

Package ‘bestsubset’

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Title Tools for best subset selection in regression

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Depends ggplot2, glmnet, gurobi

Description An implementation of best subset selection in regression based on a mixed integer quadratic program formulation of the subset selection problem, and the Gurobi mixed integer program optimizer; also, tools for running simulations comparing best subset selection to other common sparse regression estimators such as the lasso and forward stepwise.

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bestsubset-package	<i>Simulations for best subset selection in regression</i>
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Description

Tools for running simulations that compare best subset selection in regression to other common sparse regression estimators such as the lasso and forward stepwise.

Details

The simulation setup is based on the paper: "Best subset selection via a modern optimization lens" by Dimitris Bertsimas, Angela King, and Rahul Mazumder, *Annals of Statistics*, 44(2), 813-852, 2016.

bs	<i>Best subset selection.</i>
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Description

Compute best subset selection solutions.

Usage

```
bs(x, y, k = 0:min(nrow(x), ncol(x)), intercept = TRUE,
  form = ifelse(nrow(x) < ncol(x), 2, 1), time.limit = 100, nruns = 50,
  maxiter = 1000, tol = 1e-04, polish = TRUE, verbose = FALSE)
```

Arguments

x	Matrix of predictors, of dimension (say) $n \times p$.
y	Vector of responses, of length (say) n .
k	Sparsity level, i.e., number of nonzero coefficients to allow in the subset regression model; can be a vector, in which case the best subset selection problem is solved for every value of the sparsity level. Default is $1:\min(n,p)$.
intercept	Should an intercept be included in the regression model? Default is TRUE.
form	Either of 1 or 2, specifying the formulation to use for best subset solution as a mixed integer quadratic program. Formulations 1 and 2 correspond to equations (2.5) and (2.6) in Bertsimas, King, and Mazumder (2016), see references below. Default is 1 if $n \geq p$, and 2 if $n < p$.
time.limit	The maximum amount of time (in seconds) to allow Gurobi to compute the subset selection solution at each value of k . Default is 100.
nruns	The number of runs of projected gradient descent to use, where each run begins at a random initialization for the coefficients. The best estimate over all these runs (achieving the lowest criterion value) is passed to Gurobi as a warm start. Default is 50.
maxiter	The maximum number of iterations for each run of projected gradient descent. Default is 1000.

tol	The tolerance for the relative difference in coefficients between iterations of projected gradient descent (the algorithm terminates when the relative difference is less than the specified tolerance). Default is 1e-4.
polish	Should the project gradient descent algorithm replace the estimate at each iteration by the least squares solution on the active set? Default is TRUE.
Should	intermediate progress be printed out? Default is FALSE.

Details

This function solves best subset selection program:

$$\min_{\beta} \|Y - X\beta\|_2^2 \text{ s.t. } \|\beta\|_0 \leq k$$

for a response vector Y and predictor matrix X . It follows the algorithm suggested by Bertsimas, King, and Mazumder (2016) (see below for the full reference): it first uses projected gradient descent to find an approximate solution to the above nonconvex program, and then calls Gurobi's MIO (mixed integer optimization) solver with this approximate solution as a warm start. There are two options for how to formulate best subset selection as a mixed integer quadratic program, one recommended when $n \geq p$, and the other when $n < p$. They correspond to equations (2.5) and (2.6) in the paper by Bertsimas, King, and Mazumder (2016), respectively.

Value

A list with the following components:

- beta: matrix of regression coefficients, one column per sparsity level
- status: vector of status strings returned by Gurobi's MIO solver, one element for each sparsity level
- k: vector of sparsity levels
- x, y: the passed x and y
- bx, by: the means of the columns of x, and the mean of y
- intercept: was an intercept included?

Author(s)

Ryan Tibshirani

References

This function utilizes the MIO formulation for subset selection as described in "Best subset selection via a modern optimization lens" by Dimitris Bertsimas, Angela King, and Rahul Mazumder, *Annals of Statistics*, 44(2), 813-852, 2016. This R implementation is based on Matlab code written by Rahul Mazumder.

