

# Data-Dependence

Yulei Sui

University of Technology Sydney, Australia

Self-build  
Graph



Graph Traversal  
Algorithm

Assignment-1

C program



Compiler  
IR



Code Graphs  
ICFG,  
Constraint Graph



Control dependence  
ICFG



Assignment-3  
Data dependence  
Constraint Graph  
Today's class

Assignment-2

# Data-Dependence

Definition-use relations between variables. Two types of variables on LLVM IR:

- **Top-level variables**, whose addresses are not taken (ValPN in SVF)
  - Including stack virtual **registers** (symbols starting with “%”) and **global** variables (symbols starting with “@”) are explicit, i.e., directly accessed.

# Data-Dependence

Definition-use relations between variables. Two types of variables on LLVM IR:

- **Top-level variables**, whose addresses are not taken (ValPN in SVF)
  - Including stack virtual **registers** (symbols starting with “%”) and **global** variables (symbols starting with “@”) are explicit, i.e., directly accessed.
  - **Def-use for top-level variables are directly available on LLVM’s SSA form.**
  - For example, def-use for **%a1** from Instruction-1 to Instruction-2.
    - Instruction-1: **%a1** = alloca i8, align 1;
    - Instruction-2: store i8\* **%a1**, i8\*\* %a, align 8

# Data-Dependence

Definition-use relations between variables. Two types of variables on LLVM IR:

- **Top-level variables**, whose addresses are not taken ( $ValPN$  in SVF)
  - Including stack virtual **registers** (symbols starting with “%”) and **global** variables (symbols starting with “@”) are explicit, i.e., directly accessed.
  - **Def-use for top-level variables are directly available on LLVM’s SSA form.**
  - For example, def-use for **%a1** from Instruction-1 to Instruction-2.
    - Instruction-1: **%a1** = alloca i8, align 1;
    - Instruction-2: store i8\* **%a1**, i8\*\* %a, align 8
- **Address-taken variables** (abstract objects), accessed indirectly at load or store instructions via top-level variables ( $ObjPN$  in SVF)
  - A **stack object** created at an LLVM’s ‘alloca’ instruction or a **heap object** created via (e.g., ‘malloc’ callsite) or a **global object**.

# Data-Dependence

Definition-use relations between variables. Two types of variables on LLVM IR:

- **Top-level variables**, whose addresses are not taken (ValPN in SVF)
  - Including stack virtual **registers** (symbols starting with “%”) and **global** variables (symbols starting with “@”) are explicit, i.e., directly accessed.
  - **Def-use for top-level variables are directly available on LLVM’s SSA form.**
  - For example, def-use for **%a1** from Instruction-1 to Instruction-2.
    - Instruction-1: **%a1** = alloca i8, align 1;
    - Instruction-2: store i8\* **%a1**, i8\*\* %a, align 8
- **Address-taken variables** (abstract objects), accessed indirectly at load or store instructions via top-level variables (ObjPN in SVF)
  - A **stack object** created at an LLVM’s ‘alloca’ instruction or a **heap object** created via (e.g., ‘malloc’ callsite) or a **global object**.
  - **Def-use for address-taken variables are computed via pointer analysis.**
  - For example, there is a def-use for object o from Instruction-1 to Instruction-2 if pointers **%a** and **%b** both point to o.
    - Instruction-1: store i8\* %a1, i8\*\* **%a**, align 8
    - Instruction-2: %c = load i8\*\* **%b**, align 8

# Pointer analysis

- Points-to Analysis: aims to statically determine the possible runtime values of a pointer at compile-time.
  - Compute the *points-to set* (**a set of address-taken variables**) of each *pointer* (**top-level variable**)
  - For example,  $p = \&a$ ;  $p = q$ ;
  - The resulting points-to sets of  $p$  and  $q$  are:  $\text{pts}(p) = \text{pts}(q) = \{a\}$

