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Operating Systems

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Last Class



- Copy on write
- Page replacement algorithm
 - FIFO
 - Belady's Anomaly
 - Optimal
 - LRU
- LRU Implementation
 - using counter
 - using stack

Comparison of OPT with LRU and FIFO



Reference string:

2 3 2 1 5 2 4 5 3 2 5 2

Assume three frames

Least Recently Used (LRU) Algorithm

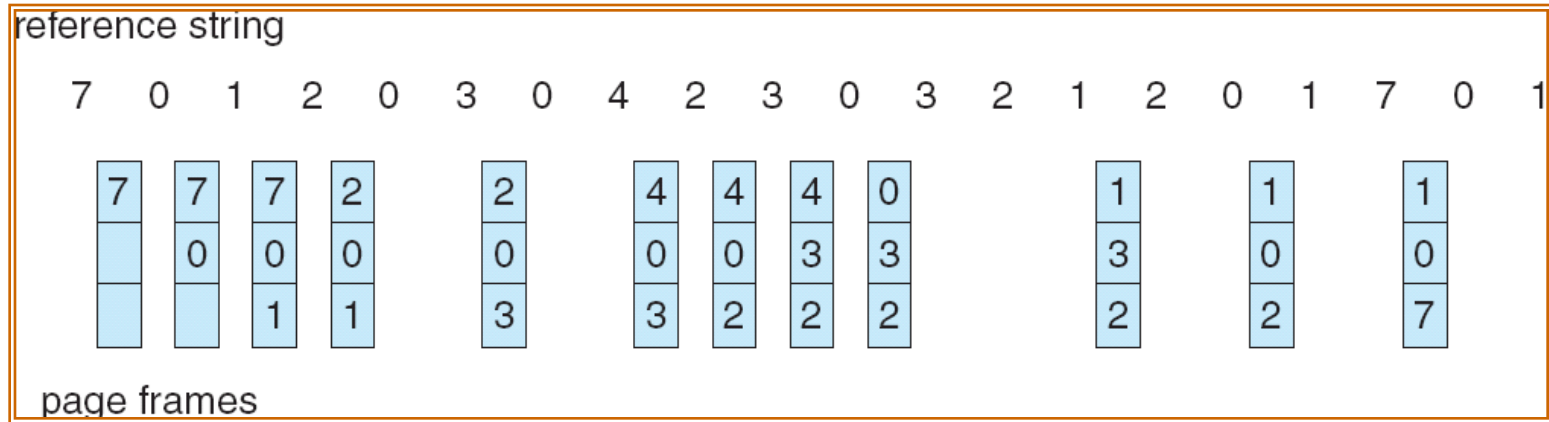
Reference string: 1, 2, 3, 4, 1, 2, **5**, 1, 2, **3**, **4**, **5**

1	1	1	1	5
2	2	2	2	2
3	5	5	4	4
4	4	3	3	3

Counter implementation

- Every page entry has a counter; every time page is referenced through this entry, copy the clock into the counter
- When a page needs to be changed, look at the counters to determine which are to change