Examples

```
# Simulate some simple regression data with the first 5 coefficients
# being nonzero
set.seed(0)
n = 100
p = 20
xy.obj = sim.xy(n,p,nval=0,s=5,beta.type=2,snr=1)
```

```

x = xy.obj$x
y = xy.obj$y

# Run forward stepwise regression for 8 steps
fs.obj = fs(x,y,intercept=FALSE,maxsteps=8,verbose=TRUE)
fs.beta = coef(fs.obj)
fs.supp = apply(fs.beta != 0, 2, which)

# Solve best subset selection for 8 sparsity levels
bs.obj = bs(x,y,intercept=FALSE,k=0:8,verbose=TRUE)
bs.beta = coef(bs.obj)
bs.supp = apply(bs.beta != 0, 2, which)

# Compare supports of the solutions with 5 and 8 variables
fs.supp[[6]]; bs.supp[[6]]
fs.supp[[9]]; bs.supp[[9]]

# Predict on test data and record test error
ntest = 10000
xy.obj.test = sim.xy(ntest,p,nval=0,s=5,beta.type=2,snr=1)
xtest = xy.obj.test$x
ytest = xy.obj.test$y

fs.pred = predict(fs.obj,newx=xtest)
bs.pred = predict(bs.obj,newx=xtest)
colMeans((fs.pred - ytest)^2)
colMeans((bs.pred - ytest)^2)

```

coef.bs

*Coefficient function for bs object.***Description**

Compute coefficients at a particular sparsity level of the best subset selection model.

Usage

```

## S3 method for class 'bs'
coef(object, s, ...)

```

Arguments

object	The bs object, as produced by the bs function.
s	The sparsity level (or vector of sparsity levels) at which coefficients should be computed. If missing, then the default is use all sparsity levels of the passed bs object.
...	Other arguments (currently not used).

coef.fs	<i>Coefficient function for fs object.</i>
---------	--

Description

Compute coefficients at a particular step of the forward stepwise path.

Usage

```
## S3 method for class 'fs'
coef(object, s, ...)
```

Arguments

object	The fs object, as produced by the fs function.
s	The step (or vector of steps) of the path at which coefficients should be computed. Can be fractional, in which case interpolation is performed. If missing, then the default is use all steps of the passed fs object.
...	Other arguments (currently not used).

Details

Note that at $s = 1$, there is one nonzero coefficient, at $s = 2$, there are two nonzero coefficients, etc. (This differs from the parametrization used in the `coef.fs` function in the R package `selectiveInference`, as the latter function delivers $s-1$ nonzero coefficients at step s , and was written to be consistent with the natural parametrization for the least angle regression path.)

coef.lasso	<i>Coef function for lasso object.</i>
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Description

Coef function for lasso object.

Usage

```
## S3 method for class 'lasso'
coef(object, s = NULL, gamma = NULL)
```

fs	<i>Forward stepwise regression.</i>
----	-------------------------------------

Description

Compute the forward stepwise regression path.

Usage

```
fs(x, y, maxsteps = min(ncol(x), 2000), intercept = TRUE,
  normalize = TRUE, verbose = FALSE)
```

Arguments

x	Matrix of predictors, of dimension (say) $n \times p$.
y	Vector of responses, of length (say) n .
maxsteps	Maximum number of steps of the forward stepwise path to compute. Default is $\min(p, 2000)$.
intercept, normalize	Should an intercept be included in the regression model? Should the predictors be normalized before computing the path? Default is TRUE for both.
verbose	Should intermediate progress be printed out? Default is FALSE.

Details

This function implements forward stepwise regression, adding the predictor at each step that maximizes the absolute correlation between the predictors—once orthogonalized with respect to the current model—and the residual. This entry criterion is standard, and is equivalent to choosing the variable that achieves the biggest drop in RSS at each step; it is used, e.g., by the `step` function in R. Note that, for example, the `lars` package implements a stepwise option (with `type="step"`), but uses a (mildly) different entry criterion, based on maximal absolute correlation between the original (non-orthogonalized) predictors and the residual.

