

**A Project Report on**  
**“Phase variable model & dq model of Induction Motor “**  
**“Open loop V/F speed Control Technique with Voltage fed Inverter”**  
**“Direct Rotor field FOC using SPWM technique”**  
**“DIRECT TORQUE CONTROL OF INDUCTION MOTOR”**

**Submitted in partial fulfillment of the requirement for the Second Semester of**

**Master of Technology**  
**In**  
**“Power Engineering”**  
**Of**  
**Indian Institute of Technology, Ropar**

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## Aim- Phase variable model & dq model of IM (synchronous reference frame)

Q1: Compare the torque, speed and stator currents of both the models (Report in the docx file)

Q2: Find the slip of the motor under full load condition from both the models.

Q3: In the dq model find the magnitude of the  $V_{qds}$ ,  $I_{qds}$ ,  $I_{qdr}$ ,  $\lambda_{qds}$ ,  $\lambda_{qdr}$  when 2/3 constant is used for abc to qd0 transformation and compare it with  $V_{abs}$ ,  $I_{abs}$ ,  $I_{abr}$ ,  $\lambda_{abs}$ ,  $\lambda_{abr}$ . Do similar exercise when sqrt (2/3) constant is used for the transformation

Q.4 using three phase inverter which is operated using Sine PWM technique at 0.9 modulation index. (use the dc link voltage judiciously). Operate the inverter in such a way that the torque ripple is less than 5% of the nominal. Use open loop v/f control technique to operate the motor in both the direction of speed and two different speed reference.

Q.5 implement direct Rotor field FOC using SPWM technique.

Q.6 Direct Torque control of induction motor

## Ratings and Parameters

Rated Voltage [V]	V	460
Rated Frequency [Hz]	$f$	60
Rated Speed [rpm]	$\omega_m$	1760
Stator Resistance [ $\Omega$ ]	$R_s$	0.09961
Rotor Resistance [ $\Omega$ ]	$R_r$	0.05837
Mutual Inductance [H]	$L_m$	0.03039
Stator Leakage Inductance [H]	$L_{ls}$	0.000867
Rotor Leakage Inductance [H]	$L_{lr}$	0.000867
Motor Inertia [ $\text{kg.m}^2$ ]	$J$	0.4
Damping Coefficient [Nms/rad]	$B$	0.00005

## Theory: -

### 1)PHASE VARIABLE MODEL

The modelling of the electromagnetic part which contains stator and rotor was done in the a-b-c three-phase stationary frame.

Electromagnetic Part

The three-phase stator voltages  $V_{as}$ ,  $V_{bs}$ ,  $V_{cs}$  with respect to the motor neutral point can be given as:

$$\begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \end{bmatrix} = R_s \begin{bmatrix} i_{as} \\ i_{bs} \\ i_{cs} \end{bmatrix} + \frac{d}{dt} \begin{bmatrix} \psi_{as} \\ \psi_{bs} \\ \psi_{cs} \end{bmatrix} \quad \begin{bmatrix} \psi_{as} \\ \psi_{bs} \\ \psi_{cs} \end{bmatrix} = [L_s] \begin{bmatrix} i_{as} \\ i_{bs} \\ i_{cs} \end{bmatrix} + [L_{sr}] \begin{bmatrix} i_{ar} \\ i_{br} \\ i_{cr} \end{bmatrix}$$

where  $R_s$  is the stator resistance  $i_{as}$ ,  $i_{bs}$ ,  $i_{cs}$  are the stator phase currents,  $\psi_{as}$ ,  $\psi_{bs}$ ,  $\psi_{cs}$  are the three-phase stator flux linkages,  $i_{ar}$ ,  $i_{br}$ ,  $i_{cr}$  are the rotor phase currents,  $[L_s]$  and  $[L_{sr}]$  can be written as

$$[L_s] = \begin{bmatrix} L_{ls} + L_{ms} & -\frac{L_{ms}}{2} & -\frac{L_{ms}}{2} \\ -\frac{L_{ms}}{2} & L_{ls} + L_{ms} & -\frac{L_{ms}}{2} \\ -\frac{L_{ms}}{2} & -\frac{L_{ms}}{2} & L_{ls} + L_{ms} \end{bmatrix} \quad [L_{sr}] = L_{sr} \begin{bmatrix} \cos \theta_r & \cos(\theta_r + \frac{2\pi}{3}) & \cos(\theta_r - \frac{2\pi}{3}) \\ \cos(\theta_r - \frac{2\pi}{3}) & \cos \theta_r & \cos(\theta_r + \frac{2\pi}{3}) \\ \cos(\theta_r + \frac{2\pi}{3}) & \cos(\theta_r - \frac{2\pi}{3}) & \cos \theta_r \end{bmatrix}$$

On the rotor part, the rotor windings for a squirrel-cage type induction motor are short circuit. Then, the three-phase rotor voltage equation can be written as

$$\begin{bmatrix} \psi_{ar} \\ \psi_{br} \\ \psi_{cr} \end{bmatrix} = [L_{sr}]^T \begin{bmatrix} i_{as} \\ i_{bs} \\ i_{cs} \end{bmatrix} + [L_r] \begin{bmatrix} i_{ar} \\ i_{br} \\ i_{cr} \end{bmatrix} \quad [L_r] = \begin{bmatrix} L_{lr} + L_{mr} & -\frac{L_{mr}}{2} & -\frac{L_{mr}}{2} \\ -\frac{L_{mr}}{2} & L_{lr} + L_{mr} & -\frac{L_{mr}}{2} \\ -\frac{L_{mr}}{2} & -\frac{L_{mr}}{2} & L_{lr} + L_{mr} \end{bmatrix}$$

where  $L_{lr}$  and  $L_{mr}$  are, respectively, the leakage and magnetizing inductance of the rotor winding. Assuming the three-phase stator current are balanced, that is  $i_{as} + i_{bs} + i_{cs} = 0$

motor developed electromagnetic torque

$$T_e = \frac{P}{2} \frac{dE_c}{d\theta_r} = \frac{P}{2} [i_{as} \ i_{bs} \ i_{cs}] \frac{d[L_{sr}]}{d\theta_r} \begin{bmatrix} i_{ar} \\ i_{br} \\ i_{cr} \end{bmatrix}$$

## 2. Modelling of Induction Motor [dq Model in Synchronous reference frame]

The dynamic model of the induction motor is derived in terms of direct and quadrature axes components. This method is required to obtain the conceptual simplicity with the two sets of the windings, one is on the stator and the other is on the rotor.

