

IPTC

*IPTC - NAA
D i g i t a l
Newsphoto
Parameter
R e c o r d
Guideline 1*

Comité International des Télécommunications de Presse

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BACKGROUND

When a photographic image is scanned [either a positive (print) or a negative] the output is achieved by measuring the amount of light being reflected from or transmitted through the image. The scanner normally does this in a mode or domain called linear transmittance (for a negative) or linear reflectance (for a print). The characteristics of Linear Transmittance/Reflectance (Lin_{TR}) information are such that they are not suitable for accurate display or printing of the scanned image. If it is necessary to display or print the image conversions must be carried out into the domains that are normally used for display and printing devices. These are commonly known as TV Gamma ($TV \gamma$) and Linear Density respectively. The conversion from Lin_{TR} to $TV \gamma$ and Linear Density is carried out by applying different mathematical formulae to the data. When a common range of values is used for the Lin_{TR} data then these changes can be expressed by means of simple look-up tables.

INTRODUCTION

The Digital Newsphoto Parameter Record (DNPR) provides a standard for the transmission of digitised newsphoto images together with essential information related to the generation of the image data file. One of the parameters included (DataSet 3:120) is the quantisation method. Most scanners create image data using linear reflectance/transmittance as the quantisation method, although some convert internally to the linear density domain.

More scanners are becoming available that operate in the TV Gamma domain specifically intended to provide images for display on monitors rather than for printing purposes.

Image files received into picture desk systems are often converted into the linear density mode prior to display, manipulation and storage. This conversion process depends upon the maximum density range of the system and the resultant data file values remain characterised by this initial linear density range. It is also possible to convert within the same domain for devices with different maximum density ranges. The following diagram shows these different conversion processes.

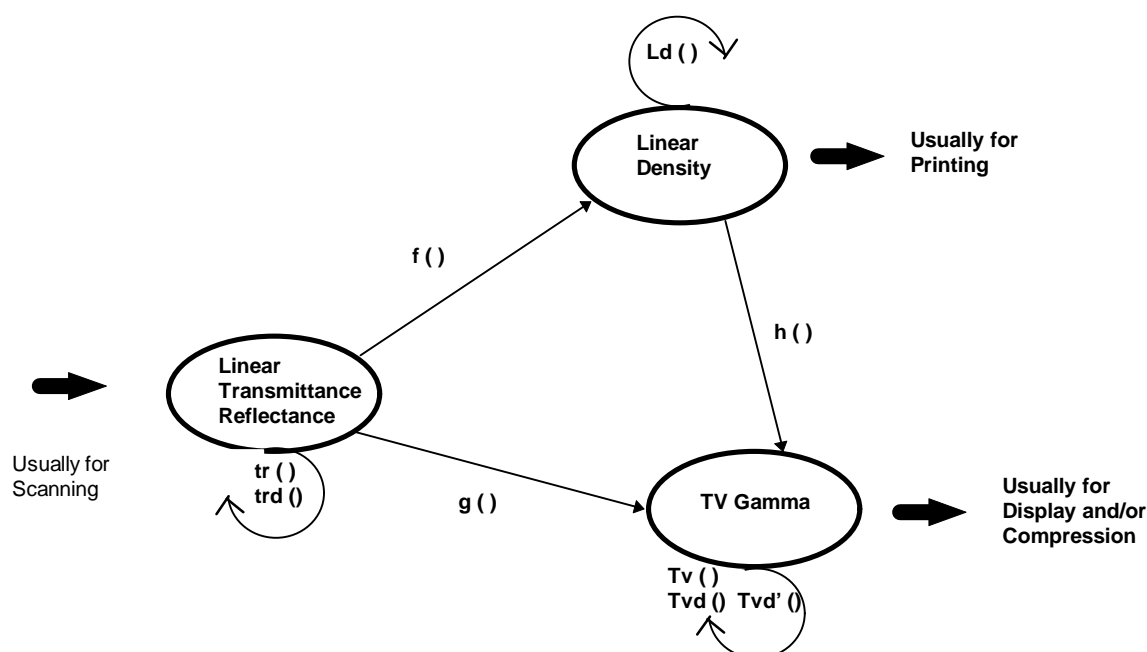


Figure 1: Domain Translation Possibilities

Although the DNPR can indicate that the image quantisation is changed to linear density it currently has no method of indicating the maximum density range applicable to the conversion process.

The maximum density range of any one system is not significant when images are stored and retrieved locally or are transferred to and from other systems with the same maximum density range. However if a printer is used with a different maximum density range or images are transferred between systems with different maximum density ranges (the general case between products from different vendors) then perceived image density suffers. Images can appear either excessively light or excessively dark and this is not acceptable to the end user. In order to solve this problem it is necessary to explore the nature of the conversions involved and then decide how to compensate for the different maximum density ranges of the various systems.

MAXIMUM DENSITY RANGE

Maximum density range is the difference between D_{\max} and D_{\min} . It is assumed that D_{\min} is (or can be set to zero) and the term D_{\max} is adopted to mean the maximum density range. It is the value of the maximum density at which the scanner is able to produce an output that is discernible above the sensor threshold. This information is normally published by the scanner manufacturer. Current scanners are able to detect maximum densities in the order of 2.5.

This parameter is significant since if the material to be scanned has a density range greater than the scanner the scanner limits the output at the D_{\max} point. Scanning is always done to achieve the best result and so full advantage is taken of scanner output range of values when the material has a maximum density less than the scanner D_{\max} . The scanner operator or the automatic driver software will adjust the operating conditions by exposure control or other mechanisms to ensure the output data covers the total scanner range irrespective of the actual material maximum density.

The value of D_{\max} will be used in the formulae derived for domain translation and should be available with the image data as part of the output from a scanning process. If the image data is subsequently re-processed in another system such that the value of D_{\max} is changed then this new value must be used to update the D_{\max} (DataSet 3:140). D_{\max} is relevant no matter which colour space is used. For some colour spaces the end points are relevant (DataSet 3:125) and in these cases if the NCPS values are not used the actual end point values can be mapped to the receiving system internal values that represent minimum and maximum density.

The formulae covering the conversion between systems of different D_{\max} allow the retention of the smaller density range i.e. when converting to a higher range system values beyond the D_{\max} of the lower do not appear as coded values. Similarly, from a higher range system the values above the D_{\max} of the lower are all set to the D_{\max} of the lower range system. This approach was adopted following practical tests and is considered to be satisfactory for news industry purposes.

