代码模板

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开始

宏定义

```
#include<bits/stdc++.h>
   using namespace std;
   typedef long long LL;
   typedef __int128 LLL;
   typedef unsigned u32;
   typedef unsigned long long u64;
   typedef long double LD;
   #define il inline
   #define pln putchar('\n')
   #define For(i,a,b) for(int i=(a),(i\#\#i)=(b);i<=(i\#\#i);++i)
   #define Rep(i,n) for(int i=0,(i##i)=(n);i<(i##i);++i)
   #define Fodn(i,a,b) for(int i=(a),(i##i)=(b);i>=(i##i);--i)
   const int M=10000000007,INF=0x3f3f3f3f;
13
   const long long INFLL=0x3f3f3f3f3f3f3f3f3f1Ll;
14
   const int N=1000010;
    快读
   ios::sync_with_stdio(0);cin.tie(0);cout.tie(0);
   template <typename T>
1
    inline bool read(T &x) {
       x = 0; char c = getchar(); int f = 1;
        while (!isdigit(c) && (c != '-') && (c != EOF)) c = getchar();
        if (c == EOF) return 0;
        if (c == '-') f = -1, c = getchar();
        while (isdigit(c)) { x = x * 10 + (c \& 15); c = getchar();}
        x *= f; return 1;
10
    template <typename T, typename... Args>
11
12
   inline bool read(T &x, Args &...args) {
        bool res = 1;
13
        res &= read(x);
        res &= read(args...);
15
16
        return res;
   }
17
    对拍
   //in.txt
   //AC.exe std.txt
   //MY.exe my.txt
   void init(){
        FILE*F=fopen("int.txt","w");
       //srand(time(0));
        //int a=(long long)rand()*rand()%1001;
        //fscanf(F,"%d",&a);fprintf(F,"%d\n",a);
10
11
        fclose(F);
12
   }
13
    int main(){
15
        init();
16
        while(1){
17
            system("AC.exe < in.txt > std.txt");
18
19
            system("MY.exe < in.txt > my.txt");
20
21
            if(system("fc std.txt my.txt")){
22
                puts("WA");
23
24
                return 0;
            }else puts("AC\n\n");
25
```

```
27 init();
28 }
29 }
```

数学

模乘模幂

• longlong 范围用 fpl

```
inline LL mul(LL a, LL b, LL p) {
        LL res = a * b - ((LL)((LD)a * b / p) * p);
2
        return res < 0 ? res + p : (res < p ? res : res - p);</pre>
3
4
5
    inline LL fp(LL a, LL b, LL Mod) {
        LL res = (Mod != 1);
        for (; b; b >>= 1, a = a * a \% Mod)
8
9
            if (b & 1)
                res = res * a % Mod;
10
11
        return res;
    }
12
13
    inline LL fpl(LL a, LL b, LL Mod) {
14
15
        LL res = (Mod != 1);
        for (; b; b >>= 1, a = mul(a, a, Mod))
16
            if (b & 1)
17
18
                res = mul(res, a, Mod);
        return res;
19
    }
20
    GCD
    template <typename T>
    inline T gcd(T a, T b) {
2
3
        while (b){
            T t = b;
            b = a \% b;
            a = t;
        }
        return a;
    }
11
    template <typename T>
12
    inline T lcm(T a, T b) { return a / gcd(a, b) * b; }
13
    template <typename T>
14
    T exgcd(T a, T b, T &x, T &y) {
        if (!b) {
16
17
           x = 1;
            y = 0;
18
            return a;
19
        T res = exgcd(b, a \% b, x, y);
21
22
        T t = x;
        x = y;
23
        y = t - a / b * y;
24
        return res;
25
   }
26
```

