Linear and nonlinear regression HUST Bioinformatics course series

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section 1: TOC

前情提要

- R basics
- R data wrangler
- R plot
- R string, regular expression
- R parallel computing

本次提要

- linear regression
- nonlinear regression
- modeling and prediction
- K-fold & X times cross-validation
- external validation

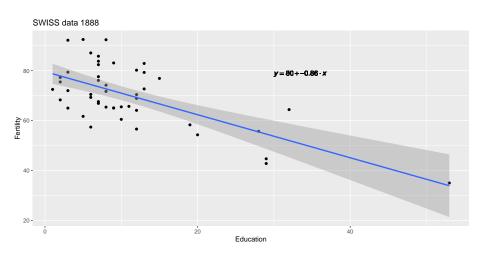
section 2: Linear regression

what is linear regression?

线性回归是利用数理统计中回归分析,来确定两种或两种以上变量间相互 依赖的定量关系的一种统计分析方法

- Y 可以被一个变量 X 解释; 一元线性回归
- Y 可以被 X, Z 等多个变量解释; multivariate linear regression

举例



解释

```
m <- lm(Fertility ~ Education, data = swiss);</pre>
summarv(m):
##
## Call:
## lm(formula = Fertility ~ Education, data = swiss)
##
## Residuals:
      Min
               10 Median
                               30
                                     Max
## -17.036 -6.711 -1.011 9.526 19.689
##
## Coefficients:
              Estimate Std. Error t value Pr(>|t|)
##
## (Intercept) 79.6101
                           2.1041 37.836 < 2e-16 ***
## Education -0.8624
                           0.1448 -5.954 3.66e-07 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 9.446 on 45 degrees of freedom
## Multiple R-squared: 0.4406, Adjusted R-squared: 0.4282
## F-statistic: 35.45 on 1 and 45 DF, p-value: 3.659e-07
```

lm([target variable] ~ [predictor variables], data = [data source])



得到 Coefficients

```
coef( m );
## (Intercept) Education
## 79.6100585 -0.8623503
```

other useful functions

```
# Other useful functions
coefficients(m) # model coefficients
confint(m, level=0.95) # CIs for model parameters
fitted(m) # predicted values
residuals(m) # residuals
anova(m) # anova table
vcov(m) # covariance matrix for model parameters
influence(m) # regression diagnostics
```

R-squred a.k.a R2 是怎么来的?

```
library(magrittr);
library(caret);
predictions <- m %>% predict( swiss ); ## or use fitted(m) instead ...

# Model performance
data.frame(
    RMSE = RMSE(predictions, swiss$Fertility),
    R2 = R2(predictions, swiss$Fertility)
)
```

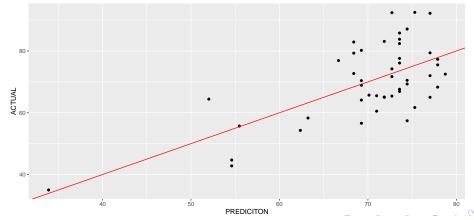
```
## RMSE R2
## 1 9.242865 0.4406156
```

RMSE mean squared error, the smaller the better R2 R, higher the better * F-statistic: Higher the better

R-squred a.k.a R2 是怎么来的?cont.

```
data.frame( PREDICITON = predictions, ACTUAL = swiss$Fertility ) %>%
    ggplot(aes( PREDICITON, ACTUAL )) + geom_point() +
    ggtitle( "SWISS DATA 1888 Fertility" ) +
    geom_abline(intercept = 0, slope = 1, colour = "red")
```





Multivariate linear modeling

datarium package

```
install.packages("datarium");
library(datarium);
head(marketing);
```

```
276.12
              45.36
                       83.04 26.52
    53.40
             47.16
                       54.12 12.48
## 3
    20.64
            55.08
                       83.16 11.16
     181.80
            49.56
                       70.20 22.20
     216.96
             12.96
                       70.08 15.48
## 6
      10.44
              58.68
                       90.00 8.64
```

voutube facebook newspaper sales

问题: 广告投放在哪里对销售有帮助??

m1 <- lm(sales ~ youtube + facebook + newspaper, data = marketing);</pre>

multivariate linear modeling, cont.

