

# **Math 3330: Regression Notes**

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# Preface

Welcome to the MATH 3330 Notes! Please install [R](#) and [R studio](#) (Or you can use VSCode if you're comfortable there.)

In order to make the most of these notes, do all of the exercises in the order they appear.

There will likely be typos and some errors, please let me know if you encounter any.

These notes should be used in conjunction with the book:

Title: Introduction to Linear Regression Analysis, *Volume 821 of Wiley Series in Probability and Statistics* Authors: Douglas C. Montgomery, Elizabeth A. Peck, G. Geoffrey Vining Edition: 5, illustrated, reprint Publisher: John Wiley & Sons, 2012 ISBN: 0470542810, 9780470542811

# 1 Introduction

## 1.1 What is the course about?

### 1.1.1 The main question

The whole course is concerned with the following problem: Suppose that  $X$  and  $Y$  are some attributes of a population. What is the relationship between  $X$  and  $Y$ . How can we use  $X$  to predict  $Y$ , or how can we use  $X$  to explain  $Y$ ?

For example, questions of this form include:

- How is location, square feet, parking available related to the price of an Airbnb?
- How is hours played and age related to win rate in League of Legends?
- How are creatine and protein consumption related to deadlift 1RM?
- How is treatment (A or B) related to pain levels of patients?

All of these can be answered with regression!

**Exercise 1.1.** What is  $X$  and what is  $Y$  here?

- $X$ : location, square feet, parking available  $Y$ : price of an Airbnb
- $X$ : hours played and age  $Y$ : win rate in League of Legends
- $X$ : creatine and protein consumption  $Y$ : deadlift 1RM
- $X$ : treatment (A or B)  $Y$ : pain levels of patients

We suppose at the population level, **on average** that  $Y = f(X)$ . By on average, we mean that each person may not have exactly  $Y = f(X)$ , but if we average out  $Y$  for many people, we will have that the average is approximately  $f(X)$ . (This will be made more formal later).

For instance, consider the pain level question in the above example. Suppose that  $f(A) = 2$  and  $f(B) = 5$ . Then, if we average the pain level of many patients who take treatment  $B$ , it should be close to 5.

Obviously, we cannot observe the whole population, and so we will assume that we have observed  $X$  and  $Y$  for a set of  $n$  individuals. Specifically, we observe some outcome  $Y_1, \dots, Y_n$ , which is a real number and some attributes (categorical or numeric) about the  $n$  individuals, denoted by  $X_1, \dots, X_n$ . Note that here  $X_i$  can be vectors or single numbers.

### 1.1.2 Using our data, how can we determine $f$ ?

Other, related questions:

- What is the form of  $f$ ? Is it linear?
- How can we estimate  $f$ , say with  $\hat{f}$ ? What is the best  $\hat{f}$ ? What is the error of  $\hat{f}$  on average?
- How can we tell if our model is good? i.e. how does  $\hat{f}$  fit the data?
- How can we tell which  $X$  values are important? How can we tell if  $X$  is related to  $Y$  at all?
- What is the effect of correlation of  $X$  values?

These are all questions we will answer in this course.

Statistical modelling starts as follows:

1. Question about a population, e.g., “How are hours played and age related to win rate in League of Legends?”
2. Data:  $(Y_1, X_1), \dots, (Y_n, X_n)$
3. Explore data with graphs and summary stats
4. Use exploratory data analysis to posit a model for the population.

Note that step 4 is necessary! Letting  $f$  be anything is too general and won’t work well, so we need to use the data to give us a hint at the form of  $f$ ! For instance, we might suppose that  $f$  is a linear function! That is,  $f \in \{g(X) = X\beta: \beta \in \mathbb{R}^d\}$ .

Next, we proceed with the following steps:

5. Estimation: How to get an estimate  $\hat{\beta}$  of  $\beta$ ?
6. Inference: What is the error of  $\hat{\beta}$ ? Is  $f$  degenerate? I.e., is  $\beta = 0$ ?
7. Fit: Does our fitted line match up with the data? What about the normality assumption?  
Do the errors appear normal?
8. Prediction: Predict any values if necessary.

### 1.1.3 Comparison with means example

Let’s compare to what we learned in previous statistics courses about two sample testing with the above steps in mind. Below we have different hours of extra sleep for two different treatments. Let’s see if the sleep for groups 1 and 2 differ.

1. Do the counts for A and B differ?

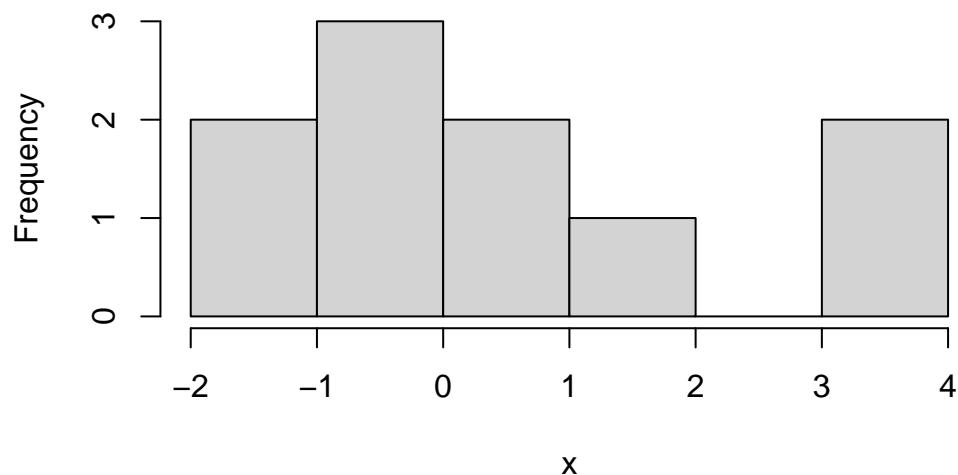
```
# 2.  
data('sleep')
```

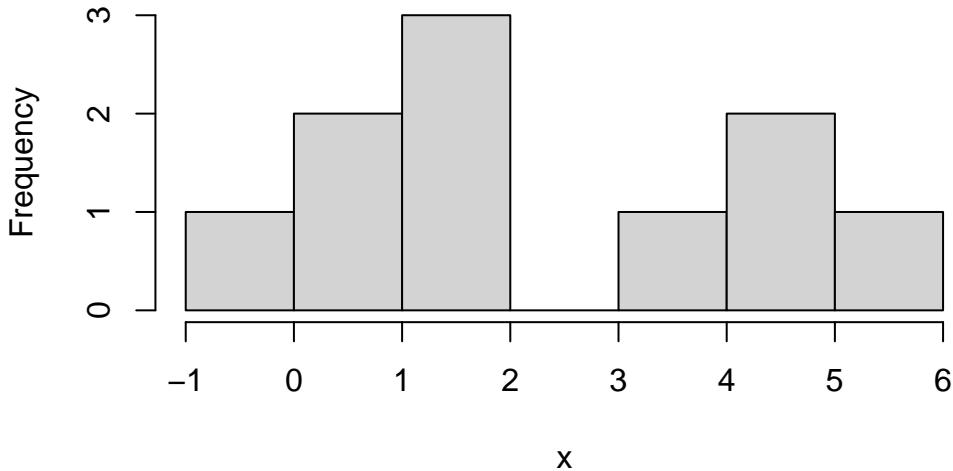
```
head(sleep)
```

```
extra group ID
1   0.7     1   1
2  -1.6     1   2
3  -0.2     1   3
4  -1.2     1   4
5  -0.1     1   5
6   3.4     1   6
```

```
# 3.
```

```
aggregate(extra ~ group, data = sleep, FUN = function(x){hist(x,main=names(x))})
```





```
Warning in format.data.frame(if (omit) x[seq_len(n0), , drop = FALSE] else x, :
corrupt data frame: columns will be truncated or padded with NAs
```

	group	extra
1	1	-2, -1, 0, 1, 2, 3, 4
2	2	-1, 0, 1, 2, 3, 4, 5, 6

```
summary_stats = aggregate(extra ~ group, data = sleep, FUN = summary)
print(summary_stats)
```

	group	extra.Min.	extra.1st Qu.	extra.Median	extra.Mean	extra.3rd Qu.
1	1	-1.600	-0.175	0.350	0.750	1.700
2	2	-0.100	0.875	1.750	2.330	4.150
		extra.Max.				
1		3.700				
2		5.500				

```
aggregate(extra ~ group, data = sleep, FUN = length)
```

```

group extra
1      1    10
2      2    10

```

We will assume that the extra hours are normal from the histograms.

Recall then that the pooled standard deviation is  $\hat{\sigma}_p = \sqrt{((n_x - 1)\hat{\sigma}_x^2 + (n_y - 1)\hat{\sigma}_y^2)/(n_x + n_y - 2)}$  and the test statistic is:

$$T = \frac{\bar{X} - \bar{Y}}{\hat{\sigma}_p \times \sqrt{1/n_x + 1/n_y}}.$$

In addition, we have that  $T \sim t_{n_x + n_y - 2}$ .

```
# 5 and 6 - here these steps are the same, since we are only doing inference
t.test(sleep$extra[sleep$group==1], sleep$extra[sleep$group==2])
```

```

Welch Two Sample t-test

data: sleep$extra[sleep$group == 1] and sleep$extra[sleep$group == 2]
t = -1.8608, df = 17.776, p-value = 0.07939
alternative hypothesis: true difference in means is not equal to 0
95 percent confidence interval:
-3.3654832  0.2054832
sample estimates:
mean of x mean of y
0.75      2.33

```

```
# 7 - we checked normality earlier, 8 is not applicable
```

Here, we fail to reject the null hypothesis, and there is not enough evidence to suggest that there is a difference between the groups. Notice that the p-value is 0.08, which is moderately low, so there is some evidence of a difference between the groups.

## 1.2 Important course information and preparation tasks

### 1.2.1 Prerequisite review

If you have forgotten, you should review the following concepts:

- Sample vs. population, estimates vs. parameters, hypothesis testing and confidence intervals
- Normal theory, random variables, conditional variance and expectation.
- CLT, LLN
- Linear algebra: Matrix operations, inverse, transpose etc.

### 1.2.2 Software

Download RStudio/R. You can use python, but I'll use R in class. If you are not familiar with R, please follow this tutorial [here](#).

### 1.2.3 Outline

The course will proceed as follows:

- Review
- Core linear regression concepts
- Special Cases
- Advanced

### 1.2.4 Homework tasks:

- Download and install RStudio and R Software
- Think of a relationship you would want to model, what is  $X$ ? what is  $Y$ ?
- Review prerequisites as stated above

## 2 Review material

### 2.1 Review of random variables

Recall that

**Definition 2.1.** A random variable  $X$  is a function which maps outcomes  $\omega \in \Omega$  to the real numbers, i.e.,  $X: \Omega \rightarrow \mathbb{R}$ .

**i** Note

Note that the notation  $f: A \rightarrow B$  means that  $f$  is a function whose domain is  $A$  and range is  $B$ . That is,  $f$  takes a value from  $A$  and outputs some value in  $B$ .

Generally, we will just write  $X$ , and ignore the fact that  $X$  is a function.

We can categorize a random variable  $X$  as follows:

- If  $X: \Omega \rightarrow S$  where  $S$  is countable, then  $X$  is a *discrete random variable*
- We say  $X$  is a *continuous random variable* if  $\Pr(X = r) = 0$  for all  $r \in \mathbb{R}$ .
- Otherwise,  $X$  is a *mixed random variable* (which we won't worry about in this course)

#### 2.1.1 Discrete Random Variables

If  $X: \Omega \rightarrow S$  where  $S$  is countable, then  $X$  is a discrete random variable.  $S$  can be finite, but can also be any infinite subset of the integers  $\mathbb{Z}$ . The distribution of  $X$  is given by its PMF, denoted by  $f(x)$ . For any  $x \in S$ ,  $f(x) = \Pr(X = x)$ . (Note that '∈' means the word "in".)

We must have that:

- $\sum_{x \in S} f(x) = 1$ , (This notation means summing over all the elements in  $S$ .)
- $\forall x \in S, 0 \leq f(x) \leq 1$ . (This notation means for all  $x$  in  $S$ ,  $0 \leq f(x) \leq 1$ .)

Examples: Binomial random variables, Poisson random variables and Geometric random variables are all discrete random variables.

**Exercise 2.1.** What is the PMF of a Binomial random variable? Can two different random variables have the same PMF? Why or why not?

First:  $\Pr(X = x) = \binom{n}{x} p^x (1-p)^{n-x}$  Second: Yes. Two random variables can be different random variables, but have the same distribution.

### 2.1.2 Continuous Random Variables

We say  $X$  is a *continuous random variable* if  $\Pr(X = r) = 0$  for all  $r \in \mathbb{R}$ . If  $X: \Omega \rightarrow S$  and  $X$  is a continuous random variable, then  $S$  is typically the real numbers, denoted by  $\mathbb{R}$ , but can be any uncountable subset of  $\mathbb{R}$ . The distribution of  $X$  is given by the PDF  $f(x)$ . For any interval  $(a, b) \subset S$ ,  $\Pr(X \in (a, b)) = \int_a^b f(x) dx$ .

We must have that:

- $\int_{-\infty}^{\infty} f(x) dx = 1$ ,
- $\forall x \in \mathbb{R}, f(x) \geq 0$ .

Examples: Normal random variables, Chi-squared random variables,  $t$  random variables, Cauchy random variables,  $F$  random variables are all continuous random variables. Generally, we will focus on continuous random variables.

**Exercise 2.2.** What is the PMF of a Normal random variable?

$$f(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-(x-\mu)^2/2\sigma^2}$$

### 2.1.3 Properties of Random Variables

Let  $X, X_1, X_2$  be random variables.

Recall the important quantities  $\text{EX}$ ,  $\text{var}X$ ,  $\text{cov}(X_1, X_2)$ ,  $\text{corr}(X_1, X_2)$ . Recall expectation:

**Definition 2.2.** The expectation of a random variable  $X$  is

$$\text{EX} = \sum_{x \in S} x \Pr(X = x),$$

if  $X$  is discrete and is

$$\text{EX} = \int_{-\infty}^{\infty} f(x) dx,$$

if  $X$  is continuous.

This is the “average” value of the random variable. Note that it is possible for it to be impossible for  $X = EX$ . Try to come up with an example of this!

**Definition 2.3.** The variance of a random variable  $X$  is

$$\text{Var}[X] = E[|X - E[X]|^2] = \sum_{x \in S} (x - E[X])^2 \Pr(X = x),$$

if  $X$  is discrete and is

$$\text{Var}[X] = E[|X - E[X]|^2] = \int_{-\infty}^{\infty} (x - E[X])^2 f(x) dx,$$

if  $X$  is continuous.

The variance describes the variation of  $X$  about its mean. In other words, it describes on “average”, how far is  $X$  from its mean.

**Definition 2.4.** The covariance between two random variables  $X$  and  $Y$  is

$$\text{cov}[X, Y] = E[(X - E[X])(Y - E[Y])].$$

The covariance describes the unnormalised linear association between  $X$  and  $Y$ .

**Definition 2.5.** The correlation between two random variables  $X$  and  $Y$  is

$$\text{corr}[X, Y] = \text{cov}[X, Y] / \sqrt{\text{Var}[X] \text{Var}[Y]}.$$

The correlation describes the normalized linear association between  $X$  and  $Y$ .

Next, recall that for a random variable  $X$ , its cumulative distribution function (CDF) is given by  $F_X(x) = \Pr(X \leq x)$ . The joint CDF of  $X$  and  $Y$  is given by  $F_{XY}(x, y) = \Pr(X \leq x, Y \leq y)$ .

Lastly, for a vector of  $d$  random variables  $\mathbf{X} = (X_1, \dots, X_d)$ , let its CDF by  $F_{\mathbf{X}}(\mathbf{x}) = \Pr(X_1 \leq x_1, \dots, X_d \leq x_d)$ , where here  $\mathbf{x} \in \mathbb{R}^d$  and  $\mathbf{x} = (x_1, \dots, x_d)$ .

We next present the concept of independence of random variables. Let  $F_{XY}(x, y)$  be the joint CDF of  $X$  and  $Y$  and let  $F_X$  and  $F_Y$  be the univariate CDFs of  $X$  and  $Y$ , respectively. For two random variables  $X$  and  $Y$ , we say that  $X$  and  $Y$  are independent if  $F_{XY}(x, y) = F_X(x)F_Y(y)$ . More generally, two vectors of random variables  $\mathbf{X}$  and  $\mathbf{Y}$  are independent if  $F_{(\mathbf{X}, \mathbf{Y})}(\mathbf{x}, \mathbf{y}) = F_{\mathbf{X}}(\mathbf{x})F_{\mathbf{Y}}(\mathbf{y})$ , where  $F_{(\mathbf{X}, \mathbf{Y})}$  is the CDF of the vector  $(\mathbf{X}, \mathbf{Y})$ . A set of random variables  $\{X_i\}_{i=1}^n$  are mutually independent if for any two mutually exclusive subsets of  $\{X_i\}_{i=1}^n$  are also independent. Note that we write  $X \perp Y$  if  $X$  is independent of  $Y$ .

We have that:

**Theorem 2.1.** *The following holds:*

- $X_1 \perp X_2 \implies E[X_1 X_2] = E[X_1] E[X_2]$
- $X_1 \perp X_2 \implies \text{corr}[X_1, X_2] = 0$
- $\text{corr}[X_1, X_2] = 0$  does not imply  $X_1 \perp X_2$

**Exercise 2.3.** Prove Theorem 2.1 .

Let  $X, X_1, X_2, \dots, X_n$  be random variables. Recall the linearity of expectation property:

**Theorem 2.2.** *For  $a, b \in \mathbb{R}$ , it holds that  $E[aX + b] = aE[X] + b$ .*

**Exercise 2.4.** Prove Theorem 2.2 .

As a corollary of Theorem 2.2 , we have that

- $E[\sum_{i=1}^n a_i X_i] = \sum_{i=1}^n a_i E[X_i]$
- $\text{Var}[\sum_{i=1}^n a_i X_i] = \sum_{i=1}^n a_i^2 \text{Var}[X_i] + \sum_{i \neq j} a_i a_j \text{cov}[X_i, X_j]$
- $\text{Var}[aX_1 + bX_2 + c] = a^2 \text{var}X_1 + b^2 \text{Var}[X_2] + 2abc \text{cov}[X_1, X_2]$

**Exercise 2.5.** What happens to  $\text{Var}[aX_1 + bX_2 + c]$  when  $\{X_i\}_{i=1}^n$  are mutually independent?

**Exercise 2.6.** Let  $X_1, X_2, \dots, X_n$  be i.i.d. (independent and identically distributed) random variables with expectation (also known as mean)  $\mu$  and variance  $\sigma^2$ . What is the expectation and variance of

$$\bar{X} = \frac{1}{n} \sum_{i=1}^n X_i / n ?.$$

#### 2.1.4 Useful properties of normal and related random variables

Let

- $\mathcal{N}(\mu, \sigma^2)$  represent the normal distribution with mean  $\mu$  and variance  $\sigma^2$ .
- $\chi_k^2$  be the Chi-squared distribution with  $k$  degrees of freedom
- $t_n$  be the student- $t$  distribution with  $n$  degrees of freedom
- $F_{m,n}$  be the  $F$  distribution with  $m$  numerator degrees of freedom and  $n$  denominator degrees of freedom

We have the following results:

**Theorem 2.3.** *Suppose that  $X \sim \mathcal{N}(\mu, \sigma^2)$ , then*

- $Z = \frac{X-\mu}{\sigma} \sim \mathcal{N}(0, 1)$
- $Z^2 \sim \chi_1^2$ .

Let  $[n] = \{1, \dots, n\}$ . We also have that

#### Theorem 2.4.

- If for  $i \in [n]$   $Y_i \sim \chi_{k_i}^2$  and  $Y_i \perp Y_j$  for  $i \neq j$  then  $\sum_{i=1}^n Y_i \sim \chi_{k_1+\dots+k_n}^2$ .
- If  $Y \sim \chi_k^2$  and  $Y \perp Z$ , then  $Z/\sqrt{Y/k} \sim t_k$ .
- If  $Y_1 \sim \chi_{k_1}^2$ ,  $Y_2 \sim \chi_{k_2}^2$  and  $Y_1 \perp Y_2$  then  $\frac{Y_1/k_1}{Y_2/k_2} \sim F_{k_1, k_2}$ .

Define

$$\hat{\sigma}^2 = \frac{1}{n-1} \sum_{i=1}^n (X_i - \bar{X})^2.$$

**Theorem 2.5.** Suppose that  $X_1, X_2, \dots, X_n \sim \mathcal{N}(\mu, \sigma^2)$  and are independent, then  $\frac{\bar{X}-\mu}{\sigma/\sqrt{n}} \sim \mathcal{N}(0, 1)$ ,  $\bar{X} \perp \hat{\sigma}^2$ ,  $(n-1)\hat{\sigma}^2/\sigma^2 \sim \chi_{n-1}^2$  and  $\frac{\bar{X}-\mu}{\hat{\sigma}/\sqrt{n}} \sim t_{n-1}$ .

#### 2.1.5 Central Limit Theorem

**CLT:** If  $X_1, X_2, \dots, X_n$  are i.i.d. with mean  $\mu$  and variance  $\sigma^2 < \infty$ , then  $\frac{\bar{X}-\mu}{\sigma/\sqrt{n}} \xrightarrow{d} \mathcal{N}(0, 1)$  as  $n \rightarrow \infty$ .

We have that in general, for large  $n$ , regardless of the distribution of the random variables, the sample mean is approximately normally distributed.

#### 2.1.6 Homework stop 1

Review your material and complete the above exercises before continuing to the next section.

## 2.2 Review of introductory statistics

The followings are some concepts that you have learned from prerequisites, and/or we have reviewed in the last two lectures.

- Sample vs. Population
- Observation vs. Random variable
- Statistic vs. Parameter
- Estimate vs. Estimator

- Estimator is a random variable and estimate is a number calculated from data
- Mean and variance of random variable
- Relationships between Normal,  $t$ ,  $\chi^2$ ,  $F$  etc.

### 2.2.1 Basic premise of statistics

The whole purpose of statistics is to learn something about a population using only a sample of units from that population. A **sample** is a smaller, typically randomly selected, subset of a population. A **population** is a collection of units which we would like to know something about. For example, we may collect a sample of hamburgers from McDonald's if we want to learn something about the population of McDonald's hamburgers.

In general, at least for this course, we assume that we have access to a sample of units from a given population. Furthermore, we assume that that sample is a **random sample**. Specifically, we assume that these units in the sample are realizations of random variables. In addition, we also assume that these random variables are mutually independent. For example, we could assume that our sample  $X_1, \dots, X_n$  is Normally distributed with some fixed mean  $\mu$  and fixed variance  $\sigma^2$ . In this case,  $\mu$  and  $\sigma^2$  are unknown **parameters** of the population. A parameter of a population is some quantity that is a function of the distribution of our given sample. For instance,  $E[X_i] = \mu$ . Generally, we are concerned with unknown population parameters, which are parts of the distribution that are unknown, and can only ever be estimated. For example, we may know our data is normal, but not know the mean parameter. In that case, we need to use an **estimate** of the parameter. We use a function of the data, typically called the estimator, say  $T$ , which produces the estimate, given by  $T$  computed at the sample we observed:  $T(X_1, \dots, X_n)$ .

For example, to estimate  $\mu$ , we typically use the sample mean. Here, the estimate is given by  $\bar{X} = \sum_{i=1}^n X_i/n$ . To be specific, the estimate is the value of  $\bar{X}$  and the estimator  $T$  is the function that maps  $n$  real numbers to their mean. In general, estimates are used to give our ‘best guess’ at population parameters.

### 2.2.2 Confidence intervals

Recall from the previous section that our estimate of a parameter is only that, an estimate. In other words, it is not exactly equal to the population parameter. For instance, if we drew a different sample our estimate would change. A confidence interval is used to acknowledge this phenomenon in the reporting of our statistics. Its used to give a range of estimates that we might have obtained from any “regular” sample we might observe. It is ultimately used to quantify the error (sometimes called uncertainty) in our estimate.

Confidence intervals consist of a level, usually denoted by  $(1 - \alpha)100\%$  and two end points. For example, you have learned confidence intervals for the population mean. When we say  $(-1, 1)$  is 95% confidence interval for the population mean, what does this mean? Colloquially,

it means that we expect the sample mean to be somewhere within  $(-1, 1)$  with high confidence. Note that confidence intervals are computed from the data, which means also that for each new sample, we would get a different confidence interval. However, the population parameter never changes. Therefore, the interval is what is varying from sample to sample. This impacts the interpretation of a confidence interval.

Continuing our example, we have that the interval  $(-1, 1)$  can be interpreted as: “if we drew many more samples, 95% of the **intervals** will contain the population parameter.” We **do not** say that the parameter has a 95% chance of falling in  $(-1, 1)$ , since the parameter is not random, the interval end points are.

For example, we have the formula for a confidence interval for the population mean is given by:  $\bar{X} \pm 1.96\hat{\sigma}$ . Notice that it is based only on the data. Therefore, it will change if we drew a new sample.

To summarize this section, a confidence interval is used to quantify the uncertainty in our reported estimates. By uncertainty, we specifically mean the uncertainty resulting from the fact that we have only a sample of the population, and our estimate varies depending on the sample.

### 2.2.3 Hypothesis tests

Hypothesis tests are used to determine whether an effect is spurious or a real property of the population. A spurious effect is one that is specific to the sample we observed, and is not a real property of the population. For example, if the heights of males and female students are measured, and we observe that the sample mean of both male and females are equal, then this would be a spurious effect. We know that the population heights of males and females are substantially different. If we drew a new sample, we would likely observe something that mirrors the population reality (provided it is large enough).

Formally, a hypothesis test compares two competing beliefs about a population parameter, called the null and alternative hypothesis. For instance, we may wish to test whether the population heights of men is greater than women, vs. the heights being less than or equal to that of men.

We write this as follows:  $H_0: \mu_{men} \leq \mu_{women}$  vs.  $H_a: \mu_{men} > \mu_{women}$ .

The null hypothesis is usually chosen to be one such that if we make a mistake, the error is most serious. However, it is usually clear from the context.

In general, we compute a test statistic and its distribution **under the null hypothesis**. Then we compute how likely it was to see the observed test statistic we saw, if the null hypothesis was true. This likelihood is given by the **p-value**. If it was sufficiently unlikely (in other words, the p-value is less than the threshold  $\alpha$ ), then we reject the null hypothesis. Otherwise, we

fail to reject the null hypothesis. If we fail to reject the null hypothesis then either the null hypothesis is true, it is not true, but there was not enough data collected to show the effect.

There are two types of errors we can make in a hypothesis test: Type 1 and Type 2 error. Type one error occurs when we reject the null hypothesis when it is true. Type two error occurs when we fail to reject the null hypothesis when the alternative is true.

Let's do an example.

**Exercise 2.7.** In a study about online dating, you are interested in determining the average age of individuals who use online dating platforms. You want to know whether the average age of online daters is significantly different from 30. You have a dataset of 40 ages of people using online dating platforms.

How would you answer this question?

$$H_0: \mu = 30 \quad vs. \quad H_1: \mu \neq 30.$$

First, we can explore the data:

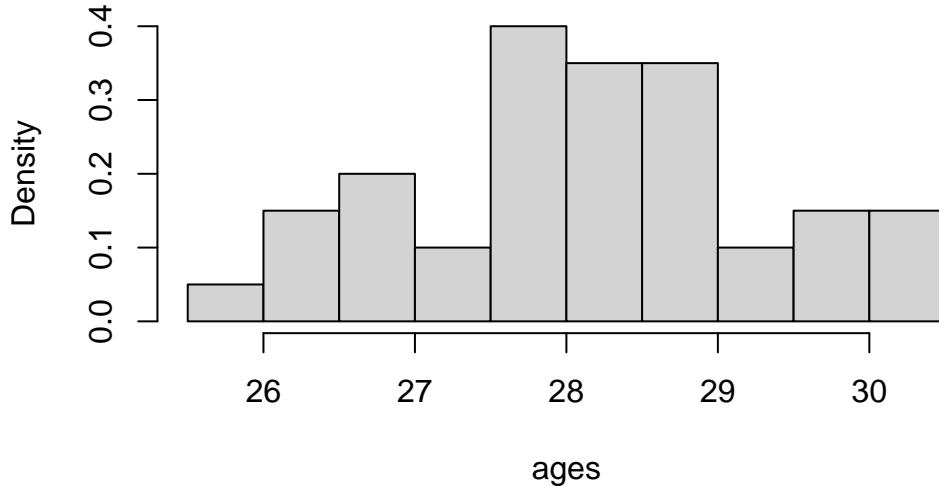
```
getwd()
```

```
[1] "C:/Users/12RAM/OneDrive - York University/Teaching/Courses/Math 3330 Regression/Math 3330
```

```
ages=read.csv('C:\\\\Users\\\\12RAM\\\\OneDrive - York University\\\\Teaching\\\\Courses\\\\Math 3330
```

```
hist(ages,freq=F)
```

## Histogram of ages



Now, assume that  $X_1, \dots, X_{40} \sim \mathcal{N}(\mu, \sigma^2)$ , and independent. (We can justify normality with the histogram, or we could also invoke the CLT to get normality of the sample mean (not the data itself).) Therefore, we can do a one sample  $t$ -test. Recall that, under the null hypothesis, we have  $\frac{\bar{X}-30}{\hat{\sigma}/\sqrt{n}} \sim t_{n-1}$ . This means that if  $\left| \frac{\bar{X}-30}{\hat{\sigma}/\sqrt{n}} \right| \geq t_{n-1, 1-\alpha/2}$ , then we reject the null hypothesis! Here,  $t_{n-1, 1-p}$  is the  $(1-p)$ th quantile of the  $t_{n-1}$  distribution. For large  $n$  and  $p = 0.025$ , this is roughly equal to 2.

Now, recall that

$$H_0: \mu = 30 \quad vs. \quad H_1: \mu \neq 30.$$

```
# Calculate the mean of the 'ages' data and assign it to xbar
xbar = mean(ages)
xbar # Print the mean
```

[1] 28.16378

```
# Calculate the variance of the 'ages' data and assign it to ssq
ssq = var(ages)
ssq # Print the variance
```

[1] 1.277377

```
# Calculate the length (number of observations) of the 'ages' data and assign it to n
n = length(ages)
n # Print the number of observations
```

```
[1] 40
```

```
# Set the significance level
alpha = 0.05

# print test statistic
ts=(xbar -30)/(sqrt(ssq/n))
print(ts)
```

```
[1] -10.27532
```

```
# compute p-value
pval=pt(ts,n-1)*2
pval
```

```
[1] 1.179149e-12
```

```
# Perform a two-sided t-test to check if the mean of 'ages' is significantly different from 30
# t.test() is the function for performing t-tests in R
test = t.test(ages, mu = 30, alternative = 'two.sided')
test # Print the test result
```

One Sample t-test

```
data: ages
t = -10.275, df = 39, p-value = 1.179e-12
alternative hypothesis: true mean is not equal to 30
95 percent confidence interval:
27.80232 28.52524
sample estimates:
mean of x
28.16378
```

We have that  $\left| \frac{\bar{X} - 30}{\hat{\sigma}/\sqrt{n}} \right| = -10.28$ . Using R, we get that the p-value is  $1.179 \times 10^{-12}$ .

Here the p-value measures how much evidence there is against the null hypothesis. If the p-value is very small, then this constitutes strong evidence against the null hypothesis. If the p-value is small, but closer to 0.05, then there is evidence against the null. If it is larger, but still small, say 0.1, then this is weak evidence against the null hypothesis. It is not helpful to throw it away if it is above 0.05, therefore we should not just take  $\alpha = 0.05$ . Choosing  $\alpha$  depends on how serious a type 1 error is. If it is not that serious, we can take  $\alpha$  larger. If it is very serious, we can take  $\alpha$  smaller.

In this example, there is very strong evidence against the null hypothesis.

### **i** Note

Note also that we can use the confidence interval method with

$$\bar{X} \pm t_{n-1, 1-\alpha/2} \sqrt{\hat{\sigma}^2/n}.$$

```
# Alternative method to calculate the confidence interval
# ci will store the confidence interval values
ci = xbar + c(-1, 1) * qt(1 - alpha / 2, n - 1) * sqrt(ssq / n)
ci # Print the confidence interval
```

[1] 27.80232 28.52524

### **i** Note

Moving beyond the one-sample testing problem, we might be interested in other population parameters, say  $\theta \in \Theta$ . Think Lecture 1:  $E[Y|X] = \beta_0 + X\beta_1$ , we might want to estimate  $E[Y|X]$ , which amounts to  $\beta_0, \beta_1 \in \mathbb{R}$ . In general, we may estimate  $\theta$  by  $\hat{\theta}$ . Then we may compute the variance and distribution of  $\hat{\theta}$ . From there, we can make confidence intervals and conduct hypothesis tests etc.

Let's do another example:

**Exercise 2.8.** In a study about online dating, you are interested in determining if the average age of those who identify as men who use online dating platforms differs from those who identify as women. You have a dataset of 20 ages of each group using online dating platforms.

What is the population parameter of interest here? It is  $\Delta = \mu_1 - \mu_2$ , the difference in means between the two populations. Now, suppose that  $X_1, \dots, X_{20} \sim \mathcal{N}(\mu_1, \sigma^2)$  and  $Y_1, \dots, Y_{20} \sim$

$\mathcal{N}(\mu_2, \sigma^2)$ , and are mutually independent. (We could also invoke the CLT instead of assuming normality.) We can estimate those parameters with **estimates**. For instance,  $\bar{X}$ ,  $\bar{Y}$ ,

$$\hat{\sigma}^2 = \frac{(n_1 - 1)\hat{\sigma}_1^2 + (n_2 - 1)\hat{\sigma}_2^2}{n_1 + n_2 - 2}.$$

**Exercise 2.9.** Suppose that  $X_1, \dots, X_{20} \sim \mathcal{N}(\mu_1, \sigma^2)$  and  $Y_1, \dots, Y_{20} \sim \mathcal{N}(\mu_2, \sigma^2)$ , and are mutually independent. Compute  $\text{Var}[\bar{X} - \bar{Y}]$ .

Using independence of  $\bar{X}$  and  $\bar{Y}$  and the result of the Exercise 2.6 , we have that

$$\text{Var}[\bar{X} - \bar{Y}] = \text{Var}[\bar{X}] + \text{Var}[\bar{Y}] = \sigma_1^2/n_1 + \sigma_2^2/n_2.$$

First, we write down the null and alternative hypothesis:

$$H_0: \Delta = 0 \quad \text{vs..} \quad H_1: \Delta \neq 0.$$

Here, we can do a two sample  $t$ -test.

Recall that the pooled variance is given by:

$$\hat{\sigma}_p^2 = \frac{(n_1 - 1)\hat{\sigma}_1^2 + (n_2 - 1)\hat{\sigma}_2^2}{(n_1 + n_2 - 2)}$$

We previously said that a multiple of a one sample standard deviation follows a Chi-squared distribution. It follows that  $(n_1 - 1)\hat{\sigma}_1^2/\sigma^2 \sim \chi_{n_1-1}^2$  and  $(n_2 - 1)\hat{\sigma}_2^2/\sigma^2 \sim \chi_{n_2-1}^2$ . Using the theory from [here](#), specifically,  $(n_1 - 1)\hat{\sigma}_1^2/\sigma^2 + (n_2 - 1)\hat{\sigma}_2^2/\sigma^2$  is a sum of independent Chi-squared random variables, and so we have  $(n_1 - 1)\hat{\sigma}_1^2/\sigma^2 + (n_2 - 1)\hat{\sigma}_2^2/\sigma^2 \sim \chi_{n_1+n_2-2}^2$ .

Again, using the theory from [here](#), under the null hypothesis, we have that

$$\frac{\bar{X} - \bar{Y}}{\hat{\sigma}_p \sqrt{1/n_1 + 1/n_2}} = \frac{(\bar{X} - \bar{Y})/\sigma \sqrt{1/n_1 + 1/n_2}}{\hat{\sigma}_p/\sigma} \sim t_{n_1+n_2-2}.$$

This follows from 3 facts, first, letting  $Z = (\bar{X} - \bar{Y})/\sqrt{\text{Var}[\bar{X} - \bar{Y}]}$ , note that  $Z \sim \mathcal{N}(0, 1)$ . We have that

$$Z = (\bar{X} - \bar{Y})/\sqrt{\text{Var}[\bar{X} - \bar{Y}]} = (\bar{X} - \bar{Y})/\sigma \sqrt{1/n_1 + 1/n_2}.$$

Next, we said earlier that  $\bar{X}$  is independent of  $\hat{\sigma}_1$  and  $\bar{Y}$  is independent of  $\hat{\sigma}_2$ . Now, recall that if two random variables are independent, then any function of them is also independent. In other words, if  $X$  and  $Y$  are independent, then for real functions  $f$  and  $g$ , we have that  $g(X)$

is independent of  $f(Y)$ . It follows that  $\bar{X}$  is independent of  $\hat{\sigma}_2$  and  $\bar{Y}$  is independent of  $\hat{\sigma}_1$ . It follows that  $\bar{X} - \bar{Y}$  is independent of  $\hat{\sigma}_p$ . Then,

$$\frac{(\bar{X} - \bar{Y})/\sigma\sqrt{1/n_1 + 1/n_2}}{\hat{\sigma}_p/\sigma}$$

is a ratio of a standard normal random variable and the square root of a Chi-squared random variable, divided by its degrees of freedom. Further, the numerator and denominator are independent. Therefore, the above quantity follows a  $t$  distribution with  $n_1 + n_2 - 2$  degrees of freedom.

This means that if  $\left| \frac{\bar{X} - \bar{Y}}{\hat{\sigma}_p\sqrt{1/n_1 + 1/n_2}} \right| \geq t_{n_1+n_2-2, 1-\alpha/2}$ , then we reject the null hypothesis.

Let's execute the test in R:

```
# Normally, I will give you a dataset. Here I generate the data
set.seed(440)
female_ages=rnorm(20,28,4)
male_ages=rnorm(20,32,4)
```

```
# Check for equal variance
var(female_ages)
```

```
[1] 15.72805
```

```
var(male_ages)
```

```
[1] 26.22371
```

```
## Putting the data in a dataframe
cbind("Age"=c(female_ages,male_ages),"Gender"=rep(c(0,1),each=20))
```

	Age	Gender
[1,]	37.19809	0
[2,]	20.69693	0
[3,]	27.80284	0
[4,]	27.69463	0
[5,]	29.53143	0

```

[6,] 29.46190      0
[7,] 30.41164      0
[8,] 33.27790      0
[9,] 22.65974      0
[10,] 30.73540     0
[11,] 34.08564     0
[12,] 27.58077     0
[13,] 23.26108     0
[14,] 30.94523     0
[15,] 31.52404     0
[16,] 29.13246     0
[17,] 26.95470     0
[18,] 24.80749     0
[19,] 28.60051     0
[20,] 26.76294     0
[21,] 25.94775     1
[22,] 40.16080     1
[23,] 25.58905     1
[24,] 32.16780     1
[25,] 29.87934     1
[26,] 35.46593     1
[27,] 35.71651     1
[28,] 37.76510     1
[29,] 27.23068     1
[30,] 33.41994     1
[31,] 40.43822     1
[32,] 31.04841     1
[33,] 32.66165     1
[34,] 38.28678     1
[35,] 34.72411     1
[36,] 39.57994     1
[37,] 26.85585     1
[38,] 31.87533     1
[39,] 23.71793     1
[40,] 30.54803     1

```

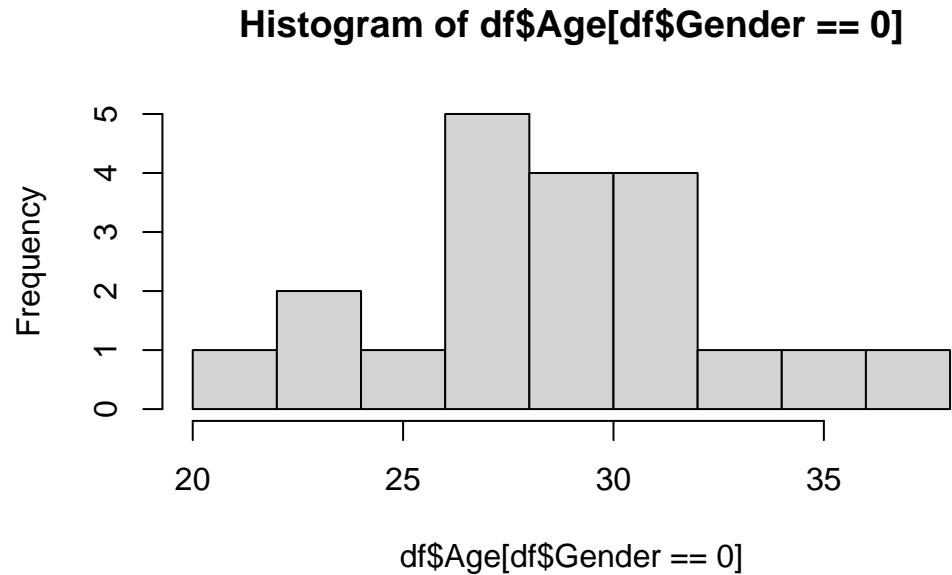
```

df=data.frame(cbind("Age"=c(female_ages,male_ages),"Gender"=rep(c(0,1),each=20)))

#exploring the data
#hist(x) creates a histogram of the vector x

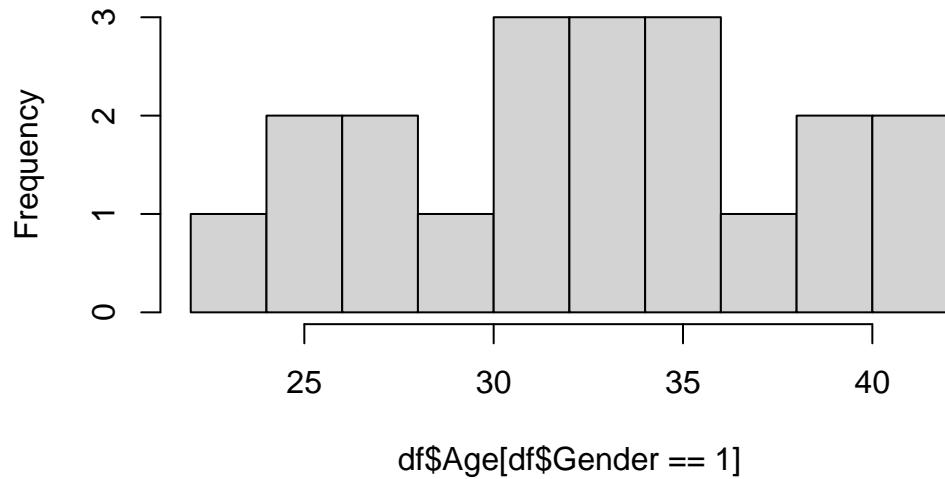
```

```
hist(df$Age [df$Gender==0])
```

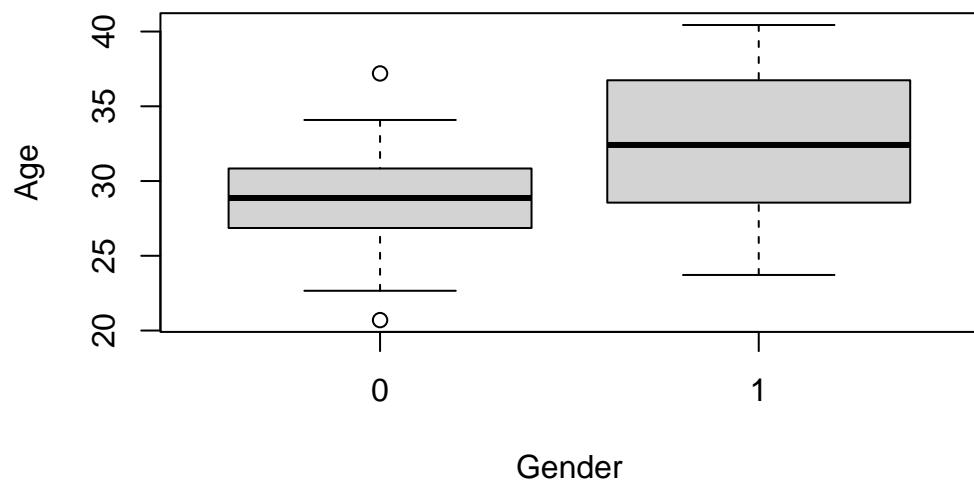


```
hist(df$Age [df$Gender==1])
```

Histogram of df\$Age[df\$Gender == 1]



```
#boxplot creates boxplots of Age against gender  
boxplot(Age~Gender, df)
```



```
test=t.t.test(Age~Gender,data=df,var.equal=TRUE)
test
```

Two Sample t-test

```
data: Age by Gender
t = -2.7603, df = 38, p-value = 0.008841
alternative hypothesis: true difference in means between group 0 and group 1 is not equal to
95 percent confidence interval:
-6.929630 -1.065749
sample estimates:
mean in group 0 mean in group 1
28.65627      32.65396
```

#Interpret the P value, and CI, what are we going to say to a stakeholder?

```
#e.g.
test$estimate
```

```
mean in group 0 mean in group 1
28.65627      32.65396
```

### i Note

Note also that we can use the confidence interval method, meaning that if 0 is in the interval:

$$\hat{\Delta} \pm t_{n_1+n_2-2,1-\alpha/2} \hat{\sigma}_p \sqrt{1/n_1 + 1/n_2},$$

then we fail to reject the null hypothesis.

## 2.2.4 Homework stop 2

**Exercise 2.10.** IBM Human Resources (HR) department is evaluating job applicants from York University.

They are interested to know if the 2020 ITEC graduating class has an average GPA higher than 6 (i.e. average GPA higher than “B’’). They collected the GPA of 25 ITEC students graduated in 2020.

4.92	4.79	6.76	5.64	6.12	7.37	6.45	6.31	6.68
6.30	4.91	6.95	5.87	6.18	6.60	6.71	6.69	5.62
6.40	5.51	6.44	6.13	8.55	7.94	4.78	-	-

💡 Tip

Use chatGPT to convert the above table to an R vector, so you don't have to waste time!

- For the one sample testing problem, i.e., you have a sample of  $n$  normal random variables, with unknown mean and variance and you want to test whether  $H_0: \mu = 0$  vs.  $H_1: \mu \neq 0$ , show that  $\frac{\bar{X}}{\hat{\sigma}/\sqrt{n}} \sim t_{n-1}$  under the null hypothesis.
- What is the distribution of each of the following:  $\bar{X}, \bar{Y}, \hat{\sigma}$  under the assumption of normal data with unknown mean and variance?

Compare and contrast the following concepts. That is, define them and explain the difference between them.

- Sample vs. Population
- Observation vs. Random variable
- Statistic vs. Parameter
- Estimate vs. Estimator

## 2.3 Review of matrices and linear algebra

Recall that

**Definition 2.6.** An  $(n \times m)$  matrix  $A$  takes the form

$$\begin{aligned} A &= \begin{pmatrix} a_{11} & a_{12} & \cdots & a_{1m} \\ a_{21} & a_{22} & \cdots & a_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ a_{n1} & a_{n2} & \cdots & a_{nm} \end{pmatrix} \\ &= ((a_{ij})) \quad i = 1, \dots, n, \quad j = 1, \dots, m \end{aligned}$$

and  $a_{ij}$  is the element in the  $i^{th}$  row and  $j^{th}$  column of the matrix  $A$

We also define the following:

- An  $(n \times 1)$  matrix is also known as a  $n$  dimensional column vector. Note: in this course, a vector means a column vector.

- A  $(1 \times m)$  matrix is also known as a  $m$  dimensional row vector
- The  $n$  dimensional one vector,  $1_n$ , (sometimes the subscript  $n$  is suppressed when the dimension is obvious), is an  $n$  dimensional column vector with all entries being 1.
- The  $(n \times n)$  identity matrix,  $I_n$ , is the  $(n \times n)$  matrix with diagonal entries set equal to 1 and the off diagonal entries set equal to 0

Throughout this section, we will use the following matrices to demonstrate the numerical calculations:

$$U = \begin{pmatrix} 1 & 2 & 3 \\ -1 & 4 & -2 \end{pmatrix}, V = \begin{pmatrix} 2 & 4 \\ 1 & -2 \\ -1 & 0 \end{pmatrix}, k = 4$$

### 2.3.1 Matrix properties

First, we define the transpose of a matrix:

**Definition 2.7.** Let  $A = ((a_{ij}))$  for  $i = 1, \dots, n$  and  $j = 1, \dots, m$ , is an  $(n \times m)$  matrix. Then  $A^\top = A$  transpose  $= ((a_{ji}))$  for  $j = 1, \dots, m$  and  $i = 1, \dots, n$ , and  $A^\top$  is an  $(m \times n)$  matrix.

When we transpose a matrix  $A$ , the rows of  $A$  becomes the columns of  $A^\top$  and the columns of  $A$  becomes the rows of  $A^\top$ .

**Example 2.1.** Using our example matrices, we have that

$$U^\top = \begin{pmatrix} 1 & -1 \\ 2 & 4 \\ 3 & -2 \end{pmatrix}, V^\top = \begin{pmatrix} 2 & 1 & -1 \\ 4 & -2 & 0 \end{pmatrix}$$

**Definition 2.8.** Let  $A = ((a_{ij}))$  and  $B = ((b_{ij}))$  be two  $(n \times m)$  matrices. Then

$$A \pm B = ((a_{ij} \pm b_{ij})).$$

Addition and subtraction of matrices required the matrices to have the same dimension.

**Example 2.2.** Using our example matrices, we have that:  $U + V$  is undefined because they are not of the same dimension, and

$$U + V^\top = \begin{pmatrix} 1+2 & 2+1 & 3+(-1) \\ (-1)+4 & 4+(-2) & (-2)+0 \end{pmatrix} = \begin{pmatrix} 3 & 3 & 3 \\ 3 & 2 & -2 \end{pmatrix}$$

**Definition 2.9.** Let  $A = ((a_{ij}))$  for  $i = 1, \dots, n$  and  $j = 1, \dots, m$ , is an  $(n \times m)$  matrix and  $k$  is a constant. Then

$$kA = ((ka_{ij})) = Ak,$$

i.e. each element of the matrix  $A$  is multiplied by  $k$ .

**Example 2.3.** Using our example matrices, we have that:

$$kU^\top = 4 \begin{pmatrix} 1 & -1 \\ 2 & 4 \\ 3 & -2 \end{pmatrix} = \begin{pmatrix} 4(1) & 4(-1) \\ 4(2) & 4(4) \\ 4(3) & 4(-2) \end{pmatrix} = \begin{pmatrix} 4 & -4 \\ 8 & 8 \\ 12 & -2 \end{pmatrix}$$

**Definition 2.10.** Let  $A$  and  $B$  be two matrices. Then  $A$  multiplied by  $B$ ,  $AB$ , is defined only if (number of columns of  $A$ ) = (number of rows of  $B$ ).

The product is a ( (number of rows of  $A$ )  $\times$  (number of columns of  $B$ ) ) matrix.

More precisely, let  $A = ((a_{ij}))$  be an  $(n \times m)$  matrix and  $B = ((b_{ij}))$  be an  $(m \times p)$  matrix. Then  $C = AB = ((c_{ij}))$  is an  $(n \times p)$  matrix with

$$c_{ij} = a_{i1}b_{1j} + a_{i2}b_{2j} + \cdots + a_{im}b_{mj}$$

**i Note**

In matrix algebra,  $AB$  is not necessarily equal to  $BA$ .

**Example 2.4.** Using our example matrices, we have that:

$$\begin{aligned} UV &= \begin{pmatrix} 1 & 2 & 3 \\ -1 & 4 & -2 \end{pmatrix} \begin{pmatrix} 2 & 4 \\ 1 & -2 \\ -1 & 0 \end{pmatrix} \\ &= \begin{pmatrix} 1(2) + 2(1) + 3(-1) & 1(4) + 2(-2) + 3(0) \\ (-1)(2) + 4(1) + (-2)(-1) & (-1)(4) + 4(-2) + (-2)(0) \end{pmatrix} \\ &= \begin{pmatrix} 1 & 0 \\ 4 & -12 \end{pmatrix} \end{aligned}$$

Assume all the matrix multiplication works. Let  $I_n$  be an  $(n \times n)$  identity matrix. Then

$$AI_n = A, \quad \text{and} \quad I_nB = B.$$

**Definition 2.11.** Let  $A$  be an  $(n \times n)$  matrix. The inverse of  $A$ ,  $A^{-1}$ , if exists satisfies

$$AA^{-1} = A^{-1}A = I_n$$

and if  $A^{-1}$  does not exist, then  $A$  is a singular matrix.

### ! Important

From your linear algebra course, a prerequisite, you have learned the condition(s) for the existence of an inverse, [The Invertible Matrix Theorem](#) and you have learned how to obtain an inverse. You should review them.

Specifically, you should know how to obtain inverse of any diagonal matrix and any  $(2 \times 2)$  non-singular matrix, i.e.,

$$\begin{pmatrix} a & b \\ c & d \end{pmatrix}^{-1} = \frac{1}{ad - bc} \begin{pmatrix} d & -b \\ -c & a \end{pmatrix}.$$

**Example 2.5.** Using our example matrices, let

$$W = UV = \begin{pmatrix} 1 & 0 \\ 4 & -12 \end{pmatrix}$$

Then

$$W^{-1} = \frac{1}{1(-12) - 0(4)} \begin{pmatrix} -12 & 0 \\ -4 & 1 \end{pmatrix} = \begin{pmatrix} 1 & 0 \\ 1/3 & -1/12 \end{pmatrix}.$$

You can verify that  $WW^{-1} = W^{-1}W = I_2$ .

### 2.3.2 Important identities

Lastly, we introduce some important identities:

$$X = \begin{pmatrix} 1 & x_1 \\ \vdots & \vdots \\ 1 & x_n \end{pmatrix}, \quad \text{and} \quad y = \begin{pmatrix} y_1 \\ \vdots \\ y_n \end{pmatrix}$$

Then

$$X^\top X = \begin{pmatrix} n & \sum_{i=1}^n x_i \\ \sum_{i=1}^n x_i & \sum_{i=1}^n x_i^2 \end{pmatrix}, \quad \text{and} \quad X^\top y = \begin{pmatrix} \sum_{i=1}^n y_i \\ \sum_{i=1}^n x_i y_i \end{pmatrix}.$$

Also  $\bar{y} = \frac{1}{n} 1^\top y$  and  $\sum_{i=1}^n y_i = n\bar{y}$  and, finally  $\sum_{i=1}^n (y_i - \bar{y})^2 = \sum_{i=1}^n y_i^2 - n\bar{y}^2$ . These are useful identities that we will use throughout this course.

**Exercise 2.11.** Prove the previously introduced identities.

Lastly, we recall an important application of matrices. An application of matrices: Suppose that we want to solve for  $x_1, x_2, x_3$  where they satisfy the following set of linear equations:

$$\begin{aligned}
2x_1 + 3x_2 - 4x_3 &= 0 \\
-x_1 + 4x_2 &= -1 \\
5x_1 + x_2 - 2x_3 &= 4
\end{aligned}$$

We can set it up in matrix form as follows:

$$\begin{pmatrix} 2 & 3 & -4 \\ -1 & 4 & 0 \\ 5 & 1 & -2 \end{pmatrix} \begin{pmatrix} x_1 \\ x_2 \\ x_3 \end{pmatrix} = \begin{pmatrix} 0 \\ -1 \\ 4 \end{pmatrix}$$

Or it can be presented as  $Ax = b$ . If  $A$  is not a singular matrix, then  $x = A^{-1}b$ . Since  $\det(A) = 62$ , it is not a singular matrix. Solving the above equation this using  $x = A^{-1}b$  yields that  $x = (1, 0, 0.5)^\top$ . Keep this in mind, we will see it return in the next chapter.

Lastly - I will remind you of two definitions:

**Definition 2.12.** A set of vectors  $v_1, \dots, v_d$  is linearly independent if the only  $d$ -dimensional set of scalars  $a_1, \dots, a_d \in \mathbb{R}$  such that  $\sum_{i=1}^d a_i v_i = 0$  implies is the  $d$ -dimensional 0 vector.

**Definition 2.13.** A  $d \times d$  symmetric matrix  $A$  is positive-definite if for all  $x \in \mathbb{R}^d \setminus \{0\}$  it holds that  $x^\top A x > 0$ .

### 2.3.3 Homework stop 3

**Exercise 2.12.** Let

$$W = \begin{pmatrix} 3 & 2 \\ -4 & 6 \end{pmatrix}$$

and  $x = (2, 1)^\top$ . Compute  $W^{-1}$ ,  $xx^\top$  and  $x^\top W$ . Verify that  $WW^{-1} = W^{-1}W = I_2$ .

- Prove each of the **important identities**.
- Verify  $X^\top A = (A^\top X)^\top$ .
- What is the rank of a matrix? Is a matrix's rank related to whether or not a matrix is invertible? Why?
- Define a positive definite matrix. When is  $X^\top X$  positive definite?

## 2.4 Review Random Vectors

### 2.4.1 Definition of random vectors

**Definition 2.14.** Let  $Y_1, \dots, Y_n$  be random variables. Then

$$Y = \begin{pmatrix} Y_1 \\ \vdots \\ Y_n \end{pmatrix}$$

is an  $n$ -dimensional random vector.

Similar to a random variable, a random vector also comes with a probability mass function (if all the  $Y_i$  are discrete) or a probability density function (if all the  $Y_i$  are continuous), or a “mixture” distribution (if some  $Y_i$  are discrete and others are continuous). In general, a random vector is drawn from a multivariate distribution, defined by the PMF or PDF. Just as before, the PMF and PDF range is non-negative, the PMF sums to 1 over all outcomes, and the PDF integrates to 1 over  $\mathbb{R}^n$ . One discrete multivariate distribution you have learned in 1131 is the Multinomial distribution. We will learn about the multivariate normal distribution soon.

### 2.4.2 Expected Value and Covariance

**Definition 2.15.** Let  $Y$  be an  $n$ -dimensional random vector, then the mean (expected value) of  $Y$  is defined as

$$\mathbf{E}(Y) = \begin{pmatrix} \mathbf{E}(Y_1) \\ \vdots \\ \mathbf{E}(Y_n) \end{pmatrix} = \mu$$

and the covariance matrix of  $Y$  is defined as

$$\text{cov}[Y] = \mathbf{E}[(Y - \mu)(Y - \mu)^\top] = ((\text{cov}[Y_i, Y_j])) = \Sigma.$$

Sometimes  $\text{cov}[Y]$  is written as  $\text{Var}[Y]$ .

The following are some facts about  $\Sigma$ :

$\Sigma$  is an  $n \times n$  matrix with the diagonal elements being the variances,  $\text{Var}[Y_i]$  for  $i = 1, \dots, n$ ,

and the off-diagonal elements being the covariances,  $\text{cov}[Y_i, Y_j]$  for  $i, j = 1, \dots, n$  and  $i \neq j$ .

$\Sigma$  is a symmetric, non-negative definite matrix. In this course, we further restrict it to be a positive definite matrix.  $\Sigma$  is referred to as the **covariance matrix**.

### 2.4.3 Properties of expected value and covariance

Let  $X, Y \in \mathbb{R}^d$  be random vectors with  $A \in \mathbb{R}^d$  and  $B \in \mathbb{R}^{n \times d}$  be matrices. It holds that

- $E(X + Y) = E(X) + E(Y)$
- $E(A + BY) = A + BE(Y)$
- $\text{cov}[A + BY] = B\text{cov}[Y]B^\top$ .

**Exercise 2.13.** Let  $Y = (Y_1, \dots, Y_n)^\top$  be a random vector, where  $Y_i$  are i.i.d. random variables with mean  $\mu$  and variance  $\sigma^2$ . What are the mean and covariance of  $Y$ ? Use properties of random vectors to compute the mean and variance of the sample mean.

First,  $E(Y) = \mu 1$  and  $\text{cov}[Y] = \sigma^2 I$ . Note that  $\bar{Y} = (Y_1 + \dots + Y_n)/n = \frac{1}{n} 1^\top Y$ . Now, we have

$$E(\bar{Y}) = E\left(\frac{1}{n} 1^\top Y\right) = \frac{1}{n} (1^\top E(Y)) = \frac{1}{n} (n\mu) = \mu$$

and,

$$\begin{aligned}\text{cov}[\bar{Y}] &= \text{cov}\left[\frac{1}{n} 1^\top Y\right] \\ &= \left(\frac{1}{n}\right)^2 (1^\top \text{cov}[Y] 1) \\ &= \left(\frac{1}{n}\right)^2 (n\sigma^2) = \frac{\sigma^2}{n}.\end{aligned}$$

### 2.4.4 Multivariate normal distribution

We say that a random vector  $X \sim \mathcal{N}_d(\mu, \Sigma)$  follows a multivariate normal distribution if  $X$  has PDF:

$$\phi(\mathbf{x}) = \left(\frac{1}{2\pi}\right)^{d/2} |\Sigma|^{-1/2} \exp\left\{-\frac{1}{2}(\mathbf{x} - \mu)' \Sigma^{-1} (\mathbf{x} - \mu)\right\}.$$

If  $X \sim \mathcal{N}_d(\mu, \Sigma)$  and  $c \in \mathbb{R}^d$ ,  $A \in \mathbb{R}^{m \times d}$  then:

- $AX \sim \mathcal{N}(A\mu, A\Sigma A^\top)$ .
- $c^\top X \sim \mathcal{N}(c^\top \mu, c^\top \Sigma c)$ .
- Any conditional distribution for a subset of the variables conditional on another subset of variables is a multivariate distribution.

Using random vectors is a simple way of deriving lots of equations for this course. Working with vectors also allows those who are “geometrically gifted” to view the whole regression concepts geometrically! If not, not to worry!

### 2.4.5 Homework stop 4

**Exercise 2.14.** For a (full-rank) non-random matrix  $X \in \mathbb{R}^{n \times p}$  with  $n > p$ , and random vector  $Y \in \mathbb{R}^{n \times 1}$  with mean  $\mu$  and covariance  $\Sigma$ , compute the following:

- Expected value and covariance matrix of  $(X^\top X)^{-1} X^\top Y$
- Expected value of  $Y^\top Y$
- Expected value and covariance matrix of  $X^\top X$
- Expected value and covariance matrix of  $X(X^\top X)^{-1} X^\top Y$

# 3 Linear Regression

## 3.1 Basics of linear regression

By the end of this section, you should be able to say what the linear and normal linear regression models are. As well as what it means to assume either of these models.

### 3.1.1 The linear regression model

Consider the following example.

**Example 3.1.** It is difficult to accurately determine a person's body fat percentage without immersing them in water. However, we can easily obtain the weight of a person. A researcher would like to know if weight and body fat percentage are related? If so, for a given weight, can the person's body fat percentage be predicted? If so, how accurate is the prediction? This researcher collected the following data:

Individual	1	2	3	4	5	6	7	8	9	10
Weight (lb)	175	181	200	159	196	192	205	173	187	188
Body Fat (%)	6	21	15	6	22	31	32	21	25	30

Individual	11	12	13	14	15	16	17	18	19	20
Weight (lb)	188	240	175	168	246	160	215	159	146	219
Body Fat (%)	10	20	22	9	38	10	27	12	10	28

How can we (as statisticians / data scientists) answer the questions raised by the researcher?

The first thing we might do is explore the data:

```

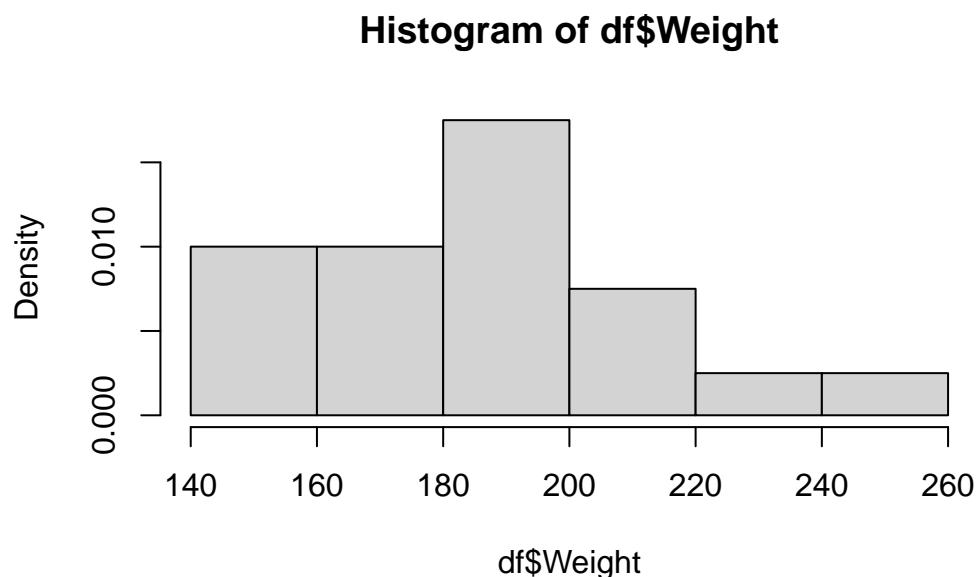
##### Exploratory analysis

# Make the data frame
Weight=c(175 , 181 , 200 , 159 , 196 , 192 , 205 , 173 , 187 , 188 ,
       188 , 240 , 175 , 168 , 246 , 160 , 215 , 159 , 146 , 219 )
BodyFat =c(6 , 21 , 15 , 6 , 22 , 31 , 32 , 21 , 25 , 30 ,
          10 , 20 , 22 , 9 , 38 , 10 , 27 , 12 , 10 , 28 )

df=data.frame(cbind(Weight=Weight,BodyFat=BodyFat))

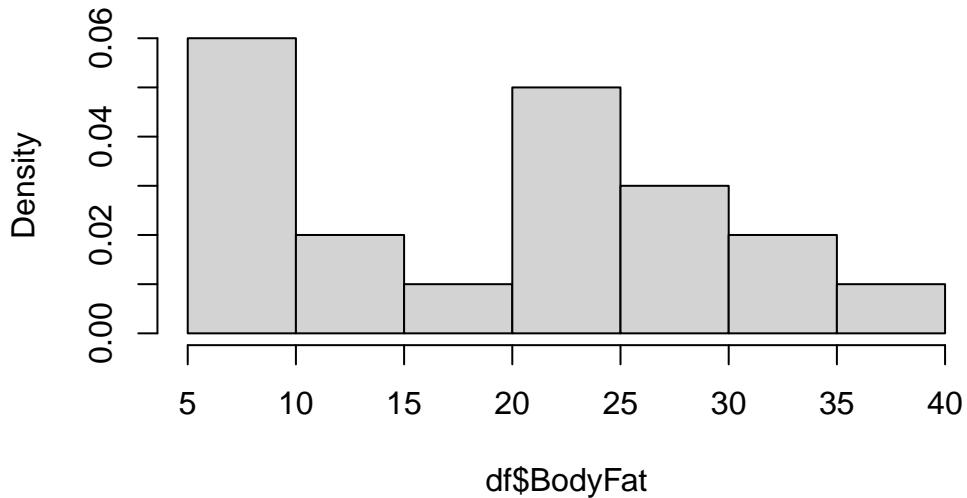
# make some histograms
hist(df$Weight,freq=F)

```



```
hist(df$BodyFat,freq=F)
```

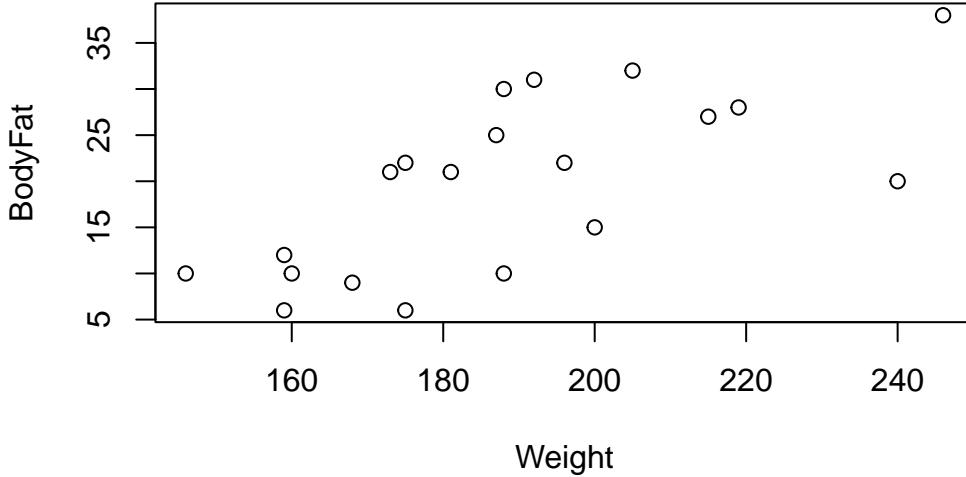
## Histogram of df\$BodyFat



```
# print summary statistics
summary(df)
```

Weight	BodyFat
Min. :146.0	Min. : 6.00
1st Qu.:171.8	1st Qu.:10.00
Median :187.5	Median :21.00
Mean :188.6	Mean :19.75
3rd Qu.:201.2	3rd Qu.:27.25
Max. :246.0	Max. :38.00

```
# There seems to be some relationship here
plot(df)
```



```
# Here is the correlation matrix, notice it is high!
cor(df)
```

```
      Weight  BodyFat
Weight  1.0000000 0.6966328
BodyFat 0.6966328 1.0000000
```

We have observed that there is a relatively strong linear relationship between these two variables. What next? We might ask, what is this relationship precisely?

In particular, note that we have observed a sample of vectors  $(Y_1, X_1), \dots, (Y_n, X_n)$ . Now, we want to say something about the relationship between  $X$  and  $Y$  in general. One way to do that is to suppose at the **population** level that

$$E[Y|X] = f(X).$$

That is, on average,  $Y$  is equal to  $f(X)$ . One way to do that is to assume that  $Y|X = f(X) + \epsilon$ , where  $\epsilon$  is a random variable that satisfies  $E[\epsilon] = 0$ . This assumption means that, for each  $Y_i$ , given  $X_i$ , we have that  $Y_i = f(X_i) + \epsilon_i$ . Note that we do not observe  $\epsilon_i$ , but we can assume it exists. We can read this as  $Y_i$  is equal to  $f(X_i)$ , plus some random, individual error  $\epsilon_i$ . The next step is to use the data to determine  $f$ .

Using the data analysis steps from the [Introduction](#) we can write out the first few steps:

- Question about a population: “How can we use weight to determine body fat percentage?”,
- Data:  $(Y_1, X_1), \dots, (Y_{20}, X_{20})$ ,  $(Y_i, X_i)$  are the body fat percentage and weight of individual  $i \in [20]$ .

We have explored the data with graphs and summary statistics. Now, we have posited the model  $Y|X = f(X) + \epsilon$ . Letting  $f$  be any function is too general. In fact, we can use the data to learn more about what  $f$  might be. Recall that earlier, we saw the scatter plot, where it looked like there was a linear relationship, (with some error), between  $Y$  and  $X$ . (We can draw a straight line through the middle of the data.)

Let's make some assumptions that make the statistical analysis easier:

1. Assume that  $\forall i \in [20]$ , it holds that

$$Y_i|X_i = \beta_0 + \beta_1 X_i + \epsilon_i.$$

This means that we assume that  $f$  is a line.

2. Next, we assume  $\forall i \in [20]$ ,  $E[\epsilon_i] = 0$  and  $\text{Var}[\epsilon_i] = \sigma^2$ . That is, the random error have the same mean and variance for each individual. In addition, the random errors average to 0.
3. We also assume that the individuals' Body fat percentage, weights and random errors are independent, that is,  $\epsilon_i \perp \epsilon_j$  for  $i \neq j$ ,  $i, j \in [20]$ .

This is the **simple linear regression model**. That is, the simple linear regression model is the set of assumptions 1-3 given above.

It is often also assumed:

4.  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$ ,

but not always. Including the normality assumption is known as the **simple normal linear regression model**.

In general, a model is a set of assumptions about a population. The particular set of assumptions 1-3 is the simple linear regression model.

The following is some terminology used in regression analysis:

- Here,  $Y_i$  is the **response variable**, also known as the dependent variable, or the outcome variable.
- Here,  $X_i$  is the **covariate**, also known as the explanatory variable, or the independent variable.

Given a “question about a population” which involves regression, you should immediately identify the response variable and the covariates.

Now, how can we interpret this model? That is, what does it mean to assume this model?

First, observe that we assume that  $E[Y|X]$  is a line. This means there is a linear relationship between the average body fat percentage and weight.

Next, observe that for any individual, their actual body fat percentage is given by  $Y = E[Y|X] + \epsilon_i = \beta_0 + \beta_1 X_i + \epsilon_i$ . Therefore, their body fat percentage will not fall exactly on the line  $\beta_0 + \beta_1 X_i$ . Rather, it will fall above or below the line, depending on  $\epsilon_i$ . Furthermore, if we assume that  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$ , then we know from the properties of the Normal distribution that this random error will not exceed  $2\sigma$  with high probability. Therefore, most of the time, an individual’s body fat percentage will fall within  $2\sigma$  of the line.

Third, notice that this quantity,  $2\sigma$ , does not depend on  $X$ . That is, for any weight, we still expect an individual’s body fat percentage to be within  $2\sigma$  of the line, regardless of the value of weight.

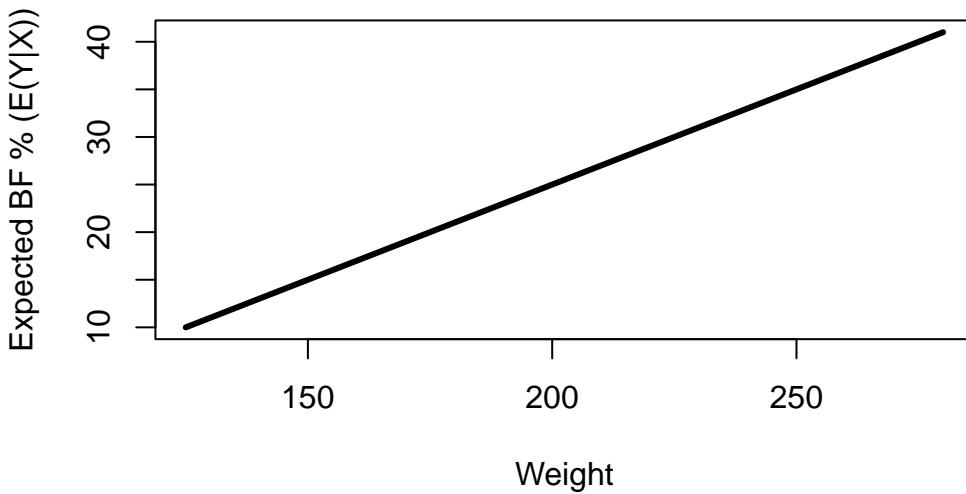
Fourth, if we knew  $\beta_0, \beta_1$ , then given someone’s weight, we could try to predict their body fat percentage given their weight. That is, we could calculate the expected body fat  $E[Y|X]$ . There would still be their individual random error  $\epsilon$ , so we would not be able to predict it exactly. However, if  $\sigma^2$  isn’t too big, then we could produce an accurate prediction.

Therefore, if the model assumptions are correct, we assume there exists some line, around which the body fat percentages are scattered uniformly.

Next, we will simulate data from the normal simple linear regression model to gain a better understanding of this model. Suppose that  $\beta_0 = -15$ ,  $\beta_1 = .2$  and  $\sigma = 5$ . Then we would observe the following.

```
#####
# Simulation
set.seed(3252)

# Suppose that beta_0=-15 and beta_1=0.2 and sigma=5,
# then we would have that the mean function E(Y|X) is given by the following line:
curve(-15+.2*x, 125, 280, lwd=3, xlab="Weight", ylab="Expected BF % (E(Y|X))")
```



```

# Next, let's simulate some body weights from the uniform distribution
Weight2=runif(20,135,250)

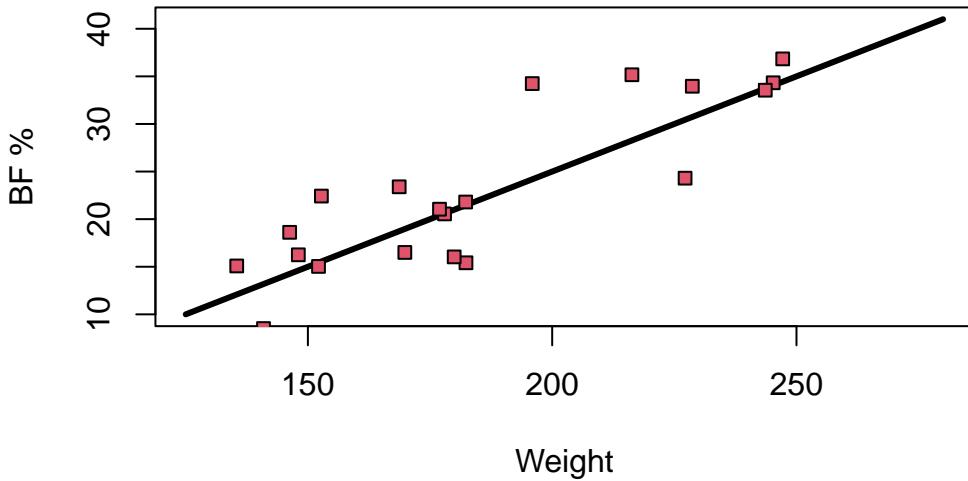
# Then, we can simulate the population body fat percentages according to the model as follows

# Simulating 20 values of the random error,
epsilon=rnorm(n=20,mean=0,sd=5)

# Computing the simulated Body fat percentages:
Bfs=-15+.2*Weight2+epsilon

# Plot the simulated values, and the mean function
curve(-15+.2*x,125,280,lwd=3,xlab="Weight",ylab="BF %")
points(Weight2,Bfs,pch=22,bg=2)

```



Notice how the data are scattered around the line uniformly? This is what data from a simple linear regression model looks like. Try changing the value in `set.seed()` and re-running the code. Notice how the data changes, but it is always scattered around the line uniformly? This is what we expect to see if the data follow a simple linear regression model.

Notice how the data simulated from our model appears similar to the body fat percentage and weights data we observed? That means this model (set of assumptions) is a good fit for our data.

### 🔥 Caution

In this model, and in regression in general, the response  $Y$  is not exactly equal to some function of  $X$  given by  $f(X)$ . The model assumes that **on average**  $Y = f(X)$ . Therefore, knowing someones “ $X$ ” value will not exactly give us their  $Y$  value, but it would give us a good guess at it. The error  $\epsilon$  is used to model the fact that someones “ $X$ ” value will not exactly give us their  $Y$  value. Notice above how the actual points are scattered around the line, and not exactly equal to it! This is due to the errors  $\epsilon$ .

### 3.1.2 The multiple linear regression model

But what about matrices? Why did we study matrices then? We can write the regression model in terms of matrices and vectors, to make it more compact.

Now, recall

$$Y_i|X_i = \beta_0 + \beta_1 X_i + \epsilon_i,$$

with  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$ . It is more convenient mathematically to let  $\mathbf{Y} = (Y_1, \dots, Y_n)^\top$ ,

$$\mathbf{X} = \begin{bmatrix} 1 & X_1 \\ \vdots & \vdots \\ 1 & X_n \end{bmatrix} = [1_n \mid (X_1, \dots, X_n)^\top],$$

$\beta = (\beta_0, \beta_1)^\top$  and  $\epsilon = (\epsilon_1, \dots, \epsilon_n)^\top$ . Then we can write

$$\mathbf{Y}|\mathbf{X} = \mathbf{X}\beta + \epsilon.$$

Often, we overload the notation  $Y$ , and use  $Y$  instead of  $\mathbf{Y}$ , and  $X$  instead of  $\mathbf{X}$ .

This form allows us to go beyond one explanatory variable very easily! Just add one column to  $X$  and one entry to  $\beta$  for each new variable. Observe the following model:

$$Y_i|(X_{i1}, \dots, X_{ik}) = \beta_0 + \beta_1 X_{i1} + \dots + \beta_k X_{ik} + \epsilon_i,$$

with  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$  and  $\epsilon_i \perp \epsilon_j$  for  $i \neq j$ ,  $i, j \in [n]$ . This is known as the **multiple linear regression model** (MLR), or just the linear regression model for short. We can write this model in the same form as above: Let

$$\mathbf{X} = \begin{bmatrix} 1 & X_{11} & X_{1k} \\ \vdots & \vdots & \vdots \\ 1 & X_{n1} & \dots & X_{nk} \end{bmatrix},$$

and  $\beta = (\beta_0, \dots, \beta_k)^\top$ . Then we can write the MLR as

$$\mathbf{Y}|\mathbf{X} = \mathbf{X}\beta + \epsilon,$$

where  $E[\epsilon] = 0$  and  $\text{Var}[\epsilon] = \sigma^2 I$ . Notice how compact this is! As in the simple case, there is also the **normal MLR**, which further assumes that  $\epsilon \sim \mathcal{N}(0, \sigma^2 I)$ .

We can then study the mathematical properties of

$$Y|X = X\beta + \epsilon$$

for general but fixed  $k$ , under the normal or vanilla MLR, which will cover many models.

### 3.1.3 Homework stop 1

**Exercise 3.1.** Try adjusting the parameters  $\beta_0, \beta_1, \sigma$  in the simulation, what happens to the data? What happens to the line?

**Exercise 3.2.** Is  $\beta$  an estimate or a population parameter? Why?

**Exercise 3.3.** Come up with another possible form of  $f$  that is not linear. Adjust the simulation to include this form of  $f$ .

**Exercise 3.4.** Write down the assumptions of the MLR and the normal MLR. What is the difference between the two models?

## 3.2 Least Squares

Now that we have settled on a model for the population, the next step is to use the data to estimate the model parameters. In particular, we need to estimate  $\beta$ . That will allow us to estimated  $E[Y|X]$  for any value of  $X$ .

Recall that we want to study the **population** model:

$$Y|X = X\beta + \epsilon.$$

### 3.2.1 Notation

For the model  $Y|X = X\beta + \epsilon$ , we have

- $Y \in \mathbb{R}^n$  is the response variable (a continuous random variable).
- $X \in \mathbb{R}^{n \times p}$  is the covariate matrix (Note that the first column is often  $1_n$ ).
- $X_i \in \mathbb{R}^p$  is the  $i^{th}$  observed explanatory variable ( $i = 1, \dots, n$ ) (not a random variable, in the sense that we condition on it).
- $\beta \in \mathbb{R}^{p \times 1}$  is the coefficient vector .
- $\epsilon \in \mathbb{R}^n$  is the random error (continuous random variable) .

We may also refer to the actual observed values (versus the abstract mathematical concept of a random variable) as follows:

- $y = (y_1, \dots, y_n)^\top \in \mathbb{R}^n$  is the observed response variable (fixed/observed)
- $x_{ij}$  is the  $i^{th}$  observation of the  $j^{th}$  explanatory variable (fixed/observed) Data:

Observation	Observed data point
1	$(y_1, x_{11}, x_{12}, \dots, x_{1p})$
2	$(y_2, x_{21}, x_{22}, \dots, x_{2p})$
⋮	⋮
n	$(y_n, x_{n1}, x_{n2}, \dots, x_{np})$

We posit that

$$Y|X = X\beta + \epsilon,$$

where we assume that

- $\forall i \in [n], E[\epsilon_i] = 0.$
- $\forall i \in [n], \text{Var}[\epsilon_i] = \sigma^2$  (constant variance and is also known as homogeneity.)
- We also would assume that  $\epsilon_i \perp \epsilon_j$  for  $i \neq j, i, j \in [n].$
- $\beta \in \mathbb{R}^{p \times 1}$  is the unknown, population coefficient vector.
- $X \in \mathbb{R}^{n \times p}$  is a covariate matrix.

Let's talk about  $\beta$ . How do we interpret  $\beta$ ? Suppose we know  $\beta$ . Then:

Note that

$$E[Y_i|X_i] = E[\beta^\top X_i + \epsilon] = \beta^\top X_i = \beta_1 X_{1,1} + \dots + \beta_p X_{i,p}$$

What does each  $\beta_j$  mean? Suppose that  $X_j$  is a continuous covariate.

We can interpret  $(\beta_j)$  as follows:

Holding  $X_{i,1}, \dots, X_{i,j-1}, X_{i,j+1}, \dots, X_{i,p}$  constant, a one unit increase in  $X_{i,j}$  causes, on average, a  $\beta_j$  unit increase in  $Y_i$ .

From another angle, we have that  $\partial E[Y]/\partial X = \beta$ , therefore, the rate of change with respect to the  $j^{th}$  covariate is  $\beta_j$ .

### 🔥 Caution

The “on average” and “holding other covariates constant” are very important components of the interpretation. First, the on average acknowledges the random error  $\epsilon$ . In other words, a one unit increase in  $X_{i,j}$  will not certainly increase  $Y_i$ , but it will on average. Next, the “holding other covariates constant” is used to mention how correlations between covariates are handled by the model. Some of the covariates in the model may be correlated, so increases in a given covariate may often be associated with changes in another covariate. This is not accounted for in the coefficient vectors  $\beta$ . That is why we must specify “holding other covariates constant”.

For instance, if a model includes terms for years of education attained and income, we know that as the number of years of education increase we expect to see a rise in income levels. As a result, to interpret the effect of coefficient on income, we must “hold years of education constant”, comparing what is expected with income changes but education does not.

### 🔥 Caution

For now, we can assume that all of the covariates  $X_j$  are continuous variables. Later in the course, there may be categorical covariates. In this case, the  $\beta_j$  corresponding to the categorical covariates have a different interpretation. We will return to this later.

Recall Example 3.1. We assume  $\forall i \in [20]$ , it holds that

$$Y_i | X_i = \beta^\top X_i + \epsilon_i,$$

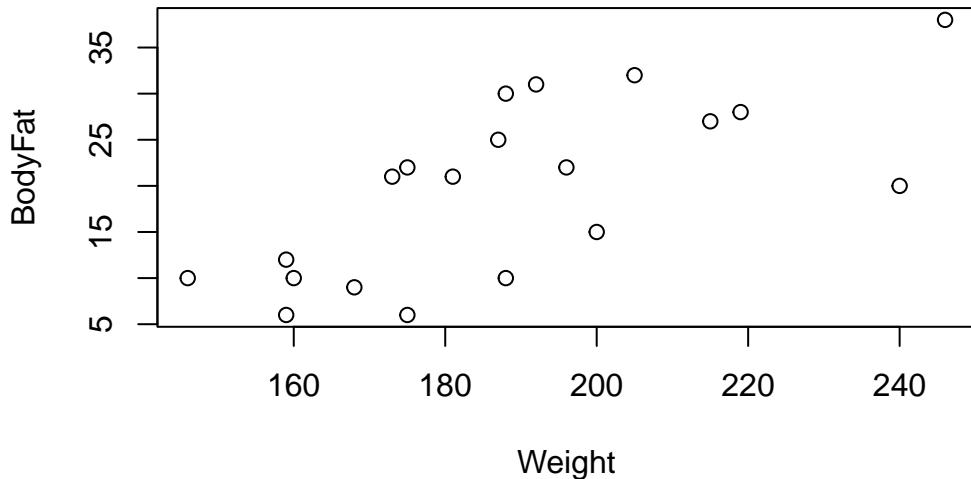
with  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$ ,  $\epsilon_i \perp \epsilon_j$  for  $i \neq j$ ,  $i, j \in [20]$ . A one unit increase in weight causes, on average, a  $\beta_2$  unit increase in body fat percentage. Since  $\beta_1$  is the intercept, it has a special interpretation.  $\beta_1$  is the average value of  $Y_i$  given  $X_i = 0$ . It is also helpful to note that  $\text{cov}(Y) = \sigma^2 I$ .

### 3.2.2 Least squares estimation

Okay, but we don't know  $\beta$ ! Just like we estimate the population mean with the sample mean, we need to estimate  $\beta$ . We would like an estimate  $\hat{\beta}$ , so that we can predict body fat percentage from weight. What is our best guess at  $\beta$ , given the data? One way to answer this, is through the method of **least squares**.

Returning to our example, recall that:

```
plot(df)
```

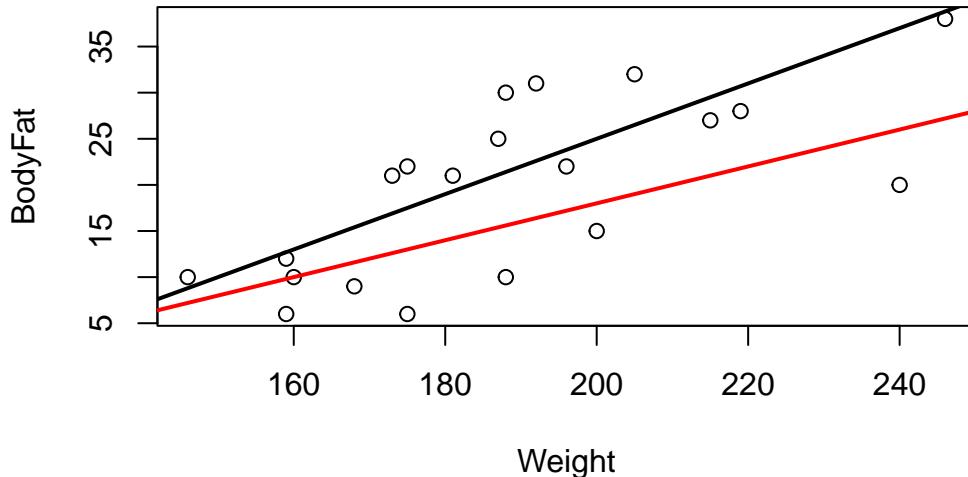


For example, suppose we want to determine if  $\beta$  is more likely to be  $(-35, 0.3)^\top$  or  $(-22, 0.2)^\top$ . How can we say which line is a better fit to our data? One way is to graph them on top of the data and determine which one looks better. Let's plot these lines.

```

plot(df)
# plot Y=-35+0.3X
abline(-35,0.3,lwd=2)
# plot Y=-25+0.2X
abline(-22,0.2,col='red',lwd=2)

```



Its not clear which one fits the data better. Even if it was clear, obviously, we cannot plot all possible lines. So how can we determine which line fits the data the “best”?

To do this, we have to define what “best” means quantitatively. For instance, one might ask which line minimizes the sum of the squared distances of the observed data points to the line? This line is then said to be the “best” line. Mathematically, given a proposed value of  $\beta$ , say  $\beta_0 \in \mathbb{R}^p$ , the signed distance to the hyperplane  $X\beta_0$  is  $\epsilon_0 = Y - X\beta_0$ . The squared distances to the hyperplane  $X\beta_0$  is then  $\epsilon_0^\top \epsilon_0 = (Y - X\beta_0)^\top (Y - X\beta_0)$ . We can then formulate this as a math problem: Which  $\beta_0 \in \mathbb{R}^p$  minimizes  $\epsilon_0^\top \epsilon_0$ ? i.e.,  $\hat{\beta} = \operatorname{argmin}_{\beta_0 \in \mathbb{R}^p} \epsilon_0^\top \epsilon_0$ . It is more convenient to just write

$$\hat{\beta} = \operatorname{argmin}_{\beta \in \mathbb{R}^p} (Y - X\beta)^\top (Y - X\beta).$$

In this framework, the “best” estimate is given by

$$\hat{\beta} = \operatorname{argmin}_{\beta \in \mathbb{R}^p} (Y - X\beta)^\top (Y - X\beta).$$

Note best is in the sense of minimizing the average squared distance to the hyperplane/line. We could also define best in terms of some other metric, such as average absolute distance to the hyperplane/line. For now, we will stick with this metric.

The next step is to solve:

$$\hat{\beta} = \underset{\beta \in \mathbb{R}^p}{\operatorname{argmin}} (Y - X\beta)^\top (Y - X\beta).$$

How do we minimize a function???

RECALL in calculus, to find the minimum of a function we:

1. Obtain the first two derivatives of the function.
2. Set the first derivative to zero and solve for the critical value.
3. Use the second derivative to verify the critical value minimized the function.

Goal: Compute  $\hat{\beta}$  – Minimize  $g(\beta) = (Y - X\beta)^\top (Y - X\beta)$ . (It may be useful to review taking derivatives with respect to vectors [here](#).

Step 1a:

$$\begin{aligned} \frac{\partial g}{\partial \beta} &= \frac{\partial g}{\partial \beta} (Y - X\beta)^\top (Y - X\beta) \\ &= \frac{\partial g}{\partial \beta} [Y^\top Y - 2(X\beta)^\top Y + (X\beta)^\top X\beta] && \text{(Transpose and distribute)} \\ &= -2 \frac{\partial g}{\partial \beta} \beta^\top X^\top Y + \frac{\partial g}{\partial \beta} \beta^\top X^\top X\beta && ((AB)^\top = B^\top A^\top) \\ &= -2X^\top Y + 2X^\top X\beta && \left( \frac{\partial}{\partial x} x^\top Ax = 2Ax \text{ if } A \text{ symmetric}, \frac{\partial}{\partial x} x^\top a = a \right) \\ &= -2X^\top (Y - X\beta). \end{aligned}$$

Step 1b: (Do this for homework)

$$\frac{\partial^2 g}{\partial \beta \partial \beta^\top} = 2X^\top X.$$

Step 2: We now need  $X^\top X$  to be invertible, so we will assume that  $X$  is full rank and  $n \geq p$ .

$$\begin{aligned} -2X^\top (Y - X\beta) &= 0 \\ \implies X^\top Y &= X^\top X\beta \\ \implies \beta &= (X^\top X)^{-1} X^\top Y. \end{aligned}$$

Step 3:

Recall that **if the Hessian matrix is positive definite at a critical point, then that critical point is a local minimum.** Since we have assumed  $X$  is full rank, this implies that  $X^\top X$  is positive definite.

To summarize, the steps have proceeded as follows:

- Step 1a:  $\frac{\partial g}{\partial \beta} = -2X^\top(Y - X\beta)$
- Step 1b:  $\frac{\partial^2 g}{\partial \beta \partial \beta^\top} = 2X^\top X$  (Do this for homework)
- Step 2:  $-2X^\top(Y - X\beta) = 0 \implies X^\top Y = X^\top X\beta \implies \beta = (X^\top X)^{-1}X^\top Y$
- Step 3:  $2X^\top X$  is positive definite, and so

$$\hat{\beta} = (X^\top X)^{-1}X^\top Y.$$

The estimate  $\hat{\beta}$  is known as the **least squares estimate** of the regression coefficients.

**Definition 3.1.** The **least squares estimate** of the regression coefficients is

$$\hat{\beta} = (X^\top X)^{-1}X^\top Y.$$

### 3.2.3 Example

**Example 3.2.** In the body weight example Example 3.1, write down  $X$ ,  $y$  and compute  $\hat{\beta}$ . Interpret  $\hat{\beta}$ .

First, we have that

$$y = (6, 21, 15, 6, 22, 31, 32, 21, 25, 30, 10, 20, 22, 9, 38, 10, 27, 12, 10, 28)^\top$$

$$X = [1_{20} | (175, 181, 200, 159, 196, 192, 205, 173, 187, 188, 188, 240, 175, 168, 246, 160, 215, 159, 146, 219)^\top]$$

#### i Note

For matrices  $A, B$  which have the same number of rows,  $C = [A|B]$  is horizontal concatenation of  $A$  and  $B$ . This notation indicates that the matrix  $C$  is formed by placing  $A$  and  $B$  side by side, joining them horizontally. Therefore,  $X$  is the matrix whose first column is made up of ones, and second column is made up of the body weights.

Let's use R to compute  $\hat{\beta}$ .

```
#Define X and Y
X=cbind(rep(1,nrow(df)), df$Weight)
Y=df$BodyFat

# cast to column vec
Y=matrix(Y,ncol=1)

#X'X
X_p_X=t(X)%*%X
```

```

#X'X inverse
X_p_X_inverse=solve(X_p_X)

#LS
beta_hat= X_p_X_inverse%*%t(X)%*%Y
beta_hat

[,1]
[1,] -27.3762623
[2,] 0.2498741

# We can also use R's lm() function to do this:
# This code is essential for the course.
# The first argument is the formula
model=lm(BodyFat ~ Weight, data=df)

#The summary function prints the model output.

summary(model)

```

Call:  
`lm(formula = BodyFat ~ Weight, data = df)`

Residuals:

Min	1Q	Median	3Q	Max
-12.5935	-5.7904	0.6536	5.2731	10.4004

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-27.37626	11.54743	-2.371	0.029119 *
Weight	0.24987	0.06065	4.120	0.000643 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.049 on 18 degrees of freedom  
Multiple R-squared: 0.4853, Adjusted R-squared: 0.4567  
F-statistic: 16.97 on 1 and 18 DF, p-value: 0.0006434

```
# The least squares estimates are given in the Estimate column of the summary.
```

The `lm()` function is used to fit multiple linear regression models in R. The basic usage involves specifying a formula and a data frame. The syntax is given by `lm(formula, data, ...)`.

The data argument should be the dataframe which contains your data. The formula argument is used to specify the model to be fitted. It provides a symbolic description of the model, indicating the response variable and the predictors/covariates, as well as the relationships between them. The left-hand side should be the name of your response variable, as it is named in your dataframe. To see the names of your variables use the `names()` function, e.g., `names(df)`. The right-hand side contains the covariates you want to include in your model. For instance, above, the formula is given by `BodyFat ~ Weight`. Note that `BodyFat` is the response and `Weight` is the covariate.

We now list some important properties of the least squares estimator.

**Exercise 3.5.** Compute  $E[\hat{\beta}]$  and  $\text{cov}(\hat{\beta})$ .

It holds that  $E[\hat{\beta}] = \beta$  and  $\text{cov}(\hat{\beta}) = \sigma^2(X^\top X)^{-1}$ .

Recall that an estimator is **unbiased** if its expectation equals the population parameter it is trying to estimate. After completing Exercise 3.5 you will see that  $\hat{\beta}$  is unbiased for the parameter  $\beta$ .

The least squares estimator is also the “best linear unbiased estimator”, or the **BLUE**. This is known as the **Gauss–Markov** theorem. This means that under the assumptions of the linear regression model, over any unbiased estimator of  $\beta$  we can construct, which is a linear combination of  $Y_1, \dots, Y_n$ , the estimator  $\hat{\beta}$  has the smallest variance (and therefore, the smallest mean squared error). Recall that for an estimator  $\hat{\alpha}$ , the mean squared error is given by  $E[||\beta - \hat{\alpha}||^2]$ .)

The Gauss–Markov theorem does not require the random error to be normally distributed. If we are willing to assume that  $\epsilon \sim \mathcal{N}(0, \sigma^2 I)$ , then  $\hat{\beta}$  is also the **maximum likelihood estimator** and the “uniformly minimum-variance unbiased estimator”, or **UMVUE**. This means that  $\hat{\beta}$  has lower variance than any other unbiased estimator, no matter what the true value of  $\beta$  is.

One might ask, how can we use  $\hat{\beta}$  to predict body fat percentage given weight? The estimate  $\hat{\beta}$  gives us a best guess at the coefficients. Therefore, our best guess at someones body fat is given by

$$\text{Best Guess} = -27.3762623 + 0.2498741 \times \text{Weight}.$$

For instance, for someone who is 170 pounds, we would guess that their body fat percentage is  $-27.3762623 + 0.2498741 \times 170 = 15.1023347$ .

### 3.2.4 Homework stop 2

**Exercise 3.6.** Why do we need  $\hat{\beta}$ , why not use  $\beta$ ?

**Exercise 3.7.** Is  $\hat{\beta}$  an estimate or a population parameter? What about  $\beta$ ?

**Exercise 3.8.** Compute,  $X$ ,  $Y$  and  $\hat{\beta}$  in the following real data example:

It is challenging to assess a student's understanding of a subject without administering an exam. However, we can easily record the number of hours a student studies. A researcher would like to know if the number of hours studied and exam scores are related. This researcher collected the following data:

Student	Hours Studied	Exam Score (%)
1	5	55
2	8	65
3	12	78
4	6	58
5	10	72
6	9	68
7	15	85
8	7	60
9	11	74
10	13	80
11	14	82
12	20	90
13	5	55
14	6	59
15	18	88
16	7	62
17	16	86
18	4	50
19	3	45
20	19	89

To help you, here is some R code the dataset:

```
# Data
study_data <- data.frame(
  Student = 1:20,
  Hours_Studied = c(5, 8, 12, 6, 10, 9, 15, 7, 11, 13, 14, 20, 5, 6, 18, 7, 16, 4, 3, 19),
  Exam_Score = c(55, 65, 78, 58, 72, 68, 85, 60, 74, 80, 82, 90, 55, 59, 88, 62, 86, 50, 45))
```

### 3.3 Least squares inference

Recall we estimate the parameter  $\beta$  using least squares:

Recall that  $\hat{\beta} = (X^\top X)^{-1} X^\top Y$ . We can predict a new weight  $Y_{new}|X = x$  with  $\hat{y}_{new} = x^\top \hat{\beta}$ . We may be interested in the following questions: How good is  $\hat{y}_{new}$  as a prediction, on average? How will new observations vary about the line? For example, given a specific weight, how will does body fat percentage vary around the regression line? How does  $\hat{\beta}$  vary around  $\beta$ ? Is there strong evidence that  $Y$  has a relationship with  $X$ ? Is  $X$  adding information about  $Y$  at all?

To answer these questions, we need to look at the variation of our estimates and our data.

#### 3.3.1 Important quantities: Residuals and fitted values

We now introduce some very important quantities: We call the estimated values given our observed  $X$  the fitted values:  $\hat{Y} = X\hat{\beta}$ . The fitted values are what our model would estimate the vector  $Y$  to be. We call  $\hat{\epsilon} = Y - \hat{Y}$  is the **residual vector**. The  $i$ th entry of  $\hat{\epsilon}$ , say  $\hat{\epsilon}_i$ , is the  $i$ th **residual**. The residuals are the signed distances from the response variable to the estimated regression hyperplane. The **sum of squared error** or **sum of squared residuals** (SSE) is given by  $\hat{\epsilon}^\top \hat{\epsilon} = \sum_{i=1}^n \hat{\epsilon}_i^2$ . Note that since we estimated  $\beta$  using the least squares method,  $\hat{\epsilon}^\top \hat{\epsilon}$  is minimized (with respect to varying  $\beta$ ).

**Example 3.3.** Recall Example 3.1. What is the residual of individual 3? How can we interpret this value?

```
residuals=Y-X%*%beta_hat; residuals
```

```
[,1]
[1,] -10.3517117
[2,]  3.1490434
[3,] -7.5985652
[4,] -6.3537255
[5,]  0.4009314
[6,] 10.4004279
[7,]  8.1520641
[8,]  5.1480365
[9,]  5.6497986
[10,] 10.3999245
```

```

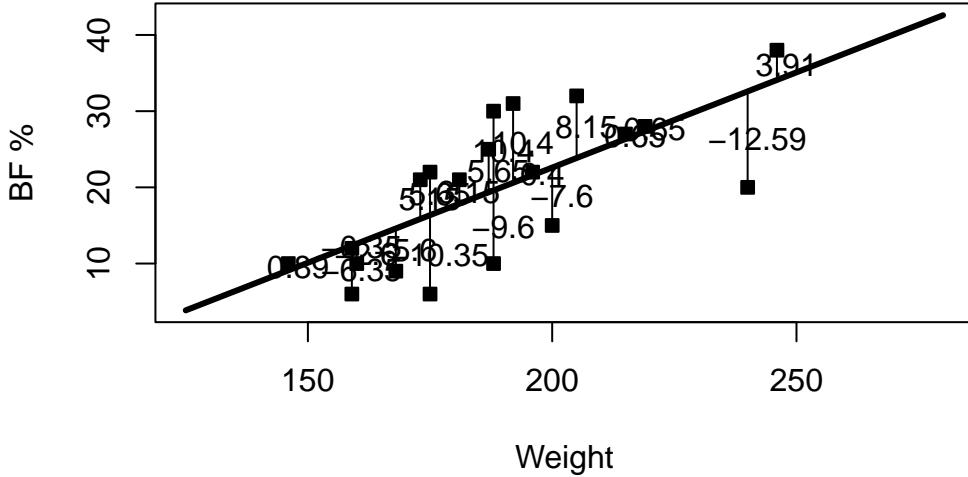
[11,] -9.6000755
[12,] -12.5935307
[13,] 5.6482883
[14,] -5.6025928
[15,] 3.9072245
[16,] -2.6035997
[17,] 0.6533228
[18,] -0.3537255
[19,] 0.8946383
[20,] 0.6538262

# This means that individual 3's body fat is 7.5 percentage points lower than the fitted line
residuals[3]

[1] -7.598565

# We can go further and plot all of the residuals
curve(beta_hat[1]+beta_hat[2]*x,125,280,lwd=3,xlab="Weight",ylab="BF %")
points(Weight,BodyFat,pch=22,bg=1)
Yvals=cbind(BodyFat,model$fitted.values)
Xvals=cbind(Weight,Weight)
for(i in 1:nrow(Yvals)){
  lines(Xvals[i,],Yvals[i,])
  text(Xvals[i,1]+2,mean(Yvals[i,]),round(residuals[i],2))
}

```



```
# Then, the population body fat percentages, given weights will look like this:
#
# Bfs=-15+.2*Weight+rnorm(20,0,sd=5)
```

### 3.3.2 Variation decomposition

Variance decomposition is a fundamental concept that explains how the total variation in the response variable can be partitioned into different sources. This decomposition is crucial for evaluating the performance of the regression model and understanding the contributions of various factors.

The residuals describe one type of variation of the response values. We can also consider the total variation of the response. The total variation of the response, or the **sum of squares total/total sum of squares ( $SST$ )** is given by  $SST = (n - 1)\hat{\sigma}_y^2 = \sum_{i=1}^n (Y_i - \bar{Y})^2 = (Y - \bar{Y})^\top (Y - \bar{Y})$ . It can be shown that the  $SST$  can be decomposed as follows:

$$SST = (Y - \bar{Y})^\top (Y - \bar{Y}) = (Y - \hat{Y})^\top (Y - \hat{Y}) + (\hat{Y} - \bar{Y})^\top (\hat{Y} - \bar{Y}) = \hat{\epsilon}^\top \hat{\epsilon} + (\hat{Y} - \bar{Y})^\top (\hat{Y} - \bar{Y}).$$

That is,  $SST = SSE + SSModel$  where

- $SSModel$ , OR  $SSM$  measures the total variations of the response explained by the covariates  $X$  via the model based on  $\beta$ .

- $SSE$  measures the total variations of the response unexplained by the covariates  $X$  via the model based on  $\hat{\beta}$ .
- Note there are sometimes other names for  $SSE$  and  $SSModel$ , such as  $SSRegression$ ,  $SSwithin$  and  $SSbetween$ , etc.

So, we have that the total variation in the response can be broken down into that which is explained by the  $X$  values, and that which is unexplained.

An interesting observation is given as follows: The first column of the  $X$  matrix is given by  $1_n$ , which implies that

$$\bar{Y}1 = X \begin{bmatrix} \bar{Y} \\ 0 \end{bmatrix}.$$

This means that if we let  $\hat{\beta}_* = (\bar{Y}, 0, \dots, 0)^\top$ , then  $(Y - \bar{Y}1)$  would be the signed distances to (or the residuals of) the regression hyperplane corresponding to  $\hat{\beta}_*$ . Since  $\hat{\beta}$  minimizes the sum of squared residuals, we must have that the hyperplane corresponding to  $\hat{\beta}$  has a smaller sum of squared residuals than the regression hyperplane corresponding to  $\hat{\beta}_*$ . Therefore, we must have that  $\hat{\epsilon}^\top \hat{\epsilon} \leq (Y - \bar{Y}1)^\top (Y - \bar{Y}1)$ .

Each of these terms in the decomposition is associated with a certain number of **degrees of freedom**.

- Total:  $dfT = n - 1$ .
- Model:  $dfM = \# \text{ non-zero } \beta - 1$ .
- Error:  $dfE = n - \# \text{ non-zero } \beta$ .

Intuitively, since the  $SSE$  is the variance unexplained by the model/covariates, the  $SSE$  is related to the error variance  $\sigma^2$ . In fact, to estimate  $\sigma^2$ , we use

$$\hat{\sigma}^2 = MSE = \frac{SSE}{dfE}.$$

The null model is defined as  $Y|X = \beta_0 + \epsilon$ . This is the model where the last  $p - 1$  terms in the true vector  $\beta$  are 0. This model says that  $Y$  does not depend on  $X$ . In the null model, we only need to estimate the mean, so  $df = n - 1$ . Therefore, under the null model,

$$\begin{aligned} \hat{\sigma}^2 &= (n - 1)^{-1} SST = \hat{\sigma}_Y^2 \\ &= (n - 1)^{-1} \sum_{i=1}^n (Y_i - \bar{Y})^2 = (n - 1)^{-1} (Y - \bar{Y}1)^\top (Y - \bar{Y}1). \end{aligned}$$

Therefore, in the null model, the estimate of  $\sigma^2$  via the  $MSE$  is just the usual estimate of the variance of the response. This is intuitive!

The following table can be used to summarize the variation in the response:

Source	SS	df	MS
Model	$SSM$	$dfM$	$MSModel = SSM/dfM$
Residual	$SSE$	$dfE$	$MSE = SSE/dfE$
Total	$SST$	$dfT$	

**i** Note

It is very important to be able to interpret these terms! The derivation is also important. However, we can use a machine to compute anything for us, so memorizing the formula is not helpful.

### 3.3.3 Coefficients of determination

A model is a good model if it can explain a fair amount of the variation in the response. (You can think that the model explains “changes” in the response.) In other words,  $SSModel$  should be as close to  $SSTotal$  as possible; or equivalently,  $SSError$  should be as close to 0 as possible. Now, “close” is a relative term, and so we need another value to reference to. This is where the  $R^2$  comes in:

$$R^2 = \frac{SSModel}{SST},$$

and is the proportion of variation explained by the model. It is clear that  $0 \leq R^2 \leq 1$ , and so rescaling the data will not affect  $R^2$  (like it would affect the sum of squares terms  $SST, SSE, SSM$ ). If  $R^2$  is close to 1, it is large – “close to 1” is a subjective/area dependent. Generally, the larger the  $R^2$ , the better the model!

To compare different models, we could potentially add different covariates and see if  $R^2$  improves. However, every time you add any variable,  $R^2$  will always increase. Therefore, it is common to use the adjusted coefficient of determination:

$$\bar{R}^2 = 1 - (1 - R^2) \frac{n - 1}{n - p}.$$

Thus, the (adjusted) coefficient of determination can be used as a measure of how well the regression model fits the data (how much variance is explained). It could also be used to compare models.

### 3.3.4 The $F$ test

The coefficients of determination are summary statistics which give an idea of the fit of the model. We would also like a significance test that tells us whether the covariates explain  $Y$ , or what we observed was simply due to sampling variation.

If  $\beta = (\beta_1, \dots, \beta_p)^\top$  then let  $\tilde{\beta} = (\beta_2, \dots, \beta_p)^\top$ . That is  $\tilde{\beta}$  is the regression coefficients without the intercept term. Similarly, let  $\tilde{\hat{\beta}} = (\hat{\beta}_2, \dots, \hat{\beta}_p)^\top$ . Now, we want to avoid the situation where  $\tilde{\beta} = 0$  but  $\tilde{\hat{\beta}} \neq 0$  due to sampling variation.

To do this, we perform a significance test:

$$H_0 : \tilde{\beta} = 0 \quad vs \quad H_1 : \tilde{\beta} \neq 0.$$

First, we need the normality assumption to perform significance test: Assume  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$ . With this assumption, the model is then known as the **Normal Multiple Linear Regression Model**. It is important to note that the least squares method does not require this assumption, and this assumption is required only for the significance test to be valid. To test the hypothesis stated above, we use the overall  $F$  test and the observed test statistic is  $F_{obs} = MSModel/MSE$ . Why?

With the extra normality assumption, we have the following holds:

- $Y|X$  is normally distributed.
- We have that  $SSM/\sigma^2 \sim \chi^2_{dfM}$  and  $SSE/\sigma^2 \sim \chi^2_{dfE}$ .
- Furthermore,  $SSM \perp SSE$ .

Recall that the ratio of two independent  $\chi^2$  distributions divided by their respective degrees of freedom follows an  $F$  distribution. Therefore, we have that  $F_{obs} \sim F_{dfM, dfE}$ . The corresponding p-value is  $\Pr(W > F_{obs})$  where  $W \sim F_{dfM; dfE}$ . We can alternatively reject the null hypothesis if  $F_{obs} > F_{dfM; dfE, 1-\alpha}$ , where  $F_{dfM; dfE, 1-\alpha}$  is the  $1 - \alpha$  quantile of the  $F_{dfM, dfE}$  distribution.

We can now present the complete ANOVA table

Source	SS	df	MS	F	p-value
Model	$SSM$	$dfM$	$MSModel = \frac{SSR}{dfM}$	$F = \frac{MSModel}{MSE}$	$\Pr(W > F_{obs})$
Residual	$SSE$	$dfE$	$MSE = \frac{SSE}{dfE}$		
Total	$SST$	$dfT$			

**Example 3.4.** In Example 3.1, compute and interpret the coefficients of determination. Compute and interpret the ANOVA table. Test whether the regression model is significant. (This means perform the  $F$  test.)

```
# recall
head(df)
```

```

Weight BodyFat
1    175      6
2    181     21
3    200     15
4    159      6
5    196     22
6    192     31

# The F test results are given in the summary
summary(model)

```

```

Call:
lm(formula = BodyFat ~ Weight, data = df)

Residuals:
    Min      1Q  Median      3Q      Max 
-12.5935 -5.7904  0.6536  5.2731 10.4004 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -27.37626   11.54743  -2.371 0.029119 *  
Weight        0.24987    0.06065   4.120 0.000643 *** 
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.049 on 18 degrees of freedom
Multiple R-squared:  0.4853,    Adjusted R-squared:  0.4567 
F-statistic: 16.97 on 1 and 18 DF,  p-value: 0.0006434

```

```

# The ANOVA table is given below

# First define the null model object using lm()
# This line fits a model with only the intercept term
null_model=lm(BodyFat~1,data=df)

# This line gets the ANOVA table
anova(null_model,model)

```

#### Analysis of Variance Table

```

Model 1: BodyFat ~ 1
Model 2: BodyFat ~ Weight
  Res.Df      RSS Df Sum of Sq      F    Pr(>F)
1       19 1737.75
2       18  894.42  1     843.33 16.972 0.0006434 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

# We can also do this by hand:

```

# Store sample size
n=nrow(df)
p=2

# Compute sum of squares
SST=t(Y-mean(Y)*rep(1,n))%*%(Y-mean(Y)*rep(1,n))
Yhat=X%*%beta_hat
res=Y-Yhat
SSE=t(res)%*%res
SSM=SST-SSE

dfe=n-p
dfm=p-1
MSM=SSM/dfm

MSE=SSE/dfe

Fv=MSM/MSE

p.val=1-pf(Fv,dfm,dfe)

# ANOVA Table:
ANOVA_Table=rbind(c(SSM,dfm,MSM,Fv,p.val),c(SSE,dfe,MSE,NA,NA),c(SST,n-1,NA,NA,NA))
rownames(ANOVA_Table)=c("Model","Error","Total")
colnames(ANOVA_Table)=c("SS","df","MS","F","p-value")
ANOVA_Table

```

SS	df	MS	F	p-value
----	----	----	---	---------

Model	843.3252	1	843.32521	16.97164	0.0006434484
Error	894.4248	18	49.69027	NA	NA
Total	1737.7500	19	NA	NA	NA

### 3.3.5 Homework stop 3

**Exercise 3.9.** In the following real data example: **Compute and interpret** the coefficient of determination, the adjusted coefficient of determination and perform the  $F$  test for model significance. Including printing the ANOVA table, the null and alternative hypothesis, an interpretation of the p-value and the conclusion of the test.

It is challenging to assess a student's understanding of a subject without administering an exam. However, we can easily record the number of hours a student studies. A researcher would like to know if the number of hours studied and exam scores are related. This researcher collected the following data:

Student	Hours Studied	Exam Score (%)
1	5	55
2	8	65
3	12	78
4	6	58
5	10	72
6	9	68
7	15	85
8	7	60
9	11	74
10	13	80
11	14	82
12	20	90
13	5	55
14	6	59
15	18	88
16	7	62
17	16	86
18	4	50
19	3	45
20	19	89

To help you, here is some R code the dataset:

```

# Data
study_data <- data.frame(
  Student = 1:20,
  Hours_Studied = c(5, 8, 12, 6, 10, 9, 15, 7, 11, 13, 14, 20, 5, 6, 18, 7, 16, 4, 3, 19),
  Exam_Score = c(55, 65, 78, 58, 72, 68, 85, 60, 74, 80, 82, 90, 55, 59, 88, 62, 86, 50, 4
)

```

**Exercise 3.10.** Write down the interpretations of:  $SSE$ ,  $MSE$ ,  $R^2$ ,  $\bar{R}^2$ ,  $SSM$ .

**Exercise 3.11.** What is the interpretation of the p-value in the ANOVA table?

**Exercise 3.12.** What extra assumption is needed to perform the  $F$ -test?

### 3.3.6 Significance of one variable

So far, we have learned that the least squares method yields the following estimate of  $\hat{\beta} = (X^\top X)^{-1} X^\top Y$  with  $E[\hat{\beta}] = \beta$  and  $\text{cov}(\hat{\beta}) = (X^\top X)^{-1} \sigma^2$ . Moreover, we use  $MSE$  to estimate  $\sigma^2$ . Next, we learned that we can summarize the  $SS$ ,  $df$ , and  $MS$  in an ANOVA table. We used the  $F$  test and the coefficient of determination to evaluate the quality of the model, i.e., to see the amount of information  $X$  provides about  $Y$ .

When the model is a significant model, then, at least one of the individual explanatory variables is useful in explaining the response. We may be interested in whether a specific covariate, or set of covariates is useful in explaining the response variable. We now learn how we can test for the significance of each individual explanatory variable separately and how we can test for the significance of a subset of explanatory variables. Note that these tests also require that the random error is normally distributed.

To test for significance and compute confidence intervals of a single variate, we have to compute the distribution of  $\hat{\beta}_j$ . We first compute the mean and variance of  $\hat{\beta}_j$ . First, given that  $E(\hat{\beta}) = \beta$ , we have  $E(\hat{\beta}_j) = \beta_j$ . Next,  $\text{Var}[\hat{\beta}_j]$  is the  $(j, j)^{th}$  entry of  $\text{cov}(\hat{\beta})$ . In addition, we have derived that  $\text{cov}(\hat{\beta}) = (X^\top X)^{-1} \sigma^2$ .

Now, recall that if  $Z$  is multivariate normal, i.e.,  $Z \sim \mathcal{N}(\mu, \Sigma)$ , then  $b + AZ \sim \mathcal{N}(b + A\mu, A\Sigma A^\top)$ , i.e.,  $b + AZ$  is also multivariate normal. Therefore, since we have assumed that  $\epsilon \sim \mathcal{N}_n(0, \sigma^2 I)$  and that  $Y|X = X\beta + \epsilon$ , it follows that  $Y|X \sim \mathcal{N}_n(X\beta, \sigma^2 I)$ . Next, we may recall that  $\hat{\beta} = (X^\top X)^{-1} X^\top Y$ . Let  $A = (X^\top X)^{-1} X^\top$ . Then  $\hat{\beta} = AY$ . It follows that  $\hat{\beta}$  is also multivariate normal! Putting everything together, we have that  $\hat{\beta} \sim \mathcal{N}_p(\beta, (X^\top X)^{-1} \sigma^2)$ .

**Theorem 3.1.** Under the assumptions of the **normal linear regression model** it holds that  $\hat{\beta} \sim \mathcal{N}_p(\beta, (X^\top X)^{-1} \sigma^2)$ .

Now that we have the distribution of  $\hat{\beta}$ , we can use it to compute the confidence intervals for  $\beta_j$ s.

Recall from introductory statistics (MATH 1131) that you learned that if we want to compute a confidence interval for the sample mean and the sample variance was unknown, we had to estimate the variance. Similarly, here, the variance of  $\hat{\beta}_j$  contains  $\sigma$ , an unknown parameter. Recall that, we estimate  $\sigma^2$  by  $MSE$ , and so we can estimate the variance of  $\hat{\beta}_j$  by  $\widehat{\text{Var}}[\hat{\beta}_j] = (X^\top X)_{j,j}^{-1}MSE$ .

It can be shown that  $\hat{\beta} \perp MSE$ . Therefore, we have that

$$\frac{\hat{\beta}_j - \beta_j}{\sqrt{\widehat{\text{Var}}(\hat{\beta}_j)}} \sim t_{dfE}.$$

Now that we know the distribution of  $\hat{\beta}_j$ , we can perform significance testing and compute confidence intervals.

If we want to test

$$H_0: \beta_j = \beta_j^0 \quad vs \quad \beta_j \neq \beta_j^0$$

we can do the following.

The observed test statistic is  $TS = \frac{\hat{\beta}_j - \beta_j^0}{\sqrt{\widehat{\text{Var}}(\hat{\beta}_j)}}$ . Note that, under the null hypothesis, we have that

$\frac{\hat{\beta}_j - \beta_j^0}{\sqrt{\widehat{\text{Var}}(\hat{\beta}_j)}} \sim t_{dfE}$ . Thus, the corresponding p-value is obtained based on the  $t_{dfE}$  distribution. Specifically, we can compute the p-value  $\Pr(-|TS| < Z) + \Pr(|TS| > Z) = 2 * \Pr(|TS| > Z)$ , where  $Z \sim t_{dfE}$ .

The test proceeds as follows:

1. State the hypotheses

$$H_0: \beta_j = \beta_j^0 \quad vs \quad H_1: \beta_j \neq \beta_j^0.$$

2. Compute the test statistic  $\frac{\hat{\beta}_j - \beta_j^0}{\sqrt{\widehat{\text{Var}}(\hat{\beta}_j)}}$  and the p-value.
3. Interpret the p-value, and use it to decide whether you reject the null hypothesis.

Often, one may choose a threshold  $\alpha$ , and reject the null hypothesis if the p-value falls below that threshold. Other times, we use the p-value as a description of evidence against the null. If it is larger than 0.05, but still small, then that still constitutes some evidence against the null hypothesis.

Let's now discuss one-sided hypotheses. First, consider:

$$H_0: \beta_j \leq \beta_j^0 \quad vs \quad H_1: \beta_j > \beta_j^0$$

Then, if the alternative hypothesis is true, we expect  $TS$  to be positive. The p-value is given by  $\Pr(TS > Z)$ , where  $Z \sim t_{dfE}$ . Notice that the p-value is measuring how extremely positive  $TS$  is. Using the threshold method, we can also check if  $TS > t_{dfE,1-\alpha}$ . Next, if we want to test

$$H_0: \beta_j \geq \beta_j^0 \quad vs \quad H_1: \beta_j < \beta_j^0,$$

then if the alternative hypothesis is true, we expect  $TS$  to be negative. The p-value is given by  $\Pr(TS < Z)$ , where  $Z \sim t_{dfE}$ . Notice that the p-value is measuring how extremely negative  $TS$  is. Using the threshold method, we can also check if  $TS < t_{dfE,\alpha}$ .

### **i** Note

We use  $t_{k,p}$  to denote the  $p$ th quantile of the  $t$  distribution with  $k$  degrees of freedom. For  $p = 0.025$  and large  $k$ , this is approximately equal to 2.

In Example 3.1, test if the coefficient for weight is equal to  $1/3$  vs. not equal to  $1/3$ . Next, test if the coefficient for weight is less than or equal to  $1/3$  vs. greater than  $1/3$ . Lastly, test if the coefficient for weight is non-zero.

First, we have that

$$\begin{aligned} H_0: \beta_1 = 1/3 &\quad vs \quad H_1: \beta_1 \neq 1/3. \\ H_0: \beta_1 \leq 1/3 &\quad vs \quad H_1: \beta_1 > 1/3. \\ H_0: \beta_1 = 0 &\quad vs \quad H_1: \beta_1 \neq 0. \end{aligned}$$

Now, let's execute the tests:

```
#changing matrix to scalar
MSE=c(MSE)
hvar_beta=solve(t(X) %*% X)*MSE

print(beta_hat)

[,1]
[1,] -27.3762623
[2,]  0.2498741

TS=(beta_hat[2]-1/3)/sqrt(hvar_beta[2,2])

# not equal
# pt(x,df) is the CDF of a t distributed RV with df degrees of freedom at x.
p_val=2*(1-pt(abs(TS),dfe))
p_val
```

```
[1] 0.1857053
```

```
# greater than  
# pt(x,df) is the CDF of a t distributed RV with df degrees of freedom at x.  
p_val=1-pt(TS,dfe)  
p_val
```

```
[1] 0.9071474
```

```
## testing equal to 0  
TS=beta_hat[2]/sqrt(hvar_beta[2,2])  
  
# not equal  
# pt(x,df) is the CDF of a t distributed RV with df degrees of freedom at x.  
p_val=2*(1-pt(abs(TS),dfe))  
p_val
```

```
[1] 0.0006434484
```

```
# We can also use the model object to test if it is not equal to 0:  
# The test statistic and the pvalue are given in the t value and Pr(>|t|) columns, respec  
summary(model)
```

Call:

```
lm(formula = BodyFat ~ Weight, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-12.5935	-5.7904	0.6536	5.2731	10.4004

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-27.37626	11.54743	-2.371	0.029119 *
Weight	0.24987	0.06065	4.120	0.000643 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.049 on 18 degrees of freedom

```
Multiple R-squared:  0.4853,    Adjusted R-squared:  0.4567
F-statistic: 16.97 on 1 and 18 DF,  p-value: 0.0006434
```

Based on the concepts that you have learned in 1131, and what we have reviewed in previous lectures, it also follows from the above analysis that a  $(1 - \alpha)100$  confidence interval for  $\beta_j$  is

$$\hat{\beta}_j \pm t_{dfE,\alpha/2} \sqrt{\widehat{var}(\hat{\beta}_j)}.$$

**Example 3.5.** In Example 3.1, compute a 99% and a 95% confidence interval for the coefficient for weight. Which one is longer? Why? Interpret these intervals.

```
# By hand
beta_hat[2]+c(-1,1)*qt(0.975,dfe)*sqrt(hvar_beta[2,2])
```

```
[1] 0.1224448 0.3773035
```

```
beta_hat[2]+c(-1,1)*qt(0.995,dfe)*sqrt(hvar_beta[2,2])
```

```
[1] 0.07528522 0.42446306
```

```
# Auto software/using lm:
confint(model,level=0.95)
```

	2.5 %	97.5 %
(Intercept)	-51.6365090	-3.1160157
Weight	0.1224448	0.3773035

```
confint(model,level=0.99)
```

	0.5 %	99.5 %
(Intercept)	-60.61484736	5.8623227
Weight	0.07528522	0.4244631

If we took many samples of size 20 and computed a 95% (99%) confidence interval for each sample, then 95% (99%) of them would contain the true coefficient for the weight variable. We can conclude that with 95% (99%) confidence, the true coefficient for weight likely falls within (0.12, 0.38) ((0.08,0.42)).

### 🔥 Caution

The key to understanding a confidence interval is to realize that the end points of the interval depend on the sample, and are therefore, random. On the other hand, the population parameter is not random, it is fixed. Therefore, if we drew a different sample, the interval would move, and there is a  $(1 - \alpha)100\%$  chance that that interval catches the population parameter. Most of the time it will contain the parameter, but not always.

Recall that the point of computing a confidence interval is to report the uncertainty in our estimate that resulted from drawing a sample. We expect the true parameter to be somewhere in that range, and our best guess at the parameter is given by the center of the interval.

### 3.3.7 Inference for the mean response and prediction intervals

We may wish to estimate the average response at a specific set of the covariates  $x$ . Given  $x$ , the theoretical mean response is  $x^\top \beta$ . Given  $x$ , we can estimate the mean response as  $x^\top \hat{\beta}$ . For instance, what is the average body fat percentage at 160 pounds? How accurate is our estimate? We can use a confidence interval to answer this question.

Note that the expectation and variance of the estimate of the mean response are given by  $E[x^\top \hat{\beta}] = x^\top \beta$  and  $\text{Var}[x^\top \hat{\beta}] = x^\top (X^\top X)^{-1} x \sigma^2$ . Again, we must estimate  $\sigma$  and we can write  $\hat{\text{Var}}[x^\top \hat{\beta}] = x^\top (X^\top X)^{-1} x MSE$ .

**Exercise 3.13.** Under the assumptions of the normal linear regression model, show that for a fixed covariate vector  $x \in \mathbb{R}^p$ ,  $x^\top \hat{\beta}$  has a multivariate normal distribution and find its mean and variance. Argue that  $\frac{x^\top \hat{\beta} - x^\top \beta}{\sqrt{\hat{\text{Var}}[x^\top \hat{\beta}]}} \sim t_{dfE}$ .

It can be shown that a  $(1 - \alpha)100\%$  confidence interval for the mean response  $E[Y|X = x]$  is

$$x^\top \hat{\beta} \pm t_{dfE, \alpha/2} \sqrt{\hat{\text{Var}}[x^\top \hat{\beta}]}.$$

Similarly, if we want to test

$$H_0: E[Y|X = x] = \mu_0 \quad vs \quad E[Y|X = x] \neq \mu_0$$

we can do the following:

The observed test statistic is  $TS(x, \mu_0) = \frac{x^\top \hat{\beta} - \mu_0}{\sqrt{\hat{\text{Var}}[x^\top \hat{\beta}]}}$ . Observe that under the null hypothesis, we have that  $TS(x, \mu_0) \sim t_{dfE}$ . Therefore, the p-value is given by  $2 * \Pr(|TS(x, \mu_0)| > Z)$ .

Similar to the previous section, we can also perform one-sided tests:

- Right-sided test ( $H_1: x^\top \beta > \mu_0$ ): p-value  $\Pr(TS(x, \mu_0) > Z)$ .
- Left-sided test ( $H_1: x^\top \beta < \mu_0$ ): p-value  $\Pr(TS(x, \mu_0) < Z)$ .

We may also wish to predict what the response will be, given a new set of covariates. On top of that, we may again wish to quantify how much error there is in our prediction. For instance, what is the predicted body fat percentage of someone who is 160 pounds? Note that this differs from the previous section. In the previous section, we were interested in the average body fat percentage of someone who is 160 pounds. Here, we are interested in predicting the body fat percentage of a single, specific person, and not the average of the whole population.

Specifically, suppose that we have a subject whose covariates are given by  $z$ , but we do not know the value of the subjects response, which we can denote by  $Y_{new}$ . Then the true response is  $(Y_{new}|Z = z) = z^\top \beta + \epsilon_{new}$ .

Suppose we want to predict  $Y_{new}$  and give an idea of how much error is in our prediction. The predicted response is known, and is given by  $E[Y_{new}|Z = z] = z^\top \hat{\beta}$ . We have  $\text{Var}[Y_{new}|Z = z] = \text{Var}[z\hat{\beta}] + \text{Var}[\epsilon_{new}] = z^\top (X^\top X)^{-1} z \sigma^2 + \sigma^2$ . Therefore, the variation in a new response is the variation in our estimate of  $\beta$  plus the inherent population variation,  $\sigma^2$ . We have that this can be estimated with:  $\hat{\text{Var}}[Y_{new}|Z = z] = z^\top (X^\top X)^{-1} z MSE + MSE$ .

**Exercise 3.14.** Under the assumptions of the normal linear regression model, show that for a fixed covariate vector  $z \in \mathbb{R}^p$ ,  $Y_{new}|Z = z$  has a multivariate normal distribution and find it's mean and variance. Argue that given  $Z = z$ ,

$$\frac{Y_{new} - z^\top \beta}{\sqrt{\hat{\text{Var}}[Y_{new}]}} \sim t_{dfE}.$$

Therefore, the  $(1 - \alpha)100\%$  prediction interval for  $Y_{new}$  is given by:

$$z\hat{\beta} \pm t_{dfE, \alpha/2} \sqrt{z^\top (X^\top X)^{-1} z MSE + MSE}.$$

Note that the prediction interval is wider than that of the mean response interval for the same covariate vector  $z$ . That is because it is more difficult to predict the response for a specific person than it is to estimate a mean of a population. Furthermore, the interpretation of a prediction interval is different. A  $(1 - \alpha)100\%$  prediction interval can be interpreted it as follows. Given a  $(1 - \alpha)100\%$  prediction interval for  $Y_{new}|Z = z$ , say  $(a, b)$ , we say that the probability  $Y_{new}$  is in  $(a, b)$  is  $(1 - \alpha)100\%$ . Note that this differs substantially from a confidence interval!

**Example 3.6.** In Example 3.1, execute the following: What is a 95% confidence interval for the mean of someone who weighs 165 pounds? What is a 95% prediction interval for the BF% of someone who weighs 165 pounds? Interpret these intervals.

```

# Intervals are given as follows:

z <- data.frame(Weight=165)
predict(model, newdata = z, interval = 'confidence')

      fit      lwr      upr
1 13.85297 9.379675 18.32627

predict(model, newdata = z, interval = 'prediction')

      fit      lwr      upr
1 13.85297 -1.617547 29.32349

```

We are 95% confident the mean body fat of a person who weighs 165 pounds is in 13.8529704, 9.3796749, 18.3262658. There is a 95% probability that the body fat of a person who weights 165 pounds is in 13.8529704, -1.6175473, 29.323488 . Note that the prediction interval is wider!

### 3.3.8 Homework stop 4

**Exercise 3.15.** What is the difference between a prediction interval and an interval for the mean response ?

**Exercise 3.16.** Code the confidence intervals for the mean response and prediction interval without using the predict function.

**Exercise 3.17.** Complete the chapter 3 practice problems from the problem list.

### 3.3.9 Partial testing

We may be interested in executing the following hypothesis test:

$$H_0: (\beta_1, \dots, \beta_k) = 0 \quad vs \quad (\beta_1, \dots, \beta_k) \neq 0.$$

This amounts to testing whether the subset of variables  $(\beta_1, \dots, \beta_k)$  adds anything to the model beyond  $(\beta_{k+1}, \dots, \beta_p)$ . For example, you may be interested in whether location related covariates affect the price of Airbnb. The overall idea is to compare the reduced (null) model with  $p - k$  covariates to the complete (saturated, full) model (which contains all covariates).

Let's first review the  $F$ -test. We learned about the  $F$  test, which compares the following models:

$$Y|X = \beta^\top X + \epsilon \quad vs \quad Y|X = \beta_1 + \epsilon.$$

Here, the complete model is given by  $Y|X = \beta^\top X + \epsilon$  and the reduced model is given by  $Y|X = \beta_1 + \epsilon$ . Recall that the test statistic is given by

$$\frac{SSM/dfM}{SSE/dfE} = \frac{(SST - SSE)/(dfT - dfE)}{SSE/dfE},$$

where the degrees of freedom are in terms of the full model (not the null model). We could then rewrite this test statistic as

$$\frac{SSM_C/dfM_C}{SSE_C/dfE_C} = \frac{(SST_C - SSE_C)/(dfT_C - dfE_C)}{SSE_C/dfE_C},$$

where  $C$  stands for the complete model. (All that has changed is the notation, we added a  $C$  subscript.)

Now, note that  $SST = \sum_{i=1}^n (Y_i - \bar{Y})^2$  has nothing to do with what covariates are in the model. In other words,  $SST$  is always the same, not matter what covariates are in the model. Therefore,  $SST_C = SST_R = SST$ , where  $SST_R$  stands for the “sum of squares total” in the reduced model. In our example of the  $F$  test, the least squares estimate of  $\beta_1$  in the reduced model is  $\hat{\beta}_1 = \bar{Y}$  and the associated residual vector is given by  $\hat{\epsilon} = Y - \bar{Y}\mathbf{1}_n$ . But wait, observe that in this case, we have that  $\hat{\epsilon}^\top \hat{\epsilon} = SST$ ! Therefore, putting everything together, in this example, we have that  $SSM_C = SST_C - SSE_C = SSE_R - SSE_C$ . That is, the model sum of squares for the complete model is the difference between the sum-squared error in the reduced model and the sum-squared error in the complete model. We can then rewrite the test statistic as

$$\frac{(SSE_R - SSE_C)/(dfT_C - dfE_C)}{SSE_C/dfE_C}.$$

The difference  $SSE_R - SSE_C$  can be interpreted as the extra information gained from adding the covariates into the model OR total explained variations lost by going from the full model to the reduced model.

This idea can be generalized to develop a general method for testing hypotheses of the type:

$$H_0: (\beta_2, \dots, \beta_k) = 0 \quad vs \quad (\beta_2, \dots, \beta_k) \neq 0.$$

We complete the test as follows. Given a full model (which contains  $\beta_1, \dots, \beta_p$ ) and reduced model (which contains  $\{\beta_1, \beta_{k+1}, \dots, \beta_p\}$ ), define:

- $SSE_R - SSE_C = SSdrop$
- $dfE_R - dfE_C = dfdrop$
- $MSdrop = SSdrop/dfdrop$

Then the test statistic and p-value are given by:  $TS = MSdrop/MSE_C$  and  $\Pr(F_{dfdrop, dfE_C} \geq TS)$ , respectively.

We can interpret  $SSE_R - SSE_C$  as the extra info gained from adding the extra covariates into the model OR total explained variations lost by going from the full model to the reduced model. In addition,  $dfE_R - dfE_C = k - 1$ , or the number of covariates dropped from the full model to obtain the reduced model.

**i Note**

If you take  $k = 1$ , then this is equivalent to the  $t$ -test!

### 3.3.10 Partial coefficient of determination

We can define the **partial coefficient of determination** as follows:

$$\begin{aligned} R^2(X_1, \dots, X_{k-1} | X_k, \dots, X_p) &= (SSE_R - SSE_C)/SSE_R \\ &= SSdrop/SSE_R. \end{aligned}$$

You might also see the partial correlation coefficient:

$$R(X_1, \dots, X_{k-1} | X_k, \dots, X_p) = \sqrt{R^2(X_1, \dots, X_{k-1} | X_k, \dots, X_p)}.$$

This quantity is the extra proportion of variation explained from adding the covariates  $X_1, \dots, X_{k-1}$  to the model which already contains  $X_k, \dots, X_p$ .

**Example 3.7.** A researcher ran an experiment to see if YouTube, Facebook and newspaper ads would improve sales. Run the partial  $F$  test to see how online advertising affects sales. Compute and interpret the following quantities:

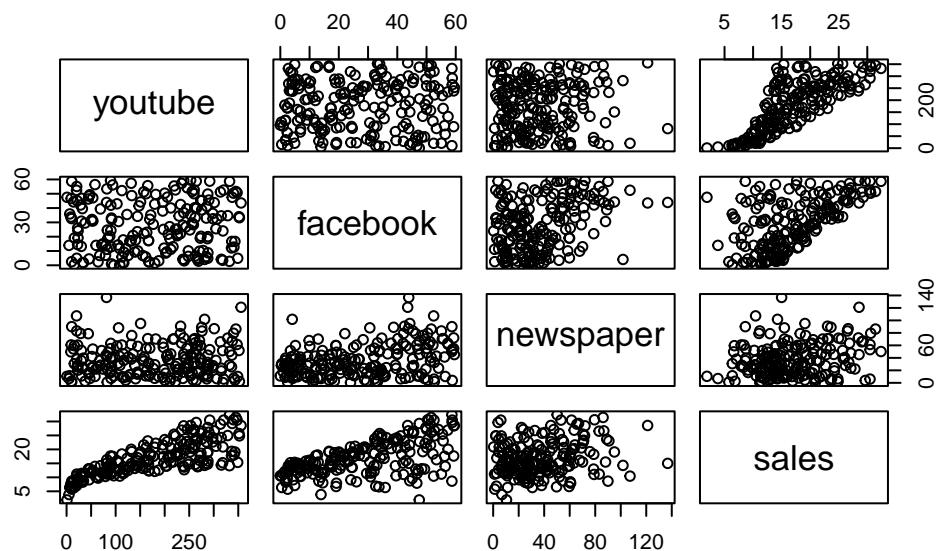
- $SSE_R - SSE_C = SSdrop$
- $dfE_R - dfE_C = dfdrop$
- $MSdrop = SSdrop/dfdrop$
- Test stat:  $TS = MSdrop/MSE_C$
- p-value:  $\Pr(F_{dfdrop, dfE_C} \geq TS)$
- Partial coefficient of determination

```
# install.packages('datarium')
data("marketing", package = "datarium")
# printing out first few rows
```

```
head(marketing, 4)
```

```
youtube facebook newspaper sales
1 276.12    45.36    83.04 26.52
2  53.40    47.16    54.12 12.48
3 20.64    55.08    83.16 11.16
4 181.80    49.56    70.20 22.20
```

```
plot(marketing)
```



```
#setting n to be a variable (sample size)
n=nrow(marketing)
```

```
# Estimation: How to get an estimate  $\hat{\beta}$  of  $\beta$ ?
# lm( sales~ , data= marketing)
full_model<- lm(sales ~ youtube+facebook+newspaper, data = marketing)
summary(full_model)
```

```

Call:
lm(formula = sales ~ youtube + facebook + newspaper, data = marketing)

Residuals:
    Min      1Q  Median      3Q     Max 
-10.5932 -1.0690  0.2902  1.4272  3.3951 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) 3.526667   0.374290   9.422 <2e-16 ***
youtube     0.045765   0.001395  32.809 <2e-16 ***
facebook    0.188530   0.008611  21.893 <2e-16 ***
newspaper   -0.001037   0.005871  -0.177    0.86    
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.023 on 196 degrees of freedom
Multiple R-squared:  0.8972,    Adjusted R-squared:  0.8956 
F-statistic: 570.3 on 3 and 196 DF,  p-value: < 2.2e-16

```

```

summ=summary(full_model)

full_model$coefficients

(Intercept)      youtube      facebook      newspaper
3.526667243  0.045764645  0.188530017 -0.001037493

MSE=summ$sigma^2

SSE_C=sum(summ$residuals^2)

# Inference: What is the error of  $\hat{\beta}$ ? Is  $f$  degenerate? I.e., is  $\beta=0$ ?

#regular ANOVA
summary(full_model)

```

Call:

```

lm(formula = sales ~ youtube + facebook + newspaper, data = marketing)

Residuals:
    Min      1Q  Median      3Q     Max 
-10.5932 -1.0690  0.2902  1.4272  3.3951 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) 3.526667   0.374290  9.422 <2e-16 ***
youtube     0.045765   0.001395 32.809 <2e-16 ***
facebook    0.188530   0.008611 21.893 <2e-16 ***
newspaper   -0.001037   0.005871 -0.177    0.86    
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.023 on 196 degrees of freedom
Multiple R-squared:  0.8972,    Adjusted R-squared:  0.8956 
F-statistic: 570.3 on 3 and 196 DF,  p-value: < 2.2e-16

#confidence intervals for beta coefficients
# confint.lm(full_model)

#Partial F Test
model_red=lm(sales ~ newspaper, data = marketing)
sum_reduced=summary(model_red)
MSER=sum_reduced$sigma^2
SSE_R=sum(sum_reduced$residuals^2)

SSdrop=SSE_R-SSE_C

MSEdrop=SSdrop/2
Fstat=MSEdrop/MSE

1-pf(Fstat,2,196)

[1] 0

part_test=anova(model_red,full_model); part_test

Analysis of Variance Table
```

```
Model 1: sales ~ newspaper
Model 2: sales ~ youtube + facebook + newspaper
  Res.Df    RSS Df Sum of Sq    F    Pr(>F)
1     198 7394.1
2     196 801.8  2     6592.3 805.71 < 2.2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
partial_c_det=SSdrop/SSE_R
```

```
SSER=sum(model_red$residuals*model_red$residuals); SSER
```

```
[1] 7394.119
```

```
dfer=model_red$df.residual; dfer
```

```
[1] 198
```

```
SSEC=sum(full_model$residuals*full_model$residuals); SSEC
```

```
[1] 801.8284
```

```
dfeC=full_model$df.residual; dfeC
```

```
[1] 196
```

```
SSdrop=SSER-SSEC; SSdrop
```

```
[1] 6592.29
```

```

dfdrop=dfer-dfeC

MSdrop=SSdrop/dfdrop; MSdrop

[1] 3296.145

R_online=SSdrop/SSER; R_online

[1] 0.8915586

part_test$F

[1] NA 805.7141

part_test$`Pr(>F)`

[1] NA 2.812622e-95

# Prediction: Predict any values if necessary.
# What if we have a 300$ budget and we only can pick one advertising method?
new_data=marketing[1:3,1:3]
new_data[1:3,]=diag(300,3)
predict(full_model,new_data)

      1          2          3
17.256061 60.085672 3.215419

# It's best to put our money in FB... meta?

# What about intervals?

predict(full_model,new_data, interval = 'confidence')

      fit      lwr      upr
1 17.256061 16.56191879 17.950203
2 60.085672 55.25061022 64.920734
3  3.215419 -0.09445737  6.525296

```

### 3.3.11 Another example

It's a good time to stop and do another example to review the topics covered so far.

**Example 3.8.** In the dataset `mtcars` we have the following variables:

- mpg: Miles/(US) gallon
- cyl: Number of cylinders
- disp: Displacement (cu.in.)
- hp: Gross horsepower
- drat: Rear axle ratio
- wt: Weight (1000 lbs)
- qsec: 1/4 mile time
- vs: V/S
- am: Transmission (0 = automatic, 1 = manual)
- gear: Number of forward gears
- carb: Number of carburetors

The data was extracted from the 1974 Motor Trend US magazine, and comprises fuel consumption and 10 aspects of automobile design and performance for 32 automobiles (1973–74 models). Overall, we would like to investigate the relationship between `mpg` and the following variables: `cyl`, `disp`, `hp`, `drat`, `wt`, `qsec`, `gear`, `carb`. Let's investigate the following questions:

1. Assume the normal MLR model. Store the covariate matrix and response in a variable.  
Fit a normal MLR model to the data. – That is use `lm()` to fit the model.
2. What are the least squares estimates? What is the *MSE*?
3. Generate the ANOVA table. Is the model significant?
4. Test if `drat` contributes anything to the model, adjusting for the other covariates. Test if `drat` is related to `mpg`, without adjusting for the other covariates.
5. Test if the subset of variables `gear`, `carb` contribute to the model jointly, adjusting for the remaining covariates. What is the partial coefficient of determination? Interpret the partial coefficient of determination. Test if the subset of variables `gear`, `carb` contribute to the model jointly, without adjusting for the remaining covariates.
6. Compute a confidence interval for the mean `mpg` of cars with the following set of covariate values 6.6, 176, 121, 4.29, 2.882, 18.106, 0, 1.1, 4.4, 4.4. Compute a prediction interval for the `mpg` of a car with the above set of covariate values.
7. Compute a confidence interval for the coefficient for `disp`.
8. Compute and interpret the coefficient of determination.

```
data("mtcars")
head(mtcars)
```

```

          mpg cyl disp  hp drat    wt  qsec vs am gear carb
Mazda RX4     21.0   6 160 110 3.90 2.620 16.46  0  1    4    4
Mazda RX4 Wag 21.0   6 160 110 3.90 2.875 17.02  0  1    4    4
Datsun 710    22.8   4 108  93 3.85 2.320 18.61  1  1    4    1
Hornet 4 Drive 21.4   6 258 110 3.08 3.215 19.44  1  0    3    1
Hornet Sportabout 18.7   8 360 175 3.15 3.440 17.02  0  0    3    2
Valiant      18.1   6 225 105 2.76 3.460 20.22  1  0    3    1

```

```
dim(mtcars)
```

```
[1] 32 11
```

```
# 1.
# response~all variables minus the two variables we will not include
model=lm(mpg~.-vs-am,data=mtcars)
summ=summary(model)
summ
```

Call:

```
lm(formula = mpg ~ . - vs - am, data = mtcars)
```

Residuals:

Min	1Q	Median	3Q	Max
-3.0230	-1.6874	-0.4109	0.9640	5.4400

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	17.88964	17.81996	1.004	0.3259
cyl	-0.41460	0.95765	-0.433	0.6691
disp	0.01293	0.01758	0.736	0.4694
hp	-0.02085	0.02072	-1.006	0.3248
drat	1.10110	1.59806	0.689	0.4977
wt	-3.92065	1.86174	-2.106	0.0463 *
qsec	0.54146	0.62122	0.872	0.3924
gear	1.23321	1.40238	0.879	0.3883
carb	-0.25510	0.81563	-0.313	0.7573

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

```
Residual standard error: 2.622 on 23 degrees of freedom
Multiple R-squared:  0.8596,    Adjusted R-squared:  0.8107
F-statistic: 17.6 on 8 and 23 DF,  p-value: 4.226e-08
```

```
X=model.matrix(model)
Y=mtcars$mpg
X[1:5,]
```

	(Intercept)	cyl	disp	hp	drat	wt	qsec	gear	carb
Mazda RX4	1	6	160	110	3.90	2.620	16.46	4	4
Mazda RX4 Wag	1	6	160	110	3.90	2.875	17.02	4	4
Datsun 710	1	4	108	93	3.85	2.320	18.61	4	1
Hornet 4 Drive	1	6	258	110	3.08	3.215	19.44	3	1
Hornet Sportabout	1	8	360	175	3.15	3.440	17.02	3	2

```
Y
```

```
[1] 21.0 21.0 22.8 21.4 18.7 18.1 14.3 24.4 22.8 19.2 17.8 16.4 17.3 15.2 10.4
[16] 10.4 14.7 32.4 30.4 33.9 21.5 15.5 15.2 13.3 19.2 27.3 26.0 30.4 15.8 19.7
[31] 15.0 21.4
```

```
# 2.
LSE=coef(model)
LSE
```

(Intercept)	cyl	disp	hp	drat	wt
17.88963741	-0.41459575	0.01293240	-0.02084886	1.10109551	-3.92064847
qsec	gear	carb			
0.54145693	1.23321026	-0.25509911			

```
MSE=summ$sigma^2
MSE
```

```
[1] 6.874941
```

```
# 3.
null_model=lm(mpg~1,data=mtcars)
anova(null_model,model)
```

#### Analysis of Variance Table

```
Model 1: mpg ~ 1
Model 2: mpg ~ (cyl + disp + hp + drat + wt + qsec + vs + am + gear +
carb) - vs - am
Res.Df   RSS Df Sum of Sq    F    Pr(>F)
1     31 1126.05
2     23 158.12  8    967.92 17.599 4.226e-08 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
# 4.
# Notice the p value is 0.5 , not sign.
summ$coefficients['drat',]
```

Estimate	Std. Error	t value	Pr(> t )
1.1010955	1.5980601	0.6890201	0.4977032

```
drat=lm(mpg~drat,,data=mtcars)
# Notice the p value is 1.78e-05 , sig! explain this difference!
summary(drat)
```

Call:  
`lm(formula = mpg ~ drat, data = mtcars)`

Residuals:  

Min	1Q	Median	3Q	Max
-9.0775	-2.6803	-0.2095	2.2976	9.0225

Coefficients:  

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-7.525	5.477	-1.374	0.18
drat	7.678	1.507	5.096	1.78e-05 ***
---				

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 4.485 on 30 degrees of freedom
Multiple R-squared: 0.464, Adjusted R-squared: 0.4461
F-statistic: 25.97 on 1 and 30 DF, p-value: 1.776e-05
```

```
# 5.
red_model=lm(mpg~.-vs-am-gear-carb,data=mtcars)
anova(red_model,model)
```

#### Analysis of Variance Table

```
Model 1: mpg ~ (cyl + disp + hp + drat + wt + qsec + vs + am + gear +
                 carb) - vs - am - gear - carb
Model 2: mpg ~ (cyl + disp + hp + drat + wt + qsec + vs + am + gear +
                 carb) - vs - am
  Res.Df   RSS Df Sum of Sq    F Pr(>F)
1     25 163.48
2     23 158.12  2      5.3532 0.3893 0.6819
```

```
ob=anova(red_model,model)
ob$`Sum of Sq`[2]/ob$RSS[1]
```

```
[1] 0.0327457
```

```
# 3.7% of the variation in mpg is explained from adding the covariate gear and carb to the
```

```
# 6.
new_ob=c(6.6,176,121,4.29,2.882,18.106,0,1.1,4.4,4.4)
new_ob=matrix(new_ob,nrow=1,ncol=length(new_ob))
colnames(new_ob)=names(mtcars[1,-1])
new_ob=data.frame(new_ob)
predict(model,new_ob, interval = 'confidence')
```

```
       fit      lwr      upr
1 22.43839 18.49468 26.38211
```

```
predict(model,new_ob, interval = 'prediction')
```

```

      fit      lwr      upr
1 22.43839 15.7322 29.14459

# 7.
confint(model)

          2.5 %    97.5 %
(Intercept) -18.97375462 54.75302945
cyl         -2.39565252  1.56646102
disp        -0.02343129  0.04929609
hp          -0.06371601  0.02201829
drat        -2.20474377  4.40693480
wt          -7.77195651 -0.06934042
qsec        -0.74362628  1.82654014
gear        -1.66782660  4.13424711
carb        -1.94235037  1.43215215

```

```

#8.
summ$r.squared

```

[1] 0.8595764

```
# 85% of the variation in mpg is explained by cyl, disp, hp, drat, wt, qsec, gear and carb
```

**Exercise 3.18.** Interpret all of the above quantites.

### 3.4 Checking model assumptions

We learned how to test significance of one or multiple variables, compute confidence intervals for the estimated coefficients, mean response, and predicted response. All the methods rely on the assumptions! Recall that we assume 1. The relationship is linear  $Y|X = X\beta + \epsilon$ , 2.  $\forall i \in [n], \epsilon_i \sim \mathcal{N}(0, \sigma^2)$  3.  $\epsilon_i \perp \epsilon_j$  for  $i \neq j, i, j \in [n]$ .

We now briefly discuss how to use the data to check if these assumptions are appropriate. We will cover this in more detail in the next chapter.

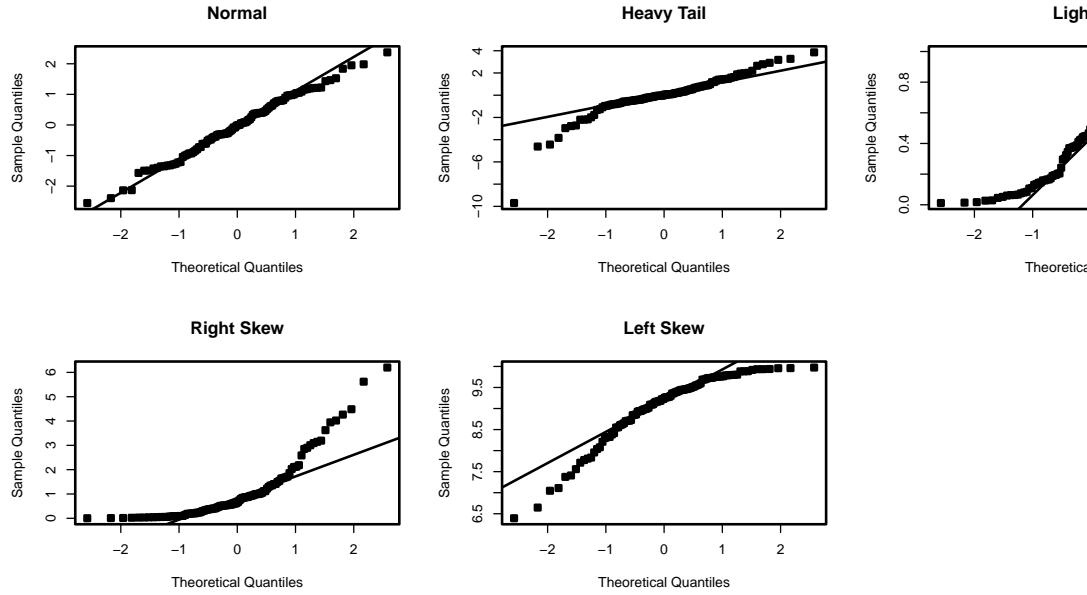
### 3.4.1 Checking normality

We do not know  $\epsilon$ , however, we do know  $\hat{\epsilon}$ , which is our best proxy for the true random error vector  $\epsilon$ . To check if the true random error vector is normally distributed we can use histograms and quantile-quantile plots. More specifically, if the histogram of the residuals looks more or less bell-shaped, with tails similar to the normal PDF, then the assumption of normality is valid.

Recall that a qq-plot compares the quantiles of the sample to the quantiles of the theoretical normal distribution. The x-axis represents the theoretical quantiles. The y-axis represents the sample quantiles. If the sample follows a normal distribution, the points in the qq-plot will approximately lie on a line.

Interpretation:

- Straight Line: If the points lie on or near the straight line, the sample appears normal.
- Heavy Tails: Points deviating upwards or downwards at the ends suggest the sample has heavier or lighter tails than the normal distribution.
- S-Shape: Points forming an S-shape indicate the sample has lighter tails and a heavier center than the normal distribution.



See below for an example:

Note that you will always have some deviation at the ends of the line in the qq-plot.

**Example 3.9.** In examples Example 3.1 and Example 3.7, check that the normality assumption is valid.

