and (2.6) in the paper by Bertismas, King, and Mazumder (2016), respectively.

Value

A list with the following components:

- beta: matrix of regression coefficients, one column per sparsity level
- status: vector of status strings returned by Gurobi's MIO solver, one element for each sparsity level
- k: vector of sparsity levels
- x, y: the passed x and y
- bx, by: the means of the columns of x, and the mean of y
- intercept: was an intercept included?

Author(s)

Ryan Tibshirani

References

This function utilizes the MIO formulation for subset selection as described in "Best subset selection via a modern optimization lens" by Dimitris Bertsimas, Angela King, and Rahul Mazumder, Annals of Statistics, 44(2), 813-852, 2016. This R implementation is based on Matlab code written by Rahul Mazumder.

Examples

```
# Simulate some simple regression data with the first 5 coefficients # being nonzero set.seed(3) n = 100 \\ p = 20 \\ ntest = 10000
```

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```
xy.obj = sim.xy(n,p,nval=0,ntest=ntest,s=5,beta.type=2,snr=1)
x = xy.obj$x
y = xy.obj\$y
xtest = xy.obj$xtest
mutest = xy.obj$mutest
# Run forward stepwise regression for 8 steps
fs.obj = fs(x,y,intercept=FALSE,maxsteps=8,verbose=TRUE)
fs.beta = coef(fs.obj)
fs.supp = apply(fs.beta != 0, 2, which)
# Solve best subset selection for 8 sparsity levels
bs.obj = bs(x,y,intercept=FALSE,k=1:8,verbose=TRUE)
bs.beta = coef(bs.obj)
bs.supp = apply(bs.beta != 0, 2, which)
# Compare supports of the solutions with 5 and 8 variables
fs.supp[[5]]; bs.supp[[5]]
fs.supp[[8]]; bs.supp[[8]]
# Predict on test data and record risk
fs.pred = predict(fs.obj,newx=xtest)
bs.pred = predict(fs.obj,newx=xtest)
colMeans((fs.pred - mutest)^2)
colMeans((bs.pred - mutest)^2)
```

coef.bs

Coefficient function for bs object.

Description

Compute coefficients at a particular sparsity level of the best subset selection model.

Usage

```
## S3 method for class bs
coef(object, s, ...)
```

Arguments

object The bs object, as produced by the bs function.

s The sparsity level (or vector of sparsity levels) at which coefficients should be computed. If missing, then the default is use all sparsity levels of the passed bs

object.

... Other arguments (currently not used).

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coef.fs	Coefficient function for fs object.	

Description

Compute coefficients at a particular step of the forward stepwise path.

Usage

```
## S3 method for class fs
coef(object, s, ...)
```

Arguments

object The fs object, as produced by the fs function.

s The step (or vector of steps) of the path at which coefficients should be computed. Can be fractional, in which case interpolation is performed. If missing, then the default is use all steps of the passed fs object.

... Other arguments (currently not used).

Details

Note that at s=1, there is one nonzero coefficient, at s=2, there are two nonzero coefficients, etc. (This differs from the parametrization used in the coef.fs function in the R package selectiveInference, as the latter function delivers s-1 nonzero coefficients at step s, and was written to be consistent with the natural parametrization for the least angle regression path.)

coef.lasso	Coef function for lasso object.	

Description

Coef function for lasso object.

```
## S3 method for class lasso
coef(object, s = NULL)
```

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fs Forward stepwise regression.

Description

Compute the forward stepwise regression path.

Usage

```
fs(x, y, maxsteps = min(ncol(x), 2000), intercept = TRUE,
  normalize = TRUE, verbose = FALSE)
```

Arguments

x Matrix of predictors, of dimension (say) n x p.

y Vector of responses, of length (say) n.

maxsteps Maximum number of steps of the forward stepwise path to compute. Default is

min(p,2000).

intercept, normalize

Should an intercept be included in the regression model? Should the predictors

be normalized before computing the path? Default is TRUE for both.

verbose Should intermediate progress be printed out? Default is FALSE.

Details

This function implements forward stepwise regression, adding the predictor at each step that maximizes the absolute correlation between the predictors—once orthogonalized with respect to the current model—and the residual. This entry criterion is standard, and is equivalent to choosing the variable that achieves the biggest drop in RSS at each step; it is used, e.g., by the step function in R. Note that, for example, the lars package implements a stepwise option (with type="step"), but uses a (mildly) different entry criterion, based on maximal absolute correlation between the original (non-orthogonalized) predictors and the residual.

Value

A list with the following components:

- action, sign: vectors that give the index of the variable added at each step, and the sign of this variable's correlation with the residual upon entry df
- df: vector that gives the (naive) degrees of freedom of the model at each step, i.e., the number of active predictor variables (+ 1 if there is an intercept included)
- beta: matrix of regression coefficients for each step along the path, one column per step
- completepath: a boolean indicating whether the forward stepwise path was run to completion (as opposed to being stopped early because the max number of steps was achieved)
- bls: if the complete path was computed, this is a vector that gives the least squares coefficients of the full regression model
- x, y: the passed x and y
- bx, by: the means of the columns of x, and the mean of y
- intercept, normalize: the passed values for intercept and normalize

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Author(s)

Ryan Tibshirani

Examples