m2 <- lm(sales ~ youtube, data = marketing);</pre>

```
m3 <- lm( sales ~ facebook, data = marketing):
summary(m1);
##
## Call:
## lm(formula = sales ~ youtube + facebook + newspaper, data = marketing)
##
## Residuals:
       Min
                 10 Median
                                          Max
                                  30
## -10.5932 -1.0690 0.2902 1.4272
                                       3.3951
##
## Coefficients:
##
               Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.526667 0.374290 9.422 <2e-16 ***
## voutube 0.045765 0.001395 32.809 <2e-16 ***
## facebook 0.188530 0.008611 21.893 <2e-16 ***
## newspaper -0.001037 0.005871 -0.177 0.86
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 2.023 on 196 degrees of freedom
## Multiple R-squared: 0.8972, Adjusted R-squared: 0.8956
## F-statistic: 570.3 on 3 and 196 DF, p-value: < 2.2e-16
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                                 Linear and nonlinear regression
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                                                                                     14 / 56
```

facebook vs. youtube

```
coef( m1 );

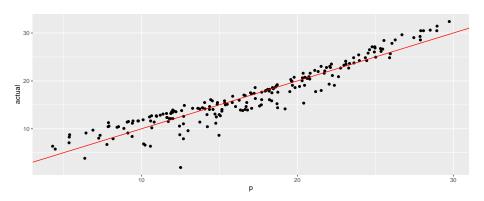
## (Intercept) youtube facebook newspaper
## 3.526667243 0.045764645 0.188530017 -0.001037493

data.frame( YOUTUBE = summary(m2)$r.squared, FACEBOOK = summary(m3)$r.squared);
```

YOUTUBE FACEBOOK 1 0.6118751 0.3320325

predicted vs. actual

```
predicted.m1 <- m1 %>% predict( marketing );
data.frame(p = predicted.m1, actual = marketing$sales ) %>%
    ggplot( aes(x = p, y = actual) ) + geom_point() +
    geom_abline(intercept = 0, slope = 1, colour = "red");
```



performance evaluation

```
# Model performance
data.frame(
   RMSE = RMSE(predicted.m1, marketing$sales ),
   R2 = R2(predicted.m1, marketing$sales )
)
```

```
## RMSE R2
## 1 2.002284 0.8972106
```

0.8971943

get rid of newspaper

```
m4 <- lm( sales ~ youtube + facebook, data = marketing );
anova(m1. m4):
## Analysis of Variance Table
##
## Model 1: sales ~ youtube + facebook + newspaper
## Model 2: sales ~ voutube + facebook
    Res.Df
              RSS Df Sum of Sq F Pr(>F)
## 1
       196 801 83
## 2 197 801.96 -1 -0.12775 0.0312 0.8599
data.frame(
 with newspapers = summary(m1)$r.squared,
 without newspapers = summary(m4)$r.squared
    with_newspapers without_newspapers
```

1

0.8972106

relative importance analysis

```
library(relaimpo);
calc.relimp( sales ~ youtube + facebook + newspaper, data = marketing );
## Response variable: sales
## Total response variance: 39.19947
## Analysis based on 200 observations
##
## 3 Regressors:
## youtube facebook newspaper
## Proportion of variance explained by model: 89.72%
## Metrics are not normalized (rela=FALSE).
##
## Relative importance metrics:
##
##
                    lmg
## youtube 0.58527298
## facebook 0.28878652
## newspaper 0.02315114
##
## Average coefficients for different model sizes:
##
##
                     1 X
                               2Xs
                                            3Xs
## voutube 0.04753664 0.04632801 0.045764645
## facebook 0.20249578 0.19351941 0.188530017
## newspaper 0.05469310 0.02543180 -0.001037493
```

interactions

interactions 考虑因素之间的依赖关系或互作关系,比如,在一平台上投放广告会促进另一个平台上广告的效果,因为两个平台的用户可能是重叠的。他们在两个平台都看到广告时,更可能购买产品。

```
m5 <- lm( sales ~ youtube + facebook + youtube:facebook, data = marketing );
anova(m4, m5);
## Analysis of Variance Table
##
## Model 1: sales ~ youtube + facebook
## Model 2: sales ~ youtube + facebook + youtube:facebook
              RSS Df Sum of Sq F Pr(>F)
    Res.Df
       197 801.96
## 1
       196 251.26 1 550.7 429.59 < 2.2e-16 ***
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
data.frame(
 no interactions = summary(m4)$r.squared,
 with interactions = summary(m5)$r.squared
    no interactions with interactions
```

