

Problem ②

x_1 = hours Studied

x_2 = undergrad GPA

y = receive an A

Coefficient in logistic Regression fit

$$\hat{\beta}_0 = -6 \quad \hat{\beta}_1 = 0.05 \quad ; \quad \hat{\beta}_2 = 1$$

given $x_1 = 40$ & $x_2 = 3.5$

$$(a) \quad \hat{p}(x) = \frac{e^{-6 + 0.05 \times 40 + 1(3.5)}}{1 + e^{-6 + 0.05 \times 40 + 1(3.5)}}$$

$$\boxed{= 0.37754}$$

(b) given $\hat{p}(x) = 50\%$ $x_2 = 3.5$

$$0.5 = \frac{e^{-6 + 0.05x_1 + 3.5}}{1 + e^{-6 + 0.05x_1 + 3.5}}$$

$$\Rightarrow \boxed{x_1 = 50} \quad \text{so hours.}$$