CRT

- 需要 GCD 64 位模乘
- 用来合并同余方程
- 返回最小正数解或最小非负解无解返回-1

```
inline LL Crt(LL a1, LL a2, LL mod1, LL mod2) {    LL u, v;
```

```
LL g = exgcd(mod1, mod2, u, v);
4
        if ((a2 - a1) % g) return -1;
        LL m12 = abs(lcm(mod1, mod2));
        LL res = (mul(mod1, mul(u, ((a2 - a1) / g), m12), m12) + a1) % m12;
        return res <= 0 ? res + m12 : res; /* 求最小正数解还是非负解 */
   }
   线性筛
   struct primenumberlist{
   #define MAXN (10000000)
2
        int cnt, pri[10000000];
3
4
        bool np[MAXN + 10];
        primenumberlist(){
            np[1] = 1; cnt = 0;
            for (int i = 2; i <= MAXN; ++i) {</pre>
                if (!np[i]) pri[++cnt] = i;
8
                for (int j = 1; j <= cnt; ++j) {</pre>
                    LL t = pri[j] * i;
10
                    if (t > MAXN) break;
                    np[t] = 1;
12
13
                    if (!(i % pri[j])) break;
                }
14
            }
15
        }
   } prime;
17
    Φ 单点欧拉函数
    template <typename T>
2
    inline T phi(T x) {
        T res = x;
3
        for (T i = 2; i * i <= x; ++i)
            if ((x % i) == 0) {
5
                res = res / i * (i - 1);
                while ((x \% i) == 0) x /= i;
        if (x > 1) res = res / x * (x - 1);
        return res;
10
   }
   Miller-Rabin 素性测试
       • n <= 10^{18}
       ● 需要 64 位模乘 64 位模幂
   inline bool MR(LL x, LL n, int t) {
        LL las = x;
2
        for (int i = 1; i <= t; ++i) {</pre>
3
            x = mul(x, x, n);
            if (x == 1 && las != 1 && las != (n - 1)) return 0;
            las = x;
8
        return x == 1;
10
    inline bool isPrime(LL n) {
        if (n == 46856248255981ll || n < 2) return 0;</pre>
12
13
        if (n == 2 || n == 3 || n == 7 || n == 61 || n == 24251) return 1;
        LL d = n - 1;
14
        int t = 0;
15
        while ((d & 1) == 0) d >>= 1, ++t;
        return MR(fpl(2, d, n), n, t) && MR(fpl(61, d, n), n, t);
17
```

Pollard-Rho 分解质因数

● 需要 64 位模乘 gcd

- 或 n 的一个大于 1 的因子可能返回 n 本身
- 调用 PR() 前务必判断 n 的素性检查 n > 1

```
mt19937 mt(time(0)); //随机化
    inline LL PR(LL n) {
        LL x = uniform_int_distribution < LL > (0, n - 1)(mt), s, t, c = uniform_int_distribution < LL > (1, n - 1)(mt); //随机化
        for (int gol = 1; 1; gol <<= 1, s = t, x = 1) {</pre>
            for (int stp = 1; stp <= gol; ++stp) {</pre>
                 t = (mul(t, t, n) + c) \% n;
                x = mul(x, abs(s - t), n);
                 if ((stp & 127) == 0) {
                     LL d = gcd(x, n);
                     if (d > 1) return d;
10
                 }
            }
12
            LL d = gcd(x, n);
13
14
            if (d > 1) return d;
15
   }
```

组合数

- 数较小模数为较大质数求逆元
- 如果模数固定可以 O(n) 预处理阶乘的逆元
- 数较大模数为较小质数用 Lucas 定理
- -

$$C_n^m \equiv C_{\lfloor \frac{n}{p} \rfloor}^{\lfloor \frac{m}{p} \rfloor} * C_{n \bmod p}^{m \bmod p} (mod \ p)$$