# Pointer analysis

- Points-to Analysis: aims to statically determine the possible runtime values of a pointer at compile-time.
  - Compute the *points-to set* (**a set of address-taken variables**) of each *pointer* (**top-level variable**)
  - For example,  $p = \&a$ ;  $p = q$ ;
  - The resulting points-to sets of  $p$  and  $q$  are:  $\text{pts}(p) = \text{pts}(q) = \{a\}$
- Alias Analysis: determine whether two pointer dereferences refer to the same memory location.
  - If the points-to sets of two pointers  $p$  and  $q$  have overlapping elements (i.e.,  $\text{pts}(p) \cap \text{pts}(q)$  is not empty) then  $p$  and  $q$  are aliases. The dereferences of  $p$  and  $q$  may refer to the same memory location.



# Pointer analysis

Why shall we learn pointer analysis?

- Essential for building data-dependence relations between variables (memory objects).

# Pointer analysis

Why shall we learn pointer analysis?

- Essential for building data-dependence relations between variables (memory objects).
- Understanding aliases through different memory accesses

# Pointer analysis

Why shall we learn pointer analysis?

- Essential for building data-dependence relations between variables (memory objects).
- Understanding aliases through different memory accesses
  - `p = &a; q = p; *p = x; y = *q;`  
y has the same value as x since `*p` and `*q` both refer to a.

# Pointer analysis

Why shall we learn pointer analysis?

- Essential for building data-dependence relations between variables (memory objects).
- Understanding aliases through different memory accesses
  - `p = &a; q = p; *p = x; y = *q;`  
y has the same value as x since `*p` and `*q` both refer to a.
- Compiler optimizations and bug detection
  - Constant propagation
    - `p = 1; *q = r; x = p;`  
x is a constant value and equals 1, if p and q do not alias with each other.
    - `*p = 1; x = *q;`  
x is a constant value and equals 1, if p and q are must-aliases (always point to the same memory location w.r.t every execution path).

# Pointer analysis

Why shall we learn pointer analysis?

- Essential for building data-dependence relations between variables (memory objects).
- Understanding aliases through different memory accesses
  - `p = &a; q = p; *p = x; y = *q;`  
y has the same value as x since `*p` and `*q` both refer to a.
- Compiler optimizations and bug detection
  - Constant propagation
    - `p = 1; *q = r; x = p;`  
x is a constant value and equals 1, if p and q do not alias with each other.
    - `*p = 1; x = *q;`  
x is a constant value and equals 1, if p and q are must-aliases (always point to the same memory location w.r.t every execution path).
  - Taint analysis
    - `*p = taintedInput; x = *q;`  
x is tainted if p and q are aliases.

# Precision Dimensions

Can be generally classified into the following precision dimensions at different levels of abstractions.

**Flow-insensitive** analysis:

- Ignores program execution order
- A single solution at each program point

**Context-insensitive** analysis:

- Merges all of all calling contexts when analysing a program method

**Path-insensitive** analysis:

- Merges all incoming path information at the joint point of the control-flow graph

**Flow-sensitive** analysis:

- Respects the program execution order
- Separate solutions across whole program

**Context-sensitive** analysis:

- Distinguishes between different calling contexts of a program method

**Path-sensitive** analysis:

- Computes a solution per (abstract) program path.

# Precision Dimensions

## Levels of Abstractions

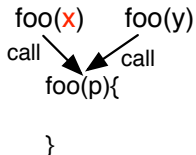
Assume **x** is a tainted value

$p = \mathbf{x}$

$p = y$

**flow-sensitivity**

at which  
**program point**  
 $p$  is tainted?



**context-sensitivity**

under which  
**calling context**  
 $p$  is tainted?

if(cond)

$p = \mathbf{x}$

else

$p = y$

**path-sensitivity**

along which  
**program path**  
 $p$  is tainted?

