Table 1: Distributions provided by the IACS module included with runions

| Name                   | 1: Distributions provided by the JA Usage  | Density  | Lower      |
|------------------------|--|--|------------|
| Pareto I <sup>1</sup>  | dpar1(alpha,sigma) $\alpha>0,\sigma>0$   | $\alpha  \sigma^{\alpha}  x^{-(\alpha+1)}$   | σ          |
| Pareto II              | $\begin{array}{l} {\rm dpar2(alpha,sigma,mu)} \\ \alpha>0,\sigma>0 \end{array}$                                | $\frac{\alpha}{\sigma} \left( \frac{\sigma + x - \mu}{\sigma} \right)^{-(\alpha + 1)}$   | $\mu$      |
| Pareto III             | $\label{eq:continuity} \begin{split} & \texttt{dpar3(sigma,mu,gamma)} \\ & \sigma > 0, \gamma > 0 \end{split}$ | $\frac{\left(\frac{x-\mu}{\sigma}\right)^{\frac{1}{\gamma}-1}\left(\frac{x-\mu}{\sigma}^{\frac{1}{\gamma}}+1\right)^{-2}}{\gamma\sigma}$                   | $\mu$      |
| Pareto IV              | dpar4(alpha,sigma,mu,gamma) $\alpha>0,\sigma>0,\gamma>0$   | $\frac{\alpha \left(\frac{x-\mu}{\sigma}\right)^{\frac{1}{\gamma}-1} \left(\frac{x-\mu}{\sigma}^{\frac{1}{\gamma}}+1\right)^{-(\alpha+1)}}{\gamma \sigma}$ | $\mu$      |
| Lomax <sup>2</sup>     | $\label{eq:alpha,sigma} \begin{split} & \texttt{dlomax(alpha,sigma)} \\ & \alpha > 0, \sigma > 0 \end{split}$  | $\frac{\alpha}{\sigma} \left( 1 + \frac{x}{\sigma} \right)^{-(\alpha+1)}$  | 0          |
| DuMouchel <sup>3</sup> | $	ext{dmouch(sigma)} \ \sigma > 0$   | $\frac{\sigma}{(x+\sigma)^2}$  | 0          |
| Gen. Par.              | $\begin{array}{l} {\tt dgenpar(sigma,mu,xi)} \\ \sigma > 0 \end{array}$  | $\frac{1}{\sigma} \left( 1 + \xi \frac{x - \mu}{\sigma} \right)^{-\left(\frac{1}{\xi} + 1\right)}$   | $\mu^{~4}$ |
|                        |  | For $\xi = 0$ : $\frac{1}{\sigma} e^{\frac{-(x-\mu)}{\sigma}}$   | $\mu$      |

This is equivalent to the dpar(alpha,c) distribution and provided for naming consistency <sup>2</sup> This is referred to as the '2<sup>nd</sup> kind Pareto' distribution by Van Hauwermeiren and Vose (2009); an alternative form for the PDF of this distribution is given by:  $\frac{\alpha \sigma^{\alpha}}{(x+\sigma)^{\alpha+1}}$ 

<sup>&</sup>lt;sup>3</sup> This distribution was suggested by DuMouchel (1994) as a suitable prior for  $\tau$  in a Bayesian meta-analysis setting, and is equivalent to a Lomax distribution with  $\alpha=1$ 

<sup>&</sup>lt;sup>4</sup> The Generalised Pareto distribution also has an upper bound of  $x \le \mu - \frac{\sigma}{\xi}$  for  $\xi < 0$