# R for bioinformatics, data summarisation and statistics

**HUST** Bioinformatics course series

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## section 1: TOC

## 前情提要

- basic plot functions
- basic ggplot2
- special letters
- equations
- advanced ggplot2

# 本次提要

- data summarisation functions (vector data)
  - median, mean, sd, quantile, summary
- 图形化的 data summarisation (two-D data/ tibble/ table)
  - dot plot
  - smooth
  - linear regression
  - correlation & variance explained
  - groupping & bar/ box/ plots
- statistics
  - parametric tests
    - t-test
    - one way ANNOVA
    - two way ANNOVA
    - linear regression
    - model / prediction / coefficients
  - non-parametric comparison



section 2: vector summarisation

#### vector data

#### distribution

```
library(tidyverse);
ggplot( swiss, aes( x = Infant.Mortality ) ) + geom_density() +
    ggtitle("Swiss Fertility and Socioeconomic Indicators (1888) Data")
```

#### Swiss Fertility and Socioeconomic Indicators (1888) Data



#### describe normal distributions

#### 可以用 mean 和 sd 来描述

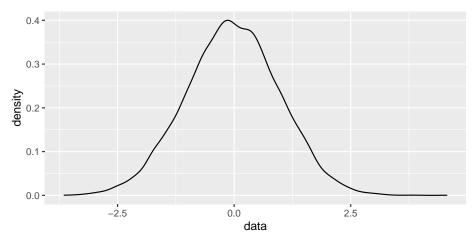
- It's symmetrical.
- Mean and median are the same.
- Most common values are near the mean; less common values are farther from it.
- Standard deviation marks the distance from the mean to the inflection point.

$$(mean + 1 * sd) >= 68%$$
  
 $(mean + 2 * sd) >= 95%$  的数据



# functions to generate random normal distrubions

```
# 生成 10000 个随机数字, 使其 mean = 0, sd = 1, 且为 normal distribution ...
x \leftarrow rnorm(10000, mean = 0, sd = 1):
ggplot( data.frame( data = x ), aes( data ) ) + geom_density( );
```



# other functions to generate random normal distributions

#### 注意,以下函数中的 q, p, x 需要自行提供

```
# generate CDF probabilities for value(s) in vector q
pnorm(q, mean = 0, sd = 1)

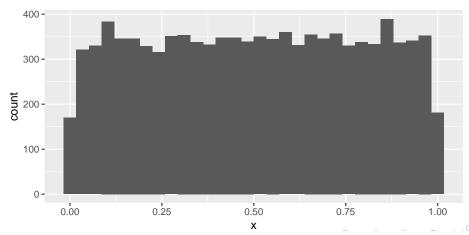
# generate quantile for probabilities in vector p
qnorm(p, mean = 0, sd = 1)

# generate density function probabilites for value(s) in vector x
dnorm(x, mean = 0, sd = 1)
```

## 其它规律的 distributions

uniform distributions

```
x <- runif( 10000 ); ## random numbers of uniform distributions between 0 and 1
ggplot( data.frame( dat = x ), aes( x ) ) + geom_histogram();</pre>
```



## uniform distribution 的各种函数

#### 注: 以下函数中的 n 需要自行决定

```
# generate n random numbers between 0 and 25
runif(n, min = 0, max = 25)

# generate n random numbers between 0 and 25 (with replacement)
sample(0:25, n, replace = TRUE)

# generate n random numbers between 0 and 25 (without replacement)
sample(0:25, n, replace = FALSE)
```

### other distributions, cont.

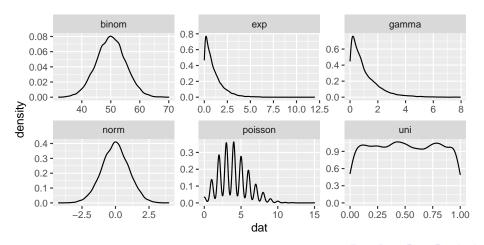
```
n <- 10000;
uni <- tibble( dat = runif(n), type = "uni" );
norm <- tibble( dat = rnorm(n), type = "norm" );
binom <- tibble( dat = rbinom(n, size = 100, prob = 0.5), type = "binom" );
poisson <- tibble( dat = rpois(n, lambda = 4), type = "poisson" );
exp <- tibble( dat = rexp(n, rate = 1) , type = "exp");
gamma <- tibble( dat = rgamma(n, shape = 1) , type = "gamma");

combined <- bind_rows( uni, norm, binom, poisson, exp, gamma );

plot1 <-
    ggplot( combined , aes( dat ) ) + geom_density() +
    facet_wrap( ~type, ncol = 3, scales = "free");</pre>
```