```

# Make the data frame
Weight=c(175 , 181 , 200 , 159 , 196 , 192 , 205 , 173 , 187 , 188 ,
       188 , 240 , 175 , 168 , 246 , 160 , 215 , 159 , 146 , 219 )
BodyFat =c(6 , 21 , 15 , 6 , 22 , 31 , 32 , 21 , 25 , 30 ,
          10 , 20 , 22 , 9 , 38 , 10 , 27 , 12 , 10 , 28 )

df=data.frame(cbind(Weight=Weight,BodyFat=BodyFat))
model= lm(BodyFat ~Weight, data = df)
summary(model)

```

Call:

```
lm(formula = BodyFat ~ Weight, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-12.5935	-5.7904	0.6536	5.2731	10.4004

Coefficients:

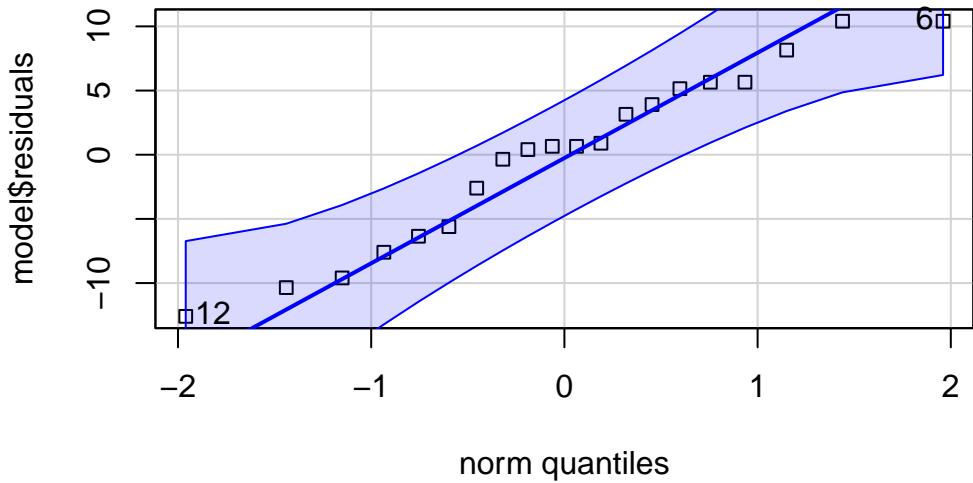
	Estimate	Std. Error	t value	Pr(> t )							
(Intercept)	-27.37626	11.54743	-2.371	0.029119 *							
Weight	0.24987	0.06065	4.120	0.000643 ***							
---											
Signif. codes:	0	'***'	0.001	'**'	0.01	'*'	0.05	'. '	0.1	' '	1

Residual standard error: 7.049 on 18 degrees of freedom

Multiple R-squared: 0.4853, Adjusted R-squared: 0.4567

F-statistic: 16.97 on 1 and 18 DF, p-value: 0.0006434

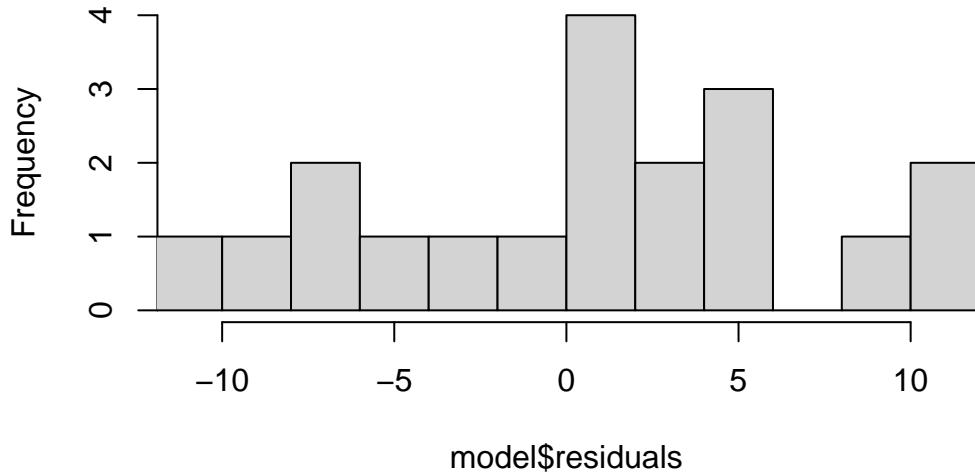
```
car::qqPlot(model$residuals,pch=22)
```



```
[1] 12 6
```

```
hist(model$residuals, breaks=10, xlim=c(-11,11))
```

## Histogram of model\$residuals



```
# This appears okay!

# Let's do the next example
# install.packages('datarium')
data("marketing", package = "datarium")

# lm( sales~    , data= marketing)
full_model<- lm(sales ~ youtube+facebook+newspaper, data = marketing)
summary(full_model)
```

Call:

```
lm(formula = sales ~ youtube + facebook + newspaper, data = marketing)
```

Residuals:

Min	1Q	Median	3Q	Max
-10.5932	-1.0690	0.2902	1.4272	3.3951

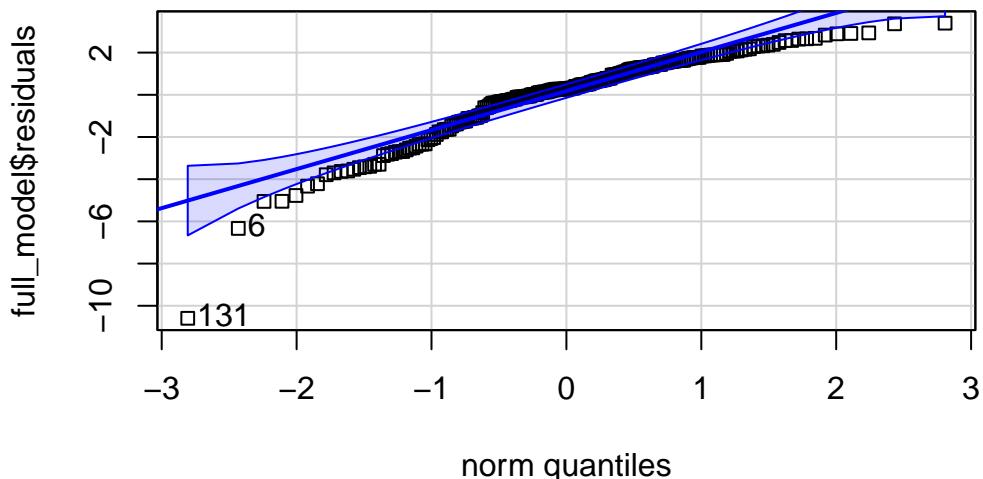
Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.526667	0.374290	9.422	<2e-16 ***

```
youtube      0.045765   0.001395   32.809   <2e-16 ***  
facebook     0.188530   0.008611   21.893   <2e-16 ***  
newspaper    -0.001037  0.005871   -0.177    0.86  
---  
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

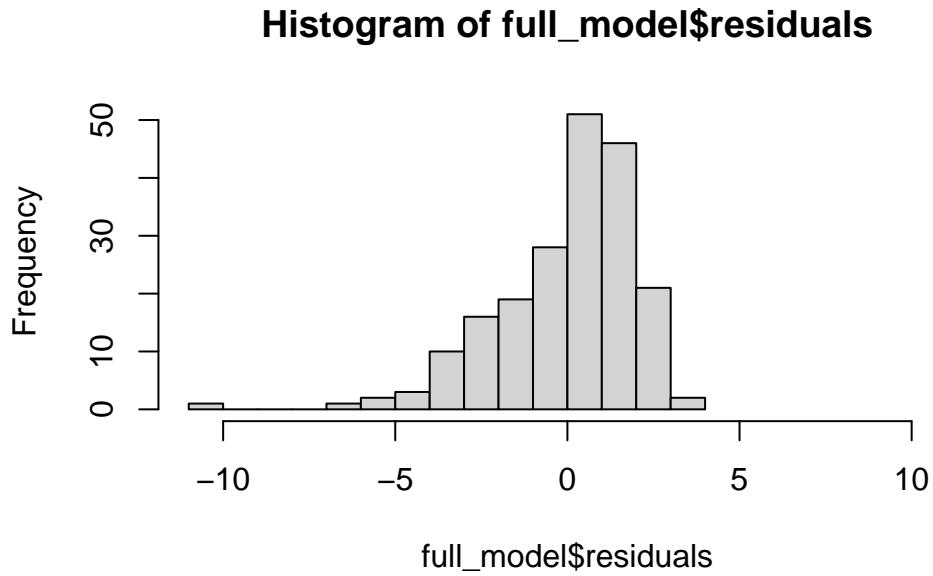
```
Residual standard error: 2.023 on 196 degrees of freedom  
Multiple R-squared:  0.8972,    Adjusted R-squared:  0.8956  
F-statistic: 570.3 on 3 and 196 DF,  p-value: < 2.2e-16
```

```
# Not great.  
car::qqPlot(full_model$residuals,pch=22)
```



```
[1] 131    6
```

```
hist(full_model$residuals,breaks=10,xlim=c(-11,11))
```



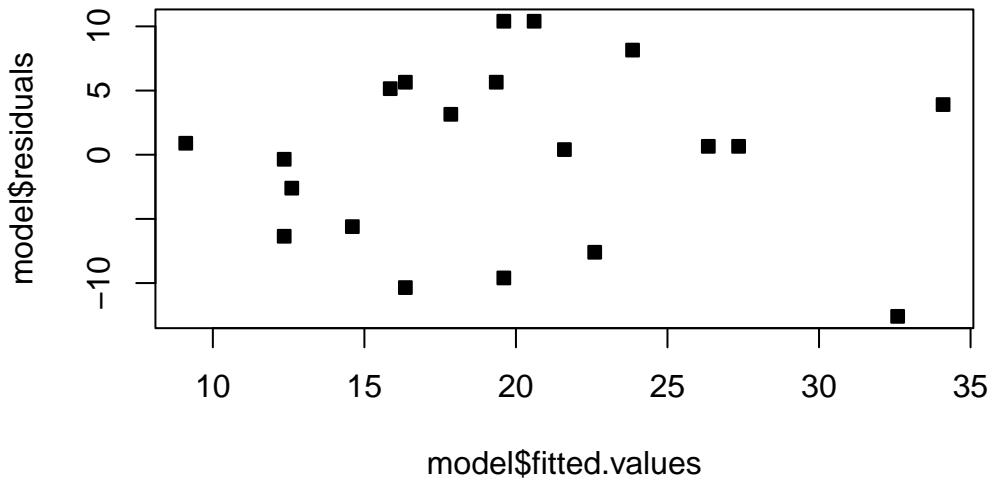
### 3.4.2 Checking the other assumptions

To check the remaining assumptions (constant variance, independence of residuals, zero mean and linear relationship), we can use some other diagnostic plots.

One plot is that of the fitted values  $\hat{Y}$  ( $x$ -axis) against the residuals  $\hat{\epsilon}$  ( $y$ -axis). If the error depends on  $\hat{y}$ , then the identically distributed assumption on the errors is probably not valid. If the assumptions are valid, we should observe on the plots that at all levels of the response, the mean of the residuals is 0 and the variance remains the same. Thus, we should see a horizontal band centered at 0 containing the observations.

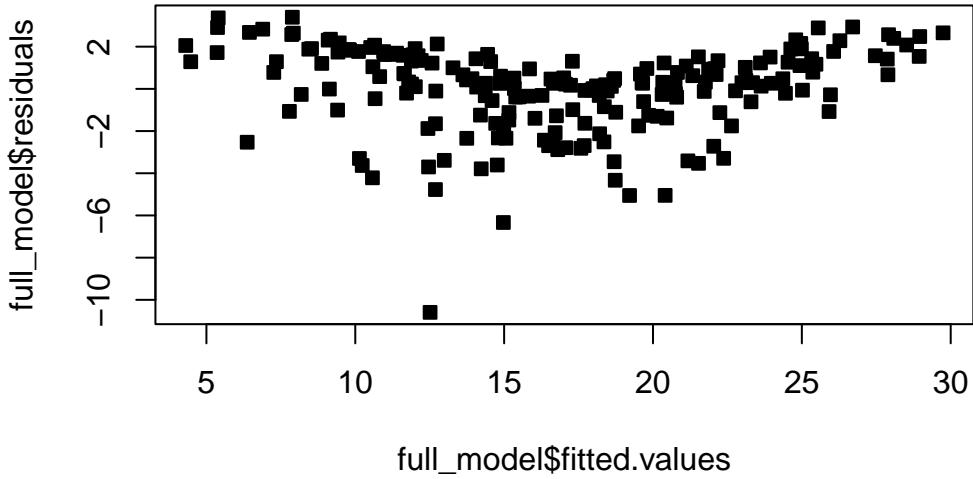
This appears to be the case in the body fat example:

```
plot(model$fitted.values, model$residuals, pch=22, bg=1)
```



Observe that in the marketing example, the residuals admit a pattern. This usually indicates either a non-linear relationship with the covariates, or an important covariate is missing. In this case, we would say the assumption of identically distributed errors is violated.

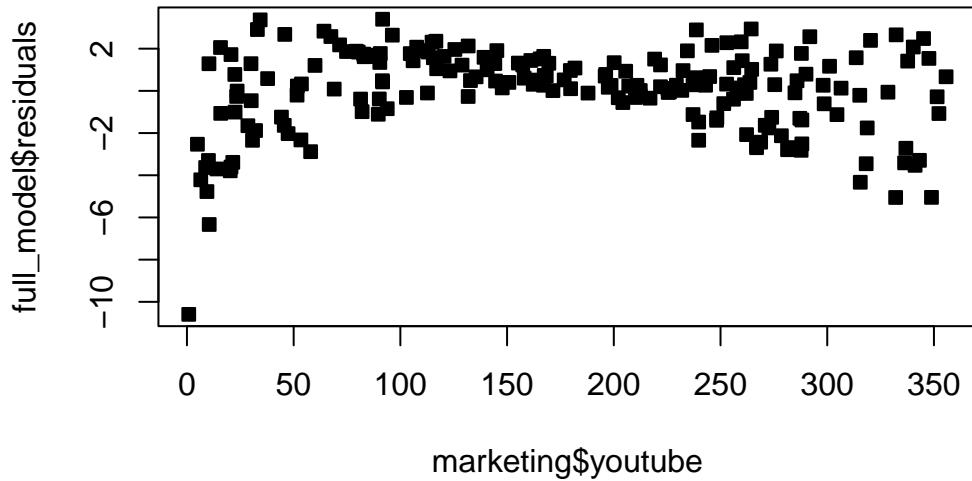
```
plot(full_model$fitted.values,full_model$residuals,pch=22, bg=1)
```



Plotting the residuals against the covariates can reveal dependence between the errors. For instance, if time is a covariate, you can plot the residuals over time to see if they have any relationship with time. If there appears to be dependence among the residuals, then the assumptions of the model are violated. That is, in these plots we should also see a horizontal band centered at 0 containing the observations. If not, then the residuals have a relationship with the given covariate.

Be VERY careful about the scale of your plot, as it can affect your interpretation. Zooming out or in too much can make everything look fine. In addition, the  $y$ -axis not being centered at 0 can cause you to misinterpret the plot.

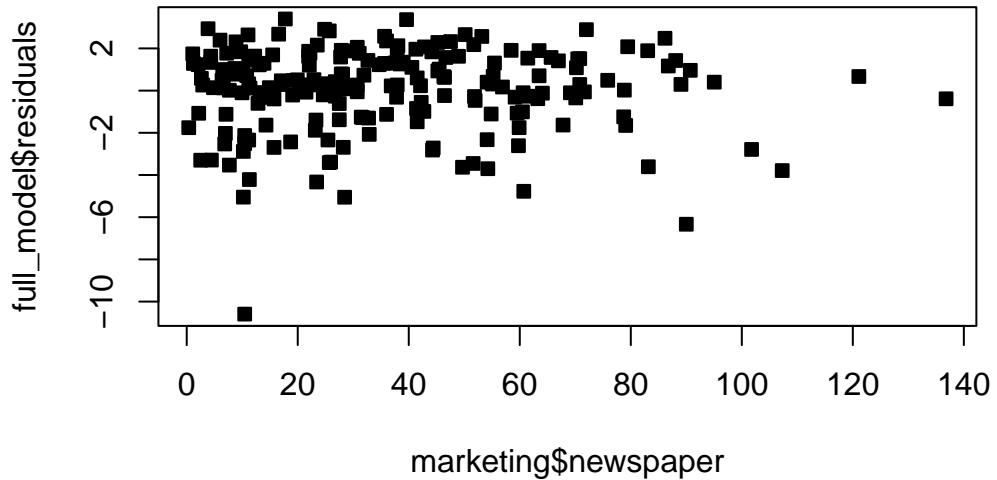
```
plot(marketing$youtube,full_model$residuals,pch=22,bg=1)
```



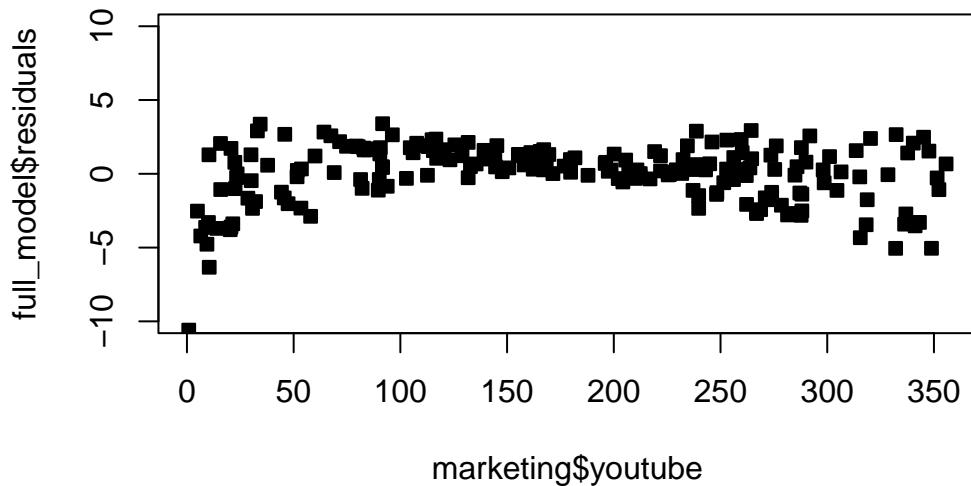
```
plot(marketing$facebook,full_model$residuals,pch=22, bg=1)
```



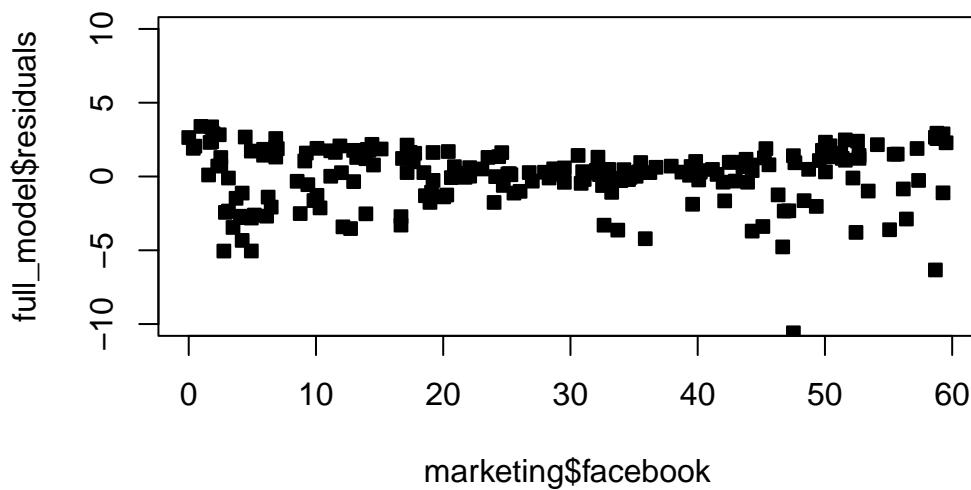
```
plot(marketing$newspaper,full_model$residuals,pch=22, bg=1)
```



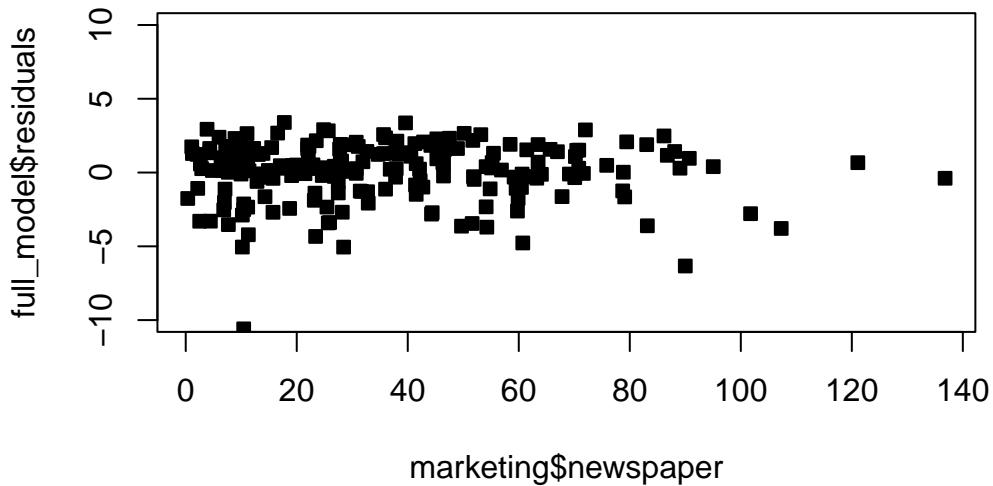
```
plot(marketing$youtube,full_model$residuals,pch=22, bg=1,ylim=c(-10,10))
```



```
plot(marketing$facebook,full_model$residuals,pch=22, bg=1,ylim=c(-10,10))
```



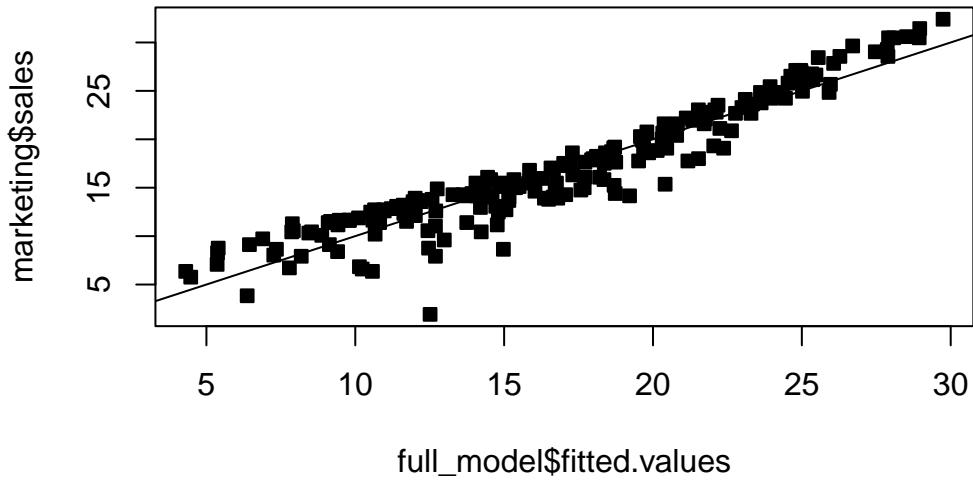
```
plot(marketing$newspaper,full_model$residuals,pch=22, bg=1, ylim=c(-10,10))
```



Notice how the newspaper plot changes with the new axis limits. It appears that the variance of the error is changing with the value of the Facebook and Youtube budgets.

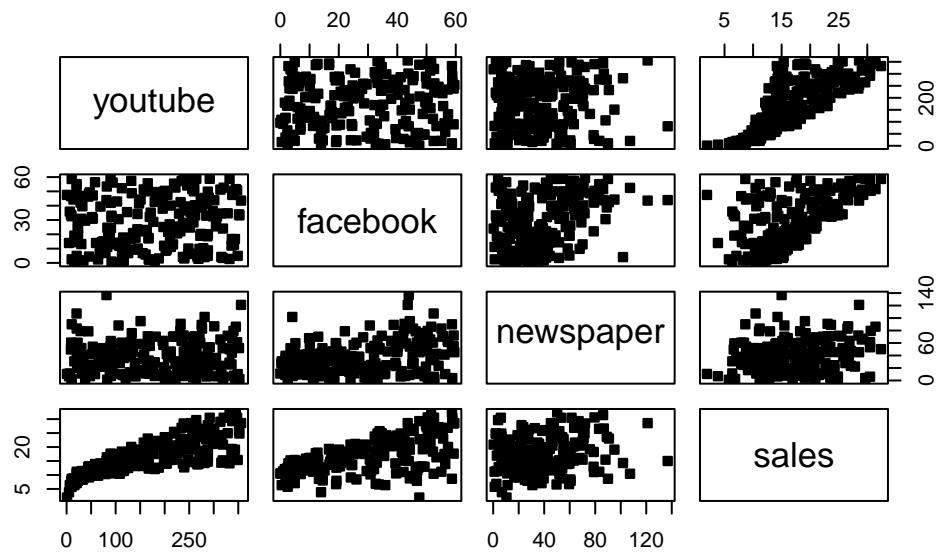
Another plot is that of the fitted values against the response. This gives an idea of the overall fit of the model. We should observe the points scatters around the line  $y = x$ .

```
plot(full_model$fitted.values,marketing$sales,pch=22, bg=1)
abline(0,1)
```



Notice that the line is slightly curved above the line at the ends. This means that at high and low values, the actual sales are empirically greater than as predicted by the model. Let's plot the actual data.

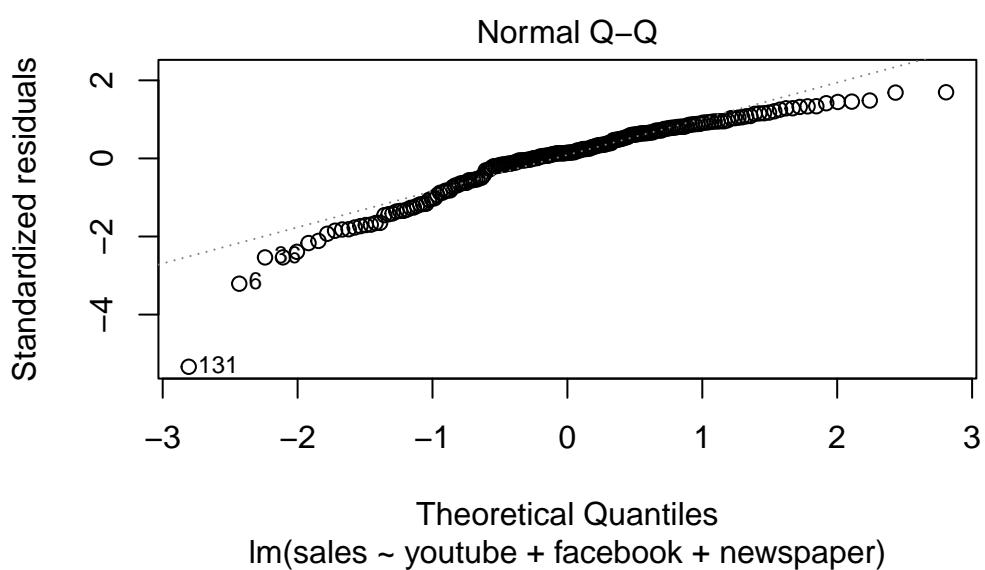
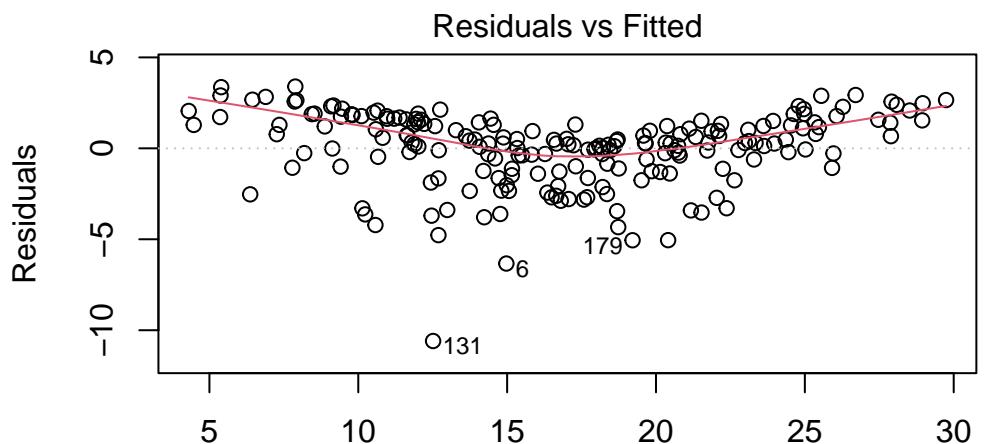
```
plot(marketing, pch=22, bg=1)
```

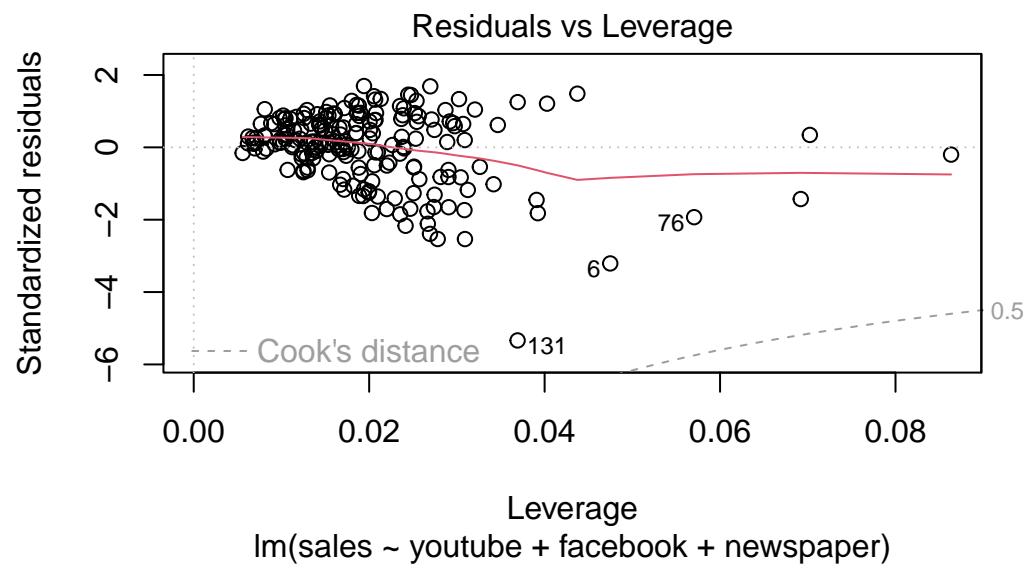
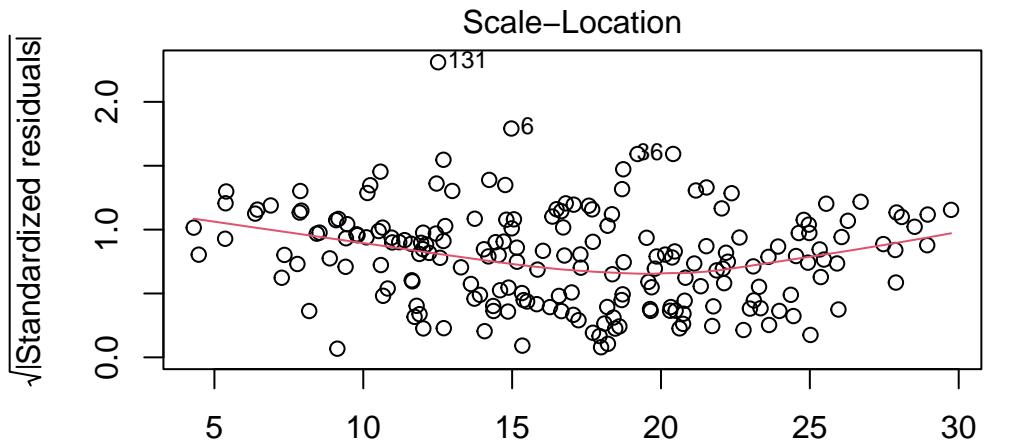


In this case, Youtube and Facebook spending seems to have a nonlinear relationship with sales. We will see how to remedy this in later chapters.

As a final note, observe that we can put the `model` object in the `plot()` function to obtain the diagnostic plots.

```
plot(full_model)
```





We will learn in later chapters how to check the assumptions more thoroughly and how to remedy violations of the assumptions.

### 3.4.3 Homework stop 5

Complete the assigned textbook problems for Chapter 4.

**Exercise 3.19.** List the assumptions for the normal MLR model and the MLR model. Write down how you would check each assumption.

## 3.5 Simple linear regression

A special case of the multiple linear regression is **simple linear regression**. A simple linear regression model is a regression model with **one explanatory variable**:  $Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$ .

$$y = \begin{pmatrix} y_1 \\ \vdots \\ y_n \end{pmatrix}, X = \begin{pmatrix} 1 & x_1 \\ \vdots & \vdots \\ 1 & x_n \end{pmatrix}, \beta = \begin{pmatrix} \beta_0 \\ \beta_1 \end{pmatrix}, \epsilon = \begin{pmatrix} \epsilon_1 \\ \vdots \\ \epsilon_n \end{pmatrix}.$$

### 3.5.1 Estimated Coefficients

In this case, following some matrix manipulations (verify this for homework), we have

$$X^\top X = \begin{pmatrix} n & \sum_{i=1}^n x_i \\ \sum_{i=1}^n x_i & \sum_{i=1}^n x_i^2 \end{pmatrix}, X^\top y = \begin{pmatrix} \sum_{i=1}^n y_i \\ \sum_{i=1}^n x_i y_i \end{pmatrix}.$$

Now, recall if

$$A = \begin{bmatrix} a & b \\ c & d \end{bmatrix}$$

then

$$A^{-1} = \frac{1}{ad - bc} \begin{bmatrix} d & -b \\ -c & a \end{bmatrix}.$$

From MATH 1131 (or simple algebraic manipulation), we know

$$\begin{aligned} \sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y}) &= \sum_{i=1}^n x_i y_i - n\bar{x}\bar{y} = \sum_{i=1}^n x_i y_i - n^{-1} \left( \sum_{i=1}^n x_i \right) \left( \sum_{i=1}^n y_i \right) \\ \sum_{i=1}^n (x_i - \bar{x})^2 &= \sum_{i=1}^n x_i^2 - n\bar{x}^2 = \sum_{i=1}^n x_i^2 - n^{-1} \left( \sum_{i=1}^n x_i \right)^2. \end{aligned}$$

Therefore

$$\begin{aligned}(X^\top X)^{-1} &= \frac{1}{n \sum_{i=1}^n x_i^2 - (\sum_{i=1}^n x_i)^2} \begin{pmatrix} \sum_{i=1}^n x_i^2 & -\sum_{i=1}^n x_i \\ -\sum_{i=1}^n x_i & n \end{pmatrix} \\ &= \frac{1}{n \sum_{i=1}^n (x_i - \bar{x})^2} \begin{pmatrix} \sum_{i=1}^n x_i^2 & -\sum_{i=1}^n x_i \\ -\sum_{i=1}^n x_i & n \end{pmatrix}.\end{aligned}$$

To summarize:

$$\begin{aligned}X^\top X &= \begin{bmatrix} n & \sum_{i=1}^n x_i \\ \sum_{i=1}^n x_i & \sum_{i=1}^n x_i^2 \end{bmatrix} \\ X^\top y &= \begin{bmatrix} \sum_{i=1}^n y_i \\ \sum_{i=1}^n x_i y_i \end{bmatrix} \\ (X^\top X)^{-1} &= \frac{1}{n \sum_{i=1}^n (x_i - \bar{x})^2} \begin{bmatrix} \sum_{i=1}^n x_i^2 & -\sum_{i=1}^n x_i \\ -\sum_{i=1}^n x_i & n \end{bmatrix}\end{aligned}$$

Now, we have that

$$\begin{aligned}\hat{\beta} &= \begin{pmatrix} \hat{\beta}_0 \\ \hat{\beta}_1 \end{pmatrix} = (X^\top X)^{-1} X^\top y \\ &= \frac{1}{n \sum_{i=1}^n (x_i - \bar{x})^2} \begin{pmatrix} \sum_{i=1}^n x_i^2 \sum_{i=1}^n y_i - \sum_{i=1}^n x_i \sum_{i=1}^n x_i y_i \\ -\sum_{i=1}^n x_i \sum_{i=1}^n y_i + n \sum_{i=1}^n x_i y_i \end{pmatrix}.\end{aligned}$$

Now,

$$\hat{\beta}_1 = \frac{1}{n \sum_{i=1}^n (x_i - \bar{x})^2} \left( -\sum_{i=1}^n x_i \sum_{i=1}^n y_i + n \sum_{i=1}^n x_i y_i \right).$$

**Exercise 3.20.** Let's show that

$$\hat{\beta}_1 = \frac{n \sum_{i=1}^n x_i y_i - \sum_{i=1}^n x_i \sum_{i=1}^n y_i}{n \sum_{i=1}^n (x_i - \bar{x})^2} = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sum_{i=1}^n (x_i - \bar{x})^2}.$$

Does this look familiar? We see that,

$$\hat{\beta}_1 = \text{cov}(X, Y) \frac{\hat{\sigma}_y}{\hat{\sigma}_x},$$

where  $\text{cov}(X, Y)$  is the estimated correlation between  $X$  and  $Y$ . Let's interpret this:

1. If  $\text{cov}(X, Y) \approx 0$  then  $\hat{\beta}_1 \approx 0$  - low correlation implies an estimated slope close to 0.
2. The estimated coefficient  $\hat{\beta}_1$  is the product of the estimated correlation between  $X$  and  $Y$  and the ratio of the estimated standard deviation of  $Y$  to that of  $X$ .

Now, looking at the intercept term, we have

$$\hat{\beta}_0 = \frac{1}{n \sum_{i=1}^n (x_i - \bar{x})^2} \left( \sum_{i=1}^n x_i^2 \sum_{i=1}^n y_i - \sum_{i=1}^n x_i \sum_{i=1}^n x_i y_i \right).$$

**Exercise 3.21.** Show that

$$\hat{\beta}_0 = \bar{y} - \hat{\beta}_1 \bar{x}.$$

Observe that the intercept is the mean of  $Y$  minus the mean of  $X$  times the estimated slope. In essence, it tells us that the intercept ( $\hat{\beta}_0$ ) represents the value of  $(X)$  when  $(X)$  is at its mean value ( $(\bar{X})$ ) and that  $(\bar{X})$  is adjusted by subtracting the contribution of  $(\hat{\beta}_1 \bar{X})$ .

This adjustment ensures that the regression line passes through the point  $((\bar{X}, \bar{X}))$ , which is the point of averages for the data.

### 3.5.2 Inference in SLR

We can also simplify the values used for inference in the SLR model. Recall that  $\text{Var} [\hat{\beta}] = (X^\top X)^{-1} \sigma^2$ , and so we have

$$\begin{aligned} \text{Var} [\hat{\beta}_0] &= \frac{\sum_{i=1}^n x_i^2}{n \sum_{i=1}^n (x_i - \bar{x})^2} \sigma^2 = \frac{\sum_{i=1}^n x_i^2 - n\bar{x}^2 + n\bar{x}^2}{n \sum_{i=1}^n (x_i - \bar{x})^2} \sigma^2 \\ &= \left[ \frac{1}{n} + \frac{\bar{x}^2}{\sum_{i=1}^n (x_i - \bar{x})^2} \right] \sigma^2 \\ \text{Var} [\hat{\beta}_1] &= \frac{1}{\sum_{i=1}^n (x_i - \bar{x})^2} \sigma^2 \\ \text{cov}(\hat{\beta}_0, \hat{\beta}_1) &= -\frac{\bar{x}}{\sum_{i=1}^n (x_i - \bar{x})^2} \sigma^2. \end{aligned}$$

We know from previous sections that a  $(1 - \alpha)100$  confidence interval of  $\beta_i$ , where  $i = 0, 1$ , is

$$\hat{\beta}_i \pm t_{df_E, \alpha/2} \sqrt{\widehat{\text{var}}(\hat{\beta}_i)}.$$

Similarly, let  $\beta_i^0$  be a hypothesized value of  $\beta_i$ , for  $i = 0, 1$ . If we want to test whether  $\beta_i = \beta_i^0$ , then the observed test statistic is given by

$$\frac{\hat{\beta}_i - \beta_i^0}{\sqrt{\widehat{\text{var}}(\hat{\beta}_i)}},$$

and the corresponding  $p$ -value is obtained via the  $t_{df_E}$  distribution as usual.

### **i** Note

Similarly, inference for the mean response and predictions can be obtained. We can also simplify the ANOVA table,  $R^2$ , etc. For instance, the  $R^2$  is the square of the sample correlation coefficient between  $X$  and  $Y$ .

### 3.5.3 Inference for the correlation coefficient

If we are interested in doing a hypothesis test, or constructing confidence intervals for the correlation between two variables, say  $X$  and  $Y$ , we can use the simple linear regression model.

We have already derived the relationship between the estimated correlation coefficient and the estimated slope of the simple linear regression model. More specifically, if the estimated correlation coefficient is 0, then the estimated slope of the simple linear regression is 0. One can show that the same relationship holds at the population level:  $\beta_1 = \rho\sigma_y/\sigma_x$ , where  $\rho = \text{corr}[X, Y]$ .

Now, suppose that we want to test if  $H_0 : \rho = 0$  versus  $H_a : \rho \neq 0$ . Using the fact that  $\beta_1 = \rho\sigma_y/\sigma_x$ , the above test is equivalent to the statement  $H_0 : \beta_1 = 0$  versus  $H_a : \beta_1 \neq 0$ . Therefore, we can just test if the slope parameter in the model  $Y|X = \beta_0 + \beta_1 X + \epsilon$  is 0.

Letting  $\hat{\rho} = \text{corr}(X, Y)$  The observed test statistic is then:

$$\frac{\hat{\beta}_1}{\sqrt{\widehat{\text{var}}(\hat{\beta}_1)}} = \frac{\hat{\rho}\sqrt{n-2}}{\sqrt{1-\hat{\rho}^2}},$$

and the corresponding  $p$ -value is obtained based on the  $t_{dfE}$  distribution.

However, when the hypothesized value for  $\rho$  is non-zero, the problem becomes very complicated. The exact distribution of  $\hat{\rho}$  is extremely difficult to obtain under the null hypothesis. The following procedure gives an approximation of the distribution of a function of  $\hat{\rho}$  under the null hypothesis. In particular, Fisher suggested the transformation for  $\rho \in (0, 1)$ ,

$$\theta = \frac{1}{2} \log \frac{1+\rho}{1-\rho}.$$

Then

$$\hat{\theta} = \frac{1}{2} \log \frac{1+\hat{\rho}}{1-\hat{\rho}},$$

is an estimate of  $\theta$ , where  $\hat{\theta}$  is approximately distributed as normal with mean  $\theta$  and variance  $\frac{1}{n-3}$ . Hence, an approximate  $(1 - \alpha)100$  confidence interval of  $\theta$  is

$$\hat{\theta} \pm z_{\alpha/2} \sqrt{\frac{1}{n-3}},$$

and the corresponding confidence interval of  $\rho$  can be obtained by the inverse transformation. Similarly, if the hypothesized value of  $\rho$  is  $\rho_0$ , then the hypothesized value of  $\theta$  is  $\theta_0 = \frac{1}{2} \log \frac{1+\rho_0}{1-\rho_0}$ . The observed test statistic can be obtained and the corresponding  $p$ -value can be obtained based on the standard normal distribution.

**Example 3.10.** In Example 3.1 test if the correlation between body fat and weight is 0. Next, test if the correlation is greater than 1/2. Construct a 95% CI for  $\rho$ .

```
#####
##### Exploratory
Weight=c(175 , 181 , 200 , 159 , 196 , 192 , 205 ,
       173 , 187 , 188 , 188 , 240 , 175 , 168 ,
       246 , 160 , 215 , 159 , 146 , 219 )
BodyFat =c(6 , 21 , 15 , 6 , 22 , 31 , 32 , 21 , 25 ,
          30 , 10 , 20 , 22 , 9 , 38 , 10 , 27 , 12 , 10 , 28 )

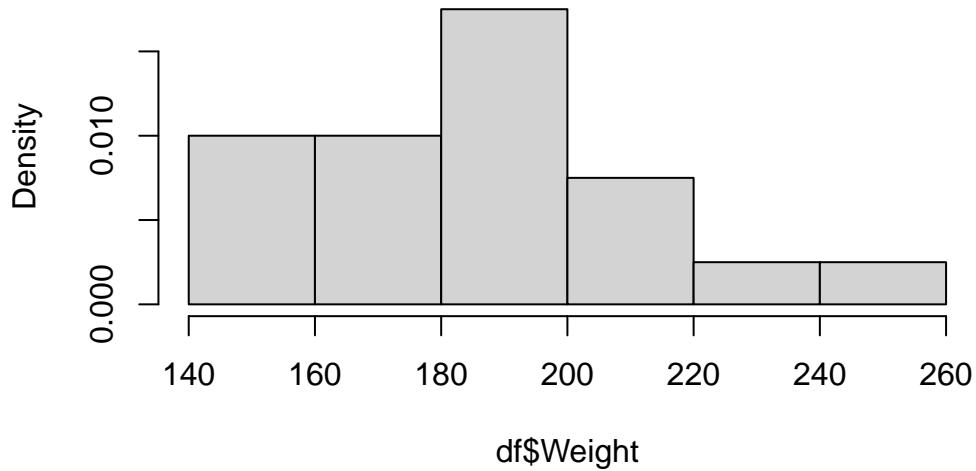
df=data.frame(cbind(Weight=Weight,BodyFat=BodyFat))

cor(df)

      Weight   BodyFat
Weight  1.0000000 0.6966328
BodyFat 0.6966328 1.0000000

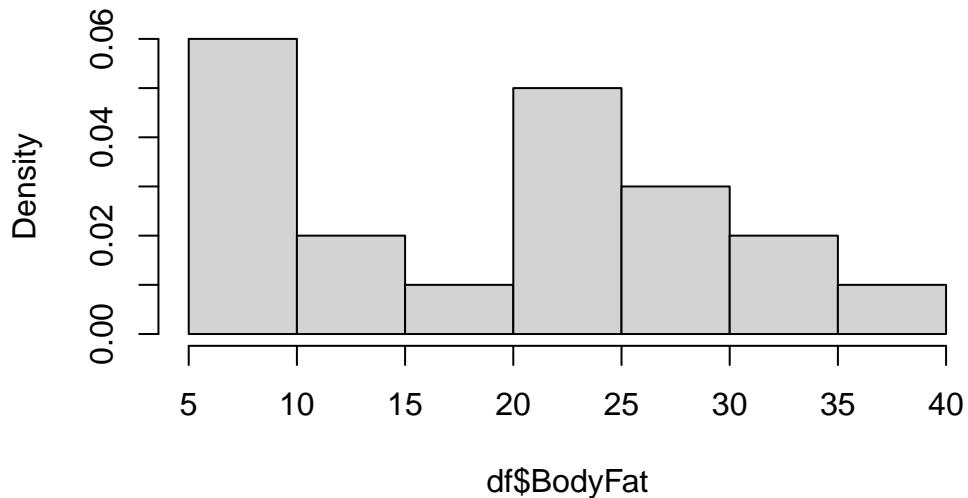
hist(df$Weight,freq=F)
```

### Histogram of df\$Weight



```
hist(df$BodyFat, freq=F)
```

### Histogram of df\$BodyFat



```
summary(df)
```

Weight	BodyFat
Min. :146.0	Min. : 6.00
1st Qu.:171.8	1st Qu.:10.00
Median :187.5	Median :21.00
Mean :188.6	Mean :19.75
3rd Qu.:201.2	3rd Qu.:27.25
Max. :246.0	Max. :38.00

```
cor(df)[1,2]
```

```
[1] 0.6966328
```

```
X=cbind(rep(1,nrow(df)), df$Weight)
Y=df$BodyFat
```

```
beta_hat= solve(t(X) %*% X) %*% t(X) %*% Y
beta_hat
```

```
[,1]
[1,] -27.3762623
[2,] 0.2498741
```

```
model=lm(BodyFat~ Weight,df)
model
```

Call:  
lm(formula = BodyFat ~ Weight, data = df)

Coefficients:  
(Intercept) Weight  
-27.3763 0.2499

```
summary(model)
```

```

Call:
lm(formula = BodyFat ~ Weight, data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-12.5935 -5.7904  0.6536  5.2731 10.4004 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -27.37626   11.54743  -2.371 0.029119 *  
Weight        0.24987    0.06065   4.120 0.000643 *** 
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1 

Residual standard error: 7.049 on 18 degrees of freedom
Multiple R-squared:  0.4853,    Adjusted R-squared:  0.4567 
F-statistic: 16.97 on 1 and 18 DF,  p-value: 0.0006434

```

```
cor(df)[1,2]^2
```

```
[1] 0.4852972
```

```
cor(df)[1,2]
```

```
[1] 0.6966328
```

```
a=function(x){
  (exp(2*x)-1)/(exp(2*x)+1)
}
a(1.36)
```

```
[1] 0.8763931
```

### 3.5.4 Homework stop 6

- Complete the Chapter 2 questions in the textbook.

**Exercise 3.22.** For

$$Y_i = \beta_0 + \beta_1 X_i + \epsilon_i$$

$$y = \begin{pmatrix} y_1 \\ \vdots \\ y_n \end{pmatrix}, X = \begin{pmatrix} 1 & x_1 \\ \vdots & \vdots \\ 1 & x_n \end{pmatrix}, \beta = \begin{pmatrix} \beta_0 \\ \beta_1 \end{pmatrix}, \epsilon = \begin{pmatrix} \epsilon_1 \\ \vdots \\ \epsilon_n \end{pmatrix}$$

- Compute  $\hat{\beta}$ ,  $\text{Var}[\hat{\beta}_1]$ ,  $\text{Var}[\hat{\beta}_0]$ ,  $\text{cov}[(\hat{\beta}_0, \hat{\beta}_1)]$
- Show  $\hat{\beta}_1 = r \frac{\hat{\sigma}_y}{\hat{\sigma}_x}$

## 3.6 Additional concepts & examples

Here we touch on a few important examples and notes about the MLR.

### 3.6.1 Beware scatter plots in MLR

Sometimes, scatter plots are misleading for determining the relationship between  $Y$  and a collection of  $p$  covariates. In the following example, it appears that  $X1$  and  $Y$  do not have a relationship, when in fact they do. Generally, this phenomena goes away with higher sample sizes.

```
# Scatter diagram beware?
# x1=c(2,3,4,1,5,6,7,8)
# x2=c(2,3,4,1,5,6,7,8)
# x=c(2,3,4,1,5,6,7,8)

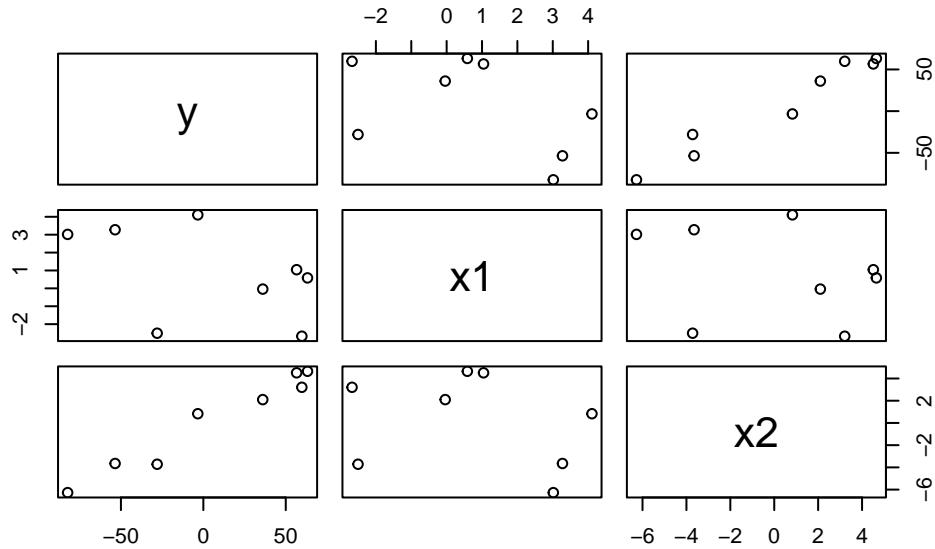
# x1=1:8
# x2=c(2,1:6,4)
# y=8-5*x1+12*x2+rnorm(8,0,2)

set.seed(445)

n=8
x1=rnorm(n,5,5)
x2=rnorm(n,3,5)
y=8-5*x1+12*x2+rnorm(n,0,2)

df=data.frame(cbind(y,x1,x2))
```

```
plot(df)
```



Next, we do an example from the textbook, which uses the NFL data. Specifically, we try to evaluate the relationship between number of wins and several explanatory variables.

**Example 3.11.** Using the following NFL data, complete 3.1-3.4, 4.1 and 4.2 in the textbook.

```
##### NFL example #####
# This gives you the data sets used in the textbook
# install.packages('MPV')
df=MPV::table.b1
# Note for more information, run ?MPV::table.b1

head(df)
```

	y	x1	x2	x3	x4	x5	x6	x7	x8	x9
1	10	2113	1985	38.9	64.7	4	868	59.7	2205	1917
2	11	2003	2855	38.8	61.3	3	615	55.0	2096	1575
3	11	2957	1737	40.1	60.0	14	914	65.6	1847	2175
4	13	2285	2905	41.6	45.3	-4	957	61.4	1903	2476
5	10	2971	1666	39.2	53.8	15	836	66.1	1457	1866

```

6 11 2309 2927 39.7 74.1 8 786 61.0 1848 2339

# names too long
names(df)

[1] "y"   "x1"  "x2"  "x3"  "x4"  "x5"  "x6"  "x7"  "x8"  "x9"

# rename to make it easier
names(df)=c("Wins","RushY","PassY","PuntaA","FGP","TurnD","PenY","PerR","ORY","OPY")
names(df)

[1] "Wins"  "RushY" "PassY" "PuntaA" "FGP"    "TurnD"  "PenY"  "PerR"  "ORY"
[10] "OPY"

# Wins~ beta_1+beta_2Passing_yrds+beta_3per_rush+beta_4ORY+epsilon
# summary(df)
# plot(df)
# run the model
regression_model=lm( Wins ~ PassY+PerR+ORY ,data= df )
summary(regression_model)

Call:
lm(formula = Wins ~ PassY + PerR + ORY, data = df)

Residuals:
    Min      1Q      Median      3Q      Max 
-3.0370 -0.7129 -0.2043  1.1101  3.7049 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -1.808372  7.900859 -0.229  0.820899    
PassY        0.003598  0.000695  5.177 2.66e-05 ***  
PerR         0.193960  0.088233  2.198 0.037815 *    
ORY          -0.004816  0.001277 -3.771 0.000938 ***  
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.706 on 24 degrees of freedom

```

```
Multiple R-squared:  0.7863,    Adjusted R-squared:  0.7596
F-statistic: 29.44 on 3 and 24 DF,  p-value: 3.273e-08
```

```
# model=lm(Wins~PassY+PerR+ORY,data=df)
# get the confidence intervals.
confint(regression_model)
```

	2.5 %	97.5 %
(Intercept)	-18.114944410	14.498200293
PassY	0.002163664	0.005032477
PerR	0.011855322	0.376065098
ORY	-0.007451027	-0.002179961

What conclusions can you make from this output? - All variables seem important! For instance, we see that for every 1% increase in percentage rushing, there is a 0.193960 increase in number of wins, on average, holding passing yards and opponent rushing yards constant.

```
##### CI
# mean response of z'\beta , z=(2000,60,1900)'
new_data=data.frame( matrix(c(2000,60,1900),ncol=3) )
names(new_data)

[1] "X1" "X2" "X3"

names(new_data)=c( 'PassY','PerR','ORY' )

predict(regression_model, new_data ,  interval = 'confidence')

      fit      lwr      upr
1 7.875942 7.072672 8.679213
```

```
predict(regression_model, new_data ,  interval = 'predict')

      fit      lwr      upr
1 7.875942 4.263986 11.4879
```

```
## ANOVA

regression_model_reduced=lm( Wins ~ 1 ,data= df )
summary(regression_model_reduced)
```

Call:

```
lm(formula = Wins ~ 1, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-6.9643	-2.9643	-0.4643	3.0357	6.0357

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	6.9643	0.6576	10.59	4.09e-11 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.48 on 27 degrees of freedom

```
anova(regression_model_reduced,regression_model)
```

Analysis of Variance Table

Model 1: Wins ~ 1

Model 2: Wins ~ PassY + PerR + ORY

Res.Df	RSS	Df	Sum of Sq	F	Pr(>F)
1	27	326.96			
2	24	69.87	3	257.09 29.437	3.273e-08 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

```
# subset test
```

```
regression_model_reduced=lm( Wins ~ PassY ,data= df )
anova(regression_model_reduced,regression_model)
```

### Analysis of Variance Table

```
Model 1: Wins ~ PassY
Model 2: Wins ~ PassY + PerR + ORY
  Res.Df   RSS Df Sum of Sq    F    Pr(>F)
1      26 250.77
2      24  69.87  2     180.9 31.069 2.189e-07 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
# summary(df)

summary(regression_model)
```

Call:

```
lm(formula = Wins ~ PassY + PerR + ORY, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-3.0370	-0.7129	-0.2043	1.1101	3.7049

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1.808372	7.900859	-0.229	0.820899
PassY	0.003598	0.000695	5.177	2.66e-05 ***
PerR	0.193960	0.088233	2.198	0.037815 *
ORY	-0.004816	0.001277	-3.771	0.000938 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.706 on 24 degrees of freedom

Multiple R-squared: 0.7863, Adjusted R-squared: 0.7596

F-statistic: 29.44 on 3 and 24 DF, p-value: 3.273e-08

```
# anova(regression_model)
summ=summary(regression_model)
summ$r.squared
```

[1] 0.7863069

```
summ$adj.r.squared

[1] 0.7595953

regression_model2=lm(Wins~PassY+ORY,data=df)

SSER=sum(regression_model2$residuals*regression_model2$residuals); SSER

[1] 83.9382

dfer=regression_model2$df.residual; dfer

[1] 25

SSEC=sum(regression_model$residuals*regression_model$residuals); SSEC

[1] 69.87

dfeC=regression_model$df.residual; dfeC

[1] 24

SSdrop=SSER-SSEC; SSdrop

[1] 14.06819

dfddrop=dfer-dfeC

MSdrop=SSdropdfddrop; MSdrop

[1] 14.06819
```

```
R_prp=SSdrop/SSER; R_prp
```

```
[1] 0.1676018
```

```
MSdrop
```

```
[1] 14.06819
```

```
1-pf(MSdrop,dfdrop,dfeC)
```

```
[1] 0.000986662
```

```
cor(regression_model$fitted.values , df$Wins)^2
```

```
[1] 0.7863069
```

```
confint(regression_model2)
```

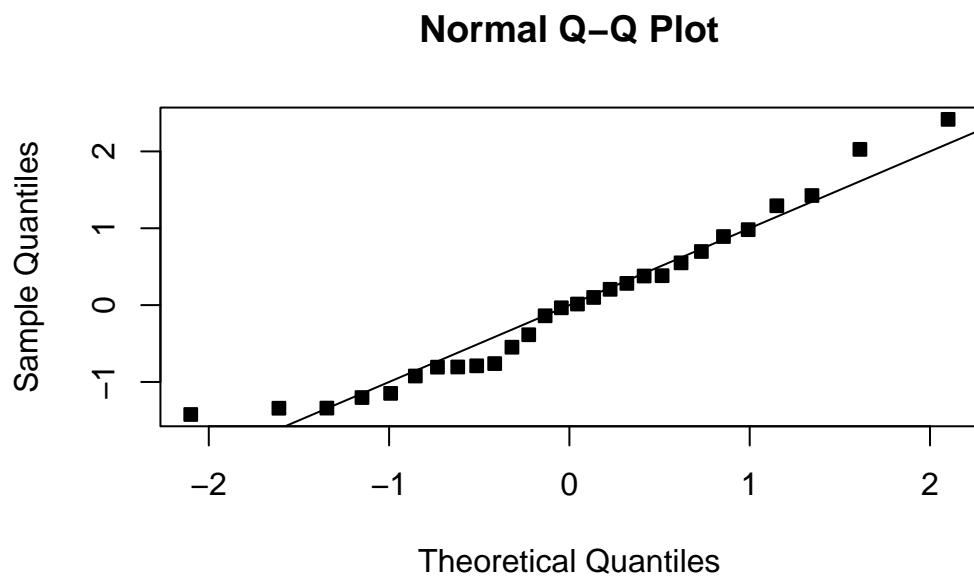
	2.5 %	97.5 %
(Intercept)	9.321778092	20.103571885
PassY	0.001654121	0.004568143
ORY	-0.008797465	-0.004819085

```
new_data=df[1,c(3,8,9)]  
new_data[1,]=c(2300 , 56 , 2100)  
predict(regression_model2,new_data,interval = 'confidence')
```

	fit	lwr	upr
1	7.5709	6.814662	8.327138

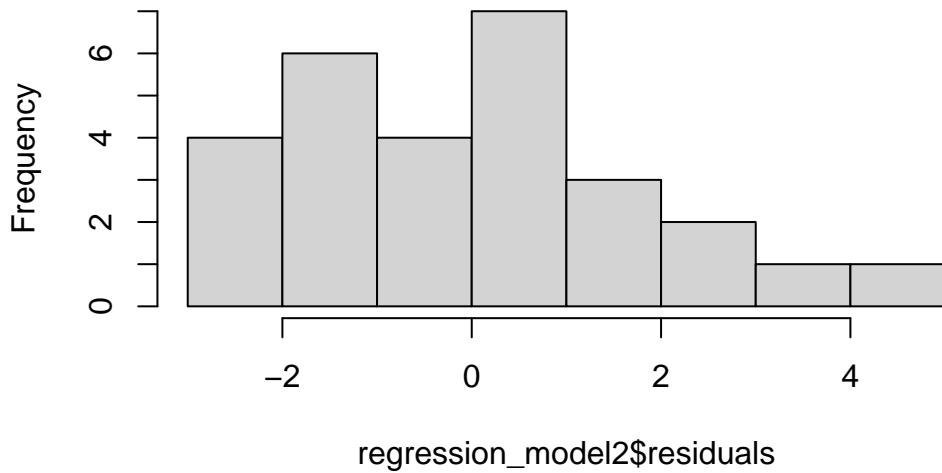
```
##### check the fit #####  
MSE=summ$sigma^2  
qqnorm(regression_model2$residuals/summ$sigma,pch=22, bg=1)
```

```
abline(0,1)
```

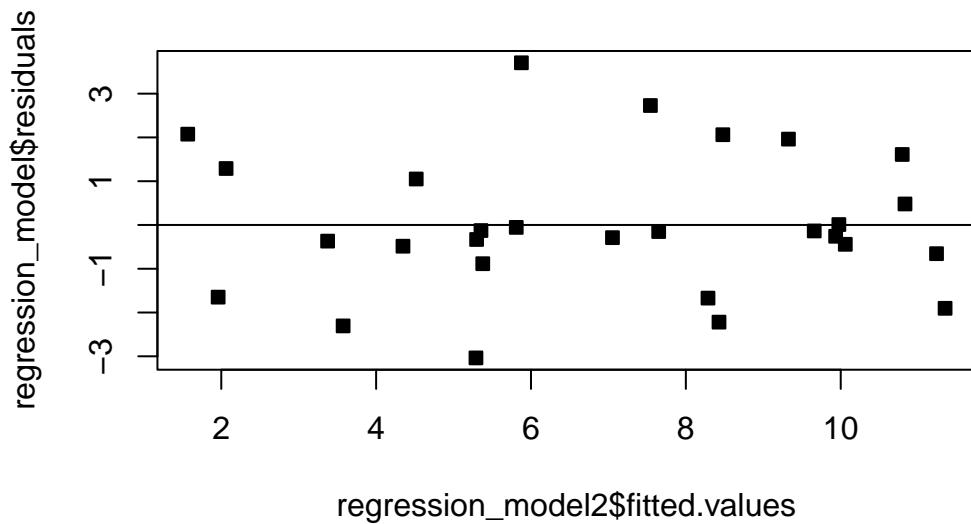


```
hist(regression_model2$residuals, breaks=6)
```

### Histogram of regression\_model2\$residuals



```
plot(regression_model2$fitted.values, regression_model$residuals, pch=22, bg=1)
abline(h=0)
```



```

n=nrow(df)
plot(1:n,regression_model2$residuals,pch=22, bg=1)
abline(h=0)

time=(1:n)
res=lm(regression_model2$residuals~time)
summary(res)

```

Call:  
`lm(formula = regression_model2$residuals ~ time)`

Residuals:

Min	1Q	Median	3Q	Max
-2.36425	-1.04520	-0.07845	1.16457	2.40353

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	1.8479	0.5610	3.294	0.002852 **
time	-0.1274	0.0338	-3.771	0.000848 ***
---				

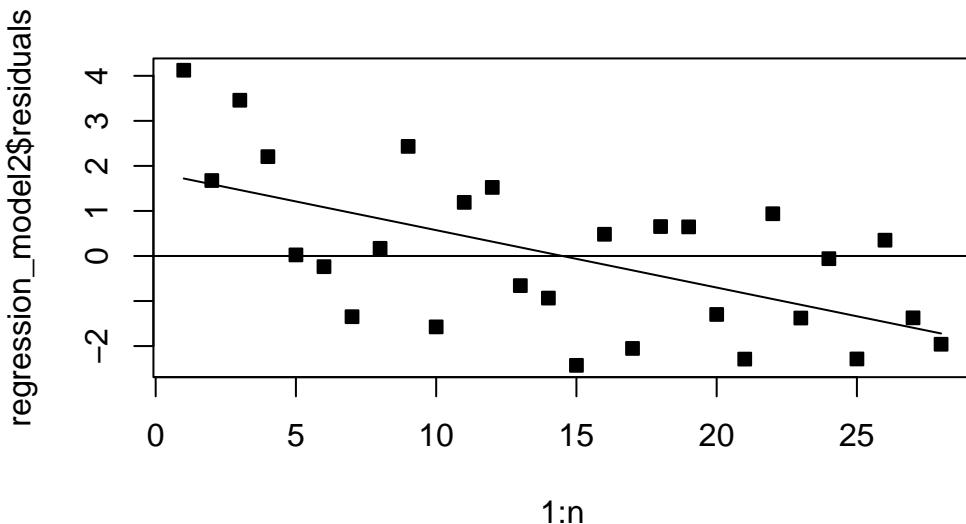
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 1.445 on 26 degrees of freedom  
Multiple R-squared: 0.3535, Adjusted R-squared: 0.3286  
F-statistic: 14.22 on 1 and 26 DF, p-value: 0.0008481

```

lines(time,res$fitted.values)

```



```
regression_model3=lm(Wins~PerR+ORY,data=df)
summ3=summary(regression_model3)
summ3
```

Call:  
`lm(formula = Wins ~ PerR + ORY, data = df)`

Residuals:

Min	1Q	Median	3Q	Max
-3.7985	-1.5166	-0.5792	1.9927	4.5248

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	17.944319	9.862484	1.819	0.08084 .
PerR	0.048371	0.119219	0.406	0.68839
ORY	-0.006537	0.001758	-3.719	0.00102 **

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 2.432 on 25 degrees of freedom  
Multiple R-squared: 0.5477, Adjusted R-squared: 0.5115

```
F-statistic: 15.13 on 2 and 25 DF, p-value: 4.935e-05
```

```
summ3$r.squared
```

```
[1] 0.5476628
```

```
summ3$adj.r.squared
```

```
[1] 0.5114759
```

```
confint(regression_model)
```

	2.5 %	97.5 %
(Intercept)	-18.114944410	14.498200293
PassY	0.002163664	0.005032477
PerR	0.011855322	0.376065098
ORY	-0.007451027	-0.002179961

```
confint(regression_model3)
```

	2.5 %	97.5 %
(Intercept)	-2.36784828	38.256485319
PerR	-0.19716429	0.293906022
ORY	-0.01015637	-0.002916818

```
new_data3=df[1,c(8,9)]  
new_data3[1,]=c(56 , 2100)  
predict(regression_model3,new_data3,interval = 'confidence')
```

	fit	lwr	upr
1	6.926243	5.828643	8.023842

```
predict(regression_model2,new_data,interval = 'confidence')
```

	fit	lwr	upr
1	7.5709	6.814662	8.327138

Be careful about extrapolating beyond the region containing the original observations. It is very possible that a model that fits well in the region of the original data will perform poorly outside that region. It is easy to inadvertently extrapolate, since the levels of the regressors jointly define a region containing the data which is impossible to visualize in its entirety beyond 2 dimensions. Ideally, we want to make inferences which lie inside the convex hull of the regressors.

We can use the diagonal of the hat matrix  $H = X(X^\top X)^{-1}X^\top$ . In general, the point that has the largest value of  $h_{ii}$ , say  $h_{max}$ , will lie on the boundary of the [convex hull](#) in a region of the  $x$ -space where the density of the observations is relatively low. Points that lie in the set  $\{x^\top(X^\top X)^{-1}x \leq h_{max}\}$  enclose the convex hull. Thus, for a value we are interested in predicting, say  $y$ , we can check if we are extrapolating with  $y^\top(X^\top X)^{-1}y \leq h_{max}$ .

A serious problem that may dramatically impact the usefulness of a regression model is multicollinearity, or near - linear dependence among the regression variables. Multicollinearity implies near - linear dependence among the regressors. The regressors are the columns of the  $X$  matrix, so clearly an exact linear dependence would result in a singular  $X^\top X$ . This will impact our ability to estimate  $\beta$ .

We can check for this dependence with the **variance inflation factor** (VIF). The variance inflation factor can be written as  $(1 - R_j^2)^{-1}$ , where  $R_j^2$  is the coefficient of determination obtained from regressing  $X_j$  on the other regressor variables. If VIF is large, say  $> 3$ , then you will likely need to make some changes to your regression model.

Sometimes, you may observe that regression coefficients have the a sign that is unexpected, or contradicts nature. This is likely due to one of the following:

- The range of some of the regressors is too small – if the range of some of the regressors is too small, then the variance of  $\hat{\beta}$  is high.
- Important regressors have not been included in the model.
- Multicollinearity is present.
- Computational errors have been made.

We close this Chapter with the following statement. Recall the modelling overview from Chapter 1:

- Posit the model: What is the linear regression model – what are all the assumptions of the linear regression model?
- Estimation: How can we estimate parameters of the linear regression model?
- Inference: How can we compute confidence intervals and run hypothesis tests associated with the linear regression model?

- Fit: Does our fitted line match up with the data? What about the normality assumption? Do the errors appear normal? Do the errors seem independent? Is the variance constant? How much variability is explained by our model?
- Prediction: How can we predict a new  $Y$ ? What is the error of this prediction

If you have learned the concepts of this chapter, you should be able to complete all of these steps! In the following chapters, we will discuss different problems that can arise in regression modelling and how to remedy them.

### 3.6.2 Homework questions

**Exercise 3.23.** Show  $\text{Var} [\hat{Y}|X] = \sigma^2 H$ .

**Exercise 3.24.** Check for multicollinearity in our past examples.

**Exercise 3.25.** Complete the problem sets from Chapter's 2, 3 and 4!

# 4 Residual analysis

Recall that we want to study the normal MLR:

$$Y|X = X\beta + \epsilon,$$

where

- $\forall i \in [n]$ ,  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$  and  $\epsilon_i \perp \epsilon_j$  for  $i \neq j$ ,  $i, j \in [n]$ .
- $\beta \in \mathbb{R}^{p \times 1}$  is the unknown, population coefficient vector
- $X \in \mathbb{R}^{n \times p}$  is a covariate matrix

We assume that: - The relationship is linear  $Y|X = X\beta + \epsilon$ , -  $\forall i \in [n]$ ,  $\epsilon_i \sim \mathcal{N}(0, \sigma^2)$ . -  $\epsilon_i \perp \epsilon_j$  for  $i \neq j$ ,  $i, j \in [n]$ .

We have seen some methods for checking if these are appropriate, we will dive deeper now.

Recall that the residuals are defined as:

$$\hat{\epsilon} = Y - \hat{Y} = Y - X\hat{\beta}.$$

Given that a residual may be viewed as the deviation between the data and the fit, it is also a measure of the variability in the response variable not explained by the regression model. It is also convenient to think of the residuals as the realized or observed values of the model errors. Thus, it's reasonable to conclude that departures from the assumptions on the errors should show up in the residuals. Analysis of the residuals is an effective way to discover several types of model inadequacies.

## 4.1 Properties of residuals

The following are some properties of the residual vector. First, the sample mean of the residuals is zero:  $\sum_{i=1}^n \hat{\epsilon}_i / n = \hat{\epsilon} \mathbf{1}_n \cdot \mathbf{1}/n = 0$ . We also have that  $E[\hat{\epsilon}] = 0$ . Next, the sample variance of the residual vector is approximately the MSE:  $\frac{1}{n-1} \sum_{i=1}^n \hat{\epsilon}_i^2 = \frac{n-p}{n-1} MSE$ . Lastly, unlike the random error  $\epsilon_i$ , the residuals **are not** independent. Sometimes we say that they are “approximately independent” if  $p \ll n$ , which we will touch on later.

## 4.2 Types of residuals

We will refer to  $\hat{\epsilon}_i$  as simply the residuals, or ordinary residuals when we need to be extra clear.

The standardized residual is given by

$$d_i = \hat{\epsilon}_i / \sqrt{MSE}.$$

This is an approximate *Z*-score for the residuals, since the residuals have 0 mean, the *MSE* is approximately the variance of the random error and the residuals approximate the random error. We say that large  $d_i$  ( $> 3$ ) indicates an outlier, though, we may want to use a more robust measure of the variance. We will generally prefer to use a different type of residual, which we now present.

We now introduce the hat matrix:  $H = X(X^\top X)^{-1}X^\top$ . Note that  $H$  is symmetric and **idempotent**. The hat matrix appears often in regression analysis, and you should remember this quantity. It is called the hat matrix because  $\hat{Y} = HY$ .

Note that the eigenvalues of  $H$ , and any idempotent matrix  $A$  are either 0 or 1:

$$\lambda x = Ax = A^2x = A\lambda x = \lambda^2x,$$

which implies that  $\lambda \in \{0, 1\}$ .

**Exercise 4.1.** Verify that  $H$  is symmetric and idempotent and that  $\hat{Y} = HY$ , where one recalls that a matrix  $A$  is idempotent if  $AA = A$ .

Now, note that:

$$\hat{\epsilon} = (I - H)Y = (I - H)\epsilon.$$

**Exercise 4.2.** Verify that  $\hat{\epsilon} = (I - H)Y = (I - H)\epsilon..$

Using this identity, we have that  $\text{Var}[\hat{\epsilon}] = (I - H)\epsilon(I - H)^\top = (I - H)\sigma^2$ .

The fact that  $H$  is symmetric and idempotent implies that its diagonal elements are between 0 and 1. It follows that the elements on the diagonal of  $(I - H)$  are also between 0 and 1. Therefore, the *MSE* overestimates the variance of the residuals: the variance of residual  $i$  is given by  $(1 - h_{ii})\sigma^2 < \sigma^2 \approx MSE$ . Here,  $h_{ii}$  denotes the  $i$ th diagonal element of the matrix  $H$ .

It can be shown that  $h_{ii}$  is a measure of how outlying  $x_i$  is, relative to the other observed covariate vectors. Therefore,  $\text{Var}[\hat{\epsilon}_i]$  depends on how outlying  $x_i$  is. Covariate vectors that are central, relative to the other observed covariate vectors, have larger variance than residuals at more remote locations. What do you think about this?

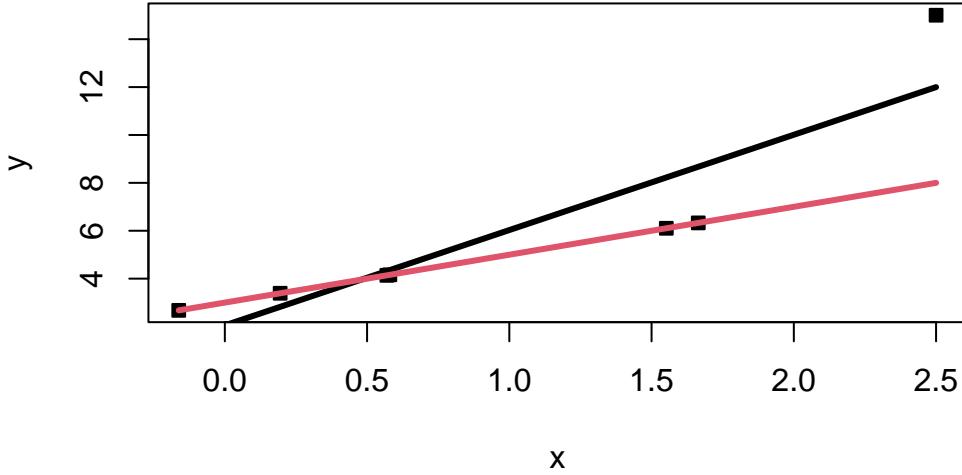
Now, intuitively, some remote points in our data may differ from the population and severely impact our model. However, the variance of the ordinary residuals is lower at these points. Therefore, these impacts may be hard to detect from solely the ordinary residuals because the ordinary residuals of remote points will usually be smaller.

Therefore, we will call points that are outlying in the  $x$ -space **leverage points**. We will refer to **influence points** are not only remote in terms of the specific values for the regressors, but the observed response is not consistent with the values that would be predicted based on only the other data points.

In the example below, observe that the right-most point is both a leverage and influential point.

```
#####
# Simulate some data
set.seed(330)
x=c(rnorm(6),2.5)
y=x*2+3
y[7]=y[7]+7

# Plot the data and fitted lines
plot(x,y,pch=22,bg=1)
a=lm(y~x)
curve(a$coefficients[1]+x*a$coefficients[2],add=T,lwd=3)
curve(x*2+3,add=T,col=2,lwd=3)
```



```
a$coefficients
```

	x
(Intercept)	2.048937
x	3.979977

We now demonstrate mathematically why leverage points can be dangerous. Let  $\hat{y}_n^*$  be the estimate of  $Y_n$  based on the other data and let  $\delta_n = y_n - \hat{y}_n^*$ . Note that one can show that  $\hat{y}_n = \hat{Y}_n^* + h_{nn}\delta_n$ . Next, we know that if  $x_n$  is outlying, i.e.,  $\|x_n\|$  is large, then  $h_{nn} \approx 1$ . This implies that  $\hat{y}_n \approx y_n$ , which means that the regression line is dragged to pass through  $(x_n, y_n)$ .

To detect these types of outlying points, it makes sense to then define the **studentized residuals**:

$$r_i = \frac{\hat{\epsilon}_i}{\sqrt{MSE(1-h_{ii})}}.$$

The studentized residuals in the simple linear regression model reduce to

$$r_i = \frac{\hat{\epsilon}_i}{\sqrt{MSE} \left[ 1 - \left( \frac{1}{n} + \frac{(X_i - \bar{X})^2}{\sum(X - \bar{X})^2} \right) \right]}.$$

Observe that as  $X_i$  grows large, we have that  $\frac{(X_i - \bar{X})^2}{\sum(X - \bar{X})^2} \rightarrow 1$ , which implies that  $\left[1 - \left(\frac{1}{n} + \frac{(X_i - \bar{X})^2}{\sum(X - \bar{X})^2}\right)\right] \rightarrow 0$  and  $r_i \rightarrow \infty$ . On the other hand, as  $\hat{\epsilon}_i$  grows large, we have that  $r_i$  grows large. Therefore, the studentized residual will be large for observations with large ordinary residuals, and for leverage observations.

Earlier, we presented  $\delta_i$ , the difference between the response of the  $i$ th observation and the predicted response based on the observations with the  $i$ th points removed. These are known as the **PRESS residuals**. This seems hard computationally, but one can show that

$$\delta_i = \frac{\hat{\epsilon}_i}{1 - h_{ii}}.$$

Note that when  $h_{ii}$  is large, this indicates a highly influential point. Observe that a large PRESS residual  $\delta_i$ , but small ordinary residual  $\hat{\epsilon}_i$ , indicates that the model fit without  $(X_i, Y_i)$  predicts  $Y_i$  poorly.

**Exercise 4.3.** Show that standardizing the PRESS residual, that is, dividing the PRESS residual by its standard deviation, results in  $\hat{\epsilon}_i / \sqrt{\sigma^2(1 - h_{ii})}$ . Compare this to the studentized residual.

Lastly, if we believe that  $(X_i, Y_i)$  is outlying, then we can also leave  $(X_i, Y_i)$  out in the MSE calculation. This results in the **R-studentized residuals**:

$$\tilde{r}_i = \frac{\hat{\epsilon}_i}{\sqrt{\widetilde{MSE}_i(1 - h_{ii})}},$$

where  $\widetilde{MSE}_i$  is the mean squared error computed from the regression model with  $(X_i, Y_i)$  excluded:

$$\widetilde{MSE}_i = \frac{(n - p + 1)MSE - \hat{\epsilon}_i^2 / (1 - h_{ii})}{n - p}.$$

### 4.3 Revisiting checking model assumptions

Recall from [Checking model assumptions](#) that we plot the residuals to check various assumptions. In this case, we can now use our upgraded residuals to make these plots. In general, any of the residuals that incorporate the values  $h_{ii}$  are acceptable. We will generally use the studentized residuals.

Recall that we may want to plot:

- QQplot of the studentized residuals
- Histogram of the studentized residuals

- Plot of studentized residuals against the fitted values
- Studentized residuals against the covariates
- Studentized residuals against covariates that are not currently in the model
- Studentized residuals against time in some contexts

### 4.3.1 Example

**Example 4.1.** Here, this data contains delivery times, the number of products in the delivery and the distance of the delivery. Perform a residual analysis on the model which regresses delivery times against the number of products in the delivery and the distance of the delivery. Compute all the different types of residuals.

```
##### Delivery Time

# Load and inspect the data
data(delivery, package="robustbase")
df=delivery
n=nrow(df)
head(df)
```

	n.prod	distance	delTime
1	7	560	16.68
2	3	220	11.50
3	3	340	12.03
4	4	80	14.88
5	6	150	13.75
6	7	330	18.11

```
# Fit the model
model=lm(delTime~., data=df)
s=summary(model); s
```

Call:  
`lm(formula = delTime ~ ., data = df)`

Residuals:

Min	1Q	Median	3Q	Max
-5.7880	-0.6629	0.4364	1.1566	7.4197

```

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 2.341231   1.096730   2.135 0.044170 *
n.prod       1.615907   0.170735   9.464 3.25e-09 ***
distance     0.014385   0.003613   3.981 0.000631 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 3.259 on 22 degrees of freedom  
 Multiple R-squared: 0.9596, Adjusted R-squared: 0.9559  
 F-statistic: 261.2 on 2 and 22 DF, p-value: 4.687e-16

```

# X matrix
X=model.matrix(model)

# Hat matrix
hat=X%*%solve(t(X)%*%X)%*%t(X)

# Compute h_ii
hii=diag(hat)
hii

```

1	2	3	4	5	6	7
0.10180178	0.07070164	0.09873476	0.08537479	0.07501050	0.04286693	0.08179867
8	9	10	11	12	13	14
0.06372559	0.49829216	0.19629595	0.08613260	0.11365570	0.06112463	0.07824332
15	16	17	18	19	20	21
0.04111077	0.16594043	0.05943202	0.09626046	0.09644857	0.10168486	0.16527689
22	23	24	25			
0.39157522	0.04126005	0.12060826	0.06664345			

```
max(hii)
```

```
[1] 0.4982922
```

```
# Notice 9 is large
```

```
##### ordinary residuals
```

```

regular_residuals=model$residuals
# or

# standardized residuals
stand_res=model$residuals/s$sigma

# studentized residuals
student_res=rstudent(model)

#PRESS residuals
press=model$residuals/(1-hii)

# Get the MSE_is
MSE_i=((n-2)*(s$sigma)^2-regular_residuals^2/(1-hii))/(n-3)

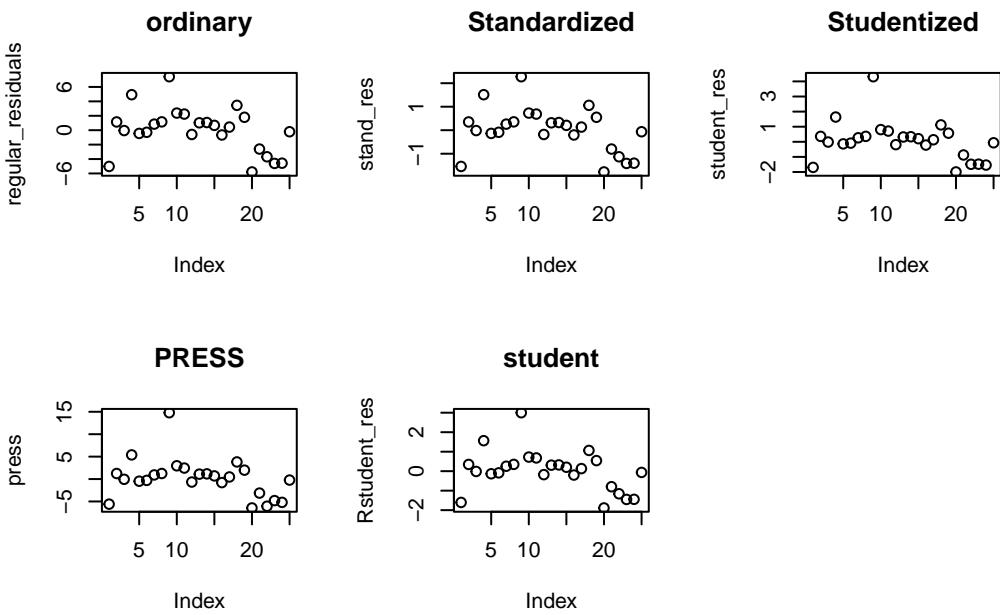
#r studentized residuals
Rstudent_res=model$residuals/sqrt(MSE_i)

# Plot them all and compare
par(mfrow=c(2,3))
plot(regular_residuals,main="ordinary")
plot(stand_res,main="Standardized")
plot(student_res,main="Studentized")
plot(press,main="PRESS")
plot(Rstudent_res,main="student")

# Notice 9 is much more outlying in the last 3 graphs.

# Reset plotting
par(mfrow=c(1,1))

```



```
# 9 is largest
which.max(student_res)
```

```
9
9
```

```
# Notice the standardized is half as large as the studentized.
student_res[9]
```

```
9
4.31078
```

```
stand_res[9]
```

```
9
2.276351
```

```

par(mfrow=c(2,2))

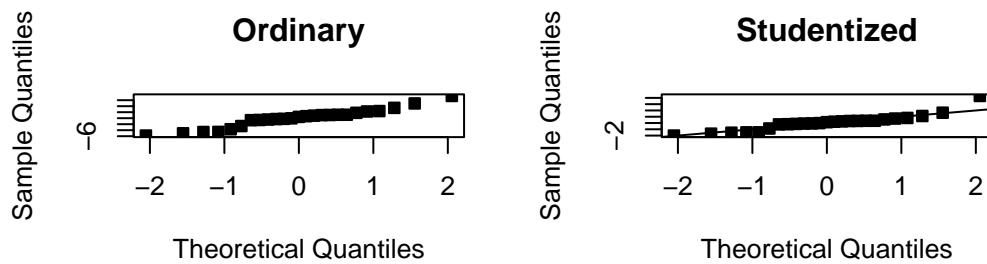
# Notice the difference !!!
qqnorm(regular_residuals,pch=22, bg=1,main="Ordinary")

qqnorm(student_res,pch=22, bg=1,main="Studentized")
abline(0,1)

# Compare all

par(mfrow=c(2,2))

```



```

qqnorm(student_res,pch=22, bg=1, ylim=c(-5,5),main="Studentized")
abline(0,1)
# hist(student_res)

qqnorm(Rstudent_res,pch=22, bg=1, ylim=c(-3,3),main="R Studentized")
qqline(Rstudent_res,pch=22, bg=1, ylim=c(-10,10))
# abline(0,1)

qqnorm(stand_res,pch=22, bg=1, ylim=c(-3,3),main="Standardized")

```

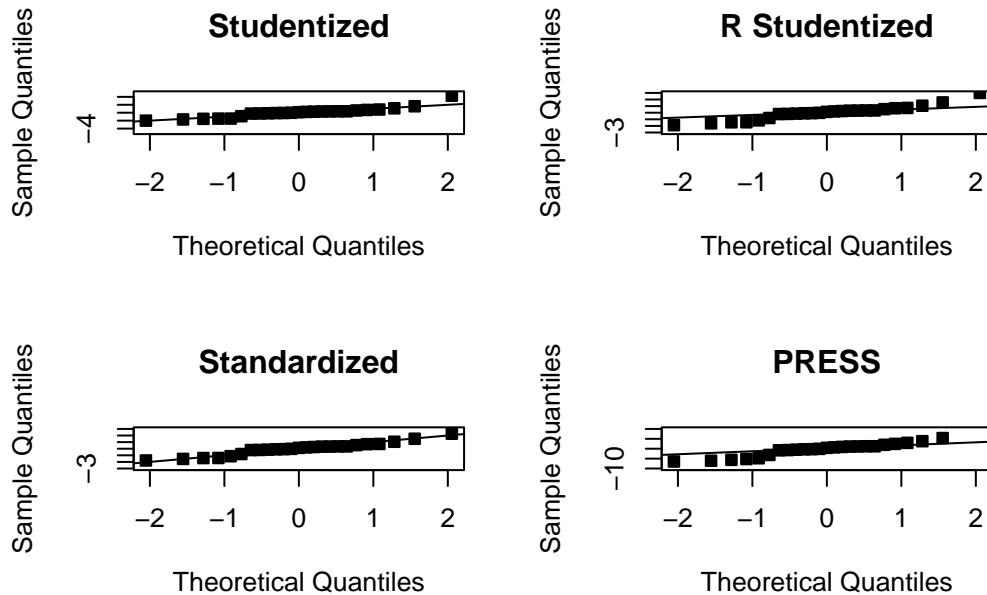
```

abline(0,1)

qqnorm(press,pch=22,bg=1,ylim=c(-10,10),main="PRESS")
qqline(press,pch=22,bg=1,ylim=c(-10,10))
#careful of the scale!

par(mfrow=c(3,2))
qqline(model$residuals,pch=22,bg=1,main="Ordinary")

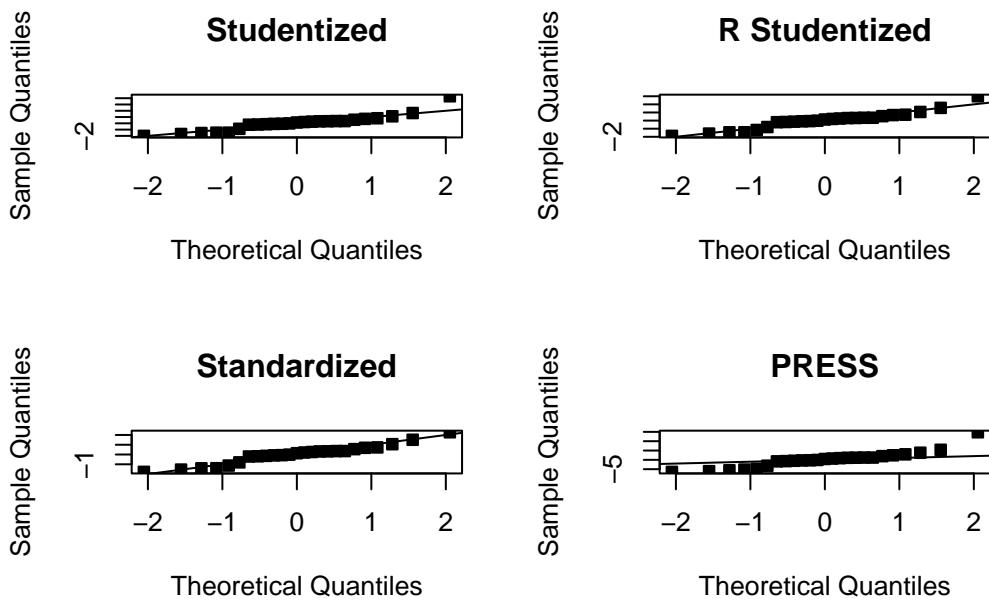
```



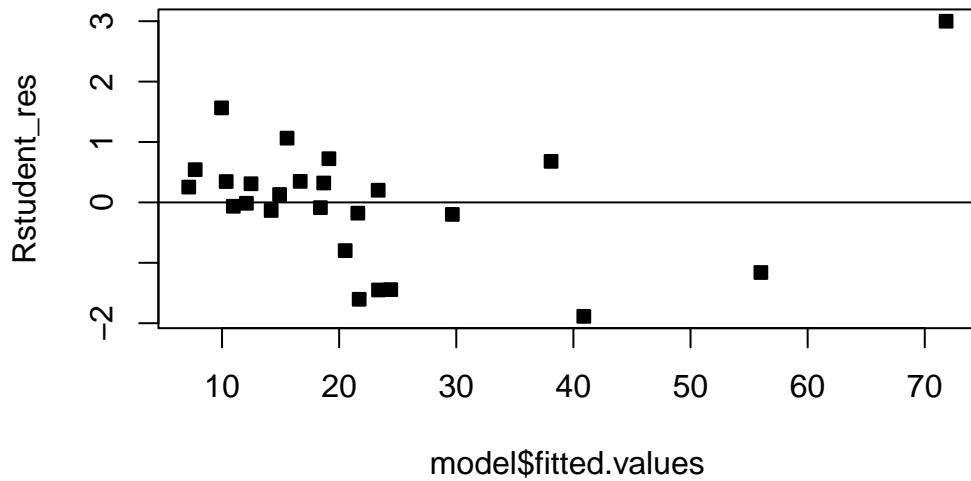
```

par(mfrow=c(2,2))
qqnorm(student_res,pch=22,bg=1,main="Studentized")
abline(0,1)
qqnorm(Rstudent_res,pch=22,bg=1,main="R Studentized")
abline(0,1)
qqnorm(stand_res,pch=22,bg=1,main="Standardized")
abline(0,1)
qqnorm(press,pch=22,bg=1,main="PRESS")
abline(0,1)

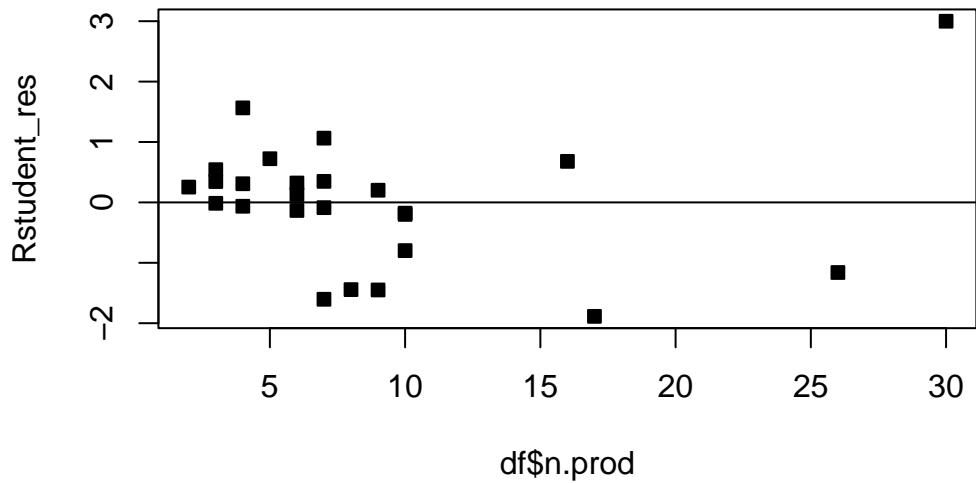
```



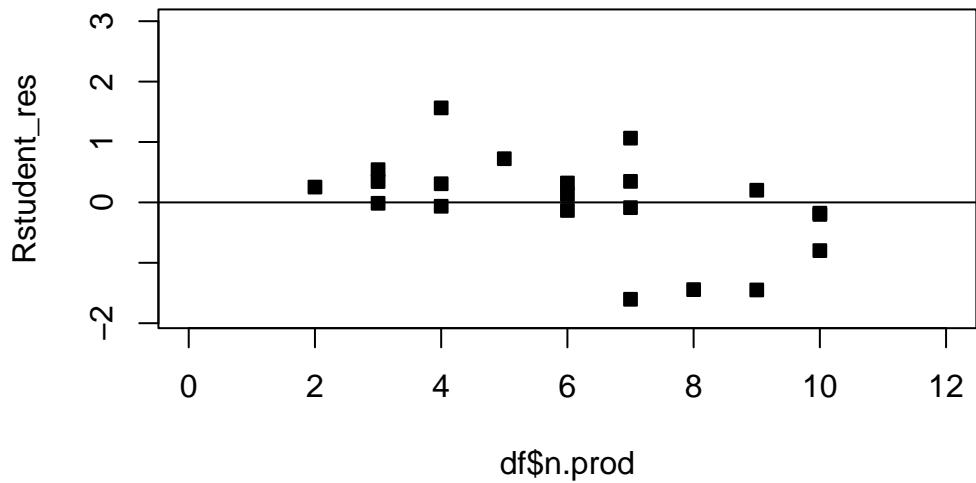
```
# Now we plot the fitted values against the R studentized residuals
par(mfrow=c(1,1),pch=22)
plot(model$fitted.values,Rstudent_res,bg=1)
abline(h=0)
```



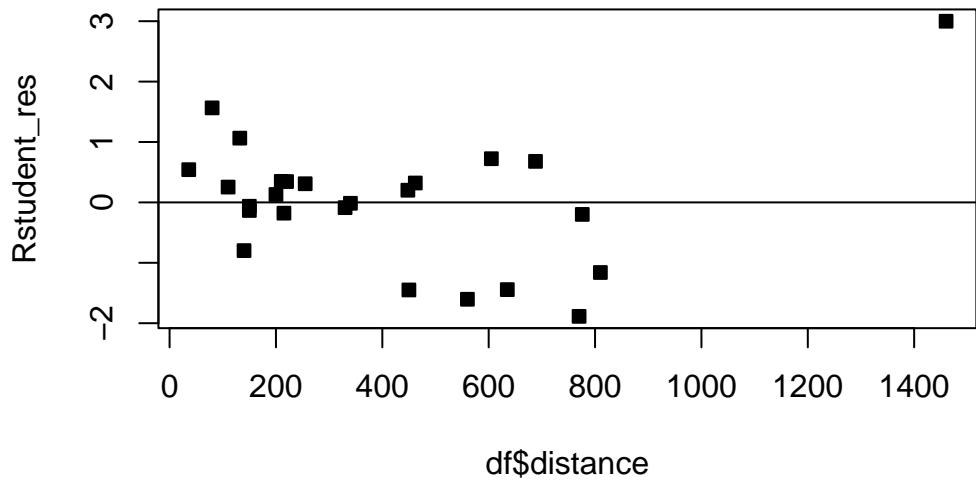
```
# Now we plot the number of products against the R studentized residuals  
# There is one moderately large delivery!  
plot(df$n.prod,Rstudent_res, bg=1)  
abline(h=0)
```



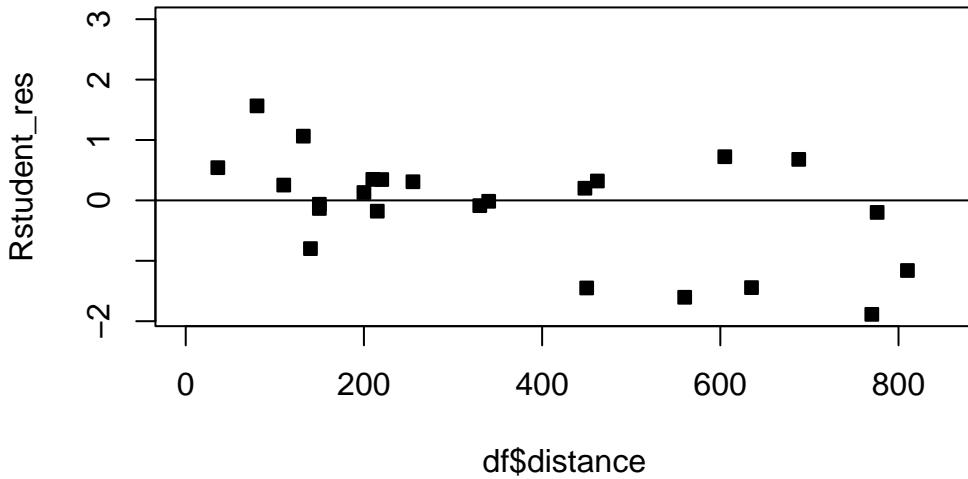
```
# Care for the scale
plot(df$n.prod,Rstudent_res,bg=1,xlim=c(0,12))
abline(h=0)
```



```
# There is one very far delivery!
plot(df$distance,Rstudent_res,bg=1)
abline(h=0)
```



```
# Care for the scale
plot(df$distance,Rstudent_res,bg=1,xlim=c(0,850))
abline(h=0)
```



```
# What happens to the model when we remove this outlying observation (the far distance del)
df2=df[-which.max(df$distance),]
```

```
# refit the model
model=lm(delTime~.,data=df2)
s=summary(model); s
```

Call:  
`lm(formula = delTime ~ ., data = df2)`

Residuals:

Min	1Q	Median	3Q	Max
-4.0325	-1.2331	0.0199	1.4730	4.8167

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	4.447238	0.952469	4.669	0.000131 ***
n.prod	1.497691	0.130207	11.502	1.58e-10 ***
distance	0.010324	0.002854	3.618	0.001614 **

---

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1  
Residual standard error: 2.43 on 21 degrees of freedom  
Multiple R-squared: 0.9487, Adjusted R-squared: 0.9438  
F-statistic: 194.2 on 2 and 21 DF, p-value: 2.859e-14
```

```
# X matrix  
X=model.matrix(model)  
  
# Hat matrix  
hat=X%*%solve(t(X)%*%X)%*%t(X)  
  
# Compute h_ii  
hii=diag(hat)  
hii
```

1	2	3	4	5	6	7
0.11083391	0.07741039	0.09998709	0.10097319	0.08066357	0.04290146	0.10024969
8	10	11	12	13	14	15
0.06537738	0.20438000	0.14675966	0.11367920	0.06437975	0.08033747	0.04661503
16	17	18	19	20	21	22
0.21115081	0.06254612	0.10128434	0.11992977	0.18537865	0.16642759	0.55671434
23	24	25				
0.04687996	0.13894064	0.07620000				

```
max(hii)
```

```
[1] 0.5567143
```

```
##### ordinary residuals  
regular_residuals=model$residuals  
# or  
  
# standardized residuals  
stand_res=model$residuals/s$sigma  
  
# studentized residuals  
student_res=rstudent(model)
```

```

#PRESS residuals
press=model$residuals/(1-hii)

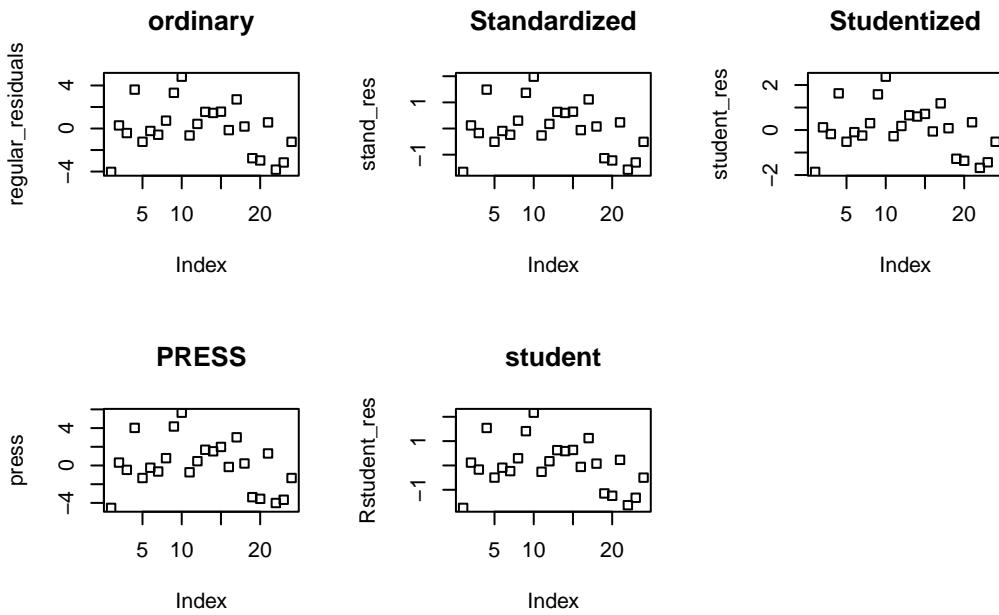
# Get the MSE_is
MSE_i=((n-2)*(s$sigma)^2-regular_residuals^2/(1-hii))/(n-3)

#r studentized residuals
Rstudent_res=model$residuals/sqrt(MSE_i)

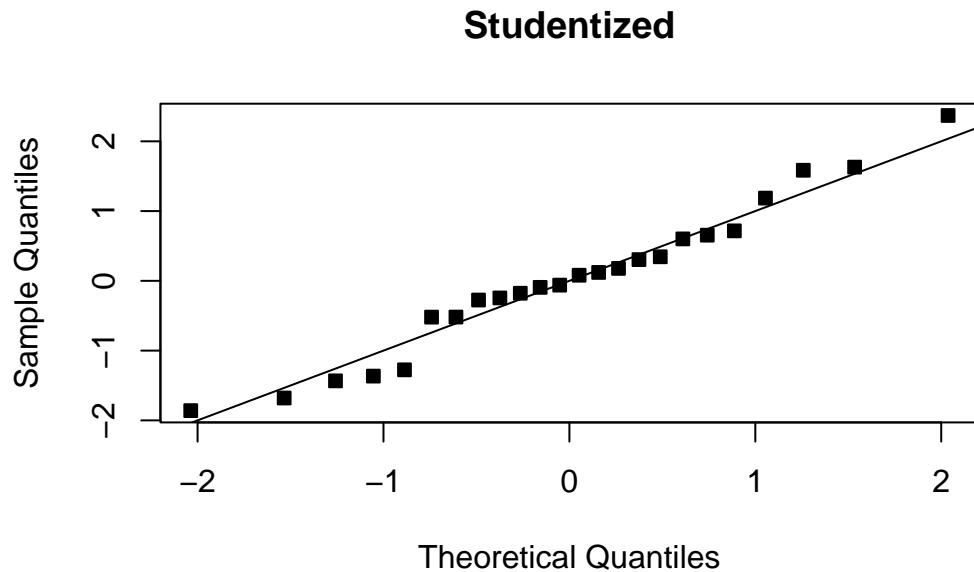
# Plot them all and compare - much better
par(mfrow=c(2,3))
plot(regular_residuals,main="ordinary")
plot(stand_res,main="Standardized")
plot(student_res,main="Studentized")
plot(press,main="PRESS")
plot(Rstudent_res,main="student")

# Notice that these graphs are fine now...
par(mfrow=c(1,1))

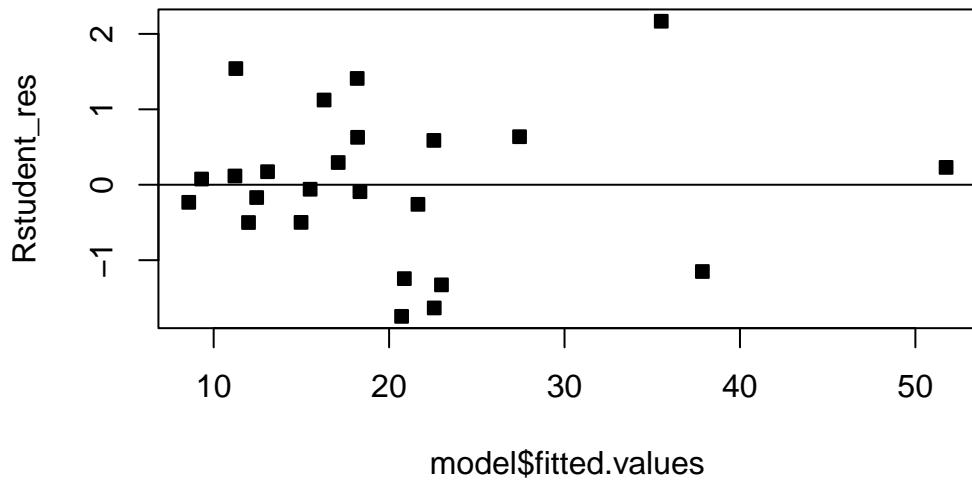
```



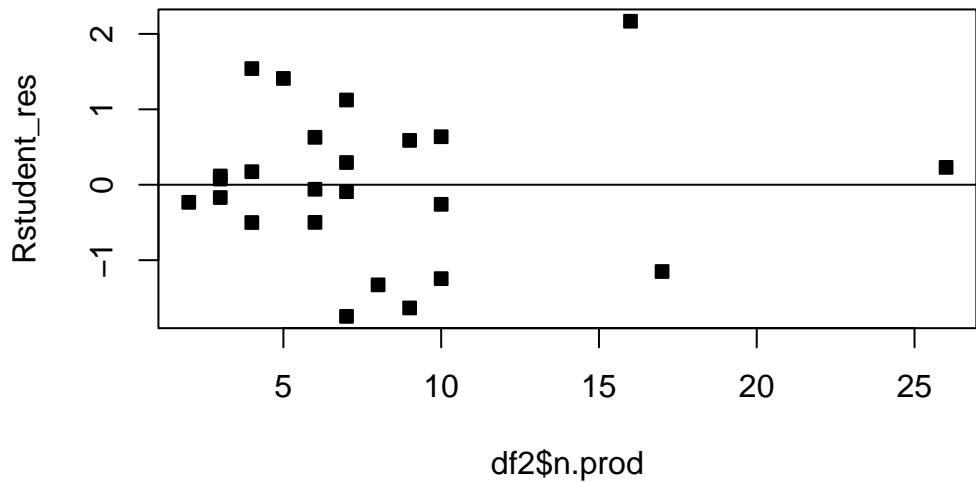
```
qqnorm(student_res,pch=22,bg=1,main="Studentized")
abline(0,1)
```



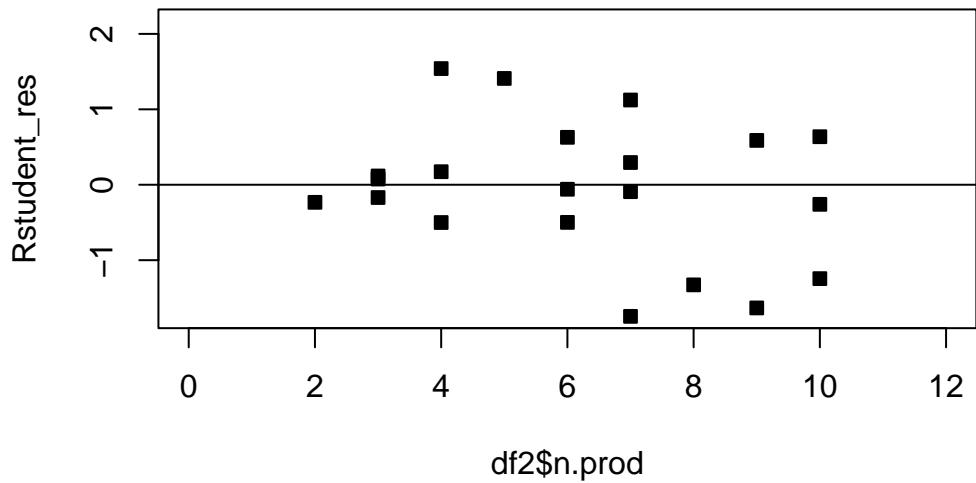
```
# Now we plot the fitted values against the R studentized residuals
par(mfrow=c(1,1),pch=22)
plot(model$fitted.values,Rstudent_res,bg=1)
abline(h=0)
```



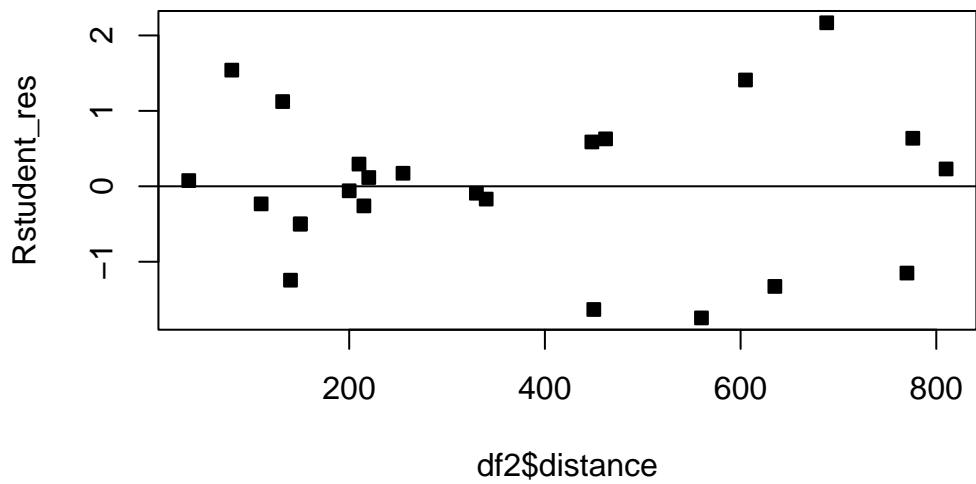
```
# Now we plot the number of products against the R studentized residuals
plot(df2$n.prod,Rstudent_res,bg=1)
abline(h=0)
```



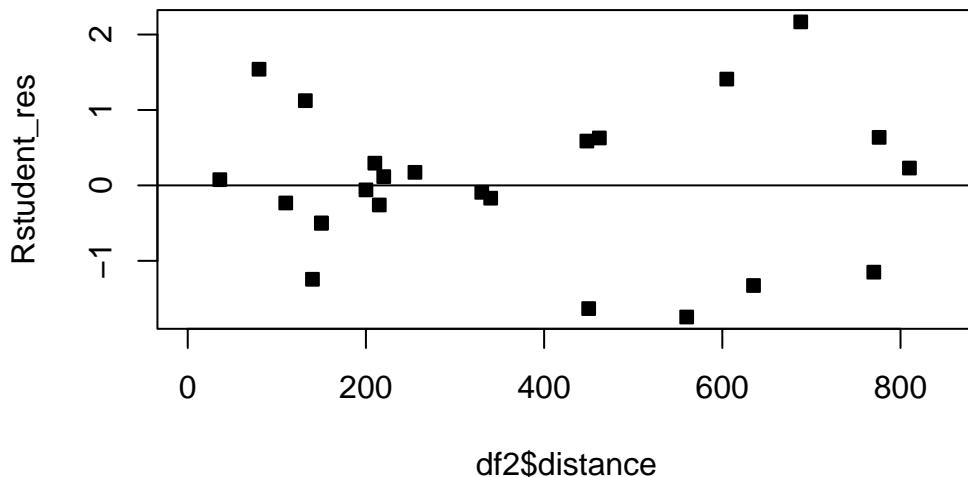
```
# Care for the scale
plot(df2$n.prod,Rstudent_res,bg=1,xlim=c(0,12))
abline(h=0)
```



```
plot(df2$distance,Rstudent_res,bg=1)
abline(h=0)
```



```
# Care for the scale
plot(df2$distance,Rstudent_res,bg=1,xlim=c(0,850))
abline(h=0)
```



Now, we have introduced different types of residuals and the appropriate graphs to examine when checking for violations of the assumptions. When we observe violations of the assumptions - what do we do? That will be the topic of the next section.

Some of these remedies include:

- Transformations of the response
- Transformations of certain regressors
- Robust methods/outlier removal
- Inclusion of new regressors

## 4.4 Homework stop

Do the Chapter 4 questions from the textbook.

**Exercise 4.4.** In the context of a regression model, do you think a point whose covariates are outlying is more problematic than a point whose response, given the covariates, is outlying?

**Exercise 4.5.** Make a table describing the differences between each type of residual.

**Exercise 4.6.** Perform a residual analysis on the marketing data from Example Example 3.7.

**Exercise 4.7.** Perform a residual analysis on the data from Example Example 3.8.

# 5 Transformations

## 5.1 Variance-stabilizing transformations

Recall that we assume that  $\forall i \in [n], \epsilon_i \sim \mathcal{N}(0, \sigma^2)$ . A common reason for a violation of this assumption is for  $Y$  to have a distribution in which the variance is related to its mean. For example, if the response  $Y$  is a Poisson random variable, i.e.,

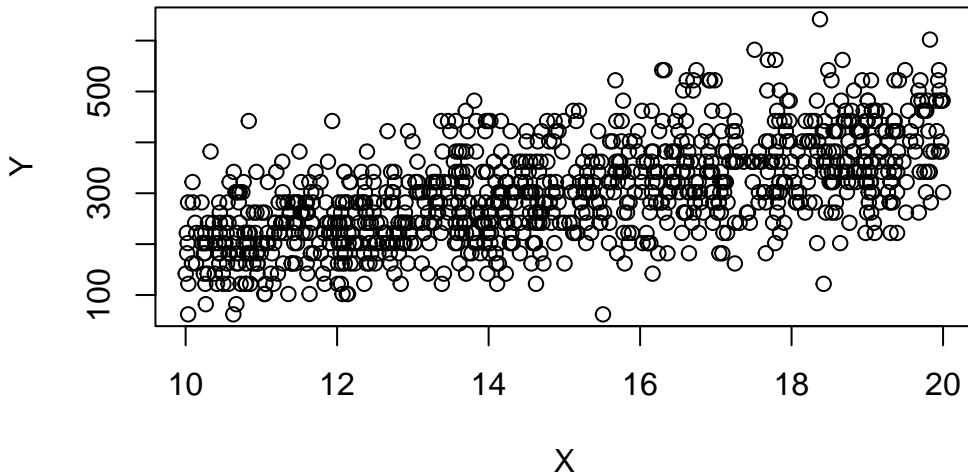
$$Y|X \sim \text{Pois}(X\beta),$$

then we have that  $E[Y] = X\beta$ , then  $E[Y] = \text{Var}[Y] = X\beta$ . In this case, the simple linear regression assumptions are violated. In particular, the variance is not the same for each observation. Here, it happens that taking the response to be roughly  $\sqrt{Y}$  fixes the problem. That is, performing the regression analysis with  $\sqrt{Y}$  as the response variable instead of  $Y$ , ensures that the regression assumptions are (approximately) satisfied. This example gives rise to the idea of **transformations**. If our data do not satisfy the assumptions for the MLR or the normal MLR, we might ask if there is some transformation of either the response, some of the covariates, or both that make the data suitable for a MLR analysis. Note that the assumptions are important. For instance, if the variance is not homogeneous, the OLS estimator will still be unbiased, but they will no longer have BLUE property. That means that some other estimator will work better for such data!

Which transformation should we choose? Sometimes, we can use prior experience or theoretical considerations to guide us in selecting an appropriate transformation. Other times, we must choose it empirically, i.e., based on the data. Often, the square root and the logarithm are popular choices. If your response is between 0 and 1, and the data appear to be “football shaped”, then you may like to take the  $\text{arcsin}(\sqrt{Y})$ .

We now demonstrate what one of these relationships looks like in simple linear regression. We now simulate a dataset where  $\sigma^2 \propto E[Y|X]$ , and plot  $X$  against  $Y$ . We use the Poisson example discussed previously.

```
set.seed(2352)
n=1000
X=runif(n,5,10)*2
Y=20*rpois(n,X)+2
plot(X,Y)
```



```
# Performing a regression analysis yields:
model=lm(Y~X)
# Notice the intercept is poorly estimated!
summary(model)
```

```
Call:
lm(formula = Y ~ X)

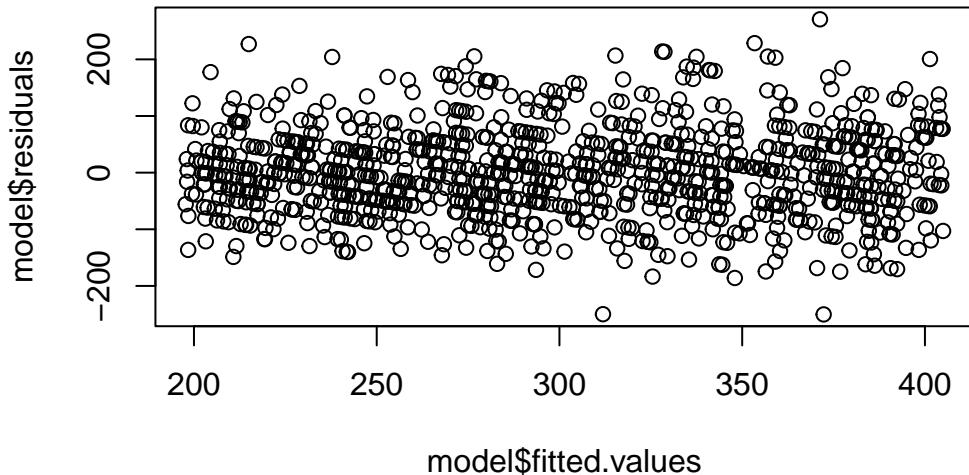
Residuals:
    Min      1Q  Median      3Q     Max 
-250.289 -53.392 -2.127  48.795 270.716 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -9.5199    13.0735  -0.728   0.467    
X           20.7241     0.8599  24.101  <2e-16 ***  
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 77.61 on 998 degrees of freedom
Multiple R-squared:  0.3679,    Adjusted R-squared:  0.3673
```

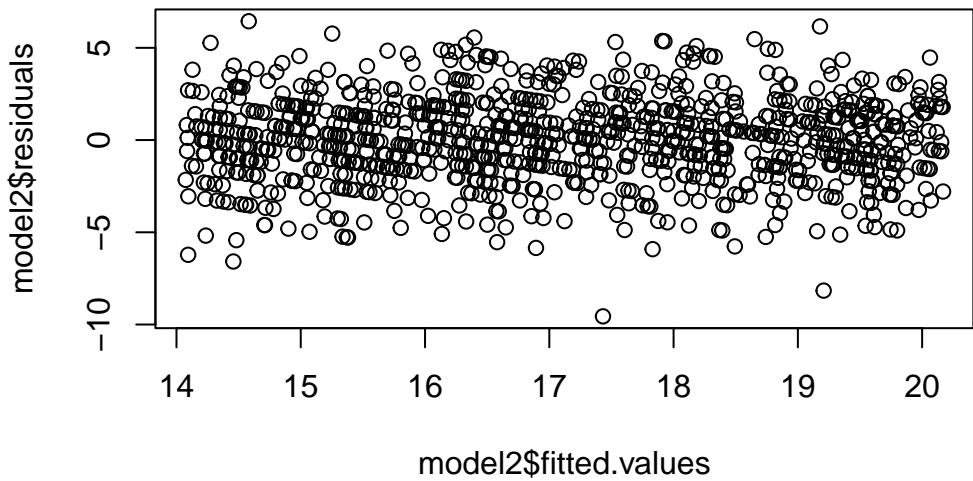
```
F-statistic: 580.9 on 1 and 998 DF, p-value: < 2.2e-16
```

```
# Notice the fan shape in the residuals against the fitted values?  
plot(model$fitted.values,model$residuals)
```

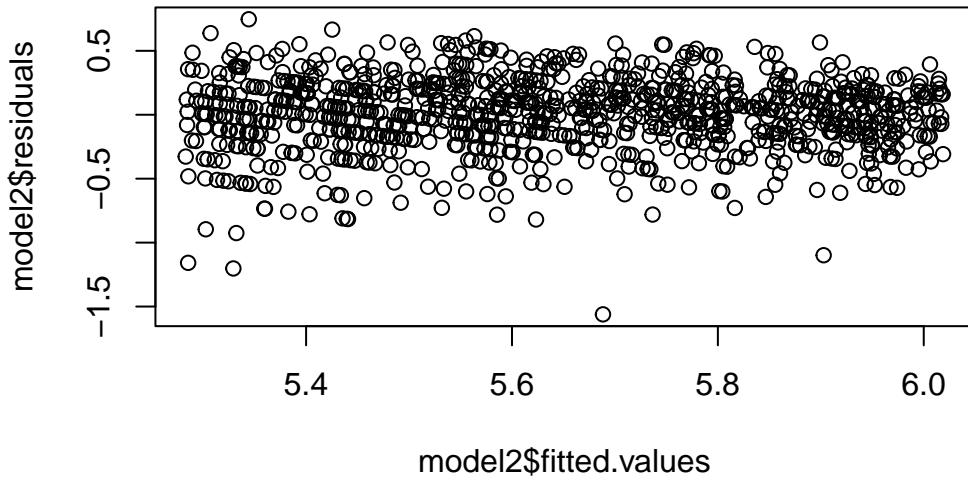


```
# Let's perform the transformations
```

```
model2=lm(sqrt(Y)~X)  
plot(model2$fitted.values,model2$residuals)
```



```
model2=lm(log(Y)~X)  
plot(model2$fitted.values,model2$residuals)
```



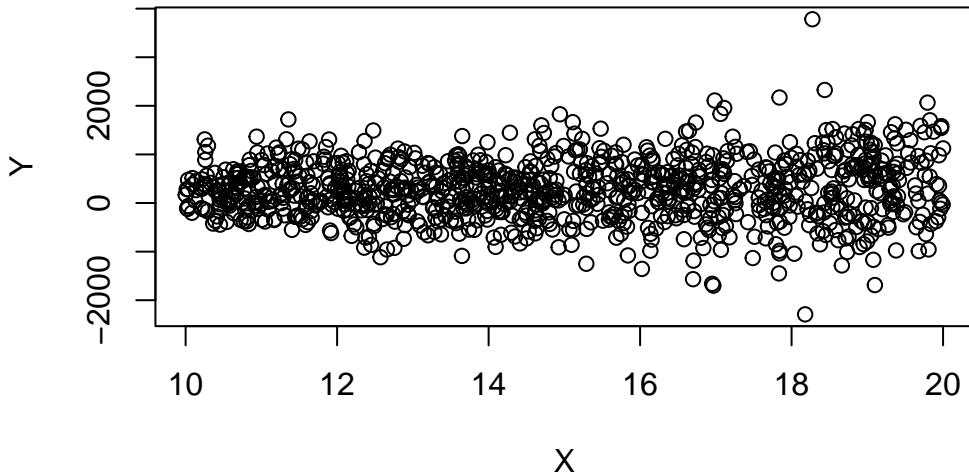
However, these transformations do not always work. Suppose we have that  $Y \sim \mathcal{N}(X, 4 * X^2)$ . We then have that  $\sigma = 2*X = 2*\text{E}[Y|X]$ . Notice how the spread of the points is increasing with  $X$ ? This is a symptom of non-homogeneous variance. However, the proposed transformations do not work.

```

set.seed(2352)
# \sigma^2\propto \text{E}[Y]
Y=20*rnorm(n,X,X*2)+2

plot(X,Y)

```



```
# Performing a regression analysis yields:
model=lm(Y~X)

# notice the intercept is poorly estimated.
summary(model)
```

Call:

`lm(formula = Y ~ X)`

Residuals:

Min	1Q	Median	3Q	Max
-2610.8	-375.3	-3.5	384.8	3460.5

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	76.844	103.345	0.744	0.4573
X	13.367	6.797	1.966	0.0495 *

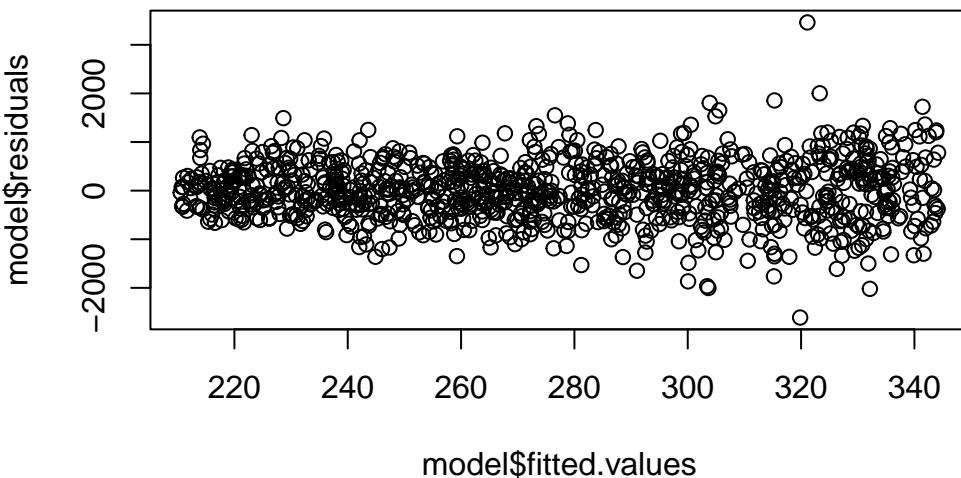
---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 613.5 on 998 degrees of freedom

```
Multiple R-squared:  0.00386,  Adjusted R-squared:  0.002861  
F-statistic: 3.867 on 1 and 998 DF,  p-value: 0.04953
```

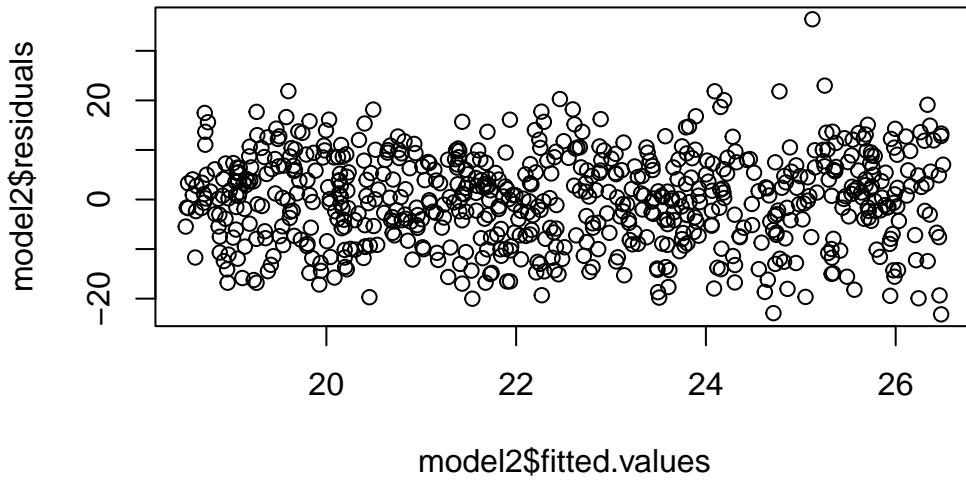
```
# Notice the fan shape in the residuals against the fitted values?  
plot(model$fitted.values,model$residuals)
```



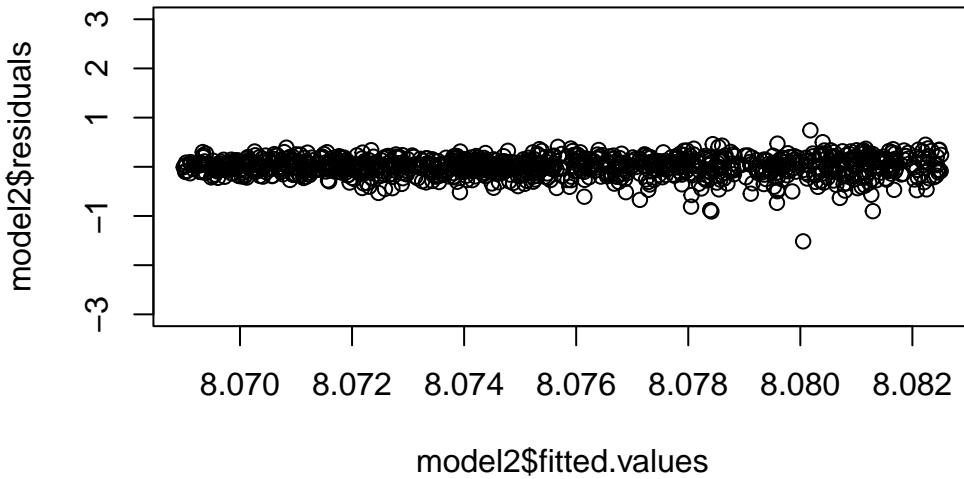
```
# Let's perform the transformation  
  
# Performing a regression analysis yields:  
model2=lm(sqrt(Y)~X)
```

```
Warning in sqrt(Y): NaNs produced
```

```
# Notice the fan shape in the residuals against the fitted values?  
plot(model2$fitted.values,model2$residuals)
```



```
# Performing a regression analysis yields:  
model2=lm(log(Y+3000)~X)  
  
# Notice the fan shape in the residuals against the fitted values?  
plot(model2$fitted.values,model2$residuals,ylim=c(-3,3))
```



In general, a good transformation to correct violated assumptions can improve estimates and test accuracy.

### 🔥 Caution

It is often necessary to convert any predicted values back to the original units. Applying the inverse transformation to predicted values gives an estimate of the median of the distribution of the (untransformed) response – instead of the mean. This implies that predictions are generally biased. Prediction and confidence intervals do not suffer this illness. They can be converted back to the original units via the inverse transformation and the interpretation will remain the same.

#### 5.1.1 Inverse transformations

Let's expand on this. It is a good time to recall that in general, for a real function  $f$ , we have that  $E[f(X)] \neq f(E[X])$ . For instance, for many random variables  $Z$ , we would have that  $E[Z^2] \neq E[Z]^2$ ,  $E[\log Z] \neq \log E[Z]$  etc. .

In a transformed regression model, we fit the following model:

$$f(Y) = X\beta + \epsilon.$$

If we are interested in predicting the value of  $Y$  given  $z$ , then it seems natural to take the predictions for  $f(Y)$  given  $z$ , which are given by  $\beta^\top z$  and apply the inverse transformation  $f^{-1}$ . For instance, to predict  $Y|Z = z$ , we may compute:  $f^{-1}(\beta^\top z)$ . It turns out, this prediction is biased, and we should use a different method instead.

To see why it's biased, observe that the predictions from the model  $f(Y) = X\beta + \epsilon$  for a new set of covariates  $z$  are given by  $\hat{f}(Y) = \hat{\beta}^\top z \approx E[f(Y)|Z = z]$ . Now, we have that

$$f^{-1}(\hat{\beta}^\top z) \approx f^{-1}(E[f(Y)|Z = z]) \neq E[f^{-1}(f(Y))|Z = z] = E[\hat{f}(Y)|Z = z].$$

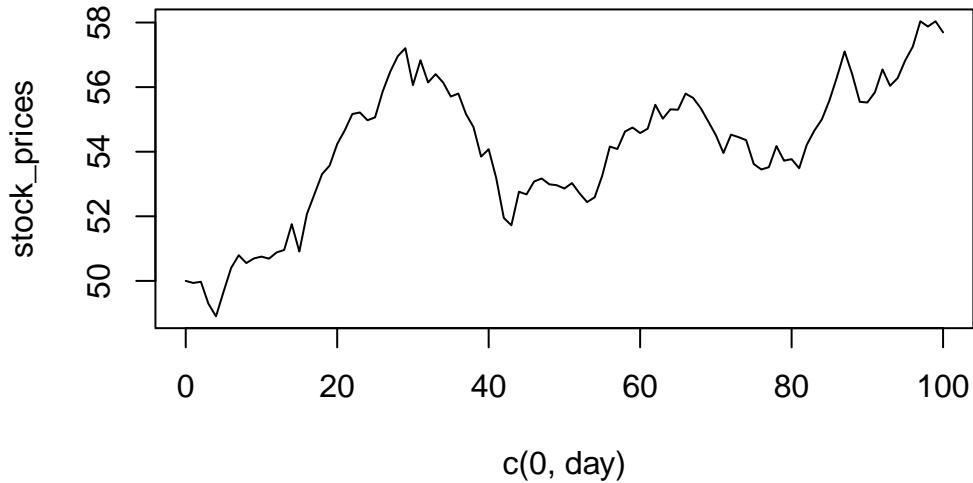
The solution to this problem is to adjust for the bias. For the log transform, we can multiply the resulting inverse transformed predictions by  $\exp(\hat{\sigma}^2/2)$ . For the square root transformation, we add  $\hat{\sigma}^2$  to the resulting inverse transformed predictions. See (Miller 1984) for more information.

One can also use confidence and prediction intervals to predict the value of  $Y$  given  $z$ . Confidence or prediction intervals may be directly converted from one metric to another – such interval estimates are percentiles of a distribution which are unaffected by the transformation. They can be converted back to the original units via the inverse transformation and the interpretation will remain the same. Optimal intervals are intervals with the shortest average interval length for a given confidence level, under a given set of assumptions. However, it may be that the resulting intervals may not be “optimal”. One way to get a prediction in the original units, is to apply the inverse transformation to the prediction interval computed from the transformed model and take the midpoint of that interval. This does not always work well - and should be checked against the original data.

**Example 5.1.** Let's simulate what happens when, given the day  $t \in [100]$ , we try to estimate the mean stock price  $P_t$  for some stock (maybe ?Gamestop?) in a model which regresses the logged rate of return against the day. Note that the logged returns at time  $t$  are given by:  $L = \log\left(\frac{P_t}{P_{t-1}}\right)$ .

```
set.seed(2352)
# Simulate the stock prices
n=100
day=seq(1:n)
log_return=rnorm(n,0.000001+0.000005*day,0.01)
# log_return=rnorm(n,0.000001+0.000005*day,0.0005)
stock_prices=c(50,50*exp(cumsum(log_return)))
# exp(log_return)[1:10]

plot(c(0,day), stock_prices,type='l')
```

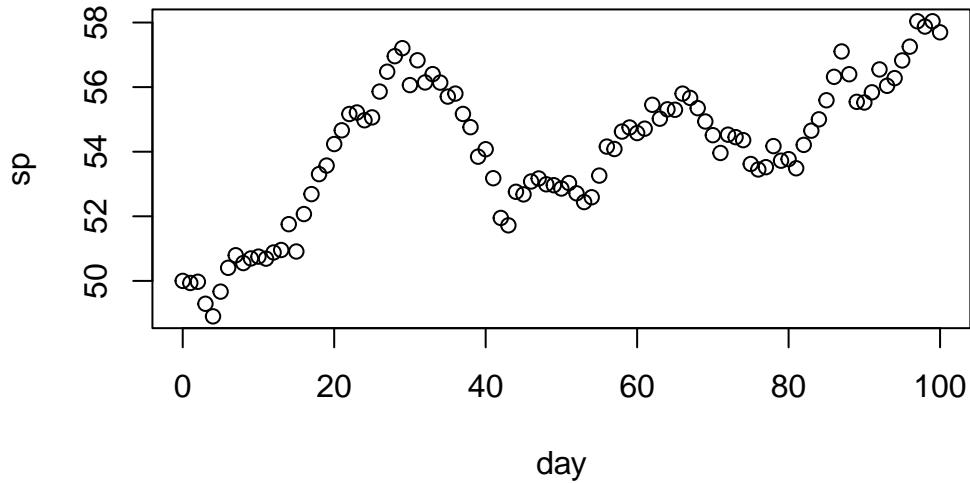


```
df=data.frame(cbind("day"=c(0,day),"sp"=stock_prices))
```

```
# Now, suppose this is our starting dataset
head(df)
```

	day	sp
1	0	50.00000
2	1	49.93624
3	2	49.97369
4	3	49.29229
5	4	48.90210
6	5	49.66743

```
# Notice that the pattern is not great... but we can regress on the transformed response
plot(df)
```



```
# Fitting the model

# Compute the log returns
df$lr=NA
df$lr[2:(n+1)]=log(df$sp[-1]/df$sp[-(n+1)])

# Sanity Check
# log_return[1:5]
# df$lr[2:6]

model=lm(lr~day,df)
summary(model)
```

Call:

`lm(formula = lr ~ day, data = df)`

Residuals:

Min	1Q	Median	3Q	Max
-0.0249054	-0.0064851	0.0000518	0.0075839	0.0208044

Coefficients:

```

      Estimate Std. Error t value Pr(>|t|)
(Intercept) 1.824e-03 1.926e-03  0.947   0.346
day         -7.771e-06 3.312e-05 -0.235   0.815

Residual standard error: 0.00956 on 98 degrees of freedom
(1 observation deleted due to missingness)
Multiple R-squared:  0.0005615, Adjusted R-squared:  -0.009637
F-statistic: 0.05506 on 1 and 98 DF,  p-value: 0.815

```

```

plot(c(0,day), stock_prices,type='l',lwd=2)
lines(50*exp(cumsum(fitted.values(model))),col='red',lty=2,lwd=2)

# Intervals for the mean at each time point
intervals=predict(model,interval = 'prediction')[,2:3]

```

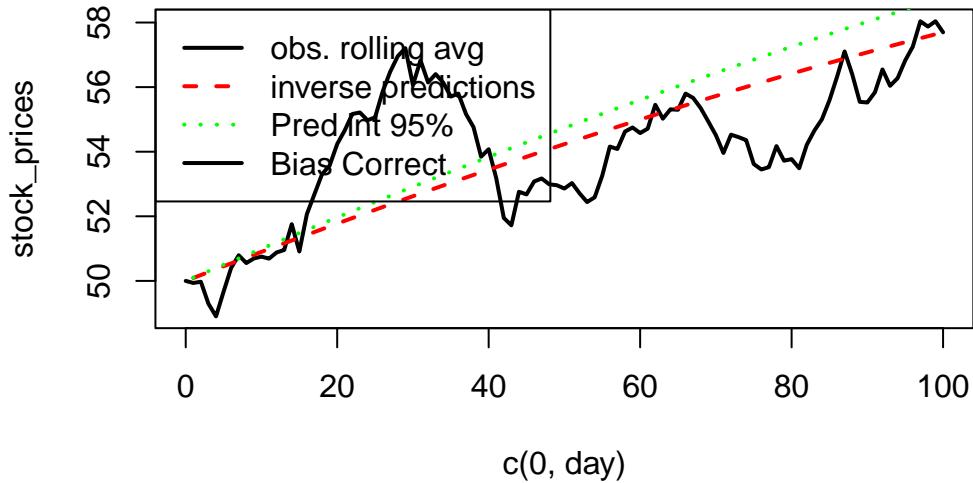
Warning in predict.lm(model, interval = "prediction"): predictions on current data refer to ...

```

midpoint=ret=rep(0,n)
for(i in 1:n){
  if(i==1){
    midpoint[i]=50*exp(intervals[i,1])/2+50*exp(intervals[i,2])/2
  }
  else
    midpoint[i]=midpoint[i-1]*(exp(intervals[i,1])+exp(intervals[i,2]))/2
}
lines(midpoint,col="green",lty=3,lwd=2)

legend("topleft",legend=c("obs. rolling avg","inverse predictions","Pred int 95%","Bias Coef"))

```



A second example...

```

set.seed(2352)
# Simulate data
n=100
X=runif(n,5,10)
logs=rnorm(n,1+0.2*X,0.5)
Y=exp(logs)
plot(X,Y)

df=data.frame(cbind("X"=X,"Y"=Y))
df=df[order(X),]

# Fitting the model
model=lm(log(Y)~X,data=df)
summary(model)

```

```

Call:
lm(formula = log(Y) ~ X, data = df)

```

Residuals:

Min	1Q	Median	3Q	Max
-1.13484	-0.31721	-0.02877	0.29765	0.85929

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	1.00060	0.21048	4.754	6.85e-06 ***
X	0.19333	0.02721	7.106	1.94e-10 ***
---				

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.4113 on 98 degrees of freedom

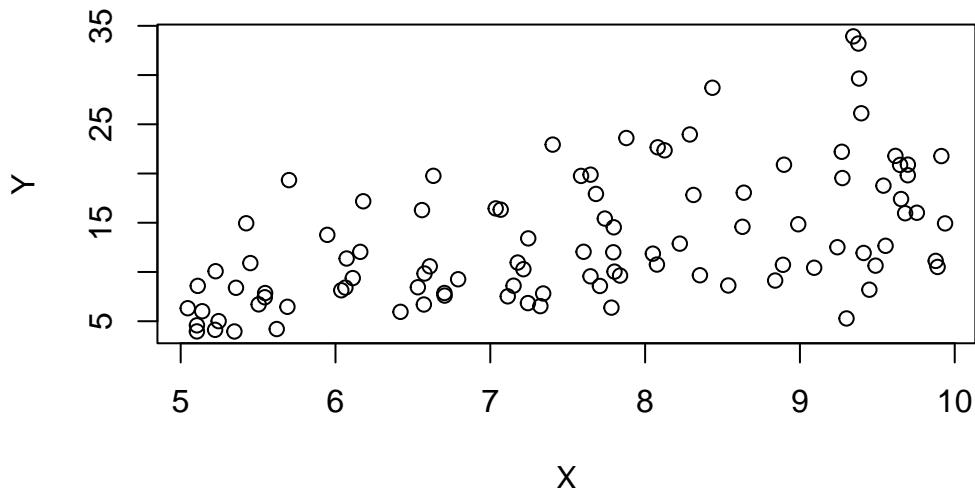
Multiple R-squared: 0.3401, Adjusted R-squared: 0.3333

F-statistic: 50.5 on 1 and 98 DF, p-value: 1.937e-10

```
s=summary(model)$sigma
```

```
# Rolling average
```

```
zb=zoo::zoo(x=df$Y,df$X)
```



```

rm=zoo::rollmean(zb,25)

plot(attributes(rm)$index,rm,lty=1,lwd=3,type='l')
# plot(X,Y)

zb=zoo::zoo(x=exp(fitted.values(model)),df$X)
rm=zoo::rollmean(zb,25)
lines(attributes(rm)$index,rm,col=2,lty=2,lwd=3)

lines(attributes(rm)$index,rm*exp(s^2/2),col=6,lty=2,lwd=3)

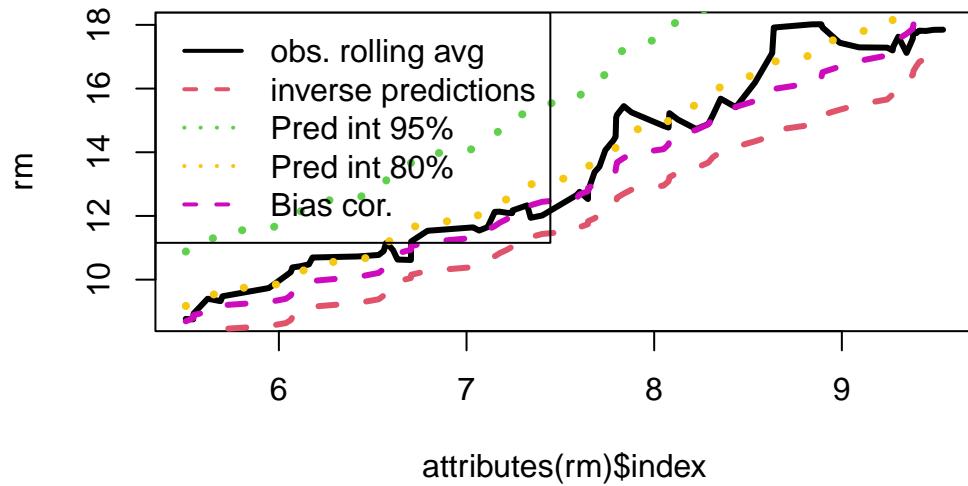
# Intervals for the mean at each time point
nd=data.frame("X"=df$X)
ivs=predict(model, newdata = nd,interval = 'prediction')[,2:3]
intervals=rowMeans(exp(ivs))
zb=zoo::zoo(x=intervals,df$X)
rm=zoo::rollmean(zb,25)
lines(attributes(rm)$index,rm,col=3,lty=3,lwd=4)

# Intervals for the mean at each time point - notice when we lower the level the performance
nd=data.frame("X"=df$X)
ivs=predict(model, newdata = nd,interval = 'prediction', level = 0.8)[,2:3]
intervals=rowMeans(exp(ivs))
zb=zoo::zoo(x=intervals,df$X)
rm=zoo::rollmean(zb,25)
lines(attributes(rm)$index,rm,col=7,lty=3,lwd=4)

# Intervals for the mean at each time point using confidence intervals
# ivs=predict(model, newdata = nd,interval = 'confidence', level = 0.8)[,2:3]
# intervals=rowMeans(exp(ivs))
# zb=zoo::zoo(x=intervals,df$X)
# rm=zoo::rollmean(zb,25)
# lines(attributes(rm)$index,rm,col=6,lty=3,lwd=3)

legend("topleft",legend=c("obs. rolling avg","inverse predictions","Pred int 95%","Pred in"))

```



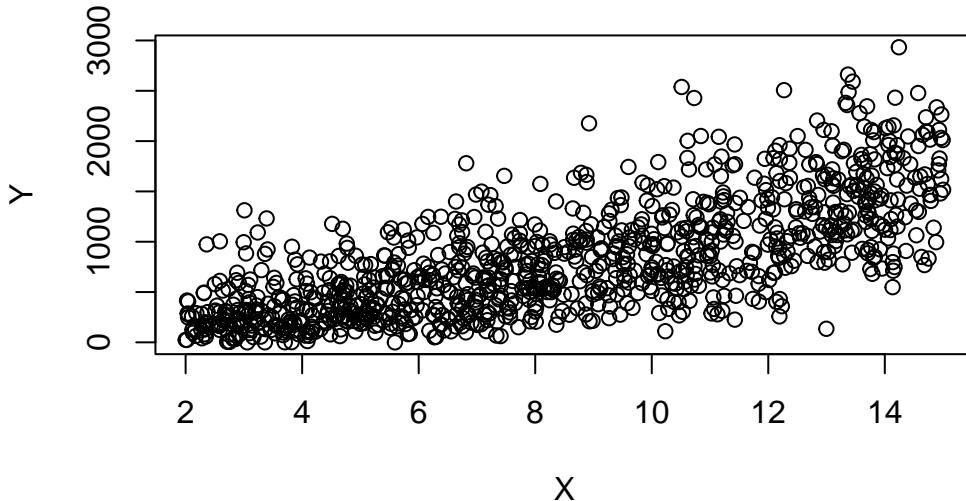
```

set.seed(2352)

# Simulate data

n=1000
X=runif(n,2,15)
sq=rnorm(n,10+2*X,7)
Y=sq^2
plot(X,Y)

```



```

df=data.frame(cbind("X"=X, "Y"=Y))
df=df[order(X),]

# Fitting the model
model=lm(sqrt(Y)~X,data=df)
summary(model)

```

Call:  
`lm(formula = sqrt(Y) ~ X, data = df)`

Residuals:

Min	1Q	Median	3Q	Max
-24.2975	-4.5612	-0.0315	4.7083	20.2670

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	9.94439	0.54223	18.34	<2e-16 ***
X	1.99810	0.05897	33.88	<2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

```
Residual standard error: 6.919 on 998 degrees of freedom
Multiple R-squared:  0.535, Adjusted R-squared:  0.5345
F-statistic: 1148 on 1 and 998 DF,  p-value: < 2.2e-16
```

```
s=summary(model)$sigma
# plot(X,Y)
# Rolling average

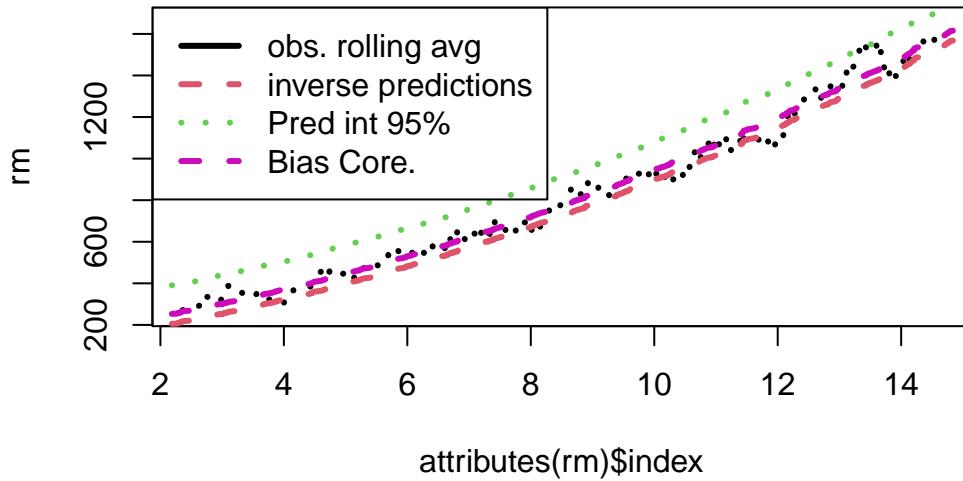
zb=zoo::zoo(x=df$Y,df$X)
rm=zoo::rollmean(zb,50)

plot(attributes(rm)$index,rm,col=1,lty=3,lwd=3,type='l')
zb=zoo::zoo(fitted.values(model)^2,df$X)
rm=zoo::rollmean(zb,25)
lines(attributes(rm)$index,rm,col=2,lty=2,lwd=3)
lines(attributes(rm)$index,rm+s^2,col=6,lty=2,lwd=3)

# Intervals for the mean at each time point
intervals=rowMeans(predict.lm(model,interval = 'prediction')[,2:3]^2)

Warning in predict.lm(model, interval = "prediction"): predictions on current data refer to ...

zb=zoo::zoo(intervals,df$X)
rm=zoo::rollmean(zb,25)
lines(attributes(rm)$index,rm,col=3,lty=3,lwd=3)
legend("topleft",legend=c("obs. rolling avg","inverse predictions","Pred int 95%","Bias Co
```



We see that the bias correction is the best performing method. However, this involves working out the bias for each transformation. For a complicated transformation, this may be quite difficult. For common transformations, this has already been completed for us.

Let's do an example with some real data. The following example is taken from the textbook:

**Example 5.2.** An electric utility is interested in developing a model relating peak - hour demand  $Y$  to total energy usage during the month  $X$ . This is an important planning problem because while most customers pay directly for energy usage (in kilowatt - hours), the generation system must be large enough to meet the maximum demand imposed. Data for 53 residential customers for the month of August is given below.

```
# Electric Utility Data

df<- data.frame(
  Customer = c(1:53),
  x_kWh = c(679, 292, 1012, 493, 582, 1156, 997, 2189, 1097, 2078, 1818, 1700, 747, 2030,
  y_kW = c(0.79, 0.44, 0.56, 0.79, 2.70, 3.64, 4.73, 9.50, 5.34, 6.85, 5.84, 5.21, 3.25,
)
```

df

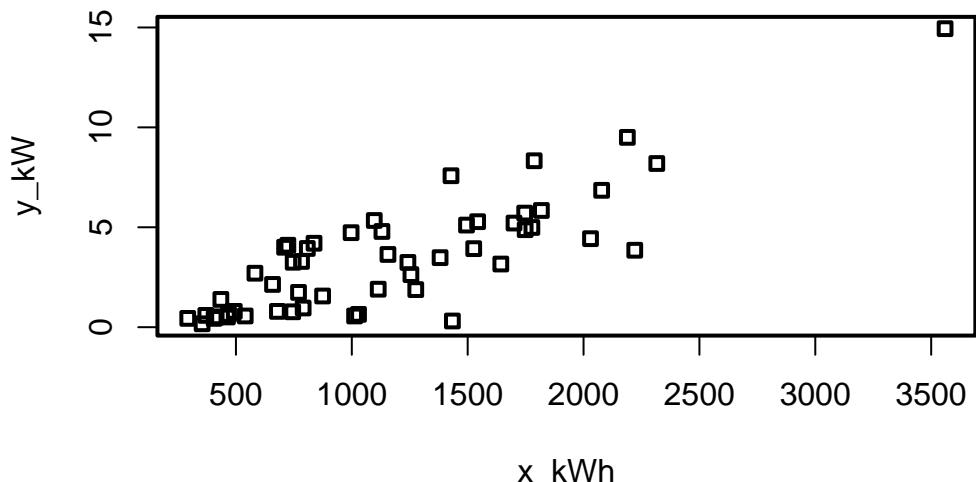
	Customer	x_kWh	y_kW
1	1	679	0.79
2	2	292	0.44
3	3	1012	0.56
4	4	493	0.79
5	5	582	2.70
6	6	1156	3.64
7	7	997	4.73
8	8	2189	9.50
9	9	1097	5.34
10	10	2078	6.85
11	11	1818	5.84
12	12	1700	5.21
13	13	747	3.25
14	14	2030	4.43
15	15	1643	3.16
16	16	414	0.50
17	17	354	0.17
18	18	1276	1.88
19	19	745	0.77
20	20	435	1.39
21	21	540	0.56
22	22	874	1.56
23	23	1543	5.28
24	24	1029	0.64
25	25	710	4.00
26	26	1434	0.31
27	27	837	4.20
28	28	1748	4.88
29	29	1381	3.48
30	30	1428	7.58
31	31	1255	2.63
32	32	1777	4.99
33	33	370	0.59
34	34	2316	8.19
35	35	1130	4.79
36	36	463	0.51
37	37	770	1.74
38	38	724	4.10
39	39	808	3.94
40	40	790	0.96
41	41	783	3.29
42	42	406	0.44

```
43      43 1242  3.24
44      44  658  2.14
45      45 1746  5.71
46      46  468  0.64
47      47 1114  1.90
48      48  413  0.51
49      49 1787  8.33
50      50 3560 14.94
51      51 1495  5.11
52      52 2221  3.85
53      53 1526  3.93
```

```
# changing the plot aesthetics
par(pch=22,lwd=2)
```

```
# Explore
```

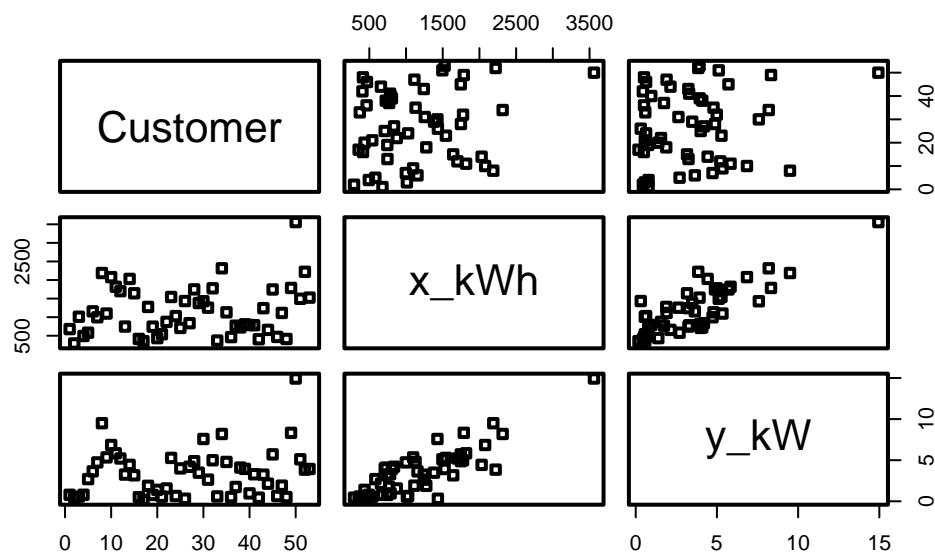
```
plot(df[,2:3])
```



```
summary(df)
```

```
Customer      x_kWh          y_kW
Min.   : 1   Min.   : 292   Min.   : 0.170
1st Qu.:14  1st Qu.: 679   1st Qu.: 0.790
Median :27   Median :1029   Median : 3.250
Mean   :27   Mean   :1153   Mean   : 3.413
3rd Qu.:40  3rd Qu.:1543  3rd Qu.: 4.880
Max.   :53   Max.   :3560   Max.   :14.940
```

```
plot(df)
```



```
# Model
model=lm(y_kW~x_kWh, df); model
```

```
Call:
lm(formula = y_kW ~ x_kWh, data = df)

Coefficients:
(Intercept)      x_kWh
-0.831304     0.003683
```

```

summ=summary(model); summ

Call:
lm(formula = y_kW ~ x_kWh, data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-4.1399 -0.8275 -0.1934  1.2376  3.1522 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -0.8313037  0.4416121 -1.882   0.0655 .  
x_kWh        0.0036828  0.0003339 11.030 4.11e-15 *** 
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

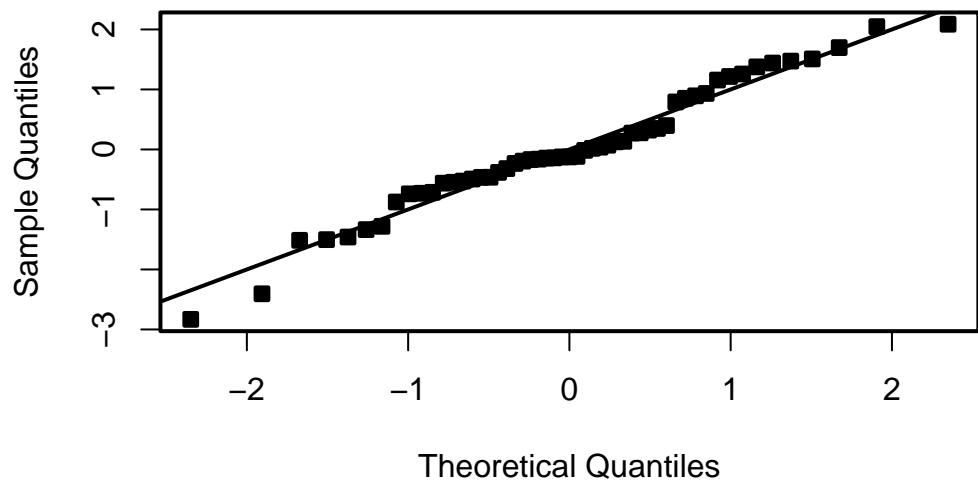
Residual standard error: 1.577 on 51 degrees of freedom
Multiple R-squared:  0.7046,    Adjusted R-squared:  0.6988 
F-statistic: 121.7 on 1 and 51 DF,  p-value: 4.106e-15

# Now do the residual analysis
# Studentized residuals
student_res=rstudent(model)
MSE=summ$sigma^2

qqnorm(student_res,pch=22,bg=1)
abline(0,1)

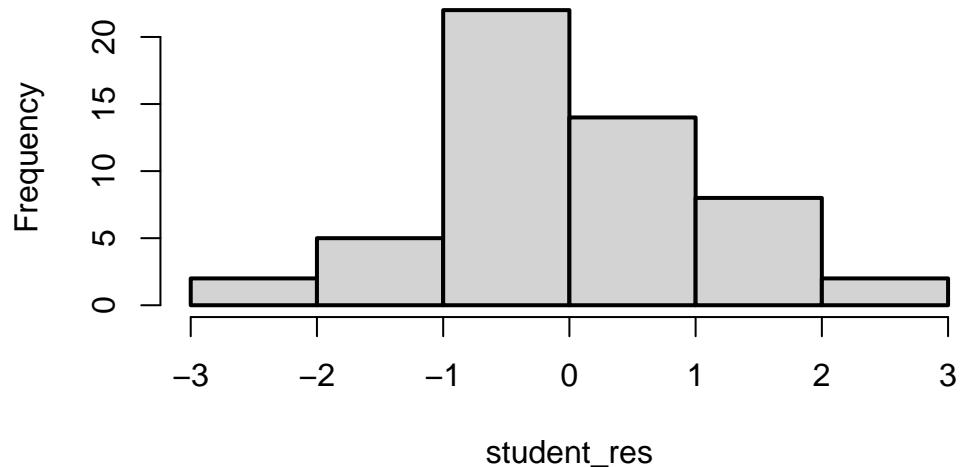
```

### Normal Q-Q Plot

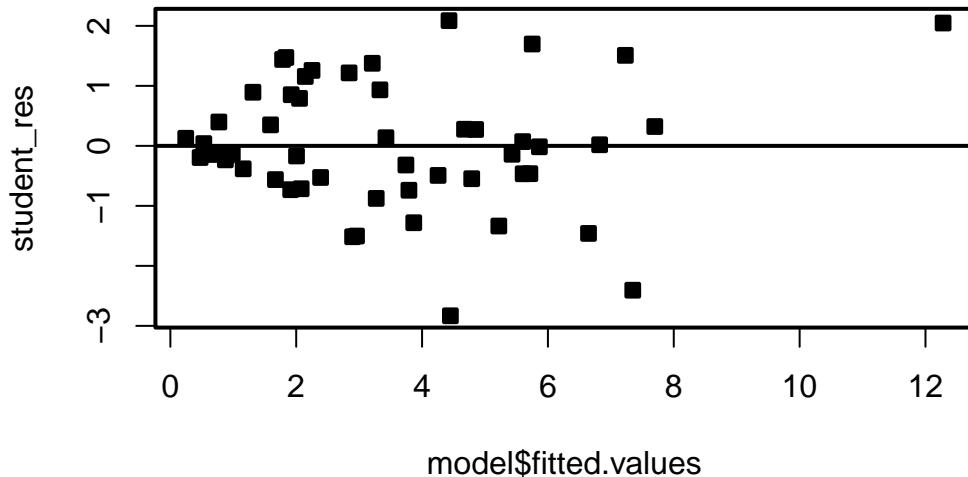


```
hist(student_res, breaks=6)
```

### Histogram of student\_res



```
plot(model$fitted.values, student_res, pch=22, bg=1)
abline(h=0)
```



We see that the residual variance increases with the mean of  $Y$ . This is easily seen by the fan shape of the residuals in the plot of the residuals against the fitted values.

