

7. Find parametric equations for the line through the point $(0, 1, 2)$ that is parallel to the plane $x + y + z = 2$ and perpendicular to the line $x = 1 + t, y = 1 - t, z = 2t$.

$$\begin{aligned} &\langle 1, 1, 1 \rangle \times \langle 1, -1, 2 \rangle \\ &= \langle 2+1, 2-1, -1-1 \rangle \\ &= \langle 3, 1, -2 \rangle \end{aligned}$$

$$\frac{x-0}{3} = \frac{y-1}{1} = \frac{z-2}{-2}$$

8. Which of the following four lines parallel? Are any of them identical?

$$L_1: x = 1 + 6t, y = 1 - 3t, z = 12t + 5. \quad \begin{matrix} 2, -1, 4 \\ 6, -3, 12 \end{matrix}$$

$$L_2: x = 1 + 2t, y = t, z = 1 + 4t \quad 2, 1, 4$$

$$L_3: 2x - 2 = 4 - 4y = z + 1 \quad 2, -4, 1$$

$$L_4: \mathbf{r} = \langle 3, 1, 5 \rangle + t \langle 4, 2, 8 \rangle \quad \begin{matrix} 4, 2, 8 \\ 2, 1, 4 \end{matrix}$$

$$\boxed{L_2, L_4}$$

9. Determine whether the planes are parallel, perpendicular, or neither, find the angle between them.

(a) $x + 4y - 3z = 1, -3x + 6y + 7z = 0$

$$\langle 1, 4, -3 \rangle \langle -3, 6, 7 \rangle \quad \text{perpendicular}$$

$$-3 + 24 - 21$$

(b) $9x - 3y + 6z = 2, 2y = 6x + 4z$

$$\langle 3, -1, 2 \rangle \langle 3, -1, 2 \rangle \quad \text{parallel}$$

(c) $x + 2y - z = 2, 2x - 2y + z = 1$

$$\langle 1, 2, -1 \rangle \langle 2, -2, 1 \rangle \quad \text{neither}$$

$$2 - 4 - 1$$

10. (a) Find the distance from the point $(-2, 2, 1)$ to the plane $3x - 5y + z = 5$.

$$\frac{|-6 - 10 + 1 - 5|}{\sqrt{9 + 25 + 1}} = \frac{20}{\sqrt{35}}$$

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(b) Find the distance between the parallel planes $2x - 3y + z = 4$ and $4x - 6y + 2z = 3$.

$$(2, 0, 0) \quad \text{distance}$$

$$\frac{|8 - 3|}{\sqrt{16 + 36 + 4}} = \frac{5}{\sqrt{56}}$$

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