```
# Simulate some simple regression data with the first 5 coefficients
# being nonzero
set.seed(3)
n = 100
p = 20
ntest = 10000
xy.obj = sim.xy(n,p,nval=0,ntest=ntest,s=5,beta.type=2,snr=1)
x = xy.obj$x
y = xy.obj\$y
xtest = xy.obj$xtest
mutest = xy.obj$mutest
# Run forward stepwise regression for 8 steps
fs.obj = fs(x,y,intercept=FALSE,maxsteps=8,verbose=TRUE)
fs.beta = coef(fs.obj)
fs.supp = apply(fs.beta != 0, 2, which)
# Solve best subset selection for 8 sparsity levels
bs.obj = bs(x,y,intercept=FALSE,k=1:8,verbose=TRUE)
bs.beta = coef(bs.obj)
bs.supp = apply(bs.beta != 0, 2, which)
# Compare supports of the solutions with 5 and 8 variables
fs.supp[[5]]; bs.supp[[5]]
fs.supp[[8]]; bs.supp[[8]]
# Predict on test data and record risk
fs.pred = predict(fs.obj,newx=xtest)
bs.pred = predict(fs.obj,newx=xtest)
colMeans((fs.pred - mutest)^2)
colMeans((bs.pred - mutest)^2)
```

lasso

Lasso and friends.

Description

This is just a simple wrapper function around the <code>glmnet</code> function in the R package of the same name. Its purpose is twofold: (i) to provide functionality where the associated coef and predict methods always produce coefficients and predictions at exactly nlambda values, by default (the <code>glmnet</code> function may produce a path with less than nlambda lambda values, depending on the data); and (ii) to provide relaxed versions of the lasso (or ridge regression, or elastic net) solutions, defined by interpolating in between each solution and the least squares coefficients on the corresponding active set. The number of interpolations is governed by the nrelax argument; all other arguments are the same as in <code>glmnet</code>.

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Usage

```
lasso(x, y, alpha = 1, nrelax = 1, nlambda = 50,
lambda.min.ratio = ifelse(nrow(x) < ncol(x), 0.01, 1e-04), lambda = NULL,
intercept = TRUE, standardize = TRUE)</pre>
```

Arguments

nrelax

The number of interpolations to produce between the lasso (or ridge, or elastic net) solution, at each value of lambda, and the least squares coefficients on the corresponding active set. (The number of interpolations counts the endpoints inclusively, i.e., the lasso and least squares solutions.) Default is 1, which means that only the lasso solution is considered (no strict relaxations), at each value of lambda.

Details

Compute the lasso, ridge regression, or elastic net solutions in regression.

Author(s)

Trevor Hastie, Robert Tibshirani, Ryan Tibshirani

plot.many.sims

Plot the results over several simulation settings.

Description

Plot results over several sets of simulations, where the same methods are run over different simulations settings.

Usage