```
##### Let's try the sqrt transformation
```

```
model2=lm(sqrt(y_kW)~x_kWh, df)
model2
```

```
Call:
lm(formula = sqrt(y_kW) ~ x_kWh, data = df)

Coefficients:
(Intercept)      x_kWh
0.5822259     0.0009529
```

```
summ2=summary(model2); summ2
```

```

Call:
lm(formula = sqrt(y_kW) ~ x_kWh, data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-1.39185 -0.30576 -0.03875  0.25378  0.81027 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) 5.822e-01  1.299e-01   4.481 4.22e-05 ***
x_kWh       9.529e-04  9.824e-05   9.699 3.61e-13 ***  
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

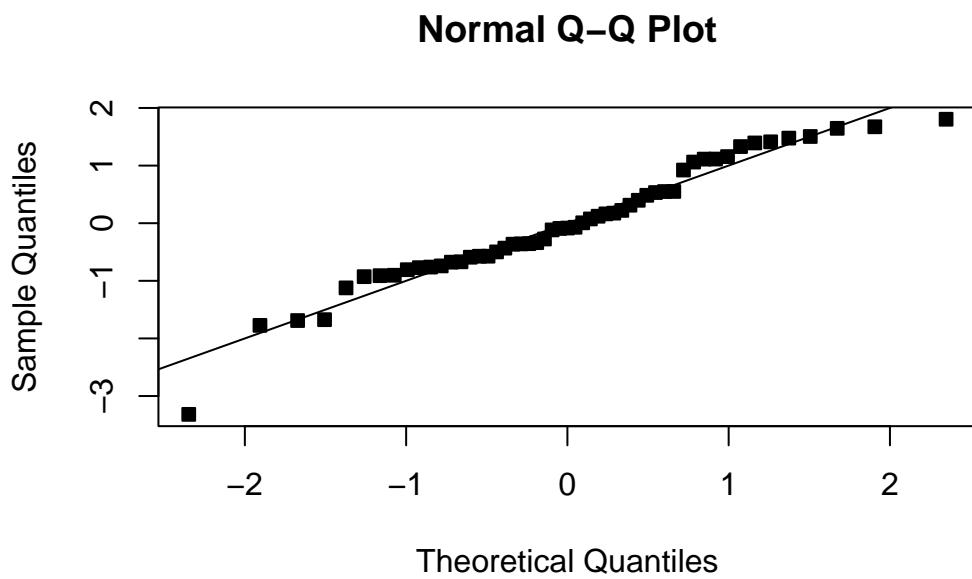
Residual standard error: 0.464 on 51 degrees of freedom
Multiple R-squared:  0.6485,    Adjusted R-squared:  0.6416 
F-statistic: 94.08 on 1 and 51 DF,  p-value: 3.614e-13

```

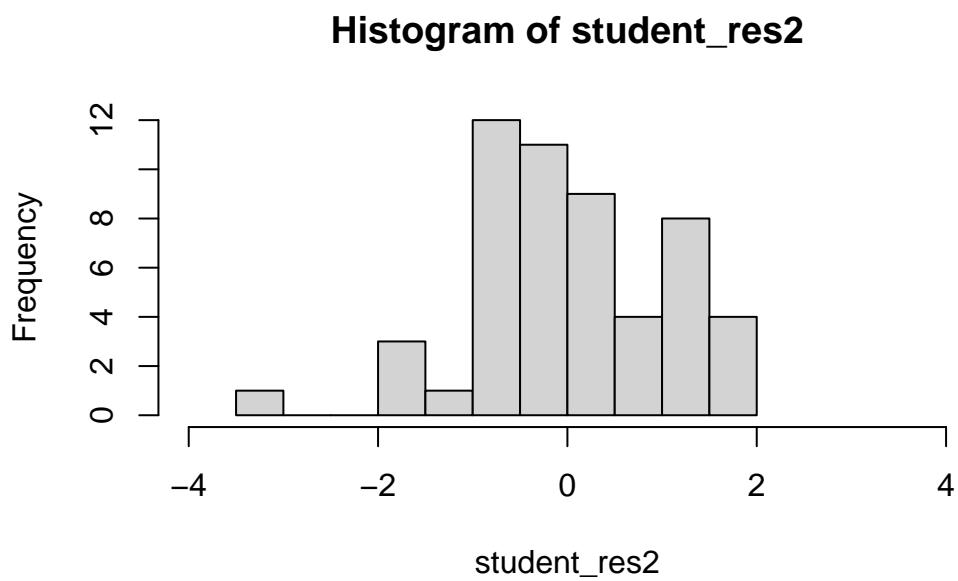
```

student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)

```

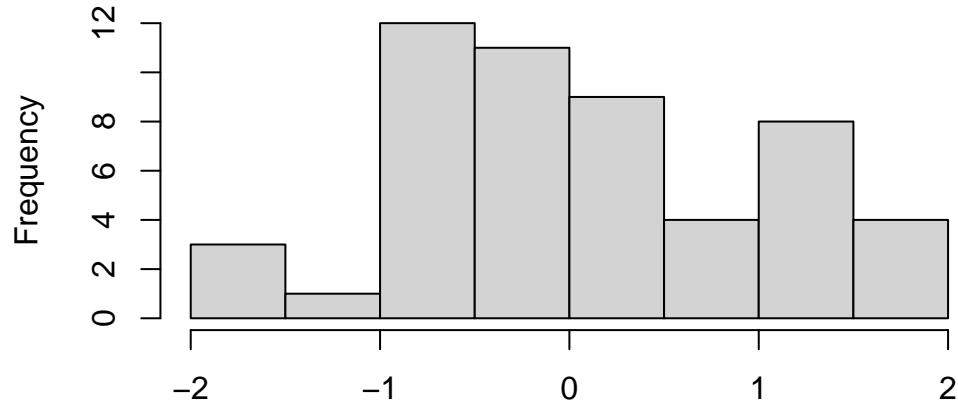


```
hist(student_res2, breaks=10, xlim=c(-4,4))
```



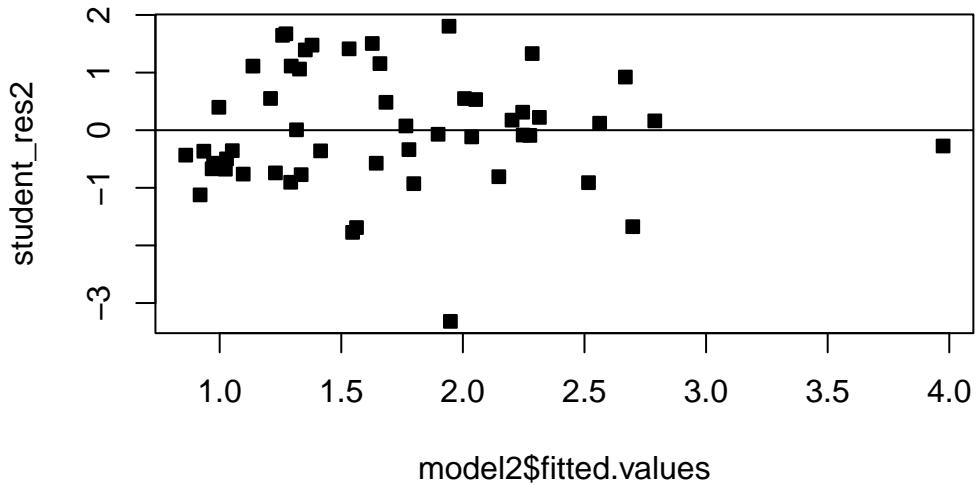
```
hist(student_res2[-which.max(abs(student_res2))],breaks=10,xlim=c(-2,2))
```

### Histogram of student\_res2[-which.max(abs(student\_res2))]

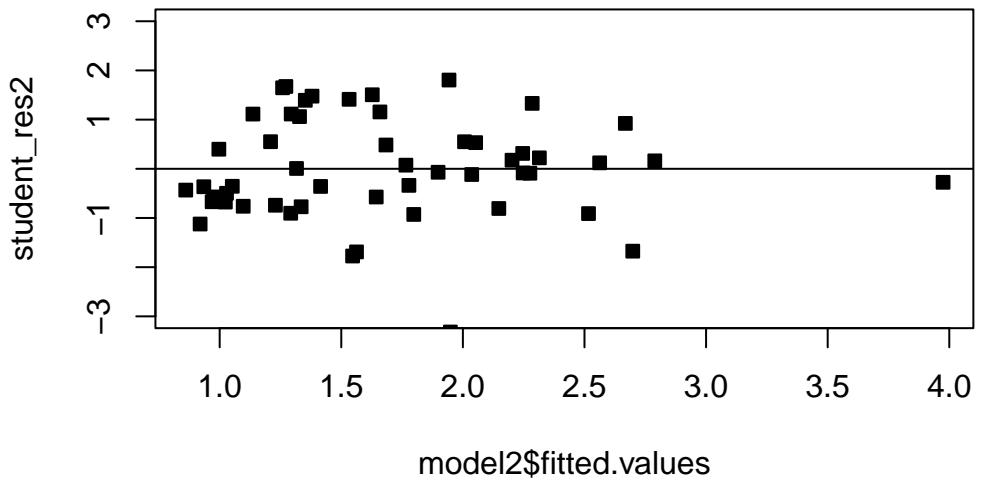


```
student_res2[-which.max(abs(student_res2))]
```

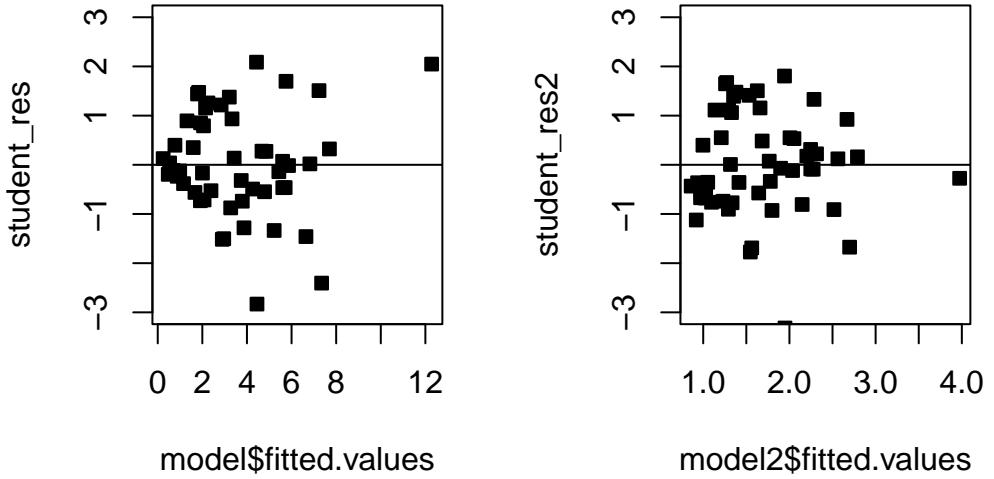
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)  
abline(h=0)
```



```
# There is one large outlier skewing the previous plot. Let's rescale and remove.  
plot(model2$fitted.values,student_res2,pch=22,bg=1,ylim=c(-3,3))  
abline(h=0)
```



```
# Compare!
par(mfrow=c(1,2))
plot(model$fitted.values,student_res,pch=22,bg=1,ylim=c(-3,3))
abline(h=0)
plot(model2$fitted.values,student_res2,pch=22,bg=1,ylim=c(-3,3))
abline(h=0)
```



We see that the transformation has solved the problem. Note that sometimes, even though the square-root transformation may be more suitable, the analyst may opt for the logarithm transform. This is because the log transformation gives a nicer interpretation to the coefficients. In this case, that is not working well, see below:

```
##### Let's try the log transformation
par(mfrow=c(1,1))
```

```
model3=lm(log(y_kW)~x_kWh, df)
model3
```

```
Call:
lm(formula = log(y_kW) ~ x_kWh, data = df)
```

```
Coefficients:
(Intercept)      x_kWh
-0.558713     0.001172
```

```
summ3=summary(model3); summ3
```

```

Call:
lm(formula = log(y_kW) ~ x_kWh, data = df)

Residuals:
    Min      1Q  Median      3Q     Max 
-2.29261 -0.47256  0.08414  0.49628  1.12143 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -0.5587131  0.2057201 -2.716   0.009 **  
x_kWh        0.0011716  0.0001555  7.533 7.86e-10 *** 
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.7347 on 51 degrees of freedom
Multiple R-squared:  0.5266,    Adjusted R-squared:  0.5174 
F-statistic: 56.74 on 1 and 51 DF,  p-value: 7.862e-10

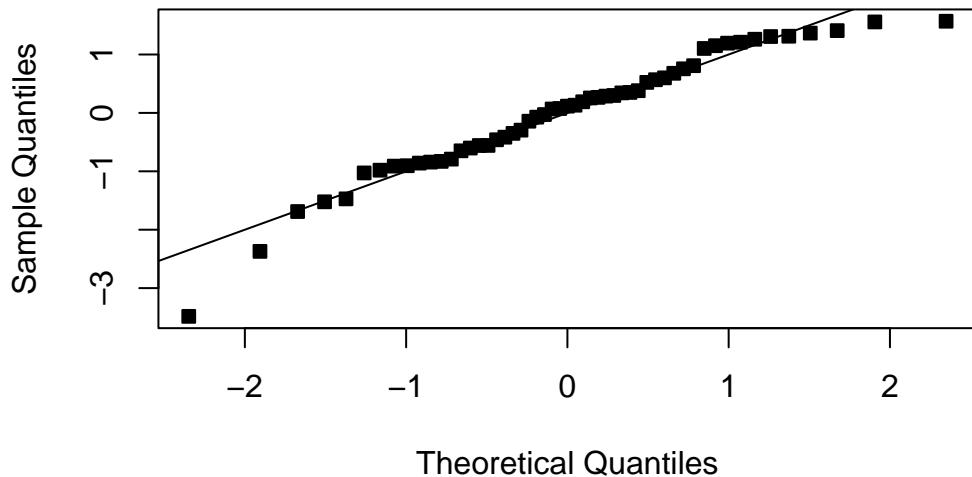
```

```

student_res3=rstudent(model3)
MSE3=summ3$sigma^2
qqnorm(student_res3,pch=22, bg=1)
abline(0,1)

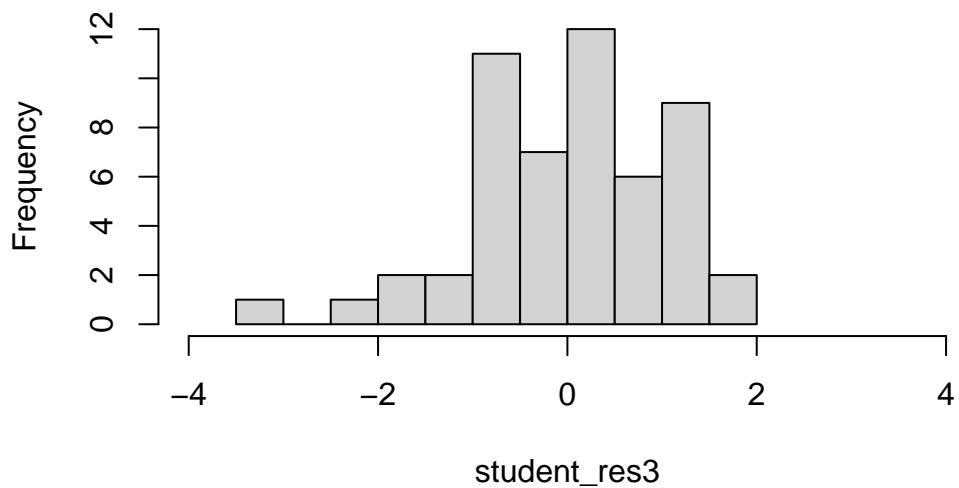
```

### Normal Q-Q Plot



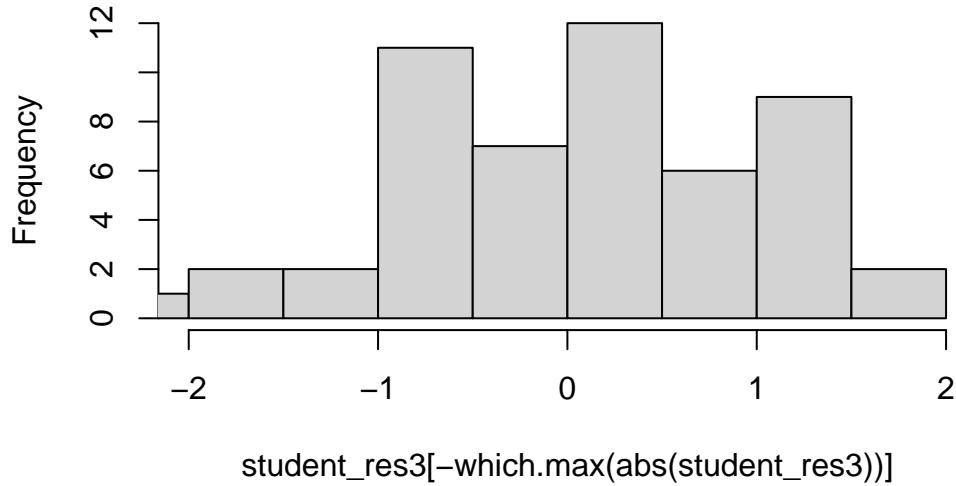
```
hist(student_res3, breaks=10, xlim=c(-4,4))
```

### Histogram of student\_res3



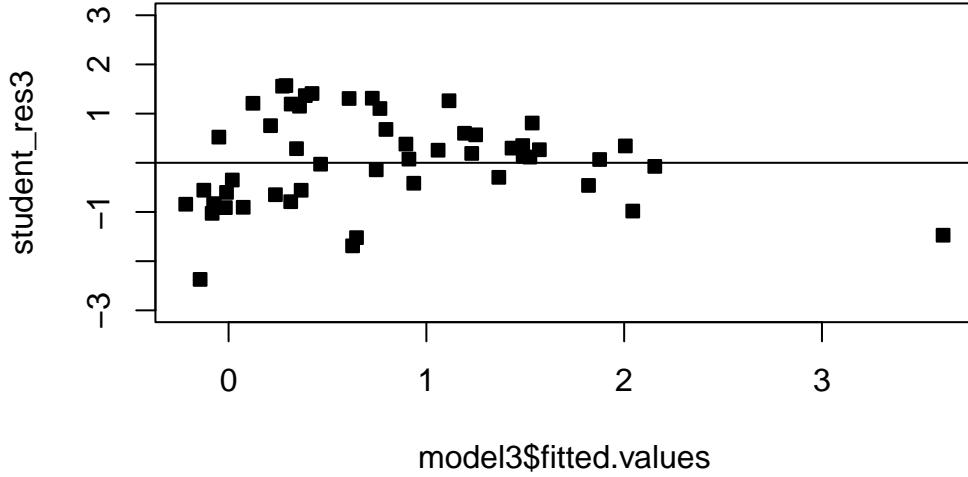
```
hist(student_res3[-which.max(abs(student_res3))],breaks=10,xlim=c(-2,2))
```

Histogram of student\_res3[-which.max(abs(student\_res3))]



```
student_res3[-which.max(abs(student_res3))]
```

```
plot(model3$fitted.values,student_res3,pch=22,bg=1,ylim=c(-3,3))
abline(h=0)
```



## 5.2 Linearizing the model

Moving on, we may suspect that the relationship between the regressors and the response is nonlinear, either through empirical evidence or theoretical justification. In some cases a nonlinear function can be linearized by using a suitable transformation. Such nonlinear models are called intrinsically linear. For example, consider the model  $Y = \beta_0 e^{\beta_1 X} \epsilon$ . Taking the log of both sides yields:

$$\log(Y) = \log(\beta_0) + \beta_1 X + \log(\epsilon).$$

Reparameterizing with  $Z = \log(Y)$ ,  $\alpha_0 = \log(\beta_0)$  and  $\eta = \log(\epsilon)$ , we have that

$$Z = \alpha_0 + \beta_1 X + \eta.$$

If we are willing to assume that  $\eta$  are symmetric about 0 with a constant variance, then we can run a linear regression with the model given above. To get estimates for the original units  $Y$ , we can transform back as previously discussed. A model is linearizable if there exists some reparameterization which places the model in the form of the MLR.

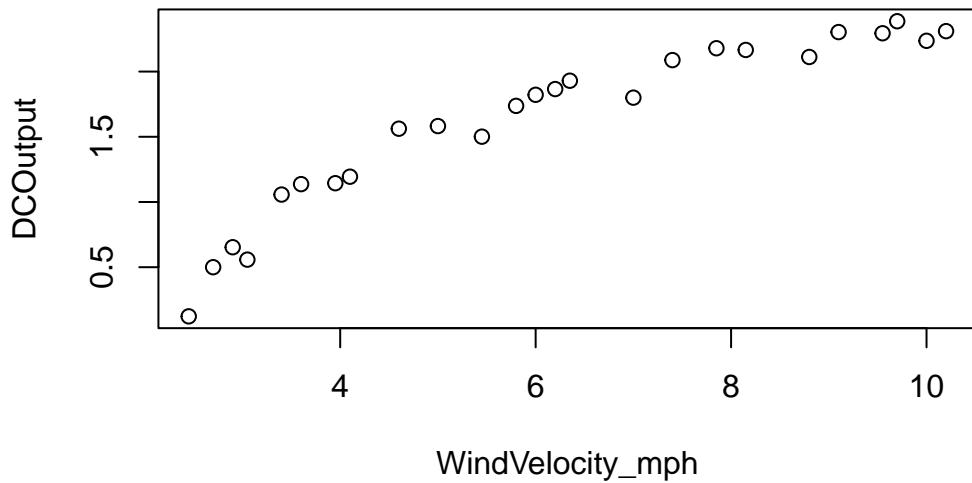
**Exercise 5.1.** Show the following models are linearizable - that is, find the linear reparameterization of the following models: 1.  $Y = \beta_0 X_1^\beta$  2.  $Y = \beta_0 X^{\beta_1 X}$  3.  $Y = \beta_0 + \log X$  4.  $Y = X / (\beta_0 X - \beta_1)$

**Example 5.3.** A research engineer is investigating the use of a windmill to generate electricity. He has collected data on the DC output from his windmill and the corresponding wind velocity. See below. Find a well-fitting regression model for this data.

```
##### Windmill data

# Create the data frame
df_wind <- data.frame(
  WindVelocity_mph = c(5.00, 6.00, 3.40, 2.70, 10.00, 9.70, 9.55, 3.05, 8.15, 6.20,
                      2.90, 6.35, 4.60, 5.80, 7.40, 3.60, 7.85, 8.80, 7.00, 5.45,
                      9.10, 10.20, 4.10, 3.95, 2.45),
  DCOutput = c(1.582, 1.822, 1.057, 0.500, 2.236, 2.386, 2.294, 0.558, 2.166, 1.866,
              0.653, 1.930, 1.562, 1.737, 2.088, 1.137, 2.179, 2.112, 1.800, 1.501,
              2.303, 2.310, 1.194, 1.144, 0.123)
)

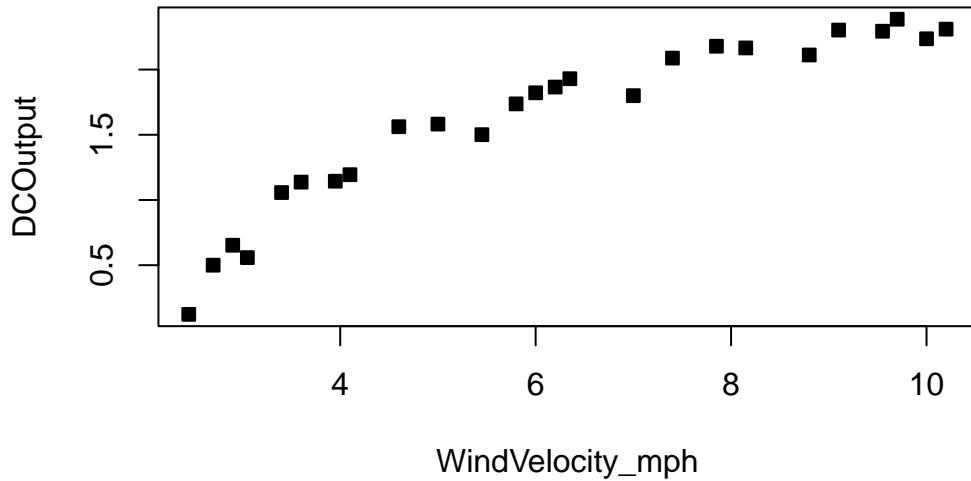
#####
par(mfrow=c(1,1))
plot(df_wind)
```



```
summary(df_wind)
```

WindVelocity_mph	DCOutput
Min. : 2.450	Min. : 0.123
1st Qu.: 3.950	1st Qu.: 1.144
Median : 6.000	Median : 1.800
Mean : 6.132	Mean : 1.610
3rd Qu.: 8.150	3rd Qu.: 2.166
Max. :10.200	Max. : 2.386

```
plot(df_wind,pch=22,bg=1)
```



```
model=lm(DCOutput~WindVelocity_mph, df_wind)
model
```

```
Call:
lm(formula = DCOutput ~ WindVelocity_mph, data = df_wind)
```

Coefficients:

(Intercept)	WindVelocity_mph
0.1309	0.2411

```
summ=summary(model); summ
```

```
Call:
lm(formula = DCOutput ~ WindVelocity_mph, data = df_wind)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.59869	-0.14099	0.06059	0.17262	0.32184

```

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 0.13088   0.12599   1.039    0.31
WindVelocity_mph 0.24115   0.01905 12.659 7.55e-12 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.2361 on 23 degrees of freedom
Multiple R-squared: 0.8745, Adjusted R-squared: 0.869
F-statistic: 160.3 on 1 and 23 DF, p-value: 7.546e-12

```

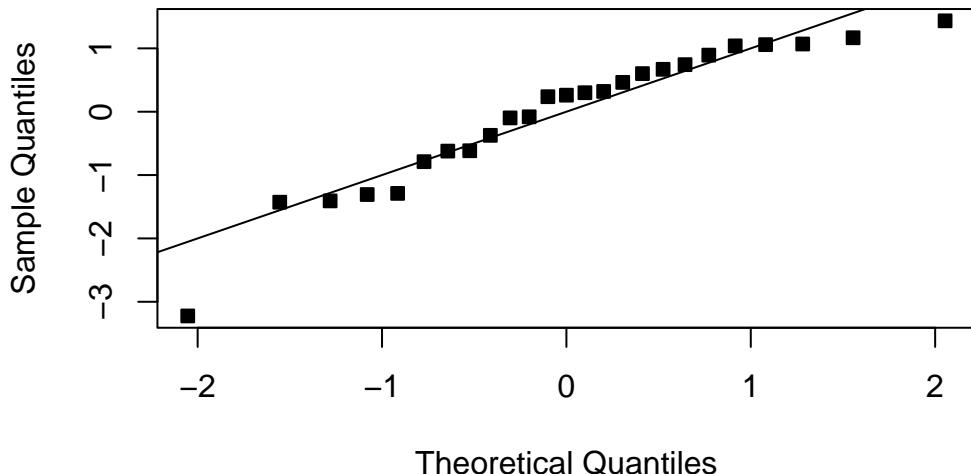
```

student_res=rstudent(model)

MSE=summ$sigma^2
qqnorm(student_res,pch=22,bg=1)
abline(0,1)

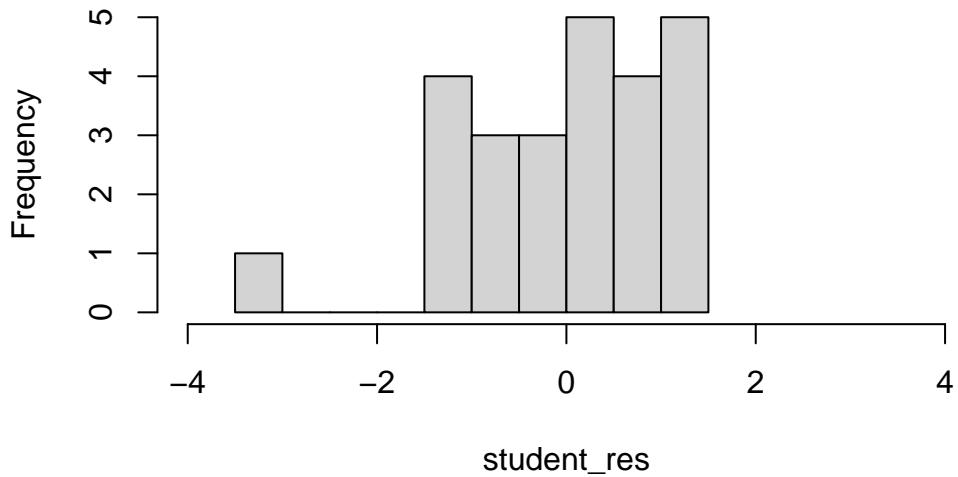
```

### Normal Q-Q Plot

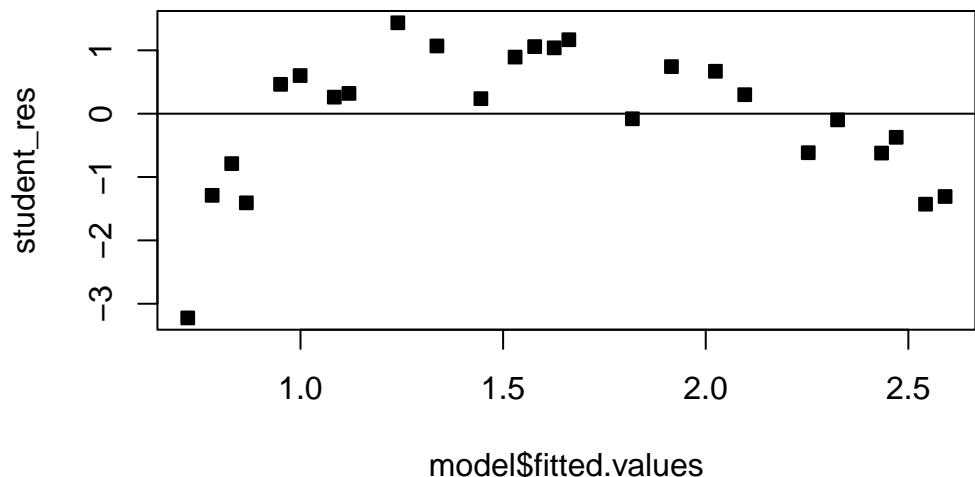


```
hist(student_res,breaks=10,xlim=c(-4,4))
```

### Histogram of student\_res

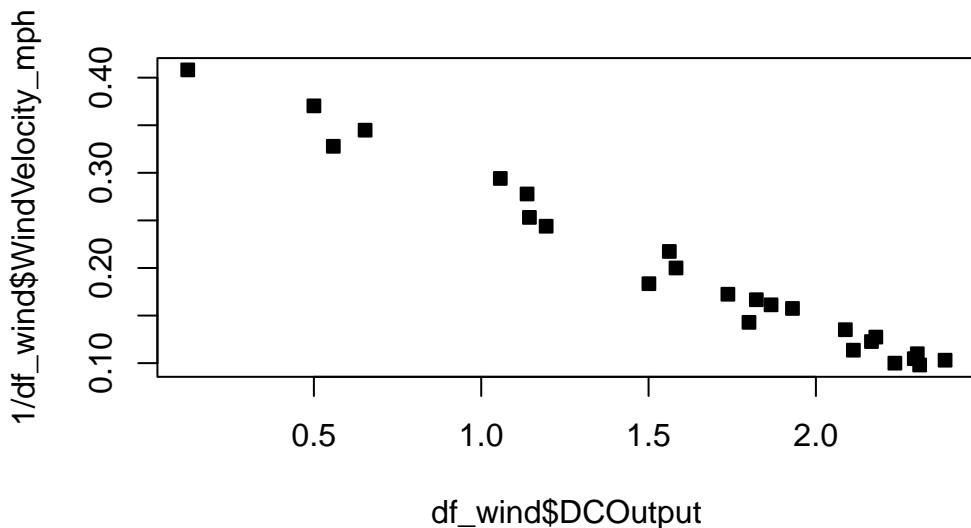


```
plot(model$fitted.values,student_res,pch=22,bg=1)
abline(h=0)
```



The fit is not good. Looking at the scatterplot, we might initially consider using a quadratic model to account for the pictured curvature. However, the scatterplot suggests that as wind speed increases, DC output approaches an upper limit of approximately 2.5. This is also consistent with the theory of windmill operation. Since the quadratic model will eventually bend downward as wind speed increases, it would not be appropriate for these data. A more reasonable model for the windmill data that incorporates an upper asymptote would be based on  $1/X$ .

```
plot(df_wind$DCOutput, 1/df_wind$WindVelocity_mph, pch=22, bg=1)
```



```
# plot(df$DCOutput, log(df$WindVelocity_mph))
df_wind$WindVelocity_mph_inv=1/df_wind$WindVelocity_mph
model2=lm(DCOutput~WindVelocity_mph_inv, df_wind)
model2
```

```
Call:
lm(formula = DCOutput ~ WindVelocity_mph_inv, data = df_wind)

Coefficients:
(Intercept)  WindVelocity_mph_inv
```

2.979 -6.935

```
summ=summary(model2); summ
```

Call:

```
lm(formula = DCOutput ~ WindVelocity_mph_inv, data = df_wind)
```

Residuals:

Min	1Q	Median	3Q	Max
-0.20547	-0.04940	0.01100	0.08352	0.12204

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	2.9789	0.0449	66.34	<2e-16 ***
WindVelocity_mph_inv	-6.9345	0.2064	-33.59	<2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

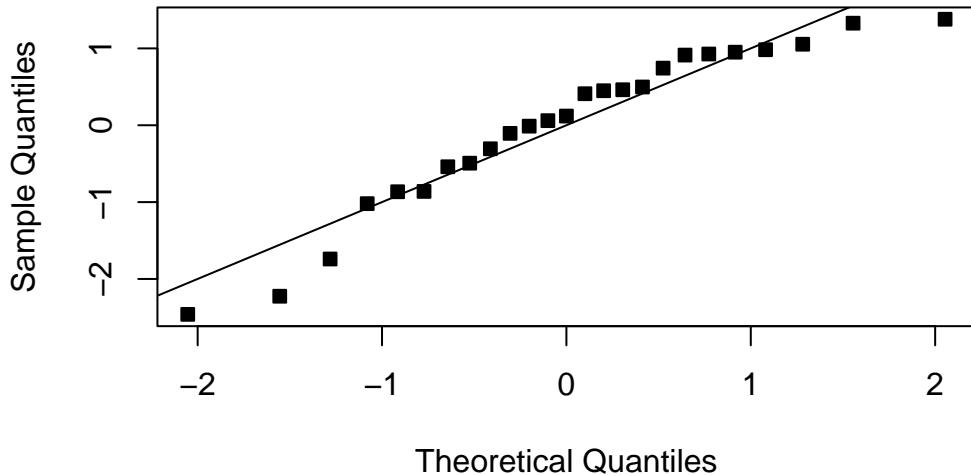
Residual standard error: 0.09417 on 23 degrees of freedom

Multiple R-squared: 0.98, Adjusted R-squared: 0.9792

F-statistic: 1128 on 1 and 23 DF, p-value: < 2.2e-16

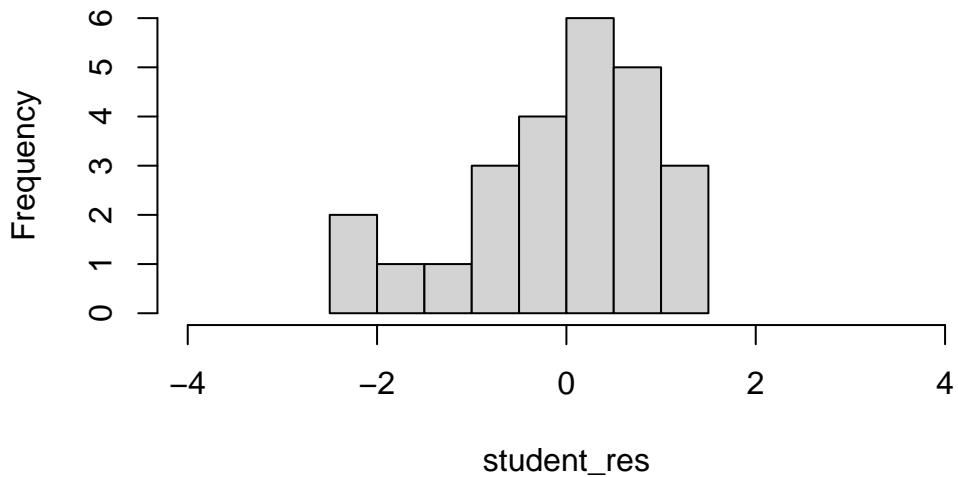
```
student_res=rstudent(model2)
MSE=summ$sigma^2
qqnorm(student_res,pch=22,bg=1)
abline(0,1)
```

### Normal Q-Q Plot

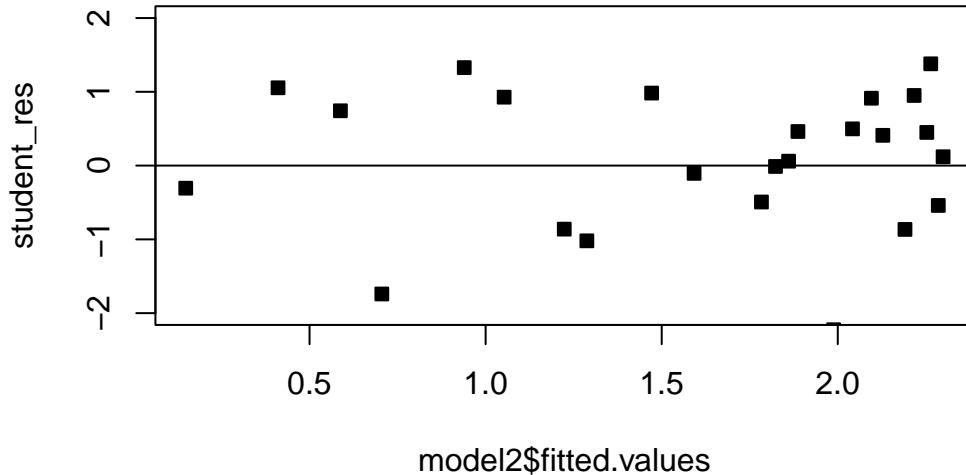


```
hist(student_res, xlim=c(-4, 4))
```

### Histogram of student\_res



```
plot(model2$fitted.values, student_res, pch=22, bg=1, ylim=c(-2,2))
abline(h=0)
```



### 5.3 Box Cox Transformations

One technique is to use the data to estimate which transformation is best, a popular instance is the Box-Cox transformation. Consider the class of transformations:  $\{y^\lambda : \lambda \in \mathbb{R}\}$ . The regression model and  $\lambda$  can be estimated simultaneously using the method of maximum likelihood. Recall that we used the method of least squares to estimate the model parameters - maximum likelihood is an alternative estimation strategy. Think of  $\lambda$  like an extra model parameter, on top of  $\beta$  and  $\sigma$  that we need to estimate.

Let

$$\tilde{y} = \log^{-1}(1/n \sum_{i=1}^n \log y_i)$$

$$y_\lambda = \begin{cases} \frac{y^\lambda - 1}{\lambda \tilde{y}^{\lambda-1}} & \lambda \neq 0 \\ \tilde{y} \log y & \lambda = 0 \end{cases}.$$

We then fit the following model

$$y_\lambda = X\beta + \epsilon.$$

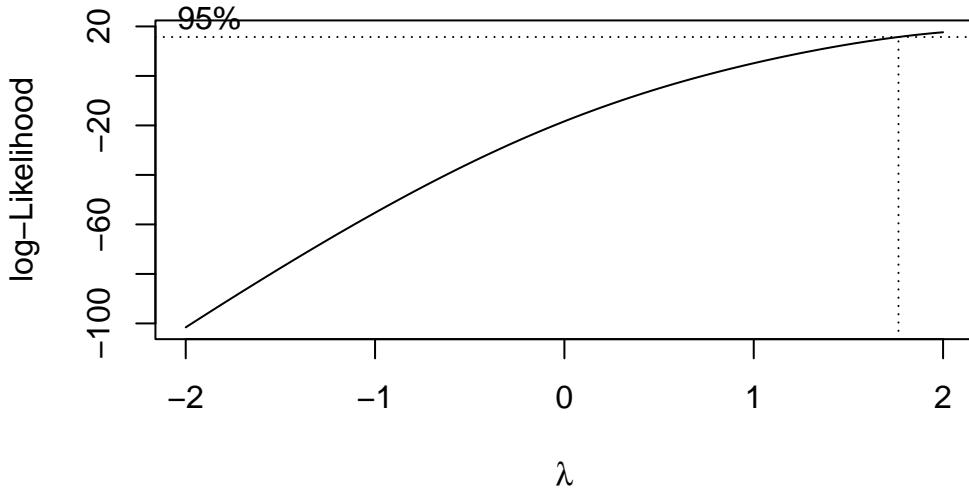
Even though  $y^\lambda \neq y_\lambda$ , we use  $y^\lambda$  (or  $\log y$  if  $\lambda = 0$ ) as the final response - as it is more interpretable. It is entirely acceptable to use  $y_\lambda$  as the response for the final model - this model will have a scale difference and an origin shift in comparison to the model using  $y^\lambda$  (or  $\log y$ ). Usually the final  $\lambda$  used in the model is rounded to a nice number for interpretation. A computational procedure is used for estimating  $\lambda$ , which we will not cover here. In general, we can compute a confidence interval for  $\lambda$ , and if it contains 1 then we may not need to transform.

**Example 5.4.** Let's apply the Box-Cox transformation to the two previous examples.

The R function `boxcox` from the `MASS` package can be used to execute the Box-Cox transformation. It requires you to specify a grid of points for  $\lambda$ , given below by `seq(-2, 2, 1/10)`. We can set the `plotit` parameter to `TRUE` in order to see if this grid is big enough. We should see a peak or mode in the log-likelihood function that is plotted. If we don't, we can expand the grid on the side which has the largest value of the log-likelihood. Observe below that we need to include points higher than 2 on the grid, as the function is still increasing for at  $\lambda = 2$ :

```
# You need the MASS package.
# install.packages('MASS')

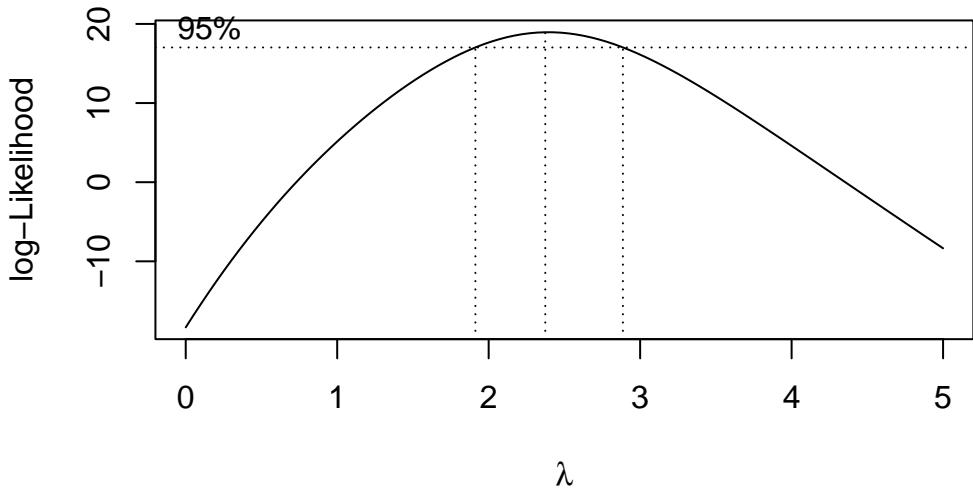
bc=MASS::boxcox(DCOutput~WindVelocity_mph,data=df_wind,
                 lambda = seq(-2, 2, 1/10),
                 plotit = TRUE,
                 eps = 1/50,
                 xlab = expression(lambda),
                 ylab = "log-Likelihood")
```



```
# bc

#Observe that

bc=MASS::boxcox(DCOutput~WindVelocity_mph,data=df_wind,
                  lambda = seq(0, 5, 1/10),
                  plotit = TRUE,
                  eps = 1/50,
                  xlab = expression(lambda),
                  ylab = "log-Likelihood")
```



```
# bc
#Seems like we should try lambda=2
```

The confidence interval goes from just below 2 to just below 3. Let's pick a round number, and try the transformation  $\lambda = 2$ .

```
# plot(df$DCOutput,log(df$WindVelocity_mph))
model3=lm(DCOutput^2~WindVelocity_mph, df_wind)
model3
```

```
Call:
lm(formula = DCOutput^2 ~ WindVelocity_mph, data = df_wind)

Coefficients:
(Intercept)  WindVelocity_mph
-1.3585          0.7107
```

```
summ3=summary(model3); summ3
```

```

Call:
lm(formula = DCOutput^2 ~ WindVelocity_mph, data = df_wind)

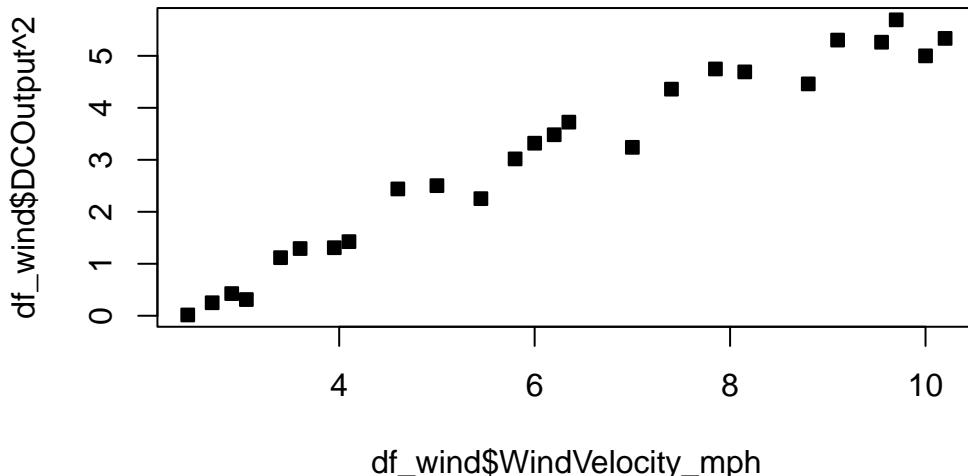
Residuals:
    Min      1Q  Median      3Q     Max 
-0.74840 -0.31027  0.05951  0.30793  0.57072 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -1.35851   0.21239 -6.396 1.58e-06 ***
WindVelocity_mph 0.71066   0.03211 22.130 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

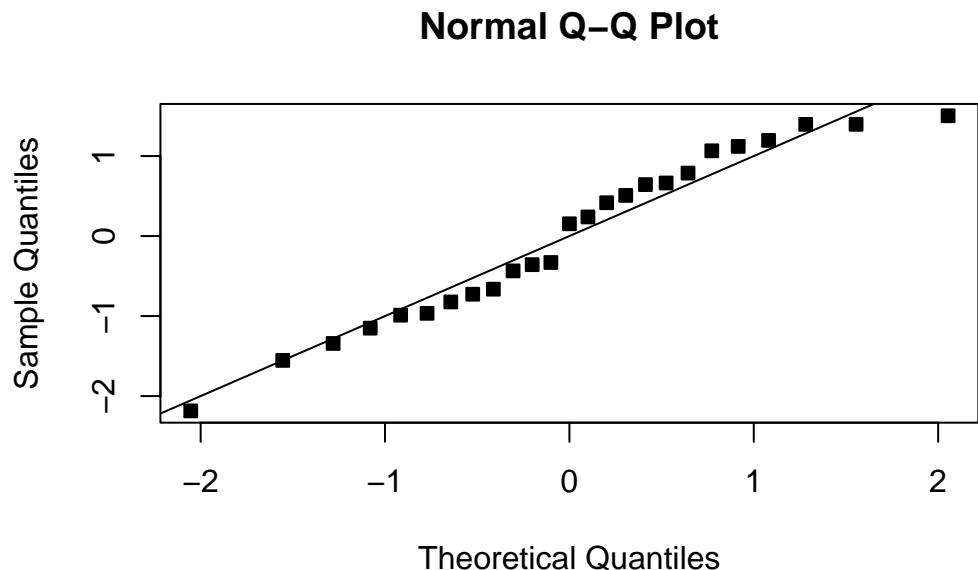
Residual standard error: 0.3979 on 23 degrees of freedom
Multiple R-squared:  0.9551,    Adjusted R-squared:  0.9532 
F-statistic: 489.7 on 1 and 23 DF,  p-value: < 2.2e-16

```

```
plot(df_wind$WindVelocity_mph,df_wind$DCOutput^2,pch=22, bg=1)
```

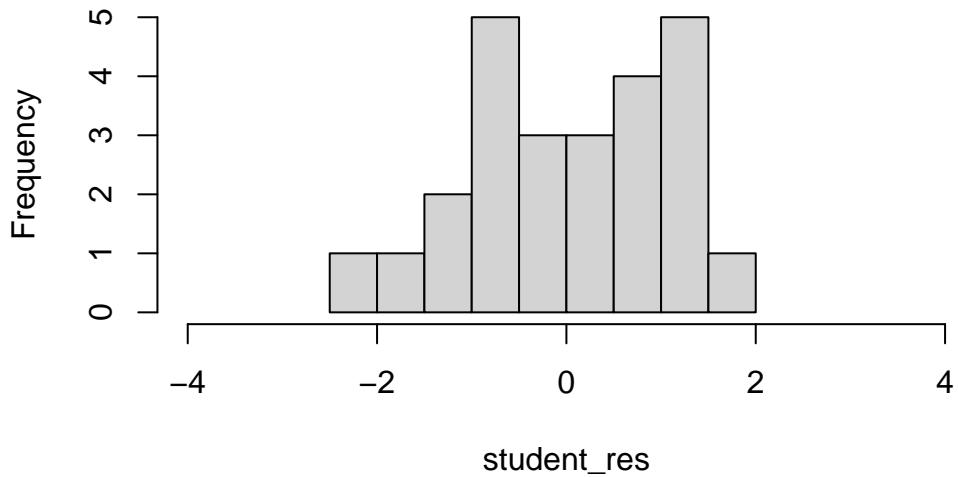


```
student_res=rstudent(model3)
MSE=summ3$sigma^2
qqnorm(student_res,pch=22,bg=1)
abline(0,1)
```

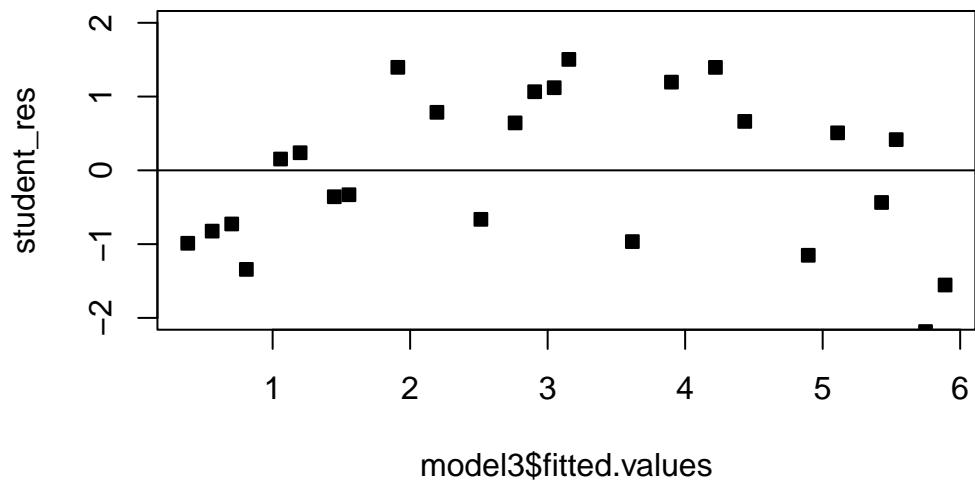


```
hist(student_res,xlim=c(-4,4))
```

### Histogram of student\_res



```
plot(model3$fitted.values,student_res,pch=22,bg=1,ylim=c(-2,2))
abline(h=0)
```



The fit is not bad. The  $R^2$  is very high. There is a pattern in the QQplot and a slight pattern in the residuals plot. For knowing nothing about wind velocity, it is not bad.

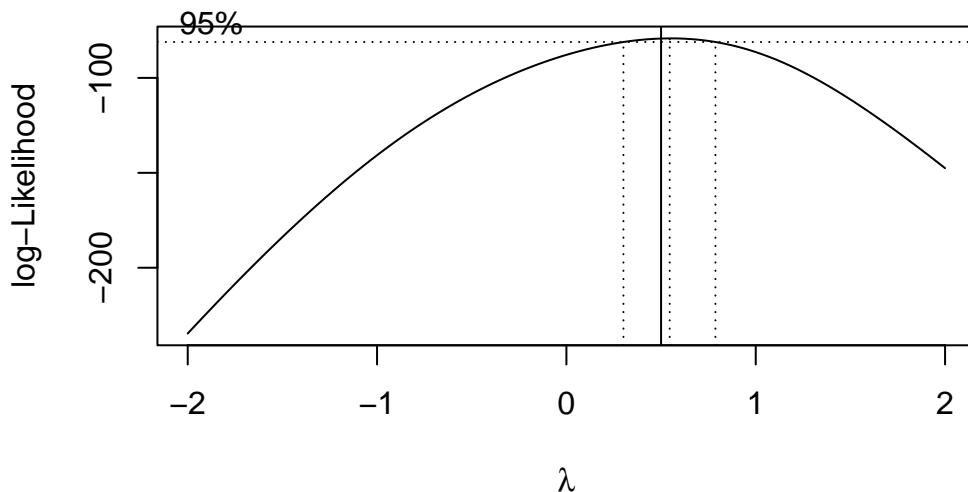
The electricity data clearly points to the square root transformation - matching the analysis we did previously.

```
## Electricity

model=lm(y_kW~x_kWh, df)

bc=MASS::boxcox(y_kW~x_kWh,data=df,
                  lambda = seq(-2, 2, 1/10),
                  plotit = TRUE,
                  eps = 1/50,
                  xlab = expression(lambda),
                  ylab = "log-Likelihood")

abline(v=0.5)
```



```
# bc
```

## **5.4 Homework stop**

Complete the assigned Chapter 5 questions and complete assignment 2.

# 6 Indicator Variables

Often we will have regressors that are categorical. We now discuss how to include those in a regression model. In general, categorical variables can be included in a regression model via **indicator variables**.

## 6.1 What are indicator variables?

If a regressor has two categories  $A$  and  $B$ , that regressor can be included in the model as

$$z = \begin{cases} 0 & \text{if the observation is type A} \\ 1 & \text{if the observation is type B} \end{cases}$$

Sometimes people choose

$$z = \begin{cases} -1 & \text{if the observation is type A} \\ 1 & \text{if the observation is type B} \end{cases}.$$

The variable  $z$  is an indicator variable. Indicator variables are in numeric form, and can therefore be included in the design matrix  $X$  in the usual way we do for continuous regressors.

**Example 6.1.** Let's recall Example 3.1 and suppose we have some new data as follows:

It is difficult to accurately determine a person's body fat percentage without immersing them in water. However, we can easily obtain the weight of a person. A researcher would like to know if weight and body fat percentage are related? They also suspect that sex plays a role in the prediction. This researcher collected the following data:

Individual	1	2	3	4	5	6	7	8	9	10
Weight (lb)	175	181	200	159	196	192	205	173	187	188
Body Fat (%)	6	21	15	6	22	31	32	21	25	30
Sex	F	M	F	F	M	F	F	M	M	F
Individual	11	12	13	14	15	16	17	18	19	20

Individual	1	2	3	4	5	6	7	8	9	10
Weight (lb)	188	240	175	168	246	160	215	159	146	219
Body Fat (%)	10	20	22	9	38	10	27	12	10	28
Sex	F	F	M	M	F	F	M	F	F	M

Write out the appropriate indicator variable for Sex. Interpret the resulting regression equation for regressing Body fat against weight and sex. Interpret the coefficient that corresponds to the Sex variable.

We have that

$$X_{2i} = \begin{cases} 0 & \text{if the subject } i \text{ is male} \\ 1 & \text{if the subject } i \text{ is female} \end{cases} .$$

The regression equation is then

$$Y_i|X = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \epsilon_i,$$

where  $X_{i1}$  is the weight of individual  $i$ .

When  $X_{i2} = 0$ , then the regression equation for males is given by  $Y_i|X = \beta_0 + \beta_1 X_{i1} + \epsilon_i$ . Therefore, the expected body fat percentage for males is  $E[Y_i|X] = \beta_0 + \beta_1 X_{i1}$ . Additionally, when  $X_{i2} = 1$ , then the regression equation for females is given by  $Y_i|X = \beta_0 + \beta_1 X_{i1} + \beta_2 + \epsilon_i$ . It follows that the expected body fat percentage for females is  $E[Y_i|X] = \beta_0 + \beta_1 X_{i1} + \beta_2$ . Thus, we have that the expected body fat percentage for females is  $\beta_2$  higher than for males, holding weight constant. This is the interpretation of the coefficient for the dummy variable in this case. Observe that for males and females, the regression lines are parallel. The model says that sex accounts for a constant shift in your expected body fat, but the slope (the coefficient for weight) of the regression line remains the same.

Let's observe.

```
# Make the data frame
Weight=c(175 , 181 , 200 , 159 , 196 , 192 , 205 , 173 , 187 , 188 ,
       188 , 240 , 175 , 168 , 246 , 160 , 215 , 159 , 146 , 219 )
BodyFat =c(6 , 21 , 15 , 6 , 22 , 31 , 32 , 21 , 25 , 30 ,
          10 , 20 , 22 , 9 , 38 , 10 , 27 , 12 , 10 , 28 )
Sex=c("F","M","F","F","M","F","M","F","F","M","F","M","F","M","F","M","F","M")

df=data.frame(Weight=Weight,BodyFat=BodyFat,Sex=Sex,stringsAsFactors = T)

df$Sex=relevel(df$Sex,"M")
```

```
mod=lm(BodyFat~Weight+Sex,data=df)
summary(mod)
```

Call:

```
lm(formula = BodyFat ~ Weight + Sex, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-11.2198	-5.3804	-0.1767	3.6719	11.7136

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-25.17526	11.73681	-2.145	0.046695 *
Weight	0.24861	0.06061	4.102	0.000743 ***
SexF	-3.27233	3.21493	-1.018	0.323014

---

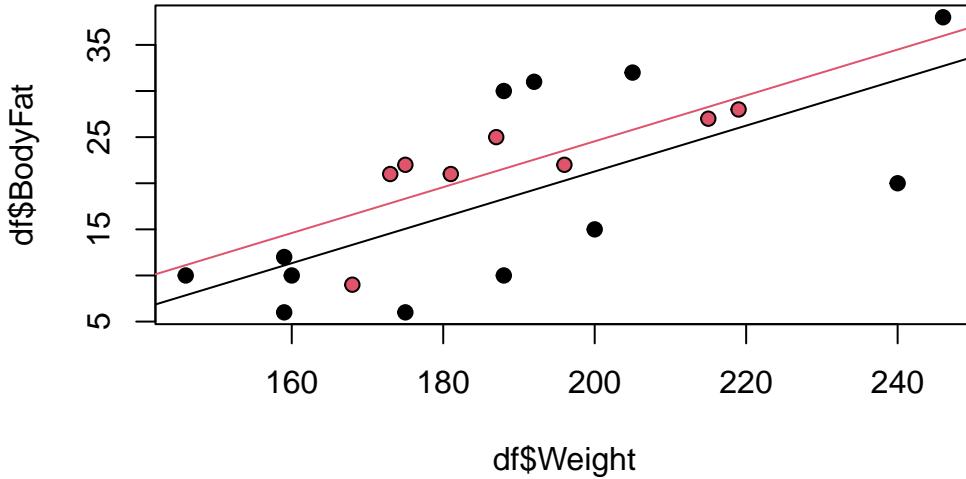
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 7.042 on 17 degrees of freedom

Multiple R-squared: 0.5149, Adjusted R-squared: 0.4578

F-statistic: 9.021 on 2 and 17 DF, p-value: 0.002137

```
plot(df$Weight,df$BodyFat,bg=((df$Sex=="M")+1),pch=21)
abline(coef(mod)[1],coef(mod)[2],col=2)
abline(coef(mod)[1]+coef(mod)[3],coef(mod)[2],col=1)
```



We can generalize this idea out of this example. In the case of two categories, the interpretation of the coefficient for the dummy variable is given as follows: Holding other regressors constant, on average, the change in response attributed to the case where the dummy variable is 1, relative to the case where the dummy variable is 0, is given by the coefficient for the dummy variable.

Moving on, a regressor that has  $k$  categories can be represented by  $k - 1$  indicator variables:

$x_1$	$x_2$	...	$x_{k-1}$	Category
0	0	...	0	1
1	0	...	0	2
0	1	...	0	3
⋮	⋮	...	⋮	⋮
0	0	...	1	$k$

In this case, the category, or level, where all dummy variables are equal to 0 is the **reference category**. The reference category is the baseline we will compare all other categories to. You may want to choose this carefully. In this case, the interpretation of each of the  $k - 1$  coefficients is going to be as follows: Holding other regressors constant, on average, the change in response attributed to the case where the dummy variable corresponding to the coefficient is 1, relative to the reference category, is given by the coefficient for the dummy variable. Note that the reference category has no variable associated with it.

**Example 6.2.** When evaluating factors that affect the price of real estate, we may wish to consider location, while adjusting for lot size, year built and finished square feet. The data set `clean_data.csv` contains the prices of various types of real estate, as well as several important regressors. Regress the sale price on location, lot size, year built and finished square feet. Interpret the coefficient related to District 14. According to the model, holding other variables constant, what district has the highest priced properties? the lowest? Observe that District 7 has a non significant coefficient. In this case, what does it mean for District 7 to have a coefficient of 0?

```
##### Packages needed ######
```

```
library(lubridate)
```

```
Warning: package 'lubridate' was built under R version 4.2.3
```

```
Attaching package: 'lubridate'
```

```
The following objects are masked from 'package:base':
```

```
date, intersect, setdiff, union
```

```
# Example: We would like to see how sale price of a home is related to  
# various factors
```

```
##### Loading data #####
```

```
df_clean2=read.csv('clean_data.csv',stringsAsFactors = T)  
df_clean2$District=as.factor(df_clean2$District)
```

```
# The first level is the reference category  
attributes(df_clean2$District)$levels[1]
```

```
[1] "1"
```

```
##### Fitting the model #####
```

```
model=lm(Sale_price~District+Fin_sqft+Lotsize+Year_Built,df_clean2)
```

```
summ=summary(model); summ
```

```

Call:
lm(formula = Sale_price ~ District + Fin_sqft + Lotsize + Year_Built,
    data = df_clean2)

Residuals:
    Min      1Q  Median      3Q     Max 
-399923 -25360      426    23383 1580056 

Coefficients:
            Estimate Std. Error t value Pr(>|t|)    
(Intercept) -9.170e+05  4.175e+04 -21.963 < 2e-16 ***
District2    1.335e+04  2.312e+03   5.772 7.92e-09 ***
District3    1.815e+05  2.462e+03  73.723 < 2e-16 ***
District4   -3.525e+04  4.777e+03  -7.378 1.66e-13 ***
District5    5.552e+04  1.988e+03  27.923 < 2e-16 ***
District6    1.202e+04  2.849e+03   4.218 2.47e-05 ***
District7   -4.300e+03  2.482e+03  -1.732  0.08327 .  
District8    1.732e+04  2.708e+03   6.396 1.62e-10 ***
District9    2.810e+04  2.474e+03  11.361 < 2e-16 ***
District10   6.363e+04  2.073e+03  30.699 < 2e-16 ***
District11   7.032e+04  1.990e+03  35.333 < 2e-16 ***
District12   1.014e+04  3.240e+03   3.129  0.00175 ** 
District13   6.877e+04  2.057e+03  33.430 < 2e-16 ***
District14   1.026e+05  2.086e+03  49.212 < 2e-16 ***
District15   -3.375e+04  3.050e+03 -11.066 < 2e-16 ***
Fin_sqft     6.519e+01  6.525e-01  99.899 < 2e-16 ***
Lotsize      3.906e+00  1.228e-01  31.812 < 2e-16 ***
Year_Built   4.506e+02  2.153e+01  20.930 < 2e-16 ***

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 55680 on 24604 degrees of freedom
Multiple R-squared:  0.5889,    Adjusted R-squared:  0.5886 
F-statistic:  2073 on 17 and 24604 DF,  p-value: < 2.2e-16

```

```
coef(model)[which.max(coef(model))]
```

```

District3
181495.9

```

```
coef(model)[order(coef(model))[1:3]]
```

(Intercept)	District4	District15
-916960.88	-35245.83	-33748.17

1. Interpret the coefficient for District 14: Holding lot size, finished square feet and year built constant, on average, the change in the price of a property in District 14, relative to District 1, is 102 600.
2. According to the model, holding other variables constant, what district has the highest priced properties on average? the lowest? The highest coefficient is District 3, and it is positive, so, holding other variables constant, on average District 3 has the highest priced properties. The lowest coefficient is District 4, and it is negative, so, holding other variables constant, on average District 4 has the lowest priced properties.
3. Observe that District 7 has a non significant coefficient. In this case, what does it mean for District 7 to have a coefficient of 0? This means that there is not enough evidence to show that District 1 and District 7 have different prices, holding other variables constant, on average.

**i** Note

If all coefficients for the dummy variables are positive, then the reference category has the lowest average value of the response. Analogously, if all coefficients for the dummy variables are negative, then the reference category has the lowest average value of the response. Why? Use the interpretation of the coefficients to answer this question.

**i** Note

ANOVA is Regression!- In one-way ANOVA, recall that we test for a difference in group means for a continuous response. We can represent the treatment groups with dummy variables and view this as a regression problem. That is, regressing the outcome on the dummy variables. It turns out that the regression ANOVA, that is, the overall  $F$ -test, applied to these dummy variables is equivalent to the one-way ANOVA (see Section 8.3 of the textbook.)

## 6.2 Interaction effects

An interaction effect occurs when the effect of one regressor on the response depends on the value of another regressor. In other words, the combined effect of two variables is not simply additive; the value of one variable modifies the impact of the other. In linear regression, this means that the coefficient of one regressor depends on the other.

We now give a simple example:

Suppose we are studying the effect of hours studied ( $X_1$ ) and attendance ( $X_2$ ) on exam scores ( $Y$ ). An interaction effect between  $X_1$  and  $X_2$  would imply that the effect of studying on exam scores is different depending on the level of attendance. This can be modeled by including an interaction term ( $X_1 \times X_2$ ) in the regression equation:

$$Y_i = \beta_0 + \beta_1 X_{1i} + \beta_2 X_{2i} + \beta_3 (X_{1i} \times X_{2i}) + \epsilon_i.$$

The coefficient ( $\beta_3$ ) represents the interaction effect between  $X_1$  and  $X_2$ . For instance, if  $\beta_3 > 0$ , then the more the student has attended the course, the more beneficial the student's hours studied will be.

Some examples of how interaction effects are applied in real life are given by:

- **Psychology:** Studying how different treatments and demographic factors interact to influence behavior.
- **Marketing:** Analyzing how different marketing strategies and customer demographics interact to affect sales.
- **Medicine:** Investigating how different drugs and patient characteristics interact to affect health outcomes.

**Example 6.3.** Let's recall Example 6.1 and suppose the researcher would like you to include the interaction effect between Weight and Sex. Explain how the regression line changes with a non-zero interaction effect. Interpret the estimated interaction effect. Is it significant?

The regression equation is

$$Y_i|X = \beta_0 + \beta_1 X_{i1} + \beta_2 X_{i2} + \beta_3 X_{i1} X_{i2} + \epsilon_i.$$

If  $\beta_3 \neq 0$  then we proceed as follows. When  $X_{i2} = 0$ , then the regression equation for males is still given by  $Y_i|X = \beta_0 + \beta_1 X_{i1} + \epsilon_i$ . Therefore, the expected body fat percentage for males is  $E[Y_i|X] = \beta_0 + \beta_1 X_{i1}$ . Additionally, when  $X_{i2} = 1$ , then the regression equation for females is given by

$$Y_i|X = \beta_0 + \beta_1 X_{i1} + \beta_2 + \beta_3 X_{i1} + \epsilon_i = \beta_0 + (\beta_1 + \beta_3) X_{i1} + \beta_2 + \epsilon_i.$$

It follows that the expected body fat percentage for females is  $E[Y_i|X] = \beta_0 + (\beta_1 + \beta_3) X_{i1} + \beta_2$ . Thus, adding an interaction effect allows the model to generate a completely different regression line, that is a different slope **and** intercept for females. The expected body fat percentage for females is then  $\beta_2 + \beta_3 X_{i1}$  higher than for males, holding weight constant. Adding an interaction effect allows the slope to also vary, depending on whether the subject is male or female.

Let's observe.

```

# Make the data frame
Weight=c(175 , 181 , 200 , 159 , 196 , 192 , 205 , 173 , 187 , 188 ,
       188 , 240 , 175 , 168 , 246 , 160 , 215 , 159 , 146 , 219 )
BodyFat =c(6 , 21 , 15 , 6 , 22 , 31 , 32 , 21 , 25 , 30 ,
          10 , 20 , 22 , 9 , 38 , 10 , 27 , 12 , 10 , 28 )
Sex=c("F","M","F","F","M","F","M","M","F","F","F","M","M","F","F","M","F","F","M")

df=data.frame(Weight=Weight,BodyFat=BodyFat,Sex=Sex,stringsAsFactors = T)

df$Sex=relevel(df$Sex,"M")

mod=lm(BodyFat~Weight+Sex+Weight*Sex,data=df)
summary(mod)

```

Call:

```
lm(formula = BodyFat ~ Weight + Sex + Weight * Sex, data = df)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-11.4171	-5.3084	0.1178	3.4912	11.7087

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-22.13450	27.12486	-0.816	0.426
Weight	0.23255	0.14269	1.630	0.123
SexF	-7.02921	30.18090	-0.233	0.819
Weight:SexF	0.01987	0.15869	0.125	0.902

Residual standard error: 7.255 on 16 degrees of freedom

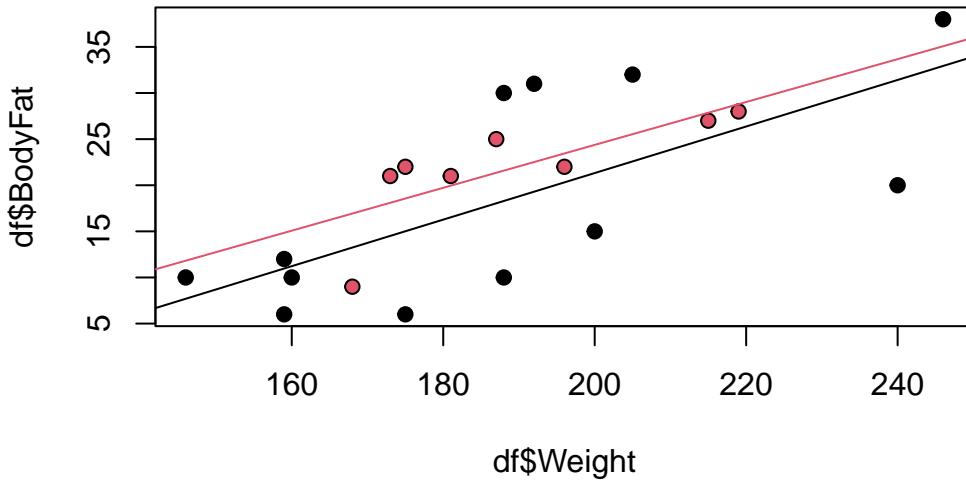
Multiple R-squared: 0.5153, Adjusted R-squared: 0.4245

F-statistic: 5.671 on 3 and 16 DF, p-value: 0.007662

```

plot(df$Weight,df$BodyFat,bg=((df$Sex=="M")+1),pch=21)
abline(coef(mod)[1],coef(mod)[2],col=2)
abline(coef(mod)[1]+coef(mod)[3],coef(mod)[2]+coef(mod)[4],col=1)

```



Notice how the slopes of the regression lines differ! Now, the estimated interaction effect is 0.01987. Let's interpret it. We have that, on average, for every one lb increase in weight, the body fat percentage of a female increases by 0.01987 more than that of a male.

(In this case, the term is not significant, so we would probably drop it.)

#### i Note

We can include interaction effects in the regression model in R by adding `variable_1*variable_2` to the right-hand side of the formula equation.

**Example 6.4.** When evaluating factors that affect the price of real estate, we may wish to consider location, while adjusting for lot size, year built and finished square feet. The data set `clean_data.csv` contains the prices of various types of real estate, as well as several important regressors. Regress the sale price on location, lot size, year built and finished square feet. Add an interaction term between year built and location. Interpret the interaction term for District 14.

```
##### Fitting the model #####
model=lm(Sale_price~District+Fin_sqft+Lotsize+Year_Built+Year_Built*District,df_clean2)

summ=summary(model); summ
```

Call:

```
lm(formula = Sale_price ~ District + Fin_sqft + Lotsize + Year_Built +  
    Year_Built * District, data = df_clean2)
```

Residuals:

Min	1Q	Median	3Q	Max
-400250	-24589	441	23005	1569420

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1.567e+06	2.215e+05	-7.077	1.52e-12 ***
District2	9.848e+05	3.594e+05	2.740	0.006148 **
District3	-2.929e+05	2.723e+05	-1.076	0.282044
District4	6.838e+05	3.573e+05	1.914	0.055676 .
District5	1.551e+06	2.634e+05	5.888	3.97e-09 ***
District6	5.445e+05	2.683e+05	2.029	0.042446 *
District7	-7.242e+05	3.234e+05	-2.239	0.025139 *
District8	8.463e+05	3.000e+05	2.821	0.004790 **
District9	-5.339e+04	3.041e+05	-0.176	0.860634
District10	8.690e+05	2.602e+05	3.339	0.000842 ***
District11	1.899e+05	2.660e+05	0.714	0.475313
District12	1.282e+06	2.994e+05	4.283	1.85e-05 ***
District13	6.296e+05	2.557e+05	2.463	0.013799 *
District14	1.502e+06	2.392e+05	6.278	3.49e-10 ***
District15	5.815e+04	2.610e+05	0.223	0.823727
Fin_sqft	6.497e+01	6.659e-01	97.556	< 2e-16 ***
Lotsize	3.989e+00	1.237e-01	32.256	< 2e-16 ***
Year_Built	7.850e+02	1.139e+02	6.891	5.68e-12 ***
District2:Year_Built	-4.986e+02	1.841e+02	-2.708	0.006770 **
District3:Year_Built	2.547e+02	1.409e+02	1.807	0.070772 .
District4:Year_Built	-3.703e+02	1.858e+02	-1.993	0.046287 *
District5:Year_Built	-7.666e+02	1.352e+02	-5.668	1.46e-08 ***
District6:Year_Built	-2.727e+02	1.388e+02	-1.965	0.049443 *
District7:Year_Built	3.734e+02	1.667e+02	2.240	0.025118 *
District8:Year_Built	-4.278e+02	1.555e+02	-2.751	0.005938 **
District9:Year_Built	3.721e+01	1.555e+02	0.239	0.810891
District10:Year_Built	-4.146e+02	1.340e+02	-3.093	0.001985 **
District11:Year_Built	-6.285e+01	1.366e+02	-0.460	0.645462
District12:Year_Built	-6.608e+02	1.555e+02	-4.251	2.14e-05 ***
District13:Year_Built	-2.887e+02	1.314e+02	-2.198	0.027981 *
District14:Year_Built	-7.231e+02	1.232e+02	-5.869	4.43e-09 ***
District15:Year_Built	-4.403e+01	1.347e+02	-0.327	0.743706

```

---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 55410 on 24590 degrees of freedom
Multiple R-squared: 0.5931, Adjusted R-squared: 0.5925
F-statistic: 1156 on 31 and 24590 DF, p-value: < 2.2e-16

```

Observe that the interaction term between year built and District 14 is -723.1\$. In addition, note that year built has a positive coefficient of 785\$. We can interpret the interaction effect as follows: Holding finished square feet and lot size constant, a one year increase in year built for a home in District 14 results in an increase in price that is 723.1 lower than that of District 1. We can also reword this to make it a little more clear - Holding finished square feet and lot size constant, a one year increase in year built for a home in District 1 results in an increase in price that is 723.1 higher than that of District 1.

To see this observe that for a one unit increase in year built in District 14, we have that the price goes up by  $785.0 - 723.1 = 61.9$  on average, holding other variables constant. On the other hand, in District 1, the price goes up by 785.0 on average, holding other variables constant. Therefore, in general, newer homes are much more valuable in District 1.

**Exercise 6.1.** Interpret the main effects and the interaction effect with year built for Districts 2-4. (The main effects are the coefficients for Districts 2-4.)

 Warning

The interpretation for interaction effects is difficult and nuanced. Make sure you study this topic carefully.

### 6.3 Increasing codes and quantitative regressors via dummy variables

Another approach to the treatment of a qualitative variable in regression is to measure the levels of the variable by an allocated code. Suppose we model the effect of the number of bedrooms on real estate price by its numerical value, instead of categorical value. Let's see what happens to the regression equation. In general, ordinal variables may be better represented by dummy variables/indicators - however, dummy variables increase the complexity of the model, which we may not have enough data to support, and could lead to overfitting.

**Example 6.5.** When evaluating factors that affect the price of real estate, we may wish to consider the unadjusted effect of the number of bedrooms. Regress the sale price on number of

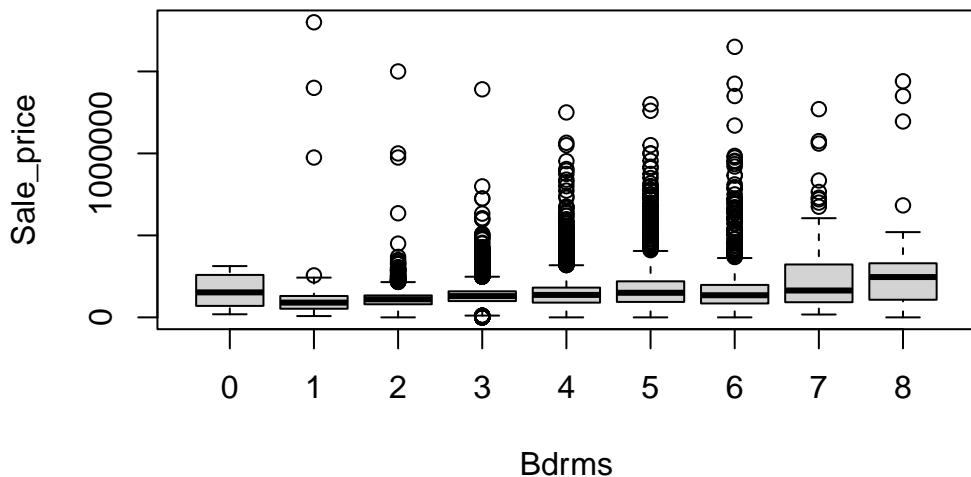
bedrooms treating number of bedrooms as a continuous variable. Then, regress the sale price on number of bedrooms treating number of bedrooms as a categorical variable. Compare and contrast the two models, and the resulting fits.

```
##### Fitting the model #####
unique(df_clean2$Bdrms)

[1] >8 2 0 4 7 3 1 6 8 5
Levels: >8 0 1 2 3 4 5 6 7 8

# Drop these rows
df_clean3=df_clean2[df_clean2$Bdrms != '>8',]
df_clean3$Bdrms=droplevels(df_clean3$Bdrms)
df_clean3$Bdrms=relevel(df_clean3$Bdrms, "0")
# Add new continuous variable
df_clean3$Bdrms2=as.numeric(df_clean3$Bdrms)-1

boxplot(Sale_price~Bdrms, df_clean3)
```



```
model_ca=lm(Sale_price~Bdrms,df_clean3)
model_co=lm(Sale_price~Bdrms2,df_clean3)
```

```
summ=summary(model_ca); summ
```

Call:

```
lm(formula = Sale_price ~ Bdrms, data = df_clean3)
```

Residuals:

Min	1Q	Median	3Q	Max
-271312	-43342	-6342	26658	1672084

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	161825	29764	5.437	5.47e-08 ***
Bdrms1	-33909	30818	-1.100	0.271216
Bdrms2	-53113	29800	-1.782	0.074712 .
Bdrms3	-28483	29774	-0.957	0.338758
Bdrms4	-15157	29785	-0.509	0.610830
Bdrms5	24156	29852	0.809	0.418414
Bdrms6	6826	29861	0.229	0.819189
Bdrms7	81735	30717	2.661	0.007798 **
Bdrms8	109487	31332	3.494	0.000476 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 84190 on 24586 degrees of freedom

Multiple R-squared: 0.05675, Adjusted R-squared: 0.05644

F-statistic: 184.9 on 8 and 24586 DF, p-value: < 2.2e-16

```
summ=summary(model_co); summ
```

Call:

```
lm(formula = Sale_price ~ Bdrms2, data = df_clean3)
```

Residuals:

Min	1Q	Median	3Q	Max
-224144	-43153	-6651	26849	1705343

```

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) 76159.0     1849.3    41.18 <2e-16 ***
Bdrms2       18498.1      522.4    35.41 <2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 84540 on 24593 degrees of freedom
Multiple R-squared:  0.04851,   Adjusted R-squared:  0.04847
F-statistic:  1254 on 1 and 24593 DF,  p-value: < 2.2e-16

```

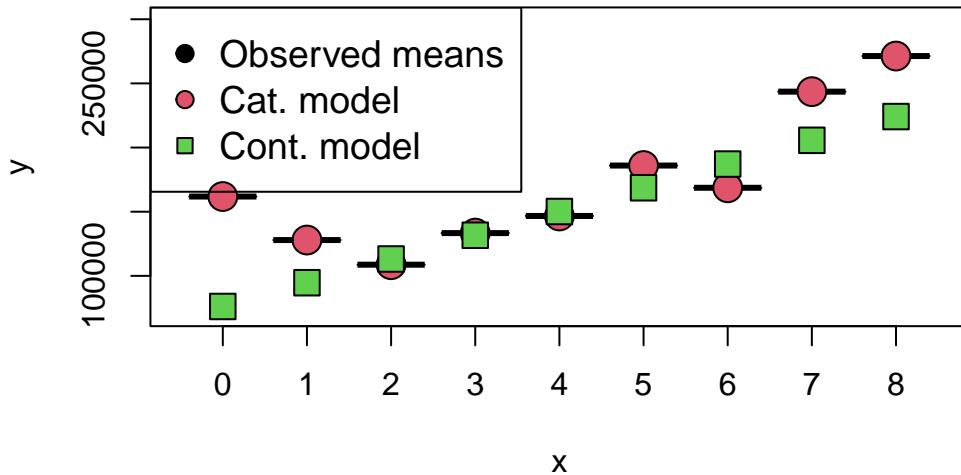
Observe that the continuous model says that for every additional bedroom, on average the price increases by 18 498\$. On the other hand, the categorical model says that the change in price depends on the number of bedrooms. For example, going from 0 bedrooms to 1 bedroom, we actually see a reduction in price of -33 909\$. Let's graph the expected price for each number of bedrooms from both models:

```

##### Fitting the model #####
new_dat=data.frame('Bdrms'=sort(unique(df_clean3$Bdrms)))
new_dat2=data.frame('Bdrms2'=0:8)
# predict(model_ca,new_dat)
# predict(model_co,new_dat2)

observed_means=aggregate(Sale_price~Bdrms,data=df_clean3, FUN = "mean")
plot(observed_means[,1],observed_means[,2],pch=25,bg=1,cex=3,ylim=c( 70000,300000))
points(x=observed_means[,1],predict(model_ca,new_dat),pch=21,bg=2,cex=2)
points(x=observed_means[,1],predict(model_co,new_dat2),pch=22,bg=3,cex=2)
legend("topleft",legend=c("Observed means","Cat. model","Cont. model"),pch=c(21,21,22),pt.

```



Observe that the continuous model does not match the data at all, while the categorical model is able to model the **non-linear** relationship between the number of bedrooms and the sale price! Why is this the case? Treating a regressor as continuous implies that there is a linear relationship between that regressor and the response. On the other hand, modelling the variable with indicators does not place any assumption on the relationship between the regressor and the response. The drawback, is that we need 7 more parameters in the model.

### ⚠ Warning

When deciding to treat continuous or ordinal variables as continuous, it is critical that you evaluate whether it is acceptable to assume a linear relationship between the regression and the response. If you cannot verify this assumption, or it seems invalid, it is best to treat the regressor as categorical.

Quantitative regressors can also be represented by indicator variables. Sometimes this is necessary because it is difficult to collect accurate information on the quantitative regressor, or the exact values are obscured for privacy reasons. Treating a quantitative factor as a qualitative one increases the complexity of the model. This approach also reduces the degrees of freedom for error. However, the indicator variable approach does not require the analyst to make any prior assumptions about the functional form of the relationship between the response and the regressor variable, as previously discussed.

## 6.4 A larger scale example

It is a good time to stop introducing new material and do a larger scale example.

**Example 6.6.** Explore the pricing data, and evaluate what factors influence the price of a property. Be sure to assess the fit of the model and check assumptions.

```
##### Packages needed #####
library(lubridate)

# Example: We would like to see how sale price of a home is related to
# various factors

##### Loading data #####
df_clean2=read.csv('clean_data.csv',stringsAsFactors = T)

##### Analyzing the data via EDA #####
names(df_clean2)

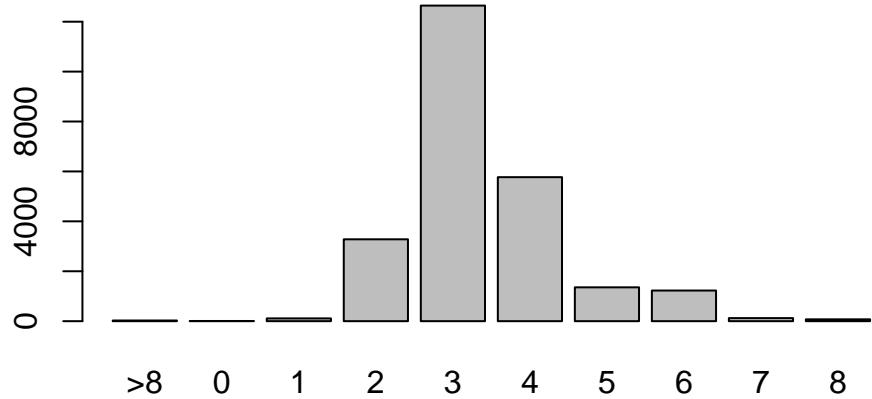
[1] "District"    "Extwall"      "Stories"       "Year_Built"   "Fin_sqft"
[6] "Units"        "Bdrms"        "Fbath"        "Lotsize"     "Sale_date"
[11] "Sale_price"

head(df_clean2)

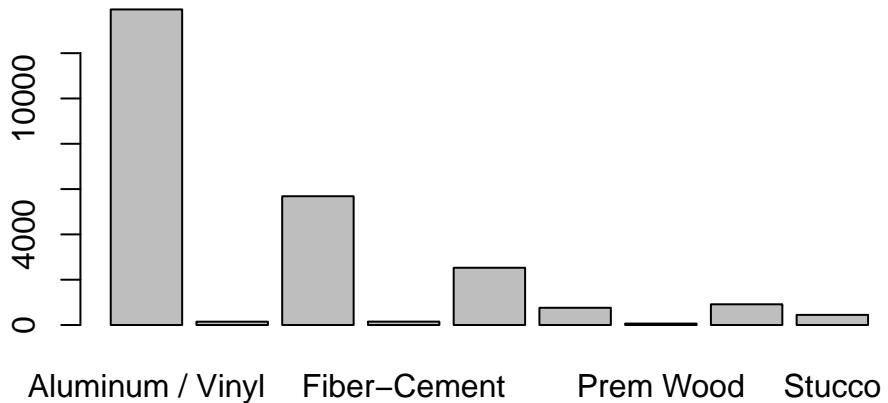
  District Extwall Stories Year_Built Fin_sqft Units Bdrms Fbath Lotsize
1         7   Frame       2      1913     3476    >3    >8      1    5040
2         3   Frame       2      1897     1992    >3      2      2    2880
3         4   Frame       2      1907     2339    >3      0      1    3185
4         4   Frame       2      1890     2329    >3      4      1    5781
5         4   Stone      >2      1891     7450      2      7    >4   15600
6        12   Frame      1.5     1906     2462      2      3      2    5075
  Sale_date Sale_price
1     11719      42000
2     11808     145000
3     11839      30000
4     11961      66500
```

```
5      11992      150500
6      11992      75000
```

```
barplot(table(df_clean2$Bdrms))
```



```
barplot(table(df_clean2$Extwall))
barplot(table(df_clean2$Extwall))
```



```
dim(df_clean2)
```

```
[1] 24622      11
```

```
##### Fitting the model #####
model=lm(Sale_price~.,df_clean2)
```

```
summ=summary(model); summ
```

Call:

```
lm(formula = Sale_price ~ ., data = df_clean2)
```

Residuals:

Min	1Q	Median	3Q	Max
-638318	-30032	1735	29252	1621794

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-3.674e+05	4.580e+04	-8.023	1.08e-15 ***

District	1.854e+03	9.619e+01	19.271	< 2e-16	***
ExtwallBlock	4.751e+03	5.104e+03	0.931	0.3520	
ExtwallBrick	7.562e+03	1.011e+03	7.480	7.67e-14	***
ExtwallFiber-Cement	1.096e+04	5.220e+03	2.101	0.0357	*
ExtwallFrame	-6.693e+03	1.357e+03	-4.934	8.13e-07	***
ExtwallMasonry / Frame	1.391e+02	2.385e+03	0.058	0.9535	
ExtwallPrem Wood	-1.128e+03	7.818e+03	-0.144	0.8853	
ExtwallStone	1.679e+02	2.136e+03	0.079	0.9374	
ExtwallStucco	1.389e+04	2.990e+03	4.646	3.40e-06	***
Stories1	7.364e+04	1.436e+04	5.127	2.96e-07	***
Stories1.5	8.066e+04	1.434e+04	5.624	1.89e-08	***
Stories2	8.842e+04	1.429e+04	6.188	6.17e-10	***
Year_Built	1.244e+01	1.973e+01	0.631	0.5283	
Fin_sqft	1.000e+02	1.313e+00	76.166	< 2e-16	***
Units1	1.335e+05	1.014e+04	13.169	< 2e-16	***
Units2	4.277e+04	1.014e+04	4.219	2.47e-05	***
Units3	-1.593e+04	1.092e+04	-1.458	0.1447	
Bdrms0	1.731e+05	2.578e+04	6.714	1.93e-11	***
Bdrms1	2.070e+05	1.385e+04	14.948	< 2e-16	***
Bdrms2	1.647e+05	1.259e+04	13.082	< 2e-16	***
Bdrms3	1.575e+05	1.251e+04	12.588	< 2e-16	***
Bdrms4	1.397e+05	1.246e+04	11.208	< 2e-16	***
Bdrms5	1.357e+05	1.246e+04	10.890	< 2e-16	***
Bdrms6	1.166e+05	1.248e+04	9.341	< 2e-16	***
Bdrms7	8.164e+04	1.331e+04	6.133	8.75e-10	***
Bdrms8	1.006e+05	1.398e+04	7.195	6.43e-13	***
Fbath0	-1.564e+05	1.841e+04	-8.494	< 2e-16	***
Fbath1	-1.346e+05	1.327e+04	-10.142	< 2e-16	***
Fbath2	-1.191e+05	1.318e+04	-9.031	< 2e-16	***
Fbath3	-6.609e+04	1.310e+04	-5.045	4.57e-07	***
Fbath4	5.041e+03	1.405e+04	0.359	0.7197	
Lotsize	1.947e+00	1.349e-01	14.429	< 2e-16	***
Sale_date	5.089e+00	3.635e-01	13.999	< 2e-16	***
---					
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1					

Residual standard error: 61440 on 24588 degrees of freedom

Multiple R-squared: 0.4997, Adjusted R-squared: 0.499

F-statistic: 744.1 on 33 and 24588 DF, p-value: < 2.2e-16

```
##### Now, let's interpret the output #####
summ$r.squared
```

```
[1] 0.4996725
```

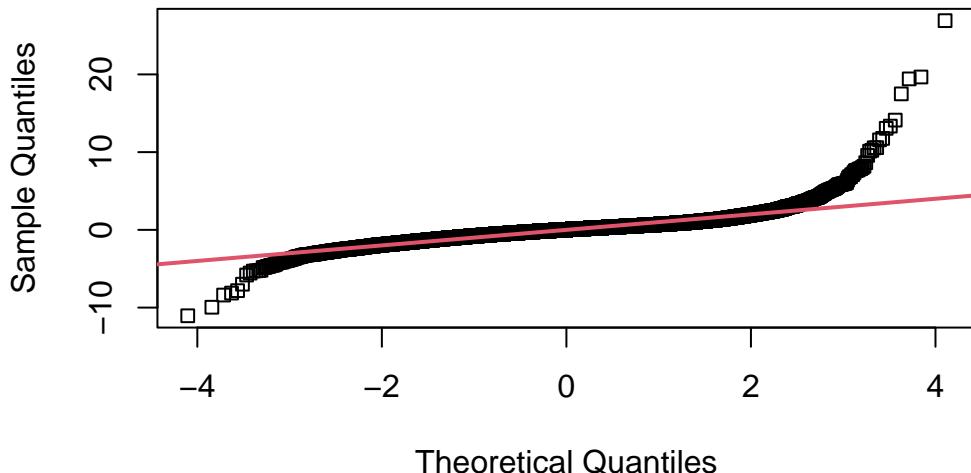
```
summ$adj.r.squared
```

```
[1] 0.499001
```

```
##### Residual analysis #####
student_res=rstudent(model)
MSE=summ$sigma^2
```

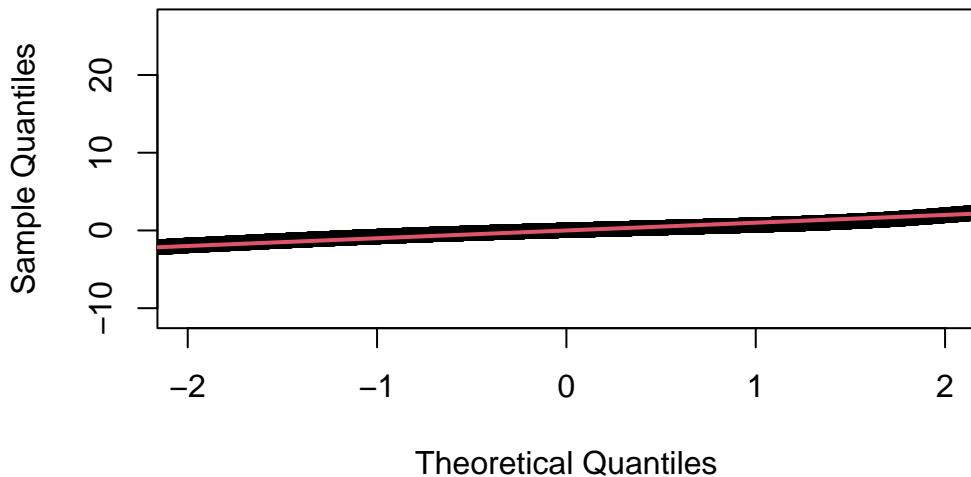
```
qqnorm(student_res,pch=22)
abline(0,1,col=2,lwd=2)
```

### Normal Q-Q Plot



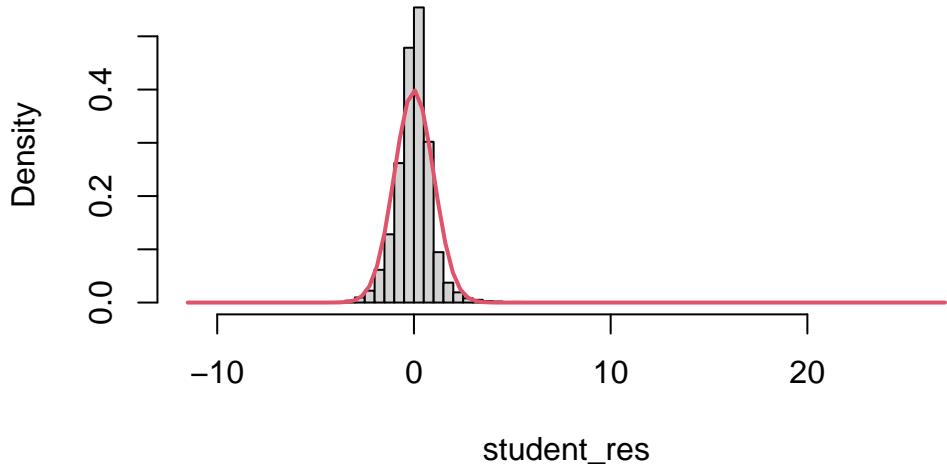
```
qqnorm(student_res,pch=22,xlim=c(-2,2))
abline(0,1,col=2,lwd=2)
```

### Normal Q-Q Plot

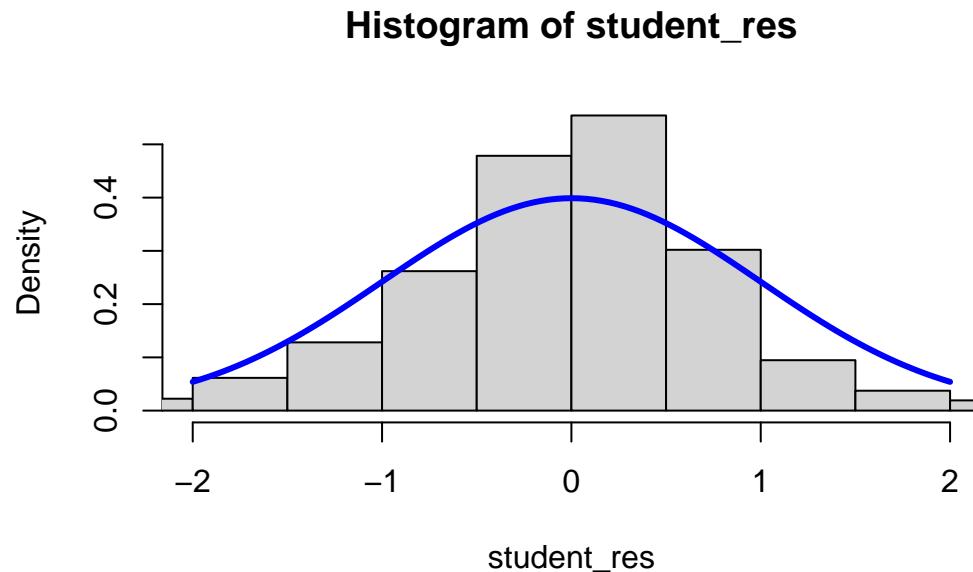


```
hist(student_res,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T,col=2,lwd=2)
```

### Histogram of student\_res

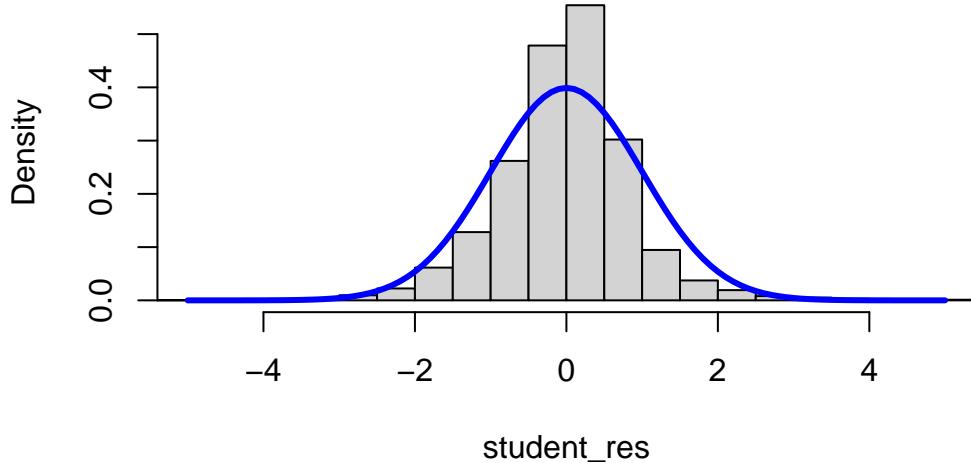


```
hist(student_res,freq=F,breaks=100,xlim=c(-2,2))
curve(dnorm(x,0,1),add=T,col='blue',lwd=3)
```

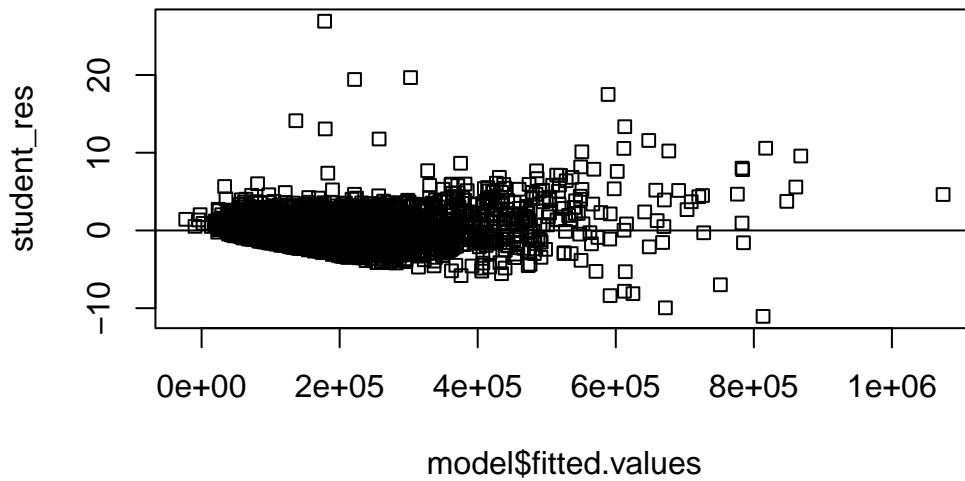


```
hist(student_res,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T,col='blue',lwd=3)
```

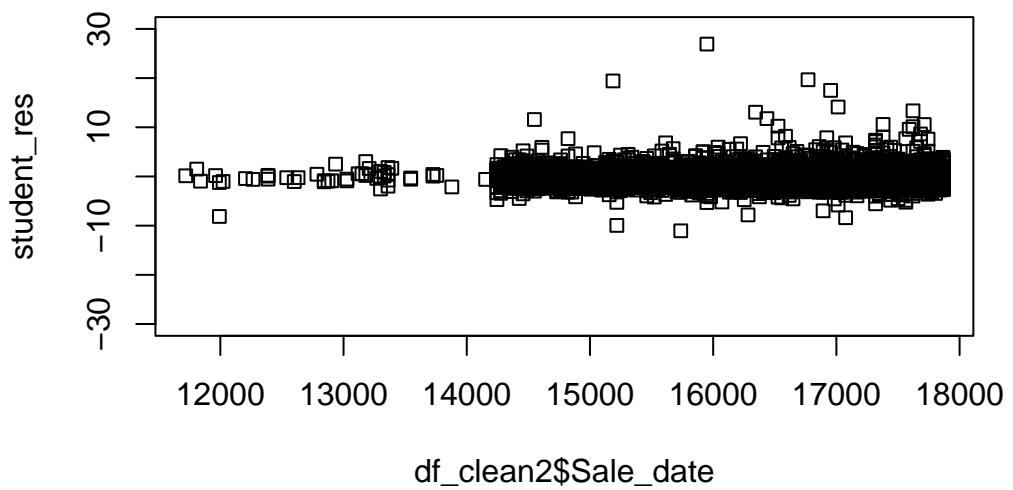
### Histogram of student\_res



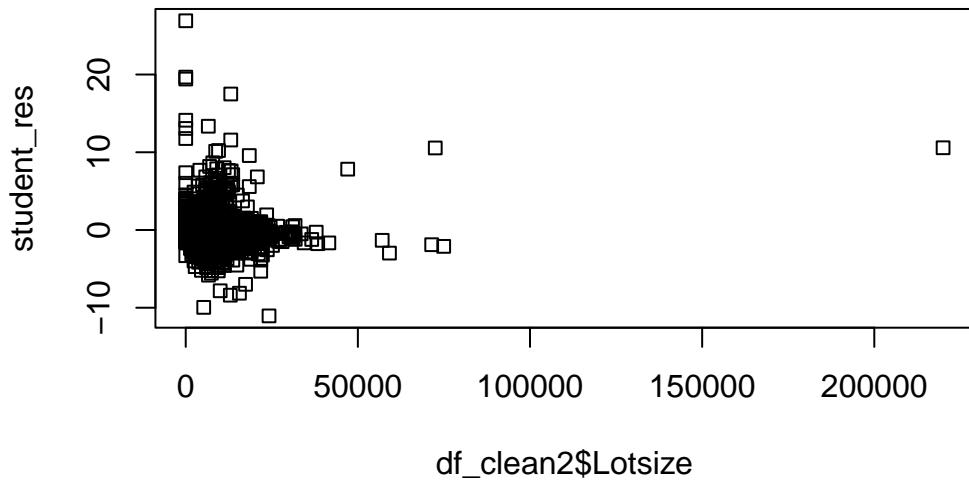
```
# SOS
plot(model$fitted.values,student_res,pch=22)
abline(h=0)
```



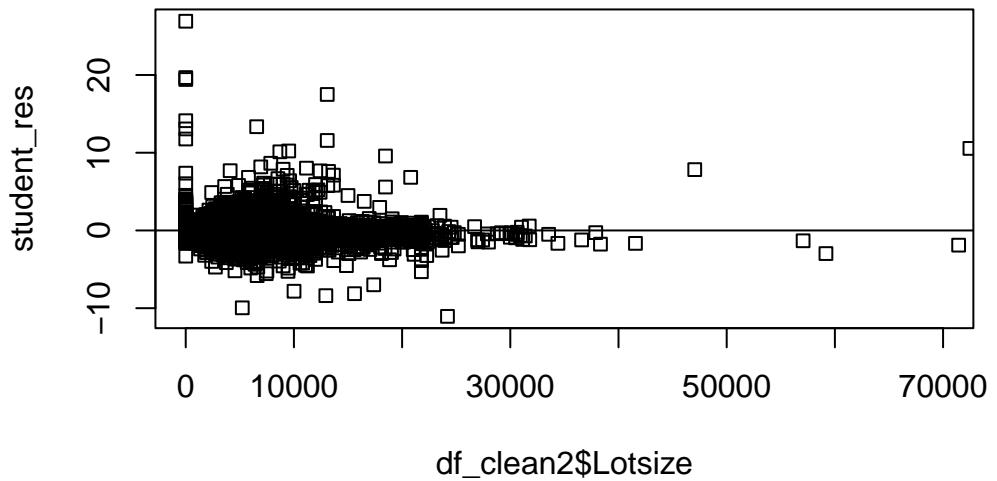
```
plot(df_clean2$Sale_date ,student_res,pch=22,ylim=c(-30,30))
```



```
plot(df_clean2$Lotsize ,student_res,pch=22)
```



```
plot(df_clean2$Lotsize ,student_res,pch=22,xlim=c(0,70000))  
abline(h=0)
```



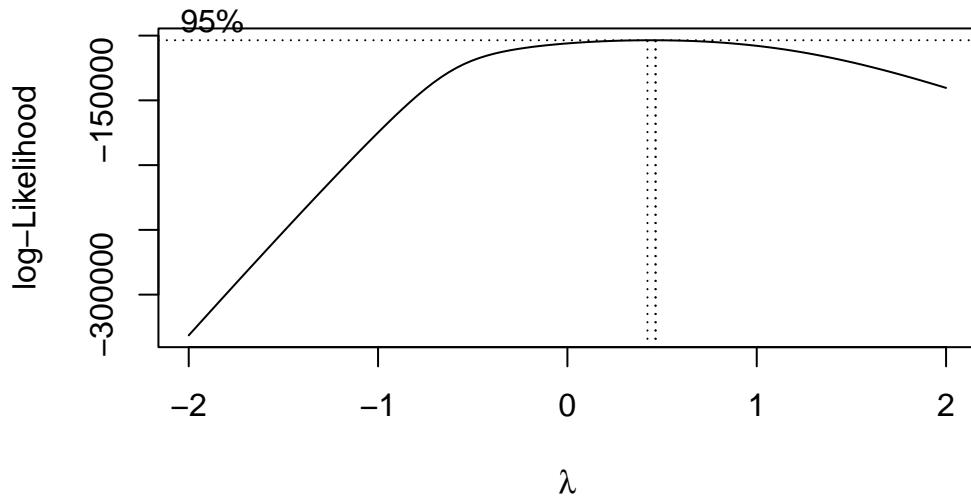
```

# Let's try a transformation

# model=lm(Sale_price~.,df_clean2)
df_clean2=df_clean2[df_clean2$Sale_price>0,]

bc=MASS::boxcox(Sale_price~.,data=df_clean2,
                 lambda = seq(-2, 2, 1/10),
                 plotit = TRUE,
                 eps = 1/50,
                 xlab = expression(lambda),
                 ylab = "log-Likelihood")

```

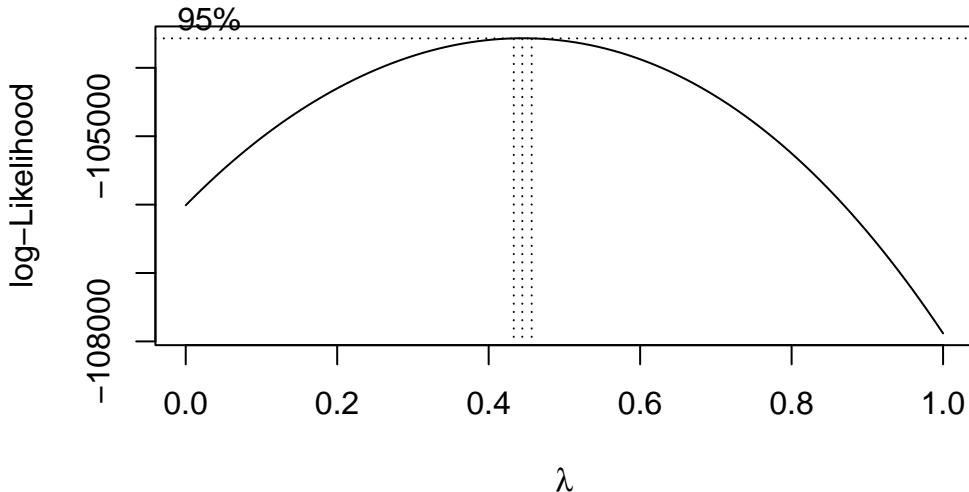


```

df_clean3=df_clean2[df_clean2$Sale_price>0,]
# bc=MASS::boxcox(Sale_price~.,data=df_clean3,
#                   lambda = seq(-2, 2, 1/10),
#                   plotit = TRUE,
#                   eps = 1/50,
#                   xlab = expression(lambda),
#                   ylab = "log-Likelihood")

bc=MASS::boxcox(Sale_price~.,data=df_clean3,
                 lambda = seq(0, 1, 1/10),
                 plotit = TRUE,
                 eps = 1/50,
                 xlab = expression(lambda),
                 ylab = "log-Likelihood")

```



```

model2=lm(sqrt(Sale_price)~.,df_clean3)
# model2=lm(Sale_price^(0.4)~.,df_clean3)

summ2=summary(model2); summ2

```

Call:  
`lm(formula = sqrt(Sale_price) ~ ., data = df_clean3)`

Residuals:

Min	1Q	Median	3Q	Max
-542.68	-37.46	6.16	42.34	973.57

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-7.741e+02	5.556e+01	-13.932	< 2e-16 ***
District	3.607e+00	1.167e-01	30.915	< 2e-16 ***
ExtwallBlock	4.563e-01	6.189e+00	0.074	0.941222
ExtwallBrick	1.310e+01	1.226e+00	10.684	< 2e-16 ***
ExtwallFiber-Cement	1.593e+01	6.329e+00	2.518	0.011815 *
ExtwallFrame	-9.554e+00	1.646e+00	-5.806	6.48e-09 ***

```

ExtwallMasonry / Frame 7.916e+00 2.896e+00 2.734 0.006268 **
ExtwallPrem Wood      1.176e+01 9.479e+00 1.240 0.214945
ExtwallStone           8.667e+00 2.591e+00 3.345 0.000823 ***
ExtwallStucco          1.884e+01 3.626e+00 5.195 2.07e-07 ***
Stories1                4.819e+01 1.741e+01 2.767 0.005660 **
Stories1.5              6.198e+01 1.739e+01 3.564 0.000366 ***
Stories2                7.132e+01 1.732e+01 4.117 3.86e-05 ***
Year_Built              2.876e-01 2.394e-02 12.011 < 2e-16 ***
Fin_sqft               1.009e-01 1.593e-03 63.301 < 2e-16 ***
Units1                 1.272e+02 1.229e+01 10.348 < 2e-16 ***
Units2                 2.193e+01 1.229e+01 1.784 0.074427 .
Units3                 -2.377e+01 1.324e+01 -1.795 0.072732 .
Bdrms0                 1.537e+02 3.125e+01 4.917 8.85e-07 ***
Bdrms1                 1.697e+02 1.679e+01 10.109 < 2e-16 ***
Bdrms2                 1.460e+02 1.526e+01 9.566 < 2e-16 ***
Bdrms3                 1.481e+02 1.517e+01 9.764 < 2e-16 ***
Bdrms4                 1.281e+02 1.511e+01 8.480 < 2e-16 ***
Bdrms5                 1.245e+02 1.511e+01 8.244 < 2e-16 ***
Bdrms6                 1.025e+02 1.513e+01 6.776 1.26e-11 ***
Bdrms7                 7.174e+01 1.614e+01 4.445 8.84e-06 ***
Bdrms8                 1.004e+02 1.698e+01 5.917 3.33e-09 ***
Fbath0                 -6.028e+01 2.232e+01 -2.700 0.006930 **
Fbath1                 -3.910e+01 1.609e+01 -2.430 0.015100 *
Fbath2                 -1.371e+01 1.599e+01 -0.858 0.391107
Fbath3                 3.069e+01 1.589e+01 1.932 0.053401 .
Fbath4                 6.407e+01 1.703e+01 3.762 0.000169 ***
Lotsize                1.851e-03 1.636e-04 11.317 < 2e-16 ***
Sale_date               6.306e-03 4.411e-04 14.295 < 2e-16 ***
---
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 74.49 on 24559 degrees of freedom
Multiple R-squared: 0.436, Adjusted R-squared: 0.4353
F-statistic: 575.4 on 33 and 24559 DF, p-value: < 2.2e-16

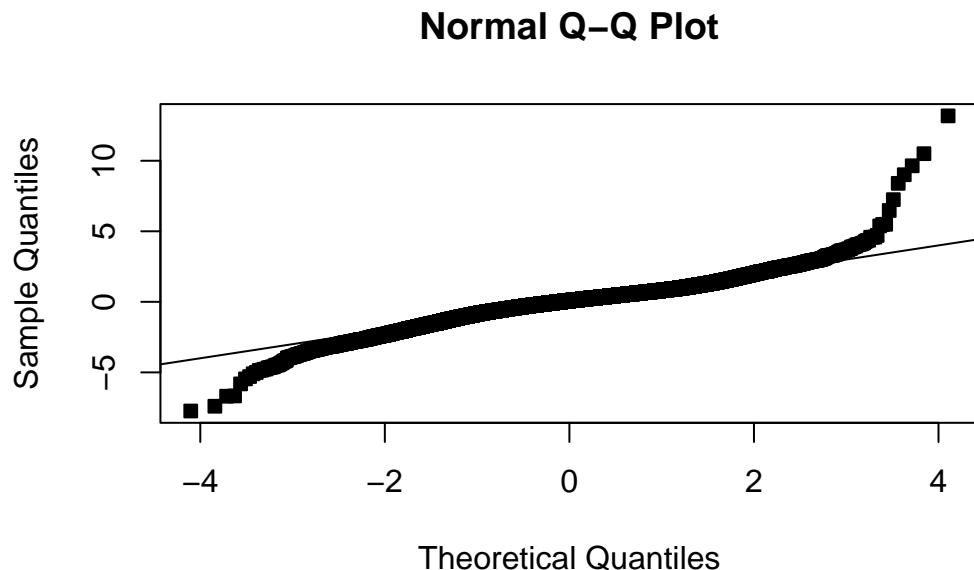
```

```
summ2$adj.r.squared
```

```
[1] 0.4352901
```

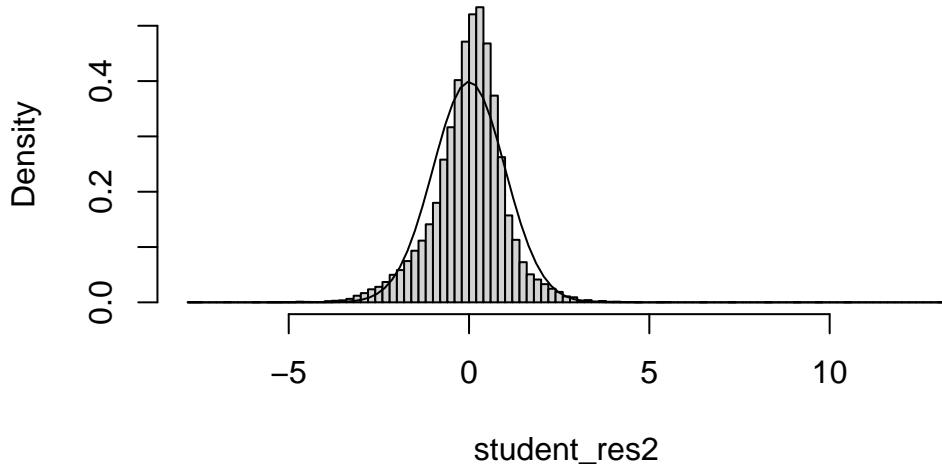
```
student_res2=rstudent(model2)

MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22,bg=1)
abline(0,1)
```



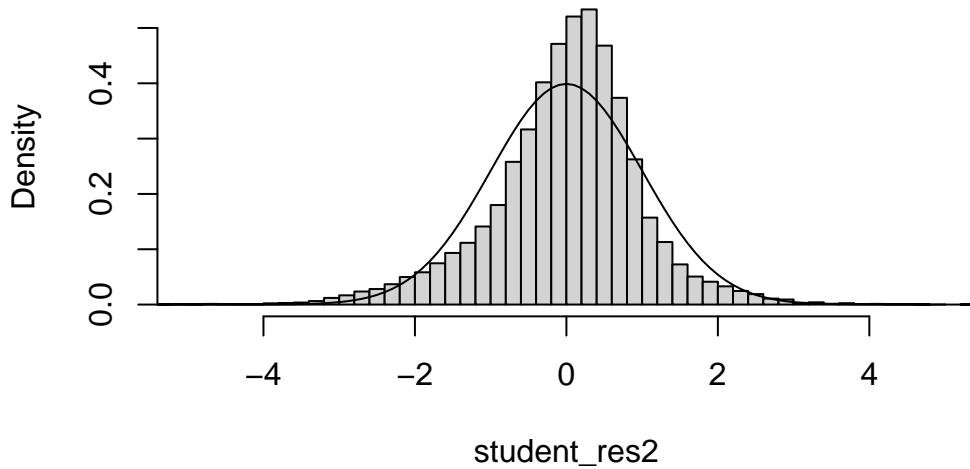
```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

### Histogram of student\_res2

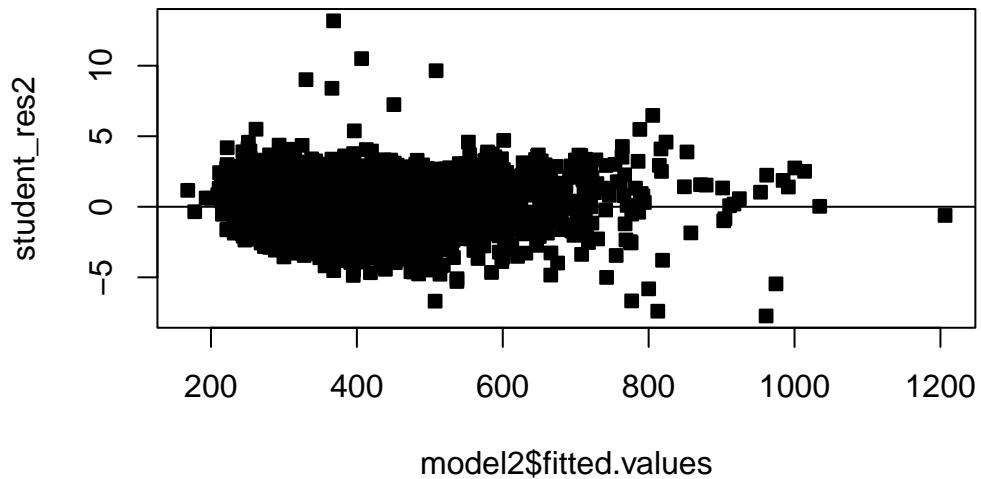


```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```

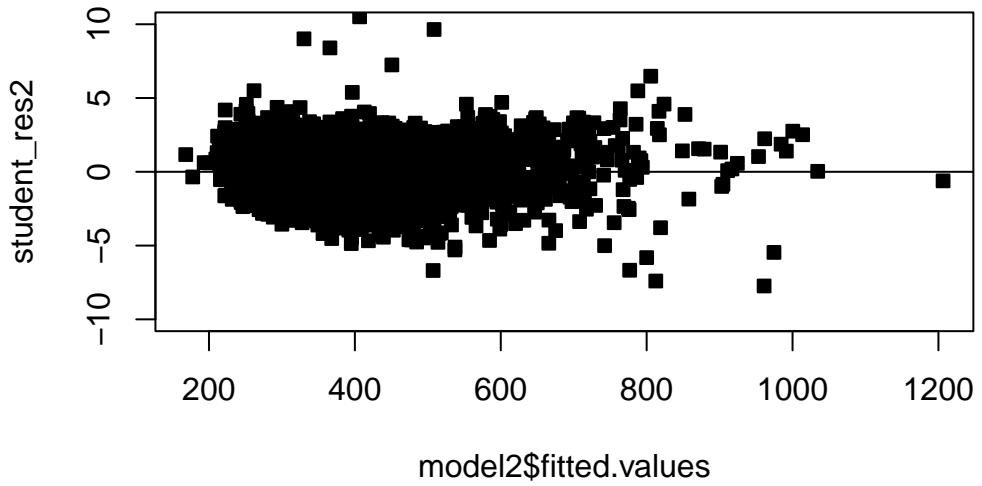
### Histogram of student\_res2



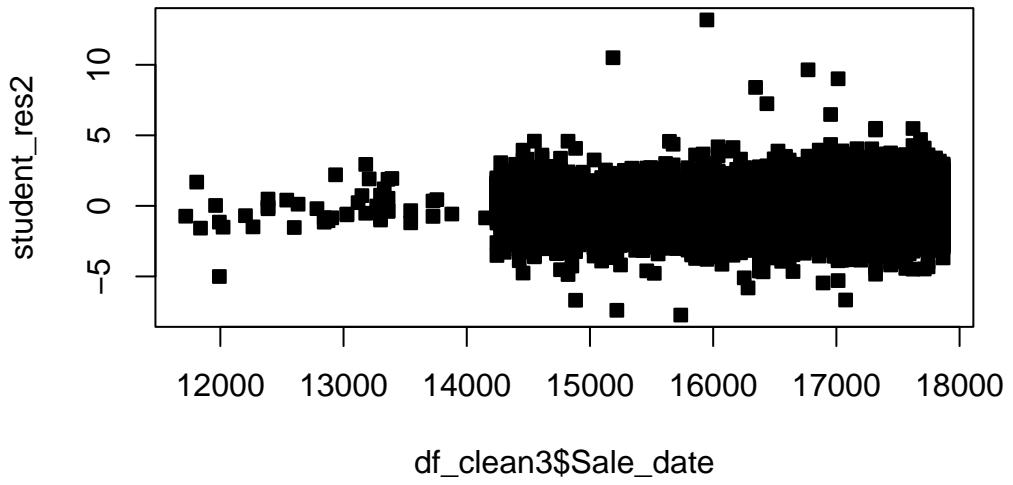
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



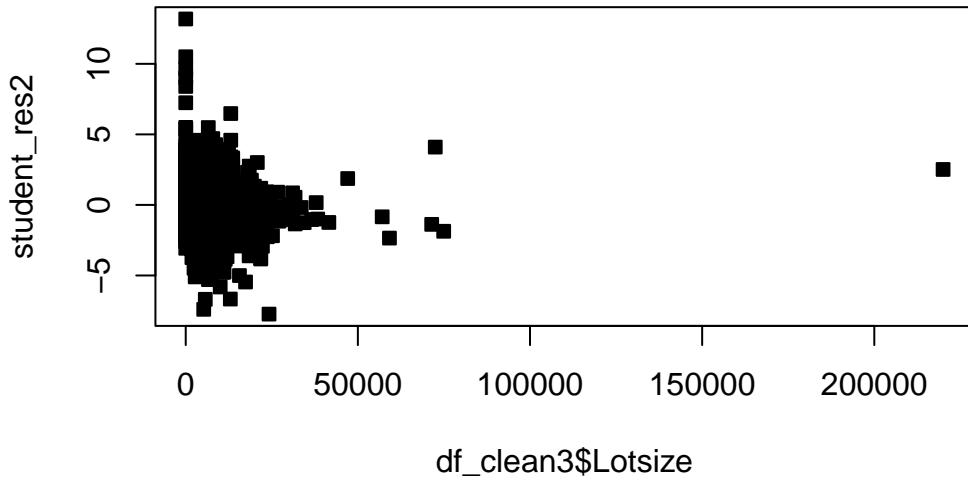
```
plot(model2$fitted.values,student_res2,pch=22,bg=1,ylim=c(-10,10))
abline(h=0)
```



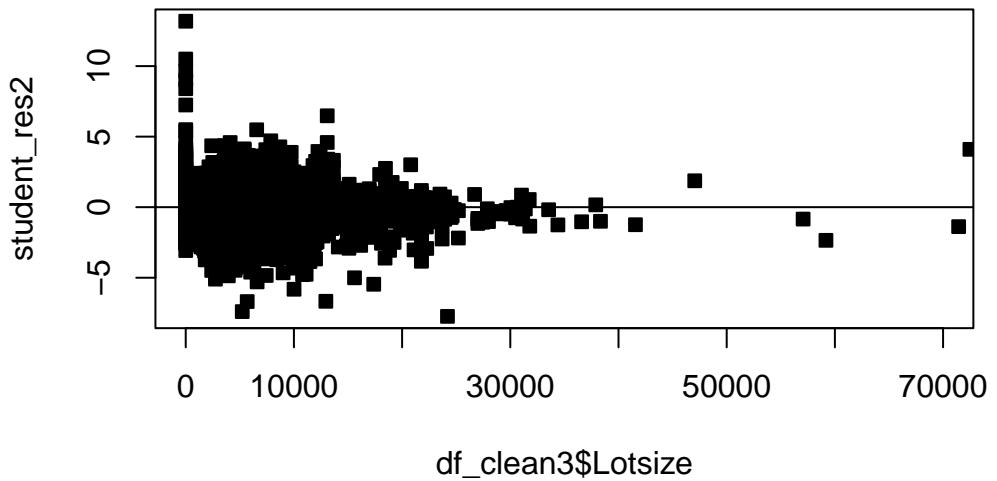
```
plot(df_clean3$Sale_date ,student_res2,pch=22,bg=1)
```



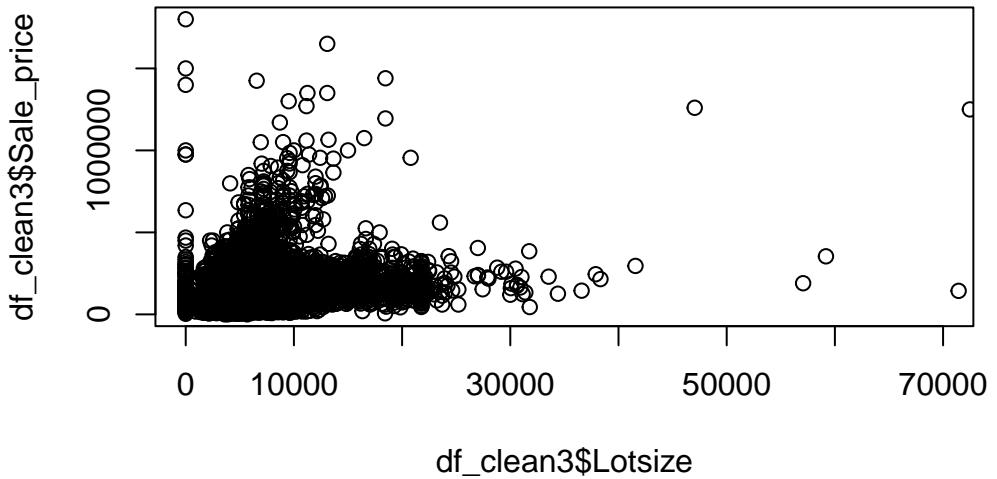
```
plot(df_clean3$Lotsize ,student_res2,pch=22, bg=1)
```



```
plot(df_clean3$Lotsize ,student_res2,pch=22, bg=1,xlim=c(0,70000))  
abline(h=0)
```



```
# It feels like the slope of lot size  
# depends on something,  
#like two categories  
plot(df_clean3$Lotsize,df_clean3$Sale_price,xlim=c(0,70000))
```



```
# plot(1/df_clean3$Lotsize,df_clean3$Sale_price)
```

```
sum(df_clean3$Lotsize==0)
```

```
[1] 146
```

```
df_clean4=df_clean3[df_clean3$Lotsize!=0,]
```

```
model2=lm(sqrt(Sale_price)~.,df_clean4)
# model2=lm(Sale_price^(0.4)~.,df_clean3)
```

```
summ2=summary(model2); summ2
```

Call:

```
lm(formula = sqrt(Sale_price) ~ ., data = df_clean4)
```

Residuals:

	Min	1Q	Median	3Q	Max
	-544.58	-36.99	6.27	42.23	481.64

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-7.754e+02	5.483e+01	-14.142	< 2e-16 ***
District	3.744e+00	1.148e-01	32.609	< 2e-16 ***
ExtwallBlock	-3.526e+00	6.132e+00	-0.575	0.565249
ExtwallBrick	1.266e+01	1.204e+00	10.511	< 2e-16 ***
ExtwallFiber-Cement	1.604e+01	6.210e+00	2.584	0.009776 **
ExtwallFrame	-9.920e+00	1.627e+00	-6.095	1.11e-09 ***
ExtwallMasonry / Frame	8.766e+00	2.845e+00	3.082	0.002061 **
ExtwallPrem Wood	1.158e+01	9.299e+00	1.245	0.213087
ExtwallStone	8.975e+00	2.542e+00	3.530	0.000416 ***
ExtwallStucco	1.876e+01	3.573e+00	5.251	1.52e-07 ***
Stories1	4.698e+01	1.708e+01	2.750	0.005963 **
Stories1.5	6.078e+01	1.706e+01	3.563	0.000368 ***
Stories2	6.916e+01	1.699e+01	4.070	4.72e-05 ***
Year_Built	2.939e-01	2.365e-02	12.427	< 2e-16 ***
Fin_sqft	1.000e-01	1.570e-03	63.697	< 2e-16 ***
Units1	1.221e+02	1.222e+01	9.992	< 2e-16 ***
Units2	1.633e+01	1.223e+01	1.336	0.181724
Units3	-2.964e+01	1.316e+01	-2.253	0.024293 *
Bdrms0	1.533e+02	3.080e+01	4.976	6.54e-07 ***
Bdrms1	1.302e+02	1.678e+01	7.760	8.80e-15 ***
Bdrms2	1.424e+02	1.498e+01	9.507	< 2e-16 ***
Bdrms3	1.461e+02	1.489e+01	9.817	< 2e-16 ***
Bdrms4	1.268e+02	1.483e+01	8.553	< 2e-16 ***
Bdrms5	1.240e+02	1.482e+01	8.363	< 2e-16 ***
Bdrms6	1.027e+02	1.485e+01	6.914	4.83e-12 ***
Bdrms7	7.282e+01	1.583e+01	4.599	4.27e-06 ***
Bdrms8	1.021e+02	1.666e+01	6.129	8.97e-10 ***
Fbath0	-6.484e+01	2.266e+01	-2.861	0.004228 **
Fbath1	-4.116e+01	1.579e+01	-2.606	0.009163 **
Fbath2	-1.549e+01	1.569e+01	-0.987	0.323435
Fbath3	2.939e+01	1.559e+01	1.885	0.059381 .
Fbath4	6.073e+01	1.672e+01	3.632	0.000282 ***
Lotsize	2.086e-03	1.613e-04	12.936	< 2e-16 ***
Sale_date	6.175e-03	4.340e-04	14.230	< 2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

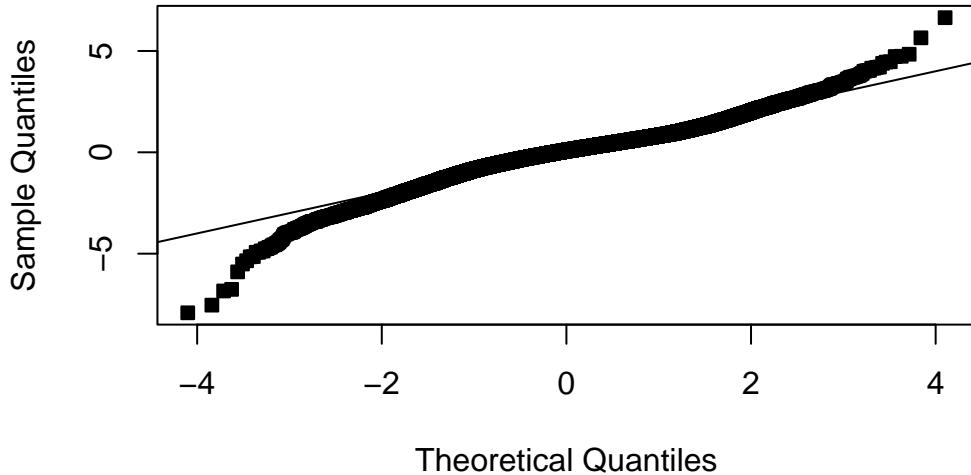
```
Residual standard error: 73.07 on 24413 degrees of freedom
Multiple R-squared:  0.4468,    Adjusted R-squared:  0.446
F-statistic: 597.4 on 33 and 24413 DF,  p-value: < 2.2e-16
```

```
summ2$adj.r.squared
```

```
[1] 0.4460105
```

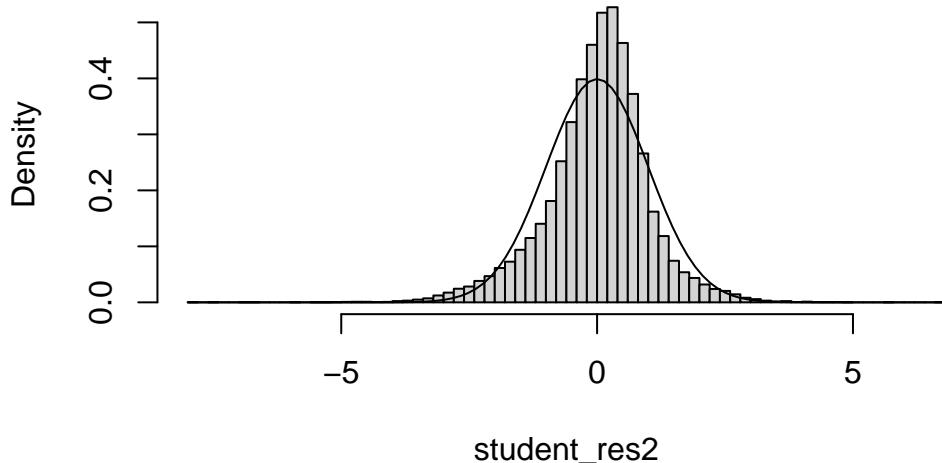
```
student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22,bg=1)
abline(0,1)
```

Normal Q-Q Plot



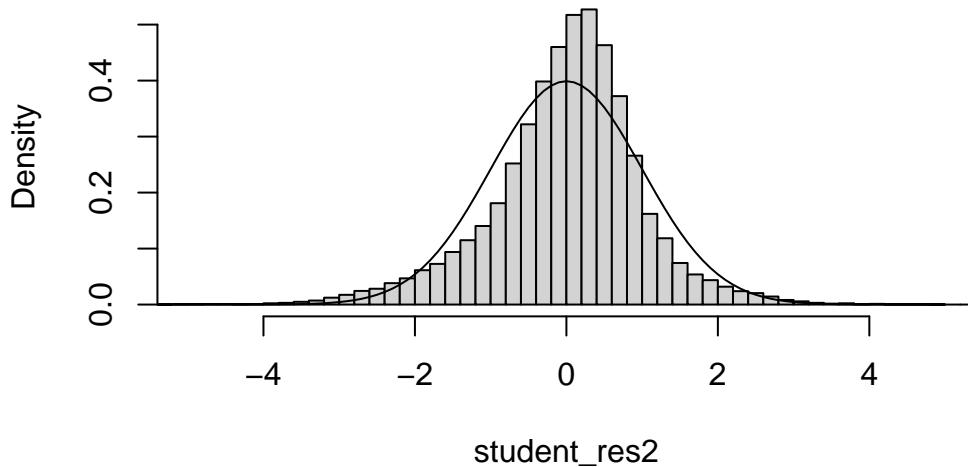
```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

### Histogram of student\_res2

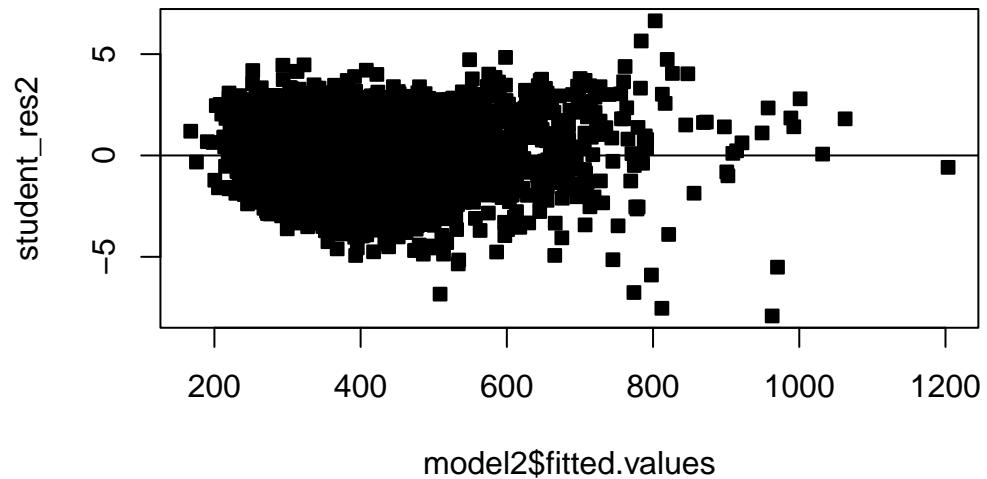


```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```

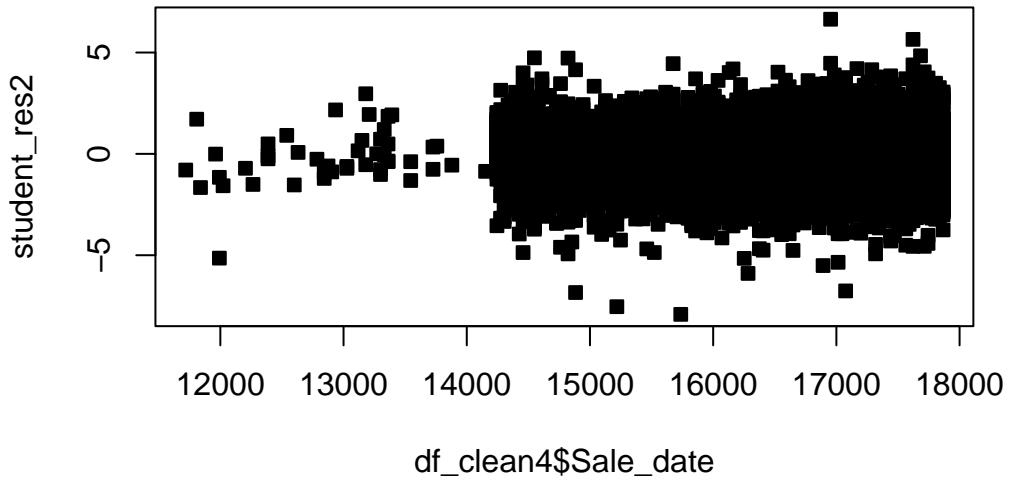
### Histogram of student\_res2



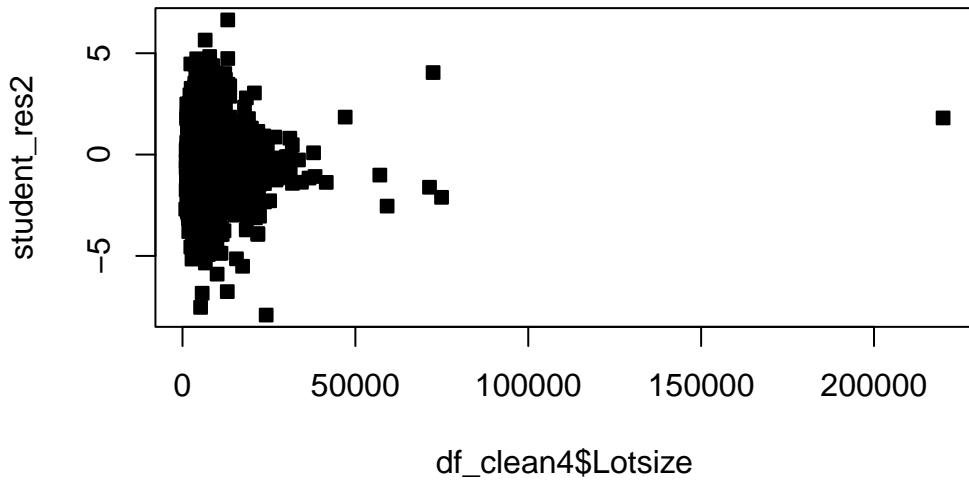
```
plot(model2$fitted.values,student_res2,pch=22, bg=1)
abline(h=0)
```



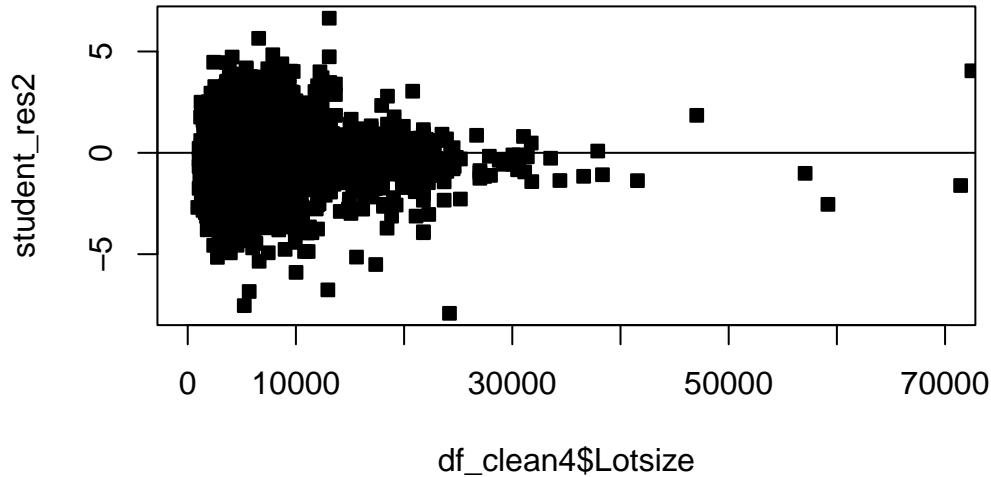
```
plot(df_clean4$Sale_date ,student_res2,pch=22, bg=1)
```



```
plot(df_clean4$Lotsize ,student_res2,pch=22,bg=1)
```



```
plot(df_clean4$Lotsize ,student_res2,pch=22, bg=1,xlim=c(0,70000))
abline(h=0)
```



```
df_clean4=df_clean4[df_clean4$Lotsize<70000,]
```

```
model2=lm(sqrt(Sale_price)~.,df_clean4)
# model2=lm(Sale_price^(0.4)~.,df_clean3)
```

```
summ2=summary(model2); summ2
```

```
Call:  
lm(formula = sqrt(Sale_price) ~ ., data = df_clean4)
```

```
Residuals:  
    Min     1Q   Median     3Q    Max  
-542.27  -36.96    6.36   42.19  482.94
```

```
Coefficients:  
Estimate Std. Error t value Pr(>|t|)
```

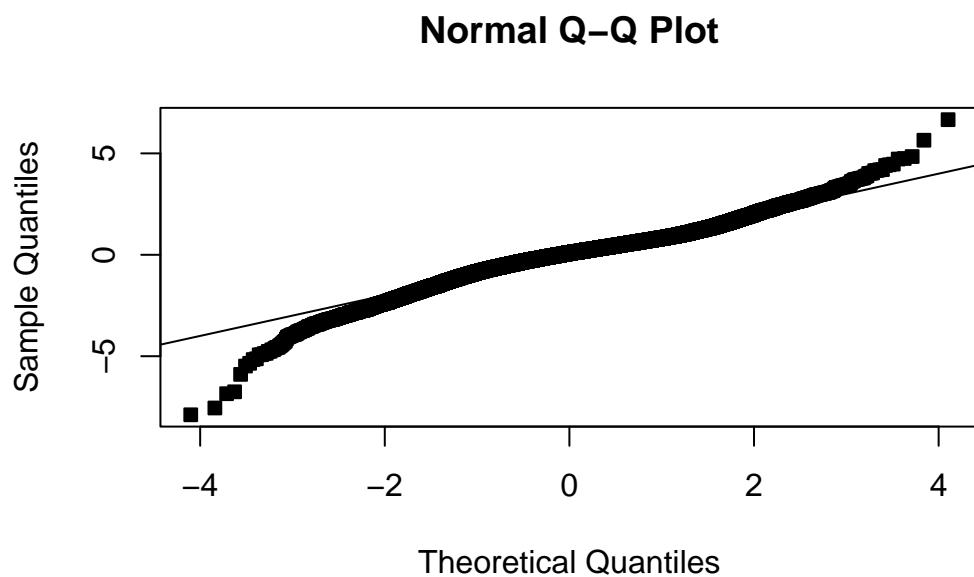
(Intercept)	-7.909e+02	5.585e+01	-14.161	< 2e-16	***						
District	3.748e+00	1.148e-01	32.656	< 2e-16	***						
ExtwallBlock	-5.561e+00	6.150e+00	-0.904	0.365881							
ExtwallBrick	1.270e+01	1.204e+00	10.551	< 2e-16	***						
ExtwallFiber-Cement	1.606e+01	6.207e+00	2.588	0.009663	**						
ExtwallFrame	-9.858e+00	1.627e+00	-6.059	1.39e-09	***						
ExtwallMasonry / Frame	8.679e+00	2.844e+00	3.051	0.002281	**						
ExtwallPrem Wood	1.454e+01	9.363e+00	1.553	0.120525							
ExtwallStone	9.085e+00	2.541e+00	3.575	0.000351	***						
ExtwallStucco	1.885e+01	3.572e+00	5.278	1.32e-07	***						
Stories1	4.700e+01	1.708e+01	2.752	0.005926	**						
Stories1.5	6.081e+01	1.705e+01	3.566	0.000363	***						
Stories2	6.931e+01	1.699e+01	4.080	4.52e-05	***						
Year_Built	3.028e-01	2.426e-02	12.480	< 2e-16	***						
Fin_sqft	1.000e-01	1.580e-03	63.322	< 2e-16	***						
Units1	1.221e+02	1.222e+01	9.998	< 2e-16	***						
Units2	1.621e+01	1.222e+01	1.327	0.184655							
Units3	-2.941e+01	1.315e+01	-2.236	0.025354	*						
Bdrms0	1.529e+02	3.078e+01	4.967	6.84e-07	***						
Bdrms1	1.300e+02	1.677e+01	7.752	9.38e-15	***						
Bdrms2	1.421e+02	1.498e+01	9.492	< 2e-16	***						
Bdrms3	1.459e+02	1.488e+01	9.805	< 2e-16	***						
Bdrms4	1.266e+02	1.482e+01	8.539	< 2e-16	***						
Bdrms5	1.239e+02	1.482e+01	8.359	< 2e-16	***						
Bdrms6	1.024e+02	1.484e+01	6.902	5.25e-12	***						
Bdrms7	7.278e+01	1.583e+01	4.598	4.28e-06	***						
Bdrms8	1.020e+02	1.665e+01	6.127	9.09e-10	***						
Fbath0	-6.549e+01	2.265e+01	-2.891	0.003843	**						
Fbath1	-4.185e+01	1.579e+01	-2.651	0.008027	**						
Fbath2	-1.614e+01	1.568e+01	-1.030	0.303245							
Fbath3	2.830e+01	1.558e+01	1.817	0.069294	.						
Fbath4	6.041e+01	1.671e+01	3.614	0.000302	***						
Lotsize	1.921e-03	1.888e-04	10.173	< 2e-16	***						
Sale_date	6.170e-03	4.338e-04	14.225	< 2e-16	***						
---											
Signif. codes:	0	'***'	0.001	'**'	0.01	'*'	0.05	'. '	0.1	' '	1

Residual standard error: 73.04 on 24409 degrees of freedom  
 Multiple R-squared: 0.4443, Adjusted R-squared: 0.4436  
 F-statistic: 591.5 on 33 and 24409 DF, p-value: < 2.2e-16

```
summ2$adj.r.squared
```

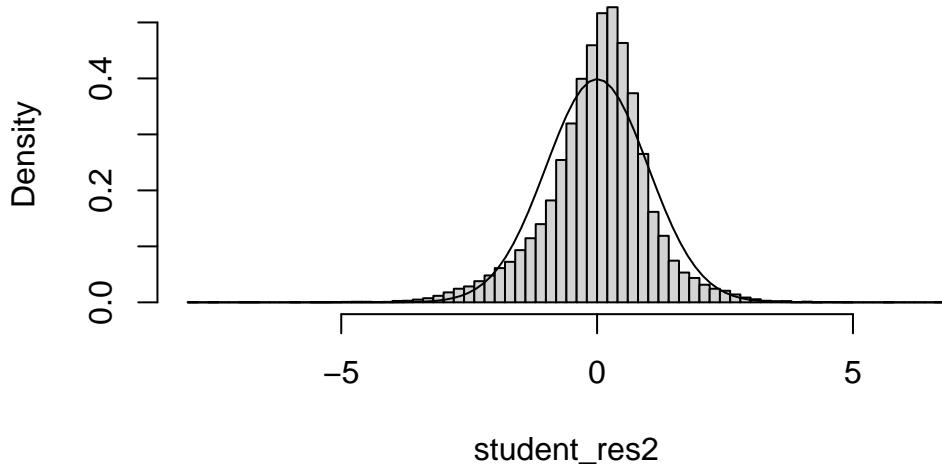
```
[1] 0.4435961
```

```
student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)
```



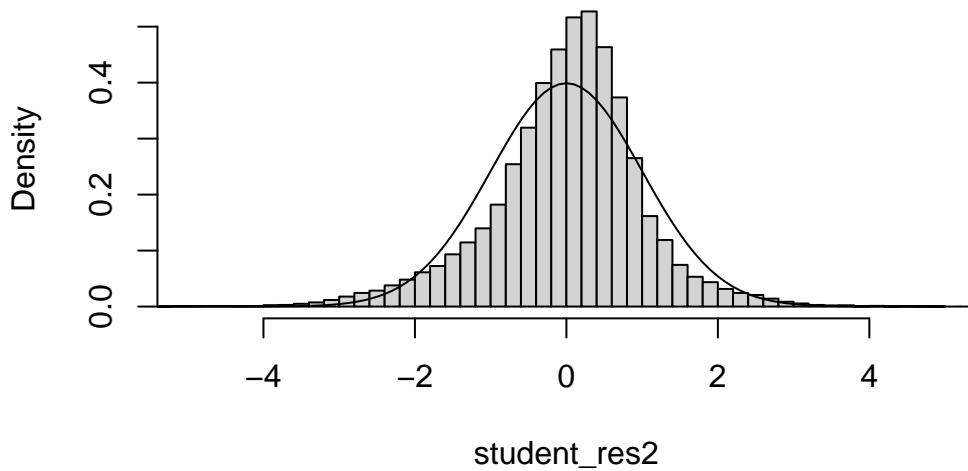
```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

### Histogram of student\_res2

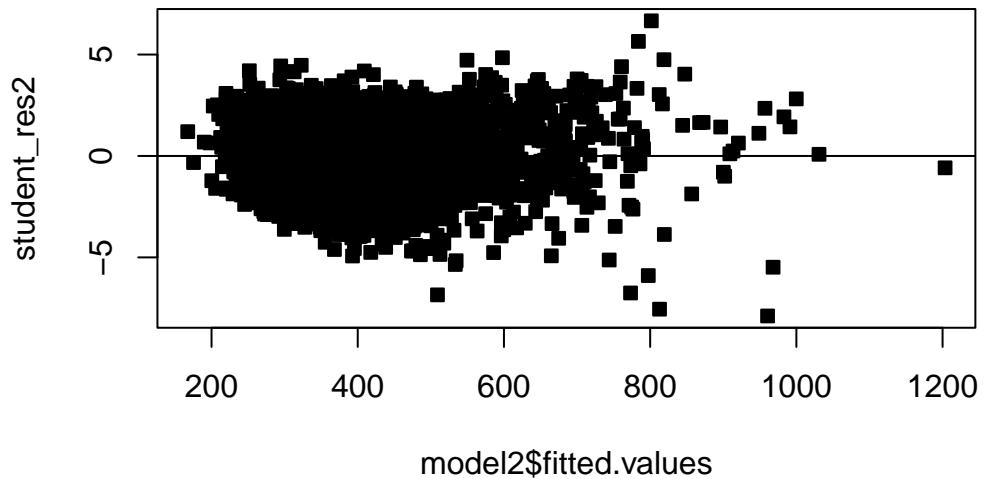


```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```

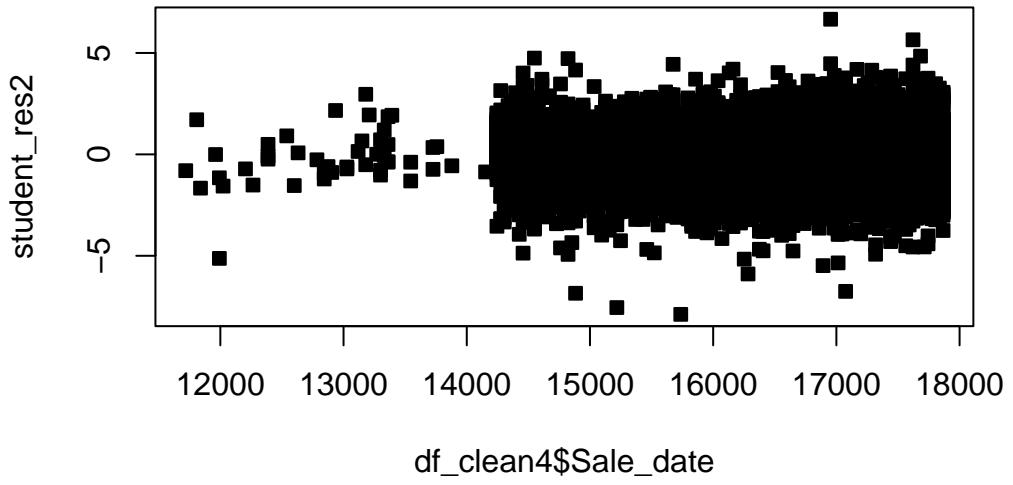
### Histogram of student\_res2



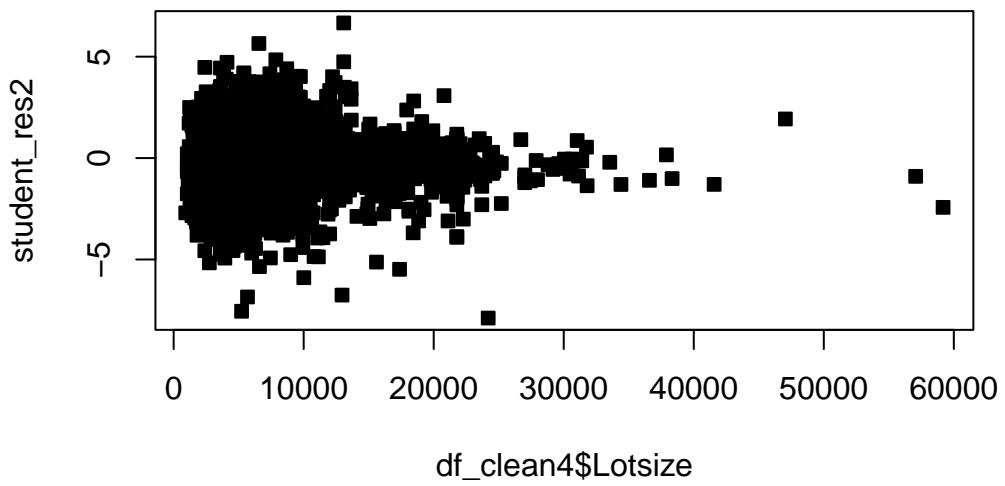
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



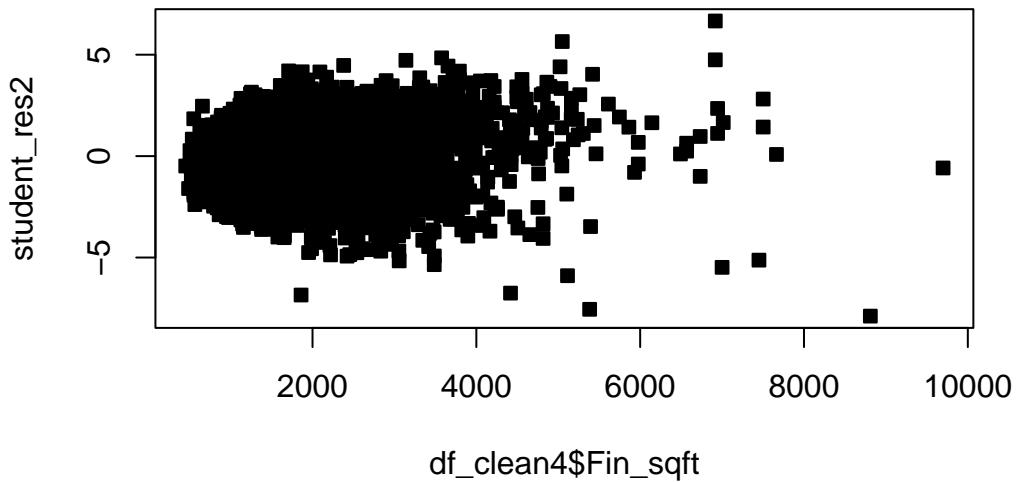
```
plot(df_clean4$Sale_date ,student_res2,pch=22,bg=1)
```



```
plot(df_clean4$Lotsize ,student_res2,pch=22,bg=1)
```

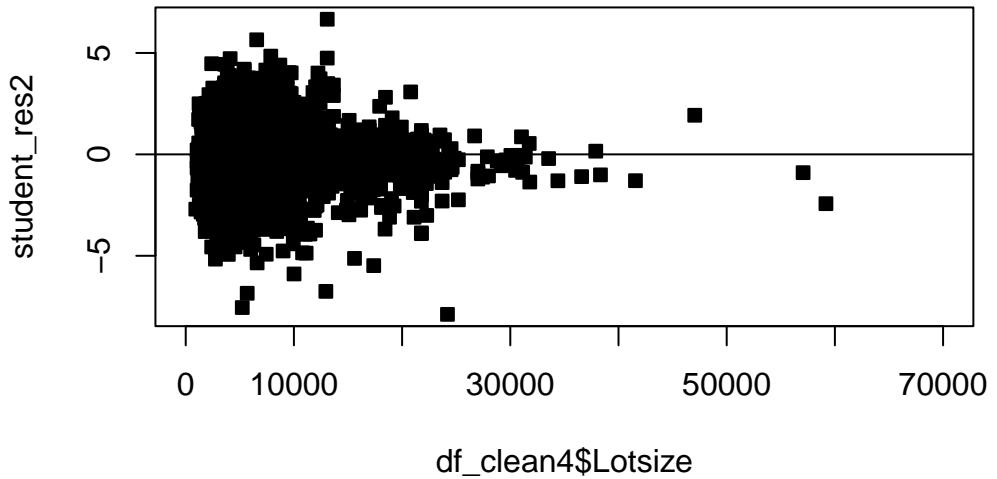


```
plot(df_clean4$Fin_sqft ,student_res2,pch=22,bg=1)
```



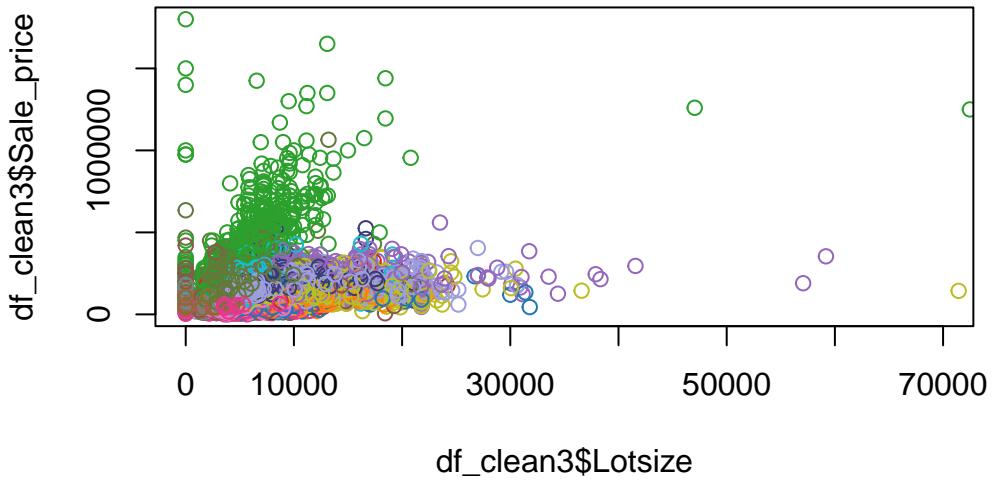
`df_clean4$Fin_sqft`

```
plot(df_clean4$Lotsize ,student_res2,pch=22,bg=1,xlim=c(0,70000))
abline(h=0)
```

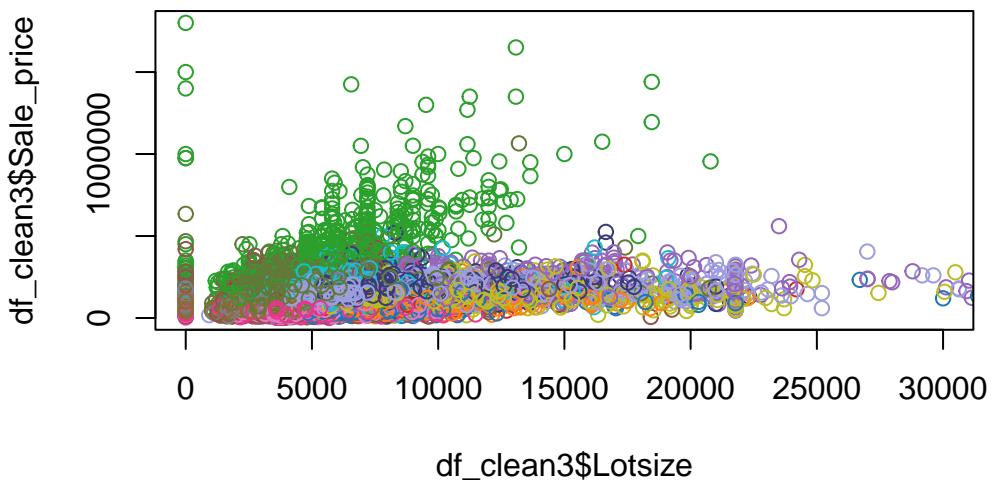


```
custom_palette <- c(
  "#1f77b4", "#ff7f0e", "#2ca02c", "#d62728",
  "#9467bd", "#8c564b", "#e377c2", "#7f7f7f",
  "#bcbd22", "#17becf", "#393b79",
  "#8c6d31", "#9c9ede", "#637939", "#eb348f"
)

plot(df_clean3$Lotsize, df_clean3$Sale_price,
      xlim=c(0,70000),
      col=custom_palette[df_clean3$District])
```



```
plot(df_clean3$Lotsize,df_clean3$Sale_price,xlim=c(0,30000),  
     col=custom_palette[df_clean3$District])
```

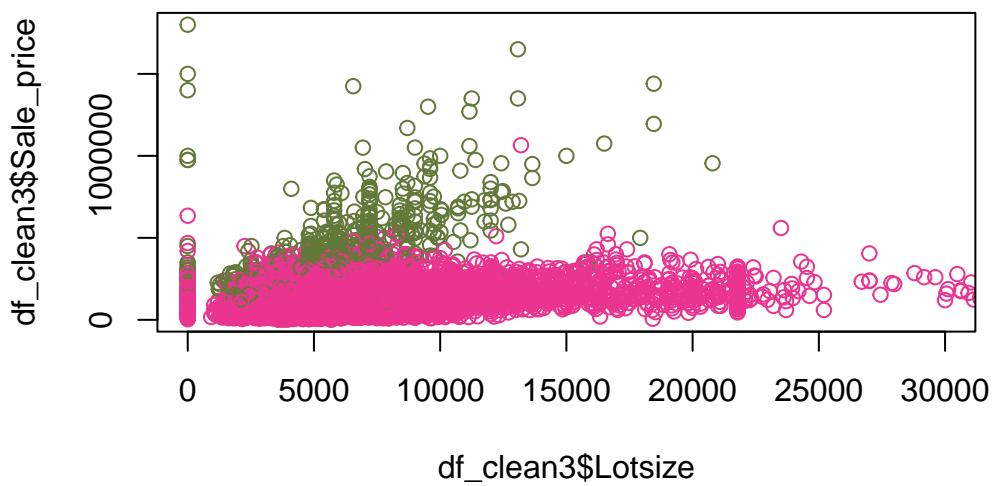


```

custom_palette <- c(
  "#eb348f", "#eb348f", "#637939", "#eb348f",
  "#eb348f", "#eb348f", "#eb348f", "#eb348f",
  "#eb348f", "#eb348f", "#eb348f",
  "#eb348f", "#eb348f", "#eb348f", "#eb348f"
)

plot(df_clean3$Lotsize, df_clean3$Sale_price, xlim=c(0,30000), col=custom_palette[df_clean3$D

```



#green is 3 and 14 here

```

# order is
# Red
# Green
# Blue
# Cyan
# Magenta
# Yellow
# Black
# Gray

```

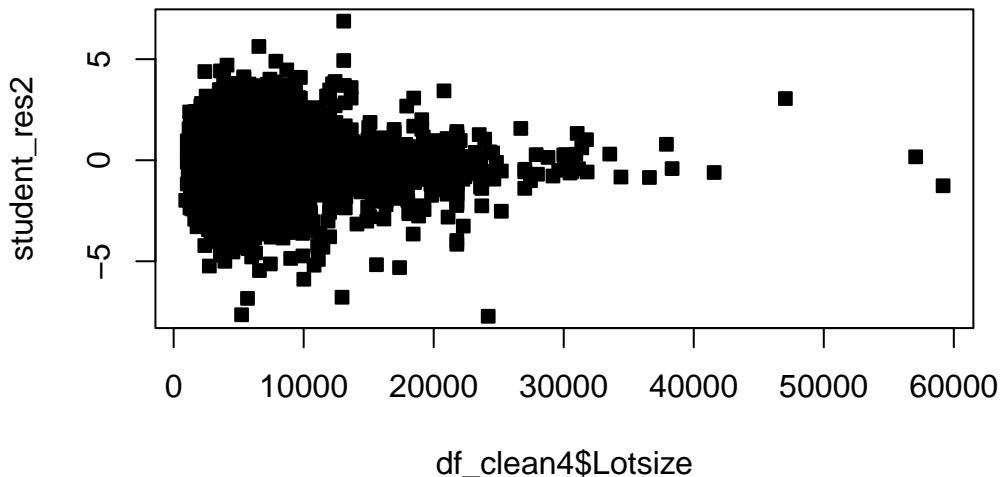
```

df_clean4$d_3=df_clean4$District==3
#df_clean4$d_3=mapply('||',df_clean4$District==3,df_clean4$District==14)
model2=lm(sqrt(Sale_price)~ District + Extwall +
          Stories + Year_Built + Fin_sqft +
          Units + Bdrms +
          Fbath + log(Lotsize) + Sale_date + d_3*log(Lotsize)-d_3,
          df_clean4)

model2=lm(sqrt(Sale_price)~ District + Extwall +
          Stories + Year_Built + Fin_sqft +
          Units + Bdrms +
          Fbath + log(Lotsize) + Sale_date + log(Lotsize)*District,
          df_clean4)

student_res2=rstudent(model2)
plot(df_clean4$Lotsize ,student_res2,pch=22,bg=1)

```



```
# model2=lm(Sale_price^(0.4)~.,df_clean3)

summ2=summary(model2); summ2
```

Call:

```
lm(formula = sqrt(Sale_price) ~ District + Extwall + Stories +
    Year_Built + Fin_sqft + Units + Bdrms + Fbath + log(Lotsize) +
    Sale_date + log(Lotsize) * District, data = df_clean4)
```

Residuals:

Min	1Q	Median	3Q	Max
-542.77	-37.26	5.82	41.94	496.12

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-5.146e+02	5.836e+01	-8.818	< 2e-16 ***
District	-2.657e+01	2.617e+00	-10.150	< 2e-16 ***
ExtwallBlock	-5.663e+00	6.119e+00	-0.925	0.354740
ExtwallBrick	1.153e+01	1.198e+00	9.625	< 2e-16 ***
ExtwallFiber-Cement	1.916e+01	6.187e+00	3.096	0.001965 **
ExtwallFrame	-1.042e+01	1.619e+00	-6.437	1.24e-10 ***
ExtwallMasonry / Frame	7.347e+00	2.831e+00	2.595	0.009466 **
ExtwallPrem Wood	1.642e+01	9.309e+00	1.763	0.077851 .
ExtwallStone	8.615e+00	2.528e+00	3.407	0.000657 ***
ExtwallStucco	1.742e+01	3.554e+00	4.902	9.54e-07 ***
Stories1	4.078e+01	1.701e+01	2.398	0.016479 *
Stories1.5	5.520e+01	1.698e+01	3.251	0.001150 **
Stories2	6.383e+01	1.691e+01	3.774	0.000161 ***
Year_Built	2.076e-01	2.572e-02	8.072	7.22e-16 ***
Fin_sqft	9.922e-02	1.574e-03	63.021	< 2e-16 ***
Units1	1.243e+02	1.215e+01	10.225	< 2e-16 ***
Units2	1.859e+01	1.216e+01	1.529	0.126302
Units3	-2.874e+01	1.309e+01	-2.196	0.028078 *
Bdrms0	1.500e+02	3.063e+01	4.898	9.76e-07 ***
Bdrms1	1.301e+02	1.669e+01	7.796	6.65e-15 ***
Bdrms2	1.411e+02	1.490e+01	9.474	< 2e-16 ***
Bdrms3	1.441e+02	1.480e+01	9.731	< 2e-16 ***
Bdrms4	1.252e+02	1.475e+01	8.489	< 2e-16 ***
Bdrms5	1.218e+02	1.474e+01	8.263	< 2e-16 ***
Bdrms6	1.009e+02	1.477e+01	6.834	8.47e-12 ***

```

Bdrms7          7.057e+01  1.575e+01   4.481 7.45e-06 ***
Bdrms8          9.879e+01  1.657e+01   5.963 2.51e-09 ***
Fbath0         -7.195e+01  2.255e+01  -3.192 0.001417 **
Fbath1         -4.903e+01  1.572e+01  -3.120 0.001811 **
Fbath2         -2.305e+01  1.561e+01  -1.477 0.139781
Fbath3          2.206e+01  1.551e+01   1.422 0.154986
Fbath4          5.559e+01  1.663e+01   3.342 0.000832 ***
log(Lotsize)    -7.558e+00  3.074e+00  -2.458 0.013971 *
Sale_date        6.125e-03  4.316e-04  14.193 < 2e-16 ***
District:log(Lotsize) 3.514e+00  3.031e-01  11.595 < 2e-16 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

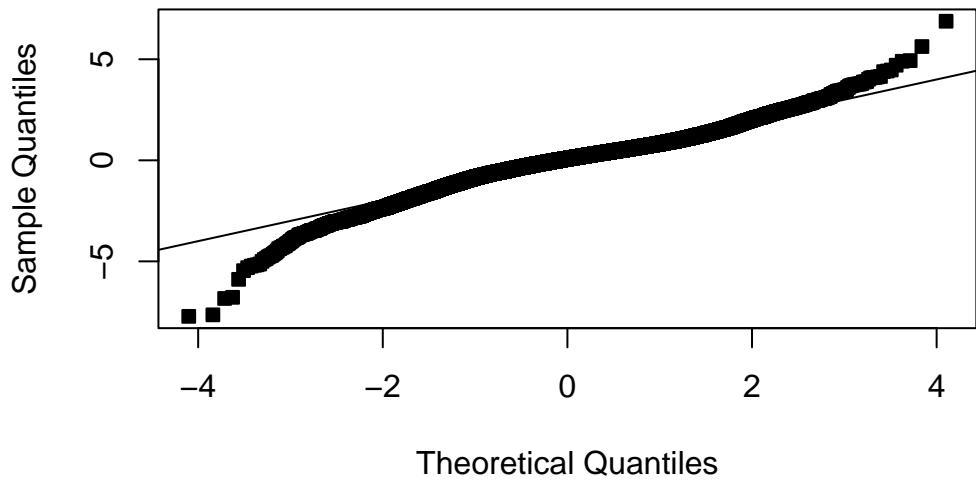
Residual standard error: 72.67 on 24408 degrees of freedom  
 Multiple R-squared: 0.45, Adjusted R-squared: 0.4492  
 F-statistic: 587.3 on 34 and 24408 DF, p-value: < 2.2e-16

```
summ2$adj.r.squared
```

```
[1] 0.4492185
```

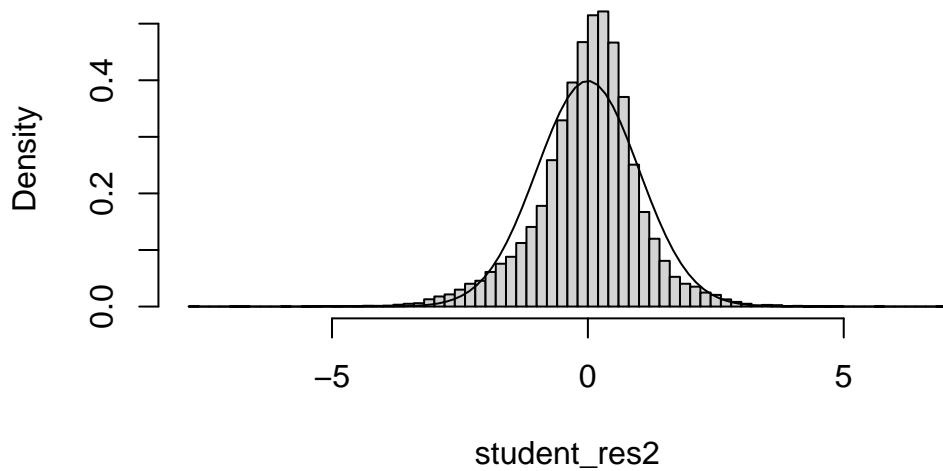
```
student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)
```