IMAGE HANDLING - TRANSFER BETWEEN SYSTEMS

The formulae in this guideline are intended to be used on monochrome or primary colour image separations only. The following terms are used throughout: Lin_{tr} = the Linear Transmittance/Reflectance value, Lin_d = the linear density value, TV_{γ} = is the TV gamma value. N_{tr} , N_d and N_{γ} are the bit resolutions of the digitised signals in the Lin_{tr} , Lin_d and TV_{γ} domains respectively. It should be noted that the theory assumes that the whitest point corresponds to zero density. In the computer domain it is normal that a data value of zero produces the blackest output. It is necessary to convert density values to their $2^N - 1$

complement where N is the number of bits used for coding. The formulae reflect this conversion and the term Clin_d applies to the converted values. Clin_d = (2^N - 1) - Lin_d.

1. CONVERSION BETWEEN LINEAR REFLECTANCE/TRANSMITTANCE AND LINEAR DENSITY

As shown in Appendix A in a practical system with a real D_{max}:

$$\text{Clin}_d = (2^{N_d} - 1) + \frac{2^{N_d} - 1}{D_{\max}} \log_{10} \left(\frac{\text{Lin}_{tr}}{2^{N_{tr}} - 1} (1 - 10^{-D_{\max}}) + 10^{-D_{\max}} \right)$$

$$\begin{aligned} \text{With} \quad 0 &\leq \text{Lin}_{tr} \leq 2^{N_{tr}} - 1 \\ 0 &\leq \text{Clin}_d \leq 2^{N_d} - 1 \end{aligned}$$

[A table of values derived for an 8 bit system with a D_{max} of 1.6 is given at Appendix C]

Transfer function f () : conversion from linear reflectance / transmittance to density

From this formula it is possible to calculate Lin_{tr} from Clin_d:

$$\text{Lin}_{tr} = (2^{N_{tr}} - 1) \frac{10^{\frac{\text{Clin}_d - (2^{N_d} - 1)}{2^{N_d} - 1} D_{\max}} - 10^{-D_{\max}}}{1 - 10^{-D_{\max}}}$$

$$\begin{aligned} \text{With} \quad 0 &\leq \text{Lin}_{tr} \leq 2^{N_{tr}} - 1 \\ 0 &\leq \text{Clin}_d \leq 2^{N_d} - 1 \end{aligned}$$

Transfer function f ()⁻¹ : conversion from density to linear reflectance / transmittance

2. CONVERSION BETWEEN LINEAR REFLECTANCE/TRANSMITTANCE AND TV GAMMA

- Let Lin_{tr} be the digitized linear reflectance/transmittance signal coded with 2^{N_{tr}} levels between 0 and 2^{N_{tr}} - 1 within a maximum density range of D_{max}.
- Let TV_γ be the digitized TV gamma signal coded with 2^{N_γ} levels between 0 and 2^{N_γ} - 1

The relation between Lin_{tr} and TV_γ is given by :

$$\frac{TV_{\gamma}}{2^{N_{\gamma}} - 1} = \left(\frac{Lin_{tr}}{2^{N_{tr}} - 1} \right)^{1/\gamma}$$

$$0 \leq TV_{\gamma} \leq 2^{N_{\gamma}} - 1$$

$$0 \leq Lin_{tr} \leq 2^{N_{tr}} - 1$$

$$\gamma = 2.22 \text{ for NTSC}$$

Transfer function g () : conversion from linear reflectance/transmittance to TV Gamma

The inverse relation is given by :

$$\frac{Lin_{tr}}{2^{N_{tr}} - 1} = \left(\frac{TV_{\gamma}}{2^{N_{\gamma}} - 1} \right)^{\gamma}$$

$$0 \leq Lin_{tr} \leq 2^{N_{tr}} - 1$$

$$0 \leq TV_{\gamma} \leq 2^{N_{\gamma}} - 1$$

$$\gamma = 2.22 \text{ for NTSC}$$

Transfer function g ()⁻¹ : conversion from TV Gamma to linear reflectance/transmittance

3. CONVERSION BETWEEN DENSITY AND TV GAMMA

If we combine functions f ()⁻¹ and g () it comes to :

$$\frac{TV_{\gamma}}{2^{N_{\gamma}} - 1} = \left(\frac{10^{\frac{Clin_d - (2^{N_d} - 1)}{2^{N_d} - 1} D_{max}} - 10^{-D_{max}}}{1 - 10^{-D_{max}}} \right)^{1/\gamma}$$

With $0 \leq Clin_d \leq 2^{N_d} - 1$

$$0 \leq TV_{\gamma} \leq 2^{N_{\gamma}} - 1$$

$$\gamma = 2.22 \text{ for NTSC}$$

Transfer function h () : conversion from density to TV Gamma

If we combine functions f () and g ()⁻¹ then :

$$\text{Clin}_d = (2^{N_d} - 1) + \frac{2^{N_d} - 1}{D_{\max}} \log_{10} \left(\left(\frac{TV_\gamma}{2^{N_\gamma} - 1} \right)^\gamma (1 - 10^{-D_{\max}}) + 10^{-D_{\max}} \right)$$

$$0 \leq \text{Clin}_d \leq 2^{N_d} - 1$$

$$0 \leq TV_\gamma \leq 2^{N_\gamma} - 1$$

$$\gamma = 2.22 \text{ for NTSC}$$

Transfer function h ()⁻¹ : conversion from TV Gamma to density

4. CONVERSION FROM DENSITY TO DENSITY WITH DIFFERENT D_{max}

- let Clin_{dA} be a digitized density signal coded with a density range of D_{maxA} between 0 and 2^{N_{dA}} - 1 for system A.
- let Clin_{dB} be a digitized density signal coded with a density range of D_{maxB} between 0 and 2^{N_{dB}} - 1 for system B.

As can be seen in Appendix B :

$$(2^{N_{dB}} - 1) - \text{Clin}_{dB} = \left(\frac{2^{N_{dB}} - 1}{2^{N_{dA}} - 1} \right) \left(\frac{D_{\max A}}{D_{\max B}} \right) ((2^{N_{dA}} - 1) - \text{Clin}_{dA}) + (2^{N_{dB}} - 1) \left(\frac{D_{\max B} - D_{\max A}}{D_{\max B}} \right)$$

$$0 \leq \text{Clin}_{dA} \leq 2^{N_{dA}} - 1$$

$$0 \leq \text{Clin}_{dB} \leq 2^{N_{dB}} - 1$$

Transfer function Ld () : conversion from density to density with different D_{max}

5. CONVERSION FROM LINEAR REFLECTANCE/TRANSMITTANCE TO LINEAR REFLECTANCE/TRANSMITTANCE WITH DIFFERENT D_{MAX}

- let Lin_{trA} be a digitized reflectance/transmittance signal coded with a density range of D_{maxA} between 0 and $2^{N_{\text{dA}}} - 1$ for system A.
- let Lin_{trB} be a digitized reflectance/transmittance signal coded with a density range of D_{maxB} between 0 and $2^{N_{\text{dB}}} - 1$ for system B.