```
## S3 method for class many.sims
plot(file.list, grouping, snr.vec, method.nums = NULL,
  method.names = NULL, what = c("error", "prop", "nonzero"),
  tuning = c("validation", "oracle"), type = c("ave", "med"), std = TRUE,
  fig.dir = ".", file.name = NULL, w = 6, h = 6, mar = NULL,
  cols = 1:8, main = NULL, cex.main = 1.25, log = ifelse(what == "prop",
  "", "x"), legend.pos = "bottomright", tex.dir = NULL)
```

Arguments

file.list	vector of strings that point to saved sim objects (each object produced by a call to $sim.master$).
grouping	integer or factor vector indicating the grouping to use for the simulations. Within each group, the relative test error achieved by each method is plotted across the available SNR levels.
snr.vec	Vector giving the SNR levels considered within each group.
method.nums	the indices of the methods that should be plotted. Default is NULL, in which case all methods are plotted.

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method.names	the names of the methods that should be plotted. Default is NULL, in which case the names are extracted from the sim objects.		
what	one of "error", "prop", or "nonzero", indicating whether to plot the relative test error, test proportion of variance explained, or number of nonzeros, for each method across the given SNR levels. When what is "prop", the x-axis is population proportion of variance explained, instead of SNR. Default is "error".		
tuning	one of "validation" or "oracle", indicating whether the tuning parameter for each method should be chosen according to minimizing validation error, or according to minimizing test error. Default is "validation".		
type	Either "ave" or "med", indicating whether the average or median of the test error (or number of nonzeros, if what is "nonzero") should be displayed. Default is "ave".		
std	Should standard errors be displayed (in parantheses)? When type is set to "med", the median absolute deviations are shown in place of the standard errors. Default is TRUE.		
fig.dir	The figure directory to use. Default is ".".		
file.name	Vector of strings, giving the file names to use for the saved figures. Default is NULL, in which case the names "sim1", "sim2", etc. are used. (Extensions of "pdf" are always appended to the given file names.)		
w, h	the width and height (in inches) for the plots. Defaults are 6 for both.		
mar	the margins to use for the plots. Default is NULL, in which case the margins are set automatically (depending on whether not main is NULL).		
cols, main, cex	c.main, log, legend.pos graphical parameters.		
tex.dir	The latex directory to use. Default is NULL, which means that no lines of tex (includegraphics statements, for the figures created) will be produced.		

plot.sim

Plot function for sim object.

Description

Plot the results of a set of simulations, stored in an object of class sim (produced by sim.master).

```
## S3 method for class sim
plot(x, method.nums = 1:length(x$err.train.ave),
  method.names = NULL, type = c("ave", "med"), std = TRUE, cols = 1:8,
  main = NULL, cex.main = 1.25, legend.pos = c("topright"),
  make.pdf = FALSE, fig.dir = ".", file.name = "sim", w = 6, h = 6,
  mar = NULL)
```

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Arguments

x The sim object.

method.nums the indices of the methods that should be plotted. Default is to 1:length(x\$err.rel.ave),

which plots all methods.

method.names the names of the methods that should be plotted. Default is NULL, in which

case the names are extracted from the sim object.

type Either "ave" or "med", indicating whether the average or median of the relative

test error metric should be displayed. Default is "ave".

std Should standard errors be displayed (in parantheses)? When type is set to "med",

the median absolute deviations are shown in place of the standard errors. Default

is TRUE.

cols, main, cex.main, legend.pos

graphical parameters.

make.pdf Should a pdf be produced? Default is FALSE.

fig.dir, file.name

The figure directory and file name to use, only when make.pdf is TRUE. Defaults are "." and "sim". (An extension of "pdf" is always appended to the given file

name.)

w, h the width and height (in inches) for the plot, used only when make.pdf is TRUE.

Defaults are 6 for both.

mar the margins to use for the plot. Default is NULL, in which case the margins are

set automatically (depending on whether not main is NULL).

predict.bs

Predict function for bs object.

Description

Predict the response from a new set of predictor variables, using the coefficients from a particular step of the forward stepwise path.

Usage

```
## S3 method for class bs
predict(object, newx, s, ...)
```

Arguments

object The vs path object, as produced by the vs function.

newx Matrix of new predictor variables at which predictions should be made; if miss-

ing, the original (training) predictors are used.

s The sparsity level (or vector of sparsity levels) at which coefficients should be

computed. If missing, then the default is use all sparsity levels of the passed bs

object.

... Other arguments (currently not used).

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predict.fs	Predict function for fs object.	

Description

Predict the response from a new set of predictor variables, using the coefficients from a particular step of the forward stepwise path.

Usage

```
## S3 method for class fs
predict(object, newx, s, ...)
```

Arguments

object	The fs path object, as produced by the fs function.
newx	Matrix of new predictor variables at which predictions should be made; if missing, the original (training) predictors are used.
S	The step (or vector of steps) of the path at which coefficients should be computed. Can be fractional, in which case interpolation is performed. If missing, then the default is use all steps of the passed fs object.
	Other arguments (currently not used).

Details

Note that at s=1, there is one nonzero coefficient, at s=2, there are two nonzero coefficients, etc. (This differs from the parametrization used in the coef.fs function in the R package selectiveInference, as the latter function delivers s-1 nonzero coefficients at step s, and was written to be consistent with the natural parametrization for the least angle regression path.)

. 1asso Treatet junction for tasso object.	dict.lasso Predict function for lasso object.
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Description

Predict function for lasso object.