Value

A list with the following components:

- `action, sign`: vectors that give the index of the variable added at each step, and the sign of this variable's correlation with the residual upon entry `df`
- `df`: vector that gives the (naive) degrees of freedom of the model at each step, i.e., the number of active predictor variables (+ 1 if there is an intercept included)
- `beta`: matrix of regression coefficients for each step along the path, one column per step
- `completepath`: a boolean indicating whether the forward stepwise path was run to completion (as opposed to being stopped early because the max number of steps was achieved)
- `bls`: if the complete path was computed, this is a vector that gives the least squares coefficients of the full regression model
- `x, y`: the passed `x` and `y`
- `bx, by`: the means of the columns of `x`, and the mean of `y`
- `intercept, normalize`: the passed values for `intercept` and `normalize`

Author(s)

Ryan Tibshirani

Examples

```
# Simulate some simple regression data with the first 5 coefficients
# being nonzero
set.seed(0)
n = 100
p = 20
xy.obj = sim.xy(n,p,nval=0,s=5,beta.type=2,snr=1)
x = xy.obj$x
y = xy.obj$y

# Run forward stepwise regression for 8 steps
fs.obj = fs(x,y,intercept=FALSE,maxsteps=8,verbose=TRUE)
fs.beta = coef(fs.obj)
fs.supp = apply(fs.beta != 0, 2, which)

# Solve best subset selection for 8 sparsity levels
bs.obj = bs(x,y,intercept=FALSE,k=0:8,verbose=TRUE)
bs.beta = coef(bs.obj)
bs.supp = apply(bs.beta != 0, 2, which)

# Compare supports of the solutions with 5 and 8 variables
fs.supp[[6]]; bs.supp[[6]]
fs.supp[[9]]; bs.supp[[9]]

# Predict on test data and record test error
ntest = 10000
xy.obj.test = sim.xy(ntest,p,nval=0,s=5,beta.type=2,snr=1)
xtest = xy.obj.test$x
ytest = xy.obj.test$y

fs.pred = predict(fs.obj,newx=xtest)
bs.pred = predict(bs.obj,newx=xtest)
colMeans((fs.pred - ytest)^2)
colMeans((bs.pred - ytest)^2)
```

lasso

*Lasso and friends.***Description**

This is just a simple wrapper function around the [glmnet](#) function in the R package of the same name. Its purpose is twofold: (i) to provide functionality where the associated `coef` and `predict` methods always produce coefficients and predictions at exactly `nlambda` values, by default (the [glmnet](#) function may produce a path with less than `nlambda` `lambda` values, depending on the data); and (ii) to provide relaxed versions of the lasso (or ridge regression, or elastic net) solutions, defined by interpolating in between each solution and the least squares coefficients on the corresponding active set. The number of interpolations is governed by the `nrelax` argument; all other arguments are the same as in [glmnet](#).

Usage

```
lasso(x, y, alpha = 1, nrelax = 1, nlambdas = 50,
      lambda.min.ratio = ifelse(nrow(x) < ncol(x), 0.01, 1e-04), lambda = NULL,
      intercept = TRUE, standardize = TRUE)
```

Arguments

nrelax The number of interpolations to produce between the lasso (or ridge, or elastic net) solution, at each value of lambda, and the least squares coefficients on the corresponding active set. (The number of interpolations counts the endpoints inclusively, i.e., the lasso and least squares solutions.) Default is 1, which means that only the lasso solution is considered (no strict relaxations), at each value of lambda.

Details

Compute the lasso, ridge regression, or elastic net solutions in regression.

Author(s)

Trevor Hastie, Robert Tibshirani, Ryan Tibshirani

plot.from.file	<i>Plot the results over several simulation settings.</i>
----------------	---

Description

Plot results over several sets of simulations saved in files, where the same methods are run over different simulations settings.