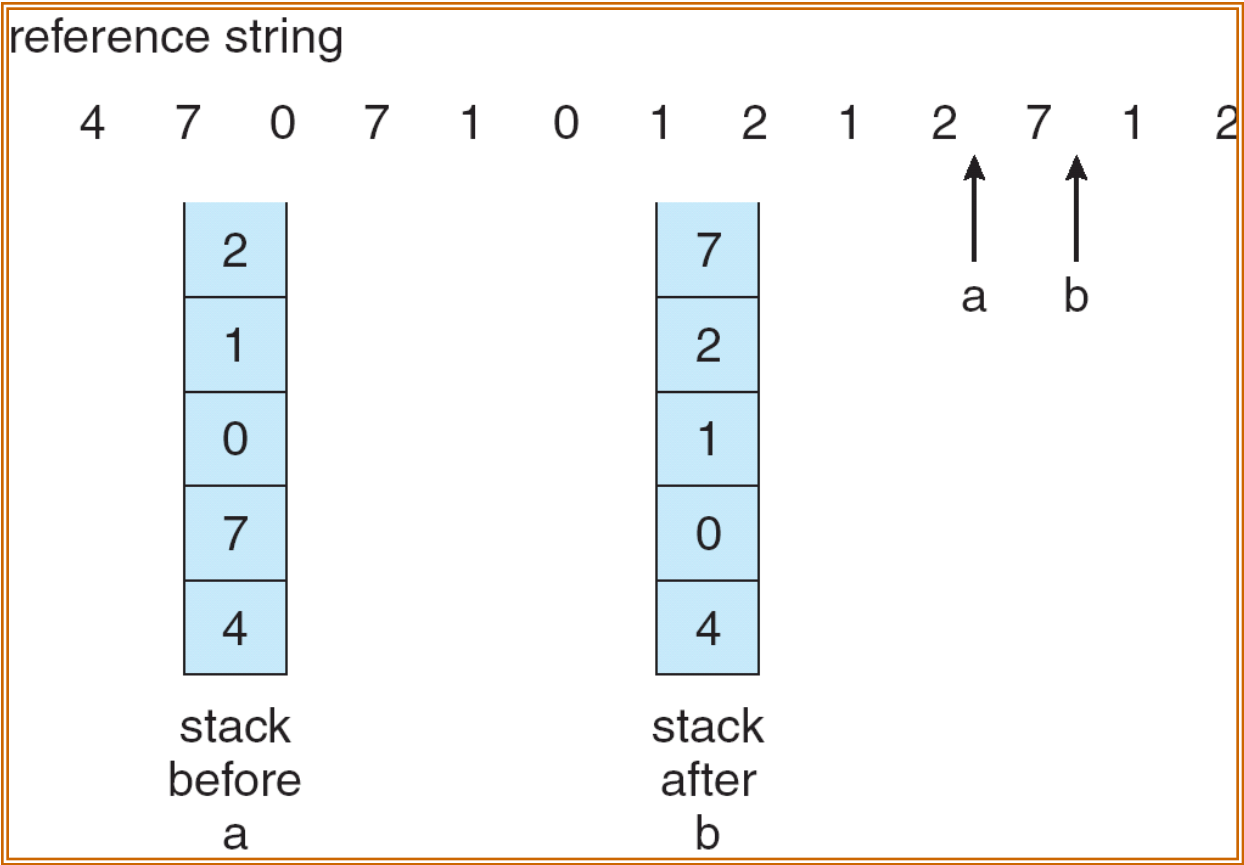
Example



LRU Algorithm (Cont.)

- Stack implementation – keep a stack of page numbers
 - Page referenced:
 - move it to the top
 - implemented using doubly linked list
 - No search for replacement
 - How many pointers are needed ?

Example



Advantages of Optimal and LRU page replacement algorithm



- never exhibits Belady's anomaly

Hardware Matrix LRU implementation



- For n pages, keep an $n \times n$ bit matrix.
- Whenever page frame k is referenced, the hardware first sets all the bits of row k to 1, then sets all the bits of column k to 0.
- At any instant, the row whose binary value is lowest is the least recently used,
- Consider a reference string : 0 1 2 3 2 1 0 3 2 3

Contd..

		Page			
		0	1	2	3
0		0	1	1	1
1		0	0	0	0
2		0	0	0	0
3		0	0	0	0

(a)

		Page			
		0	1	2	3
0	0	0	1	1	
1	1	0	1	1	
2	0	0	0	0	
3	0	0	0	0	

(b)

		Page			
		0	1	2	3
0	0	0	0	0	1
1	1	0	0	0	1
2	1	1	0	0	1
3	0	0	0	0	0

(c)

		Page			
		0	1	2	3
0	0	0	0	0	0
1	1	0	0	0	0
2	1	1	0	0	0
3	1	1	1	0	0

(d)

		Page			
		0	1	2	3
0	0	0	0	0	0
1	0	0	0	0	0
2	1	1	0	1	1
3	1	1	0	0	0

(e)

0	0	0	0
1	0	1	1
1	0	0	1
1	0	0	0

(f)

0	1	1	1
0	0	1	1
0	0	0	1
0	0	0	0

(g)

0	1	1	0
0	0	1	0
0	0	0	0
1	1	1	0

(h)

0	1	0	0
0	0	0	0
1	1	0	1
1	1	0	0

(i)

0	1	0	0
0	0	0	0
1	1	0	0
1	1	1	0

(j)

