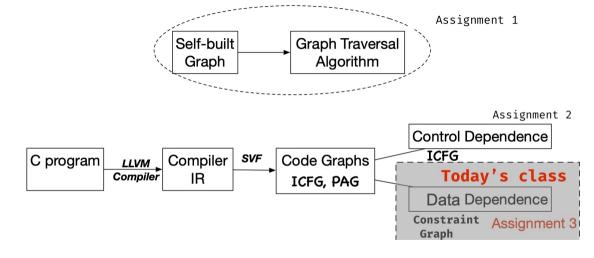
Yulei Sui

University of Technology Sydney, Australia



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 - Including stack virtual registers (symbols starting with "%") and global variables (symbols starting with "@") are explicit, i.e., directly accessed.

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 - Def-use for address-taken variables are computed via pointer analysis.
 - For example, there is a def-use for object o from Instruction-1 to Instruction-2 if pointers %a and %b both point to o.
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 - Instruction-2: %c = load i8** %b, align 8

- Points-to Analysis: aims to statically determine the possible runtime values of a pointer at compile-time.
 - Compute the points-to set (a set of address-taken variables) of each pointer (top-level variable)
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- Alias Analysis: determine whether two pointer dereferences refer to the same memory location.
 - If the points-to sets of two pointers p and q have overlapping elements (i.e., pts(p) ∩ pts(q) = ∅) then p and q are aliases. The derereferences of p and q may refer to the same memory location.

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 Essential for building data-dependence relations between variables (memory objects).

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- Compiler optimizations and bug detection
 - Constant propagation
 - p = 1; *q = r; x = p;
 x is a constant value and equals 1, if p and q do not alias with each other.
 - *p = 1; x = *q;
 x is a constant value and equals 1, if p and q are must-aliases (always point to the same memory location w.r.t every execution path).

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```
    *p = 1; x = *q;
    x is a constant value and equals 1, if p and q are must-aliases (always point to the same memory location w.r.t every execution path).
```

Taint analysis

```
    *p = taintedInput; x = *q;
    x is tainted if p and g are aliases.
```

Precision Dimensions

Can be generally classified into the following precision dimensions at different levels of abstractions.

Flow-insensitive analysis:

- Ignores program execution order
- A single solution at each program point

Context-insensitive analysis:

 Merges all of all calling contexts when analysing a program method

Path-insensitive analysis:

 Merges all incoming path information at the joint point of the control-flow graph

Flow-sensitive analysis:

- Respects the program execution order
- A Separate solution across whole program

Context-sensitive analysis:

 Distinguishes between different calling contexts of a program method

Path-sensitive analysis:

Computes a solution per (abstract) program path.

Precision Dimensions

Levels of Abstractions

Assume x is a tainted value

$$p = x$$

$$p = y$$

flow-sensitivity

at which program point p is tainted?

context-sensitivity

under which calling context p is tainted?

$$\begin{aligned} &\text{if(cond)}\\ &&p=\textbf{x}\\ &\text{else}\\ &&p=\textbf{y} \end{aligned}$$

path-sensitivity

along which program path p is tainted?

Flow-, context-, and path-insensitive analysis

In this subject, we will practice **Andersen's analysis**¹, a **flow-insensitive**, **context-insensitive and path-insensitive Andersen's analysis** through analyzing the **Constraint Graph** of a program.

- One of the most popular and widely used pointer analyses
- Constraint solving, i.e., inclusion-based constraint solving between program variables (PAGNode in SVF)

¹ Andersen, L. O. (1994). Program analysis and specialization for the C programming language (Doctoral dissertation, University of Cophenhagen).

An inclusion-based analysis operating on top of the constraint graph of a program.SVF transforms each LLVM instruction into a constraint edge connecting two nodes

- Node represents
 - A pointer: (LLVM Value in pointer type) or
 - An object: (heap, stack, global, function)
- Edge represents a constraint between two nodes

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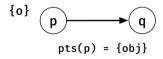
Constraint Type	C code	LLVM IR	Constraint rules
Address:	p = &o	%p = alloca //o	pts(p) = pts(p) U pts(o)
Copy:	q = p	%p = bitcast %q	pts(q) = pts(q) U pts(p)
Load:	q =*p	%q = load %p	\forall o \in pts(p): pts(o) = pts(o) U pts(q)
Store:	*p = q	store %q, %p	\forall o \in pts(p): pts(q) = pts(q) U pts(o)

Constraint Type	C code	LLVM IR	Constraint rules
Address:	p = &o	%p = alloca //o	<pre>pts(p) = pts(p) U pts(o)</pre>
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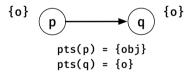


$$pts(p) = {o}$$

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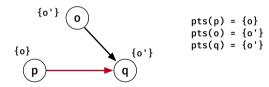


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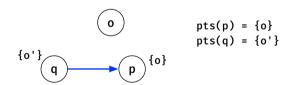


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Store:	*p = q	store %q, %p	\forall o \in pts(p): pts(q) = pts(q) U pts(o)
		{o'}	pts(p) = {o} pts(o) = {o'}
		{o}	q

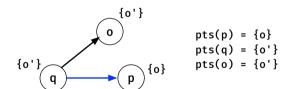
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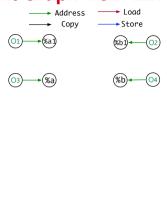


Compile C Code to LLVM IR