Usage

```
## S3 method for class 'from.file'
plot(file.list, row = c("beta", "rho", "snr"),
     col = c("rho", "beta", "snr"), method.nums = NULL, method.names = NULL,
     what = c("error", "risk", "prop", "nonzero"), rel.to = NULL,
     tuning = c("validation", "oracle"), type = c("ave", "med"), std = TRUE,
     lwd = 1, pch = 19, main = NULL, ylim = NULL, make.pdf = FALSE,
     fig.dir = ".", file.name = "sim", w = 8, h = 10)
```

Arguments

file.list	Vector of strings that point to saved sim objects (each object produced by a call to sim.master).
row, col	One of "beta", "rho", or "snr", indicating the variables for the rows and columns of plotting grid; note that row and col must be different. Default is row="beta" and col="rho", so that the plotting grid displays the metric specified in what (default is relative test error, see below) versus the SNR, in a plotting grid with the coefficient types across the rows, and the correlation levels across the columns.
method.nums	The indices of the methods that should be plotted. Default is NULL, in which case all methods are plotted.

method.names	The names of the methods that should be plotted. Default is NULL, in which case the names are extracted from the sim objects.
what	One of "error", "risk", "prop", or "nonzero", indicating whether to plot the relative test error, test proportion of variance explained, or number of nonzeros, for each method across the given SNR levels. When what is "prop", the x-axis is population proportion of variance explained, instead of SNR. Default is "error".
tuning	Either "validation" or "oracle", indicating whether the tuning parameter for each method should be chosen according to minimizing validation error, or according to minimizing test error. Default is "validation".
type	Either "ave" or "med", indicating whether the average or median of the test error (or number of nonzeros, if what is "nonzero") should be displayed. Default is "ave".
std	Should standard errors be displayed (in parantheses)? When type is set to "med", the median absolute deviations are shown in place of the standard errors. Default is TRUE.
lwd, pch, main, ylim	graphical parameters.
make.pdf	Should a pdf be produced? Default is FALSE.
fig.dir, file.name	The figure directory and file name to use, only when make.pdf is TRUE. Defaults are "." and "sim". (An extension of "pdf" is always appended to the given file name.)
w, h	the width and height (in inches) for the plot, used only when make.pdf is TRUE. Defaults are 8 and 10, respectively.

plot.sim

Plot function for sim object.

Description

Plot the results of a set of simulations, stored in an object of class sim (produced by [sim.master](#)).

Usage

```
## S3 method for class 'sim'
plot(x, method.nums = 1:length(x$serr.test),
     method.names = NULL, what = c("error", "risk"), type = c("ave", "med"),
     std = TRUE, lwd = 1, pch = 19, main = NULL, legend = TRUE,
     make.pdf = FALSE, fig.dir = ".", file.name = "sim", w = 6, h = 6)
```

Arguments

x	The sim object.
method.nums	the indices of the methods that should be plotted. Default is to 1:length(x\$serr.test), which plots all methods.
method.names	the names of the methods that should be plotted. Default is NULL, in which case the names are extracted from the sim object.
what	Either "error" or "risk", indicating whether the relative test error or relative risk should be displayed. Default is "error".

type	Either "ave" or "med", indicating whether the average or median of the relative test error metric should be displayed. Default is "ave".
std	Should standard errors be displayed (in parantheses)? When type is set to "med", the median absolute deviations are shown in place of the standard errors. Default is TRUE.
lwd, pch, main, legend	graphical parameters.
make.pdf	Should a pdf be produced? Default is FALSE.
fig.dir, file.name	The figure directory and file name to use, only when make.pdf is TRUE. Defaults are "." and "sim". (An extension of "pdf" is always appended to the given file name.)
w, h	the width and height (in inches) for the plot, used only when make.pdf is TRUE. Defaults are 6 for both.

predict.bs

Predict function for bs object.

Description

Predict the response from a new set of predictor variables, using the coefficients from a particular step of the forward stepwise path.

Usage

```
## S3 method for class 'bs'
predict(object, newx, s, ...)
```

Arguments

object	The vs path object, as produced by the vs function.
newx	Matrix of new predictor variables at which predictions should be made; if missing, the original (training) predictors are used.
s	The sparsity level (or vector of sparsity levels) at which coefficients should be computed. If missing, then the default is use all sparsity levels of the passed bs object.
...	Other arguments (currently not used).

predict.fs	<i>Predict function for fs object.</i>
------------	--

Description

Predict the response from a new set of predictor variables, using the coefficients from a particular step of the forward stepwise path.