0.8971943 0.9677905

1

interactions, cont.

```
## m5 <- lm( sales ~ youtube + facebook + youtube:facebook, data = marketing );</pre>
## 上面的 m5 可以直接写为:
m6 <- lm( sales ~ youtube*facebook, data = marketing );
summary(m6);
##
## Call:
## lm(formula = sales ~ youtube * facebook, data = marketing)
##
## Residuals:
              10 Median
##
      Min
                              30
                                    Max
## -7.6039 -0.4833 0.2197 0.7137 1.8295
##
## Coefficients:
##
                   Estimate Std. Error t value Pr(>|t|)
## (Intercept) 8.100e+00 2.974e-01 27.233 <2e-16 ***
## voutube
                1.910e-02 1.504e-03 12.699 <2e-16 ***
## facebook
                 2.886e-02 8.905e-03 3.241 0.0014 **
## voutube:facebook 9.054e-04 4.368e-05 20.727 <2e-16 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error: 1.132 on 196 degrees of freedom
## Multiple R-squared: 0.9678, Adjusted R-squared: 0.9673
## F-statistic: 1963 on 3 and 196 DF. p-value: < 2.2e-16
                                                         ◆□▶ ◆問▶ ◆量▶ ◆量 ◆ のQ@
```

visualize interactions

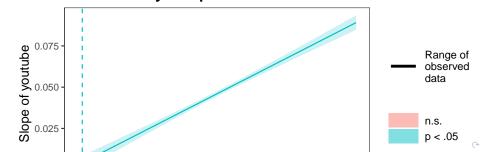
```
## install.packages("interactions"); 如需要,请安装这个包library(interactions); ## 装入
sim_slopes(m6, pred = youtube, modx = facebook, jnplot = TRUE)

## JOHNSON-NEYMAN INTERVAL
```

```
## When facebook is OUTSIDE the interval [-26.70, -16.41], the slope of
## youtube is p < .05.
##</pre>
```

Note: The range of observed values of facebook is [0.00, 59.52]

Johnson-Neyman plot



relative importance analysis including interactions

```
library(relaimpo);
calc.relimp( sales ~ youtube*facebook, data = marketing );
## Response variable: sales
## Total response variance: 39.19947
## Analysis based on 200 observations
##
## 3 Regressors:
## youtube facebook youtube:facebook
## Proportion of variance explained by model: 96.78%
## Metrics are not normalized (rela=FALSE).
##
## Relative importance metrics:
##
##
                           lmg
## youtube
                   0.58851843
## facebook
                    0.30867583
## voutube:facebook 0.07059629
##
## Average coefficients for different model sizes:
##
##
                            1 X
                                       2Xs
                                                    3Xs
## voutube
                    0.04753664 0.04575482 0.0191010738
## facebook
                    0.20249578 0.18799423 0.0288603399
## youtube:facebook
                           NaN
                                      NaN 0.0009054122
```

assumptions of linear regression

重要信息

- 任何检验都有基本的假设
- 将检验应用于不符合假设的数据是统计学最大的滥用

assumptions

- 1 Linearity: The relationship between X and the mean of Y is linear.
- 4 Homoscedasticity: The variance of residual is the same for any value of X.
- Independence: Observations are independent of each other.
- Normality: For any fixed value of X, Y is normally distributed.

glm vs. lm

```
lm(formula, data, ...)
glm(formula, family=gaussian, data, ...)
glm:
     当 family=gaussian 时,二者是一样的。
library(texreg);
m.lm <- lm(am ~ disp + hp, data=mtcars);</pre>
m.glm <- glm(am ~ disp + hp, data=mtcars);</pre>
screenreg(1 = list(m.lm, m.glm))
##
##
                   Model 1
                              Model 2
   (Intercept)
                  0.76 *** 0.76 ***
                   (0.16) (0.16)
##
## disp
                   -0.00 ***
                              -0.00 ***
##
                   (0.00)
                           (0.00)
## hp
                  0.00 *
                           0.00 *
                   (0.00)
##
                               (0.00)
## R^2
                   0.48
## Adj. R^2
                  0.45
## Num. obs.
                   32
                               32
## AIC
                               32.13
```

glm 还可用于其它类型数据的分析

Logistic regression (family=binomial)

预测的结果(Y)是 binary 的分类, 比如 Yes, No, 且只能有两个值;

```
## 34 2.220446e-16 setosa
## 24 4.132652e-11 setosa
## 7 7.748530e-13 setosa
## 14 2.220446e-16 setosa
## 63 1.000000e+00 virginica
## 94 1.000000e+00 virginica
```

注意:

glm 的 Poisson regression (family=poisson)

Poisson regression is a special type of regression in which the response variable consists of **count data**.