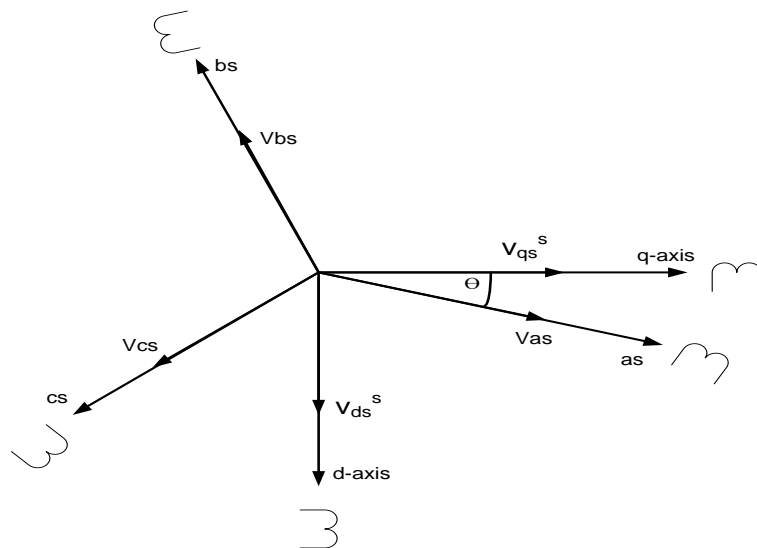
The  $(as-bs-cs)$  components resolved into voltages  $v_{ds}^s$  and  $v_{qs}^s$  and can be represented in matrix form as:

$$\begin{bmatrix} v_{qs}^s \\ v_{ds}^s \\ v_{os}^s \end{bmatrix} = \begin{bmatrix} \cos \theta & \cos(\theta - 120) & \cos(\theta + 120) \\ \sin \theta & \sin(\theta - 120) & \sin(\theta + 120) \\ 0.5 & 0.5 & 0.5 \end{bmatrix} \begin{bmatrix} v_{as} \\ v_{bs} \\ v_{cs} \end{bmatrix}$$

where  $v_{os}^s$  is added as the zero-sequence component, which may or may not be present.

$$v_{qs}^s = \frac{2}{3} v_{as} - \frac{1}{3} v_{bs} - \frac{1}{3} v_{cs} = v_{as}$$

$$v_{ds}^s = -\frac{1}{\sqrt{3}} v_{bs} + \frac{1}{\sqrt{3}} v_{cs}$$



**Figure 2.1** Stationary frame  $a-b-c$  to  $ds-qs$  axes transformation

In  $d^e$ - $q^e$  frame these equations can be written as:

$$v_{qs} = R_s i_{qs} + \frac{d}{dt} \psi_{qs} + \omega_e \psi_{ds}$$

$$v_{ds} = R_s i_{ds} + \frac{d}{dt} \psi_{ds} - \omega_e \psi_{qs}$$

where  $\psi_{qs}^s$  and  $\psi_{ds}^s$  are  $q$ -axis and  $d$ -axis stator flux linkages, respectively.

Since the rotor is rotating at a speed  $\omega_r$ , then in  $d^e$ - $q^e$  frame, the rotor equations should be modified as

$$v_{qr} = R_r i_{qr} + \frac{d}{dt} \psi_{qr} + (\omega_e - \omega_r) \psi_{dr}$$

$$v_{dr} = R_r i_{dr} + \frac{d}{dt} \psi_{dr} - (\omega_e - \omega_r) \psi_{qr}$$

where  $\psi_{qr}$  and  $\psi_{dr}$  are  $q$ -axis and  $d$ -axis rotor flux linkages respectively.

The state-space equations are given as

$$\frac{dF_{qs}}{dt} = \omega_b \left[ v_{qs} - \frac{\omega_e}{\omega_b} F_{ds} - \frac{R_s}{X_{ls}} (F_{qs} - F_{qm}) \right]$$

$$\frac{dF_{ds}}{dt} = \omega_b \left[ v_{ds} + \frac{\omega_e}{\omega_b} F_{qs} - \frac{R_s}{X_{ls}} (F_{ds} - F_{dm}) \right]$$

$$\frac{dF_{qr}}{dt} = -\omega_b \left[ \frac{(\omega_e - \omega_r)}{\omega_b} F_{dr} + \frac{R_r}{X_{lr}} (F_{qr} - F_{qm}) \right]$$

$$\frac{dF_{dr}}{dt} = -\omega_b \left[ -\frac{(\omega_e - \omega_r)}{\omega_b} F_{qr} + \frac{R_r}{X_{lr}} (F_{dr} - F_{dm}) \right]$$

where  $\omega_b$ =base frequency of the machine and  $F_{qs}$   $F_{ds}$   $F_{qr}$   $F_{dr}$  are the flux linkage variables and

$$F_{qm} = X_{ml} \left[ \frac{F_{qs}}{X_{ls}} + \frac{F_{qr}}{X_{lr}} \right]$$

$$F_{dm} = X_{ml} \left[ \frac{F_{ds}}{X_{ls}} - \frac{F_{dr}}{X_{lr}} \right]$$

$$X_{ml} = \frac{1}{\frac{1}{X_m} + \frac{1}{X_{ls}} + \frac{1}{X_{lr}}}$$

The currents in d-q reference frame are given as

$$I_{qs} = \frac{1}{X_{ls}} [F_{qs} - F_{qm}]$$

$$I_{ds} = \frac{1}{X_{ls}} [F_{ds} - F_{dm}]$$

$$I_{qr} = \frac{1}{X_{lr}} [F_{qr} - F_{qm}]$$

$$I_{dr} = \frac{1}{X_{lr}} [F_{dr} - F_{dm}]$$

Torque expression is given as follows:

$$T_e = \frac{3}{2} \left( \frac{P}{2} \right) \frac{1}{\omega_b} (F_{ds} i_{qs} - F_{qs} i_{ds})$$

Magnitude and angle of the stator flux are calculated as:

$$F_s = \sqrt{F_{qs}^2 + F_{ds}^2}$$

$$\theta_s = \tan^{-1} \frac{F_{qs}}{F_{ds}}$$

The sector is selected on the basis of  $\theta_s$ .