### Normal Q-Q Plot

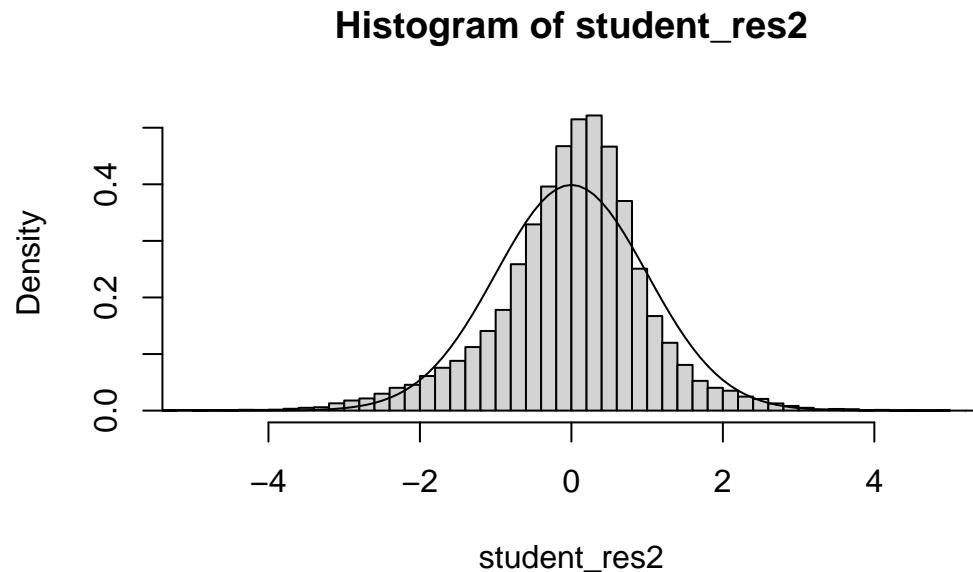


```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

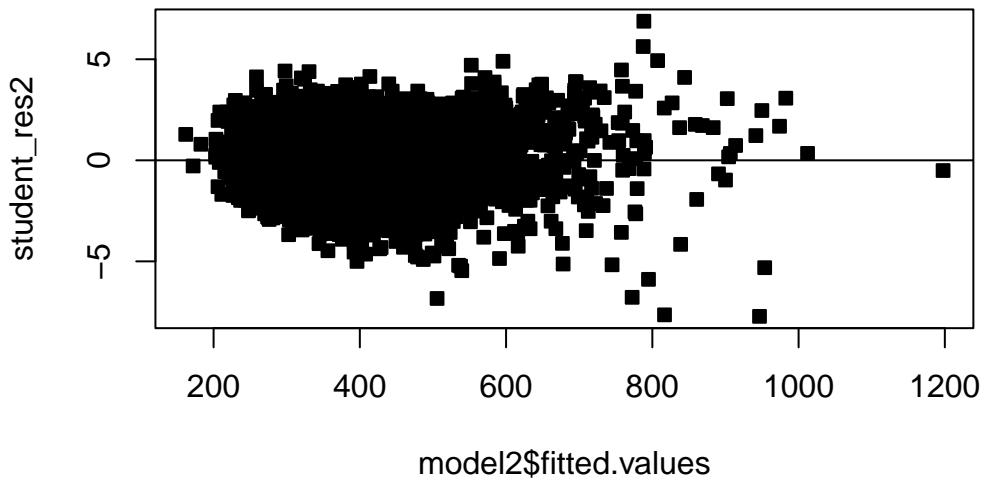
### Histogram of student\_res2



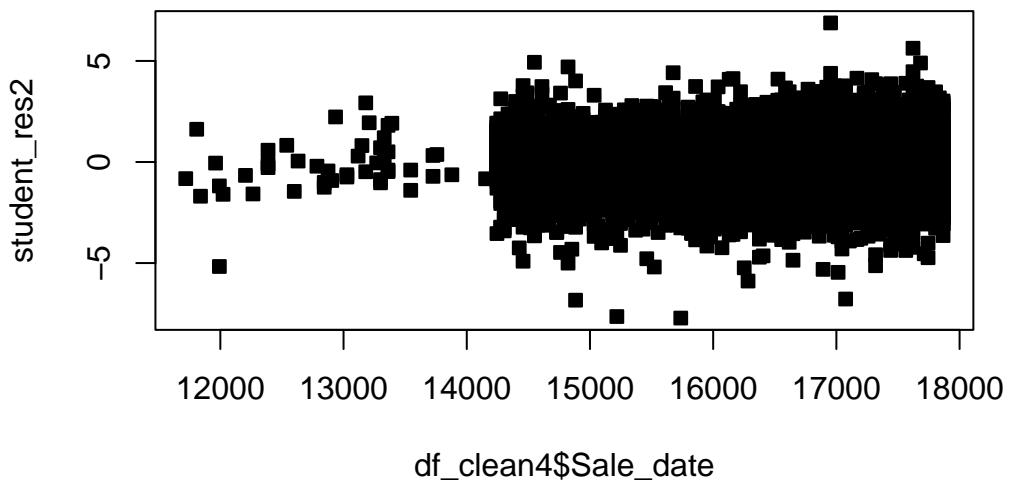
```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```



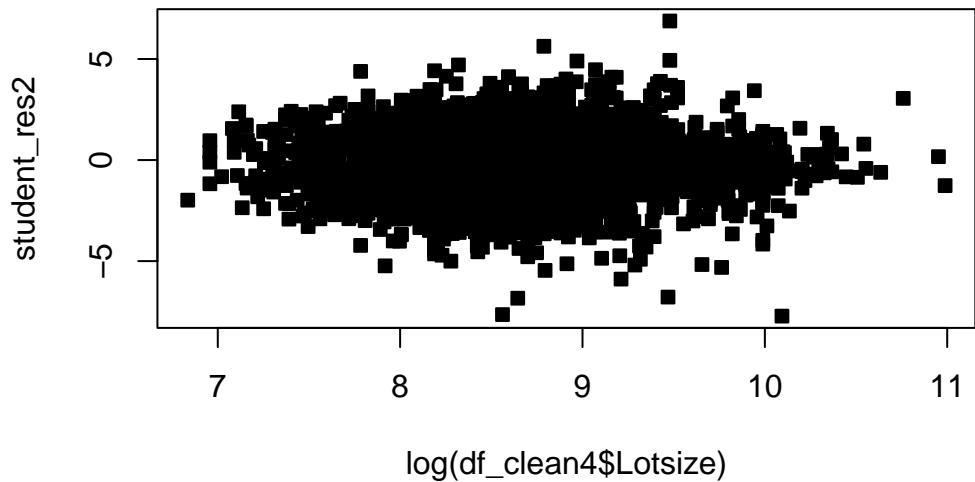
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



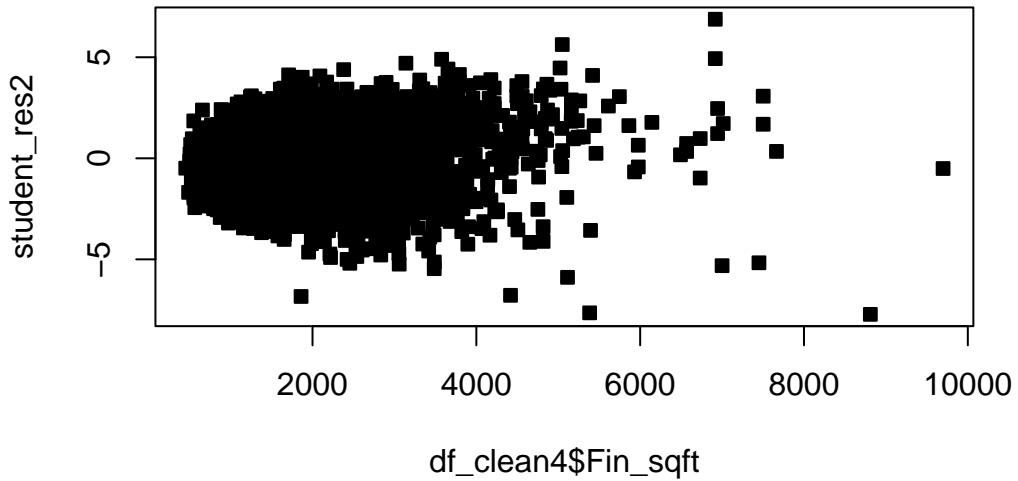
```
plot(df_clean4$Sale_date ,student_res2,pch=22,bg=1)
```



```
plot(log(df_clean4$Lotsize) ,student_res2,pch=22, bg=1)
```



```
plot(df_clean4$Fin_sqft ,student_res2,pch=22, bg=1)
```



```
# plot(df_clean4$Lotsize ,student_res2,pch=22,bg=1,xlim=c(0,70000))
# abline(h=0)

# df_clean4$d_3=df_clean4$District==3
# df_clean4$d_3or14=mapply('||',df_clean4$District==3,df_clean4$District==14)
model2=lm(sqrt(Sale_price)~District + Extwall + Stories + Year_Built + Fin_sqft
          Fbath + Sale_date ,df_clean4)
# model2=lm(Sale_price^(0.4)~.,df_clean3)

summ2=summary(model2); summ2
```

Call:  
`lm(formula = sqrt(Sale_price) ~ District + Extwall + Stories +
 Year_Built + Fin_sqft + Units + Bdrms + Fbath + Sale_date,
 data = df_clean4)`

Residuals:

Min	1Q	Median	3Q	Max
-----	----	--------	----	-----

-552.23 -37.27 6.58 42.12 481.52

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1.005e+03	5.184e+01	-19.385	< 2e-16 ***
District	3.749e+00	1.150e-01	32.598	< 2e-16 ***
ExtwallBlock	-5.282e+00	6.163e+00	-0.857	0.391428
ExtwallBrick	1.209e+01	1.205e+00	10.035	< 2e-16 ***
ExtwallFiber-Cement	1.379e+01	6.216e+00	2.219	0.026525 *
ExtwallFrame	-9.325e+00	1.630e+00	-5.722	1.06e-08 ***
ExtwallMasonry / Frame	9.131e+00	2.850e+00	3.204	0.001358 **
ExtwallPrem Wood	1.819e+01	9.375e+00	1.940	0.052362 .
ExtwallStone	9.162e+00	2.546e+00	3.598	0.000321 ***
ExtwallStucco	1.866e+01	3.579e+00	5.213	1.87e-07 ***
Stories1	5.433e+01	1.710e+01	3.178	0.001487 **
Stories1.5	6.722e+01	1.708e+01	3.937	8.29e-05 ***
Stories2	7.451e+01	1.702e+01	4.379	1.20e-05 ***
Year_Built	4.088e-01	2.196e-02	18.617	< 2e-16 ***
Fin_sqft	1.041e-01	1.531e-03	67.975	< 2e-16 ***
Units1	1.241e+02	1.224e+01	10.138	< 2e-16 ***
Units2	1.628e+01	1.225e+01	1.329	0.183906
Units3	-2.981e+01	1.318e+01	-2.262	0.023709 *
Bdrms0	1.556e+02	3.085e+01	5.043	4.61e-07 ***
Bdrms1	1.349e+02	1.680e+01	8.026	1.05e-15 ***
Bdrms2	1.460e+02	1.500e+01	9.731	< 2e-16 ***
Bdrms3	1.495e+02	1.491e+01	10.026	< 2e-16 ***
Bdrms4	1.295e+02	1.485e+01	8.717	< 2e-16 ***
Bdrms5	1.262e+02	1.485e+01	8.503	< 2e-16 ***
Bdrms6	1.041e+02	1.487e+01	6.998	2.66e-12 ***
Bdrms7	7.311e+01	1.586e+01	4.610	4.05e-06 ***
Bdrms8	1.010e+02	1.668e+01	6.052	1.45e-09 ***
Fbath0	-6.371e+01	2.270e+01	-2.807	0.005010 **
Fbath1	-4.003e+01	1.582e+01	-2.531	0.011389 *
Fbath2	-1.436e+01	1.571e+01	-0.914	0.360934
Fbath3	3.044e+01	1.561e+01	1.950	0.051242 .
Fbath4	6.273e+01	1.675e+01	3.746	0.000180 ***
Sale_date	6.220e-03	4.347e-04	14.310	< 2e-16 ***

---

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 73.19 on 24410 degrees of freedom

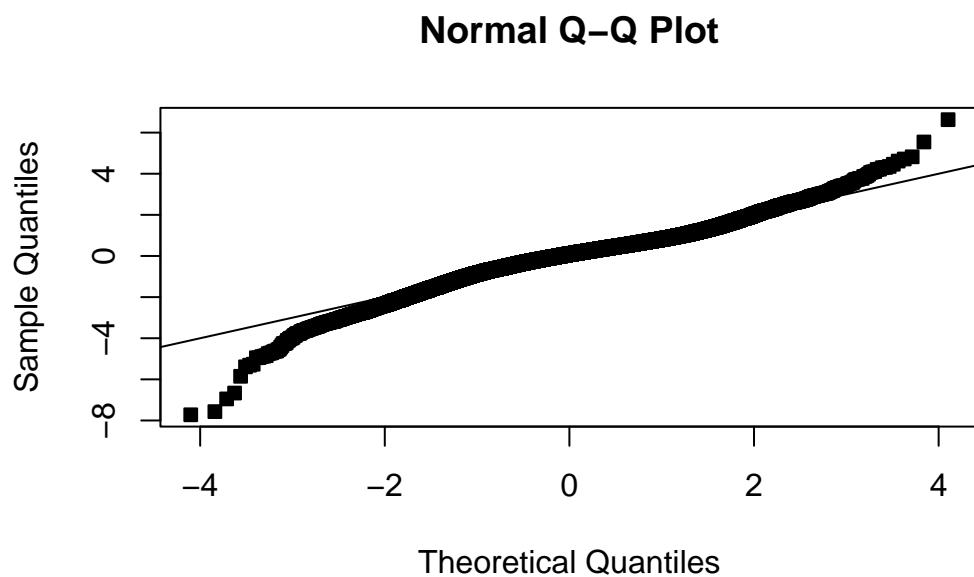
Multiple R-squared: 0.442, Adjusted R-squared: 0.4413

F-statistic: 604.2 on 32 and 24410 DF, p-value: < 2.2e-16

```
summ2$adj.r.squared
```

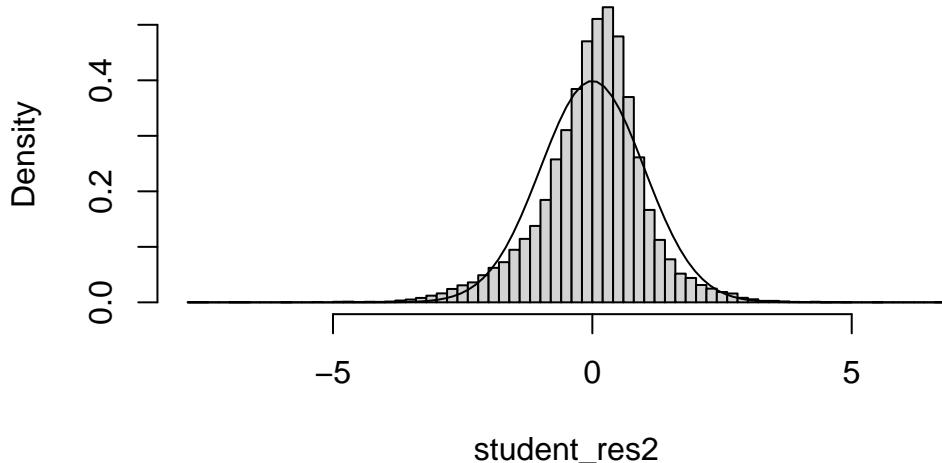
```
[1] 0.4412601
```

```
student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)
```



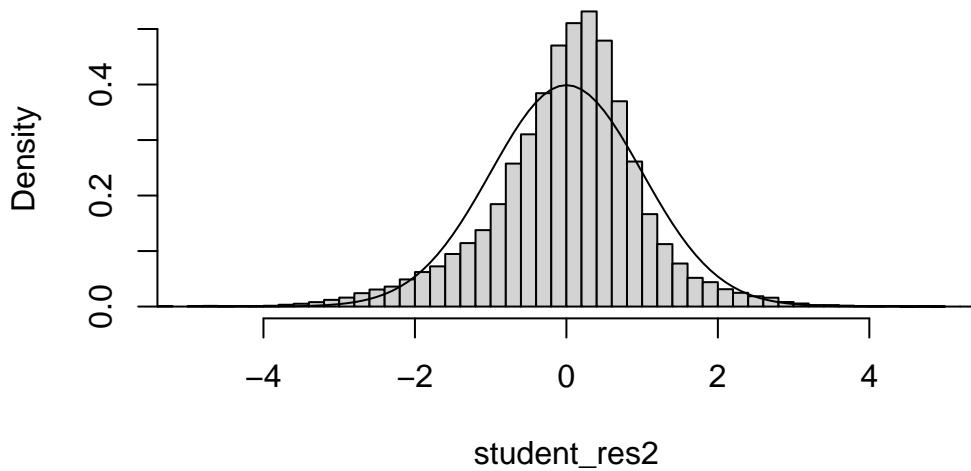
```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

### Histogram of student\_res2

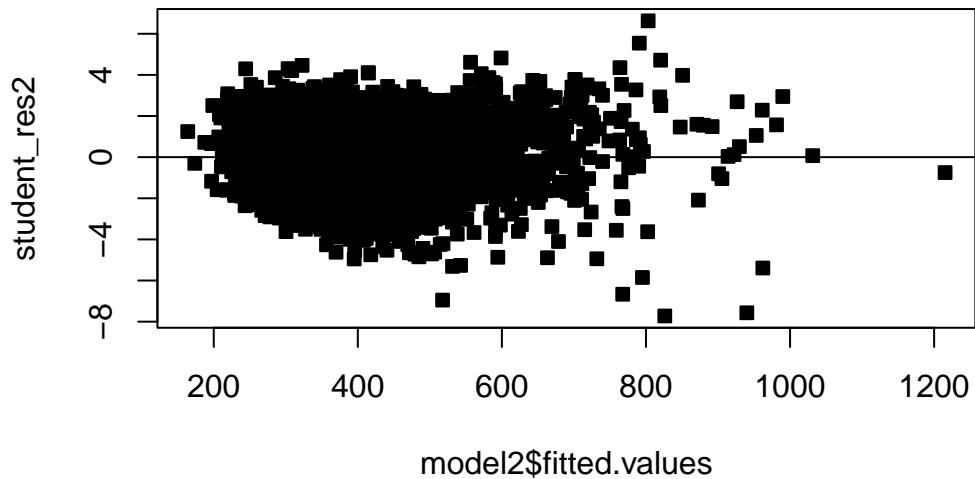


```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```

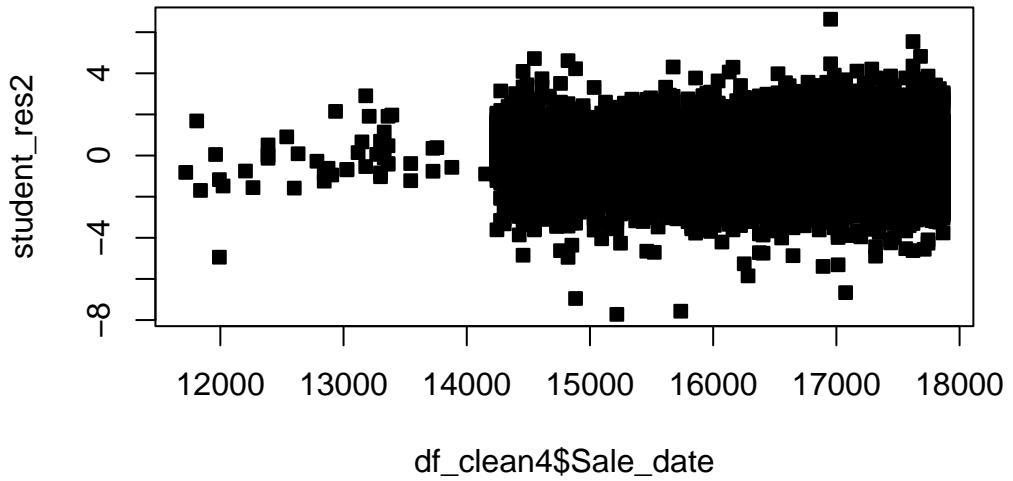
### Histogram of student\_res2



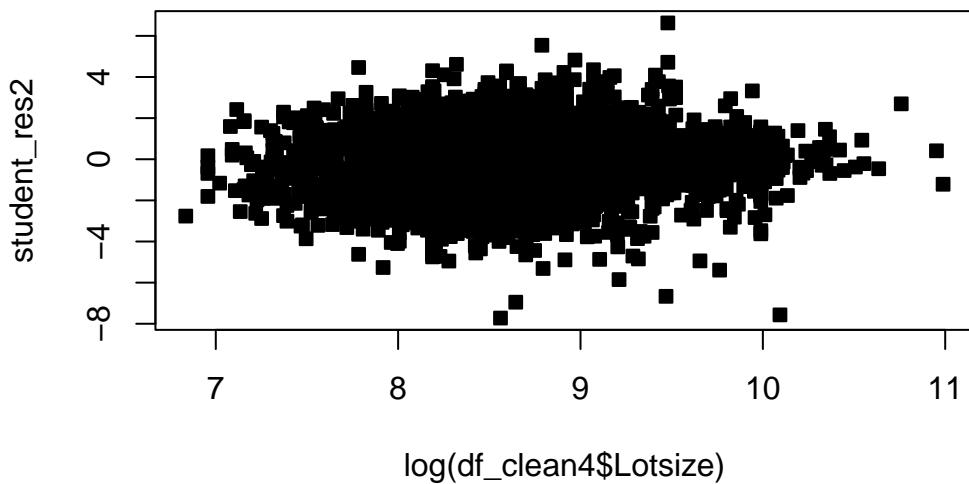
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



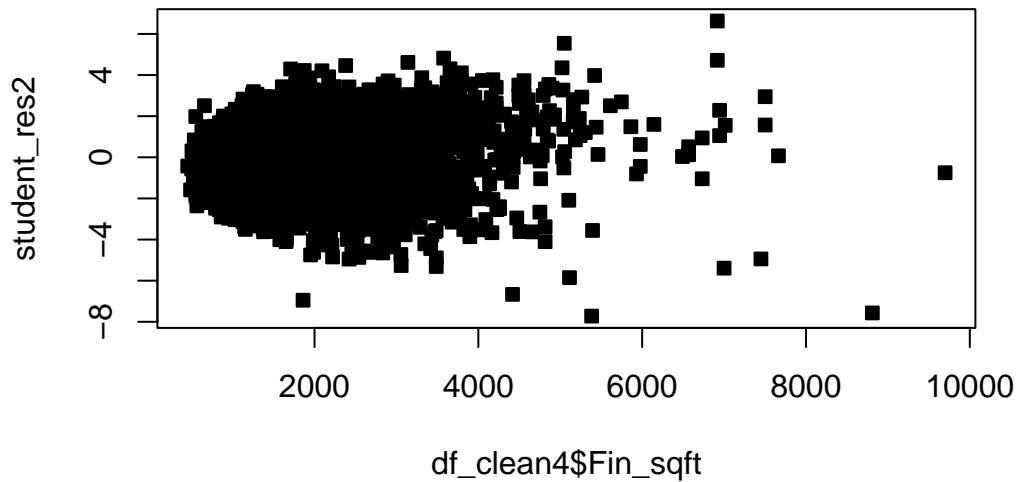
```
plot(df_clean4$Sale_date ,student_res2,pch=22,bg=1)
```



```
plot(log(df_clean4$Lotsize) ,student_res2,pch=22, bg=1)
```

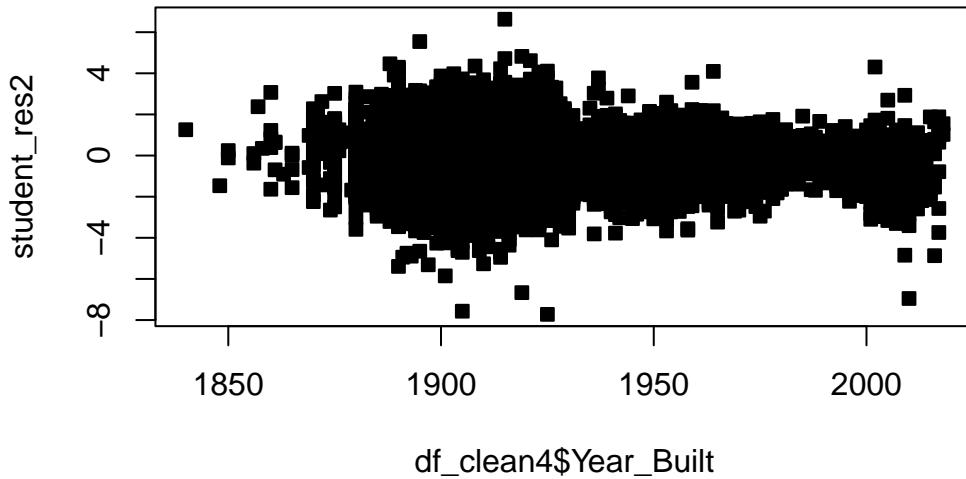


```
plot(df_clean4$Fin_sqft ,student_res2,pch=22,bg=1)
```



df\_clean4\$Fin\_sqft

```
plot(df_clean4$Year_Built ,student_res2,pch=22,bg=1)
```



```
# abline(h=0)

# df_clean4$d_3=df_clean4$District==3
# df_clean4$d_3or14=mapply('||',df_clean4$District==3,df_clean4$District==14)
model2=lm(sqrt(Sale_price)~District + Extwall + Stories + sqrt(Year_Built) + Fin
          Fbath + Sale_date ,df_clean4)
# model2=lm(Sale_price^(0.4)~,df_clean3)

summ2=summary(model2); summ2
```

Call:

```
lm(formula = sqrt(Sale_price) ~ District + Extwall + Stories +
    sqrt(Year_Built) + Fin_sqft + Units + Bdrms + Fbath + Sale_date,
    data = df_clean4)
```

Residuals:

Min	1Q	Median	3Q	Max
-----	----	--------	----	-----

-552.29 -37.29 6.60 42.10 481.44

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1.801e+03	9.029e+01	-19.944	< 2e-16 ***
District	3.749e+00	1.150e-01	32.601	< 2e-16 ***
ExtwallBlock	-5.304e+00	6.163e+00	-0.861	0.389455
ExtwallBrick	1.207e+01	1.205e+00	10.011	< 2e-16 ***
ExtwallFiber-Cement	1.388e+01	6.215e+00	2.233	0.025572 *
ExtwallFrame	-9.313e+00	1.630e+00	-5.715	1.11e-08 ***
ExtwallMasonry / Frame	9.091e+00	2.850e+00	3.190	0.001426 **
ExtwallPrem Wood	1.822e+01	9.375e+00	1.943	0.052001 .
ExtwallStone	9.123e+00	2.546e+00	3.583	0.000341 ***
ExtwallStucco	1.865e+01	3.579e+00	5.210	1.90e-07 ***
Stories1	5.427e+01	1.710e+01	3.174	0.001506 **
Stories1.5	6.718e+01	1.708e+01	3.934	8.38e-05 ***
Stories2	7.446e+01	1.702e+01	4.376	1.21e-05 ***
sqrt(Year_Built)	3.607e+01	1.934e+00	18.656	< 2e-16 ***
Fin_sqft	1.041e-01	1.531e-03	67.988	< 2e-16 ***
Units1	1.241e+02	1.224e+01	10.137	< 2e-16 ***
Units2	1.625e+01	1.225e+01	1.326	0.184694
Units3	-2.983e+01	1.318e+01	-2.263	0.023639 *
Bdrms0	1.556e+02	3.085e+01	5.045	4.57e-07 ***
Bdrms1	1.349e+02	1.680e+01	8.030	1.02e-15 ***
Bdrms2	1.460e+02	1.500e+01	9.732	< 2e-16 ***
Bdrms3	1.495e+02	1.491e+01	10.027	< 2e-16 ***
Bdrms4	1.295e+02	1.485e+01	8.719	< 2e-16 ***
Bdrms5	1.263e+02	1.485e+01	8.504	< 2e-16 ***
Bdrms6	1.041e+02	1.487e+01	6.998	2.66e-12 ***
Bdrms7	7.312e+01	1.586e+01	4.610	4.04e-06 ***
Bdrms8	1.010e+02	1.668e+01	6.052	1.45e-09 ***
Fbath0	-6.361e+01	2.270e+01	-2.802	0.005078 **
Fbath1	-4.000e+01	1.582e+01	-2.529	0.011446 *
Fbath2	-1.432e+01	1.571e+01	-0.911	0.362183
Fbath3	3.048e+01	1.561e+01	1.952	0.050931 .
Fbath4	6.277e+01	1.675e+01	3.748	0.000179 ***
Sale_date	6.219e-03	4.346e-04	14.309	< 2e-16 ***
---				

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 73.19 on 24410 degrees of freedom

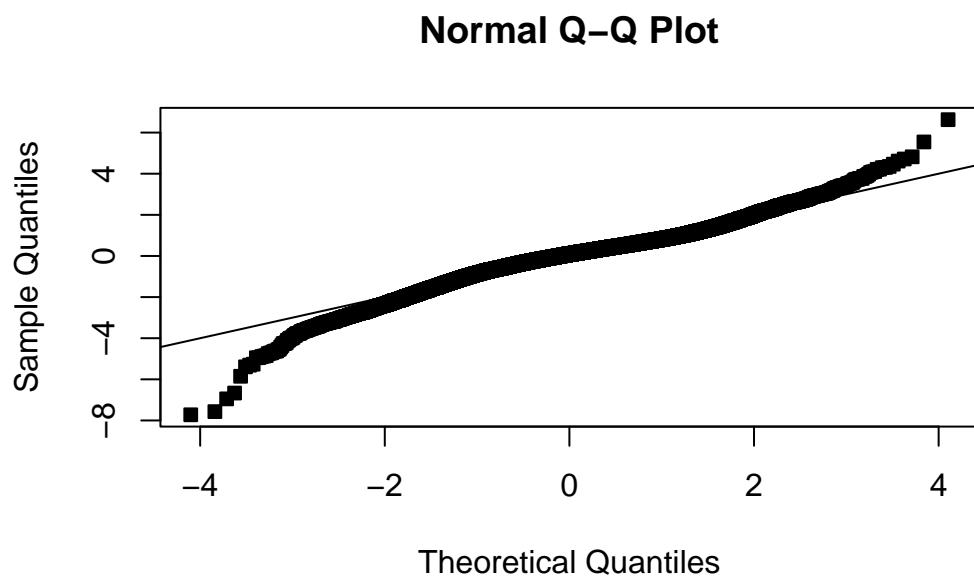
Multiple R-squared: 0.442, Adjusted R-squared: 0.4413

F-statistic: 604.3 on 32 and 24410 DF, p-value: < 2.2e-16

```
summ2$adj.r.squared
```

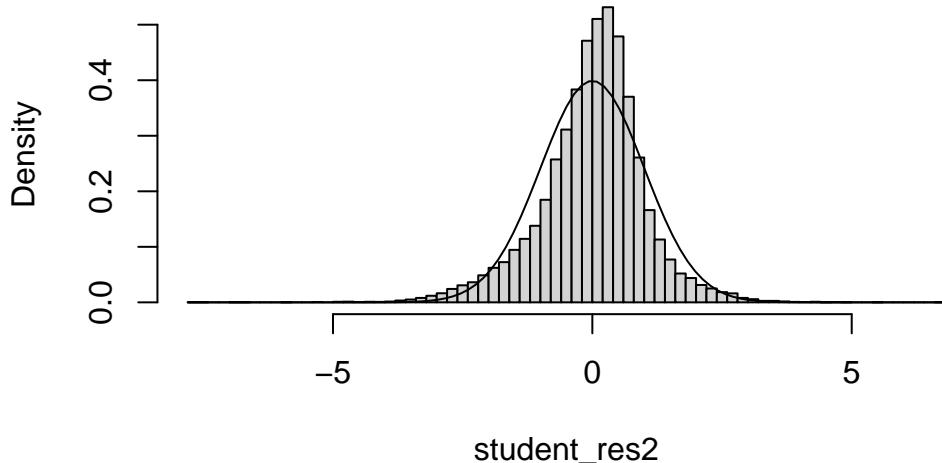
```
[1] 0.4412929
```

```
student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)
```



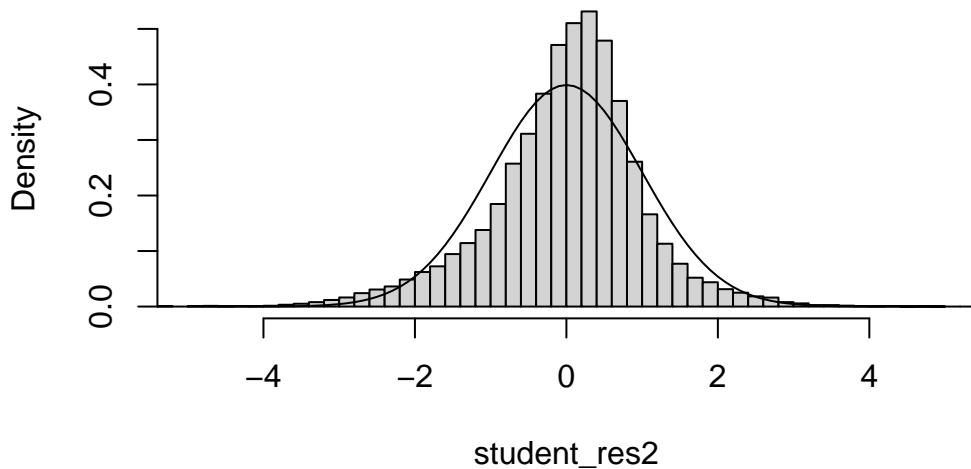
```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

### Histogram of student\_res2

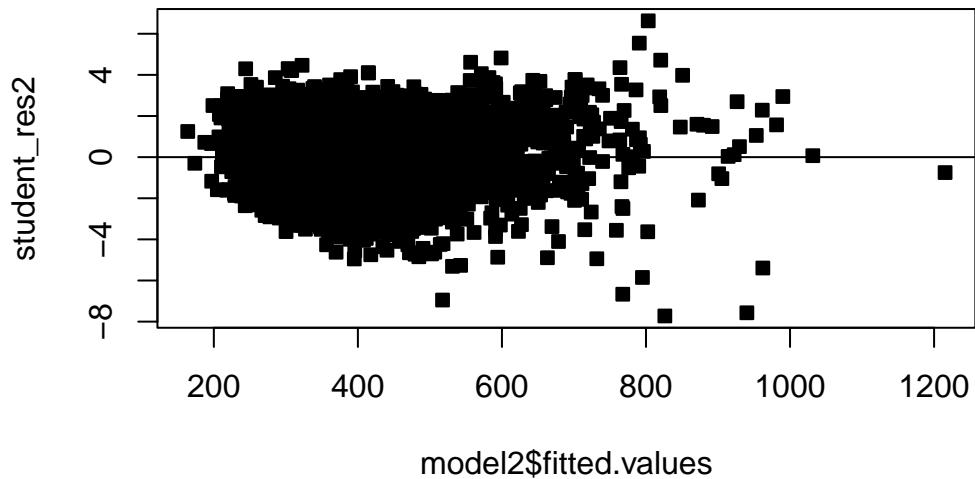


```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```

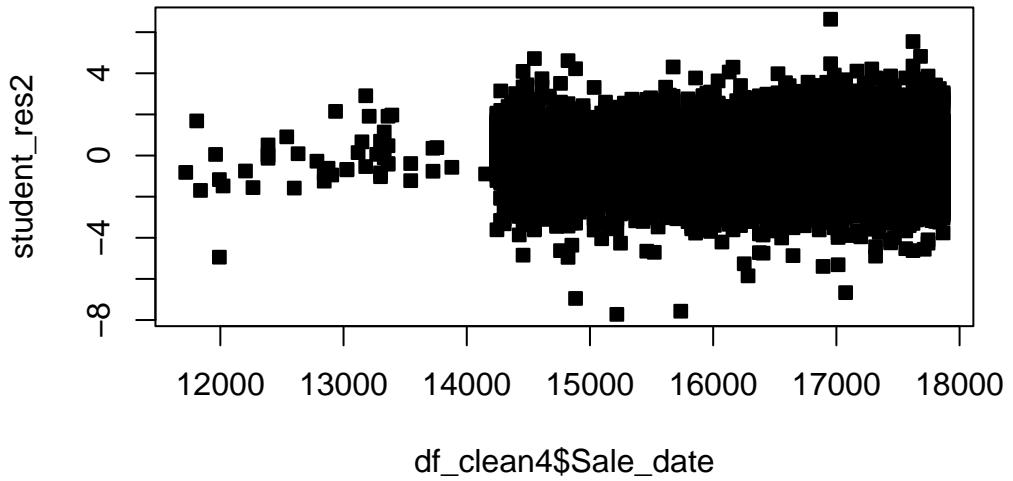
### Histogram of student\_res2



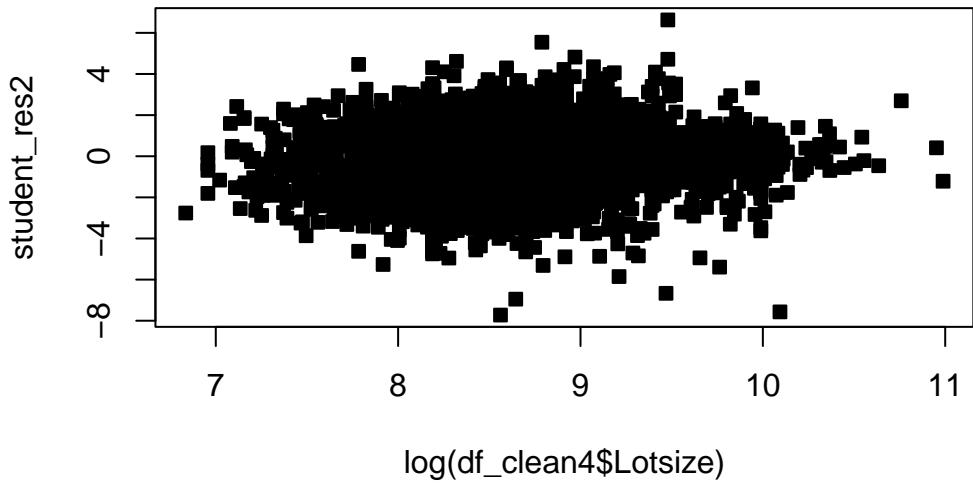
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



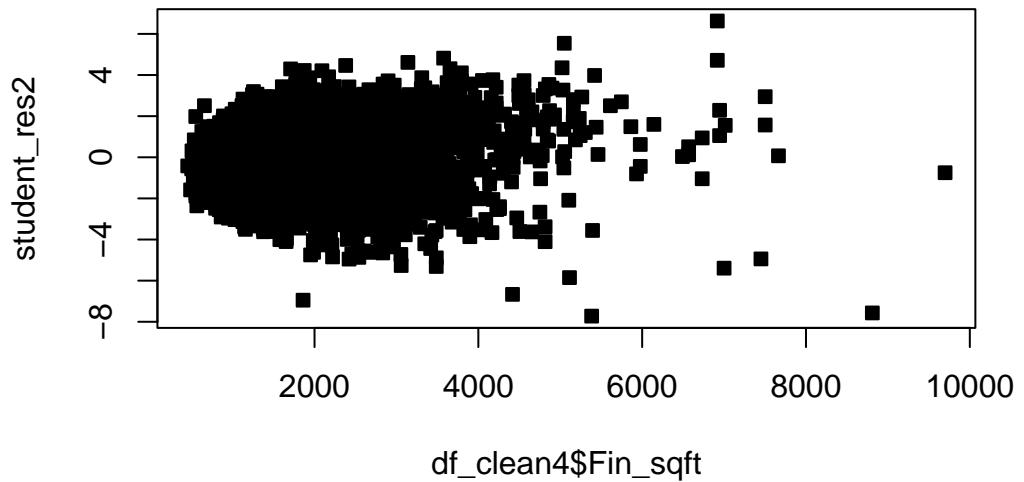
```
plot(df_clean4$Sale_date ,student_res2,pch=22,bg=1)
```



```
plot(log(df_clean4$Lotsize) ,student_res2,pch=22, bg=1)
```

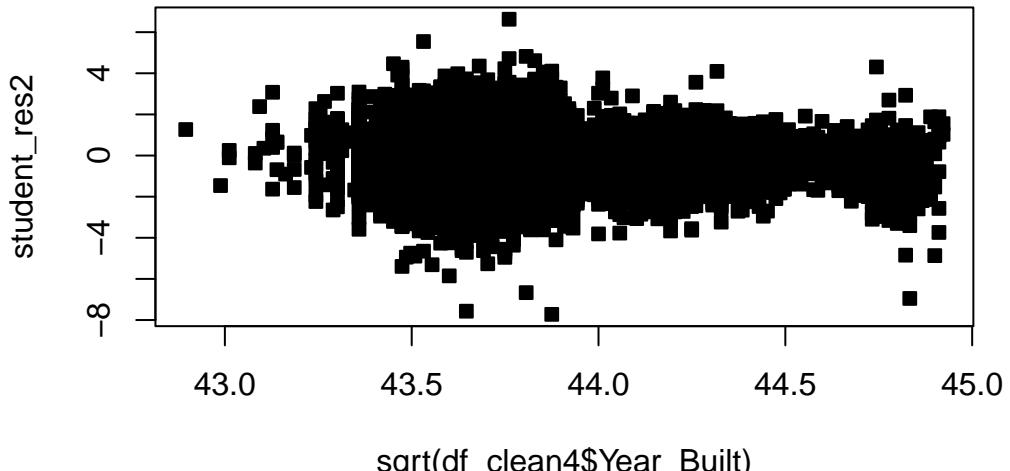


```
plot(df_clean4$Fin_sqft ,student_res2,pch=22,bg=1)
```



df\_clean4\$Fin\_sqft

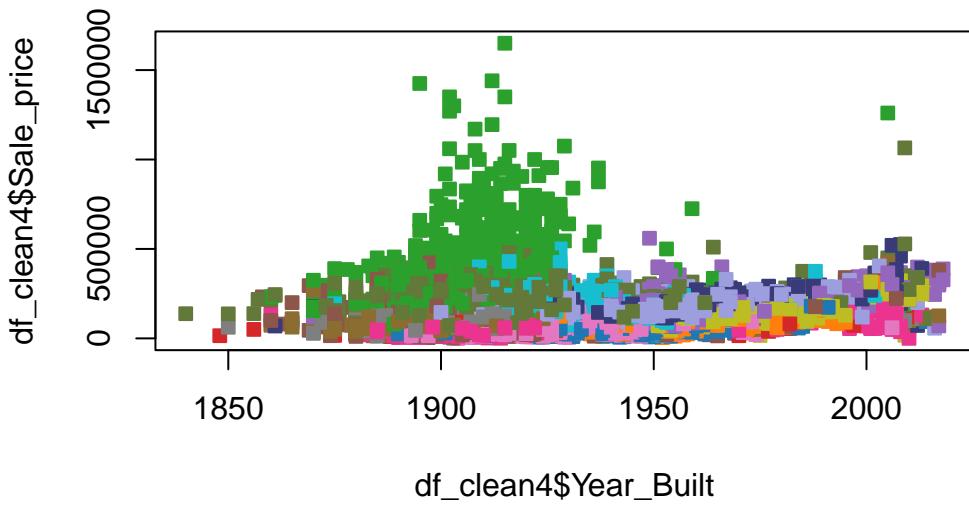
```
plot(sqrt(df_clean4$Year_Built) ,student_res2,pch=22,bg=1)
```



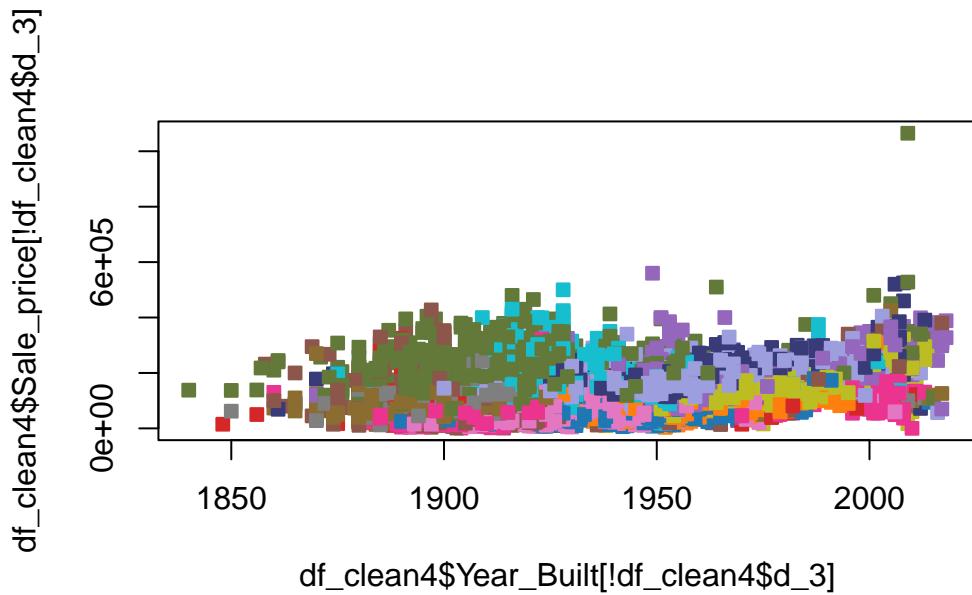
```
# abline(h=0)

custom_palette <- c(
  "#1f77b4", "#ff7f0e", "#2ca02c", "#d62728",
  "#9467bd", "#8c564b", "#e377c2", "#7f7f7f",
  "#bcbd22", "#17becf", "#393b79",
  "#8c6d31", "#9c9ede", "#637939", "#eb348f"
)

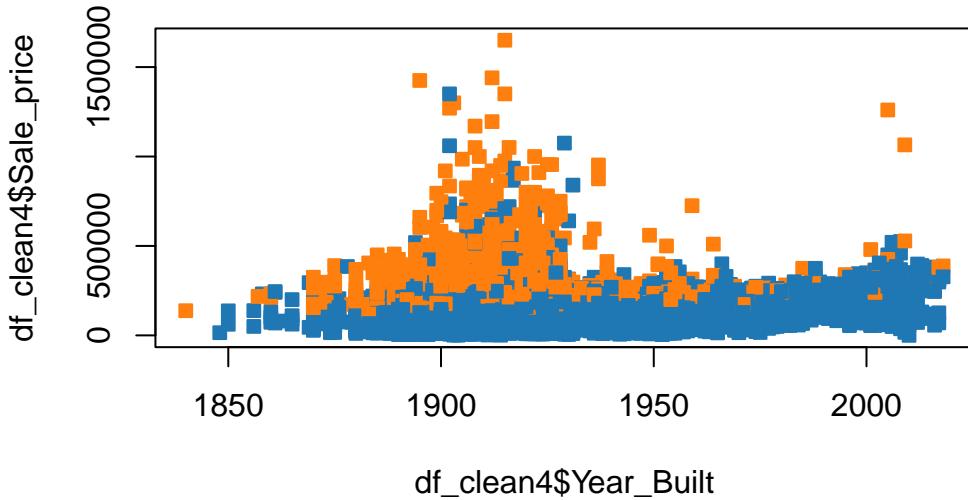
plot(df_clean4$Year_Built, df_clean4$Sale_price, pch=22, bg=custom_palette[df_clean4$District]
```



```
plot(df_clean4$Year_Built[!df_clean4$d_3] ,  
      df_clean4$Sale_price[!df_clean4$d_3] ,  
      pch=22 ,  
      bg=custom_palette[df_clean4$District[!df_clean4$d_3]] , col=custom_palette[df_clean4$Di
```



```
df_clean4$r_t=student_res2>quantile(student_res2,.9)
plot(df_clean4$Year_Built,df_clean4$Sale_price,
     pch=22,
     bg=custom_palette[df_clean4$r_t+1],
     col=custom_palette[df_clean4$r_t+1])
```



```

# plot(df_clean4$Year_Built,df_clean4$Sale_price,col=custom_palette[df_clean4$Extwall])
# for(colu in names(df_clean4)){
#   if (is.factor(df_clean2[,colu])){
#     print(colu)
#     print(table(df_clean2[,colu]))
#     df_clean2[,colu]=droplevels(df_clean2[,colu])
#   }
# }

# df_clean4$d_3or14=mapply('|||',df_clean4$District==3,df_clean4$District==14)
model2=lm(sqrt(Sale_price)~District +  Extwall +      Stories + Year_Built+  District*Year
          Fbath +      log(Lotsize) + Sale_date +District* log(Lotsize),df_clean4)

# model2=lm(Sale_price^(0.4)~,df_clean3)

```

```
summ2=summary(model2); summ2
```

Call:

```
lm(formula = sqrt(Sale_price) ~ District + Extwall + Stories +
  Year_Built + District * Year_Built + Fin_sqft + Units + Bdrms +
  Fbath + log(Lotsize) + Sale_date + District * log(Lotsize),
  data = df_clean4)
```

Residuals:

Min	1Q	Median	3Q	Max
-547.36	-35.61	5.89	41.47	474.14

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	1.396e+03	9.630e+01	14.494	< 2e-16 ***
District	-2.441e+02	9.158e+00	-26.656	< 2e-16 ***
ExtwallBlock	-6.108e+00	6.044e+00	-1.011	0.312259
ExtwallBrick	1.146e+01	1.183e+00	9.684	< 2e-16 ***
ExtwallFiber-Cement	2.442e+01	6.115e+00	3.993	6.55e-05 ***
ExtwallFrame	-1.069e+01	1.599e+00	-6.682	2.41e-11 ***
ExtwallMasonry / Frame	8.342e+00	2.797e+00	2.983	0.002858 **
ExtwallPrem Wood	1.492e+01	9.195e+00	1.622	0.104761
ExtwallStone	9.094e+00	2.497e+00	3.641	0.000272 ***
ExtwallStucco	1.537e+01	3.511e+00	4.378	1.20e-05 ***
Stories1	4.059e+01	1.680e+01	2.416	0.015681 *
Stories1.5	5.480e+01	1.677e+01	3.268	0.001084 **
Stories2	6.143e+01	1.670e+01	3.678	0.000236 ***
Year_Built	-9.488e-01	5.316e-02	-17.847	< 2e-16 ***
Fin_sqft	9.479e-02	1.565e-03	60.560	< 2e-16 ***
Units1	1.238e+02	1.200e+01	10.312	< 2e-16 ***
Units2	2.178e+01	1.201e+01	1.813	0.069845 .
Units3	-2.191e+01	1.293e+01	-1.695	0.090108 .
Bdrms0	1.493e+02	3.025e+01	4.936	8.03e-07 ***
Bdrms1	1.229e+02	1.648e+01	7.455	9.28e-14 ***
Bdrms2	1.344e+02	1.472e+01	9.133	< 2e-16 ***
Bdrms3	1.393e+02	1.462e+01	9.524	< 2e-16 ***
Bdrms4	1.213e+02	1.456e+01	8.327	< 2e-16 ***
Bdrms5	1.187e+02	1.456e+01	8.151	3.78e-16 ***
Bdrms6	9.863e+01	1.459e+01	6.762	1.39e-11 ***
Bdrms7	6.771e+01	1.555e+01	4.353	1.35e-05 ***

```

Bdrms8          9.538e+01  1.636e+01  5.829 5.65e-09 ***
Fbath0         -6.106e+01  2.227e+01 -2.742 0.006118 **
Fbath1         -3.703e+01  1.553e+01 -2.385 0.017096 *
Fbath2         -1.015e+01  1.543e+01 -0.658 0.510580
Fbath3          3.187e+01  1.532e+01  2.080 0.037538 *
Fbath4          6.184e+01  1.643e+01  3.764 0.000168 ***
log(Lotsize)    3.120e+01  3.416e+00  9.133 < 2e-16 ***
Sale_date       5.995e-03  4.263e-04 14.064 < 2e-16 ***
District:Year_Built 1.315e-01  5.309e-03 24.762 < 2e-16 ***
District:log(Lotsize) -8.262e-01  3.469e-01 -2.382 0.017230 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

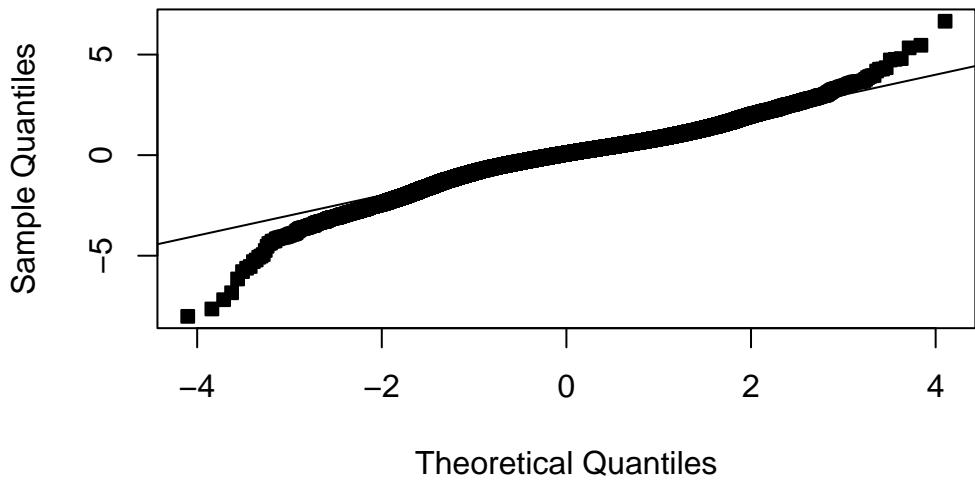
Residual standard error: 71.77 on 24407 degrees of freedom  
 Multiple R-squared: 0.4635, Adjusted R-squared: 0.4627  
 F-statistic: 602.4 on 35 and 24407 DF, p-value: < 2.2e-16

```
summ2$adj.r.squared
```

```
[1] 0.4626948
```

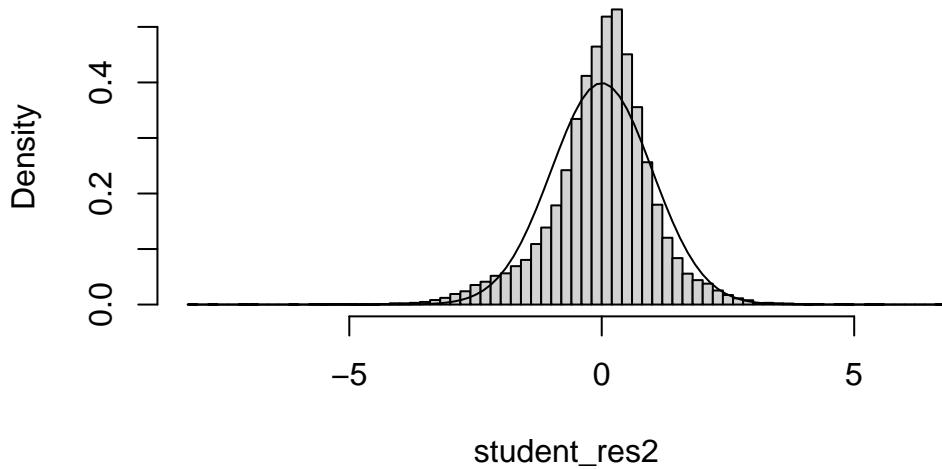
```
student_res2=rstudent(model2)
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)
```

### Normal Q-Q Plot

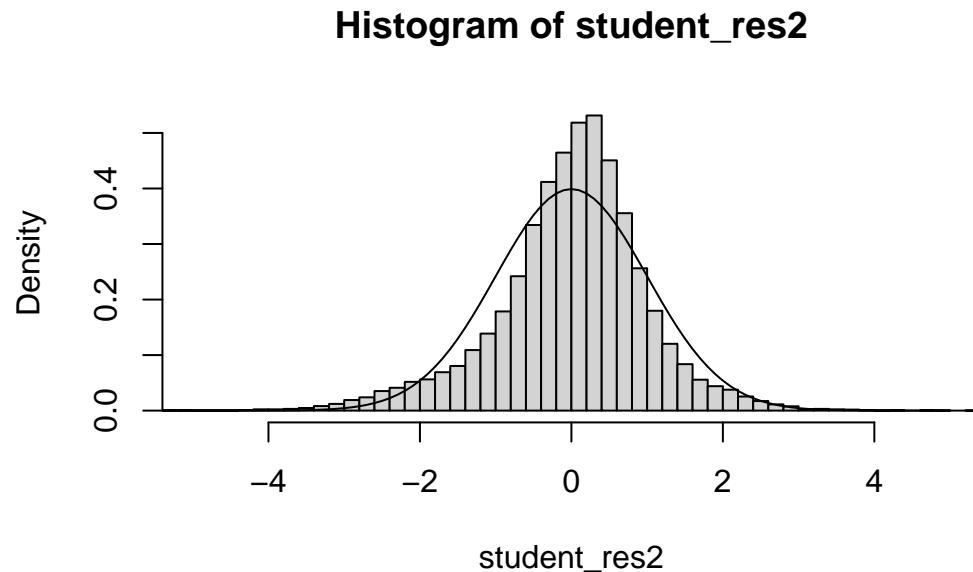


```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

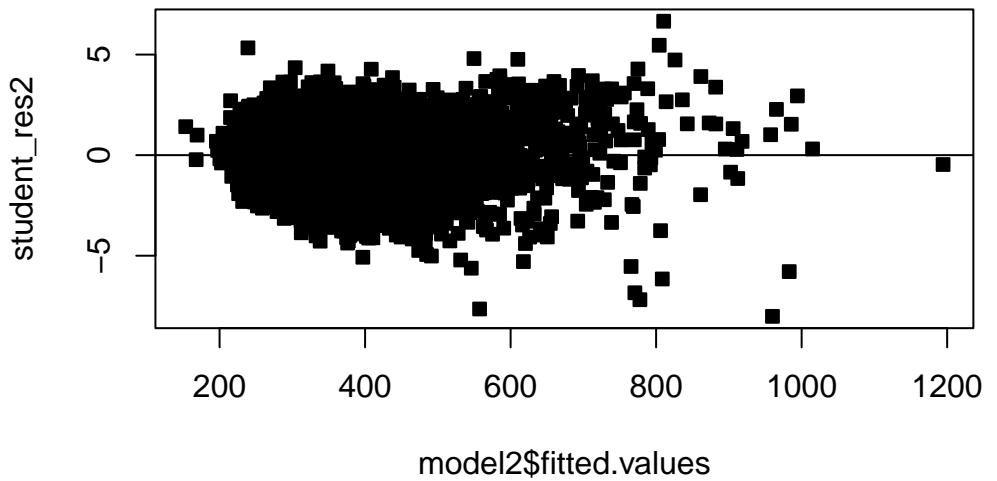
### Histogram of student\_res2



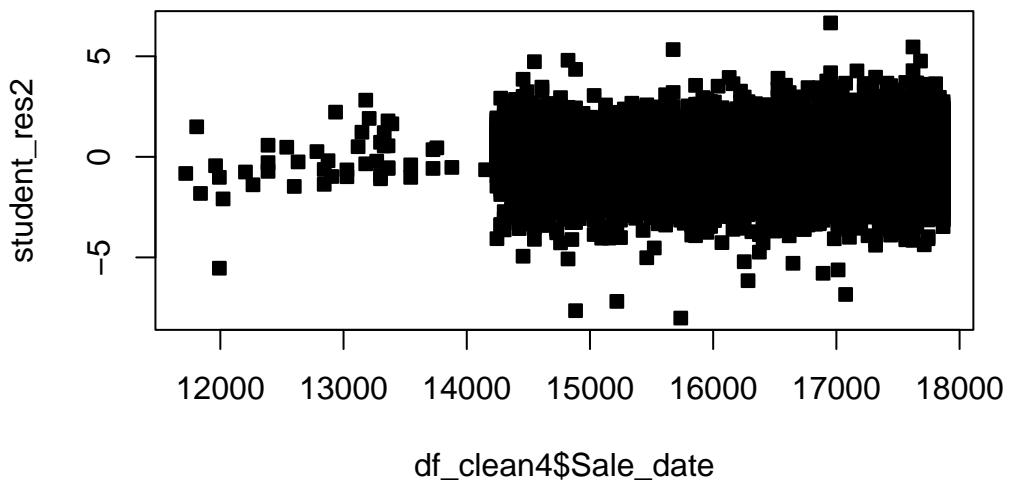
```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```



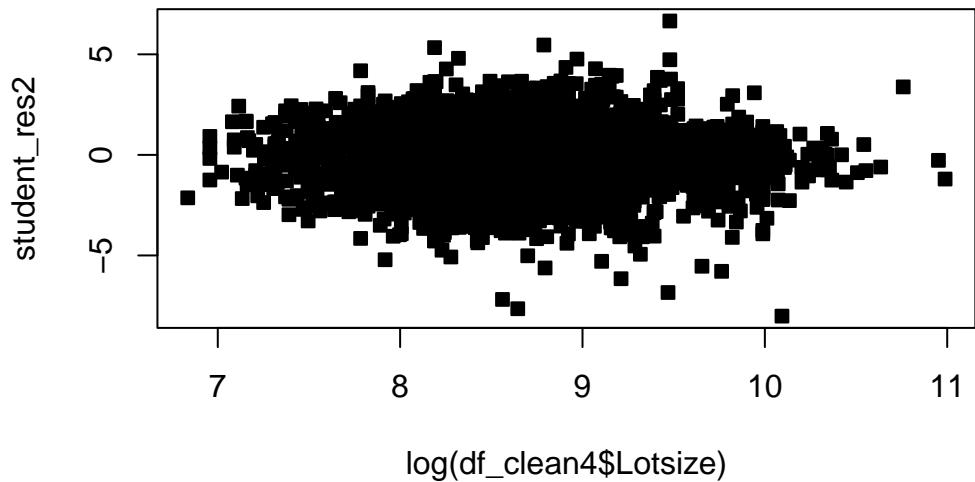
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



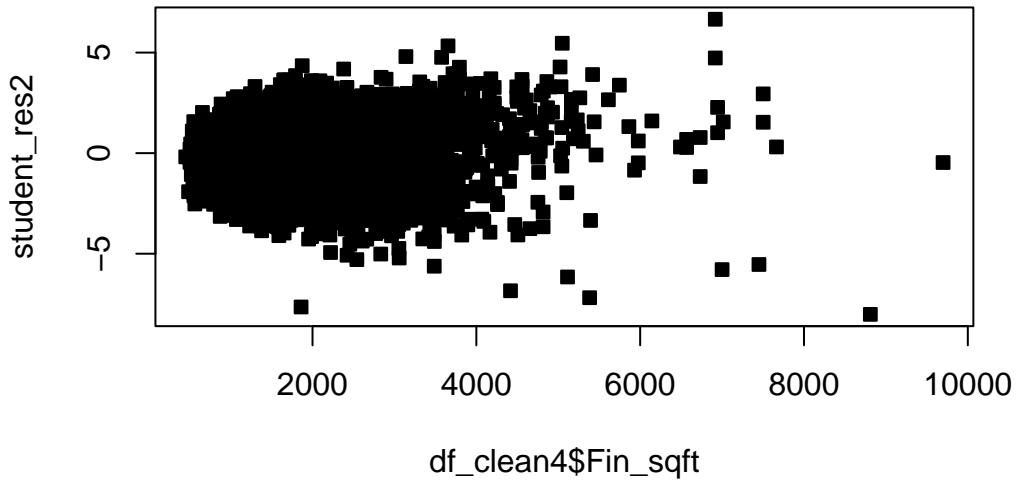
```
plot(df_clean4$Sale_date ,student_res2,pch=22,bg=1)
```



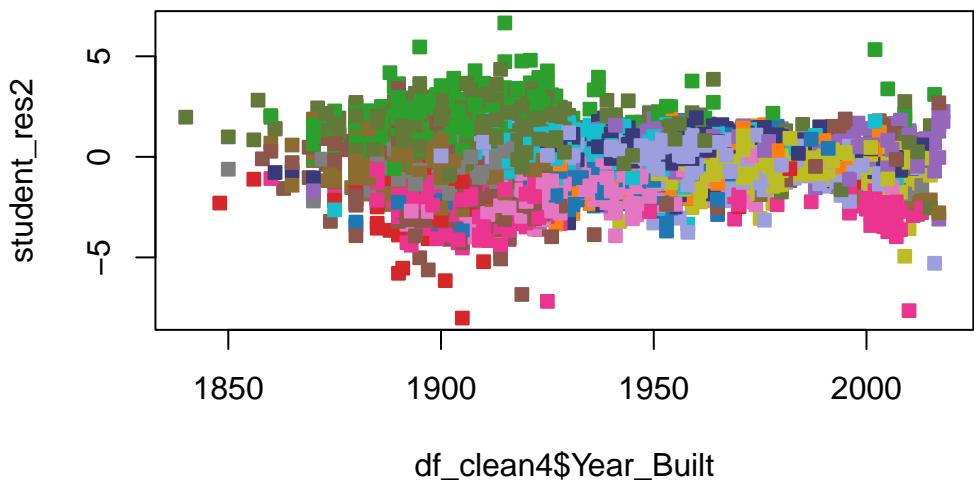
```
plot(log(df_clean4$Lotsize) ,student_res2,pch=22, bg=1)
```