Usage

```
## S3 method for class 'fs'
predict(object, newx, s, ...)
```

Arguments

object	The fs path object, as produced by the fs function.
newx	Matrix of new predictor variables at which predictions should be made; if missing, the original (training) predictors are used.
s	The step (or vector of steps) of the path at which coefficients should be computed. Can be fractional, in which case interpolation is performed. If missing, then the default is use all steps of the passed fs object.
...	Other arguments (currently not used).

Details

Note that at $s = 1$, there is one nonzero coefficient, at $s = 2$, there are two nonzero coefficients, etc. (This differs from the parametrization used in the `coef.fs` function in the R package `selectiveInference`, as the latter function delivers $s-1$ nonzero coefficients at step s , and was written to be consistent with the natural parametrization for the least angle regression path.)

predict.lasso	<i>Predict function for lasso object.</i>
---------------	---

Description

Predict function for lasso object.

Usage

```
## S3 method for class 'lasso'
predict(object, newx, s = NULL)
```

print.sim	<i>Print function for sim object.</i>
-----------	---------------------------------------

Description

Summarize and print the results of a set of simulations, stored in an object of class sim (produced by `sim.master`).

Usage

```
## S3 method for class 'sim'
print(x, what = c("error", "risk"), type = c("ave", "med"),
      std = TRUE, digits = 3, ...)
```

Arguments

x	The sim object.
what	Either "error" or "risk", indicating whether the relative test error or relative risk should be displayed. Default is "error".
type	Either "ave" or "med", indicating whether the average or median of the relative test error metric should be displayed. Default is "ave".
std	Should standard errors be displayed (in parantheses)? When type is set to "med", the median absolute deviations are shown in place of the standard errors. Default is TRUE.
digits	Number of digits to display. Default is 3.
...	Other arguments (currently not used).

print.tex	<i>Print function for latex-style tables.</i>
-----------	---

Description

Print a given table in format digestable by latex.

Usage

```
## S3 method for class 'tex'
print(tab, tab.se = NULL, digits = 3, file = NULL,
      align = "l")
```

sim.master	<i>Master function for running simulations.</i>
------------	---

Description

Run a set of simulations with the specified configuration.

Usage

```
sim.master(n, p, nval, reg.funs, nrep = 50, seed = NULL, verbose = FALSE,
  file = NULL, file.rep = 5, rho = 0, s = 5, beta.type = 1, snr = 1,
  reorder = FALSE)
```

Arguments

n, p	The number of training observations, and the number of predictors.
nval	The number of validation observations.
reg.funs	This is a list of functions, representing the regression procedures to be used (evaluated) in the simulation. Each element of the list must be a function that takes x, y (the training predictor matrix and response vector) as its only two (mandatory) arguments, and must return an object with associated coef and predict methods. The coef method must take obj (the returned object) and return a matrix of coefficients, with one column per tuning parameter value inherent to the regression method. The predict method must take obj, newx (the returned object and a new predictor matrix) and return a matrix of predictions, again with one column per tuning parameter value inherent to the regression method.
seed	Seed to be set for the overall random number generation, i.e., set before repetitions are begun (for reproducibility of the simulation results). Default is NULL, which effectively sets no seed.
verbose	Should intermediate progress be printed out? Default is FALSE.
file, file.rep	Name of a file to which simulation results are saved (using saveRDS), and a number of repetitions after which intermediate results are saved. Setting file to NULL is interpreted to mean that no simulations results should be saved; setting file.rep to 0 is interpreted to mean that simulations results should be saved at the very end, i.e., no intermediate saving. Defaults are NULL and 5, respectively.
rho, s, beta.type, snr, reorder.	Arguments to pass to sim.xy ; see the latter's help file for details.
Number	of repetitions of which to average the results. Default is 50.

Value

A list with components err.train, err.val, err.test, prop, risk, nzs, opt for the training error, validation error, test error, test proportion of variance explained, risk, number of selected nonzero coefficients, and relative optimism (difference in test error and training error, divided by training error). These are each lists of length N, where N is the number of regression methods under consideration (the length of reg.funs). The ith element of each list is then a matrix of dimension nrep x m, where m is the number of tuning parameters inherent to the ith method.