We have established in Appendix B that :

$$\text{Lin}_{\text{trB}} = \text{Lin}_{\text{trA}} \frac{(2^{N_{\text{dB}}} - 1)(1 - 10^{-D_{\text{maxA}}})}{(2^{N_{\text{dA}}} - 1)(1 - 10^{-D_{\text{maxB}}})} + (2^{N_{\text{dB}}} - 1) \left(\frac{10^{-D_{\text{maxA}}} - 10^{-D_{\text{maxB}}}}{1 - 10^{-D_{\text{maxB}}}} \right)$$

$$0 \leq \text{Lin}_{\text{trA}} \leq 2^{N_{\text{dA}}} - 1$$

$$0 \leq \text{Lin}_{\text{trB}} \leq 2^{N_{\text{dB}}} - 1$$

Transfer function $\text{trd}()$: conversion between two linear reflectance/transmittance signal with different D_{max}

6. CONVERSION FROM TV GAMMA DOMAIN TO TV GAMMA DOMAIN WITH DIFFERENT D_{MAX}

- let $\text{TV}_{\gamma A}$ be a digitized TV gamma signal coded with a density range of D_{maxA} between 0 and $2^{N_{\gamma A}} - 1$ with a gamma value of γ for system A.

let $\text{TV}_{\gamma B}$ be a digitized TV gamma signal coded with a density range of D_{maxB} between 0 and $2^{N_{\gamma B}} - 1$ with the same gamma value of γ for system B.

Combining functions $g()^{-1}$, $\text{trd}()$, $g()$:

$$\frac{\text{TV}_{\gamma B}}{2^{N_{\gamma B}} - 1} = \left(\left(\frac{\text{TV}_{\gamma A}}{2^{N_{\gamma A}} - 1} \right)^{\gamma} \frac{1 - 10^{-D_{\text{maxA}}}}{1 - 10^{-D_{\text{maxB}}}} + \frac{10^{-D_{\text{maxA}}} - 10^{-D_{\text{maxB}}}}{1 - 10^{-D_{\text{maxB}}}} \right)^{1/\gamma}$$

$$0 \leq \text{TV}_{\gamma B} \leq 2^{N_{\gamma B}} - 1$$

$$0 \leq \text{TV}_{\gamma A} \leq 2^{N_{\gamma A}} - 1$$

$$\gamma = 2.22 \text{ for NTSC}$$

Transfer function $\text{Tvd}()$: conversion between two TV gamma signals with different D_{max}

7. CONVERSION FROM TV GAMMA DOMAIN TO TV GAMMA DOMAIN WITH DIFFERENT GAMMA

- let TV_{γ_A} be a digitized TV gamma signal coded with a density range of D_{\max} between 0 and $2^{N_{\gamma A}} - 1$ with a gamma value of γ_A for system A.
- let TV_{γ_B} be a digitized TV gamma signal coded with a density range of D_{\max} between 0 and $2^{N_{\gamma B}} - 1$ with the same gamma value of γ_B for system B.

Combining functions $g()$ and $g()^{-1}$:

$$\frac{TV_{\gamma_B}}{2^{N_{\gamma B}} - 1} = \left(\frac{TV_{\gamma_A}}{2^{N_{\gamma A}} - 1} \right)^{\frac{\gamma_A}{\gamma_B}}$$

$$0 \leq TV_{\gamma_A} \leq 2^{N_{\gamma A}} - 1$$

$$0 \leq TV_{\gamma_B} \leq 2^{N_{\gamma B}} - 1$$

γ_A and γ_B as γ values

Transfer function $Tv()$: Conversion between two TV gamma signals with different gamma

8. CONVERSION FROM TV GAMMA DOMAIN TO TV GAMMA DOMAIN WITH DIFFERENT GAMMA AND DIFFERENT D_{\max}

- let TV_{γ_A} be a digitized TV gamma signal coded with a density range of $D_{\max A}$ between 0 and $2^{N_{\gamma A}} - 1$ with a gamma value of γ_A for system A.
- let TV_{γ_B} be a digitized TV gamma signal coded with a density range of $D_{\max B}$ between 0 and $2^{N_{\gamma B}} - 1$ with a gamma value of γ_B for system B.

Combining functions $g()^{-1}$, $\text{trd}()$, $g()$:

$$\frac{TV_{\gamma_B}}{2^{N_{\gamma B}} - 1} = \left(\left(\frac{TV_{\gamma_A}}{2^{N_{\gamma A}} - 1} \right)^{\gamma_A} \frac{1 - 10^{-D_{\max A}}}{1 - 10^{-D_{\max B}}} + \frac{10^{-D_{\max A}} - 10^{-D_{\max B}}}{1 - 10^{-D_{\max B}}} \right)^{1/\gamma_B}$$

$$0 \leq TV_{\gamma_A} \leq 2^{N_{\gamma A}} - 1$$

$$0 \leq TV_{\gamma_B} \leq 2^{N_{\gamma B}} - 1$$

γ_A and γ_B as gamma values

Transfer function $Tvd'()$: conversion between two TV gamma signals with different gamma and different D_{\max}

PRACTICAL RESULTS

IPTC and NAA have carried out test using these relationships for the transfer of images between different systems available in the market. The results confirmed that the theory is satisfactory for uncompressed image files. However, in order to be universally applicable it is necessary to append the D_{\max} value of the source system to an image file. It is proposed to achieve this by extending the use of the DNPR DataSet 3:140 so that it is valid for all quantisation methods. The contents of DataSet 3:140 will be the value of $D_{\max} \times 100$.

To allow for systems not yet able to implement this feature users are advised that an assumed default value of 160 applies. Information Providers will need to ensure that their customers are notified by other means if the value of D_{\max} applicable to their images is other than the default of 1.6. Once the change to DataSet 3:140 is implemented then separate notification will be unnecessary.