## Open loop V/F speed Control Technique with Voltage fed Inverter to Operate Induction motor

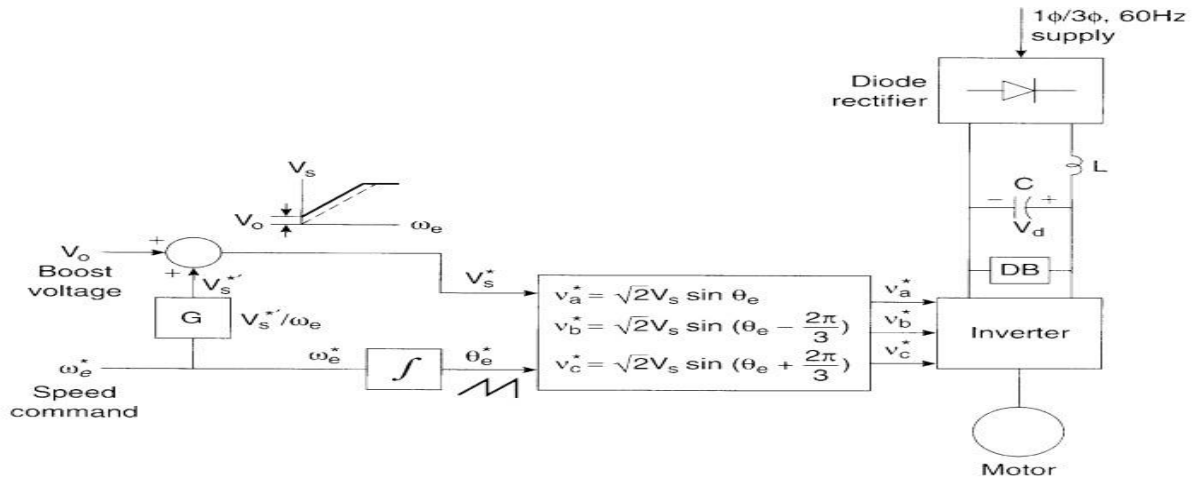
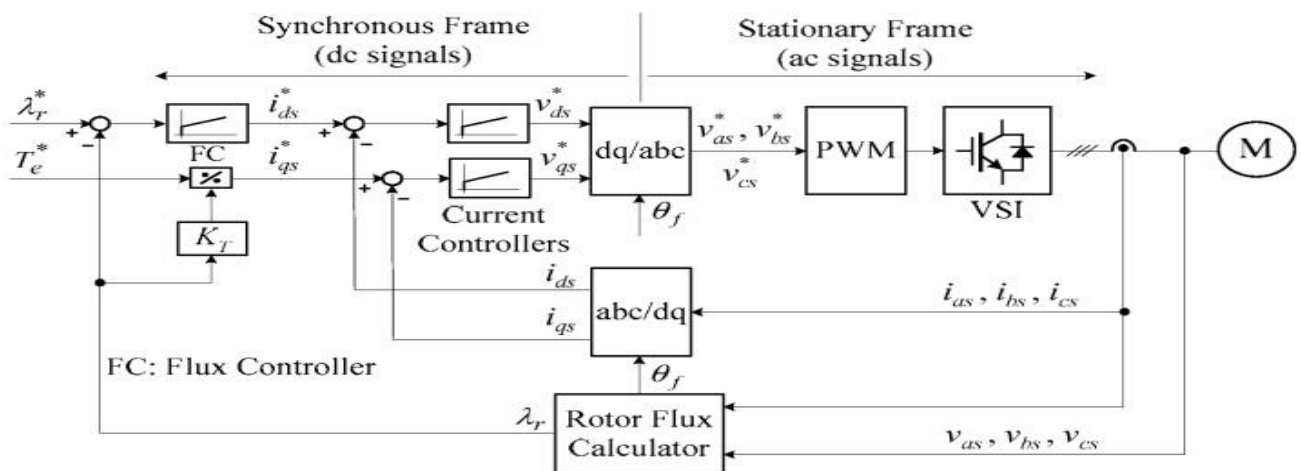


Figure 8.4 Open loop volts/Hz speed control with voltage-fed inverter

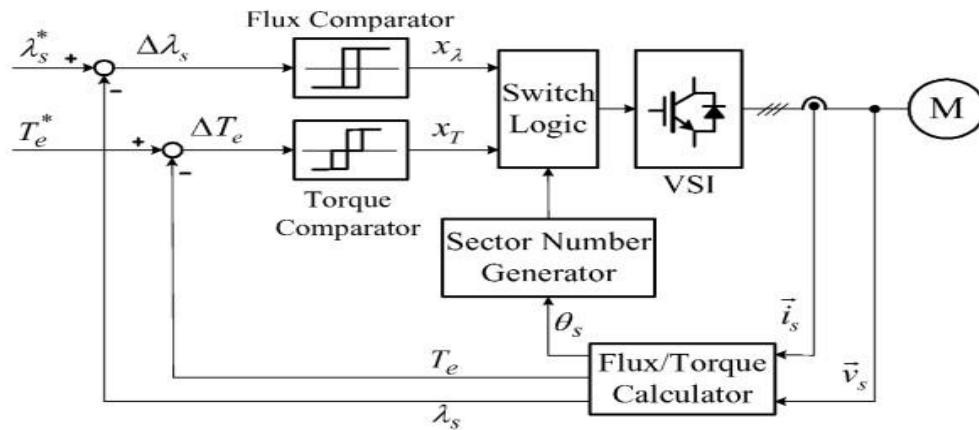
## Direct Rotor field FOC using SPWM technique



Direct field-oriented control with rotor flux orientation.