Asumptions:

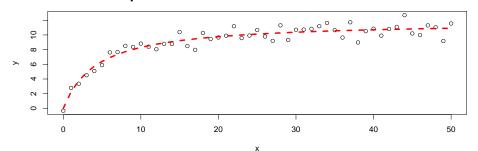
- The response variable consists of count data.
- Observations are independent.
- The mean and variance of the model are equal.
- The distribution of counts follows a Poisson distribution.

section 3: Non-linear regression (nls)

一元 nls

什么是 nls? to predict a target variable using a non-linear function consisting of parameters and one or more independent variables.

non-linear least squares



non-linear least squares

```
## 1. generate data
set.seed(20160227)
x<-seq(0,50,1)
y<-((runif(1,10,20)*x)/(runif(1,0,10)+x))+rnorm(51,0,1)

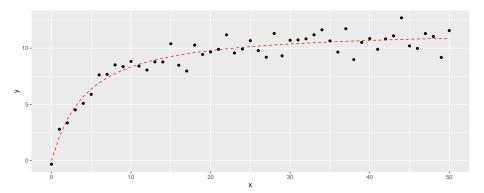
## 2. fit model using nls
m<-nls(y-a*x/(b+x), start = list(a=0.1, b=0.1));

## 3. show how good is the fitting ...
#get some estimation of goodness of fit
plot(x,y)
lines(x,predict(m),lty=2,col="red",lwd=3)</pre>
```

```
1 nls( equation, data = data, start = ...)
2 y-a*x/(b+x)
```

non-linear least squares, using drc

```
library(drc); ## Analysis of Dose-Response Curves
m13 <- drm( y ~ x, fct = LL.3() ); ## here LL.3() is a least square function
data.frame( x = x, y = y, fitted = predict(m13) ) %>% ggplot( aes(x=x,y=y) ) +
  geom_point() + geom_line( aes(x = x, y = fitted), colour = "red", linetype = 2 );
```



non-linear functions

Polynomials

- Linear equation
- Quadratic polynomial

Concave/Convex curves (no inflection)

- Exponential equation
- Asymptotic equation
- Negative exponential equation
- Power curve equation
- Logarithmic equation
- Rectangular hyperbola

Sygmoidal curves

- Logistic equation
- Gompertz equation
- Log-logistic equation (Hill equation)

example: Exponential equation

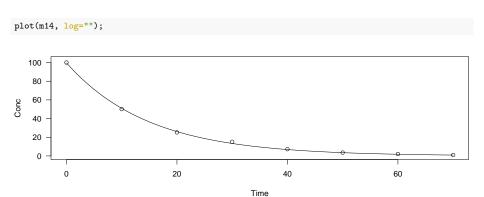
```
Exponential decay
```

library(aomisc);

```
y = a * (exp(k * X) * k)
```

```
## Loading required package: plvr
## You have loaded plvr after dplvr - this is likely to cause problems.
## If you need functions from both plyr and dplyr, please load plyr first, then dplyr:
## library(plyr); library(dplyr)
##
## Attaching package: 'plyr'
## The following objects are masked from 'package:dplyr':
##
##
      arrange, count, desc. failwith, id. mutate, rename, summarise,
      summarize
##
## The following object is masked from 'package:purrr':
```

plot Exponential decay



Power curve

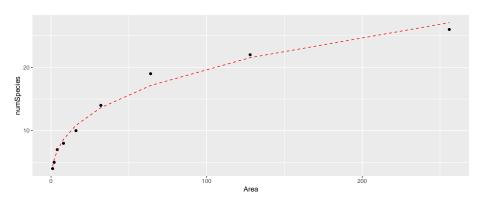
##

```
## Model fitted: Power curve (Freundlich equation) (2 parms)
##
## Parameter estimates:
##
## Estimate Std. Error t-value p-value
## a:(Intercept) 4.348404 0.337197 12.896 3.917e-06 ***
## b:(Intercept) 0.329770 0.016723 19.719 2.155e-07 ***
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
##
## Residual standard error:
##
## 0.9588598 (7 degrees of freedom)
```