LRU Approximation Algorithms

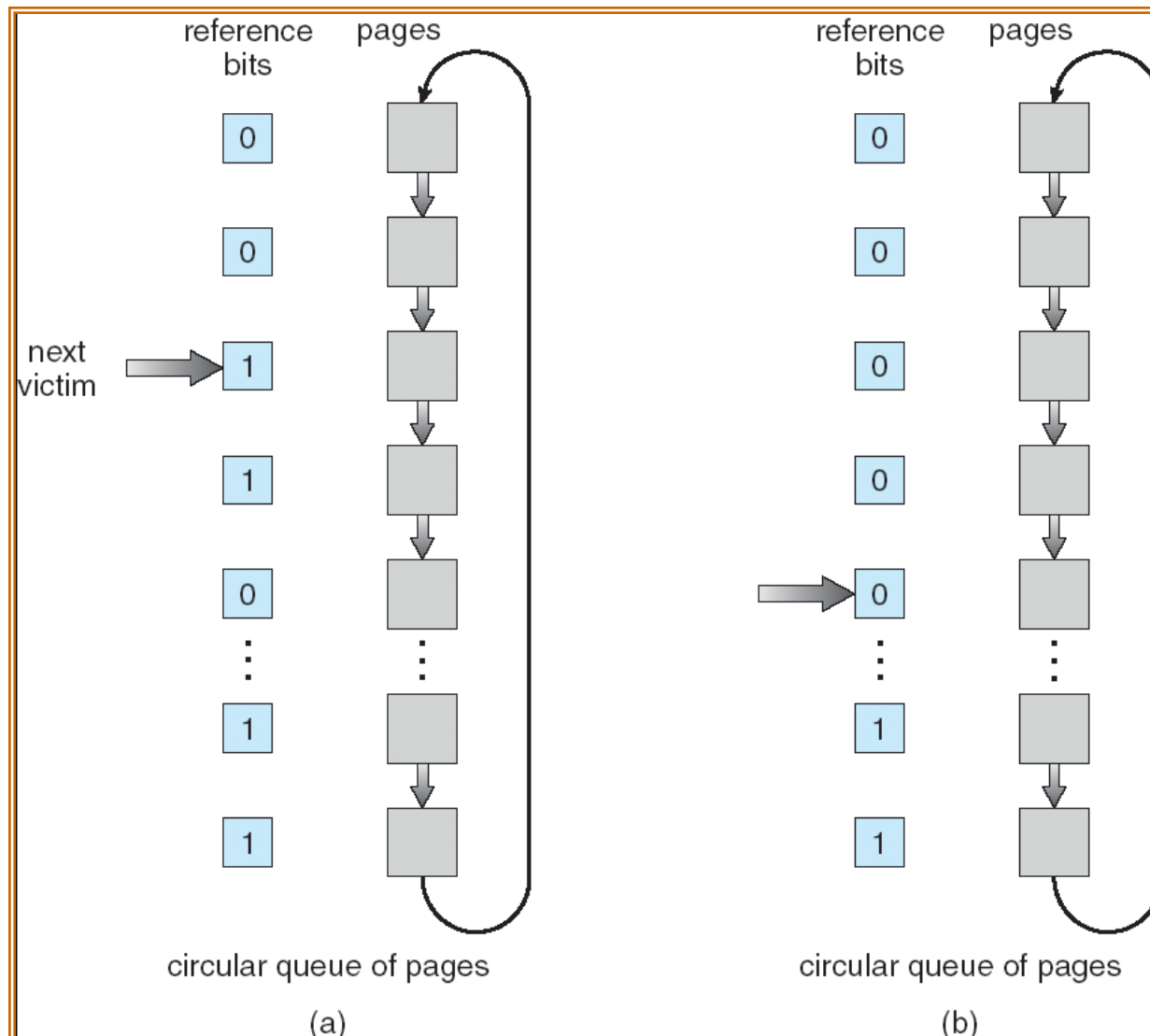
Reference bit

- With each page associate a bit, initially = 0
- When page is referenced bit set to 1
- Replace the one which is 0 (if one exists)
 - We do not know the order, however

Second chance

- Need reference bit
- Clock replacement
- If page to be replaced (in clock order) has reference bit = 1 then:
 - set reference bit 0
 - leave page in memory
 - replace next page (in clock order), subject to same rules

Second-Chance (clock) Page-Replacement Algorithm



Example



Reference string:

0 1 3 6 2 4 5 2 5 0 3 1 2 5 4 1 0

Assume 4 frames

Global vs. Local Allocation

Global replacement – process selects a replacement frame from the set of all frames; one process can take a frame from another

Local replacement – each process selects from only its own set of allocated frames

Thrashing

If a process does not have “enough” pages, the page-fault rate is very high. This leads to:

- low CPU utilization
- operating system thinks that it needs to increase the degree of multiprogramming
- another process added to the system

Thrashing \equiv a process is busy swapping pages in and out