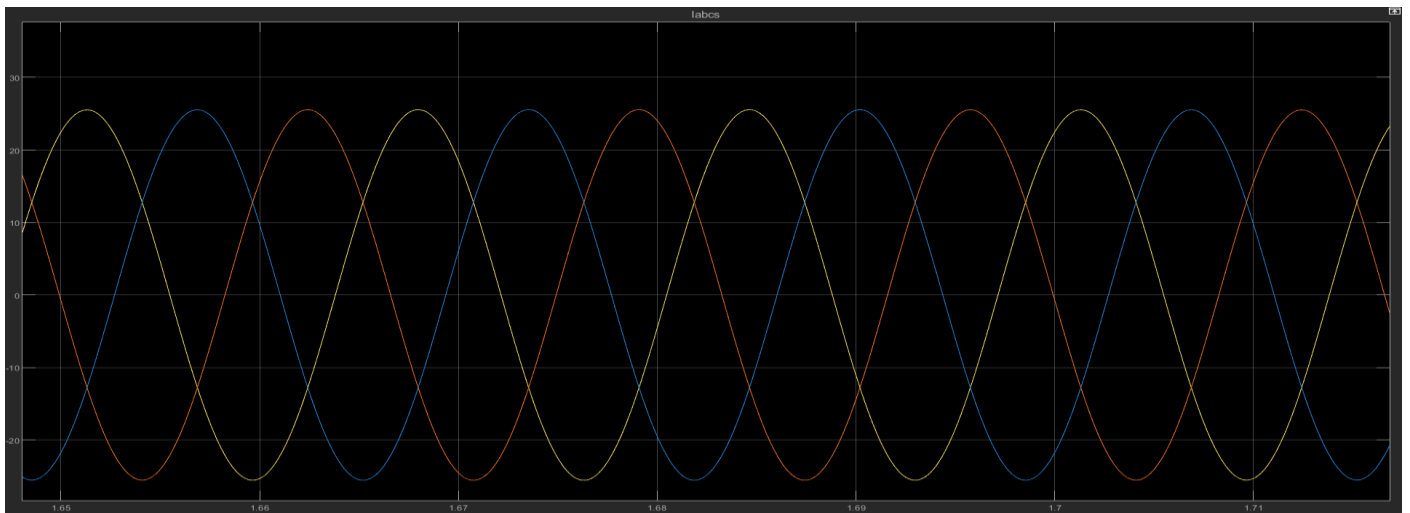
# **“DIRECT TORQUE CONTROL OF INDUCTION MOTOR”**

The main variable to be controlled in the DTC scheme is the stator flux vector( $\lambda_{ss}$ )