• 数较大模数较小用 exLucas 定理求 $C_n^m mod P$

exLucas

- 需要模乘 CRT
- O(P log P)
- 不要求 P 为质数

```
namespace EXLUCAS {
1
2
        inline LL idxp(LL n, LL p) {
            LL nn = n;
3
            while (n > 0) nn -= (n \% p), n /= p;
            return nn / (p - 1);
5
6
        LL facp(LL n, LL p, LL pk) {
8
            if (n == 0) return 1;
            LL res = 1;
10
11
            if (n >= pk) {
                LL t = n / pk, k = 1, els = n - t * pk;
12
                for (LL i = 1; i <= els; ++i) if (i % p) k = k * i % pk;</pre>
13
14
                res = k;
                for (LL i = els + 1; i < pk; ++i) if (i % p) k = k * i % pk;
15
                res = res * fp(k, n / pk, pk) % pk;
17
            else for (LL i = 1; i <= n; ++i) if (i % p) res = res * i % pk;
19
            return res * facp(n / p, p, pk) % pk;
        }
20
21
        inline LL exlucas(LL n, LL m, LL p, LL pk, LL k) {
22
            LL a = facp(n, p, pk) * fp(facp(n - m, p, pk) * facp(m, p, pk) % pk, pk / p * (p - 1) - 1, pk) % pk;
23
            LL b = idxp(n, p) - idxp(m, p) - idxp(n - m, p);
24
25
            if (b >= k) return 0;
            while (b--) a *= p;
26
            return a % pk;
27
        }
```

```
29
30
        /* 接口 */ inline LL exlucas(LL n, LL m, LL p) {
            LL a = 0, b = 1;
31
            for (LL i = 2; i * i <= p; ++i) {
32
                if (p % i) continue;
                LL t = 0, pk = 1;
34
                while (p % i == 0) ++t, p /= i, pk *= i;
35
                a = Crt(a, exlucas(n, m, i, pk, t), b, pk);
36
37
38
            return (p > 1) ? Crt(a, exlucas(n, m, p, p, 1), b, p) : a;
39
40
   }
41
```

二维计算几何

- Point 直接支持整型和浮点型
- 部分函数可以对整型改写
- 多边形 (凸包) 按逆时针存在下标 1..n

点向量基本运算

```
template <typename T>
   struct Point {
2
        T x, y;
        Point() {}
        Point(T u, T v) : x(u), y(v) {}
5
        Point operator+(const Point &a) const { return Point(x + a.x, y + a.y); }
        Point operator-(const Point &a) const { return Point(x - a.x, y - a.y); }
        Point operator*(const T &a) const { return Point(x * a, y * a); }
        T operator*(const Point &a) const { return x * a.x + y * a.y; }
        T operator%(const Point &a) const { return x * a.y - y * a.x; }
10
        double len() const { return hypot(x, y); }
11
        double operator^(const Point &a) const { return (a - (*this)).len(); }
12
        double angle() const { return atan2(y, x); }
        bool id() const { return y < 0 \mid | (y == 0 \&\& x < 0); }
14
        bool operator<(const Point &a) const { return id() == a.id() ? (*this) % a > 0 : id() < a.id(); }</pre>
15
16
   };
   typedef Point<double> point;
17
   #define sqr(x) ((x) * (x))
19
   const point O(0, 0);
20
   const double PI(acos(-1.0)), EPS(1e-8);
21
   inline bool dcmp(const double &x, const double &y) { return fabs(x - y) < EPS; }
   inline int sgn(const double &x) \{ return fabs(x) < EPS ? 0 : ((x < 0) ? -1 : 1); \}
   inline double mul(point p1, point p2, point p0) { return (p1 - p0) % (p2 - p0); }
    位置关系
    inline bool in_same_seg(point p, point a, point b) {
        if (fabs(mul(p, a, b)) < EPS) {</pre>
2
            if (a.x > b.x) swap(a, b);
            return (a.x <= p.x && p.x <= b.x && ((a.y <= p.y && p.y <= b.y) || (a.y >= p.y && p.y >= b.y)));
        } else return 0:
    inline bool is_right(point st, point ed, point a) {
8
        return ((ed - st) % (a - st)) < 0;
10
   inline point intersection(point s1, point t1, point s2, point t2) {
12
        return s1 + (t1 - s1) * (((s1 - s2) % (t2 - s2)) / ((t2 - s2) % (t1 - s1)));
13
14
15
    inline bool parallel(point a, point b, point c, point d) {
        return dcmp((b - a) % (d - c), 0);
17
18
19
```

```
inline double point2line(point p, point s, point t) {
20
21
       return fabs(mul(p, s, t) / (t - s).len());
22
23
   inline double point2seg(point p, point s, point t) {
       25
26
   多边形
   求多边形面积
   inline double area(int n, point s[]) {
       double res = 0;
2
       s[n + 1] = s[1];
       for (int i = 1; i \le n; ++i)
          res += s[i] % s[i + 1];
       return fabs(res / 2);
   }
   判断点是否在多边形内
      • 特判边上的点
      ● 使用了 a[1]...a[n+1] 的数组
   inline bool in_the_area(point p, int n, point area[]) {
       bool ans = 0; double x;
       area[n + 1] = area[1];
       for (int i = 1; i <= n; ++i) {</pre>
          point p1 = area[i], p2 = area[i + 1];
          if (in_same_seg(p, p1, p2)) return 1; //特判边上的点
          if (p1.y == p2.y) continue;
          if (p.y < min(p1.y, p2.y)) continue;</pre>
          if (p.y >= max(p1.y, p2.y)) continue;
          ans ^{=} (((p.y - p1.y) * (p2.x - p1.x) / (p2.y - p1.y) + p1.x) > p.x);
10
11
12
       return ans;
   }
13
   凸包
      ● Andrew 算法
      • O(n log n)
```