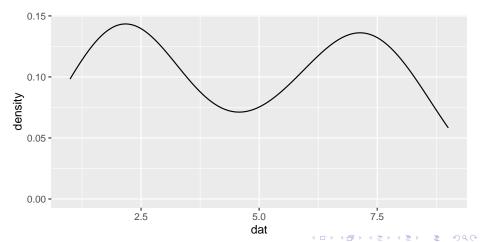
# other distributions, plot

plot1;



## non-parametric distribution

```
## votes on people's desire to visit
bi <- c(7, 3, 2, 1, 7, 3, 4, 5, 7, 6, 2, 2, 1, 3, 7, 2, 6, 8, 2, 7, 2, 2, 1,
3, 5, 8, 2, 6, 7, 8, 6, 2, 8, 7, 9, 2, 7, 5, 1, 8, 8, 2, 3, 7, 3, 8);
ggplot( data.frame( dat = bi ), aes(dat)) + geom_density();
```



## 量化描述数据

#### 使用以下同名函数

**mean**: aka average, is the sum of all of the numbers in the data set divided by the size of the data set.

**median**: The median is the value that is in the middle when the numbers in a data set are sorted in increasing order.

sd: standard deviation

var: measures how far a set of numbers are spread out

range: 取值范围

note: from: https://www.ai-therapy.com/psychology-statistics/
descriptive/mean-mode-median

## 量化描述函数

```
mean( norm$dat );
median( norm$dat );
## mode( norm$dat ); ## ???

sd(norm$dat);
var(norm$dat);
range(norm$dat);
```

# quantile and summary

```
quantile( norm$dat );
         0% 25% 50% 75% 100%
## -4.24468164 -0.68741487 -0.01378277 0.65486633 3.97261680
## quantile 还接受其它参数
quantile( norm$dat, probs = seq(0, 1, length = 11)):
            10% 20%
         0%
                                     30%
                                               40% 50%
## -4.24468164 -1.29991274 -0.85030211 -0.53849383 -0.25823357 -0.01378277
        60%
                  70%
                           80%
                                     90%
                                              100%
## 0.23090100 0.49407917 0.82783819 1.27228748 3.97261680
## summary ...
summary( norm$dat );
## Min. 1st Qu. Median Mean 3rd Qu.
                                         Max.
## -4.24468 -0.68741 -0.01378 -0.01782 0.65487 3.97262
## summary 也可应用于非数值
summary( combined$type );
    Length Class Mode
```

60000 character character

##

### summary, cont.

dat.

```
## summary 可应用于整个表格; 相当于对每列进行 summary ...
summary( combined );
```

```
type
## Min. :-4.2447
                  Length:60000
  1st Qu.: 0.3121 Class :character
   Median: 0.9401
                  Mode :character
## Mean : 9.4213
   3rd Qu.: 4.0000
   Max. :70.0000
```

### table 函数

#### 返回 vector 当中 unique 值和它们的出现次数

```
table( combined$type );
```

```
## ## binom exp gamma norm.poisson uni
## 10000 10000 10000 10000 10000 10000
```

\*\* 注 \*\*: table 还接受 data.frame 作为输入,比如 table(combined)。请自行尝试并理解结果

section 3: two column data: part 1

## 数据介绍: a numeric vector and a facterial vector

#### 此类数据,通常一列是数值,另一列是分组信息,如下例:

```
data.fig3a <- read_csv( file = "data/talk10/nc2015_data_for_fig3a.csv" );
head( data.fig3a[ c("tai", "trans.at") ] ); ## 只显示有用的两列
```

```
## tai trans.at

*dbl> <dbl> <dbl>
## 1 1 0.195

## 2 1 -0.320

## 3 1 -0.327

## 4 1 -0.304

## 5 1 -0.275
```

## # A tibble: 6 x 2

### 数据介绍,cont.

tai: 表达量的一种计算方式, 1 == lowest, 5 == highest

trans.at: A - T 碱基使用偏好;

