

Input Parameters:

N : no of Machine for sale

C : no of dollars at start of Period

D : Planning Period

D_i : day on which the M/c is for sale

P_i : Purchasing Price

R_i : Reselling Price

G_i : Profit Per day

Problem approach

a. I have created a network with sink and source including N (no of M/c) with ascending order day of availability of M/c.

b. let suppose source is a virtual M/c with

$$D_{\text{source}} = 0$$

$$P_{\text{source}} = 0$$

$$R_{\text{source}} = 0$$

$$G_{\text{source}} = 0$$

c. Let suppose sink is a virtual M/c with

$$D_{\text{sink}} = D+1$$

$$P_{\text{sink}} = 0$$

$$R_{\text{sink}} = 0$$

$$G_{\text{sink}} = 0$$

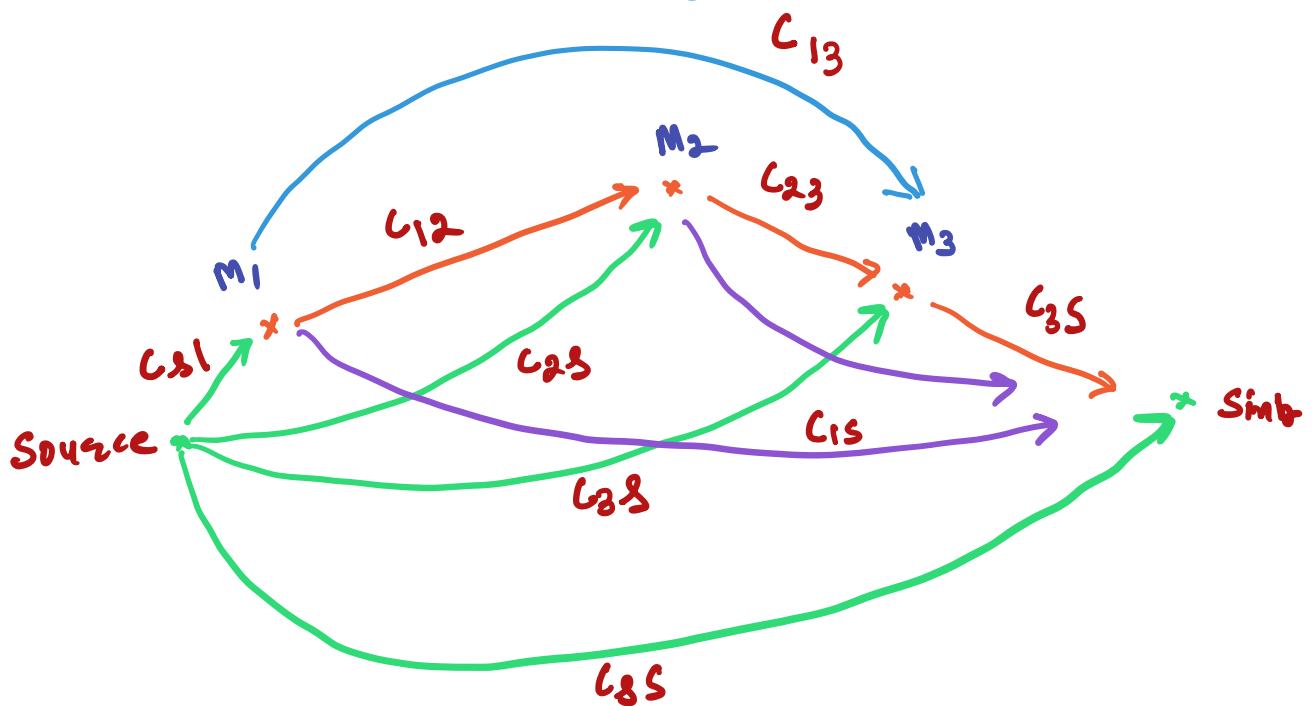


fig. (1)

d. calculations of C_{ij}

(i) when $i = \text{source}$ and $j = 1 \dots N$

$$C_{sj} = C - P_j$$

$\left[\begin{array}{l} C = \text{initial dollar} \\ P_j = \text{Purchasing Price} \\ \text{of } J^{\text{th}} \text{ } M/C \end{array} \right]$