```
plot(df_clean4$Fin_sqft ,student_res2,pch=22, bg=1)
```



```
plot(df_clean4$Year_Built ,student_res2,pch=22,bg=custom_palette[df_clean4$District],col=c
```



df\_clean4

	District	Extwall	Stories	Year_Built	Fin_sqft	Units	Bdrms	Fbath
1	7	Frame	2	1913	3476	>3	>8	1
2	3	Frame	2	1897	1992	>3	2	2
3	4	Frame	2	1907	2339	>3	0	1
4	4	Frame	2	1890	2329	>3	4	1
5	4	Stone	>2	1891	7450	2	7	>4
6	12	Frame	1.5	1906	2462	2	3	2
7	4	Frame	1.5	1890	2372	>3	2	2
8	11	Brick	1	1950	1149	1	3	1
9	1	Aluminum / Vinyl	1	1947	994	1	3	1
10	1	Stucco	2	1905	2938	>3	3	1
11	1	Brick	1	1951	1620	1	4	2
12	13	Brick	1	1956	986	1	3	1
13	3	Frame	2	1890	2360	>3	1	2
14	8	Aluminum / Vinyl	1	1903	1156	1	2	1
15	4	Frame	2	1895	3269	>3	6	1
16	15	Frame	2	1899	3380	>3	>8	1
17	4	Frame	2	1908	2775	>3	4	1
18	12	Frame	2	1889	2796	>3	0	2
19	12	Frame	2	1889	1930	>3	1	2
20	4	Frame	2	1913	2872	>3	3	2
21	13	Brick	2	1949	2430	>3	6	1
22	4	Frame	2	1890	3243	>3	8	1
23	6	Frame	2	1905	3346	>3	4	1
24	12	Frame	2	1900	2679	>3	7	2
25	12	Frame	2	1880	3459	>3	8	1
26	3	Stucco	2	1895	3208	>3	5	1
27	6	Block	2	1956	1920	>3	4	1
28	3	Stucco	2	1916	2800	>3	2	1
29	6	Brick	2	1908	2646	2	6	2
30	4	Frame	2	1908	3466	2	6	4
31	7	Frame	2	1913	3476	>3	>8	1
32	7	Frame	1	1932	761	1	3	1
33	6	Frame	2	1905	3346	>3	4	1
34	15	Frame	2	1899	4225	>3	>8	1
35	4	Frame	2	1908	3380	>3	4	1
36	4	Aluminum / Vinyl	2	1901	2898	2	6	4
37	8	Aluminum / Vinyl	2	1903	2880	>3	6	1
38	8	Aluminum / Vinyl	1.5	1892	2091	>3	4	1
39	4	Frame	2	1901	2770	>3	6	1

40	7	Frame	2	1913	2696	>3	4	1
41	12	Frame	2	1889	2796	>3	7	2
42	6	Block	2	1956	1920	>3	4	1
43	9	Aluminum / Vinyl	2	2007	2237	1	4	2
44	8	Aluminum / Vinyl	2	1903	3552	>3	7	1
45	8	Frame	2	1903	3552	2	7	4
46	2	Frame	1	1962	1169	1	3	2
47	1	Stone	1	1938	1188	1	2	1
48	1	Aluminum / Vinyl	1	1951	1054	1	3	1
49	1	Aluminum / Vinyl	1	1950	998	1	3	1
50	1	Aluminum / Vinyl	1	1951	988	1	3	1
51	1	Aluminum / Vinyl	2	2004	1470	1	3	2
52	1	Masonry / Frame	2	1949	2460	2	5	2
53	1	Brick	1.5	1900	4507	1	5	1
54	2	Brick	1	1954	1456	1	3	1
55	2	Aluminum / Vinyl	1.5	1962	1875	2	5	2
56	2	Aluminum / Vinyl	1	1966	1379	1	3	1
57	2	Brick	1	1962	1361	1	3	1
58	2	Brick	1	1964	1334	1	3	1
59	2	Brick	1	1962	1334	1	3	1
60	2	Brick	1	1959	1288	1	3	2
61	2	Frame	1	1970	1120	1	4	1
62	2	Frame	1	1955	864	1	3	1
63	2	Aluminum / Vinyl	1	1957	864	1	3	1
64	3	Stucco	>2	1894	3255	1	3	2
65	3	Frame	1	1910	977	1	3	1
66	3	Aluminum / Vinyl	2	1912	2152	2	4	2
67	3	Aluminum / Vinyl	1.5	1908	1656	2	4	2
68	3	Aluminum / Vinyl	1	1909	1359	1	3	2
69	3	Aluminum / Vinyl	2	1921	1248	1	3	1
70	5	Brick	1	1950	1338	1	3	1
71	5	Brick	1	1949	1284	1	3	1
72	5	Brick	1	1950	1201	1	2	1
73	5	Aluminum / Vinyl	1	1956	1176	1	4	2
74	5	Aluminum / Vinyl	1	1947	1165	1	4	1
75	5	Aluminum / Vinyl	1	1953	1144	1	3	1
76	5	Stone	1	1950	989	1	2	1
77	5	Masonry / Frame	2	1957	2234	2	6	2
78	5	Aluminum / Vinyl	1.5	1955	1995	2	5	2
79	5	Brick	1	1958	1110	1	3	1
80	6	Frame	1	1922	1029	1	2	1
81	7	Aluminum / Vinyl	1.5	1910	1729	2	6	2
82	8	Frame	2	1913	1364	1	3	1

83	8	Frame	1	1901	1256	1	3	1
85	9	Frame	2	1965	1591	1	4	1
86	9	Aluminum / Vinyl	2	1980	1455	1	3	1
87	10	Brick	1.5	1952	1435	1	2	1
88	10	Brick	1.5	1936	1276	1	2	1
89	10	Aluminum / Vinyl	1	1948	1012	1	3	1
90	10	Brick	2	1940	1556	1	4	1
91	10	Aluminum / Vinyl	1.5	1924	1697	2	3	2
92	10	Brick	1	1928	1853	1	4	1
93	10	Aluminum / Vinyl	1	1927	1025	1	3	1
94	10	Aluminum / Vinyl	2	1919	1452	1	4	1
95	10	Aluminum / Vinyl	1	1924	916	1	2	2
96	11	Brick	1.5	1941	1203	1	2	1
97	11	Aluminum / Vinyl	1	1938	1157	1	4	1
98	11	Aluminum / Vinyl	2	1992	2159	1	3	2
99	11	Brick	1.5	1937	1859	2	3	2
100	11	Brick	1	1932	1369	1	3	1
101	11	Aluminum / Vinyl	1	1961	1336	1	3	1
102	11	Aluminum / Vinyl	1	1979	1321	1	3	2
103	11	Brick	1	1958	1119	1	3	2
104	11	Brick	1	1953	1048	1	2	1
105	11	Aluminum / Vinyl	1	1949	870	1	2	1
106	13	Brick	1	1950	1188	1	3	2
107	13	Aluminum / Vinyl	1.5	1946	1122	1	2	1
108	13	Aluminum / Vinyl	1	1943	971	1	3	1
109	13	Brick	1	1966	1957	1	3	1
110	13	Brick	1	1967	1414	1	3	1
111	13	Aluminum / Vinyl	1	1959	1175	1	3	1
112	13	Brick	1	1964	1122	1	3	1
113	14	Aluminum / Vinyl	2	1954	1078	1	2	1
114	14	Aluminum / Vinyl	2	1910	2128	2	4	2
115	14	Aluminum / Vinyl	1	1924	973	1	3	1
117	14	Frame	1.5	1900	1340	1	3	2
118	14	Block	1.5	1920	1326	1	2	1
119	1	Brick	1.5	1938	1184	1	2	1
120	1	Aluminum / Vinyl	2	1929	2429	2	6	2
121	1	Brick	2	1943	1786	2	4	2
122	1	Aluminum / Vinyl	1	1923	1431	1	3	1
123	2	Brick	1	1955	1074	1	3	1
124	2	Aluminum / Vinyl	1	1956	1034	1	3	1
125	2	Aluminum / Vinyl	2	1959	1428	1	3	1
126	2	Aluminum / Vinyl	2	1960	2070	2	6	2
127	2	Brick	1	1955	1115	1	2	1

128	2	Aluminum / Vinyl	2	1970	2785	2	6	2
129	3	Brick	2	1946	2684	2	5	2
130	3	Frame	2	1887	3352	2	5	2
131	3	Brick	2	1907	2849	1	5	3
132	5	Brick	1.5	1952	1568	1	3	2
133	5	Stone	1	1947	1425	1	4	1
134	5	Stone	1	1952	1408	1	3	1
135	5	Aluminum / Vinyl	1	1951	1036	1	3	1
136	5	Aluminum / Vinyl	1	1949	978	1	4	1
137	5	Aluminum / Vinyl	2	1960	1686	1	3	1
138	5	Frame	2	1951	1540	1	3	1
139	5	Brick	1	1954	1282	1	3	1
140	5	Aluminum / Vinyl	1	1962	1268	1	3	1
141	5	Aluminum / Vinyl	1	1956	1132	1	3	1
142	5	Aluminum / Vinyl	1	1955	978	1	3	1
143	5	Masonry / Frame	2	1954	2498	3	5	3
144	6	Frame	2	1914	2425	2	6	2
145	6	Brick	2	1914	3087	2	5	2
146	6	Frame	1	1924	1696	1	4	1
147	7	Brick	1	1950	1598	1	4	2
148	7	Aluminum / Vinyl	1	1941	1272	1	3	1
149	7	Aluminum / Vinyl	1	1938	957	1	3	1
150	7	Frame	2	1920	2208	2	4	2
151	7	Brick	1	1960	1442	1	4	2
152	8	Aluminum / Vinyl	2	1921	2647	2	6	2
153	8	Brick	1	1927	1493	1	4	2
154	9	Brick	1	1958	1275	1	3	1
155	9	Aluminum / Vinyl	1	1936	1262	1	4	2
156	9	Aluminum / Vinyl	1	1972	1140	1	3	1
157	9	Aluminum / Vinyl	1	1976	906	1	3	1
158	9	Aluminum / Vinyl	1	1954	672	1	2	1
159	10	Aluminum / Vinyl	1	1940	1128	1	3	2
160	10	Brick	1.5	1936	1109	1	2	1
161	10	Aluminum / Vinyl	2	1988	2666	1	4	2
162	10	Frame	>2	1912	2600	1	4	2
163	10	Frame	1.5	1924	1665	2	3	2
164	10	Brick	1	1948	778	1	2	1
165	10	Brick	1	1926	1427	1	3	1
166	10	Stucco	1.5	1917	1398	1	3	1
167	11	Aluminum / Vinyl	1.5	1970	2032	1	5	1
168	11	Stone	1.5	1951	1940	1	3	2
169	11	Aluminum / Vinyl	1.5	1940	1197	1	3	1
170	11	Aluminum / Vinyl	1	1950	1176	1	3	1

171	11	Brick	1	1948	948	1	3	1
172	11	Aluminum / Vinyl	2	1953	1904	2	6	2
173	11	Aluminum / Vinyl	1	1943	1550	2	4	2
174	11	Brick	1	1954	1037	1	3	1
175	11	Aluminum / Vinyl	1	1928	1088	1	2	1
176	11	Brick	1.5	1937	1925	1	3	1
177	12	Aluminum / Vinyl	1	1919	1118	1	5	1
178	12	Aluminum / Vinyl	1	1921	1076	1	4	1
179	13	Aluminum / Vinyl	1	1947	1210	1	3	1
180	13	Aluminum / Vinyl	1	1940	1195	1	3	1
181	13	Brick	1	1955	1010	1	3	1
182	13	Aluminum / Vinyl	1	1939	1001	1	2	1
183	13	Aluminum / Vinyl	1	1979	1268	1	3	1
184	13	Brick	1	1967	1199	1	3	1
185	13	Aluminum / Vinyl	1	1966	1012	1	3	1
186	13	Aluminum / Vinyl	1	1953	880	1	2	1
187	13	Aluminum / Vinyl	1	1915	1424	1	3	0
188	13	Aluminum / Vinyl	1	1923	1238	1	4	1
189	14	Aluminum / Vinyl	1.5	1941	1346	1	4	1
190	14	Aluminum / Vinyl	2	1929	2695	2	4	2
191	14	Frame	2	1898	3148	1	4	3
192	14	Frame	1	1906	1896	1	4	2
193	14	Frame	2	1890	1636	1	4	2
194	14	Prem Wood	1	1920	1332	1	3	2
195	14	Fiber-Cement	1	1890	1274	1	3	2
196	14	Brick	1	1930	1196	1	3	1
197	15	Aluminum / Vinyl	2	1913	2502	2	6	2
199	15	Frame	1	1918	1434	1	3	1
200	15	Aluminum / Vinyl	1	1895	1362	1	4	1
201	1	Brick	1	1955	1259	1	4	1
202	1	Brick	2	1954	1940	2	4	2
203	1	Frame	1	1946	856	1	2	1
204	2	Brick	1	1956	1406	1	3	1
205	2	Stone	1	1955	1120	1	2	1
206	2	Aluminum / Vinyl	1	1957	951	1	3	1
207	2	Aluminum / Vinyl	2	1974	2484	2	6	2
208	3	Frame	2	1922	1852	1	3	1
209	3	Frame	1.5	1921	2101	1	4	2
210	3	Stucco	1	1915	1414	1	2	1
211	5	Brick	1.5	1953	2429	1	3	2
212	5	Brick	1	1951	1318	1	3	2
213	5	Brick	1.5	1949	1258	1	2	1
214	5	Aluminum / Vinyl	1	1950	1257	1	3	2

215	5 Aluminum / Vinyl	1	1952	934	1	3	1
216	5 Aluminum / Vinyl	1	1942	923	1	3	2
217	5 Aluminum / Vinyl	1	1956	784	1	2	1
218	5 Aluminum / Vinyl	2	1984	1686	1	3	2
219	5 Stone	2	1957	2146	2	6	2
220	5 Frame	2	1961	2092	2	6	2
221	5 Frame	1	1968	1500	1	3	1
222	5 Aluminum / Vinyl	1	1997	1262	1	3	1
223	5 Brick	1	1952	1239	1	3	1
224	5 Brick	1	1958	1232	1	3	1
225	5 Brick	1	1956	1223	1	3	1
226	5 Aluminum / Vinyl	1	1956	1154	1	3	1
227	5 Aluminum / Vinyl	1	1956	1077	1	3	1
228	5 Brick	1	1966	1059	1	3	1
229	5 Aluminum / Vinyl	1	1950	1036	1	3	1
230	5 Aluminum / Vinyl	1	1957	954	1	3	1
231	5 Frame	1	1948	833	1	2	1
232	5 Aluminum / Vinyl	2	1962	2484	2	6	2
233	5 Aluminum / Vinyl	2	1978	2451	2	6	2
234	6 Aluminum / Vinyl	2	1922	2086	2	4	2
235	6 Aluminum / Vinyl	1.5	1896	1728	2	4	2
236	6 Aluminum / Vinyl	1.5	1910	1468	2	4	2
237	6 Aluminum / Vinyl	1.5	1909	1740	1	3	2
238	6 Frame	1.5	1892	1366	1	3	1
239	6 Frame	1.5	1892	1366	1	3	1
240	6 Stone	1	1925	820	1	1	1
241	7 Masonry / Frame	2	1936	2780	2	4	2
242	7 Aluminum / Vinyl	1.5	1929	2082	2	4	2
243	7 Aluminum / Vinyl	1.5	1899	1452	2	4	1
244	7 Stone	1	1941	1118	1	2	1
245	7 Aluminum / Vinyl	1	1914	1515	1	5	1
246	8 Masonry / Frame	2	1912	2904	1	6	1
247	8 Aluminum / Vinyl	2	1883	2234	2	6	2
248	8 Aluminum / Vinyl	1.5	1904	1912	2	3	2
249	8 Aluminum / Vinyl	1	1916	1578	1	4	2
250	8 Aluminum / Vinyl	1.5	1912	1652	1	2	1
251	8 Aluminum / Vinyl	1	1910	1438	1	3	1
252	8 Aluminum / Vinyl	1	1886	1252	1	3	1
253	9 Aluminum / Vinyl	2	2008	2361	1	4	2
254	9 Aluminum / Vinyl	1	1971	1200	1	4	1
255	10 Aluminum / Vinyl	1	1950	1170	1	4	1
256	10 Aluminum / Vinyl	1.5	1930	1852	2	4	2
257	10 Brick	2	1950	1900	2	4	2

258	10	Aluminum / Vinyl	1	1926	1557	1	4	2
259	10	Frame	1	1919	1499	1	3	2
260	10	Aluminum / Vinyl	1	1925	1401	1	4	1
261	10	Frame	1	1930	1318	1	3	1
262	10	Aluminum / Vinyl	1	1927	1189	1	3	1
263	10	Aluminum / Vinyl	1	1926	1034	1	3	1
264	10	Aluminum / Vinyl	1	1940	864	1	2	1
265	11	Aluminum / Vinyl	1	1948	1188	1	3	1
266	11	Aluminum / Vinyl	1	1951	865	1	2	1
267	11	Stone	1	1948	1057	1	2	1
268	11	Frame	1	1953	998	1	3	1
269	11	Aluminum / Vinyl	1	1956	988	1	3	1
270	11	Brick	1	1950	869	1	2	1
271	11	Aluminum / Vinyl	1	1955	694	1	2	1
272	12	Aluminum / Vinyl	2	1894	1780	2	6	2
273	12	Frame	1	1924	1202	1	4	1
274	12	Aluminum / Vinyl	1	1895	1004	1	3	1
275	13	Stone	1.5	1937	1819	1	3	1
276	13	Aluminum / Vinyl	1	1941	1763	1	5	2
277	13	Masonry / Frame	2	1937	1494	1	4	1
278	13	Aluminum / Vinyl	1	1954	1476	1	3	2
279	13	Brick	1.5	1946	1406	1	2	1
280	13	Aluminum / Vinyl	1	1954	1034	1	3	1
281	13	Aluminum / Vinyl	1	1943	1006	1	3	1
282	13	Frame	2	1979	1746	1	3	2
283	13	Brick	2	1940	2076	2	4	2
284	13	Brick	1	1990	2044	1	3	2
285	13	Brick	1	1957	1308	1	4	1
286	13	Aluminum / Vinyl	1	1950	1269	1	2	1
287	13	Brick	1	1956	1102	1	2	1
288	13	Aluminum / Vinyl	1	1958	1056	1	3	1
289	13	Aluminum / Vinyl	1	1959	1051	1	3	1
290	13	Aluminum / Vinyl	1	1960	1048	1	3	1
291	13	Aluminum / Vinyl	1	1960	907	1	3	2
292	14	Brick	1.5	1956	2073	1	4	3
293	14	Stone	1	1950	1571	1	4	1
294	14	Brick	1	1947	926	1	3	1
295	14	Aluminum / Vinyl	1.5	1927	2109	2	4	3
296	14	Aluminum / Vinyl	2	1895	1968	1	5	2
297	14	Frame	2	1876	1674	2	3	2
298	14	Aluminum / Vinyl	1.5	1921	1391	2	3	2
299	14	Brick	1	1926	1548	1	4	1
300	14	Aluminum / Vinyl	1	1925	1430	1	3	1

301	14	Block	1	1947	858	1	2	1
302	14	Aluminum / Vinyl	1.5	1898	1611	1	3	2
303	14	Frame	1	1922	1334	1	4	2
304	14	Aluminum / Vinyl	1	1900	1220	1	3	2
305	15	Aluminum / Vinyl	2	1913	2902	2	6	2
306	15	Aluminum / Vinyl	1.5	1905	1596	2	3	2
307	15	Stucco	1	1916	1680	1	5	3
308	1	Aluminum / Vinyl	2	1939	1816	1	5	1
309	1	Aluminum / Vinyl	1.5	1929	1596	2	4	2
310	1	Aluminum / Vinyl	1.5	1929	1596	2	4	2
311	1	Frame	1.5	1925	1546	2	3	2
312	1	Aluminum / Vinyl	1	1927	1278	1	4	1
313	1	Aluminum / Vinyl	1	1953	1082	1	3	1
314	1	Aluminum / Vinyl	1	1926	1334	1	4	2
315	2	Aluminum / Vinyl	1	1956	1107	1	3	1
316	2	Aluminum / Vinyl	1	1942	1073	1	3	1
317	2	Aluminum / Vinyl	1	1951	862	1	2	1
318	2	Masonry / Frame	2	1956	2588	2	6	2
319	2	Aluminum / Vinyl	2	1957	2066	2	6	2
320	2	Aluminum / Vinyl	1	1965	1223	1	3	1
321	2	Aluminum / Vinyl	1	1963	1218	1	3	1
322	2	Brick	1	1947	1077	1	2	1
323	2	Aluminum / Vinyl	1	1957	988	1	3	1
324	3	Aluminum / Vinyl	2	1925	2848	2	6	2
325	3	Aluminum / Vinyl	2	1923	2724	2	6	2
326	3	Aluminum / Vinyl	1.5	1890	1570	2	2	2
327	3	Masonry / Frame	2	1909	3701	1	6	4
328	3	Frame	2	1909	2167	1	3	1
329	3	Aluminum / Vinyl	1	1890	1113	1	3	1
330	5	Stone	1	1948	1247	1	3	1
331	5	Brick	1	1949	1218	1	3	1
332	5	Aluminum / Vinyl	1	1952	1173	1	3	1
333	5	Aluminum / Vinyl	1	1952	1124	1	3	1
334	5	Aluminum / Vinyl	1.5	1941	1084	1	3	1
335	5	Frame	1.5	1941	1035	1	3	1
336	5	Aluminum / Vinyl	1	1951	954	1	3	1
337	5	Brick	1	1951	948	1	2	1
338	5	Aluminum / Vinyl	1	1952	722	1	2	1
339	5	Masonry / Frame	2	1972	2464	1	4	1
340	5	Aluminum / Vinyl	2	1954	1872	1	4	1
341	5	Aluminum / Vinyl	2	1988	1800	1	3	1
342	5	Aluminum / Vinyl	2	1948	1378	1	3	1
343	5	Brick	2	1966	2744	2	6	2

344	5	Masonry / Frame	2	1955	2192	2	6	2
345	5	Brick	1.5	1953	1930	2	4	2
346	5	Brick	1	1963	1446	1	3	1
347	5	Stone	1	1951	1280	1	2	2
348	5	Aluminum / Vinyl	1	1953	1263	1	3	1
349	5	Brick	1	1958	1219	1	3	1
350	5	Aluminum / Vinyl	1	1971	1217	1	4	1
351	5	Brick	1	1955	1200	1	3	1
352	5	Brick	1	1958	1076	1	3	2
353	5	Aluminum / Vinyl	1	1956	997	1	3	1
354	5	Aluminum / Vinyl	1	1958	963	1	3	2
355	5	Masonry / Frame	2	1967	2424	2	6	2
356	6	Frame	1.5	1902	1990	2	5	2
357	6	Brick	1	1928	1653	1	4	1
358	7	Stone	1	1935	1711	1	4	1
359	7	Brick	1.5	1937	1647	1	4	2
360	7	Brick	1	1948	1590	1	3	1
361	7	Stone	1	1947	1402	1	4	3
362	7	Aluminum / Vinyl	2	1923	2496	2	4	2
363	7	Stone	1.5	1943	1973	2	3	2
364	7	Aluminum / Vinyl	1.5	1929	1930	2	4	2
365	8	Frame	1	1885	652	1	2	1
366	8	Frame	2	1914	2540	2	6	2
368	9	Aluminum / Vinyl	1	1953	1020	1	4	1
369	9	Brick	1	1957	1217	1	3	2
370	9	Brick	1	1957	1188	1	3	1
371	9	Masonry / Frame	1	1957	1161	1	3	1
372	10	Aluminum / Vinyl	1.5	1947	1636	1	3	1
373	10	Brick	1	1945	946	1	3	2
374	10	Masonry / Frame	2	1926	2407	1	3	2
375	10	Aluminum / Vinyl	1	1900	1240	1	3	1
376	10	Stucco	1.5	1925	1759	2	3	2
377	10	Brick	1	1926	2011	1	3	1
378	10	Brick	1	1927	2005	1	4	2
379	10	Brick	1	1927	1733	1	3	1
380	10	Aluminum / Vinyl	1	1920	1620	1	4	1
381	10	Brick	1	1931	1557	1	3	1
382	10	Brick	1	1927	1214	1	2	1
383	10	Stone	1	1952	1728	1	3	1
384	10	Stone	1	1955	1289	1	3	1
385	10	Frame	1	1951	1202	1	3	1
386	10	Aluminum / Vinyl	1	1953	792	1	2	2
387	10	Brick	1	1948	788	1	2	1

388	10	Aluminum / Vinyl	1.5	1926	1223	1	4	1
389	10	Frame	1	1916	934	1	3	1
390	11	Aluminum / Vinyl	1	1941	1320	1	3	2
391	11	Aluminum / Vinyl	1	1950	1220	1	3	1
392	11	Aluminum / Vinyl	1	1954	1187	1	4	1
393	11	Aluminum / Vinyl	1	1953	1163	1	3	1
394	11	Brick	1	1958	1100	1	2	2
395	11	Brick	1	1949	863	1	2	1
396	11	Prem Wood	2	2002	2674	1	4	2
397	11	Aluminum / Vinyl	2	1949	1275	1	3	1
398	11	Brick	2	1957	2550	2	6	2
399	11	Aluminum / Vinyl	2	1957	1884	2	6	2
400	11	Frame	1	1927	1618	1	5	2
401	11	Frame	1	1954	1478	1	3	1
402	11	Frame	1	1964	1292	1	4	1
403	11	Aluminum / Vinyl	1	1959	1233	1	3	1
404	11	Brick	1	1954	1149	1	2	1
405	11	Aluminum / Vinyl	1	1961	1062	1	3	1
406	11	Aluminum / Vinyl	1	1954	972	1	3	1
407	11	Aluminum / Vinyl	1	1955	972	1	3	1
408	11	Frame	1	1951	958	1	2	1
409	11	Aluminum / Vinyl	1	1954	943	1	3	1
410	11	Aluminum / Vinyl	1	1954	906	1	3	1
411	11	Frame	1	1951	811	1	2	1
412	11	Aluminum / Vinyl	1	1956	672	1	2	1
413	13	Brick	1.5	1948	1897	1	4	1
414	13	Aluminum / Vinyl	1	1941	1365	1	4	1
415	13	Stone	1	1940	927	1	2	1
416	13	Brick	1	1939	891	1	1	1
417	13	Aluminum / Vinyl	2	1940	1869	1	3	1
418	13	Frame	1.5	1912	2151	2	6	2
419	13	Aluminum / Vinyl	1	1929	1035	1	3	1
420	13	Brick	1	1960	1541	1	3	1
421	13	Brick	1	1969	1534	1	2	2
422	13	Brick	1	1959	1257	1	3	1
423	13	Aluminum / Vinyl	1	1960	1254	1	3	1
424	13	Frame	1	1966	1176	1	3	1
425	13	Aluminum / Vinyl	1	1954	1116	1	3	1
426	13	Brick	1	1963	1092	1	3	2
427	13	Aluminum / Vinyl	1	1959	1021	1	3	1
428	13	Aluminum / Vinyl	1	1954	1008	1	3	1
429	13	Aluminum / Vinyl	1	1961	983	1	3	1
430	13	Aluminum / Vinyl	1	1950	912	1	3	1

431	13	Aluminum / Vinyl	1	1954	864	1	3	1
432	13	Aluminum / Vinyl	1	1955	672	1	2	1
433	14	Block	1	1944	1055	1	3	2
434	14	Aluminum / Vinyl	1.5	1940	1003	1	2	1
435	14	Frame	1	1948	782	1	2	1
436	14	Aluminum / Vinyl	2	1945	1360	1	3	1
437	14	Aluminum / Vinyl	2	1937	1056	1	2	1
438	14	Aluminum / Vinyl	1.5	1927	2059	2	4	2
439	14	Frame	1	1926	1412	1	3	1
440	14	Aluminum / Vinyl	1	1923	1251	1	4	1
441	14	Aluminum / Vinyl	1	1918	908	1	2	1
442	14	Aluminum / Vinyl	1	1942	848	1	2	1
443	14	Aluminum / Vinyl	2	1909	1956	1	4	1
444	14	Stucco	1.5	1916	1561	1	4	2
445	14	Aluminum / Vinyl	1.5	1909	1523	1	3	1
446	14	Aluminum / Vinyl	2	1901	1503	1	3	1
447	1	Brick	1.5	1937	1461	1	3	1
448	1	Frame	1	1956	1212	1	2	1
449	1	Frame	1	1941	1048	1	3	1
450	1	Aluminum / Vinyl	1	1942	920	1	3	1
451	1	Aluminum / Vinyl	1	1937	919	1	2	1
452	1	Brick	2	1954	1810	2	6	2
453	1	Brick	2	1943	1786	2	4	2
454	1	Aluminum / Vinyl	1	1956	1425	1	3	2
455	1	Aluminum / Vinyl	1	1927	876	1	3	1
456	1	Prem Wood	1.5	1931	2883	1	4	1
457	2	Brick	1.5	1952	1450	1	4	2
458	2	Brick	1	1956	1365	1	3	2
459	2	Aluminum / Vinyl	1.5	1963	1885	2	5	2
460	2	Aluminum / Vinyl	1	1952	969	1	2	1
461	2	Aluminum / Vinyl	1	1952	969	1	2	1
462	2	Aluminum / Vinyl	1	1952	969	1	2	1
463	2	Aluminum / Vinyl	1	1952	969	1	2	1
464	2	Aluminum / Vinyl	1	1971	936	1	3	1
465	2	Aluminum / Vinyl	1	1955	672	1	2	1
466	2	Aluminum / Vinyl	1	1930	2152	1	3	2
467	3	Frame	1	1951	1653	1	4	1
468	3	Brick	1.5	1923	2351	1	4	2
469	3	Brick	1.5	1923	2351	1	4	2
470	3	Masonry / Frame	2	1925	1984	1	4	1
471	3	Frame	2	1889	2478	2	7	2
472	3	Brick	2	1923	5438	1	5	4
473	3	Aluminum / Vinyl	1	1927	1530	1	4	2

474	3	Masonry / Frame	2	1915	3417	1	5	3
475	3	Frame	2	1899	2340	1	5	2
476	3	Aluminum / Vinyl	2	1890	2077	1	4	2
477	3	Stone	1.5	1925	1787	1	3	2
478	3	Frame	2	1901	1717	1	4	1
479	3	Frame	1	1910	1501	1	3	1
480	3	Frame	2	1904	1254	1	4	1
481	3	Aluminum / Vinyl	1	1895	1230	1	5	2
482	3	Aluminum / Vinyl	1	1923	1132	1	3	1
483	3	Aluminum / Vinyl	1.5	1897	1095	1	2	1
484	5	Stone	1	1938	1745	1	3	2
485	5	Brick	1	1952	1543	1	4	2
486	5	Brick	1	1947	1464	1	3	1
487	5	Brick	1	1951	1438	1	4	1
488	5	Brick	1.5	1949	1409	1	3	1
489	5	Aluminum / Vinyl	1	1940	1402	1	4	1
490	5	Aluminum / Vinyl	1	1952	1399	1	4	1
491	5	Brick	1	1940	1381	1	2	2
492	5	Aluminum / Vinyl	1	1952	1368	1	3	1
493	5	Aluminum / Vinyl	1	1948	1251	1	3	1
494	5	Aluminum / Vinyl	1	1950	1171	1	3	1
495	5	Aluminum / Vinyl	1	1950	1170	1	3	1
496	5	Aluminum / Vinyl	1	1950	1147	1	3	1
497	5	Aluminum / Vinyl	1	1956	1114	1	3	1
498	5	Aluminum / Vinyl	1	1953	1104	1	3	1
499	5	Aluminum / Vinyl	1	1950	1011	1	3	1
500	5	Aluminum / Vinyl	1	1955	994	1	3	2
501	5	Aluminum / Vinyl	1	1950	888	1	2	1
502	5	Brick	1	1947	883	1	2	1
503	5	Aluminum / Vinyl	1	1952	693	1	2	1
504	5	Aluminum / Vinyl	2	2008	2506	1	4	2
505	5	Masonry / Frame	2	1956	1598	1	3	1
506	5	Aluminum / Vinyl	2	1950	1572	1	3	1
507	5	Masonry / Frame	2	1938	1557	1	3	1
508	5	Stone	1	1952	1657	1	3	1
509	5	Brick	1	1958	1627	1	3	2
510	5	Aluminum / Vinyl	1	1959	1431	1	4	1
511	5	Brick	1	1959	1429	1	3	1
512	5	Aluminum / Vinyl	1	1993	1226	1	3	2
513	5	Brick	1	1956	1223	1	3	1
514	5	Brick	1	1957	1201	1	3	1
515	5	Brick	1	1959	1151	1	2	1
516	5	Aluminum / Vinyl	1	1954	1142	1	3	2

517	5	Aluminum / Vinyl	1	1957	1053	1	3	1
518	5	Frame	1	1951	1053	1	3	1
519	5	Brick	1	1951	1033	1	3	1
520	5	Brick	1	1954	1006	1	2	1
521	5	Aluminum / Vinyl	1	1956	983	1	3	1
522	5	Stone	1	1950	980	1	2	1
523	5	Frame	1	1954	962	1	3	1
524	6	Frame	2	1904	3476	2	6	2
525	6	Aluminum / Vinyl	1.5	1919	1969	1	4	2
526	6	Aluminum / Vinyl	1.5	1910	1210	1	3	1
527	6	Frame	1	1903	998	1	3	1
528	7	Block	1	1944	1014	1	3	1
529	7	Aluminum / Vinyl	2	1924	2674	2	6	2
530	7	Aluminum / Vinyl	1	1924	1497	1	4	1
531	7	Frame	1	1926	1453	1	5	1
532	7	Masonry / Frame	1	1946	1035	1	3	1
533	7	Aluminum / Vinyl	1	1947	1029	1	3	1
534	7	Masonry / Frame	2	1936	1678	1	3	1
535	8	Aluminum / Vinyl	2	2008	1672	1	3	2
536	8	Frame	1.5	1918	1809	2	3	2
537	8	Aluminum / Vinyl	1.5	1926	2095	2	5	2
538	8	Aluminum / Vinyl	1	1927	1601	1	5	1
539	8	Frame	2	1913	1364	1	3	1
540	8	Aluminum / Vinyl	1	1904	1161	1	3	1
541	8	Aluminum / Vinyl	1	1900	1074	1	3	1
542	8	Masonry / Frame	2	1914	3632	3	7	4
543	9	Aluminum / Vinyl	1	1980	1320	1	3	1
544	9	Brick	1	1959	924	1	3	1
545	9	Frame	1	1977	906	1	3	1
546	10	Stone	1.5	1937	1815	1	3	2
547	10	Masonry / Frame	1.5	1950	1505	1	3	1
548	10	Aluminum / Vinyl	1	1953	1307	1	3	1
549	10	Brick	1	1953	1255	1	3	1
550	10	Aluminum / Vinyl	1	1948	1094	1	3	1
551	10	Aluminum / Vinyl	1	1948	978	1	2	1
552	10	Aluminum / Vinyl	1	1951	920	1	2	1
553	10	Brick	1	1947	845	1	2	1
554	10	Stucco	2	1914	3591	2	6	3
555	10	Stone	2	1948	2520	2	4	2
556	10	Brick	1	1931	1741	1	4	2
557	10	Frame	1	1927	1584	1	3	2
558	10	Aluminum / Vinyl	1	1925	1225	1	3	1
559	10	Aluminum / Vinyl	1	1927	1010	1	2	1

560	10	Aluminum / Vinyl	1	1925	768	1	1	1
561	10	Aluminum / Vinyl	1	1955	1063	1	3	2
562	10	Brick	1	1957	1032	1	3	1
563	10	Aluminum / Vinyl	1	1943	810	1	2	1
564	10	Aluminum / Vinyl	2	1926	1320	1	3	2
565	11	Stone	1	1946	1278	1	2	1
566	11	Stone	1	1945	1182	1	4	1
567	11	Aluminum / Vinyl	1	1954	1103	1	4	1
568	11	Brick	1	1945	992	1	3	1
570	11	Aluminum / Vinyl	2	1964	1754	1	3	1
571	11	Stone	1.5	1937	2045	2	4	2
572	11	Brick	1	1952	1533	1	4	2
573	11	Frame	1	1960	1285	1	3	1
574	11	Aluminum / Vinyl	1	1958	1202	1	3	1
575	11	Aluminum / Vinyl	1	1959	1177	1	3	1
576	11	Brick	1	1951	1166	1	3	1
577	11	Brick	1	1956	1145	1	3	1
578	11	Aluminum / Vinyl	1	1960	1097	1	3	1
579	11	Brick	1	1958	1086	1	2	1
580	11	Aluminum / Vinyl	1	1959	1072	1	3	1
581	11	Brick	1	1956	1061	1	3	1
582	11	Brick	1	1954	1053	1	3	1
583	11	Brick	1	1956	1035	1	2	1
584	11	Brick	1	1950	1031	1	2	2
585	11	Brick	1	1950	1008	1	3	1
586	11	Aluminum / Vinyl	1	1954	955	1	3	1
587	11	Aluminum / Vinyl	1	1959	943	1	3	1
588	11	Brick	1	1955	925	1	2	1
589	11	Aluminum / Vinyl	1	1953	879	1	3	1
590	11	Aluminum / Vinyl	1	1953	879	1	3	1
591	11	Aluminum / Vinyl	1	1956	876	1	3	1
592	11	Frame	1	1952	802	1	2	1
593	11	Aluminum / Vinyl	1	1956	672	1	2	1
594	11	Aluminum / Vinyl	1	1936	1427	1	3	2
595	13	Frame	1.5	1986	2523	1	3	2
596	13	Aluminum / Vinyl	1.5	1939	1096	1	3	1
598	13	Aluminum / Vinyl	2	1929	1065	1	3	1
599	13	Aluminum / Vinyl	2	2000	2018	2	4	2
600	13	Brick	1	1982	1837	1	3	3
601	13	Brick	1	1971	1693	1	3	2
602	13	Brick	1	1959	1548	1	2	2
603	13	Aluminum / Vinyl	1	1967	1538	1	3	2
604	13	Aluminum / Vinyl	1	1975	1480	1	3	1

605	13	Aluminum / Vinyl	1	1984	1351	1	3	1
606	13	Aluminum / Vinyl	1	1950	1186	1	2	1
607	13	Aluminum / Vinyl	1	1959	1171	1	3	1
608	13	Aluminum / Vinyl	1	1967	1151	1	3	1
609	13	Brick	1	1959	1150	1	3	1
610	13	Brick	1	1960	1150	1	3	1
611	13	Brick	1	1955	1119	1	3	2
612	13	Brick	1	1959	1101	1	3	1
613	13	Aluminum / Vinyl	1	1961	981	1	3	1
615	14	Frame	1	1948	1540	1	4	1
616	14	Stone	1	1936	1246	1	3	1
617	14	Brick	1.5	1936	1222	1	2	1
618	14	Brick	1	1955	1108	1	2	1
619	14	Aluminum / Vinyl	1	1947	1102	1	3	1
620	14	Aluminum / Vinyl	1	1950	1021	1	3	1
621	14	Aluminum / Vinyl	2	1948	1378	1	3	1
622	14	Aluminum / Vinyl	1	1928	1638	2	3	2
623	14	Brick	2	1951	2260	2	4	2
624	14	Aluminum / Vinyl	1.5	1898	2343	2	5	2
625	14	Aluminum / Vinyl	1.5	1910	1894	2	3	2
626	14	Aluminum / Vinyl	1.5	1898	1748	2	4	2
627	14	Aluminum / Vinyl	1.5	1927	1715	1	4	1
628	14	Frame	1	1926	1607	1	3	1
629	14	Aluminum / Vinyl	1	1928	1477	1	3	1
630	14	Aluminum / Vinyl	1	1922	1164	1	3	1
631	14	Aluminum / Vinyl	1	1948	864	1	3	1
632	14	Aluminum / Vinyl	1	1950	808	1	2	1
633	14	Aluminum / Vinyl	1	1898	1449	1	3	2
634	14	Aluminum / Vinyl	2	1892	1240	1	2	1
635	14	Aluminum / Vinyl	1	1912	954	1	3	1
636	14	Aluminum / Vinyl	1	1922	896	1	2	1
637	15	Brick	2	1905	1894	1	4	1
638	1	Block	1.5	1950	1425	1	4	2
639	1	Aluminum / Vinyl	1	1942	1110	1	3	1
640	1	Brick	1	1951	1070	1	3	1
641	1	Brick	2	1953	2016	2	6	2
642	1	Aluminum / Vinyl	2	1956	1938	2	6	2
643	1	Aluminum / Vinyl	1.5	1937	1459	2	3	2
644	1	Brick	1	1929	1673	1	4	1
645	1	Aluminum / Vinyl	1	1925	1632	1	5	1
646	1	Masonry / Frame	1	1961	1646	1	3	2
647	1	Brick	1	1956	1270	1	3	1
648	1	Brick	1	1962	1042	1	3	2

649	1 Aluminum / Vinyl	1	1955	1040	1	3	1
650	1 Frame	1.5	1913	1186	1	3	1
651	2 Aluminum / Vinyl	1	1997	1481	1	3	2
652	2 Brick	1.5	1955	1839	1	4	2
653	2 Brick	1	1954	1553	1	4	1
654	2 Aluminum / Vinyl	1	1947	1172	1	3	1
655	2 Brick	1	1956	1096	1	2	1
656	2 Aluminum / Vinyl	1	1940	1028	1	3	1
657	2 Aluminum / Vinyl	2	2001	2321	1	3	2
658	2 Aluminum / Vinyl	2	1948	1267	1	3	1
659	2 Brick	1	1970	1334	1	3	2
660	2 Brick	1	1960	1185	1	3	1
661	2 Brick	1	1958	1159	1	3	1
662	2 Brick	1	1953	1126	1	3	1
663	2 Aluminum / Vinyl	1	1956	1058	1	3	1
664	2 Aluminum / Vinyl	1	1961	1056	1	3	1
665	2 Aluminum / Vinyl	1	1956	948	1	3	1
666	2 Aluminum / Vinyl	1	1955	936	1	3	1
667	2 Aluminum / Vinyl	1	1952	761	1	2	1
668	3 Frame	1.5	1926	1880	2	3	2
669	3 Aluminum / Vinyl	1.5	1890	1789	2	4	2
670	3 Frame	2	1906	2640	1	4	2
671	3 Frame	2	1900	2138	1	3	1
672	3 Stucco	2	1915	1923	1	4	1
673	3 Aluminum / Vinyl	1.5	1897	1364	1	3	1
675	5 Masonry / Frame	1.5	1947	1668	1	3	2
676	5 Brick	1	1950	1530	1	3	1
677	5 Aluminum / Vinyl	1	1940	1515	1	3	1
678	5 Brick	1	1949	1428	1	3	2
679	5 Brick	1	1947	1370	1	3	1
680	5 Brick	1	1948	1367	1	3	1
681	5 Aluminum / Vinyl	1	1953	1317	1	3	1
682	5 Aluminum / Vinyl	1	1951	1232	1	3	1
683	5 Aluminum / Vinyl	1	1950	1229	1	3	1
684	5 Stone	1	1948	1188	1	2	1
685	5 Aluminum / Vinyl	1	1956	1180	1	4	2
686	5 Aluminum / Vinyl	1	1952	1180	1	3	1
687	5 Brick	1	1952	1125	1	4	1
688	5 Aluminum / Vinyl	1	1951	1107	1	3	1
689	5 Frame	1	1946	1090	1	3	2
690	5 Brick	1	1955	1088	1	2	1
691	5 Stone	1	1940	1057	1	2	1
692	5 Aluminum / Vinyl	1	1953	1030	1	3	1

693	5 Aluminum / Vinyl	1	1952	1000	1	3	1
694	5 Aluminum / Vinyl	1	1949	971	1	3	1
695	5 Fiber-Cement	2	2009	2150	1	4	2
696	5 Masonry / Frame	2	1937	1674	1	3	1
697	5 Aluminum / Vinyl	2	1948	2032	2	4	2
698	5 Aluminum / Vinyl	1.5	1963	1866	2	4	2
699	5 Brick	1	1967	1665	1	3	2
700	5 Brick	1	1956	1223	1	3	1
701	5 Aluminum / Vinyl	1	1972	1204	1	4	1
702	5 Aluminum / Vinyl	1	1949	1140	1	3	1
703	5 Brick	1	1964	1090	1	3	1
704	5 Brick	1	1957	1080	1	3	2
705	5 Brick	1	1951	1056	1	2	2
706	5 Aluminum / Vinyl	1	1950	1022	1	3	1
707	5 Brick	1	1951	1016	1	3	1
708	5 Frame	1	1956	988	1	3	1
709	5 Aluminum / Vinyl	1	1956	948	1	2	1
710	5 Aluminum / Vinyl	1	1950	904	1	3	1
711	5 Aluminum / Vinyl	1	1951	833	1	2	1
712	5 Aluminum / Vinyl	1	1950	707	1	2	1
713	5 Aluminum / Vinyl	1	1950	1099	1	3	1
714	5 Masonry / Frame	2	1951	2040	2	4	2
715	6 Aluminum / Vinyl	2	1984	2052	1	4	2
716	6 Aluminum / Vinyl	2	2008	1848	1	3	1
717	6 Frame	1.5	1926	2000	2	4	2
718	6 Aluminum / Vinyl	2	1890	1998	2	4	2
720	6 Frame	1	1885	2212	1	3	1
721	7 Brick	1.5	1945	1486	1	3	1
722	7 Aluminum / Vinyl	1	1948	1099	1	3	1
723	7 Aluminum / Vinyl	1	1948	1063	1	3	1
724	7 Aluminum / Vinyl	2	1941	1346	1	3	1
725	7 Aluminum / Vinyl	2	1924	2535	2	6	2
726	7 Brick	1.5	1919	2391	2	4	2
727	7 Brick	2	1950	2394	2	4	2
728	7 Aluminum / Vinyl	1.5	1931	1279	1	3	1
729	7 Stone	1	1933	1244	1	3	2
730	8 Aluminum / Vinyl	2	1911	3331	2	7	3
731	8 Aluminum / Vinyl	1	1919	1512	1	4	1
732	8 Aluminum / Vinyl	1	1926	1427	1	3	1
733	8 Aluminum / Vinyl	1	1921	1325	1	3	1
734	8 Aluminum / Vinyl	1	1959	917	1	3	1
735	8 Aluminum / Vinyl	1.5	1910	1294	1	2	1
736	8 Aluminum / Vinyl	2	1912	2438	3	6	3

737	9	Aluminum / Vinyl	1	1955	1274	1	4	2
738	9	Aluminum / Vinyl	2	2004	2016	1	3	2
739	9	Aluminum / Vinyl	1	1930	1089	1	3	1
740	9	Aluminum / Vinyl	1	1948	720	1	2	1
741	9	Aluminum / Vinyl	1	2008	1721	1	3	2
742	9	Aluminum / Vinyl	1	1957	1211	1	3	1
743	9	Aluminum / Vinyl	1	1971	1200	1	4	1
744	9	Aluminum / Vinyl	1	1972	1200	1	4	1
745	9	Aluminum / Vinyl	1	1962	1132	1	3	2
746	9	Brick	1	1961	1117	1	3	1
747	9	Aluminum / Vinyl	1	1981	1077	1	2	2
748	9	Aluminum / Vinyl	1	1969	1063	1	3	1
749	9	Frame	1	1956	1033	1	3	1
750	9	Aluminum / Vinyl	1	1965	1006	1	3	1
751	9	Aluminum / Vinyl	1	1954	958	1	3	1
752	9	Frame	1	1980	912	1	3	2
753	9	Aluminum / Vinyl	1	1977	1512	1	3	1
754	10	Aluminum / Vinyl	1	1951	1292	1	3	2
755	10	Brick	1	1951	1536	1	3	1
756	10	Brick	1.5	1952	1435	1	2	1
757	10	Brick	1	1955	1344	1	3	1
758	10	Brick	1	1948	1336	1	3	1
759	10	Stone	1	1939	1335	1	3	1
760	10	Aluminum / Vinyl	1	1948	1206	1	3	1
761	10	Aluminum / Vinyl	1	1950	1196	1	3	1
762	10	Aluminum / Vinyl	1	1953	1184	1	2	1
763	10	Aluminum / Vinyl	1	1948	1170	1	4	1
764	10	Brick	1.5	1946	1060	1	2	1
765	10	Aluminum / Vinyl	1	1948	1047	1	3	1
766	10	Aluminum / Vinyl	1	1952	784	1	2	1
767	10	Brick	2	1928	2900	2	6	2
768	10	Aluminum / Vinyl	2	1917	2190	2	4	2
769	10	Aluminum / Vinyl	2	1925	1990	2	4	2
770	10	Frame	1.5	1913	1980	2	3	2
771	10	Masonry / Frame	2	1925	2698	2	4	2
772	10	Stone	2	1939	2183	2	5	2
773	10	Brick	1	1928	2116	1	5	2
774	10	Frame	1	1924	1637	1	4	1
775	10	Frame	1	1927	1316	1	3	2
776	10	Aluminum / Vinyl	1	1926	934	1	3	1
777	10	Frame	1	1927	926	1	2	1
778	10	Aluminum / Vinyl	1	1953	1384	1	3	1
779	10	Brick	1	1954	1303	1	3	1

780	10	Aluminum / Vinyl	1	1953	955	1	2	1
781	10	Aluminum / Vinyl	2	1900	1769	1	3	2
782	10	Frame	1	1923	1140	1	3	1
783	11	Aluminum / Vinyl	1	1962	1788	1	4	2
784	11	Brick	1	1939	1581	1	3	1
785	11	Aluminum / Vinyl	1.5	1954	1347	1	4	1
786	11	Brick	1	1954	1248	1	3	1
787	11	Aluminum / Vinyl	1	1955	1181	1	3	1
788	11	Aluminum / Vinyl	1	1947	1063	1	2	1
789	11	Aluminum / Vinyl	1	1950	1060	1	3	1
790	11	Brick	1	1951	1017	1	2	1
791	11	Aluminum / Vinyl	1	1949	925	1	3	1
792	11	Masonry / Frame	2	1951	2383	1	3	2
793	11	Aluminum / Vinyl	2	1987	2331	1	3	2
794	11	Frame	2	1984	2034	1	3	2
795	11	Masonry / Frame	2	1955	1846	1	4	2
796	11	Brick	1	1929	1865	1	3	1
797	11	Aluminum / Vinyl	1	1954	1436	1	2	1
798	11	Stone	1	1955	1407	1	3	2
799	11	Aluminum / Vinyl	1	1954	1183	1	3	1
800	11	Brick	1	1955	1153	1	3	1
801	11	Brick	1	1956	1150	1	3	1
802	11	Frame	1	1955	1147	1	3	1
803	11	Aluminum / Vinyl	1	1964	1094	1	3	1
804	11	Aluminum / Vinyl	1	1959	1073	1	3	1
805	11	Brick	1	1954	1013	1	3	1
806	11	Brick	1	1954	1013	1	3	1
807	11	Brick	1	1954	1010	1	3	1
808	11	Brick	1	1951	1008	1	3	1
809	11	Aluminum / Vinyl	1	1954	1001	1	3	1
810	11	Brick	1	1955	977	1	3	1
811	11	Aluminum / Vinyl	1	1954	941	1	3	1
812	11	Brick	1	1944	824	1	2	1
813	11	Aluminum / Vinyl	1	1952	778	1	2	1
814	11	Prem Wood	1	1964	2416	1	4	2
815	11	Aluminum / Vinyl	2	1975	2478	2	6	2
816	11	Aluminum / Vinyl	2	1963	2214	2	6	2
817	12	Aluminum / Vinyl	2	1966	1162	1	3	1
818	12	Aluminum / Vinyl	1	1903	828	1	2	1
819	12	Aluminum / Vinyl	2	1908	2316	2	6	2
820	12	Frame	1.5	1893	1728	2	4	2
821	13	Brick	1	1955	2184	1	5	2
822	13	Aluminum / Vinyl	1	1958	1408	1	4	1

823	13	Brick	1	1957	1026	1	2	1
824	13	Brick	1.5	1940	986	1	2	1
825	13	Aluminum / Vinyl	1	1923	877	1	2	2
826	13	Brick	1	1956	1829	1	4	2
827	13	Frame	1	1965	1555	1	4	1
828	13	Brick	1	1967	1427	1	4	1
829	13	Brick	1	1964	1289	1	3	1
830	13	Brick	1	1957	1168	1	3	1
831	13	Brick	1	1956	1150	1	2	2
832	13	Aluminum / Vinyl	1	1965	1124	1	3	1
833	13	Aluminum / Vinyl	1	1958	1120	1	3	1
834	13	Brick	1	1963	1116	1	3	1
835	13	Aluminum / Vinyl	1	1982	1064	1	3	1
836	13	Aluminum / Vinyl	1	1959	1053	1	3	1
837	13	Aluminum / Vinyl	1	1959	1029	1	3	1
838	13	Brick	1	1960	1025	1	3	1
839	13	Aluminum / Vinyl	1	1952	1016	1	3	1
840	13	Aluminum / Vinyl	1	1951	864	1	3	1
841	13	Aluminum / Vinyl	1	1951	783	1	2	1
842	13	Aluminum / Vinyl	1	1955	1273	1	2	1
843	14	Aluminum / Vinyl	1.5	1954	1409	1	4	1
844	14	Stucco	1	1944	1198	1	3	1
845	14	Brick	1	1948	1153	1	3	2
846	14	Aluminum / Vinyl	2	1954	1553	1	3	1
847	14	Aluminum / Vinyl	2	1938	1056	1	2	1
848	14	Aluminum / Vinyl	1.5	1927	2093	2	3	2
849	14	Aluminum / Vinyl	2	1923	2067	2	4	2
850	14	Aluminum / Vinyl	2	1905	3278	2	6	2
851	14	Aluminum / Vinyl	1.5	1906	2488	2	4	2
852	14	Aluminum / Vinyl	2	1884	2250	2	6	3
853	14	Aluminum / Vinyl	1.5	1890	1768	2	3	2
854	14	Aluminum / Vinyl	1.5	1908	1603	2	4	2
855	14	Aluminum / Vinyl	1.5	1922	1363	2	4	2
856	14	Frame	1	1933	1444	1	3	1
857	14	Brick	1	1956	1099	1	2	1
858	14	Brick	1	1959	980	1	2	1
859	14	Aluminum / Vinyl	1	1950	912	1	3	1
860	14	Brick	1	1953	892	1	2	1
861	14	Aluminum / Vinyl	1	1950	672	1	2	1
862	14	Aluminum / Vinyl	1.5	1890	2009	1	4	1
863	14	Frame	1.5	1890	1541	1	4	2
864	14	Aluminum / Vinyl	2	1925	1525	1	3	1
865	14	Aluminum / Vinyl	1	1910	1518	1	5	1

866	14 Aluminum / Vinyl	2	1909	1476	1	3	2
867	14 Aluminum / Vinyl	1.5	1905	1366	1	2	1
868	14 Aluminum / Vinyl	2	1909	1267	1	3	1
869	14 Aluminum / Vinyl	1.5	1920	1238	1	4	2
870	14 Stucco	1	1916	1135	1	2	1
871	14 Aluminum / Vinyl	1	1912	1070	1	3	1
872	14 Aluminum / Vinyl	1	1902	968	1	2	1
873	14 Aluminum / Vinyl	1	1908	892	1	3	1
874	14 Brick	1.5	1929	1639	1	3	1
875	15 Aluminum / Vinyl	2	2006	1458	1	3	1
876	15 Frame	2	1915	2616	2	6	2
877	15 Aluminum / Vinyl	2	1900	2009	2	4	2
878	15 Frame	1	1918	1835	1	5	1
879	15 Aluminum / Vinyl	1	1918	1506	1	5	1
880	1 Aluminum / Vinyl	1	1950	1071	1	3	1
881	1 Frame	2	1940	1186	1	3	1
882	1 Stone	1.5	1942	2168	2	3	2
883	1 Aluminum / Vinyl	1	1926	1169	1	3	1
884	1 Aluminum / Vinyl	1	1980	1619	1	3	2
885	1 Aluminum / Vinyl	1	1955	1082	1	3	1
886	1 Aluminum / Vinyl	1	1955	1082	1	3	1
887	1 Aluminum / Vinyl	1	1952	765	1	2	1
888	2 Aluminum / Vinyl	1	1951	1125	1	4	1
889	2 Aluminum / Vinyl	1	1962	1260	1	3	1
890	2 Brick	1	1955	1160	1	3	2
891	2 Brick	1	1956	1082	1	3	1
892	2 Brick	1	1955	1024	1	3	1
893	2 Frame	1	1961	1002	1	3	1
894	2 Aluminum / Vinyl	1	1955	950	1	3	1
895	2 Aluminum / Vinyl	1	1956	936	1	3	1
896	2 Aluminum / Vinyl	1	1957	874	1	3	1
897	2 Aluminum / Vinyl	1	1955	672	1	2	1
898	2 Aluminum / Vinyl	1	1955	1414	1	3	1
899	2 Masonry / Frame	2	1963	2281	2	6	2
900	2 Brick	1	1931	1436	1	4	1
901	3 Brick	2	1925	2934	2	4	2
902	3 Brick	1.5	1926	2555	2	5	2
903	3 Aluminum / Vinyl	1.5	1922	1641	2	3	2
904	3 Aluminum / Vinyl	1.5	1898	1846	2	5	2
905	3 Aluminum / Vinyl	1	1923	1919	1	4	2
906	3 Aluminum / Vinyl	2	1907	1993	1	3	1
907	3 Block	2	1905	1722	1	3	1
908	3 Aluminum / Vinyl	1	1889	1137	1	2	1

910	3	Brick	2	1914	3307	1	4	2
911	5	Aluminum / Vinyl	1	1941	1648	1	3	2
912	5	Aluminum / Vinyl	1	1952	1457	1	4	1
913	5	Frame	1	1950	1426	1	3	1
914	5	Brick	1	1955	1376	1	3	1
915	5	Brick	1	1949	1220	1	3	1
916	5	Aluminum / Vinyl	1	1948	1206	1	3	1
917	5	Brick	1.5	1947	1205	1	3	2
918	5	Aluminum / Vinyl	1	1952	1171	1	3	1
919	5	Stucco	1	1952	1156	1	3	2
920	5	Aluminum / Vinyl	1	1952	1153	1	3	1
921	5	Aluminum / Vinyl	1	1950	1132	1	3	1
922	5	Aluminum / Vinyl	1	1957	1130	1	4	1
923	5	Brick	1	1952	1088	1	3	1
924	5	Block	1	1940	1084	1	3	1
925	5	Aluminum / Vinyl	1	1950	1054	1	3	1
926	5	Aluminum / Vinyl	1	1951	1036	1	3	1
927	5	Brick	1	1953	1025	1	2	1
928	5	Aluminum / Vinyl	1	1950	1012	1	3	1
929	5	Aluminum / Vinyl	1	1942	981	1	3	1
930	5	Aluminum / Vinyl	1	1953	973	1	3	1
931	5	Aluminum / Vinyl	1	1950	971	1	3	1
932	5	Aluminum / Vinyl	1	1950	967	1	3	1
933	5	Aluminum / Vinyl	1	1953	963	1	3	1
934	5	Brick	1	1950	962	1	3	1
935	5	Aluminum / Vinyl	1	1950	691	1	2	1
936	5	Masonry / Frame	2	1958	2388	2	6	2
937	5	Masonry / Frame	2	1957	2330	2	6	2
938	5	Aluminum / Vinyl	1	1926	1345	1	4	1
939	5	Brick	1	1954	1744	1	2	1
940	5	Aluminum / Vinyl	1	1964	1399	1	3	1
941	5	Aluminum / Vinyl	1	1955	1361	1	3	1
942	5	Brick	1	1952	1200	1	3	2
943	5	Brick	1	1955	1161	1	3	1
944	5	Brick	1	1957	1134	1	3	1
945	5	Aluminum / Vinyl	1	1950	1130	1	3	2
946	5	Aluminum / Vinyl	1	1960	1120	1	3	1
947	5	Brick	1	1955	1068	1	2	1
948	5	Brick	1	1958	1040	1	3	2
949	5	Aluminum / Vinyl	1	1955	1022	1	3	1
950	5	Frame	1	1956	1008	1	3	1
951	5	Brick	1	1952	981	1	2	1
952	5	Stone	1	1950	980	1	2	1

953	5 Aluminum / Vinyl	1	1955	974	1	3	1
954	5 Frame	1	1955	974	1	3	1
955	5 Aluminum / Vinyl	1	1956	974	1	3	2
956	5 Aluminum / Vinyl	1	1955	948	1	3	1
957	5 Frame	1	1956	948	1	3	1
958	5 Aluminum / Vinyl	1	1957	907	1	2	1
959	5 Aluminum / Vinyl	1	1950	696	1	2	1
960	6 Aluminum / Vinyl	1	1895	798	1	2	1
961	6 Frame	2	1913	2778	2	6	2
962	6 Stucco	1.5	1914	1488	2	3	1
963	6 Aluminum / Vinyl	1.5	1925	1354	2	2	2
964	6 Frame	2	1900	2858	1	4	2
965	6 Aluminum / Vinyl	1	1900	1322	1	3	1
966	6 Frame	1	1900	1220	1	3	1
967	6 Frame	2	1912	2960	3	6	3
968	7 Stone	1	1948	1719	1	4	1
969	7 Masonry / Frame	2	1946	1455	1	3	1
970	7 Brick	2	1926	3128	2	6	2
971	7 Masonry / Frame	2	1937	2668	2	6	2
972	7 Frame	2	1912	1949	2	4	2
973	7 Brick	1	1926	1651	1	4	1
974	7 Brick	1	1952	1011	1	2	1
975	7 Aluminum / Vinyl	1.5	1915	1402	1	4	1
976	7 Aluminum / Vinyl	1	1916	1110	1	3	1
977	8 Aluminum / Vinyl	1	1885	1170	1	4	2
978	8 Brick	2	1908	2020	2	5	2
979	8 Aluminum / Vinyl	1.5	1898	1592	2	4	2
980	8 Aluminum / Vinyl	1	1890	1426	2	3	1
981	8 Aluminum / Vinyl	1	1896	1482	1	4	1
982	8 Frame	1	1898	1405	1	4	2
983	8 Aluminum / Vinyl	1	1920	1179	1	3	1
984	9 Aluminum / Vinyl	2	2001	2421	1	3	2
985	9 Aluminum / Vinyl	2	1978	1826	1	3	1
986	9 Aluminum / Vinyl	2	1996	1503	1	3	2
987	9 Frame	1	1938	711	1	2	1
988	9 Stone	1	1958	1750	1	3	1
989	9 Frame	1	1965	1227	1	3	1
990	9 Aluminum / Vinyl	1	1971	1200	1	3	1
991	9 Frame	1	1972	1200	1	4	1
992	9 Aluminum / Vinyl	1	1972	1120	1	3	1
993	9 Aluminum / Vinyl	1	1966	1107	1	3	1
994	9 Frame	1	1957	1080	1	3	1
995	9 Aluminum / Vinyl	1	1956	1064	1	3	1

996	9	Aluminum / Vinyl	1	1968	1063	1	3	1
997	9	Brick	1	1958	973	1	3	1
998	9	Brick	1	1958	927	1	3	1
999	9	Frame	1	1974	906	1	3	1
1000	10	Brick	1	1942	1624	1	3	1
1001	10	Aluminum / Vinyl	1	1952	1389	1	3	1
1002	10	Aluminum / Vinyl	1.5	1951	1353	1	3	2
1003	10	Brick	1	1947	1319	1	3	1
1004	10	Aluminum / Vinyl	1	1947	1275	1	3	1
1005	10	Frame	1	1952	1217	1	3	1
1006	10	Aluminum / Vinyl	1	1951	1119	1	3	1
1007	10	Aluminum / Vinyl	1	1947	1101	1	3	1
1008	10	Aluminum / Vinyl	1	1948	982	1	3	1
1009	10	Frame	2	1957	1980	1	3	2
1010	10	Aluminum / Vinyl	2	2004	1459	1	3	2
1011	10	Masonry / Frame	2	1926	1407	1	3	1
1012	10	Masonry / Frame	2	1929	2422	2	4	2
1013	10	Brick	1.5	1926	2365	2	4	2
1014	10	Aluminum / Vinyl	2	1928	2330	2	4	2
1015	10	Aluminum / Vinyl	1.5	1924	1830	2	4	2
1016	10	Aluminum / Vinyl	1.5	1929	1797	2	4	2
1017	10	Aluminum / Vinyl	2	1940	2012	2	4	2
1018	10	Brick	2	1952	1944	2	4	2
1019	10	Aluminum / Vinyl	2	1956	1872	2	4	2
1020	10	Aluminum / Vinyl	1	1926	1565	1	3	2
1021	10	Frame	1	1928	1452	1	4	1
1022	10	Frame	1	1928	1200	1	4	1
1023	10	Frame	1	1925	1188	1	2	1
1024	10	Aluminum / Vinyl	1	1927	1151	1	3	1
1025	10	Aluminum / Vinyl	1	1953	1384	1	3	1
1026	10	Aluminum / Vinyl	1.5	1904	1568	1	4	2
1027	10	Aluminum / Vinyl	1	1925	1448	1	3	1
1028	10	Aluminum / Vinyl	1	1905	1363	1	4	1
1029	10	Aluminum / Vinyl	1.5	1925	1215	1	3	1
1030	10	Aluminum / Vinyl	1	1910	936	1	2	2
1031	11	Stone	1	1938	1517	1	3	1
1032	11	Brick	1	1936	1412	1	3	1
1033	11	Stone	1	1942	1325	1	3	1
1034	11	Brick	1	1952	1264	1	2	1
1035	11	Brick	1	1955	1207	1	3	2
1036	11	Aluminum / Vinyl	1	1955	1193	1	4	1
1037	11	Brick	1	1953	1091	1	3	1
1038	11	Aluminum / Vinyl	1	1952	1034	1	3	1

1039	11	Aluminum / Vinyl	1	1952	983	1	3	1
1040	11	Aluminum / Vinyl	2	1954	1450	1	3	2
1041	11	Masonry / Frame	1.5	1964	2330	2	5	3
1042	11	Frame	1.5	1929	1904	2	3	2
1043	11	Aluminum / Vinyl	1	1959	1615	1	3	2
1044	11	Aluminum / Vinyl	1	1964	1334	1	3	1
1045	11	Brick	1	1957	1284	1	3	1
1046	11	Aluminum / Vinyl	1	1959	1257	1	3	1
1047	11	Block	1	1949	1244	1	2	1
1048	11	Brick	1	1958	1184	1	3	1
1049	11	Aluminum / Vinyl	1	1966	1174	1	3	1
1050	11	Brick	1	1956	1170	1	2	1
1051	11	Aluminum / Vinyl	1	1953	1158	1	3	1
1052	11	Brick	1	1955	1153	1	3	1
1053	11	Stone	1	1954	1138	1	2	1
1054	11	Aluminum / Vinyl	1	1957	1128	1	3	1
1055	11	Brick	1	1959	1120	1	3	1
1056	11	Brick	1	1954	1084	1	3	1
1057	11	Stone	1	1951	1059	1	2	1
1058	11	Brick	1	1958	1033	1	3	1
1059	11	Brick	1	1959	1031	1	3	1
1060	11	Brick	1	1959	1022	1	3	1
1061	11	Brick	1	1959	1022	1	3	1
1062	11	Aluminum / Vinyl	1	1956	1019	1	3	1
1063	11	Aluminum / Vinyl	1	1953	887	1	3	1
1064	11	Aluminum / Vinyl	1	1953	879	1	3	1
1065	11	Aluminum / Vinyl	1	1956	876	1	3	1
1066	11	Aluminum / Vinyl	1	1953	874	1	3	1
1067	11	Brick	1	1953	831	1	2	1
1068	11	Block	1	1945	742	1	2	1
1069	11	Brick	1	1969	1206	1	2	1
1070	11	Aluminum / Vinyl	2	1975	2478	2	6	2
1071	12	Aluminum / Vinyl	1	1900	1086	1	3	1
1072	12	Aluminum / Vinyl	1	1965	1104	1	3	1
1073	12	Brick	2	1922	1792	1	3	1
1074	12	Aluminum / Vinyl	1	1892	1597	1	4	1
1075	12	Aluminum / Vinyl	1	1905	1201	1	4	2
1077	13	Brick	1.5	1950	1504	1	3	2
1078	13	Stone	1	1947	1162	1	3	1
1079	13	Stucco	1	1939	1094	1	4	1
1080	13	Aluminum / Vinyl	1.5	1940	1002	1	3	1
1081	13	Brick	1	1954	883	1	2	1
1082	13	Aluminum / Vinyl	1.5	1949	1941	2	3	2

1083	13	Aluminum / Vinyl	2	1950	1502	2	4	2
1084	13	Aluminum / Vinyl	1	1926	1542	1	3	1
1085	13	Aluminum / Vinyl	1	1915	1338	1	3	1
1086	13	Aluminum / Vinyl	1	1925	1134	1	3	1
1087	13	Brick	1	1969	1837	1	3	1
1088	13	Brick	1	1960	1493	1	3	2
1089	13	Aluminum / Vinyl	1	1967	1433	1	3	1
1090	13	Brick	1	1959	1140	1	3	1
1091	13	Brick	1	1964	1116	1	3	2
1092	13	Aluminum / Vinyl	1	1981	1078	1	3	1
1093	13	Aluminum / Vinyl	1	1981	1066	1	3	1
1094	13	Aluminum / Vinyl	1	1961	1062	1	3	1
1095	13	Brick	1	1956	1051	1	3	1
1096	13	Aluminum / Vinyl	1	1960	972	1	3	1
1097	13	Aluminum / Vinyl	1	1959	956	1	3	1
1098	13	Aluminum / Vinyl	1	1960	942	1	3	1
1099	13	Aluminum / Vinyl	1	1953	900	1	3	1
1100	13	Brick	1	1955	811	1	2	1
1101	13	Frame	1	1953	745	1	2	1
1102	13	Aluminum / Vinyl	1	1947	672	1	2	1
1103	13	Aluminum / Vinyl	1	1932	1294	1	3	1
1104	14	Stone	1	1949	1407	1	2	2
1105	14	Aluminum / Vinyl	1	1947	1235	1	3	1
1106	14	Aluminum / Vinyl	1	1947	1107	1	3	1
1107	14	Aluminum / Vinyl	1	1953	1102	1	3	1
1108	14	Frame	1	1953	978	1	3	1
1109	14	Aluminum / Vinyl	1	1944	959	1	3	1
1110	14	Aluminum / Vinyl	1	1944	942	1	3	1
1111	14	Aluminum / Vinyl	1	1910	2015	1	3	1
1112	14	Aluminum / Vinyl	1	1898	810	1	2	1
1113	14	Aluminum / Vinyl	1	1898	810	1	2	1
1114	14	Aluminum / Vinyl	1	1895	796	1	2	1
1115	14	Aluminum / Vinyl	2	1926	2134	2	4	2
1116	14	Frame	1.5	1920	2062	2	4	2
1117	14	Aluminum / Vinyl	1.5	1922	1990	2	5	2
1118	14	Aluminum / Vinyl	1.5	1926	1943	2	5	2
1119	14	Stone	2	1939	2627	2	3	2
1120	14	Aluminum / Vinyl	2	1899	2525	2	6	2
1121	14	Aluminum / Vinyl	2	1892	1560	2	4	2
1122	14	Aluminum / Vinyl	2	1890	2548	2	5	2
1123	14	Brick	1	1930	2024	1	5	1
1124	14	Brick	1	1926	1711	1	4	1
1125	14	Brick	1	1929	1528	1	3	2

1126	14	Aluminum / Vinyl	1	1925	1340	1	3	1
1127	14	Brick	1	1968	1203	1	3	1
1128	14	Aluminum / Vinyl	1	1953	1056	1	2	1
1129	14	Aluminum / Vinyl	1	1931	866	1	2	1
1130	14	Aluminum / Vinyl	1	1947	791	1	2	1
1131	14	Masonry / Frame	2	1903	3896	1	5	0
1132	14	Stucco	2	1910	2248	1	5	2
1133	14	Aluminum / Vinyl	1	1914	1326	1	4	1
1134	14	Aluminum / Vinyl	1.5	1900	1057	1	3	1
1135	14	Frame	1.5	1925	765	1	1	1
1136	15	Aluminum / Vinyl	2	1996	1667	1	3	1
1137	15	Stucco	2	1914	2464	2	6	3
1138	15	Aluminum / Vinyl	1	1921	1397	1	3	1
1139	15	Frame	1	1890	949	1	3	1
1140	1	Aluminum / Vinyl	1.5	1938	1603	1	3	2
1141	1	Stucco	1	1950	1120	1	4	1
1142	1	Brick	1	1929	1420	1	3	1
1143	1	Aluminum / Vinyl	1	1929	1394	1	4	1
1144	1	Aluminum / Vinyl	1	1928	1205	1	4	1
1145	1	Aluminum / Vinyl	1	1929	798	1	2	1
1146	1	Aluminum / Vinyl	1	1958	1234	1	3	1
1147	1	Aluminum / Vinyl	1	1960	1151	1	3	1
1148	1	Aluminum / Vinyl	1	1951	720	1	2	1
1149	1	Aluminum / Vinyl	1	1951	713	1	2	1
1150	1	Stucco	1	1951	698	1	2	1
1151	1	Brick	1.5	1927	1105	1	2	1
1152	2	Aluminum / Vinyl	2	2003	2797	1	5	3
1153	2	Aluminum / Vinyl	2	2002	2706	1	4	2
1154	2	Stone	1	1952	1356	1	3	1
1155	2	Aluminum / Vinyl	1	1965	1223	1	3	1
1156	2	Aluminum / Vinyl	1	1966	1216	1	3	1
1157	2	Aluminum / Vinyl	1	1965	1149	1	3	1
1158	2	Aluminum / Vinyl	1	1960	1027	1	3	1
1159	2	Aluminum / Vinyl	1	1956	1019	1	3	1
1160	2	Brick	1	1957	947	1	2	1
1161	2	Aluminum / Vinyl	1	1958	936	1	3	1
1162	2	Aluminum / Vinyl	1	1957	909	1	3	1
1163	2	Aluminum / Vinyl	1	1957	903	1	3	1
1164	2	Aluminum / Vinyl	1	1957	873	1	2	1
1165	2	Frame	1	1955	864	1	3	1
1166	3	Brick	2	1935	2865	1	5	3
1167	3	Aluminum / Vinyl	2	1895	1806	2	4	2
1168	3	Frame	1	1916	1993	1	5	2

1169	3	Frame	2	1903	1804	1	5	1
1170	3	Aluminum / Vinyl	2	1889	2513	2	6	2
1171	5	Brick	1	1951	1642	1	3	2
1172	5	Stone	1	1951	1518	1	2	1
1173	5	Brick	1	1950	1432	1	3	1
1174	5	Brick	1.5	1937	1364	1	4	1
1175	5	Brick	1	1949	1359	1	3	1
1176	5	Aluminum / Vinyl	1	1953	1346	1	3	1
1177	5	Aluminum / Vinyl	1	1948	1341	1	4	1
1178	5	Brick	1	1951	1278	1	3	1
1179	5	Brick	1	1951	1278	1	3	1
1180	5	Frame	1	1952	1264	1	3	2
1181	5	Aluminum / Vinyl	1.5	1949	1238	1	4	1
1182	5	Aluminum / Vinyl	1	1952	1190	1	3	1
1183	5	Aluminum / Vinyl	1	1942	1165	1	2	1
1184	5	Brick	1	1951	1164	1	3	1
1185	5	Aluminum / Vinyl	1	1949	1140	1	3	1
1186	5	Brick	1	1950	1123	1	3	1
1187	5	Aluminum / Vinyl	1	1950	1070	1	3	1
1188	5	Aluminum / Vinyl	1	1948	1051	1	3	1
1189	5	Aluminum / Vinyl	1	1951	1050	1	3	1
1190	5	Aluminum / Vinyl	1	1953	1030	1	4	1
1191	5	Aluminum / Vinyl	1	1952	1014	1	3	1
1192	5	Aluminum / Vinyl	1	1954	964	1	3	1
1193	5	Aluminum / Vinyl	1	1950	906	1	3	2
1194	5	Aluminum / Vinyl	1	1955	840	1	2	1
1195	5	Fiber-Cement	2	2000	2573	1	4	3
1196	5	Aluminum / Vinyl	2	1953	1768	1	3	1
1197	5	Stone	1	1928	1889	2	3	2
1198	5	Masonry / Frame	2	1959	2783	2	6	2
1199	5	Brick	2	1952	2410	2	5	2
1200	5	Brick	2	1955	2278	2	4	2
1201	5	Brick	1	1953	1915	1	2	2
1202	5	Brick	1	1960	1281	1	3	1
1203	5	Aluminum / Vinyl	1	1958	1264	1	3	1
1204	5	Aluminum / Vinyl	1	1959	1217	1	3	1
1205	5	Aluminum / Vinyl	1	1980	1199	1	3	1
1206	5	Brick	1	1957	1188	1	3	1
1207	5	Aluminum / Vinyl	1	1955	1132	1	3	1
1208	5	Brick	1	1961	1075	1	3	1
1209	5	Aluminum / Vinyl	1	1952	1064	1	2	1
1210	5	Brick	1	1950	1032	1	3	1
1211	5	Aluminum / Vinyl	1	1956	1027	1	3	1

1212	5	Brick	1	1959	986	1	3	1
1213	5	Aluminum / Vinyl	1	1954	984	1	3	1
1214	5	Aluminum / Vinyl	1	1954	981	1	2	1
1215	5	Aluminum / Vinyl	1	1955	970	1	3	1
1216	6	Aluminum / Vinyl	1.5	1923	1896	2	3	2
1217	6	Aluminum / Vinyl	1	1925	1384	1	2	1
1218	6	Aluminum / Vinyl	1	1895	1088	1	3	1
1219	7	Stone	1	1937	1762	1	5	2
1220	7	Stone	1	1935	1397	1	3	1
1221	7	Aluminum / Vinyl	1	1938	1296	1	2	1
1222	7	Stucco	1.5	1937	1127	1	2	1
1223	7	Aluminum / Vinyl	1	1953	1008	1	2	1
1224	7	Aluminum / Vinyl	1	1927	856	1	3	1
1225	7	Masonry / Frame	2	1930	2782	2	4	2
1226	7	Stone	2	1939	2560	2	4	2
1227	7	Aluminum / Vinyl	1.5	1957	2002	2	5	2
1228	7	Stone	1	1939	951	1	2	1
1229	7	Brick	1	1950	752	1	2	1
1230	8	Aluminum / Vinyl	1	1940	896	1	2	1
1231	8	Aluminum / Vinyl	2	1908	3356	2	8	2
1232	8	Frame	2	1912	2138	2	5	2
1233	8	Aluminum / Vinyl	1.5	1916	1760	2	5	2
1234	8	Frame	1.5	1906	1365	2	3	2
1235	8	Aluminum / Vinyl	1	1928	1612	1	4	1
1236	8	Aluminum / Vinyl	1.5	1899	1767	1	3	2
1237	8	Aluminum / Vinyl	1	1902	961	1	4	1
1238	9	Aluminum / Vinyl	2	2009	2220	1	4	2
1239	9	Aluminum / Vinyl	2	1967	1602	1	4	1
1240	9	Aluminum / Vinyl	1	2005	1920	1	3	3
1241	9	Stone	1	1958	1750	1	3	1
1242	9	Aluminum / Vinyl	1	1978	1327	1	3	1
1243	9	Aluminum / Vinyl	1	1966	1227	1	3	1
1244	9	Aluminum / Vinyl	1	1981	1209	1	3	2
1245	9	Frame	1	1962	1177	1	3	1
1246	9	Aluminum / Vinyl	1	1967	1063	1	3	1
1247	9	Brick	1	1959	992	1	3	1
1248	9	Aluminum / Vinyl	2	1980	2464	2	6	2
1249	10	Brick	1.5	1939	1619	1	3	2
1250	10	Aluminum / Vinyl	1.5	1939	1573	1	3	1
1251	10	Brick	1	1953	1389	1	3	1
1252	10	Brick	1	1947	1127	1	3	1
1253	10	Stone	1	1941	1120	1	2	1
1254	10	Frame	1.5	1939	1116	1	2	1

1255	10	Brick	1	1946	1038	1	3	1
1256	10	Brick	1	1951	1033	1	3	1
1257	10	Aluminum / Vinyl	1	1952	728	1	2	1
1258	10	Masonry / Frame	2	1952	1486	1	3	1
1259	10	Aluminum / Vinyl	2	1938	1134	1	2	1
1260	10	Aluminum / Vinyl	1.5	1927	1947	2	3	2
1261	10	Brick	1.5	1929	1945	2	3	2
1262	10	Masonry / Frame	2	1952	2688	2	6	2
1263	10	Aluminum / Vinyl	1.5	1926	1708	1	4	3
1264	10	Aluminum / Vinyl	1	1924	1701	1	4	1
1265	10	Aluminum / Vinyl	1	1919	1632	1	5	2
1266	10	Brick	1	1923	1557	1	4	1
1267	10	Aluminum / Vinyl	1	1926	1424	1	3	1
1268	10	Aluminum / Vinyl	1	1926	1404	1	3	1
1269	10	Aluminum / Vinyl	1	1919	1314	1	4	1
1270	10	Aluminum / Vinyl	1	1927	1062	1	2	1
1271	10	Brick	1	1931	1053	1	2	1
1272	10	Aluminum / Vinyl	1	1919	1027	1	4	1
1273	10	Aluminum / Vinyl	1	1926	982	1	2	1
1274	10	Aluminum / Vinyl	1	1926	923	1	2	1
1275	10	Brick	1	1955	1488	1	4	1
1276	10	Brick	1	1954	1278	1	3	1
1277	10	Aluminum / Vinyl	1	1950	743	1	2	1
1278	10	Aluminum / Vinyl	1	1955	692	1	2	1
1279	10	Aluminum / Vinyl	1	1920	1304	1	3	1
1280	10	Frame	1	1924	1175	1	3	2
1281	10	Aluminum / Vinyl	1	1923	1008	1	3	1
1282	10	Brick	1	1923	880	1	2	1
1283	10	Aluminum / Vinyl	1	1921	768	1	2	1
1284	10	Stone	1.5	1931	1837	1	3	1
1285	10	Stone	1.5	1931	1837	1	3	1
1286	11	Aluminum / Vinyl	1	1952	1833	1	4	2
1287	11	Stone	1	1951	1710	1	2	1
1288	11	Aluminum / Vinyl	1	1956	1611	1	4	1
1289	11	Stone	1.5	1950	1598	1	3	1
1290	11	Aluminum / Vinyl	1	1950	1588	1	3	2
1291	11	Aluminum / Vinyl	1	1953	1325	1	3	3
1292	11	Brick	1	1949	1294	1	3	2
1293	11	Aluminum / Vinyl	1	1959	1159	1	4	1
1294	11	Aluminum / Vinyl	1	1954	1142	1	4	2
1295	11	Aluminum / Vinyl	1	1949	1032	1	3	1
1296	11	Aluminum / Vinyl	1	1942	1023	1	3	1
1297	11	Brick	1	1950	975	1	2	1

1298	11	Stone	2	1945	1858	1	3	1
1299	11	Aluminum / Vinyl	2	1956	1540	1	3	1
1300	11	Brick	2	1936	1448	1	3	1
1301	11	Aluminum / Vinyl	1.5	1968	1985	2	5	2
1302	11	Brick	1	1966	1443	1	3	1
1303	11	Aluminum / Vinyl	1	1942	1411	1	3	2
1304	11	Brick	1	1967	1383	1	3	1
1305	11	Brick	1	1958	1350	1	3	1
1306	11	Brick	1	1966	1264	1	3	1
1307	11	Aluminum / Vinyl	1	1959	1250	1	3	1
1308	11	Brick	1	1959	1225	1	2	1
1309	11	Aluminum / Vinyl	1	1962	1169	1	3	1
1310	11	Brick	1	1960	1144	1	3	1
1311	11	Brick	1	1959	1135	1	3	1
1312	11	Brick	1	1959	1131	1	3	2
1313	11	Brick	1	1959	1126	1	3	1
1314	11	Aluminum / Vinyl	1	1965	1107	1	3	1
1315	11	Aluminum / Vinyl	1	1959	1080	1	3	1
1316	11	Brick	1	1972	1078	1	1	2
1317	11	Aluminum / Vinyl	1	1962	1058	1	3	1
1318	11	Frame	1	1957	1053	1	3	1
1319	11	Brick	1	1959	1023	1	3	1
1320	11	Stone	1	1955	1015	1	3	1
1321	11	Brick	1	1953	1013	1	3	1
1322	11	Aluminum / Vinyl	1	1942	1008	1	3	1
1323	11	Aluminum / Vinyl	1	1956	973	1	2	1
1324	11	Frame	1	1953	962	1	2	1
1325	11	Aluminum / Vinyl	1	1953	956	1	3	1
1326	11	Aluminum / Vinyl	1	1960	931	1	3	1
1327	11	Brick	1	1956	923	1	3	1
1328	11	Frame	1	1951	886	1	2	1
1329	11	Aluminum / Vinyl	1	1953	864	1	3	1
1330	11	Aluminum / Vinyl	1	1956	864	1	3	1
1331	11	Aluminum / Vinyl	1	1942	794	1	2	1
1332	11	Block	1	1945	781	1	2	2
1333	11	Aluminum / Vinyl	1	1951	644	1	2	1
1334	11	Brick	1.5	1918	1616	1	2	1
1335	12	Aluminum / Vinyl	2	2006	1684	1	4	2
1336	12	Aluminum / Vinyl	1	1899	1191	1	3	2
1337	12	Aluminum / Vinyl	1	1900	1178	1	3	1
1338	12	Aluminum / Vinyl	1	1900	978	1	3	1
1339	12	Aluminum / Vinyl	1	1905	1496	2	4	2
1340	12	Aluminum / Vinyl	1.5	1873	1692	1	4	2

1341	12	Stucco	1	1903	1024	1	3	1
1343	12	Frame	2	1900	2766	3	7	3
1344	13	Brick	1	1955	1583	1	4	2
1345	13	Brick	1	1952	1400	1	4	1
1346	13	Brick	1	1950	1377	1	3	2
1347	13	Brick	1	1950	1172	1	2	1
1348	13	Aluminum / Vinyl	1	1961	1160	1	4	1
1349	13	Brick	1	1951	1142	1	3	1
1350	13	Stone	1	1950	1109	1	3	1
1351	13	Brick	1.5	1936	1078	1	2	1
1352	13	Aluminum / Vinyl	1	1947	1046	1	3	1
1353	13	Brick	1	1953	1042	1	3	1
1354	13	Aluminum / Vinyl	1	1947	834	1	2	1
1355	13	Aluminum / Vinyl	1	1906	1320	1	4	2
1356	13	Aluminum / Vinyl	1.5	1885	1143	1	2	1
1357	13	Brick	1.5	1925	2224	2	5	2
1358	13	Masonry / Frame	2	1949	1800	2	4	2
1359	13	Aluminum / Vinyl	2	1950	1417	2	3	2
1360	13	Frame	1	1927	1324	1	3	2
1361	13	Brick	1	1968	1539	1	2	2
1362	13	Aluminum / Vinyl	1	1974	1324	1	3	1
1363	13	Brick	1	1961	1196	1	3	1
1364	13	Aluminum / Vinyl	1	1963	1148	1	3	1
1365	13	Aluminum / Vinyl	1	1950	1102	1	2	1
1366	13	Brick	1	1960	1064	1	3	1
1367	13	Brick	1	1961	1036	1	3	2
1368	13	Aluminum / Vinyl	1	1959	970	1	3	1
1369	13	Aluminum / Vinyl	1	1953	744	1	2	1
1370	13	Aluminum / Vinyl	1	1950	699	1	2	1
1371	13	Aluminum / Vinyl	1	1955	672	1	2	1
1372	13	Frame	1	1929	1130	1	2	1
1373	14	Aluminum / Vinyl	1	1951	1098	1	4	1
1374	14	Brick	2	1940	1838	1	3	1
1375	14	Aluminum / Vinyl	2	2006	1682	1	3	2
1376	14	Aluminum / Vinyl	2	1941	1213	1	2	1
1377	14	Aluminum / Vinyl	2	1950	986	1	2	1
1378	14	Aluminum / Vinyl	1	1896	1127	1	3	1
1379	14	Aluminum / Vinyl	1	1898	864	1	2	1
1380	14	Aluminum / Vinyl	1.5	1930	2152	2	5	2
1381	14	Aluminum / Vinyl	1.5	1925	1873	2	4	2
1382	14	Aluminum / Vinyl	1.5	1927	1626	2	3	2
1383	14	Aluminum / Vinyl	1.5	1925	1410	2	3	2
1384	14	Block	1.5	1900	1761	2	4	2

1385	14	Aluminum / Vinyl	1.5	1921	1627	1	3	2
1386	14	Brick	1.5	1930	2062	1	4	2
1387	14	Aluminum / Vinyl	1	1924	1931	1	5	2
1388	14	Brick	1	1925	1774	1	3	1
1389	14	Aluminum / Vinyl	1.5	1920	1155	1	3	1
1390	14	Aluminum / Vinyl	1	1927	1060	1	2	1
1391	14	Aluminum / Vinyl	1	1964	1792	1	3	1
1392	14	Aluminum / Vinyl	1	1951	1056	1	3	1
1393	14	Aluminum / Vinyl	1	1969	973	1	2	1
1394	14	Aluminum / Vinyl	1	1941	934	1	2	1
1395	14	Aluminum / Vinyl	1	1941	853	1	2	1
1396	14	Aluminum / Vinyl	1	1950	725	1	2	1
1397	14	Aluminum / Vinyl	1	1948	679	1	2	1
1398	14	Stucco	1	1952	672	1	1	1
1399	14	Prem Wood	1	1905	1479	1	2	1
1400	14	Aluminum / Vinyl	1	1899	1419	1	3	2
1401	14	Aluminum / Vinyl	1.5	1922	1386	1	2	3
1402	14	Frame	1	1904	1315	1	2	1
1403	14	Aluminum / Vinyl	1	1916	1191	1	3	1
1404	14	Aluminum / Vinyl	1	1922	1060	1	3	1
1405	14	Frame	1.5	1921	1002	1	2	1
1406	14	Brick	1	1932	888	1	2	1
1407	14	Aluminum / Vinyl	1	1925	829	1	2	1
1408	14	Brick	2	1954	1769	2	4	2
1409	15	Aluminum / Vinyl	1.5	1900	1771	1	4	2
1410	15	Aluminum / Vinyl	1	1890	1425	1	4	1
1411	15	Frame	1	1891	1124	1	4	1
1412	15	Masonry / Frame	2	1928	2922	1	5	2
1413	1	Stone	1	1946	1670	1	4	1
1414	1	Aluminum / Vinyl	1	1964	1213	1	3	1
1415	1	Frame	1	1952	1144	1	3	1
1416	1	Aluminum / Vinyl	2	1924	1171	1	2	2
1417	1	Aluminum / Vinyl	1	1927	957	1	4	1
1418	2	Brick	1	1956	1090	1	3	1
1419	2	Masonry / Frame	2	1959	1635	1	3	1
1420	2	Frame	1	1925	640	1	2	1
1421	2	Brick	1.5	1958	2013	2	5	2
1422	2	Brick	1	1958	1287	1	3	1
1423	2	Aluminum / Vinyl	1	1955	1284	1	2	1
1424	2	Brick	1	1958	1215	1	3	1
1425	2	Aluminum / Vinyl	1	1960	1183	1	3	1
1426	2	Brick	1	1959	1153	1	3	1
1427	2	Frame	1	1971	948	1	3	1

1428	2	Aluminum / Vinyl	1	1958	938	1	3	1
1429	2	Aluminum / Vinyl	1	1955	936	1	3	1
1430	2	Frame	1	1955	864	1	3	1
1431	3	Fiber-Cement	2	1890	1852	1	5	3
1432	3	Frame	2	1922	2196	2	4	2
1433	3	Aluminum / Vinyl	1.5	1889	1680	2	5	2
1434	3	Frame	1.5	1901	1643	2	4	2
1435	3	Frame	1.5	1895	1557	2	4	1
1436	3	Aluminum / Vinyl	1	1926	1384	1	4	1
1437	3	Frame	2	1897	4077	1	5	3
1438	3	Stucco	2	1920	3037	1	5	3
1439	3	Brick	2	1922	2242	1	4	2
1440	3	Aluminum / Vinyl	1.5	1890	1408	1	3	2
1441	3	Aluminum / Vinyl	1.5	1891	1291	1	3	2
1442	3	Stucco	2	1911	3486	1	5	2
1443	4	Brick	2	1885	4140	2	6	2
1444	5	Brick	1	1948	1473	1	4	2
1445	5	Brick	1	1948	1274	1	3	1
1446	5	Brick	1	1953	1261	1	3	1
1447	5	Aluminum / Vinyl	1	1949	1255	1	3	1
1448	5	Aluminum / Vinyl	1	1951	1255	1	3	1
1449	5	Aluminum / Vinyl	1	1948	1142	1	3	1
1450	5	Brick	1	1949	1125	1	2	1
1451	5	Brick	1	1949	1086	1	3	1
1452	5	Aluminum / Vinyl	1	1946	1048	1	3	1
1453	5	Aluminum / Vinyl	1	1952	1005	1	3	1
1454	5	Aluminum / Vinyl	1	1941	921	1	3	1
1455	5	Masonry / Frame	2	1951	1473	1	3	1
1456	5	Masonry / Frame	2	1939	1188	1	3	1
1457	5	Brick	1	1950	2411	2	4	2
1458	5	Masonry / Frame	2	1959	2386	2	6	2
1459	5	Brick	1.5	1952	2156	2	5	2
1460	5	Stone	1	1950	1922	1	2	2
1461	5	Masonry / Frame	1	1961	1749	1	3	1
1462	5	Aluminum / Vinyl	1	2004	1672	1	3	2
1463	5	Frame	1	1956	1498	1	3	1
1464	5	Brick	1	1948	1426	1	3	1
1465	5	Brick	1	1956	1388	1	3	1
1466	5	Aluminum / Vinyl	1	1957	1384	1	4	1
1467	5	Aluminum / Vinyl	1	1963	1120	1	3	1
1468	5	Brick	1	1949	1053	1	2	1
1469	5	Aluminum / Vinyl	1	1956	1051	1	3	1
1470	5	Aluminum / Vinyl	1	1955	1050	1	3	1

1471	5	Brick	1	1951	1016	1	3	1
1472	5	Aluminum / Vinyl	1	1949	989	1	2	1
1473	5	Aluminum / Vinyl	1	1954	962	1	3	1
1474	5	Brick	1	1955	935	1	2	2
1475	5	Brick	1	1951	744	1	2	1
1476	5	Aluminum / Vinyl	1.5	1925	1019	1	3	1
1477	6	Aluminum / Vinyl	1.5	1924	1807	2	4	2
1478	6	Aluminum / Vinyl	1	1919	1313	1	2	1
1479	6	Frame	1	1925	1212	1	3	1
1480	6	Aluminum / Vinyl	2	1963	956	1	3	1
1481	7	Aluminum / Vinyl	1.5	1939	1315	1	3	1
1482	7	Brick	1	1937	941	1	3	1
1483	7	Aluminum / Vinyl	1	1949	678	1	2	1
1484	7	Stone	2	1944	2408	2	4	2
1485	7	Aluminum / Vinyl	1.5	1926	2045	2	4	2
1486	7	Aluminum / Vinyl	1.5	1913	1712	2	4	2
1487	7	Frame	1	1925	1593	1	3	1
1488	7	Brick	1	1927	1589	1	4	1
1489	7	Brick	1.5	1934	1604	1	3	1
1490	8	Aluminum / Vinyl	1	1900	1031	1	3	1
1491	8	Aluminum / Vinyl	1.5	1913	2019	2	4	2
1492	8	Frame	1.5	1918	1809	2	3	2
1493	8	Aluminum / Vinyl	1	1924	1556	1	4	2
1494	8	Stucco	1	1920	1458	1	5	1
1495	8	Frame	2	1924	1762	1	3	3
1496	8	Aluminum / Vinyl	1.5	1900	1637	1	5	2
1497	8	Aluminum / Vinyl	1	1909	1576	1	5	1
1498	8	Aluminum / Vinyl	1.5	1920	1024	1	3	1
1499	8	Stucco	1.5	1910	2816	3	6	3
1500	9	Aluminum / Vinyl	1	1957	1482	1	4	1
1501	9	Aluminum / Vinyl	1	1964	1390	1	4	1
1502	9	Aluminum / Vinyl	1	1969	1325	1	3	1
1503	9	Aluminum / Vinyl	1	1978	1320	1	3	1
1504	9	Brick	1	1957	1131	1	3	1
1505	9	Aluminum / Vinyl	1	1962	1074	1	3	1
1506	10	Frame	1	1952	1291	1	3	1
1507	10	Aluminum / Vinyl	1	1942	1247	1	3	2
1508	10	Stone	1	1945	1113	1	3	1
1509	10	Aluminum / Vinyl	1	1942	968	1	3	1
1510	10	Aluminum / Vinyl	1	1952	728	1	2	1
1511	10	Stone	2	1941	1894	1	3	1
1512	10	Brick	2	1938	1694	1	3	1
1513	10	Aluminum / Vinyl	2	1921	1657	1	3	1

1514	10	Aluminum / Vinyl	2	1926	1271	1	3	1
1515	10	Aluminum / Vinyl	1	1927	872	1	1	1
1516	10	Brick	1.5	1928	2108	2	5	2
1517	10	Brick	1	1925	1975	2	3	3
1518	10	Aluminum / Vinyl	2	1923	1918	2	4	2
1519	10	Brick	1.5	1929	1821	2	4	2
1520	10	Brick	2	1967	2104	2	4	2
1521	10	Stone	2	1945	2026	2	4	2
1522	10	Stone	2	1945	2026	2	4	2
1523	10	Aluminum / Vinyl	1	1928	1279	1	3	1
1524	10	Aluminum / Vinyl	1	1929	1253	1	3	1
1525	10	Brick	1	1922	1221	1	3	1
1526	10	Stone	1	1949	1370	1	2	1
1527	10	Stone	1	1949	1011	1	2	1
1528	10	Aluminum / Vinyl	1	1949	808	1	2	1
1529	10	Stucco	1	1916	1397	1	3	1
1530	10	Aluminum / Vinyl	1	1923	990	1	4	1
1531	10	Frame	1	1925	870	1	1	1
1532	10	Frame	2	1928	2990	3	5	3
1533	10	Brick	2	1928	3178	1	5	3
1534	10	Brick	1	1928	1413	1	2	1
1535	11	Aluminum / Vinyl	1	1963	1696	1	4	2
1536	11	Aluminum / Vinyl	1.5	1940	1467	1	3	1
1537	11	Brick	1	1952	1400	1	4	1
1538	11	Brick	1	1950	1320	1	4	1
1539	11	Stone	1	1953	1246	1	3	1
1540	11	Brick	1	1950	1225	1	3	1
1541	11	Brick	1	1938	1205	1	3	1
1542	11	Aluminum / Vinyl	1	1949	1183	1	3	1
1543	11	Aluminum / Vinyl	1	1952	1082	1	4	1
1544	11	Aluminum / Vinyl	1	1946	1036	1	3	1
1545	11	Aluminum / Vinyl	1	1953	1004	1	3	1
1546	11	Aluminum / Vinyl	1	1958	934	1	3	1
1547	11	Brick	1	1940	887	1	2	1
1548	11	Aluminum / Vinyl	1	1955	800	1	2	1
1549	11	Stone	2	1932	2942	1	4	1
1550	11	Aluminum / Vinyl	2	1985	1858	1	4	2
1551	11	Brick	2	1950	1604	1	3	1
1552	11	Stone	2	1937	1584	1	3	1
1553	11	Aluminum / Vinyl	2	1942	1288	1	3	1
1554	11	Aluminum / Vinyl	1.5	1929	1954	2	4	2
1555	11	Masonry / Frame	2	1959	2299	2	6	2
1556	11	Aluminum / Vinyl	1.5	1957	2237	2	5	2

1557	11	Brick	1.5	1956	2114	2	5	3
1558	11	Brick	1.5	1957	1616	2	4	2
1559	11	Aluminum / Vinyl	1	1920	1645	1	4	1
1560	11	Brick	1	1928	1102	1	3	1
1561	11	Brick	1	1964	1806	1	4	2
1562	11	Brick	1	1959	1468	1	3	1
1563	11	Brick	1	1958	1189	1	3	1
1564	11	Brick	1	1955	1153	1	3	1
1565	11	Aluminum / Vinyl	1	1954	1123	1	3	1
1566	11	Brick	1	1954	1112	1	3	1
1567	11	Brick	1	1955	1109	1	3	1
1568	11	Brick	1	1958	1094	1	3	1
1569	11	Brick	1	1959	1091	1	3	1
1570	11	Brick	1	1954	1085	1	3	1
1571	11	Aluminum / Vinyl	1	1950	1072	1	3	1
1572	11	Aluminum / Vinyl	1	1955	1020	1	2	1
1573	11	Brick	1	1952	1013	1	3	1
1574	11	Brick	1	1954	998	1	2	1
1575	11	Stone	1	1950	982	1	3	2
1576	11	Aluminum / Vinyl	1	1955	955	1	2	2
1577	11	Aluminum / Vinyl	1	1952	954	1	2	1
1578	11	Brick	1	1956	940	1	3	1
1579	11	Aluminum / Vinyl	1	1953	879	1	3	1
1580	11	Aluminum / Vinyl	1	1956	864	1	2	1
1581	11	Aluminum / Vinyl	1	1942	833	1	2	1
1582	11	Brick	1	1947	826	1	2	1
1583	11	Aluminum / Vinyl	1	1952	811	1	2	1
1584	11	Aluminum / Vinyl	2	1986	2524	2	4	2
1585	11	Brick	2	1944	1870	2	4	2
1586	12	Frame	2	1913	1692	2	4	2
1587	13	Aluminum / Vinyl	1	1971	1494	1	4	1
1588	13	Brick	1	1954	1619	1	4	1
1589	13	Aluminum / Vinyl	1	1966	1608	1	4	2
1590	13	Block	1	1936	1430	1	4	1
1591	13	Aluminum / Vinyl	1	1942	1242	1	3	1
1592	13	Aluminum / Vinyl	1	1935	1215	1	3	1
1593	13	Aluminum / Vinyl	1	1950	1183	1	3	1
1594	13	Brick	1	1939	1173	1	3	2
1595	13	Aluminum / Vinyl	1	1943	1148	1	3	1
1596	13	Stucco	1	1949	1057	1	3	2
1597	13	Aluminum / Vinyl	1	1958	991	1	3	1
1598	13	Aluminum / Vinyl	1.5	1950	2005	2	3	3
1599	13	Block	1	1912	1572	2	4	2

1600	13	Aluminum / Vinyl	1	1928	1446	1	3	2
1601	13	Aluminum / Vinyl	1	1977	1550	1	3	1
1602	13	Frame	1	1958	1424	1	3	2
1603	13	Aluminum / Vinyl	1	1963	1329	1	3	2
1604	13	Brick	1	1960	1201	1	2	2
1605	13	Brick	1	1956	1189	1	3	1
1606	13	Aluminum / Vinyl	1	1969	1092	1	3	1
1607	13	Frame	1	1960	965	1	3	1
1608	13	Aluminum / Vinyl	1	1950	911	1	3	1
1609	13	Aluminum / Vinyl	1	1954	870	1	2	1
1610	13	Aluminum / Vinyl	1	1947	861	1	2	1
1611	13	Aluminum / Vinyl	1	1940	852	1	2	1
1612	13	Aluminum / Vinyl	1	1947	732	1	2	1
1613	13	Aluminum / Vinyl	1.5	1926	1172	1	4	1
1614	14	Aluminum / Vinyl	1	1939	1238	1	3	2
1615	14	Aluminum / Vinyl	1	1953	1226	1	4	1
1616	14	Aluminum / Vinyl	1	1944	1168	1	3	1
1617	14	Brick	1	1944	1100	1	4	1
1618	14	Aluminum / Vinyl	1	1953	1090	1	4	1
1619	14	Aluminum / Vinyl	1	1950	1040	1	4	1
1620	14	Prem Wood	2	2007	1826	1	4	2
1621	14	Aluminum / Vinyl	2	1938	1320	1	3	1
1622	14	Aluminum / Vinyl	1.5	1900	1356	1	3	2
1623	14	Aluminum / Vinyl	2	1924	2472	2	5	2
1624	14	Brick	2	1932	2208	2	4	2
1625	14	Aluminum / Vinyl	1.5	1923	1875	2	4	2
1626	14	Aluminum / Vinyl	2	1890	2424	2	4	2
1627	14	Brick	1.5	1930	2381	2	3	2
1628	14	Aluminum / Vinyl	2	1925	1848	2	4	2
1629	14	Aluminum / Vinyl	1.5	1910	1680	2	3	2
1630	14	Aluminum / Vinyl	1	1913	1922	2	5	2
1631	14	Aluminum / Vinyl	2	1892	1814	2	4	2
1632	14	Brick	1	1925	2261	1	3	2
1633	14	Stone	1	1933	1650	1	3	1
1634	14	Aluminum / Vinyl	1	1930	1542	1	4	1
1635	14	Aluminum / Vinyl	1	1926	1434	1	3	1
1636	14	Aluminum / Vinyl	1	1910	1372	1	3	1
1637	14	Aluminum / Vinyl	1	1927	1248	1	3	1
1638	14	Brick	1	1928	1145	1	3	1
1639	14	Aluminum / Vinyl	1	1956	1003	1	3	1
1640	14	Aluminum / Vinyl	1	1943	710	1	2	1
1641	14	Frame	1	1908	1519	1	5	2
1642	14	Aluminum / Vinyl	1	1906	1470	1	4	2

1643	14	Aluminum / Vinyl	1.5	1908	1290	1	3	1
1644	14	Aluminum / Vinyl	1.5	1911	1283	1	4	1
1645	14	Aluminum / Vinyl	1	1921	1120	1	3	1
1646	14	Aluminum / Vinyl	1	1890	959	1	2	1
1647	15	Aluminum / Vinyl	1	1922	1962	1	5	2
1648	15	Aluminum / Vinyl	1	1899	1238	1	4	1
1649	1	Brick	1	1937	1466	1	3	2
1650	1	Brick	1	1941	1456	1	4	1
1651	1	Aluminum / Vinyl	1	1946	1384	1	5	1
1652	1	Aluminum / Vinyl	1	1953	1298	1	4	2
1653	1	Aluminum / Vinyl	1.5	1937	1120	1	2	1
1654	1	Aluminum / Vinyl	1.5	1936	1054	1	2	1
1655	1	Aluminum / Vinyl	2	1936	1144	1	3	1
1656	1	Aluminum / Vinyl	2	1914	1835	2	4	2
1657	1	Aluminum / Vinyl	1	1924	1340	1	4	1
1658	1	Aluminum / Vinyl	1	1926	1214	1	3	1
1659	1	Aluminum / Vinyl	1	1955	1082	1	3	1
1660	1	Aluminum / Vinyl	1	1954	963	1	3	1
1661	1	Aluminum / Vinyl	1	1953	870	1	3	1
1662	1	Aluminum / Vinyl	1	1939	795	1	2	1
1663	1	Brick	1	1929	1548	1	4	2
1664	2	Aluminum / Vinyl	1.5	1951	1428	1	4	1
1665	2	Aluminum / Vinyl	1.5	1935	1309	1	5	1
1666	2	Aluminum / Vinyl	1	1952	1073	1	4	1
1667	2	Brick	1	1947	920	1	2	1
1668	2	Aluminum / Vinyl	1	1929	1153	1	3	1
1669	2	Frame	1	1963	1408	1	3	2
1670	2	Frame	1	1966	1308	1	4	1
1671	2	Aluminum / Vinyl	1	1967	1215	1	3	1
1672	2	Aluminum / Vinyl	1	1959	1135	1	3	1
1673	2	Brick	1	1959	1116	1	3	2
1674	2	Aluminum / Vinyl	1	1946	1040	1	2	1
1675	2	Aluminum / Vinyl	1	1956	925	1	3	1
1676	2	Frame	1	1959	910	1	3	1
1677	2	Aluminum / Vinyl	1	1957	886	1	3	1
1678	2	Aluminum / Vinyl	1	1955	864	1	3	1
1679	2	Aluminum / Vinyl	1	1954	864	1	3	1
1680	3	Aluminum / Vinyl	1	1898	1296	1	3	1
1681	3	Aluminum / Vinyl	1	1895	870	1	4	2
1682	3	Aluminum / Vinyl	1.5	1925	2225	2	4	2
1683	3	Frame	2	1920	2016	2	6	2
1684	3	Aluminum / Vinyl	1.5	1917	1761	2	4	2
1685	3	Brick	1	1926	1420	1	3	1

1686	3	Brick	2	1912	3066	1	6	2
1687	3	Stucco	2	1922	1947	1	4	1
1688	3	Stucco	2	1910	1886	1	3	1
1689	3	Stucco	2	1910	1886	1	3	1
1690	3	Stucco	2	1912	1805	1	4	1
1691	3	Aluminum / Vinyl	1	1892	1080	1	3	1
1692	4	Frame	2	1908	2362	1	5	1
1693	5	Stone	1	1951	1417	1	3	1
1694	5	Brick	1	1947	1374	1	3	1
1695	5	Stone	1	1946	1272	1	3	1
1696	5	Aluminum / Vinyl	1	1946	1264	1	3	1
1697	5	Brick	1	1952	1230	1	2	1
1698	5	Brick	1	1952	1166	1	3	2
1699	5	Aluminum / Vinyl	1	1952	981	1	3	1
1700	5	Aluminum / Vinyl	1	1951	980	1	2	1
1701	5	Aluminum / Vinyl	1	1951	980	1	2	1
1702	5	Aluminum / Vinyl	1	1942	812	1	2	1
1703	5	Masonry / Frame	2	1965	2252	1	5	3
1704	5	Aluminum / Vinyl	1.5	1922	1817	2	5	2
1705	5	Brick	1	1956	2458	2	5	2
1706	5	Aluminum / Vinyl	1	1968	1552	1	3	1
1707	5	Stone	1	1956	1535	1	3	1
1708	5	Stone	1	1950	1507	1	4	2
1709	5	Brick	1	1997	1456	1	3	1
1710	5	Aluminum / Vinyl	1	1949	1328	1	2	2
1711	5	Brick	1	1961	1324	1	3	2
1712	5	Brick	1	1958	1180	1	3	1
1713	5	Brick	1	1952	1153	1	2	1
1714	5	Brick	1	1953	1142	1	3	1
1715	5	Aluminum / Vinyl	1	1957	1136	1	3	1
1716	5	Brick	1	1957	1124	1	2	1
1717	5	Brick	1	1959	1107	1	3	1
1718	5	Aluminum / Vinyl	1	1955	1064	1	3	1
1719	5	Aluminum / Vinyl	1	1955	1043	1	3	1
1720	5	Brick	1	1952	1029	1	2	1
1721	5	Brick	1	1961	1011	1	3	1
1722	5	Aluminum / Vinyl	1	1955	1008	1	3	1
1723	5	Aluminum / Vinyl	1	1955	1008	1	3	1
1724	5	Stone	1	1950	960	1	2	1
1725	5	Aluminum / Vinyl	1	1950	927	1	3	1
1726	5	Stone	1	1939	924	1	2	1
1727	5	Stone	1	1956	920	1	3	1
1728	5	Aluminum / Vinyl	1	1948	800	1	2	1

1729	5 Aluminum / Vinyl	1	1950	728	1	2	2
1730	5 Aluminum / Vinyl	2	1977	2896	2	6	2
1731	6 Aluminum / Vinyl	1	1895	934	1	2	1
1732	6 Aluminum / Vinyl	2	1922	2612	2	4	2
1733	6 Frame	2	1911	2202	2	4	2
1734	6 Aluminum / Vinyl	1.5	1916	1965	2	4	2
1735	6 Frame	1.5	1914	1693	2	4	2
1736	6 Aluminum / Vinyl	1.5	1873	1664	2	4	2
1737	6 Aluminum / Vinyl	1.5	1893	2037	1	4	2
1738	6 Aluminum / Vinyl	2	1910	1736	1	4	1
1739	7 Brick	1	1945	1731	1	4	1
1740	7 Brick	1	1951	1372	1	4	2
1741	7 Aluminum / Vinyl	1	1954	1176	1	4	1
1742	7 Aluminum / Vinyl	1	1950	1113	1	3	1
1743	7 Masonry / Frame	2	1952	2020	1	4	3
1744	7 Aluminum / Vinyl	1	1928	774	1	2	1
1745	7 Aluminum / Vinyl	1	1930	563	1	2	1
1746	7 Aluminum / Vinyl	2	1950	1932	2	4	2
1747	7 Frame	2	1913	2152	2	4	2
1748	7 Stone	1	1954	1448	1	3	1
1749	7 Aluminum / Vinyl	1	1953	912	1	3	1
1750	7 Aluminum / Vinyl	1	1920	1244	1	3	1
1751	7 Stone	2	1935	1980	1	3	1
1752	8 Aluminum / Vinyl	1	1951	1375	1	3	2
1753	8 Aluminum / Vinyl	1	1952	779	1	2	1
1754	8 Stucco	1.5	1915	2003	2	5	2
1755	8 Frame	2	1912	2528	2	6	2
1756	8 Frame	2	1907	1936	2	5	2
1757	8 Aluminum / Vinyl	1	1880	1875	2	4	2
1758	8 Stucco	1	1921	1870	1	3	2
1759	8 Aluminum / Vinyl	1.5	1920	1510	1	3	1
1760	8 Aluminum / Vinyl	1	1923	1454	1	4	2
1761	8 Aluminum / Vinyl	1	1925	1440	1	3	2
1762	8 Stucco	1	1923	1255	1	3	1
1763	8 Frame	1	1925	1237	1	3	1
1764	8 Aluminum / Vinyl	1	1926	1106	1	2	1
1765	8 Aluminum / Vinyl	1	1900	1431	1	4	1
1767	9 Aluminum / Vinyl	1	1956	1872	1	3	1
1768	9 Aluminum / Vinyl	1.5	1976	1437	1	4	2
1769	9 Aluminum / Vinyl	1	1953	1050	1	4	1
1770	9 Aluminum / Vinyl	2	2008	2208	1	4	2
1771	9 Brick	1	1964	1669	1	3	1
1772	9 Aluminum / Vinyl	1	1979	1581	1	4	2

1773	9 Aluminum / Vinyl	1	1974	1324	1	3	1
1774	9 Aluminum / Vinyl	1	1953	1309	1	3	2
1775	9 Aluminum / Vinyl	1	1956	1246	1	3	1
1776	9 Aluminum / Vinyl	1	1973	1200	1	4	1
1777	9 Frame	1	1966	1184	1	3	1
1778	9 Masonry / Frame	1	1957	1165	1	3	1
1779	9 Aluminum / Vinyl	1	1957	1155	1	3	1
1780	9 Aluminum / Vinyl	1	1992	1143	1	3	1
1781	9 Aluminum / Vinyl	1	1972	1140	1	3	1
1782	9 Frame	1	1968	1063	1	2	1
1783	9 Aluminum / Vinyl	1	1965	1033	1	3	1
1784	9 Aluminum / Vinyl	1	1965	1033	1	3	1
1785	9 Brick	1	1956	962	1	3	1
1786	9 Aluminum / Vinyl	1	1976	906	1	3	1
1787	9 Aluminum / Vinyl	1	1937	826	1	2	1
1788	10 Stone	1.5	1948	1920	1	4	2
1789	10 Brick	1.5	1932	1424	1	3	1
1790	10 Aluminum / Vinyl	1	1945	1307	1	3	2
1791	10 Aluminum / Vinyl	1	1955	1046	1	3	1
1792	10 Aluminum / Vinyl	1	1948	1012	1	4	1
1793	10 Masonry / Frame	2	1921	3268	2	6	2
1794	10 Aluminum / Vinyl	2	1927	2756	2	4	2
1795	10 Stucco	2	1927	2564	2	6	2
1796	10 Aluminum / Vinyl	2	1926	2300	2	4	2
1797	10 Aluminum / Vinyl	1.5	1920	2234	2	4	2
1798	10 Frame	1.5	1928	2076	2	5	2
1799	10 Aluminum / Vinyl	1.5	1928	1973	2	4	2
1800	10 Aluminum / Vinyl	2	1903	1834	2	4	2
1801	10 Brick	1	1923	2010	1	4	2
1802	10 Aluminum / Vinyl	1	1912	1672	1	3	2
1803	10 Aluminum / Vinyl	1	1925	1225	1	3	1
1804	10 Aluminum / Vinyl	1	1925	1188	1	4	2
1805	10 Aluminum / Vinyl	1	1926	1141	1	3	1
1806	10 Aluminum / Vinyl	1	1925	964	1	3	1
1807	10 Frame	1	1924	951	1	3	1
1808	10 Brick	1	1953	1264	1	2	1
1809	10 Aluminum / Vinyl	1	1952	1173	1	3	2
1810	10 Aluminum / Vinyl	1	1953	1036	1	3	1
1811	10 Aluminum / Vinyl	1	1951	700	1	2	1
1812	10 Aluminum / Vinyl	2	1925	1430	1	3	1
1813	10 Aluminum / Vinyl	1	1927	1415	1	3	2
1814	10 Aluminum / Vinyl	2	1918	1407	1	2	2
1815	10 Frame	1	1914	1302	1	3	1

1816	10	Aluminum / Vinyl	1	1917	1266	1	3	1
1817	10	Aluminum / Vinyl	2	1927	1197	1	3	1
1818	10	Stone	1.5	1923	2519	1	4	3
1819	11	Aluminum / Vinyl	1	1954	1105	1	3	2
1820	11	Aluminum / Vinyl	1	1943	1093	1	3	1
1821	11	Aluminum / Vinyl	1	1957	1069	1	3	2
1822	11	Stone	1	1951	1024	1	2	1
1823	11	Brick	1	1950	967	1	2	1
1824	11	Aluminum / Vinyl	1	1941	907	1	3	1
1825	11	Aluminum / Vinyl	1	1938	902	1	3	1
1826	11	Aluminum / Vinyl	1	1942	763	1	2	1
1827	11	Aluminum / Vinyl	1	1954	745	1	2	1
1828	11	Aluminum / Vinyl	2	1938	1496	1	3	1
1829	11	Masonry / Frame	2	1930	1478	1	3	2
1830	11	Block	2	1949	1056	1	2	1
1831	11	Aluminum / Vinyl	1.5	1980	1897	2	4	2
1832	11	Aluminum / Vinyl	2	1954	1728	2	6	2
1833	11	Aluminum / Vinyl	2	1954	1728	2	6	2
1834	11	Aluminum / Vinyl	2	1954	1728	2	6	2
1835	11	Brick	1	1963	1632	1	4	1
1836	11	Stone	1	1954	1497	1	2	1
1837	11	Aluminum / Vinyl	1	1965	1317	1	4	1
1838	11	Stone	1	1952	1312	1	2	1
1839	11	Aluminum / Vinyl	1	1963	1251	1	3	1
1840	11	Aluminum / Vinyl	1	1953	1207	1	4	2
1841	11	Brick	1	1958	1206	1	3	1
1842	11	Brick	1	1954	1176	1	3	1
1843	11	Brick	1	1956	1150	1	3	1
1844	11	Aluminum / Vinyl	1	1957	1147	1	3	1
1845	11	Brick	1	1959	1130	1	3	1
1846	11	Brick	1	1957	1129	1	3	1
1847	11	Brick	1	1959	1114	1	3	1
1848	11	Aluminum / Vinyl	1	1953	1069	1	3	1
1849	11	Brick	1	1956	989	1	3	1
1850	11	Aluminum / Vinyl	1	1960	988	1	3	1
1851	11	Aluminum / Vinyl	1	1955	988	1	3	1
1852	11	Aluminum / Vinyl	1	1953	987	1	3	1
1853	11	Frame	1	1953	980	1	3	1
1854	11	Aluminum / Vinyl	1	1953	960	1	3	1
1855	11	Brick	1	1953	921	1	3	1
1856	11	Aluminum / Vinyl	1	1957	914	1	2	1
1857	11	Aluminum / Vinyl	1	1953	894	1	2	1
1858	11	Frame	1	1952	879	1	3	1

1859	11	Aluminum / Vinyl	1	1953	870	1	2	1
1860	11	Aluminum / Vinyl	1	1947	850	1	2	1
1861	11	Aluminum / Vinyl	1	1951	770	1	2	1
1862	11	Aluminum / Vinyl	1	1950	734	1	2	1
1863	11	Aluminum / Vinyl	1	1953	672	1	2	1
1864	11	Aluminum / Vinyl	1	1937	788	1	2	1
1865	11	Aluminum / Vinyl	2	1972	2385	2	6	2
1866	11	Brick	1.5	1930	2016	1	4	1
1867	12	Aluminum / Vinyl	1	1924	1221	1	4	1
1868	13	Aluminum / Vinyl	1	1947	1608	1	3	1
1869	13	Brick	1	1948	1217	1	3	1
1870	13	Brick	1	1951	1120	1	3	1
1871	13	Aluminum / Vinyl	1	1952	1075	1	3	1
1872	13	Brick	1	1951	1002	1	3	1
1873	13	Brick	1	1955	986	1	2	1
1874	13	Aluminum / Vinyl	2	1965	1747	1	3	2
1875	13	Aluminum / Vinyl	2	1959	2052	2	6	2
1876	13	Brick	1.5	1961	1875	2	5	2
1877	13	Aluminum / Vinyl	1.5	1908	1643	2	3	2
1878	13	Frame	1.5	1920	1493	2	3	2
1879	13	Frame	1	1928	1083	1	2	1
1880	13	Frame	1	1938	1530	1	3	1
1881	13	Aluminum / Vinyl	1	1970	1352	1	3	1
1882	13	Brick	1	1966	1160	1	3	1
1883	13	Brick	1	1965	1157	1	3	1
1884	13	Aluminum / Vinyl	1	1958	1154	1	3	1
1885	13	Brick	1	1973	1100	1	2	1
1886	13	Frame	1	1958	1081	1	3	1
1887	13	Aluminum / Vinyl	1	1983	1064	1	3	1
1888	13	Aluminum / Vinyl	1	1958	1045	1	3	1
1889	13	Brick	1	1962	1036	1	3	1
1890	13	Frame	1	1949	843	1	2	1
1891	13	Aluminum / Vinyl	1	1953	705	1	2	1
1892	13	Frame	1.5	1910	1690	1	3	2
1893	13	Aluminum / Vinyl	1	1927	1325	1	4	1
1894	13	Aluminum / Vinyl	1	1928	1225	1	3	2
1895	13	Aluminum / Vinyl	1	1908	1093	1	3	1
1896	14	Aluminum / Vinyl	1	1947	1387	1	4	3
1897	14	Brick	1	1944	1353	1	4	2
1898	14	Block	1	1948	1163	1	3	1
1899	14	Aluminum / Vinyl	1	1951	1035	1	3	1
1900	14	Stucco	1	1951	1014	1	3	2
1901	14	Aluminum / Vinyl	1	1944	1004	1	3	1

1902	14	Frame	1	1950	885	1	3	1
1903	14	Aluminum / Vinyl	1	1947	828	1	2	1
1904	14	Stone	2	1921	2352	1	3	1
1905	14	Aluminum / Vinyl	2	1940	1426	1	4	2
1906	14	Aluminum / Vinyl	2	2004	1380	1	3	2
1907	14	Aluminum / Vinyl	2	1949	1374	1	3	1
1908	14	Aluminum / Vinyl	1.5	1927	1721	2	4	2
1909	14	Aluminum / Vinyl	1.5	1949	1533	2	3	2
1910	14	Frame	2	1906	2612	2	6	2
1911	14	Aluminum / Vinyl	1	1944	1950	2	6	2
1912	14	Aluminum / Vinyl	1.5	1928	1946	1	4	2
1913	14	Brick	1	1928	1541	1	4	1
1914	14	Aluminum / Vinyl	1	1923	1218	1	3	2
1915	14	Aluminum / Vinyl	1	1925	1149	1	3	1
1916	14	Aluminum / Vinyl	1	1953	976	1	3	1
1917	14	Aluminum / Vinyl	1	1943	803	1	2	1
1918	14	Aluminum / Vinyl	1	1947	784	1	2	1
1919	14	Frame	1	1943	689	1	2	1
1920	14	Aluminum / Vinyl	1.5	1915	1612	1	3	1
1921	14	Frame	1	1908	1428	1	5	1
1922	14	Frame	1	1901	1406	1	3	1
1923	14	Aluminum / Vinyl	1	1920	1199	1	4	1
1924	14	Aluminum / Vinyl	1	1900	1169	1	3	1
1925	14	Aluminum / Vinyl	1	1901	1107	1	4	1
1926	14	Aluminum / Vinyl	1	1915	1064	1	3	1
1927	14	Aluminum / Vinyl	1	1924	1040	1	3	2
1928	14	Aluminum / Vinyl	1	1897	1032	1	3	1
1929	14	Aluminum / Vinyl	2	1910	1980	3	4	3
1930	15	Brick	2	1916	3354	2	4	2
1931	1	Aluminum / Vinyl	1.5	1950	1324	1	4	2
1932	1	Frame	1.5	1935	1308	1	3	1
1933	1	Frame	1.5	1940	1228	1	3	1
1934	1	Aluminum / Vinyl	1.5	1940	1191	1	4	2
1935	1	Aluminum / Vinyl	1	1947	821	1	3	1
1936	1	Aluminum / Vinyl	2	1954	1536	2	4	2
1937	1	Aluminum / Vinyl	1	1960	1104	1	3	1
1938	1	Aluminum / Vinyl	1	1955	1082	1	3	1
1939	1	Aluminum / Vinyl	1	1949	868	1	2	1
1940	1	Aluminum / Vinyl	1	1949	868	1	2	1
1941	1	Aluminum / Vinyl	1	1942	796	1	2	1
1942	1	Aluminum / Vinyl	1	1941	720	1	2	2
1943	2	Brick	1	1957	1638	1	4	1
1944	2	Aluminum / Vinyl	1	1940	1385	1	4	1

1945	2	Brick	1	1955	1317	1	3	1
1946	2	Aluminum / Vinyl	1	1955	1056	1	3	1
1947	2	Aluminum / Vinyl	1	1947	975	1	4	1
1948	2	Aluminum / Vinyl	1.5	1957	1764	2	5	2
1949	2	Brick	1	1957	1242	1	3	1
1950	2	Brick	1	1960	1204	1	3	1
1951	2	Frame	1	1960	1188	1	3	1
1952	2	Frame	1	1956	1188	1	3	1
1953	2	Brick	1	1958	1177	1	3	1
1954	2	Frame	1	1971	1156	1	4	1
1955	2	Brick	1	1955	1115	1	2	1
1956	2	Brick	1	1958	1090	1	3	1
1957	2	Aluminum / Vinyl	1	1966	1083	1	3	1
1958	2	Frame	1	1955	1046	1	3	1
1959	2	Frame	1	1975	1023	1	3	1
1960	2	Brick	1	1955	1020	1	2	1
1961	2	Aluminum / Vinyl	1	1953	970	1	3	1
1962	2	Aluminum / Vinyl	1	1953	970	1	3	1
1963	2	Brick	1	1957	942	1	3	1
1964	2	Aluminum / Vinyl	1	1956	936	1	2	1
1965	2	Frame	1	1957	925	1	3	1
1966	2	Aluminum / Vinyl	1	1958	918	1	2	1
1967	2	Aluminum / Vinyl	1	1956	905	1	3	1
1968	2	Aluminum / Vinyl	1	1957	900	1	3	1
1969	2	Aluminum / Vinyl	1	1957	900	1	3	1
1970	2	Aluminum / Vinyl	1	1955	864	1	3	1
1971	2	Aluminum / Vinyl	1	1955	756	1	2	1
1972	2	Aluminum / Vinyl	1	1955	1414	1	3	1
1973	2	Aluminum / Vinyl	1	1955	1414	1	3	2
1974	2	Masonry / Frame	2	1963	2281	2	6	2
1975	3	Brick	2	1924	3595	1	7	3
1976	3	Frame	2	1924	2944	2	6	2
1977	3	Aluminum / Vinyl	1	1949	1413	2	3	2
1978	3	Stucco	2	1910	3886	2	6	3
1979	3	Frame	2	1908	1710	2	4	2
1980	3	Stone	2	1915	6917	3	6	4
1981	3	Frame	2	1898	3033	1	5	2
1982	3	Aluminum / Vinyl	2	1900	1800	1	3	2
1983	3	Frame	1	1917	1559	1	3	1
1984	3	Brick	1	1905	948	1	3	1
1985	4	Aluminum / Vinyl	1	1924	1282	1	4	1
1986	4	Aluminum / Vinyl	2	1890	2133	1	5	2
1987	4	Frame	2	1904	1772	1	4	1

1988	5	Brick	1	1954	1622	1	4	2
1989	5	Brick	1.5	1956	1589	1	3	1
1990	5	Brick	1	1953	1584	1	4	1
1991	5	Stone	1.5	1948	1558	1	3	1
1992	5	Brick	1	1953	1512	1	4	1
1993	5	Brick	1	1955	1501	1	3	1
1994	5	Stone	1.5	1948	1432	1	3	1
1995	5	Stone	1	1950	1415	1	3	1
1996	5	Masonry / Frame	1	1952	1352	1	3	2
1997	5	Aluminum / Vinyl	1	1949	1293	1	3	2
1998	5	Frame	1	1952	1292	1	3	1
1999	5	Brick	1	1955	1242	1	3	1
2000	5	Aluminum / Vinyl	1	1954	1219	1	3	1
2001	5	Aluminum / Vinyl	1	1955	1200	1	4	1
2002	5	Aluminum / Vinyl	1	1952	1120	1	3	1
2003	5	Brick	1	1946	1111	1	3	1
2004	5	Brick	1.5	1947	1109	1	3	1
2005	5	Aluminum / Vinyl	1	1950	1092	1	3	1
2006	5	Aluminum / Vinyl	1	1953	1035	1	4	1
2007	5	Aluminum / Vinyl	1	1952	1034	1	3	1
2008	5	Aluminum / Vinyl	1	1951	933	1	3	1
2009	5	Aluminum / Vinyl	1	1957	784	1	2	1
2010	5	Aluminum / Vinyl	2	2008	2473	1	4	2
2011	5	Brick	2	1957	2422	2	6	2
2012	5	Brick	1	1964	2065	2	4	2
2013	5	Aluminum / Vinyl	2	1953	2016	2	4	2
2014	5	Aluminum / Vinyl	1	2009	2482	1	3	2
2015	5	Aluminum / Vinyl	1	1960	1595	1	3	2
2016	5	Brick	1	1957	1509	1	3	1
2017	5	Brick	1	1969	1360	1	3	1
2018	5	Stone	1	1956	1342	1	2	2
2019	5	Aluminum / Vinyl	1	1959	1287	1	3	1
2020	5	Aluminum / Vinyl	1	1955	1256	1	3	2
2021	5	Aluminum / Vinyl	1	1969	1228	1	3	1
2022	5	Aluminum / Vinyl	1	1954	1176	1	3	1
2023	5	Brick	1	1956	1144	1	3	1
2024	5	Brick	1	1958	1120	1	3	1
2025	5	Frame	1	1952	1106	1	2	1
2026	5	Aluminum / Vinyl	1	1955	1077	1	3	2
2027	5	Brick	1	1958	1058	1	3	1
2028	5	Aluminum / Vinyl	1	1956	1044	1	3	1
2029	5	Brick	1	1956	1040	1	2	1
2030	5	Frame	1	1950	1032	1	3	1

2031	5	Brick	1	1956	1025	1	3	1
2032	5	Brick	1	1955	1019	1	3	1
2033	5	Aluminum / Vinyl	1	1956	999	1	3	1
2034	5	Brick	1	1947	936	1	2	1
2035	5	Brick	1	1947	863	1	2	1
2036	5	Aluminum / Vinyl	1	1949	772	1	2	1
2037	5	Aluminum / Vinyl	1	1949	707	1	2	1
2038	5	Aluminum / Vinyl	1.5	1926	1083	1	2	1
2039	5	Masonry / Frame	2	1965	2222	2	6	2
2040	6	Aluminum / Vinyl	2	2008	1536	1	3	1
2041	6	Frame	1	1880	1134	1	3	2
2042	6	Frame	2	1922	2626	2	6	2
2043	6	Aluminum / Vinyl	1.5	1926	1919	2	4	2
2044	6	Frame	1.5	1926	1737	2	4	2
2045	6	Brick	2	1914	2628	2	5	2
2046	6	Aluminum / Vinyl	2	1906	2488	2	4	2
2047	6	Frame	1	1927	1547	1	3	2
2048	6	Aluminum / Vinyl	1	1925	1718	1	4	1
2049	6	Frame	1.5	1902	1589	1	4	1
2050	6	Aluminum / Vinyl	1	1911	1392	1	5	1
2051	6	Frame	1	1904	944	1	2	1
2052	6	Frame	2	1904	3482	3	7	3
2053	7	Brick	1.5	1940	1612	1	3	1
2054	7	Aluminum / Vinyl	1.5	1943	1499	1	3	1
2055	7	Brick	1.5	1939	1488	1	4	1
2056	7	Aluminum / Vinyl	1	1941	1446	1	4	1
2057	7	Brick	1	1946	1349	1	4	2
2058	7	Stone	1	1941	1311	1	3	1
2059	7	Masonry / Frame	2	1950	1970	1	4	1
2060	7	Stone	2	1940	2692	2	4	2
2061	7	Aluminum / Vinyl	1.5	1922	1613	1	4	1
2062	7	Aluminum / Vinyl	1	1928	1475	1	3	1
2063	7	Aluminum / Vinyl	1	1927	1344	1	3	1
2064	7	Aluminum / Vinyl	1	1927	1344	1	3	1
2065	7	Aluminum / Vinyl	1	1927	1264	1	3	1
2066	7	Aluminum / Vinyl	1	1924	1191	1	3	1
2067	7	Aluminum / Vinyl	1	1928	1170	1	2	1
2068	7	Aluminum / Vinyl	1	1950	1101	1	2	2
2069	7	Brick	1	1955	1074	1	2	1
2070	8	Aluminum / Vinyl	1	1891	1080	1	2	2
2071	8	Aluminum / Vinyl	2	1913	2772	2	6	2
2072	8	Aluminum / Vinyl	2	1905	2684	2	8	2
2073	8	Frame	2	1923	2388	2	4	2

2074	8	Frame	1.5	1904	2063	2	4	2
2075	8	Aluminum / Vinyl	2	1884	1632	2	4	2
2076	8	Brick	1	1923	1589	1	3	1
2077	8	Aluminum / Vinyl	1	1924	843	1	2	1
2078	8	Aluminum / Vinyl	2	1912	1675	1	3	2
2079	8	Aluminum / Vinyl	1.5	1916	1549	1	2	1
2080	8	Aluminum / Vinyl	1	1900	1188	1	4	1
2081	8	Aluminum / Vinyl	1	1898	1008	1	3	1
2082	9	Aluminum / Vinyl	1	1954	1084	1	3	1
2083	9	Aluminum / Vinyl	1	1953	1020	1	4	1
2084	9	Aluminum / Vinyl	2	2001	2868	1	4	2
2085	9	Aluminum / Vinyl	2	2009	2350	1	4	2
2086	9	Aluminum / Vinyl	2	1954	1728	2	6	2
2087	9	Aluminum / Vinyl	1	1930	1223	1	3	1
2088	9	Frame	1	1966	1420	1	3	1
2089	9	Aluminum / Vinyl	1	1975	1227	1	3	1
2090	9	Brick	1	1963	1191	1	3	1
2091	9	Aluminum / Vinyl	1	1958	1175	1	3	1
2092	9	Aluminum / Vinyl	1	1980	1077	1	3	1
2093	9	Aluminum / Vinyl	1	1963	1074	1	3	1
2094	9	Aluminum / Vinyl	1	1957	1059	1	3	1
2095	9	Brick	1	1957	1050	1	3	2
2096	9	Aluminum / Vinyl	1	1964	1038	1	3	1
2097	9	Brick	1	1963	1032	1	3	1
2098	9	Aluminum / Vinyl	1	1976	906	1	3	1
2099	9	Masonry / Frame	1	1959	1598	1	4	1
2100	10	Aluminum / Vinyl	1	1942	1055	1	3	1
2101	10	Aluminum / Vinyl	1	1946	1663	1	3	1
2102	10	Aluminum / Vinyl	1	1952	1389	1	3	1
2103	10	Aluminum / Vinyl	1.5	1950	1323	1	5	2
2104	10	Aluminum / Vinyl	1	1953	1185	1	4	1
2105	10	Aluminum / Vinyl	1	1953	1110	1	4	1
2106	10	Brick	2	1929	3219	2	6	2
2107	10	Frame	2	1914	2752	2	6	3
2108	10	Aluminum / Vinyl	2	1920	2556	2	4	2
2109	10	Masonry / Frame	2	1927	2528	2	4	2
2110	10	Frame	2	1914	2294	2	4	2
2111	10	Aluminum / Vinyl	1.5	1959	1812	2	3	2
2112	10	Brick	1	1923	2589	1	4	2
2113	10	Brick	1	1930	2368	1	4	1
2114	10	Frame	1	1919	1768	1	4	2
2115	10	Aluminum / Vinyl	1	1928	1470	1	4	2
2116	10	Aluminum / Vinyl	1	1926	1417	1	3	1

2117	10	Aluminum / Vinyl	1	1925	1416	1	3	2
2118	10	Aluminum / Vinyl	1	1924	1395	1	3	1
2119	10	Aluminum / Vinyl	1	1930	1345	1	4	1
2120	10	Aluminum / Vinyl	1	1923	1274	1	2	1
2121	10	Aluminum / Vinyl	1	1923	921	1	2	1
2122	10	Aluminum / Vinyl	1	1953	1384	1	3	2
2123	10	Frame	1	1956	936	1	2	1
2124	10	Aluminum / Vinyl	1	1942	924	1	2	1
2125	10	Aluminum / Vinyl	1	1946	667	1	2	1
2126	10	Aluminum / Vinyl	1	1914	1593	1	3	2
2127	10	Frame	1.5	1896	1492	1	3	2
2128	10	Aluminum / Vinyl	1	1921	1080	1	2	1
2129	10	Frame	1	1926	990	1	3	1
2130	11	Fiber-Cement	1	2008	4405	1	6	4
2131	11	Stone	1	1948	1767	1	4	1
2132	11	Aluminum / Vinyl	1	1970	1548	1	4	2
2133	11	Aluminum / Vinyl	1	1951	1424	1	3	1
2134	11	Brick	1	1942	1316	1	3	1
2135	11	Aluminum / Vinyl	1	1959	1159	1	4	1
2136	11	Aluminum / Vinyl	1	1949	1107	1	3	1
2137	11	Brick	1	1942	980	1	2	1
2138	11	Aluminum / Vinyl	2	1958	2233	2	6	2
2139	11	Aluminum / Vinyl	2	1954	1728	2	6	2
2140	11	Aluminum / Vinyl	1	1928	1188	1	3	2
2141	11	Frame	1	1954	1364	1	3	1
2142	11	Brick	1	1953	1313	1	3	1
2143	11	Aluminum / Vinyl	1	1948	1270	1	2	1
2144	11	Brick	1	1967	1235	1	3	1
2145	11	Brick	1	1960	1201	1	3	1
2146	11	Frame	1	1953	1173	1	3	1
2147	11	Brick	1	1956	1161	1	3	1
2148	11	Brick	1	1966	1158	1	3	1
2149	11	Brick	1	1953	1140	1	2	1
2150	11	Brick	1	1959	1118	1	3	1
2151	11	Aluminum / Vinyl	1	1965	1107	1	3	1
2152	11	Aluminum / Vinyl	1	1964	1105	1	3	1
2153	11	Brick	1	1956	1093	1	2	1
2154	11	Aluminum / Vinyl	1	1958	1080	1	3	2
2155	11	Aluminum / Vinyl	1	1949	1072	1	2	1
2156	11	Aluminum / Vinyl	1	1958	1048	1	3	1
2157	11	Brick	1	1955	1013	1	3	1
2158	11	Brick	1	1959	1011	1	3	1
2159	11	Brick	1	1954	999	1	2	1

2160	11	Brick	1	1952	980	1	2	1
2161	11	Aluminum / Vinyl	1	1953	966	1	3	1
2162	11	Brick	1	1959	965	1	3	1
2163	11	Brick	1	1956	947	1	3	1
2164	11	Frame	1	1955	944	1	3	1
2165	11	Brick	1	1955	925	1	3	1
2166	11	Aluminum / Vinyl	1	1960	925	1	3	1
2167	11	Aluminum / Vinyl	1	1960	896	1	3	2
2168	11	Aluminum / Vinyl	1	1953	882	1	3	1
2169	11	Aluminum / Vinyl	1	1953	876	1	3	1
2170	11	Aluminum / Vinyl	1	1953	874	1	3	1
2171	11	Frame	1	1953	864	1	3	1
2172	11	Aluminum / Vinyl	1	1938	756	1	2	1
2173	12	Frame	2	1966	1821	1	4	1
2174	12	Frame	2	1910	1980	2	4	2
2175	12	Aluminum / Vinyl	2	1885	1968	2	4	2
2176	12	Aluminum / Vinyl	1	1893	1699	1	4	2
2177	12	Aluminum / Vinyl	1.5	1906	1600	2	4	2
2178	12	Frame	1.5	1910	1402	1	4	1
2180	13	Aluminum / Vinyl	1	1974	1789	1	4	2
2181	13	Brick	1	1948	1528	1	4	1
2182	13	Brick	1	1953	1252	1	3	1
2183	13	Brick	1	1948	1249	1	4	1
2184	13	Aluminum / Vinyl	1	1950	1143	1	3	2
2185	13	Aluminum / Vinyl	1	1951	1093	1	4	1
2186	13	Brick	1	1951	1090	1	2	1
2187	13	Brick	1	1946	1076	1	3	1
2188	13	Aluminum / Vinyl	1	1942	1074	1	4	1
2189	13	Aluminum / Vinyl	1	1949	830	1	2	1
2190	13	Aluminum / Vinyl	2	1998	2259	1	3	2
2191	13	Frame	2	1979	1943	1	3	2
2192	13	Stone	2	1936	1386	1	2	1
2193	13	Aluminum / Vinyl	1.5	1936	821	1	3	1
2194	13	Aluminum / Vinyl	2	1957	2209	2	6	2
2195	13	Brick	1.5	1951	2082	2	4	2
2196	13	Aluminum / Vinyl	1	1955	1209	1	3	1
2197	13	Stone	1	1939	1177	1	2	1
2198	13	Aluminum / Vinyl	1	1981	1156	1	3	1
2199	13	Brick	1	1960	1148	1	3	1
2200	13	Brick	1	1961	1090	1	3	1
2201	13	Brick	1	1962	1037	1	3	1
2202	13	Stone	1	1950	1026	1	2	1
2203	13	Aluminum / Vinyl	1	1960	998	1	3	1

2204	13 Aluminum / Vinyl	1	1949	912	1	3	1
2205	13 Aluminum / Vinyl	1	1951	840	1	2	1
2206	13 Aluminum / Vinyl	1	1950	812	1	2	1
2207	13 Frame	1	1942	745	1	2	1
2208	13 Aluminum / Vinyl	1	1953	743	1	2	1
2209	13 Aluminum / Vinyl	1	1943	707	1	2	1
2210	13 Brick	2	1929	2236	1	3	1
2211	13 Aluminum / Vinyl	2	1966	2132	2	6	2
2212	14 Aluminum / Vinyl	1	1953	1182	1	4	1
2213	14 Brick	1	1956	945	1	3	1
2214	14 Aluminum / Vinyl	2	1939	1144	1	2	1
2215	14 Aluminum / Vinyl	1	1890	1256	1	4	1
2216	14 Aluminum / Vinyl	1	1906	1225	1	3	1
2217	14 Frame	1	1900	1027	1	4	1
2218	14 Aluminum / Vinyl	1.5	1926	1688	2	4	2
2219	14 Aluminum / Vinyl	2	1978	2054	2	6	2
2220	14 Aluminum / Vinyl	2	1920	2670	2	5	2
2221	14 Aluminum / Vinyl	2	1915	2268	2	4	2
2222	14 Frame	2	1915	1832	2	4	2
2223	14 Brick	1.5	1926	1644	1	4	1
2224	14 Brick	1	1930	1618	1	4	2
2225	14 Aluminum / Vinyl	1	1921	1185	1	3	1
2226	14 Brick	1	1902	1048	1	3	1
2227	14 Brick	1	1953	1115	1	3	1
2228	14 Aluminum / Vinyl	1	1955	936	1	3	1
2229	14 Aluminum / Vinyl	1	1943	689	1	2	1
2230	14 Aluminum / Vinyl	1.5	1890	1759	1	5	1
2231	14 Aluminum / Vinyl	2	1924	1663	1	4	1
2232	14 Frame	1	1918	1025	1	2	1
2233	14 Aluminum / Vinyl	1	1920	880	1	2	1
2234	14 Aluminum / Vinyl	1	1900	810	1	2	1
2235	14 Aluminum / Vinyl	1	1921	775	1	2	1
2237	14 Aluminum / Vinyl	2	1953	1256	1	3	1
2238	15 Aluminum / Vinyl	2	2006	1458	1	3	1
2239	15 Frame	2	1921	2984	2	8	2
2240	15 Aluminum / Vinyl	2	1914	2536	2	6	2
2241	15 Aluminum / Vinyl	2	1914	2536	2	6	2
2242	15 Aluminum / Vinyl	2	1914	2532	2	6	2
2243	15 Aluminum / Vinyl	2	1910	2182	2	4	2
2244	15 Aluminum / Vinyl	1.5	1899	1749	2	4	3
2245	15 Aluminum / Vinyl	2	1922	2008	1	3	2
2246	15 Frame	1.5	1920	1548	1	4	1
2247	1 Aluminum / Vinyl	1.5	1940	1367	1	3	1

2248	1	Brick	1	1937	1288	1	4	1
2249	1	Aluminum / Vinyl	1	1954	1194	1	4	1
2250	1	Frame	1	1953	1096	1	4	1
2251	1	Frame	1	1940	944	1	4	1
2252	1	Aluminum / Vinyl	1	1943	884	1	3	1
2253	1	Aluminum / Vinyl	1	1925	894	1	2	1
2254	1	Aluminum / Vinyl	2	1918	2440	2	6	2
2255	1	Aluminum / Vinyl	1	1966	1578	1	3	1
2256	1	Aluminum / Vinyl	1	2007	1439	1	3	2
2257	1	Aluminum / Vinyl	1	1951	938	1	3	1
2258	1	Frame	1	1952	831	1	3	1
2259	2	Aluminum / Vinyl	1	1955	1253	1	4	2
2260	2	Aluminum / Vinyl	1	1953	1118	1	4	1
2261	2	Frame	1	1954	1053	1	3	1
2262	2	Aluminum / Vinyl	2	1968	1465	1	4	1
2263	2	Frame	2	1960	1387	1	3	1
2264	2	Frame	2	1956	2200	2	6	2
2265	2	Aluminum / Vinyl	2	1960	2070	2	6	2
2266	2	Aluminum / Vinyl	2	1958	1879	2	4	2
2267	2	Aluminum / Vinyl	2	1939	1650	2	4	2
2268	2	Aluminum / Vinyl	1	1930	1545	2	3	2
2269	2	Aluminum / Vinyl	1	1955	1465	1	4	1
2270	2	Brick	1	1956	1243	1	3	1
2271	2	Brick	1	1954	1046	1	3	1
2272	2	Aluminum / Vinyl	1	1958	1039	1	3	1
2273	2	Aluminum / Vinyl	1	1948	985	1	2	1
2274	2	Frame	1	1958	973	1	3	1
2275	2	Aluminum / Vinyl	1	1955	963	1	3	1
2276	2	Aluminum / Vinyl	1	1958	936	1	3	1
2277	2	Aluminum / Vinyl	1	1958	936	1	3	1
2278	2	Aluminum / Vinyl	1	1958	918	1	3	2
2279	2	Aluminum / Vinyl	1	1955	864	1	3	1
2280	2	Aluminum / Vinyl	1	1951	723	1	2	1
2281	2	Frame	1	1955	672	1	2	1
2282	3	Frame	2	1906	1352	1	4	1
2283	3	Masonry / Frame	2	1916	3476	2	6	2
2284	3	Aluminum / Vinyl	2	1923	2546	2	6	2
2285	3	Brick	1.5	1931	2234	2	4	2
2286	3	Frame	1.5	1926	1880	2	3	2
2287	3	Aluminum / Vinyl	1	1900	1525	2	2	2
2288	3	Frame	2	1904	2899	1	4	2
2289	3	Frame	2	1899	2350	1	4	1
2290	3	Aluminum / Vinyl	1.5	1900	1549	1	4	1

2292	4 Aluminum / Vinyl	2	2007	1879	1	4	2
2293	4 Frame	2	1900	3046	2	6	2
2294	4 Brick	2	1921	2806	2	4	2
2295	5 Brick	1	1952	1502	1	3	1
2296	5 Aluminum / Vinyl	1	1949	1279	1	4	1
2297	5 Aluminum / Vinyl	1	1952	1098	1	4	2
2298	5 Aluminum / Vinyl	2	1997	1976	1	3	2
2299	5 Aluminum / Vinyl	2	1940	1396	1	3	1
2300	5 Brick	1	1955	3025	2	5	2
2301	5 Brick	2	1959	2598	2	6	3
2302	5 Aluminum / Vinyl	1.5	1965	2479	2	6	2
2303	5 Frame	1	1968	1500	1	3	1
2304	5 Brick	1	1957	1335	1	3	1
2305	5 Brick	1	1957	1335	1	3	1
2306	5 Aluminum / Vinyl	1	1993	1226	1	3	2
2307	5 Brick	1	1964	1191	1	3	2
2308	5 Brick	1	1952	1064	1	2	1
2309	5 Aluminum / Vinyl	1	1955	948	1	3	1
2310	5 Aluminum / Vinyl	1	1952	901	1	2	1
2311	6 Aluminum / Vinyl	2	1907	2028	2	4	2
2312	6 Aluminum / Vinyl	1.5	1890	1622	1	4	1
2313	7 Brick	1	1951	1709	1	4	2
2314	7 Aluminum / Vinyl	1	1936	1628	1	5	1
2315	7 Stone	1	1947	1416	1	3	1
2316	7 Aluminum / Vinyl	1.5	1925	2064	2	4	2
2317	7 Frame	2	1927	2068	2	4	2
2318	7 Aluminum / Vinyl	1.5	1906	1816	2	4	2
2319	7 Frame	1.5	1894	1678	2	4	2
2320	7 Aluminum / Vinyl	1	1926	1392	1	4	1
2321	7 Aluminum / Vinyl	1	1920	1218	1	3	1
2322	7 Brick	1.5	1931	1717	1	4	1
2323	7 Frame	1	1910	1386	1	4	1
2324	7 Aluminum / Vinyl	1.5	1928	1164	1	4	1
2325	7 Stone	1	1933	1816	1	3	1
2326	8 Frame	2	1922	1824	1	4	1
2327	8 Frame	2	1922	1824	1	4	1
2328	8 Aluminum / Vinyl	2	1971	1169	1	4	1
2329	8 Frame	1.5	1924	1963	2	5	3
2330	8 Aluminum / Vinyl	2	1908	2300	2	6	2
2331	8 Frame	2	1894	1904	2	4	2
2332	8 Aluminum / Vinyl	1.5	1926	1819	2	4	2
2333	8 Aluminum / Vinyl	1.5	1903	1603	2	4	2
2334	8 Aluminum / Vinyl	1	1890	1999	1	5	2

2335	8 Aluminum / Vinyl	1.5	1910	1843	1	3	1
2336	8 Aluminum / Vinyl	2	1911	1649	1	5	1
2337	8 Aluminum / Vinyl	1	1880	1260	1	4	2
2338	8 Frame	1	1898	1200	1	3	1
2341	8 Stucco	2	1880	2779	3	6	2
2342	9 Aluminum / Vinyl	1	1948	637	1	2	1
2343	9 Masonry / Frame	1	1959	1610	1	4	3
2344	9 Aluminum / Vinyl	1	1973	1596	1	4	1
2345	9 Aluminum / Vinyl	1	1978	1467	1	3	1
2346	9 Aluminum / Vinyl	1	1965	1227	1	3	1
2347	9 Stone	1	1949	1086	1	2	2
2348	9 Aluminum / Vinyl	1	1951	960	1	3	1
2349	9 Aluminum / Vinyl	1	1951	792	1	2	1
2350	9 Aluminum / Vinyl	1	1951	792	1	2	1
2351	9 Masonry / Frame	2	1971	3500	3	>8	3
2352	10 Masonry / Frame	2	1932	1772	1	3	1
2353	10 Aluminum / Vinyl	1	1910	944	1	3	1
2354	10 Aluminum / Vinyl	2	1922	2903	2	6	2
2355	10 Frame	2	1928	2236	2	4	2
2356	10 Aluminum / Vinyl	2	1924	1924	2	4	2
2357	10 Brick	2	1912	3048	2	6	2
2358	10 Brick	1.5	1938	2150	2	4	2
2359	10 Frame	1.5	1924	1413	2	3	2
2360	10 Aluminum / Vinyl	1	1924	1865	1	4	1
2361	10 Aluminum / Vinyl	1	1926	982	1	3	1
2362	10 Aluminum / Vinyl	1	1926	982	1	3	1
2363	10 Aluminum / Vinyl	1	1926	916	1	3	2
2364	10 Aluminum / Vinyl	1	1951	936	1	3	1
2365	10 Aluminum / Vinyl	1	1955	864	1	3	1
2366	10 Aluminum / Vinyl	1	1940	772	1	2	1
2367	10 Stucco	2	1916	2266	1	4	2
2368	10 Aluminum / Vinyl	1	1925	616	1	2	1
2369	11 Brick	1.5	1959	1850	1	4	1
2370	11 Frame	1	1952	1077	1	4	1
2371	11 Stucco	1	1939	980	1	3	1
2372	11 Brick	2	1962	3044	2	6	2
2373	11 Aluminum / Vinyl	2	1953	1554	2	4	2
2374	11 Frame	1	1953	1176	1	3	1
2375	11 Aluminum / Vinyl	1	1955	1012	1	3	2
2376	11 Brick	1	1959	1010	1	3	1
2377	11 Brick	1	1957	967	1	2	1
2378	11 Brick	1	1956	967	1	3	1
2379	11 Aluminum / Vinyl	1	1954	867	1	2	1

2380	11	Aluminum / Vinyl	1	1949	846	1	2	1
2381	11	Aluminum / Vinyl	1	1954	735	1	2	1
2382	12	Aluminum / Vinyl	1	1906	1870	2	5	2
2383	12	Aluminum / Vinyl	1	1923	1001	1	2	1
2384	13	Aluminum / Vinyl	1	1948	1516	1	4	2
2385	13	Aluminum / Vinyl	1	1947	1144	1	4	1
2386	13	Brick	1	1946	994	1	3	1
2387	13	Brick	1	1949	942	1	2	1
2388	13	Aluminum / Vinyl	2	1985	2084	1	3	2
2389	13	Aluminum / Vinyl	1	1918	759	1	3	1
2390	13	Frame	2	1956	2098	2	5	2
2391	14	Aluminum / Vinyl	1	1953	1153	1	3	1
2392	14	Brick	1	1953	1125	1	4	1
2393	14	Aluminum / Vinyl	2	1940	1590	1	3	1
2394	14	Stucco	2	1945	1006	1	2	1
2395	14	Frame	2	1918	1964	2	4	2
2396	14	Frame	2	1924	1848	2	4	2
2397	14	Aluminum / Vinyl	1	1926	1758	1	4	1
2398	14	Frame	1.5	1925	1658	1	4	2
2399	14	Aluminum / Vinyl	1	1926	1567	1	4	1
2400	14	Aluminum / Vinyl	1	1926	1350	1	3	1
2401	14	Aluminum / Vinyl	1	1953	704	1	2	1
2402	14	Stucco	1	1913	1594	1	4	2
2403	14	Aluminum / Vinyl	1.5	1911	1526	1	4	2
2404	14	Aluminum / Vinyl	1.5	1907	1298	1	3	1
2405	14	Aluminum / Vinyl	1	1915	951	1	3	1
2406	15	Frame	1	1895	1032	1	2	1
2407	15	Aluminum / Vinyl	2	1917	2590	2	6	2
2408	15	Frame	2	1908	2491	2	6	2
2409	15	Frame	2	1908	2491	2	6	2
2410	15	Aluminum / Vinyl	2	1922	2378	2	4	2
2411	15	Aluminum / Vinyl	2	1901	2320	2	6	2
2412	15	Aluminum / Vinyl	2	1911	2068	2	4	2
2413	15	Aluminum / Vinyl	1	1921	1107	1	4	1
2414	1	Stone	1	1935	1779	1	5	2
2415	1	Brick	1	1963	1529	1	3	1
2416	3	Brick	2	1902	4050	1	7	4
2417	3	Aluminum / Vinyl	2	1896	2644	2	5	2
2418	3	Masonry / Frame	2	1901	4899	1	5	>4
2419	3	Brick	2	1910	2694	1	5	2
2420	3	Stucco	2	1908	2582	1	3	2
2421	5	Brick	1	1957	2735	1	5	2
2422	5	Stucco	1	1946	1134	1	3	1

2423	5 Aluminum / Vinyl	1	1948	1048	1	2	1
2424	5 Aluminum / Vinyl	1	1952	1008	1	3	1
2425	5 Stone	2	1947	2430	2	4	2
2426	5 Brick	1	1958	1404	1	3	1
2427	5 Aluminum / Vinyl	1	1952	1096	1	3	1
2428	6 Aluminum / Vinyl	2	2004	2204	1	3	2
2429	6 Aluminum / Vinyl	2	1897	2025	2	6	2
2430	6 Frame	1.5	1913	1528	2	4	2
2431	7 Stone	1	1936	1364	1	3	1
2432	7 Aluminum / Vinyl	2	1946	1456	1	3	1
2433	7 Brick	1	1929	1333	1	3	1
2434	8 Aluminum / Vinyl	1.5	1915	1688	1	3	1
2435	8 Aluminum / Vinyl	2	1900	2727	3	8	3
2436	10 Brick	1	1953	1222	1	4	1
2437	10 Aluminum / Vinyl	1	1920	608	1	1	1
2438	10 Aluminum / Vinyl	1.5	1926	1594	2	3	2
2439	11 Aluminum / Vinyl	1	1953	1318	1	3	1
2440	11 Aluminum / Vinyl	1	1937	917	1	2	1
2441	11 Masonry / Frame	2	1974	2071	1	4	2
2442	11 Aluminum / Vinyl	2	1959	1912	2	6	2
2443	11 Frame	1	1937	1282	1	3	1
2444	11 Stone	1	1954	1278	1	2	1
2445	11 Aluminum / Vinyl	1	1972	1152	1	3	1
2446	11 Brick	1	1959	1137	1	3	1
2447	11 Aluminum / Vinyl	1	1960	1042	1	3	2
2448	11 Aluminum / Vinyl	1	1963	1000	1	3	1
2449	11 Brick	1	1956	982	1	2	2
2450	11 Aluminum / Vinyl	1	1942	826	1	2	1
2451	12 Aluminum / Vinyl	1	1883	611	1	1	1
2452	12 Frame	2	1905	2032	2	6	2
2453	13 Aluminum / Vinyl	1	1958	1447	1	4	2
2454	13 Aluminum / Vinyl	1	1953	1286	1	4	2
2455	13 Aluminum / Vinyl	1	1940	1152	1	3	1
2456	13 Brick	1	1948	818	1	2	1
2457	13 Aluminum / Vinyl	1.5	1928	1860	2	3	2
2458	13 Brick	1	1960	1150	1	3	1
2459	14 Aluminum / Vinyl	1	1949	771	1	2	1
2460	14 Brick	1.5	1927	2362	2	3	2
2461	14 Brick	1.5	1926	2204	2	4	2
2462	14 Frame	1.5	1921	2708	1	4	1
2463	14 Brick	1	1956	1082	1	3	1
2464	14 Aluminum / Vinyl	2	1905	1458	1	3	1
2465	14 Aluminum / Vinyl	2	1903	1402	1	4	1

2466	1	Frame	1	1925	909	1	2	1
2467	1	Brick	1	1952	1620	1	3	1
2468	1	Stucco	1	1951	1242	1	3	1
2469	2	Aluminum / Vinyl	1	1951	1164	1	3	1
2470	3	Frame	1	1900	912	1	3	1
2471	3	Aluminum / Vinyl	2	1913	1632	1	4	2
2472	3	Stucco	2	1924	2163	1	4	2
2473	3	Aluminum / Vinyl	1	1900	1963	1	4	2
2474	5	Fiber-Cement	1.5	2003	3229	1	4	3
2475	5	Brick	1	1948	1369	1	3	1
2476	5	Aluminum / Vinyl	1	1952	1221	1	3	1
2477	5	Brick	1.5	1947	1109	1	3	1
2478	5	Aluminum / Vinyl	1	1956	976	1	2	1
2479	5	Masonry / Frame	2	1948	2058	2	4	2
2480	5	Brick	1.5	1956	2003	2	5	2
2481	5	Stone	1	1953	1749	1	3	1
2482	5	Frame	1	1953	1489	1	3	1
2483	5	Brick	1	1956	1223	1	3	2
2484	5	Aluminum / Vinyl	1	1960	1183	1	4	1
2485	5	Aluminum / Vinyl	1	1959	1171	1	3	1
2486	5	Aluminum / Vinyl	1	1956	1148	1	3	1
2487	5	Aluminum / Vinyl	1	1955	1084	1	3	1
2488	5	Aluminum / Vinyl	1	1955	948	1	3	1
2489	5	Brick	1	1955	937	1	3	1
2490	6	Aluminum / Vinyl	2	1893	1884	2	4	2
2491	6	Aluminum / Vinyl	1	1925	1509	1	3	1
2492	6	Aluminum / Vinyl	1	1916	1474	1	3	1
2493	6	Aluminum / Vinyl	1	1895	1485	1	3	2
2494	6	Aluminum / Vinyl	1	1895	1433	1	5	1
2495	7	Brick	1	1938	1554	1	3	2
2496	7	Aluminum / Vinyl	1.5	1941	1424	1	3	1
2497	7	Aluminum / Vinyl	1	1952	1116	1	2	1
2498	8	Frame	2	1924	2500	2	6	2
2499	8	Frame	1.5	1915	2229	2	5	2
2500	8	Aluminum / Vinyl	2	1910	2032	2	4	2
2501	8	Aluminum / Vinyl	1	1928	1612	1	3	1
2502	8	Aluminum / Vinyl	2	1900	1685	1	4	1
2503	8	Frame	1.5	1908	1431	1	3	1
2504	8	Aluminum / Vinyl	1	1918	984	1	2	1
2505	9	Aluminum / Vinyl	2	2005	2236	1	4	2
2506	9	Aluminum / Vinyl	1	1957	1211	1	3	1
2507	10	Aluminum / Vinyl	1	1953	1185	1	4	1
2508	10	Frame	1	1905	1323	1	2	2

2509	10	Aluminum / Vinyl	2	1929	2617	2	5	2
2510	10	Aluminum / Vinyl	2	1924	2498	2	4	2
2511	10	Frame	2	1927	2087	2	4	2
2512	10	Aluminum / Vinyl	1.5	1968	2066	2	5	2
2513	10	Aluminum / Vinyl	1	1919	1743	1	4	1
2514	10	Aluminum / Vinyl	1	1926	1431	1	4	2
2515	10	Aluminum / Vinyl	1.5	1927	1265	1	3	1
2516	10	Brick	1	1958	1218	1	2	1
2517	10	Aluminum / Vinyl	1	1949	1056	1	3	1
2518	10	Aluminum / Vinyl	1	1954	1008	1	2	1
2519	10	Frame	1.5	1926	1208	1	3	1
2520	11	Brick	1	1953	1210	1	3	2
2521	11	Aluminum / Vinyl	1	1937	1432	1	3	2
2522	11	Aluminum / Vinyl	2	1954	1728	2	6	2
2523	11	Frame	2	1955	1586	2	4	2
2524	11	Brick	1	1957	1175	1	3	1
2525	11	Brick	1	1961	1102	1	2	2
2526	11	Aluminum / Vinyl	1	1956	995	1	3	1
2527	11	Aluminum / Vinyl	1	1955	890	1	3	1
2528	11	Aluminum / Vinyl	1	1939	775	1	2	1
2529	12	Frame	1	1892	1452	1	3	1
2530	13	Stone	1	1948	1378	1	4	2
2531	13	Aluminum / Vinyl	1	1936	1141	1	2	1
2532	13	Aluminum / Vinyl	1	1925	865	1	2	1
2533	13	Aluminum / Vinyl	1	1977	1493	1	3	1
2534	13	Aluminum / Vinyl	1	1960	985	1	3	1
2535	13	Aluminum / Vinyl	1	1948	804	1	2	1
2536	14	Aluminum / Vinyl	1	1938	1354	1	4	1
2537	14	Aluminum / Vinyl	2	1968	2112	2	6	2
2538	14	Aluminum / Vinyl	1	1926	1587	1	4	2
2539	14	Aluminum / Vinyl	1	1930	1431	1	3	3
2540	14	Aluminum / Vinyl	1	1923	974	1	3	1
2541	14	Aluminum / Vinyl	2	1880	1712	1	4	1
2542	14	Aluminum / Vinyl	1	1896	1320	1	3	2
2543	14	Aluminum / Vinyl	1	1900	1160	1	3	1
2544	15	Aluminum / Vinyl	2	2009	1860	1	4	3
2545	15	Aluminum / Vinyl	2	2001	1456	1	3	2
2546	1	Masonry / Frame	2	1946	1564	1	3	1
2547	1	Aluminum / Vinyl	1.5	1929	2184	2	4	2
2548	1	Aluminum / Vinyl	1	1928	1145	1	3	1
2549	1	Brick	1	1931	1028	1	3	2
2550	1	Frame	1	1925	908	1	3	1
2551	2	Brick	1	1946	1037	1	3	1

2552	2 Aluminum / Vinyl	1.5	1967	2628	2	6	4
2553	2 Frame	1	1964	1416	1	3	2
2554	2 Aluminum / Vinyl	1	1970	1148	1	4	1
2555	2 Aluminum / Vinyl	1	1957	1040	1	3	1
2556	2 Aluminum / Vinyl	1	1952	969	1	2	1
2557	2 Aluminum / Vinyl	1	1955	963	1	3	1
2558	2 Brick	1	1958	888	1	2	1
2559	2 Frame	1	1957	742	1	2	1
2560	2 Aluminum / Vinyl	1	1955	1514	1	4	1
2561	2 Masonry / Frame	1	1961	1485	1	4	1
2562	3 Aluminum / Vinyl	1.5	1925	2020	2	4	2
2563	3 Aluminum / Vinyl	2	1906	1870	2	4	3
2564	3 Brick	1	1923	1557	1	3	1
2565	3 Brick	2	1903	3874	1	5	3
2566	3 Aluminum / Vinyl	2	1897	2932	1	4	2
2567	3 Brick	2	1925	2329	1	4	2
2568	3 Aluminum / Vinyl	2	1899	2219	1	4	1
2569	3 Stucco	2	1912	2104	1	5	2
2570	3 Stucco	2	1920	1992	1	4	1
2571	5 Aluminum / Vinyl	1	1949	1515	1	3	1
2572	5 Aluminum / Vinyl	1	1951	1512	1	4	2
2573	5 Brick	1	1950	1512	1	4	1
2574	5 Brick	1.5	1937	1413	1	2	1
2575	5 Frame	1	1952	1292	1	3	1
2576	5 Brick	1	1955	1231	1	3	1
2577	5 Stone	1	1948	1213	1	3	1
2578	5 Aluminum / Vinyl	1	1951	1211	1	3	1
2579	5 Aluminum / Vinyl	1	1951	1170	1	3	2
2580	5 Brick	1	1955	1026	1	2	1
2581	5 Brick	2	1939	1472	1	3	1
2582	5 Aluminum / Vinyl	1	1989	1833	1	3	2
2583	5 Brick	1	1962	1265	1	3	1
2584	5 Brick	1	1954	1237	1	3	1
2585	5 Aluminum / Vinyl	1	1971	1230	1	3	1
2586	5 Brick	1	1957	1134	1	3	1
2587	5 Aluminum / Vinyl	1	1957	1120	1	3	1
2588	5 Brick	1	1955	1120	1	3	1
2589	5 Aluminum / Vinyl	1	1956	1019	1	3	1
2590	5 Aluminum / Vinyl	1	1962	946	1	3	1
2591	5 Aluminum / Vinyl	1	1954	872	1	3	1
2592	6 Aluminum / Vinyl	1	1941	1577	1	4	1
2593	6 Aluminum / Vinyl	1.5	1904	1737	2	4	2
2594	6 Aluminum / Vinyl	1.5	1904	1737	2	4	2

2595	7	Brick	1	1952	1324	1	3	1
2596	7	Aluminum / Vinyl	1	1947	1133	1	3	1
2597	7	Brick	1	1946	1088	1	3	1
2598	7	Aluminum / Vinyl	1	1946	996	1	3	2
2599	8	Aluminum / Vinyl	1	1883	994	1	2	1
2600	8	Aluminum / Vinyl	1.5	1928	1868	2	4	2
2601	8	Frame	2	1915	2947	2	>8	2
2602	8	Masonry / Frame	1.5	1935	1644	1	3	1
2603	9	Aluminum / Vinyl	1	1969	1453	1	3	1
2604	9	Aluminum / Vinyl	1	1966	1385	1	3	1
2605	9	Brick	1	1957	1222	1	3	1
2606	9	Aluminum / Vinyl	1	1978	1219	1	3	1
2607	9	Brick	1	1957	1050	1	3	1
2608	9	Aluminum / Vinyl	1	1956	946	1	3	1
2609	9	Brick	1	1958	924	1	3	1
2610	10	Brick	1.5	1937	1496	1	4	1
2611	10	Aluminum / Vinyl	1.5	1947	1481	1	5	2
2612	10	Block	1.5	1941	1415	1	3	1
2613	10	Aluminum / Vinyl	1	1947	1012	1	3	2
2614	10	Aluminum / Vinyl	1.5	1900	1342	1	2	1
2615	10	Brick	2	1954	3018	2	6	2
2616	10	Aluminum / Vinyl	1.5	1914	1822	2	4	2
2617	10	Aluminum / Vinyl	1	1920	1727	1	4	1
2618	10	Brick	1	1923	1659	1	3	2
2619	10	Aluminum / Vinyl	1	1923	1604	1	4	2
2620	10	Frame	1	1920	1569	1	4	2
2621	10	Frame	1	1924	1529	1	3	2
2622	10	Aluminum / Vinyl	1	1928	1470	1	4	2
2623	10	Aluminum / Vinyl	1	1924	1081	1	3	1
2624	10	Stucco	1.5	1916	1422	1	3	1
2625	11	Aluminum / Vinyl	1	1953	1411	1	4	1
2626	11	Aluminum / Vinyl	1	1943	1399	1	3	1
2627	11	Brick	1	1955	1151	1	3	2
2628	11	Aluminum / Vinyl	1	1944	1004	1	3	1
2629	11	Masonry / Frame	2	1955	1846	1	4	2
2630	11	Aluminum / Vinyl	1.5	1955	2083	2	5	2
2631	11	Aluminum / Vinyl	1	1952	1588	1	3	1
2632	11	Brick	1	1955	1208	1	3	2
2633	11	Aluminum / Vinyl	1	1960	1171	1	2	1
2634	11	Brick	1	1955	1150	1	3	1
2635	11	Aluminum / Vinyl	1	1959	1113	1	3	1
2636	11	Aluminum / Vinyl	1	1959	1093	1	3	1
2637	11	Aluminum / Vinyl	1	1955	999	1	2	1

2638	11	Aluminum / Vinyl	1	1953	971	1	3	1
2639	11	Aluminum / Vinyl	1	1954	943	1	3	1
2640	11	Brick	1	1956	938	1	2	1
2641	11	Aluminum / Vinyl	1	1950	833	1	2	1
2642	11	Aluminum / Vinyl	1	1945	717	1	2	1
2643	12	Aluminum / Vinyl	2	1891	2371	2	6	2
2644	12	Frame	1.5	1900	1804	2	4	2
2645	13	Prem Wood	1.5	1979	2074	1	4	3
2646	13	Aluminum / Vinyl	1.5	1940	1215	1	2	1
2647	13	Aluminum / Vinyl	2	1969	1973	1	3	1
2648	13	Brick	2	1960	2642	2	6	3
2649	13	Brick	1.5	1948	2081	2	4	2
2650	13	Brick	1.5	1958	2056	2	5	2
2651	13	Stone	1	1951	1541	1	3	2
2652	13	Brick	1	1963	1175	1	3	1
2653	13	Aluminum / Vinyl	1	1968	1092	1	3	1
2654	13	Aluminum / Vinyl	1	1960	981	1	3	1
2655	13	Aluminum / Vinyl	1	1950	922	1	3	1
2656	13	Aluminum / Vinyl	1	1954	720	1	2	1
2657	14	Aluminum / Vinyl	1	1954	1128	1	3	1
2658	14	Brick	1	1940	1109	1	4	1
2659	14	Aluminum / Vinyl	1	1951	1092	1	4	1
2660	14	Aluminum / Vinyl	2	1954	1403	1	3	1
2661	14	Aluminum / Vinyl	1	1923	1556	2	3	2
2662	14	Brick	1.5	1954	2416	2	6	2
2663	14	Aluminum / Vinyl	1	1922	1452	1	3	2
2664	14	Frame	1	1918	1394	1	3	1
2665	14	Masonry / Frame	1	1959	1539	1	3	1
2666	15	Frame	2	1895	1642	2	4	2
2667	15	Frame	1	1920	1725	1	4	2
2668	15	Aluminum / Vinyl	1	2005	1344	1	3	1
2669	1	Aluminum / Vinyl	1	1951	1274	1	4	1
2670	1	Aluminum / Vinyl	1	1948	1248	1	3	1
2671	1	Aluminum / Vinyl	1	1951	802	1	2	1
2672	1	Frame	1	1926	1347	1	3	1
2673	1	Aluminum / Vinyl	1	1960	1130	1	3	1
2674	1	Aluminum / Vinyl	1	1960	1104	1	3	1
2675	1	Masonry / Frame	1	1956	1045	1	3	2
2676	1	Aluminum / Vinyl	1	1954	1024	1	1	1
2677	1	Brick	1	1929	1422	1	4	2
2678	2	Brick	1	1950	1630	1	3	2
2679	2	Aluminum / Vinyl	1	1954	1299	1	3	1
2680	2	Brick	2	1959	2469	2	6	2

2681	2	Frame	1	1962	1538	1	3	2
2682	2	Aluminum / Vinyl	1	1965	1312	1	3	1
2683	2	Aluminum / Vinyl	1	1967	1205	1	3	1
2684	2	Stone	1	1961	1196	1	3	1
2685	2	Aluminum / Vinyl	1	1955	1175	1	3	1
2686	2	Aluminum / Vinyl	1	1974	1122	1	3	1
2687	2	Masonry / Frame	1	1948	1032	1	3	1
2688	2	Brick	1	1955	1024	1	3	1
2689	2	Aluminum / Vinyl	1	1955	950	1	3	1
2690	2	Aluminum / Vinyl	1	1959	936	1	3	1
2691	2	Brick	1	1956	936	1	3	1
2692	2	Aluminum / Vinyl	1	1951	912	1	3	1
2694	2	Aluminum / Vinyl	1	1966	2092	1	3	1
2695	2	Aluminum / Vinyl	1	1961	1510	1	4	1
2696	3	Aluminum / Vinyl	2	1922	2755	2	6	2
2697	3	Aluminum / Vinyl	2	1896	3128	2	8	2
2698	3	Aluminum / Vinyl	1	1891	2111	2	4	2
2699	3	Frame	2	1906	2105	1	3	3
2700	3	Frame	2	1901	1915	1	4	1
2701	3	Masonry / Frame	2	1926	1757	1	3	1
2702	3	Frame	2	1921	1694	1	3	1
2703	3	Frame	1	1900	1036	1	1	1
2704	4	Block	2	1893	1810	1	4	1
2705	5	Brick	1	1950	1729	1	4	2
2706	5	Brick	1	1951	1507	1	3	2
2707	5	Brick	1	1949	1477	1	4	1
2708	5	Frame	1	1950	1315	1	3	1
2709	5	Aluminum / Vinyl	1.5	1940	1312	1	3	1
2710	5	Aluminum / Vinyl	1	1949	1288	1	5	2
2711	5	Brick	1	1949	1263	1	3	1
2712	5	Aluminum / Vinyl	1	1956	1257	1	4	2
2713	5	Aluminum / Vinyl	1	1957	1225	1	3	1
2714	5	Stone	1	1949	1224	1	3	1
2715	5	Brick	1	1950	1156	1	2	1
2716	5	Aluminum / Vinyl	1	1952	1142	1	4	1
2717	5	Aluminum / Vinyl	1.5	1930	1919	2	3	2
2718	5	Stone	1	1953	1863	1	3	2
2719	5	Stone	1	1954	1760	1	2	1
2720	5	Brick	1	1967	1632	1	3	1
2721	5	Aluminum / Vinyl	1	1985	1465	1	3	2
2722	5	Frame	1	1959	1220	1	3	1
2723	5	Brick	1	1959	1219	1	3	1
2724	5	Aluminum / Vinyl	1	1971	1212	1	4	1

2725	5	Frame	1	1956	1130	1	3	1
2726	5	Aluminum / Vinyl	1	1962	1102	1	3	1
2727	5	Aluminum / Vinyl	1	1957	963	1	3	1
2728	5	Aluminum / Vinyl	1	1957	963	1	3	1
2729	5	Aluminum / Vinyl	1	1954	962	1	3	1
2730	5	Brick	1	1947	952	1	2	2
2731	5	Brick	1	1947	952	1	2	2
2732	5	Aluminum / Vinyl	1	1950	874	1	2	1
2733	5	Aluminum / Vinyl	1	1951	772	1	2	1
2734	5	Aluminum / Vinyl	1	1952	698	1	2	1
2735	5	Aluminum / Vinyl	1	1924	1086	1	3	1
2736	6	Brick	1.5	1927	2027	2	4	2
2737	6	Frame	1.5	1900	1635	2	4	2
2738	6	Aluminum / Vinyl	1	1925	1267	1	3	2
2739	6	Aluminum / Vinyl	1	1926	1243	1	3	1
2740	6	Aluminum / Vinyl	2	1888	1996	1	4	2
2741	7	Aluminum / Vinyl	1	1942	1307	1	3	1
2742	7	Brick	1.5	1937	1231	1	2	1
2743	7	Brick	1	1950	1227	1	3	1
2744	7	Stone	1	1947	1192	1	3	1
2745	7	Masonry / Frame	2	1951	2173	1	3	1
2746	7	Aluminum / Vinyl	2	1928	2410	2	6	2
2747	7	Aluminum / Vinyl	1.5	1926	2372	2	4	2
2748	7	Aluminum / Vinyl	2	1920	2354	2	5	2
2749	7	Frame	1	1927	1642	2	3	2
2750	7	Block	1	1926	797	1	3	1
2751	7	Aluminum / Vinyl	2	1900	1208	1	3	1
2752	8	Block	1	1946	1047	1	2	1
2753	8	Aluminum / Vinyl	1	1897	1003	1	3	1
2754	8	Aluminum / Vinyl	1.5	1929	2013	2	5	2
2755	8	Aluminum / Vinyl	2	1912	1848	2	4	2
2756	8	Brick	1	1921	1849	1	5	1
2757	8	Brick	1.5	1925	2004	1	4	1
2758	8	Aluminum / Vinyl	1.5	1906	1431	1	3	1
2759	8	Aluminum / Vinyl	1	1890	1429	1	3	1
2760	8	Aluminum / Vinyl	1	1910	1398	1	4	1
2761	8	Aluminum / Vinyl	1	1905	1088	1	3	1
2762	8	Aluminum / Vinyl	1	1925	1052	1	2	1
2763	9	Brick	1	1949	1147	1	3	1
2764	9	Aluminum / Vinyl	1	1969	1318	1	4	1
2765	9	Aluminum / Vinyl	1	1957	1188	1	3	1
2766	9	Aluminum / Vinyl	1	1958	1071	1	3	1
2767	9	Aluminum / Vinyl	1	1957	1018	1	3	1

2768	9	Aluminum / Vinyl	1	1981	912	1	3	2
2769	10	Stone	1	1948	1516	1	3	2
2770	10	Brick	1	1953	1368	1	3	1
2771	10	Brick	1	1952	1222	1	3	1
2772	10	Aluminum / Vinyl	1	1947	1211	1	3	1
2773	10	Aluminum / Vinyl	1	1947	1046	1	3	1
2774	10	Aluminum / Vinyl	1	1955	964	1	3	1
2775	10	Frame	2	1913	2091	1	4	1
2776	10	Frame	2	1923	1655	1	4	1
2777	10	Masonry / Frame	2	1948	1597	1	3	1
2778	10	Aluminum / Vinyl	2	1922	1390	1	3	2
2779	10	Aluminum / Vinyl	2	1926	1291	1	3	1
2780	10	Aluminum / Vinyl	2	1951	1260	1	3	1
2781	10	Masonry / Frame	2	1951	1151	1	3	1
2782	10	Aluminum / Vinyl	2	1926	2618	2	4	2
2783	10	Aluminum / Vinyl	2	1922	2460	2	6	2
2784	10	Aluminum / Vinyl	2	1959	1962	2	6	2
2785	10	Brick	2	1944	1722	2	4	2
2786	10	Aluminum / Vinyl	1	1924	1514	1	3	1
2787	10	Aluminum / Vinyl	1	1926	1270	1	3	1
2788	10	Aluminum / Vinyl	1	1925	1268	1	4	2
2789	10	Aluminum / Vinyl	1	1929	1219	1	3	1
2790	10	Aluminum / Vinyl	1	1926	948	1	2	1
2791	10	Brick	1	1953	1189	1	3	1
2792	10	Aluminum / Vinyl	1	1955	864	1	3	1
2793	10	Aluminum / Vinyl	1	1947	728	1	2	1
2794	10	Aluminum / Vinyl	1	1926	1142	1	3	1
2795	10	Stucco	1	1925	932	1	2	1
2796	11	Brick	1.5	1937	1751	1	3	1
2797	11	Brick	1	1953	1363	1	4	1
2798	11	Aluminum / Vinyl	1	1952	1012	1	3	1
2799	11	Aluminum / Vinyl	1	1942	984	1	3	1
2800	11	Fiber-Cement	2	2006	3027	1	4	2
2801	11	Masonry / Frame	2	1963	2328	1	4	2
2802	11	Aluminum / Vinyl	2	2009	1320	1	3	0
2803	11	Aluminum / Vinyl	1	1922	1364	1	3	1
2804	11	Brick	1	1955	1359	1	2	1
2805	11	Stone	1	1952	1193	1	2	1
2806	11	Brick	1	1954	1168	1	3	1
2807	11	Brick	1	1956	1148	1	3	2
2808	11	Brick	1	1959	1131	1	3	1
2809	11	Brick	1	1961	1127	1	2	1
2810	11	Aluminum / Vinyl	1	1957	1106	1	2	1

2811	11	Aluminum / Vinyl	1	1953	1104	1	3	1
2812	11	Aluminum / Vinyl	1	1964	1074	1	3	1
2813	11	Aluminum / Vinyl	1	1966	1033	1	3	1
2814	11	Aluminum / Vinyl	1	1963	1026	1	3	1
2815	11	Aluminum / Vinyl	1	1956	1019	1	3	1
2816	11	Aluminum / Vinyl	1	1954	1000	1	3	1
2817	11	Aluminum / Vinyl	1	1957	958	1	3	1
2818	11	Aluminum / Vinyl	1	1953	943	1	3	1
2819	11	Aluminum / Vinyl	1	1952	914	1	3	1
2820	11	Aluminum / Vinyl	1	1954	904	1	3	1
2821	11	Brick	1	1950	895	1	2	1
2822	11	Aluminum / Vinyl	1	1952	880	1	3	1
2823	11	Aluminum / Vinyl	1	1953	879	1	3	1
2824	11	Aluminum / Vinyl	1	1953	879	1	3	1
2825	11	Aluminum / Vinyl	1	1953	879	1	3	1
2826	11	Aluminum / Vinyl	1	1953	876	1	3	1
2827	11	Aluminum / Vinyl	1	1956	876	1	3	1
2828	11	Aluminum / Vinyl	1	1953	864	1	3	1
2829	11	Aluminum / Vinyl	1	1952	811	1	2	1
2830	11	Aluminum / Vinyl	1	1949	706	1	2	1
2831	11	Aluminum / Vinyl	1	1953	672	1	2	1
2832	11	Frame	1	1899	1426	1	3	1
2833	11	Aluminum / Vinyl	1	1925	1301	1	3	2
2834	11	Aluminum / Vinyl	1	1927	1028	1	2	1
2835	11	Brick	2	1956	2806	2	6	2
2836	11	Stone	1.5	1939	1235	1	3	1
2837	12	Frame	2	1914	1768	2	4	2
2838	12	Frame	1	1901	1248	1	3	1
2839	12	Aluminum / Vinyl	1	1912	1180	1	3	1
2840	12	Aluminum / Vinyl	1	1896	1037	1	3	0
2841	12	Aluminum / Vinyl	1	1885	996	1	3	1
2842	12	Aluminum / Vinyl	2	1912	1628	3	4	3
2843	13	Brick	1	1947	1238	1	3	2
2844	13	Brick	1	1951	1200	1	3	1
2845	13	Brick	1	1950	1134	1	3	1
2846	13	Aluminum / Vinyl	1	1940	1078	1	2	2
2847	13	Aluminum / Vinyl	1	1952	1053	1	3	1
2848	13	Aluminum / Vinyl	1	1948	981	1	3	1
2849	13	Aluminum / Vinyl	2	1939	1198	1	2	1
2850	13	Aluminum / Vinyl	2	1940	1193	1	2	1
2851	13	Aluminum / Vinyl	1	1928	1588	2	3	2
2852	13	Brick	2	1960	2076	2	6	2
2853	13	Aluminum / Vinyl	1	1927	1229	1	3	2

2854	13	Aluminum / Vinyl	1	1974	1473	1	3	1
2855	13	Brick	1	1964	1140	1	3	1
2856	13	Brick	1	1967	1129	1	3	1
2857	13	Brick	1	1948	993	1	2	1
2858	13	Aluminum / Vinyl	1	1950	796	1	2	1
2859	13	Aluminum / Vinyl	1	1947	672	1	2	1
2860	14	Aluminum / Vinyl	1	1940	1173	1	3	1
2861	14	Aluminum / Vinyl	1	1953	652	1	2	1
2862	14	Masonry / Frame	2	1925	1580	1	3	1
2863	14	Aluminum / Vinyl	2	1939	1372	1	3	1
2864	14	Aluminum / Vinyl	1	1901	1122	1	4	1
2865	14	Aluminum / Vinyl	2	1924	2148	2	4	2
2866	14	Aluminum / Vinyl	1.5	1927	1890	2	3	2
2867	14	Aluminum / Vinyl	1.5	1916	1648	2	3	2
2868	14	Frame	1.5	1925	1632	2	4	2
2869	14	Aluminum / Vinyl	1	1900	1623	2	5	2
2870	14	Aluminum / Vinyl	1.5	1913	1764	1	5	1
2871	14	Frame	1.5	1929	1173	1	3	1
2872	14	Aluminum / Vinyl	1	1923	1150	1	4	2
2873	14	Aluminum / Vinyl	1	1929	1021	1	2	1
2874	14	Aluminum / Vinyl	1	1944	768	1	2	1
2875	14	Aluminum / Vinyl	1.5	1886	1728	1	4	1
2876	14	Aluminum / Vinyl	1	1900	1431	1	4	2
2877	14	Frame	1	1922	1178	1	3	1
2878	14	Aluminum / Vinyl	1	1928	1065	1	3	1
2879	14	Aluminum / Vinyl	1	1884	1050	1	4	2
2880	14	Frame	1	1928	864	1	1	1
2881	15	Brick	2	1924	2224	1	4	1
2882	15	Aluminum / Vinyl	2	1907	2138	2	4	2
2883	15	Aluminum / Vinyl	2	1875	1656	2	4	2
2884	15	Aluminum / Vinyl	1	1924	748	1	1	1
2886	1	Stone	1	1940	1488	1	4	1
2887	1	Brick	1	1952	1256	1	4	1
2888	1	Aluminum / Vinyl	1	1951	1193	1	4	2
2889	1	Aluminum / Vinyl	1	1941	879	1	3	1
2890	1	Frame	1	1952	1247	1	3	1
2891	1	Aluminum / Vinyl	1	1926	1142	1	3	1
2892	1	Brick	2	1927	1822	1	3	1
2893	2	Stone	2	1934	1806	1	5	1
2894	2	Masonry / Frame	2	1957	2323	2	6	2
2895	2	Aluminum / Vinyl	2	1956	2200	2	6	2
2896	2	Brick	1.5	1956	2077	2	4	2
2897	2	Brick	1	1955	1177	1	3	1

2898	2	Aluminum / Vinyl	1	1967	1072	1	3	1
2899	2	Brick	1	1959	1016	1	3	1
2900	2	Aluminum / Vinyl	1	1955	950	1	3	2
2901	2	Aluminum / Vinyl	1	1955	950	1	3	1
2902	2	Frame	1	1957	925	1	3	1
2903	3	Frame	1	1890	1184	1	3	1
2904	3	Aluminum / Vinyl	1	1880	917	1	2	1
2905	3	Aluminum / Vinyl	2	1912	3350	2	7	3
2906	3	Aluminum / Vinyl	2	1912	1548	1	3	1
2907	4	Stucco	2	1908	2584	1	5	1
2908	5	Brick	1.5	1941	2003	1	4	2
2909	5	Stone	1.5	1949	1758	1	4	2
2910	5	Stone	1	1946	1397	1	3	1
2911	5	Stone	1	1947	1389	1	4	1
2912	5	Brick	1	1956	1258	1	4	2
2913	5	Aluminum / Vinyl	1.5	1954	1192	1	4	2
2914	5	Brick	1	1950	1158	1	3	1
2915	5	Aluminum / Vinyl	1	1953	1102	1	3	2
2916	5	Aluminum / Vinyl	1	1950	980	1	3	1
2917	5	Aluminum / Vinyl	1	1948	858	1	2	1
2918	5	Aluminum / Vinyl	2	1953	1422	1	3	1
2919	5	Aluminum / Vinyl	2	1950	3191	2	6	2
2920	5	Brick	2	1959	2478	2	6	2
2921	5	Brick	2	1959	2478	2	6	2
2922	5	Brick	2	1952	2455	2	4	2
2923	5	Prem Wood	1	2001	2073	1	3	2
2924	5	Brick	1	1955	1475	1	3	2
2925	5	Brick	1	1954	1465	1	2	1
2926	5	Brick	1	1958	1415	1	2	1
2927	5	Brick	1	1956	1382	1	3	1
2928	5	Aluminum / Vinyl	1	1969	1331	1	3	1
2929	5	Brick	1	1960	1235	1	2	2
2930	5	Aluminum / Vinyl	1	1971	1204	1	4	1
2931	5	Brick	1	1956	1150	1	3	1
2932	5	Aluminum / Vinyl	1	1949	1136	1	3	1
2933	5	Aluminum / Vinyl	1	1956	1132	1	3	1
2934	5	Brick	1	1960	1127	1	3	1
2935	5	Aluminum / Vinyl	1	1957	1107	1	3	1
2936	5	Aluminum / Vinyl	1	1955	1099	1	3	1
2937	5	Brick	1	1958	1084	1	3	1
2938	5	Aluminum / Vinyl	1	1948	1027	1	2	1
2939	5	Aluminum / Vinyl	1	1955	1008	1	3	1
2940	5	Aluminum / Vinyl	1	1959	994	1	3	1

2941	5	Aluminum / Vinyl	1	1955	993	1	3	1
2942	5	Brick	1	1956	978	1	3	1
2943	5	Brick	1	1956	936	1	3	1
2944	5	Aluminum / Vinyl	1	1950	871	1	3	1
2945	5	Aluminum / Vinyl	1	1951	789	1	2	1
2946	5	Aluminum / Vinyl	1	1959	1557	1	3	1
2947	6	Fiber-Cement	2	2004	2146	1	3	2
2948	6	Frame	1	1880	1120	1	1	2
2949	6	Frame	2	1890	2428	1	4	2
2950	6	Aluminum / Vinyl	1.5	1910	1645	1	5	1
2951	6	Frame	1	1890	1488	1	3	1
2952	6	Aluminum / Vinyl	1.5	1913	1391	1	3	1
2953	6	Frame	1.5	1880	1350	1	2	1
2954	6	Aluminum / Vinyl	1	1923	1276	1	4	1
2955	6	Aluminum / Vinyl	1	1901	1228	1	4	1
2956	7	Stone	1.5	1934	1755	1	3	1
2957	7	Stone	1	1947	1441	1	3	2
2958	7	Frame	1	1936	1001	1	2	1
2959	7	Aluminum / Vinyl	1	1922	589	1	1	1
2960	7	Brick	2	1958	2284	2	6	2
2961	7	Aluminum / Vinyl	1	1922	1743	1	4	2
2962	7	Aluminum / Vinyl	1	1900	990	1	3	1
2963	8	Aluminum / Vinyl	2	1900	2278	2	6	2
2964	8	Frame	1.5	1918	1636	2	3	2
2965	8	Aluminum / Vinyl	1	1923	1088	1	4	1
2966	8	Brick	1	1955	1188	1	3	1
2967	8	Frame	2	1916	2076	1	3	1
2968	8	Aluminum / Vinyl	1	1892	1523	1	4	2
2969	8	Aluminum / Vinyl	1	1892	1523	1	4	2
2970	8	Aluminum / Vinyl	1.5	1904	1386	1	3	1
2971	8	Aluminum / Vinyl	1.5	1904	1386	1	3	1
2972	9	Fiber-Cement	1	2010	2153	1	3	2
2973	9	Aluminum / Vinyl	1	1968	2127	1	4	2
2974	9	Aluminum / Vinyl	1	1974	1584	1	3	1
2975	9	Aluminum / Vinyl	1	1969	1142	1	2	1
2976	9	Frame	1	1959	1092	1	3	2
2977	9	Aluminum / Vinyl	1	1956	946	1	3	1
2978	9	Aluminum / Vinyl	2	1980	2464	2	6	2
2979	10	Stone	1	1940	1524	1	3	1
2980	10	Aluminum / Vinyl	1	1952	1221	1	4	1
2981	10	Brick	1	1950	1220	1	3	1
2982	10	Aluminum / Vinyl	1	1946	1093	1	3	2
2983	10	Brick	2	1940	1709	1	3	2

2984	10	Block	2	1948	1639	1	3	2
2985	10	Aluminum / Vinyl	2	1951	1514	1	2	1
2986	10	Aluminum / Vinyl	1	1928	1014	1	2	1
2987	10	Aluminum / Vinyl	1	1914	787	1	2	1
2988	10	Brick	2	1922	3609	2	6	2
2989	10	Aluminum / Vinyl	1.5	1925	1891	1	3	2
2990	10	Aluminum / Vinyl	1	1924	1209	1	2	1
2991	10	Aluminum / Vinyl	1	1924	1132	1	3	1
2992	10	Frame	1	1926	1073	1	3	1
2993	10	Aluminum / Vinyl	1	1922	1013	1	2	1
2994	10	Aluminum / Vinyl	1	1918	972	1	4	1
2995	10	Aluminum / Vinyl	1	1955	969	1	3	1
2996	10	Aluminum / Vinyl	1	1954	965	1	3	1
2997	10	Brick	1	1953	784	1	2	1
2998	10	Frame	1	1950	728	1	2	1
2999	10	Masonry / Frame	2	1917	2713	1	5	2
3000	10	Aluminum / Vinyl	2	1893	1741	1	3	1
3001	10	Aluminum / Vinyl	1.5	1900	1685	1	5	1
3002	10	Aluminum / Vinyl	1.5	1922	1392	1	3	2
3003	10	Frame	1	1900	1327	1	3	2
3004	10	Aluminum / Vinyl	1	1919	1063	1	3	1
3005	10	Frame	1	1927	970	1	3	1
3006	10	Stone	2	1956	3630	3	7	4
3007	10	Brick	2	1930	2681	1	3	1
3008	10	Brick	1.5	1931	1560	1	3	1
3009	11	Brick	1.5	1951	2384	1	5	2
3010	11	Aluminum / Vinyl	1	1956	1942	1	3	1
3011	11	Aluminum / Vinyl	1.5	1942	1254	1	2	1
3012	11	Aluminum / Vinyl	1	1952	1129	1	3	1
3013	11	Aluminum / Vinyl	1	1953	1073	1	3	1
3014	11	Aluminum / Vinyl	1	1953	996	1	3	1
3015	11	Aluminum / Vinyl	2	1984	1902	1	3	2
3016	11	Aluminum / Vinyl	2	1957	1378	1	3	1
3017	11	Brick	2	1955	2924	2	5	2
3018	11	Brick	2	1957	2268	2	6	2
3019	11	Aluminum / Vinyl	2	1956	1948	2	6	2
3020	11	Aluminum / Vinyl	1	1984	1597	1	3	3
3021	11	Brick	1	1967	1173	1	3	1
3022	11	Brick	1	1955	1153	1	3	2
3023	11	Brick	1	1959	1130	1	3	1
3024	11	Stone	1	1954	1120	1	3	1
3025	11	Brick	1	1954	1058	1	3	1
3026	11	Aluminum / Vinyl	1	1956	1019	1	3	1

3027	11	Brick	1	1953	1013	1	3	1
3028	11	Aluminum / Vinyl	1	1961	985	1	3	1
3029	11	Aluminum / Vinyl	1	1956	958	1	2	1
3030	11	Aluminum / Vinyl	1	1955	955	1	3	1
3031	11	Brick	1	1956	934	1	3	1
3032	11	Brick	1.5	1918	1479	1	4	1
3033	12	Frame	1	1885	1528	1	5	1
3034	12	Frame	1	1900	1232	1	3	2
3035	12	Aluminum / Vinyl	1	1895	948	1	3	1
3036	12	Aluminum / Vinyl	1	1905	2530	2	7	2
3037	12	Aluminum / Vinyl	2	1900	1814	2	4	1
3039	13	Aluminum / Vinyl	1	1950	1132	1	4	1
3040	13	Stone	1.5	1940	1098	1	2	1
3041	13	Stone	1	1946	968	1	3	1
3042	13	Aluminum / Vinyl	1	1953	840	1	2	1
3043	13	Aluminum / Vinyl	1	1940	816	1	3	1
3044	13	Aluminum / Vinyl	2	1946	1378	1	3	1
3045	13	Aluminum / Vinyl	1	1926	1348	1	4	1
3046	13	Frame	1	1964	1726	1	3	1
3047	13	Aluminum / Vinyl	1	1938	1395	1	3	2
3048	13	Aluminum / Vinyl	1	1965	1144	1	3	1
3049	13	Frame	1	1961	1098	1	3	1
3050	13	Aluminum / Vinyl	1	1966	1036	1	3	1
3051	13	Aluminum / Vinyl	1	1961	981	1	3	2
3052	13	Aluminum / Vinyl	1	1959	927	1	3	1
3053	13	Aluminum / Vinyl	1	1959	921	1	3	2
3054	13	Aluminum / Vinyl	1	1958	905	1	3	1
3055	13	Aluminum / Vinyl	1	1954	872	1	3	1
3056	13	Stone	1	1953	825	1	2	1
3057	13	Aluminum / Vinyl	1	1946	679	1	2	1
3058	13	Aluminum / Vinyl	1	1950	651	1	2	1
3059	14	Aluminum / Vinyl	1.5	1949	1765	1	3	1
3060	14	Aluminum / Vinyl	1	1956	1203	1	2	1
3061	14	Stucco	1	1944	1188	1	2	2
3062	14	Brick	1	1950	1095	1	3	1
3063	14	Brick	1	1948	828	1	2	1
3064	14	Aluminum / Vinyl	2	1948	1378	1	3	1
3065	14	Aluminum / Vinyl	1	1901	1130	1	3	1
3066	14	Aluminum / Vinyl	1	1895	640	1	3	1
3067	14	Brick	1.5	1926	2358	2	5	2
3068	14	Masonry / Frame	2	1928	1942	2	3	3
3069	14	Brick	2	1939	1906	2	4	2
3070	14	Frame	2	1910	2172	2	5	2

3071	14	Aluminum / Vinyl	1.5	1918	1786	2	5	2
3072	14	Aluminum / Vinyl	1.5	1912	1294	2	2	2
3073	14	Aluminum / Vinyl	1	1890	1516	2	3	2
3074	14	Aluminum / Vinyl	1	1905	1360	2	4	1
3075	14	Aluminum / Vinyl	1	1926	1894	1	4	2
3076	14	Aluminum / Vinyl	1.5	1925	1691	1	4	2
3077	14	Frame	1	1926	1622	1	3	2
3078	14	Frame	1	1923	1414	1	4	2
3079	14	Frame	1	1926	1410	1	4	1
3080	14	Frame	1	1927	1331	1	3	1
3081	14	Aluminum / Vinyl	1	1926	1325	1	2	1
3082	14	Stucco	1	1944	1399	1	3	2
3083	14	Aluminum / Vinyl	1	1953	1100	1	3	1
3084	14	Aluminum / Vinyl	1	1953	1100	1	3	1
3085	14	Aluminum / Vinyl	1	1911	1823	1	3	2
3086	14	Aluminum / Vinyl	1.5	1900	1556	1	4	2
3087	14	Aluminum / Vinyl	1	1908	1549	1	4	1
3088	14	Frame	1.5	1885	1336	1	3	2
3089	14	Aluminum / Vinyl	1.5	1888	1179	1	3	1
3090	15	Aluminum / Vinyl	2	2004	2197	1	3	2
3091	15	Aluminum / Vinyl	>2	2006	1884	1	2	2
3092	15	Frame	1	1922	1419	1	3	1
3093	15	Aluminum / Vinyl	1	1970	1023	1	3	1
3094	1	Brick	2	1953	1388	1	4	1
3095	1	Stone	1	1941	1276	1	3	1
3096	1	Brick	1	1946	1173	1	3	1
3097	1	Brick	1	1953	1058	1	3	1
3098	1	Brick	1	1953	1058	1	3	1
3099	1	Brick	1	1949	744	1	2	1
3100	1	Aluminum / Vinyl	1	1905	820	1	2	1
3101	1	Aluminum / Vinyl	1.5	1928	2012	2	4	2
3102	1	Masonry / Frame	2	1951	1692	2	4	2
3103	1	Aluminum / Vinyl	1.5	1920	1188	2	3	2
3104	1	Frame	1	1928	1624	1	4	1
3105	1	Aluminum / Vinyl	1	2007	1439	1	3	2
3106	1	Frame	1	1952	1144	1	3	1
3107	1	Brick	1	1952	998	1	2	1
3108	1	Brick	1	1949	816	1	1	1
3109	2	Brick	1	1959	1416	1	4	2
3110	2	Brick	1	1951	1350	1	2	1
3111	2	Aluminum / Vinyl	1	1955	1211	1	3	1
3112	2	Brick	1.5	1940	1104	1	2	1
3113	2	Aluminum / Vinyl	1	1955	1068	1	4	1

3114	2	Brick	2	1959	2662	2	6	2
3115	2	Brick	1	1959	1206	1	3	1
3116	2	Brick	1	1955	1177	1	3	1
3117	2	Frame	1	1972	1144	1	4	1
3118	2	Aluminum / Vinyl	1	1955	1120	1	3	1
3119	2	Aluminum / Vinyl	1	1956	1041	1	3	1
3120	2	Aluminum / Vinyl	1	1976	1022	1	3	1
3121	2	Brick	1	1955	1020	1	3	1
3122	2	Aluminum / Vinyl	1	1955	950	1	3	1
3123	2	Aluminum / Vinyl	1	1956	936	1	3	1
3124	2	Aluminum / Vinyl	1	1950	930	1	2	1
3125	2	Aluminum / Vinyl	1	1957	925	1	3	1
3126	2	Aluminum / Vinyl	1	1956	905	1	3	1
3127	3	Frame	2	1923	2210	1	4	2
3128	3	Masonry / Frame	2	1925	1994	1	3	1
3129	3	Aluminum / Vinyl	2	1890	1813	1	4	2
3130	3	Aluminum / Vinyl	2	1890	2973	2	6	2
3131	3	Frame	1.5	1890	2507	2	4	2
3132	3	Aluminum / Vinyl	2	1900	1642	2	4	2
3133	3	Brick	1	1929	1999	1	4	2
3134	3	Frame	1.5	1920	1980	1	4	1
3135	3	Aluminum / Vinyl	1.5	1922	1970	1	3	1
3136	3	Frame	1	1914	1692	1	4	1
3137	3	Frame	1.5	1889	1494	1	3	1
3138	3	Frame	1	1900	1049	1	3	1
3139	4	Stucco	1	1909	1040	1	4	2
3140	5	Aluminum / Vinyl	1	1976	1784	1	4	3
3141	5	Brick	1.5	1948	1748	1	4	2
3142	5	Stone	1.5	1947	1646	1	4	2
3143	5	Brick	1	1950	1600	1	4	2
3144	5	Aluminum / Vinyl	1.5	1939	1553	1	3	2
3145	5	Aluminum / Vinyl	1	1954	1510	1	3	1
3146	5	Brick	1	1947	1322	1	3	1
3147	5	Aluminum / Vinyl	1	1952	1215	1	3	1
3148	5	Aluminum / Vinyl	1	1952	1168	1	4	2
3149	5	Aluminum / Vinyl	1	1952	1080	1	4	2
3150	5	Brick	1	1940	1071	1	3	1
3151	5	Fiber-Cement	2	2008	3535	1	5	3
3152	5	Aluminum / Vinyl	2	2009	2195	1	4	2
3153	5	Brick	2	1946	1498	1	3	1
3154	5	Masonry / Frame	2	1955	2079	2	4	2
3155	5	Brick	1	1954	2129	1	2	1
3156	5	Brick	1	1977	1358	1	3	2

3157	5	Brick	1	1960	1254	1	3	1
3158	5	Brick	1	1955	1237	1	3	2
3159	5	Aluminum / Vinyl	1	1952	1188	1	4	1
3160	5	Brick	1	1954	1177	1	3	1
3161	5	Brick	1	1957	1115	1	3	1
3162	5	Masonry / Frame	1	1956	1060	1	3	1
3163	5	Aluminum / Vinyl	1	1953	1052	1	3	1
3164	5	Aluminum / Vinyl	1	1956	1019	1	3	1
3165	5	Aluminum / Vinyl	1	1956	1019	1	3	1
3166	5	Aluminum / Vinyl	1	1955	1008	1	3	1
3167	5	Aluminum / Vinyl	1	1962	999	1	3	1
3168	5	Aluminum / Vinyl	1	1953	888	1	3	2
3169	5	Aluminum / Vinyl	1	1953	864	1	3	1
3170	5	Aluminum / Vinyl	1	1924	1235	1	3	1
3171	5	Aluminum / Vinyl	1	1981	1970	1	3	2
3172	6	Frame	1	1924	1368	1	4	1
3174	6	Aluminum / Vinyl	2	1992	2788	2	6	2
3175	7	Stone	1	1936	1716	1	4	2
3176	7	Brick	1.5	1938	1492	1	2	1
3177	7	Brick	1.5	1939	1488	1	4	1
3178	7	Brick	1.5	1938	1408	1	2	1
3179	7	Frame	1	1962	1162	1	4	1
3180	7	Aluminum / Vinyl	1	1952	1075	1	3	1
3181	7	Aluminum / Vinyl	2	1924	2882	2	7	2
3182	7	Aluminum / Vinyl	1.5	1927	1725	2	3	2
3183	7	Brick	1	1928	1721	1	4	1
3184	7	Aluminum / Vinyl	1	1915	840	1	3	1
3185	7	Brick	1	1950	1270	1	4	2
3186	7	Stone	1	1947	1206	1	2	1
3187	7	Brick	2	1931	1772	1	3	1
3188	8	Prem Wood	1.5	1913	1245	1	3	2
3189	8	Aluminum / Vinyl	1	1924	1905	1	5	1
3190	8	Aluminum / Vinyl	1	1928	1614	1	4	2
3191	8	Brick	1	1928	1551	1	4	1
3192	8	Frame	1	1957	1026	1	3	1
3193	8	Aluminum / Vinyl	1	1913	1239	1	3	2
3194	8	Aluminum / Vinyl	1	1912	934	1	3	1
3195	9	Masonry / Frame	1.5	1925	1377	1	3	1
3196	9	Aluminum / Vinyl	1	2005	1932	1	3	2
3197	9	Aluminum / Vinyl	1	2010	1709	1	3	2
3198	9	Aluminum / Vinyl	1	1958	1515	1	3	1
3199	9	Aluminum / Vinyl	1	1972	1219	1	3	1
3200	9	Aluminum / Vinyl	1	1956	996	1	3	1

3201	9	Aluminum / Vinyl	1	1957	991	1	4	2
3202	10	Stone	1	1936	1807	1	4	2
3203	10	Brick	1	1948	1108	1	3	1
3204	10	Aluminum / Vinyl	1	1957	1100	1	3	2
3205	10	Brick	2	1937	1727	1	3	1
3206	10	Masonry / Frame	2	1955	1675	1	3	2
3207	10	Aluminum / Vinyl	2	1926	1271	1	3	1
3208	10	Aluminum / Vinyl	1	1925	760	1	3	1
3209	10	Aluminum / Vinyl	2	1926	2139	2	5	2
3210	10	Aluminum / Vinyl	1.5	1925	2337	1	5	2
3211	10	Aluminum / Vinyl	1	1918	1873	1	3	2
3212	10	Aluminum / Vinyl	1	1924	1685	1	4	2
3213	10	Aluminum / Vinyl	1	1925	1273	1	3	1
3214	10	Brick	1	1941	1516	1	2	1
3215	10	Brick	1	1951	912	1	2	2
3216	10	Brick	1	1926	2036	1	3	2
3217	10	Aluminum / Vinyl	1	1911	2028	1	3	2
3218	10	Aluminum / Vinyl	1.5	1927	1451	1	4	2
3219	10	Brick	1.5	1923	1304	1	3	1
3220	11	Stone	1.5	1938	1434	1	3	1
3221	11	Aluminum / Vinyl	1	1954	1037	1	3	1
3222	11	Brick	1	1949	800	1	2	1
3223	11	Masonry / Frame	2	1941	1720	1	3	1
3224	11	Stone	2	1937	1652	1	3	1
3225	11	Aluminum / Vinyl	1.5	1955	1916	2	5	2
3226	11	Aluminum / Vinyl	2	1954	1728	2	6	2
3227	11	Brick	1	1931	1177	1	2	1
3228	11	Stone	1	1950	1392	1	2	2
3229	11	Aluminum / Vinyl	1	1968	1275	1	4	1
3230	11	Brick	1	1961	1192	1	3	1
3231	11	Stone	1	1949	1127	1	3	1
3232	11	Brick	1	1956	1112	1	3	1
3233	11	Brick	1	1958	1112	1	3	1
3234	11	Frame	1	1964	1094	1	3	1
3235	11	Aluminum / Vinyl	1	1961	1058	1	3	2
3236	11	Brick	1	1954	1013	1	3	2
3237	11	Aluminum / Vinyl	1	1953	971	1	2	2
3238	11	Aluminum / Vinyl	1	1951	884	1	3	1
3239	11	Aluminum / Vinyl	1	1955	876	1	3	1
3240	11	Brick	1	1950	839	1	2	1
3241	11	Brick	1	1924	1154	1	3	1
3242	11	Stone	1.5	1939	1565	1	4	2
3243	12	Frame	1.5	1909	1265	1	3	1

3244	12	Aluminum / Vinyl	1	1860	740	1	1	1
3245	12	Frame	1.5	1914	2408	2	5	3
3246	12	Aluminum / Vinyl	1	1905	1516	1	4	1
3247	13	Brick	1	1949	1312	1	3	1
3248	13	Frame	1	1951	1284	1	4	2
3249	13	Aluminum / Vinyl	1	1941	1213	1	3	1
3250	13	Aluminum / Vinyl	1	1948	1114	1	3	2
3251	13	Aluminum / Vinyl	1	1947	1046	1	2	1
3252	13	Aluminum / Vinyl	1	1956	780	1	2	1
3253	13	Aluminum / Vinyl	2	1967	1638	1	4	1
3254	13	Stucco	1.5	1920	1741	2	5	2
3255	13	Aluminum / Vinyl	1.5	1926	1474	1	4	2
3256	13	Brick	1	1967	1475	1	3	1
3257	13	Brick	1	1969	1409	1	3	1
3258	13	Aluminum / Vinyl	1	1970	1177	1	3	1
3259	13	Aluminum / Vinyl	1	1960	1030	1	3	1
3260	13	Aluminum / Vinyl	1	1956	943	1	3	1
3261	14	Brick	1	1953	1285	1	3	1
3262	14	Aluminum / Vinyl	1	1947	1226	1	3	1
3263	14	Aluminum / Vinyl	1	1938	996	1	3	1
3264	14	Brick	2	1951	2196	1	3	2
3265	14	Aluminum / Vinyl	2	1924	1356	1	3	1
3266	14	Aluminum / Vinyl	2	1949	968	1	2	1
3267	14	Aluminum / Vinyl	1.5	1921	1295	1	4	2
3268	14	Aluminum / Vinyl	2	1926	1785	2	4	2
3269	14	Aluminum / Vinyl	1.5	1926	1644	2	3	2
3270	14	Aluminum / Vinyl	2	1891	2482	2	6	2
3271	14	Brick	2	1876	2274	2	4	3
3272	14	Aluminum / Vinyl	2	1913	1634	2	4	2
3273	14	Frame	1.5	1926	1510	1	4	1
3274	14	Aluminum / Vinyl	1.5	1916	1327	1	3	2
3275	14	Aluminum / Vinyl	1	1921	1238	1	3	1
3276	14	Aluminum / Vinyl	1.5	1918	1160	1	3	1
3277	14	Aluminum / Vinyl	1	1926	1058	1	3	1
3278	14	Aluminum / Vinyl	1	1925	1029	1	1	1
3279	14	Aluminum / Vinyl	1	1941	840	1	2	1
3280	14	Aluminum / Vinyl	1	1948	826	1	2	1
3281	14	Aluminum / Vinyl	1	1942	826	1	2	1
3282	14	Aluminum / Vinyl	1	1951	795	1	2	1
3283	14	Aluminum / Vinyl	2	1891	2514	1	3	2
3284	14	Frame	2	1905	2017	1	3	2
3285	14	Frame	1.5	1889	1382	1	3	1
3286	14	Aluminum / Vinyl	1	1913	1062	1	2	3

3287	15	Frame	2	1890	2898	2	5	3
3288	15	Frame	2	1904	2662	2	6	2
3289	1	Stucco	1.5	1926	2251	2	4	2
3290	1	Aluminum / Vinyl	1.5	1914	1921	2	5	2
3291	1	Aluminum / Vinyl	1	1964	1213	1	3	2
3292	1	Aluminum / Vinyl	1	1954	963	1	3	2
3293	1	Frame	1	1949	768	1	2	1
3294	2	Brick	1	1954	1267	1	3	1
3295	2	Aluminum / Vinyl	1	1955	1240	1	4	1
3296	2	Stone	1	1963	1392	1	4	1
3297	2	Brick	1	1957	1274	1	3	2
3298	2	Brick	1	1957	1147	1	3	1
3299	2	Aluminum / Vinyl	1	1958	1040	1	3	1
3300	2	Aluminum / Vinyl	1	1961	960	1	3	1
3301	2	Aluminum / Vinyl	1	1956	936	1	2	1
3302	2	Aluminum / Vinyl	1	1952	925	1	2	1
3303	2	Aluminum / Vinyl	1	1955	838	1	2	1
3304	3	Aluminum / Vinyl	1.5	1894	1774	2	3	2
3305	3	Aluminum / Vinyl	1.5	1911	1559	2	4	3
3306	3	Aluminum / Vinyl	1	1890	2053	2	3	2
3307	3	Aluminum / Vinyl	1	1926	1126	1	3	1
3308	3	Masonry / Frame	2	1909	2156	1	4	1
3309	3	Aluminum / Vinyl	2	1893	1543	1	3	1
3310	4	Frame	2	1909	2014	1	4	1
3311	5	Aluminum / Vinyl	1	1950	1156	1	3	2
3312	5	Aluminum / Vinyl	1	1951	1139	1	3	1
3313	5	Aluminum / Vinyl	1	1952	1102	1	3	1
3314	5	Aluminum / Vinyl	2	1969	1709	1	4	2
3315	5	Aluminum / Vinyl	2	1954	1415	1	3	1
3316	5	Masonry / Frame	2	1951	2016	2	4	2
3317	5	Aluminum / Vinyl	1.5	1960	1841	2	5	2
3318	5	Aluminum / Vinyl	1	1966	1332	1	4	1
3319	5	Brick	1	1956	1101	1	2	1
3320	5	Aluminum / Vinyl	1	1952	768	1	2	1
3321	5	Aluminum / Vinyl	2	1970	2405	2	6	2
3322	6	Aluminum / Vinyl	1.5	1923	1452	2	3	2
3323	7	Aluminum / Vinyl	1	1953	1283	1	4	1
3324	7	Aluminum / Vinyl	1	1941	1188	1	4	1
3325	7	Masonry / Frame	2	1924	1888	1	4	1
3326	7	Stone	2	1944	1884	2	4	2
3327	7	Frame	2	1942	1722	2	4	2
3328	7	Aluminum / Vinyl	1	1932	1204	1	3	1
3329	8	Aluminum / Vinyl	2	1925	2088	2	4	2

3330	8	Aluminum / Vinyl	1.5	1915	1872	2	3	2
3331	8	Aluminum / Vinyl	2	1915	2484	2	6	2
3332	8	Aluminum / Vinyl	2	1915	2450	2	5	2
3333	8	Frame	2	1905	1652	2	5	2
3334	8	Frame	1	1919	1619	1	4	1
3335	8	Aluminum / Vinyl	1	1928	1250	1	4	1
3336	8	Brick	1.5	1924	2298	1	3	0
3337	8	Frame	1	1900	2085	1	5	2
3338	8	Aluminum / Vinyl	1.5	1889	1697	1	4	2
3339	8	Aluminum / Vinyl	2	1916	1532	1	3	1
3340	8	Frame	1	1900	1096	1	3	1
3341	8	Frame	1	1911	1022	1	3	1
3342	9	Brick	1	1957	1308	1	3	1
3343	9	Aluminum / Vinyl	1	1959	1117	1	3	1
3344	9	Aluminum / Vinyl	1	1959	1024	1	3	1
3345	9	Aluminum / Vinyl	1	1954	958	1	3	1
3346	10	Brick	2	1929	2122	1	3	2
3347	10	Masonry / Frame	2	1953	1657	1	3	1
3348	10	Masonry / Frame	2	1925	2600	2	4	2
3349	10	Aluminum / Vinyl	1	1921	1824	1	4	3
3350	10	Frame	1	1917	1636	1	4	1
3351	10	Aluminum / Vinyl	1	1927	1454	1	5	2
3352	10	Aluminum / Vinyl	1	1926	1398	1	3	1
3353	10	Aluminum / Vinyl	1	1927	1269	1	3	1
3354	10	Stone	1	1955	1519	1	2	1
3355	10	Aluminum / Vinyl	1	1956	1045	1	2	1
3356	10	Aluminum / Vinyl	1	1949	746	1	2	1
3357	10	Aluminum / Vinyl	1	1937	616	1	2	1
3358	10	Aluminum / Vinyl	1.5	1896	1492	1	3	2
3359	10	Aluminum / Vinyl	1	1925	1185	1	3	1
3360	10	Aluminum / Vinyl	1	1917	1113	1	3	1
3361	11	Frame	1.5	1955	1340	1	3	1
3362	11	Brick	1	1949	1210	1	3	1
3363	11	Aluminum / Vinyl	1.5	1997	2404	2	5	3
3364	11	Aluminum / Vinyl	2	1953	1904	2	6	2
3365	11	Brick	1	1956	1260	1	3	2
3366	11	Brick	1	1966	1170	1	3	1
3367	11	Brick	1	1956	1150	1	3	1
3368	11	Aluminum / Vinyl	1	1956	1073	1	3	2
3369	11	Aluminum / Vinyl	1	1954	986	1	3	1
3370	11	Aluminum / Vinyl	1	1954	972	1	3	1
3371	11	Brick	1	1956	947	1	3	1
3372	13	Brick	1	1980	1945	1	3	2

3373	13	Brick	1	1953	1224	1	4	1
3374	13	Brick	1	1959	1203	1	3	1
3375	13	Brick	1	1953	1200	1	3	1
3376	13	Aluminum / Vinyl	1	1939	1187	1	3	1
3377	13	Brick	1	1955	1091	1	4	1
3378	13	Aluminum / Vinyl	2	1998	2196	1	3	2
3379	13	Aluminum / Vinyl	1.5	1943	1240	2	4	2
3380	13	Aluminum / Vinyl	1	1926	1310	1	4	1
3381	13	Aluminum / Vinyl	1	1936	1101	1	3	2
3382	13	Aluminum / Vinyl	1	1958	1243	1	2	1
3383	13	Aluminum / Vinyl	1	1913	1524	1	4	1
3384	13	Brick	2	1954	2588	3	4	3
3385	13	Aluminum / Vinyl	1.5	1904	1722	3	3	3
3386	14	Brick	1	1952	1515	1	4	1
3387	14	Block	1	1944	995	1	3	1
3388	14	Brick	1	1951	977	1	3	1
3389	14	Aluminum / Vinyl	1	1950	776	1	2	1
3390	14	Aluminum / Vinyl	1	1890	733	1	2	1
3391	14	Masonry / Frame	2	1919	3721	2	4	3
3392	14	Aluminum / Vinyl	1	1922	1724	1	5	1
3393	14	Brick	1	1929	1618	1	4	1
3394	14	Frame	1	1916	1584	1	4	2
3395	14	Frame	1	1926	1417	1	3	1
3396	14	Aluminum / Vinyl	1	1927	1038	1	3	1
3397	14	Brick	1	1955	840	1	2	2
3398	14	Brick	1	1953	763	1	2	2
3399	14	Brick	2	1929	1629	1	3	1
3400	14	Aluminum / Vinyl	1	1910	1560	1	3	1
3401	14	Frame	1.5	1920	1339	1	3	1
3402	14	Aluminum / Vinyl	1	1921	1139	1	3	2
3403	15	Frame	2	1970	1350	1	4	1
3404	15	Frame	2	1923	2754	2	4	2
3405	15	Frame	2	1923	2232	2	4	2
3406	15	Aluminum / Vinyl	2	1923	2217	2	4	2
3407	15	Frame	2	1913	2189	2	4	2
3408	1	Stone	1	1939	1346	1	3	1
3409	1	Aluminum / Vinyl	1	1951	1158	1	3	1
3410	1	Brick	1	1936	1078	1	3	1
3411	1	Aluminum / Vinyl	1	1951	1002	1	3	2
3412	1	Aluminum / Vinyl	1	1979	1215	1	3	1
3413	1	Stone	1	1936	1047	1	2	1
3414	1	Stone	1	1936	1047	1	2	1
3415	1	Aluminum / Vinyl	1	1954	983	1	3	1

3416	1	Masonry / Frame	1	1959	1698	1	3	2
3417	2	Brick	1	1960	1220	1	3	1
3418	2	Aluminum / Vinyl	1	1958	1039	1	3	1
3419	2	Aluminum / Vinyl	1	1954	980	1	2	1
3420	2	Frame	1	1955	950	1	3	1
3421	2	Brick	1	1953	825	1	2	1
3422	3	Aluminum / Vinyl	1.5	1926	1877	2	4	2
3423	3	Aluminum / Vinyl	2	1911	2310	2	4	2
3424	3	Brick	2	1928	3768	1	5	3
3425	3	Frame	2	1901	2419	1	5	2
3426	3	Aluminum / Vinyl	2	1902	2383	1	4	1
3427	3	Aluminum / Vinyl	2	1906	2185	1	6	1
3428	3	Brick	2	1921	3140	1	3	2
3429	5	Aluminum / Vinyl	1.5	1953	1434	1	3	1
3430	5	Aluminum / Vinyl	1	1952	1381	1	3	2
3431	5	Aluminum / Vinyl	1	1949	1180	1	3	1
3432	5	Aluminum / Vinyl	1	1949	1170	1	3	2
3433	5	Brick	1	1946	1128	1	3	1
3434	5	Aluminum / Vinyl	1	1948	1049	1	3	1
3435	5	Aluminum / Vinyl	1	1951	728	1	2	1
3436	5	Aluminum / Vinyl	2	2010	2473	1	4	2
3437	5	Brick	1.5	1952	2092	2	3	2
3438	5	Aluminum / Vinyl	1.5	1958	1814	2	5	2
3439	5	Stone	1	1955	2290	1	3	2
3440	5	Aluminum / Vinyl	1	2010	2222	1	3	2
3441	5	Brick	1	1956	1157	1	3	1
3442	5	Brick	1	1959	1153	1	3	1
3443	6	Fiber-Cement	2	2003	1848	1	3	2
3444	6	Aluminum / Vinyl	2	1914	2422	2	4	3
3445	6	Frame	2	1906	1935	2	4	2
3446	6	Aluminum / Vinyl	1	1900	1107	1	3	1
3447	7	Stucco	1.5	1942	1827	1	3	1
3448	7	Brick	1	1940	1198	1	2	1
3449	7	Masonry / Frame	2	1938	1411	1	3	1
3450	7	Aluminum / Vinyl	2	1972	1134	1	4	1
3451	7	Frame	2	1925	2184	2	4	2
3452	7	Aluminum / Vinyl	1	1946	744	1	2	1
3453	8	Aluminum / Vinyl	1	1890	1415	1	2	2
3454	8	Aluminum / Vinyl	1.5	1920	1855	2	4	2
3455	8	Brick	2	1959	2624	2	4	2
3456	8	Aluminum / Vinyl	1.5	1926	1819	2	4	2
3457	8	Aluminum / Vinyl	2	1890	1408	2	4	2
3458	8	Aluminum / Vinyl	1	1896	1482	1	4	1

3459	8	Aluminum / Vinyl	1.5	1917	1357	1	2	1
3460	8	Aluminum / Vinyl	1	1920	1322	1	3	2
3461	9	Aluminum / Vinyl	2	1957	1940	2	6	2
3462	9	Masonry / Frame	1	1959	1610	1	4	3
3463	9	Aluminum / Vinyl	1	1971	1210	1	4	1
3464	9	Aluminum / Vinyl	1	1957	1149	1	3	1
3465	10	Stone	1.5	1941	1889	1	4	2
3466	10	Aluminum / Vinyl	1	1946	1030	1	3	2
3467	10	Brick	2	1935	1692	1	4	2
3468	10	Masonry / Frame	2	1953	1657	1	3	1
3469	10	Block	2	1916	2130	2	6	2
3470	10	Brick	1	1931	1874	1	4	1
3471	10	Brick	1	1921	1857	1	4	1
3472	10	Frame	1	1920	1654	1	4	1
3473	10	Aluminum / Vinyl	1	1922	1495	1	4	1
3474	10	Aluminum / Vinyl	1	1929	1324	1	3	1
3475	10	Aluminum / Vinyl	1	1925	1152	1	3	1
3476	10	Brick	1	1951	762	1	2	1
3477	10	Aluminum / Vinyl	1	1925	768	1	3	1
3478	11	Stone	1	1946	1691	1	4	1
3479	11	Stone	1	1939	1320	1	3	1
3480	11	Brick	1	1951	1309	1	3	1
3481	11	Brick	1	1949	1079	1	3	1
3482	11	Masonry / Frame	2	1936	1376	1	3	1
3483	11	Aluminum / Vinyl	2	1953	1554	2	4	2
3484	11	Brick	1.5	1939	1868	2	4	2
3485	11	Aluminum / Vinyl	1.5	1920	1844	1	5	2
3486	11	Frame	1	1956	1490	1	5	1
3487	11	Aluminum / Vinyl	1	1977	1334	1	3	2
3488	11	Masonry / Frame	1	1959	1319	1	3	1
3489	11	Aluminum / Vinyl	1	1959	1190	1	3	1
3490	11	Brick	1	1958	1114	1	3	1
3491	11	Frame	1	1955	1008	1	3	1
3492	11	Aluminum / Vinyl	1	1954	972	1	3	1
3493	12	Stucco	1.5	1900	1630	2	4	2
3494	12	Aluminum / Vinyl	1	1903	1030	1	3	1
3495	13	Brick	1.5	1969	1718	1	4	2
3496	13	Aluminum / Vinyl	1	1951	1304	1	4	1
3497	13	Aluminum / Vinyl	1	1939	1301	1	2	2
3498	13	Brick	1	1949	1158	1	3	1
3499	13	Brick	1.5	1938	1148	1	2	2
3500	13	Aluminum / Vinyl	2	1941	1252	1	3	1
3501	13	Aluminum / Vinyl	2	1953	1082	1	2	1

3502	13	Brick	2	1955	2160	2	4	2
3503	13	Brick	1.5	1947	2019	2	3	2
3504	13	Brick	1	1955	1032	1	3	1
3505	13	Aluminum / Vinyl	1	1960	891	1	3	1
3506	14	Brick	1	1953	1342	1	4	1
3507	14	Aluminum / Vinyl	1	1941	826	1	3	2
3508	14	Brick	1.5	1939	2042	2	4	2
3509	14	Brick	2	1942	2016	2	4	2
3510	14	Brick	1	1926	1902	1	4	2
3511	14	Aluminum / Vinyl	1	1931	1669	1	4	2
3512	14	Brick	1	1929	1407	1	3	2
3513	14	Aluminum / Vinyl	1	1927	1359	1	4	1
3514	14	Frame	1	1922	1324	1	3	1
3515	14	Aluminum / Vinyl	1	1927	1198	1	3	1
3516	14	Aluminum / Vinyl	1	1926	1029	1	2	1
3517	14	Aluminum / Vinyl	1	1942	791	1	2	1
3518	14	Aluminum / Vinyl	1.5	1925	1449	1	4	1
3519	15	Frame	2	1915	2316	2	4	2
3520	15	Aluminum / Vinyl	2	1893	2080	2	4	2
3521	15	Brick	1	1921	2287	1	3	2
3522	15	Aluminum / Vinyl	2	1913	1674	1	5	1
3523	15	Frame	1	1914	1624	1	3	1
3524	1	Brick	1	1949	1059	1	3	1
3525	1	Aluminum / Vinyl	2	1966	1649	1	4	1
3526	1	Brick	1	1925	1469	1	4	2
3527	1	Aluminum / Vinyl	1	1931	794	1	2	1
3528	2	Aluminum / Vinyl	1	1941	1109	1	4	1
3529	2	Stone	1	1962	1280	1	3	1
3530	2	Aluminum / Vinyl	1	1966	1077	1	3	1
3531	2	Aluminum / Vinyl	1	1961	1053	1	3	1
3532	2	Stone	1	1951	964	1	3	1
3533	2	Aluminum / Vinyl	1	1955	912	1	3	1
3534	3	Aluminum / Vinyl	1	1946	700	1	2	1
3535	3	Frame	1.5	1914	2072	2	3	2
3536	3	Frame	1	1926	1422	1	3	1
3537	3	Aluminum / Vinyl	1	1922	1392	1	4	1
3538	3	Aluminum / Vinyl	2	1908	2156	1	4	1
3539	3	Aluminum / Vinyl	2	1897	1530	1	3	1
3540	5	Frame	1	1953	1494	1	3	1
3541	5	Brick	1	1949	1260	1	3	1
3542	5	Brick	1	1947	801	1	2	1
3543	5	Aluminum / Vinyl	2	2007	1984	1	3	2
3544	5	Aluminum / Vinyl	2	1968	1631	1	4	1

3545	5	Frame	2	1959	1484	1	4	1
3546	5	Aluminum / Vinyl	2	1963	1200	1	3	1
3547	5	Brick	1	1963	2235	2	5	2
3548	5	Brick	1.5	1956	1818	2	4	2
3549	5	Aluminum / Vinyl	1	1971	1499	1	3	1
3550	5	Frame	1	1956	1276	1	3	2
3551	5	Brick	1	1960	1237	1	3	2
3552	5	Aluminum / Vinyl	1	1964	1212	1	3	1
3553	5	Block	1	1942	1170	1	2	2
3554	5	Aluminum / Vinyl	1	1949	1056	1	3	1
3555	5	Brick	1	1958	1036	1	2	1
3556	5	Aluminum / Vinyl	1	1950	1000	1	2	1
3557	5	Aluminum / Vinyl	1	1955	948	1	3	1
3558	5	Aluminum / Vinyl	1	1949	624	1	2	1
3559	5	Aluminum / Vinyl	1	1993	2240	1	4	3
3560	6	Frame	2	1923	2092	2	2	2
3561	6	Frame	1	1925	1212	1	3	1
3562	6	Aluminum / Vinyl	2	1904	1610	1	6	1
3563	7	Brick	1	1950	1271	1	3	1
3564	7	Brick	2	1958	2774	2	6	4
3565	7	Aluminum / Vinyl	1.5	1923	2024	1	5	2
3566	7	Aluminum / Vinyl	1.5	1923	2024	1	5	2
3567	8	Masonry / Frame	2	1928	2200	2	4	2
3568	8	Frame	1	1924	1248	1	4	1
3569	9	Aluminum / Vinyl	1	1952	1480	1	3	2
3570	9	Aluminum / Vinyl	1	1956	1192	1	4	1
3571	9	Aluminum / Vinyl	2	2004	2561	1	4	2
3572	9	Aluminum / Vinyl	2	1987	1737	1	3	1
3573	9	Brick	1	1957	1282	1	3	1
3574	9	Aluminum / Vinyl	1	1975	1227	1	3	2
3575	9	Brick	1	1958	1112	1	3	2
3576	9	Brick	1	1958	1100	1	3	1
3577	9	Frame	1	1962	1045	1	3	1
3578	9	Aluminum / Vinyl	1	1957	948	1	3	1
3579	10	Brick	1	1957	1892	1	5	2
3580	10	Aluminum / Vinyl	1	1950	1037	1	4	1
3581	10	Aluminum / Vinyl	2	1969	2094	2	6	2
3582	10	Brick	1.5	1949	1529	2	3	2
3583	10	Brick	1	1927	1874	1	4	2
3584	10	Aluminum / Vinyl	1	1926	1055	1	3	1
3585	10	Aluminum / Vinyl	1	1949	945	1	2	1
3586	10	Frame	1.5	1925	1406	1	3	2
3587	10	Aluminum / Vinyl	1	1920	1099	1	3	1

3588	11	Brick	1	1954	1645	1	4	1
3589	11	Brick	1	1945	1243	1	3	1
3590	11	Frame	1	1958	1211	1	4	1
3591	11	Brick	1.5	1938	1164	1	3	1
3592	11	Aluminum / Vinyl	1	1949	1086	1	3	1
3593	11	Aluminum / Vinyl	1	1954	952	1	3	1
3594	11	Masonry / Frame	2	1959	1682	1	3	1
3595	11	Aluminum / Vinyl	2	1958	2249	2	6	2
3596	11	Aluminum / Vinyl	1.5	1955	1587	2	4	2
3597	11	Aluminum / Vinyl	1	1966	1853	1	3	2
3598	11	Aluminum / Vinyl	1	1953	1285	1	3	1
3599	11	Frame	1	1947	1254	1	3	2
3600	11	Stone	1	1950	1251	1	2	2
3601	11	Frame	1	1957	1158	1	3	1
3602	11	Brick	1	1958	1114	1	3	1
3604	11	Brick	1	1956	1025	1	3	1
3605	11	Frame	1	1972	1944	1	3	2
3606	11	Aluminum / Vinyl	2	1968	3214	3	7	3
3607	12	Aluminum / Vinyl	1	1880	950	1	3	1
3608	12	Aluminum / Vinyl	2	1914	2328	2	5	2
3609	12	Frame	2	1890	2297	2	6	2
3610	13	Aluminum / Vinyl	1	1945	1184	1	3	1
3611	13	Aluminum / Vinyl	1	1943	1006	1	3	1
3612	13	Prem Wood	2	1974	1980	1	5	1
3613	13	Aluminum / Vinyl	1.5	1928	1734	2	4	2
3614	13	Aluminum / Vinyl	1	1950	956	1	3	1
3615	13	Brick	1	1955	811	1	2	1
3616	13	Aluminum / Vinyl	1	1954	768	1	2	1
3617	13	Aluminum / Vinyl	1	1952	705	1	2	1
3618	13	Aluminum / Vinyl	2	1928	1234	1	3	1
3619	13	Aluminum / Vinyl	1.5	1924	1073	1	3	1
3620	14	Aluminum / Vinyl	1	1953	1056	1	3	1
3621	14	Aluminum / Vinyl	1	1953	784	1	2	1
3622	14	Aluminum / Vinyl	2	1909	2746	2	6	2
3623	14	Aluminum / Vinyl	1.5	1900	1566	2	4	2
3624	14	Frame	1	1900	1233	1	2	1
3625	14	Frame	1	1928	1094	1	2	1
3626	14	Aluminum / Vinyl	1	1924	1028	1	2	1
3627	15	Aluminum / Vinyl	1	2000	1430	1	2	1
3628	15	Aluminum / Vinyl	2	1969	1042	1	3	1
3629	15	Aluminum / Vinyl	1	1922	760	1	1	1
3630	15	Stucco	2	1916	2964	2	6	2
3631	15	Aluminum / Vinyl	2	1909	2350	2	6	2

3632	15	Brick	1.5	1924	2435	1	5	2
3633	15	Brick	1	1920	1960	1	3	2
3634	15	Aluminum / Vinyl	1.5	1890	1358	1	4	1
3635	1	Brick	1	1950	1001	1	3	1
3636	1	Aluminum / Vinyl	2	1967	2010	2	6	2
3637	1	Frame	1	1963	1633	1	3	1
3638	1	Aluminum / Vinyl	1	1974	1503	1	3	1
3639	1	Aluminum / Vinyl	1	1955	1082	1	3	1
3640	1	Aluminum / Vinyl	1	1947	1041	1	3	1
3641	1	Aluminum / Vinyl	1	1951	713	1	2	1
3642	2	Frame	1	1953	1268	1	4	2
3643	2	Aluminum / Vinyl	1	1955	1176	1	4	1
3644	2	Frame	1	1935	740	1	2	1
3645	2	Brick	1	1959	1173	1	3	1
3646	2	Aluminum / Vinyl	1	1956	982	1	3	1
3647	2	Brick	1	1957	942	1	3	1
3648	3	Frame	2	2003	2793	1	3	2
3649	3	Brick	2	1906	4098	1	6	3
3650	3	Brick	1	1927	1686	1	3	2
3651	3	Frame	1	1904	968	1	3	1
3652	5	Frame	1.5	1958	1664	1	4	1
3653	5	Brick	1	1952	1642	1	4	1
3654	5	Brick	1	1948	1276	1	3	1
3655	5	Brick	1	1949	1245	1	3	1
3656	5	Aluminum / Vinyl	1	1953	1005	1	3	2
3657	5	Brick	1	1956	941	1	2	1
3658	5	Aluminum / Vinyl	2	1950	1344	1	3	2
3659	5	Masonry / Frame	2	1956	2282	2	5	2
3660	5	Aluminum / Vinyl	1	1960	1384	1	3	2
3661	5	Brick	1	1959	1287	1	3	1
3662	5	Aluminum / Vinyl	1	1956	1206	1	3	1
3663	5	Aluminum / Vinyl	1	1957	997	1	3	1
3664	6	Aluminum / Vinyl	2	2004	1564	1	4	2
3665	6	Aluminum / Vinyl	2	1911	2196	2	4	2
3666	6	Aluminum / Vinyl	2	1905	2332	2	4	2
3667	6	Aluminum / Vinyl	1	1885	983	1	3	1
3668	7	Aluminum / Vinyl	1	1929	1223	1	3	1
3669	7	Aluminum / Vinyl	1	1923	1222	1	3	1
3670	8	Aluminum / Vinyl	2	1910	2022	2	4	2
3671	8	Aluminum / Vinyl	1	1925	1547	1	4	2
3672	8	Stucco	1	1913	1262	1	4	1
3673	9	Aluminum / Vinyl	2	1957	1940	2	6	2
3674	9	Aluminum / Vinyl	1.5	1957	1749	2	4	3

3675	9 Aluminum / Vinyl	1	2009	2041	1	3	2
3676	9 Frame	1	1961	1727	1	3	1
3677	9 Aluminum / Vinyl	1	1968	1556	1	3	1
3678	9 Aluminum / Vinyl	1	1956	1132	1	3	1
3679	9 Frame	1	1971	1120	1	4	1
3680	9 Aluminum / Vinyl	1	1971	1087	1	4	1
3681	9 Block	1	1946	948	1	2	1
3682	10 Aluminum / Vinyl	1	1926	760	1	2	1
3683	10 Brick	2	1926	2953	2	4	2
3684	10 Aluminum / Vinyl	2	1924	2462	2	4	2
3685	10 Aluminum / Vinyl	1	1925	1627	1	4	2
3686	10 Brick	1	1927	1371	1	3	1
3687	10 Aluminum / Vinyl	1	1951	1188	1	3	2
3688	10 Brick	1	1953	961	1	3	1
3689	10 Aluminum / Vinyl	1	1951	824	1	2	1
3690	10 Stucco	1	1916	1617	1	5	3
3691	10 Aluminum / Vinyl	1	1930	821	1	2	1
3692	10 Stone	1	1933	1974	1	5	2
3693	11 Brick	1	1951	1213	1	3	1
3694	11 Brick	1	1952	1188	1	3	1
3695	11 Aluminum / Vinyl	1	1958	1125	1	4	1
3696	11 Aluminum / Vinyl	1	1957	1108	1	3	1
3697	11 Frame	1	1928	1188	1	3	1
3698	11 Brick	1	1966	1437	1	3	1
3699	11 Brick	1	1963	1290	1	3	1
3700	11 Aluminum / Vinyl	1	1959	1228	1	3	1
3701	11 Brick	1	1963	1216	1	3	1
3702	11 Brick	1	1957	1152	1	3	2
3703	11 Aluminum / Vinyl	1	1962	1092	1	3	1
3704	11 Aluminum / Vinyl	1	1959	1086	1	3	1
3705	11 Brick	1	1954	1023	1	2	1
3706	11 Brick	1	1960	1014	1	3	1
3707	11 Stucco	1	1954	972	1	3	1
3708	11 Brick	1	1955	934	1	3	1
3709	11 Aluminum / Vinyl	1	1953	879	1	3	1
3710	11 Brick	1	1939	858	1	2	1
3711	11 Aluminum / Vinyl	1	1953	672	1	2	1
3712	12 Aluminum / Vinyl	1	1923	1172	1	2	1
3713	13 Brick	1	1953	1080	1	2	1
3714	13 Masonry / Frame	2	1973	2216	1	4	2
3715	13 Masonry / Frame	2	1974	1957	1	3	1
3716	13 Aluminum / Vinyl	1.5	1895	1630	2	4	2
3717	13 Brick	1	1955	1155	1	3	2

3718	13	Brick	1	1959	1133	1	3	1
3719	14	Aluminum / Vinyl	1	1940	1307	1	4	1
3720	14	Aluminum / Vinyl	1	1953	1034	1	3	1
3721	14	Aluminum / Vinyl	1	1895	960	1	3	1
3722	14	Brick	1.5	1925	2343	2	5	3
3723	14	Aluminum / Vinyl	2	1973	2138	2	6	2
3724	14	Frame	2	1956	1529	2	4	2
3725	14	Frame	2	1904	2545	2	6	2
3726	14	Brick	2	1871	2502	2	6	2
3727	14	Frame	2	1910	2288	2	4	2
3728	14	Aluminum / Vinyl	2	1910	2274	2	5	2
3729	14	Frame	1.5	1914	1874	2	4	2
3730	14	Aluminum / Vinyl	1	1926	1317	1	3	1
3731	14	Aluminum / Vinyl	1	1922	990	1	3	1
3732	14	Aluminum / Vinyl	2	1907	2138	1	5	1
3733	14	Aluminum / Vinyl	1	1915	1526	1	4	1
3734	15	Aluminum / Vinyl	2	2010	1860	1	4	3
3735	15	Aluminum / Vinyl	2	1917	2945	2	6	2
3736	15	Frame	2	1893	2140	2	4	2
3737	15	Aluminum / Vinyl	2	1891	1958	2	4	2
3738	15	Frame	1	1920	1476	1	4	1
3739	15	Aluminum / Vinyl	1	1970	1101	1	3	1
3740	15	Aluminum / Vinyl	1	1895	847	1	2	1
3741	1	Aluminum / Vinyl	1	1960	964	1	3	1
3742	1	Frame	2	1926	1559	1	4	1
3743	2	Aluminum / Vinyl	1.5	1955	1402	1	4	1
3744	2	Brick	1	1953	1389	1	3	1
3745	2	Aluminum / Vinyl	1	1958	1266	1	3	2
3746	2	Aluminum / Vinyl	1	1955	1176	1	2	1
3747	2	Aluminum / Vinyl	1	1952	914	1	3	1
3748	2	Aluminum / Vinyl	1.5	1958	1535	2	3	2
3749	2	Aluminum / Vinyl	1	1963	2060	1	5	2
3750	2	Aluminum / Vinyl	1	1955	864	1	3	1
3751	3	Brick	2	1902	4277	1	6	3
3752	3	Brick	2	1915	3618	1	3	2
3753	3	Frame	2	1890	3025	1	5	2
3754	3	Stucco	2	1894	2348	1	4	1
3755	5	Brick	1	1954	1504	1	4	2
3756	5	Aluminum / Vinyl	1	1941	1434	1	4	2
3757	5	Frame	1	1957	1216	1	4	1
3758	5	Brick	1	1947	1168	1	3	1
3759	5	Masonry / Frame	2	1954	2523	1	3	2
3760	5	Masonry / Frame	2	1948	1629	1	3	1

3761	5	Masonry / Frame	2	1939	1393	1	3	1
3762	5	Brick	2	1959	2623	2	6	2
3763	5	Brick	1	1954	1686	1	2	1
3764	5	Brick	1	1963	1293	1	3	1
3765	5	Brick	1	1965	1288	1	3	2
3766	6	Aluminum / Vinyl	2	1923	2266	2	4	2
3767	6	Aluminum / Vinyl	2	1892	2948	1	5	1
3768	7	Brick	1	1939	1542	1	3	2
3769	7	Brick	2	1940	2431	1	4	2
3770	7	Masonry / Frame	2	1939	1511	1	3	1
3771	7	Masonry / Frame	2	1930	2323	2	4	2
3772	7	Frame	1.5	1929	1451	2	4	3
3773	7	Stone	1	1950	1262	1	2	1
3774	7	Brick	1	1950	1249	1	3	1
3775	8	Aluminum / Vinyl	2	1914	2304	2	6	2
3776	8	Stucco	1	1917	1695	1	4	2
3777	8	Aluminum / Vinyl	1	1906	1411	1	5	1
3778	9	Aluminum / Vinyl	2	2005	3722	1	4	3
3779	9	Aluminum / Vinyl	1	1968	1399	1	3	1
3780	9	Aluminum / Vinyl	1	1958	1089	1	3	1
3781	9	Aluminum / Vinyl	1	1971	1086	1	4	2
3782	9	Brick	1	1957	1044	1	3	1
3783	9	Aluminum / Vinyl	1	1976	906	1	3	1
3784	9	Aluminum / Vinyl	2	1920	2797	1	6	2
3785	10	Aluminum / Vinyl	1	1952	1277	1	4	1
3786	10	Aluminum / Vinyl	1	1937	883	1	3	1
3787	10	Aluminum / Vinyl	1.5	1928	2067	2	4	2
3788	10	Brick	2	1936	2316	2	4	2
3789	10	Aluminum / Vinyl	2	1930	1232	2	2	2
3790	10	Aluminum / Vinyl	2	1913	2792	2	5	2
3791	10	Stucco	2	1920	1276	2	3	2
3792	10	Brick	1	1927	1816	1	4	2
3793	10	Aluminum / Vinyl	1	1919	1728	1	4	2
3794	10	Frame	1	1928	1239	1	3	2
3795	10	Aluminum / Vinyl	1.5	1914	1913	1	3	1
3796	10	Frame	1	1907	1412	1	3	2
3797	11	Brick	2	1947	1349	1	3	1
3798	11	Brick	1	1964	1411	1	3	2
3799	11	Aluminum / Vinyl	1	1956	1108	1	3	1
3800	12	Aluminum / Vinyl	2	1907	1948	2	6	2
3801	12	Brick	2	1900	1786	1	3	1
3802	13	Aluminum / Vinyl	1.5	1946	1544	1	3	1
3803	13	Brick	1	1950	1517	1	4	1

3804	13	Brick	1	1953	1203	1	3	1
3805	13	Brick	1	1949	1081	1	3	1
3806	13	Aluminum / Vinyl	2	1948	1056	1	2	2
3807	13	Aluminum / Vinyl	1.5	1928	1920	2	4	2
3808	13	Aluminum / Vinyl	1.5	1928	1461	2	4	2
3809	13	Brick	1	1969	1590	1	3	1
3810	13	Aluminum / Vinyl	1	1959	1085	1	3	2
3811	13	Aluminum / Vinyl	1	1960	1047	1	3	1
3812	13	Aluminum / Vinyl	1	1947	732	1	2	1
3813	13	Aluminum / Vinyl	1	1908	1264	1	3	2
3814	13	Frame	1	1930	779	1	1	1
3815	14	Stone	1	1937	951	1	2	1
3816	14	Stone	2	1941	1944	1	3	1
3817	14	Aluminum / Vinyl	2	1942	1929	1	3	1
3818	14	Aluminum / Vinyl	1.5	1913	2034	2	5	2
3819	14	Brick	1	1930	2004	1	3	2
3820	14	Aluminum / Vinyl	1	1952	672	1	2	1
3821	14	Aluminum / Vinyl	1	1900	1242	1	3	1
3822	14	Stone	1.5	1936	1358	1	3	2
3823	15	Aluminum / Vinyl	2	2002	1184	1	3	1
3824	15	Aluminum / Vinyl	2	1911	2034	2	5	2
3825	15	Aluminum / Vinyl	1	1969	1098	1	3	1
3826	15	Brick	2	1921	2300	1	3	1
3827	1	Frame	1.5	1951	1576	1	3	2
3828	1	Aluminum / Vinyl	1.5	1925	1539	2	3	2
3829	1	Masonry / Frame	2	1927	2186	2	4	2
3830	1	Brick	1	1930	1289	1	3	1
3831	1	Aluminum / Vinyl	1	1957	894	1	3	1
3832	1	Aluminum / Vinyl	1	1950	768	1	2	1
3833	1	Frame	1	1929	1273	1	3	1
3834	1	Frame	1	1929	1273	1	3	1
3835	1	Brick	1.5	1931	1784	1	3	2
3836	1	Stone	1.5	1938	1586	1	3	1
3837	2	Brick	1	1950	1978	1	5	2
3838	2	Frame	1	1961	1268	1	4	1
3839	2	Frame	1	1961	1147	1	4	1
3840	2	Aluminum / Vinyl	1	1957	1130	1	3	1
3841	2	Brick	1	1959	1322	1	3	1
3842	2	Aluminum / Vinyl	1	1956	1120	1	3	1
3843	2	Brick	1	1957	1083	1	3	1
3844	2	Frame	1	1955	912	1	3	1
3845	3	Stucco	1.5	1914	2708	1	5	3
3846	3	Masonry / Frame	2	1909	2633	1	6	2

3847	3	Aluminum / Vinyl	1.5	1902	1627	1	4	2
3848	3	Frame	1	1924	898	1	2	1
3849	5	Brick	1	1949	1466	1	3	3
3850	5	Brick	1	1947	1251	1	3	1
3851	5	Aluminum / Vinyl	1	1950	1242	1	3	1
3852	5	Aluminum / Vinyl	1	1952	1231	1	4	1
3853	5	Stone	1	1947	1134	1	2	1
3854	5	Frame	1	1953	1108	1	4	1
3855	5	Fiber-Cement	2	2005	3583	1	5	4
3856	5	Masonry / Frame	2	1956	2189	2	5	2
3857	5	Brick	1	1953	1220	1	3	1
3858	5	Frame	1	1957	1060	1	3	1
3859	5	Aluminum / Vinyl	1	1959	988	1	3	2
3860	5	Frame	1	1958	919	1	3	1
3861	6	Aluminum / Vinyl	1.5	1890	1817	2	4	2
3862	7	Brick	1.5	1950	1604	1	3	1
3863	7	Aluminum / Vinyl	2	1940	1128	1	3	1
3864	7	Aluminum / Vinyl	1	1890	552	1	2	1
3865	7	Frame	2	1922	2608	2	6	2
3866	7	Aluminum / Vinyl	1.5	1920	1720	2	4	2
3867	7	Aluminum / Vinyl	1	1930	1680	1	4	2
3868	7	Aluminum / Vinyl	1	1928	1502	1	4	1
3869	8	Aluminum / Vinyl	1	1923	1141	1	3	1
3870	8	Aluminum / Vinyl	2	1898	1496	1	4	1
3872	9	Brick	1	1960	1527	1	3	1
3873	9	Brick	1	1957	1356	1	3	1
3874	9	Aluminum / Vinyl	1	1956	1232	1	3	2
3875	9	Brick	1	1957	1176	1	3	1
3876	9	Brick	1	1958	1124	1	3	1
3877	9	Frame	1	1957	1073	1	3	2
3878	9	Aluminum / Vinyl	1	1963	987	1	3	1
3879	10	Stone	1.5	1950	2125	1	5	2
3880	10	Masonry / Frame	2	1953	1657	1	3	1
3881	10	Aluminum / Vinyl	2	1927	2094	2	4	2
3882	10	Stone	1	1938	1112	1	2	1
3883	10	Aluminum / Vinyl	1	1953	1025	1	2	1
3884	10	Stucco	1	1915	1598	1	4	1
3885	10	Masonry / Frame	2	1928	1439	1	3	1
3886	10	Aluminum / Vinyl	1.5	1920	1186	1	3	1
3887	11	Aluminum / Vinyl	1	1949	1211	1	3	1
3888	11	Aluminum / Vinyl	1	1955	1155	1	4	1
3889	11	Aluminum / Vinyl	1	1954	1124	1	4	2
3890	11	Frame	1	1953	958	1	3	1

3891	11	Block	2	1945	1252	1	3	1
3892	11	Aluminum / Vinyl	1	1925	1883	1	5	2
3893	11	Masonry / Frame	1	1957	1914	1	2	2
3894	11	Brick	1	1957	1160	1	3	1
3895	11	Aluminum / Vinyl	1	1958	1138	1	3	1
3896	11	Brick	1	1953	1058	1	3	1
3897	11	Brick	1	1955	1019	1	3	2
3898	11	Aluminum / Vinyl	1	1960	981	1	3	1
3899	11	Aluminum / Vinyl	1	1953	890	1	3	1
3900	11	Frame	2	1920	1531	1	3	1
3901	12	Aluminum / Vinyl	1.5	1902	1693	1	4	2
3902	12	Aluminum / Vinyl	1	1885	1320	1	2	1
3903	13	Brick	1.5	1954	1812	1	4	2
3904	13	Aluminum / Vinyl	1.5	1939	1334	1	3	1