#### 假说:

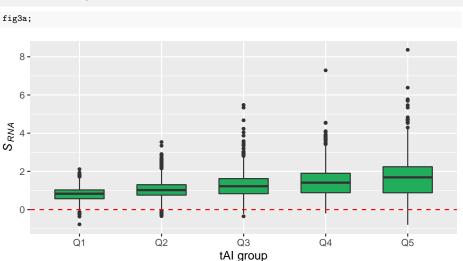
- de novo synthesis cost of A is higher than T,
- therefore highly expressed genes will tend to use T than A when possible.
- ◎ 因此,在高表达的基因当中,A T 的差值会变大(更负)。

data source: Chen et al, Nature Communications, 2016

## boxplot

```
fig3a <-
ggplot( data.fig3a, aes( factor(tai), zAA1.at ) ) +
geom_boxplot( fill = "#22AD5C", linetype = 1 ,outlier.size = 1, width = 0.6) +
xlab( "tAI group" ) +
ylab( expression( paste( italic(S[RNA]) ) ) ) +
scale_x_discrete(breaks= 1:5 , labels= paste("Q", 1:5, sep = "") ) +
geom_hline( yintercept = 0, colour = "red", linetype = 2);</pre>
```

# show the plot



说明:

业种情况下,我们通常只看 median 值的趋势;

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# another example plot

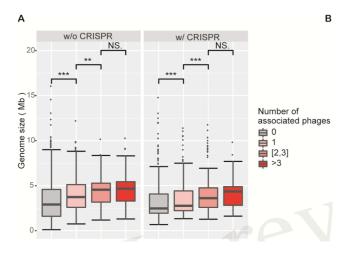
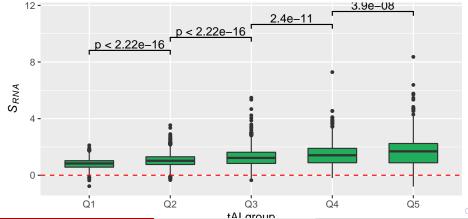


Figure 1: a figure from an in-press manuscript

## how to add significance indicators to plot??

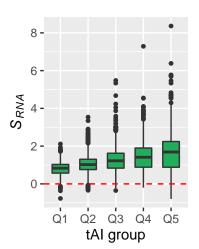
ggplot2 的扩展包, geom\_signif; 如果第一次使用, 请先安装。



# boxplot 画图注意事项

正确的画法为: 要高瘦, 不要矮胖!!!!

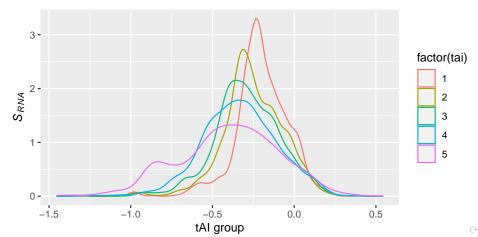
fig3a;



## 此类数据的另一种可视化方式

density plot; 但在此例中,不如 boxplot 好。

```
ggplot( data.fig3a, aes( trans.at, colour = factor(tai) ) ) + geom_density( ) +
xlab( "tAI group" ) + ylab( expression( paste( italic(S[RNA]) ) ) );
```



section 4: two column data: part 2

#### 数据介绍: two numerical vectors

#### 多用于描述两组(量化)数据之间的关系;

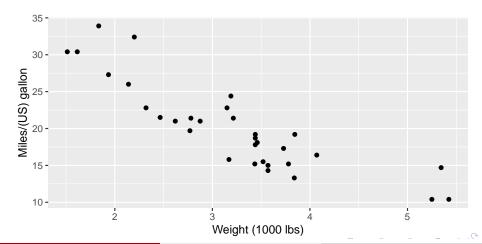
以 mtcars 为例:

```
head(mtcars);
```

```
mpg cyl disp hp drat
                                              wt qsec vs am gear carb
                    21.0
## Mazda RX4
                           6 160 110 3.90 2.620 16.46 0
## Mazda RX4 Wag
                    21.0
                              160 110 3.90 2.875 17.02 0 1
                              108 93 3.85 2.320 18.61 1 1 4
258 110 3.08 3.215 19.44 1 0 3
## Datsun 710
                    22.8
## Hornet 4 Drive
                    21.4
                              360 175 3.15 3.440 17.02 0 0
## Hornet Sportabout 18.7 8
## Valiant
                    18.1
                              225 105 2.76 3.460 20.22 1 0
```

## 查看重量与燃油效率之间的关系

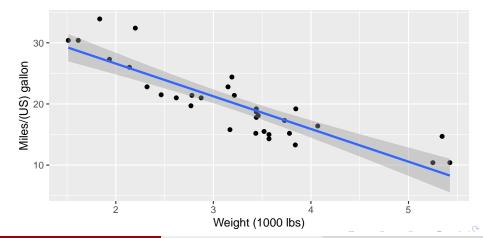
```
plotcars <-
   ggplot( mtcars, aes( x = wt, y = mpg ) ) +
      geom_point() + xlab( "Weight (1000 lbs)" ) + ylab( "Miles/(US) gallon" );
plotcars;</pre>
```