重点: 1. DRC.powerCurve 作为建模的参数,来自 library(aomisc)

Power curve 结果作图

```
speciesArea %>% mutate( fitted = predict( m15, speciesArea ) ) %>%
ggplot( aes(x= Area, y= numSpecies) ) +
geom_point() + geom_line( aes(x = Area, y = fitted), colour = "red", linetype = 2 );
```



how good is the model?

```
## [1] 0.9874392

## compare with a linear model
m16 <- lm( numSpecies ~ Area, data = speciesArea );
R2( speciesArea$numSpecies, predict( m16, speciesArea );</pre>
```

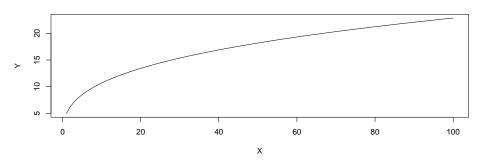
[1] 0.8110041

数据生成函数

aomisc 包和 drc 包带了非常多数据生成的函数, 其使用示例如下:

注 a * (X^(b - 1) * b) 需要两个参数, a 和 b

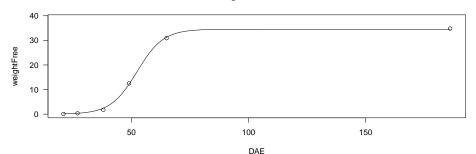
Power curve (b = 0.33)



logistic function

```
data(beetGrowth)
m17 <- drm(weightFree ~ DAE, fct = L.3(), data = beetGrowth)
plot(m17, log="", main = "Logistic function")</pre>
```

Logistic function



多元 non-linear regression

- mars: Multivariate Adaptive Regression Splines (多元自适应回归样条)
- 2 machine learning

推荐一本教程: Hands-On Machine Learning with R



(A) One knot

Multivariate adaptive regression splines (MARS) provide a convenient approach to capture the nonlinear relationships in the data by assessing cutpoints (knots). The procedure assesses each data point for each predictor as a knot and creates a linear regression model with the candidate feature(s).

(R) Two knots

library(AmesHousing); ## The Ames Iowa Housing Data

fit a basic MARS model, get data ready...

```
ames <- AmesHousing::make ames();
head(ames):
## # A tibble: 6 x 81
##
    MS SubClass
                     MS Zoning
                                   Lot Frontage Lot Area Street Alley Lot Shape
    <fct>
                     <fct>
                                          <dbl>
                                                   <int> <fct> <fct>
                                                                        <fct>
##
## 1 One_Story_1946_~ Residential_~
                                            141
                                                   31770 Pave
                                                                No All~ Slightly ~
## 2 One Story 1946 ~ Residential ~
                                             80
                                                   11622 Pave
                                                                No All~ Regular
## 3 One_Story_1946_~ Residential_~
                                                   14267 Pave
                                                                No_All~ Slightly_~
                                             81
## 4 One Story 1946 ~ Residential ~
                                             93
                                                   11160 Pave
                                                                No All~ Regular
## 5 Two Story 1946 ~ Residential ~
                                             74
                                                  13830 Pave
                                                                No All~ Slightly ~
## 6 Two Story 1946 ~ Residential ~
                                             78
                                                    9978 Pave
                                                                No All~ Slightly ~
## # ... with 74 more variables: Land_Contour <fct>, Utilities <fct>,
      Lot Config <fct>, Land Slope <fct>, Neighborhood <fct>, Condition 1 <fct>,
## #
## #
      Condition_2 <fct>, Bldg_Type <fct>, House_Style <fct>, Overall_Qual <fct>,
## #
      Overall Cond <fct>, Year Built <int>, Year Remod Add <int>,
      Roof_Style <fct>, Roof_Matl <fct>, Exterior_1st <fct>, Exterior_2nd <fct>,
## #
## #
      Mas Vnr Type <fct>, Mas Vnr Area <dbl>, Exter Qual <fct>, Exter Cond <fct>,
## #
      Foundation <fct>, Bsmt Qual <fct>, Bsmt Cond <fct>, Bsmt Exposure <fct>,
      BsmtFin_Type_1 <fct>, BsmtFin_SF_1 <dbl>, BsmtFin_Type_2 <fct>,
## #
## #
      BsmtFin SF 2 <dbl>, Bsmt Unf SF <dbl>, Total Bsmt SF <dbl>, Heating <fct>,
      Heating QC <fct>, Central Air <fct>, Electrical <fct>, First Flr SF <int>,
## #
## #
      Second_Flr_SF <int>, Low_Qual_Fin_SF <int>, Gr_Liv_Area <int>,
## #
      Bsmt Full Bath <dbl>, Bsmt Half Bath <dbl>, Full Bath <int>,
      Half_Bath <int>, Bedroom_AbvGr <int>, Kitchen AbvGr <int>.
## #
## #
      Kitchen Qual <fct>. TotRms AbvGrd <int>. Functional <fct>.
```