# Andersen's Pointer analysis

## Flow-, context-, and path-insensitive analysis

In this subject, we will practice **Andersen's analysis**<sup>1</sup>, a **flow-insensitive, context-insensitive and path-insensitive Andersen's analysis** through analyzing the **Constraint Graph** of a program.

- One of the most popular and widely used pointer analyses
- Constraint solving, i.e., inclusion-based constraint solving between program variables (PAGNode in SVF)

---

<sup>1</sup> Andersen, L. O. (1994). Program analysis and specialization for the C programming language (Doctoral dissertation, University of Copenhagen).



# Andersen's Pointer Analysis

An inclusion-based analysis operating on top of the constraint graph of a program. SVF transforms each LLVM instruction into a constraint edge connecting two nodes

- A `ConstraintNode` represents
  - A pointer: (top-level variable) or
  - An object: (address-taken variable, i.e., heap, stack, global or function object)
- A `ConstraintEdge` represents a constraint between two nodes

# Andersen's Pointer Analysis

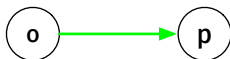
An inclusion-based analysis operating on top of the constraint graph of a program. SVF transforms each LLVM instruction into a constraint edge connecting two nodes

- A `ConstraintNode` represents
  - A pointer: (top-level variable) or
  - An object: (address-taken variable, i.e., heap, stack, global or function object)
- A `ConstraintEdge` represents a constraint between two nodes

Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$

# Andersen's Pointer Analysis

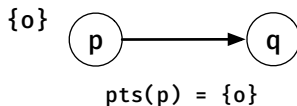
Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$



$\text{pts}(p) = \{o\}$

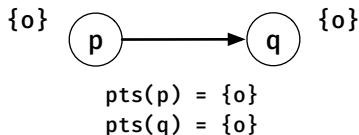
# Andersen's Pointer Analysis

Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$



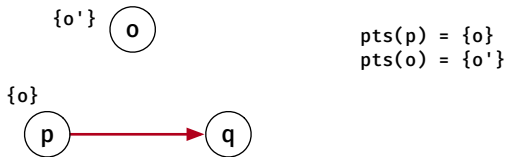
# Andersen's Pointer Analysis

Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$



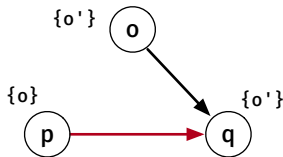
# Andersen's Pointer Analysis

Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$



# Andersen's Pointer Analysis

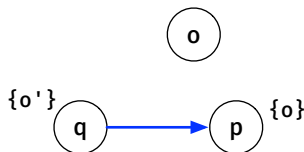
Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$



$\text{pts}(p) = \{o\}$   
 $\text{pts}(o) = \{o'\}$   
 $\text{pts}(q) = \{o'\}$

# Andersen's Pointer Analysis

Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$

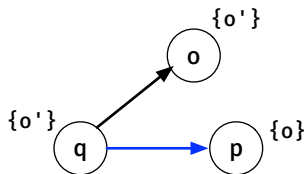


$\text{pts}(p) = \{o\}$   
 $\text{pts}(q) = \{o'\}$



# Andersen's Pointer Analysis

Constraint Type	C code	LLVM IR	Constraint rules
Address:	<code>p = &amp;o</code>	<code>%p = alloca //o</code>	$\text{pts}(p) = \text{pts}(p) \cup \text{pts}(o)$
Copy:	<code>q = p</code>	<code>%q = bitcast %p</code>	$\text{pts}(q) = \text{pts}(q) \cup \text{pts}(p)$
Load:	<code>q = *p</code>	<code>%q = load %p</code>	$\forall o \in \text{pts}(p): \text{pts}(q) = \text{pts}(o) \cup \text{pts}(q)$
Store:	<code>*p = q</code>	<code>store %q, %p</code>	$\forall o \in \text{pts}(p): \text{pts}(o) = \text{pts}(q) \cup \text{pts}(o)$