# smooth, 减少噪音

```
plotcars + geom_smooth( method = "lm" ); ## default is lowess
```

## `geom\_smooth()` using formula 'y ~ x'



# expression(R^2) variance of x explained by y ...

```
( r <- with( mtcars, cor.test( mpg, wt )$estimate ) );

## cor
## -0.8676594

## variance of mpg can be explained by weight
r^2;</pre>
```

## cor ## 0.7528328

## 当趋势不明显时,可以按另一组数据分组

这里还以 mtcars 为例。

两种分组(binning)方法 equal-distance, equal-size binning

举例:

## ntile 函数的参数

#### ... \*tile 函数都是 equal size

```
## ntile 的结果
table( mtcars2$group1 );
```

```
##
## 1 2 3 4
## 8 8 8 8
```

#### cut 函数

### 按指定的间隔 (breaks) 对数据进行分割。

```
##
## [1.51,2.49] (2.49,3.47] (3.47,4.45] (4.45,5.42]
## 8 13 8 3
```

#### 使用方法:

```
cut(x, ...)
# S3 method for default
cut(x, breaks, labels = NULL,
   include.lowest = FALSE, right = TRUE, dig.lab = 3,
   ordered_result = FALSE, ...)
```

#### cut 示例

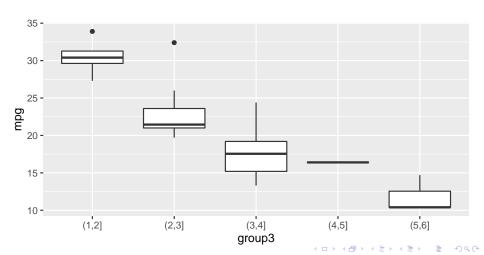
#### 不仅可用于 equal distance, 还可以用于任意间距

```
mtcars3 <- mtcars2 %>%
  mutate( group3 = cut( mtcars$wt, breaks = c(0,1,2,3,4,5,6) ) ) ;
table(mtcars3$group3);
```

```
##
## (0,1] (1,2] (2,3] (3,4] (4,5] (5,6]
## 0 4 8 16 1 3
```

# 分组后的数据适合用 boxplot

```
ggplot( mtcars3, aes( group3, mpg ) ) +
  geom_boxplot();
```



#### 小结

#### 目前讲述了以下内容:

#### 一维数据

table, summary, range, quantile, mean, median ...

#### 二维数据

- boxplot
- point plot
- correlation
- 分组: equal distance, equal size binning ...

# section 5: parametric tests

### parametric tests

- 包括:
  - t-test
  - analysis of variance
  - linear regression
- ② 数据有较明确的分布 (e.g. normal distribution), 或假设数据有明确的分布; 当假设不成立时, 检测会无效;
- 更灵敏 (相比 nonparametric test), p-value 更低

more to read: http://rcompanion.org/handbook/I\_01.html

#### 适用性

#### 适用于

- 数量化性状,比如:身高、体重、产量、污染值
- 整数值: 成绩、年龄、每天步数

#### 不适用于

- 其它 count data 或者 discrete data;
- 或者有太多趋向于 min 或 max 的值
- 百分比或比例

详见: http://rcompanion.org/handbook/index.html

## 需要的 packages

#### 需要的 packages

```
## chooseCRANmirror()
if(!require(psych)) {
    install.packages("psych");
}
if( !require(rcompanion) ) {
    install.packages("rcompanion");
}
library(psych);
library(rcompanion)
```

## 数据

#### 注意 source() 函数的用法

## 'data frame': 26 obs. of 5 variables:

```
source("data/talk10/input_data1.R"); ## 裴入 Data data.frame ...
str(Data);
```

```
## $ Student: chr "a" "b" "c" "d" ...
## $ Sex : chr "female" "female" "female" "female" ...
## $ Teacher: chr "Catbus" "Catbus" "Catbus" "Catbus" ...
## $ Steps : int 8000 9000 10000 7000 8000 7000 5000 9000 7000 ...
## $ Rating : int 7 10 9 5 4 8 6 5 10 8 ...
```

## 检查数据

```
library(psych)
```

```
##
## Attaching package: 'psych'
## The following objects are masked from 'package:ggplot2':
##
##  %+%, alpha
```