fit a basic MARS model, fit a basic model

```
library(earth);
mars1 <- earth( Sale_Price ~ ., data = ames );
print(mars1);

## Selected 37 of 40 terms, and 26 of 308 predictors</pre>
```

```
## Selected 37 of 40 terms, and 26 of 308 predictors

## Termination condition: RSq changed by less than 0.001 at 40 terms

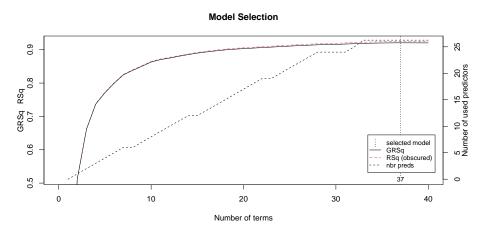
## Importance: Gr_Liv_Area, Year_Built, Total_Bsmt_SF, Overall_QualExcellent, ...

## Number of terms at each degree of interaction: 1 36 (additive model)

## GCV 506531262 RSS 1.411104e+12 GRSa 0.9206569 RSa 0.9245098
```

MARS model, model selection

```
plot(mars1, which = 1);
```



如何解释?

mars model with interactions

```
mars2 <- earth(Sale_Price ~ ., data = ames, degree = 2);
summary(mars2) %>% .$coefficients %>% head(10)
```

```
##
                                                Sale Price
## (Intercept)
                                              3.040042e+05
## h(Gr Liv Area-3228)
                                              1.975129e+02
## h(3228-Gr Liv Area)
                                             -4.415067e+01
## h(Year Built-2003)
                                              7.976946e+03
## h(2003-Year Built)
                                             -4.970063e+02
## h(Total Bsmt SF-2452)
                                              4.990177e+01
## h(2452-Total Bsmt SF)
                                             -5.482326e+01
## h(Year Built-2003)*h(2439-Gr Liv Area)
                                             -5.515644e+00
## h(2003-Year Built)*h(Total Bsmt SF-1117)
                                             -7.288488e-01
## h(2003-Year Built)*h(1117-Total Bsmt SF)
                                              3.682410e-01
```

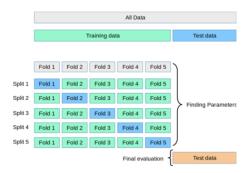
Parameter tuning: cross validation

K fold, N times

	FOLD 1	FOLD 2	FOLD 3	FOLD 4	FOLD 5	
ITERATION 1	TRAIN	TRAIN	TRAIN	TRAIN	TEST	
ITERATION 2	TRAIN	TRAIN	TRAIN	TEST	TRAIN	
ITERATION 3	TRAIN	TRAIN	TEST	TRAIN	TRAIN	
ITERATION 4	TRAIN	TEST	TRAIN	TRAIN	TRAIN	
ITERATION 5	TEST	TRAIN	TRAIN	TRAIN	TRAIN	
	DATASET PARTITIONED INTO FOLDS					

