

8.

$P'10 \longrightarrow P10$

Let a be any number and $b = 0$. Then by P'10, we obtain P10:

Let P denote the positive numbers. For any number a , one and only one of the following holds:

(i) $a = 0$

(ii) $0 < a \implies a$ is in the collection P

(iii) $a < 0 \implies -a > 0 \implies -a$ is in the collection P

$P'11 \wedge P'12 \longrightarrow P11$

Let a and b be any numbers such that $0 < a$ and $0 < b$. By P'12, $(0 < a) \implies (0 + b < a + b)$. By P'11, $(0 < b$ and $b < a + b) \implies (0 < a + b)$, so we obtain P11:

Let P denote the positive numbers. If a and b are in the collection P , then $a + b$ is in P .

$P'13 \longrightarrow P12$

Let a and b be any numbers such that $0 < a$ and $0 < b$. By P'13, $0(b) < a(b) \implies 0 < ab$. Thus we obtain P12:

Let P denote the positive numbers. If a and b are in the collection P , then ab is in P .