3905	13	Brick	1	1952	1070	1	3	1
3906	13	Brick	2	1939	1443	1	3	1
3907	13	Aluminum / Vinyl	1	1926	947	1	2	1
3908	13	Aluminum / Vinyl	1	1968	1392	1	3	1
3909	13	Brick	1	1967	1364	1	3	1
3910	13	Aluminum / Vinyl	1	1950	756	1	2	1
3911	14	Aluminum / Vinyl	2	1948	1378	1	3	1
3912	14	Aluminum / Vinyl	2	1941	1090	1	2	1
3913	14	Aluminum / Vinyl	2	1913	1696	2	4	2
3914	14	Aluminum / Vinyl	1	1925	1529	1	3	1
3915	14	Aluminum / Vinyl	1	1928	1504	1	3	2
3916	14	Aluminum / Vinyl	1	1924	1390	1	4	1
3917	14	Aluminum / Vinyl	1	1926	1237	1	3	2
3918	14	Aluminum / Vinyl	1	1900	945	1	2	1
3919	14	Aluminum / Vinyl	1	1956	1078	1	3	1
3920	14	Aluminum / Vinyl	1.5	1910	1669	1	3	1
3921	14	Aluminum / Vinyl	2	1913	1512	1	3	1
3922	14	Stone	1.5	1936	1684	1	3	2
3923	15	Stucco	1	1920	1855	1	4	2
3924	15	Brick	1.5	1927	2441	1	3	1
3925	15	Aluminum / Vinyl	1	1900	1386	1	3	1
3926	1	Brick	1	1944	1318	1	4	2
3927	1	Frame	2	1941	1843	1	3	1
3928	1	Frame	2	1949	1818	2	4	2
3929	1	Brick	1	1926	2152	1	5	2
3930	2	Aluminum / Vinyl	1.5	1963	1909	2	5	2
3931	2	Stone	1	1955	1131	1	3	1
3932	2	Aluminum / Vinyl	1	1959	942	1	3	1
3933	3	Frame	1	1925	1052	1	3	1

3934	3	Stucco	2	1909	3518	1	6	3
3935	5	Brick	1	1947	2014	1	5	2
3936	5	Brick	1	1947	1503	1	3	1
3937	5	Brick	1	1953	1322	1	4	2
3938	5	Aluminum / Vinyl	1	1950	1171	1	4	1
3939	5	Aluminum / Vinyl	1	1950	1156	1	3	2
3940	5	Aluminum / Vinyl	1	1952	1092	1	4	1
3941	5	Aluminum / Vinyl	1	1952	1074	1	3	1
3942	5	Aluminum / Vinyl	1	1952	1039	1	3	1
3943	5	Aluminum / Vinyl	1	1950	1022	1	3	1
3944	5	Aluminum / Vinyl	1	1952	1016	1	3	1
3945	5	Aluminum / Vinyl	1	1950	948	1	3	1
3946	5	Brick	2	1957	2584	2	6	2
3947	5	Aluminum / Vinyl	1	1962	1420	1	3	1
3948	5	Frame	1	1955	1064	1	3	1
3949	5	Aluminum / Vinyl	1	1950	912	1	3	1
3950	5	Aluminum / Vinyl	1	1957	1487	1	3	2
3951	6	Brick	2	1922	2714	2	6	2
3952	6	Aluminum / Vinyl	1.5	1915	1809	2	4	2
3953	6	Aluminum / Vinyl	1	1927	955	1	2	1
3954	7	Aluminum / Vinyl	1	1950	1200	1	3	1
3955	7	Aluminum / Vinyl	1.5	1941	1824	2	3	2
3956	8	Frame	2	1923	2425	2	4	2
3957	8	Aluminum / Vinyl	1.5	1922	1702	2	3	2
3958	8	Aluminum / Vinyl	1.5	1910	1722	2	3	2
3959	8	Aluminum / Vinyl	1	1925	952	1	3	1
3960	8	Aluminum / Vinyl	1	1900	1320	1	4	2
3961	9	Aluminum / Vinyl	1	1977	1219	1	3	1
3962	10	Brick	1	1945	1098	1	3	2
3963	10	Aluminum / Vinyl	2	1926	2256	2	4	2
3964	10	Brick	1.5	1927	1949	1	4	1
3965	10	Brick	1	1927	1856	1	4	2
3966	10	Aluminum / Vinyl	1	1926	1617	1	5	1
3967	10	Stucco	1	1915	1565	1	3	2
3968	10	Brick	1	1927	1272	1	2	1
3969	11	Stone	1	1947	1356	1	3	2
3970	11	Aluminum / Vinyl	1	1952	1347	1	4	1
3971	11	Stone	1	1954	1310	1	3	1
3972	11	Aluminum / Vinyl	1	1953	1106	1	3	1
3973	11	Aluminum / Vinyl	2	1955	1521	1	5	2
3974	11	Brick	2	1944	1564	2	4	2
3975	11	Frame	1	1956	1363	1	3	1
3976	11	Brick	1	1960	1286	1	3	1

3977	11	Brick	1	1952	1269	1	3	1
3978	11	Prem Wood	1	1958	1252	1	3	1
3979	11	Brick	1	1960	1138	1	3	1
3980	11	Brick	1	1954	1104	1	3	1
3981	12	Aluminum / Vinyl	1	1870	452	1	1	1
3982	13	Stucco	1	1930	1487	1	3	2
3983	13	Brick	2	1964	2736	3	5	3
3984	14	Aluminum / Vinyl	1	1953	1166	1	4	1
3985	14	Brick	1.5	1926	2250	2	5	2
3986	14	Aluminum / Vinyl	1.5	1926	1929	2	4	2
3987	14	Aluminum / Vinyl	2	1891	2424	2	6	2
3988	14	Aluminum / Vinyl	2	1921	2406	2	5	2
3989	14	Aluminum / Vinyl	2	1900	1620	2	4	2
3990	14	Frame	2	1897	1916	1	3	2
3991	15	Aluminum / Vinyl	2	1922	2801	2	4	2
3992	15	Aluminum / Vinyl	1.5	1924	1826	2	5	2
3993	1	Stone	1	1951	1198	1	3	1
3994	1	Aluminum / Vinyl	1	1925	1016	1	3	1
3995	2	Frame	1.5	1951	1673	1	4	2
3996	2	Aluminum / Vinyl	1	1956	853	1	2	1
3997	2	Masonry / Frame	2	1958	2276	2	5	2
3998	2	Masonry / Frame	1.5	1958	1900	2	5	2
3999	3	Brick	1	1953	1028	1	2	2
4000	3	Frame	2	1901	2496	1	5	2
4001	5	Brick	1	1953	1598	1	3	2
4002	5	Brick	1	1956	1517	1	4	1
4003	5	Stone	1	1947	1479	1	3	1
4004	5	Frame	1	1948	1118	1	4	1
4005	5	Brick	1	1955	1256	1	3	1
4006	5	Brick	1	1956	1207	1	3	1
4007	5	Brick	1	1963	1043	1	3	2
4008	5	Brick	1	1955	1025	1	3	1
4009	5	Brick	1	1950	1009	1	3	1
4010	5	Aluminum / Vinyl	2	1976	2451	2	6	2
4011	5	Aluminum / Vinyl	2	1978	2451	2	6	2
4012	7	Aluminum / Vinyl	1.5	1941	1483	1	4	1
4013	7	Brick	1	1926	1651	1	4	2
4014	8	Aluminum / Vinyl	2	1914	1722	1	3	1
4015	8	Aluminum / Vinyl	1	1922	1582	1	4	2
4016	9	Aluminum / Vinyl	1	1953	990	1	4	1
4017	9	Aluminum / Vinyl	2	2010	2571	1	4	2
4018	10	Aluminum / Vinyl	1.5	1923	1260	1	3	2
4019	10	Brick	1.5	1928	1995	2	3	2

4020	10	Aluminum / Vinyl	1.5	1923	1468	2	5	2
4021	11	Aluminum / Vinyl	1	1951	1266	1	3	1
4022	11	Brick	1	1947	1230	1	4	1
4023	11	Aluminum / Vinyl	1	1940	896	1	3	2
4024	11	Brick	1	1959	1335	1	3	1
4025	11	Brick	1	1962	1297	1	3	1
4026	11	Aluminum / Vinyl	1	1960	1222	1	3	1
4027	11	Aluminum / Vinyl	1	1954	1000	1	3	1
4028	11	Brick	1	1959	983	1	3	2
4029	11	Aluminum / Vinyl	1	1960	931	1	3	1
4030	12	Aluminum / Vinyl	1	1903	942	1	3	1
4031	13	Block	1.5	1940	913	1	2	2
4032	13	Aluminum / Vinyl	1	1927	1482	1	4	2
4033	13	Brick	1	1960	1218	1	3	1
4034	13	Brick	1	1959	988	1	3	2
4035	14	Aluminum / Vinyl	1	1947	1035	1	3	1
4036	14	Fiber-Cement	2	2006	2040	1	3	2
4037	14	Aluminum / Vinyl	2	1937	1144	1	2	1
4038	14	Aluminum / Vinyl	2	1945	990	1	2	1
4039	14	Aluminum / Vinyl	2	1916	2882	2	6	2
4040	14	Aluminum / Vinyl	1	1927	1689	1	4	2
4041	14	Aluminum / Vinyl	1	1928	992	1	3	1
4042	15	Aluminum / Vinyl	1	1920	1681	1	4	2
4043	15	Brick	1.5	1927	2539	1	5	2
4044	1	Frame	1	1928	1624	1	4	1
4045	1	Stone	1	1955	1482	1	2	1
4046	1	Brick	1	1958	1469	1	4	1
4047	1	Aluminum / Vinyl	1	1960	988	1	3	1
4048	1	Aluminum / Vinyl	1	1924	1170	1	3	1
4049	2	Brick	2	1957	2452	2	7	2
4050	2	Aluminum / Vinyl	2	1973	2340	2	6	2
4051	2	Aluminum / Vinyl	2	1973	2340	2	6	2
4052	2	Aluminum / Vinyl	2	1973	2340	2	6	2
4053	2	Frame	2	1954	1536	2	4	2
4054	2	Stone	1	1952	1424	1	2	1
4055	2	Aluminum / Vinyl	1	1954	972	1	2	1
4056	2	Aluminum / Vinyl	1	1955	1414	1	3	1
4057	3	Aluminum / Vinyl	2	1899	3304	1	5	3
4058	3	Aluminum / Vinyl	1	1887	1050	1	3	1
4059	3	Aluminum / Vinyl	2	1900	1520	2	4	2
4060	3	Stucco	2	1913	1545	1	3	1
4061	3	Aluminum / Vinyl	1	1893	1147	1	3	1
4062	5	Aluminum / Vinyl	1	1942	1546	1	4	1

4063	5	Brick	1	1950	1355	1	3	1
4064	5	Aluminum / Vinyl	1	1952	1296	1	3	1
4065	5	Aluminum / Vinyl	1	1949	1119	1	3	2
4066	5	Aluminum / Vinyl	1	1946	1068	1	3	1
4067	5	Masonry / Frame	2	2010	1441	1	3	2
4068	5	Aluminum / Vinyl	2	1953	1422	1	3	1
4069	5	Masonry / Frame	2	1946	1174	1	3	1
4070	5	Aluminum / Vinyl	1	1957	1252	1	3	1
4071	5	Brick	1	1957	1238	1	3	2
4072	5	Brick	1	1956	979	1	2	1
4073	5	Aluminum / Vinyl	1	1928	852	1	3	1
4074	6	Aluminum / Vinyl	2	1927	1321	1	3	1
4075	6	Aluminum / Vinyl	1.5	1891	1827	2	4	2
4076	6	Aluminum / Vinyl	1	1903	1378	1	4	1
4077	6	Stucco	1	1924	1028	1	3	1
4078	7	Aluminum / Vinyl	1.5	1940	1438	1	5	2
4079	7	Brick	2	1927	2902	2	6	2
4080	7	Masonry / Frame	2	1930	2626	2	4	2
4081	7	Frame	2	1961	1879	2	4	2
4082	7	Brick	2	1945	2119	2	4	2
4083	8	Aluminum / Vinyl	1.5	1920	1933	2	4	2
4084	8	Aluminum / Vinyl	1	1924	1598	1	4	1
4085	8	Aluminum / Vinyl	1	1903	1015	1	4	1
4086	9	Aluminum / Vinyl	2	2010	1852	1	3	2
4087	9	Aluminum / Vinyl	2	1968	1636	1	4	1
4088	9	Aluminum / Vinyl	1.5	1936	1574	2	2	2
4089	9	Aluminum / Vinyl	1	2001	1940	1	3	2
4090	9	Frame	1	1957	1009	1	3	1
4091	10	Aluminum / Vinyl	1.5	1948	1238	1	3	2
4092	10	Aluminum / Vinyl	2	1925	1615	1	3	1
4093	10	Aluminum / Vinyl	2	1922	2928	2	6	2
4094	10	Aluminum / Vinyl	2	1927	2247	2	4	2
4095	10	Stucco	2	1952	1670	2	4	2
4096	10	Aluminum / Vinyl	2	1928	2120	2	4	2
4097	10	Aluminum / Vinyl	1	1925	1302	1	4	2
4098	10	Aluminum / Vinyl	1	1929	1252	1	2	1
4099	10	Aluminum / Vinyl	1	1926	961	1	3	1
4100	11	Brick	1	1949	1420	1	3	1
4101	11	Aluminum / Vinyl	1.5	1953	1205	1	3	1
4102	11	Aluminum / Vinyl	1	1959	1124	1	3	2
4103	11	Aluminum / Vinyl	1	1942	868	1	3	1
4104	11	Brick	1.5	1962	2201	2	5	2
4105	11	Brick	1	1963	1216	1	3	1

4106	11	Stone	1	1946	1105	1	2	1
4107	11	Brick	1	1955	1013	1	3	1
4108	11	Brick	1	1954	976	1	3	1
4109	11	Frame	1	1961	935	1	3	1
4110	11	Aluminum / Vinyl	1	1950	802	1	3	1
4111	11	Aluminum / Vinyl	2	1975	2478	2	6	2
4112	12	Aluminum / Vinyl	1	1900	1425	1	4	2
4113	12	Frame	1	1909	1098	1	3	1
4115	13	Brick	1	1946	1133	1	2	1
4116	13	Aluminum / Vinyl	2	1973	2515	1	3	2
4117	13	Aluminum / Vinyl	2	1930	1353	1	3	1
4118	13	Aluminum / Vinyl	2	1969	1228	1	3	1
4119	13	Frame	1	1962	1000	1	3	2
4120	13	Aluminum / Vinyl	1	1959	919	1	3	2
4121	13	Masonry / Frame	2	1972	2390	2	6	2
4122	13	Brick	1.5	1932	1846	1	3	1
4123	13	Brick	2	1932	1594	1	3	1
4124	14	Stone	1	1940	1262	1	2	2
4125	14	Aluminum / Vinyl	2	2010	1354	1	3	2
4126	14	Brick	1.5	1925	2112	2	3	2
4127	14	Aluminum / Vinyl	2	1898	1848	2	5	2
4128	14	Frame	1.5	1916	1758	1	3	2
4129	14	Aluminum / Vinyl	1	1930	1542	1	4	1
4130	14	Aluminum / Vinyl	1	1945	979	1	3	1
4131	14	Aluminum / Vinyl	1	1906	1641	1	3	2
4132	14	Aluminum / Vinyl	1.5	1916	1632	1	3	2
4133	14	Aluminum / Vinyl	1	1920	1095	1	2	1
4134	14	Aluminum / Vinyl	2	1910	1080	1	2	1
4135	14	Aluminum / Vinyl	1	1924	1017	1	3	1
4136	15	Brick	2	1921	2180	1	4	1
4137	15	Frame	2	1895	1642	2	4	2
4138	1	Masonry / Frame	2	1950	1775	2	4	2
4139	1	Aluminum / Vinyl	1	1960	1095	1	3	1
4140	2	Stucco	1.5	1941	1484	1	4	1
4141	2	Aluminum / Vinyl	1	1955	1084	1	4	1
4142	2	Brick	1	1958	1372	1	3	1
4143	2	Aluminum / Vinyl	1	1955	1080	1	3	2
4144	2	Aluminum / Vinyl	1	1958	1040	1	3	1
4145	2	Aluminum / Vinyl	1	1955	864	1	3	1
4146	3	Brick	2	1921	3764	1	3	2
4147	3	Brick	2	1919	3263	1	5	3
4148	3	Brick	1.5	1928	1497	1	3	2
4149	3	Aluminum / Vinyl	2	1924	1307	1	3	1

4150	3 Aluminum / Vinyl	1	1889	1205	1	3	1
4151	5 Frame	1	1952	1664	1	4	1
4152	5 Aluminum / Vinyl	1	1952	1549	1	3	2
4153	5 Aluminum / Vinyl	1	1952	1394	1	3	1
4154	5 Aluminum / Vinyl	1	1955	1110	1	4	1
4155	5 Brick	1	1946	1089	1	3	1
4156	5 Aluminum / Vinyl	1	1951	1076	1	3	2
4157	5 Aluminum / Vinyl	1	1953	1026	1	4	1
4158	5 Aluminum / Vinyl	2	1940	1240	1	3	1
4159	5 Brick	1	1979	1469	1	3	2
4160	5 Brick	1	1957	1198	1	3	1
4161	5 Brick	1	1956	1156	1	3	1
4162	5 Frame	1	1956	1064	1	3	2
4163	5 Aluminum / Vinyl	1	1956	999	1	3	1
4164	5 Aluminum / Vinyl	1	1952	802	1	2	1
4165	6 Frame	2	1892	2260	2	6	2
4166	6 Aluminum / Vinyl	2	1911	2044	2	6	2
4167	7 Brick	1	1948	1047	1	3	1
4168	7 Aluminum / Vinyl	1	1922	2074	1	5	1
4169	7 Brick	1	1925	1891	1	4	2
4170	8 Aluminum / Vinyl	1	1949	1135	1	3	1
4171	8 Aluminum / Vinyl	1	1895	1390	1	3	2
4172	8 Frame	1	1893	1336	1	3	2
4173	8 Aluminum / Vinyl	1	1903	910	1	3	1
4174	9 Brick	1	1942	1207	1	3	2
4175	9 Aluminum / Vinyl	1	1964	1232	1	3	1
4176	10 Aluminum / Vinyl	2	1945	1607	1	4	2
4177	10 Brick	1	1949	1512	1	3	2
4178	10 Block	1	1946	1075	1	3	1
4179	10 Aluminum / Vinyl	1	1948	1070	1	3	1
4180	10 Brick	1	1947	899	1	3	1
4181	10 Aluminum / Vinyl	1.5	1927	1452	2	4	2
4182	10 Brick	1.5	1940	1502	2	3	2
4183	10 Stucco	1	1918	1722	1	5	1
4184	10 Aluminum / Vinyl	1	1954	1100	1	2	1
4185	10 Aluminum / Vinyl	1	1954	982	1	3	1
4186	10 Brick	1.5	1924	1997	1	3	1
4187	10 Aluminum / Vinyl	1.5	1900	1685	1	5	1
4188	11 Brick	1	1960	1321	1	4	2
4189	11 Frame	1.5	1939	1186	1	2	1
4190	11 Aluminum / Vinyl	1	1953	2385	2	5	2
4191	11 Aluminum / Vinyl	1.5	1959	2314	2	6	2
4192	11 Aluminum / Vinyl	2	1954	1728	2	6	2

4193	11	Brick	1	1967	1414	1	3	1
4194	11	Brick	1	1963	1376	1	3	1
4195	11	Brick	1	1956	1189	1	3	1
4196	11	Aluminum / Vinyl	1	1964	1114	1	3	1
4197	11	Aluminum / Vinyl	1	1956	1095	1	3	1
4198	11	Aluminum / Vinyl	1	1957	1063	1	3	1
4199	11	Brick	1	1955	1062	1	2	1
4200	11	Brick	1	1953	1019	1	3	1
4201	11	Aluminum / Vinyl	1	1956	995	1	3	1
4202	11	Brick	1	1954	988	1	3	1
4203	11	Aluminum / Vinyl	1	1954	955	1	3	1
4204	11	Frame	1	1960	932	1	3	1
4205	11	Brick	1	1950	871	1	2	1
4206	12	Aluminum / Vinyl	1	1903	1404	1	3	1
4207	13	Aluminum / Vinyl	1	1947	1348	1	4	2
4208	13	Aluminum / Vinyl	1	1950	1257	1	3	2
4209	13	Aluminum / Vinyl	1	1947	1149	1	3	1
4210	13	Aluminum / Vinyl	2	1951	1564	1	5	2
4211	13	Aluminum / Vinyl	1.5	1927	2199	1	3	2
4212	13	Brick	1	1967	1808	1	3	2
4213	13	Brick	1	1973	1720	1	3	1
4214	13	Brick	1	1969	1490	1	3	1
4215	13	Aluminum / Vinyl	1	1978	1354	1	3	1
4216	13	Aluminum / Vinyl	1	1962	896	1	3	1
4217	13	Aluminum / Vinyl	1	1944	746	1	2	1
4218	13	Aluminum / Vinyl	1	1954	720	1	2	1
4219	14	Aluminum / Vinyl	1	1953	1164	1	3	1
4220	14	Brick	1	1948	992	1	3	1
4221	14	Aluminum / Vinyl	1	1949	910	1	3	1
4222	14	Aluminum / Vinyl	1	1899	814	1	2	1
4223	14	Brick	2	1929	2159	2	4	2
4224	14	Frame	1.5	1920	1614	2	4	2
4225	14	Frame	2	1911	2083	2	3	2
4226	14	Aluminum / Vinyl	1	1927	1669	1	3	2
4227	14	Frame	1	1925	1339	1	3	1
4228	14	Aluminum / Vinyl	1	1926	1160	1	3	1
4229	14	Aluminum / Vinyl	1	1953	922	1	3	1
4230	14	Aluminum / Vinyl	2	1919	1888	1	3	2
4231	14	Block	1.5	1920	1308	1	2	1
4232	14	Aluminum / Vinyl	1	1918	1252	1	3	1
4233	14	Prem Wood	1	1923	1224	1	3	2
4234	14	Frame	1	1921	1030	1	3	1
4235	15	Aluminum / Vinyl	2	2008	1914	1	4	2

4236	15	Aluminum / Vinyl	2	1921	3084	2	6	2
4237	1	Brick	1	1952	1288	1	4	1
4238	1	Aluminum / Vinyl	1	1929	1076	1	2	1
4239	1	Aluminum / Vinyl	1.5	1952	1831	2	4	2
4240	1	Frame	1	1959	1132	1	3	1
4241	1	Aluminum / Vinyl	1	1956	1130	1	3	2
4242	1	Stone	1	1946	967	1	2	1
4243	1	Aluminum / Vinyl	1	1950	672	1	2	1
4244	1	Aluminum / Vinyl	1.5	1925	1324	1	2	1
4245	1	Aluminum / Vinyl	1	1932	1076	1	4	1
4246	2	Aluminum / Vinyl	1	1995	1458	1	3	2
4247	2	Aluminum / Vinyl	1	1953	1300	1	3	2
4248	2	Brick	1.5	1953	1965	2	4	2
4249	2	Frame	1	1950	1332	1	3	1
4250	2	Aluminum / Vinyl	1	1963	1163	1	3	1
4251	2	Brick	1	1955	1131	1	3	1
4252	2	Aluminum / Vinyl	1	1958	1108	1	3	2
4253	2	Aluminum / Vinyl	1	1963	1017	1	3	1
4254	2	Aluminum / Vinyl	1	1955	864	1	3	1
4255	3	Aluminum / Vinyl	2	1890	1632	1	2	2
4256	3	Frame	1	1891	1152	1	3	2
4257	3	Aluminum / Vinyl	1	1885	680	1	2	1
4258	3	Brick	1.5	1929	2211	2	4	2
4259	3	Aluminum / Vinyl	2	1912	2291	2	4	2
4260	3	Frame	2	1907	2132	2	4	2
4261	3	Stucco	1	1916	2280	1	5	2
4262	3	Brick	2	1913	4332	1	6	3
4263	3	Aluminum / Vinyl	2	1904	1986	1	4	1
4264	3	Frame	2	1889	1667	1	3	1
4266	5	Frame	1	1984	1843	1	3	2
4267	5	Brick	1	1950	1449	1	3	2
4268	5	Brick	1	1945	1172	1	3	2
4269	5	Aluminum / Vinyl	1	1952	1120	1	3	1
4270	5	Aluminum / Vinyl	1	1949	1036	1	3	1
4271	5	Aluminum / Vinyl	1	1953	935	1	3	1
4272	5	Masonry / Frame	2	1955	2310	1	4	1
4273	5	Frame	1	1952	1320	1	3	1
4274	5	Brick	1	1950	1206	1	3	2
4275	5	Brick	1	1953	1200	1	3	1
4276	5	Brick	1	1952	1176	1	3	1
4277	5	Brick	1	1953	1125	1	2	1
4278	5	Aluminum / Vinyl	1	1957	1123	1	3	1
4279	5	Aluminum / Vinyl	1	1955	1067	1	3	1

4280	5	Brick	1	1954	1036	1	3	1
4281	6	Aluminum / Vinyl	1.5	1916	1985	1	4	2
4282	6	Frame	1.5	1898	1711	1	0	1
4283	6	Aluminum / Vinyl	1	1900	1152	1	3	1
4284	7	Aluminum / Vinyl	2	1923	2207	2	4	2
4285	7	Aluminum / Vinyl	2	1915	2161	2	4	2
4286	7	Aluminum / Vinyl	1	1893	1150	1	4	1
4287	7	Stone	1	1933	1971	1	4	2
4288	8	Aluminum / Vinyl	1	1922	1326	1	4	1
4289	8	Aluminum / Vinyl	1	1900	1278	1	3	1
4290	8	Aluminum / Vinyl	1	1895	944	1	2	1
4291	9	Frame	1	1940	1173	1	4	1
4292	10	Stone	1	1948	1785	1	4	1
4293	10	Aluminum / Vinyl	1.5	1948	1418	1	4	2
4294	10	Stone	1	1946	1149	1	3	1
4295	10	Stucco	1	1952	1095	1	4	2
4296	10	Aluminum / Vinyl	1	1952	992	1	3	1
4297	10	Aluminum / Vinyl	1	1953	984	1	3	1
4298	10	Brick	2	1924	4137	1	5	3
4299	10	Stucco	2	1915	2883	2	4	2
4300	10	Aluminum / Vinyl	1	1927	1512	1	4	2
4301	10	Aluminum / Vinyl	1	1925	1506	1	2	2
4302	10	Aluminum / Vinyl	1	1953	1068	1	3	1
4303	10	Aluminum / Vinyl	1	1954	1008	1	3	1
4304	10	Aluminum / Vinyl	1	1951	768	1	2	1
4305	10	Aluminum / Vinyl	1	1953	720	1	2	1
4306	10	Stone	1.5	1940	1890	1	3	2
4307	10	Stone	1	1936	1819	1	3	2
4308	11	Aluminum / Vinyl	1	1946	795	1	2	1
4309	11	Aluminum / Vinyl	1.5	1925	2174	2	4	3
4310	11	Brick	2	1958	2528	2	6	2
4311	11	Masonry / Frame	2	1971	2496	2	5	2
4312	11	Aluminum / Vinyl	1.5	1890	2058	2	5	3
4313	11	Brick	1	1929	1865	1	3	1
4314	11	Aluminum / Vinyl	1	1928	1000	1	3	1
4315	11	Brick	1	1955	1600	1	4	1
4316	11	Brick	1	1958	1399	1	3	2
4317	11	Brick	1	1959	1230	1	3	1
4318	11	Aluminum / Vinyl	1	1967	1216	1	3	1
4319	11	Brick	1	1958	1114	1	3	1
4320	11	Aluminum / Vinyl	1	1958	1078	1	3	1
4321	11	Aluminum / Vinyl	1	1958	1072	1	3	1
4322	11	Brick	1	1956	1064	1	3	1

4323	11 Aluminum / Vinyl	1	1957	1026	1	3	1
4324	11 Aluminum / Vinyl	1	1954	989	1	3	1
4325	11 Aluminum / Vinyl	1	1955	984	1	3	1
4326	11 Brick	1	1958	910	1	2	1
4327	11 Aluminum / Vinyl	1	1953	879	1	3	1
4328	11 Aluminum / Vinyl	1	1953	879	1	3	1
4329	11 Aluminum / Vinyl	1.5	1934	1138	1	3	1
4330	12 Frame	1	1900	1088	1	2	1
4331	13 Aluminum / Vinyl	1	1940	1283	1	3	1
4332	13 Brick	1	1962	1325	1	3	1
4333	13 Brick	1	1955	1198	1	3	1
4334	13 Stone	1	1964	1100	1	2	1
4335	13 Aluminum / Vinyl	1	1960	1084	1	3	1
4336	13 Aluminum / Vinyl	1	1946	681	1	2	1
4337	13 Frame	1.5	1929	1184	1	3	1
4338	14 Aluminum / Vinyl	1	1944	1140	1	3	1
4339	14 Frame	2	1920	2096	2	4	2
4340	14 Aluminum / Vinyl	2	1892	2741	2	3	2
4341	14 Aluminum / Vinyl	2	1919	1616	2	4	2
4342	14 Aluminum / Vinyl	1.5	1942	1215	2	3	2
4343	14 Stone	1	1926	1539	1	3	1
4344	14 Aluminum / Vinyl	1.5	1927	1661	1	3	2
4345	14 Frame	1	1915	1430	1	3	1
4346	14 Aluminum / Vinyl	1.5	1926	1133	1	2	1
4347	15 Aluminum / Vinyl	2	1911	1973	2	4	2
4348	1 Brick	1.5	1937	1247	1	3	1
4349	1 Frame	1	1941	1065	1	3	1
4350	1 Brick	2	1954	2026	2	4	2
4351	1 Brick	2	1954	1810	2	6	2
4352	1 Brick	1	1926	1209	1	3	1
4353	2 Stone	1	1952	1378	1	4	1
4354	2 Stone	1	1942	1360	1	3	1
4355	2 Aluminum / Vinyl	1	1956	1124	1	3	2
4356	2 Frame	1	1962	1330	1	3	1
4357	2 Aluminum / Vinyl	1	1956	988	1	3	1
4358	2 Brick	1	1957	964	1	2	2
4359	3 Masonry / Frame	2	1926	2088	1	3	1
4360	3 Aluminum / Vinyl	1.5	1927	1737	2	4	3
4361	3 Aluminum / Vinyl	2	1880	2686	2	6	2
4362	3 Brick	2	1916	4123	1	4	3
4363	3 Brick	2	1910	5028	1	6	4
4364	3 Brick	2	1915	3618	1	3	2
4365	3 Frame	2	1904	2899	1	4	2

4366	3	Frame	2	1922	1344	1	3	1
4367	3	Aluminum / Vinyl	2	1890	3036	3	5	3
4368	5	Stone	1	1946	1902	1	3	2
4369	5	Aluminum / Vinyl	1	1951	1496	1	3	1
4370	5	Stone	1	1952	1456	1	3	2
4371	5	Aluminum / Vinyl	1.5	1949	1367	1	4	1
4372	5	Brick	1	1948	1299	1	3	2
4373	5	Brick	1	1955	1285	1	4	1
4374	5	Aluminum / Vinyl	1	1949	1190	1	4	1
4375	5	Aluminum / Vinyl	1	1937	1143	1	2	1
4376	5	Aluminum / Vinyl	1	1946	1068	1	3	1
4377	5	Aluminum / Vinyl	2	1993	2153	1	3	2
4378	5	Brick	2	1960	2524	2	6	2
4379	5	Masonry / Frame	1.5	1956	1733	2	3	2
4380	5	Aluminum / Vinyl	1.5	1910	2161	2	4	2
4381	5	Brick	1	1965	1862	1	3	1
4382	5	Masonry / Frame	1	1962	1751	1	3	2
4383	5	Brick	1	1962	1345	1	4	1
4384	5	Brick	1	1959	1300	1	3	1
4385	5	Brick	1	1961	1221	1	3	1
4386	5	Aluminum / Vinyl	1	1956	1216	1	3	1
4387	5	Aluminum / Vinyl	1	1976	1211	1	3	1
4388	5	Aluminum / Vinyl	1	1959	1211	1	3	1
4389	5	Aluminum / Vinyl	1	1971	1204	1	4	1
4390	5	Masonry / Frame	1	1956	1114	1	3	2
4391	5	Aluminum / Vinyl	1	1956	1067	1	3	1
4392	5	Aluminum / Vinyl	1	1957	958	1	3	1
4393	5	Aluminum / Vinyl	1	1952	885	1	3	1
4394	6	Frame	2	1924	2206	2	4	2
4395	6	Aluminum / Vinyl	2	1908	2314	2	6	2
4396	6	Aluminum / Vinyl	1	1908	1384	1	3	1
4397	6	Aluminum / Vinyl	1	1904	1294	1	3	1
4398	6	Aluminum / Vinyl	1	1905	1283	1	5	1
4399	7	Stone	1.5	1936	2305	1	4	2
4400	7	Brick	1	1951	1261	1	2	1
4401	7	Brick	1.5	1932	2051	1	4	1
4402	7	Aluminum / Vinyl	1	1896	1488	1	5	2
4403	7	Masonry / Frame	2	1936	1600	1	3	1
4404	8	Aluminum / Vinyl	2	1912	2516	2	5	2
4405	8	Aluminum / Vinyl	1	1922	1270	1	4	2
4406	8	Frame	1	1900	1034	1	3	1
4407	9	Masonry / Frame	2	1957	1679	1	4	1
4408	9	Aluminum / Vinyl	1	1986	1409	1	3	1

4409	9	Aluminum / Vinyl	1	1980	1209	1	3	2
4410	9	Aluminum / Vinyl	1	1971	1200	1	4	1
4411	9	Masonry / Frame	1	1957	1058	1	3	1
4412	9	Brick	1	1957	1051	1	3	1
4413	9	Aluminum / Vinyl	1	1968	1018	1	3	1
4414	9	Frame	1	1964	1006	1	3	1
4415	9	Brick	1	1956	994	1	3	1
4416	9	Brick	1	1958	1858	1	3	1
4417	9	Aluminum / Vinyl	2	1966	2451	2	6	2
4418	10	Brick	1.5	1953	1791	1	4	2
4419	10	Brick	1	1952	1657	1	3	2
4420	10	Brick	1	1952	1134	1	3	2
4421	10	Aluminum / Vinyl	1	1948	1075	1	3	1
4422	10	Aluminum / Vinyl	1	1917	686	1	2	1
4423	10	Aluminum / Vinyl	1.5	1928	2261	2	4	2
4424	10	Frame	1.5	1928	1901	2	4	2
4425	10	Aluminum / Vinyl	1.5	1888	1740	2	4	2
4426	10	Aluminum / Vinyl	1	1922	1686	1	4	2
4427	10	Aluminum / Vinyl	1	1925	1191	1	3	1
4428	10	Brick	1	1954	1125	1	3	2
4429	10	Stone	1	1938	1115	1	2	1
4430	10	Aluminum / Vinyl	1	1922	1066	1	3	1
4431	10	Aluminum / Vinyl	1	1925	1023	1	4	1
4432	10	Brick	1	1926	1884	1	4	2
4433	11	Aluminum / Vinyl	1.5	1954	1779	1	3	2
4434	11	Aluminum / Vinyl	1	1953	1498	1	4	2
4435	11	Aluminum / Vinyl	1	1941	1121	1	3	1
4436	11	Brick	1	1953	986	1	2	1
4437	11	Aluminum / Vinyl	1	1952	953	1	3	1
4438	11	Brick	1	1949	941	1	2	1
4439	11	Aluminum / Vinyl	2	1928	2778	1	5	1
4440	11	Masonry / Frame	2	1940	2174	1	3	1
4441	11	Aluminum / Vinyl	2	1957	2206	2	6	2
4442	11	Masonry / Frame	1.5	1964	2198	2	5	2
4443	11	Brick	1.5	1931	2252	1	3	1
4444	11	Aluminum / Vinyl	1	1955	1481	1	3	2
4445	11	Aluminum / Vinyl	1	1938	1245	1	3	1
4446	11	Aluminum / Vinyl	1	1957	1202	1	3	1
4447	11	Brick	1	1956	1153	1	3	2
4448	11	Brick	1	1957	1152	1	2	1
4449	11	Aluminum / Vinyl	1	1971	1136	1	4	1
4450	11	Frame	1	1964	1128	1	3	1
4451	11	Brick	1	1955	1112	1	3	1

4452	11	Aluminum / Vinyl	1	1953	1076	1	3	1
4453	11	Stone	1	1940	1054	1	2	2
4454	11	Aluminum / Vinyl	1	1957	1040	1	3	1
4455	11	Aluminum / Vinyl	1	1956	1019	1	3	1
4456	11	Frame	1	1956	995	1	3	1
4457	11	Brick	1	1955	924	1	3	1
4458	11	Aluminum / Vinyl	1	1955	876	1	3	1
4459	11	Aluminum / Vinyl	1	1953	770	1	2	2
4460	13	Stone	1	1942	1561	1	4	2
4461	13	Aluminum / Vinyl	1	1950	1253	1	3	2
4462	13	Stone	1.5	1953	2103	2	4	2
4463	13	Aluminum / Vinyl	1	1923	1239	1	3	2
4464	13	Brick	1	1964	1724	1	3	1
4465	13	Aluminum / Vinyl	1	1968	1503	1	4	1
4466	13	Brick	1	1969	1329	1	3	2
4467	13	Brick	1	1956	1150	1	3	2
4468	13	Brick	1	1955	1119	1	3	1
4469	13	Aluminum / Vinyl	1	1961	1059	1	3	1
4470	13	Aluminum / Vinyl	1	1960	956	1	3	1
4471	13	Aluminum / Vinyl	1	1959	919	1	3	1
4472	13	Aluminum / Vinyl	1	1947	771	1	2	1
4473	13	Aluminum / Vinyl	1	1944	759	1	2	1
4474	13	Aluminum / Vinyl	1	1944	730	1	2	1
4475	13	Aluminum / Vinyl	1	1944	730	1	2	1
4476	13	Aluminum / Vinyl	1	1951	696	1	2	1
4477	13	Aluminum / Vinyl	1	1929	782	1	2	1
4478	14	Aluminum / Vinyl	2	2010	1320	1	3	2
4479	14	Aluminum / Vinyl	1	1896	640	1	1	1
4480	14	Aluminum / Vinyl	1	1910	532	1	2	1
4481	14	Masonry / Frame	2	1954	2090	2	4	2
4482	14	Aluminum / Vinyl	1.5	1918	1264	1	3	1
4483	14	Brick	1	1929	1252	1	3	1
4484	14	Brick	1	1955	840	1	2	1
4485	14	Frame	1.5	1918	1560	1	3	2
4486	14	Frame	1	1900	1288	1	3	1
4487	14	Aluminum / Vinyl	1	1916	952	1	3	1
4488	14	Stone	1.5	1936	2141	1	4	1
4489	15	Aluminum / Vinyl	2	1910	2050	2	5	2
4490	1	Aluminum / Vinyl	1	1953	1120	1	4	1
4491	1	Brick	1.5	1936	1099	1	2	1
4492	1	Masonry / Frame	2	1951	1306	1	3	1
4493	1	Aluminum / Vinyl	2	1936	1144	1	3	1
4494	1	Brick	2	1957	2576	2	4	2

4495	1	Brick	1	1954	1185	1	3	1
4496	1	Aluminum / Vinyl	1	1953	1082	1	3	1
4497	2	Aluminum / Vinyl	1	1955	1119	1	3	1
4498	2	Aluminum / Vinyl	1	1952	1019	1	4	2
4499	2	Aluminum / Vinyl	1	1936	945	1	2	1
4500	2	Aluminum / Vinyl	2	1958	1872	2	4	2
4501	2	Aluminum / Vinyl	1	1961	1274	1	3	1
4502	2	Brick	1	1959	1169	1	3	1
4503	2	Aluminum / Vinyl	1	1958	942	1	3	1
4504	2	Aluminum / Vinyl	1	1954	879	1	3	1
4505	3	Brick	2	1916	3543	1	4	2
4506	3	Aluminum / Vinyl	1	1920	1918	1	4	2
4507	3	Aluminum / Vinyl	1	1919	1635	1	3	2
4508	3	Brick	2	1928	3768	1	5	3
4509	3	Brick	2	1915	3666	1	5	3
4510	3	Stucco	2	1915	3507	1	4	2
4511	3	Frame	2	1902	2781	1	4	2
4512	3	Frame	1	1908	1512	1	3	1
4513	3	Frame	1	1908	1483	1	3	1
4514	5	Aluminum / Vinyl	1.5	1998	1819	1	3	2
4515	5	Aluminum / Vinyl	1	1952	1244	1	3	1
4516	5	Aluminum / Vinyl	1	1956	1154	1	4	1
4517	5	Frame	1.5	1939	1139	1	2	1
4518	5	Aluminum / Vinyl	1	1952	1021	1	4	1
4519	5	Aluminum / Vinyl	1.5	1949	999	1	3	1
4520	5	Masonry / Frame	2	1952	1528	1	3	1
4521	5	Aluminum / Vinyl	1.5	1922	1817	2	5	2
4522	5	Stone	1	1952	1604	1	3	1
4523	5	Brick	1	1954	1232	1	2	1
4524	5	Brick	1	1949	1216	1	2	1
4525	5	Frame	1	1971	1212	1	4	1
4526	5	Aluminum / Vinyl	1	1956	1132	1	3	2
4527	5	Brick	1	1956	1082	1	3	1
4528	5	Frame	1	1960	1079	1	3	1
4529	5	Aluminum / Vinyl	1	1956	1074	1	3	1
4530	5	Aluminum / Vinyl	1	1952	1064	1	2	1
4531	5	Aluminum / Vinyl	1	1950	715	1	2	1
4532	6	Aluminum / Vinyl	2	1905	3485	2	7	3
4533	6	Aluminum / Vinyl	1.5	1908	1538	2	3	2
4534	6	Aluminum / Vinyl	1	1920	826	1	2	1
4535	7	Aluminum / Vinyl	1	1953	1227	1	4	1
4536	7	Brick	1.5	1931	2008	2	3	2
4537	7	Aluminum / Vinyl	1	1921	1644	1	4	1

4538	7 Aluminum / Vinyl	1	1891	920	1	2	1
4539	8 Aluminum / Vinyl	1	1885	1208	1	3	1
4540	8 Aluminum / Vinyl	1.5	1929	2156	2	4	2
4541	8 Aluminum / Vinyl	1.5	1921	2049	2	4	2
4542	8 Aluminum / Vinyl	2	1913	2558	2	6	2
4543	8 Aluminum / Vinyl	1.5	1900	1497	1	4	1
4544	8 Aluminum / Vinyl	1.5	1907	1470	1	4	1
4545	8 Aluminum / Vinyl	1.5	1900	1255	1	3	1
4546	8 Aluminum / Vinyl	1	1903	1254	1	4	2
4547	9 Brick	1	1939	944	1	3	2
4548	9 Aluminum / Vinyl	1	1957	1332	1	3	1
4549	9 Aluminum / Vinyl	1	1958	1039	1	3	1
4550	9 Aluminum / Vinyl	1	1965	1033	1	3	1
4551	10 Brick	1	1937	1875	1	4	1
4552	10 Stone	1	1935	1490	1	2	1
4553	10 Brick	1	1949	1204	1	3	1
4554	10 Brick	1	1948	1129	1	3	1
4555	10 Aluminum / Vinyl	1	1952	1100	1	3	1
4556	10 Aluminum / Vinyl	1	1948	1082	1	3	1
4557	10 Aluminum / Vinyl	1	1947	1063	1	2	1
4558	10 Stucco	2	1923	2304	1	4	1
4559	10 Aluminum / Vinyl	2	2004	2227	1	4	2
4560	10 Aluminum / Vinyl	2	1946	1342	1	3	1
4561	10 Aluminum / Vinyl	2	1917	2678	2	6	2
4562	10 Brick	1.5	1941	1991	2	3	2
4563	10 Aluminum / Vinyl	1.5	1917	2011	1	3	1
4564	10 Brick	1	1933	1345	1	3	1
4565	10 Aluminum / Vinyl	1	1917	964	1	3	1
4566	10 Aluminum / Vinyl	1	1917	964	1	3	1
4567	10 Brick	1	1954	1380	1	3	2
4568	10 Aluminum / Vinyl	1	1954	864	1	3	1
4569	10 Aluminum / Vinyl	1	1918	1340	1	3	1
4570	10 Aluminum / Vinyl	1	1922	1208	1	3	2
4571	10 Brick	1.5	1928	2297	1	3	1
4572	11 Stone	1	1942	2928	1	3	2
4573	11 Brick	1	1952	1705	1	4	1
4574	11 Stone	1	1950	1279	1	3	1
4575	11 Aluminum / Vinyl	1	1946	958	1	3	1
4576	11 Brick	1.5	1959	2184	2	4	2
4577	11 Aluminum / Vinyl	1.5	1941	1841	2	3	2
4578	11 Stone	1.5	1942	1808	2	3	2
4579	11 Aluminum / Vinyl	1	1959	1235	1	3	1
4580	11 Aluminum / Vinyl	1	1970	1172	1	4	1

4581	11	Aluminum / Vinyl	1	1962	1161	1	3	1
4582	11	Brick	1	1959	1053	1	3	1
4583	11	Aluminum / Vinyl	1	1955	1002	1	3	2
4584	11	Aluminum / Vinyl	1	1954	984	1	3	1
4585	11	Aluminum / Vinyl	1	1954	984	1	3	1
4586	11	Aluminum / Vinyl	1	1960	937	1	3	1
4587	11	Brick	1	1954	918	1	3	1
4588	11	Aluminum / Vinyl	1	1953	899	1	3	1
4589	12	Aluminum / Vinyl	2	2009	1672	1	3	2
4590	12	Aluminum / Vinyl	1	1885	1295	1	4	1
4591	12	Aluminum / Vinyl	1	1880	882	1	2	1
4592	12	Frame	1	1903	1530	2	4	2
4593	13	Stone	1.5	1937	1433	1	2	1
4594	13	Brick	1	1951	1348	1	3	1
4595	13	Brick	1	1947	1163	1	3	1
4596	13	Aluminum / Vinyl	1	1954	1137	1	3	1
4597	13	Brick	1.5	1951	2463	2	5	2
4598	13	Brick	1	1964	1167	1	3	1
4599	13	Brick	1	1956	961	1	2	1
4600	14	Aluminum / Vinyl	1	1952	784	1	2	1
4601	14	Frame	2	1913	1536	1	4	2
4602	14	Aluminum / Vinyl	2	1945	1360	1	2	1
4603	14	Masonry / Frame	2	1984	2660	2	6	2
4604	14	Masonry / Frame	2	1940	2378	2	5	2
4605	14	Aluminum / Vinyl	1	1929	1450	1	3	1
4606	14	Aluminum / Vinyl	1	1928	992	1	2	1
4607	14	Aluminum / Vinyl	1	1955	864	1	3	1
4608	14	Aluminum / Vinyl	2	1908	2520	1	4	2
4609	14	Aluminum / Vinyl	1.5	1883	2024	1	4	2
4610	14	Aluminum / Vinyl	1.5	1910	1745	1	4	2
4611	14	Frame	2	1910	1520	1	4	1
4612	14	Aluminum / Vinyl	1	1910	1512	1	3	1
4613	14	Frame	2	1925	1320	1	3	1
4614	15	Aluminum / Vinyl	2	2009	1604	1	3	2
4615	1	Brick	1	1951	1308	1	3	1
4616	1	Brick	1	1951	1143	1	3	1
4617	1	Aluminum / Vinyl	1	1981	1007	1	3	1
4618	1	Aluminum / Vinyl	2	1928	1359	1	3	2
4619	2	Brick	1.5	1952	1715	1	4	1
4620	2	Brick	1	1951	1235	1	3	2
4621	2	Brick	1	1960	1044	1	2	1
4622	2	Aluminum / Vinyl	1	1956	1025	1	3	1
4623	2	Aluminum / Vinyl	1	1955	1008	1	3	1

4624	2	Aluminum / Vinyl	1	1955	756	1	2	1
4625	3	Frame	2	1902	4321	1	6	2
4626	3	Brick	1.5	1928	2201	2	4	2
4627	3	Frame	1.5	1905	1929	2	5	2
4628	3	Aluminum / Vinyl	1	1920	1490	1	3	1
4629	3	Brick	2	1904	4760	1	3	2
4630	3	Masonry / Frame	2	1910	3607	1	5	3
4631	3	Brick	2	1926	3434	1	4	3
4632	3	Stucco	1	1912	2823	1	3	3
4633	3	Aluminum / Vinyl	2	1907	2568	1	6	1
4634	3	Masonry / Frame	2	1917	2063	1	1	1
4635	3	Frame	2	1904	1812	1	3	2
4637	3	Frame	1.5	1910	1564	1	3	1
4638	3	Brick	2	1907	4417	1	6	3
4639	4	Frame	2	1909	2280	2	4	2
4640	5	Brick	1	1952	1659	1	3	2
4641	5	Brick	1	1952	1476	1	3	1
4642	5	Brick	1.5	1937	1392	1	3	1
4643	5	Brick	1	1947	1332	1	4	2
4644	5	Brick	1	1949	1298	1	3	1
4645	5	Brick	1	1948	1233	1	3	1
4646	5	Aluminum / Vinyl	1	1953	1064	1	3	2
4647	5	Aluminum / Vinyl	1.5	1950	1060	1	3	1
4648	5	Aluminum / Vinyl	1	1952	1018	1	4	1
4649	5	Aluminum / Vinyl	2	1969	1852	1	4	2
4650	5	Masonry / Frame	2	1952	2384	2	4	2
4651	5	Prem Wood	1	1993	2908	1	4	3
4652	5	Aluminum / Vinyl	1	1969	1573	1	3	1
4653	5	Aluminum / Vinyl	1	1972	1424	1	3	2
4654	5	Stone	1	1955	1294	1	3	1
4655	5	Aluminum / Vinyl	1	1955	1028	1	3	1
4656	5	Brick	1	1955	1016	1	3	1
4657	5	Aluminum / Vinyl	1	1950	995	1	2	1
4658	6	Aluminum / Vinyl	2	1893	2206	2	4	2
4659	6	Frame	1	1869	1512	2	4	3
4660	6	Frame	1.5	1900	1651	1	1	0
4661	6	Aluminum / Vinyl	2	1922	1306	1	3	1
4662	6	Aluminum / Vinyl	1	1893	1012	1	3	2
4663	7	Stone	1	1935	1962	1	4	2
4664	7	Brick	1.5	1953	1358	1	4	1
4665	7	Frame	2	1924	2586	2	6	2
4666	7	Brick	1	1927	1743	1	3	1
4667	7	Aluminum / Vinyl	1	1926	1422	1	3	1

4668	7	Brick	1	1950	1163	1	3	2
4669	8	Aluminum / Vinyl	1	1892	886	1	3	1
4670	8	Aluminum / Vinyl	1.5	1922	1702	2	3	2
4671	8	Brick	1	1927	1485	1	4	1
4672	8	Frame	1	1925	980	1	3	1
4673	8	Aluminum / Vinyl	1.5	1920	1255	1	3	1
4674	8	Brick	1	1929	1390	1	3	1
4675	9	Frame	1	1966	2092	1	3	1
4676	9	Aluminum / Vinyl	1	1952	1080	1	4	1
4677	9	Brick	2	1956	1949	2	4	2
4678	9	Aluminum / Vinyl	1	1966	1333	1	4	1
4679	9	Aluminum / Vinyl	1	1968	1175	1	3	1
4680	9	Aluminum / Vinyl	1	1958	1122	1	3	1
4681	9	Brick	1	1957	1103	1	3	1
4682	9	Brick	1	1957	973	1	3	1
4683	10	Aluminum / Vinyl	2	1914	2247	1	4	2
4684	10	Brick	2	1927	2004	1	3	1
4685	10	Brick	2	1937	1734	1	3	1
4686	10	Aluminum / Vinyl	2	1941	1484	1	3	1
4687	10	Brick	2	1921	2720	2	6	2
4688	10	Aluminum / Vinyl	2	1924	2491	2	6	2
4689	10	Aluminum / Vinyl	2	1924	2212	2	4	2
4690	10	Stucco	1	1918	1637	1	4	2
4691	10	Aluminum / Vinyl	1	1929	1607	1	3	2
4692	10	Aluminum / Vinyl	1	1928	1586	1	4	2
4693	10	Brick	1	1956	1284	1	3	1
4694	10	Brick	1	1956	1269	1	3	2
4695	10	Aluminum / Vinyl	1	1955	1120	1	2	2
4696	10	Aluminum / Vinyl	1	1953	768	1	2	1
4697	11	Stone	1.5	1946	1855	1	4	1
4698	11	Stucco	1	1946	1371	1	3	1
4699	11	Aluminum / Vinyl	1	1953	1329	1	4	1
4700	11	Aluminum / Vinyl	1	1952	1296	1	3	1
4701	11	Stone	1	1941	1198	1	3	1
4702	11	Brick	1	1941	1183	1	2	1
4703	11	Aluminum / Vinyl	1	1952	1096	1	3	2
4704	11	Aluminum / Vinyl	1	1954	789	1	2	1
4705	11	Aluminum / Vinyl	2	1974	1669	1	3	2
4706	11	Masonry / Frame	2	1952	2310	2	4	2
4707	11	Brick	1	1958	1418	1	3	2
4708	11	Aluminum / Vinyl	1	1968	1413	1	4	1
4709	11	Aluminum / Vinyl	1	1979	1247	1	3	1
4710	11	Masonry / Frame	1	1952	1216	1	3	1

4711	11	Aluminum / Vinyl	1	1972	1152	1	3	1
4712	11	Brick	1	1956	1142	1	3	1
4713	11	Brick	1	1957	1114	1	3	1
4714	11	Aluminum / Vinyl	1	1955	1055	1	3	1
4715	11	Aluminum / Vinyl	1	1957	1035	1	3	1
4716	11	Brick	1	1950	975	1	3	1
4717	11	Brick	1	1960	965	1	3	1
4718	11	Brick	1	1954	959	1	3	2
4719	11	Aluminum / Vinyl	1	1950	826	1	2	1
4720	11	Aluminum / Vinyl	1	1949	726	1	2	1
4721	13	Brick	1	1949	1353	1	3	2
4722	13	Aluminum / Vinyl	1	1971	1134	1	4	1
4723	13	Aluminum / Vinyl	2	1924	2440	2	5	2
4724	13	Aluminum / Vinyl	2	1954	1536	2	4	2
4725	13	Aluminum / Vinyl	1	1979	1878	1	3	2
4726	13	Aluminum / Vinyl	1	1977	1744	1	3	3
4727	13	Aluminum / Vinyl	1	1972	1407	1	3	1
4728	13	Brick	1	1973	1325	1	3	1
4729	13	Brick	1	1964	1164	1	3	1
4730	13	Frame	1	1963	1012	1	3	1
4731	13	Aluminum / Vinyl	1	1950	832	1	2	1
4732	14	Aluminum / Vinyl	1	1953	1233	1	3	1
4733	14	Aluminum / Vinyl	1	1953	1054	1	3	1
4734	14	Aluminum / Vinyl	2	1947	1378	1	3	1
4735	14	Aluminum / Vinyl	1	1900	686	1	2	2
4736	14	Brick	1.5	1953	2073	2	4	2
4737	14	Aluminum / Vinyl	2	1943	1620	2	4	2
4738	14	Aluminum / Vinyl	2	1954	1490	2	4	2
4739	14	Aluminum / Vinyl	2	1918	1752	2	4	2
4740	14	Aluminum / Vinyl	1.5	1915	1735	1	4	2
4741	14	Aluminum / Vinyl	1	1925	1530	1	4	2
4742	14	Aluminum / Vinyl	1	1924	906	1	3	1
4743	14	Brick	1	1952	1099	1	2	1
4744	14	Aluminum / Vinyl	1	1954	891	1	3	1
4745	14	Aluminum / Vinyl	1	1953	704	1	2	1
4746	14	Brick	1	1923	1648	1	4	1
4747	14	Aluminum / Vinyl	1.5	1897	1591	1	3	2
4748	14	Frame	1.5	1916	1424	1	4	1
4749	14	Aluminum / Vinyl	1	1905	1197	1	4	3
4750	14	Aluminum / Vinyl	1	1924	1102	1	4	1
4751	15	Aluminum / Vinyl	1	1987	1362	1	3	2
4752	15	Stucco	1.5	1919	2262	1	4	1
4753	1	Stone	1	1946	1416	1	4	1

4754	1	Prem Wood	2	1931	2113	1	3	2
4755	1	Frame	1	1958	1236	1	3	1
4756	1	Brick	1	1955	1197	1	3	1
4757	1	Aluminum / Vinyl	1	1967	1186	1	3	1
4758	1	Aluminum / Vinyl	1	1954	672	1	2	1
4759	2	Frame	1	1972	1434	1	4	1
4760	2	Aluminum / Vinyl	1	1955	1302	1	4	1
4761	2	Masonry / Frame	2	1942	1310	1	3	1
4762	2	Aluminum / Vinyl	1	1971	1164	1	4	1
4763	3	Frame	2	1900	3323	1	4	3
4764	3	Stucco	2	1916	3307	1	4	3
4765	3	Frame	2	1894	1274	1	3	1
4766	3	Brick	2	1931	2552	2	4	2
4767	3	Aluminum / Vinyl	2	1915	2402	2	6	2
4768	3	Brick	2	1921	3082	1	4	2
4769	3	Fiber-Cement	2	1890	2350	1	4	2
4770	3	Frame	2	1891	2280	1	4	2
4771	3	Brick	1	1925	2253	1	3	2
4772	3	Aluminum / Vinyl	2	1912	1608	1	3	1
4773	4	Aluminum / Vinyl	2	2001	2236	1	3	3
4774	4	Aluminum / Vinyl	1	1888	574	1	2	1
4775	4	Frame	2	1903	2396	1	5	1
4776	4	Aluminum / Vinyl	2	1885	2208	1	4	2
4777	5	Brick	1	1952	1502	1	3	2
4778	5	Brick	1.5	1957	1421	1	3	2
4779	5	Stone	1.5	1953	1349	1	3	1
4780	5	Brick	1	1948	1341	1	3	1
4781	5	Aluminum / Vinyl	1	1946	1234	1	3	1
4782	5	Brick	1	1952	1159	1	3	1
4783	5	Aluminum / Vinyl	1	1950	1113	1	3	2
4784	5	Aluminum / Vinyl	1	1950	1087	1	3	2
4785	5	Brick	1	1952	950	1	2	1
4786	5	Stucco	1	1953	784	1	2	1
4787	5	Aluminum / Vinyl	2	2011	3166	1	5	3
4788	5	Brick	2	1956	2426	2	4	2
4789	5	Masonry / Frame	2	1947	2072	2	4	2
4790	5	Aluminum / Vinyl	1	1934	1476	1	4	2
4791	5	Brick	1	1961	1300	1	3	2
4792	5	Stone	1	1950	1254	1	2	1
4793	5	Brick	1	1959	1197	1	3	1
4794	5	Aluminum / Vinyl	1	1964	1164	1	3	1
4795	5	Aluminum / Vinyl	1	1958	970	1	3	1
4796	5	Aluminum / Vinyl	1	1954	962	1	3	1

4797	5 Aluminum / Vinyl	1	1955	948	1	3	1
4798	5 Aluminum / Vinyl	1	1950	720	1	2	1
4799	6 Aluminum / Vinyl	2	1905	2148	2	4	2
4800	6 Aluminum / Vinyl	1	1926	1275	1	3	2
4801	6 Brick	2	1890	3026	1	5	2
4802	7 Brick	1	1946	1073	1	3	1
4803	7 Aluminum / Vinyl	1.5	1923	2042	2	4	2
4804	7 Aluminum / Vinyl	1.5	1892	1661	2	5	2
4805	7 Brick	1.5	1925	2063	1	3	1
4806	8 Aluminum / Vinyl	2	2009	1870	1	3	2
4807	8 Frame	1	1890	1035	1	3	1
4808	8 Aluminum / Vinyl	2	1950	2260	2	4	2
4809	8 Aluminum / Vinyl	1.5	1908	1760	1	5	2
4810	8 Aluminum / Vinyl	1	1910	1639	1	3	1
4811	8 Aluminum / Vinyl	1	1903	1545	1	4	1
4813	9 Aluminum / Vinyl	1	1974	1430	1	4	2
4814	9 Aluminum / Vinyl	1	1967	1303	1	3	1
4815	9 Aluminum / Vinyl	1	1966	1227	1	3	1
4816	10 Stone	1	1945	1391	1	4	2
4817	10 Aluminum / Vinyl	1	1947	1107	1	3	2
4818	10 Brick	1.5	1920	2535	2	4	2
4819	10 Brick	1.5	1942	2240	2	3	2
4820	10 Aluminum / Vinyl	1	1929	1390	2	3	2
4821	10 Brick	2	1958	5394	2	6	4
4822	10 Masonry / Frame	2	1952	1900	2	4	2
4823	10 Aluminum / Vinyl	1.5	1971	1889	2	5	2
4824	10 Aluminum / Vinyl	1.5	1924	1307	2	2	2
4825	10 Aluminum / Vinyl	1	1924	982	1	2	1
4826	10 Brick	1	1952	960	1	2	1
4827	10 Aluminum / Vinyl	1	1951	874	1	2	1
4828	10 Aluminum / Vinyl	1	1952	828	1	2	1
4829	10 Aluminum / Vinyl	1	1926	1078	1	3	2
4830	10 Aluminum / Vinyl	1	1924	1019	1	2	1
4831	11 Brick	1	1953	1333	1	3	1
4832	11 Aluminum / Vinyl	1	1958	1054	1	3	1
4833	11 Aluminum / Vinyl	2	1959	2162	2	5	2
4834	11 Aluminum / Vinyl	2	1959	1946	2	6	2
4835	11 Aluminum / Vinyl	2	1954	1824	2	6	2
4836	11 Brick	1.5	1923	2365	1	4	2
4837	11 Frame	1	1964	1553	1	3	1
4838	11 Brick	1	1960	1438	1	3	2
4839	11 Aluminum / Vinyl	1	1964	1240	1	3	1
4840	11 Frame	1	1959	1203	1	3	1

4841	11 Aluminum / Vinyl	1	1957	1078	1	3	1
4842	11 Aluminum / Vinyl	1	1960	1063	1	3	1
4843	11 Brick	1	1955	946	1	3	1
4844	11 Aluminum / Vinyl	1	1952	846	1	2	1
4845	11 Aluminum / Vinyl	1	1941	800	1	2	1
4846	11 Aluminum / Vinyl	1	1954	768	1	2	1
4847	11 Aluminum / Vinyl	2	1971	3102	2	6	2
4848	12 Aluminum / Vinyl	1	1903	1808	1	5	2
4849	13 Aluminum / Vinyl	1.5	1940	1360	1	4	2
4850	13 Stone	1	1940	1159	1	3	2
4851	13 Brick	1	1945	1075	1	3	1
4852	13 Aluminum / Vinyl	2	1948	1378	1	3	1
4853	13 Aluminum / Vinyl	1	1971	1196	1	2	1
4854	13 Aluminum / Vinyl	1	1945	826	1	2	1
4855	13 Aluminum / Vinyl	1.5	1921	1314	1	2	1
4856	13 Brick	2	1956	2435	3	5	3
4857	14 Aluminum / Vinyl	1	1940	1300	1	3	1
4858	14 Aluminum / Vinyl	1	1948	1044	1	3	1
4859	14 Brick	2	1915	2716	1	4	1
4860	14 Aluminum / Vinyl	2	2009	2052	1	3	1
4861	14 Aluminum / Vinyl	2	2010	1354	1	3	2
4862	14 Brick	2	1929	2850	2	6	2
4863	14 Brick	2	1929	2850	2	6	2
4864	14 Brick	1.5	1926	2664	2	5	3
4865	14 Brick	1.5	1929	2284	2	5	2
4866	14 Stucco	1.5	1923	1842	2	3	2
4867	14 Aluminum / Vinyl	1.5	1885	2410	2	6	2
4868	14 Brick	1	1926	2134	1	3	2
4869	14 Aluminum / Vinyl	1	1925	1145	1	3	1
4870	14 Aluminum / Vinyl	1	1952	877	1	2	1
4871	14 Aluminum / Vinyl	2	1903	1728	1	4	1
4872	14 Fiber-Cement	2	1890	1604	1	3	2
4873	14 Frame	2	1900	1520	1	3	2
4874	14 Aluminum / Vinyl	1	1916	1458	1	3	1
4875	14 Frame	1	1895	1130	1	3	1
4876	14 Aluminum / Vinyl	1	1900	1088	1	2	1
4877	15 Brick	1	1924	2175	1	3	2
4878	15 Aluminum / Vinyl	1	2001	1298	1	3	2
4879	15 Brick	1.5	1925	5383	1	4	>4
4880	1 Stone	1	1950	1627	1	3	1
4881	1 Brick	2	1958	2156	1	5	3
4882	1 Aluminum / Vinyl	2	1966	1292	1	3	1
4883	1 Aluminum / Vinyl	1	1954	1314	1	3	1

4884	1 Aluminum / Vinyl	1	1955	1082	1	3	1
4885	1 Frame	1	1925	970	1	3	1
4886	2 Brick	1	1957	1698	2	3	2
4887	2 Aluminum / Vinyl	1	1961	1398	1	3	1
4888	2 Brick	1	1956	1237	1	3	1
4889	2 Aluminum / Vinyl	1	1959	1108	1	3	1
4890	2 Brick	1	1962	1022	1	3	1
4891	2 Frame	1	1955	963	1	3	1
4892	2 Frame	1	1955	875	1	3	1
4893	2 Aluminum / Vinyl	1	1947	858	1	2	1
4894	3 Aluminum / Vinyl	2	1870	2016	1	3	2
4895	3 Brick	2	1905	7014	2	6	4
4896	3 Frame	2	1901	2960	1	5	2
4897	3 Brick	1.5	1927	2669	1	4	2
4898	3 Masonry / Frame	2	1916	2426	1	4	2
4899	3 Aluminum / Vinyl	1	1890	1113	1	3	1
4900	4 Brick	2	1916	3607	2	6	2
4901	4 Aluminum / Vinyl	2	1899	2329	1	3	1
4902	5 Aluminum / Vinyl	1	1956	1696	1	4	2
4903	5 Stone	1	1947	1410	1	3	1
4904	5 Brick	1	1954	1359	1	4	1
4905	5 Stone	1	1948	1335	1	3	1
4906	5 Aluminum / Vinyl	1	1955	1293	1	4	2
4907	5 Brick	1	1947	1279	1	2	1
4908	5 Aluminum / Vinyl	1	1952	1176	1	3	1
4909	5 Aluminum / Vinyl	1	1954	1001	1	4	1
4910	5 Aluminum / Vinyl	1	1953	993	1	4	1
4911	5 Aluminum / Vinyl	2	1940	1248	1	3	1
4912	5 Aluminum / Vinyl	2	1942	1084	1	2	1
4913	5 Brick	2	1952	2846	2	6	2
4914	5 Aluminum / Vinyl	1	2010	2222	1	3	2
4915	5 Brick	1	1980	1573	1	2	2
4916	5 Stone	1	1963	1385	1	3	1
4917	5 Brick	1	1961	1309	1	3	1
4918	5 Aluminum / Vinyl	1	1956	1132	1	3	1
4919	5 Brick	1	1955	1101	1	2	2
4920	5 Aluminum / Vinyl	1	1956	1064	1	3	1
4921	5 Aluminum / Vinyl	1	1950	977	1	3	1
4922	5 Aluminum / Vinyl	1	1954	861	1	3	1
4923	5 Aluminum / Vinyl	1	1949	828	1	2	1
4924	5 Aluminum / Vinyl	1	1948	704	1	2	1
4925	6 Fiber-Cement	2	2004	1824	1	3	2
4926	6 Aluminum / Vinyl	2	1922	1898	2	4	2

4927	6	Aluminum / Vinyl	1.5	1908	1302	1	3	1
4928	7	Aluminum / Vinyl	1	1941	1480	1	4	1
4929	7	Stone	1	1938	1454	1	4	1
4930	7	Brick	1	1955	1180	1	3	1
4931	7	Aluminum / Vinyl	1	1929	924	1	3	1
4932	8	Aluminum / Vinyl	1	1925	960	1	2	1
4933	8	Frame	1	1890	1707	1	3	1
4934	8	Aluminum / Vinyl	2	1915	1702	1	4	1
4935	8	Aluminum / Vinyl	1	1913	1403	1	4	2
4936	8	Aluminum / Vinyl	1	1916	1096	1	3	1
4937	9	Frame	1	1960	936	1	3	1
4938	9	Masonry / Frame	2	1971	3500	3	>8	3
4939	10	Aluminum / Vinyl	1.5	1948	1380	1	3	1
4940	10	Frame	1	1952	1291	1	3	1
4941	10	Aluminum / Vinyl	1	1949	1056	1	3	1
4942	10	Stucco	2	1913	2942	2	6	2
4943	10	Brick	1	1926	1707	1	5	2
4944	10	Brick	1	1927	1368	1	3	1
4945	10	Aluminum / Vinyl	1	1953	1098	1	3	2
4946	10	Aluminum / Vinyl	1	1922	912	1	3	1
4947	11	Stucco	1	1941	1271	1	3	1
4948	11	Brick	1	1950	1150	1	3	1
4949	11	Stone	1	1952	1056	1	2	1
4950	11	Aluminum / Vinyl	1	1942	848	1	3	1
4951	11	Aluminum / Vinyl	2	1949	1400	1	3	1
4952	11	Aluminum / Vinyl	2	1954	1554	2	4	2
4953	11	Aluminum / Vinyl	1	1963	1342	1	3	1
4954	11	Brick	1	1956	1288	1	3	1
4955	11	Brick	1	1966	1170	1	3	2
4956	11	Brick	1	1958	1121	1	3	1
4957	11	Frame	1	1956	1090	1	3	1
4958	11	Aluminum / Vinyl	1	1957	1011	1	3	1
4959	11	Aluminum / Vinyl	1	1956	958	1	3	1
4960	11	Brick	1	1955	935	1	3	1
4961	12	Aluminum / Vinyl	1.5	1923	2055	2	4	2
4962	13	Stone	1	1946	1280	1	3	1
4963	13	Masonry / Frame	2	1981	1785	1	3	1
4964	13	Brick	1.5	1930	2102	2	3	2
4965	13	Aluminum / Vinyl	1	1966	1371	1	3	1
4966	13	Brick	1	1963	1333	1	3	2
4967	13	Brick	1	1959	1312	1	3	1
4968	13	Aluminum / Vinyl	1	1969	1302	1	3	2
4969	13	Brick	1	1956	1150	1	3	1

4970	13	Aluminum / Vinyl	1	1958	982	1	3	1
4971	13	Aluminum / Vinyl	1	1960	950	1	3	1
4972	13	Aluminum / Vinyl	1	1940	702	1	2	1
4973	14	Aluminum / Vinyl	1.5	1926	2073	2	4	2
4974	14	Brick	1.5	1958	2059	2	5	2
4975	14	Aluminum / Vinyl	2	1974	2012	2	6	2
4976	14	Frame	2	1913	2544	2	4	2
4977	14	Frame	1	1912	1973	2	5	2
4978	14	Aluminum / Vinyl	1	1923	1757	1	3	2
4979	14	Aluminum / Vinyl	1	1929	1175	1	4	1
4980	14	Aluminum / Vinyl	1	1992	914	1	3	1
4981	14	Aluminum / Vinyl	2	1909	2141	1	3	2
4982	14	Aluminum / Vinyl	2	1903	1440	1	4	1
4983	14	Aluminum / Vinyl	1.5	1913	1424	1	4	1
4984	14	Frame	1.5	1900	1339	1	3	1
4985	14	Aluminum / Vinyl	1	1917	1176	1	4	1
4986	14	Frame	1	1899	1000	1	2	1
4987	15	Aluminum / Vinyl	2	1912	2856	2	6	2
4988	15	Aluminum / Vinyl	2	1911	2145	2	4	2
4989	15	Aluminum / Vinyl	2	1911	2144	2	4	2
4990	15	Aluminum / Vinyl	1.5	1883	1510	2	4	2
4991	1	Aluminum / Vinyl	2	1969	2502	2	6	2
4992	1	Aluminum / Vinyl	1	1962	1068	1	3	2
4993	2	Aluminum / Vinyl	1	1953	1518	1	4	2
4994	2	Aluminum / Vinyl	1	1953	986	1	3	1
4995	2	Aluminum / Vinyl	2	2003	3079	1	5	3
4996	2	Brick	1	1952	1290	1	2	1
4997	2	Brick	1	1951	1008	1	3	1
4998	2	Brick	1	1956	936	1	3	1
4999	2	Brick	1	1956	936	1	3	1
5000	3	Aluminum / Vinyl	1	1895	1778	2	4	1
5001	3	Masonry / Frame	2	1910	3135	1	4	2
5002	3	Aluminum / Vinyl	2	1899	1556	1	4	1
5003	3	Aluminum / Vinyl	2	1895	1516	1	2	2
5004	3	Frame	1.5	1900	1317	1	3	1
5005	5	Aluminum / Vinyl	1	1955	1316	1	4	1
5006	5	Brick	1	1952	1259	1	2	1
5007	5	Aluminum / Vinyl	1	1949	1231	1	4	1
5008	5	Aluminum / Vinyl	1	1940	1150	1	3	1
5009	5	Masonry / Frame	2	1952	3312	1	5	2
5010	5	Aluminum / Vinyl	2	1953	1411	1	3	1
5011	5	Aluminum / Vinyl	2	1954	1976	2	4	2
5012	5	Brick	1	1955	2262	1	2	1

5013	5	Brick	1	1958	1492	1	3	1
5014	5	Brick	1	1949	1453	1	3	2
5015	5	Brick	1	1955	1205	1	3	1
5016	5	Aluminum / Vinyl	1	1971	1204	1	4	1
5017	5	Aluminum / Vinyl	1	1958	1129	1	3	1
5018	6	Aluminum / Vinyl	2	1910	2274	2	5	2
5019	6	Aluminum / Vinyl	2	1895	1424	1	4	1
5021	7	Stone	1.5	1941	1643	1	3	2
5022	7	Aluminum / Vinyl	1	1947	1328	1	4	1
5023	7	Block	1	1948	1120	1	3	2
5024	7	Aluminum / Vinyl	1.5	1940	2124	2	3	2
5025	7	Aluminum / Vinyl	2	1942	1798	2	4	2
5026	8	Frame	2	1910	2208	2	4	2
5027	8	Aluminum / Vinyl	1.5	1913	2100	2	4	2
5028	8	Aluminum / Vinyl	1	1925	1357	1	4	1
5029	8	Stucco	2	1916	2000	1	3	2
5031	9	Aluminum / Vinyl	1	1951	1040	1	4	1
5032	9	Aluminum / Vinyl	2	2011	2096	1	4	2
5033	10	Brick	1.5	1936	1471	1	3	1
5034	10	Brick	1.5	1946	1402	1	4	2
5035	10	Aluminum / Vinyl	1	1890	1296	1	3	3
5036	10	Masonry / Frame	2	1926	2804	2	6	2
5037	10	Brick	1.5	1931	2505	2	4	3
5038	10	Masonry / Frame	2	1925	2495	2	6	2
5039	10	Frame	2	1920	2314	2	4	2
5040	10	Brick	1	1928	2315	1	4	1
5041	10	Aluminum / Vinyl	1	1927	1461	1	3	1
5042	10	Brick	1	1952	1292	1	3	1
5043	10	Aluminum / Vinyl	1	1919	1659	1	3	1
5044	10	Aluminum / Vinyl	1.5	1911	1525	1	3	1
5045	10	Brick	1	1931	1474	1	3	1
5046	11	Brick	1.5	1953	2008	1	3	2
5047	11	Aluminum / Vinyl	1	1954	1417	1	4	1
5048	11	Stone	1	1940	1221	1	3	1
5049	11	Brick	1	1953	1184	1	3	1
5050	11	Aluminum / Vinyl	1.5	1929	1760	2	4	2
5051	11	Masonry / Frame	2	1964	2229	2	6	2
5052	11	Aluminum / Vinyl	1.5	1978	2061	2	5	2
5053	11	Brick	1	1952	1489	1	3	2
5054	11	Brick	1	1960	1423	1	3	1
5055	11	Aluminum / Vinyl	1	1954	1271	1	3	1
5056	11	Brick	1	1954	1257	1	3	2
5057	11	Aluminum / Vinyl	1	1963	1168	1	3	1

5058	11	Brick	1	1959	1134	1	3	1
5059	11	Brick	1	1954	1116	1	3	1
5060	11	Fiber-Cement	1	1957	1099	1	3	2
5061	11	Brick	1	1959	1052	1	2	1
5062	11	Brick	1	1957	1040	1	3	1
5063	11	Brick	1	1953	1013	1	3	1
5064	11	Aluminum / Vinyl	1	1953	864	1	3	1
5065	11	Aluminum / Vinyl	1	1952	811	1	2	1
5066	11	Aluminum / Vinyl	1	1954	804	1	2	1
5067	12	Brick	2	1908	2566	2	4	2
5068	12	Aluminum / Vinyl	1	1890	1547	2	4	2
5069	12	Aluminum / Vinyl	1	1884	1370	1	4	1
5070	13	Brick	1	1966	2073	1	4	2
5071	13	Aluminum / Vinyl	1.5	1949	1373	1	3	2
5072	13	Aluminum / Vinyl	1	1952	1247	1	3	2
5073	13	Brick	1	1949	1200	1	3	1
5074	13	Aluminum / Vinyl	1	1942	1099	1	3	1
5075	13	Brick	1	1954	971	1	2	1
5076	13	Aluminum / Vinyl	1	1947	860	1	2	1
5077	13	Aluminum / Vinyl	1	1941	732	1	2	1
5078	13	Aluminum / Vinyl	2	1966	1957	1	3	1
5079	13	Aluminum / Vinyl	1	1925	1349	1	3	2
5080	13	Aluminum / Vinyl	1	1969	1824	1	3	1
5081	13	Brick	1	1973	1501	1	3	1
5082	13	Aluminum / Vinyl	1	1969	1345	1	3	1
5083	13	Aluminum / Vinyl	1	1960	1139	1	3	1
5084	13	Aluminum / Vinyl	1	1942	763	1	2	1
5085	14	Aluminum / Vinyl	1	1937	948	1	2	1
5086	14	Aluminum / Vinyl	1.5	1922	1384	2	3	3
5087	14	Aluminum / Vinyl	2	1900	1496	2	3	2
5088	14	Brick	1	1931	1472	1	4	2
5089	14	Brick	1	1956	1002	1	3	1
5090	14	Aluminum / Vinyl	1	1952	976	1	2	1
5091	14	Aluminum / Vinyl	1.5	1915	1557	1	4	2
5092	15	Aluminum / Vinyl	2	1915	2616	2	6	2
5095	1	Aluminum / Vinyl	1	1955	1188	1	4	1
5096	1	Aluminum / Vinyl	1	1940	1077	1	4	1
5097	2	Brick	1	1952	1321	1	4	1
5098	2	Frame	1.5	1955	1208	1	4	1
5099	2	Aluminum / Vinyl	1	1953	984	1	3	1
5100	2	Stone	1	1946	2152	2	3	2
5101	2	Frame	1	1929	1489	1	5	2
5102	2	Brick	1	1961	1261	1	3	1

5103	2 Aluminum / Vinyl	1	1965	1144	1	3	1
5104	2 Aluminum / Vinyl	1	1961	1101	1	3	1
5105	2 Aluminum / Vinyl	1	1957	882	1	3	2
5106	2 Aluminum / Vinyl	2	1984	2504	2	6	2
5107	3 Frame	2	1929	2259	2	4	2
5108	3 Aluminum / Vinyl	1.5	1922	1659	2	4	2
5109	3 Stone	2	1929	7664	1	7	4
5110	3 Brick	2	1909	5862	1	5	4
5111	3 Brick	2	1926	4843	1	6	>4
5112	3 Frame	2	1896	3342	1	6	2
5113	3 Aluminum / Vinyl	2	1898	2887	1	4	2
5114	3 Masonry / Frame	2	1906	2490	1	3	2
5115	3 Frame	2	1900	2206	1	4	1
5116	3 Frame	1	1914	1692	1	4	1
5117	3 Aluminum / Vinyl	1.5	1889	1688	1	3	1
5118	3 Brick	2	1912	4792	1	6	3
5119	4 Aluminum / Vinyl	1	1890	1302	1	3	1
5120	5 Brick	1.5	1952	1624	1	3	2
5121	5 Stone	1	1948	1331	1	4	2
5122	5 Aluminum / Vinyl	1	1940	1127	1	2	1
5123	5 Aluminum / Vinyl	1	1952	1114	1	4	2
5124	5 Aluminum / Vinyl	2	2011	3302	1	4	3
5125	5 Brick	2	1955	2101	1	3	1
5126	5 Masonry / Frame	2	1955	2816	2	6	2
5127	5 Masonry / Frame	2	1957	2222	2	5	2
5128	5 Brick	1	1969	1642	1	3	1
5129	5 Brick	1	1951	1388	1	3	1
5130	5 Brick	1	1956	1234	1	3	1
5131	5 Brick	1	1954	1185	1	3	1
5132	5 Brick	1	1959	1124	1	3	2
5133	5 Brick	1	1951	1098	1	3	2
5134	5 Masonry / Frame	1	1954	1065	1	3	2
5135	5 Aluminum / Vinyl	1	1959	1063	1	3	1
5136	5 Aluminum / Vinyl	2	1981	2423	2	6	2
5137	6 Aluminum / Vinyl	2	1910	2952	2	6	2
5138	6 Aluminum / Vinyl	2	1908	2296	2	4	2
5139	6 Aluminum / Vinyl	2	1908	2294	2	4	2
5140	6 Aluminum / Vinyl	1	1925	1384	1	2	1
5141	6 Aluminum / Vinyl	2	1906	2092	1	4	2
5142	6 Aluminum / Vinyl	2	1910	2860	3	5	3
5143	7 Aluminum / Vinyl	1	1930	1362	1	3	1
5144	7 Aluminum / Vinyl	1.5	1924	1330	1	3	2
5145	7 Aluminum / Vinyl	1.5	1925	1229	1	3	2

5146	7	Brick	1.5	1956	2597	2	6	2
5147	8	Aluminum / Vinyl	2	1912	1408	2	4	2
5148	8	Aluminum / Vinyl	1.5	1928	1634	1	3	2
5149	9	Aluminum / Vinyl	2	2011	3441	1	4	2
5150	9	Aluminum / Vinyl	1	2011	1566	1	3	2
5151	9	Aluminum / Vinyl	1	1971	1108	1	4	1
5152	9	Aluminum / Vinyl	1	1960	936	1	3	1
5153	10	Brick	1	1949	1338	1	4	3
5154	10	Aluminum / Vinyl	1.5	1948	1265	1	3	2
5155	10	Brick	1.5	1926	2213	2	4	2
5156	10	Aluminum / Vinyl	1.5	1924	1942	2	4	2
5157	10	Aluminum / Vinyl	1.5	1924	1797	2	4	2
5158	10	Aluminum / Vinyl	2	1911	2250	2	6	2
5159	10	Aluminum / Vinyl	1	1919	1641	1	4	2
5160	10	Stucco	1	1924	1293	1	3	1
5161	10	Stucco	1	1924	1089	1	2	1
5162	10	Aluminum / Vinyl	1	1948	880	1	1	1
5163	10	Aluminum / Vinyl	2	1886	1476	1	3	1
5164	11	Aluminum / Vinyl	1	1953	1186	1	4	1
5165	11	Aluminum / Vinyl	1	1953	1177	1	4	1
5166	11	Aluminum / Vinyl	1	1941	907	1	4	1
5167	11	Brick	1	1955	1697	1	3	2
5168	11	Brick	1	1959	1307	1	3	1
5169	11	Brick	1	1959	1126	1	3	1
5170	11	Brick	1	1956	1057	1	3	1
5171	11	Aluminum / Vinyl	1	1953	1035	1	3	1
5172	11	Aluminum / Vinyl	1	1954	991	1	3	1
5173	11	Aluminum / Vinyl	1	1956	979	1	3	1
5174	11	Brick	1	1960	965	1	3	1
5175	11	Aluminum / Vinyl	1	1954	933	1	3	1
5176	11	Brick	1	1954	838	1	2	1
5177	11	Aluminum / Vinyl	1	1951	811	1	2	1
5178	11	Aluminum / Vinyl	1	1952	749	1	2	1
5179	12	Aluminum / Vinyl	1	1884	832	1	2	1
5180	13	Brick	1	1942	1491	1	3	2
5181	13	Aluminum / Vinyl	1	1951	1091	1	3	1
5182	13	Brick	2	1961	2156	2	4	2
5183	13	Aluminum / Vinyl	1.5	1929	1837	2	3	2
5184	13	Aluminum / Vinyl	1	1930	1348	1	4	1
5185	13	Brick	1	1971	1674	1	4	1
5186	13	Aluminum / Vinyl	1	1964	1342	1	3	1
5187	13	Brick	1	1953	1044	1	3	1
5188	14	Aluminum / Vinyl	1	1947	1022	1	3	1

5189	14 Aluminum / Vinyl	1	1927	1248	1	3	1
5190	14 Aluminum / Vinyl	1	1926	1004	1	3	1
5191	14 Frame	2	1904	1813	1	4	1
5192	14 Aluminum / Vinyl	2	1908	1276	1	2	1
5193	15 Aluminum / Vinyl	1.5	1925	1950	2	4	2
5194	15 Aluminum / Vinyl	2	1908	2976	2	6	2
5195	1 Aluminum / Vinyl	1	1940	1206	1	3	1
5196	1 Aluminum / Vinyl	1	1952	908	1	2	1
5197	2 Brick	1	1953	1512	1	3	2
5198	2 Aluminum / Vinyl	1	1956	1326	1	4	1
5199	2 Aluminum / Vinyl	2	2003	1991	1	4	2
5200	2 Aluminum / Vinyl	1	1955	1247	1	4	1
5201	2 Aluminum / Vinyl	1	1963	1151	1	3	2
5202	2 Brick	1	1957	1148	1	3	2
5203	2 Brick	1	1956	1144	1	2	2
5204	2 Masonry / Frame	1	1948	1032	1	3	1
5205	2 Brick	1	1950	794	1	2	1
5206	2 Aluminum / Vinyl	2	1981	2402	2	6	2
5207	3 Brick	2	1920	3212	1	5	4
5208	3 Brick	1.5	1925	2234	2	4	2
5209	3 Aluminum / Vinyl	2	1940	1872	2	4	2
5210	3 Brick	2	1921	3346	1	4	2
5211	3 Frame	2	1898	2492	1	5	2
5212	5 Stone	1	1947	1442	1	3	1
5213	5 Brick	1	1949	1338	1	3	2
5214	5 Brick	1	1955	1221	1	4	2
5215	5 Brick	1	1950	1146	1	3	1
5216	5 Aluminum / Vinyl	1	1953	693	1	2	1
5217	5 Aluminum / Vinyl	1	1957	1120	1	3	1
5218	5 Brick	1	1956	1031	1	3	2
5219	6 Frame	1	1890	1722	1	2	1
5220	6 Aluminum / Vinyl	2	1890	2288	2	5	2
5221	6 Aluminum / Vinyl	1	1890	1476	1	4	1
5222	7 Stone	1.5	1936	1775	1	4	3
5223	7 Brick	1	1947	1561	1	3	2
5224	7 Masonry / Frame	2	1926	1532	1	3	1
5225	7 Aluminum / Vinyl	1	1925	1596	1	3	2
5226	8 Aluminum / Vinyl	1	1890	1268	1	4	1
5227	8 Aluminum / Vinyl	1	1922	1138	1	3	1
5228	8 Aluminum / Vinyl	1	1913	1549	1	4	1
5229	8 Aluminum / Vinyl	1.5	1907	1398	1	3	2
5230	9 Aluminum / Vinyl	1	1955	984	1	3	1
5231	9 Aluminum / Vinyl	2	1978	1347	1	4	1

5232	10	Aluminum / Vinyl	1	1948	1170	1	4	1
5233	10	Aluminum / Vinyl	1.5	1924	1682	2	4	2
5234	10	Aluminum / Vinyl	2	1930	1232	2	2	2
5235	10	Aluminum / Vinyl	1.5	1927	1929	1	4	3
5236	10	Aluminum / Vinyl	1	1927	1513	1	4	2
5237	10	Aluminum / Vinyl	1	1926	1224	1	3	1
5238	10	Aluminum / Vinyl	1.5	1913	2135	1	3	2
5239	10	Aluminum / Vinyl	1	1924	840	1	2	1
5240	11	Frame	1	1971	2008	1	4	2
5241	11	Brick	1	1954	1442	1	4	1
5242	11	Aluminum / Vinyl	1	1953	1406	1	4	2
5243	11	Aluminum / Vinyl	1	1953	1113	1	3	1
5244	11	Masonry / Frame	2	1954	1671	2	3	2
5245	11	Brick	1	1929	2067	1	3	1
5246	11	Frame	1	1964	1126	1	3	2
5247	11	Brick	1	1950	893	1	2	1
5248	11	Stone	1	1948	819	1	2	1
5249	11	Aluminum / Vinyl	1	1942	762	1	2	1
5250	12	Aluminum / Vinyl	1	1925	1872	2	5	3
5251	13	Frame	1.5	1947	1276	1	3	2
5252	13	Brick	1	1949	1183	1	3	1
5253	13	Aluminum / Vinyl	1	1951	836	1	2	1
5254	13	Masonry / Frame	2	1968	2073	1	5	1
5255	13	Brick	1.5	1955	1518	2	4	2
5256	13	Aluminum / Vinyl	2	1920	2230	2	6	2
5257	13	Aluminum / Vinyl	1	1973	1106	1	4	1
5258	13	Aluminum / Vinyl	1	1959	978	1	3	1
5259	14	Stucco	1	1943	1131	1	2	1
5260	14	Aluminum / Vinyl	1.5	1923	1951	2	4	2
5261	14	Brick	1	1929	1677	1	3	2
5262	14	Aluminum / Vinyl	1	1924	1532	1	3	2
5263	14	Stucco	1.5	1911	2206	1	4	3
5264	14	Aluminum / Vinyl	2	1908	1726	1	3	1
5265	14	Aluminum / Vinyl	1	1906	1404	1	4	2
5266	14	Aluminum / Vinyl	1	1900	1374	1	3	2
5267	14	Frame	1	1910	1298	1	3	1
5268	14	Aluminum / Vinyl	1	1905	1136	1	4	1
5269	15	Brick	1	1919	2270	1	4	2
5270	1	Masonry / Frame	2	1970	1237	1	4	1
5271	1	Aluminum / Vinyl	1	1951	1302	1	4	1
5272	2	Aluminum / Vinyl	1	1955	1229	1	3	1
5273	2	Stone	1.5	1925	2033	2	4	2
5274	2	Brick	2	1957	2522	3	5	3

5275	3	Stucco	2	1920	2292	1	5	1
5276	3	Aluminum / Vinyl	>2	2003	2112	1	3	3
5277	3	Aluminum / Vinyl	2	1910	3944	2	6	2
5278	3	Aluminum / Vinyl	2	1912	2090	2	5	3
5279	3	Brick	2	1912	5044	1	5	3
5280	3	Brick	1.5	1930	2439	1	3	2
5281	4	Masonry / Frame	2	1907	3006	3	6	2
5282	5	Aluminum / Vinyl	1	1946	1108	1	3	2
5283	5	Aluminum / Vinyl	1	1947	1598	1	3	2
5284	5	Frame	1	1951	1256	1	3	2
5285	5	Aluminum / Vinyl	1	1956	1219	1	3	1
5286	5	Brick	1	1949	1216	1	2	1
5287	5	Aluminum / Vinyl	1	1954	1163	1	3	1
5288	5	Frame	1	1956	1093	1	3	1
5290	5	Brick	1	1956	1040	1	3	1
5291	5	Aluminum / Vinyl	1	1956	1019	1	3	1
5292	7	Stone	1	1950	1908	1	3	2
5293	8	Aluminum / Vinyl	2	1912	2516	2	5	2
5294	8	Aluminum / Vinyl	1.5	1921	1741	2	4	2
5295	8	Frame	1	1893	1385	1	4	1
5296	9	Frame	1	1970	1600	1	3	1
5297	9	Brick	1	1958	1396	1	3	1
5298	9	Aluminum / Vinyl	1	1961	967	1	3	1
5299	10	Frame	1	1949	1263	1	3	1
5300	10	Stucco	1	1919	2054	1	4	2
5301	10	Brick	1	1928	2008	1	3	1
5302	10	Brick	1	1928	1673	1	5	2
5303	10	Aluminum / Vinyl	1.5	1920	1098	1	3	1
5304	11	Aluminum / Vinyl	1	1953	1393	1	3	1
5305	11	Aluminum / Vinyl	1	1952	1016	1	3	1
5306	11	Aluminum / Vinyl	2	1964	1662	1	3	1
5307	11	Brick	2	1932	2225	2	4	2
5308	11	Frame	1	1928	1913	1	4	2
5309	11	Block	1	1951	1088	1	2	1
5310	11	Brick	2	1928	2733	1	3	1
5311	11	Aluminum / Vinyl	2	1964	2176	2	6	2
5312	13	Brick	1	1938	1443	1	3	2
5313	13	Aluminum / Vinyl	2	1994	1850	1	3	2
5314	13	Masonry / Frame	1.5	1959	1991	2	5	2
5315	13	Aluminum / Vinyl	1	1960	891	1	3	1
5316	14	Brick	1.5	1948	1401	1	4	1
5317	14	Aluminum / Vinyl	1	1957	1168	1	3	1
5318	14	Frame	2	1918	2034	2	6	2

5319	14	Frame	1	1912	1973	2	5	2
5320	14	Aluminum / Vinyl	1	1922	1462	1	4	1
5321	14	Aluminum / Vinyl	1.5	1913	1163	1	3	1
5322	14	Aluminum / Vinyl	1	1910	897	1	3	2
5323	14	Aluminum / Vinyl	1	1910	840	1	1	2
5324	15	Brick	1	1920	1974	1	3	1
5325	1	Aluminum / Vinyl	1	1942	1339	1	3	2
5326	1	Block	1.5	1947	1664	2	4	2
5327	1	Stucco	1	1924	1495	1	4	1
5328	1	Aluminum / Vinyl	1	1927	1087	1	3	1
5329	2	Brick	1	1951	1168	1	3	2
5330	2	Brick	1	1922	1174	1	2	2
5331	3	Frame	2	1898	2526	1	4	2
5332	3	Aluminum / Vinyl	2	1960	1534	1	4	1
5333	3	Frame	2	1902	2949	1	4	1
5334	3	Brick	2	1909	2068	1	4	1
5335	5	Brick	1	1952	1573	1	3	1
5336	5	Brick	1	1948	1512	1	3	1
5337	5	Frame	1	1952	1326	1	3	1
5338	5	Aluminum / Vinyl	1	1948	1256	1	4	1
5339	5	Brick	1	1947	1251	1	4	1
5340	5	Brick	1	1951	1205	1	3	1
5341	5	Brick	1	1949	1059	1	2	2
5342	5	Aluminum / Vinyl	1	1950	1040	1	3	1
5343	5	Aluminum / Vinyl	2	2010	2506	1	4	2
5344	5	Aluminum / Vinyl	2	2011	2480	1	4	2
5345	5	Brick	2	1952	2330	2	4	2
5346	5	Stone	1	1951	1703	1	2	2
5347	5	Aluminum / Vinyl	1	1969	1629	1	3	2
5348	5	Frame	1	1952	1407	1	3	1
5349	5	Frame	1	1951	1256	1	3	2
5350	5	Aluminum / Vinyl	1	1962	1238	1	3	2
5351	5	Brick	1	1959	1128	1	3	1
5352	6	Aluminum / Vinyl	2	1891	1980	2	6	3
5353	6	Prem Wood	2	1890	1878	1	4	2
5354	6	Aluminum / Vinyl	1	1892	1116	1	2	1
5355	7	Aluminum / Vinyl	1.5	1940	1504	1	3	1
5356	7	Stone	2	1945	1817	1	3	2
5357	7	Brick	2	1935	1555	1	3	1
5358	7	Brick	2	1944	1824	2	4	2
5359	8	Aluminum / Vinyl	1.5	1924	1896	2	4	2
5360	8	Aluminum / Vinyl	2	1903	1916	2	4	2
5361	8	Frame	2	1906	1875	2	4	2

5363	9	Fiber-Cement	2	2006	2028	1	3	2
5364	9	Brick	1	1957	997	1	3	1
5365	9	Aluminum / Vinyl	1	1975	906	1	3	1
5366	10	Aluminum / Vinyl	1	1984	1414	1	3	2
5367	10	Brick	1.5	1955	2230	1	4	2
5368	10	Aluminum / Vinyl	1	1953	1363	1	3	2
5369	10	Brick	1	1953	1350	1	3	1
5370	10	Masonry / Frame	2	1937	1671	1	3	1
5371	10	Aluminum / Vinyl	2	1914	2768	2	5	2
5372	10	Aluminum / Vinyl	1.5	1918	2178	1	5	2
5373	10	Frame	1	1919	1391	1	3	1
5374	10	Aluminum / Vinyl	1	1923	1387	1	4	1
5375	10	Frame	1	1926	1354	1	3	1
5376	10	Aluminum / Vinyl	1	1917	964	1	3	1
5377	10	Aluminum / Vinyl	2	1926	1356	1	4	1
5378	10	Aluminum / Vinyl	1	1928	906	1	2	1
5379	11	Aluminum / Vinyl	1	1942	1728	1	3	1
5380	11	Aluminum / Vinyl	1	1953	1525	1	4	2
5381	11	Brick	1	1948	1477	1	4	2
5382	11	Aluminum / Vinyl	1	1948	958	1	3	1
5383	11	Stone	2	1937	1676	1	3	1
5384	11	Masonry / Frame	2	1954	2168	2	4	2
5385	11	Aluminum / Vinyl	1.5	1955	1697	2	4	2
5386	11	Frame	1	1928	1121	1	3	1
5387	11	Aluminum / Vinyl	1	1953	1727	1	3	2
5388	11	Brick	1	1951	1455	1	3	1
5389	11	Brick	1	1967	1232	1	3	1
5390	11	Brick	1	1955	1166	1	3	2
5391	11	Aluminum / Vinyl	1	1970	1107	1	3	2
5392	11	Aluminum / Vinyl	1	1956	1073	1	3	1
5393	11	Brick	1	1953	1013	1	3	1
5394	11	Aluminum / Vinyl	1	1958	936	1	3	1
5395	11	Aluminum / Vinyl	1	1939	858	1	2	1
5396	11	Frame	1	1956	672	1	2	1
5397	12	Aluminum / Vinyl	2	2009	1848	1	4	2
5398	12	Aluminum / Vinyl	2	1909	2117	2	5	2
5399	12	Aluminum / Vinyl	1	1930	1588	1	4	1
5400	13	Brick	1	1947	1292	1	4	1
5401	13	Block	1	1940	1227	1	4	2
5402	13	Brick	1	1950	1190	1	3	1
5403	13	Aluminum / Vinyl	1	1950	1141	1	3	2
5404	13	Aluminum / Vinyl	1	1949	979	1	3	1
5405	13	Aluminum / Vinyl	2	1994	1636	1	3	1

5406	13	Brick	2	1949	1404	1	3	1
5407	13	Aluminum / Vinyl	1.5	1930	1397	2	4	2
5408	13	Brick	1	1968	1463	1	2	1
5409	13	Brick	1	1963	1242	1	3	1
5410	13	Brick	1	1963	1104	1	3	1
5411	13	Aluminum / Vinyl	1	1960	891	1	3	1
5412	13	Fiber-Cement	1	1929	1056	1	3	1
5413	13	Aluminum / Vinyl	2	1976	2538	2	6	2
5414	14	Aluminum / Vinyl	1	1947	1132	1	3	1
5415	14	Aluminum / Vinyl	1	1948	1054	1	3	1
5416	14	Prem Wood	2	1981	1574	1	2	1
5417	14	Aluminum / Vinyl	2	1941	1196	1	2	1
5418	14	Aluminum / Vinyl	1.5	1925	1982	2	5	2
5419	14	Aluminum / Vinyl	2	1885	2660	2	5	2
5420	14	Brick	1	1952	961	1	3	1
5421	14	Brick	2	1922	2761	1	5	1
5422	14	Frame	2	1888	1627	1	3	2
5423	14	Aluminum / Vinyl	1.5	1885	1232	1	3	2
5424	15	Aluminum / Vinyl	2	2000	1449	1	3	1
5425	15	Aluminum / Vinyl	2	1924	2022	2	4	2
5426	15	Aluminum / Vinyl	1	1920	1655	1	4	2
5427	15	Frame	1	1922	1553	1	4	1
5428	1	Stone	1	1936	1560	1	4	1
5429	1	Aluminum / Vinyl	1	1941	1062	1	3	1
5430	1	Brick	1	1945	1033	1	3	1
5431	1	Brick	1	1948	1302	1	4	2
5432	2	Brick	1	1952	1699	1	3	1
5433	2	Frame	1	1970	1120	1	4	1
5434	2	Aluminum / Vinyl	1	1959	1103	1	3	1
5435	2	Aluminum / Vinyl	1	1950	936	1	3	1
5436	3	Frame	2	1906	5160	2	5	4
5437	3	Aluminum / Vinyl	2	1927	1725	1	3	1
5438	3	Masonry / Frame	2	1906	3056	2	6	2
5439	3	Aluminum / Vinyl	1.5	1898	1594	2	3	2
5440	3	Frame	1	1920	1420	1	3	1
5441	3	Brick	2	1922	4044	1	5	3
5442	3	Aluminum / Vinyl	1.5	1900	1786	1	4	1
5443	3	Brick	1.5	1939	1313	1	2	1
5444	4	Aluminum / Vinyl	2	1898	1882	1	4	1
5445	4	Aluminum / Vinyl	1.5	1888	1568	1	3	1
5446	5	Brick	1	1950	1530	1	4	2
5447	5	Brick	1	1947	1294	1	3	1
5448	5	Aluminum / Vinyl	1.5	1956	1271	1	4	1

5449	5	Brick	1	1949	1186	1	3	2
5450	5	Aluminum / Vinyl	1	1947	1072	1	3	1
5451	5	Stone	1	1950	989	1	2	1
5452	5	Aluminum / Vinyl	1	1951	971	1	3	1
5453	5	Aluminum / Vinyl	1	1953	946	1	3	1
5454	5	Aluminum / Vinyl	2	1950	1378	1	3	1
5455	5	Brick	1.5	1980	2366	2	5	2
5456	5	Masonry / Frame	1	1950	1733	1	3	2
5457	5	Aluminum / Vinyl	1	1968	1616	1	3	2
5458	5	Brick	1	1953	1308	1	3	2
5459	5	Brick	1	1959	1290	1	3	2
5460	5	Aluminum / Vinyl	1	1949	1286	1	3	1
5461	5	Brick	1	1958	1276	1	3	1
5462	5	Aluminum / Vinyl	1	1954	1168	1	3	1
5463	5	Masonry / Frame	1	1954	1137	1	3	1
5464	5	Frame	1	1960	1115	1	3	1
5465	5	Aluminum / Vinyl	1	1952	1040	1	2	1
5466	5	Aluminum / Vinyl	1	1956	1019	1	3	1
5467	6	Aluminum / Vinyl	2	1890	2028	2	4	2
5468	7	Brick	1	1945	1460	1	4	2
5469	7	Stone	1	1938	1396	1	3	1
5470	7	Aluminum / Vinyl	1	1942	1357	1	3	1
5471	7	Aluminum / Vinyl	2	1940	1364	1	3	1
5472	7	Frame	2	1924	2618	2	4	2
5473	7	Masonry / Frame	2	1924	2930	1	5	2
5474	7	Brick	1	1924	2429	1	4	2
5476	7	Brick	1	1956	1498	1	3	2
5477	8	Aluminum / Vinyl	1.5	1913	1783	2	4	2
5478	8	Aluminum / Vinyl	1	1925	1261	1	4	2
5479	8	Frame	1	1923	945	1	3	1
5480	9	Aluminum / Vinyl	2	1999	1503	1	3	1
5481	9	Aluminum / Vinyl	1	1957	1560	1	4	1
5482	9	Aluminum / Vinyl	1	1971	1210	1	3	1
5483	10	Stone	1	1939	1688	1	3	1
5484	10	Brick	1.5	1937	1496	1	4	1
5485	10	Frame	1	1953	1484	1	3	2
5486	10	Brick	1	1952	1376	1	4	1
5487	10	Brick	1	1923	1342	1	3	2
5488	10	Aluminum / Vinyl	1	1949	1204	1	3	2
5489	10	Aluminum / Vinyl	1	1952	1144	1	3	1
5490	10	Frame	1	1890	920	1	3	1
5491	10	Frame	2	1923	2530	2	4	2
5492	10	Stone	2	1937	2417	2	4	2

5493	10	Aluminum / Vinyl	2	1923	2212	2	4	2
5494	10	Masonry / Frame	1.5	1929	2053	2	4	2
5495	10	Aluminum / Vinyl	1.5	1928	1973	2	4	2
5496	10	Frame	1	1918	1835	1	3	2
5497	10	Frame	1	1900	1684	1	3	1
5498	10	Aluminum / Vinyl	1	1930	1454	1	4	1
5499	10	Aluminum / Vinyl	1	1924	1235	1	3	1
5500	10	Aluminum / Vinyl	1	1929	1169	1	3	1
5501	10	Aluminum / Vinyl	1	1926	1120	1	4	1
5502	10	Aluminum / Vinyl	1	1926	1010	1	3	1
5503	10	Stone	1.5	1940	1890	1	3	2
5504	11	Brick	1	1950	1588	1	4	1
5505	11	Aluminum / Vinyl	1	1954	1321	1	3	1
5507	11	Aluminum / Vinyl	1	1949	1106	1	3	1
5508	11	Aluminum / Vinyl	1	1950	1032	1	3	1
5509	11	Masonry / Frame	2	1989	2481	1	4	2
5510	11	Masonry / Frame	2	1968	1577	1	4	1
5511	11	Masonry / Frame	2	1955	2096	2	4	2
5512	11	Brick	1.5	1956	1846	2	4	2
5513	11	Aluminum / Vinyl	2	1954	1728	2	6	2
5514	11	Brick	1	1959	1533	1	3	1
5515	11	Brick	1	1968	1506	1	3	1
5516	11	Brick	1	1956	1334	1	3	2
5517	11	Brick	1	1958	1304	1	2	2
5518	11	Brick	1	1963	1172	1	3	1
5519	11	Frame	1	1964	1128	1	3	1
5520	11	Aluminum / Vinyl	1	1954	1065	1	3	1
5521	11	Brick	1	1958	1050	1	3	1
5522	11	Brick	1	1953	1013	1	3	1
5523	11	Brick	1	1930	1822	1	4	2
5524	12	Aluminum / Vinyl	2	2010	1892	1	4	2
5525	12	Aluminum / Vinyl	2	2011	1848	1	4	2
5526	12	Frame	2	1909	2052	2	4	2
5527	12	Frame	2	1923	2032	2	6	2
5528	12	Aluminum / Vinyl	1	1902	1118	1	3	1
5529	13	Aluminum / Vinyl	1	1955	2475	1	4	1
5530	13	Brick	1	1949	1327	1	3	1
5531	13	Stone	1	1941	1291	1	3	1
5532	13	Aluminum / Vinyl	1	1946	1137	1	3	1
5533	13	Brick	1	1949	1120	1	3	1
5534	13	Aluminum / Vinyl	2	1940	1468	1	3	1
5535	13	Aluminum / Vinyl	2	1948	1300	1	3	1
5536	13	Aluminum / Vinyl	1	1976	1820	1	3	2

5537	13	Brick	1	1965	1116	1	3	1
5538	13	Brick	1	1952	1092	1	3	1
5539	13	Aluminum / Vinyl	1	1944	698	1	2	1
5540	13	Frame	1.5	1890	1602	1	3	2
5541	13	Aluminum / Vinyl	1.5	1924	1458	1	2	1
5542	13	Aluminum / Vinyl	1.5	1900	1141	1	2	1
5543	13	Frame	1	1900	1007	1	2	1
5544	14	Aluminum / Vinyl	1	1947	1021	1	3	1
5545	14	Aluminum / Vinyl	1	1949	998	1	4	1
5546	14	Frame	>2	1959	1996	1	3	2
5547	14	Aluminum / Vinyl	2	1940	1248	1	3	1
5548	14	Aluminum / Vinyl	1.5	1950	1456	2	3	2
5549	14	Aluminum / Vinyl	1	1924	1772	1	5	1
5550	14	Aluminum / Vinyl	1	1925	1474	1	3	2
5551	14	Aluminum / Vinyl	1	1926	1165	1	3	1
5552	14	Aluminum / Vinyl	1	1950	768	1	2	1
5553	14	Stucco	1.5	1889	1800	1	4	2
5554	14	Aluminum / Vinyl	1.5	1890	1766	1	3	2
5555	14	Aluminum / Vinyl	1	1910	1333	1	3	2
5556	14	Aluminum / Vinyl	1.5	1919	1247	1	3	2
5557	14	Aluminum / Vinyl	1	1898	1187	1	3	1
5558	14	Aluminum / Vinyl	1.5	1926	934	1	2	1
5560	15	Aluminum / Vinyl	1	1917	1863	1	3	2
5561	15	Fiber-Cement	1	2010	2008	1	4	2
5562	1	Prem Wood	1.5	1915	1386	1	4	2
5563	1	Aluminum / Vinyl	2	1923	1357	1	3	1
5564	1	Aluminum / Vinyl	1	1989	1548	1	3	1
5565	2	Brick	1	1953	1230	1	3	1
5566	2	Aluminum / Vinyl	1	1953	1207	1	3	1
5567	2	Brick	2	1961	2768	2	6	2
5568	2	Aluminum / Vinyl	1	1954	1256	1	3	1
5569	2	Aluminum / Vinyl	1	1957	909	1	3	1
5570	2	Brick	2	1953	2880	3	5	3
5571	3	Aluminum / Vinyl	1	1890	1000	1	2	1
5572	3	Aluminum / Vinyl	2	1897	2468	2	2	2
5573	3	Stone	2	1930	4517	1	5	3
5574	3	Masonry / Frame	2	1912	3605	1	7	2
5575	3	Masonry / Frame	2	1913	1795	1	4	1
5576	3	Aluminum / Vinyl	1	1875	1484	1	2	1
5577	3	Aluminum / Vinyl	1	1925	1152	1	2	1
5578	3	Aluminum / Vinyl	1	1904	1144	1	3	1
5579	3	Prem Wood	1.5	1885	1042	1	2	1
5580	3	Brick	2	1922	3858	1	5	3

5581	3	Masonry / Frame	2	1910	3795	1	5	3
5582	4	Frame	2	1904	1786	1	4	2
5583	5	Aluminum / Vinyl	1.5	1950	1402	1	3	1
5584	5	Brick	1	1952	1354	1	3	1
5585	5	Aluminum / Vinyl	1	1952	1351	1	4	2
5586	5	Aluminum / Vinyl	1	1951	1275	1	3	1
5587	5	Block	1	1948	1267	1	3	1
5588	5	Brick	1	1950	1259	1	3	2
5589	5	Brick	1	1949	1246	1	3	1
5590	5	Aluminum / Vinyl	1	1952	1235	1	4	2
5591	5	Aluminum / Vinyl	1	1951	1209	1	4	1
5592	5	Aluminum / Vinyl	1	1951	1172	1	3	1
5593	5	Aluminum / Vinyl	1	1952	1089	1	3	1
5594	5	Brick	1	1946	1087	1	3	1
5595	5	Aluminum / Vinyl	1	1950	988	1	3	1
5596	5	Masonry / Frame	2	1952	1680	1	3	1
5597	5	Aluminum / Vinyl	2	1941	1486	1	3	1
5598	5	Brick	2	1969	2668	2	6	2
5599	5	Brick	2	1957	2234	2	6	2
5600	5	Brick	1	1956	1269	1	4	1
5601	5	Aluminum / Vinyl	1	1952	1138	1	3	2
5602	5	Brick	1	1960	1117	1	2	1
5603	5	Brick	1	1956	1112	1	3	1
5604	5	Aluminum / Vinyl	1	1955	1028	1	3	1
5605	5	Aluminum / Vinyl	1	1954	984	1	3	2
5606	5	Aluminum / Vinyl	1	1949	912	1	3	1
5607	5	Aluminum / Vinyl	1	1949	842	1	2	1
5608	6	Aluminum / Vinyl	2	1895	2833	1	6	2
5609	6	Aluminum / Vinyl	1	1927	1200	1	3	2
5610	6	Aluminum / Vinyl	1.5	1915	1779	1	5	2
5611	6	Aluminum / Vinyl	2	1930	1500	1	3	1
5612	7	Aluminum / Vinyl	1	1940	1219	1	3	1
5613	7	Aluminum / Vinyl	2	1924	3056	2	6	2
5614	7	Stone	2	1936	2302	2	4	2
5615	7	Aluminum / Vinyl	1	1927	1576	1	3	1
5616	7	Brick	1	1927	1538	1	3	2
5617	7	Brick	2	1933	1886	1	2	1
5618	8	Frame	1	1890	1320	1	4	1
5619	8	Aluminum / Vinyl	2	1916	2260	2	4	2
5620	8	Aluminum / Vinyl	2	1908	1502	1	4	1
5621	8	Aluminum / Vinyl	1	1910	1110	1	3	1
5622	9	Aluminum / Vinyl	2	2008	2190	1	3	2
5623	9	Frame	2	1966	2108	1	4	2

5624	9	Frame	2	1968	1636	1	4	1
5625	9	Aluminum / Vinyl	1	1964	1227	1	3	1
5626	9	Aluminum / Vinyl	1	1958	1119	1	3	1
5627	9	Aluminum / Vinyl	1	1957	985	1	3	1
5628	9	Aluminum / Vinyl	1	1952	864	1	3	1
5629	10	Aluminum / Vinyl	1.5	1942	1715	1	4	2
5630	10	Brick	1	1938	1479	1	4	2
5631	10	Brick	1	1949	1296	1	3	1
5632	10	Aluminum / Vinyl	1	1954	1223	1	3	1
5633	10	Aluminum / Vinyl	1	1955	1024	1	3	1
5634	10	Aluminum / Vinyl	1	1953	965	1	3	1
5635	10	Stone	2	1946	1982	1	3	1
5636	10	Masonry / Frame	2	1956	1873	1	3	1
5637	10	Aluminum / Vinyl	1.5	1916	1658	1	3	1
5638	10	Aluminum / Vinyl	2	1945	1260	1	3	1
5639	10	Frame	2	1912	3012	2	6	2
5640	10	Brick	1	1930	2099	1	4	4
5641	10	Stucco	1.5	1915	2091	1	4	2
5642	10	Brick	1.5	1927	1980	1	4	2
5643	10	Brick	1	1928	1944	1	3	2
5644	10	Brick	1	1925	1715	1	4	1
5645	10	Brick	1	1927	1633	1	3	1
5646	10	Aluminum / Vinyl	1	1926	1462	1	3	1
5647	10	Aluminum / Vinyl	1	1953	918	1	3	1
5648	10	Aluminum / Vinyl	2	1920	1464	1	3	2
5649	10	Aluminum / Vinyl	2	1926	1444	1	3	2
5650	11	Stucco	1.5	1955	2580	1	4	2
5651	11	Brick	1.5	1937	1751	1	3	1
5652	11	Brick	1.5	1952	1395	1	4	1
5653	11	Aluminum / Vinyl	1	1938	1157	1	4	1
5654	11	Brick	1	1950	1148	1	3	1
5655	11	Aluminum / Vinyl	1	1951	1096	1	3	1
5656	11	Brick	1	1949	1044	1	2	1
5657	11	Aluminum / Vinyl	1	1922	999	1	3	1
5658	11	Aluminum / Vinyl	2	1959	2174	1	4	2
5659	11	Aluminum / Vinyl	2	1940	1256	1	3	1
5660	11	Stone	1.5	1952	1977	2	4	2
5661	11	Brick	1.5	1942	1636	2	4	2
5662	11	Aluminum / Vinyl	1	1928	1452	1	4	1
5663	11	Aluminum / Vinyl	1	1953	1296	1	3	1
5664	11	Frame	1	1964	1292	1	4	1
5665	11	Brick	1	1959	1181	1	3	1
5666	11	Aluminum / Vinyl	1	1954	1158	1	3	1

5667	11	Brick	1	1954	1070	1	3	1
5668	11	Aluminum / Vinyl	1	1954	1034	1	3	1
5669	11	Brick	1	1955	1013	1	2	1
5670	11	Aluminum / Vinyl	1	1954	882	1	3	1
5671	11	Brick	1	1958	1845	1	4	2
5672	12	Frame	1.5	1885	1445	2	4	2
5673	13	Aluminum / Vinyl	1	1941	1436	1	3	1
5674	13	Aluminum / Vinyl	1	1947	1294	1	3	1
5675	13	Aluminum / Vinyl	1	1948	1154	1	3	2
5676	13	Aluminum / Vinyl	1	1943	1008	1	3	1
5677	13	Aluminum / Vinyl	2	1990	1856	1	2	3
5678	13	Aluminum / Vinyl	2	1957	2237	2	6	2
5679	13	Brick	2	1957	2224	2	5	2
5680	13	Brick	1	1961	1660	1	3	1
5681	13	Frame	1	1956	1650	1	3	2
5682	13	Aluminum / Vinyl	1	1973	1465	1	3	1
5683	13	Brick	1	1953	1188	1	3	2
5684	13	Aluminum / Vinyl	1	1959	1181	1	3	1
5685	13	Brick	1	1956	1150	1	3	2
5686	13	Stone	1	1951	967	1	3	1
5687	13	Brick	1	1932	1515	1	3	2
5688	13	Aluminum / Vinyl	1	1918	1410	1	4	1
5689	14	Stone	1.5	1948	1717	1	3	3
5690	14	Frame	1	1954	1273	1	3	2
5691	14	Aluminum / Vinyl	1	1953	1128	1	3	1
5692	14	Aluminum / Vinyl	2	1915	2745	2	5	3
5693	14	Aluminum / Vinyl	1.5	1928	1980	2	5	2
5694	14	Aluminum / Vinyl	1.5	1927	1900	2	4	2
5695	14	Aluminum / Vinyl	1.5	1925	1817	2	4	2
5696	14	Aluminum / Vinyl	1.5	1915	1892	1	4	2
5697	14	Stucco	1	1911	1294	1	3	2
5698	14	Aluminum / Vinyl	1	1925	1223	1	3	2
5699	14	Aluminum / Vinyl	1	1929	1198	1	3	1
5700	14	Aluminum / Vinyl	1	1923	1178	1	3	1
5701	14	Aluminum / Vinyl	1	1922	1060	1	3	1
5702	14	Aluminum / Vinyl	1	1954	1353	1	3	1
5703	14	Aluminum / Vinyl	1	1951	884	1	2	1
5704	14	Brick	1	1955	878	1	2	1
5705	14	Brick	1	1956	874	1	2	1
5706	14	Aluminum / Vinyl	1	1951	867	1	2	1
5707	14	Aluminum / Vinyl	1	1953	704	1	2	1
5708	14	Aluminum / Vinyl	2	2011	1785	1	2	3
5709	14	Aluminum / Vinyl	1.5	1889	1656	1	3	2

5710	14 Aluminum / Vinyl	1.5	1919	1414	1	4	2
5711	14 Aluminum / Vinyl	1	1920	1392	1	4	1
5712	14 Aluminum / Vinyl	1.5	1916	1305	1	3	1
5713	14 Aluminum / Vinyl	1	1887	1158	1	3	1
5714	14 Aluminum / Vinyl	1	1905	951	1	2	1
5715	15 Aluminum / Vinyl	1	1997	1588	1	4	2
5716	15 Aluminum / Vinyl	2	1913	2464	2	6	2
5717	15 Aluminum / Vinyl	1.5	1901	1741	1	3	1
5718	15 Frame	1	1894	1401	1	5	1
5719	15 Aluminum / Vinyl	1	1890	1100	1	3	1
5720	1 Brick	1	1947	1538	1	3	1
5721	1 Brick	1	1956	1174	1	3	1
5722	2 Brick	1	1952	1199	1	3	2
5723	2 Brick	1	1958	1017	1	2	1
5724	2 Aluminum / Vinyl	1	1961	1406	1	3	1
5725	2 Aluminum / Vinyl	1	1948	1091	1	3	1
5726	2 Brick	1	1958	1043	1	3	1
5727	3 Stucco	2	1913	2918	2	6	2
5728	3 Aluminum / Vinyl	2	1913	2362	2	4	3
5729	3 Aluminum / Vinyl	2	1894	1936	2	6	2
5730	3 Aluminum / Vinyl	1	1927	1035	1	3	1
5731	3 Stucco	2	1911	3553	1	6	3
5732	3 Stucco	2	1916	3097	1	6	3
5733	3 Frame	2	1889	2552	1	4	1
5734	3 Masonry / Frame	2	1911	1950	1	4	1
5735	3 Frame	2	1894	1924	1	3	1
5736	3 Frame	2	1902	1672	1	4	1
5737	3 Aluminum / Vinyl	1	1893	1610	1	4	1
5738	3 Frame	1	1890	1443	1	3	2
5739	3 Aluminum / Vinyl	1	1900	1382	1	3	2
5740	3 Frame	1	1894	1246	1	3	2
5741	3 Brick	2	1922	4733	1	6	>4
5742	5 Aluminum / Vinyl	1	1971	1566	1	4	1
5743	5 Aluminum / Vinyl	1	1950	1447	1	4	1
5744	5 Brick	1	1951	1386	1	4	1
5745	5 Aluminum / Vinyl	1	1948	1338	1	3	1
5746	5 Brick	1	1952	1336	1	3	1
5747	5 Aluminum / Vinyl	1.5	1952	1332	1	3	1
5748	5 Brick	1	1950	1329	1	3	1
5749	5 Aluminum / Vinyl	1	1950	1308	1	3	1
5750	5 Masonry / Frame	1	1959	1304	1	3	1
5751	5 Brick	1	1951	1273	1	3	1
5752	5 Aluminum / Vinyl	1	1949	1029	1	4	1

5753	5 Aluminum / Vinyl	2	2011	3110	1	5	3
5754	5 Brick	2	1948	2376	2	4	2
5755	5 Masonry / Frame	1.5	1957	2045	2	4	2
5756	5 Stone	1	1954	1415	1	3	2
5757	5 Stone	1	1956	1405	1	3	1
5758	5 Brick	1	1957	1288	1	3	1
5759	5 Brick	1	1962	1283	1	3	1
5760	5 Brick	1	1952	1268	1	2	1
5761	5 Brick	1	1959	1197	1	3	1
5762	5 Aluminum / Vinyl	1	1954	1168	1	3	1
5763	5 Aluminum / Vinyl	1	1958	1163	1	2	1
5764	5 Aluminum / Vinyl	1	1957	1163	1	3	1
5765	5 Brick	1	1954	1051	1	3	1
5766	5 Aluminum / Vinyl	1	1955	1008	1	3	1
5767	5 Frame	1	1952	873	1	2	1
5768	5 Aluminum / Vinyl	1	1950	828	1	2	1
5769	6 Brick	1.5	1929	2133	2	4	2
5770	6 Aluminum / Vinyl	2	1890	2013	2	4	2
5771	6 Aluminum / Vinyl	2	1890	1717	1	4	2
5773	7 Fiber-Cement	2	2003	1908	1	4	2
5774	7 Frame	1	1926	1453	1	5	1
5775	8 Frame	1	1925	850	1	2	1
5776	8 Aluminum / Vinyl	1	1896	1550	1	4	2
5777	8 Frame	1.5	1912	1383	1	3	1
5778	9 Aluminum / Vinyl	1	1954	1111	1	3	1
5779	9 Aluminum / Vinyl	2	2004	2016	1	3	2
5780	9 Aluminum / Vinyl	2	1969	1743	1	4	1
5781	9 Frame	2	1980	1445	1	3	1
5782	9 Aluminum / Vinyl	1	1958	1322	1	3	1
5783	9 Aluminum / Vinyl	1	1972	1134	1	3	1
5784	9 Aluminum / Vinyl	1	1964	1054	1	3	1
5785	9 Brick	1	1960	1014	1	3	1
5786	9 Frame	1	1963	1006	1	3	1
5787	9 Frame	1	1965	1006	1	3	1
5788	9 Aluminum / Vinyl	1	1974	906	1	3	1
5789	9 Aluminum / Vinyl	1	1985	1668	1	3	1
5790	10 Frame	1	1951	1410	1	3	2
5791	10 Stone	1	1951	1391	1	4	2
5792	10 Aluminum / Vinyl	1	1949	1114	1	3	1
5793	10 Brick	2	1938	1608	1	3	1
5794	10 Frame	2	1925	1536	1	3	2
5795	10 Frame	1	1925	720	1	1	1
5796	10 Aluminum / Vinyl	2	1930	2642	2	4	2

5797	10	Aluminum / Vinyl	1.5	1915	2220	1	4	1
5798	10	Aluminum / Vinyl	1	1922	1800	1	3	1
5799	10	Stucco	1	1918	1589	1	4	1
5800	10	Aluminum / Vinyl	1	1928	1584	1	4	1
5801	10	Aluminum / Vinyl	1	1925	1332	1	3	1
5802	10	Aluminum / Vinyl	1	1915	1296	1	4	2
5803	10	Frame	1	1925	1158	1	4	2
5804	10	Aluminum / Vinyl	1	1922	1125	1	3	1
5805	10	Aluminum / Vinyl	1.5	1923	1050	1	2	1
5806	10	Aluminum / Vinyl	1	1925	932	1	2	2
5807	10	Brick	1	1926	1449	1	2	2
5808	10	Aluminum / Vinyl	1	1969	1132	1	2	1
5809	10	Brick	1	1953	937	1	3	1
5810	10	Brick	1	1931	1548	1	3	1
5811	11	Stone	1.5	1942	1670	1	3	1
5812	11	Brick	1	1950	1450	1	4	2
5813	11	Aluminum / Vinyl	1	1938	1146	1	2	1
5814	11	Aluminum / Vinyl	1	1949	1072	1	2	2
5815	11	Aluminum / Vinyl	1	1942	1001	1	3	1
5816	11	Aluminum / Vinyl	1	1940	975	1	3	1
5817	11	Stucco	1	1938	928	1	3	1
5818	11	Aluminum / Vinyl	2	1958	2228	1	3	1
5819	11	Aluminum / Vinyl	2	2004	2174	1	3	2
5820	11	Aluminum / Vinyl	1.5	1923	1979	2	5	2
5821	11	Brick	1.5	1966	2274	2	5	2
5822	11	Brick	1.5	1961	1960	2	5	2
5823	11	Aluminum / Vinyl	1.5	1950	1669	2	3	2
5824	11	Brick	2	1932	2225	2	4	2
5825	11	Aluminum / Vinyl	1	1929	1653	1	4	2
5826	11	Brick	1	1962	1952	1	3	2
5827	11	Brick	1	1958	1524	1	3	1
5828	11	Brick	1	1962	1342	1	3	1
5829	11	Aluminum / Vinyl	1	1957	1137	1	3	1
5830	11	Brick	1	1954	1120	1	3	1
5831	11	Aluminum / Vinyl	1	1956	1073	1	3	1
5832	11	Brick	1	1956	1070	1	3	1
5833	11	Aluminum / Vinyl	1	1958	1055	1	2	2
5834	11	Aluminum / Vinyl	1	1956	1033	1	3	1
5835	11	Aluminum / Vinyl	1	1955	1020	1	3	1
5836	11	Aluminum / Vinyl	1	1955	972	1	3	2
5837	11	Aluminum / Vinyl	1	1955	867	1	3	1
5838	11	Aluminum / Vinyl	2	1990	3355	2	6	4
5840	12	Aluminum / Vinyl	1	1893	1870	2	5	2

5841	13	Brick	1	1951	1638	1	3	2
5842	13	Brick	1	1955	1619	1	4	2
5843	13	Aluminum / Vinyl	1	1946	1421	1	3	1
5844	13	Brick	1	1950	1347	1	2	1
5845	13	Brick	1	1959	1227	1	3	1
5846	13	Aluminum / Vinyl	1	1943	1008	1	3	1
5847	13	Frame	2	1984	1895	1	3	1
5848	13	Masonry / Frame	2	1977	1769	1	3	1
5849	13	Aluminum / Vinyl	2	1940	1144	1	2	1
5850	13	Masonry / Frame	2	1958	2352	2	4	2
5851	13	Masonry / Frame	2	1944	2111	2	4	2
5852	13	Aluminum / Vinyl	2	1952	2090	2	4	2
5853	13	Aluminum / Vinyl	1.5	1959	1744	2	4	2
5854	13	Stone	1.5	1952	1616	2	3	2
5855	13	Frame	1.5	1887	1919	2	5	1
5856	13	Aluminum / Vinyl	1	1929	1462	1	3	1
5857	13	Brick	1	1966	1726	1	4	2
5858	13	Brick	1	1963	1427	1	3	1
5859	13	Aluminum / Vinyl	1	1961	1411	1	4	1
5860	13	Aluminum / Vinyl	1	1976	1338	1	3	2
5861	13	Brick	1	1959	1174	1	3	1
5862	13	Aluminum / Vinyl	1	1960	1021	1	3	1
5863	13	Aluminum / Vinyl	1	1960	909	1	3	1
5864	13	Aluminum / Vinyl	1	1961	902	1	3	1
5866	13	Aluminum / Vinyl	1.5	1932	1600	1	5	2
5867	13	Aluminum / Vinyl	1.5	1925	1366	1	4	1
5868	14	Frame	1	1950	1361	1	4	1
5869	14	Aluminum / Vinyl	1	1949	1167	1	3	1
5870	14	Aluminum / Vinyl	1	1941	1150	1	2	1
5871	14	Aluminum / Vinyl	1	1951	1098	1	3	1
5872	14	Aluminum / Vinyl	1	1948	1048	1	3	1
5873	14	Aluminum / Vinyl	1	1890	1040	1	3	1
5874	14	Aluminum / Vinyl	1.5	1926	2100	2	4	2
5875	14	Aluminum / Vinyl	1	1895	1951	2	6	2
5876	14	Aluminum / Vinyl	1	1926	1726	1	3	2
5877	14	Aluminum / Vinyl	1	1925	1621	1	4	1
5878	14	Aluminum / Vinyl	1	1926	1425	1	4	2
5879	14	Aluminum / Vinyl	1	1919	1386	1	4	2
5881	14	Aluminum / Vinyl	1	1929	1164	1	3	1
5882	14	Aluminum / Vinyl	1	1919	848	1	3	1
5883	14	Brick	1	1961	984	1	3	1
5884	14	Aluminum / Vinyl	1	1947	784	1	2	1
5885	14	Aluminum / Vinyl	2	1915	1768	1	2	1

5886	14	Stucco	2	1913	1373	1	2	1
5887	14	Aluminum / Vinyl	1	1918	1368	1	2	1
5888	14	Aluminum / Vinyl	1	1911	997	1	2	1
5889	15	Aluminum / Vinyl	2	1918	2963	2	6	2
5890	15	Aluminum / Vinyl	2	1922	2712	2	4	2
5891	15	Brick	1	1927	2971	1	5	3
5892	15	Aluminum / Vinyl	1	1921	1407	1	4	1
5893	1	Aluminum / Vinyl	1	1940	1359	1	3	1
5894	1	Frame	1	1952	672	1	2	1
5895	2	Aluminum / Vinyl	1.5	1993	2324	1	3	2
5896	2	Aluminum / Vinyl	2	1961	2070	2	6	2
5897	2	Aluminum / Vinyl	1	1974	1959	1	4	2
5898	2	Stone	1	1954	1298	1	3	2
5899	2	Aluminum / Vinyl	1	1955	988	1	3	2
5900	2	Aluminum / Vinyl	1	1956	963	1	3	1
5901	2	Brick	1	1958	888	1	2	1
5902	2	Aluminum / Vinyl	1	1932	1231	1	3	1
5903	3	Stucco	1.5	1918	1305	1	2	1
5904	3	Masonry / Frame	2	1907	3809	1	4	2
5905	3	Aluminum / Vinyl	2	1905	2744	1	5	2
5906	3	Brick	2	1910	2694	1	5	2
5907	3	Stucco	2	1909	2629	1	5	2
5908	3	Masonry / Frame	2	1910	2414	1	3	1
5909	3	Masonry / Frame	2	1907	2358	1	4	2
5910	3	Stucco	2	1916	1937	1	4	1
5911	3	Aluminum / Vinyl	2	1896	1707	1	3	1
5912	3	Aluminum / Vinyl	1.5	1897	1345	1	4	2
5913	5	Stone	1	1949	2254	1	5	2
5914	5	Brick	1	1950	1400	1	4	2
5915	5	Brick	1	1956	1304	1	3	1
5916	5	Stone	1.5	1948	1301	1	3	1
5917	5	Frame	1	1950	1298	1	4	1
5918	5	Brick	1	1952	1167	1	3	1
5919	5	Brick	1	1950	1164	1	3	1
5920	5	Frame	1	1950	1149	1	3	1
5921	5	Aluminum / Vinyl	1	1951	1119	1	3	1
5922	5	Aluminum / Vinyl	1	1939	1049	1	2	1
5923	5	Aluminum / Vinyl	1	1950	846	1	3	1
5924	5	Aluminum / Vinyl	2	1980	2248	1	4	2
5925	5	Masonry / Frame	2	1955	2064	2	4	2
5926	5	Frame	1	1965	1865	1	3	2
5927	5	Frame	1	1965	1750	1	3	1
5928	5	Brick	1	1962	1225	1	3	1

5929	5	Brick	1	1957	1183	1	3	1
5930	5	Stone	1	1951	1147	1	3	1
5931	5	Aluminum / Vinyl	1	1950	1103	1	2	1
5932	5	Aluminum / Vinyl	1	1952	1084	1	3	1
5933	5	Aluminum / Vinyl	1	1963	1080	1	3	1
5934	5	Aluminum / Vinyl	1	1955	1008	1	3	1
5935	5	Aluminum / Vinyl	1	1953	977	1	3	2
5937	5	Brick	1	1953	952	1	2	1
5938	5	Aluminum / Vinyl	1	1949	915	1	2	1
5939	5	Aluminum / Vinyl	1	1951	772	1	2	1
5940	6	Frame	1.5	1922	2028	2	4	2
5941	6	Aluminum / Vinyl	1.5	1894	1629	2	4	2
5942	6	Aluminum / Vinyl	1	1925	1440	1	4	1
5943	6	Frame	2	1898	2572	1	4	2
5944	6	Aluminum / Vinyl	1.5	1880	1752	1	3	0
5945	7	Frame	1.5	1950	1336	1	4	2
5946	7	Brick	1	1951	1335	1	3	1
5947	7	Brick	2	1931	1734	1	4	2
5948	7	Aluminum / Vinyl	1.5	1931	1574	1	3	2
5949	7	Aluminum / Vinyl	1.5	1880	1415	1	5	2
5950	8	Aluminum / Vinyl	1.5	1907	1678	2	3	2
5951	8	Frame	1.5	1889	1645	1	4	2
5952	8	Aluminum / Vinyl	1.5	1906	1402	1	4	2
5953	8	Aluminum / Vinyl	1.5	1922	1197	1	3	1
5954	9	Aluminum / Vinyl	1	1952	990	1	4	1
5955	9	Fiber-Cement	2	1994	2325	1	3	2
5956	9	Aluminum / Vinyl	2	2008	2055	1	4	2
5957	9	Aluminum / Vinyl	1	1972	1210	1	3	1
5958	9	Aluminum / Vinyl	1	1965	1147	1	3	1
5959	9	Aluminum / Vinyl	1	1961	1041	1	3	1
5960	9	Frame	1	1959	898	1	3	1
5961	9	Frame	1	1957	1608	1	4	1
5962	9	Aluminum / Vinyl	1	1992	1547	1	3	2
5963	10	Stone	1.5	1941	1794	1	2	2
5964	10	Aluminum / Vinyl	1	1950	1482	1	3	1
5965	10	Brick	1	1949	1453	1	4	2
5966	10	Brick	1	1948	1395	1	4	1
5967	10	Aluminum / Vinyl	1	1953	1380	1	3	1
5968	10	Stone	1	1951	1290	1	3	2
5969	10	Brick	1	1940	1248	1	3	2
5970	10	Aluminum / Vinyl	1.5	1940	1153	1	3	1
5971	10	Aluminum / Vinyl	2	1948	1300	1	3	1
5972	10	Brick	1.5	1931	2553	2	4	2

5973	10	Aluminum / Vinyl	2	1923	2486	2	6	2
5974	10	Aluminum / Vinyl	2	1928	2364	2	5	2
5975	10	Stone	1.5	1935	2129	2	4	2
5976	10	Aluminum / Vinyl	1.5	1929	1386	2	3	2
5977	10	Aluminum / Vinyl	1.5	1894	1654	2	4	2
5978	10	Brick	1	1926	1863	1	3	2
5979	10	Aluminum / Vinyl	1.5	1926	1811	1	3	2
5980	10	Frame	1	1925	1734	1	4	2
5981	10	Brick	1	1927	1727	1	3	2
5982	10	Aluminum / Vinyl	1	1921	1719	1	3	1
5983	10	Aluminum / Vinyl	1	1925	1556	1	3	2
5984	10	Aluminum / Vinyl	1	1928	1445	1	4	2
5985	10	Aluminum / Vinyl	1	1925	1398	1	3	2
5986	10	Aluminum / Vinyl	1	1928	1373	1	4	1
5987	10	Brick	1	1965	1636	1	3	1
5988	10	Frame	1	1952	1056	1	3	2
5989	10	Brick	1	1948	788	1	2	1
5990	10	Brick	1.5	1930	1860	1	3	1
5991	10	Aluminum / Vinyl	1	1926	1318	1	3	0
5992	10	Aluminum / Vinyl	1	1927	691	1	2	1
5993	11	Stone	1	1936	1702	1	3	2
5994	11	Aluminum / Vinyl	1	1961	1098	1	3	1
5995	11	Aluminum / Vinyl	1	1942	1038	1	3	1
5996	11	Masonry / Frame	2	1953	1896	1	6	2
5997	11	Aluminum / Vinyl	2	1953	1554	1	3	1
5998	11	Aluminum / Vinyl	2	1938	1032	1	2	1
5999	11	Aluminum / Vinyl	2	1957	1946	2	4	2
6000	11	Brick	2	1954	1925	2	4	2
6001	11	Brick	2	1865	2274	2	4	2
6002	11	Frame	1	1987	1581	1	3	2
6003	11	Brick	1	1952	1305	1	2	1
6004	11	Brick	1	1959	1235	1	3	1
6005	11	Brick	1	1960	1201	1	3	1
6006	11	Aluminum / Vinyl	1	1965	1110	1	3	1
6007	11	Brick	1	1965	1057	1	3	1
6008	11	Aluminum / Vinyl	1	1958	1018	1	3	1
6009	11	Brick	1	1955	1013	1	3	1
6010	11	Brick	1	1959	1004	1	2	1
6011	11	Aluminum / Vinyl	1	1957	915	1	3	1
6012	11	Aluminum / Vinyl	1	1953	879	1	3	1
6013	11	Aluminum / Vinyl	1	1953	879	1	3	1
6014	11	Aluminum / Vinyl	1	1953	864	1	3	1
6015	12	Frame	2	1918	1796	2	4	2

6016	12	Aluminum / Vinyl	1.5	1890	1828	2	5	2
6017	12	Stone	1.5	1940	2315	1	5	2
6018	12	Brick	2	1895	3627	>3	>8	3
6019	13	Brick	1.5	1951	1822	1	4	2
6020	13	Brick	1	1976	1601	1	3	2
6021	13	Stucco	1	1951	1453	1	4	2
6022	13	Aluminum / Vinyl	1.5	1939	1338	1	3	1
6023	13	Brick	1	1949	1327	1	3	1
6024	13	Frame	1	1951	1300	1	3	1
6025	13	Brick	1	1964	1036	1	2	1
6026	13	Brick	1	1953	826	1	2	1
6027	13	Brick	1	1951	825	1	2	1
6028	13	Aluminum / Vinyl	1	1948	805	1	2	1
6029	13	Aluminum / Vinyl	2	1957	2098	2	6	2
6030	13	Aluminum / Vinyl	1.5	1959	1738	2	4	3
6031	13	Brick	1	1948	1497	2	3	2
6032	13	Aluminum / Vinyl	1.5	1923	1660	1	4	2
6033	13	Frame	1	1923	1653	1	4	2
6034	13	Brick	1	1966	1678	1	3	1
6035	13	Brick	1	1964	1116	1	3	1
6036	13	Aluminum / Vinyl	1	1959	936	1	3	1
6037	13	Aluminum / Vinyl	1	1900	1199	1	2	1
6038	14	Aluminum / Vinyl	1	1947	1468	1	3	2
6040	14	Fiber-Cement	>2	2005	3504	1	4	3
6041	14	Frame	1.5	1895	1190	1	3	1
6042	14	Aluminum / Vinyl	1	1890	592	1	1	1
6043	14	Aluminum / Vinyl	2	1923	2217	2	5	2
6044	14	Aluminum / Vinyl	2	1913	1968	2	5	2
6045	14	Aluminum / Vinyl	1.5	1900	1840	2	4	2
6046	14	Aluminum / Vinyl	1.5	1917	1582	1	3	2
6047	14	Aluminum / Vinyl	1	1925	1573	1	3	2
6048	14	Stucco	1	1922	1380	1	3	2
6049	14	Brick	1	1956	1505	1	3	1
6050	14	Aluminum / Vinyl	1	1950	923	1	3	1
6051	14	Aluminum / Vinyl	1	1947	826	1	2	1
6052	14	Brick	1.5	1918	1521	1	3	1
6053	14	Aluminum / Vinyl	1	1919	1290	1	3	1
6054	14	Aluminum / Vinyl	1	1895	1276	1	4	2
6055	14	Aluminum / Vinyl	2	1931	3265	3	7	3
6056	15	Aluminum / Vinyl	2	1883	2378	2	4	2
6057	15	Aluminum / Vinyl	1.5	1890	1746	2	5	2
6058	15	Brick	2	1905	2455	1	3	1
6059	1	Masonry / Frame	2	1931	2770	2	6	2

6060	1	Brick	1	1928	1706	1	4	1
6061	1	Aluminum / Vinyl	1	1955	1082	1	3	1
6062	2	Aluminum / Vinyl	1	1997	1360	1	3	2
6063	2	Aluminum / Vinyl	1	1955	1384	1	3	1
6064	2	Aluminum / Vinyl	1	1957	1084	1	3	2
6065	2	Aluminum / Vinyl	1	1959	1226	1	3	1
6066	2	Stone	1	1950	1147	1	3	1
6067	2	Brick	1	1962	1121	1	3	1
6068	2	Brick	1	1961	1071	1	3	1
6069	2	Brick	1	1958	1019	1	3	1
6070	2	Aluminum / Vinyl	1	1947	844	1	2	2
6071	2	Aluminum / Vinyl	1	1956	784	1	2	1
6072	2	Aluminum / Vinyl	1	1955	756	1	2	1
6073	2	Aluminum / Vinyl	1	1955	1486	1	3	1
6074	3	Frame	1	1956	1488	1	3	1
6075	3	Aluminum / Vinyl	1	1892	1662	2	3	2
6076	3	Aluminum / Vinyl	1	1901	900	1	1	1
6077	3	Frame	2	1924	2940	2	6	2
6078	3	Frame	2	1916	2420	2	4	2
6079	3	Stucco	2	1922	2047	2	4	2
6080	3	Aluminum / Vinyl	2	1895	2310	2	4	2
6081	3	Brick	2	1916	4562	1	6	3
6082	3	Aluminum / Vinyl	2	1898	3185	2	4	2
6083	3	Brick	2	1923	3137	1	4	2
6084	3	Brick	2	1906	2403	1	4	1
6085	3	Frame	2	1905	2328	1	4	2
6086	3	Aluminum / Vinyl	2	1912	1749	1	4	1
6087	4	Aluminum / Vinyl	2	1970	1471	1	4	1
6088	4	Frame	2	1902	3685	2	5	3
6089	4	Aluminum / Vinyl	2	1910	1661	1	3	1
6090	5	Brick	1	1953	1609	1	4	2
6091	5	Aluminum / Vinyl	1	1955	1477	1	3	1
6092	5	Brick	1	1949	1467	1	3	1
6094	5	Aluminum / Vinyl	1.5	1950	1251	1	3	2
6095	5	Aluminum / Vinyl	1	1953	1181	1	3	1
6096	5	Brick	1	1947	1158	1	2	1
6097	5	Aluminum / Vinyl	1	1950	1105	1	3	1
6098	5	Aluminum / Vinyl	1	1950	1092	1	3	3
6099	5	Aluminum / Vinyl	1	1953	1027	1	3	1
6100	5	Masonry / Frame	2	1952	1795	1	3	1
6101	5	Aluminum / Vinyl	2	1955	1419	1	3	1
6102	5	Aluminum / Vinyl	2	1939	1248	1	2	1
6103	5	Aluminum / Vinyl	2	1967	2100	2	6	2

6104	5	Aluminum / Vinyl	1.5	1963	2018	2	5	2
6105	5	Brick	1	1952	1516	1	3	1
6106	5	Frame	1	1964	1491	1	3	1
6107	5	Stone	1	1958	1252	1	3	1
6108	5	Brick	1	1960	1238	1	3	1
6109	5	Aluminum / Vinyl	1	1964	1212	1	3	1
6110	5	Aluminum / Vinyl	1	1961	1024	1	3	1
6111	5	Aluminum / Vinyl	1	1956	1019	1	2	2
6112	5	Aluminum / Vinyl	1	1956	1014	1	3	1
6113	5	Aluminum / Vinyl	1	1957	987	1	3	1
6114	5	Brick	1	1956	965	1	3	1
6115	5	Aluminum / Vinyl	1	1952	912	1	3	1
6116	5	Aluminum / Vinyl	1	1952	910	1	3	1
6117	5	Aluminum / Vinyl	1	1952	768	1	2	1
6118	6	Aluminum / Vinyl	2	2004	2366	1	3	2
6119	6	Aluminum / Vinyl	2	1924	2192	2	4	2
6120	6	Brick	1	1927	2212	1	5	2
6121	6	Aluminum / Vinyl	1.5	1881	1871	1	3	2
6122	7	Brick	2	1932	2696	2	5	3
6123	7	Aluminum / Vinyl	2	1924	2422	2	4	2
6124	7	Aluminum / Vinyl	1	1920	1781	1	5	1
6125	7	Aluminum / Vinyl	1	1932	1233	1	3	1
6126	7	Brick	1.5	1940	1802	1	3	1
6127	8	Frame	2	1922	2557	2	6	2
6128	8	Aluminum / Vinyl	1.5	1885	2071	2	5	3
6129	9	Frame	1	1957	1181	1	3	1
6130	9	Aluminum / Vinyl	1	1962	1001	1	3	1
6131	10	Brick	1	1952	1346	1	4	1
6132	10	Aluminum / Vinyl	1	1951	1134	1	3	2
6133	10	Brick	1	1941	1031	1	3	1
6134	10	Brick	1	1950	932	1	2	1
6135	10	Masonry / Frame	2	1941	1546	1	3	1
6136	10	Masonry / Frame	2	1941	1448	1	3	1
6137	10	Aluminum / Vinyl	2	1947	1117	1	2	1
6138	10	Brick	1.5	1928	2283	2	4	2
6139	10	Aluminum / Vinyl	1.5	1919	2012	2	4	2
6140	10	Aluminum / Vinyl	1	1919	1939	1	3	1
6141	10	Brick	2	1926	1792	1	4	2
6142	10	Aluminum / Vinyl	1	1927	1582	1	4	2
6143	10	Aluminum / Vinyl	1	1925	1458	1	3	2
6144	10	Aluminum / Vinyl	1	1923	962	1	3	1
6145	10	Brick	1	1952	1049	1	2	1
6146	10	Brick	1	1952	1035	1	2	1

6147	10	Aluminum / Vinyl	1	1953	704	1	2	1
6148	10	Stucco	1.5	1921	2090	1	5	1
6149	10	Frame	1	1918	1152	1	3	2
6150	10	Frame	1	1925	748	1	2	1
6151	11	Aluminum / Vinyl	1	1941	1448	1	4	1
6152	11	Aluminum / Vinyl	1	1925	1026	1	2	1
6153	11	Brick	1	1970	1484	1	3	1
6155	11	Brick	1	1956	1382	1	2	1
6156	11	Brick	1	1958	1191	1	3	1
6157	11	Aluminum / Vinyl	1	1960	1186	1	3	1
6158	11	Aluminum / Vinyl	1	1958	1079	1	3	1
6159	11	Aluminum / Vinyl	1	1960	946	1	2	1
6160	11	Brick	1	1956	941	1	3	1
6161	11	Stone	1	1939	924	1	2	1
6162	11	Aluminum / Vinyl	1	1949	726	1	2	1
6163	12	Aluminum / Vinyl	1	1903	1575	2	5	2
6164	13	Aluminum / Vinyl	1.5	1989	2103	1	4	2
6165	13	Brick	1	1953	1379	1	3	2
6166	13	Brick	1	1949	1217	1	3	1
6167	13	Brick	1	1947	1152	1	3	1
6168	13	Brick	1	1955	1090	1	3	2
6169	13	Aluminum / Vinyl	1	1947	923	1	3	1
6170	13	Masonry / Frame	2	1938	1569	1	3	1
6171	13	Aluminum / Vinyl	2	1959	2293	2	6	2
6172	13	Brick	1.5	1956	2016	2	5	2
6173	13	Aluminum / Vinyl	1.5	1953	1650	2	4	2
6174	13	Aluminum / Vinyl	1	1922	1333	1	2	2
6175	13	Masonry / Frame	1	1961	1863	1	3	2
6176	13	Brick	1	1981	1797	1	3	2
6177	13	Aluminum / Vinyl	1	1975	1466	1	3	1
6179	13	Aluminum / Vinyl	1	1954	1194	1	3	1
6180	13	Brick	1	1963	1090	1	3	1
6181	13	Aluminum / Vinyl	1	1969	1087	1	3	1
6182	13	Brick	1	1958	1048	1	3	1
6183	13	Brick	1	1958	998	1	3	1
6184	13	Brick	1	1964	997	1	3	1
6185	13	Aluminum / Vinyl	1	1960	994	1	3	2
6186	13	Aluminum / Vinyl	1	1958	978	1	3	1
6187	13	Stucco	1	1954	936	1	3	1
6188	13	Aluminum / Vinyl	1	1961	907	1	3	1
6189	14	Aluminum / Vinyl	1	1950	1392	1	4	2
6190	14	Aluminum / Vinyl	1	1951	1150	1	4	1
6191	14	Aluminum / Vinyl	1	1952	795	1	2	1

6192	14	Aluminum / Vinyl	2	1950	1512	1	3	1
6193	14	Brick	2	1948	1391	1	3	1
6194	14	Aluminum / Vinyl	2	1948	979	1	2	1
6195	14	Aluminum / Vinyl	1	1929	747	1	2	1
6196	14	Aluminum / Vinyl	2	1908	3403	2	6	4
6197	14	Aluminum / Vinyl	2	1893	2648	2	4	2
6198	14	Aluminum / Vinyl	2	1890	1952	2	3	2
6199	14	Aluminum / Vinyl	1.5	1896	1849	2	4	2
6200	14	Frame	1	1926	1444	1	2	1
6201	14	Brick	1	1929	1340	1	3	1
6202	14	Aluminum / Vinyl	1	1929	1194	1	3	1
6204	15	Aluminum / Vinyl	2	1919	2714	2	6	2
6205	15	Aluminum / Vinyl	1.5	1910	1713	2	3	2
6206	1	Aluminum / Vinyl	1	1951	1213	1	3	1
6207	1	Aluminum / Vinyl	1	1955	1082	1	3	1
6208	2	Brick	1	1954	1512	1	3	1
6209	2	Brick	1	1954	1204	1	4	1
6210	2	Aluminum / Vinyl	2	1957	1984	2	6	2
6211	2	Frame	1	1956	1046	1	3	1
6212	3	Frame	2	1898	3159	1	5	4
6213	3	Aluminum / Vinyl	1.5	1921	1678	2	4	2
6214	3	Brick	2	1953	2080	2	4	2
6215	3	Frame	2	1890	2224	2	4	2
6216	3	Brick	1	1890	1898	2	4	2
6217	3	Stucco	2	1917	6567	1	6	3
6218	3	Brick	2	1915	6143	1	6	3
6219	3	Brick	2	1916	3872	1	4	3
6220	3	Brick	2	1922	3365	1	5	3
6221	3	Aluminum / Vinyl	2	1904	2251	1	4	1
6222	3	Aluminum / Vinyl	2	1900	2068	1	3	2
6223	3	Frame	2	1901	1717	1	4	1
6224	3	Aluminum / Vinyl	1	1903	1465	1	3	2
6225	3	Stucco	1	1922	1371	1	3	2
6226	4	Frame	1	1848	853	1	3	1
6227	4	Aluminum / Vinyl	2	1885	2528	2	4	2
6228	5	Aluminum / Vinyl	1	1948	1226	1	3	2
6229	5	Aluminum / Vinyl	1	1942	1165	1	2	1
6230	5	Brick	1	1949	892	1	2	1
6231	5	Aluminum / Vinyl	1	1952	828	1	2	2
6232	5	Fiber-Cement	2	2002	2452	1	3	2
6233	5	Aluminum / Vinyl	2	1976	1610	1	3	1
6234	5	Aluminum / Vinyl	2	1941	1270	1	3	1
6235	5	Aluminum / Vinyl	2	1947	1205	1	3	1

6236	5 Aluminum / Vinyl	2	1956	2240	2	6	2
6237	5 Aluminum / Vinyl	1	1950	1430	1	3	1
6238	5 Brick	1	1960	1237	1	3	2
6239	5 Aluminum / Vinyl	1	1971	1204	1	4	1
6240	5 Brick	1	1956	1075	1	3	1
6241	5 Aluminum / Vinyl	1	1957	936	1	3	1
6242	7 Frame	2	1924	3280	2	7	2
6243	7 Aluminum / Vinyl	1.5	1925	1822	2	4	2
6244	7 Aluminum / Vinyl	2	1892	2028	2	4	2
6245	7 Brick	1	1929	1584	1	3	1
6246	7 Stone	1.5	1936	1647	1	3	1
6247	8 Aluminum / Vinyl	1.5	1921	1186	1	4	1
6248	8 Stucco	1	1915	1531	1	2	1
6249	8 Aluminum / Vinyl	1.5	1910	1133	1	3	2
6250	9 Aluminum / Vinyl	2	2002	1900	1	3	2
6251	9 Aluminum / Vinyl	1	1980	1609	1	3	1
6252	9 Aluminum / Vinyl	1	1968	1426	1	3	1
6253	9 Aluminum / Vinyl	1	1964	1327	1	3	1
6254	9 Aluminum / Vinyl	1	1969	1232	1	3	1
6255	9 Aluminum / Vinyl	1	1973	1194	1	3	1
6256	9 Brick	1	1956	1042	1	3	1
6257	9 Frame	1	1964	1006	1	3	1
6258	9 Brick	1	1958	953	1	3	1
6259	9 Aluminum / Vinyl	1	1992	1751	1	4	2
6261	10 Aluminum / Vinyl	1	1942	1113	1	3	1
6262	10 Brick	1	1945	1107	1	3	1
6263	10 Brick	2	1924	2334	1	4	1
6264	10 Masonry / Frame	2	1937	1751	1	3	1
6265	10 Aluminum / Vinyl	2	1928	1152	1	3	1
6266	10 Masonry / Frame	1.5	1931	2391	2	5	2
6267	10 Aluminum / Vinyl	1.5	1928	2081	2	4	2
6268	10 Frame	1.5	1924	1914	2	4	2
6269	10 Aluminum / Vinyl	1	1926	1417	1	3	2
6270	10 Aluminum / Vinyl	1	1927	1339	1	3	2
6271	10 Frame	1	1930	1318	1	3	1
6272	10 Aluminum / Vinyl	1	1955	828	1	2	1
6273	10 Aluminum / Vinyl	1	1913	1663	1	4	2
6274	10 Aluminum / Vinyl	1.5	1920	1186	1	3	1
6275	10 Frame	1.5	1912	1122	1	3	1
6276	11 Brick	1.5	1951	1883	1	4	2
6277	11 Brick	1	1941	1487	1	4	1
6278	11 Stone	1	1952	1305	1	3	2
6279	11 Aluminum / Vinyl	1	1942	1095	1	3	1

6280	11	Prem Wood	2	2003	2204	1	4	2
6281	11	Aluminum / Vinyl	1	1958	1519	1	3	1
6282	11	Stone	1	1952	1501	1	3	1
6283	11	Brick	1	1955	1392	1	3	1
6284	11	Brick	1	1957	1240	1	2	2
6285	11	Stone	1	1951	1181	1	2	1
6286	11	Brick	1	1961	1172	1	3	1
6287	11	Aluminum / Vinyl	1	1953	1158	1	3	1
6288	11	Aluminum / Vinyl	1	1966	1157	1	3	2
6289	11	Brick	1	1958	1114	1	3	2
6290	11	Aluminum / Vinyl	1	1954	1073	1	3	1
6291	11	Brick	1	1959	1052	1	2	2
6292	11	Aluminum / Vinyl	1	1957	1023	1	2	2
6293	11	Aluminum / Vinyl	1	1958	1001	1	3	1
6294	11	Frame	1	1953	985	1	3	1
6295	11	Aluminum / Vinyl	1	1955	984	1	3	1
6296	11	Aluminum / Vinyl	1	1960	931	1	3	1
6297	11	Brick	1	1949	862	1	2	1
6298	11	Aluminum / Vinyl	1	1955	793	1	2	1
6299	11	Aluminum / Vinyl	1	1950	776	1	2	1
6300	11	Aluminum / Vinyl	1	1952	759	1	2	1
6301	11	Aluminum / Vinyl	1	1937	740	1	2	1
6302	11	Aluminum / Vinyl	1	1949	726	1	2	1
6303	11	Aluminum / Vinyl	1.5	1932	870	1	3	1
6304	11	Aluminum / Vinyl	2	1966	2409	2	6	2
6305	12	Frame	1	1884	740	1	3	1
6306	12	Block	2	1906	2998	2	6	2
6307	12	Frame	2	1870	1840	2	5	2
6308	12	Aluminum / Vinyl	1	1886	976	1	4	1
6309	13	Brick	1	1949	1398	1	4	2
6310	13	Aluminum / Vinyl	1	1955	1243	1	3	1
6311	13	Aluminum / Vinyl	1	1948	1184	1	4	1
6312	13	Stone	1	1951	1045	1	3	1
6313	13	Stucco	1	1942	1027	1	3	1
6314	13	Brick	1	1957	1025	1	2	1
6315	13	Aluminum / Vinyl	2	1989	2009	1	3	1
6316	13	Brick	1	1955	1304	1	3	2
6317	13	Aluminum / Vinyl	1	1961	1275	1	4	1
6318	13	Aluminum / Vinyl	1	1936	1092	1	3	1
6319	13	Frame	1	1963	1011	1	3	2
6320	13	Aluminum / Vinyl	1	1963	999	1	3	1
6321	13	Brick	1	1956	827	1	2	1
6322	13	Aluminum / Vinyl	1	1951	707	1	2	1

6323	14	Brick	1	1947	1731	1	5	2
6324	14	Brick	1	1948	1153	1	3	2
6325	14	Aluminum / Vinyl	1	1947	1026	1	3	2
6326	14	Aluminum / Vinyl	2	1940	1528	1	3	1
6327	14	Aluminum / Vinyl	1.5	1927	2295	2	4	2
6328	14	Aluminum / Vinyl	2	1880	2106	2	4	2
6329	14	Aluminum / Vinyl	2	1922	1716	2	4	2
6330	14	Brick	1	1929	1461	1	3	1
6331	14	Brick	1	1931	1174	1	3	1
6332	14	Aluminum / Vinyl	1	1955	936	1	3	1
6333	14	Aluminum / Vinyl	1.5	1917	1636	1	4	2
6334	14	Aluminum / Vinyl	2	1911	1478	1	4	1
6335	14	Frame	1.5	1907	1415	1	4	2
6336	14	Aluminum / Vinyl	1.5	1899	1339	1	3	1
6337	1	Block	2	1949	1664	1	3	2
6338	1	Frame	1.5	1925	1342	2	4	2
6339	1	Aluminum / Vinyl	1	1928	1480	1	5	1
6340	1	Masonry / Frame	1	1953	912	1	3	1
6341	1	Aluminum / Vinyl	1	1954	728	1	2	1
6342	1	Frame	1.5	1901	1824	1	3	1
6343	1	Aluminum / Vinyl	1	1929	924	1	3	1
6344	2	Aluminum / Vinyl	1	1947	1509	1	4	2
6345	2	Aluminum / Vinyl	2	1957	2142	2	6	2
6346	2	Brick	1	1954	1176	1	3	1
6347	2	Aluminum / Vinyl	1	1960	1044	1	3	1
6348	2	Aluminum / Vinyl	1	1958	1040	1	3	1
6349	2	Brick	1	1958	1019	1	3	2
6350	2	Aluminum / Vinyl	1	1940	918	1	2	1
6351	3	Stucco	1	1900	1694	1	2	1
6352	3	Aluminum / Vinyl	1.5	1924	1952	2	4	2
6353	3	Aluminum / Vinyl	1	1890	2020	2	4	2
6354	3	Aluminum / Vinyl	2	1922	1988	2	4	2
6355	3	Stone	2	1926	4818	1	6	3
6356	3	Stucco	2	1906	2350	1	5	1
6357	3	Aluminum / Vinyl	1	1918	1450	1	3	1
6358	5	Brick	1	1945	1465	1	3	1
6359	5	Aluminum / Vinyl	1	1952	1288	1	3	2
6360	5	Brick	1	1952	1224	1	3	1
6361	5	Aluminum / Vinyl	1	1947	1221	1	2	2
6362	5	Aluminum / Vinyl	1	1952	1188	1	4	1
6363	5	Aluminum / Vinyl	1	1950	1176	1	4	1
6364	5	Aluminum / Vinyl	1	1950	1166	1	3	1
6365	5	Aluminum / Vinyl	1	1952	1163	1	4	1

6366	5 Aluminum / Vinyl	1	1950	1133	1	3	1
6367	5 Aluminum / Vinyl	1	1954	1037	1	3	1
6368	5 Aluminum / Vinyl	1	1940	1026	1	3	1
6369	5 Aluminum / Vinyl	2	1953	1422	1	3	1
6370	5 Brick	2	1950	2240	2	4	2
6371	5 Aluminum / Vinyl	2	1957	2076	2	6	2
6372	5 Aluminum / Vinyl	1	1954	1904	2	4	3
6373	5 Aluminum / Vinyl	1	1952	1486	1	3	2
6374	5 Aluminum / Vinyl	1	1957	1300	1	3	1
6375	5 Brick	1	1957	1246	1	3	1
6376	5 Brick	1	1960	1208	1	3	1
6377	5 Aluminum / Vinyl	1	1969	1136	1	3	1
6378	5 Brick	1	1956	1082	1	3	2
6379	5 Aluminum / Vinyl	1	1956	1019	1	3	1
6380	5 Aluminum / Vinyl	1	1956	997	1	3	2
6381	5 Aluminum / Vinyl	1	1952	972	1	3	1
6382	5 Aluminum / Vinyl	1	1957	963	1	3	1
6383	5 Frame	1	1957	948	1	2	2
6384	6 Frame	2	1885	3122	2	5	2
6385	6 Aluminum / Vinyl	2	1880	4091	2	6	2
6386	7 Brick	1	1936	1632	1	4	1
6387	7 Brick	2	1929	3074	2	6	2
6388	7 Masonry / Frame	2	1928	2265	2	5	2
6389	7 Stone	1	1949	916	1	2	1
6390	7 Aluminum / Vinyl	1.5	1928	1348	1	3	1
6391	7 Aluminum / Vinyl	1	1923	864	1	3	1
6392	8 Aluminum / Vinyl	2	1910	2666	2	4	2
6393	8 Aluminum / Vinyl	1	1928	1556	1	4	2
6394	8 Aluminum / Vinyl	1	1926	1263	1	3	1
6395	8 Frame	2	1895	1718	1	4	1
6396	9 Brick	1	1958	1616	1	4	2
6397	10 Aluminum / Vinyl	1.5	1951	1575	1	3	2
6398	10 Aluminum / Vinyl	1.5	1939	1573	1	3	1
6399	10 Brick	1	1947	1402	1	3	1
6400	10 Aluminum / Vinyl	1	1953	1260	1	4	1
6401	10 Aluminum / Vinyl	1	1942	1242	1	3	1
6402	10 Brick	1	1941	1199	1	3	1
6403	10 Aluminum / Vinyl	1	1950	1114	1	3	1
6404	10 Brick	2	1936	1869	1	3	1
6405	10 Aluminum / Vinyl	2	1914	1754	1	3	2
6406	10 Aluminum / Vinyl	2	1941	1641	1	3	1
6407	10 Aluminum / Vinyl	2	1921	1237	1	4	1
6408	10 Aluminum / Vinyl	2	1926	2204	2	4	2

6409	10	Aluminum / Vinyl	1.5	1925	1891	1	3	2
6410	10	Aluminum / Vinyl	1	1928	1707	1	4	2
6411	10	Aluminum / Vinyl	1	1919	1617	1	4	2
6412	10	Aluminum / Vinyl	1	1925	1570	1	4	2
6413	10	Aluminum / Vinyl	1	1922	1126	1	3	1
6414	10	Aluminum / Vinyl	1	1942	828	1	2	1
6415	10	Brick	2	1931	2000	1	3	1
6416	11	Aluminum / Vinyl	1.5	1952	2276	1	4	3
6417	11	Aluminum / Vinyl	1	1956	1320	1	4	2
6418	11	Aluminum / Vinyl	1	1953	1198	1	4	1
6419	11	Brick	1	1949	1017	1	3	1
6420	11	Aluminum / Vinyl	2	1959	1378	1	3	1
6421	11	Aluminum / Vinyl	2	1968	1264	1	3	1
6422	11	Brick	1	1929	1865	1	3	1
6423	11	Frame	1	1958	1354	1	3	1
6424	11	Aluminum / Vinyl	1	1954	1210	1	3	1
6425	11	Aluminum / Vinyl	1	1959	1122	1	3	1
6426	11	Aluminum / Vinyl	1	1963	1109	1	3	1
6427	11	Brick	1	1954	1076	1	3	2
6428	11	Aluminum / Vinyl	1	1964	1064	1	3	2
6429	11	Frame	1	1957	1038	1	3	1
6430	11	Brick	1	1954	1013	1	3	1
6431	11	Aluminum / Vinyl	1	1955	988	1	3	1
6432	11	Aluminum / Vinyl	1	1953	922	1	3	1
6433	11	Aluminum / Vinyl	1	1953	906	1	3	1
6434	11	Brick	1	1953	886	1	2	1
6435	11	Aluminum / Vinyl	1	1956	876	1	3	1
6436	11	Brick	2	1931	2200	1	4	1
6437	13	Aluminum / Vinyl	1	1947	1321	1	4	3
6438	13	Block	1	1935	922	1	2	1
6439	13	Aluminum / Vinyl	2	1997	2669	1	5	2
6440	13	Aluminum / Vinyl	1.5	1952	2232	2	4	2
6441	13	Stone	1	1964	1663	1	3	2
6442	13	Brick	1	1960	1510	1	4	2
6443	13	Brick	1	1963	1428	1	3	1
6444	13	Brick	1	1966	1298	1	3	1
6445	13	Aluminum / Vinyl	1	1958	1168	1	3	1
6446	13	Aluminum / Vinyl	1	1953	1067	1	3	1
6447	13	Aluminum / Vinyl	1	1958	1016	1	3	2
6448	13	Brick	1	1955	982	1	3	1
6449	13	Brick	1	1954	784	1	2	1
6450	14	Aluminum / Vinyl	1	1953	1296	1	3	1
6451	14	Aluminum / Vinyl	1	1949	1022	1	3	1

6452	14	Brick	1.5	1926	1777	2	4	2
6453	14	Aluminum / Vinyl	2	1893	2372	2	6	2
6454	14	Aluminum / Vinyl	1.5	1928	1699	1	3	2
6455	14	Frame	1	1924	1381	1	3	1
6456	14	Aluminum / Vinyl	1	1928	1312	1	5	1
6457	14	Aluminum / Vinyl	1	1924	1074	1	3	1
6458	14	Brick	1	1955	840	1	2	1
6459	14	Aluminum / Vinyl	1	1942	792	1	2	1
6460	14	Aluminum / Vinyl	1	1950	725	1	2	1
6461	14	Frame	1.5	1913	1610	1	4	2
6462	14	Aluminum / Vinyl	1.5	1894	1548	1	4	2
6463	14	Frame	2	1913	1544	1	4	1
6464	14	Aluminum / Vinyl	1	1925	1196	1	2	1
6465	14	Aluminum / Vinyl	1	1921	1122	1	3	1
6466	14	Aluminum / Vinyl	1	1924	850	1	1	1
6467	15	Brick	1	1921	2189	1	5	1
6468	1	Aluminum / Vinyl	1.5	1950	1401	1	4	1
6469	1	Aluminum / Vinyl	1.5	1969	1779	2	4	2
6470	1	Brick	1	1927	1507	1	3	1
6471	1	Aluminum / Vinyl	1	1950	672	1	2	1
6472	2	Brick	1	1954	1008	1	2	1
6473	2	Aluminum / Vinyl	2	1965	1970	2	6	2
6474	2	Brick	1	1956	1243	1	3	2
6475	2	Aluminum / Vinyl	1	1957	925	1	3	1
6476	3	Aluminum / Vinyl	2	1908	1496	2	4	2
6477	3	Stucco	2	1920	3037	1	5	3
6478	3	Frame	2	1892	2850	1	4	2
6479	3	Aluminum / Vinyl	2	1885	1235	1	3	1
6481	3	Frame	2	1903	3572	3	8	3
6482	3	Masonry / Frame	2	1922	3282	1	4	3
6483	4	Aluminum / Vinyl	2	1904	2191	2	5	2
6484	4	Aluminum / Vinyl	1.5	1891	2064	1	4	2
6485	5	Fiber-Cement	2	2006	2694	1	4	2
6486	5	Brick	1	1950	1832	1	4	2
6487	5	Stone	1	1952	1550	1	3	1
6488	5	Brick	1	1952	1502	1	3	1
6489	5	Aluminum / Vinyl	1	1949	1338	1	3	2
6490	5	Stone	1	1950	1223	1	2	1
6491	5	Masonry / Frame	2	1952	2027	1	4	2
6492	5	Brick	2	1967	2672	2	6	2
6493	5	Aluminum / Vinyl	1	1951	1619	1	3	1
6494	5	Brick	1	1967	1300	1	3	1
6495	5	Masonry / Frame	1	1957	1216	1	3	1

6496	5	Frame	1	1956	1131	1	3	1
6497	5	Brick	1	1962	1129	1	3	1
6498	5	Aluminum / Vinyl	1	1955	1095	1	3	1
6499	5	Aluminum / Vinyl	1	1950	1062	1	2	1
6500	5	Brick	1	1945	990	1	2	2
6501	5	Aluminum / Vinyl	1	1956	977	1	3	2
6502	5	Aluminum / Vinyl	1	1958	919	1	3	1
6503	5	Aluminum / Vinyl	1	1940	912	1	2	1
6504	5	Aluminum / Vinyl	1	1955	1489	1	3	2
6505	6	Fiber-Cement	1	1900	1524	1	3	2
6506	6	Aluminum / Vinyl	2	1880	2270	2	4	2
6507	6	Frame	1	1863	1652	1	2	2
6508	7	Aluminum / Vinyl	1	1940	1279	1	3	1
6509	7	Aluminum / Vinyl	1	1924	1110	1	2	1
6510	7	Aluminum / Vinyl	1.5	1925	2078	1	5	3
6511	7	Brick	1	1948	1152	1	3	1
6512	7	Aluminum / Vinyl	1	1974	1086	1	3	1
6513	8	Brick	1	1922	1626	1	3	1
6514	8	Aluminum / Vinyl	1	1913	1461	1	3	1
6515	9	Aluminum / Vinyl	1	1974	1695	1	4	2
6516	9	Aluminum / Vinyl	2	2001	1916	1	3	1
6517	9	Aluminum / Vinyl	1	1980	1218	1	3	2
6518	9	Brick	1	1957	1176	1	3	1
6519	9	Aluminum / Vinyl	1	1964	1132	1	3	2
6520	9	Frame	1	1968	1063	1	3	1
6521	9	Aluminum / Vinyl	1	1961	762	1	2	1
6522	10	Brick	1.5	1939	1608	1	3	2
6523	10	Brick	2	1941	1920	1	4	1
6524	10	Stucco	1.5	1921	2080	2	4	2
6525	10	Frame	1.5	1919	2010	2	4	2
6526	10	Aluminum / Vinyl	1.5	1925	1972	2	4	2
6527	10	Aluminum / Vinyl	1.5	1972	2122	2	5	2
6528	10	Aluminum / Vinyl	1	1951	768	1	2	1
6529	10	Aluminum / Vinyl	1	1951	707	1	2	1
6530	11	Stone	1.5	1948	1767	1	4	2
6531	11	Brick	1	1949	1150	1	2	1
6532	11	Frame	2	1919	1724	1	4	2
6533	11	Brick	1	1960	1227	1	3	1
6534	11	Masonry / Frame	1	1952	1216	1	3	1
6535	11	Aluminum / Vinyl	1	1963	1156	1	3	1
6536	11	Brick	1	1960	1016	1	3	1
6537	11	Brick	1	1954	1013	1	3	1
6538	11	Brick	1	1959	957	1	2	1

6539	11 Aluminum / Vinyl	1	1956	919	1	2	1
6540	11 Aluminum / Vinyl	1	1954	867	1	2	1
6541	13 Aluminum / Vinyl	1	1953	1373	1	3	1
6542	13 Aluminum / Vinyl	1	1951	1117	1	3	1
6543	13 Aluminum / Vinyl	2	2003	2271	1	4	3
6544	13 Aluminum / Vinyl	1.5	1967	2158	2	5	3
6545	13 Aluminum / Vinyl	1	1926	1348	1	4	1
6546	13 Aluminum / Vinyl	1	1926	1192	1	3	1
6547	13 Brick	1	1966	1666	1	3	1
6548	13 Brick	1	1974	1644	1	3	1
6549	13 Brick	1	1954	1346	1	3	2
6550	13 Brick	1	1958	1208	1	3	1
6551	13 Brick	1	1958	1074	1	3	2
6552	13 Aluminum / Vinyl	1	1958	1053	1	3	1
6553	13 Aluminum / Vinyl	1	1959	1041	1	3	1
6554	13 Aluminum / Vinyl	1	1915	1424	1	3	2
6555	14 Aluminum / Vinyl	1	1953	1222	1	4	1
6556	14 Stucco	2	1913	1441	1	3	1
6557	14 Frame	2	1947	1378	1	3	1
6558	14 Aluminum / Vinyl	1	1905	842	1	2	1
6559	14 Aluminum / Vinyl	1	1900	711	1	2	2
6560	14 Brick	1.5	1929	2510	2	4	2
6561	14 Brick	>2	1900	4634	2	4	2
6562	14 Aluminum / Vinyl	1.5	1911	1786	2	3	3
6563	14 Aluminum / Vinyl	1	1926	1711	1	5	2
6564	14 Aluminum / Vinyl	1	1923	1617	1	3	2
6565	14 Aluminum / Vinyl	1	1924	1143	1	3	1
6566	14 Aluminum / Vinyl	2	1900	1931	1	4	2
6567	14 Masonry / Frame	2	1935	1793	1	3	1
6568	14 Frame	2	1895	1673	1	4	1
6569	14 Aluminum / Vinyl	1.5	1891	1336	1	3	1
6571	14 Frame	2	1889	2885	3	5	3
6572	1 Aluminum / Vinyl	1.5	1924	1624	2	3	3
6573	1 Aluminum / Vinyl	2	1953	1824	2	6	2
6574	1 Aluminum / Vinyl	1	1927	1426	1	4	1
6575	1 Aluminum / Vinyl	1	1953	768	1	2	1
6576	1 Aluminum / Vinyl	1	1915	1371	1	4	1
6577	2 Brick	1.5	1952	1389	1	4	2
6578	2 Aluminum / Vinyl	1	1980	1198	1	3	2
6579	3 Brick	2	1919	2466	1	4	3
6580	3 Frame	2	1895	1872	2	4	2
6581	3 Fiber-Cement	1.5	1890	1796	2	4	2
6582	3 Frame	2	1910	1642	2	4	2

6583	3	Stucco	2	1912	2624	1	2	2
6584	3	Masonry / Frame	2	1906	2316	1	3	2
6585	3	Aluminum / Vinyl	2	1904	1790	1	4	2
6586	3	Frame	1.5	1891	1669	1	3	2
6587	3	Aluminum / Vinyl	1.5	1901	1427	1	3	2
6588	3	Aluminum / Vinyl	>2	2002	3654	3	>8	3
6589	3	Brick	2	1926	2817	1	5	3
6590	5	Stone	1.5	1949	1772	1	4	2
6591	5	Stone	1	1948	1333	1	3	1
6592	5	Aluminum / Vinyl	1	1952	1243	1	3	1
6593	5	Aluminum / Vinyl	1	1956	1210	1	3	1
6594	5	Aluminum / Vinyl	1	1953	1176	1	3	1
6595	5	Aluminum / Vinyl	1	1950	1171	1	3	1
6596	5	Aluminum / Vinyl	1	1949	1036	1	4	1
6597	5	Aluminum / Vinyl	1	1952	1011	1	3	1
6598	5	Brick	1	1950	847	1	2	1
6599	5	Prem Wood	2	1964	3042	1	4	2
6600	5	Masonry / Frame	2	1948	2448	1	5	3
6601	5	Aluminum / Vinyl	1	1964	1304	1	3	1
6602	5	Aluminum / Vinyl	1	1956	1132	1	3	1
6603	5	Brick	1	1956	1110	1	3	1
6604	5	Aluminum / Vinyl	1	1955	1084	1	3	2
6605	5	Aluminum / Vinyl	1	1956	1014	1	3	2
6606	5	Brick	1	1953	986	1	2	1
6607	5	Aluminum / Vinyl	1	1957	963	1	3	1
6608	5	Aluminum / Vinyl	1	1958	952	1	3	1
6609	5	Aluminum / Vinyl	1	1961	1826	1	3	2
6610	6	Aluminum / Vinyl	1.5	1909	1845	2	4	2
6611	7	Aluminum / Vinyl	1	1940	1581	1	4	1
6612	7	Stone	1	1937	1547	1	4	1
6613	8	Block	1	1951	1522	1	4	1
6614	8	Aluminum / Vinyl	1	1941	1135	1	3	1
6615	8	Aluminum / Vinyl	1.5	1887	1519	1	5	1
6616	8	Aluminum / Vinyl	1	1907	1008	1	3	1
6617	9	Aluminum / Vinyl	2	1961	2088	2	6	2
6618	9	Aluminum / Vinyl	1	1990	1751	1	4	2
6619	10	Stone	1	1940	1416	1	3	2
6620	10	Aluminum / Vinyl	1	1941	1170	1	3	1
6621	10	Aluminum / Vinyl	2	1900	2026	2	4	2
6622	10	Stucco	1	1915	1307	1	3	1
6623	10	Aluminum / Vinyl	1.5	1920	1093	1	3	1
6624	11	Brick	1	1953	1534	1	3	2
6625	11	Brick	1	1941	982	1	2	1

6626	11	Frame	2	1942	1792	1	3	1
6627	11	Masonry / Frame	2	1950	1754	1	3	1
6628	11	Masonry / Frame	2	1940	1470	1	3	1
6629	11	Brick	1.5	1957	1947	2	3	2
6630	11	Brick	1	1979	1717	1	3	2
6631	11	Brick	1	1959	1122	1	3	1
6632	11	Brick	1	1958	1114	1	3	1
6633	11	Aluminum / Vinyl	1	1956	1050	1	3	1
6634	11	Aluminum / Vinyl	1	1959	1033	1	3	1
6635	11	Frame	1	1959	936	1	3	1
6636	12	Aluminum / Vinyl	1.5	1897	1364	1	4	1
6637	12	Frame	2	1895	1455	2	5	2
6638	12	Frame	2	1890	2141	1	3	1
6639	13	Aluminum / Vinyl	1	1947	1348	1	4	2
6640	13	Aluminum / Vinyl	1	1958	1131	1	4	2
6641	13	Stucco	2	1938	1714	1	3	1
6642	13	Aluminum / Vinyl	1.5	1898	1596	2	4	2
6643	13	Aluminum / Vinyl	1	1929	1333	1	3	2
6644	13	Aluminum / Vinyl	1	1974	1361	1	3	1
6645	13	Aluminum / Vinyl	2	1875	1611	1	4	1
6646	13	Aluminum / Vinyl	1	1925	1470	1	3	2
6647	13	Brick	2	1972	2390	2	6	2
6648	14	Aluminum / Vinyl	1	1942	1306	1	3	1
6649	14	Aluminum / Vinyl	1	1946	1204	1	2	1
6650	14	Brick	1	1950	1187	1	3	1
6651	14	Stucco	1	1944	1174	1	4	2
6652	14	Aluminum / Vinyl	2	1909	2538	2	6	2
6653	14	Aluminum / Vinyl	1.5	1921	1782	1	5	2
6654	14	Aluminum / Vinyl	1	1927	1074	1	3	1
6655	14	Brick	1	1954	1716	1	3	2
6656	14	Aluminum / Vinyl	1	1947	826	1	2	1
6657	14	Aluminum / Vinyl	1	1950	735	1	2	1
6658	14	Aluminum / Vinyl	2	1890	2193	1	4	2
6659	14	Frame	1	1918	1117	1	3	1
6660	14	Aluminum / Vinyl	1.5	1922	929	1	2	2
6661	14	Brick	2	1954	1769	2	4	2
6662	15	Aluminum / Vinyl	1.5	1924	2189	2	3	2
6663	15	Frame	2	1890	1964	2	4	2
6664	1	Brick	1	1951	1535	1	4	2
6665	1	Aluminum / Vinyl	1	1943	704	1	2	1
6666	2	Brick	1	1940	1180	1	3	1
6667	2	Aluminum / Vinyl	1	1957	1306	1	4	2
6668	2	Aluminum / Vinyl	1	1964	1254	1	3	1

6669	2	Brick	1	1957	1155	1	3	1
6670	2	Brick	1	1957	942	1	3	1
6671	2	Aluminum / Vinyl	1	1958	936	1	3	1
6672	3	Brick	2	1926	3954	1	4	3
6673	3	Aluminum / Vinyl	2	1899	1961	1	4	1
6674	3	Frame	1	1895	1705	3	3	3
6675	5	Fiber-Cement	2	2003	2703	1	4	4
6676	5	Stone	1	1947	1538	1	3	2
6677	5	Aluminum / Vinyl	1	1952	1444	1	4	1
6678	5	Aluminum / Vinyl	1.5	1956	1194	1	4	2
6679	5	Aluminum / Vinyl	1	1953	1074	1	3	1
6680	5	Aluminum / Vinyl	2	1964	1988	2	6	2
6681	5	Aluminum / Vinyl	1	1956	1324	1	3	1
6682	5	Brick	1	1955	1149	1	3	2
6683	5	Aluminum / Vinyl	1	1954	933	1	3	1
6684	5	Stone	1.5	1936	1552	1	3	1
6685	6	Frame	1	1900	1320	1	2	1
6686	6	Aluminum / Vinyl	1	1884	880	1	2	1
6687	7	Stone	1	1938	1460	1	4	2
6688	7	Stone	2	1935	2007	1	4	1
6689	8	Aluminum / Vinyl	1	1896	1189	1	3	1
6690	9	Aluminum / Vinyl	2	2012	2600	1	4	3
6691	9	Aluminum / Vinyl	1	1980	1505	1	3	1
6692	9	Frame	1	1966	1315	1	3	1
6693	9	Aluminum / Vinyl	1	1958	1217	1	3	1
6694	10	Aluminum / Vinyl	1	1951	998	1	3	1
6695	10	Frame	1	1948	928	1	3	2
6696	10	Brick	2	1914	2698	1	4	2
6697	10	Aluminum / Vinyl	2	1925	2480	2	6	2
6698	10	Aluminum / Vinyl	2	1928	2170	2	4	2
6699	10	Aluminum / Vinyl	1.5	1927	1964	2	4	2
6700	10	Brick	1	1955	2666	2	7	3
6701	10	Stucco	1	1919	2054	1	4	2
6702	10	Aluminum / Vinyl	1	1926	1398	1	3	1
6703	10	Aluminum / Vinyl	2	1908	1886	1	3	1
6704	10	Aluminum / Vinyl	1.5	1924	1445	1	3	1
6705	10	Aluminum / Vinyl	1.5	1926	1169	1	2	2
6706	10	Frame	1	1926	1018	1	3	1
6707	10	Brick	1.5	1914	3040	3	4	3
6708	11	Aluminum / Vinyl	1	1941	1617	1	4	2
6709	11	Stucco	1	1942	1330	1	3	1
6710	11	Aluminum / Vinyl	1	1948	934	1	3	1
6711	11	Aluminum / Vinyl	1.5	1960	2114	2	5	2

6712	11 Aluminum / Vinyl	1	1980	1463	1	3	1
6713	11 Frame	1	1961	1358	1	3	1
6714	11 Aluminum / Vinyl	1	1953	1088	1	3	1
6715	11 Brick	1	1950	1014	1	3	1
6716	11 Aluminum / Vinyl	1	1961	1007	1	3	1
6717	11 Brick	1	1955	924	1	3	1
6718	11 Aluminum / Vinyl	1	1953	906	1	2	1
6719	11 Brick	1	1949	863	1	2	1
6720	11 Stucco	1	1927	1147	1	3	1
6721	11 Masonry / Frame	1	1958	1537	1	3	1
6722	11 Brick	2	1933	1572	1	3	1
6723	12 Aluminum / Vinyl	1	1891	1512	1	6	2
6724	12 Frame	2	1890	2698	1	4	2
6725	12 Aluminum / Vinyl	1	1901	1058	1	2	1
6727	13 Brick	1	1960	1569	1	3	2
6728	13 Frame	1.5	1928	1654	1	4	2
6729	13 Aluminum / Vinyl	1	1950	1305	1	3	1
6730	13 Aluminum / Vinyl	1	1969	1132	1	3	2
6731	13 Aluminum / Vinyl	1	1942	808	1	2	1
6732	14 Aluminum / Vinyl	2	1939	1170	1	2	1
6733	14 Brick	1.5	1926	2154	2	5	2
6734	14 Aluminum / Vinyl	1.5	1908	1667	2	3	3
6735	14 Aluminum / Vinyl	2	1919	1616	2	4	2
6736	14 Aluminum / Vinyl	1	1929	1658	1	3	2
6737	14 Aluminum / Vinyl	1	1928	1209	1	3	1
6738	14 Brick	1	1956	1140	1	3	1
6739	14 Stucco	1	1944	784	1	2	1
6740	14 Aluminum / Vinyl	1	1942	753	1	2	1
6741	14 Aluminum / Vinyl	2	1890	1487	1	3	2
6742	14 Aluminum / Vinyl	1	1888	1320	1	2	1
6743	14 Aluminum / Vinyl	1	1898	1074	1	2	1
6744	14 Aluminum / Vinyl	1	1905	1048	1	3	2
6745	14 Aluminum / Vinyl	1	1905	748	1	2	1
6746	15 Aluminum / Vinyl	2	1902	2650	2	6	2
6747	1 Aluminum / Vinyl	1	1942	1198	1	4	2
6748	1 Aluminum / Vinyl	1	1951	1027	1	4	1
6749	1 Aluminum / Vinyl	2	1981	2143	2	5	2
6750	1 Aluminum / Vinyl	1	1953	1082	1	3	2
6751	2 Brick	1	1938	1395	1	3	2
6752	2 Aluminum / Vinyl	2	1961	1652	1	3	1
6753	2 Aluminum / Vinyl	2	1956	2265	2	6	2
6754	2 Aluminum / Vinyl	2	1940	1762	2	4	2
6755	2 Aluminum / Vinyl	1	1955	1404	1	4	2

6756	2 Aluminum / Vinyl	1	1949	820	1	2	1
6757	2 Aluminum / Vinyl	1	1955	1414	1	3	1
6758	3 Aluminum / Vinyl	2	1922	2771	2	6	2
6759	3 Aluminum / Vinyl	2	1897	2468	2	4	3
6760	3 Aluminum / Vinyl	2	1907	2130	1	5	1
6761	3 Brick	2	1909	3821	1	5	3
6762	3 Brick	2	1927	3234	1	4	3
6763	4 Aluminum / Vinyl	2	1925	2414	2	4	2
6764	4 Brick	>2	1905	8810	1	>8	>4
6765	5 Aluminum / Vinyl	1	1952	1360	1	3	2
6766	5 Aluminum / Vinyl	1	1957	1231	1	4	2
6767	5 Aluminum / Vinyl	1	1950	1152	1	4	1
6768	5 Brick	1	1946	1148	1	3	1
6769	5 Aluminum / Vinyl	1	1952	1092	1	4	2
6770	5 Aluminum / Vinyl	1	1952	1009	1	3	1
6771	5 Aluminum / Vinyl	2	1953	2063	2	6	2
6772	5 Brick	1	1960	1757	1	3	2
6773	5 Brick	1	1957	1340	1	3	1
6774	5 Brick	1	1956	1222	1	3	1
6775	5 Brick	1	1954	1150	1	3	1
6776	5 Aluminum / Vinyl	1	1951	1073	1	3	1
6777	5 Aluminum / Vinyl	1	1956	999	1	3	1
6778	5 Aluminum / Vinyl	1	1955	991	1	3	1
6779	5 Aluminum / Vinyl	1	1958	960	1	3	1
6780	5 Aluminum / Vinyl	1	1950	909	1	3	1
6781	5 Aluminum / Vinyl	1	1951	899	1	2	1
6782	5 Aluminum / Vinyl	1.5	1928	1622	1	3	2
6783	5 Masonry / Frame	2	1983	2641	2	6	2
6784	6 Aluminum / Vinyl	1.5	1909	1983	2	6	2
6785	6 Aluminum / Vinyl	1.5	1904	1549	1	4	1
6786	6 Frame	1	1922	1461	1	2	1
6788	7 Stone	1	1939	1714	1	3	1
6789	7 Brick	1	1927	1804	1	5	2
6790	8 Aluminum / Vinyl	2	1911	2408	2	6	2
6791	8 Aluminum / Vinyl	2	1927	1668	1	3	1
6792	8 Masonry / Frame	2	1909	2714	1	5	1
6793	8 Brick	1	1900	1399	1	3	1
6794	8 Aluminum / Vinyl	2	1924	1249	1	3	1
6795	8 Aluminum / Vinyl	1	1929	1152	1	3	1
6796	8 Aluminum / Vinyl	1	1900	2344	3	5	3
6797	9 Aluminum / Vinyl	2	2008	2224	1	4	2
6798	9 Frame	2	1963	2007	1	5	2
6799	10 Aluminum / Vinyl	1	1951	975	1	3	1

6800	10	Frame	2	1920	2063	1	4	1
6801	10	Aluminum / Vinyl	1	1930	1333	1	3	2
6802	10	Brick	1	1928	1298	1	3	1
6803	10	Aluminum / Vinyl	1	1953	704	1	2	1
6804	10	Aluminum / Vinyl	1	1923	1129	1	4	1
6806	10	Masonry / Frame	2	1933	2514	2	6	2
6807	11	Brick	1	1945	1243	1	3	1
6808	11	Aluminum / Vinyl	1	1953	1103	1	3	1
6809	11	Aluminum / Vinyl	1	1942	1000	1	3	1
6810	11	Aluminum / Vinyl	1	1937	917	1	2	1
6811	11	Prem Wood	2	1990	2238	1	4	2
6812	11	Aluminum / Vinyl	1	1928	984	1	3	1
6813	11	Brick	1	1967	1177	1	3	1
6814	11	Brick	1	1957	1131	1	3	1
6815	11	Aluminum / Vinyl	1	1957	1090	1	3	2
6816	11	Aluminum / Vinyl	1	1960	1077	1	3	1
6817	11	Brick	1	1955	947	1	3	1
6818	11	Aluminum / Vinyl	1	1929	1190	1	4	1
6819	12	Frame	1.5	1900	1810	1	3	2
6820	12	Aluminum / Vinyl	1	1903	1690	2	4	2
6821	13	Stone	1	1940	1251	1	4	2
6822	13	Masonry / Frame	2	1976	3014	1	4	2
6823	13	Aluminum / Vinyl	2	1953	1842	1	3	1
6824	13	Brick	2	1936	1770	1	3	1
6825	13	Brick	1	1965	1491	1	3	1
6826	13	Brick	1	1960	1082	1	3	1
6827	13	Aluminum / Vinyl	1	1936	893	1	3	1
6828	13	Frame	1.5	1900	1231	1	3	2
6829	14	Aluminum / Vinyl	1	1953	1129	1	3	1
6830	14	Aluminum / Vinyl	1.5	1924	1809	2	4	2
6831	14	Aluminum / Vinyl	1.5	1926	1800	2	3	2
6832	14	Aluminum / Vinyl	2	1920	2208	2	4	2
6834	14	Aluminum / Vinyl	1	1905	1130	1	3	1
6835	14	Brick	1	1948	684	1	2	1
6836	14	Frame	1.5	1900	1563	1	3	1
6837	14	Aluminum / Vinyl	1	1910	1003	1	3	1
6838	14	Stucco	1.5	1940	1453	1	3	1
6839	15	Aluminum / Vinyl	2	2012	1854	1	4	2
6840	15	Aluminum / Vinyl	2	1900	2264	2	6	2
6841	15	Frame	2	1892	2464	2	6	2
6842	1	Brick	1	1948	1248	1	3	1
6843	1	Brick	1	1951	1143	1	3	1
6844	1	Aluminum / Vinyl	1	1949	1041	1	3	1

6845	1	Masonry / Frame	2	1940	1684	1	3	1
6846	1	Frame	1	1907	544	1	1	1
6847	1	Aluminum / Vinyl	1	1955	1082	1	3	1
6848	1	Aluminum / Vinyl	1	1955	1082	1	3	1
6849	2	Brick	1	1955	1290	1	4	1
6850	2	Aluminum / Vinyl	1	1956	1286	1	4	1
6851	2	Aluminum / Vinyl	2	1964	1778	1	4	1
6852	2	Frame	1	1966	1237	1	3	1
6853	2	Brick	1	1956	1097	1	3	1
6854	2	Frame	1	1955	970	1	3	1
6855	2	Aluminum / Vinyl	1	1956	905	1	3	2
6856	3	Brick	1	1956	1469	1	3	1
6857	3	Aluminum / Vinyl	1.5	1900	1421	1	2	1
6858	3	Aluminum / Vinyl	2	1910	4435	2	8	3
6859	3	Frame	2	1900	2520	2	6	3
6860	3	Aluminum / Vinyl	2	1902	2112	2	5	2
6861	3	Aluminum / Vinyl	1.5	1900	1456	2	4	2
6862	3	Aluminum / Vinyl	2	1880	1952	2	4	2
6863	3	Brick	2	1911	4113	1	5	4
6864	3	Frame	2	1904	3555	1	5	2
6865	3	Frame	2	1897	3373	1	4	4
6866	3	Stucco	2	1908	2582	1	3	2
6867	3	Aluminum / Vinyl	2	1904	2345	1	4	3
6868	3	Frame	2	1899	2340	1	5	2
6869	3	Brick	1.5	1941	1368	1	2	1
6870	4	Aluminum / Vinyl	2	1977	1253	1	4	1
6871	4	Frame	2	1892	2080	2	4	2
6872	5	Frame	1	1950	1484	1	4	2
6873	5	Brick	1.5	1948	1885	1	4	2
6874	5	Aluminum / Vinyl	1	1941	1238	1	3	2
6875	5	Aluminum / Vinyl	1.5	1950	1231	1	3	1
6876	5	Aluminum / Vinyl	1	1951	1218	1	3	1
6877	5	Brick	1	1951	1133	1	2	1
6878	5	Aluminum / Vinyl	2	1979	2137	1	4	2
6879	5	Aluminum / Vinyl	2	1942	1088	1	2	1
6880	5	Brick	2	1957	2744	2	6	3
6881	5	Aluminum / Vinyl	2	2012	3027	1	3	3
6882	5	Aluminum / Vinyl	1	1969	1569	1	3	1
6883	5	Aluminum / Vinyl	1	1956	1405	1	3	1
6884	5	Brick	1	1952	1316	1	4	1
6885	5	Aluminum / Vinyl	1	1976	1287	1	3	1
6886	5	Brick	1	1953	1108	1	3	1
6887	5	Aluminum / Vinyl	1	1956	1077	1	3	1

6888	5	Brick	1	1949	1053	1	2	1
6889	5	Aluminum / Vinyl	1	1950	950	1	2	1
6890	5	Aluminum / Vinyl	1	1954	940	1	2	2
6891	5	Aluminum / Vinyl	1	1956	864	1	2	1
6892	5	Brick	2	1910	1848	1	3	1
6893	6	Aluminum / Vinyl	1.5	1917	1786	2	4	2
6894	6	Aluminum / Vinyl	2	1899	2374	2	5	2
6895	6	Aluminum / Vinyl	1	1925	1355	1	3	1
6896	6	Aluminum / Vinyl	1	1894	1070	1	3	1
6897	6	Frame	1	1926	833	1	2	1
6898	7	Aluminum / Vinyl	1.5	1940	949	1	2	1
6899	7	Brick	2	1923	3069	2	6	2
6900	7	Brick	1	1937	1737	1	4	1
6901	7	Aluminum / Vinyl	1	1926	1512	1	4	2
6902	8	Aluminum / Vinyl	1	1955	966	1	3	1
6903	8	Aluminum / Vinyl	1.5	1905	1367	1	3	1
6904	9	Aluminum / Vinyl	1	2008	1971	1	3	2
6905	9	Aluminum / Vinyl	1	1980	1505	1	3	1
6906	9	Brick	1	1958	1166	1	3	1
6907	9	Aluminum / Vinyl	1	1957	1110	1	3	2
6908	9	Aluminum / Vinyl	2	1977	2613	2	6	2
6909	9	Aluminum / Vinyl	2	1979	2290	2	6	2
6910	10	Stucco	1	1947	1389	1	4	1
6911	10	Masonry / Frame	1	1952	1335	1	4	2
6912	10	Aluminum / Vinyl	1	1952	1050	1	3	1
6913	10	Aluminum / Vinyl	1	1948	1012	1	3	1
6914	10	Aluminum / Vinyl	1	1948	982	1	3	1
6915	10	Brick	2	1918	3306	1	4	2
6916	10	Brick	2	1935	1692	1	4	2
6917	10	Aluminum / Vinyl	1	1920	680	1	1	1
6918	10	Masonry / Frame	2	1942	1766	2	4	2
6919	10	Frame	2	1957	2132	2	6	2
6920	10	Masonry / Frame	2	1957	1993	2	6	2
6921	10	Aluminum / Vinyl	1	1955	1038	1	3	1
6922	10	Stucco	2	1914	2520	1	4	1
6923	11	Brick	1	1940	1578	1	3	2
6924	11	Aluminum / Vinyl	1	1952	1389	1	3	1
6925	11	Stucco	1	1948	1382	1	3	1
6926	11	Aluminum / Vinyl	1.5	1947	1221	1	4	1
6927	11	Brick	1	1954	1183	1	3	1
6928	11	Aluminum / Vinyl	1	1939	1118	1	3	1
6929	11	Aluminum / Vinyl	1	1949	900	1	3	1
6930	11	Aluminum / Vinyl	2	1922	1410	1	3	1

6931	11	Brick	1.5	1929	1924	2	3	2
6932	11	Brick	1.5	1931	1789	1	3	2
6933	11	Fiber-Cement	1	2002	2344	1	4	3
6934	11	Brick	1	1956	1236	1	4	1
6935	11	Brick	1	1956	1188	1	3	1
6936	11	Aluminum / Vinyl	1	1963	1184	1	3	2
6937	11	Brick	1	1960	1138	1	3	1
6938	11	Brick	1	1949	1037	1	3	1
6939	11	Aluminum / Vinyl	1	1960	1036	1	3	1
6940	11	Aluminum / Vinyl	1	1955	984	1	3	1
6941	11	Aluminum / Vinyl	1	1953	908	1	3	1
6942	12	Aluminum / Vinyl	2	2012	2016	1	4	3
6943	12	Aluminum / Vinyl	1	1881	1260	1	3	1
6944	12	Aluminum / Vinyl	1	1921	1369	1	3	1
6945	12	Aluminum / Vinyl	1	1900	1518	1	3	1
6946	13	Aluminum / Vinyl	1.5	1996	3701	1	5	3
6947	13	Aluminum / Vinyl	1.5	1991	2300	1	3	2
6948	13	Aluminum / Vinyl	1	1939	1149	1	3	1
6949	13	Aluminum / Vinyl	1	1948	1019	1	3	1
6950	13	Aluminum / Vinyl	2	2001	2190	1	3	2
6951	13	Brick	2	1949	1414	1	3	1
6952	13	Aluminum / Vinyl	2	1958	2044	2	6	2
6953	13	Brick	2	1946	2000	2	4	2
6954	13	Brick	1	1959	1276	1	3	1
6955	13	Aluminum / Vinyl	1	1954	1216	1	2	2
6956	13	Brick	1	1961	1036	1	3	1
6957	13	Brick	1	1959	988	1	3	2
6958	13	Frame	1	1952	948	1	2	1
6959	13	Aluminum / Vinyl	1	1959	919	1	3	1
6960	13	Aluminum / Vinyl	1	1954	768	1	3	1
6961	13	Masonry / Frame	1	1959	1841	1	3	2
6962	14	Aluminum / Vinyl	1	1942	1307	1	3	1
6963	14	Aluminum / Vinyl	1	1956	1415	1	4	2
6964	14	Aluminum / Vinyl	1	1900	1406	1	2	2
6965	14	Frame	1.5	1900	1349	1	3	1
6966	14	Aluminum / Vinyl	1.5	1918	1045	1	1	1
6967	14	Aluminum / Vinyl	1.5	1901	1916	2	4	1
6968	14	Aluminum / Vinyl	2	1914	1672	2	4	1
6969	14	Brick	1	1928	1145	1	3	1
6970	14	Aluminum / Vinyl	1	1930	1144	1	3	2
6971	14	Fiber-Cement	1	1924	1132	1	2	1
6972	14	Frame	1	1988	1365	1	3	2
6973	14	Aluminum / Vinyl	1.5	1907	1641	1	3	2

6974	14	Aluminum / Vinyl	1.5	1895	1519	1	4	1
6975	14	Aluminum / Vinyl	1.5	1923	1175	1	3	2
6976	14	Masonry / Frame	1	1962	1921	1	2	1
6977	15	Frame	2	1914	2545	2	6	2
6978	1	Frame	1	1942	1057	1	3	2
6979	1	Aluminum / Vinyl	1	1951	971	1	4	1
6980	1	Brick	2	1953	1680	2	4	2
6981	1	Brick	2	1953	1680	2	4	2
6982	1	Frame	1	1929	1274	1	3	1
6983	1	Aluminum / Vinyl	1	1925	937	1	2	1
6984	2	Aluminum / Vinyl	1	1952	1019	1	3	1
6985	2	Brick	1	1955	1619	1	3	2
6986	2	Aluminum / Vinyl	1	1955	1356	1	3	2
6987	2	Stone	1	1954	1164	1	3	1
6988	2	Brick	1	1958	1139	1	3	1
6989	2	Stone	1	1953	1024	1	3	1
6990	2	Aluminum / Vinyl	1	1960	1002	1	3	2
6991	2	Aluminum / Vinyl	1	1955	900	1	3	2
6992	3	Brick	2	1922	2242	1	4	2
6993	3	Brick	2	1916	2188	1	3	2
6994	3	Aluminum / Vinyl	2	1901	2020	2	5	2
6995	3	Aluminum / Vinyl	2	1908	1496	2	4	2
6996	3	Aluminum / Vinyl	1	1927	1530	1	4	2
6997	3	Brick	2	1912	3973	2	4	3
6998	3	Aluminum / Vinyl	2	1902	3480	1	6	2
6999	3	Aluminum / Vinyl	2	1898	3222	1	6	2
7000	3	Frame	2	1899	2383	1	5	2
7001	3	Fiber-Cement	1.5	1889	2174	1	4	2
7002	3	Frame	2	1905	2141	1	3	2
7003	3	Aluminum / Vinyl	1.5	1928	1736	1	4	2
7004	3	Aluminum / Vinyl	1.5	1903	1510	1	3	2
7005	3	Frame	1	1890	1488	1	3	2
7006	3	Aluminum / Vinyl	2	1888	1378	1	3	1
7007	3	Frame	1.5	1900	1257	1	3	1
7008	3	Aluminum / Vinyl	2	1912	2486	3	5	3
7009	3	Brick	1.5	1914	3791	1	3	>4
7010	4	Aluminum / Vinyl	2	1894	2699	2	6	2
7011	5	Aluminum / Vinyl	1.5	1942	1737	1	4	2
7012	5	Brick	1	1950	1720	1	3	2
7013	5	Aluminum / Vinyl	1.5	1949	1511	1	3	2
7014	5	Brick	1.5	1947	1473	1	4	2
7015	5	Brick	1	1947	1368	1	4	1
7016	5	Brick	1.5	1937	1364	1	3	1

7017	5 Aluminum / Vinyl	1.5	1949	1357	1	4	2
7018	5 Stone	1	1950	1140	1	2	1
7019	5 Aluminum / Vinyl	1	1954	1130	1	4	1
7020	5 Aluminum / Vinyl	1	1952	1092	1	4	2
7021	5 Aluminum / Vinyl	1	1951	1041	1	3	1
7022	5 Aluminum / Vinyl	1	1949	1029	1	4	1
7023	5 Aluminum / Vinyl	1	1952	977	1	3	1
7024	5 Aluminum / Vinyl	2	1986	2069	1	3	2
7025	5 Masonry / Frame	2	2010	1441	1	3	2
7026	5 Masonry / Frame	2	1956	2240	2	6	3
7027	5 Aluminum / Vinyl	1	1971	2048	2	4	4
7028	5 Brick	1	1955	1320	1	3	1
7029	5 Aluminum / Vinyl	1	1962	1255	1	3	1
7030	5 Stone	1	1953	1254	1	2	1
7031	5 Masonry / Frame	1	1957	1247	1	3	1
7032	5 Aluminum / Vinyl	1	1962	1080	1	3	1
7033	5 Brick	1	1956	964	1	3	1
7034	5 Aluminum / Vinyl	1	1953	864	1	3	1
7035	5 Aluminum / Vinyl	1	1950	728	1	2	1
7036	6 Fiber-Cement	2	2007	2685	1	4	2
7037	6 Aluminum / Vinyl	2	2007	1584	1	3	3
7038	6 Aluminum / Vinyl	2	2007	1584	1	3	3
7039	6 Aluminum / Vinyl	1.5	1925	1661	2	4	2
7040	6 Aluminum / Vinyl	2	1913	1976	2	4	2
7041	6 Aluminum / Vinyl	1.5	1905	1960	2	4	2
7042	6 Frame	1.5	1917	1447	2	4	2
7043	6 Aluminum / Vinyl	2	1895	2092	2	5	3
7044	6 Brick	2	1897	3868	1	4	3
7045	6 Aluminum / Vinyl	1	1890	953	1	3	1
7046	7 Masonry / Frame	2	1946	1475	1	3	2
7047	7 Brick	1	1927	1815	1	4	3
7048	7 Stucco	1	1919	1521	1	4	1
7049	7 Aluminum / Vinyl	1	1913	1149	1	3	1
7050	7 Stone	1	1947	1363	1	4	2
7051	7 Aluminum / Vinyl	1	1955	976	1	3	1
7052	8 Frame	1.5	1900	1426	2	3	2
7053	8 Frame	1	1892	1188	2	3	2
7054	8 Stucco	1.5	1914	1267	1	3	2
7055	8 Aluminum / Vinyl	1	1925	947	1	3	1
7056	8 Aluminum / Vinyl	1	1895	1320	1	4	1
7057	9 Aluminum / Vinyl	2	1957	2052	2	6	2
7058	9 Aluminum / Vinyl	1	1968	1422	1	3	1
7059	9 Aluminum / Vinyl	1	1957	1052	1	3	2

7060	10	Brick	1.5	1937	1584	1	3	1
7061	10	Brick	1	1953	1368	1	3	1
7062	10	Aluminum / Vinyl	1	1949	1343	1	4	1
7063	10	Brick	1	1946	1150	1	3	2
7064	10	Aluminum / Vinyl	1	1949	974	1	3	1
7065	10	Frame	2	1925	1588	1	3	1
7066	10	Aluminum / Vinyl	2	1952	1473	1	3	1
7067	10	Stone	2	1940	2595	2	4	2
7068	10	Brick	1.5	1928	2108	2	5	2
7069	10	Aluminum / Vinyl	1.5	1925	1355	2	3	2
7070	10	Stucco	1	1925	1900	1	5	1
7071	10	Brick	1	1927	1807	1	3	1
7072	10	Aluminum / Vinyl	1	1924	1670	1	3	1
7073	10	Brick	1	1927	1593	1	4	1
7074	10	Aluminum / Vinyl	1	1921	1310	1	4	1
7075	10	Aluminum / Vinyl	1	1953	864	1	3	2
7076	10	Aluminum / Vinyl	1	1953	753	1	2	1
7077	10	Aluminum / Vinyl	2	1924	2071	3	2	3
7078	11	Aluminum / Vinyl	1.5	1942	1674	1	4	2
7079	11	Aluminum / Vinyl	1	1949	1257	1	3	1
7080	11	Aluminum / Vinyl	1	1942	1163	1	3	1
7081	11	Aluminum / Vinyl	1	1942	1134	1	3	1
7082	11	Brick	2	1946	1437	1	3	1
7083	11	Aluminum / Vinyl	1	1936	1374	1	2	2
7084	11	Aluminum / Vinyl	1	1956	1151	1	3	1
7085	11	Aluminum / Vinyl	1	1953	1144	1	3	2
7086	11	Brick	1	1955	1062	1	2	1
7087	11	Aluminum / Vinyl	1	1956	1054	1	2	1
7088	11	Brick	1	1958	1052	1	3	1
7089	11	Aluminum / Vinyl	1	1949	1032	1	2	1
7090	11	Brick	1	1956	994	1	3	1
7091	11	Block	1	1949	857	1	2	1
7092	11	Stone	1	1945	806	1	2	1
7093	11	Masonry / Frame	1	1965	2947	1	3	2
7094	12	Aluminum / Vinyl	2	1913	2148	2	6	2
7095	12	Aluminum / Vinyl	2	1914	1854	2	4	2
7096	12	Brick	>2	1894	3001	1	3	2
7098	13	Brick	1	1951	1419	1	3	2
7099	13	Aluminum / Vinyl	1	1948	977	1	3	1
7100	13	Brick	1.5	1931	2151	2	4	2
7101	13	Aluminum / Vinyl	1.5	1926	1950	2	5	2
7102	13	Brick	2	1952	2080	2	4	2
7103	13	Brick	1	1966	1302	1	3	2

7104	13	Brick	1	1960	1201	1	2	2
7105	13	Frame	1	1961	998	1	3	1
7106	13	Brick	1	1969	964	1	2	1
7107	13	Aluminum / Vinyl	1	1959	936	1	3	1
7108	13	Aluminum / Vinyl	1	1939	921	1	2	1
7109	13	Aluminum / Vinyl	1	1939	845	1	2	1
7110	13	Frame	1	1950	818	1	2	1
7111	13	Aluminum / Vinyl	1	1947	771	1	2	1
7112	13	Aluminum / Vinyl	1	1914	828	1	1	1
7113	13	Masonry / Frame	2	1965	2222	2	6	2
7114	14	Aluminum / Vinyl	1	1938	1140	1	3	1
7115	14	Aluminum / Vinyl	2	1939	1212	1	3	1
7116	14	Aluminum / Vinyl	2	1919	2075	2	5	2
7117	14	Brick	2	1956	2160	2	4	2
7118	14	Frame	2	1921	1935	2	4	2
7119	14	Aluminum / Vinyl	1.5	1900	1824	2	3	2
7120	14	Aluminum / Vinyl	1	1944	1624	2	4	2
7121	14	Brick	1	1929	1878	1	4	3
7122	14	Aluminum / Vinyl	1.5	1925	1845	1	3	2
7123	14	Aluminum / Vinyl	1	1925	1518	1	4	1
7124	14	Aluminum / Vinyl	1	1927	1448	1	3	1
7125	14	Aluminum / Vinyl	1	1928	1244	1	3	1
7126	14	Aluminum / Vinyl	1	1926	1172	1	2	1
7127	14	Aluminum / Vinyl	1	1943	707	1	2	1
7128	14	Aluminum / Vinyl	1.5	1891	1623	1	3	2
7129	14	Aluminum / Vinyl	1.5	1896	1441	1	4	2
7130	14	Aluminum / Vinyl	1.5	1920	1415	1	4	2
7131	14	Aluminum / Vinyl	1.5	1900	1205	1	3	1
7132	14	Aluminum / Vinyl	1	1890	1154	1	3	2
7133	14	Aluminum / Vinyl	1	1910	1044	1	3	2
7134	14	Fiber-Cement	1	1900	972	1	2	1
7135	14	Block	2	1915	3186	3	8	3
7136	15	Brick	2	1913	2333	1	5	1
7137	15	Aluminum / Vinyl	1.5	1919	1797	2	4	2
7138	15	Aluminum / Vinyl	1.5	1919	1797	2	4	2
7139	15	Fiber-Cement	1	2010	2008	1	4	2
7140	1	Aluminum / Vinyl	1	1951	1309	1	3	1
7141	1	Aluminum / Vinyl	1.5	1926	1863	2	3	2
7142	1	Fiber-Cement	1	1942	796	1	2	1
7143	2	Aluminum / Vinyl	1	1958	1136	1	3	1
7144	2	Aluminum / Vinyl	1	1955	1070	1	3	1
7145	2	Aluminum / Vinyl	1	1939	1013	1	3	1
7146	2	Stone	2	1948	1847	1	4	1

7147	2 Aluminum / Vinyl	2	1947	1124	1	4	2
7148	2 Frame	1.5	1956	2138	2	5	2
7149	2 Aluminum / Vinyl	1	1964	1306	1	4	1
7150	2 Brick	1	1960	1260	1	3	1
7151	2 Masonry / Frame	1	1961	1246	1	3	1
7152	2 Brick	1	1959	1135	1	3	1
7153	2 Aluminum / Vinyl	1	1957	945	1	3	1
7154	2 Aluminum / Vinyl	1	1959	938	1	3	1
7155	2 Aluminum / Vinyl	1	1957	909	1	3	1
7156	2 Stone	1	1954	842	1	2	2
7157	3 Brick	2	1916	4075	1	5	3
7158	3 Aluminum / Vinyl	2	1924	2432	2	4	2
7159	3 Masonry / Frame	2	1902	6733	1	>8	>4
7160	3 Brick	2	1906	5977	1	7	>4
7161	3 Frame	1.5	1921	2101	1	4	2
7162	3 Brick	1	1924	2080	1	3	2
7163	3 Aluminum / Vinyl	1	1925	1607	1	3	2
7164	3 Brick	2	1912	4304	1	4	3
7165	3 Aluminum / Vinyl	2	1902	1476	1	3	1
7166	3 Aluminum / Vinyl	1	1904	1417	1	3	2
7167	3 Aluminum / Vinyl	1.5	1900	1307	1	3	2
7168	3 Masonry / Frame	2	1926	2388	1	4	2
7169	4 Brick	2	1906	3035	2	6	2
7170	4 Frame	2	1890	3040	1	4	2
7171	5 Aluminum / Vinyl	1	1971	1746	1	4	1
7172	5 Aluminum / Vinyl	1.5	1955	1874	1	4	2
7173	5 Brick	1	1947	1613	1	4	2
7174	5 Stone	1	1952	1560	1	3	2
7175	5 Stone	1	1939	1522	1	3	2
7176	5 Brick	1	1948	1520	1	3	2
7177	5 Brick	1	1951	1511	1	3	1
7178	5 Aluminum / Vinyl	1.5	1949	1485	1	3	2
7179	5 Aluminum / Vinyl	1	1952	1445	1	3	2
7180	5 Brick	1	1951	1442	1	4	2
7181	5 Brick	1	1947	1440	1	3	2
7182	5 Frame	1	1948	1383	1	4	1
7183	5 Brick	1	1949	1372	1	3	1
7184	5 Aluminum / Vinyl	1.5	1950	1269	1	3	2
7185	5 Aluminum / Vinyl	1	1951	1192	1	3	1
7186	5 Brick	1	1951	1169	1	4	1
7187	5 Aluminum / Vinyl	1	1952	1144	1	4	1
7188	5 Aluminum / Vinyl	1	1942	1128	1	4	1
7189	5 Aluminum / Vinyl	1	1948	1051	1	3	1

7190	5	Aluminum / Vinyl	1	1949	1036	1	3	1
7191	5	Aluminum / Vinyl	1	1949	926	1	3	1
7192	5	Brick	1	1947	897	1	2	1
7193	5	Fiber-Cement	2	2005	3214	1	4	3
7194	5	Aluminum / Vinyl	2	1988	1800	1	3	1
7195	5	Brick	2	1949	1650	1	3	1
7196	5	Aluminum / Vinyl	2	1948	1493	1	3	1
7197	5	Stone	1	1952	1856	1	3	1
7198	5	Aluminum / Vinyl	1	1980	1768	1	3	2
7199	5	Aluminum / Vinyl	1	1969	1627	1	3	2
7200	5	Brick	1	1957	1339	1	3	1
7201	5	Brick	1	1956	1338	1	3	2
7202	5	Aluminum / Vinyl	1	1976	1236	1	3	1
7203	5	Brick	1	1952	1204	1	2	1
7204	5	Aluminum / Vinyl	1	1981	1176	1	3	1
7205	5	Brick	1	1961	1126	1	3	1
7206	5	Aluminum / Vinyl	1	1956	1094	1	3	1
7207	5	Aluminum / Vinyl	1	1951	1078	1	3	1
7208	5	Brick	1	1957	1076	1	3	1
7209	5	Brick	1	1959	1050	1	3	2
7210	5	Brick	1	1956	1020	1	3	1
7211	5	Aluminum / Vinyl	1	1952	720	1	2	1
7212	5	Brick	1	1931	1467	1	4	1
7213	5	Brick	1	1961	1727	1	4	2
7214	6	Fiber-Cement	2	2005	2886	1	3	2
7215	6	Aluminum / Vinyl	2	1915	2374	2	4	2
7216	6	Aluminum / Vinyl	2	1906	2256	2	5	2
7217	6	Aluminum / Vinyl	1.5	1892	1868	1	4	2
7218	6	Aluminum / Vinyl	1.5	1898	1720	1	3	1
7219	6	Aluminum / Vinyl	1	1890	1210	1	4	1
7220	6	Aluminum / Vinyl	2	1992	2762	2	6	2
7221	7	Aluminum / Vinyl	1	1949	990	1	3	1
7222	7	Brick	1	1936	1549	1	4	2
7223	7	Brick	1	1936	1549	1	4	2
7224	7	Aluminum / Vinyl	1	1916	1478	1	5	1
7225	8	Aluminum / Vinyl	2	1910	1994	1	4	1
7226	8	Frame	1	1896	1328	1	4	1
7227	8	Frame	1	1896	1328	1	4	1
7228	8	Frame	1	1896	1328	1	4	1
7229	8	Frame	1.5	1901	1186	1	3	1
7230	9	Stucco	2	1981	1354	1	3	1
7231	9	Aluminum / Vinyl	1	1965	1333	1	4	1
7232	10	Stone	1.5	1940	1470	1	3	1

7233	10	Aluminum / Vinyl	1	1950	1217	1	3	1
7234	10	Aluminum / Vinyl	1	1953	1082	1	3	1
7235	10	Aluminum / Vinyl	1	1942	1013	1	3	1
7236	10	Aluminum / Vinyl	1	1947	1010	1	3	1
7237	10	Masonry / Frame	2	1937	1513	1	4	1
7238	10	Aluminum / Vinyl	2	1923	1451	1	3	1
7239	10	Aluminum / Vinyl	2	1926	1365	1	3	1
7240	10	Aluminum / Vinyl	1.5	1924	1736	2	4	2
7241	10	Stone	2	1947	2272	2	4	2
7242	10	Frame	1	1919	1606	1	4	2
7243	10	Aluminum / Vinyl	1	1921	824	1	3	1
7244	10	Aluminum / Vinyl	1	1915	760	1	2	1
7245	11	Aluminum / Vinyl	1	1950	1748	1	4	2
7246	11	Brick	1.5	1953	1629	1	3	1
7247	11	Aluminum / Vinyl	1	1951	1353	1	3	1
7248	11	Brick	1.5	1936	1306	1	2	1
7249	11	Brick	1	1951	1209	1	3	1
7250	11	Brick	1	1947	1200	1	3	1
7251	11	Brick	1	1955	1151	1	3	2
7252	11	Aluminum / Vinyl	1.5	1941	1079	1	3	1
7253	11	Aluminum / Vinyl	1	1955	821	1	3	1
7254	11	Aluminum / Vinyl	1.5	1930	1743	2	4	3
7255	11	Aluminum / Vinyl	2	1963	2563	2	6	3
7256	11	Aluminum / Vinyl	1	1925	1338	1	3	2
7257	11	Aluminum / Vinyl	1	1965	1285	1	3	1
7258	11	Brick	1	1959	1270	1	3	1
7259	11	Aluminum / Vinyl	1	1959	1257	1	3	1
7260	11	Brick	1	1961	1127	1	3	1
7261	11	Brick	1	1964	1116	1	3	1
7262	11	Brick	1	1957	1053	1	3	1
7263	11	Stone	1	1940	1035	1	2	1
7264	11	Aluminum / Vinyl	1	1964	1025	1	3	1
7265	11	Aluminum / Vinyl	1	1955	984	1	3	1
7266	11	Aluminum / Vinyl	1	1962	912	1	3	1
7267	11	Aluminum / Vinyl	1	1953	888	1	3	1
7268	11	Aluminum / Vinyl	1	1952	884	1	3	1
7269	11	Aluminum / Vinyl	1	1953	879	1	3	1
7270	11	Masonry / Frame	1	1958	2210	1	4	2
7271	11	Brick	2	1958	2760	3	5	3
7272	11	Stone	2	1936	1674	1	3	1
7273	12	Frame	1	1895	1330	2	5	2
7274	12	Brick	1	1924	1268	1	4	1
7275	12	Aluminum / Vinyl	1	1925	1075	1	3	1

7276	13	Aluminum / Vinyl	1	1953	1176	1	3	1
7277	13	Aluminum / Vinyl	1	1948	1165	1	3	1
7278	13	Brick	1	1946	1116	1	4	1
7279	13	Aluminum / Vinyl	1	1947	1072	1	3	1
7280	13	Block	1.5	1937	1003	1	2	2
7281	13	Brick	2	1939	1859	1	3	1
7282	13	Aluminum / Vinyl	2	1940	2260	2	4	3
7283	13	Brick	1	1960	1267	1	3	1
7284	13	Brick	1	1968	1245	1	3	1
7285	13	Brick	1	1964	1126	1	3	1
7286	13	Aluminum / Vinyl	1	1960	985	1	3	1
7287	13	Aluminum / Vinyl	1	1960	966	1	3	2
7288	13	Aluminum / Vinyl	1	1951	960	1	3	1
7289	13	Aluminum / Vinyl	1	1960	941	1	3	1
7290	13	Brick	1	1954	864	1	3	1
7291	13	Aluminum / Vinyl	1	1947	732	1	2	1
7292	13	Aluminum / Vinyl	1	1948	686	1	2	1
7293	13	Aluminum / Vinyl	1	1912	972	1	3	2
7294	14	Brick	1	1953	1524	1	4	2
7295	14	Stucco	1.5	1940	1501	1	4	1
7296	14	Aluminum / Vinyl	1	1952	1096	1	4	1
7297	14	Aluminum / Vinyl	1	1950	1092	1	3	1
7298	14	Aluminum / Vinyl	2	1948	1248	1	3	1
7299	14	Brick	2	1900	2825	2	5	2
7300	14	Frame	2	1913	1616	2	4	2
7301	14	Frame	2	1913	1616	2	4	2
7302	14	Aluminum / Vinyl	1.5	1921	1404	2	3	2
7303	14	Aluminum / Vinyl	1	1923	1638	1	5	2
7304	14	Brick	1	1927	1297	1	3	1
7305	14	Aluminum / Vinyl	1	1926	924	1	3	1
7306	14	Aluminum / Vinyl	2	1897	2064	1	5	3
7307	14	Frame	2	1918	1514	1	2	1
7308	14	Frame	1	1910	1377	1	4	2
7309	14	Prem Wood	1	1923	1224	1	3	2
7310	14	Brick	2	1929	2008	1	3	1
7311	15	Aluminum / Vinyl	2	1922	2798	2	6	2
7312	15	Stucco	1	1913	1770	1	3	2
7313	15	Aluminum / Vinyl	1	1905	1276	1	5	1
7314	15	Aluminum / Vinyl	1	1890	1101	1	4	1
7315	1	Brick	1	1952	1256	1	4	1
7316	1	Aluminum / Vinyl	1	1958	985	1	3	1
7317	1	Frame	2	1940	1186	1	3	1
7318	1	Frame	1.5	1957	1618	2	4	2

7319	1 Aluminum / Vinyl	1	1954	963	1	3	2
7320	1 Aluminum / Vinyl	1	1940	898	1	3	1
7321	1 Aluminum / Vinyl	1	1952	882	1	2	1
7322	1 Aluminum / Vinyl	1	1950	876	1	2	1
7323	1 Aluminum / Vinyl	1	1951	689	1	2	1
7324	1 Brick	2	1928	2270	1	4	1
7325	2 Masonry / Frame	1.5	1960	1779	1	3	1
7326	2 Brick	1	1956	1242	1	3	1
7327	2 Brick	1	1956	1188	1	3	1
7328	2 Brick	1	1958	1152	1	3	1
7329	2 Aluminum / Vinyl	1	1957	914	1	3	2
7330	2 Aluminum / Vinyl	1	1954	870	1	3	1
7331	2 Aluminum / Vinyl	1	1951	792	1	2	1
7332	3 Brick	2	1924	1773	1	4	1
7333	3 Brick	2	1931	2552	2	4	2
7334	3 Aluminum / Vinyl	2	1923	2464	2	6	2
7335	3 Aluminum / Vinyl	1.5	1925	1838	2	4	2
7336	3 Brick	2	1901	4662	2	7	4
7337	3 Masonry / Frame	2	1905	3297	2	5	2
7338	3 Frame	2	1912	3075	2	7	2
7339	3 Aluminum / Vinyl	2	1910	2107	2	4	3
7340	3 Frame	1.5	1903	1664	2	3	2
7341	3 Aluminum / Vinyl	2	1900	1664	2	4	2
7342	3 Brick	2	1928	4588	1	6	3
7343	3 Brick	1.5	1919	4187	1	5	3
7344	3 Aluminum / Vinyl	1	1945	859	1	2	1
7345	3 Brick	2	1918	3579	1	4	3
7346	3 Masonry / Frame	2	1896	2922	1	4	1
7347	3 Brick	2	1929	2795	1	4	4
7348	3 Prem Wood	2	1885	1858	1	2	2
7349	3 Frame	1	1910	1501	1	3	1
7350	3 Brick	1.5	1921	1424	1	3	1
7351	3 Aluminum / Vinyl	1	1902	1173	1	3	1
7352	3 Aluminum / Vinyl	2	1914	2220	3	4	2
7353	4 Aluminum / Vinyl	1	1970	1104	1	3	1
7354	4 Frame	2	1906	2073	1	3	1
7355	4 Aluminum / Vinyl	1	1892	940	1	2	1
7356	5 Brick	1	1942	1452	1	3	1
7357	5 Brick	1	1954	1448	1	3	1
7358	5 Stone	1	1950	1433	1	4	2
7359	5 Brick	1	1951	1411	1	4	1
7360	5 Brick	1	1949	1328	1	3	1
7361	5 Brick	1	1949	1316	1	3	1

7362	5 Aluminum / Vinyl	1	1952	1225	1	3	2
7363	5 Aluminum / Vinyl	1	1948	1221	1	3	2
7364	5 Aluminum / Vinyl	1	1953	1217	1	4	2
7365	5 Brick	1	1952	1183	1	3	1
7366	5 Brick	1	1949	1156	1	3	1
7367	5 Brick	1	1949	1145	1	2	1
7368	5 Brick	1	1950	1134	1	2	1
7369	5 Aluminum / Vinyl	1	1949	1018	1	3	2
7370	5 Brick	1	1961	2238	2	5	3
7371	5 Brick	1.5	1952	2050	2	5	2
7372	5 Aluminum / Vinyl	1.5	1951	1510	2	4	2
7373	5 Brick	1	1956	1480	1	3	1
7374	5 Brick	1	1957	1335	1	3	1
7375	5 Aluminum / Vinyl	1	1956	1292	1	3	1
7376	5 Brick	1	1968	1290	1	3	1
7377	5 Frame	1	1971	1204	1	4	2
7378	5 Brick	1	1957	1102	1	2	1
7379	5 Masonry / Frame	1	1954	1065	1	3	1
7380	5 Aluminum / Vinyl	1	1955	1064	1	3	2
7381	5 Aluminum / Vinyl	1	1957	1060	1	3	1
7382	5 Aluminum / Vinyl	1	1956	1055	1	3	2
7383	5 Brick	1	1956	1020	1	3	1
7384	5 Aluminum / Vinyl	1	1956	1019	1	3	1
7385	5 Brick	1	1950	1009	1	3	1
7386	5 Aluminum / Vinyl	1	1954	1390	1	3	2
7387	5 Aluminum / Vinyl	1	1949	998	1	3	1
7388	5 Stone	2	1937	1568	1	3	1
7389	6 Aluminum / Vinyl	2	1922	2436	2	4	2
7390	6 Stucco	1.5	1904	1737	2	4	2
7391	6 Aluminum / Vinyl	1.5	1890	1736	2	4	2
7392	6 Aluminum / Vinyl	2	1894	2064	1	4	1
7393	6 Frame	2	1912	2960	3	6	3
7394	7 Stone	1.5	1941	2029	1	3	2
7395	7 Brick	1	1947	1501	1	3	1
7396	7 Aluminum / Vinyl	1	1945	1054	1	3	1
7397	7 Brick	2	1934	2240	1	4	1
7398	7 Stone	1	1950	1262	1	2	1
7399	7 Aluminum / Vinyl	1	1932	1359	1	3	3
7400	8 Stucco	1	1910	600	1	2	1
7401	8 Aluminum / Vinyl	1.5	1907	1969	2	4	2
7402	8 Frame	1.5	1900	1426	2	3	2
7403	8 Aluminum / Vinyl	1.5	1908	1760	1	5	2
7404	8 Brick	1	1920	1644	1	4	2

7405	8	Aluminum / Vinyl	1	1918	1544	1	4	1
7406	9	Aluminum / Vinyl	1	1974	1450	1	3	2
7407	9	Aluminum / Vinyl	2	2010	2044	1	4	2
7408	9	Aluminum / Vinyl	1	1970	1460	1	3	1
7409	9	Aluminum / Vinyl	1	1960	1117	1	3	2
7410	9	Aluminum / Vinyl	1	1968	1110	1	3	1
7411	9	Brick	1	1957	1050	1	3	1
7412	9	Aluminum / Vinyl	2	1970	2423	2	6	2
7413	10	Stone	1	1947	2310	1	3	3
7414	10	Stone	1.5	1936	1663	1	3	1
7415	10	Stone	1	1946	1549	1	3	2
7416	10	Aluminum / Vinyl	1.5	1948	1380	1	4	1
7417	10	Aluminum / Vinyl	1.5	1953	1338	1	3	2
7418	10	Brick	1	1938	1307	1	3	1
7419	10	Aluminum / Vinyl	1	1952	1277	1	4	1
7420	10	Stone	2	1940	2152	1	3	1
7421	10	Masonry / Frame	2	1946	1570	1	3	1
7422	10	Aluminum / Vinyl	2	1925	3714	2	5	2
7423	10	Aluminum / Vinyl	2	1926	2816	2	4	2
7424	10	Brick	2	1929	2771	2	5	2
7425	10	Aluminum / Vinyl	2	1918	2503	2	4	2
7426	10	Aluminum / Vinyl	2	1924	1924	2	4	2
7427	10	Stone	2	1945	2544	2	4	2
7428	10	Masonry / Frame	2	1947	2302	2	4	2
7429	10	Aluminum / Vinyl	1.5	1885	1607	2	4	2
7430	10	Brick	1	1920	2286	1	5	1
7431	10	Frame	1.5	1931	1904	1	3	2
7432	10	Brick	1	1926	1401	1	2	1
7433	10	Aluminum / Vinyl	1	1925	1384	1	3	1
7434	10	Aluminum / Vinyl	1	1954	1232	1	3	1
7435	10	Stucco	1.5	1915	2003	1	4	2
7436	10	Stone	1.5	1934	1992	1	3	1
7437	10	Aluminum / Vinyl	1	1926	1981	1	3	2
7438	10	Brick	1.5	1926	1258	1	2	1
7439	10	Aluminum / Vinyl	1	1929	1132	1	3	1
7440	10	Frame	1	1924	888	1	2	1
7441	10	Stone	1.5	1937	1796	1	3	1
7442	10	Brick	1.5	1930	1618	1	3	1
7443	11	Aluminum / Vinyl	1	1942	1208	1	4	1
7444	11	Brick	1	1940	1186	1	3	1
7445	11	Aluminum / Vinyl	1	1948	998	1	3	1
7446	11	Stone	2	1937	1652	1	3	1
7447	11	Aluminum / Vinyl	2	1974	1345	1	4	1

7448	11	Aluminum / Vinyl	2	1942	1288	1	3	1
7449	11	Brick	1	1954	2350	2	5	2
7450	11	Frame	1.5	1904	1706	2	3	2
7451	11	Stone	1	1949	1363	1	2	1
7452	11	Aluminum / Vinyl	1	1958	1172	1	3	1
7453	11	Aluminum / Vinyl	1	1959	1142	1	3	1
7454	11	Frame	1	1956	1090	1	3	1
7455	11	Aluminum / Vinyl	1	1956	1073	1	3	2
7456	11	Aluminum / Vinyl	1	1953	1064	1	3	2
7457	11	Brick	1	1958	1037	1	3	1
7458	11	Brick	1	1954	999	1	3	2
7459	11	Aluminum / Vinyl	1	1957	971	1	2	1
7460	11	Brick	1	1951	896	1	2	1
7461	11	Aluminum / Vinyl	1	1954	869	1	3	1
7462	11	Aluminum / Vinyl	1	1956	864	1	3	1
7463	11	Aluminum / Vinyl	1	1942	734	1	2	1
7464	11	Aluminum / Vinyl	1	1948	720	1	2	1
7465	11	Brick	2	1958	2768	3	6	3
7466	12	Aluminum / Vinyl	2	1914	2248	2	6	2
7467	13	Brick	1	1950	1503	1	4	2
7468	13	Aluminum / Vinyl	1	1958	1468	1	4	2
7469	13	Aluminum / Vinyl	1	1946	1165	1	3	1
7470	13	Brick	1	1949	1155	1	3	1
7471	13	Stone	2	1939	1749	1	3	1
7472	13	Aluminum / Vinyl	1	1913	1662	1	4	1
7473	13	Brick	1	1968	1748	1	3	1
7474	13	Aluminum / Vinyl	1	1974	1584	1	3	1
7475	13	Brick	1	1960	1284	1	3	1
7476	13	Brick	1	1969	1266	1	3	1
7477	13	Brick	1	1967	1248	1	3	1
7478	13	Aluminum / Vinyl	1	1964	1112	1	3	1
7479	13	Aluminum / Vinyl	1	1952	1001	1	3	1
7480	13	Aluminum / Vinyl	1	1959	1000	1	3	1
7481	13	Aluminum / Vinyl	1	1963	980	1	3	1
7482	13	Aluminum / Vinyl	1	1934	953	1	2	1
7483	13	Aluminum / Vinyl	1	1959	877	1	3	1
7484	13	Aluminum / Vinyl	1	1942	760	1	2	1
7485	13	Aluminum / Vinyl	2	1925	869	1	2	1
7486	14	Aluminum / Vinyl	1.5	1949	1422	1	4	2
7487	14	Aluminum / Vinyl	1	1943	1158	1	3	1
7488	14	Brick	1	1953	1063	1	3	1
7489	14	Aluminum / Vinyl	1	1944	1004	1	3	1
7490	14	Aluminum / Vinyl	1	1947	854	1	2	1

7491	14	Aluminum / Vinyl	2	1940	1426	1	4	2
7492	14	Aluminum / Vinyl	1	1890	1570	1	2	2
7493	14	Aluminum / Vinyl	1	1900	915	1	3	1
7494	14	Aluminum / Vinyl	2	1929	2660	2	5	2
7495	14	Brick	1.5	1946	1450	2	4	2
7496	14	Aluminum / Vinyl	2	1907	1976	2	4	2
7497	14	Frame	1	1908	1805	2	6	2
7498	14	Aluminum / Vinyl	1.5	1928	1741	1	4	1
7499	14	Aluminum / Vinyl	1	1928	1452	1	3	2
7500	14	Aluminum / Vinyl	1	1924	1320	1	4	1
7501	14	Aluminum / Vinyl	1	1928	1230	1	3	2
7502	14	Aluminum / Vinyl	1	1928	1229	1	3	1
7503	14	Aluminum / Vinyl	1	1929	1021	1	2	1
7504	14	Frame	1	1955	1134	1	3	1
7505	14	Aluminum / Vinyl	1	1952	1012	1	3	1
7506	14	Aluminum / Vinyl	1	1949	725	1	2	1
7507	14	Aluminum / Vinyl	1.5	1916	1694	1	4	1
7508	14	Aluminum / Vinyl	1.5	1927	1548	1	4	1
7509	14	Aluminum / Vinyl	1.5	1880	1444	1	3	1
7510	14	Aluminum / Vinyl	1	1913	1433	1	3	2
7511	14	Aluminum / Vinyl	1	1918	1276	1	2	1
7512	14	Aluminum / Vinyl	1	1900	1255	1	2	2
7513	14	Aluminum / Vinyl	1	1883	1218	1	3	1
7514	14	Aluminum / Vinyl	1	1905	1059	1	3	1
7515	14	Frame	1	1890	1052	1	2	1
7516	14	Aluminum / Vinyl	1	1929	1014	1	2	1
7517	14	Aluminum / Vinyl	1	1918	952	1	2	1
7518	15	Fiber-Cement	2	2011	2000	1	3	2
7519	15	Aluminum / Vinyl	2	2013	1854	1	3	2
7520	15	Aluminum / Vinyl	2	1915	2706	2	6	2
7521	15	Frame	2	1912	2172	2	4	2
7522	15	Brick	1	1919	1981	1	4	2
7523	15	Aluminum / Vinyl	1	1919	1699	1	4	2
7524	1	Brick	1	1953	1467	1	4	1
7525	1	Block	2	1945	1662	2	4	2
7526	2	Aluminum / Vinyl	1	1953	1152	1	3	1
7527	2	Aluminum / Vinyl	1	1955	1118	1	3	1
7528	2	Aluminum / Vinyl	1	1955	1114	1	4	1
7529	2	Aluminum / Vinyl	1.5	1963	2258	2	5	2
7530	2	Aluminum / Vinyl	1	1963	1253	1	4	1
7531	2	Brick	1	1957	1232	1	3	1
7532	2	Brick	1	1953	1223	1	3	1
7533	2	Brick	1	1962	1199	1	3	1

7534	2	Frame	1	1970	1120	1	4	1
7535	2	Aluminum / Vinyl	1	1957	909	1	3	1
7536	2	Aluminum / Vinyl	1	1955	1414	1	3	1
7537	3	Aluminum / Vinyl	2	1930	2748	2	6	2
7538	3	Aluminum / Vinyl	2	1925	2685	2	4	2
7539	3	Aluminum / Vinyl	1.5	1924	1890	2	5	2
7540	3	Frame	2	1961	1800	2	4	2
7541	3	Aluminum / Vinyl	2	1914	2382	2	4	2
7542	3	Aluminum / Vinyl	2	1890	2220	2	4	2
7543	3	Aluminum / Vinyl	2	1898	2188	2	4	2
7544	3	Aluminum / Vinyl	1.5	1904	2020	2	4	2
7545	3	Aluminum / Vinyl	1.5	1906	1495	2	4	2
7546	3	Brick	2	1908	3878	1	6	3
7547	3	Brick	2	1915	3666	1	5	3
7548	3	Frame	2	1901	2592	1	3	1
7549	3	Stucco	2	1920	2314	1	3	2
7550	3	Masonry / Frame	2	1908	2195	1	5	2
7551	3	Frame	1.5	1901	2121	1	3	3
7553	3	Frame	1.5	1890	1990	1	4	1
7554	3	Fiber-Cement	2	1890	1674	1	3	1
7555	5	Brick	1	1951	2000	1	3	2
7556	5	Brick	1	1951	1635	1	5	1
7557	5	Aluminum / Vinyl	1.5	1950	1453	1	4	2
7558	5	Brick	1	1950	1421	1	3	1
7559	5	Brick	1.5	1937	1413	1	2	1
7560	5	Brick	1	1948	1392	1	4	1
7561	5	Aluminum / Vinyl	1.5	1940	1351	1	2	1
7562	5	Brick	1	1949	1322	1	3	1
7563	5	Aluminum / Vinyl	1	1955	1316	1	4	1
7564	5	Brick	1	1951	1189	1	2	1
7565	5	Stone	1.5	1947	1188	1	3	1
7566	5	Brick	1	1953	1167	1	2	1
7567	5	Brick	1	1948	1149	1	3	1
7568	5	Brick	1	1952	1125	1	3	1
7569	5	Brick	1	1947	1124	1	3	1
7570	5	Aluminum / Vinyl	1	1952	1080	1	4	2
7571	5	Aluminum / Vinyl	1	1949	1036	1	3	1
7572	5	Aluminum / Vinyl	1	1949	1004	1	3	1
7573	5	Aluminum / Vinyl	1	1953	1003	1	4	2
7574	5	Aluminum / Vinyl	1	1950	1000	1	3	1
7575	5	Aluminum / Vinyl	1	1950	921	1	3	1
7576	5	Aluminum / Vinyl	2	2012	3379	1	4	3
7577	5	Aluminum / Vinyl	1	1952	1486	1	3	1

7578	5	Brick	1	1955	1246	1	3	2
7579	5	Brick	1	1957	1224	1	3	1
7580	5	Aluminum / Vinyl	1	1954	1220	1	2	1
7581	5	Aluminum / Vinyl	1	1960	1202	1	3	1
7582	5	Brick	1	1957	1164	1	3	2
7583	5	Brick	1	1958	1138	1	3	1
7584	5	Aluminum / Vinyl	1	1958	1040	1	3	1
7585	5	Aluminum / Vinyl	1	1950	1032	1	3	1
7586	5	Brick	1	1952	1014	1	3	1
7587	5	Aluminum / Vinyl	1	1955	1008	1	3	1
7588	5	Aluminum / Vinyl	1	1952	998	1	3	1
7589	5	Aluminum / Vinyl	1	1951	992	1	3	1
7590	5	Brick	1	1945	990	1	2	2
7591	5	Aluminum / Vinyl	1	1954	984	1	3	1
7592	5	Aluminum / Vinyl	1	1957	963	1	3	2
7593	5	Aluminum / Vinyl	1	1956	948	1	2	1
7594	5	Aluminum / Vinyl	1	1958	919	1	3	1
7595	5	Frame	1	1948	916	1	2	1
7596	5	Aluminum / Vinyl	1	1950	912	1	3	1
7597	5	Aluminum / Vinyl	1	1950	768	1	2	1
7598	5	Aluminum / Vinyl	1	1950	687	1	2	1
7599	5	Aluminum / Vinyl	1	1950	672	1	2	1
7600	6	Aluminum / Vinyl	1.5	1923	1982	2	4	2
7601	6	Aluminum / Vinyl	1.5	1926	1858	2	4	2
7602	6	Aluminum / Vinyl	1.5	1903	1688	2	4	2
7603	6	Aluminum / Vinyl	1	1926	1315	1	3	1
7604	6	Brick	2	1890	2850	1	3	3
7605	7	Aluminum / Vinyl	1	1940	1198	1	3	1
7606	7	Brick	1.5	1946	1075	1	2	1
7607	7	Aluminum / Vinyl	1	1938	817	1	3	1
7608	8	Brick	2	1913	2150	1	4	1
7609	8	Aluminum / Vinyl	1	1900	1151	1	3	1
7610	8	Aluminum / Vinyl	1.5	1926	1875	2	5	3
7611	8	Aluminum / Vinyl	1.5	1927	1805	2	4	2
7612	8	Aluminum / Vinyl	1	1922	1288	1	4	1
7613	8	Frame	2	1904	2168	1	4	2
7614	8	Frame	2	1913	2024	1	4	1
7615	8	Aluminum / Vinyl	1.5	1914	1481	1	3	1
7616	8	Aluminum / Vinyl	1	1924	1341	1	3	2
7617	8	Aluminum / Vinyl	1	1903	1222	1	3	1
7618	9	Aluminum / Vinyl	2	1969	1791	1	4	2
7619	9	Aluminum / Vinyl	1	2006	1888	1	4	2
7620	9	Aluminum / Vinyl	1	1966	1421	1	3	1

7621	9	Aluminum / Vinyl	1	1963	1205	1	4	2
7622	9	Frame	1	1968	1063	1	3	1
7623	9	Brick	1	1957	1050	1	3	1
7624	9	Aluminum / Vinyl	1	1975	908	1	3	1
7625	10	Stone	1.5	1937	1874	1	4	1
7626	10	Aluminum / Vinyl	1	1942	1591	1	4	1
7627	10	Brick	1.5	1935	1571	1	3	1
7628	10	Stone	1	1935	1490	1	2	1
7629	10	Brick	1	1946	1038	1	3	1
7630	10	Aluminum / Vinyl	1	1953	1015	1	4	1
7631	10	Stone	2	1937	1960	1	4	2
7632	10	Masonry / Frame	2	1937	1951	1	3	1
7633	10	Brick	2	1940	1417	1	3	1
7634	10	Aluminum / Vinyl	2	1951	1396	1	3	1
7635	10	Aluminum / Vinyl	1	1924	700	1	1	1
7636	10	Aluminum / Vinyl	2	1913	2596	2	6	2
7637	10	Aluminum / Vinyl	2	1924	2427	2	4	2
7638	10	Aluminum / Vinyl	2	1921	2328	2	6	2
7639	10	Frame	1.5	1917	1977	2	4	2
7640	10	Aluminum / Vinyl	1	1920	1763	1	4	2
7641	10	Aluminum / Vinyl	1	1920	1746	1	4	2
7642	10	Aluminum / Vinyl	1	1926	1729	1	3	2
7643	10	Aluminum / Vinyl	1	1920	1727	1	4	1
7644	10	Aluminum / Vinyl	1	1925	1683	1	4	2
7645	10	Frame	1	1916	1617	1	4	2
7646	10	Brick	1	1924	1580	1	2	1
7647	10	Aluminum / Vinyl	1	1930	1491	1	3	1
7648	10	Aluminum / Vinyl	1	1930	1491	1	3	1
7649	10	Frame	1	1928	1336	1	3	2
7650	10	Aluminum / Vinyl	1.5	1919	1329	1	3	1
7651	10	Frame	1	1956	1155	1	3	2
7652	10	Aluminum / Vinyl	1	1953	972	1	3	1
7653	10	Frame	1	1949	914	1	1	1
7654	10	Brick	2	1927	1876	1	2	1
7655	10	Stucco	1	1921	1299	1	3	2
7656	10	Frame	1	1910	977	1	3	1
7657	10	Aluminum / Vinyl	1	1926	932	1	3	1
7658	10	Frame	1	1922	812	1	2	1
7659	10	Aluminum / Vinyl	1	1926	697	1	2	1
7660	11	Fiber-Cement	1	2004	1969	1	3	2
7661	11	Stone	1	1940	1645	1	4	1
7662	11	Stone	1.5	1937	1548	1	4	1
7663	11	Brick	1	1947	1476	1	3	2

7664	11	Brick	1	1954	1437	1	4	1
7665	11	Aluminum / Vinyl	1.5	1940	1223	1	3	1
7666	11	Aluminum / Vinyl	1	1949	1086	1	3	2
7667	11	Aluminum / Vinyl	1.5	1963	1960	2	5	3
7668	11	Prem Wood	1	1968	1873	1	3	1
7669	11	Brick	1	1965	1407	1	3	1
7670	11	Aluminum / Vinyl	1	1954	1396	1	2	2
7671	11	Stone	1	1955	1299	1	3	1
7672	11	Aluminum / Vinyl	1	1959	1266	1	3	1
7673	11	Aluminum / Vinyl	1	1963	1150	1	3	1
7674	11	Aluminum / Vinyl	1	1949	1126	1	2	1
7676	11	Brick	1	1963	1124	1	3	1
7677	11	Brick	1	1955	1069	1	3	1
7678	11	Brick	1	1954	1053	1	3	1
7679	11	Stone	1	1947	1042	1	2	1
7680	11	Brick	1	1958	1041	1	3	1
7681	11	Brick	1	1958	1037	1	3	1
7682	11	Aluminum / Vinyl	1	1958	1035	1	3	1
7683	11	Aluminum / Vinyl	1	1964	1028	1	3	1
7684	11	Aluminum / Vinyl	1	1957	994	1	3	2
7685	11	Brick	1	1956	994	1	3	2
7686	11	Aluminum / Vinyl	1	1954	957	1	3	1
7687	11	Aluminum / Vinyl	1	1955	948	1	3	2
7688	11	Aluminum / Vinyl	1	1953	864	1	3	1
7689	11	Brick	1	1954	838	1	2	1
7690	11	Aluminum / Vinyl	1	1950	638	1	2	1
7691	11	Aluminum / Vinyl	2	1968	2172	2	6	2
7692	12	Aluminum / Vinyl	1	1925	1122	1	3	1
7693	12	Aluminum / Vinyl	1.5	1870	1679	1	4	1
7694	13	Aluminum / Vinyl	1	1976	1850	1	4	2
7695	13	Brick	1	1950	1470	1	3	1
7696	13	Aluminum / Vinyl	1	1958	1464	1	5	2
7697	13	Aluminum / Vinyl	1	1951	1407	1	3	1
7698	13	Aluminum / Vinyl	1	1951	1369	1	3	1
7699	13	Frame	1	1940	1251	1	3	2
7700	13	Brick	1	1951	1166	1	3	1
7701	13	Brick	1	1947	1162	1	3	2
7702	13	Brick	1	1950	1134	1	3	1
7703	13	Brick	1	1952	988	1	3	1
7704	13	Stone	2	1938	1433	1	2	1
7705	13	Aluminum / Vinyl	1.5	1928	1888	2	5	2
7706	13	Frame	1	1928	1511	1	5	1
7707	13	Brick	1	1926	1499	1	3	1

7708	13	Stucco	1	1922	1459	1	4	2
7709	13	Aluminum / Vinyl	1	1961	1223	1	3	1
7710	13	Aluminum / Vinyl	1	1961	1201	1	3	2
7711	13	Brick	1	1952	1108	1	2	2
7712	13	Brick	1	1956	1093	1	2	1
7713	13	Aluminum / Vinyl	1	1970	1080	1	4	1
7714	13	Aluminum / Vinyl	1	1959	1067	1	3	1
7715	13	Aluminum / Vinyl	1	1960	1046	1	3	1
7716	13	Aluminum / Vinyl	1	1959	896	1	3	1
7717	13	Aluminum / Vinyl	1	1944	719	1	2	1
7718	13	Aluminum / Vinyl	1	1943	608	1	1	1
7719	14	Brick	1	1952	1262	1	3	1
7720	14	Aluminum / Vinyl	1	1947	1235	1	3	1
7721	14	Aluminum / Vinyl	1	1950	1148	1	3	1
7722	14	Aluminum / Vinyl	1	1942	979	1	3	2
7723	14	Aluminum / Vinyl	2	1948	1378	1	3	1
7724	14	Aluminum / Vinyl	2	1964	1298	1	3	1
7725	14	Aluminum / Vinyl	2	1941	1213	1	2	1
7726	14	Aluminum / Vinyl	2	1945	990	1	2	1
7727	14	Aluminum / Vinyl	1	1898	998	1	2	1
7728	14	Aluminum / Vinyl	2	1927	2320	2	4	2
7729	14	Aluminum / Vinyl	2	1928	2108	2	4	2
7730	14	Brick	2	1958	2306	2	6	2
7731	14	Brick	1.5	1957	2039	2	5	2
7732	14	Aluminum / Vinyl	2	1906	3183	2	6	2
7733	14	Aluminum / Vinyl	2	1890	2703	2	5	3
7734	14	Frame	2	1894	2321	2	4	2
7735	14	Aluminum / Vinyl	1.5	1925	1860	1	4	2
7736	14	Aluminum / Vinyl	1	1926	1849	1	4	2
7737	14	Brick	1	1928	1791	1	3	2
7738	14	Aluminum / Vinyl	1.5	1915	1715	1	3	2
7739	14	Aluminum / Vinyl	1	1923	1617	1	3	2
7740	14	Aluminum / Vinyl	1	1927	1072	1	3	1
7741	14	Aluminum / Vinyl	2	1924	2096	1	4	3
7742	14	Aluminum / Vinyl	1.5	1917	1665	1	3	2
7743	14	Aluminum / Vinyl	2	1901	1450	1	4	2
7744	14	Aluminum / Vinyl	1	1888	1419	1	4	1
7745	14	Aluminum / Vinyl	1	1910	1352	1	3	2
7746	14	Aluminum / Vinyl	2	1905	1342	1	3	1
7747	14	Aluminum / Vinyl	1	1890	1275	1	2	1
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7724	3690	15887	155000	FALSE	FALSE
7725	5828	15887	156000	FALSE	FALSE
7726	5280	15887	127500	FALSE	FALSE
7727	3700	15887	190000	FALSE	TRUE
7728	4920	15887	176000	FALSE	FALSE
7729	3600	15887	238000	FALSE	TRUE
7730	6500	15887	168500	FALSE	FALSE
7731	5130	15887	163000	FALSE	FALSE
7732	2400	15887	171000	FALSE	FALSE
7733	3600	15887	152000	FALSE	FALSE
7734	4000	15887	219500	FALSE	TRUE
7735	4560	15887	242000	FALSE	FALSE
7736	5200	15887	224500	FALSE	FALSE
7737	4920	15887	230500	FALSE	FALSE
7738	3900	15887	253500	FALSE	FALSE
7739	4680	15887	233500	FALSE	FALSE
7740	3750	15887	174500	FALSE	TRUE
7741	4080	15887	299000	FALSE	FALSE
7742	3000	15887	206000	FALSE	FALSE
7743	5616	15887	210000	FALSE	FALSE
7744	3045	15887	165000	FALSE	FALSE
7745	18480	15887	210000	FALSE	FALSE
7746	3270	15887	285000	FALSE	TRUE
7747	6400	15887	120000	FALSE	FALSE
7748	3399	15887	120000	FALSE	FALSE
7749	3600	15887	94900	FALSE	FALSE

[ reached 'max' / getOption("max.print") -- omitted 16751 rows ]