$\text{pts}(p) = \{o\}$   
 $\text{pts}(q) = \{o'\}$   
 $\text{pts}(o) = \{o'\}$

# Compile C Code to LLVM IR

```
void swap(char **p, char **q){  
    char* t = *p;  
    *p = *q;  
    *q = t;  
}  
int main(){  
    char a1, b1;  
    char *a = &a1;  
    char *b = &b1;  
    swap(&a,&b);  
}
```

compile to

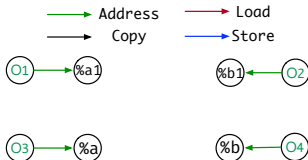


```
define i32 @main() #0 {  
entry:  
    %a1 = alloca i8, align 1      // O1  
    %b1 = alloca i8, align 1      // O2  
    %a = alloca i8*, align 8      // O3  
    %b = alloca i8*, align 8      // O4  
    store i8* %a1, i8** %a, align 8  
    store i8* %b1, i8** %b, align 8  
    call void @swap(i8** %a, i8** %b)  
    ret i32 0  
}  
define void @swap(i8** %p, i8** %q)  
#0 {  
entry:  
    %0 = load i8** %p, align 8  
    %1 = load i8** %q, align 8  
    store i8* %1, i8** %p, align 8  
    store i8* %0, i8** %q, align 8  
    ret void  
}
```

\*<https://github.com/SVF-tools/SVF-Teaching/wiki/CodeGraph#2-llvm-ir-generation>

# Construct a Constraint Graph from LLVM IR

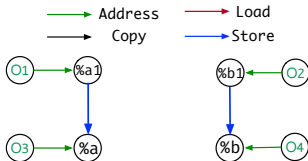
```
define i32 @main() #0 {  
entry:  
%a1 = alloca i8, align 1      // O1  
%b1 = alloca i8, align 1      // O2  
%a = alloca i8*, align 8      // O3  
%b = alloca i8*, align 8      // O4  
store i8* %a1, i8** %a, align 8  
store i8* %b1, i8** %b, align 8  
call void @swap(i8** %a, i8** %b)  
ret i32 0  
}  
define void @swap(i8** %p, i8** %q)  
#0 {  
entry:  
%0 = load i8** %p, align 8  
%1 = load i8** %q, align 8  
store i8* %1, i8** %p, align 8  
store i8* %0, i8** %q, align 8  
ret void  
}
```



<https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag>

# Construct a Constraint Graph from LLVM IR

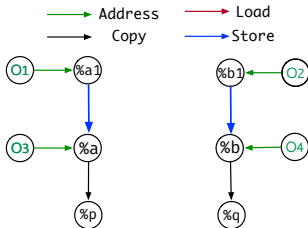
```
define i32 @main() #0 {  
  entry:  
  %a1 = alloca i8, align 1      // O1  
  %b1 = alloca i8, align 1      // O2  
  %a = alloca i8*, align 8      // O3  
  %b = alloca i8*, align 8      // O4  
  store i8* %a1, i8** %a, align 8  
  store i8* %b1, i8** %b, align 8  
  call void @swap(i8** %a, i8** %b)  
  ret i32 0  
}  
  
define void @swap(i8** %p, i8** %q)  
#0 {  
  entry:  
  %0 = load i8** %p, align 8  
  %1 = load i8** %q, align 8  
  store i8* %1, i8** %p, align 8  
  store i8* %0, i8** %q, align 8  
  ret void  
}
```