#### headTail(Data); ## psych 包提供的函数

```
##
      Student
                 Sex Teacher Steps Rating
## 1
            a female Cathus
                              8000
            b female Catbus
## 2
                              9000
                                       10
            c female Catbus 10000
            d female Cathus 7000
         <NA> <NA>
                     <NA>
                              . . .
                                      . . .
## 23
            w male Totoro
                              6000
                                       8
## 24
            x male
                      Totoro
                              8000
                                      10
## 25
                male
                      Totoro
                              7000
## 26
                male Totoro
                              7000
                                       7
```

## 杳看数据, cont.

```
## 其它常用函数
str(Data)
## 'data.frame':
                   26 obs. of 5 variables:
   $ Student: chr
                   "a" "b" "c" "d" ...
   $ Sex
         : chr "female" "female" "female" "female" ...
  $ Teacher: chr "Catbus" "Catbus" "Catbus" "Catbus" ...
   $ Steps : int 8000 9000 10000 7000 6000 8000 7000 5000 9000 7000 ...
##
##
   $ Rating: int 7 10 9 5 4 8 6 5 10 8 ...
summary(Data)
```

```
##
     Student
                          Sex
                                          Teacher
                                                               Steps
   Length:26
                     Length:26
                                        Length:26
                                                           Min.
                                                                  : 5000
   Class :character
                      Class :character
                                        Class : character
                                                           1st Qu.: 7000
                                        Mode : character
                                                           Median: 8000
   Mode :character
                      Mode :character
##
                                                           Mean : 7692
##
                                                           3rd Qu.: 8750
##
                                                           Max.
                                                                  :10000
##
       Rating
   Min. : 4.000
   1st Qu.: 7.000
   Median : 8.000
##
  Mean : 7.615
   3rd Qu.: 9.000
   Max.
          :10.000
```

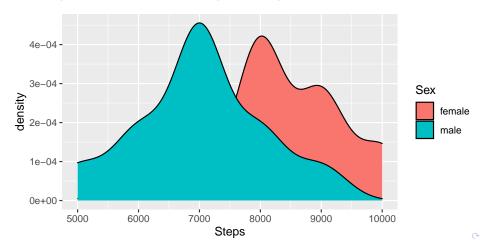
## parametric test 的要求

- 随机取样
- ② 值或 residuals 为正态分布;residules 是指观察值与预测值 (mean) 之 差

## 数据的分布

```
ggplot(Data, aes(Steps, fill = Sex)) +
    geom_density(position="dodge", alpha = 1)
```

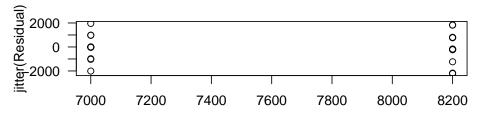
## Warning: Width not defined. Set with `position\_dodge(width = ?)`



### parametric test 的要求, cont.

#### ● 有相同的 variance

```
M1 = mean(Data$Steps[Data$Sex=="female"])
M2 = mean(Data$Steps[Data$Sex=="male"])
Data$Mean[Data$Sex=="female"]
Data$Mean[Data$Sex=="male"]
                              = M2
Data$Residual = Data$Steps - Data$Mean
plot(jitter(Residual) ~ Mean, data = Data, las = 1);
```



#### how to detect outlier ??

一个很模糊的定义: Outliers are extreme values that fall a long way outside of the other observations. For example, in a normal distribution, outliers may be values on the tails of the distribution.

对于 normal distribution,通常 mean +- 2 or 3 \* sd

对于 non-parametric distribution (注: IRQ 计算可使用同名函数: IRQ):

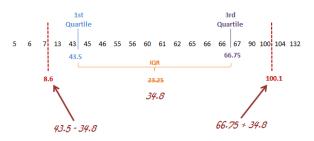
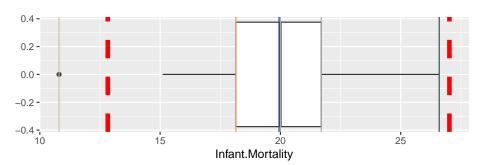


Figure 2: Tukey's method for outlier detection

## an example of outlier values



## one sample t-test

#### 检测分布是否与预期一致;比如:男生每天的步数是否显著区别于 1 万

```
with( Data, t.test( Steps[ Sex == "male" ], mu = 10000 ) );
```

```
##
## One Sample t-test
##
## data: Steps[Sex == "male"]
## t = -9.083, df = 10, p-value = 3.81e-06
## alternative hypothesis: true mean is not equal to 10000
## 95 percent confidence interval:
## 6264.07 7735.93
## sample estimates:
## mean of x
## 7000
```

## two samples t-test

with( Data, t.test( Steps ~ Sex ) )