DISPLAY ADJUSTMENT

The correction of an image quantisation values to allow for the different maximum density range of the originating and receiving systems will not always result in a perfect screen display. It may be necessary to apply a gamma correction to allow for the response of the screen phosphors. Appendix D provides a table for correction to the density values when a gamma of 2.2 occurs. (This is the normal CCIR TV monitor value).

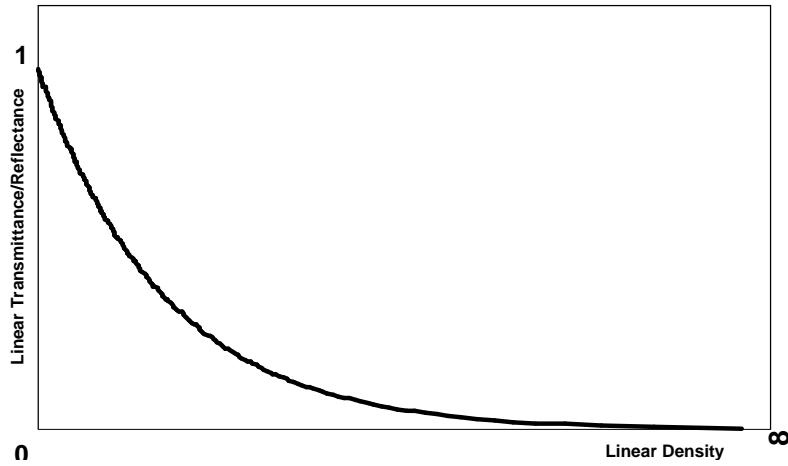
APPENDIX A

Derivation of Linear Density Linear Reflectance/Transmittance Relationship for a System with a Finite Maximum Density Range (D_{\max})

The general relationship for an infinite density range is given by:

$$Lin_{tr} = (Lin_{tr \max}) 10^{-d}$$

This can be plotted as shown below. The density values are unbounded at the high end.



Where a maximum density value is given (the practical case) the equation must be modified as follows:

$$Lin_{tr} = A(Lin_{tr \max}) 10^{-d} + B$$

Where the following boundary conditions apply

When $Lin_{tr} = 0$ then $d = D_{\max}$
and $Lin_{tr} = Lin_{tr \max}$ for $d = 0$

Hence

$$\begin{aligned} 0 &= A(Lin_{tr \max}) 10^{-D_{\max}} + B \\ -A(Lin_{tr \max}) 10^{-D_{\max}} &= B \end{aligned}$$

By substitution

$$\begin{aligned} Lin_{tr} &= A(Lin_{tr \max}) 10^{-d} - A(Lin_{tr \max}) 10^{-D_{\max}} \\ A &= \frac{1}{1 - 10^{-D_{\max}}} \end{aligned}$$

Hence

$$B = \frac{-(Lin_{tr \max}) 10^{-D_{\max}}}{1 - 10^{-D_{\max}}}$$

Giving

$$10^{-d} = \frac{Lin_{tr}}{Lin_{trmax}}(1 - 10^{-D_{max}}) + 10^{-D_{max}}$$

or

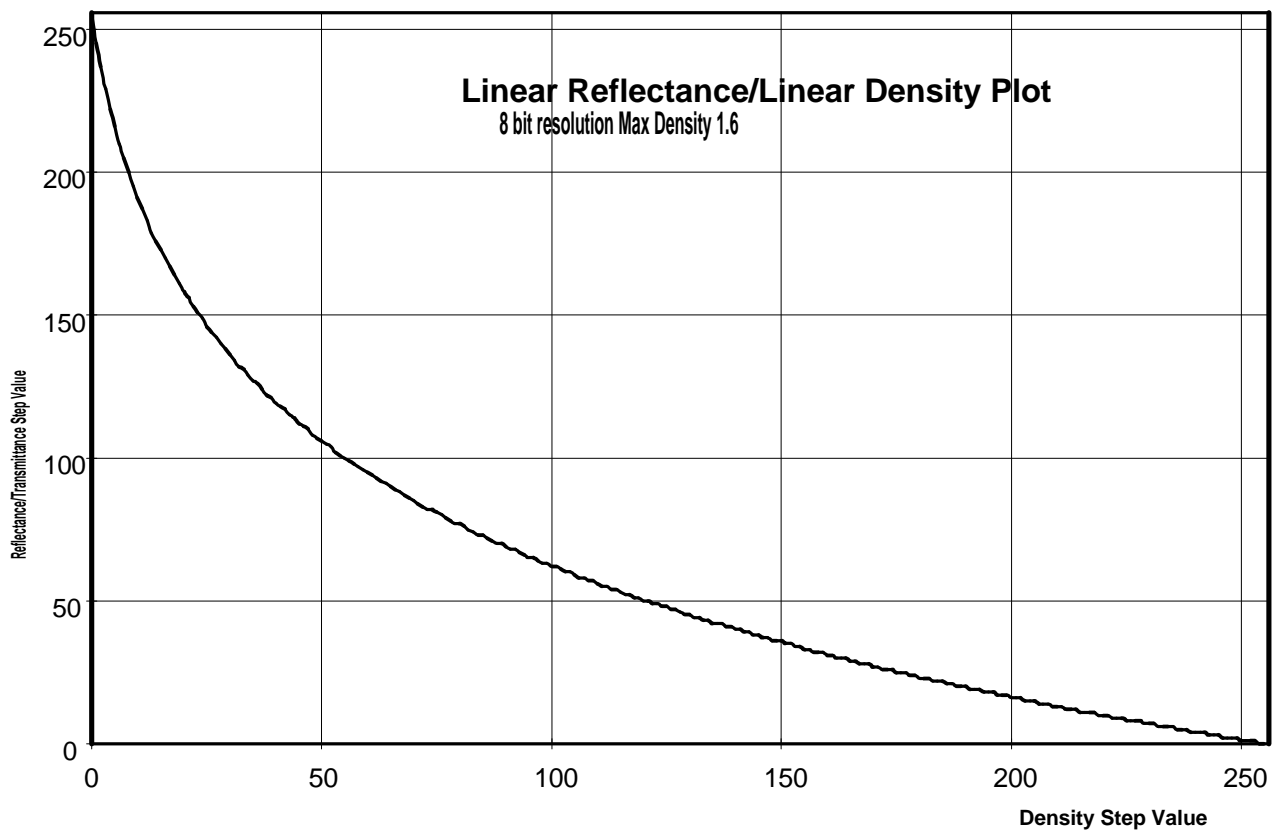
$$d = -\log_{10}\left(\frac{Lin_{tr}}{Lin_{trmax}}(1 - 10^{-D_{max}}) + 10^{-D_{max}}\right)$$

For 8 bit systems ($n = 8$) Lin_{trmax} will be normalised to $2^n - 1$ ($= 255$) and the normalised form for density values is:

$$d = -\left(\frac{2^n - 1}{D_{max}}\right)\log_{10}\left(\frac{Lin_{tr}}{2^n - 1}(1 - 10^{-D_{max}}) + 10^{-D_{max}}\right)$$

where $0 \leq d \leq 255$ and is a discrete presentation of the DENSITY which varies between 0 and 1.6.