\*<https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag>

# Construct a Constraint Graph from LLVM IR

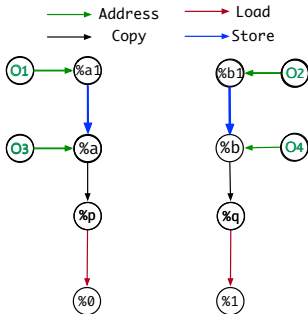
```
define i32 @main() #0 {  
  entry:  
  %a1 = alloca i8, align 1      // O1  
  %b1 = alloca i8, align 1      // O2  
  %a = alloca i8*, align 8      // O3  
  %b = alloca i8*, align 8      // O4  
  store i8* %a1, i8** %a, align 8  
  store i8* %b1, i8** %b, align 8  
  call void @swap(i8** %a, i8** %b)  
  ret i32 0  
}  
define void @swap(i8** %p, i8** %q)  
#0 {  
  entry:  
  %0 = load i8** %p, align 8  
  %1 = load i8** %q, align 8  
  store i8* %1, i8** %p, align 8  
  store i8* %0, i8** %q, align 8  
  ret void  
}
```



<https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag>

# Construct a Constraint Graph from LLVM IR

```
define i32 @main() #0 {
entry:
%a1 = alloca i8, align 1      // O1
%b1 = alloca i8, align 1      // O2
%a = alloca i8*, align 8      // O3
%b = alloca i8*, align 8      // O4
store i8* %a1, i8** %a, align 8
store i8* %b1, i8** %b, align 8
call void @swap(i8** %a, i8** %b)
ret i32 0
}
define void @swap(i8** %p, i8** %q)
#0 {
entry:
%0 = load i8** %p, align 8
%1 = load i8** %q, align 8
store i8* %1, i8** %p, align 8
store i8* %0, i8** %q, align 8
ret void
}
```

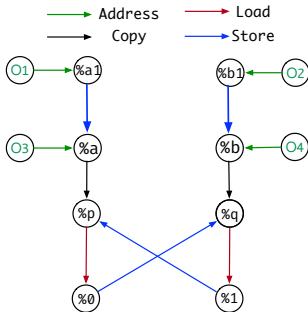


<https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag>

# Construct a Constraint Graph from LLVM IR

```
define i32 @main() #0 {
entry:
%a1 = alloca i8, align 1      // O1
%b1 = alloca i8, align 1      // O2
%a = alloca i8*, align 8      // O3
%b = alloca i8*, align 8      // O4
store i8* %a1, i8** %a, align 8
store i8* %b1, i8** %b, align 8
call void @swap(i8** %a, i8** %b)
ret i32 0
}

define void @swap(i8** %p, i8** %q)
#0 {
entry:
%0 = load i8** %p, align 8
%1 = load i8** %q, align 8
store i8* %1, i8** %p, align 8
store i8* %0, i8** %q, align 8
ret void
}
```

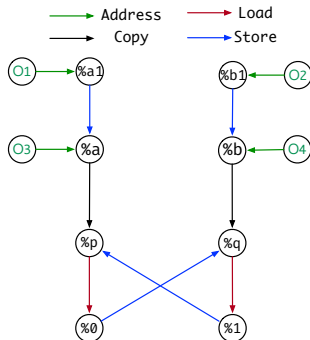


<https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag>

# Andersen's Pointer Analysis

## Algorithm

```
define i32 @main() #0 {
entry:
%a1 = alloca i8, align 1      // O1
%b1 = alloca i8, align 1      // O2
%a = alloca i8*, align 8      // O3
%b = alloca i8*, align 8      // O4
store i8* %a1, i8** %a, align 8
store i8* %b1, i8** %b, align 8
call void @swap(i8** %a, i8** %b)
ret i32 0
}
define void @swap(i8** %p, i8** %q)
#0 {
entry:
%0 = load i8** %p, align 8
%1 = load i8** %q, align 8
store i8* %1, i8** %p, align 8
store i8* %0, i8** %q, align 8
ret void
}
```