```

model2=lm(sqrt(Sale_price)~District + Extwall + Stories + Year_Built+ District*Year_Built+
           Fbath + log(Lotsize) + Sale_date +District* log(Lotsize),df_clean4)
# model2=lm(Sale_price^(0.4)~,df_clean3)

```

```

summ2=summary(model2); summ2

```

Call:

```

lm(formula = sqrt(Sale_price) ~ District + Extwall + Stories +
    Year_Built + District * Year_Built + Fin_sqft + Units + Bdrms +
    Fbath + log(Lotsize) + Sale_date + District * log(Lotsize),
    data = df_clean4)

```

Residuals:

Min	1Q	Median	3Q	Max
-547.36	-35.61	5.89	41.47	474.14

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	1.396e+03	9.630e+01	14.494	< 2e-16 ***
District	-2.441e+02	9.158e+00	-26.656	< 2e-16 ***
ExtwallBlock	-6.108e+00	6.044e+00	-1.011	0.312259
ExtwallBrick	1.146e+01	1.183e+00	9.684	< 2e-16 ***
ExtwallFiber-Cement	2.442e+01	6.115e+00	3.993	6.55e-05 ***
ExtwallFrame	-1.069e+01	1.599e+00	-6.682	2.41e-11 ***
ExtwallMasonry / Frame	8.342e+00	2.797e+00	2.983	0.002858 **
ExtwallPrem Wood	1.492e+01	9.195e+00	1.622	0.104761
ExtwallStone	9.094e+00	2.497e+00	3.641	0.000272 ***
ExtwallStucco	1.537e+01	3.511e+00	4.378	1.20e-05 ***
Stories1	4.059e+01	1.680e+01	2.416	0.015681 *
Stories1.5	5.480e+01	1.677e+01	3.268	0.001084 **
Stories2	6.143e+01	1.670e+01	3.678	0.000236 ***
Year_Built	-9.488e-01	5.316e-02	-17.847	< 2e-16 ***
Fin_sqft	9.479e-02	1.565e-03	60.560	< 2e-16 ***
Units1	1.238e+02	1.200e+01	10.312	< 2e-16 ***
Units2	2.178e+01	1.201e+01	1.813	0.069845 .
Units3	-2.191e+01	1.293e+01	-1.695	0.090108 .
Bdrms0	1.493e+02	3.025e+01	4.936	8.03e-07 ***
Bdrms1	1.229e+02	1.648e+01	7.455	9.28e-14 ***
Bdrms2	1.344e+02	1.472e+01	9.133	< 2e-16 ***
Bdrms3	1.393e+02	1.462e+01	9.524	< 2e-16 ***

```

Bdrms4           1.213e+02  1.456e+01   8.327 < 2e-16 ***
Bdrms5           1.187e+02  1.456e+01   8.151 3.78e-16 ***
Bdrms6           9.863e+01  1.459e+01   6.762 1.39e-11 ***
Bdrms7           6.771e+01  1.555e+01   4.353 1.35e-05 ***
Bdrms8           9.538e+01  1.636e+01   5.829 5.65e-09 ***
Fbath0          -6.106e+01  2.227e+01  -2.742 0.006118 **
Fbath1          -3.703e+01  1.553e+01  -2.385 0.017096 *
Fbath2          -1.015e+01  1.543e+01  -0.658 0.510580
Fbath3           3.187e+01  1.532e+01   2.080 0.037538 *
Fbath4           6.184e+01  1.643e+01   3.764 0.000168 ***
log(Lotsize)    3.120e+01  3.416e+00   9.133 < 2e-16 ***
Sale_date        5.995e-03  4.263e-04  14.064 < 2e-16 ***
District:Year_Built 1.315e-01  5.309e-03  24.762 < 2e-16 ***
District:log(Lotsize) -8.262e-01  3.469e-01  -2.382 0.017230 *
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 71.77 on 24407 degrees of freedom  
 Multiple R-squared: 0.4635, Adjusted R-squared: 0.4627  
 F-statistic: 602.4 on 35 and 24407 DF, p-value: < 2.2e-16

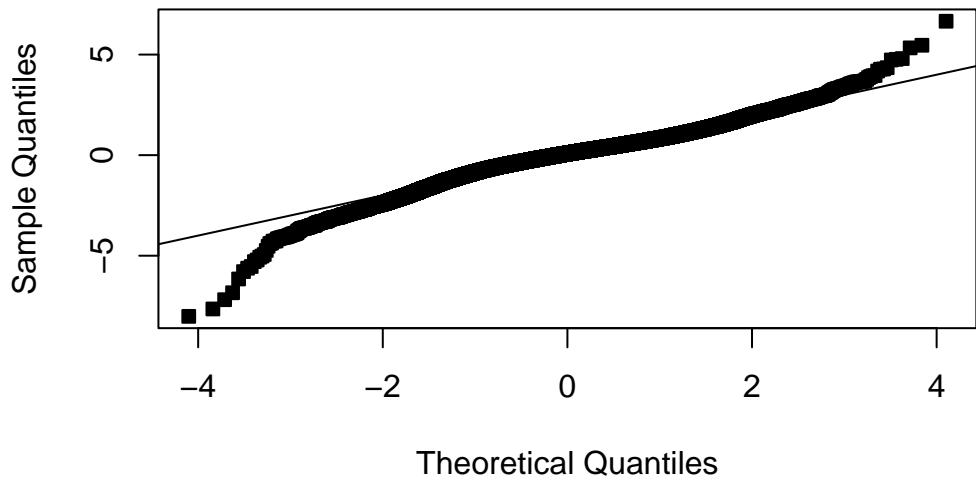
```
summ2$adj.r.squared
```

```
[1] 0.4626948
```

```
student_res2=rstudent(model2)

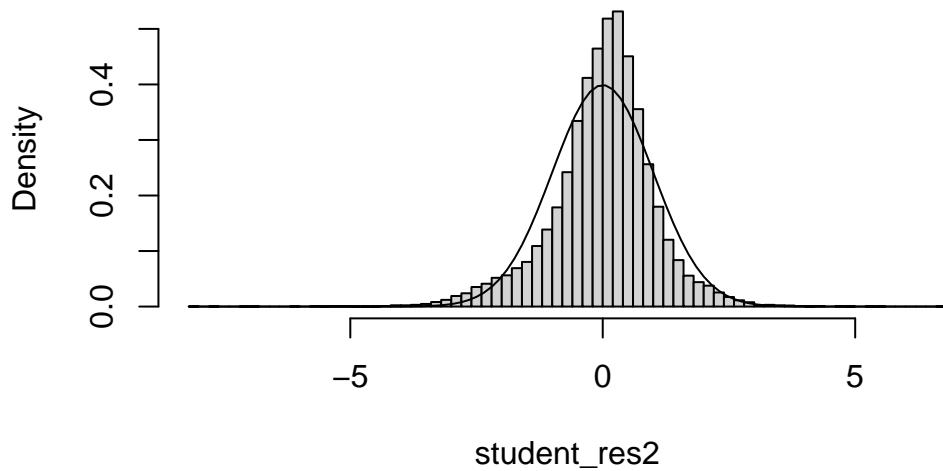
MSE2=summ2$sigma^2
qqnorm(student_res2,pch=22, bg=1)
abline(0,1)
```

### Normal Q-Q Plot

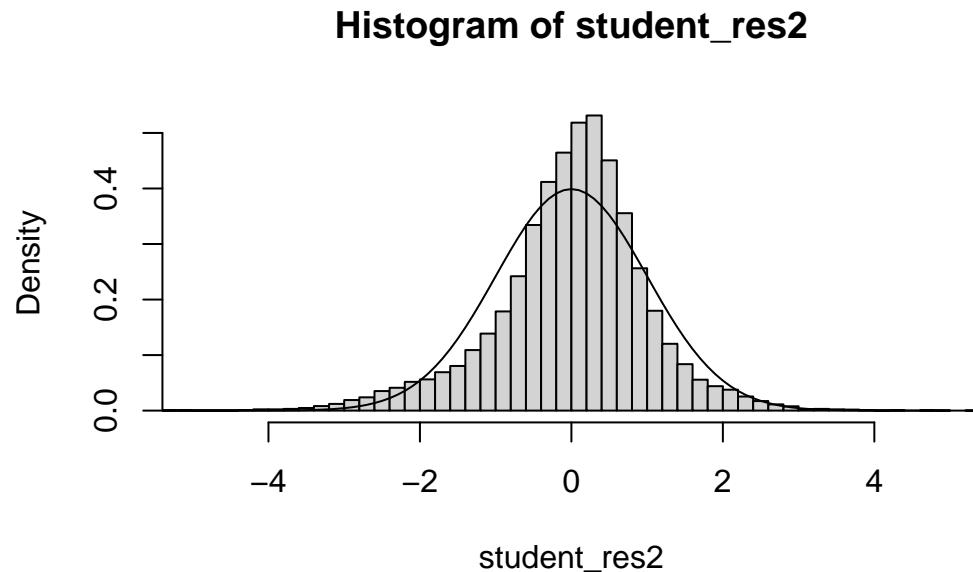


```
hist(student_res2,freq=F,breaks=100)
curve(dnorm(x,0,1),add=T)
```

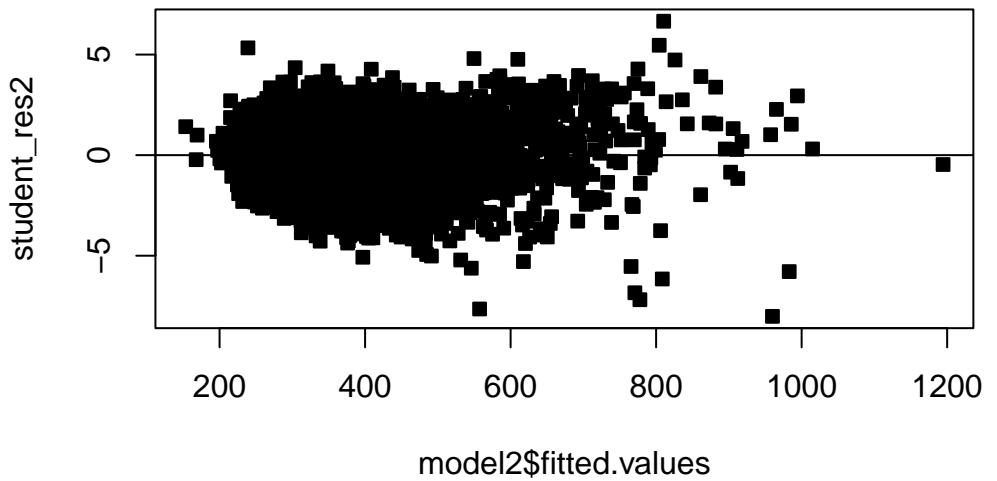
### Histogram of student\_res2



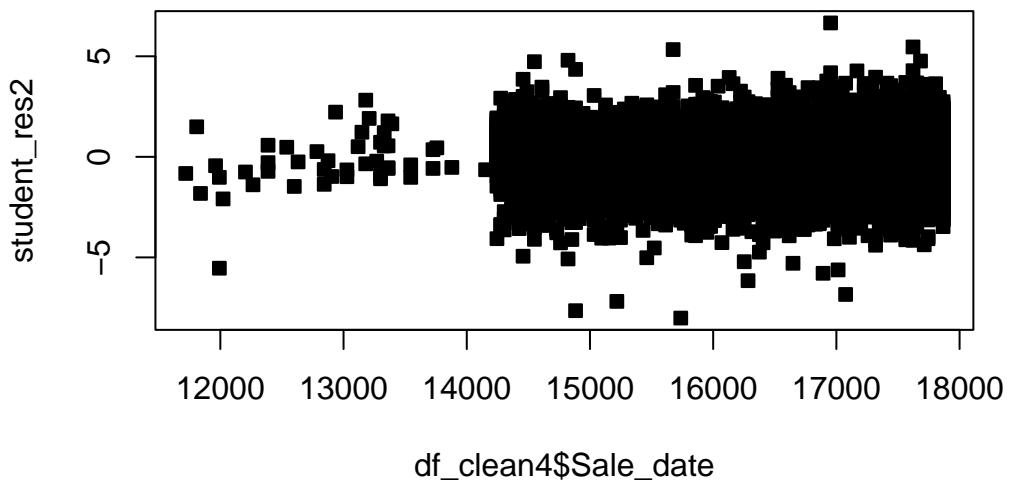
```
hist(student_res2,freq=F,xlim=c(-5,5),breaks=100)
curve(dnorm(x,0,1),add=T)
```



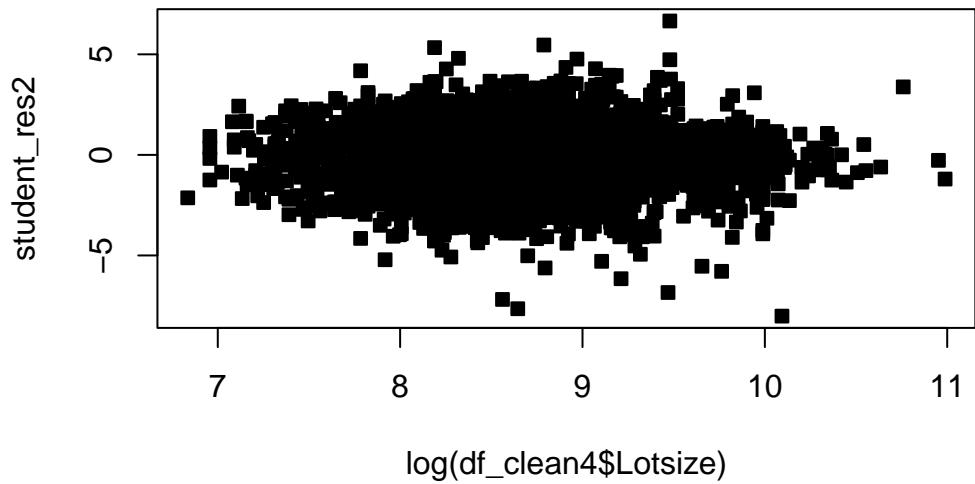
```
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



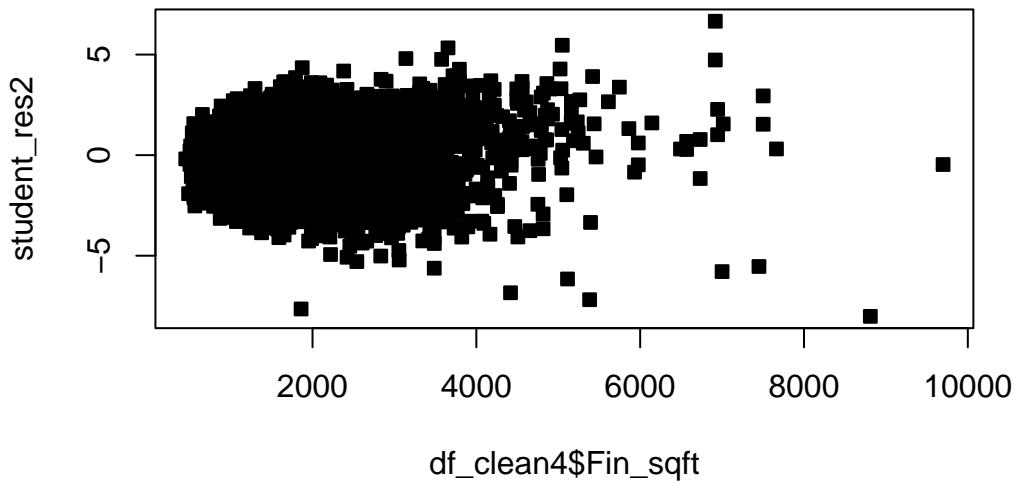
```
plot(df_clean4$Sale_date ,student_res2,pch=22,bg=1)
```



```
plot(log(df_clean4$Lotsize) ,student_res2,pch=22, bg=1)
```

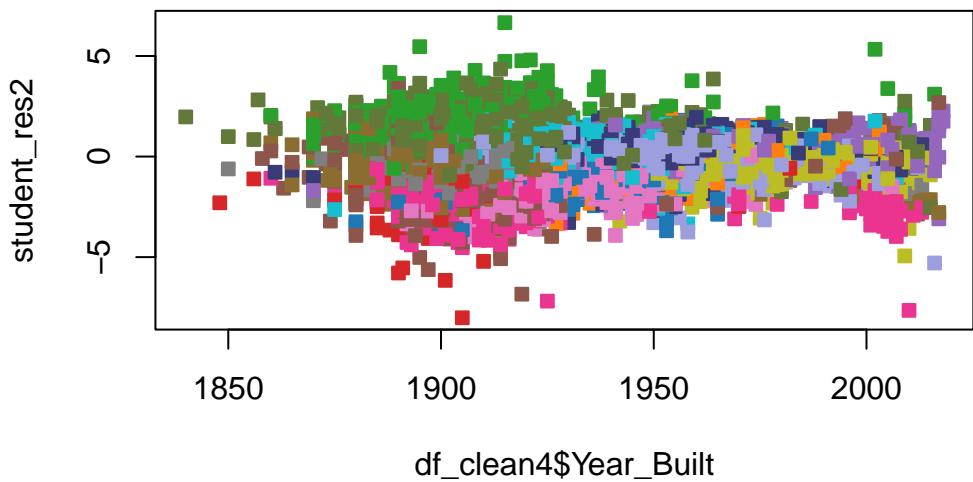


```
plot(df_clean4$Fin_sqft ,student_res2,pch=22, bg=1)
```



```
#Year built is probably nonlinear...
```

```
plot(df_clean4$Year_Built ,student_res2,pch=22,bg=custom_palette[df_clean4$District],col=c
```



## 6.5 Homework questions

**Exercise 6.2.** Consider a ML regression model for bread quality against bake time and 3 types of yeast (A, B and C). Write out the dummy variables for the variable yeast type. What is the interpretation of the coefficient of each of the dummy variables, in this context?

**Exercise 6.3.** Suppose we regress real estate price against number of bathrooms. What is the difference in interpretation between representing number of bedrooms with dummy variables versus a continuous variable?

**Exercise 6.4.** Consider a ML regression model for bread quality against bake time and 3 types of yeast (A, B and C). Write out the regression equation that includes an interaction between yeast and bake time. What is the interpretation of the coefficient for each of the interaction effects? Compare and contrast the regression model in Exercise 6.2 to this one.

Complete the Chapter 8 questions.

# 7 Leverage and Influence

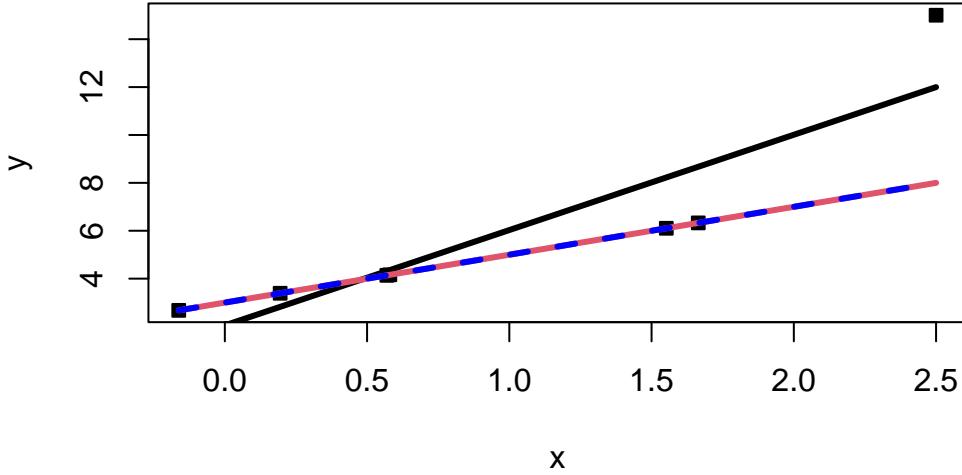
## 7.1 Influential observations and leverage

Recall that violations of model assumptions are more likely at remote points, and these violations may be hard to detect from inspection of the ordinary residuals because their residuals will usually be smaller. Points that are outlying in the  $x$ -direction are known as **leverage points**. **Influential points** are not only remote in terms of the specific values for the regressors, but the observed response is not consistent with the values that would be predicted based on only the other data points. It is important to find these influential points and assess their impact on the model.

Below gives an example of an influential point. The seventh point in the data set is outlying in the  $x$ -direction, and its response value is not consistent with the regression line based on the other six observations:

```
set.seed(330)
x=c(rnorm(6),2.5)
y=x*2+3
y[7]=y[7]+7
plot(x,y,pch=22,bg=1)
a=lm(y~x)
curve(a$coefficients[1]+x*a$coefficients[2],add=T,lwd=3)
curve(x*2+3,add=T,col=2,lwd=3)

a2=lm(y[-7]~x[-7])
curve(a2$coefficients[1]+x*a2$coefficients[2],add=T,lwd=3,col='blue',lty=2)
```



```
a$coefficients
```

(Intercept)	x
2.048937	3.979977

Sometimes we find that a regression coefficient may have a sign that does not make engineering or scientific sense, a regressor known to be important may be statistically insignificant, or a model that fits the data well and that is logical from an application – environment perspective may produce poor predictions. These situations may be the result of one or, perhaps, a few influential observations.

Recall the hat matrix  $H = X(X^\top X)^{-1}X^\top$ , as well as that it holds that  $\text{Var}[\hat{\epsilon}] = \sigma^2(I - H)$  and  $\text{Var}[\hat{Y}] = \sigma^2H$ . Note that  $h_{ij}$  can be interpreted as the amount of leverage exerted by the  $i$ th observation  $y_i$  on the  $j$ th fitted value  $\hat{y}_j$ . We usually focus attention on the diagonal elements  $h_{ii}$  of the hat matrix  $H$ , which may be written as

$$h_{ii} = x_i^\top (X^\top X)^{-1} x_i,$$

where  $X_i^\top$  is the  $i$ th row of  $X$ . The hat matrix diagonal is a standardized measure of the distance of the  $i$ th observation from the center (or centroid) of the  $x$ -space. Therefore, large values of  $h_{ii}$  implies that  $x_i$  is potentially influential. Furthermore, note that  $\text{rank}(H) = p$  since the trace of an idempotent matrix equals its rank, which means that  $\bar{h} = p/n$ . It follows that values well above  $p/n$ , say  $h_{ii} > 2p/n$ , can be called leverage points.

```

X=as.matrix(cbind(rep(1,length(x)),x))
# or

X=model.matrix(a)
hat=X%*%solve(t(X)%*%X)%*%t(X)

diag(hat)

```

```

1           2           3           4           5           6           7
0.2027453 0.2288737 0.2596869 0.1751432 0.1735495 0.3887329 0.5712686

```

```

p=2
n=7
diag(hat)>2*p/n

```

```

1   2   3   4   5   6   7
FALSE FALSE FALSE FALSE FALSE FALSE FALSE

```

## 7.2 Cook's Distance

Cook's Distance is one way to incorporate both the  $X$  and  $Y$  values into an outlyingness measure:

$$D_i(X^\top X, p, MSE) \equiv D_i = \frac{(\hat{\beta}_{(i)} - \hat{\beta})^\top X^\top X (\hat{\beta}_{(i)} - \hat{\beta})}{pMSE}, \quad i = \in [n],$$

where  $\hat{\beta}_{(i)}$  is the OLS estimator with the  $i$ th point removed. Large values of Cook's distance signal a leverage point.

What do we mean by a large value? We can compare  $D_i$  to the 50th percentile of the  $F_{p,n-p}$  distribution. This gives the interpretation that deleting the  $i$ th point moves the estimate to the boundary of a 50% confidence interval.  $F_{p,n-p} \approx 1$ , and so usually take  $D_i \geq 1$  to be large.

Observe that

$$D_i = \frac{r_i^2}{p} \frac{\text{Var}(\hat{Y}_i)}{\text{Var}(\hat{\epsilon}_i)} = \frac{r_i^2}{p} \frac{h_{ii}}{1-h_{ii}}, \quad i = 1, 2, \dots, n,$$

where it is important to recall that  $r_i$  is the studentized residual. Now, the quantity  $\frac{h_{ii}}{1-h_{ii}}$  can be shown to be the distance from the vector  $x_i$  to the centroid of the remaining data.

Therefore,  $D_i$  is the product of outlyingness in both the  $X$  and  $Y$  directions. We may also write  $D_i$  as

$$D_i = \frac{\|\hat{y}_{(i)} - \hat{y}\|^2}{pMSE},$$

which allows for the interpretation: The Cook's distance of the  $i$ th point is the normalized distance between the fitted value with and without point  $i$ .

```
#cut off
cooks.distance(a)
```

```
1           2           3           4           5           6
0.1708029420 0.2516095165 0.0180669722 0.0009569213 0.0011772793 0.2002829110
7
3.3311562309
```

```
cooks.distance(a)>1
```

```
1   2   3   4   5   6   7
FALSE FALSE FALSE FALSE FALSE FALSE  TRUE
```

```
df=data.frame(cbind(y,x))
df[cooks.distance(a)>1,]
```

```
y   x
7 15 2.5
```

### 7.3 Data depth functions

A more modern approach and nonparametric approach to outlier detection is through data depth. A data depth function gives meaning to centrality, order and outlyingness in spaces beyond  $\mathbb{R}$ . A data depth function is a function which takes a sample and a point, and returns how central the point is, with respect to the sample. Depth functions can be written as  $D: \mathbb{R}^d \times \text{Sample} \rightarrow \mathbb{R}^+$ . There are different definitions of depth, so I will give a few.

Let  $S^{d-1} = \{x \in \mathbb{R}^d : \|x\| = 1\}$  be the set of unit vectors in  $\mathbb{R}^d$ , let  $\mathbb{X}_n = \{(Y_1, X_{1,1}, \dots, X_{1,p-1}), \dots, (Y_n, X_{n,1}, \dots, X_{n,p})\}$  let  $\mathbb{X}_n^\top u$  be  $\mathbb{X}_n$  projected onto  $u \in S^{d-1}$  and let  $\widehat{F}_u$  be the empirical CDF with respect to  $\mathbb{X}_n^\top u$ .

The halfspace depth  $D_H$  of a point  $x \in \mathbb{R}^d$  with respect to a distribution  $F$  over  $\mathbb{R}^d$  is

$$D_H(x; F) = \inf_{u \in S^{d-1}} \widehat{F}_u(x^\top u) \wedge (1 - F_u(x^\top u)) = \inf_{u \in S^{d-1}} F_u(x^\top u).$$

Given a translation and scale equivariant location estimate  $\mu$  and a translation and scale invariant scale estimate  $\sigma$ , the outlyingness at  $x \in \mathbb{R}^d$  is defined as

$$O(x) = \sup_{u \in S^{d-1}} \frac{|x^\top u - \mu(\mathbb{X}_n^\top u)|}{\sigma(\mathbb{X}_n^\top u)}.$$

Define projection depth as

$$D_p(x) = (1 + O(x))^{-1}.$$

In order to detect outliers, we look for observations that have low depth. See, continuing our toy example:

```
# install.packages('ddalpha')
depths=ddalpha::depth.projection(cbind(x,y), cbind(x,y))
depths

[1] 0.276409011 0.255272074 0.500000000 0.973754328 0.973046927 0.338954415
[7] 0.001695292

depths<0.015

[1] FALSE FALSE FALSE FALSE FALSE FALSE TRUE
```

**Example 7.1.** Recall example Example 6.6. Check for leverage and influential points in the proposed models. Compute all three measures of leverage/influence/outlyingness introduced in this lesson. What do you find?

I will load in the data below:

We can now analyze the data:

```
# df=df[df$Lotsize<70000,]

custom_palette <- c(
  "#1f77b4", "#ff7f0e", "#2ca02c", "#d62728",
```

```

  "#9467bd", "#8c564b", "#e377c2", "#7f7f7f",
  "#bcbd22", "#17becf", "#393b79",
  "#8c6d31", "#9c9ede", "#637939", "#eb348f"
)

# Our model from the previous lecture
df=df_clean2[-which.max(df_clean2$Lotsize),]
df=df[df$Lotsize>0,]
df['district_3']=df['District']==3
df['district_4']=df['District']==4
df['district_15']=df['District']==15
model2=lm(Sale_price~.-district_3-district_4-district_15+district_3*Year_Built+district_3*Fin_sqft+district_15*Fin_sqft, data=df)

# Compute residuals
student_res2=rstudent(model2)

summ2=summary(model2); summ2

```

Call:

```
lm(formula = Sale_price ~ . - district_3 - district_4 - district_15 +
  district_3 * Year_Built + district_3 * Lotsize + district_4 *
  Lotsize + district_4 * Year_Built + district_15 * Year_Built +
  district_15 * Lotsize + district_3 * Fin_sqft + district_4 *
  Fin_sqft + district_15 * Fin_sqft, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-303393	-24422	-942	23352	719561

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1.129e+06	3.625e+04	-31.143	< 2e-16 ***
District	5.695e+03	7.701e+01	73.950	< 2e-16 ***
ExtwallBlock	-3.944e+03	3.688e+03	-1.069	0.284879
ExtwallBrick	6.725e+03	7.245e+02	9.281	< 2e-16 ***
ExtwallFiber-Cement	3.847e+04	3.754e+03	10.246	< 2e-16 ***
ExtwallFrame	-4.986e+03	9.786e+02	-5.095	3.51e-07 ***
ExtwallMasonry / Frame	3.751e+03	1.711e+03	2.192	0.028404 *
ExtwallPrem Wood	1.894e+04	5.596e+03	3.385	0.000714 ***

ExtwallStone	1.162e+04	1.531e+03	7.594	3.22e-14	***						
ExtwallStucco	3.514e+03	2.149e+03	1.635	0.102070							
Stories1	3.684e+02	1.047e+04	0.035	0.971935							
Stories1.5	1.317e+04	1.046e+04	1.259	0.207954							
Stories2	1.451e+04	1.042e+04	1.392	0.163802							
Year_Built	4.629e+02	1.606e+01	28.823	< 2e-16	***						
Fin_sqft	6.048e+01	1.080e+00	55.986	< 2e-16	***						
Units1	5.778e+04	7.389e+03	7.820	5.48e-15	***						
Units2	-9.774e+03	7.386e+03	-1.323	0.185735							
Units3	-4.087e+04	7.940e+03	-5.147	2.67e-07	***						
Bdrms0	1.155e+05	1.854e+04	6.227	4.82e-10	***						
Bdrms1	7.894e+04	1.016e+04	7.766	8.41e-15	***						
Bdrms2	8.331e+04	9.086e+03	9.170	< 2e-16	***						
Bdrms3	8.791e+04	9.033e+03	9.733	< 2e-16	***						
Bdrms4	7.905e+04	9.001e+03	8.782	< 2e-16	***						
Bdrms5	7.507e+04	9.002e+03	8.340	< 2e-16	***						
Bdrms6	6.149e+04	9.006e+03	6.828	8.80e-12	***						
Bdrms7	2.462e+04	9.572e+03	2.573	0.010100	*						
Bdrms8	1.242e+04	1.008e+04	1.233	0.217672							
Fbath0	-1.936e+04	1.388e+04	-1.395	0.162964							
Fbath1	-1.050e+04	9.795e+03	-1.072	0.283695							
Fbath2	7.289e+03	9.751e+03	0.748	0.454721							
Fbath3	2.935e+04	9.641e+03	3.044	0.002339	**						
Fbath4	6.757e+04	1.025e+04	6.595	4.35e-11	***						
Lotsize	1.419e+00	1.131e-01	12.545	< 2e-16	***						
Sale_date	4.839e+00	2.603e-01	18.587	< 2e-16	***						
district_3TRUE	9.189e+05	1.373e+05	6.693	2.23e-11	***						
district_4TRUE	1.088e+06	2.504e+05	4.346	1.39e-05	***						
district_15TRUE	4.475e+05	1.212e+05	3.692	0.000223	***						
Year_Built:district_3TRUE	-5.100e+02	7.205e+01	-7.078	1.51e-12	***						
Lotsize:district_3TRUE	1.227e+01	4.803e-01	25.549	< 2e-16	***						
Lotsize:district_4TRUE	-3.796e+00	1.569e+00	-2.420	0.015512	*						
Year_Built:district_4TRUE	-5.558e+02	1.306e+02	-4.255	2.09e-05	***						
Year_Built:district_15TRUE	-2.829e+02	6.295e+01	-4.493	7.05e-06	***						
Lotsize:district_15TRUE	3.140e+00	1.213e+00	2.589	0.009620	**						
Fin_sqft:district_3TRUE	6.621e+01	1.517e+00	43.639	< 2e-16	***						
Fin_sqft:district_4TRUE	-2.049e+01	4.181e+00	-4.901	9.61e-07	***						
Fin_sqft:district_15TRUE	-1.161e+01	3.163e+00	-3.672	0.000241	***						
---											
Signif. codes:	0	'***'	0.001	'**'	0.01	'*'	0.05	'. '	0.1	' '	1

Residual standard error: 43870 on 24429 degrees of freedom  
 Multiple R-squared: 0.7301, Adjusted R-squared: 0.7296

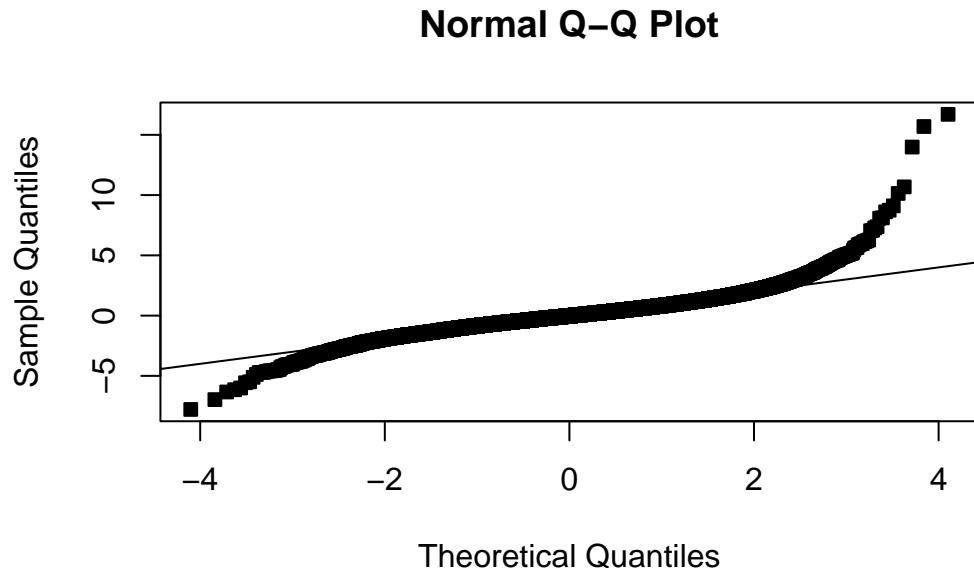
```
F-statistic: 1468 on 45 and 24429 DF, p-value: < 2.2e-16
```

```
summ2$adj.r.squared
```

```
[1] 0.7295574
```

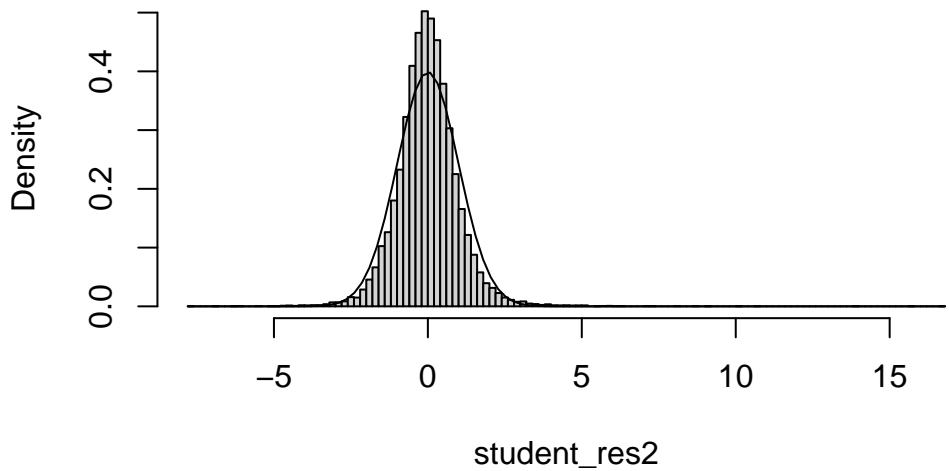
```
# Compute residual analysis
```

```
MSE2=summ2$sigma^2  
qqnorm(student_res2,pch=22,bg=1)  
abline(0,1)
```

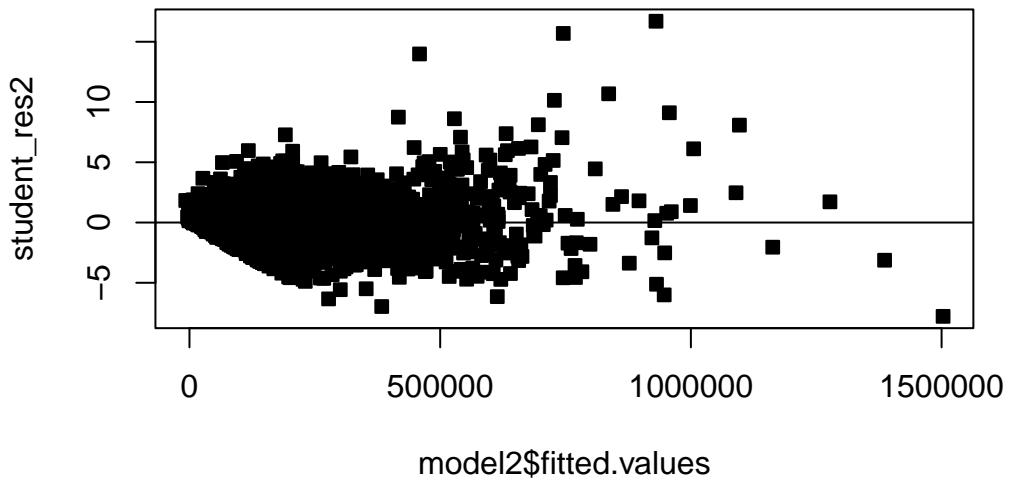


```
hist(student_res2,freq=F,breaks=100)  
curve(dnorm(x,0,1),add=T)
```

### Histogram of student\_res2



```
# hist(student_res2,freq=F,breaks=100)
# curve(dnorm(x,0,1),add=T)
plot(model2$fitted.values,student_res2,pch=22,bg=1)
abline(h=0)
```



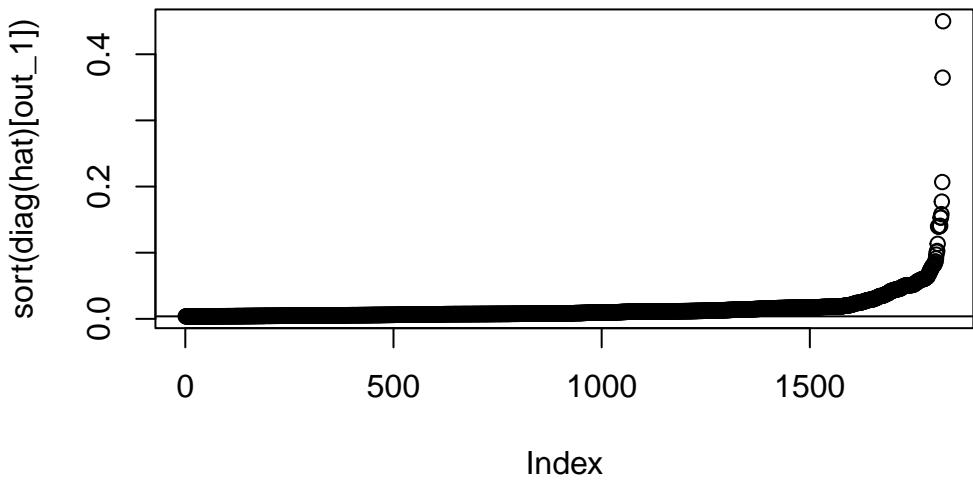
```

# First measure

X=model.matrix(model2)
hat=X%*%solve(t(X)%*%X)%*%t(X)

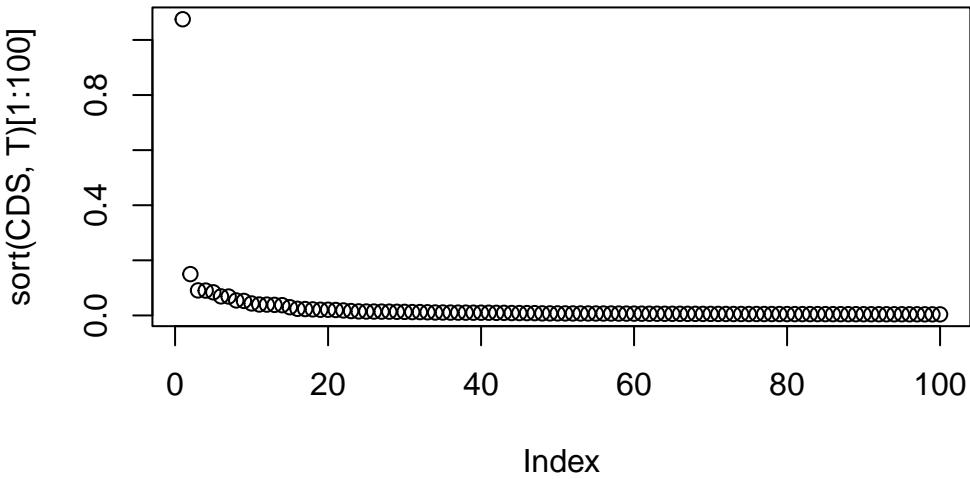
# diag(hat)
p=ncol(X)
n=nrow(X)
out_1=which(diag(hat)>2*p/n)
plot(sort(diag(hat)[out_1]))
abline(h=2*p/n)

```



```
# I would still look at those after the elbow
```

```
# Cooks distances
CDS=cooks.distance(model2)
plot(sort(CDS,T)[1:100])
```



```
which(CDS>1)
```

```
22532
22398
```

```
max(CDS)
```

```
[1] 1.075144
```

```
df [CDS>1, ]
```

	District	Extwall	Stories	Year_Built	Fin_sqft	Units	Bdrms	Fbath	Lotsize
22532	3	Block	1	1960	4323	1	4	3	72480
	Sale_date	Sale_price	District	District	District				
22532	17713	1250000	TRUE	FALSE	FALSE				

```
# I would still look at those two values that are far from the other distances
# I would still look at those before the elbow
```

```

# We may only look at numeric values for depth functions - so we can either
numer=NULL
for(i in names(df)){
  if(!is.factor(df[1,i])){
    numer=c(numer,i)
  }
}
numer

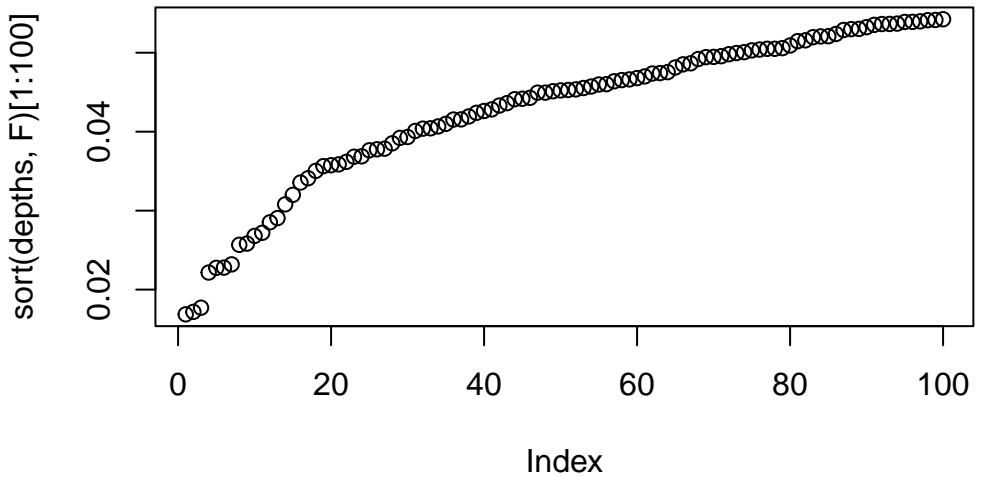
[1] "District"      "Year_Built"     "Fin_sqft"      "Lotsize"       "Sale_date"
[6] "Sale_price"     "district_3"     "district_4"     "district_15"

df_mat=as.matrix(df[,numer])
depths=ddalpha::depth.projection(df_mat,df_mat)
which(depths<0.1)[1:10]

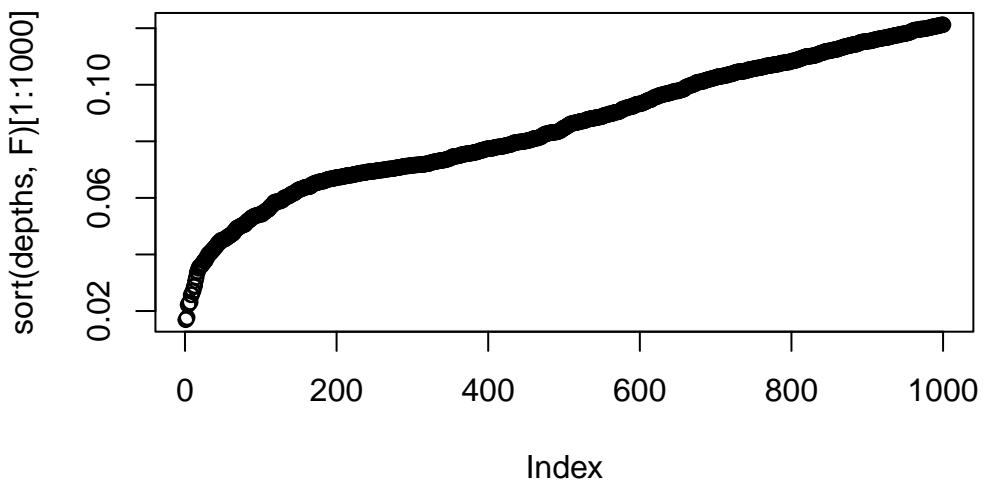
[1] 5 64 130 326 345 471 473 593 637 669

plot(sort(depths,F)[1:100])

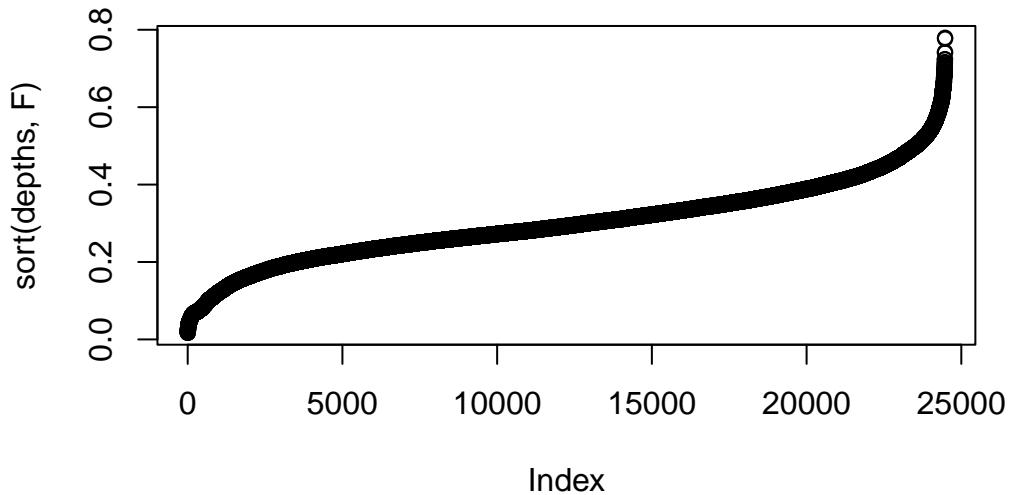
```



```
# Notice there is a crack around 0.035, I would look at those observations  
plot(sort(depths,F)[1:1000])
```



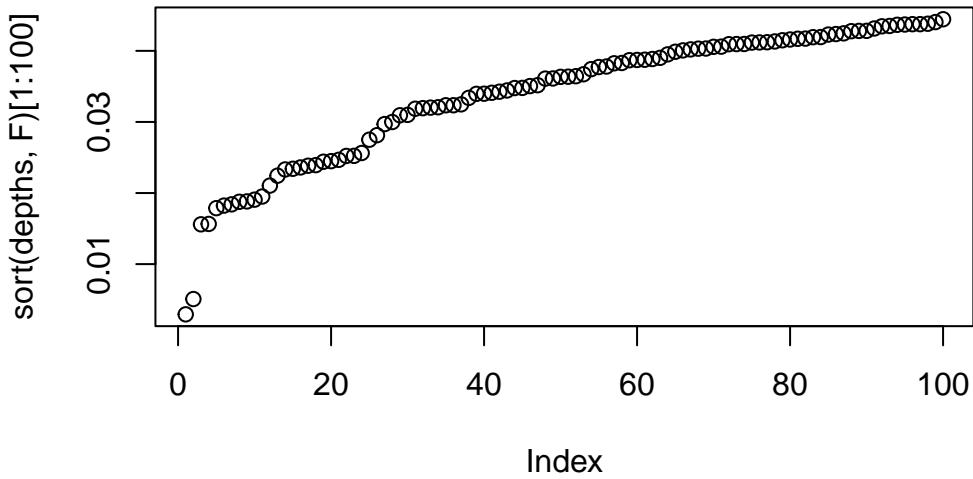
```
plot(sort(depths,F))
```



```
# OR  
depths=ddalpha::depth.projection(cbind(X,df$Sale_price),cbind(X,df$Sale_price))  
which(depths<0.1)[1:10]
```

```
[1] 3 4 5 7 15 16 17 20 22 26
```

```
plot(sort(depths,F)[1:100])
```



```
which.max(diag(hat))
```

22532  
22398

```
which.max(CDS)
```

22532  
22398

```
which.min(depths)
```

[1] 22398

```
# Hugely expensive home!  
df[which.min(depths),]
```

```

District Extwall Stories Year_Built Fin_sqft Units Bdrms Fbath Lotsize
22532      3   Block      1      1960      4323      1      4      3    72480
Sale_date Sale_price District District District
22532     17713     1250000     TRUE     FALSE     FALSE

```

```
df[which.max(CDS),]
```

```

District Extwall Stories Year_Built Fin_sqft Units Bdrms Fbath Lotsize
22532      3   Block      1      1960      4323      1      4      3    72480
Sale_date Sale_price District District District
22532     17713     1250000     TRUE     FALSE     FALSE

```

```
df[which.max(diag(hat)),]
```

```

District Extwall Stories Year_Built Fin_sqft Units Bdrms Fbath Lotsize
22532      3   Block      1      1960      4323      1      4      3    72480
Sale_date Sale_price District District District
22532     17713     1250000     TRUE     FALSE     FALSE

```

```

model3=lm(Sale_price~.-district_3-district_4-district_15+district_3*Year_Built+district_3*
# OR

model4=lm(Sale_price~.-district_3-district_4-district_15+district_3*Year_Built+district_3*


# Compare
s=summary(model3)
summary(model3)

```

Call:

```
lm(formula = Sale_price ~ . - district_3 - district_4 - district_15 +
  district_3 * Year_Built + district_3 * Lotsize + district_4 *
  Lotsize + district_4 * Year_Built + district_15 * Year_Built +
  district_15 * Lotsize + district_3 * Fin_sqft + district_4 *
  Fin_sqft + district_15 * Fin_sqft, data = df[-(order(depths)[1:100]),])
```

Residuals:

	Min	1Q	Median	3Q	Max
	-275556	-24244	-1138	22988	320067

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-1.048e+06	3.556e+04	-29.483	< 2e-16 ***
District	5.685e+03	7.266e+01	78.235	< 2e-16 ***
ExtwallBlock	-2.286e+03	3.485e+03	-0.656	0.511872
ExtwallBrick	6.808e+03	6.867e+02	9.914	< 2e-16 ***
ExtwallFiber-Cement	4.306e+04	3.557e+03	12.107	< 2e-16 ***
ExtwallFrame	-4.593e+03	9.248e+02	-4.967	6.86e-07 ***
ExtwallMasonry / Frame	4.277e+03	1.626e+03	2.630	0.008545 **
ExtwallPrem Wood	2.179e+04	5.317e+03	4.098	4.18e-05 ***
ExtwallStone	1.053e+04	1.449e+03	7.267	3.78e-13 ***
ExtwallStucco	6.748e+03	2.045e+03	3.300	0.000969 ***
Stories1	-2.495e+04	1.022e+04	-2.443	0.014591 *
Stories1.5	-1.181e+04	1.020e+04	-1.158	0.246999
Stories2	-8.609e+03	1.017e+04	-0.846	0.397364
Year_Built	4.540e+02	1.529e+01	29.696	< 2e-16 ***
Fin_sqft	5.631e+01	1.032e+00	54.554	< 2e-16 ***
Units1	5.444e+04	6.991e+03	7.787	7.11e-15 ***
Units2	-1.130e+04	6.987e+03	-1.617	0.105980
Units3	-4.301e+04	7.520e+03	-5.720	1.08e-08 ***
Bdrms0	9.220e+04	1.761e+04	5.236	1.66e-07 ***
Bdrms1	4.984e+04	9.823e+03	5.074	3.93e-07 ***
Bdrms2	5.665e+04	8.828e+03	6.417	1.42e-10 ***
Bdrms3	6.222e+04	8.778e+03	7.089	1.39e-12 ***
Bdrms4	5.422e+04	8.747e+03	6.199	5.76e-10 ***
Bdrms5	5.172e+04	8.745e+03	5.914	3.39e-09 ***
Bdrms6	3.924e+04	8.749e+03	4.485	7.31e-06 ***
Bdrms7	1.455e+04	9.306e+03	1.564	0.117931
Bdrms8	8.431e+03	9.786e+03	0.861	0.388983
Fbath0	-2.592e+04	1.516e+04	-1.710	0.087331 .
Fbath1	-1.398e+04	1.199e+04	-1.166	0.243478
Fbath2	4.532e+03	1.195e+04	0.379	0.704540
Fbath3	2.618e+04	1.190e+04	2.199	0.027856 *
Fbath4	3.017e+04	1.261e+04	2.392	0.016750 *
Lotsize	1.693e+00	1.133e-01	14.950	< 2e-16 ***
Sale_date	4.690e+00	2.460e-01	19.061	< 2e-16 ***
district_3TRUE	1.033e+06	1.361e+05	7.590	3.30e-14 ***
district_4TRUE	1.060e+06	2.364e+05	4.482	7.43e-06 ***
district_15TRUE	4.386e+05	1.144e+05	3.834	0.000127 ***
Year_Built:district_3TRUE	-5.544e+02	7.159e+01	-7.745	9.95e-15 ***

```

Lotsize:district_3TRUE      1.745e+01  8.874e-01  19.670 < 2e-16 ***
Lotsize:district_4TRUE     -2.501e+00  1.728e+00  -1.447 0.147918
Year_Built:district_4TRUE   -5.488e+02  1.235e+02  -4.442 8.95e-06 ***
Year_Built:district_15TRUE  -2.770e+02  5.942e+01  -4.661 3.16e-06 ***
Lotsize:district_15TRUE     3.255e+00  1.145e+00   2.843 0.004469 **
Fin_sqft:district_3TRUE    3.990e+01  1.725e+00  23.127 < 2e-16 ***
Fin_sqft:district_4TRUE    -1.681e+01  4.447e+00  -3.780 0.000157 ***
Fin_sqft:district_15TRUE   -1.344e+01  2.992e+00  -4.491 7.11e-06 ***
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

Residual standard error: 41380 on 24329 degrees of freedom  
Multiple R-squared: 0.6712, Adjusted R-squared: 0.6706  
F-statistic: 1104 on 45 and 24329 DF, p-value: < 2.2e-16

```
summary(model2)
```

```

Call:
lm(formula = Sale_price ~ . - district_3 - district_4 - district_15 +
district_3 * Year_Built + district_3 * Lotsize + district_4 *
Lotsize + district_4 * Year_Built + district_15 * Year_Built +
district_15 * Lotsize + district_3 * Fin_sqft + district_4 *
Fin_sqft + district_15 * Fin_sqft, data = df)

Residuals:
    Min      1Q      Median      3Q      Max 
-303393 -24422     -942     23352    719561 

Coefficients:
                                         Estimate Std. Error t value Pr(>|t|)    
(Intercept)                         -1.129e+06  3.625e+04 -31.143 < 2e-16 ***
District                                5.695e+03  7.701e+01   73.950 < 2e-16 ***
ExtwallBlock                            -3.944e+03  3.688e+03  -1.069 0.284879  
ExtwallBrick                             6.725e+03  7.245e+02   9.281 < 2e-16 ***
ExtwallFiber-Cement                     3.847e+04  3.754e+03  10.246 < 2e-16 ***
ExtwallFrame                            -4.986e+03  9.786e+02  -5.095 3.51e-07 ***
ExtwallMasonry / Frame                  3.751e+03  1.711e+03   2.192 0.028404 *  
ExtwallPrem Wood                        1.894e+04  5.596e+03   3.385 0.000714 *** 
ExtwallStone                             1.162e+04  1.531e+03   7.594 3.22e-14 *** 
ExtwallStucco                           3.514e+03  2.149e+03   1.635 0.102070  

```

Stories1	3.684e+02	1.047e+04	0.035	0.971935
Stories1.5	1.317e+04	1.046e+04	1.259	0.207954
Stories2	1.451e+04	1.042e+04	1.392	0.163802
Year_Built	4.629e+02	1.606e+01	28.823	< 2e-16 ***
Fin_sqft	6.048e+01	1.080e+00	55.986	< 2e-16 ***
Units1	5.778e+04	7.389e+03	7.820	5.48e-15 ***
Units2	-9.774e+03	7.386e+03	-1.323	0.185735
Units3	-4.087e+04	7.940e+03	-5.147	2.67e-07 ***
Bdrms0	1.155e+05	1.854e+04	6.227	4.82e-10 ***
Bdrms1	7.894e+04	1.016e+04	7.766	8.41e-15 ***
Bdrms2	8.331e+04	9.086e+03	9.170	< 2e-16 ***
Bdrms3	8.791e+04	9.033e+03	9.733	< 2e-16 ***
Bdrms4	7.905e+04	9.001e+03	8.782	< 2e-16 ***
Bdrms5	7.507e+04	9.002e+03	8.340	< 2e-16 ***
Bdrms6	6.149e+04	9.006e+03	6.828	8.80e-12 ***
Bdrms7	2.462e+04	9.572e+03	2.573	0.010100 *
Bdrms8	1.242e+04	1.008e+04	1.233	0.217672
Fbath0	-1.936e+04	1.388e+04	-1.395	0.162964
Fbath1	-1.050e+04	9.795e+03	-1.072	0.283695
Fbath2	7.289e+03	9.751e+03	0.748	0.454721
Fbath3	2.935e+04	9.641e+03	3.044	0.002339 **
Fbath4	6.757e+04	1.025e+04	6.595	4.35e-11 ***
Lotsize	1.419e+00	1.131e-01	12.545	< 2e-16 ***
Sale_date	4.839e+00	2.603e-01	18.587	< 2e-16 ***
district_3TRUE	9.189e+05	1.373e+05	6.693	2.23e-11 ***
district_4TRUE	1.088e+06	2.504e+05	4.346	1.39e-05 ***
district_15TRUE	4.475e+05	1.212e+05	3.692	0.000223 ***
Year_Built:district_3TRUE	-5.100e+02	7.205e+01	-7.078	1.51e-12 ***
Lotsize:district_3TRUE	1.227e+01	4.803e-01	25.549	< 2e-16 ***
Lotsize:district_4TRUE	-3.796e+00	1.569e+00	-2.420	0.015512 *
Year_Built:district_4TRUE	-5.558e+02	1.306e+02	-4.255	2.09e-05 ***
Year_Built:district_15TRUE	-2.829e+02	6.295e+01	-4.493	7.05e-06 ***
Lotsize:district_15TRUE	3.140e+00	1.213e+00	2.589	0.009620 **
Fin_sqft:district_3TRUE	6.621e+01	1.517e+00	43.639	< 2e-16 ***
Fin_sqft:district_4TRUE	-2.049e+01	4.181e+00	-4.901	9.61e-07 ***
Fin_sqft:district_15TRUE	-1.161e+01	3.163e+00	-3.672	0.000241 ***
---				

Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 43870 on 24429 degrees of freedom

Multiple R-squared: 0.7301, Adjusted R-squared: 0.7296

F-statistic: 1468 on 45 and 24429 DF, p-value: < 2.2e-16

```

# Notice that some of the coefficients moved several standard errors!! This is a huge chan
sort(abs(model3$coefficients-model2$coefficients)/s$coefficients[,2],T)

Fin_sqft:district_3TRUE      Lotsize:district_3TRUE
  15.24505072                  5.84301996
    Fin_sqft                      Bdrms2
  4.04375955                  3.02074093
      Fbath4                      Bdrms1
  2.96653316                  2.96269835
      Bdrms3                      Bdrms4
  2.92678462                  2.83832863
      Bdrms5                      Bdrms6
  2.67068305                  2.54317351
      Stories1                     Stories1.5
  2.47860999                  2.44804272
      Lotsize                      Stories2
  2.42348227                  2.27328085
(Intercept)                   ExtwallStucco
  2.26165432                  1.58135003
      Bdrms0                      ExtwallFiber-Cement
  1.32148050                  1.29194315
      Bdrms7                      district_3TRUE
  1.08240741                  0.83667557
Fin_sqft:district_4TRUE       ExtwallStone
  0.82686340                  0.75295649
Lotsize:district_4TRUE        Year_Built:district_3TRUE
  0.74951182                  0.62078382
Fin_sqft:district_15TRUE      Sale_date
  0.60937648                  0.60556257
Year_Built                     ExtwallPrem Wood
  0.58139942                  0.53606561
      Units1                      ExtwallBlock
  0.47841864                  0.47569367
      Fbath0                      ExtwallFrame
  0.43234373                  0.42503952
      Bdrms8                      ExtwallMasonry / Frame
  0.40777572                  0.32346851
      Fbath1                      Units3
  0.29018635                  0.28524471
      Fbath3                      Fbath2
  0.26581945                  0.23068338
      Units2                      District

```

0.21782363	0.13426306
ExtwallBrick	district_4TRUE
0.12107709	0.12052136
Lotsize:district_15TRUE	Year_Built:district_15TRUE
0.10019176	0.09899458
district_15TRUE	Year_Built:district_4TRUE
0.07738453	0.05719434

How should we treat influential observations? The easiest course of action is removal. If there are many influential observations, then you might want to try robust model fitting methods, which automatically account for outliers and influential observations.

## 7.4 Homework questions

Complete the Chapter 6 textbook questions.

**Exercise 7.1.** What are the three methods we have learned for detecting influential/leverage points?

**Exercise 7.2.** Compute the hat values, Cook's distances and the depth values for the body weight example. Are there any influential/leverage points/outliers?

**Exercise 7.3.** Compute the hat values, Cook's distances and the depth values for the cars example. Are there any outliers/influential/leverage points?

**Exercise 7.4.** Fit a model without location to the real estate data of your choosing. Compute the hat values, Cook's distances and the depth values for the cars example. Are there any influential/leverage points/outliers? Print out the influential/leverage points/outliers. Why do you think they are outlying? Should we remove them?

# 8 Multicollinearity

## 8.1 Multicollinearity and the problems it creates

A serious problem that may dramatically impact the usefulness of a regression model is multicollinearity, or near-linear dependence among the regression variables. That is multicollinearity refers to near-linear dependence among the regressors. The regressors are the columns of the  $X$  matrix, so clearly an exact linear dependence among the regressors would result in a singular  $X^\top X$ . This will impact our ability to estimate  $\beta$ .

To elaborate, assume that the regressor variables and the response have been centered and scaled to unit length. The matrix  $X^\top X$  is then a  $p \times p$  correlation matrix (of the vector of regressors) and  $X^\top Y$  is the vector of correlations between the regressors and response. Recall that a set of vectors  $v_1, \dots, v_n$  are linearly dependent if there exists  $c \neq 0$  such that  $\sum_{i=1}^n c_i v_i = 0$ . If the columns of  $X$  are linearly dependent, then  $X^\top X$  is not invertible! We say there is multicollinearity if there exists  $c \neq 0$  such that  $\sum_{i=1}^n c_i v_i < \epsilon$  for some small  $\epsilon$ .

Multicollinearity results in large variances and covariances for the least - squares estimators of the regression coefficients. Let  $A = (X^\top X)^{-1}$ , where the regressors have been centered and scaled to unit length. That is, columns  $2, \dots, p$  of  $X$  have their mean subtracted and are divided by their respective norms. Then

$$A_{jj} = (1 - R_j^2)^{-1},$$

where  $R_j^2$  is the coefficient of multiple determination from the regression of  $X_j$  on the remaining  $p - 1$  regressor variables. Now, recall that  $\text{Var}[\hat{\beta}_j] = A_{jj}\sigma^2$ . What happens when the correlation is approximately 1 between  $X_j$  and another regressor? It is easy to see that the variance of coefficient  $j$  goes to  $\infty$  as  $\text{corr}[X_j, X_i] \rightarrow 1$ .

This huge variance results in large magnitude of the least squares estimators of the regression coefficients. We have that  $E[\|\hat{\beta} - \beta\|^2] = \sum_{i=1}^p \text{Var}[\hat{\beta}_i] = \sigma^2 \text{trace}(X^\top X)^{-1}$ . Recall!  $\text{trace}(A)$  is the sum of its eigenvalues. If  $X^\top X$  has near linearly dependent columns, then some of the eigenvalues  $\lambda_1, \dots, \lambda_p$  will be near 0 (why?). Thus,

$$E[\|\hat{\beta} - \beta\|^2] = \sigma^2 \text{trace}(X^\top X)^{-1} = \sigma^2 \sum_{i=1}^p \frac{1}{\lambda_i}.$$

We can also show that

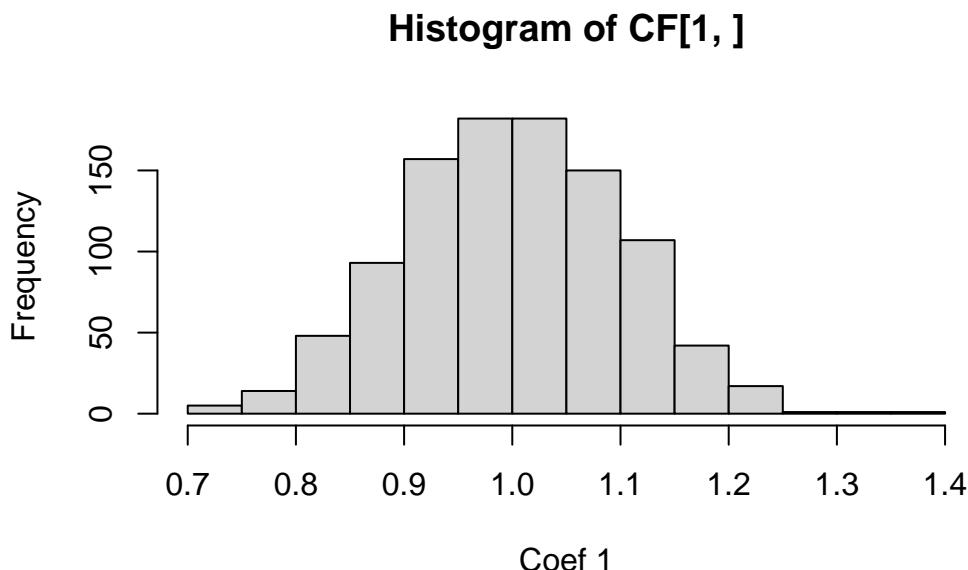
$$E \left[ \hat{\beta}^\top \hat{\beta} \right] = \beta^\top \beta + \sigma^2 \text{Tr} (X^\top X)^{-1},$$

which gives the same interpretation.

We can also observe this empirically.

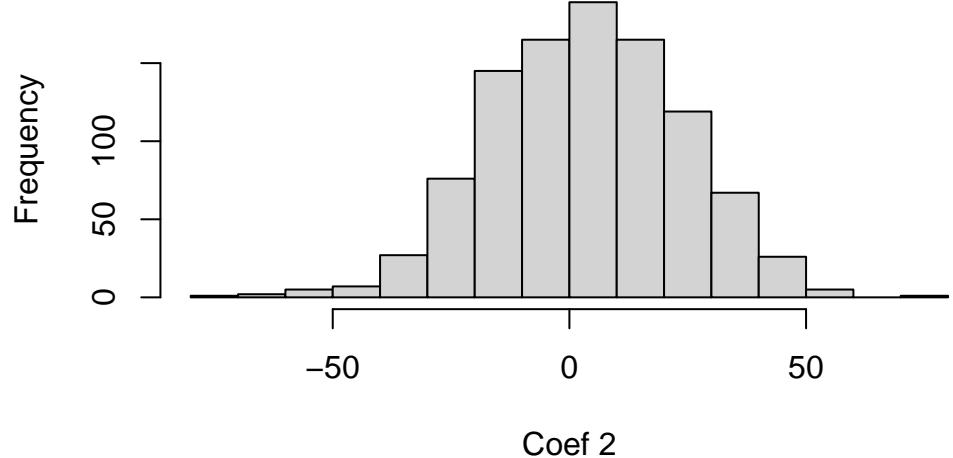
```
# Let's simulate data from a regression model with highly correlated regressors.
simulate_coef=function(){
  n=100
  X=rnorm(n)
  X2=2*X+rnorm(n,0,0.01)
  Y=1+2*X+X2*2+rnorm(n)
  return(coef(lm(Y~X+X2)))
}

# See the HUGE variance in the estimated coefficients? O this is from MCL!
CF=replicate(1000,simulate_coef())
hist(CF[1],xlab='Coef 1')
```



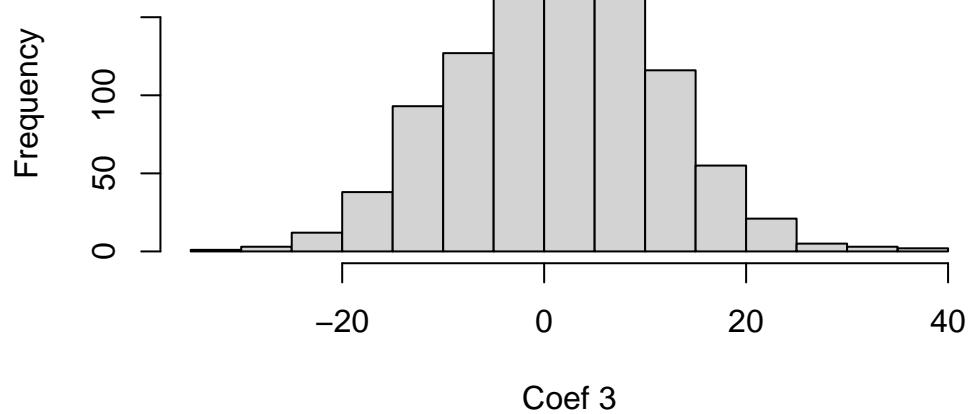
```
hist(CF[2],xlab='Coef 2')
```

### Histogram of CF[2, ]



```
hist(CF[3,],xlab='Coef 3')
```

### Histogram of CF[3, ]



It is easy to see from this analysis that multicollinearity is a serious problem, and we should check for it in regression modelling.

## 8.2 Multicollinearity Diagnostics

### 8.2.1 VIF

We need some diagnostics to detect multicollinearity. The first of which is the **correlation matrix**, which is good for detecting pairwise correlations, but not so much for more complicated dependencies! To correct this, a popular diagnostic is the **variance inflation factor** (VIF): these are the diagonals of  $(X^\top X)^{-1}$ . A VIF that exceeds 3, 5 or 10 is an indication that the associated regression coefficients are poorly estimated because of multicollinearity. The variance inflation factor can be written as  $(1 - R_j^2)^{-1}$ , where  $R_j^2$  is the coefficient of determination obtained from regressing  $x_j$  on the other regressor variables. For categorical variables, we may look at their VIF together, instead of for the individual dummy variables. This is done via the **generalized VIF (GVIF)**, which was developed by our very own Georges Monette and John Fox (Fox and Monette 1992). We can consider the  $(GVIF^{(1/(2\text{number of dummy variables}))})$ . However, we want to compare these to the square root of our rules of thumb, so  $\sqrt{3}, \sqrt{5}, \sqrt{10}$ . The values  $(GVIF^{(1/(2\text{number of dummy variables}))})$  are computed automatically in R. When your model has interaction effects, or polynomial terms, it is best to exclude those and compute the VIFs. In summary:

- Compare the VIF of continuous variables to 3, 5 or 10, above those values signals multicollinearity
- Compare the  $(GVIF^{(1/(2\text{number of dummy variables}))})$  of categorical variables to  $\sqrt{3}, \sqrt{5},$  or  $\sqrt{10}$ , above those values signals multicollinearity
- When computing VIF and GVIF, it is best to exclude interaction effects and or polynomial terms
- The given thresholds are rules of thumb, and we should not discard evidence of multicollinearity if we are very close to a threshold, e.g., 9.9.

### 8.2.2 Condition number

One can also look at the eigenvalues of  $X^\top X$ , where the regressors are centered and normalized to unit length. If the eigenvalues are small, this indicates multicollinearity. One metric computed from the eigenvalues is the **condition number** of  $X^\top X$ :  $\kappa = \max \lambda_j / \min \lambda_j$ , where the regressors are centered and normalized to unit length. Condition numbers between 100 and 1000 imply moderate to strong multicollinearity, and if  $\kappa$  exceeds 1000, severe multicollinearity is indicated. Diagonalizing via  $X^\top X = \Lambda D \Lambda^\top$  yields the eigenvectors, which help us determine the exact dependence between variables is. You can check the eigenvectors associated with the small eigenvalues. Components that are large in the eigenvector indicate that that variable

is contributing to the multicollinearity. Again, for this computation, it is best to exclude interaction effects and or polynomial terms.

**i** Note

While the method of least squares will generally produce poor estimates of the individual model parameters when strong multicollinearity is present, this does not necessarily imply that the fitted model is a poor predictor.

1. If predictions are confined to regions of the  $X$ -space where the multicollinearity holds approximately, the fitted model often produces satisfactory predictions.
2. The linear combinations  $X\beta$  may be estimated well, even if  $\beta$  is not.

**Example 8.1.** Recall example Example 6.6. Check for multicollinearity in the proposed models.

I will load in the data below:

```
model2=lm(Sale_price~.+District*Year_Built+District*Lotsize+District*Fin_sqft  
          ,df)  
  
X=model.matrix(model2)  
depths=ddalpha::depth.projection(cbind(X,df$Sale_price),cbind(X,df$Sale_price))  
  
model3=lm(Sale_price~.+District*Year_Built+District*Lotsize+District*Fin_sqft  
          ,df[-(order(depths)[1:100]),])  
  
  
summary(model3)
```

Call:

```
lm(formula = Sale_price ~ . + District * Year_Built + District *  
  Lotsize + District * Fin_sqft, data = df[-(order(depths)[1:100]),  
  ])
```

Residuals:

Min	1Q	Median	3Q	Max
-----	----	--------	----	-----

-605729 -27681 733 26954 454626

Coefficients:

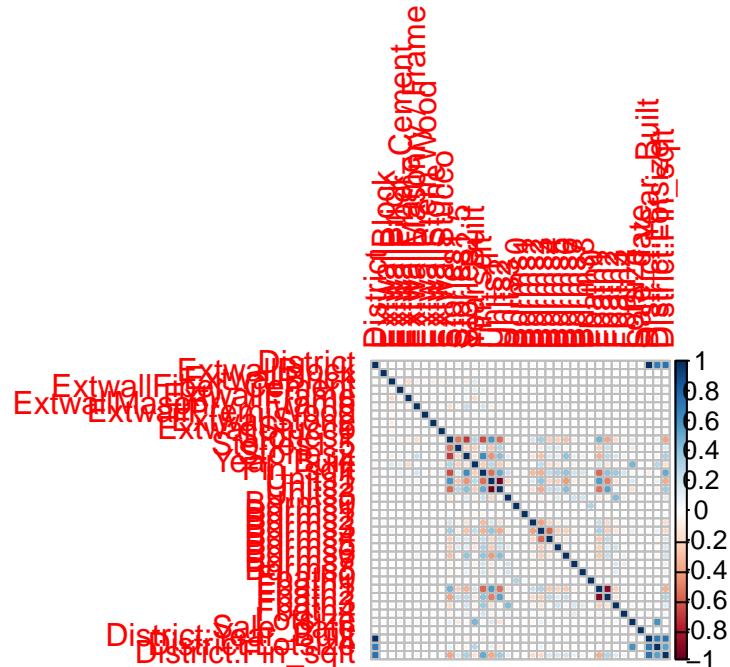
	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	3.497e+05	7.854e+04	4.453	8.51e-06 ***
District	-9.652e+04	7.589e+03	-12.718	< 2e-16 ***
ExtwallBlock	-2.883e+03	4.445e+03	-0.649	0.516580
ExtwallBrick	7.562e+03	8.735e+02	8.658	< 2e-16 ***
ExtwallFiber-Cement	2.919e+04	4.511e+03	6.471	9.93e-11 ***
ExtwallFrame	-5.128e+03	1.178e+03	-4.353	1.35e-05 ***
ExtwallMasonry / Frame	3.248e+03	2.064e+03	1.574	0.115595
ExtwallPrem Wood	7.980e+03	6.991e+03	1.142	0.253654
ExtwallStone	3.273e+03	1.847e+03	1.772	0.076384 .
ExtwallStucco	1.336e+04	2.588e+03	5.161	2.47e-07 ***
Stories1	3.254e+04	1.237e+04	2.630	0.008535 **
Stories1.5	4.380e+04	1.235e+04	3.547	0.000390 ***
Stories2	5.023e+04	1.230e+04	4.084	4.44e-05 ***
Year_Built	-3.760e+02	3.874e+01	-9.705	< 2e-16 ***
Fin_sqft	1.244e+02	1.579e+00	78.778	< 2e-16 ***
Units1	1.073e+05	8.840e+03	12.138	< 2e-16 ***
Units2	2.757e+04	8.840e+03	3.118	0.001820 **
Units3	-1.979e+04	9.521e+03	-2.079	0.037654 *
Bdrms0	1.410e+05	2.227e+04	6.332	2.46e-10 ***
Bdrms1	1.175e+05	1.217e+04	9.655	< 2e-16 ***
Bdrms2	1.236e+05	1.087e+04	11.374	< 2e-16 ***
Bdrms3	1.257e+05	1.080e+04	11.639	< 2e-16 ***
Bdrms4	1.130e+05	1.075e+04	10.508	< 2e-16 ***
Bdrms5	1.126e+05	1.075e+04	10.477	< 2e-16 ***
Bdrms6	9.129e+04	1.076e+04	8.482	< 2e-16 ***
Bdrms7	6.829e+04	1.147e+04	5.951	2.70e-09 ***
Bdrms8	6.948e+04	1.213e+04	5.729	1.02e-08 ***
Fbath0	-4.625e+04	1.725e+04	-2.681	0.007341 **
Fbath1	-3.279e+04	1.262e+04	-2.598	0.009390 **
Fbath2	-1.305e+04	1.256e+04	-1.040	0.298543
Fbath3	3.011e+04	1.248e+04	2.412	0.015867 *
Fbath4	4.767e+04	1.340e+04	3.558	0.000374 ***
Lotsize	7.107e-01	3.166e-01	2.245	0.024785 *
Sale_date	4.769e+00	3.138e-01	15.196	< 2e-16 ***
District:Year_Built	5.486e+01	3.923e+00	13.985	< 2e-16 ***
District:Lotsize	1.054e-01	3.591e-02	2.934	0.003348 **
District:Fin_sqft	-5.619e+00	1.440e-01	-39.024	< 2e-16 ***

---

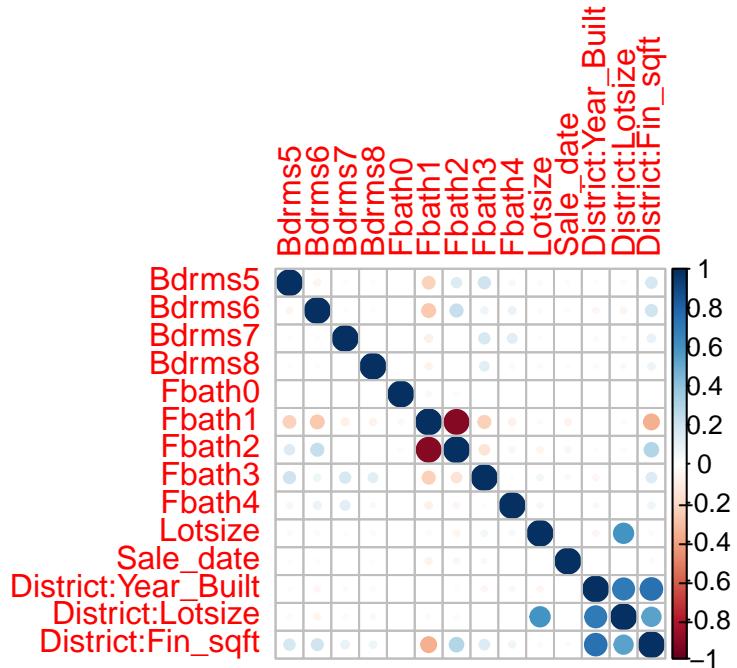
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 52780 on 24338 degrees of freedom  
Multiple R-squared: 0.5262, Adjusted R-squared: 0.5255  
F-statistic: 750.9 on 36 and 24338 DF, p-value: < 2.2e-16

```
# Correlations  
X=model.matrix(model3)  
corrplot::corrplot(cor(X[,-1]))
```



```
corrplot::corrplot(cor(X[,-(1:23)]))
```



```
# VIFs
# predictor removes the interactions
car::vif(model3, type = 'predictor')
```

GVIFs computed for predictors

	GVIF	Df	GVIF^(1/(2*Df))	Interacts With
District	5.938550	7	1.135698	Year_Built, Lotsize, Fin_sqft
Extwall	1.408741	8	1.021650	--
Stories	2.837098	3	1.189814	--
Year_Built	27.273468	3	1.734962	District
Fin_sqft	40881.039870	3	5.869309	District
Units	3.279782	3	1.218917	--
Bdrms	4.229339	9	1.083410	--
Fbath	3.333999	5	1.127967	--
Lotsize	12316.565475	3	4.805607	District
Sale_date	1.018330	1	1.009123	--
Other Predictors:				
District				Extwall, Stories, Units, Bdrms, Fbath, Sale_date
Extwall				District, Stories, Year_Built, Fin_sqft, Units, Bdrms, Fbath, Lotsize, Sale_date
Stories				District, Extwall, Year_Built, Fin_sqft, Units, Bdrms, Fbath, Lotsize, Sale_date

```

Year_Built          Extwall, Stories, Fin_sqft, Units, Bdrms, Fbath, Lotsize, Sale_date
Fin_sqft           Extwall, Stories, Year_Built, Units, Bdrms, Fbath, Lotsize, Sale_date
Units              District, Extwall, Stories, Year_Built, Fin_sqft, Bdrms, Fbath, Lotsize, Sale_date
Bdrms              District, Extwall, Stories, Year_Built, Fin_sqft, Units, Fbath, Lotsize, Sale_date
Fbath              District, Extwall, Stories, Year_Built, Fin_sqft, Units, Bdrms, Lotsize, Sale_date
Lotsize             Extwall, Stories, Year_Built, Fin_sqft, Units, Bdrms, Fbath, Sale_date
Sale_date           District, Extwall, Stories, Year_Built, Fin_sqft, Units, Bdrms, Fbath, Lotsize

model4=lm(Sale_price~Extwall +Stories+Year_Built+Fin_sqft+Units+Bdrms+Fbath+Sale_date+District
          ,df[-(order(depths)[1:100]),])

car::vif(model4,type = 'predictor')

```

GVIFs computed for predictors

	GVIF	Df	GVIF^(1/(2*Df))	Interacts With
Extwall	1.395529	8	1.021048	--
Stories	2.794397	3	1.186810	--
Year_Built	10.284838	3	1.474686	District
Fin_sqft	31689.695476	3	5.625395	District
Units	3.242258	3	1.216582	--
Bdrms	4.186673	9	1.082800	--
Fbath	3.331086	5	1.127869	--
Sale_date	1.018215	1	1.009066	--
District	5.553636	5	1.187019	Year_Built, Fin_sqft

	Other Predictors				
Extwall	Stories, Year_Built, Fin_sqft, Units, Bdrms, Fbath, Sale_date, District				
Stories	Extwall, Year_Built, Fin_sqft, Units, Bdrms, Fbath, Sale_date, District				
Year_Built	Extwall, Stories, Fin_sqft, Units, Bdrms, Fbath, Sale_date				
Fin_sqft	Extwall, Stories, Year_Built, Units, Bdrms, Fbath, Sale_date				
Units	Extwall, Stories, Year_Built, Fin_sqft, Bdrms, Fbath, Sale_date, District				
Bdrms	Extwall, Stories, Year_Built, Fin_sqft, Units, Fbath, Sale_date, District				
Fbath	Extwall, Stories, Year_Built, Fin_sqft, Units, Bdrms, Sale_date, District				
Sale_date	Extwall, Stories, Year_Built, Fin_sqft, Units, Bdrms, Fbath, District				
District	Extwall, Stories, Units, Bdrms, Fbath, Sale_date				

```

model4=lm(Sale_price~Extwall +Stories+Year_Built+
          Lotsize+Units+Bdrms+Fbath+Sale_date+District*Year_Built+District+District*Lots
          ,df[-(order(depths)[1:100]),])

```

```
X=model.matrix(model4)
car::vif(model4,type = 'predictor')
```

GVIFs computed for predictors

	GVIF	Df	GVIF^(1/(2*Df))	Interacts With
Extwall	1.278176	8	1.015458	--
Stories	2.158353	3	1.136808	--
Year_Built	12.133152	3	1.515871	District
Lotsize	10081.538963	3	4.647875	District
Units	3.188879	3	1.213220	--
Bdrms	3.148134	9	1.065785	--
Fbath	2.677922	5	1.103519	--
Sale_date	1.017871	1	1.008896	--
District	1.381580	5	1.032851	Year_Built, Lotsize
Other Predictors				
Extwall	Stories, Year_Built, Lotsize, Units, Bdrms, Fbath, Sale_date, District			
Stories	Extwall, Year_Built, Lotsize, Units, Bdrms, Fbath, Sale_date, District			
Year_Built	Extwall, Stories, Lotsize, Units, Bdrms, Fbath, Sale_date			
Lotsize	Extwall, Stories, Year_Built, Units, Bdrms, Fbath, Sale_date			
Units	Extwall, Stories, Year_Built, Lotsize, Bdrms, Fbath, Sale_date, District			
Bdrms	Extwall, Stories, Year_Built, Lotsize, Units, Fbath, Sale_date, District			
Fbath	Extwall, Stories, Year_Built, Lotsize, Units, Bdrms, Sale_date, District			
Sale_date	Extwall, Stories, Year_Built, Lotsize, Units, Bdrms, Fbath, District			
District	Extwall, Stories, Units, Bdrms, Fbath, Sale_date			

```
model4=lm(Sale_price~Extwall +Stories+
          Lotsize+Units+Bdrms+Fbath+Sale_date+District+District*Lotsize
          ,df[-(order(depths)[1:100]),])
```

```
car::vif(model4,type = 'predictor')
```

GVIFs computed for predictors

	GVIF	Df	GVIF^(1/(2*Df))	Interacts With
Extwall	1.196395	8	1.011270	--
Stories	2.068411	3	1.128772	--
Lotsize	1.111905	3	1.017836	District
Units	3.165637	3	1.211742	--

Bdrms	3.063017	9	1.064163	--
Fbath	2.653707	5	1.102517	--
Sale_date	1.017665	1	1.008794	--
District	1.111905	3	1.017836	Lotsize
				Other Predictors
Extwall			Stories, Lotsize, Units, Bdrms, Fbath, Sale_date, District	
Stories			Extwall, Lotsize, Units, Bdrms, Fbath, Sale_date, District	
Lotsize			Extwall, Stories, Units, Bdrms, Fbath, Sale_date	
Units			Extwall, Stories, Lotsize, Bdrms, Fbath, Sale_date, District	
Bdrms			Extwall, Stories, Lotsize, Units, Fbath, Sale_date, District	
Fbath			Extwall, Stories, Lotsize, Units, Bdrms, Sale_date, District	
Sale_date			Extwall, Stories, Lotsize, Units, Bdrms, Fbath, District	
District			Extwall, Stories, Units, Bdrms, Fbath, Sale_date	

```
# Let's go back to
```

```
model4=lm(Sale_price~Extwall +Stories+Year_Built+
          Lotsize+Units+Bdrms+Fbath+Sale_date+District*Year_Built+District+District*Lots
          ,df[-(order(depths)[1:100]),])
```

```
# remove interactions to compute the condition number
```

```
model4=lm(Sale_price~Extwall +Stories+Year_Built+
          Lotsize+Units+Bdrms+Fbath+Sale_date+District
          ,df[-(order(depths)[1:100]),])
```

```
X=model.matrix(model4)
```

```
# Correlations
```

```
# X=X[, -1]
```

```
X2=apply(X, 2, function(x){(x-mean(x))/sqrt(sum((x-mean(x))^2))}); dim(X2)
```

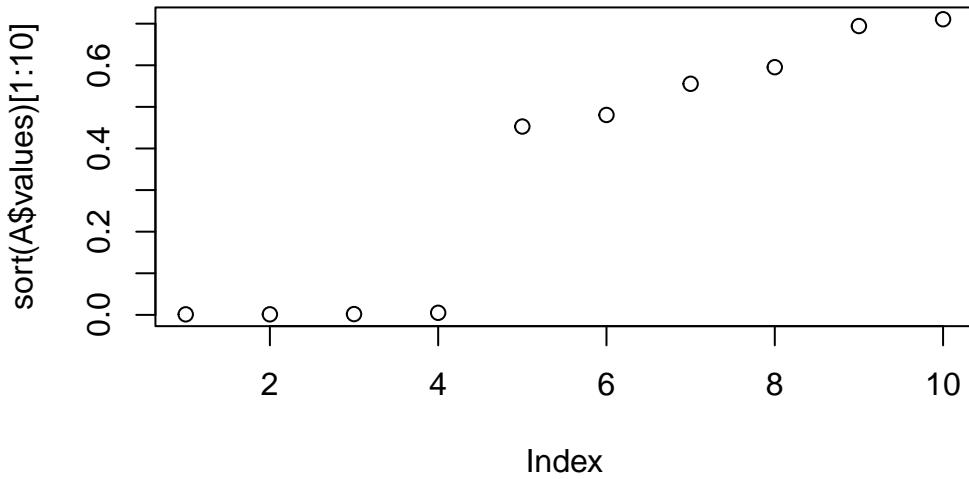
```
[1] 24375      33
```

```
X2[, 1]=X[, 1]
```

```
X=X2
```

```
A=eigen(t(X)%*%X)
```

```
plot(sort(A$values)[1:10])
```



```

sort(A$values)[1:10]

[1] 33

dim(A$vectors)

[1] 33 33

#Condition number
max(A$values)/min(A$values)

[1] 19002497

rownames(A$vectors)=names(model4$coefficients)

# Which components are important here

A$vectors[,which.min(A$values)]

```

(Intercept)	ExtwallBlock	ExtwallBrick
0.000000e+00	2.157874e-04	5.978469e-04
ExtwallFiber-Cement	ExtwallFrame	ExtwallMasonry / Frame
7.423672e-04	-6.847029e-04	-2.499551e-04
ExtwallPrem Wood	ExtwallStone	ExtwallStucco
6.226662e-05	4.436149e-04	-4.341195e-05
Stories1	Stories1.5	Stories2
-1.096523e-01	-7.806434e-02	-9.473269e-02
Year_Built	Lotsize	Units1
-9.817844e-04	1.334084e-03	6.123567e-02
Units2	Units3	Bdrms0
5.775492e-02	1.114147e-02	-1.374989e-02
Bdrms1	Bdrms2	Bdrms3
-4.871769e-02	-2.715348e-01	-4.006905e-01
Bdrms4	Bdrms5	Bdrms6
-3.387437e-01	-1.808355e-01	-1.715717e-01
Bdrms7	Bdrms8	Fbath0
-5.178211e-02	-3.999879e-02	3.083921e-02
Fbath1	Fbath2	Fbath3
5.084776e-01	4.976796e-01	1.911793e-01
Fbath4	Sale_date	District
6.281346e-02	-2.373692e-04	-2.413410e-04

```
# round(A$vectors[,which.min(A$values)],1)
round(A$vectors[,which.min(A$values)][abs(round(A$vectors[,which.min(A$values)],1))>0],1)
```

Stories1	Stories1.5	Stories2	Units1	Units2	Bdrms2	Bdrms3
-0.1	-0.1	-0.1	0.1	0.1	-0.3	-0.4
Bdrms4	Bdrms5	Bdrms6	Bdrms7	Fbath1	Fbath2	Fbath3
-0.3	-0.2	-0.2	-0.1	0.5	0.5	0.2
Fbath4						
0.1						

```
min_4=order(A$values)[1:4]
A$vectors[,min_4]
```

	[,1]	[,2]	[,3]	[,4]
(Intercept)	0.000000e+00	0.000000e+00	0.0000000000	0.000000e+00
ExtwallBlock	2.157874e-04	-9.248583e-05	0.0002779889	-1.667631e-03
ExtwallBrick	5.978469e-04	-1.428128e-04	-0.0010585073	-6.556687e-04

ExtwallFiber-Cement	7.423672e-04	-4.286608e-04	-0.0007023650	-4.203278e-05			
ExtwallFrame	-6.847029e-04	5.086148e-05	-0.0005434478	-4.403961e-03			
ExtwallMasonry / Frame	-2.499551e-04	5.955587e-04	-0.0009708358	9.946691e-04			
ExtwallPrem Wood	6.226662e-05	2.760081e-05	0.0001286685	-2.165509e-05			
ExtwallStone	4.436149e-04	-1.433889e-04	-0.0003263289	-3.862695e-04			
ExtwallStucco	-4.341195e-05	-8.011335e-04	0.0001710557	-1.563241e-03			
Stories1	-1.096523e-01	-6.007637e-01	-0.2607427050	2.131969e-03			
Stories1.5	-7.806434e-02	-4.332066e-01	-0.1881242671	9.060758e-04			
Stories2	-9.473269e-02	-5.191819e-01	-0.2266943948	-2.650768e-03			
Year_Built	-9.817844e-04	-3.955217e-04	0.0018717800	2.586720e-03			
Lotsize	1.334084e-03	8.206240e-04	-0.0020666455	-6.621107e-04			
Units1	6.123567e-02	-3.705218e-02	0.0595563386	-6.979876e-01			
Units2	5.775492e-02	-3.591622e-02	0.0578395460	-6.828344e-01			
Units3	1.114147e-02	-7.410112e-03	0.0101288065	-1.715009e-01			
Bdrms0	-1.374989e-02	8.383116e-03	-0.0135203489	-1.164538e-02			
Bdrms1	-4.871769e-02	2.977888e-02	-0.0480132104	-1.179837e-02			
Bdrms2	-2.715348e-01	1.655464e-01	-0.2678050333	-5.423330e-02			
Bdrms3	-4.006905e-01	2.445033e-01	-0.3950766818	-7.970937e-02			
Bdrms4	-3.387437e-01	2.071965e-01	-0.3344989333	-6.761525e-02			
Bdrms5	-1.808355e-01	1.111307e-01	-0.1789307374	-3.566710e-02			
Bdrms6	-1.715717e-01	1.064450e-01	-0.1715086899	-3.431019e-02			
Bdrms7	-5.178211e-02	3.353689e-02	-0.0558980648	-1.545699e-02			
Bdrms8	-3.999879e-02	2.518976e-02	-0.0426789439	-1.354742e-02			
Fbath0	3.083921e-02	6.468728e-03	-0.0276744921	2.916203e-03			
Fbath1	5.084776e-01	1.037524e-01	-0.4491473633	-1.266652e-03			
Fbath2	4.976796e-01	1.008202e-01	-0.4404995267	1.570382e-03			
Fbath3	1.911793e-01	3.888777e-02	-0.1731428547	8.703757e-04			
Fbath4	6.281346e-02	1.210395e-02	-0.0561070476	-3.668197e-03			
Sale_date	-2.373692e-04	7.838366e-04	0.0002838833	7.182291e-03			
District	-2.413410e-04	-4.293919e-04	0.0006999058	7.545907e-04			

```
# round(A$vectors[,which.min(A$values)],1)
for(i in min_4)
  print(round(A$vectors[,i][abs(round(A$vectors[,i],1))>0],1))
```

Stories1	Stories1.5	Stories2	Units1	Units2	Bdrms2	Bdrms3
-0.1	-0.1	-0.1	0.1	0.1	-0.3	-0.4
Bdrms4	Bdrms5	Bdrms6	Bdrms7	Fbath1	Fbath2	Fbath3
-0.3	-0.2	-0.2	-0.1	0.5	0.5	0.2
Fbath4						
0.1						

```

Stories1 Stories1.5   Stories2      Bdrms2      Bdrms3      Bdrms4      Bdrms5
-0.6       -0.4       -0.5        0.2         0.2         0.2         0.1
Bdrms6     Fbath1    Fbath2
0.1        0.1        0.1
Stories1 Stories1.5   Stories2      Units1      Units2      Bdrms2      Bdrms3
-0.3       -0.2       -0.2        0.1         0.1         -0.3        -0.4
Bdrms4     Bdrms5    Bdrms6      Bdrms7      Fbath1    Fbath2      Fbath3
-0.3       -0.2       -0.2        -0.1       -0.4        -0.4        -0.2
Fbath4
-0.1
Units1 Units2 Units3 Bdrms2 Bdrms3 Bdrms4
-0.7     -0.7     -0.2     -0.1     -0.1     -0.1

```

```

model5=lm(Sale_price~Extwall +Year_Built+
          Lotsize+Bdrms+Sale_date+District
          ,df[-(order(depths)[1:100]),])
X=model.matrix(model5)

# Correlations
# X=X[, -1]
X2=apply(X, 2, function(x){(x-mean(x))/sqrt(sum((x-mean(x))^2))}); dim(X2)

```

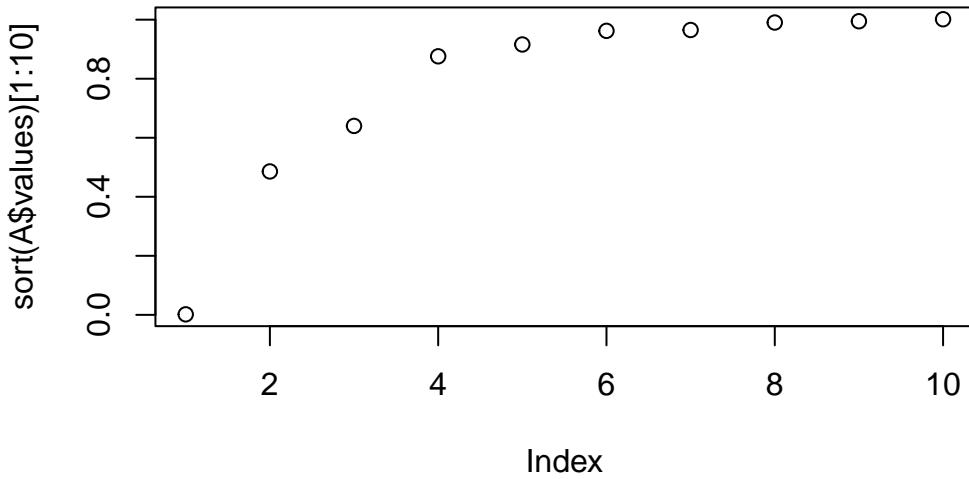
```
[1] 24375    22
```

```

X2[, 1]=X[, 1]
X=X2
A=eigen(t(X)%*%X)

plot(sort(A$values)[1:10])

```



```
which.min(A$values)
```

```
[1] 22
```

```
dim(A$vectors)
```

```
[1] 22 22
```

```
#Condition number
max(A$values)/min(A$values)
```

```
[1] 14485425
```

```
rownames(A$vectors)=names(model5$coefficients)
```

```
# Which components are important here
```

```
A$vectors[,which.min(A$values)]
```

(Intercept)	ExtwallBlock	ExtwallBrick
0.000000e+00	-4.381720e-05	4.819699e-04
ExtwallFiber-Cement	ExtwallFrame	ExtwallMasonry / Frame
1.010497e-04	1.468968e-03	1.348000e-03
ExtwallPrem Wood	ExtwallStone	ExtwallStucco
-2.910105e-05	-1.075400e-04	-1.670649e-04
Year_Built	Lotsize	Bdrms0
-1.509724e-03	9.687646e-04	2.236661e-02
Bdrms1	Bdrms2	Bdrms3
7.531941e-02	4.183638e-01	6.175005e-01
Bdrms4	Bdrms5	Bdrms6
5.236352e-01	2.813968e-01	2.687451e-01
Bdrms7	Bdrms8	Sale_date
8.635652e-02	6.651558e-02	-4.121579e-04
District		
-5.815139e-04		

```
# round(A$vectors[,which.min(A$values)],1)
round(A$vectors[,which.min(A$values)][abs(round(A$vectors[,which.min(A$values)],1))>0],1)
```

```
Bdrms1 Bdrms2 Bdrms3 Bdrms4 Bdrms5 Bdrms6 Bdrms7 Bdrms8
0.1     0.4     0.6     0.5     0.3     0.3     0.1     0.1
```

```
# This is fine
```

**Example 8.2.** Example 9.1 from the textbook - The Acetylene Data. Below presents data concerning the percentage of conversion of *n* - heptane to acetylene and three explanatory variables. These are typical chemical process data for which a full quadratic response surface in all three regressors is often considered to be an appropriate tentative model. Let's build the model and see how the extrapolation performs.