Author(s)

Trevor Hastie, Robert Tibshirani, Ryan Tibshirani

References

The structure of this simulation code based on that from the conformalInference package.

See Also

[sim.xy](#)

Examples

```
# Simulate in simple regression setting with the first 5 coefficients
# being nonzero
set.seed(0)
n = 100
p = 20
nval = n

# Check for gurobi package
if (!require("gurobi",quietly=TRUE)) {
  stop("Package gurobi not installed (required here)!")
}

# Regression functions: lasso, forward stepwise, and best subset selection
reg.funs = list()
reg.funs[["Lasso"]] = function(x,y) lasso(x,y,intercept=FALSE,nlam=50)
reg.funs[["Stepwise"]] = function(x,y) fs(x,y,intercept=FALSE)
reg.funs[["Best subset"]] = function(x,y) bs(x,y,intercept=FALSE)
reg.funs[["Relaxed lasso"]] = function(x,y) lasso(x,y,intercept=FALSE,
                                                  nrelax=5,nlam=50)

# Run the master simulation function, for two different SNRs
sim.obj.hisnr = sim.master(n,p,nval,reg.funs=reg.funs,nrep=10,seed=0,
                          beta.type=2,s=5,snr=1,verbose=TRUE)
sim.obj.losnr = sim.master(n,p,nval,reg.funs=reg.funs,nrep=10,seed=0,
                          beta.type=2,s=5,snr=0.1,verbose=TRUE)

# Print simulation results
sim.obj.hisnr
sim.obj.losnr

# Plot simulation results, excluding relaxed lasso
par(mfrow=c(1,2))
plot(sim.obj.hisnr, method.num=1:3, main="SNR = 1", legend.pos="topright")
plot(sim.obj.losnr, method.num=1:3, main="SNR = 0.1", legend.pos="topleft")

# Plot simulation results, including relaxed lasso (it looks a bit crazy)
par(mfrow=c(1,2))
plot(sim.obj.hisnr, method.num=1:4, main="SNR = 1", legend.pos="topright")
plot(sim.obj.losnr, method.num=1:4, main="SNR = 0.1", legend.pos="topleft")
```

sim.xy

*Predictors and responses generation.***Description**

Generate a predictor matrix x , and response vector y , following a specified setup. Actually, two pairs of predictors and responses are generated: one for training, and one for validation.

Usage

```
sim.xy(n, p, nval, rho = 0, s = 5, beta.type = 1, snr = 1,
       reorder = FALSE)
```

Arguments

<code>n</code> , <code>p</code>	The number of training observations, and the number of predictors.
<code>nval</code>	The number of validation observations.
<code>rho</code>	Parameter that drives pairwise correlations of the predictor variables; specifically, predictors i and j have population correlation $\rho^{\text{abs}(i-j)}$. Default is 0.
<code>s</code>	number of nonzero coefficients in the underlying regression model. Default is 5. (Ignored if <code>beta.type</code> is 4, in which case the number of nonzero coefficients is 6; and if <code>beta.type</code> is 5, it is interpreted as a the number of strongly nonzero coefficients in a weak sparsity model.)
<code>beta.type</code>	Integer taking values in between 1 and 5, used to specify the pattern of nonzero coefficients in the underlying regression model; see details below. Default is 1.
<code>snr</code>	Desired signal-to-noise ratio (SNR), i.e., $\text{var}(\mu)/\sigma^2$ where μ is mean and σ^2 is the error variance. The error variance is set so that the given SNR is achieved. Default is 1.
<code>reorder</code>	Reorder the variables at random? Default is FALSE.

Details

The data model is: $Y \sim N(X\beta, \sigma^2 I)$. The predictor variables have covariance matrix Σ , with (i,j) th entry $\rho^{\text{abs}(i-j)}$. The error variance σ^2 is set according to the desired signal-to-noise ratio. The first 4 options for the nonzero pattern of the underlying regression coefficients β follow the simulation setup in Bertsimas, King, and Mazumder (2016), and the 5th is a weak sparsity option:

- 1: β has s components of 1, occurring at (roughly) equally-spaced indices in between 1 and p
- 2: β has its first s components equal to 1
- 3: β has its first s components taking nonzero values, where the decay in a linear fashion from 10 to 0.5
- 4: β has its first 6 components taking the nonzero values -10,-6, -2,2,6,10
- 5: β has its first s components equal to 1, and the rest decaying to zero at an exponential rate

Value

A list with the following components: x, y, xval, yval, Sigma, beta, and sigma.