---

```
G = < V, E > // Constraint Graph
V: a set of nodes in graph
E: a set of edges in graph
WorkList: a vector of nodes
1 foreach address p = &o do // address rule
2   pts(p) = {o}
3   pushIntoWorklist(p)
4 while WorkList ≠ ∅ do
5   p ← popFromWorklist()
6   foreach o ∈ pts(p) do
7     foreach store *p = q do // store rule
8       if q → o ∉ E then
9         E ← E ∪ {q → o} // add copy edge
10        pushIntoWorklist(q)
11      foreach load r = *p do // load rule
12        if o → r ∉ E then
13          E ← E ∪ {o → r} // add copy edge
14          pushIntoWorklist(o)
15    foreach p → x ∈ E do // copy rule
16      pts(x) ← pts(x) ∪ pts(p)
17      if pts(x) changed then
18        pushIntoWorklist(x)
```

---

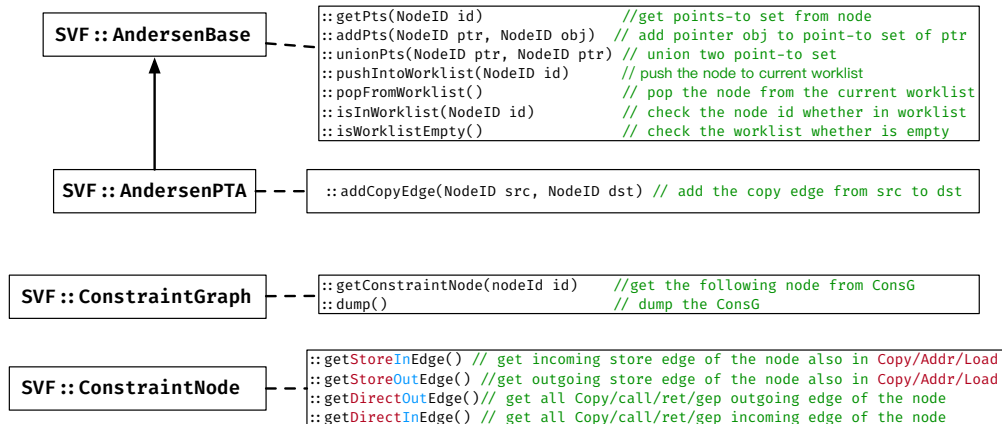


# Andersen's Pointer Analysis

## Constraint solving Algorithm

- A worklist holds a set of constraint graph nodes for processing
- Pop a node  $p$  from the worklist.
- Handle each incoming `store` edge and each outgoing `load` edge of node  $p$  by adding `copy` edges.
- Handle each outgoing `copy` edge of  $p$  by propagating points-to information.
- The constraint solving stops when no points-to set of a pointer is changed.

# APIs for Implementing Andersen's analysis



<https://github.com/SVF-tools/SVF-Teaching/wiki/SVF-CPP-API#worklist-operations>

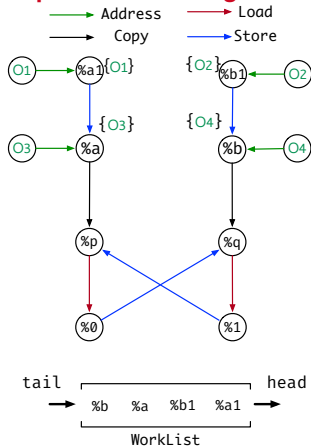
<https://github.com/SVF-tools/SVF-Teaching/wiki/SVF-CPP-API#points-to-set-operations>

<https://github.com/SVF-tools/SVF-Teaching/wiki/SVF-CPP-API#constraintgraph-constraintnode-and-constrainededge>

# Andersen's Pointer Analysis

## Constraint graph before the while loop worklist solving

```
define i32 @main() #0 {  
  entry:  
  %a1 = alloca i8, align 1      // O1  
  %b1 = alloca i8, align 1      // O2  
  %a = alloca i8*, align 8      // O3  
  %b = alloca i8*, align 8      // O4  
  store i8* %a1, i8** %a, align 8  
  store i8* %b1, i8** %b, align 8  
  call void @swap(i8** %a, i8** %b)  
  ret i32 0  
}  
  
define void @swap(i8** %p, i8** %q)  
#0 {  
  entry:  
  %0 = load i8** %p, align 8  
  %1 = load i8** %q, align 8  
  store i8* %1, i8** %p, align 8  
  store i8* %0, i8** %q, align 8  
  ret void  
}
```