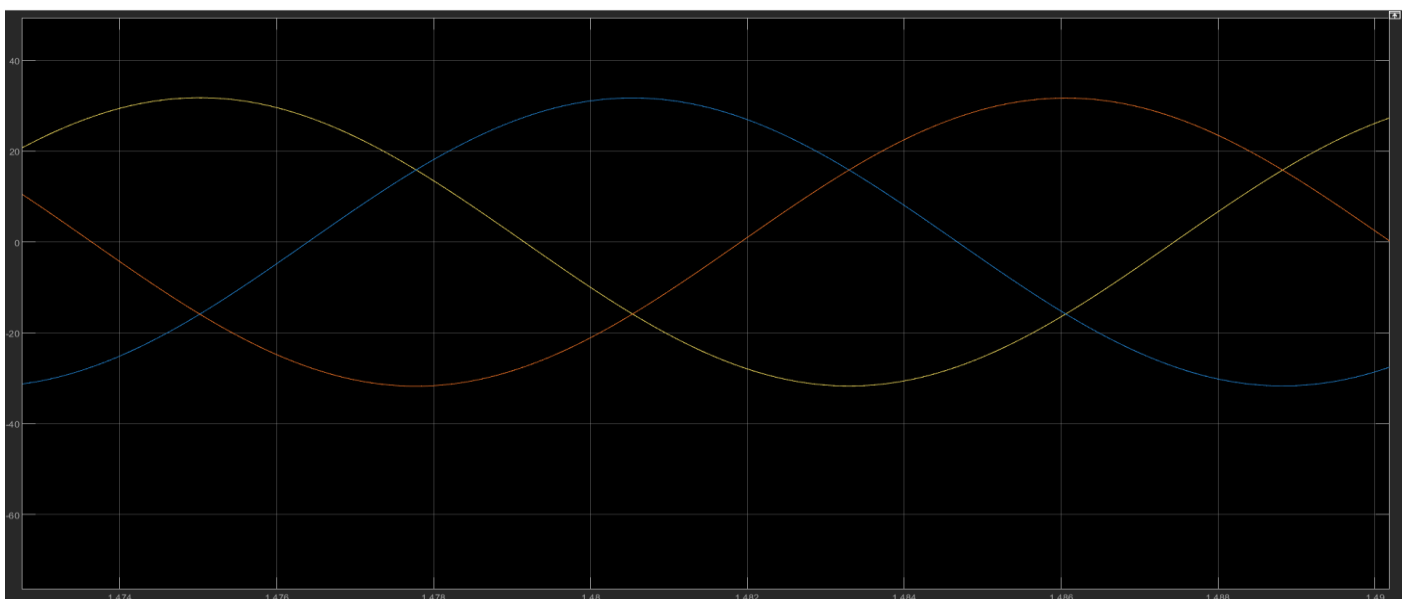


Block diagram of direct torque control scheme

## **SIMULATION AND RESULTS**



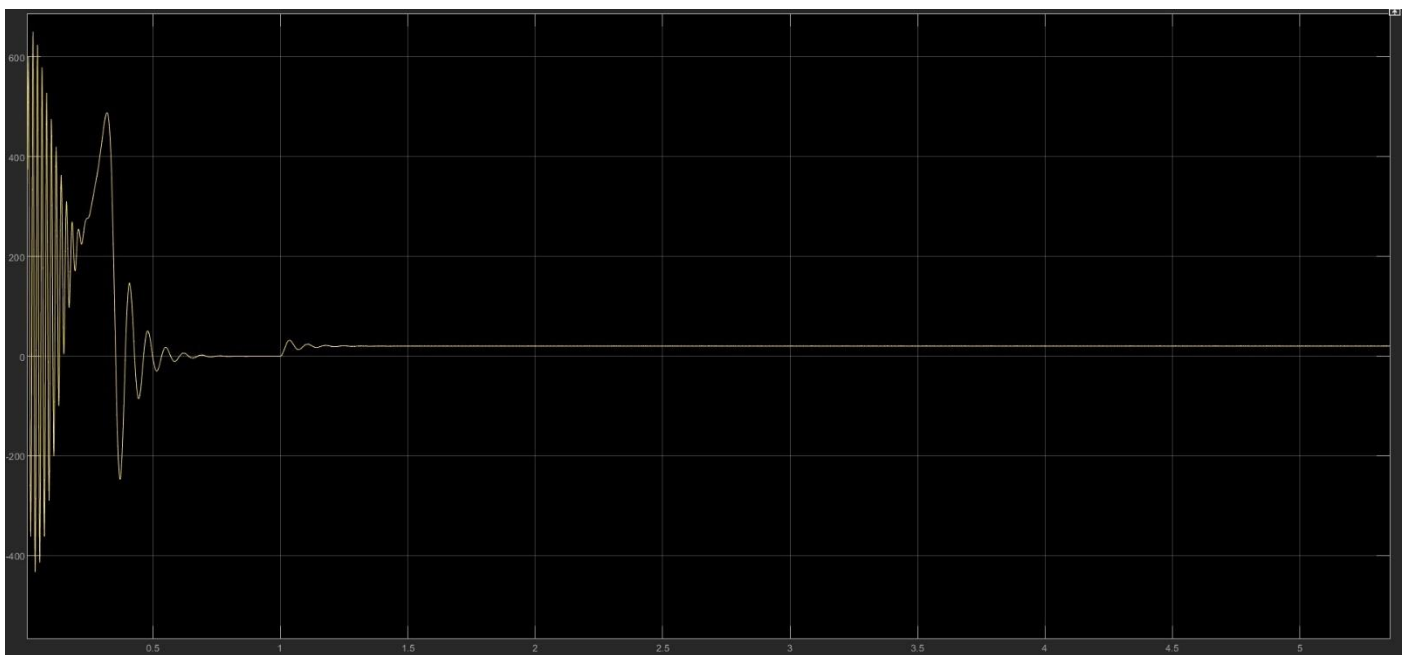
**Fig(a)  $i_{abc}$  (stator current )(Phase variable Model (abc model))**



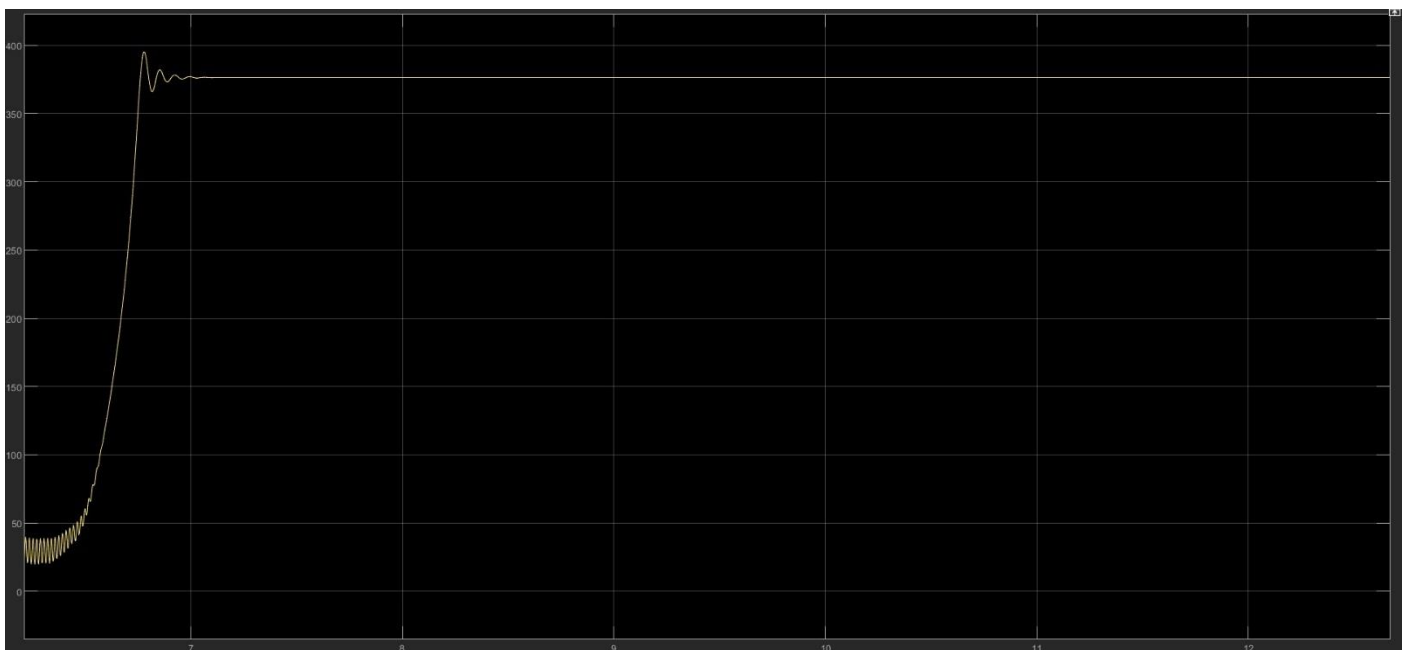
**Fig(b)  $i_{abc}$  (stator current )(dq0 model(synchronous reference frame))**



**Fig(c) Torque (Phase variable Model (abc model))**



**Fig(d) Torque(d-q model(synchronous reference frame))**



**Fig(e) speed  $\omega_r$  (Phase variable Model (abc model))**



**Fig(e) speed (dq model)**

**2) the slip of the motor under full load condition from both the models.**

At Full load

$T_{load} = 200$

$Slip = (N_s - N_r) / N_s$

$N_s = 120 * f / P = 1800$

$Slip = (1800 - 1757) / 1800 = 0.023888$

**3) In the dq model find the magnitude of the  $V_{qds}$ ,  $I_{qds}$ ,  $I_{qdr}$ ,  $\lambda_{qds}$ ,  $\lambda_{qdr}$  when  $2/3$  constant is used for abc to qd0 transformation and compare it with  $V_{abs}$ ,  $I_{abs}$ ,  $I_{abr}$ ,  $\lambda_{abs}$ ,  $\lambda_{abr}$  (from the phase variable model). Do similar exercise when  $\sqrt{2/3}$  constant is used for the transformation.**