A plot of the resultant curve is shown below with D_{max} constrained to a value of 1.6. The values used are shown in the table at Appendix C.



A further relationship may be derived between the linear reflectance values represented within 2 systems using a different maximum density range. In general the relationship between the reflectance/transmittance output of a system and the density value observed is given by:

$$v = v_0 * 10^{-d}$$

or

$$v = \alpha 10^{-d} - \beta$$

with conditions such that

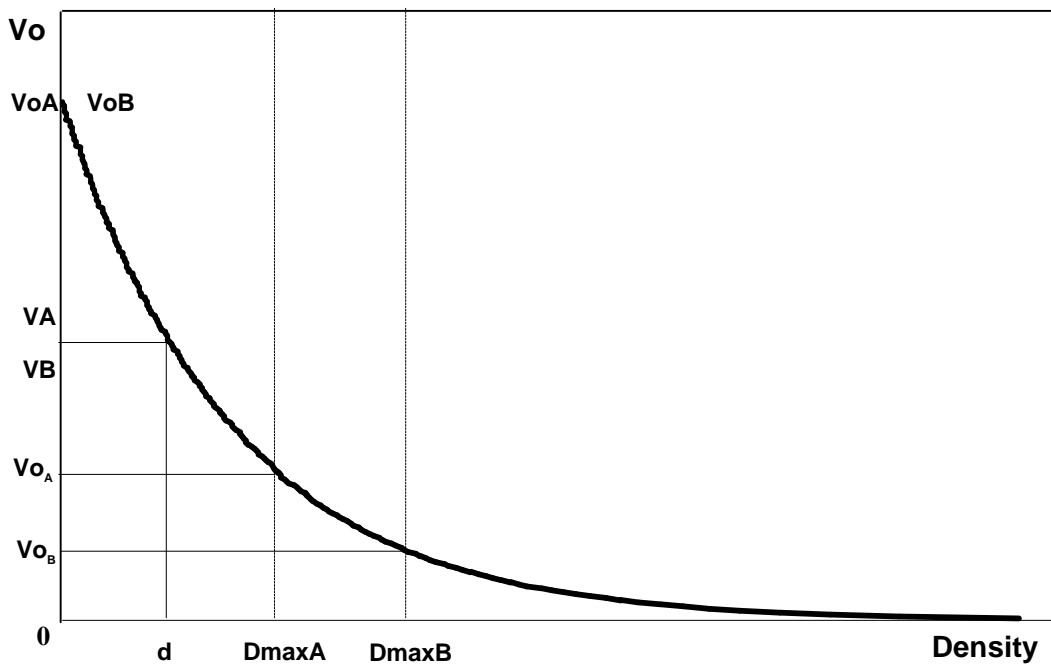
$$\begin{array}{ll} \text{when } d = 0 & v = v_0 \\ d = D_{\max} & v = 0 \end{array}$$

leads to

$$\alpha = v_0 \frac{1}{1 - 10^{-D_{\max}}}$$

and

$$\beta = v_0 \frac{10^{-D_{\max}}}{1 - 10^{-D_{\max}}}$$



A composite plot of reflectance against density for 2 systems with different maximum density ranges is shown above. Equations for both system A and system B can be solved for the values of v_A and v_B at a density value of d using the above result. This leads an expression for v_B in terms of v_A :

$$v_B = \frac{1 - 10^{-D_{\max A}}}{1 - 10^{-D_{\max B}}} v_A + v_0 \left(\frac{10^{-D_{\max A}} - 10^{-D_{\max B}}}{1 - 10^{-D_{\max B}}} \right)$$

or more generally

$$v_B = av_A + b$$

This allows the linear transformation of information from one system to another providing the D_{\max} for each system is known in advance.

Determination of D_{\max} when manufacturer's information is not available.

By re-arranging the general equation given at the start of this Guideline and assuming that the value of reflectance for a known density can be measured or obtained by other means then:

$$D_{\max} = -\log_{10} \left(\frac{Lin_{tr} - (2^n - 1)10^{-d}}{Lin_{tr} - (2^n - 1)} \right)$$

providing that for 8 bit systems

$255 \geq Lin_{tr} \geq 0$ and $0 \leq d \leq D_{\max}$ (maximum reflectance/transmittance \equiv minimum density ie the WHITE value)

This allows a value of D_{\max} to be obtained for use in any domain translation required by the user.

APPENDIX B

Derivation of function Ld ()

The general relationship between linear reflectance/transmittance and linear density is given by $v=v_o 10^{-d}$ (see Appendix A). This may be re-arranged as:-

$$d = -\log_{10}\left(\frac{v}{v_o}\right)$$

$$d = -(\log_{10} v - \log_{10} v_o)$$

$$d = \log_{10} v_o - \log_{10} v$$

or

$$d = D_{\max} - \left(\frac{Lin_d}{2^{Nd} - 1}\right) D_{\max}$$

$$\text{for } 0 \leq Lin_d \leq 2^{Nd} - 1$$

$$D_{\max} \geq d \geq 0$$

This can be re-written as:

$$d = D_{\max A} - \left(\frac{Lin_{dA}}{2^{NdA} - 1}\right) D_{\max A} \quad \text{where } d \text{ is the value for system A}$$

and

$$d = D_{\max B} - \left(\frac{Lin_{dB}}{2^{NdB} - 1}\right) D_{\max B} \quad \text{where } d \text{ is the value for system B}$$

when the value of d is the same for both systems then

$$D_{\max B} (2^{NdB} - 1) - Lin_{dB} D_{\max B} = D_{\max A} (2^{NdB} - 1) - D_{\max A} \left(\frac{2^{NdB} - 1}{2^{NdA} - 1}\right) Lin_{dA}$$

$$Lin_{dB} = \left(\frac{D_{\max B} (2^{NdB} - 1) + D_{\max A} \left(\frac{2^{NdB} - 1}{2^{NdA} - 1}\right) Lin_{dA} - D_{\max A} (2^{NdB} - 1)}{D_{\max B}} \right)$$

or

$$Lin_{dB} = \left(\frac{2^{NdB} - 1}{2^{NdA} - 1} \right) \frac{D_{\max A}}{D_{\max B}} Lin_{dA} + (2^{NdB} - 1) \frac{D_{\max B} - D_{\max A}}{D_{\max B}}$$

and by substitution of $Clin_d = (2^{Nd} - 1) - Lin_d$

$$(2^{NdB} - 1) - Clin_{dB} = \left(\frac{2^{NdB} - 1}{2^{NdA} - 1} \right) \left(\frac{D_{\max A}}{D_{\max B}} \right) (2^{NdA} - 1) - Clin_{dA} + (2^{NdB} - 1) \left(\frac{D_{\max B} - D_{\max A}}{D_{\max B}} \right)$$

