

Problem 2

Given dissimilarity Matrix

$$\begin{array}{c} \textcircled{1} \\ \textcircled{2} \\ \textcircled{3} \\ \textcircled{4} \end{array} \begin{bmatrix} - & 0.3 & 0.4 & 0.7 \\ 0.3 & - & 0.5 & 0.8 \\ 0.4 & 0.5 & - & 0.45 \\ 0.7 & 0.8 & 0.45 & - \end{bmatrix}$$

$\textcircled{1} \quad \textcircled{2} \quad \textcircled{3} \quad \textcircled{4}$

a) Hierarchical Clustering (using Complete Linkage)

Step ①: minimum dissimilarity is 0.3 between $\textcircled{1}$ & $\textcircled{2}$.

\Rightarrow so combine them to form a cluster at height 0.3.

new dissimilarity matrix

$$\Rightarrow \begin{array}{c} \textcircled{1,2} \\ \textcircled{3} \\ \textcircled{4} \end{array} \begin{bmatrix} - & 0.5 & 0.8 \\ 0.5 & - & 0.45 \\ 0.8 & 0.45 & - \end{bmatrix}$$

$(\textcircled{1,2}) \quad \textcircled{3} \quad \textcircled{4}$

Step ②: minimum dissimilarity is 0.45 between $\textcircled{3}$ & $\textcircled{4}$

combine them to form a cluster at height = 0.45.

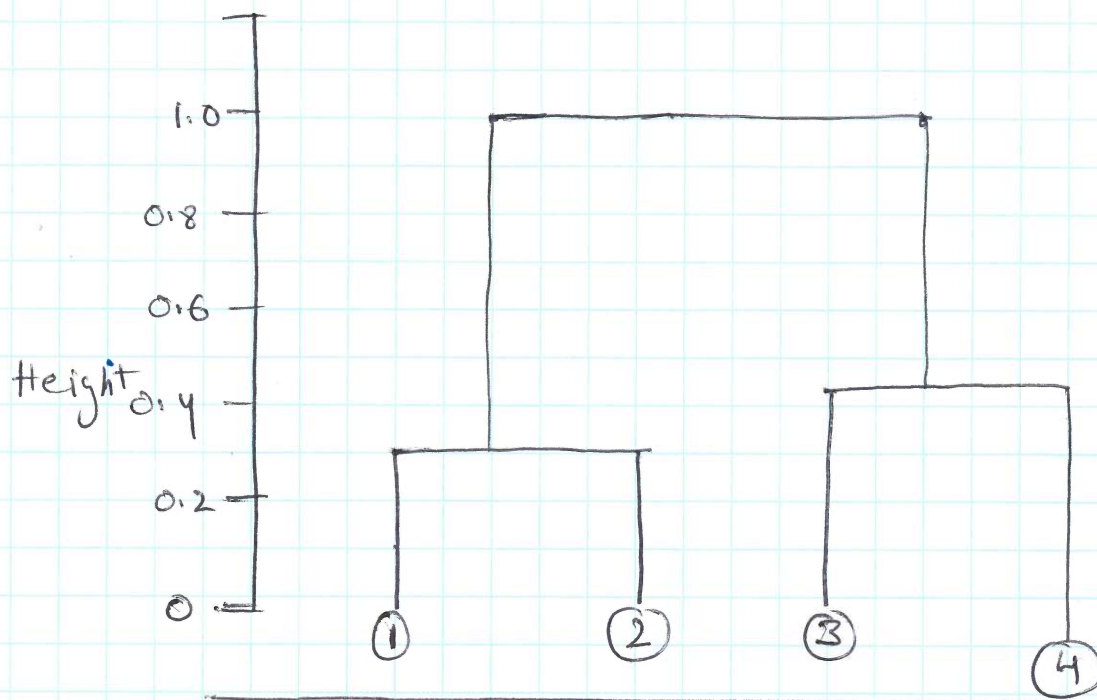
Reduced dissimilarity matrix

$$\Rightarrow \begin{array}{c} \textcircled{1,2} \\ \textcircled{3,4} \end{array} \begin{bmatrix} - & 0.8 \\ 0.8 & - \end{bmatrix}$$

$(\textcircled{1,2}) \quad (\textcircled{3,4})$

final step: Combine $(\textcircled{1,2})$ & $(\textcircled{3,4})$ at height at 0.8.

Cluster dendrogram [Complete Linkage]



b) Hierarchical Clustering [Single Linkage]

Step ①: minimum dissimilarity is 0.3
between ① & ② combine
them to form a cluster at
height = 0.3

⇒ New dissimilarity
matrix

(①, ②)	-	0.4	0.7
③	0.4	-	0.45
④	0.7	0.45	-

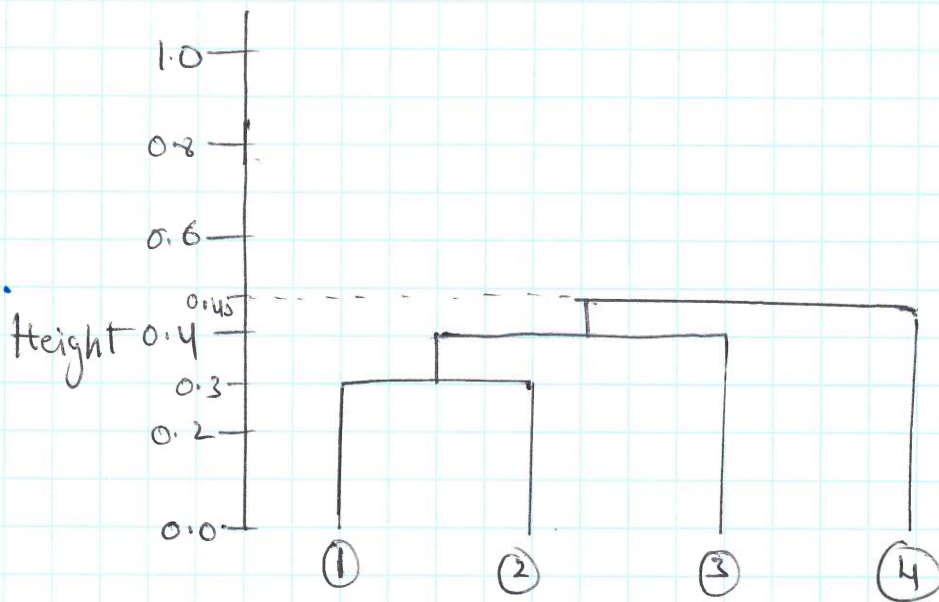
(①, ②) ③, ④

⇒ Similarly clusters will created with

$[(①, ②), ③]$ at height = 0.4 and

$[(①, ②), ③], ④$ at height = 0.45.

Cluster dendrogram [Single Linkage]



c) Cut Dendrogram from (a) to form two clusters.

\Rightarrow we have clusters ~~3~~ two clusters with $(1, 2)$ & $(3, 4)$

d) Cut Dendrogram from (b) to form two clusters.

\Rightarrow we have two clusters with

$[(1, 2), 3]$ and 4

e) Swap observations such that no meaning is changed in dendrogram with Complete linkage.

e)

Cluster diagram with Swapped Observations
[in Complete Linkage Case]