(ii) when $i, j \in [1 \dots N]$ and $i < j$

$$C_{ij} = C - P_i + R_i + \max(D_j - D_{i-1}, 0) * G_i - P_j$$

(iii) when $i = 1 \dots N$ and $j = \text{Sink}$

$$C_{i\text{Sink}} = C - P_i + R_i + (D - D_i) * G_i$$

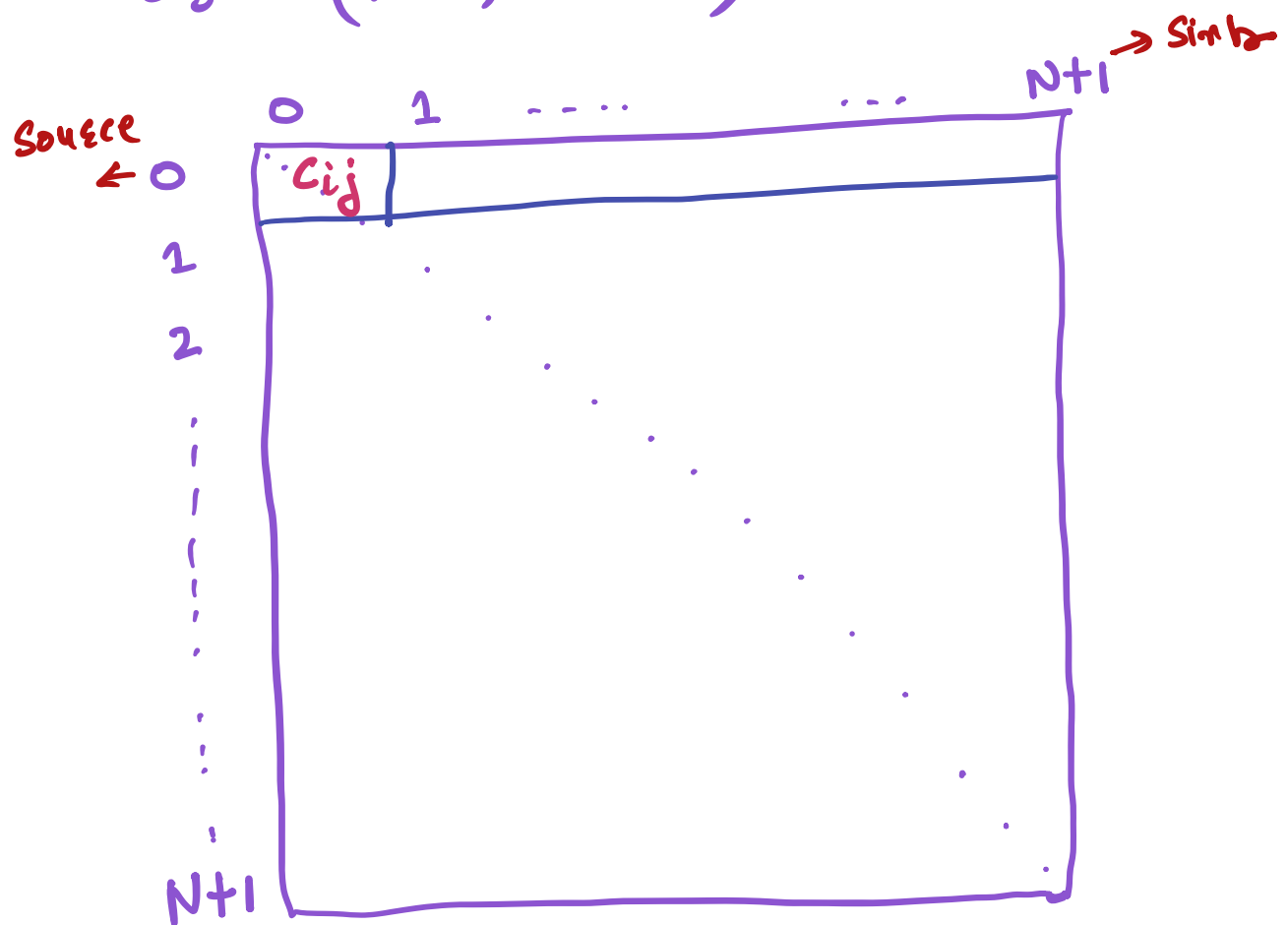
(iv) when $i = \text{source}$, $j = \text{Sink}$

$$C_{\text{source, Sink}} = C$$

(v) when $i \geq j$

$$C_{ij} = -10000$$

Now we have a Matrix of
Size $(N+2, N+2)$



Model formulation

$$\text{obj } z = \max \sum_i \sum_j c_{ij} \cdot x_{ij}$$

OR

$$\text{obj } z = - \left[\text{minimize } \sum_i \sum_j (-c_{ij}) \cdot x_{ij} \right]$$

$$x_{ij} = [0, 1]$$

Subject to :-

$$\sum_j x_{ij} - \sum_j x_{ji} = \begin{cases} 1 & \text{if } i = 0 \\ -1 & \text{if } i = N+1 \\ 0 & \text{otherwise} \end{cases}$$

* Above formulation become shortest path problem between source and sink.

Solution strategy.

1. we have a directed graph with negative/positive weights on the edges with single source.
2. I'm choosing Floyd-warshall algo for solving this problem.