Derivation of function trd ()

From function $f()^{-1}$

$$Lin_{trA} = \left(\frac{2^{NtrA} - 1}{1 - 10^{-D_{\max A}}} \right) 10^{-dA} - \left(\frac{2^{NtrA} - 1}{1 - 10^{-D_{\max A}}} \right) 10^{-D_{\max A}}$$

$$10^{-dA} = \frac{Lin_{trA} (1 - 10^{-D_{\max A}}) + (2^{NtrA} - 1) 10^{-D_{\max A}}}{2^{NtrA} - 1}$$

and

$$10^{-dB} = \frac{Lin_{trB} (1 - 10^{-D_{\max B}}) + (2^{NtrB} - 1) 10^{-D_{\max B}}}{2^{NtrB} - 1}$$

When $dA = dB$ then

$$\begin{aligned} & Lin_{trA} (1 - 10^{-D_{\max A}}) (2^{NtrB} - 1) + (2^{NtrA} - 1) (2^{NtrB} - 1) 10^{-D_{\max A}} \\ &= Lin_{trB} (1 - 10^{-D_{\max B}}) (2^{NtrA} - 1) + (2^{NtrB} - 1) (2^{NtrA} - 1) 10^{-D_{\max B}} \end{aligned}$$

Leading to

$$Lin_{trB} = Lin_{trA} \left(\frac{1 - 10^{-D_{\max A}}}{1 - 10^{-D_{\max B}}} \right) \left(\frac{2^{NtrB} - 1}{2^{NtrA} - 1} \right) + (2^{NtrB} - 1) \left(\frac{10^{-D_{\max A}} - 10^{-D_{\max B}}}{1 - 10^{-D_{\max B}}} \right)$$

Appendix C . Coded Values of Linear Transmittance Reflectance, Corresponding Linear Density for 8 Bit System and Absolute Density. $D_{\max} = 1.6$.

| Encoded Lin_{tr} | Encoded Density | Absolute Density | Encoded Lin_{tr} | Encoded Density | Absolute Density | Encoded Lin_{tr} | Encoded Density | Encoded Density |
|-----------------------|--------------------|---------------------|-----------------------|--------------------|---------------------|-----------------------|--------------------|--------------------|
| 255 | 255 | 0.00 | 209 | 242 | 0.08 | 163 | 225 | 0.19 |
| 254 | 255 | 0.00 | 208 | 241 | 0.09 | 162 | 225 | 0.19 |
| 253 | 254 | 0.01 | 207 | 241 | 0.09 | 161 | 224 | 0.19 |
| 252 | 254 | 0.01 | 206 | 241 | 0.09 | 160 | 224 | 0.19 |
| 251 | 254 | 0.01 | 205 | 240 | 0.09 | 159 | 223 | 0.20 |
| 250 | 254 | 0.01 | 204 | 240 | 0.09 | 158 | 223 | 0.20 |
| 249 | 253 | 0.01 | 203 | 240 | 0.09 | 157 | 223 | 0.20 |
| 248 | 253 | 0.01 | 202 | 239 | 0.10 | 156 | 222 | 0.21 |
| 247 | 253 | 0.01 | 201 | 239 | 0.10 | 155 | 222 | 0.21 |
| 246 | 253 | 0.01 | 200 | 239 | 0.10 | 154 | 221 | 0.21 |
| 245 | 252 | 0.02 | 199 | 238 | 0.11 | 153 | 221 | 0.21 |
| 244 | 252 | 0.02 | 198 | 238 | 0.11 | 152 | 220 | 0.22 |
| 243 | 252 | 0.02 | 197 | 238 | 0.11 | 151 | 220 | 0.22 |
| 242 | 251 | 0.03 | 196 | 237 | 0.11 | 150 | 219 | 0.23 |
| 241 | 251 | 0.03 | 195 | 237 | 0.11 | 149 | 219 | 0.23 |
| 240 | 251 | 0.03 | 194 | 237 | 0.11 | 148 | 219 | 0.23 |
| 239 | 251 | 0.03 | 193 | 236 | 0.12 | 147 | 218 | 0.23 |
| 238 | 250 | 0.03 | 192 | 236 | 0.12 | 146 | 218 | 0.23 |
| 237 | 250 | 0.03 | 191 | 236 | 0.12 | 145 | 217 | 0.24 |
| 236 | 250 | 0.03 | 190 | 235 | 0.13 | 144 | 217 | 0.24 |
| 235 | 249 | 0.04 | 189 | 235 | 0.13 | 143 | 216 | 0.24 |
| 234 | 249 | 0.04 | 188 | 235 | 0.13 | 142 | 216 | 0.24 |
| 233 | 249 | 0.04 | 187 | 234 | 0.13 | 141 | 215 | 0.25 |
| 232 | 249 | 0.04 | 186 | 234 | 0.13 | 140 | 215 | 0.25 |
| 231 | 248 | 0.04 | 185 | 233 | 0.14 | 139 | 214 | 0.26 |
| 230 | 248 | 0.04 | 184 | 233 | 0.14 | 138 | 214 | 0.26 |
| 229 | 248 | 0.04 | 183 | 233 | 0.14 | 137 | 213 | 0.26 |
| 228 | 247 | 0.05 | 182 | 232 | 0.14 | 136 | 213 | 0.26 |
| 227 | 247 | 0.05 | 181 | 232 | 0.14 | 135 | 213 | 0.26 |
| 226 | 247 | 0.05 | 180 | 232 | 0.14 | 134 | 212 | 0.27 |
| 225 | 247 | 0.05 | 179 | 231 | 0.15 | 133 | 212 | 0.27 |
| 224 | 246 | 0.06 | 178 | 231 | 0.15 | 132 | 211 | 0.28 |
| 223 | 246 | 0.06 | 177 | 230 | 0.16 | 131 | 211 | 0.28 |
| 222 | 246 | 0.06 | 176 | 230 | 0.16 | 130 | 210 | 0.28 |
| 221 | 245 | 0.06 | 175 | 230 | 0.16 | 129 | 210 | 0.28 |
| 220 | 245 | 0.06 | 174 | 229 | 0.16 | 128 | 209 | 0.29 |
| 219 | 245 | 0.06 | 173 | 229 | 0.16 | 127 | 208 | 0.29 |
| 218 | 244 | 0.07 | 172 | 229 | 0.16 | 126 | 208 | 0.29 |
| 217 | 244 | 0.07 | 171 | 228 | 0.17 | 125 | 207 | 0.30 |
| 216 | 244 | 0.07 | 170 | 228 | 0.17 | 124 | 207 | 0.30 |
| 215 | 244 | 0.07 | 169 | 227 | 0.18 | 123 | 206 | 0.31 |
| 214 | 243 | 0.08 | 168 | 227 | 0.18 | 122 | 206 | 0.31 |
| 213 | 243 | 0.08 | 167 | 227 | 0.18 | 121 | 205 | 0.31 |
| 212 | 243 | 0.08 | 166 | 226 | 0.18 | 120 | 205 | 0.31 |
| 211 | 242 | 0.08 | 165 | 226 | 0.18 | 119 | 204 | 0.32 |
| 210 | 242 | 0.08 | 164 | 225 | 0.19 | 118 | 204 | 0.32 |