```
## S3 method for class lasso
predict(object, newx, s = NULL)
```

print.tex

n	rı	nt	•	1	m

Print function for sim object.

Description

Summarize and print the results of a set of simulations, stored an object of class sim (produced by sim.master).

Usage

```
## S3 method for class sim
print(x, type = c("ave", "med"), std = TRUE, digits = 3,
...)
```

Arguments

X	The sim object.
type	Either "ave" or "med", indicating whether the average or median of the relative test error metric should be displayed. Default is "ave".
std	Should standard errors be displayed (in parantheses)? When type is set to "med", the median absolute deviations are shown in place of the standard errors. Default is TRUE.
digits	Number of digits to display. Default is 3.
• • •	Other arguments (currently not used).

Print function for latex-style tables.

Description

Print a given table in format digestable by latex.

```
## S3 method for class tex
print(tab, tab.se = NULL, digits = 3, file = NULL,
    align = "1")
```

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sim.master

Master function for running simulations.

Description

Run a set of simulations with the specified configuration.

Usage

```
sim.master(n, p, nval, reg.funs, nrep = 50, seed = NULL, verbose = FALSE,
file = NULL, file.rep = 5, rho = 0, s = 5, beta.type = 1, snr = 1)
```

Arguments

seed

n, p The number of training observations, and the number of predictors.

nval The number of validation observations.

reg. funs This is a list of functions, representing the regression procedures to be used

(evaluated) in the simulation. Each element of the list must be a function that takes x, y (the training predictor matrix and response vector) as its only two (mandatory) arguments, and must return an object with associated coef and predict methods. The coef method must take obj (the returned object) and return a matrix of coefficients, with one column per tuning parameter value inherent to the regression method. The predict method must take obj, newx (the returned object and a new predictor matrix) and return a matrix of predictions, again with

one column per tuning parameter value inherent to the regression method.

Seed to be set for the overall random number generation, i.e., set before repetitions are begun (for reproducibility of the simulation results). Default is NULL,

which effectively sets no seed.

verbose Should intermediate progress be printed out? Default is FALSE.

file, file.rep Name of a file to which simulation results are saved (using saveRDS), and a number of repetitions after which intermediate results are saved. Setting file to

NULL is interpreted to mean that no simulations results should be saved; setting file.rep to 0 is interpreted to mean that simulations results should be saved at the very end, i.e., no intermediate saving. Defaults are NULL and 5, respectively.

rho, s, beta.type, snr

Arguments to pass to sim.xy; see the latter's help file for details.

Number of repetitions of which to average the results. Default is 50.

Value

A list with components err.train, err.val, err.test, err.rel, prop, risk, nzs, opt for the training error, validation error, test error, relative test error (test error divided by sigma^2), test proportion of variance explained, risk, number of selected nonzero coefficients, and relative optimism (difference in test error and training error, divided by training error). These are each lists of length N, where N is the number of regression methods under consideration (the length of reg.funs). The ith element of each list is then a matrix of dimension nrep x m, where m is the number of tuning parameters inherent to the ith method. The returned components err.train.ave, err.val.ave, etc. return the average of the training errors, validation errors, etc. over the nrep repetitions. Similarly for the components with postfixes .std, .med, .mad, which return the standard deviation, median, and median absolute

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deviation. The returned components with postfixes .tun.val and .tun.orc are each lists of length N, which return the appropriate metric when the tuning parameter for each regression method in each repetition is chosen by validation tuning (best validation error) or by oracle tuning (best test error).

Author(s)

Trevor Hastie, Robert Tibshirani, Ryan Tibshirani

References

The structure of this simulation code based on that from the conformalInference package.

See Also