- 可以应对凸包退化成直线/单点的情况但后续旋转卡壳时应注意特判
- 注意是否应该统计凸包边上的点

```
inline bool pcmp1(const point &a, const point &b) { return a.x == b.x ? a.y < b.y : a.x < b.x; }</pre>
    inline int Andrew(int n, point p[], point ans[]) { //ans[] 逆时针存凸包
       sort(p + 1, p + 1 + n, pcmp1);
       int m = 0;
        for (int i = 1; i <= n; ++i) {</pre>
            while (m > 1 && mul(ans[m - 1], ans[m], p[i]) < 0) --m; //特判凸包边上的点
            ans[++m] = p[i];
       int k = m;
10
        for (int i = n - 1; i >= 1; --i) {
            while (m > k && mul(ans[m - 1], ans[m], p[i]) < 0) --m; //特判凸包边上的点
12
           ans[++m] = p[i];
13
14
       return m - (n > 1); //返回凸包有多少个点
15
```

凸包直径·平面最远点对

• 旋转卡壳算法

```
• O(n)
       • 凸包的边上只能有端点, 否则不满足严格单峰
       ● 凸包不能退化成直线,调用前务必检查 n>=3
       ● 使用了 a[1]...a[n+1] 的数组
   inline double Rotating_Caliper(int n, point a[]) {
1
        a[n + 1] = a[1];
2
        double ans = 0;
3
        int j = 2;
4
        for (int i = 1; i <= n; ++i) {</pre>
5
            while (fabs(mul(a[i], a[i + 1], a[j])) < fabs(mul(a[i], a[i + 1], a[j + 1]))) j = (j % n + 1);</pre>
            ans = \max(ans, \max((a[j] ^ a[i]), (a[j] ^ a[i + 1])));
        return ans;
10
   }
    平面最近点对
       ● 分治+归并

    O(n log n)

   namespace find_the_closest_pair_of_points {
1
        const int N = 200010; //maxn
2
        inline bool cmp1(const point &a, const point &b) { return a.x < b.x \mid | (a.x == b.x && a.y < b.y); }
3
        inline bool operator>(const point &a, const point &b) { return a.y > b.y || (a.y == b.y && a.x > b.x); }
5
        point a[N], b[N];
        double ans;
        inline void upd(const point &i, const point &j) { ans = min(ans, i ^ j); }
        void find(int l, int r) {
10
            if (l == r) return;
11
            if (l + 1 == r) {
12
                if (a[l] > a[r]) swap(a[l], a[r]);
13
14
                upd(a[l], a[r]); return;
15
            int mid = (l + r) >> 1;
16
            double mx = (a[mid + 1].x + a[mid].x) / 2;
17
            find(l, mid); find(mid + 1, r);
18
19
            int i = l, j = mid + 1;
            for (int k = 1; k \le r; ++k) b[k] = a[((j > r) | | (i \le mid \&\& a[j] > a[i])) ? (i++) : (j++)];
20
21
            for (int k = l; k <= r; ++k) a[k] = b[k];</pre>
            int tot = 0;
22
            for (int k = l; k <= r; ++k) if (fabs(a[k].x - mx) <= ans) {</pre>
24
                for (int j = tot; j >= 1 && (a[k].y - b[j].y <= ans); --j) upd(a[k], b[j]);</pre>
                b[++tot] = a[k];
25
26
            }
        }
27
        //接口
29
        inline double solve(int n, point ipt[]){
30
            ans = 0x3f3f3f3f3f3f3f3f3f1l; //max distance
31
            for (int i = 1; i <= n; ++i) a[i] = ipt[i];</pre>
32
            sort(a + 1, a + 1 + n, cmp1);
            find(1, n);
34
            return ans;
35
36
   }
37
    圆
    三点垂心
```