Appendix C . Coded Values of Linear Transmittance Reflectance, Corresponding Linear Density for 8 Bit System and Absolute Density. $D_{\max} = 1.6$.

| Encoded Lin_{tr} | Encoded Density | Absolute Density | Encoded Lin_{tr} | Encoded Density | Absolute Density | Encoded Lin_{tr} | Encoded Density | Absolute Density |
|-----------------------|--------------------|---------------------|-----------------------|--------------------|---------------------|-----------------------|--------------------|---------------------|
| 117 | 203 | 0.33 | 71 | 171 | 0.53 | 25 | 109 | 0.92 |
| 116 | 203 | 0.33 | 70 | 170 | 0.53 | 24 | 106 | 0.93 |
| 115 | 202 | 0.33 | 69 | 169 | 0.54 | 23 | 104 | 0.95 |
| 114 | 201 | 0.34 | 68 | 168 | 0.55 | 22 | 102 | 0.96 |
| 113 | 201 | 0.34 | 67 | 167 | 0.55 | 21 | 99 | 0.98 |
| 112 | 200 | 0.35 | 66 | 166 | 0.56 | 20 | 97 | 0.99 |
| 111 | 200 | 0.35 | 65 | 165 | 0.56 | 19 | 94 | 1.01 |
| 110 | 199 | 0.35 | 64 | 164 | 0.57 | 18 | 91 | 1.03 |
| 109 | 198 | 0.36 | 63 | 163 | 0.58 | 17 | 88 | 1.05 |
| 108 | 198 | 0.36 | 62 | 162 | 0.58 | 16 | 85 | 1.07 |
| 107 | 197 | 0.36 | 61 | 161 | 0.59 | 15 | 82 | 1.09 |
| 106 | 197 | 0.36 | 60 | 160 | 0.60 | 14 | 79 | 1.10 |
| 105 | 196 | 0.37 | 59 | 159 | 0.60 | 13 | 76 | 1.12 |
| 104 | 195 | 0.38 | 58 | 158 | 0.61 | 12 | 72 | 1.15 |
| 103 | 195 | 0.38 | 57 | 157 | 0.61 | 11 | 68 | 1.17 |
| 102 | 194 | 0.38 | 56 | 156 | 0.62 | 10 | 64 | 1.20 |
| 101 | 193 | 0.39 | 55 | 155 | 0.63 | 9 | 60 | 1.22 |
| 100 | 193 | 0.39 | 54 | 154 | 0.63 | 8 | 55 | 1.25 |
| 99 | 192 | 0.40 | 53 | 153 | 0.64 | 7 | 50 | 1.29 |
| 98 | 192 | 0.40 | 52 | 151 | 0.65 | 6 | 45 | 1.32 |
| 97 | 191 | 0.40 | 51 | 150 | 0.66 | 5 | 39 | 1.36 |
| 96 | 190 | 0.41 | 50 | 149 | 0.67 | 4 | 33 | 1.39 |
| 95 | 190 | 0.41 | 49 | 148 | 0.67 | 3 | 26 | 1.44 |
| 94 | 189 | 0.41 | 48 | 147 | 0.68 | 2 | 18 | 1.49 |
| 93 | 188 | 0.42 | 47 | 145 | 0.69 | 1 | 10 | 1.54 |
| 92 | 187 | 0.43 | 46 | 144 | 0.70 | 0 | 0 | 1.60 |
| 91 | 187 | 0.43 | 45 | 143 | 0.70 | | | |
| 90 | 186 | 0.43 | 44 | 141 | 0.72 | | | |
| 89 | 185 | 0.44 | 43 | 140 | 0.72 | | | |
| 88 | 185 | 0.44 | 42 | 138 | 0.73 | | | |
| 87 | 184 | 0.45 | 41 | 137 | 0.74 | | | |
| 86 | 183 | 0.45 | 40 | 136 | 0.75 | | | |
| 85 | 182 | 0.46 | 39 | 134 | 0.76 | | | |
| 84 | 182 | 0.46 | 38 | 133 | 0.77 | | | |
| 83 | 181 | 0.46 | 37 | 131 | 0.78 | | | |
| 82 | 180 | 0.47 | 36 | 129 | 0.79 | | | |
| 81 | 179 | 0.48 | 35 | 128 | 0.80 | | | |
| 80 | 178 | 0.48 | 34 | 126 | 0.81 | | | |
| 79 | 178 | 0.48 | 33 | 124 | 0.82 | | | |
| 78 | 177 | 0.49 | 32 | 123 | 0.83 | | | |
| 77 | 176 | 0.50 | 31 | 121 | 0.84 | | | |
| 76 | 175 | 0.50 | 30 | 119 | 0.85 | | | |
| 75 | 174 | 0.51 | 29 | 117 | 0.87 | | | |
| 74 | 173 | 0.51 | 28 | 115 | 0.88 | | | |
| 73 | 173 | 0.51 | 27 | 113 | 0.89 | | | |
| 72 | 172 | 0.52 | 26 | 111 | 0.90 | | | |