```
define i32 @main() #0 {
                                                                entry:
                                                                %a1 = alloca i8, alian 1
                                                                %b1 = alloca i8, align 1
                                                                                               // O2
void swap(char **p, char **a){
                                                                %a = alloca i8*, alian 8
                                                                                               // O3
  char* t = *p:
                                                                %b = alloca i8*, alian 8
                                                                                               // 04
       *p = *a:
                                                                store i8* %a1, i8** %a, alian 8
       *a = t:
                                                                store i8* %b1, i8** %b, align 8
                                                                call void @swap(i8** %a, i8** %b)
                                      compile to
int main(){
                                                                 ret i32 0
      char al. b1:
     char *a = &a1;
                                                                define void @swap(i8** %p, i8** %q)
      char *b = \&b1;
                                                                #0 {
      swap(&a.&b):
                                                                entry:
                                                                \%0 = load i8** \%p, alian 8
                                                                %1 = load i8** %a, alian 8
                                                                store i8* %1, i8** %p, alian 8
                                                                store i8* %0. i8** %a. alian 8
                                                                ret void
```

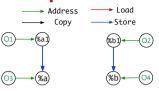
*https://github.com/SVF-tools/SVF-Teaching/wiki/CodeGraph#2-1lvm-ir-generation

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define i32 @main() #0 {
entry:
%a1 = alloca i8. alian 1
                               // O1
%b1 = alloca i8, align 1
                               // O2
‰a = alloca i8*, alian 8
                               // O3
%b = alloca i8*, alian 8
                               // O4
store i8* %a1, i8** %a, alian 8
store i8* %b1, i8** %b, align 8
call void @swap(i8** %a, i8** %b)
ret i32 0
define void @swap(i8** %p. i8** %a)
#0 {
entry:
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store i8* %1, i8** %p, alian 8
store i8* %0, i8** %a, alian 8
ret void
```



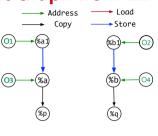
 $\verb|https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program \#5-pag|$

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%a1 = alloca i8. alian 1
                               // O1
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                               // O2
%a = alloca i8*, alian 8
                               // O3
%b = alloca i8*, alian 8
                               // O4
store i8* %a1. i8** %a. alian 8
store i8* %b1, i8** %b, align 8
call void @swap(i8** %a, i8** %b)
ret i32 0
define void @swap(i8** %p. i8** %a)
#0 {
entry:
%0 = load i8** %p. alian 8
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store i8* %1, i8** %p, alian 8
store i8* %0, i8** %a, alian 8
ret void
```



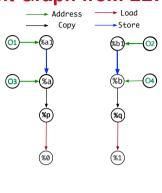
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%1 = load i8** %a, alian 8
store i8* %1, i8** %p, alian 8
store i8* %0, i8** %a, alian 8
ret void
```



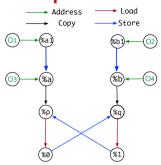
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                               // O2
%a = alloca i8*, alian 8
                               // O3
%b = alloca i8*, alian 8
                               // O4
store i8* %a1. i8** %a. alian 8
store i8* %b1, i8** %b, align 8
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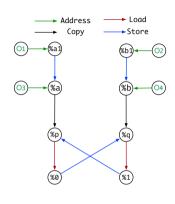
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%1 = load i8** %a, alian 8
store i8* %1, i8** %p, alian 8
store i8* %0, i8** %a, alian 8
ret void
```



https://github.com/svf-tools/SVF/wiki/Analyze-a-Simple-C-Program#5-pag

Algorithm