```
sim.xy
```

Examples

```
# Simulate in simple regression setting with the first 5 coefficients
# being nonzero
set.seed(0)
n = 100
p = 20
nval = n
# Check for gurobi package
if (!require("gurobi",quietly=TRUE)) {
  stop("Package gurobi not installed (required here)!")
# Regression functions: lasso, forward stepwise, and best subset selection
reg.funs = list()
reg.funs[["Lasso"]] = function(x,y) lasso(x,y,intercept=FALSE,nlam=50)
reg.funs[["Stepwise"]] = function(x,y) fs(x,y,intercept=FALSE)
reg.funs[["Best subset"]] = function(x,y) bs(x,y,intercept=FALSE)
reg.funs[["Relaxed lasso"]] = function(x,y) lasso(x,y,intercept=FALSE,
                                                  nrelax=5,nlam=50)
# Run the master simulation function, for two different SNRs
sim.obj.hisnr = sim.master(n,p,nval,reg.funs=reg.funs,nrep=10,seed=0,
                           beta.type=2,s=5,snr=1,verbose=TRUE)
sim.obj.losnr = sim.master(n,p,nval,reg.funs=reg.funs,nrep=10,seed=0,
                           beta.type=2,s=5,snr=0.1,verbose=TRUE)
# Print simulation results
sim.obj.hisnr
sim.obj.losnr
# Plot simulation results, excluding relaxed lasso (it looks a bit crazy)
par(mfrow=c(1,2))
plot(sim.obj.hisnr, method.nums=1:3, main="SNR = 1", legend.pos="topright")
plot(sim.obj.losnr, method.nums=1:3, main="SNR = 0.1", legend.pos="topleft")
# Plot simulation results, including relaxed lasso (it looks a bit crazy)
par(mfrow=c(1,2))
plot(sim.obj.hisnr, main="SNR = 1", legend.pos="topright")
plot(sim.obj.losnr, main="SNR = 0.1", legend.pos="topleft")
```

sim.xy

sim.xy Predictors and responses generation.	
---	--

Description

Generate a predictor matrix x, and response vector y, following a specified setup. Actually, two pairs of predictors and responses are generated: one for training, and one for validation.

Usage

```
sim.xy(n, p, nval, rho = 0, s = 5, beta.type = 1, snr = 1)
```

Arguments

n, p	The number of training observations, and the number of predictors.
nval	The number of validation observations.
rho	Parameter that drives pairwise correlations of the predictor variables; specifically, predictors i and j have population correlation rho^abs(i-j). Default is 0.
S	number of nonzero coefficients in the underlying regression model. Default is 5. (Ignored if beta.type is 4, in which case the number of nonzero coefficients is 6; and if beta.type is 5, it is interpreted as a the number of strongly nonzero coefficients in a weak sparsity model.)
beta.type	Integer taking values in between 1 and 5, used to specify the pattern of nonzero coefficients in the underlying regression model; see details below. Default is 1.
snr	Desired signal-to-noise ratio (SNR), i.e., var(mu)/sigma^2 where mu is mean and sigma^2 is the error variance. The error variance is set so that the given SNR is achieved. Default is 1.

Details

The data model is: $Y \sim N(X\beta, \sigma^2 I)$. The predictor variables have covariance matrix Sigma, with (i,j)th entry rho^abs(i-j). The error variance sigma^2 is set according to the desired signal-to-noise ratio. The first 4 options for the nonzero pattern of the underlying regression coefficients beta follow the simulation setup in Bertsimas, King, and Mazumder (2016), and the 5th is a weak sparsity option:

- 1: beta has s components of 1, occurring at (roughly) equally-spaced indices in between 1 and
- 2: beta has its first s components equal to 1
- 3: beta has its first s components taking nonzero values, where the decay in a linear fashion from 10 to 0.5
- 4: beta has its first 6 components taking the nonzero values -10,-6, -2,2,6,10
- 5: beta has its first s components equal to 1, and the rest decaying to zero at an exponential rate

Value

A list with the following components: x, y, xval, yval, Sigma, beta, and sigma.

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Author(s)

Trevor Hastie, Rob Tibshirani, Ryan Tibshirani

References

Simulation setup based on "Best subset selection via a modern optimization lens" by Dimitris Bertsimas, Angela King, and Rahul Mazumder, Annals of Statistics, 44(2), 813-852, 2016.

Examples

```
# Simulate some simple regression data with the first 5 coefficients
# being nonzero
set.seed(3)
n = 100
p = 20
ntest = 10000
xy.obj = sim.xy(n,p,nval=0,ntest=ntest,s=5,beta.type=2,snr=1)
x = xy.obj$x
y = xy.obj\$y
xtest = xy.obj$xtest
mutest = xy.obj$mutest
# Run forward stepwise regression for 8 steps
fs.obj = fs(x,y,intercept=FALSE,maxsteps=8,verbose=TRUE)
fs.beta = coef(fs.obj)
fs.supp = apply(fs.beta != 0, 2, which)
# Solve best subset selection for 8 sparsity levels
bs.obj = bs(x,y,intercept=FALSE,k=1:8,verbose=TRUE)
bs.beta = coef(bs.obj)
bs.supp = apply(bs.beta != 0, 2, which)
\# Compare supports of the solutions with 5 and 8 variables
fs.supp[[5]]; bs.supp[[5]]
fs.supp[[8]]; bs.supp[[8]]
# Predict on test data and record risk
fs.pred = predict(fs.obj,newx=xtest)
bs.pred = predict(fs.obj,newx=xtest)
colMeans((fs.pred - mutest)^2)
colMeans((bs.pred - mutest)^2)
```

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