#### 比较 sd 和 mean ,可应用于正态分布。几种使用方法:

```
##
## Welch Two Sample t-test
##
## data: Steps by Sex
## t = 2.6424, df = 22.816, p-value = 0.01461
## alternative hypothesis: true difference in means between group female and group male is not
## 95 percent confidence interval:
## 260.1421 2139.8579
## sample estimates:
## mean in group female mean in group male
## 8200 7000
```

# two sample t-test 使用方法 2

```
##
## Welch Two Sample t-test
##
## data: Steps[Sex == "male"] and Steps[Sex == "female"]
## t = -2.6424, df = 22.816, p-value = 0.01461
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## -2139.8579 -260.1421
## sample estimates:
## mean of x mean of y
## 7000 8200
```

# two sample t test 检测结果

```
res <- with( Data, t.test( Steps ~ Sex ) );
str(res):
## List of 10
   $ statistic : Named num 2.64
## ..- attr(*, "names")= chr "t"
## $ parameter : Named num 22.8
    ..- attr(*, "names")= chr "df"
## $ p.value : num 0.0146
## $ conf.int : num [1:2] 260 2140
## ..- attr(*, "conf.level")= num 0.95
## $ estimate : Named num [1:2] 8200 7000
    ..- attr(*, "names")= chr [1:2] "mean in group female" "mean in group male"
   $ null.value : Named num 0
    ..- attr(*, "names")= chr "difference in means between group female and group male"
## $ stderr : num 454
## $ alternative: chr "two.sided"
## $ method : chr "Welch Two Sample t-test"
   $ data.name : chr "Steps by Sex"
   - attr(*, "class")= chr "htest"
```

## paired two sample t test

## 例如: 辅导前后的学生成绩:

```
source("data/talk10/input_data2.R");
head(scores);
```

```
## 1 Before a 65
## 2 Before b 75
## 3 Before c 86
## 4 Before d 69
## 5 Before e 60
```

Time Student Score

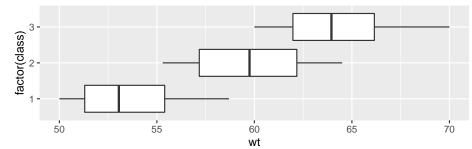
## paired two sample t test

```
scores.wide <- scores %>% spread( Time, Score );
head(scores.wide. n = 3):
    Student After Before
               77
                      65
          b 98
                      75
## 3
               92
                   86
with( scores.wide, t.test( After, Before, paired = T ) );
##
   Paired t-test
##
## data: After and Before
## t = 3.8084, df = 9, p-value = 0.004163
## alternative hypothesis: true difference in means is not equal to 0
## 95 percent confidence interval:
## 4.141247 16.258753
## sample estimates:
## mean of the differences
##
                     10.2
```

## one way ANOVA

**ANOVA**: similar to indepedent t-test, but can be applied to multiple groups

#### 比如: 3 个班学生的体重



## one way ANOVA, cont.

```
library(FSA); ## 如果没有这个句, 请先安装 ...
## ## FSA v0.9.0. See citation('FSA') if used in publication.
## ## Run fishR() for related website and fishR('IFAR') for related book.
##
## Attaching package: 'FSA'
## The following object is masked from 'package:psych':
##
##
       headtail
with( wts. Summarize( wt ~ class. digits = 3 ) ):
```

```
## class n mean sd min Q1 median Q3 max
## 1 1 20 53.755 2.906 50.0 51.300 53.05 55.400 58.7
## 2 2 20 59.860 2.827 55.3 57.175 59.75 62.175 64.5
## 3 3 20 64.415 3.146 60.0 61.975 63.95 66.150 70.0
```

#### linear model

#### 两个问题:

● 组间有显著区别吗?

```
model <- lm( wt ~ class, data = wts );
anova( model );</pre>
```

#### **ANOVA**

summary( model );

② 分组对变量的贡献(r-square, aka. variance explained )

```
##
## Call:
## lm(formula = wt ~ class, data = wts)
##
## Residuals:
      Min
               1Q Median
                              3Q
                                     Max
## -4.6733 -2.4508 -0.2933 2.1142 5.3267
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 48.6833
                          1.0112 48.14 <2e-16 ***
                          0.4681 11.39 <2e-16 ***
## class
              5.3300
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.961 on 58 degrees of freedom
## Multiple R-squared: 0.6909, Adjusted R-squared: 0.6856
## F-statistic: 129.6 on 1 and 58 DF, p-value: < 2.2e-16
```

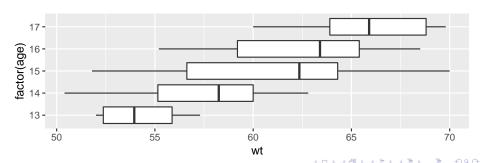
#### 其中的值都是什么意思???