$V_{ds} = 375.6$

$V_{qs} = 0$

$I_{qs} = 31.84$

$I_{ds} = 6.973$

$I_{dr} = 6.895$

$I_{qr} = 0$

$\lambda_{ds} = 0.008413$

$\lambda_{qs} = -0.09944$

$\lambda_{dr} = -0.0003611$

$\lambda_{qr} = -0.9688$

$V_{abs} = 265.6$

$I_{abs} = 52.56$

$I_{abr} = 68.81$

$\lambda_{abc} = [0.4878, -0.7838, 0.4904]$

$\lambda_{abr} = [-0.07672, -0.7838, 0.4904]$

**Do similar exercise when  $\sqrt{2/3}$  constant is used for the transformation**



$V_{ds}=460$

$V_{qs}=0$

$I_{qs}=38.99$

$I_{ds}=5.8$

$I_{dr}=5.627$

$I_{qr}=0$

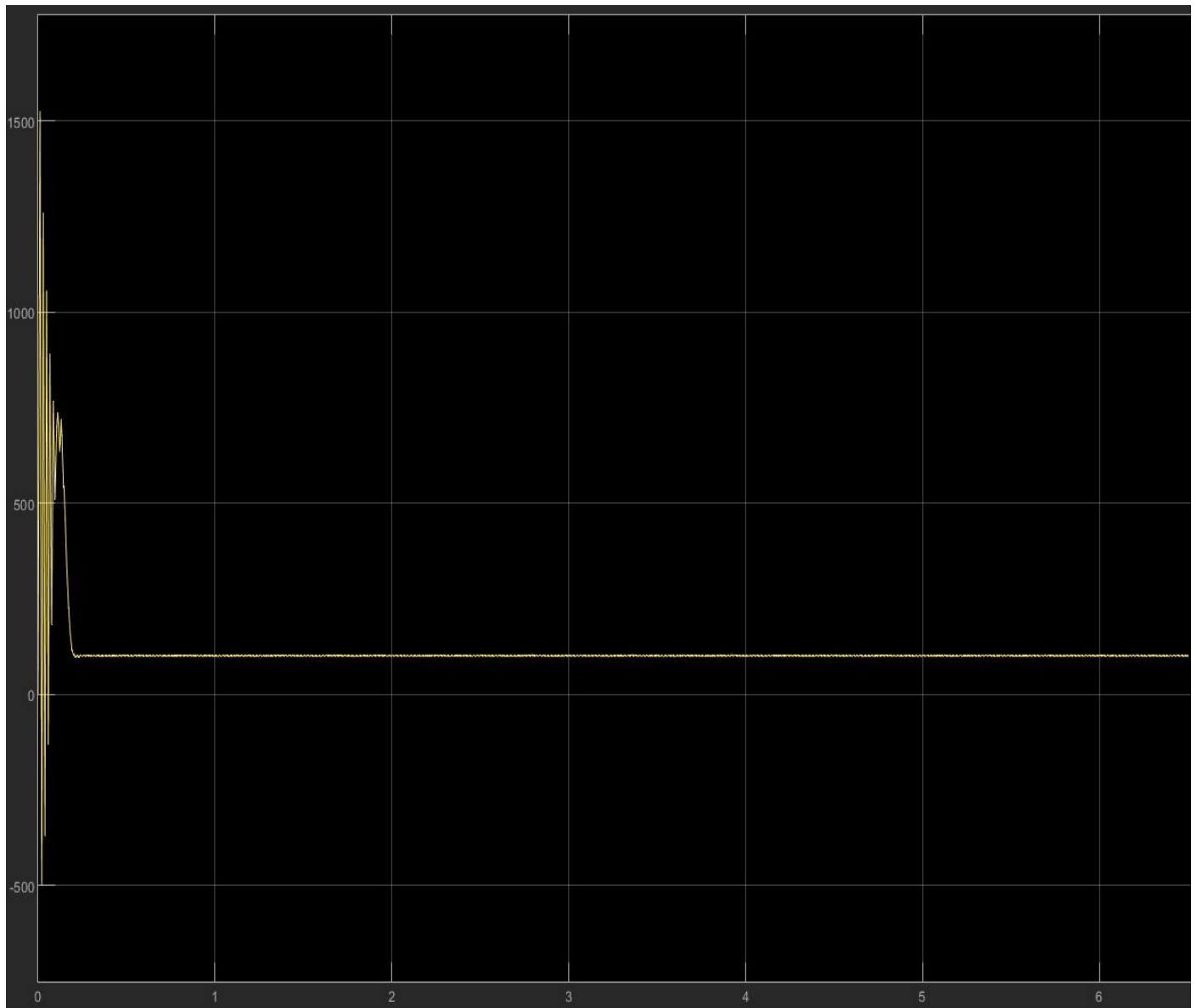
$\text{Lamda}(ds)=0.0103$