注 1. 每个 iteration 为随机 split; 2. 得到 K * N 个模型;

cross validation & additional test



Parameter tuning

```
## 1 1 2 2 2 2 ## 3 3 2 ## 4 1 12 ## 5 2 12 ## 6 3 12
```

degree nprune

Parameter tuning, cont.

```
set.seed(123) # for reproducibility
cv mars <- train(</pre>
  x = subset(ames, select = -Sale Price).
 v = ames$Sale Price,
 method = "earth".
 metric = "RMSE".
 trControl = trainControl(method = "cv", number = 10),
 tuneGrid = hyper grid
## Warning: Setting row names on a tibble is deprecated.
## Warning: Setting row names on a tibble is deprecated.
## Warning: Setting row names on a tibble is deprecated.
## Warning: Setting row names on a tibble is deprecated.
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## Warning: Setting row names on a tibble is deprecated.
## Warning: Setting row names on a tibble is deprecated.
## Warning: Setting row names on a tibble is deprecated.
```

Warning: Setting row names on a tibble is deprecated.

Parameter tuning, show results

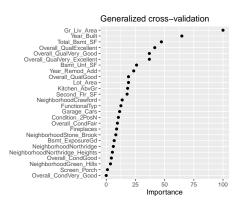
```
cv mars$bestTune:
     nprune degree
         45
cv mars$results %>%
 filter(nprune == cv mars$bestTune$nprune, degree == cv mars$bestTune$degree);
     degree nprune RMSE Rsquared MAE RMSESD RsquaredSD
                                                                         MAESD
                45 25312.47 0.8968114 16326.29 4233.975 0.04749767 1172.919
ggplot(cv_mars) ## plot
RMSE (Cross–Validation)
                                                                                      Product Degree
                         25
                                           50
                                           #Terms
```

compare with other methods e.g., 1m

```
cv lm <- train(
 Sale Price ~ .,
 data = ames.
 method = "lm".
 trControl = trainControl(method = "repeatedcv", number = 10, repeats = 3)
);
## Warning in predict.lm(modelFit, newdata): prediction from a rank-deficient fit
## may be misleading
## Warning in predict.lm(modelFit, newdata): prediction from a rank-deficient fit
## may be misleading
## Warning in predict.lm(modelFit, newdata): prediction from a rank-deficient fit
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## may be misleading
## Warning in predict.lm(modelFit, newdata): prediction from a rank-deficient fit
## may be misleading
## Warning in predict.lm(modelFit, newdata): prediction from a rank-deficient fit
## may be misleading
```

variable importance plot (VIP)

```
library(vip):
p1 <- vip(cv_mars, num_features = 40, geom = "point", value = "gcv") + ggtitle("Generalized cro
p2 <- vip(cv mars, num features = 40, geom = "point", value = "rss") + ggtitle("Residual Sums o
gridExtra::grid.arrange(p1, p2, ncol = 2)
```



Gr_Liv_Area -Year Built -Total Bsmt SF -Overall QualExcellent -Overall QualVery Good -Overall QualVery Excellent -Bsmt Unf SF -Year Remod Add -Overall QualGood -Lot Area -Kitchen AbvGr-Second Fir SF -NeighborhoodCrawford -

FunctionalTvp -

Garage Cars -

Fireplaces -

Condition 2PosN -

Overall CondFair -

Bsmt ExposureGd -

Overall CondGood -

Screen Porch -

NeighborhoodStone Brook -

NeighborhoodGreen Hills

Overall CondVery Good -

NeighborhoodNorthridge_Heights -

NeighborhoodNorthridge -

Residual Sums of Squares

25

Importance

27 October, 2021

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mars: final thoughts

advantages

- First, MARS naturally handles mixed types of predictors (quantitative and qualitative).
- MARS also requires minimal feature engineering (e.g., feature scaling) and performs automated feature selection.
- 4 Highly correlated predictors do not impede predictive accuracy as much as they do with OLS models.

shortcomings

- typically slower to train
- ② Also, although correlated predictors do not necessarily impede model performance, they can make model interpretation difficult.

section 4: 小结及作业!

本次小结

linear regression

- Im vs. glm
- 一元
- 多元
- 相关函数
- performance evaluation
- interactions
- visualizations

non-linear regression

- nls
- mars
- earth
- cross validation
- K fold, N times (下次详细讲)

下次预告

- Random Forest
- Support Vector Machine
- Deep learning

作业

- Exercises and homework 目录下 talk11-homework.Rmd 文件;
- 完成时间: 见钉群的要求

important

 all codes are available at Github: https://github.com/evolgeniusteam/R-for-bioinformatics