inline point geto(point p1, point p2, point p3) {
 double a = p2.x - p1.x;
 double b = p2.y - p1.y;
 double c = p3.x - p2.x;
 double d = p3.y - p2.y;
 double e = sqr(p2.x) + sqr(p2.y) - sqr(p1.x) - sqr(p1.y);

```
double f = sqr(p3.x) + sqr(p3.y) - sqr(p2.x) - sqr(p2.y);
return {(f * b - e * d) / (c * b - a * d) / 2, (a * f - e * c) / (a * d - b * c) / 2};

最小覆盖圆
● 随机增量 O(n)
```

```
inline void min_circlefill(point &o, double &r, int n, point a[]) {
        mt19937 myrand(20011224); shuffle(a + 1, a + 1 + n, myrand); //越随机越难 hack
        o = a[1];
        r = 0;
        for (int i = 1; i <= n; ++i) if ((a[i] ^ o) > r + EPS) {
            o = a[i];
            r = 0;
            for (int j = 1; j < i; ++j) if ((o ^ a[j]) > r + EPS) {
                o = (a[i] + a[j]) * 0.5;
                r = (a[i] ^ a[j]) * 0.5;
10
                for (int k = 1; k < j; ++k) if ((o ^ a[k]) > r + EPS) {
11
                    o = geto(a[i], a[j], a[k]);
12
                    r = (o \land a[i]);
13
                }
            }
15
        }
16
   }
17
```

图论

存图

- 前向星
- 注意边数开够

```
int Head[N], Ver[N*2], Next[N*2], Ew[N*2], Gtot=1;
inline void graphinit(int n) {Gtot=1; for(int i=1; i<=n; ++i) Head[i]=0;}
inline void edge(int u, int v, int w=1) {Ver[++Gtot]=v; Next[Gtot]=Head[u]; Ew[Gtot]=w; Head[u]=Gtot;}
#define go(i,st,to) for (int i=Head[st], to=Ver[i]; i; i=Next[i], to=Ver[i])</pre>
```

最短路

Dijkstra

• 非负权图

```
namespace DIJK{//适用非负权图 满足当前 dist 最小的点一定不会再被松弛
       typedef pair<long long,int> pii;
       long long dist[N];//存最短路长度
3
       bool vis[N];//记录每个点是否被从队列中取出 每个点只需第一次取出时扩展
       priority_queue<pii,vector<pii>,greater<pii> >pq;//维护当前 dist[] 最小值及对应下标 小根堆
       inline void dijk(int s,int n){//s 是源点 n 是点数
           while(pq.size())pq.pop();for(int i=1;i<=n;++i)dist[i]=INFLL,vis[i]=0;//所有变量初始化
           dist[s]=0;pq.push(make_pair(0,s));
10
           while(pq.size()){
               int now=pq.top().second;pq.pop();
11
               if(vis[now])continue;vis[now]=1;
12
               go(i,now,to){
13
                   const long long relx(dist[now]+Ew[i]);
14
                   if(dist[to]>relx){dist[to]=relx;pq.push(make_pair(dist[to],to));}//松弛
15
16
               }
17
           }
       }
18
   }
19
```