Appendix D. Normalised Linear Transmittance Reflectance and Gamma Corrected Values (γ CV) for 8 Bit System. $\gamma = 2.22$

| LinTR | γ CV | LinTR | γ CV | LinTR | γ CV |
|-------|-------------|-------|-------------|-------|-------------|
| 0 | 0 | 64 | 137 | 128 | 187 |
| 1 | 21 | 65 | 138 | 129 | 188 |
| 2 | 29 | 66 | 139 | 130 | 188 |
| 3 | 35 | 67 | 140 | 131 | 189 |
| 4 | 39 | 68 | 141 | 132 | 190 |
| 5 | 43 | 69 | 142 | 133 | 190 |
| 6 | 47 | 70 | 143 | 134 | 191 |
| 7 | 51 | 71 | 143 | 135 | 192 |
| 8 | 54 | 72 | 144 | 136 | 192 |
| 9 | 57 | 73 | 145 | 137 | 193 |
| 10 | 59 | 74 | 146 | 138 | 193 |
| 11 | 62 | 75 | 147 | 139 | 194 |
| 12 | 64 | 76 | 148 | 140 | 195 |
| 13 | 67 | 77 | 149 | 141 | 195 |
| 14 | 69 | 78 | 150 | 142 | 196 |
| 15 | 71 | 79 | 150 | 143 | 197 |
| 16 | 73 | 80 | 151 | 144 | 197 |
| 17 | 75 | 81 | 152 | 145 | 198 |
| 18 | 77 | 82 | 153 | 146 | 198 |
| 19 | 79 | 83 | 154 | 147 | 199 |
| 20 | 81 | 84 | 155 | 148 | 200 |
| 21 | 83 | 85 | 156 | 149 | 200 |
| 22 | 85 | 86 | 156 | 150 | 201 |
| 23 | 86 | 87 | 157 | 151 | 201 |
| 24 | 88 | 88 | 158 | 152 | 202 |
| 25 | 90 | 89 | 159 | 153 | 203 |
| 26 | 91 | 90 | 160 | 154 | 203 |
| 27 | 93 | 91 | 160 | 155 | 204 |
| 28 | 94 | 92 | 161 | 156 | 204 |
| 29 | 96 | 93 | 162 | 157 | 205 |
| 30 | 97 | 94 | 163 | 158 | 206 |
| 31 | 99 | 95 | 164 | 159 | 206 |
| 32 | 100 | 96 | 164 | 160 | 207 |
| 33 | 102 | 97 | 165 | 161 | 207 |
| 34 | 103 | 98 | 166 | 162 | 208 |
| 35 | 104 | 99 | 167 | 163 | 208 |
| 36 | 106 | 100 | 167 | 164 | 209 |
| 37 | 107 | 101 | 168 | 165 | 210 |
| 38 | 108 | 102 | 169 | 166 | 210 |
| 39 | 110 | 103 | 170 | 167 | 211 |
| 40 | 111 | 104 | 170 | 168 | 211 |
| 41 | 112 | 105 | 171 | 169 | 212 |
| 42 | 113 | 106 | 172 | 170 | 212 |
| 43 | 114 | 107 | 173 | 171 | 213 |
| 44 | 116 | 108 | 173 | 172 | 214 |
| 45 | 117 | 109 | 174 | 173 | 214 |
| 46 | 118 | 110 | 175 | 174 | 215 |
| 47 | 119 | 111 | 175 | 175 | 215 |
| 48 | 120 | 112 | 176 | 176 | 216 |
| 49 | 121 | 113 | 177 | 177 | 216 |
| 50 | 122 | 114 | 178 | 178 | 217 |
| 51 | 124 | 115 | 178 | 179 | 217 |
| 52 | 125 | 116 | 179 | 180 | 218 |
| 53 | 126 | 117 | 180 | 181 | 219 |
| 54 | 127 | 118 | 180 | 182 | 219 |
| 55 | 128 | 119 | 181 | 183 | 220 |
| 56 | 129 | 120 | 182 | 184 | 220 |
| 57 | 130 | 121 | 182 | 185 | 221 |
| 58 | 131 | 122 | 183 | 186 | 221 |
| 59 | 132 | 123 | 184 | 187 | 222 |
| 60 | 133 | 124 | 184 | 188 | 222 |
| 61 | 134 | 125 | 185 | 189 | 223 |
| 62 | 135 | 126 | 186 | 190 | 223 |
| 63 | 136 | 127 | 186 | 191 | 224 |

Appendix D. Normalised Linear Transmittance Reflectance and Gamma Corrected Values (γ CV) for 8 Bit System. $\gamma = 2.22$

| LinTR | γ CV |
|-------|-------------|
| 192 | 224 |
| 193 | 225 |
| 194 | 225 |
| 195 | 226 |
| 196 | 227 |
| 197 | 227 |
| 198 | 228 |
| 199 | 228 |
| 200 | 229 |
| 201 | 229 |
| 202 | 230 |
| 203 | 230 |
| 204 | 231 |
| 205 | 231 |
| 206 | 232 |
| 207 | 232 |
| 208 | 233 |
| 209 | 233 |
| 210 | 234 |
| 211 | 234 |
| 212 | 235 |
| 213 | 235 |
| 214 | 236 |
| 215 | 236 |
| 216 | 237 |
| 217 | 237 |
| 218 | 238 |
| 219 | 238 |
| 220 | 239 |
| 221 | 239 |
| 222 | 240 |
| 223 | 240 |
| 224 | 241 |
| 225 | 241 |
| 226 | 242 |
| 227 | 242 |
| 228 | 242 |
| 229 | 243 |
| 230 | 243 |
| 231 | 244 |
| 232 | 244 |
| 233 | 245 |
| 234 | 245 |
| 235 | 246 |
| 236 | 246 |
| 237 | 247 |
| 238 | 247 |
| 239 | 248 |
| 240 | 248 |
| 241 | 249 |
| 242 | 249 |
| 243 | 250 |
| 244 | 250 |
| 245 | 250 |
| 246 | 251 |
| 247 | 251 |
| 248 | 252 |
| 249 | 252 |
| 250 | 253 |
| 251 | 253 |
| 252 | 254 |
| 253 | 254 |
| 254 | 255 |
| 255 | 255 |