Author(s)

Trevor Hastie, Rob Tibshirani, Ryan Tibshirani

References

Simulation setup based on "Best subset selection via a modern optimization lens" by Dimitris Bertsimas, Angela King, and Rahul Mazumder, Annals of Statistics, 44(2), 813-852, 2016.

Examples

```
# Simulate some simple regression data with the first 5 coefficients
# being nonzero
set.seed(0)
n = 100
p = 20
xy.obj = sim.xy(n,p,nval=0,s=5,beta.type=2,snr=1)
x = xy.obj$x
y = xy.obj$y

# Run forward stepwise regression for 8 steps
fs.obj = fs(x,y,intercept=FALSE,maxsteps=8,verbose=TRUE)
fs.beta = coef(fs.obj)
fs.supp = apply(fs.beta != 0, 2, which)

# Solve best subset selection for 8 sparsity levels
bs.obj = bs(x,y,intercept=FALSE,k=0:8,verbose=TRUE)
bs.beta = coef(bs.obj)
bs.supp = apply(bs.beta != 0, 2, which)

# Compare supports of the solutions with 5 and 8 variables
fs.supp[[6]]; bs.supp[[6]]
fs.supp[[9]]; bs.supp[[9]]

# Predict on test data and record test error
ntest = 10000
xy.obj.test = sim.xy(ntest,p,nval=0,s=5,beta.type=2,snr=1)
xtest = xy.obj.test$x
ytest = xy.obj.test$y

fs.pred = predict(fs.obj,newx=xtest)
bs.pred = predict(bs.obj,newx=xtest)
colMeans((fs.pred - ytest)^2)
colMeans((bs.pred - ytest)^2)
```

tune.and.aggregate	<i>Tuning and aggregation function for sim object.</i>
--------------------	--

Description

Tune and aggregate a given metric across a set of simulations, stored in a sim object (produced by [sim.master](#)).

Usage

```
tune.and.aggregate(obj, z, tune = TRUE)
```

Arguments

<code>obj</code>	The sim object.
<code>z</code>	The metric to be tuned. Should be a list of length N , where N is the number of methods under consideration in the simulation, and in the i th element of the list should be a matrix of dimension $nrep \times m$, where $nrep$ is the number of repetitions in the simulation, and m is the number of tuning parameters for the i th method.
<code>tune</code>	Either TRUE or FALSE, indicating whether the metric should be tuned; if FALSE, then it is only aggregated (for each value of the tuning parameter). Default is TRUE.

Value

A list with components `z.ave`, `z.std`, `z.med`, `z.mad`, `z.val`, `z.ora`, `z.val.ave`, `z.val.std`, `z.val.med`, `z.val.mad`, `z.ora.ave`, `z.ora.std`, `z.ora.med`, `z.ora.mad`. The elements `z.ave`, `z.std`, `z.med`, `z.mad` are lists of length N , where N is the number of methods in the simulation; in the i th element of `z.ave` is a vector of length m , the number of tuning parameters for the i th method, giving the averages of the metric across the repetitions for each tuning parameter value; similarly `z.std` contains standard errors, `z.med` contains medians, and `z.mad` contains median absolute deviations. The elements `z.val`, `z.ora` are matrices of dimension $nrep \times N$, where $nrep$ is the number of repetitions, whose rows contain the metric after it has been tuned on each repetition by selecting the tuning parameter for each method in one of two ways: validation tuning, where the tuning parameter is selected to minimize prediction error on the validation set, and oracle tuning, where the tuning parameter is selected to minimize average test error. The elements named `z.val.xxx`, where `xxx` is one of `ave`, `std`, `med`, or `mad`, are each vectors of length N , containing the average of the metric for each method under validation tuning; similarly for the postfixes `std`, `med`, and `mad`; and for the elements named `z.ora.xxx`.

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