LCA

- 倍增求 lca
- 数组开够

```
namespace LCA_Log{
                              int fa[N][22],dep[N];
 2
                              int t,now;
                              void dfs(int x){
                                             dep[x]=dep[fa[x][0]]+1;
                                             go(i,x,to){
                                                            if(dep[to])continue;
                                                            fa[to][0]=x; for(int j=1;j<=t;++j)fa[to][j]=fa[fa[to][j-1]][j-1];
                                                            dfs(to);
                                             }
                             }
11
12
                              //初始化接口
13
                              inline void lcainit(int n,int rt){//记得初始化全部变量
14
                                            now=1;t=0;while(now<n)++t,now<<=1;</pre>
15
                                             for(int i=1;i<=n;++i)dep[i]=0,fa[i][0]=0;</pre>
16
17
                                             for(int i=1;i<=t;++i)fa[rt][i]=0;</pre>
                                            dfs(rt);
18
19
                             }
20
                              //求 lca 接口
21
22
                              inline int lca(int u,int v){
                                             if(dep[u]>dep[v])swap(u,v);
23
                                             for(int i=t;~i;--i)if(dep[fa[v][i]]>=dep[u])v=fa[v][i];
                                             if(u==v)return u;
25
26
                                             for(int i=t;~i;--i)if(fa[u][i]!=fa[v][i])u=fa[u][i],v=fa[v][i];
                                             return fa[u][0];
27
                             }
28
             }
              连通性
               有向图强联通分量
                            • tarjan O(n)
              namespace SCC{
 2
                             int dfn[N],clk,low[N];
                              bool ins[N]; int sta[N], tot; //栈 存正在构建的强连通块
 3
                              vector<int>scc[N];int c[N],cnt;//cnt 为强联通块数 scc[i] 存放每个块内点 c[i] 为原图每个结点属于的块
                              void dfs(int x){
                                             dfn[x]=low[x]=(++clk);//low[] 在这里初始化
                                             ins[x]=1;sta[++tot]=x;
                                             go(i,x,to){
                                                            if(!dfn[to]){dfs(to);low[x]=min(low[x],low[to]);}//走树边
                                                            else if(ins[to])low[x]=min(low[x],dfn[to]);//走返祖边
10
11
                                             if(dfn[x]==low[x]){//该结点为块的代表元
12
13
                                                            \label{eq:cont_scc} \textbf{do}\{\textbf{u} = \textbf{sta}[\texttt{tot--}]; \texttt{ins}[\textbf{u}] = \textbf{0}; \texttt{c}[\textbf{u}] = \texttt{cnt}; \texttt{scc}[\texttt{cnt}]. \texttt{push\_back}(\textbf{u}); \} \\ \textbf{while}(\textbf{x} \mid = \textbf{u}); \\ \textbf{v} = \textbf
14
                                             }
15
16
                              inline void tarjan(int n){//n 是点数
17
                                             for(int i=1;i<=cnt;++i)scc[i].clear();//清除上次的 scc 防止被卡 MLE
18
19
                                             for(int i=1;i<=n;++i)dfn[i]=ins[i]=0;tot=clk=cnt=0;//全部变量初始化
```

for(int i=1;i<=n;++i)if(!dfn[i])dfs(i);</pre>

20

21

22 23 } }

for(int i=1;i<=n;++i)c[i]+=n;//此行 (可以省略) 便于原图上加点建新图 加新点前要初始化 Head[]=0