```
define i32 @main() #0 {
entry:
%a1 = alloca i8, alian 1
                               // 01
%b1 = alloca i8, alian 1
                               // O2
%a = alloca i8*, alian 8
                               // O3
%b = alloca i8*, alian 8
                               // 04
store i8* %a1, i8** %a, alian 8
store i8* %b1, i8** %b, alian 8
call void @swap(i8** %a, i8** %b)
ret i32 0
define void @swap(i8** %p, i8** %a)
#0 {
entry:
\%0 = load i8** \%p, alian 8
%1 = load i8** %a, alian 8
store i8* %1, i8** %p, alian 8
store i8* %0. i8** %a. alian 8
ret void
```



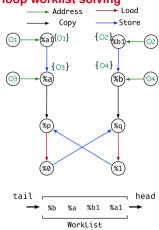
```
G = < V,E > // Constraint Graph
  V: a set of nodes in graph
   E: a set of edges in graph
  WorkList: a vector of nodes
  foreach address p = &o do
        nts(p) = \{0\}
        pushIntoWorklist(p)
  while WorkList ≠ Ø do
      p ← popFromWorklist()
      foreach o E pts(p) do
         foreach store *p = q do
             if q→o ∉ E then
                E \leftarrow E \cup \{a \rightarrow o\}
                pushIntoWorklist(q)
10
         foreach load r = *p do
11
             if o→r ∉ F then
12
                   E \leftarrow E \cup \{o \rightarrow r\}
13
                   pushIntoWorklist(o)
14
      foreach p \rightarrow x \in E do
15
16
           pts(x) \leftarrow pts(x) \cup pts(p)
           if pts(x) changed then
17
                  pushIntoWorklist(x)
18
```

Constraint solving Algorithm

- A worklist holds a set of constraint graph nodes for processing
- Pop a node p from the worklist.
- Handle each incoming store edge and each outgoing load edge of node p by adding copy edges.
- Handle each outgoing copy edge of p by propagating points information.
- The constraint solving stops when no points-to set of a pointer is changed.

Constraint graph before the while loop worklist solving

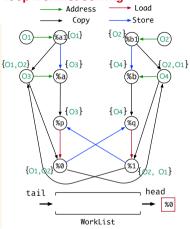
```
define i32 @main() #0 {
entry:
%a1 = alloca i8, alian 1
                               // 01
%b1 = alloca i8, alian 1
                               // O2
%a = alloca i8*, alian 8
                               // O3
%b = alloca i8*, alian 8
                               // 04
store i8* %a1, i8** %a, alian 8
store i8* %b1, i8** %b, alian 8
call void @swap(i8** %a, i8** %b)
ret i32 0
define void @swap(i8** %p, i8** %a)
#0 S
entry:
\%0 = load i8** \%p, alian 8
%1 = load i8** %a, alian 8
store i8* %1, i8** %p, alian 8
store i8* %0. i8** %a. alian 8
ret void
```



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      p ← popFromWorklist()
      foreach o ∈ pts(p) do
          foreach store *p = q do
             if a→o ∉ F then
                 E \leftarrow E \cup \{a \rightarrow o\}
                 pushIntoWorklist(q)
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Constraint graph after the while loop worklist solving

```
define i32 @main() #0 {
entry:
%a1 = alloca i8, alian 1
                               // 01
%b1 = alloca i8, alian 1
                               // O2
%a = alloca i8*, alian 8
                               // 03
%b = alloca i8*, alian 8
                               // 04
store i8* %a1, i8** %a, alian 8
store i8* %b1, i8** %b, alian 8
call void @swap(i8** %a, i8** %b)
ret i32 0
define void @swap(i8** %p, i8** %a)
#0 S
entry:
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             if o→r ∉ E then
12
                   F \leftarrow F \cup \{o \rightarrow r\}
13
                   pushIntoWorklist(o)
14
15
      foreach p \rightarrow x \in E do
16
           pts(x) \leftarrow pts(x) \cup pts(p)
           if pts(x) changed then
17
                  pushIntoWorklist(x)
18
```

What's next?

- (1) Understand data-dependence in today's slides
- (2) Implement Andersen's pointer analysis, i.e., Task in Assignment 3
 - Refer to 'Assignment-3.pdf' on Canvas to know more about Assignment 3.