## one way ANOVA with blocks

#### 同时有多个因素影响体重时,哪些才是主要的?

```
wts2 <- bind_rows(
    tibble( class = 1, age = sample( 13:15, 20, replace = T ), wt = sample( seq(50, 60, by = 0.1
    tibble( class = 2, age = sample( 14:16, 20, replace = T ), wt = sample( seq(55, 65, by = 0.1
    tibble( class = 3, age = sample( 15:17, 20, replace = T ), wt = sample( seq(60, 70, by = 0.1
);

ggplot(wts2, aes( factor( age ), wt ) ) + geom_boxplot() + coord_flip();</pre>
```



## one way ANOVA with blocks, cont.

如何获得 r.squre value ???

# one way ANOVA with blocks, 各个 factor 的重要性??

```
library(relaimpo);
res3 <- calc.relimp( wt ~ factor(class) + age, data = wts2 );
res3$R2: ## A R2
## [1] 0.6868643
res3$1mg; ## 每个因素的贡献;
## factor(class)
                         age
      0.5163988 0.1704654
## 测试 rela 参数:
res4 <- calc.relimp( wt ~ factor(class) + age, data = wts2, rela = T);
res4$R2: ## A R2
## [1] 0.6868643
res4$1mg: ## 每个因素的贡献;
## factor(class)
                         age
```

0.7518208 0.2481792

# two way ANOVA

一个变量受另外两个因素影响的分;比如上例中 体重受 年级和 年龄的影响。

年级和 年龄至少有 4 个 unique combinations.

3 8 65.213 2.182 62.2 63.475

3 7 65 871 3 606 60 0 63 900

Summarize(wt ~ age + class, data = wts2, digits=3);

实际上,上面的 block test 可以认为是 two-way ANOVA 分析

```
Q1 median
    age class n
                   mean
                          sd min
                                                   03
## 1
     13
               4 54.300 2.499 52.0 52.375 53.95 55.875 57.3
## 2
     14
            1 12 56,300 2,905 50,4 54,650 57,20 58,700 59,6
## 3
            1 4 53.925 1.725 51.8 53.075 54.00 54.850 55.9
            2 4 62.075 0.690 61.2 61.725 62.15 62.500 62.8
            2 9 60.778 3.384 56.5 57.100 62.60 63.700 64.4
## 5
     15
## 6
     16
            2 7 58.957 3.668 55.2 55.850 58.90 61.100 64.7
```

3 5 66.080 3.006 62.1 65.000 65.40 67.900 70.0

## 7 15

## 8 16

## 9 17

65.20 66.675 68.5

65.90 68.800 69.8

# two way ANOVA, cont.

```
model3 <- lm( wt ~ class + age + class:age, data = wts2);
anova( model3 );

## Analysis of Variance Table
##
## Response: wt
## Df Sum Sq Mean Sq F value Pr(>F)
## class 1 1047.55 1047.55 121.5567 1.182e-15 ***
## age 1 11.98 11.98 1.3902 0.2434
## class:age 1 0.56 0.56 0.0649 0.7999
```

其中: class 和 age 称为 main effects, class:age 称为 interaction effects

## Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.05 '.' 0.1 ' ' 1

## Residuals 56 482.60 8.62

## relative importance of interactions

```
res5 <- calc.relimp( wt ~ factor(class) + age + factor(class):age, data = wts2);
res5$R2; ## 总 R2

## [1] 0.6967638

res5$lmg; ## 每个因素的贡献;

## factor(class) factor(class):age age
```

0.170465426

more to read about the interaction effects:

0.009899486

http://oak.ucc.nau.edu/rh232/courses/EPS625/Handouts/Two-way% 20ANOVA/Understanding%20the%20Two-way%20ANOVA.pdf

0.516398844

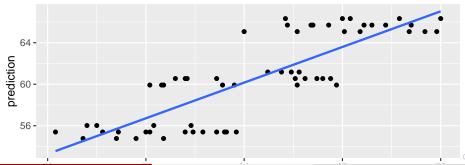
# 用模型进行预测 predict

```
model2 = lm(formula = wt ~ class + age, data = wts2)
```

```
newdata <- wts2 %>% dplyr::select( class, age );
wt.predicted <- predict( model2, newdata );

dat <- data.frame( reference = wts2$wt, prediction = wt.predicted );
ggplot( dat , aes( x = reference, y = prediction ) ) + geom_point() +
    geom_smooth( method = "lm", se = F );</pre>
```

```
## `geom_smooth()` using formula 'y ~ x'
```