$\text{Lambda}(qs)=-1.219$

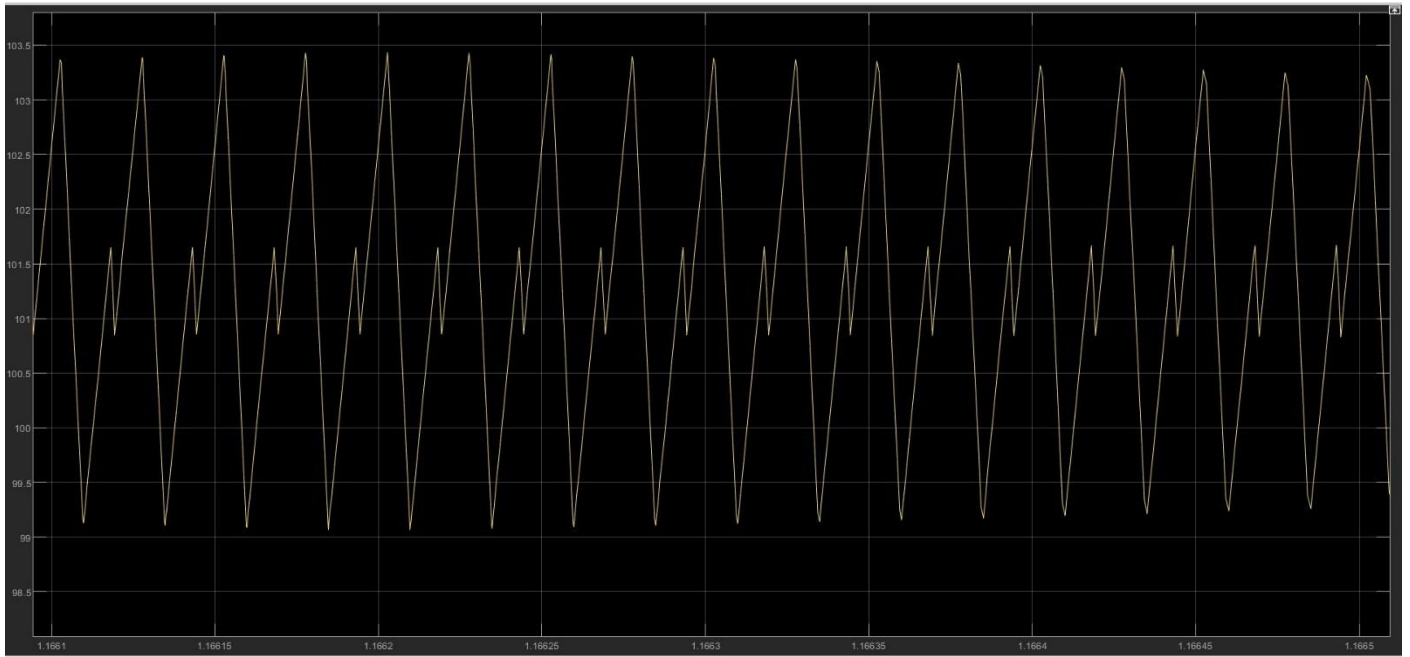
$\text{Lambda}(dr)=-0.0003941$

$\text{Lamda}(qr)=-1.185$

### AIM-3 (“Open loop V/F speed Control Technique with Voltage fed Inverter”)



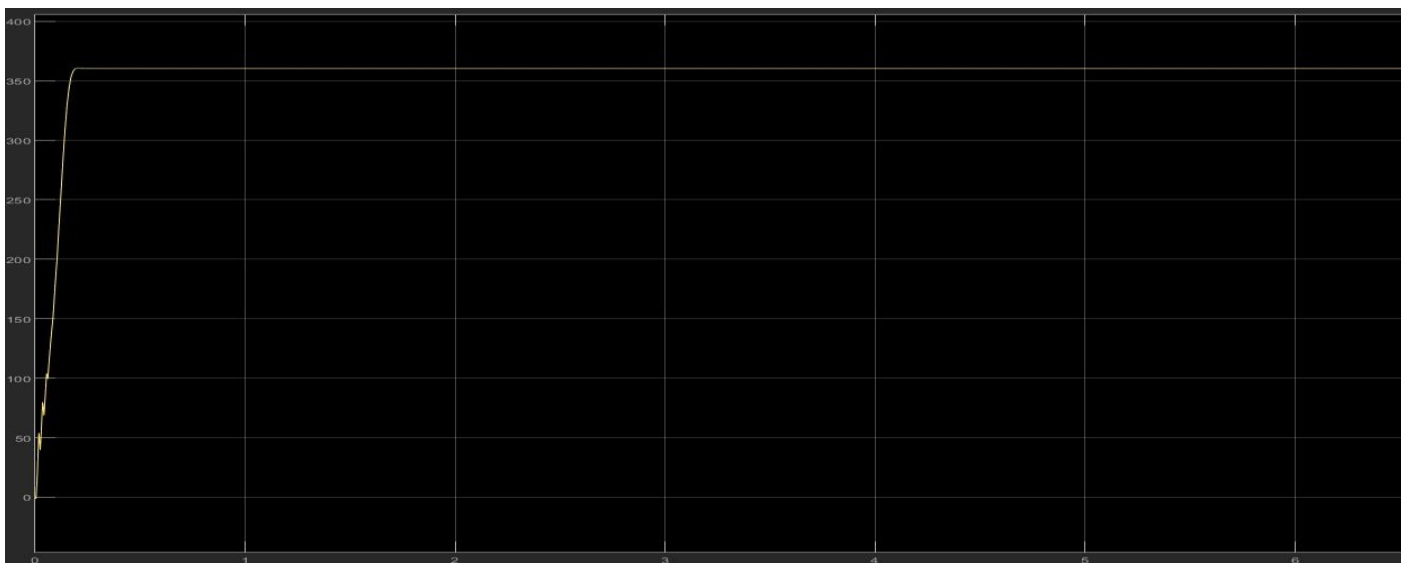
**Fig3.a: - ELECTROMAGNETIC TORQUE**



**Fig 3.b: - 4% Ripple in Torque**

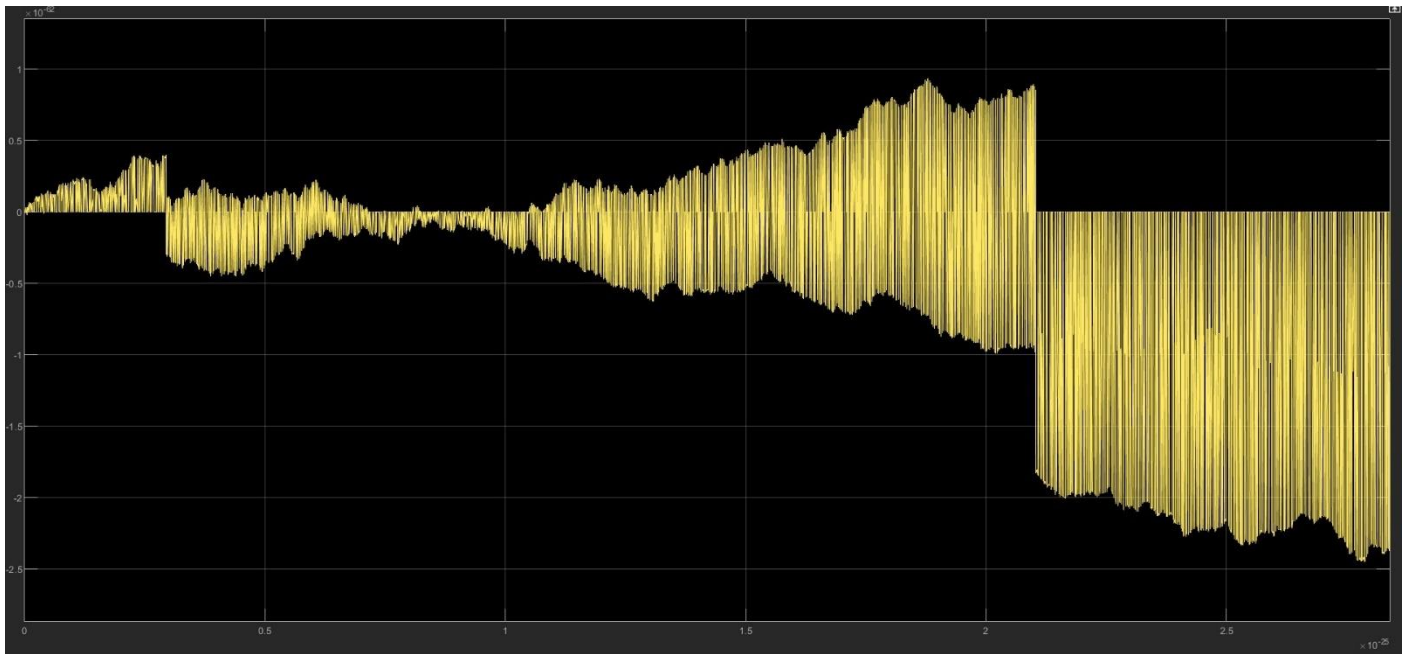


**Fig 3.c: - *Nr* (speed of the rotor get reduced)**



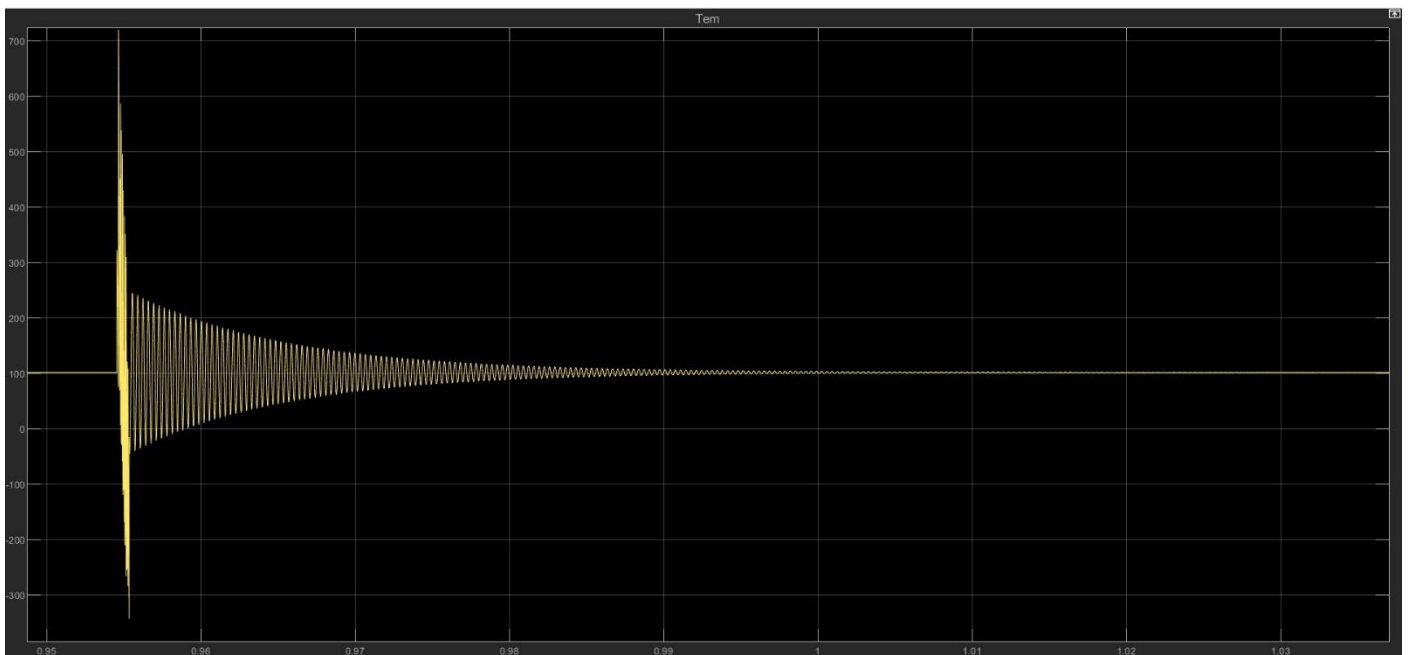
**Fig©: - *Wr* also gets reduced**

**AIM-4:- “DIRECT TORQUE CONTROL OF INDUCTION MOTOR”**



***ELECTROMAGNETIC TORQUE***

**AIM-5:- “Direct Rotor field FOC using SPWM technique”**



**Fig 5.a- Electromagnetic Torque**

*Spikes is coming at the reference torque*

## ***References***

[1] Ms. Tripti Rai, Prof. Prashant Debre “*Generalized Modelling Model Of three phase Induction Motor*” 978-1-4673-9925-8/16/\$31.00 ©2016 IEEE

2) A New Version of Phase-Variable Modeling of an Induction Motor Using PSIM Ming-Fa Tsai, Chung-Shi Tseng, Yu-Yuan Chen\*, and Wen-Yang Peng\* Department of Electrical Engineering, Minghsin University of Science and Technology, Hsinchu, Taiwan \*Industrial Technology Research Institute of Taiwan, ROC