---

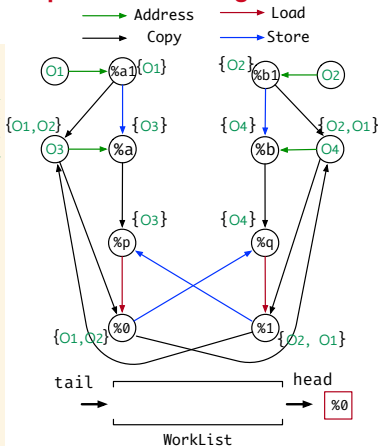
```
G = < V, E > // Constraint Graph  
V: a set of nodes in graph  
E: a set of edges in graph  
WorkList: a vector of nodes  
1 foreach address p = &o do // address rule  
2   pts(p) = {o}  
3   pushIntoWorklist(p)  
4 while WorkList ≠ ∅ do  
5   p ← popFromWorklist()  
6   foreach o ∈ pts(p) do  
7     foreach store *p = q do // store rule  
8       if q → o ∉ E then  
9         E ← E ∪ {q → o} // add copy edge  
10        pushIntoWorklist(q)  
11      foreach load r = *p do // load rule  
12        if o → r ∉ E then  
13          E ← E ∪ {o → r} // add copy edge  
14          pushIntoWorklist(o)  
15      foreach p → x ∈ E do // copy rule  
16        pts(x) ← pts(x) ∪ pts(p)  
17        if pts(x) changed then  
18          pushIntoWorklist(x)
```

---

# Andersen's Pointer Analysis

## Constraint graph after the while loop worklist solving

```
define i32 @main() #0 {  
  entry:  
  %a1 = alloca i8, align 1      // O1  
  %b1 = alloca i8, align 1      // O2  
  %a = alloca i8*, align 8      // O3  
  %b = alloca i8*, align 8      // O4  
  store i8* %a1, i8** %a, align 8  
  store i8* %b1, i8** %b, align 8  
  call void @swap(i8** %a, i8** %b)  
  ret i32 0  
}  
define void @swap(i8** %p, i8** %q)  
#0 {  
  entry:  
  %0 = load i8** %p, align 8  
  %1 = load i8** %q, align 8  
  store i8* %1, i8** %p, align 8  
  store i8* %0, i8** %q, align 8  
  ret void  
}
```



```
G = < V, E > // Constraint Graph  
V: a set of nodes in graph  
E: a set of edges in graph  
WorkList: a vector of nodes  
1 foreach address p = &o do // address rule  
2   pts(p) = {o}  
3   pushIntoWorkList(p)  
4 while WorkList ≠ ∅ do  
5   p ← popFromWorkList()  
6   foreach o ∈ pts(p) do  
7     foreach store *p = q do // store rule  
8       if q → o ∉ E then  
9         E ← E ∪ {q → o} // add copy edge  
10        pushIntoWorkList(q)  
11     foreach load r = *p do // load rule  
12       if o → r ∉ E then  
13         E ← E ∪ {o → r} // add copy edge  
14        pushIntoWorkList(o)  
15   foreach p → x ∈ E do // copy rule  
16     pts(x) ← pts(x) ∪ pts(p)  
17     if pts(x) changed then  
18       pushIntoWorkList(x)
```

# What's next?

- (1) Understand data-dependence in today's slides
- (2) Implement Andersen's pointer analysis, i.e., Task in Assignment 3
  - Refer to 'Assignment-3.pdf' on Canvas to know more about Assignment 3.