```
##### Example 2
```

```
df <- data.frame(
  Conversion_of_n_Heptane_to_Acetylene = c(49.0, 50.2, 50.5, 48.5, 47.5, 44.5, 28.0, 31.5,
  Reactor_Temperature_deg_C = c(1300, 1300, 1300, 1300, 1300, 1300, 1200, 1200, 1200,
  Ratio_of_H2_to_n_Heptane_mole_ratio = c(7.5, 9.0, 11.0, 13.5, 17.0, 23.0, 5.3, 7.5, 11.0)
```

```

  Contact_Time_sec = c(0.0120, 0.0120, 0.0115, 0.0130, 0.0135, 0.0120, 0.0400, 0.0380, 0.0120)
}

# Printing the dataframe
head(df)

Conversion_of_n_Heptane_to_Acetylene Reactor_Temperature_deg_C
1                               49.0          1300
2                               50.2          1300
3                               50.5          1300
4                               48.5          1300
5                               47.5          1300
6                               44.5          1300

Ratio_of_H2_to_n_Heptane_mole_ratio Contact_Time_sec
1                         7.5      0.0120
2                         9.0      0.0120
3                        11.0      0.0115
4                        13.5      0.0130
5                        17.0      0.0135
6                        23.0      0.0120

# For standardizing via Z scores
unit_norm=function(x){
  x=x-mean(x)
  return(sqrt(length(x)-1)*x/sqrt(sum(x^2)))
}

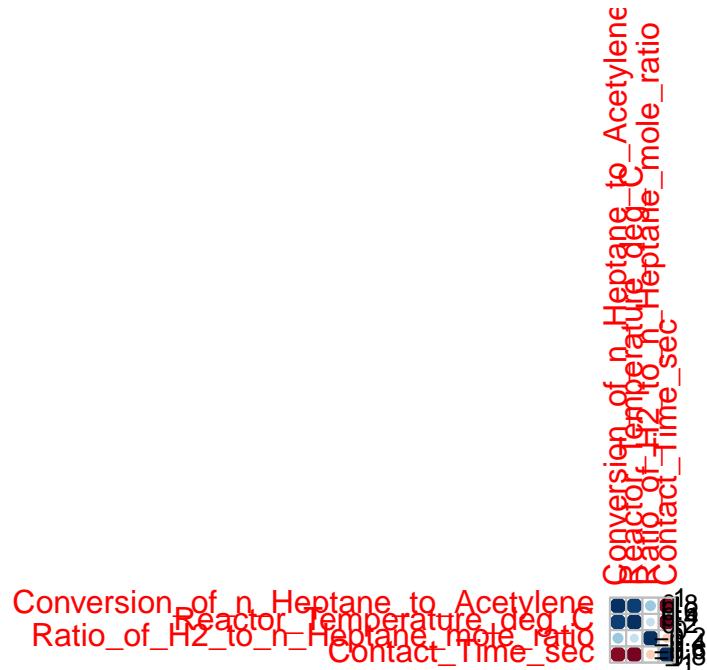
df2=df

#standardizing the regressors
df2[,2:4]=apply(df[,2:4],2,unit_norm)

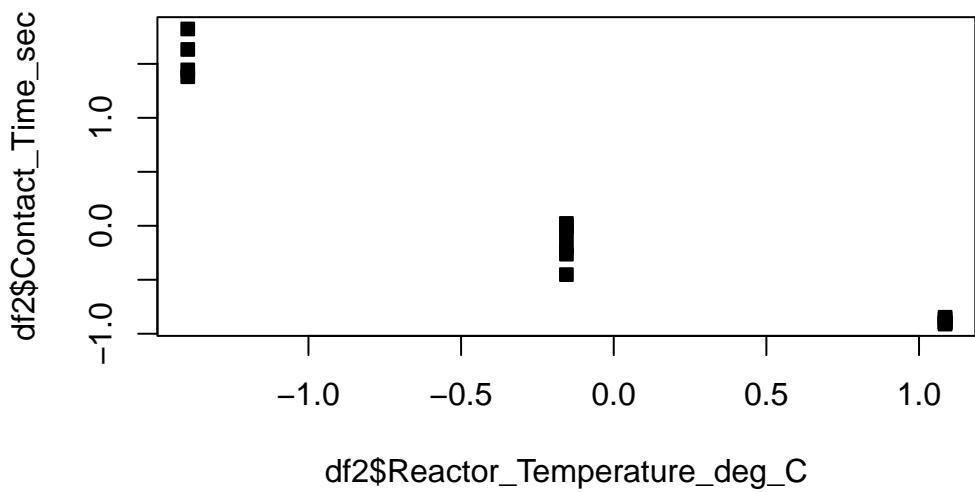
df2=data.frame(df2)
corrplot::corrplot(cor(df2))

```

Warning in corrplot::corrplot(cor(df2)): Not been able to calculate text margin, please try again with a clean new empty window using {plot.new(); dev.off()} or reduce tl.cex



```
# Observe the high correlations between Contact time and Reactor temperature
plot(df2$Reactor_Temperature_deg_C,df2$Contact_Time_sec,pch=22,bg=1)
```



```

orig=names(df2)
names(df2)=c('P','t','H','C')

df2$t2=df2$t^2
df2$H2=df2$H^2
df2$C2=df2$C^2

RS=lm(P~t+H+C+t*C+H*t2+H2+C2 ,df2)
summary(RS)

```

Call:

```
lm(formula = P ~ t + H + C + t * H + t * C + C * H + t2 + H2 +
   C2, data = df2)
```

Residuals:

Min	1Q	Median	3Q	Max
-1.3499	-0.3411	0.1297	0.5011	0.6720

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )		
(Intercept)	35.8958	1.0916	32.884	5.26e-08 ***		
t	4.0038	4.5087	0.888	0.408719		
H	2.7783	0.3071	9.048	0.000102 ***		
C	-8.0423	6.0707	-1.325	0.233461		
t2	-12.5236	12.3238	-1.016	0.348741		
H2	-0.9727	0.3746	-2.597	0.040844 *		
C2	-11.5932	7.7063	-1.504	0.183182		
t:H	-6.4568	1.4660	-4.404	0.004547 **		
t:C	-26.9804	21.0213	-1.283	0.246663		
H:C	-3.7681	1.6553	-2.276	0.063116 .		
---						
Signif. codes:	0 '***'	0.001 '**'	0.01 '*'	0.05 '.'	0.1 ' '	1

Residual standard error: 0.9014 on 6 degrees of freedom  
Multiple R-squared: 0.9977, Adjusted R-squared: 0.9943  
F-statistic: 289.7 on 9 and 6 DF, p-value: 3.225e-07

```

# Crazy high VIF
car::vif(RS)

```

```
there are higher-order terms (interactions) in this model
consider setting type = 'predictor'; see ?vif
```

	t	H	C	t2	H2	C2
375.247759	1.740631	680.280039	1762.575365	3.164318	1156.766284	
	t:H	t:C	H:C			
31.037059	6563.345193		35.611286			

```
car::vif(RS,type='predictor')
```

GVIFs computed for predictors

	GVIF	Df	GVIF^(1/(2*Df))	Interacts With Other Predictors
t	51654.740516	6	2.470354	H, C t2, H2, C2
H	51654.740516	6	2.470354	t, C t2, H2, C2
C	51654.740516	6	2.470354	t, H t2, H2, C2
t2	1762.575365	1	41.983037	-- t, H, C, H2, C2
H2	3.164318	1	1.778853	-- t, H, C, t2, C2
C2	1156.766284	1	34.011267	-- t, H, C, t2, H2

```
# hidden extrapolation - be careful
```

```
# Create a grid to extrapolate over
c_grid=seq(-2,2,l=100)
t_grid=seq(-2,2,l=100)
g=expand.grid(t_grid,c_grid)
```

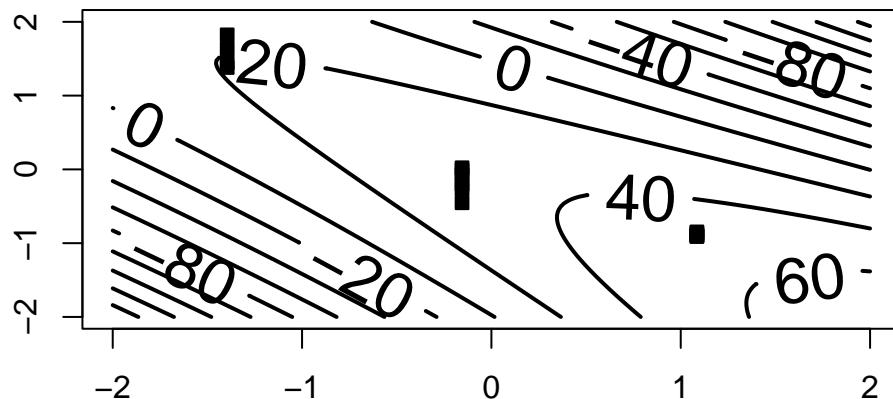
```
# Adding a fixed value of H=-0.6082179
g=cbind(g,rep(-0.6082179,nrow(g)))
# Adding H^2
g=cbind(g,g^2)
```

```
# Making new dataframe for predictions
new_dat=data.frame(g)
names(new_dat)=c("t","C","H","t2","C2","H2")
```

```
# Predicting the values on the grid
Z=predict.lm(RS,new_dat)
```

```
contour(c_grid,t_grid,matrix(Z, ncol = length(t_grid)),lwd=2,labcex=2,ylim=c(-1,1)*2,xlim=
```

```
points(df2$t,df2$C,pch=22,bg=1)
```



```
## Notice that as soon as we leave the region with data, the response becomes negative.  
# Recall that it is a percentage and can't be negative  
## This shows that mild extrapolation dangerous!
```

**Example 8.3.** Use the NFL data from the textbook - regress the number of wins against all variables. Check for multicollinearity. Propose a method to resolve the multicollinearity.

```
#####  
#  
#  
#  
#      NFL DATA EXAMPLE  
#  
#  
#####  
  
df=MPV::table.b1  
# Note
```

```
df
```

	y	x1	x2	x3	x4	x5	x6	x7	x8	x9
1	10	2113	1985	38.9	64.7	4	868	59.7	2205	1917
2	11	2003	2855	38.8	61.3	3	615	55.0	2096	1575
3	11	2957	1737	40.1	60.0	14	914	65.6	1847	2175
4	13	2285	2905	41.6	45.3	-4	957	61.4	1903	2476
5	10	2971	1666	39.2	53.8	15	836	66.1	1457	1866
6	11	2309	2927	39.7	74.1	8	786	61.0	1848	2339
7	10	2528	2341	38.1	65.4	12	754	66.1	1564	2092
8	11	2147	2737	37.0	78.3	-1	761	58.0	1821	1909
9	4	1689	1414	42.1	47.6	-3	714	57.0	2577	2001
10	2	2566	1838	42.3	54.2	-1	797	58.9	2476	2254
11	7	2363	1480	37.3	48.0	19	984	67.5	1984	2217
12	10	2109	2191	39.5	51.9	6	700	57.2	1917	1758
13	9	2295	2229	37.4	53.6	-5	1037	58.8	1761	2032
14	9	1932	2204	35.1	71.4	3	986	58.6	1709	2025
15	6	2213	2140	38.8	58.3	6	819	59.2	1901	1686
16	5	1722	1730	36.6	52.6	-19	791	54.4	2288	1835
17	5	1498	2072	35.3	59.3	-5	776	49.6	2072	1914
18	5	1873	2929	41.1	55.3	10	789	54.3	2861	2496
19	6	2118	2268	38.2	69.6	6	582	58.7	2411	2670
20	4	1775	1983	39.3	78.3	7	901	51.7	2289	2202
21	3	1904	1792	39.7	38.1	-9	734	61.9	2203	1988
22	3	1929	1606	39.7	68.8	-21	627	52.7	2592	2324
23	4	2080	1492	35.5	68.8	-8	722	57.8	2053	2550
24	10	2301	2835	35.3	74.1	2	683	59.7	1979	2110
25	6	2040	2416	38.7	50.0	0	576	54.9	2048	2628
26	8	2447	1638	39.9	57.1	-8	848	65.3	1786	1776
27	2	1416	2649	37.4	56.3	-22	684	43.8	2876	2524
28	0	1503	1503	39.3	47.0	-9	875	53.5	2560	2241

```
summary(df)
```

	y	x1	x2	x3	x4
Min.	: 0.000	Min. :1416	Min. :1414	Min. :35.10	Min. :38.10
1st Qu.	: 4.000	1st Qu.:1896	1st Qu.:1714	1st Qu.:37.38	1st Qu.:52.42
Median	: 6.500	Median :2111	Median :2106	Median :38.85	Median :57.70
Mean	: 6.964	Mean :2110	Mean :2127	Mean :38.64	Mean :59.40
3rd Qu.	:10.000	3rd Qu.:2303	3rd Qu.:2474	3rd Qu.:39.70	3rd Qu.:68.80

```

Max.    :13.000   Max.    :2971    Max.    :2929    Max.    :42.30    Max.    :78.30
      x5          x6          x7          x8
Min.    :-22.00   Min.    : 576.0   Min.    :43.80   Min.    :1457
1st Qu.: -5.75   1st Qu.: 710.5   1st Qu.:54.77   1st Qu.:1848
Median  :  1.00   Median  : 787.5   Median  :58.65   Median  :2050
Mean    :  0.00   Mean    : 789.9   Mean    :58.16   Mean    :2110
3rd Qu.:  6.25   3rd Qu.: 869.8   3rd Qu.:61.10   3rd Qu.:2320
Max.    : 19.00   Max.    :1037.0   Max.    :67.50   Max.    :2876
      x9
Min.    :1575
1st Qu.:1913
Median  :2101
Mean    :2128
3rd Qu.:2328
Max.    :2670

```

```
names(df)
```

```
[1] "y"   "x1"  "x2"  "x3"  "x4"  "x5"  "x6"  "x7"  "x8"  "x9"
```

```

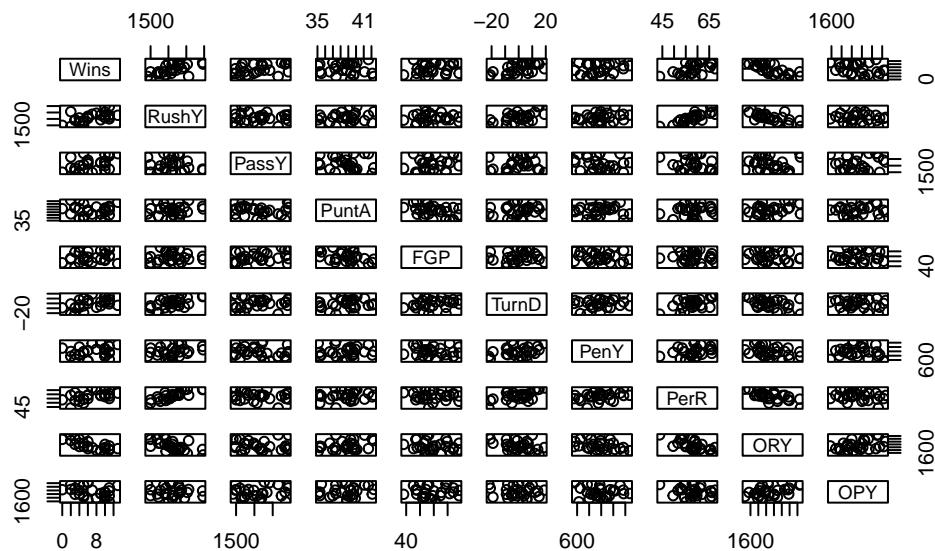
names(df)=c("Wins", "RushY", "PassY",
          "PuntaA", "FGP", "TurnD",
          "PenY", "PerR", "ORY", "OPY")
summary(df)

```

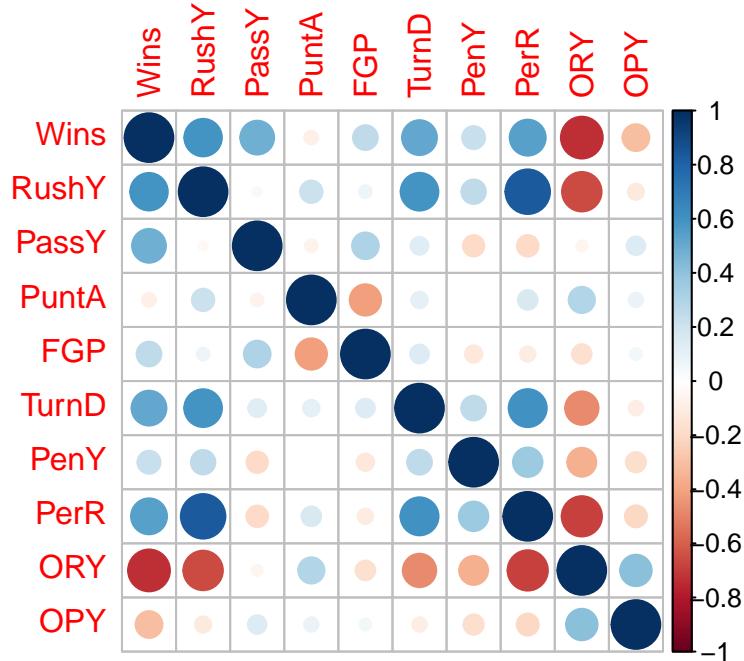
	Wins	RushY	PassY	PuntaA	FGP
Min.	0.000	Min.    :1416	Min.    :1414	Min.    :35.10	Min.    :38.10
1st Qu.	4.000	1st Qu.:1896	1st Qu.:1714	1st Qu.:37.38	1st Qu.:52.42
Median	6.500	Median  :2111	Median  :2106	Median  :38.85	Median  :57.70
Mean	6.964	Mean    :2110	Mean    :2127	Mean    :38.64	Mean    :59.40
3rd Qu.	10.000	3rd Qu.:2303	3rd Qu.:2474	3rd Qu.:39.70	3rd Qu.:68.80
Max.	13.000	Max.    :2971	Max.    :2929	Max.    :42.30	Max.    :78.30
	TurnD	PenY	PerR	ORY	
Min.	-22.00	Min.    : 576.0	Min.    :43.80	Min.    :1457	
1st Qu.	-5.75	1st Qu.: 710.5	1st Qu.:54.77	1st Qu.:1848	
Median	1.00	Median  : 787.5	Median  :58.65	Median  :2050	
Mean	0.00	Mean    : 789.9	Mean    :58.16	Mean    :2110	
3rd Qu.	6.25	3rd Qu.: 869.8	3rd Qu.:61.10	3rd Qu.:2320	
Max.	19.00	Max.    :1037.0	Max.    :67.50	Max.    :2876	
	OPY				

```
Min.    :1575  
1st Qu.:1913  
Median  :2101  
Mean    :2128  
3rd Qu.:2328  
Max.    :2670
```

```
plot(df)
```



```
model=lm(Wins~.,data=df)  
##### Multicollinearity  
  
##### Corr plot  
corrplot::corrplot(cor(df))
```



```
##### VIF
car::vif(model)
```

```
RushY      PassY      PuntA      FGP       TurnD      PenY      PerR      ORY
4.827645  1.420161  2.126597  1.566107  1.924035  1.275979  5.414572  4.535643
          OPY
1.423390
```

```
# recalculating via the X'X matrix
X=model.matrix(model)
dim(X)
```

```
[1] 28 10
```

```
#standardizing
X2=apply(X,2,function(x){(x-mean(x))/sqrt(sum((x-mean(x))^2))}); dim(X2)
```

```
[1] 28 10
```

```

#replacing with column of ones again
X2[,1]=X[,1]
X=X2
diag(solve(t(X)%*%X))

(Intercept)      RushY      PassY      PuntA      FGP      TurnD
0.03571429  4.82764538  1.42016105  2.12659726  1.56610698  1.92403474
          PenY      PerR      ORY      OPY
1.27597850  5.41457162  4.53564335  1.42338989

# observe that
model=lm(RushY~.,data=df[,-1])
s=summary(model)
(1-s$r.squared)^(-1)

[1] 4.827645

##### Condition Number / Eigenvalue / Eigenvector
X=model.matrix(model)
dim(X)

[1] 28  9

#standardizing
X2=apply(X,2,function(x){(x-mean(x))/sqrt(sum((x-mean(x))^2))}); dim(X2)

[1] 28  9

X2[,1]=X[,1]
X=X2

ev=eigen(t(X)%*%X)
xev=ev$values
condition_number=max(xev)/min(xev)
condition_number

[1] 215.646

```

```

sort(xev)

[1] 0.1298424 0.3552922 0.5328487 0.6867363 0.8232325 1.2191453 1.6977743
[8] 2.5551283 28.0000000

#index of minimum eigenvalue
minn=which.min(xev)
ev$vectors[,minn]

[1] -1.675215e-16 -2.109094e-01 2.615778e-01 -4.250523e-02 1.442042e-01
[6] -4.744502e-02 -6.475229e-01 -6.423531e-01 1.741790e-01

rownames(ev$vectors)=names(model$coefficients)
ev$vectors

 [,1]          [,2]          [,3]          [,4]
(Intercept) 1.000000e+00 -3.434947e-17 5.656001e-17 1.332883e-16
PassY       -1.931673e-17  8.040232e-02 4.548137e-01 -4.590825e-01
Punta        1.733313e-16  2.847481e-02 -5.282204e-01 -5.050070e-01
FGP          6.643674e-18 -1.498563e-02 6.360469e-01 -4.652414e-02
TurnD        1.358771e-18 -4.436052e-01 9.254740e-02 -4.700157e-01
PenY         -4.747269e-17 -3.638914e-01 -1.751243e-01 1.469074e-01
PerR         -4.843659e-17 -5.401530e-01 -1.437332e-01 -1.847958e-01
ORY          -9.496374e-17  5.364518e-01 -2.217080e-01 -1.153371e-01
OPY          1.353659e-16  2.893988e-01 2.291129e-02 -4.920345e-01
 [,5]          [,6]          [,7]          [,8]
(Intercept) 1.753269e-17 4.497241e-17 -8.295922e-18 9.898359e-17
PassY       3.414787e-01 5.912719e-01 2.410126e-01 -8.451722e-02
Punta        2.835269e-01 3.495064e-02 -3.785463e-01 -4.145009e-01
FGP          -1.687798e-01 -2.417375e-01 -6.140270e-01 -3.567854e-01
TurnD        -9.900605e-03 -1.291665e-01 -2.199263e-01 6.984198e-01
PenY         -5.210958e-01 6.822653e-01 -2.680418e-01 -6.487362e-02
PerR         -4.221330e-02 -3.015818e-01 2.274534e-01 -2.994520e-01
ORY          -9.681973e-02 2.538335e-02 -3.566234e-01 3.161428e-01
OPY          -7.012299e-01 -1.302810e-01 3.499387e-01 -1.101525e-01
 [,9]
(Intercept) -1.675215e-16
PassY       -2.109094e-01
Punta        2.615778e-01

```

```

FGP      -4.250523e-02
TurnD    1.442042e-01
PenY    -4.744502e-02
PerR    -6.475229e-01
ORY     -6.423531e-01
OPY     1.741790e-01

```

```

# names(model$coefficients)[abs(round(ev$vectors[,minn],1))>0]
round(ev$vectors[,minn],1)

```

(Intercept)	PassY	PuntA	FGP	TurnD	PenY
0.0	-0.2	0.3	0.0	0.1	0.0
PerR	ORY	OPY			
-0.6	-0.6	0.2			

```
# What should we do?
```

```

df$RushDiff=(df$RushY-df$ORY)
# df$RushDiffPer=df$RushY/(df$RushY+df$ORY)

# paste(names(df),collapse='+')

model=lm(Wins~PassY+PuntA+FGP+TurnD+PenY+PerR+OPY+RushDiff,data=df)
summary(model)

```

Call:

```
lm(formula = Wins ~ PassY + PuntA + FGP + TurnD + PenY + PerR +
    OPY + RushDiff, data = df)
```

Residuals:

Min	1Q	Median	3Q	Max
-3.6976	-0.8333	0.0823	0.7845	2.7968

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	-6.5581613	12.7312595	-0.515	0.612409
PassY	0.0037880	0.0008196	4.622	0.000186 ***
PuntA	-0.0208741	0.2052446	-0.102	0.920057
FGP	0.0249704	0.0407274	0.613	0.547073

```

TurnD      -0.0029187  0.0465199  -0.063  0.950628
PenY       0.0021519  0.0031747   0.678  0.506053
PerR       0.1388836  0.1504572   0.923  0.367542
OPY        -0.0023446  0.0012749  -1.839  0.081587 .
RushDiff    0.0023289  0.0011199   2.080  0.051347 .

---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

```

```

Residual standard error: 1.822 on 19 degrees of freedom
Multiple R-squared:  0.8071,    Adjusted R-squared:  0.7258
F-statistic: 9.935 on 8 and 19 DF,  p-value: 2.305e-05

```

```

corrplot::corrplot(cor(df))
car::vif(model)

```

```

PassY      PuntA      FGP      TurnD      PenY      PerR      OPY RushDiff
1.360875  1.347757  1.514088  1.914974  1.230133  5.347319  1.162295 4.774672

```

```

model=lm(Wins~PassY+PuntA+FGP+TurnD+PenY+OPY+RushDiff,data=df)
summary(model)

```

Call:

```

lm(formula = Wins ~ PassY + PuntA + FGP + TurnD + PenY + OPY +
    RushDiff, data = df)

```

Residuals:

Min	1Q	Median	3Q	Max
-3.9325	-0.9011	-0.1062	0.9020	3.0495

Coefficients:

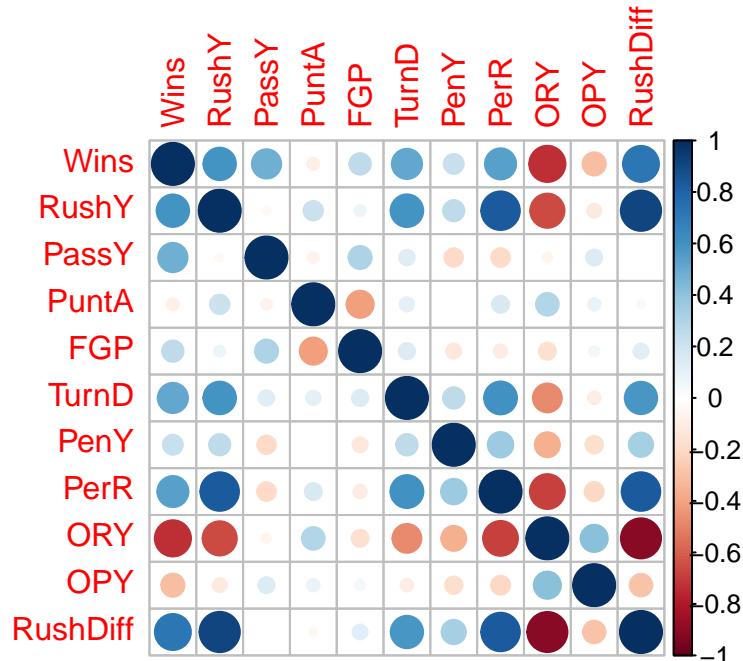
	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	0.8643720	9.8338943	0.088	0.930833
PassY	0.0035079	0.0007586	4.624	0.000164 ***
PuntA	0.0143946	0.2009097	0.072	0.943594
FGP	0.0156562	0.0393115	0.398	0.694659
TurnD	0.0114784	0.0436650	0.263	0.795336
PenY	0.0023024	0.0031587	0.729	0.474510
OPY	-0.0021934	0.0012596	-1.741	0.096996 .
RushDiff	0.0031495	0.0006787	4.641	0.000158 ***

```
---
```

```
Signif. codes: 0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1
```

```
Residual standard error: 1.815 on 20 degrees of freedom  
Multiple R-squared: 0.7984, Adjusted R-squared: 0.7279  
F-statistic: 11.32 on 7 and 20 DF, p-value: 9.485e-06
```

```
corrplot::corrplot(cor(df))
```



```
car::vif(model)
```

	PassY	PuntA	FGP	TurnD	PenY	OPY	RushDiff
PassY	1.174416						
PuntA	1.301051	1.421150					
FGP	1.421150	1.699715	1.226886				
TurnD	1.699715	1.226886	1.143100				
PenY	1.226886	1.143100	1.766523				
OPY							
RushDiff							

There are four primary sources/causes of multicollinearity :

- The data collection method employed: In this case, some of the variables are typically confounded and/or the experiment/study was not well-designed.
- Constraints on the model or in the population: Sometimes, only certain combinations of levels of variables can be observed together.

- Model specification: Sometimes you have two or more variables in your model that are measuring the same thing.
- An overdefined model: You have too many variables in your model.

Make sure to check for each of these. Sometimes, regression coefficients have the wrong sign. This is likely due to one of the following:

- The range of some of the regressors is too small – if the range of some of the regressors is too small, then the variance of  $\hat{\beta}$  is high.
- Important regressors have not been included in the model.
- **Multicollinearity is present.**
- Computational errors have been made.

Multicollinearity can be cured with:

1. more data (lol often not possible), 2, model re-specification: Can you include a function of the variables that preserves the information, but aren't linearly dependent? Can you remove a variable?
2. Or, a modified version of regression, one of Lasso, ridge or elastic net regression.

## 8.3 Homework questions

Complete the Chapter 9 textbook questions.

**Exercise 8.1.** Check for multicollinearity in all of our past examples.

**Exercise 8.2.** Summarize the 3 multicollinearity diagnostics.

# 9 Variable/Model Selection

## 9.1 Variable Selection

In the preceding lessons we have assumed that the regressor variables included in the model are known to be important. Our focus was on techniques to ensure that the functional form of the model was correct and that the underlying assumptions were not violated. In previous lessons, we have employed the classical approach to regression model selection, which assumes that we have a very good idea of the basic form of the model and that we know all (or nearly all) of the regressors that should be used.

Our approach so far can be summarized as follows:

- Fit the full model.
- Perform a thorough analysis of this model, including a full residual analysis and investigation of multicollinearity.
- Determine if transformations of the response or of some of the regressors are necessary.
- Use the  $t$ -tests/ $F$ -tests on the individual regressors to edit the model.
- Perform a thorough analysis of the edited model, especially a residual analysis, to determine the model's adequacy.

In many problems the analyst has a rather large pool of possible candidate regressors, of which only a few are likely to be important. Finding an appropriate subset of regressors for the model is often called the **variable selection** problem .

 Note

Variable selection can address multicollinearity, through the removal of unnecessary variables.

Building a regression model that includes only a subset of the available regressors involves two conflicting objectives:

1. We would like the model to include as many regressors as possible so that the information about  $Y$  contained in these factors can influence the predicted value of  $\hat{Y}$ .
2. We want the model to include as few regressors as possible because the variance of  $\hat{Y}$  increases as the number of regressors increases. Also the more regressors there are in a model, the greater the costs of data collection and model maintenance.

Therefore, we seek a model that is a compromise between these two objectives. There are several algorithms that can be used for variable selection, and these procedures frequently specify different subsets of the candidate regressors as best.

Variable selection is often developed in an idealized setting: Assumed that the correct functional specification of the regressors is known, and no outliers are present. In practice – it's messy. Residual analysis is useful in revealing functional forms of regressors that might be investigated, in pointing out new candidate regressors, and for identifying defects in the data such as outliers. The effect of influential observations should also be determined. Although ideally these problems should be solved simultaneously, an iterative approach is often employed, in which (1) a particular variable selection strategy is employed and then (2) the resulting subset model is checked for correct functional specification, outliers, and influential observations. This may indicate that step 1 must be repeated. Several iterations may be required to produce an adequate model.

None of the variable selection procedures described are guaranteed to produce the best model for a given data set. In fact, there is usually not a single best model but rather several equally good ones. Variable selection algorithms are heavily algorithmic so it is tempting to place a lot of confidence in the results of a particular procedure. Beware of this - experience, professional judgment and subjective considerations are also critical to the variable selection problem. Variable selection procedures should be used in conjunction with these.

Two key aspects of the variable selection problem are:

1. Generating the subset models.
2. Deciding if one subset is better than another.

## 9.2 Deciding if one subset is better than another

### 9.2.1 Coefficients of determination

Recall that

$$R^2 = \frac{SSModel}{SST} = 1 - \frac{SSE}{SST}.$$

We know that  $R^2$  increases as  $p$  increases, so we cannot choose the model with the largest  $R^2$ . However, we could add variables one at a time until the marginal increase in  $R^2$  is small.

**Example 9.1.** Recall example Example 6.6. Investigate the  $R^2$  curve through adding the variables one at a time.

```
custom_palette = c(
  "#1f77b4", "#ff7f0e", "#2ca02c", "#d62728",
  "#9467bd", "#8c564b", "#e377c2", "#7f7f7f",
```

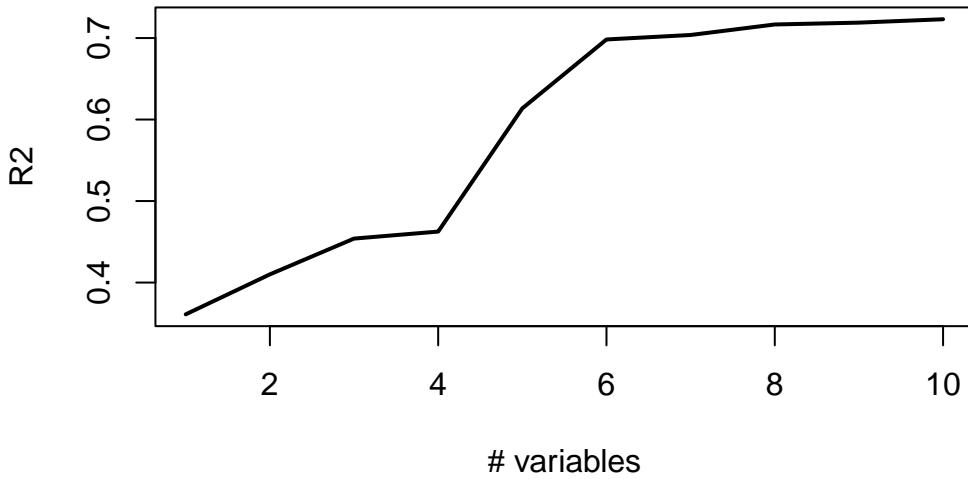
```

  "#bcbd22", "#17becf", "#393b79",
  "#8c6d31", "#9c9ede", "#637939", "#eb348f"
)

df_clean4$d_3=df_clean4$District==3
var_list=names(df_clean4)[-c(11,12)]
df2=df_clean4[-11142,]
#previous...
full_model=lm(Sale_price~ District + Extwall +
               Stories + Year_Built + Fin_sqft +
               Units + Bdrms +
               Fbath + Lotsize + Sale_date +District*Lotsize,df2)

#####
# R2
r2=c()
for(i in 1:length(var_list)){
  vars=c(var_list[1:i],"Sale_price")
  model2=lm(Sale_price~.,df2[,vars])
  sm=summary(model2)
  r2=c(r2,sm$r.squared)
}
plot(r2,type='l',lwd=2,ylab="R2",xlab="# variables")

```



```
var_list[1:6]
```

```
[1] "District"    "Extwall"     "Stories"      "Year_Built"  "Fin_sqft"
[6] "Units"
```

Notice how the curve levels off at 6 variables. This would indicate that we are not gaining much explained variation beyond the first 6 variables. These variables are printed above.

Recall that

$$\bar{R}^2 = 1 - \frac{n-1}{n-p}(1 - R^2).$$

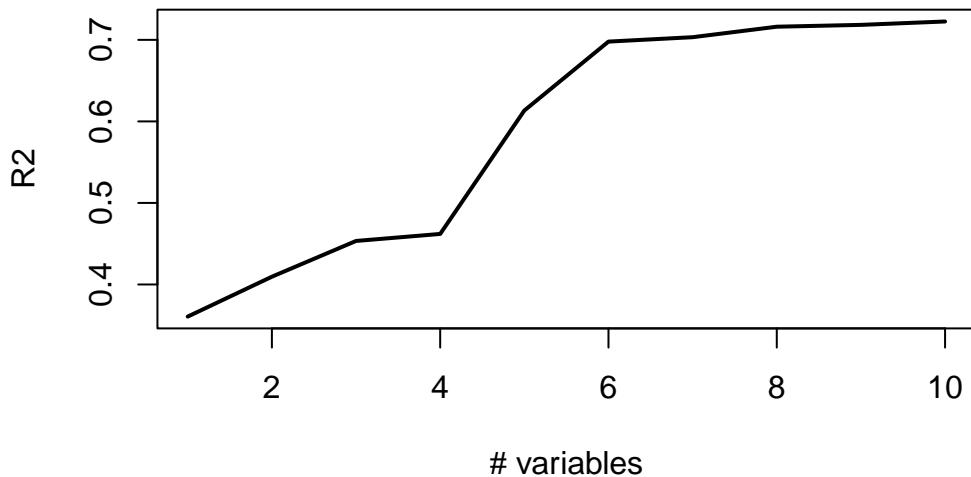
The  $\bar{R}^2$  statistic does not necessarily increase as additional regressors are introduced into the model. In fact, it can be shown that if  $s$  regressors are added to the model, the new  $\bar{R}^2$  will exceed the original  $\bar{R}^2$  if and only if the partial  $F$  statistic for testing the significance of the  $s$  additional regressors exceeds 1. Consequently, one criterion for selection of an optimum subset model is to choose the model that has a maximum  $\bar{R}^2$ . In addition, note that maximizing  $\bar{R}^2$  is equivalent to choosing the model with the minimum  $MSE$ .

```
# R2 adjusted
r2=c()
for(i in 1:length(var_list)){
  vars=c(var_list[1:i],"Sale_price")
```

```

model2=lm(Sale_price~.,df2[,vars])
sm=summary(model2)
r2=c(r2,sm$adj.r.squared)
}
plot(r2,type='l',lwd=2,ylab="R2",xlab="# variables")

```



```
var_list[1:6]
```

```
[1] "District"    "Extwall"      "Stories"       "Year_Built"   "Fin_sqft"
[6] "Units"
```

### 9.2.2 Mallows $C_k$ criterion

Consider the complete model:

$$(C) \quad Y = \beta_1 + \beta_2 X_1 + \cdots + \beta_p X_p + \epsilon$$

and a reduced model with  $(k - 1)$  explanatory variables

$$Y = \beta_1 + \beta_1 X_1 + \cdots + \beta_k X_k + \epsilon.$$

Mallows (1973) defined the  $C_k$  statistic as

$$C_k = \frac{SSE_R}{MSE_C} - (n - 2k)$$

where  $k$  is the number of columns in  $X$  in the reduced model.

Observe that if  $k = p$  then

$$C_k = C_p = dfE_C - [n - 2p] = p = k.$$

Let  $\text{Bias} = E[\hat{Y}_i] - E[Y_i]$  where  $\hat{Y}_i$  are generated from the reduced model. It can be shown that

$$E[C_k | \text{Bias} = 0] = k.$$

That is, if the regression model based on the subset of  $k - 1$  predictors is unbiased, then we expect  $C_k$  to be roughly  $k$ . In addition, if there is bias, then  $E[C_k] > k$ . Therefore, it is suggested that from all possible models, we choose the model with  $C_k$  close to  $k$  **and**  $C_k \leq k$ . This is a little bit subjective: For example, the smallest  $C_k$  is  $C_4 = 4.1$  and the next smallest is  $C_5 = 4.7$ .  $C_4$  is smallest but  $C_4 > 4$  – the model may be biased. Now,  $C_5$  is the second smallest,  $C_5 < 5$  implies the model is likely not biased.

**Example 9.2.** Recall example Example 6.6. Investigate the Mallows  $C_k$  of the models considered in Example 9.9. In addition, compare the `model_1` and `model_2` below, using `full_model` as the complete model.

```
# Mallows C
# install.packages('olsrr')

# Recall the complete model
full_model=lm(Sale_price~ District + Extwall +
               Stories + Year_Built + Fin_sqft +
               Units + Bdrms +
               Fbath + Lotsize + Sale_date +District*Lotsize,df2)

# Potential models
model_1=lm(Sale_price~ District + Fin_sqft + Sale_date ,df2)

model_2=lm(Sale_price~ District + Extwall +
               Stories + Year_Built + Fin_sqft +
               Units + Bdrms +
               Fbath + Lotsize + Sale_date ,df2)
```

```

olsrr::ols_mallows_cp(model_1,full_model)

[1] 17131

olsrr::ols_mallows_cp(model_2,full_model)

[1] 3505.586

for(i in 1:length(var_list)){
  vars=c(var_list[1:i],"Sale_price")
  model=lm(Sale_price~.,df_clean4[,vars])
  print(paste0("k" ,i," mallows C_k ",
    olsrr::ols_mallows_cp(model,full_model),sep=""))
}

[1] "k1 mallows C_k 40548.5008352938"
[1] "k2 mallows C_k 35586.0286701987"
[1] "k3 mallows C_k 31143.8465791983"
[1] "k4 mallows C_k 30228.81611156"
[1] "k5 mallows C_k 14773.9666340633"
[1] "k6 mallows C_k 6191.00700048948"
[1] "k7 mallows C_k 5624.03575517497"
[1] "k8 mallows C_k 4298.06818957892"
[1] "k9 mallows C_k 4039.89603591008"
[1] "k10 mallows C_k 3622.28930435513"

```

If every potential model has a high value for Mallows  $C_k$ , this is an indication that some important predictor variables are likely missing from each model. Therefore, we may wish to reevaluate the real estate model.

**Example 9.3.** Use the NFL data from the textbook - Consider the following models provided below. Select the best model from `model`, `model_1` and `model_2` given below, using each of the coefficient of determination criteria and Mallows  $C_k$ .

```

df=MPV::table.b1
# Note
names(df)=c("Wins","RushY","PassY",

```

```

    "PuntaA", "FGP", "TurnD",
    "PenY", "PerR", "ORY", "OPY")
summary(df)

      Wins          RushY        PassY       PuntaA        FGP
Min.   : 0.000  Min.   :1416  Min.   :1414  Min.   :35.10  Min.   :38.10
1st Qu.: 4.000  1st Qu.:1896  1st Qu.:1714  1st Qu.:37.38  1st Qu.:52.42
Median : 6.500  Median :2111  Median :2106  Median :38.85  Median :57.70
Mean   : 6.964  Mean   :2110  Mean   :2127  Mean   :38.64  Mean   :59.40
3rd Qu.:10.000 3rd Qu.:2303  3rd Qu.:2474  3rd Qu.:39.70  3rd Qu.:68.80
Max.   :13.000  Max.   :2971  Max.   :2929  Max.   :42.30  Max.   :78.30

      TurnD          PenY        PerR        ORY
Min.   :-22.00  Min.   : 576.0  Min.   :43.80  Min.   :1457
1st Qu.: -5.75  1st Qu.: 710.5  1st Qu.:54.77  1st Qu.:1848
Median :  1.00  Median : 787.5  Median :58.65  Median :2050
Mean   :  0.00  Mean   : 789.9  Mean   :58.16  Mean   :2110
3rd Qu.:  6.25  3rd Qu.: 869.8  3rd Qu.:61.10  3rd Qu.:2320
Max.   : 19.00  Max.   :1037.0  Max.   :67.50  Max.   :2876

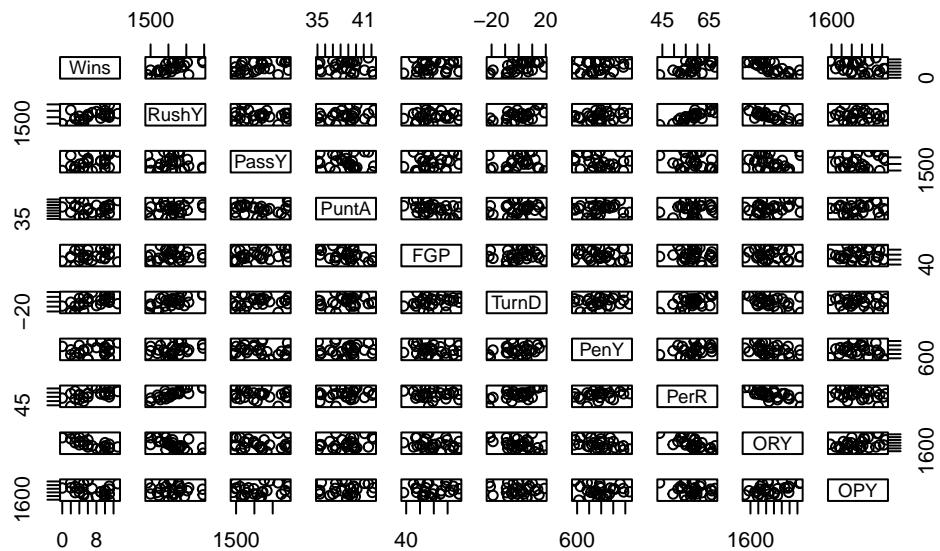
      OPY
Min.   :1575
1st Qu.:1913
Median :2101
Mean   :2128
3rd Qu.:2328
Max.   :2670

```

```
head(df)
```

	Wins	RushY	PassY	PuntaA	FGP	TurnD	PenY	PerR	ORY	OPY
1	10	2113	1985	38.9	64.7	4	868	59.7	2205	1917
2	11	2003	2855	38.8	61.3	3	615	55.0	2096	1575
3	11	2957	1737	40.1	60.0	14	914	65.6	1847	2175
4	13	2285	2905	41.6	45.3	-4	957	61.4	1903	2476
5	10	2971	1666	39.2	53.8	15	836	66.1	1457	1866
6	11	2309	2927	39.7	74.1	8	786	61.0	1848	2339

```
plot(df)
```



```

df$RushDiff=(df$RushY-df$ORY)

model=lm(Wins~PassY+PuntA+FGP+TurnD+PenY+OPY+RushDiff,data=df)
model_1=lm(Wins~ TurnD+PenY+PerR+ORY+OPY ,df)
model_2=lm(Wins~ TurnD+PenY+ORY+OPY,df)

```

```

# 3 ADJ R2
summary(model_1)$r.squared

```

```
[1] 0.5848535
```

```
summary(model_2)$r.squared
```

```
[1] 0.5843435
```

```
summary(model)$r.squared
```

```

[1] 0.7984089

# 3 ADJ R2
summary(model_1)$adj.r.squared

[1] 0.490502

summary(model_2)$adj.r.squared

[1] 0.5120555

summary(model)$adj.r.squared

[1] 0.7278521

##### Mallows C
olsrr::ols_mallows_cp(model_1,model) # k=6

[1] 25.187

olsrr::ols_mallows_cp(model_2,model) # k=5

[1] 23.23759

olsrr::ols_mallows_cp(model,model)

[1] 8

```

We would select `model` as the final model, since it has the lowest values of the Mallows  $C_k$  that is close to the number of variables. In addition, the  $R^2$  jumps significantly when moving from either `model_1` or `model_2` to `model`, so again, we would select `model`. Lastly, the adjusted  $\hat{R}^2$  is the highest for `model`.

### 9.3 Akaike information criterion

- Akaike proposed an information criterion, AIC, based on maximizing the expected *entropy* of the model.
- Entropy is simply a measure of the expected information, in this case the Kullback – Leibler divergence.
- $$AIC = n \log \frac{SSE}{n} + 2p + \text{constant}$$
- The decrease in  $SSE$  is balanced by the  $2p$  penalty
- $AIC$  can be computed for other models, but should only be compared within model classes

### 9.4 Bayesian information criterion/Schwartz information criterion

- Sawa and Schwartz extended AIC, both called BIC.
- This criterion places a greater penalty on adding regressors as the sample size increases.
- $$BIC = n \log \frac{SSE}{n} + p \log n + \text{constant}$$
- $BIC$  can be computed for other models, but should only be compared within model classes

**Example 9.4.** Recall example Example 6.6. Investigate the AIC and BIC of the models considered in Example 9.9. In addition, compare the `model_1`, `model_2` and the `full_model` using AIC and BIC.

```
# Mallows C
# install.packages('olsrr')

# Recall the complete model
full_model=lm(Sale_price~ District + Extwall +
              Stories + Year_Built + Fin_sqft +
              Units + Bdrms +
              Fbath + Lotsize + Sale_date +District*Lotsize,df_clean4)

# Potential models
model_1=lm(Sale_price~ District + Fin_sqft + Sale_date ,df_clean4)

model_2=lm(Sale_price~ District + Extwall +
```

```

Stories + Year_Built + Fin_sqft +
Units + Bdrms +
Fbath + Lotsize + Sale_date ,df_clean4)

# Aic
AIC(full_model)

[1] 589136.3

AIC(model_1)

[1] 602019.6

AIC(model_2)

[1] 592279.3

for(i in 1:length(var_list)){
  vars=c(var_list[1:i],"Sale_price")
  model=lm(Sale_price~.,df_clean4[,vars])
  print(paste0("k" ,i," AIC ",
              AIC(model),sep=""))
}

[1] "k1 AIC 612758.302056694"
[1] "k2 AIC 610831.898564347"
[1] "k3 AIC 608957.605436705"
[1] "k4 AIC 608552.940741352"
[1] "k5 AIC 600431.017183595"
[1] "k6 AIC 594395.93413908"
[1] "k7 AIC 593955.469235904"
[1] "k8 AIC 592860.729755852"
[1] "k9 AIC 592640.317423882"
[1] "k10 AIC 592279.290409805"

# Bic
BIC(full_model)

[1] 589638.7

```

```

BIC(model_1)

[1] 602165.5

BIC(model_2)

[1] 592668.3

for(i in 1:length(var_list)){
  vars=c(var_list[1:i],"Sale_price")
  model=lm(Sale_price~.,df_clean4[,vars])
  print(paste0("k" ,i," AIC ",
              BIC(model),sep=""))
}

[1] "k1 AIC 612887.96764318"
[1] "k2 AIC 611026.396944075"
[1] "k3 AIC 609176.416113899"
[1] "k4 AIC 608779.855517702"
[1] "k5 AIC 600666.0360591"
[1] "k6 AIC 594655.265312051"
[1] "k7 AIC 594287.737301273"
[1] "k8 AIC 593233.518316997"
[1] "k9 AIC 593021.210084183"
[1] "k10 AIC 592668.287169261"

```

We would select `full_model` as the final model, since it has the lowest values of both AIC and BIC.

**Example 9.5.** Use the NFL data from the textbook - Consider the following models provided below. Select the best model from `model`, `model_1` and `model_2` given below, using each of AIC and BIC.

```

model=lm(Wins~PassY+PuntA+FGP+TurnD+PenY+OPY+RushDiff,data=df)
model_1=lm(Wins~ TurnD+PenY+PerR+ORY+OPY ,df)
model_2=lm(Wins~ TurnD+PenY+ORY+OPY,df)

# Bic

```

```
BIC(model)
```

```
[1] 133.4221
```

```
BIC(model_1)
```

```
[1] 146.9846
```

```
BIC(model_2)
```

```
[1] 143.6868
```

```
# Aic  
AIC(model)
```

```
[1] 121.4323
```

```
AIC(model_1)
```

```
[1] 137.6592
```

```
AIC(model_2)
```

```
[1] 135.6936
```

We would select `model` as the final model, since it has the lowest values of both AIC and BIC.

## 9.5 Algorithms for model selection

We now discuss algorithms which auto select the “best” model.

### 9.5.1 All subsets regression

All subsets regression, also known as best subsets regression, is one way to select the best subset of regressors. This technique proceeds as the name implies - it involves evaluating all possible combinations of regressors to identify the model that best fits the data according to a chosen criterion. For instance, if the criterion is AIC, then we may compute the AIC for all possible  $2^p$  models. All subsets regression would choose the model with the lowest AIC. Any of the four criterion (AIC, BIC, Mallows  $C_k$  or adjusted  $R^2$ ) can be used for all subsets regression.

All subsets regression considers all possible subsets of regressors, ensuring that the best model is not missed by the algorithm. However, this has some downsides. First, it can be very computationally intensive for data sets with a large number of regressors. Second, if not properly controlled, examining many models can lead to **overfitting**, especially with small data sets.

Overfitting is when the model fits the data set so well, that it misses the underlying relationship between the independent and dependent variables. This results in a model that fits the data set well, but performs poorly at predicting new, unseen data due to its overly complex structure.

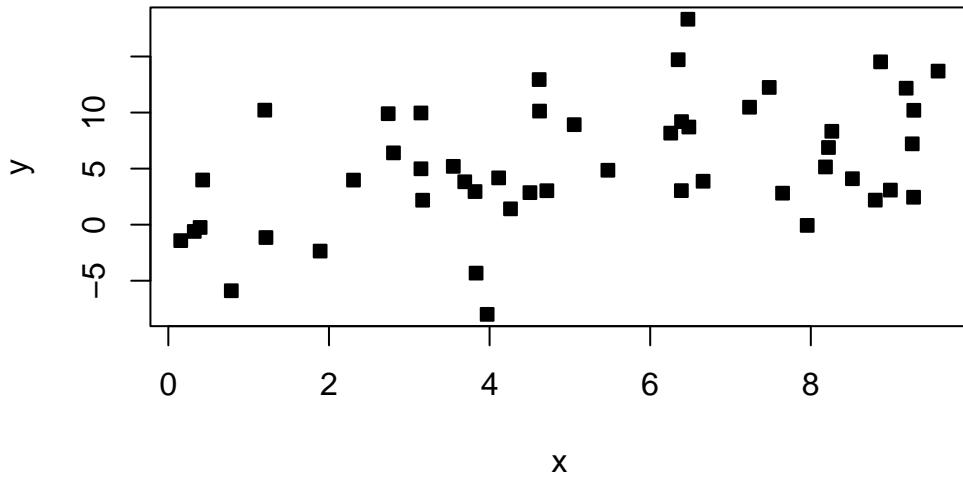
We can observe this in the example below:

```
library(ggplot2)

set.seed(4265)

# Generate sample data
n = 50
x = runif(n, min = 0, max = 10)
y = 1 + x + rnorm(n, sd = 5)

# Create a data frame
data = data.frame(x = x, y = y)
plot(data,pch=22,bg=1)
```



```
# complexity of the model
complexity=9

# Fit a linear regression model
linear_model = lm(y ~ x, data = data)

# Fit a polynomial regression model (degree = complexity) This model has more terms.
poly_model = lm(y ~ poly(x, complexity), data = data)

# Make predictions
linear_predictions = predict(linear_model, data)
poly_predictions = predict(poly_model, data)

# Calculate mean squared error (MSE)
linear_mse = mean((data$y - linear_predictions)^2)
poly_mse = mean((data$y - poly_predictions)^2)

# Print MSE values
cat("Linear Model MSE:", linear_mse, "\n")
```

Linear Model MSE: 24.03022

```

cat("Polynomial Model MSE:", poly_mse, "\n")

Polynomial Model MSE: 19.69118

```

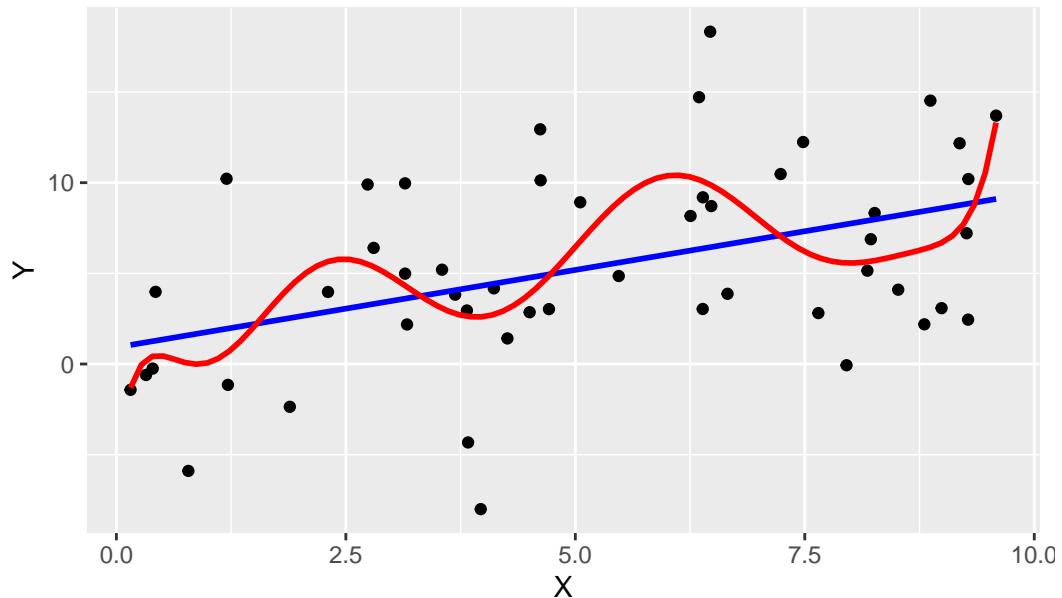
```
# Notice how the squared error is lower for the more complex model?
```

```

# Plot the results - this is GG plot, another way to plot in R
ggplot(data, aes(x, y)) +
  geom_point() +
  geom_smooth(method = "lm", se = FALSE, color = "blue", formula = y ~ x) +
  geom_smooth(method = "lm", se = FALSE, color = "red", formula = y ~ poly(x,complexity))
  labs(title = "Linear vs. Polynomial Regression (Degree 9)",
       x = "X", y = "Y")

```

Linear vs. Polynomial Regression (Degree 9)



```

# Generate new data from the same process
N = 500
xx = runif(n, min = 0, max = 10)
yy = 1 + x + rnorm(n, sd = 5)
nd = data.frame('x'=xx, 'y'=yy)

```

```

gen_linear_predictions = predict(linear_model, nd)
gen_poly_predictions = predict(poly_model, nd)

# Calculate mean squared error (MSE)
gen_linear_mse = mean((data$y - gen_linear_predictions)^2)
gen_poly_mse = mean((data$y - gen_poly_predictions)^2)

# Print MSE values
cat("Linear Model MSE:", gen_linear_mse, "\n")

```

Linear Model MSE: 45.06416

```
cat("Polynomial Model MSE:", gen_poly_mse, "\n")
```

Polynomial Model MSE: 50.40172

```
# Notice how the generalized error is lower for the linear model?
```

Above, we fit two models to the data. One that allows for polynomial functions of degree at most 9 (not just linear functions), and one that only allows linear functions. It is clear that the polynomial model has a lower error on the data set at hand. However, when we generate new data from the same process, the polynomial model has a much higher error. This is an example of overfitting - the complex model does not generalize well beyond the current data set.

**Example 9.6.** Use the NFL data from the textbook - Perform all subsets regression with each of the metrics described above.

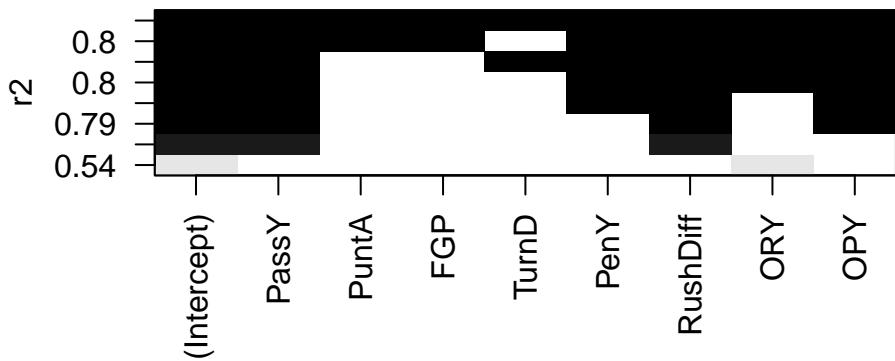
```

# install.packages('leaps')

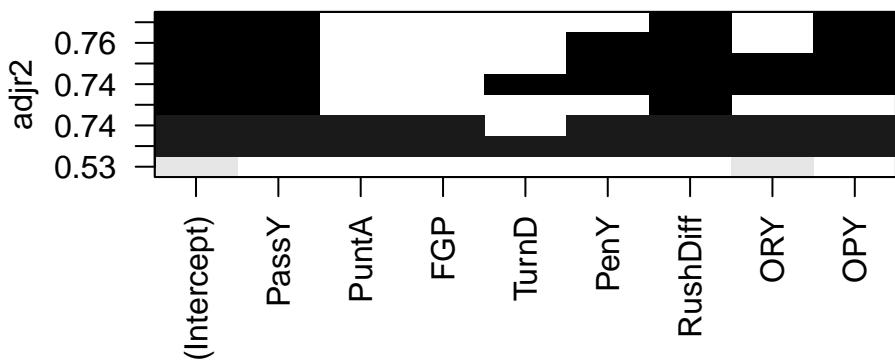
all=leaps::regsubsets(Wins~PassY+PuntA+FGP+TurnD+PenY+RushDiff+ORY+OPY,data=df,nvmax=10,me
# 2^8

plot(all,scale='r2')

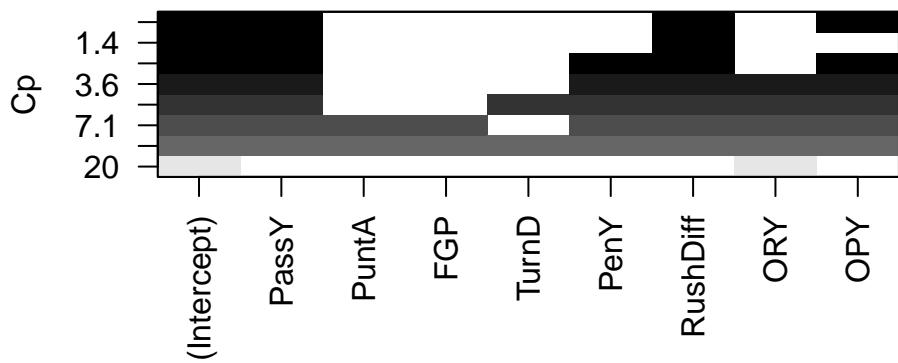
```



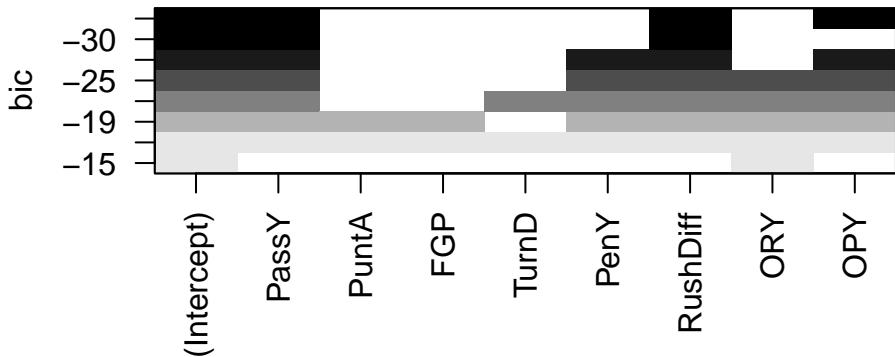
```
plot(all,scale='adjr2')
```



```
plot(all,scale='Cp')
```



```
plot(all,scale='bic')
```



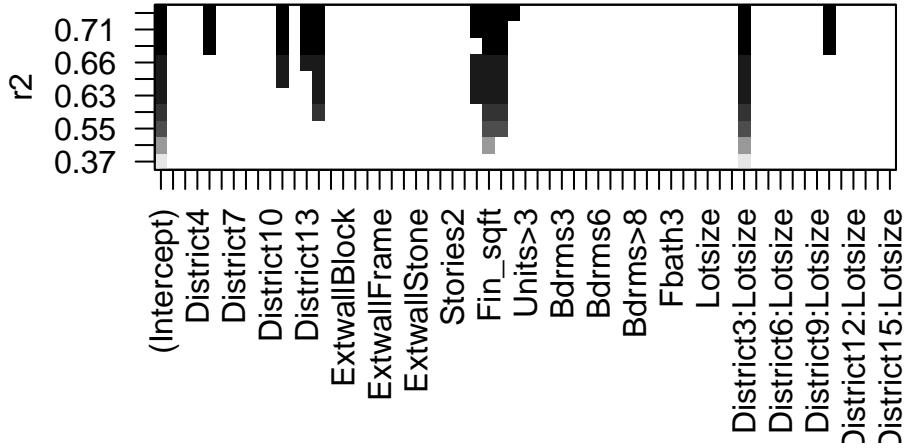
The `leaps` package allows us to do all subsets regression. We see that (with the exception of the  $R^2$ ) the best model under all criterion contains passing yards, rushing yard differential, and opponent passing yards.

We can do the same thing on the real estate data:

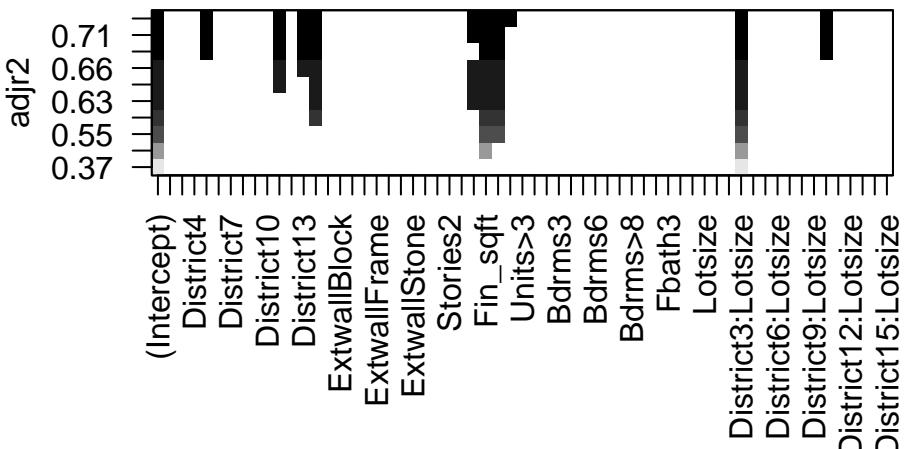
```
# install.packages('leaps')
# If you run this, you will get the following error:
# all=leaps::regsubsets(Sale_price~ District + Extwall +
#                         Stories + Year_Built + Fin_sqft +
#                         Units + Bdrms +
#                         Fbath + Lotsize + Sale_date +District*Lotsize,data=df2,nvmax=10,method="exhaustive")
# "Error in leaps.exhaustive(a, really.big) : Exhaustive search will be SLOW, must specify nvmax"
# This shows how this can quickly become computationally intensive

# You will see that running the following code takes very long!
all=leaps::regsubsets(Sale_price~ District + Extwall +
                      Stories + Year_Built + Fin_sqft +
                      Units + Bdrms +
                      Fbath + Lotsize + Sale_date+District*Lotsize,data=df2,nvmax=10,really.big=TRUE)
```

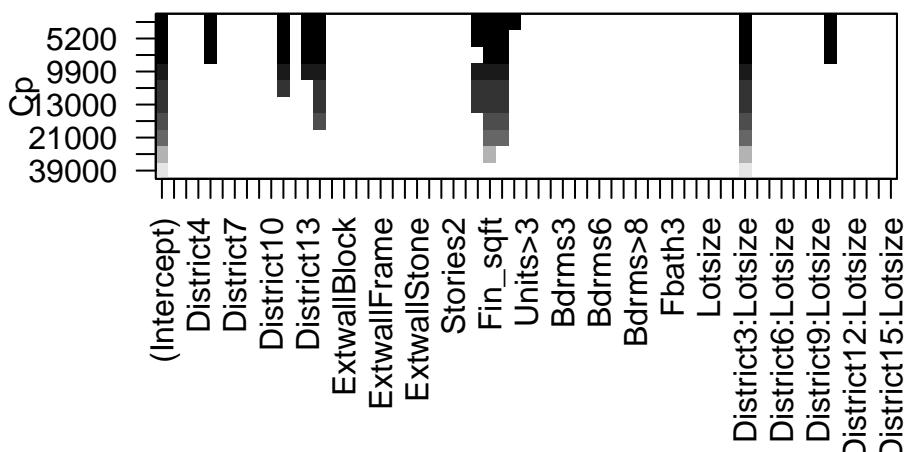
```
plot(all,scale='r2')
```



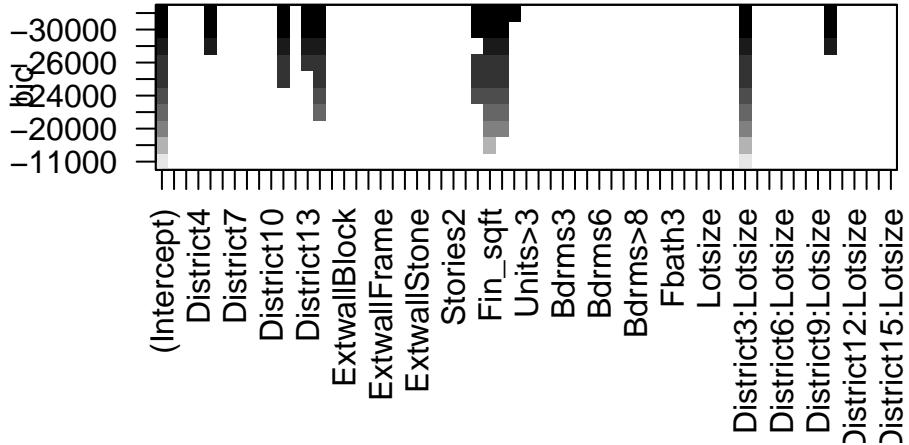
```
plot(all,scale='adjr2')
```



```
plot(all,scale='Cp')
```



```
plot(all,scale='bic')
```



The selected models appear fairly sparse!

### 9.5.2 Forward selection

Forward selection is another common algorithm used to select the best model. It involves adding regressors one by one until adding more regressors becomes unhelpful. Essentially, we find the most “significant” regressor to be added to the model, and add it if it is “significant enough”. We keep adding regressors, until none are significant enough. However, forward selection is “greedy”, in the sense that it does not consider all possible subsets of regressors. This means that it is possible that the “best” model is missed by the algorithm.

The algorithm proceeds as follows:

1. Choose  $\alpha_{entry}$ , which is the significance level for a regressor to enter the model. Set the current model to be  $Y = \beta_0 + \epsilon$ .
2. Among all regressors  $X_i$  not in the current model, test  $H_0 : X_i$  not entered versus  $H_a : X_i$  entered.
3. Choose the covariate with smallest  $p$ -value, i.e. the most likely  $X_i$  to be entered. Say the  $p$ -value for testing  $H_0 : \beta_1 = 0$  is the smallest.

4. If the chosen  $p$ -value is  $\geq \alpha_{entry}$ , then  $X_1$  is not entered, and the current model is chosen as the final model and the process terminates. Otherwise,  $X_1$  is entered and the new current model is set to the current model, with the addition of  $X_1$ .
5. Return to step 2.

Note that once an explanatory variable is entered, it will never leave the model.

**Example 9.7.** Suppose that we have 3 explanatory variables and  $\alpha_{entry}$  is chosen to be 0.05. The following is how we would proceed.

Iteration 1:

Model	$H_a :$	$p$ -value
$Y = \beta_0 + \beta_1 X_1 + \epsilon$	$\beta_1 \neq 0$	0.00033
$Y = \beta_0 + \beta_2 X_2 + \epsilon$	$\beta_2 \neq 0$	0.00490
$Y = \beta_0 + \beta_3 X_3 + \epsilon$	$\beta_3 \neq 0$	0.00101

Since 0.00033 is the smallest  $p$ -value and it is less than  $\alpha_{entry}$ , the chosen model is  $Y = \beta_0 + \beta_1 X_1 + \epsilon$ , and we continue to the next iteration.

Iteration 2:

Model	$H_a :$	$p$ -value
$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$	$\beta_2 \neq 0$	0.01330
$Y = \beta_0 + \beta_1 X_1 + \beta_3 X_3 + \epsilon$	$\beta_3 \neq 0$	0.1125

Since 0.01330 is the smallest  $p$ -value and it is less than  $\alpha_{entry}$ , the chosen model is  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$ , and we continue to the next iteration.

Iteration 3:

Model	$H_a :$	$p$ -value
$Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \epsilon$	$\beta_3 \neq 0$	0.36145

Since 0.36145 is the smallest  $p$ -value and it is greater than  $\alpha_{entry}$ , the chosen model is  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$ , and STOP.

If  $\alpha_{entry}$  is chosen to be 0.01, observe that we will stop at Step 2 and the chosen model is  $Y = \beta_0 + \beta_1 X_1 + \epsilon$ . As you can see, the chosen model is easily affected by the chosen  $\alpha_{entry}$  value.

### 9.5.3 Backward elimination

In Backward elimination, we start with the largest model, i.e., the one with all of the regressors, and eliminate regressors one by one until nothing can be eliminated. Like forward selection, backward selection is also greedy, and therefore, suffers from the same drawbacks.

For  $p - 1$  regressors, the algorithm proceeds as follows:

1. Choose:  $\alpha_{stay}$ , which is the significance level for an explanatory variable to stay in the model. Set the current model to be  $Y = \beta_0 + \beta_1 X_1 + \dots + \beta_{p-1} X_{p-1} + \epsilon$ .
2. Test  $H_0 : X_i$  eliminated versus  $H_a : X_i$  not eliminated, i.e.  $H_0 : \beta_i = 0$  versus  $H_a : \beta_i \neq 0$  with respect to the current model.
3. Choose the regressor with the largest  $p$ -value – i.e., the most likely  $X_i$  to be eliminated. Say  $p$ -value for testing  $H_0 : \beta_p = 0$  is the largest.
4. If the chosen  $p$ -value is  $< \alpha_{stay}$ , then  $X_p$  is not eliminated, and the chosen model is the current model and the process terminates. Otherwise,  $X_p$  is eliminated and the current model is set to be the old current model, with  $X_p$  removed.
5. If there are no regressors in the current model, terminate. Otherwise, go back to step 2.

**Example 9.8.** Suppose that we have 3 explanatory variables and  $\alpha_{stay}$  is chosen to be 0.05. The following is how we would proceed.

The current model is  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \beta_3 X_3 + \epsilon$ .

Iteration 1:

$H_a :$	$p$ -value
$\beta_1 \neq 0$	0.0176
$\beta_2 \neq 0$	0.05627
$\beta_3 \neq 0$	0.36145

Since 0.36145 is the largest  $p$ -value and it is greater than  $\alpha_{stay}$ , the current model is set to be  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$ , and we continue to the next iteration.

Iteration 2:

Model is  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$ .

$H_a :$	$p$ -value
$\beta_1 \neq 0$	0.00139
$\beta_2 \neq 0$	0.01330

Since 0.01330 is the smallest  $p$ -value and it is less than  $\alpha_{stay}$ , the final model is  $Y = \beta_0 + \beta_1 X_1 + \beta_2 X_2 + \epsilon$ , and the process terminates.

If  $\alpha_{stay}$  is chosen to be 0.01, then we will continue the process and eventually, the chosen model is  $Y = \beta_0 + \beta_1 X_1 + \epsilon$ . Again, the chosen model is easily affected by the chosen  $\alpha_{stay}$  value.

In forward selection, once a regressor is entered, it will be in the final model. In backward elimination, once a regressor is eliminated, it will not be in the final model. A combination of these two processes, that allows for variables to enter and exit the model is called **stepwise Regression**.

#### 9.5.4 Stepwise regression

In stepwise regression, we start the model from smallest model,  $Y = \beta_0 + \epsilon$ , and we keep adding and eliminating regressors one by one such that added regressors can be eliminated later and eliminated regressors can be added later. Like forward selection and backward selection, stepwise regression is also greedy, and therefore, suffers from the same drawbacks.

For  $p - 1$  regressors, the algorithm proceeds as follows:

1. Choose:  $\alpha_{enter}$  and  $\alpha_{stay}$ . Set the current model to be  $Y = \beta_0 + \epsilon$ .
2. Set the old model to be the current model. Perform steps 2-4 of forward selection.
3. Suppose in the previous step,  $X_1$  was added to the current model. Next, with the current model, apply steps 2-5 of backward elimination.
4. If  $X_1$  is eliminated in backward elimination, then do not remove  $X_1$  from the current model and set the current model to be the final model. The process then terminates. If the current model equals the old model, terminate. Otherwise, go back to step 2.

The stopping rule for stepwise regression is when we run into infinite loop (the same variable being added and eliminated) OR when we have nothing to add **and** nothing to eliminate.

**i** Note

1. One way to avoid the infinite loop is to choose  $\alpha_{stay} \neq \alpha_{entry}$ .
2. Some books suggest “easy to enter” and “tough to eliminate” strategy for selecting  $\alpha_{stay}, \alpha_{entry}$  but there is no strict rule.
3. R is using the AIC criterion for entering and eliminating, rather than the  $F$  test. This is also acceptable.

**Example 9.9.** Recall the real estate example - Example 6.6. Run forward selection, backward selection and stepwise regression using AIC as the criterion, including all regressors. (AIC is done automatically in R.)

```

# ##### Automated methods #####
#####
##### Forward selection with AIC #####
#####

#define intercept-only model
intercept_only = lm(Sale_price~ 1, data=df2)

# define model with all predictors
all = lm(Sale_price~ ., data=df2)

# perform forward stepwise regression
forward = step(intercept_only, direction='forward', scope=formula(all), trace=0)

#view results of forward stepwise regression
forward$anova

```

	Step	Df	Deviance	Resid. Df	Resid. Dev	AIC
1		NA	NA	24441	1.710695e+14	554078.5
2	+	District	-14	6.175224e+13	24427	1.093172e+14
3	+	Fin_sqft	-1	3.824600e+13	24426	7.107123e+13
4	+	Units	-3	1.789793e+13	24423	5.317331e+13
5	+	Fbath	-5	2.331394e+12	24418	5.084191e+13
6	+	Bdrms	-9	1.243638e+12	24409	4.959827e+13
7	+	Sale_date	-1	7.291417e+11	24408	4.886913e+13
8	+	Year_Built	-1	7.023471e+11	24407	4.816678e+13
9	+	Lotsize	-1	3.364533e+11	24406	4.783033e+13
10	+	Extwall	-8	2.479395e+11	24398	4.758239e+13
11	+	Stories	-3	2.068265e+11	24395	4.737557e+13

```
#view final model
```

```
names(forward$coefficients)
```

```
[1] "(Intercept)"                  "District2"                 "District3"
[4] "District4"                   "District5"                 "District6"
[7] "District7"                   "District8"                 "District9"
[10] "District10"                  "District11"                "District12"
[13] "District13"                  "District14"                "District15"
[16] "Fin_sqft"                    "Units2"                     "Units3"
[19] "Units>3"                     "Fbath1"                     "Fbath2"
[22] "Fbath3"                      "Fbath4"                     "Fbath>4"
[25] "Bdrms1"                      "Bdrms2"                     "Bdrms3"
```

```

[28] "Bdrms4"                      "Bdrms5"                      "Bdrms6"
[31] "Bdrms7"                      "Bdrms8"                      "Bdrms>8"
[34] "Sale_date"                    "Year_Built"                   "Lotsize"
[37] "ExtwallBlock"                "ExtwallBrick"                 "ExtwallFiber-Cement"
[40] "ExtwallFrame"                "ExtwallMasonry / Frame"    "ExtwallPrem Wood"
[43] "ExtwallStone"                "ExtwallStucco"                "Stories1.5"
[46] "Stories2"                     "Stories>2"

# ##### Backward selection with AIC #####
#define intercept-only model
intercept_only = lm(Sale_price~ 1, data=df_clean4)

#define model with all predictors
all = lm(Sale_price~ ., data=df_clean4)

#perform backward stepwise regression
backward = step(all, direction='backward', scope=formula(all), trace=0)

#view results of backward stepwise regression
backward$anova

Step Df Deviance Resid. Df   Resid. Dev      AIC
1       NA        NA     24396 4.757525e+13 522911.1
2 - d_3     0        0     24396 4.757525e+13 522911.1

#view final model
names(backward$coefficients)

[1] "(Intercept)"                  "District2"                   "District3"
[4] "District4"                   "District5"                   "District6"
[7] "District7"                   "District8"                   "District9"
[10] "District10"                  "District11"                  "District12"
[13] "District13"                  "District14"                  "District15"
[16] "ExtwallBlock"                "ExtwallBrick"                "ExtwallFiber-Cement"
[19] "ExtwallFrame"                "ExtwallMasonry / Frame"    "ExtwallPrem Wood"
[22] "ExtwallStone"                "ExtwallStucco"                "Stories1.5"
[25] "Stories2"                     "Stories>2"                   "Year_Built"
[28] "Fin_sqft"                    "Units2"                      "Units3"
[31] "Units>3"                     "Bdrms1"                      "Bdrms2"

```

```

[34] "Bdrms3"                      "Bdrms4"                      "Bdrms5"
[37] "Bdrms6"                      "Bdrms7"                      "Bdrms8"
[40] "Bdrms>8"                     "Fbath1"                      "Fbath2"
[43] "Fbath3"                      "Fbath4"                      "Fbath>4"
[46] "Lotsize"                     "Sale_date"

#####
# Stepwise Regression with AIC #####
# Define intercept-only model
intercept_only = lm(Sale_price~ 1, data=df_clean4)

# Define model with all predictors
all = lm(Sale_price~ ., data=df_clean4)

#perform stepwise regression
both = step(intercept_only, direction='both', scope=formula(all), trace=0)

#view results of Stepwise regression
both$anova



|    | Step | Df         | Deviance | Resid. Df    | Resid. Dev   | AIC          |          |
|----|------|------------|----------|--------------|--------------|--------------|----------|
| 1  |      | NA         | NA       | 24442        | 1.723269e+14 | 554279.2     |          |
| 2  | +    | District   | -14      | 6.207601e+13 | 24428        | 1.102509e+14 | 543390.1 |
| 3  | +    | Fin_sqft   | -1       | 3.865374e+13 | 24427        | 7.159711e+13 | 532839.9 |
| 4  | +    | Units      | -3       | 1.806837e+13 | 24424        | 5.352874e+13 | 525737.0 |
| 5  | +    | Fbath      | -5       | 2.390742e+12 | 24419        | 5.113800e+13 | 524630.2 |
| 6  | +    | Bdrms      | -9       | 1.268332e+12 | 24410        | 4.986967e+13 | 524034.3 |
| 7  | +    | Sale_date  | -1       | 7.299962e+11 | 24409        | 4.913967e+13 | 523675.9 |
| 8  | +    | Year_Built | -1       | 7.284709e+11 | 24408        | 4.841120e+13 | 523312.8 |
| 9  | +    | Lotsize    | -1       | 3.850140e+11 | 24407        | 4.802619e+13 | 523119.7 |
| 10 | +    | Extwall    | -8       | 2.445413e+11 | 24399        | 4.778164e+13 | 523010.9 |
| 11 | +    | Stories    | -3       | 2.063959e+11 | 24396        | 4.757525e+13 | 522911.1 |



#view final model
names(both$coefficients)

[1] "(Intercept)"                  "District2"                   "District3"
[4] "District4"                   "District5"                   "District6"
[7] "District7"                   "District8"                   "District9"
[10] "District10"                  "District11"                  "District12"
[13] "District13"                  "District14"                  "District15"

```

```

[16] "Fin_sqft"           "Units2"          "Units3"
[19] "Units>3"            "Fbath1"          "Fbath2"
[22] "Fbath3"             "Fbath4"          "Fbath>4"
[25] "Bdrms1"              "Bdrms2"          "Bdrms3"
[28] "Bdrms4"              "Bdrms5"          "Bdrms6"
[31] "Bdrms7"              "Bdrms8"          "Bdrms>8"
[34] "Sale_date"            "Year_Built"       "Lotsize"
[37] "ExtwallBlock"         "ExtwallBrick"     "ExtwallFiber-Cement"
[40] "ExtwallFrame"         "ExtwallMasonry / Frame" "ExtwallPrem Wood"
[43] "ExtwallStone"         "ExtwallStucco"    "Stories1.5"
[46] "Stories2"              "Stories>2"

```

These methods retain many more variables. It is interesting, considering all subsets contained very few.

**Example 9.10.** Use the NFL data from the textbook - Run forward selection and backward selection including all regressors using the  $F$  statistic criterion.

```

##### Forward selection by F value
# Threshold for p-value to determine variable inclusion
thresh = 0.05

# Initialize an empty vector to store currently selected variables
curr_vars = c()

# Create a vector of variable names excluding the dependent variable 'Wins' and 'PerR'
vars_left = names(df)[2:10]
vars_left = vars_left[vars_left != 'PerR']

# Initialize the passed flag to TRUE
passed = TRUE

# Loop until no more variables can be added (passed is FALSE) or there are no more variables
while(passed && length(vars_left) > 0) {

  # Initialize an empty vector to store p-values of models
  pvals = c()

  # Loop through each remaining variable
  for(var in vars_left) {
    # Create a temporary dataframe with current variables and the new candidate variable
    df_tmp = df[, c(curr_vars, var, 'Wins')]

```

```

# Fit a linear model with 'Wins' as the dependent variable
model = lm(Wins ~ ., df_tmp)

# Get the summary of the model
s = summary(model)

# Calculate the p-value of the F-statistic for the model
pval = 1 - pf(s$fstatistic[1], s$fstatistic[2], s$fstatistic[3])

# Append the p-value to the pvals vector
pvals = c(pvals, pval)
}

# Find the index of the minimum p-value
min_index = which.min(pvals)

# Get the minimum p-value
mp = pvals[min_index]

# Check if the minimum p-value is less than the threshold
passed = mp < thresh

if(passed) {
  # If passed, get the corresponding variable name
  new_var = vars_left[min_index]

  # Add the new variable to the current variables list
  curr_vars = c(curr_vars, new_var)

  # Remove the new variable from the remaining variables list
  vars_left = vars_left[vars_left != new_var]

  # Print the p-value and the variable being added
  print('pvalue')
  print(mp)
  print('adding')
  print(new_var)
}
}

[1] "pvalue"

```

```

      value
7.380709e-06
[1] "adding"
[1] "ORY"
[1] "pvalue"
      value
4.151848e-08
[1] "adding"
[1] "PassY"
[1] "pvalue"
      value
5.286139e-08
[1] "adding"
[1] "RushY"
[1] "pvalue"
      value
1.237473e-07
[1] "adding"
[1] "OPY"
[1] "pvalue"
      value
5.151486e-07
[1] "adding"
[1] "PenY"
[1] "pvalue"
      value
2.098536e-06
[1] "adding"
[1] "TurnD"
[1] "pvalue"
      value
7.894081e-06
[1] "adding"
[1] "Punta"
[1] "pvalue"
      value
2.52811e-05
[1] "adding"
[1] "FGP"

# Print the final list of selected variables
print(curr_vars)

```

```

[1] "ORY"    "PassY"  "RushY"  "OPY"    "PenY"   "TurnD"  "PuntaA" "FGP"

# Threshold for p-value to determine variable exclusion
thresh = 0.05

# Initialize a vector of variable names excluding the dependent variable 'Wins' and 'PerR'
vars_left = names(df)[2:10]
vars_left = vars_left[vars_left != 'PerR']

# Initialize the passed flag to TRUE
passed = TRUE

# Loop until no more variables need to be removed (passed is FALSE) or there are no more variables left
while(passed && length(vars_left) > 0) {
  # Create a temporary dataframe with remaining variables and the dependent variable 'Wins'
  df_tmp = df[, c(vars_left, 'Wins')]

  # Fit a linear model with 'Wins' as the dependent variable
  model = lm(Wins ~ ., df_tmp)

  # Get the summary of the model
  s = summary(model)

  # Extract the p-values of the t-statistics for the coefficients
  tv = coef(s)[, "Pr(>|t|)"]

  # Remove the intercept p-value
  tv = tv[-1]

  # Find the index of the maximum p-value
  max_index = which.max(tv)

  # Get the maximum p-value
  mp = tv[max_index]

  # Print the maximum p-value
  print(mp)

  # Check if the maximum p-value is greater than the threshold
  passed = mp > thresh

  if(passed) {

```

```

# If passed, get the corresponding variable name to be removed
rem_var = names(max_index)

# Remove the variable from the remaining variables list
vars_left = vars_left[vars_left != rem_var]

# Print the p-value and the variable being removed
print('pvalue')
print(mp)
print('removing')
print(rem_var)
}
}

```

```

TurnD
0.7312364
[1] "pvalue"
TurnD
0.7312364
[1] "removing"
[1] "TurnD"
FGP
0.5679556
[1] "pvalue"
FGP
0.5679556
[1] "removing"
[1] "FGP"
PuntaA
0.6919653
[1] "pvalue"
PuntaA
0.6919653
[1] "removing"
[1] "PuntaA"
PenY
0.5147875
[1] "pvalue"
PenY
0.5147875
[1] "removing"
[1] "PenY"

```

```

OPY
0.1752231
[1] "pvalue"
    OPY
0.1752231
[1] "removing"
[1] "OPY"
    RushY
0.06663316
[1] "pvalue"
    RushY
0.06663316
[1] "removing"
[1] "RushY"
    PassY
0.0001775241

# Print the final list of remaining variables
print(vars_left)

[1] "PassY" "ORY"

```

**Exercise 9.1.** Use the NFL data from the textbook - modify the above code to perform stepwise regression, including all regressors using the  $F$  statistic criterion.

## 9.6 Cross Validation

We may be mainly interested in predictive performance of our model. To assess the performance of our model's predictive ability, it would be ideal to test its ability to predict the response. We could test our model out on our dataset, but our model has already 'seen' this dataset. Previously, we saw that the model's predictive ability on the dataset at hand does not necessarily mean it will output good predictions for new data from the same population. This means that the predictive ability of the model on the current observations won't reflect the model's ability to predict observations it hasn't seen. It would be ideal to have some new data in order to measure predictive performance, but it is also ideal to use all data in building the model. **Cross validation** allows us to obtain an estimate of a given model's out of sample predictive performance.

Cross-validation is a technique where we repeatedly fit our model using a subset of the dataset and then compute its predictive performance on the complementary subset of the dataset.

We then average these predictive performances and use this to estimate our model's overall predictive performance.

Here is an overview of the algorithm:

1. Partition the data  $\mathbb{Z}$  into  $k$  groups of size about  $n/k$  uniformly at random. Denoted  $\mathbb{Z}_1, \dots, \mathbb{Z}_k$ .
2. For each;  $\mathbb{Z}_j$ , fit the regression model on  $\mathbb{Z} \setminus \mathbb{Z}_j$ .
3. For each observation in the left out group  $\mathbb{Z}_j$ , use the previously computed model to produce a prediction  $\hat{Y}_{j,1}, \dots, \hat{Y}_{j,n/k}$ , resulting in  $n/k$  predictions.
4. For each prediction, compute the predictive error  $(y_{j,i} - \hat{y}_{j,i})^2$  (Can also use absolute error).
5. Repeat steps 2-3 for each group  $1, \dots, k$ .
6. Average the  $n$  predictive errors.
7. Repeat for all candidate models and choose the model with the lowest prediction error.

To highlight the choice of  $k$ , we say  $k$ -fold Cross Validation – Each of the  $k$  subsets are known as folds. What do we choose for  $k$ ? LOOCV (Leave One Out Cross Validation) is a popular technique. Here,  $k = n$ . This is where each run, one observation is left out of the model. This gives a low bias, but high variation estimate of the prediction error. It also has a high run time. As a result, often,  $k$  is taken to be 5 or 10. Taking lower values of  $k$  gives a result similar to that of splitting the data into training and test sets, while higher values of  $k$  gives a result similar to LOOCV. The choice of the number of folds in cross validation is a bias-variance tradeoff: too few folds may result in high bias, while too many folds may result in high variance. (This is why  $k$  is taken between 1 and  $n$ .)

**Example 9.11.** Using the real estate data, run cross validation in a forward selection manner. That is, run the cross validation procedure for the model with the first variable, the first and the second variable, the first three variables etc. Which model has the lowest error?

The `caret` package can be used to perform 5-fold CV.

```
##### Cross Validation Regression #####
# install.packages('caret')
library(caret)
```

Warning: package 'caret' was built under R version 4.2.3

Loading required package: lattice

```

#specify the cross-validation method 5 fold in this case.
ctrl = trainControl(method = "cv", number = 5)

#fit a regression model and use k-fold CV to evaluate performance
model = train(Sale_price~., data = df2, method = "lm", trControl = ctrl)

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may be misleading

for(i in 1:length(var_list)){
  vars=c(var_list[1:i],"Sale_price")
  model = train(Sale_price~., data = df2[,vars], method = "lm", trControl = ctrl)
  print(paste0("k" ,i," CV Result ", model$results$RMSE,sep=""))
}

[1] "k1 CV Result 66912.7355323838"
[1] "k2 CV Result 64288.4426359389"
[1] "k3 CV Result 61819.6176427859"
[1] "k4 CV Result 61336.9593108528"
[1] "k5 CV Result 52061.7475798042"
[1] "k6 CV Result 46100.1776666706"
[1] "k7 CV Result 45683.6103871796"
[1] "k8 CV Result 44988.2437790465"
[1] "k9 CV Result 44668.105850592"
[1] "k10 CV Result 44282.8184779538"

```

```
#view summary of k-fold CV
print(model)

Linear Regression

24442 samples
  10 predictor

No pre-processing
Resampling: Cross-Validated (5 fold)
Summary of sample sizes: 19554, 19554, 19555, 19552, 19553
Resampling results:

RMSE      Rsquared      MAE
44282.82  0.7199015  29860.22
```

Tuning parameter 'intercept' was held constant at a value of TRUE

```
# We see that all of the variables minimize the prediction error.
```

**Example 9.12.** Use the NFL data from the textbook. 1. Compare the model `Wins~.` to the model `Wins~PassY+PuntA+FGP+TurnD+PenY+OPY+RushDiff`. 2. Run cross validation in a forward selection manner. That is, run the cross validation procedure for the model with the first variable, the first and the second variable, the first three variables etc. Which model has the lowest error? 3. Run cross validation for all subsets. Which model has the lowest error? Does it match the result in step 2?

```
##### Cross Validation Regression #####
set.seed(1251)

#specify the cross-validation method
ctrl = trainControl(method = "cv", number = 5)

#fit a regression model and use k-fold CV to evaluate performance
model_cv_1 = train(Wins~., data = df, method = "lm", trControl = ctrl)
```

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may be misleading
```

```
model_cv_1
```

```
Linear Regression
```

```
28 samples  
10 predictors
```

```
No pre-processing  
Resampling: Cross-Validated (5 fold)  
Summary of sample sizes: 21, 22, 22, 24, 23  
Resampling results:
```

RMSE	Rquared	MAE
1.962945	0.5925805	1.686354

```
Tuning parameter 'intercept' was held constant at a value of TRUE
```

```
model_cv_2 = train(Wins~PassY+PuntA+FGP+TurnD+PenY+OPY+RushDiff, data = df, method = "lm",  
model_cv_2
```

```
Linear Regression
```

```
28 samples  
7 predictor
```

```
No pre-processing  
Resampling: Cross-Validated (5 fold)
```

```
Summary of sample sizes: 23, 21, 23, 23, 22
Resampling results:
```

RMSE	Rquared	MAE
2.418524	0.6516294	1.887159

```
Tuning parameter 'intercept' was held constant at a value of TRUE
```

```
for(i in 2:ncol(df)){
  # reg=sample(2:10,sample(1:9,1))
  vars=c(names(df)[2:i],'Wins')
  model = train(Wins~., data = df[,vars], method = "lm", trControl = ctrl)
  print(paste0("k=", i-1, " vars ", paste(vars,collapse=' ')," CV Result ",
              round(model$results$RMSE,1),sep=""))
}
```

```
[1] "k=1 vars RushY Wins CV Result 2.9"
[1] "k=2 vars RushY PassY Wins CV Result 2.3"
[1] "k=3 vars RushY PassY PuntA Wins CV Result 2.2"
[1] "k=4 vars RushY PassY PuntA FGP Wins CV Result 2.4"
[1] "k=5 vars RushY PassY PuntA FGP TurnD Wins CV Result 2.6"
[1] "k=6 vars RushY PassY PuntA FGP TurnD PenY Wins CV Result 2.5"
[1] "k=7 vars RushY PassY PuntA FGP TurnD PenY PerR Wins CV Result 2.5"
[1] "k=8 vars RushY PassY PuntA FGP TurnD PenY PerR ORY Wins CV Result 2.5"
[1] "k=9 vars RushY PassY PuntA FGP TurnD PenY PerR ORY OPY Wins CV Result 2"
```

```
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```

```
[1] "k=10 vars RushY PassY PuntA FGP TurnD PenY PerR ORY OPY RushDiff Wins CV Result 2.5"

# Select model k=9 vars

#
p = ncol(df)-1
l = rep(list(0:1), p)

models=expand.grid(l); dim(models)

[1] 1024    10

cv=RMSE=c()
for(i in 2:nrow(models)){
  reg=(2:(p+1))[models[i,]==1]
  vars=c(names(df)[reg], 'Wins')
  model = train(Wins~, data = df[,vars], method = "lm", trControl = ctrl)
  RMSE=c(RMSE, model$results$RMSE)
  cv=c(cv, list(model))
  # print(paste0("k=", k, " vars ", paste(vars, collapse=' ')," CV Result ",
  #               round(model$results$RMSE, 1), sep=""))
}
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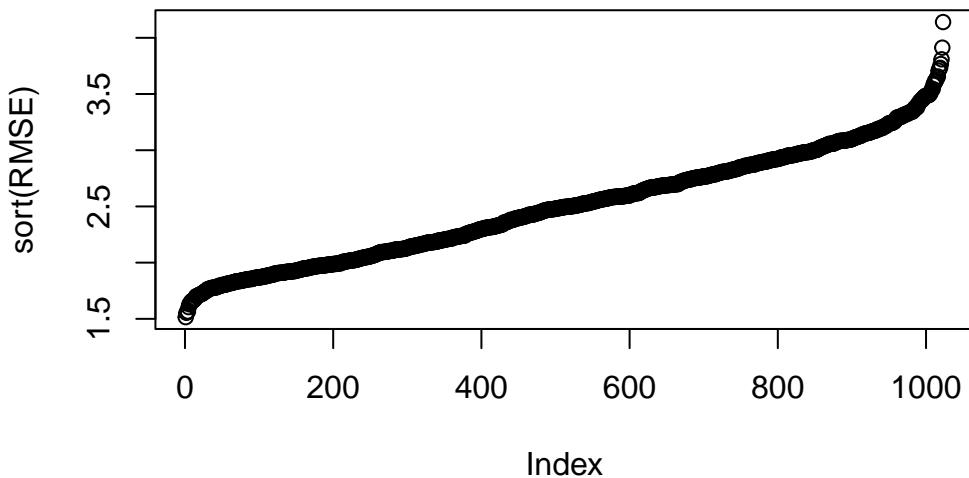
```
Warning in predict.lm(modelFit, newdata): prediction from a rank-deficient fit  
may be misleading
```

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```

```
bottom_10=order(RMSE) [1:10]  
RMSE[bottom_10]
```

```
[1] 1.514831 1.553680 1.561540 1.565194 1.604034 1.629024 1.634625 1.647743  
[9] 1.657872 1.658021
```

```
plot(sort(RMSE))
```



```

m=which.min(RMSE)
cv[which.min(RMSE)]
```

[[1]]  
 Linear Regression

28 samples  
 5 predictor

No pre-processing  
 Resampling: Cross-Validated (5 fold)  
 Summary of sample sizes: 22, 22, 23, 23, 22  
 Resampling results:

RMSE	Rsquared	MAE
1.514831	0.7945392	1.255977

Tuning parameter 'intercept' was held constant at a value of TRUE

```
df[1,(2:(p+1))[unlist(models[m,])==1]]
```

RushY	PuntA	PerR	OPY	RushDiff
1 2113	38.9	59.7	1917	-92

```
model = train(Wins~ PassY+PuntA+TurnD+PerR++OPY+RushDiff, data = df, method = "lm", trControl = crossval,
RMSE=c(RMSE,model$results$RMSE))
```

## 9.7 Homework questions

Complete the Chapter 10 questions from the textbook.

**Exercise 9.2.** Load car mileage data from Example 3.8 and run 10-fold cross validation on all subset models. Which model is the best?

# 10 Robust Regression

A serious problem that may dramatically impact the usefulness of a regression model is that of outlying observations. We have seen trying to locate and remove outliers, but an alternative technique is to use robust statistics. Robust statistics is a field of statistics that develops estimators that are not corrupted by outlying observations.

Recall that we minimize the squared error to obtain the least squares estimator. The best estimator was defined as the minimizer of

$$C(\beta) = \sum_{i=1}^n (Y_i - \beta^\top X_i)^2.$$

The squared error is an example of a **cost function**. The fact that the errors are squared implies that unusually large residuals will contribute significantly to the cost function. We may instead define the best estimator to minimize another cost function, say

$$C(\beta) = \sum_{i=1}^n |Y_i - \beta^\top X_i|.$$

The absolute value function grows linearly, thus, it is less affected by unusually large residuals. We can go a step further and design a cost function that is even less affected by unusually large residuals.

## 10.1 *M*-estimators

*M*-estimators are a group of estimators which can be defined as minimizers of cost functions. (The *M* stands for minimizers.) We can define an error function  $\rho$  as a function such that  $\rho(|x|)$  is non-negative, non-decreasing and  $\rho(0) = 0$ . We can then define the ***M*-estimator** with error function  $\rho$  as

$$\hat{\beta} = \operatorname{argmin}_{\beta} C_{\rho}(\beta) = \operatorname{argmin}_{\beta} \sum_{i=1}^n \rho(Y_i - \beta^\top X_i) = \operatorname{argmin}_{\beta} \sum_{i=1}^n \rho(\hat{\epsilon}_i(\beta)),$$

where  $\hat{\epsilon}_i(\beta) = Y_i - \beta^\top X_i$ . Note that for arbitrary  $\rho$ , the above may not have a unique minimizer, which may be problematic for computational algorithms and theoretical analysis. An *M*-estimator is an alternative to the OLS estimator. The idea is to define  $\rho$  so that large

residuals  $\hat{\epsilon}_i(\beta)$  do not contribute more than they should to the cost function. To elaborate, we would like  $\rho(\hat{\epsilon}_i(\beta))$  to be somewhat large if  $\hat{\epsilon}_i(\beta)$  is large, because that signals that the model defined by  $\beta$  does not fit the data well at that point. On the other hand, if observation  $i$  is an outlier, than we don't want to try too hard to make the model fit that point.

One drawback of  $M$ -estimators is that they are not necessarily scale invariant. For example, we have that

$$Y = X\beta + \epsilon \implies aY = aX\beta + a\epsilon.$$

Therefore, it is natural that we would expect the estimation procedure applied to  $(X, Y)$  to produce the same estimator for  $\beta$  as the estimation procedure applied to  $(aX, aY)$ . Unfortunately, this is not always the case for  $M$ -estimators. One way to remedy this is to obtain a (robust) scale estimate  $s$ , and then define the estimate as

$$\operatorname{argmin}_{\beta} \sum_{i=1}^n \rho\left(\frac{Y_i - \beta^\top X_i}{s}\right).$$

For example, the median absolute deviation divided by 0.6745 is often used.

## 10.2 Different $\rho$ functions

Let  $\psi$  be the derivative of  $\rho$ . Some common choices for  $\rho$  include the following:

### 10.2.1 Least Squares

Least squares loss, also known as quadratic loss, is the most common loss function in regression analysis. It is defined as the square of the residuals (the differences between observed and predicted values).

$$\rho(u) = u^2, \quad \psi(u) = 2u.$$

It is highly sensitive to outliers because the squared term amplifies large residuals, making it less robust in the presence of outliers.

### 10.2.2 Huber's Loss

Huber's loss is a piecewise loss function that is quadratic for small residuals and linear for large residuals. It is less sensitive to outliers compared to least squares loss. This loss provides a compromise between least squares and absolute loss, offering robustness to outliers while retaining efficiency for small residuals.

$$\rho(u) = \begin{cases} u^2/2 & \text{if } |u| \leq \delta \\ \delta(|u| - \delta/2) & \text{if } |u| > \delta \end{cases}, \quad \psi(u) = \begin{cases} u & \text{if } |u| \leq \delta \\ \delta \times \text{sign}(u) & \text{if } |u| > \delta \end{cases}.$$

The next three losses offer even more robustness to outliers, potentially at the cost of efficiency.

### 10.2.3 Ramsay's E Function

Ramsay's  $E$  function is used to give higher influence to residuals near zero and less influence to large residuals.

$$\rho(u) = \frac{1 - (1 + \delta|u|) \exp(-\delta|u|)}{\delta^2}, \quad \psi(u) = \text{sign}(u) \exp(-\delta|u|)/\delta.$$

### 10.2.4 Andrews' Wave Function

Andrews' wave function is a loss function that limits the influence of large residuals more than Huber's loss.

$$\rho(u) = \delta \left( 1 - \cos \left( \frac{u}{\delta} \right) \right), \quad \psi(u) = \frac{\sin(u/\delta)}{u/\delta}.$$

### 10.2.5 Tukey's Loss

Tukey's loss function, also known as the biweight loss function, completely cuts off the influence of residuals beyond a certain point.

$$\rho(u) = \begin{cases} \frac{c^2}{6} \left[ 1 - \left( 1 - \left( \frac{u}{c} \right)^2 \right)^3 \right] & \text{if } |u| \leq c \\ \frac{c^2}{6} & \text{if } |u| > c \end{cases}, \quad \psi(u) = \begin{cases} u \left( 1 - \left( \frac{u}{c} \right)^2 \right)^2 & \text{if } |u| \leq c \\ 0 & \text{if } |u| > c \end{cases}.$$

Let's graph each of these functions:

```
# Define the least squares loss function
least_squares_loss <- function(u) {
  return(u^2/2)
}
```

```

# Define Huber's loss function
hubers_loss <- function(u, delta=2) {
  return(ifelse(abs(u) <= delta, 0.5 * u^2, delta * (abs(u) - 0.5 * delta)))
}

# Define Ramsay's E function
ramsays_e_function <- function(u, delta=0.3) {
  return((1-(1+delta*abs(u))*exp(-delta*abs(u)))/(delta^2))
}

# Define Andrews' wave function
andrews_wave_function <- function(u, delta=1.339) {
  if(abs(u / delta)<pi)
    return(delta * (1 - cos(u / delta)))
  else
    return(NA)
}

# Define Tukey's loss function
tukeys_loss <- function(u, c=3) {
  abs_u <- abs(u)
  return(ifelse(abs_u <= c, (c^2 / 6) * (1 - (1 - (u / c)^2)^3), c^2 / 6))
}

u <- seq(-10,10, by = 0.1)

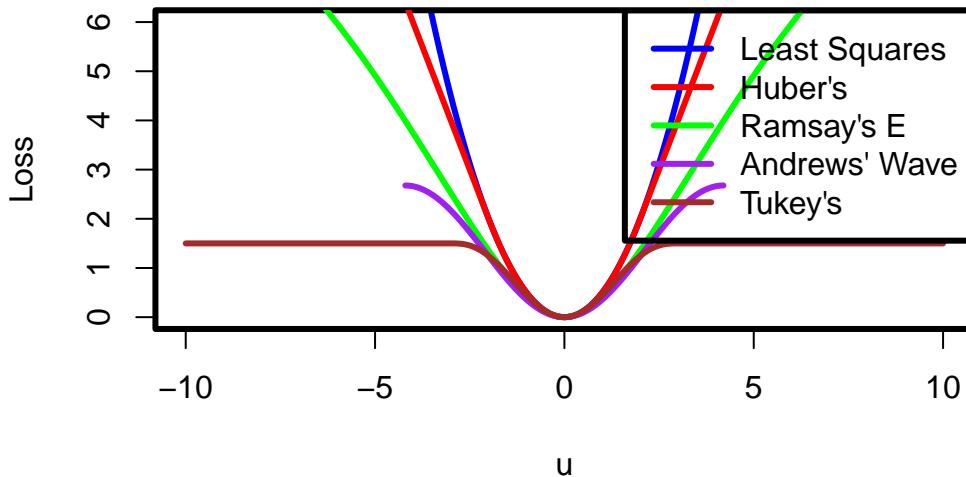
ls_loss <- sapply(u,least_squares_loss)
h_loss <- sapply(u,hubers_loss)
r_loss <- sapply(u,ramsays_e_function)
a_loss <- sapply(u, andrews_wave_function)
tukey_loss <- sapply(u,tukeys_loss)

par(lwd=3)
# Plotting example losses for visualization
plot(u, ls_loss, type = "l", col = "blue", ylim = c(0, 6), ylab = "Loss", xlab = "u", main="Loss Functions Comparison")
lines(u, h_loss, col = "red")
lines(u, r_loss, col = "green")
lines(u, a_loss, col = "purple")
lines(u, tukey_loss, col = "brown")

```

```
legend("topright", legend = c("Least Squares", "Huber's", "Ramsay's E", "Andrews' Wave",
  col = c("blue", "red", "green", "purple", "brown"), lty = 1)
```

## Loss Functions



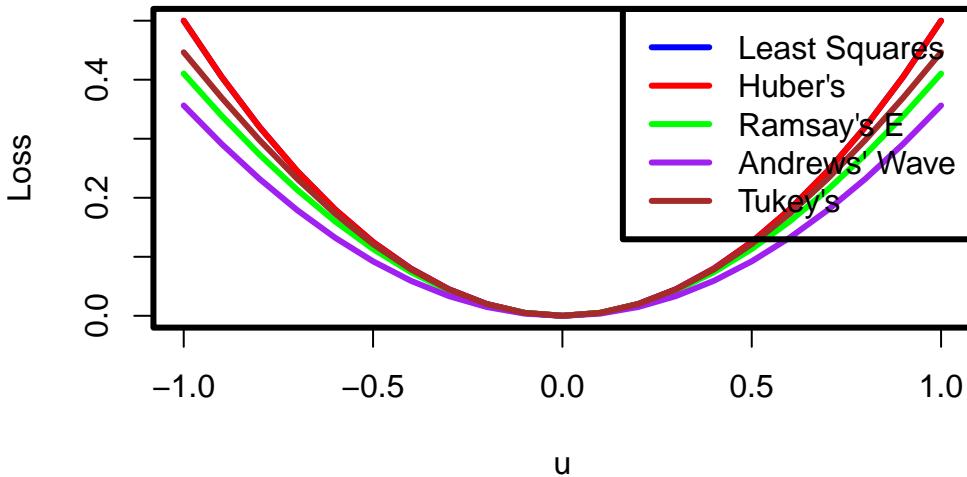
```
#Zooming in
u <- seq(-1, 1, by = 0.1)

ls_loss <- sapply(u,least_squares_loss)
h_loss <- sapply(u,hubers_loss)
r_loss <- sapply(u,ramsay's_e_function)
a_loss <- sapply(u,andyrews_wave_function)
tukey_loss <- sapply(u,tukey's_loss)

par(lwd=3)
# Plotting example losses for visualization
plot(u, ls_loss, type = "l", col = "blue", ylab = "Loss", xlab = "u", main = "Loss Function Comparison")
lines(u, h_loss, col = "red")
lines(u, r_loss, col = "green")
lines(u, a_loss, col = "purple")
lines(u, tukey_loss, col = "brown")
legend("topright", legend = c("Least Squares", "Huber's", "Ramsay's E", "Andrews' Wave", "Tukey's"))
```

```
col = c("blue", "red", "green", "purple", "brown"), lty = 1)
```

## Loss Functions



We see that the cost attributed to large residuals varies based on the chosen function. Most of the functions appear quadratic near 0, but have quite different behaviours at large values. Tukey and Andrew's Wave function completely cut off the influence of large residuals, which the remaining functions just dampen the influence (except of course, the least squares loss). Huber's function and the least squares function are convex functions, which make computation of the minimizer considerably easier. Huber's function is about as robust as we can be, while still maintaining a convex loss function. Data drawn from distributions with heavy tails (data with many “large” observations) require more robust loss functions, such as the Tukey biweight function.

The robustness of a regression procedure can be classified by the behavior of  $\psi$ , the derivative of  $\rho$ . The  $\psi$  function controls the weight given to each residual and is proportional to a central concept in robustness called the **influence function**. Unbounded influence functions are not desirable from a robustness perspective, as this means that one corrupted point is able to drag the estimated hyperplane arbitrarily far. The  $\psi$  function for least squares  $\rho$  is unbounded, and thus least squares tends to be “nonrobust” when used with data arising from a heavy - tailed distribution. On the other hand, the Huber loss function has a monotone  $\psi$  function and is not unbounded, making it more robust.

The other influence functions actually redescend as the residual becomes larger. Ramsay's  $E$  function is a soft redescender, that is, the  $\psi$  function is approaches zero as  $|z| \rightarrow \infty$ . Andrew's

wave function and Tukey loss are hard redescenders. That is, the  $\psi$  function equals zero for sufficiently large  $|z|$ . Note that the  $\rho$  functions associated with the redescending  $\psi$  functions are nonconvex, and this in theory can cause convergence problems in the iterative estimation procedure. We graph the functions below with their common default tuning parameters:

```
# Define the derivative of the least squares loss function
d_least_squares_loss <- function(u) {
  return(u)
}

# Define the derivative of Huber's loss function
d_hubers_loss <- function(u, delta = 2) {
  return(ifelse(abs(u) <= delta, u, delta * sign(u)))
}

# Define the derivative of Ramsay's E function
d_ramsays_e_function <- function(u, delta = 0.3) {
  return(sign(u)*exp(-delta*abs(u))/delta)
}

# Define the derivative of Andrews' wave function
d_andrews_wave_function <- function(u, delta = 1.339) {
  if(abs(u / delta) < pi)
    return(sin(u / delta))
  else
    return(NA)
}

# Define the derivative of Tukey's loss function
d_tukeys_loss <- function(u, c = 3) {
  abs_u <- abs(u)
  return(ifelse(abs_u <= c, u * (1 - (u / c)^2)^2, 0))
}

u <- seq(-10, 10, by = 0.1)

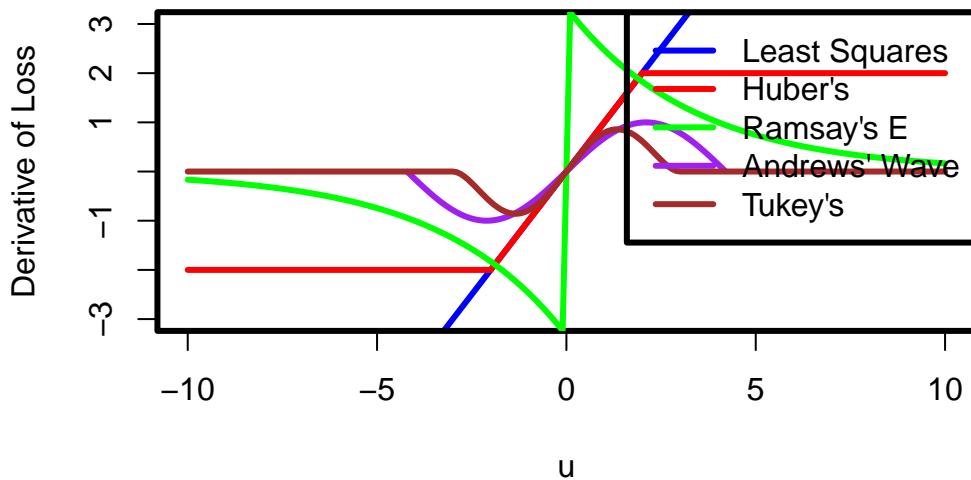
d_ls_loss <- sapply(u, d_least_squares_loss)
d_h_loss <- sapply(u, d_hubers_loss)
d_r_loss <- sapply(u, d_ramsays_e_function)
d_a_loss <- sapply(u, d_andrews_wave_function)
d_tukey_loss <- sapply(u, d_tukeys_loss)
```

```

par(lwd = 3)
# Plotting example derivatives for visualization
plot(u, d_ls_loss, type = "l", col = "blue", ylim = c(-3, 3), ylab = "Derivative of Loss",
lines(u, d_h_loss, col = "red")
lines(u, d_r_loss, col = "green")
lines(u, d_a_loss, col = "purple")
lines(u, d_tukey_loss, col = "brown")
legend("topright", legend = c("Least Squares", "Huber's", "Ramsay's E", "Andrews' Wave",
col = c("blue", "red", "green", "purple", "brown"), lty = 1)

```

## Derivatives of Loss Functions



## 10.3 Computing $M$ -estimators

### 10.3.1 Iterated re-weighted least squares

Let  $\psi$  be the derivative of  $\rho$ . A common way to compute the minimizer, of  $C_\rho(\beta)$  is to use **iterated re-weighted least squares**. First, note that to find the minimizer, of  $C_\rho(\beta)$ , we solve the following system of equations:

$$\sum_{i=1}^n X_{ij} \psi\left(\frac{Y_i - X_i^\top \beta}{s}\right) = 0, \quad j = 0, 1, \dots, k.$$

To do this, rewrite

$$\sum_{i=1}^n X_{ij} \psi\left(\frac{Y_i - X_i^\top \beta}{s}\right) \frac{Y_i - X_i^\top \beta}{s} / \frac{Y_i - X_i^\top \beta}{s} = 0$$

or,  $\sum_{i=1}^n X_{ij} w_{i,\beta} \frac{Y_i - X_i^\top \beta}{s} = 0,$

where

$$w_{i,\beta} = \psi\left(\frac{Y_i - X_i^\top \beta}{s}\right) / \frac{Y_i - X_i^\top \beta}{s}.$$

Next, one will propose an initial estimate of the parameters  $\alpha_0$  and consider

$$\sum_{i=1}^n X_{ij} w_{i,\alpha_0} (Y_i - X_i^\top \beta) = 0.$$

Equivalently, we have  $X^\top W_{\alpha_0} X \beta = X^\top W_{\alpha_0} Y$ , where  $W_{\alpha_0}$  is an  $n \times n$  diagonal matrix of “weights” with diagonal elements  $w_{1,\alpha_0}, \dots, w_{n,\alpha_0}$ . The algorithm proceeds as follows: iteratively compute  $\alpha_i = (X^\top W_{\alpha_{i-1}} X)^{-1} X^\top W_{\alpha_{i-1}} Y$  until  $\|\alpha_i - \alpha_{i-1}\| < \epsilon$  for small  $\epsilon$ .

### 10.3.2 Gradient descent

We can also use [gradient descent](#) to compute the minimizer, of  $C_\rho(\beta)$ . To do this given a step size  $\eta > 0$ , iteratively compute

$$\alpha_i = \alpha_{i-1} - \eta \times \sum_{i=1}^n X_i \psi\left(\frac{Y_i - X_i^\top \alpha_{i-1}}{s}\right),$$

until  $\|\alpha_i - \alpha_{i-1}\| < \epsilon$  for small  $\epsilon$ .

**Example 10.1.** Consider the stack loss data, it records the percentage of stack loss in the operation of a plant that uses the oxidation of ammonia to produce nitric acid. The data set contains four variables and 21 observations.

Variables - **Air.Flow**: Flow rate of cooling air (in cubic meters per hour) - **Water.Temp**: Cooling water inlet temperature (in degrees Celsius) - **Acid.Conc.**: Acid concentration (percentage) - **stack.loss**: Stack loss (percentage of the ammonia lost)

Régress stack loss on the remaining variables. Compare various robust regression estimates to the OLS estimates. Add a large outlier and repeat the process. What do you observe?

The **r1m** function in the **MASS** package allows us to run robust regression. Huber’s loss is used by default.

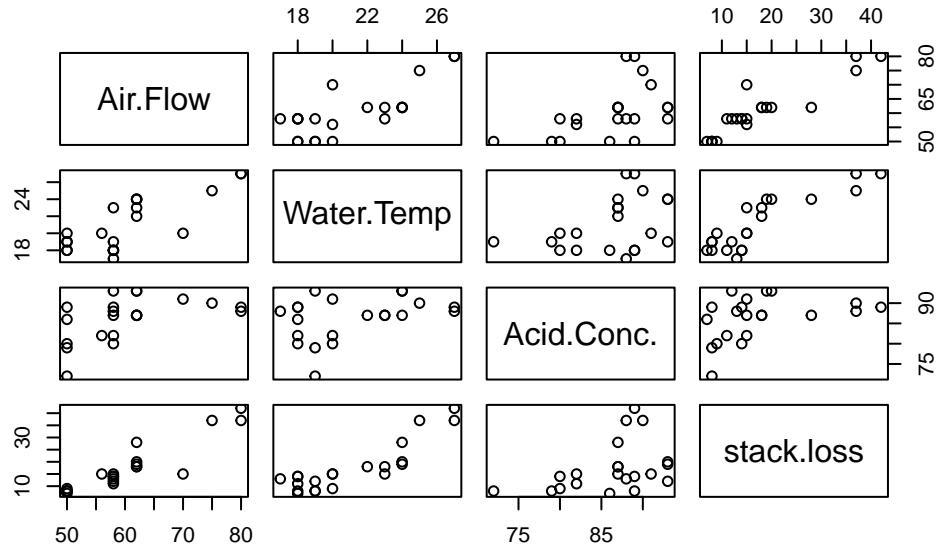
```

# Computes how many standard errors coefficients are different by between models m1 and m2
compute_movement=function(m1,m2){
  vb=summary(m2)
  return(abs(coef(m2)-coef(m1))/vb$coef[,2])
}

library(MASS)

plot(stackloss)

```



```

#fit robust regression model
# psi argument specifies psi...
# run ?rlm for more details.
OLS1=lm(stack.loss ~ ., stackloss)
RR=rlm(stack.loss ~ ., stackloss)
summary(OLS1)

```

Call:  
`lm(formula = stack.loss ~ ., data = stackloss)`

```

Residuals:
    Min      1Q  Median      3Q     Max
-7.2377 -1.7117 -0.4551  2.3614  5.6978

Coefficients:
            Estimate Std. Error t value Pr(>|t|)
(Intercept) -39.9197   11.8960  -3.356  0.00375 **
Air.Flow      0.7156    0.1349   5.307  5.8e-05 ***
Water.Temp    1.2953    0.3680   3.520  0.00263 **
Acid.Conc.   -0.1521    0.1563  -0.973  0.34405
---
Signif. codes:  0 '***' 0.001 '**' 0.01 '*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 3.243 on 17 degrees of freedom
Multiple R-squared:  0.9136,    Adjusted R-squared:  0.8983
F-statistic:  59.9 on 3 and 17 DF,  p-value: 3.016e-09

```

```
summary(RR)
```

```

Call: rlm(formula = stack.loss ~ ., data = stackloss)
Residuals:
    Min      1Q  Median      3Q     Max
-8.91753 -1.73127  0.06187  1.54306  6.50163

Coefficients:
            Value Std. Error t value
(Intercept) -41.0265   9.8073  -4.1832
Air.Flow      0.8294   0.1112   7.4597
Water.Temp    0.9261   0.3034   3.0524
Acid.Conc.   -0.1278   0.1289  -0.9922

Residual standard error: 2.441 on 17 degrees of freedom

```

```
compute_movement(RR,OLS1)
```

```
(Intercept) Air.Flow Water.Temp Acid.Conc.
0.09304446  0.84335755  1.00313478  0.15530572
```

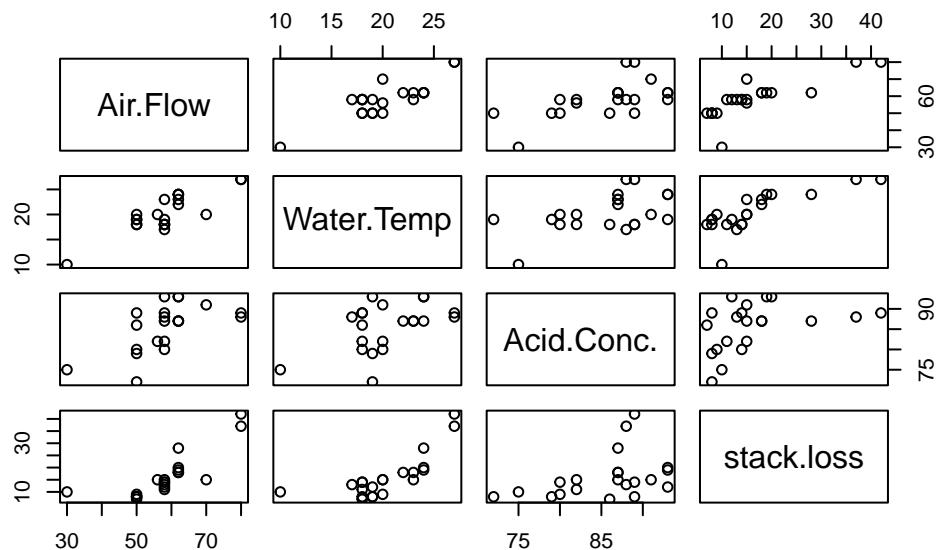
```

# Air flow and water temp moved one standard error.

# We can compare the estimates to their standard errors.

# Adding the outlier
stackloss2=stackloss
n=nrow(stackloss)
stackloss2[3,]=c(30,10,75,10)
plot(stackloss2)

```



```

OLS=lm(stack.loss ~ ., stackloss2)
RR_Hu=r1m(stack.loss ~ ., stackloss2, maxit = 100)
RR_Ha=r1m(stack.loss ~ ., stackloss2, psi = psi.hampel, maxit = 100)
RR_Tu=r1m(stack.loss ~ ., stackloss2, psi = psi.bisquare, maxit = 100)

```

Warning in r1m.default(x, y, weights, method = method, wt.method = wt.method, :  
'r1m' failed to converge in 100 steps

```

# Error from uncorrupted estimates
error=rbind(compute_movement(OLS,OLS1),
compute_movement(RR_Hu,OLS1),
compute_movement(RR_Ha,OLS1),
compute_movement(RR_Tu,OLS1))
rownames(error)=c("OLS","Huber","Hampel","Tukey")
error

(Intercept) Air.Flow Water.Temp Acid.Conc.
OLS      2.3766707 1.317436984 1.4611311 0.4406644
Huber    0.5905931 0.006153154 1.4286807 0.2686428
Hampel   0.1180260 0.047197074 0.4429042 0.1073847
Tukey    0.2180443 0.716273230 2.0518634 0.5167066

rowSums(error)

OLS     Huber     Hampel     Tukey
5.595903 2.294070 0.715512 3.502887

# summary(lm(stack.loss ~ ., stackloss2))
# summary(rlm(stack.loss ~ ., stackloss2))
# summary(rlm(stack.loss ~ ., stackloss2, psi = psi.hampel))
# summary(rlm(stack.loss ~ ., stackloss2, psi = psi.bisquare))

res=rbind(coef(OLS),
coef(RR_Hu),
coef(RR_Ha),
coef(RR_Tu),
coef(OLS1))
rownames(res)=c("OLS","Huber","Hampel","Tukey","Before Corruption")
res

(Intercept) Air.Flow Water.Temp Acid.Conc.
OLS          -11.64681 0.5379730 0.7575544 -0.22099574
Huber        -32.89398 0.7164700 0.7694970 -0.11013524
Hampel        -38.51564 0.7220051 1.1322866 -0.13533894
Tukey        -37.32582 0.8122355 0.5401506 -0.07136436
Before Corruption -39.91967 0.7156402 1.2952861 -0.15212252

```

## 10.4 Homework questions

Complete question 15.5 in the textbook.

**Exercise 10.1.** In the previous examples given in class, add a large outlier and run both least squares and robust regression. How many standard errors did the coefficients move? How large does the outlier need to be for the regression to become corrupted? Repeat the process with a cluster of small outliers.

**Exercise 10.2.** Why are the OLS estimators susceptible to outliers?

**Exercise 10.3.** Implement gradient descent and IRLS in R for Huber's loss function.

## References

- Fox, John, and Georges Monette. 1992. "Generalized Collinearity Diagnostics." *Journal of the American Statistical Association* 87 (417): 178–83. <https://doi.org/10.1080/01621459.1992.10475190>.
- Miller, Don M. 1984. "Reducing Transformation Bias in Curve Fitting." *The American Statistician* 38 (2): 124–26. <http://www.jstor.org/stable/2683247>.

# A Introduction to R software

## A.1 Some Basics

R is a Statistical Programming language, it consists of 2 types of objects: data and functions.

```
##Data  
x<-2  
print(x)
```

```
[1] 2
```

```
##function  
log(2)
```

```
[1] 0.6931472
```

Data is stored in variables and can take many forms. To store a value in a variable use “`<-`”, above we set the variable `x` equal to 2. There are many data types in R, we will go through some of them.

```
#real numbers  
num=29.333  
num
```

```
[1] 29.333
```

```
#Some math  
#adding and subtraction  
2+3-2
```

```
[1] 3
```

```
#multiplying and dividing  
num<-5*(10/25)  
num
```

```
[1] 2
```

```
#Strings  
word<-"hello"  
word
```

```
[1] "hello"
```

```
word='hello'
```

## A.2 Booleans

Booleans take on either TRUE or FALSE values, and can be very useful in R. You can set booleans to the result of a comparison of two data types, some of the syntax is below:

- <,>,<=,>= corresponds to less than, greater than, less than or equal, greater than or equal
- ==, != equals, not equals
- && , written like a&&b where a and b are booleans, it is TRUE if *both* a and b are TRUE
- || , written like a||b where a and b are booleans, it is TRUE if at least *one of* a and b are TRUE

```
#booleans can be initialize in a variety of ways, for example  
#must capitalize the true or false  
FALSE
```

```
[1] FALSE
```

```
F
```

```
[1] FALSE
```

```
T
```

```
[1] TRUE
```

```
myBoolean<-TRUE  
myBoolean
```

```
[1] TRUE
```

```
myBoolean2<- 3<4  
myBoolean2
```

```
[1] TRUE
```

```
myBoolean3<-"this"=="that"  
myBoolean3
```

```
[1] FALSE
```

```
## && (and) is TRUE if BOTH input booleans are true  
## || (or) is TRUE if AT LEAST one input boolean is true  
myBoolean4<-myBoolean2&&myBoolean  
myBoolean4
```

```
[1] TRUE
```

### A.3 Vectors

Vectors in R are used frequently, they are “lists” or “arrays” of all the same data type.

```
##vectors are created with c(data,data,data)  
myVector<-c(2,3,4,5,6,7,8,9,10)  
myVector
```

```
[1] 2 3 4 5 6 7 8 9 10
```

```
#a:b is a shortcut for a sequence from a to b adding 1  
#you can create vectors of sequences using seq(), for more type ?seq in the console  
myVector2<-2:10  
myVector2
```

```
[1] 2 3 4 5 6 7 8 9 10
```

```
as.numeric(2:10)
```

```
[1] 2 3 4 5 6 7 8 9 10
```

```
as.double(2:10)
```

```
[1] 2 3 4 5 6 7 8 9 10
```

```
myVector2<-rep(NA,l=20)
```

```
#These do not have to be numbers, they can be vectors, Strings, booleans...  
myVector<-c(myVector,myVector)  
myVector
```

```
[1] 2 3 4 5 6 7 8 9 10 2 3 4 5 6 7 8 9 10
```

```
myVector3<-c("this","is","a","vector","of","strings")  
myVector3
```

```
[1] "this"     "is"       "a"        "vector"   "of"       "strings"
```

```
#access elements with square brackets []  
myVector[1]
```

```
[1] 2
```

```
#more advanced accesssing  
#access elements 1 to 5  
myVector[1:5]
```

```
[1] 2 3 4 5 6
```

```
#access elements 1, 4 and 6  
myVector[c(1,4,6)]
```

```
[1] 2 5 7
```

```
#access elements that are greater than 2  
myVector[myVector>2]
```

```
[1] 3 4 5 6 7 8 9 10 3 4 5 6 7 8 9 10
```

```
myVector[-c(1,4,6)]
```

```
[1] 3 4 6 8 9 10 2 3 4 5 6 7 8 9 10
```

We can perform mathematical operations and comparisons on vectors

```
x<-1:10  
x
```

```
[1] 1 2 3 4 5 6 7 8 9 10
```

```
#adds 1 to every element  
x+1
```

```
[1] 2 3 4 5 6 7 8 9 10 11
```

```
#this works for comparisons  
x<4
```

```
[1] TRUE TRUE TRUE FALSE FALSE FALSE FALSE FALSE FALSE
```

```
x[x<4]
```

```
[1] 1 2 3
```

```
#multiplies element 1 to element 1 of second vectors  
x-(1:10)
```

```
[1] -1 -4 -9 -16 -25 -36 -49 -64 -81 -100
```

```
#beware repetition  
x=c(1,2)
```

```
[1] 0 0 2 2 4 4 6 6 8 8
```

```
# mathematical operations on the vector apply to each element
```

```
#squares each element  
x^2
```

```
[1] 1 4 9 16 25 36 49 64 81 100
```

```
#log each element  
log(x)
```

```
[1] 0.0000000 0.6931472 1.0986123 1.3862944 1.6094379 1.7917595 1.9459101  
[8] 2.0794415 2.1972246 2.3025851
```

```
#Example: Dot Product  
x<-c(1,2,3)  
y<-c(2,5,8)  
#sum adds the elements of the vector together  
sum(x*y)
```

```
[1] 36
```

## A.4 Matrices

You can also use matrices in R.

```
#you can create a matrix with matrix(vector of data,nrow=number of rows,ncol=number of columns)
#You can see it will fill in the data down the columns first
myMatrix<-matrix(1:9,nrow=3,ncol=3); myMatrix
```

```
[,1] [,2] [,3]
[1,]    1    4    7
[2,]    2    5    8
[3,]    3    6    9
```

```
myMatrix
```

```
[,1] [,2] [,3]
[1,]    1    4    7
[2,]    2    5    8
[3,]    3    6    9
```

```
#rbind and cbind add a row or column respectively to the matrix
```

```
#you can create matrices with rbind(rowvector1,rowvector2,...), or with cbind(column vector)
```

```
myMatrix<-rbind(c(2,3,4),c(3,4,5),c(1,2,3))
myMatrix
```

```
[,1] [,2] [,3]
[1,]    2    3    4
[2,]    3    4    5
[3,]    1    2    3
```

```
myMatrix2<-cbind(c(1,2,3),c(4,5,6),c(7,8,9))
myMatrix2
```

```
[,1] [,2] [,3]
[1,]    1    4    7
[2,]    2    5    8
[3,]    3    6    9
```

```
myMatrix3<-cbind(myMatrix2,c(10,11,12))
myMatrix3
```

```
[,1] [,2] [,3] [,4]
[1,]    1    4    7   10
[2,]    2    5    8   11
[3,]    3    6    9   12
```

```
myMatrix3<-cbind(c(10,11,12),myMatrix2)
```

We can also do Matrix math:

```
#again math functions apply to every element
myMatrix^2
```

```
[,1] [,2] [,3]
[1,]    4    9   16
[2,]    9   16   25
[3,]    1    4    9
```

```
#multiply with '%*%
myMatrix2%*%myMatrix
```

```
[,1] [,2] [,3]
[1,]   21   33   45
[2,]   27   42   57
[3,]   33   51   69
```

```
#we can find the inverse with 'solve()
X<-matrix(c(1,0,1,-2,3,0,1,4,2),nrow=3)
X
```

```
[,1] [,2] [,3]
[1,]    1   -2    1
[2,]    0    3    4
[3,]    1    0    2
```

```

solve(X)

[,1] [,2] [,3]
[1,] -1.2 -0.8  2.2
[2,] -0.8 -0.2  0.8
[3,]  0.6  0.4 -0.6

#check dimension
dim(X)

[1] 3 3

#We can also transpose with t()
t(X)

[,1] [,2] [,3]
[1,]    1    0    1
[2,]   -2    3    0
[3,]    1    4    2

#Some times to multiply vectors we have to turn them into matrix types
myVector<-c(1,2,3)
newM<-matrix(myVector,ncol=1)

```

## A.5 Functions

Functions are objects that take an input and transform it into some output, just like in mathematics. We have already seen some, such as `log()`.

They are called with this format `output<-functionName(input)`.

- The input is called *parameters*, and there can be many parameters
- parameters are usually described in the documentation
- the output is what the function *returns*
- functions can only return 1 object, but this includes a list... so it could return many objects in the form of a list object

R has many, many functions, to learn more about a function type `?functionName` and the documentation will come up.

```
#A simple function
#here the function log is called, with the parameter 2, and the output is stored in the variable x
x<-log(2)
x
```

```
[1] 0.6931472
```

```
#A more complicated function
#What are the parameters?
#not rep(a,n) gives a vector of size n where all elements are a
s<-sample(x=1:10,size=4,replace=TRUE,prob=rep(1/10,10))
s
```

```
[1] 9 3 6 1
```

We have seen other people's functions but we can also make our own! Let's see an example first:

```
#recall the dot product example...
dotProd=function(a,b){
  value<-sum(a*b)
  return(value)
}
#calling our function
dotProd(x,y)
```

```
[1] 10.39721
```

What exactly does this code say?

- We stored the function in the variable `dotProd`
- to tell the compiler we are creating a function, we use the keyword `function`
- we specify the parameters in round brackets `()`
- we put the names of the parameters in the `()` only, not what data type we expect them to be
- inside curly brackets, we put the code that the function will run when it is called
- `return()` ends the function, and sends back the variable in the brackets

Back to built in functions... R is a statistical software, what does that mean? It already includes many common statistical functions! For most common distributions there are functions for the pdf, cdf, inverse cdf as well as one to get a sample from that distribution. The syntax is in the format: `dDistName(x,parameters)`, `pDistName(x,parameters)`, `qDistName(x,parameters)` and `rDistName(x,parameters)` respectively. This will make more sense in the example below...

```
#The normal distribution, sd is the standard deviation  
#pdf  
dnorm(c(2,3,5),mean=0,sd=1)
```

```
[1] 5.399097e-02 4.431848e-03 1.486720e-06
```

```
#cdf  
pnorm(c(2,3,5),mean=0,sd=1)
```

```
[1] 0.9772499 0.9986501 0.9999997
```

```
#inverse cdf  
qnorm(c(0.2,.5,.3),mean=0,sd=1)
```

```
[1] -0.8416212 0.0000000 -0.5244005
```

```
#random sample of size 10  
rnorm(10,mean=0,sd=1)
```

```
[1] 0.1144319 1.4437119 1.2011116 -0.4250923 0.4535709 -1.0646861  
[7] -0.2045586 -0.8419064 0.8100511 -0.5563228
```

## A.6 Plotting

R is very good for plotting! There are many types of plots in R, here are some useful plotting functions, this list is not exhaustive...

- `plot(x,y,...)` produces a scatter plot.
- `abline(a=intercept,b=slope,...)`
- `curve(expr,...)` evaluates an expression along a grid to create a curve

- `hist(data)` creates a histogram

Plot functions have many parameters, some include `col` which changes the color and `add` which should be set to `TRUE` if the plot should be added to the existing plot. The best way to learn plots is with examples, I have included a regression example below.

```
#simulate errors
epsilon<-rnorm(100)
x<-rexp(100)
y<-9+2*x+epsilon

#scatter plot with true line
plot(x,y)
abline(a=9,b=2,col="blue")

#least squares line
lmm<-lm(y~x)
summary(lmm)
```

Call:

```
lm(formula = y ~ x)
```

Residuals:

Min	1Q	Median	3Q	Max
-2.50910	-0.67030	-0.00423	0.49445	2.68962

Coefficients:

	Estimate	Std. Error	t value	Pr(> t )
(Intercept)	9.2831	0.1325	70.04	<2e-16 ***
x	1.7791	0.1057	16.83	<2e-16 ***
---				

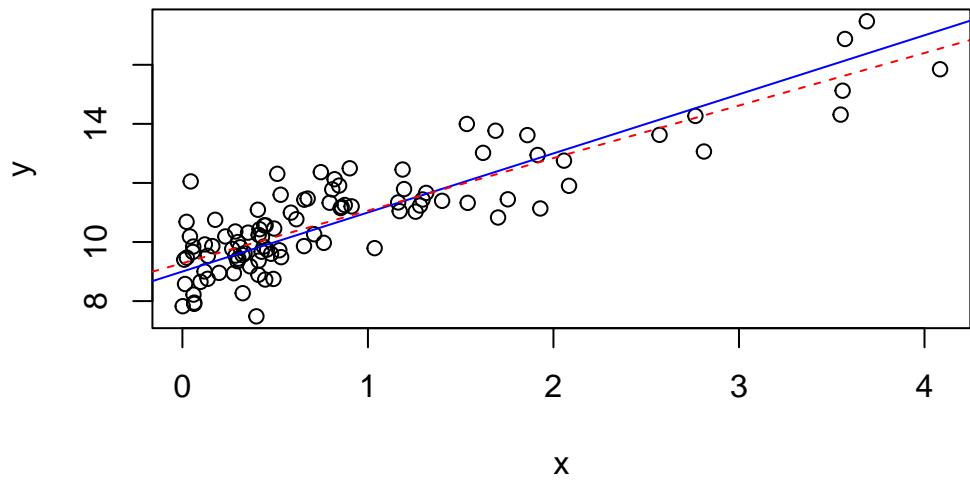
Signif. codes: 0 '\*\*\*' 0.001 '\*\*' 0.01 '\*' 0.05 '.' 0.1 ' ' 1

Residual standard error: 0.9582 on 98 degrees of freedom

Multiple R-squared: 0.7429, Adjusted R-squared: 0.7403

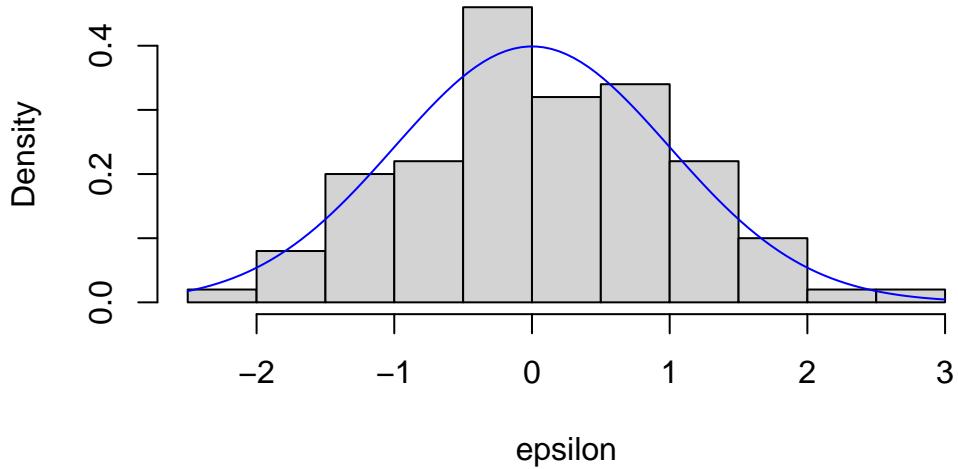
F-statistic: 283.2 on 1 and 98 DF, p-value: < 2.2e-16

```
abline(lmm$coefficients[1],lmm$coefficients[2],col="red",lty=2)
```



```
#histogram of residuals
hist(epsilon,freq = F)
#x is what you want to evaluate the grid along
curve(dnorm(x),add=T,col="blue")
```

### Histogram of epsilon



## A.7 If Statements

If statements are essential in programming, and they are a form of ‘Control Structure’. They take the form `if(boolean variable){some task}`.

When the computer runs through the code, it checks if the boolean value is `TRUE`, and if it is, it executes the code in the curly brackets, code in curly brackets is called a *block*. A simple example...

```
jim<-"nice"

if(jim=="nice"){
  alice="nice"
}
```

Placing an `else{some code}` after the if statement will execute the code in it’s block if the code in the above if statement *was not* executed. The if and else must be in the same block so I have surrounded them in curly brackets.

```
jim<-"nice"
##same block
{
```

```
if(jim=="nice"){
  alice="nice"
}
else{
  alice="not nice"
}
alice
```

```
[1] "nice"
```

```
jim<-"mean"
##same block
{
if(jim=="nice"){
  alice="nice"
}
else{
  alice="not nice"
}
alice
```

```
[1] "not nice"
```

You may also use `else if(boolean){block}`, which executes it's block if the above (else) if statement(s) did not execute. See below:

```
jim<-"okay"
##same block
{
if(jim=="nice"){
  alice="nice"
}
else if(jim=="okay"){
  alice="okay"
}
#Here if jim is not okay or nice, then we check if he is neutral.
else if(jim=="neutral"){
  alice="neutral"
```

```
    }
} else{
  alice="not nice"
}
alice
}
```

```
[1] "okay"
```

Lastly you may put if statements inside of other if statements, called ‘nested ifs’.

```
jim<-"nice"
##same block

if(jim=="nice"){
  alice=sample(c("nice","not nice"),1)
  if(alice=="nice"){
    print(alice)
  }
  else{
    print(alice)
  }
}
```

```
[1] "nice"
```

## A.8 Loops

Loops execute operations within their blocks repeatedly. There are 2 types of loops you will generally use, for loops and while loops. For loops repeat the block a set number of times, while while loops repeat until a condition is satisfied. You can also nest loops, like if statements.

```
#calculate 2 to the power of ten
x<-1
#this reads for i in 1 to 10, this can be any vector that i loops through, not just a sequence
for(i in 1:10){
  x<-x*2
}
```

```
x
```

```
[1] 1024
```

```
for(i in 1:10){  
  x<-x+i  
}  
  
vec=2:5  
  
for(i in vec){  
  x<-x+i  
}  
  
#calculate power of 2 less than 1000  
x<-1  
while(2*x<1000){  
  x<-x*2  
}  
x
```

```
[1] 512
```

```
#nested loop  
for(i in c(10,9,8,7,6,5,4,3,2,1)){  
  v<-NULL  
  for(j in 1:i){  
    v<-c(v,"*")  
  }  
  print(v)  
}
```

```
[1] "*" "*" "*" "*" "*" "*" "*" "*" "*" "*" "*" "*"  
[1] "*" "*" "*" "*" "*" "*" "*" "*" "*" "*" "*"  
[1] "*" "*" "*" "*" "*" "*" "*" "*" "*"  
[1] "*" "*" "*" "*" "*" "*" "*" "*"  
[1] "*" "*" "*" "*" "*" "*"  
[1] "*" "*" "*" "*" "*"
```

```
[1] "*" "*" "*" "*"
[1] "*" "*" "*"
[1] "*" "*"
[1] "*"
```

You can also use the `replicate` function, which replicates a line of code a specified number of times. This gives a 10 by 5 matrix.

```
replicate(5,rnorm(10))
```

	[,1]	[,2]	[,3]	[,4]	[,5]
[1,]	-0.87792227	-1.3207310	0.6672619	0.6172735	-0.6970302
[2,]	1.31751836	0.1139693	0.4894577	-0.5204016	0.8965531
[3,]	-0.38479214	0.6237071	0.4576051	-0.3716644	0.2474148
[4,]	-0.57802144	0.3996335	0.6288974	-0.1433156	0.4785685
[5,]	0.82808340	-0.9504758	0.3665279	-0.9369322	0.9818202
[6,]	-1.10535449	1.1116529	0.6306810	2.1061986	0.1538709
[7,]	0.84640052	1.5537925	1.5486722	-0.2716292	-0.6203708
[8,]	-0.06170204	1.0483459	-0.5265191	-2.0115232	-1.1135819
[9,]	-1.64816742	0.6931981	0.5275307	-0.3247686	-0.7252148
[10,]	-1.06726622	2.4724317	-1.1681384	0.1762106	-1.0338485

Similar functions include `sapply()` and `apply()`. `sapply(X,FUN,...)` applies the function that the parameter `FUN` is set to to individual elements of a vector. `apply(X,MARGIN,FUN,...)` applies `FUN` to the rows or columns depending on what `MARGIN` is set to, 1 for rows and 2 for columns.

## A.9 Coverage Probability Example

Here we generate 10000 samples of size 100 from the exponential distribution, with  $\lambda = 2$ . We calculate 10000 confidence intervals for  $1/\lambda$  with  $\$ = \$1\%$ , using the normal approximation:

$$\sqrt{n}(\bar{X} - 1/\lambda) \sim N(0, 1/\lambda^2)$$

and interval:

$$(\bar{X} - t_{99}(0.005) * S/\sqrt{n}, \bar{X} + t_{99}(0.005) * S/\sqrt{n})$$

We then check the proportion of intervals that contain the true value of  $1/\lambda$ .

```
#10000 samples, each of size 100 from the exponential distribution
x<-replicate(10000,rexp(100,rate=2))
#x is 100 by 10000, each column is a sample
dim(x)
```

```
[1] 100 10000
```

```
#calculate sample variances
S_Vector<-apply(x,2,SD);

# S_Vector

#get the t value
tval<-qt(1-0.005,99)
#calculate the means

means<-apply(x,2,mean); length(means)
```

```
[1] 10000
```

```
# lower and upper bounds
lower<-means-S_Vector*tval/10
upper<-means+S_Vector*tval/10
intervals<-rbind(lower,upper)
#example interval
intervals[,1]
```

lower	upper
0.3135737	0.5448307

```
#we now check each interval to see if it contains the mean
successes<-0
for(i in 1:ncol(intervals)){
  #if 0.5 is in the interval, add 1
  if((intervals[1,i]<0.5)&&(intervals[2,i]>0.5))
    successes<-successes+1
}
#here is the coverage probability...
```

```
coverage.prob<-successes/ncol(intervals)
coverage.prob
```

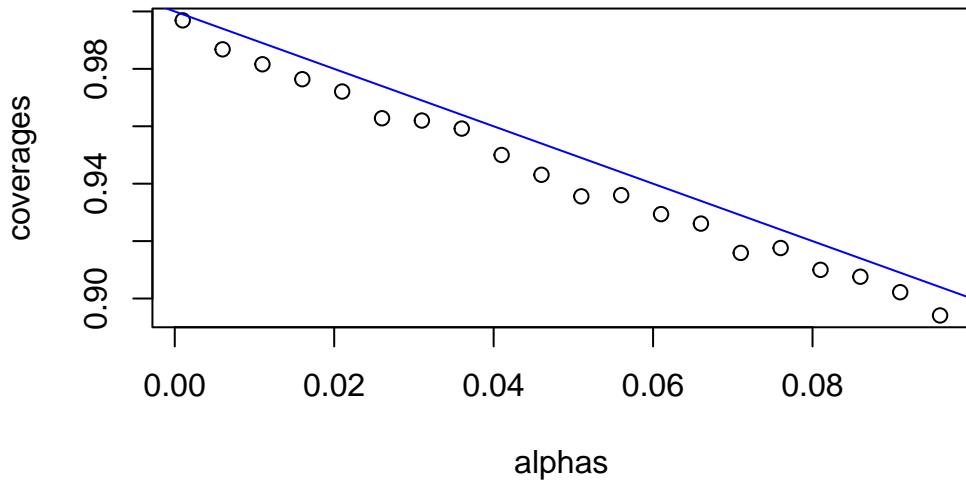
```
[1] 0.983
```

Something more advanced...

```
#Vectorizing the function changes the way the function calculates when it is passed a vector
#it will run the function once per element if it is vectorized instead of passing the vector
getCovProb<-Vectorize(function(alpha){
  #10000 samples, each of size 100 from the exponential distribution
  x<-replicate(10000,rexp(100,rate=2))
  #x is 100 by 10000, each column is a sample
  dim(x)
  #calculate sample variances
  S_Vector<-apply(x,2,sd)
  #get the t value
  tval<-qt(1-alpha/2,99)
  #calculate the means
  means<-apply(x,2,mean)
  # lower and upper bounds
  lower<-means-S_Vector*tval/10
  upper<-means+S_Vector*tval/10
  intervals<-rbind(lower,upper)
  #example interval
  intervals[,1]

  #we now check each interval to see if it contains the mean
  successes<-0
  for(i in 1:ncol(intervals)){
    #if 0.5 is in the interval, add 1
    if((intervals[1,i]<0.5)&(intervals[2,i]>0.5))
      successes<-successes+1
  }
  #here is the coverage probability...
  coverage.prob<-successes/ncol(intervals)
  return(coverage.prob)
})
#here we find the coverage probability for many alphas
alphas<-seq(from=0.001,to=0.1,by=0.005)
coverages<-getCovProb(alphas)
```

```
#adds a scatter plot  
plot(alphas,coverages)  
#adds a line  
abline(a=1,b=-1,col="blue")
```



For more information you can visit [here](#). It is also very easy to find tutorials on the web (Youtube is good), you could also look at the book by Lafaye, Drouilhet and Liquet (2013).