# prediction 与 original data 的 correlation 是多少??

```
with( dat, cor.test( prediction, reference ) ) $estimate;
         cor
## 0.8287394
## R ^ 2
with( dat, cor.test( prediction, reference ) ) $estimate ^2;
        cor
## 0.686809
## 正好是 model2 的 r.squred ...
summary( model2 )$r.squared;
```

## [1] 0.686809

# 手动计算 prediction

在一个 linear model 中, wt = intercept + a \* class + b \* age 而 intercept, a, b 的值分别为:

```
## (Intercept) class age
## 58.3992510 5.7757449 -0.6268999

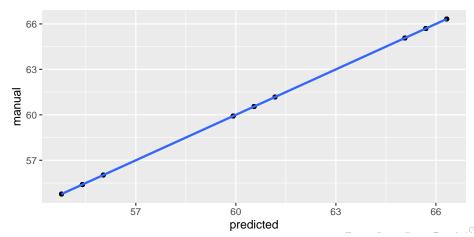
predicted2 <-
    paras[1] + paras["age"] * wts2$age + paras["class"] * wts2$class;

plot <-
    ggplot( data.frame( predicted = wt.predicted, manual = predicted2 ),
        aes( predicted, manual ) ) +
        geom_point() + geom_smooth( method = "lm", se = F );</pre>
```

# show the plot

```
plot;
```

## `geom\_smooth()` using formula 'y ~ x'



## 更多更方便的函数

#### 以下函数也可以用于 multivariable analysis / multiple regression

```
fit <- lm(y ~ x1 + x2 + x3, data=mydata)
summary(fit) # show results

# Other useful functions
coefficients(fit) # model coefficients
confint(fit, level=0.95) # CIs for model parameters
fitted(fit) # predicted values
residuals(fit) # residuals
anova(fit) # anova table
vcov(fit) # covariance matrix for model parameters
influence(fit) # regression diagnostics</pre>
```

# linear regression 注意事项

- ① 是 parametric test
- ② 假设变量之间独立 (比如: **年龄和班级**之间没有关联)
- 4 homogeneity of variance

但实际上 ...

### multivariable analysis

more to read:

- https://www.statmethods.net/stats/regression.html
- https://data.library.virginia.edu/
  getting-started-with-multivariate-multiple-regression/

```
# Multiple Linear Regression Example
fit \leftarrow lm(y \sim x1 + x2 + x3, data=mydata)
summary(fit) # show results
# compare models
fit1 \leftarrow lm(y \sim x1 + x2 + x3 + x4, data=mydata)
fit2 < -lm(y ~ x1 + x2)
anova(fit1, fit2)
# K-fold cross-validation
library(DAAG)
cv.lm(df=mydata, fit, m=3) # 3 fold cross-validation
# Stepwise Regression; feature selection
library(MASS)
fit <- lm(v~x1+x2+x3,data=mvdata)
step <- stepAIC(fit, direction="both")</pre>
step$anova # display results
```

# extended reading

- repeated measures ANOVA:http://rcompanion.org/handbook/I\_09.html, 同一变量、不同时间段的重复测量(对上例中学生的体重进行多次测量)
- correlation and linear regression: http://rcompanion.org/handbook/I\_10.html
- onn-linear regression: https://www.amazon.com/ Statistical-Tools-Nonlinear-Regression-Statistics/dp/ 0387400818

更多详见: http://rcompanion.org/handbook/I\_08.html

## section 6: non-parametric test

#### wilcox.test and kruskal.test

```
# independent 2-group Mann-Whitney U Test
with( Data, wilcox.test( Steps ~ Sex ) );
## Warning in wilcox.test.default(x = c(8000L, 9000L, 10000L, 7000L, 6000L, :
## cannot compute exact p-value with ties
##
   Wilcoxon rank sum test with continuity correction
##
## data: Steps by Sex
## W = 127.5, p-value = 0.01773
## alternative hypothesis: true location shift is not equal to 0
# Kruskal Wallis Test One Way Anova by Ranks
with( Data, kruskal.test( Steps ~ Sex ) ):
```

```
##
## Kruskal-Wallis rank sum test
##
## data: Steps by Sex
## Kruskal-Wallis chi-squared = 5.7494, df = 1, p-value = 0.01649
```

# 作业与练习

#### 作业与练习

- Exercises and homework 目录下 talk10-homework.Rmd 文件
- 完成时间: 见钉群的要求

