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Pixel-Planes 5: A Heterogeneous Multiprocessor Graphics System Using Processor-Enhanced Memories¹

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Abstract

This paper introduces the architecture and initial algorithms for Pixel-Planes 5, a heterogeneous multi-computer designed both for high-speed polygon and sphere rendering (1M Phong-shaded triangles/second) and for supporting algorithm and application research in interactive 3D graphics. Techniques are described for volume rendering at multiple frames per second, font generation directly from conic spline descriptions, and rapid calculation of radiosity form-factors. The hardware consists of up to 32 mathoriented processors, up to 16 rendering units, and a conventional 1280x1024-pixel frame buffer, interconnected by a 5 gigabit ring network. Each rendering unit consists of a 128x128-pixel array of processors-with-memory with parallel quadratic expression evaluation for every pixel. Implemented on 1.6 micron CMOS chips designed to run at 40MHz, this array has 208 bits/pixel on-chip and is connected to a video RAM memory system that provides 4,096 bits of off-chip memory. Rendering units can be independently reassigned to any part of the screen or to non-screen-oriented computation. As of April 1989, both hardware and software are still under construction, with initial system operation scheduled for fall 1989.

CR Categories and Subject Descriptors: B.2.1 [Arithmetic and Logic Structures]: Design Styles - parallel; C.1.2 [Processor Architectures]: Multiprocessors - parallel processors; I.3.1 [Computer Graphics]: Hardware Architecture - raster display devices; I.3.3 [Computer Graphics]: Picture/Image generation - display algorithms; I.3.7 [Computer Graphics]: 3D Graphics and Realism - color, shading and texture, visible surface algorithms.

Additional Key Words and Phrases: logic-enhanced memory, ring network, polygon scan-conversion

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1. Introduction

Many computer applications seek to create an illusion of interaction with a virtual world. Vehicle simulation, geometric modeling and scientific visualization, for example, all require rapid display of computer-generated imagery that changes dynamically according to the user's wishes. Much progress has been made in developing high-speed rendering hardware over the past several years, but even the current generation of graphics systems can render only modest scenes at interactive rates.

For many years our research goal has been the pursuit of truly interactive graphics systems. To achieve the necessary rendering speeds and to provide a platform for real-time algorithm research, we have been developing a massively parallel image generation architecture called *Pixel-Planes* [Fuchs 81, 82, 85, Poulton 85]. We briefly describe the basic ideas in the architecture:

Each pixel is provided with a minimal, though general, processor, together with local memory to store pixel color, z-depth, and other pixel information. Each processor receives a distinct value of a linear expression in screen-space, Ax + By + C, where A, B, C are data inputs and x,y is the pixel address in screen-space. These expressions are generated in a parallel linear expression evaluator, composed of a binary tree of tiny multiply-accumulator nodes. A custom VLSI chip contains pixel memory, together with the relatively compact pixel processors and the linear expression evaluator, both implemented in bit-serial circuitry. An array of these chips forms a "smart" frame buffer, a 2D computing surface that receives descriptions of graphics primitives in the form of coefficients (A,B,C) with instructions and locally performs all pixel-level rendering computations. Since instructions, memory addresses, and A,B,C coefficients are broadcast to all processors, the smart frame buffer forms a Single-Instruction-Multiple-Datastream computer, and has a very simple connection topology. Instructions (including memory addresses and A,B,C's) are generated in a conventional graphics transformation engine, with the relatively minor additional task of converting screen-space polygon vertices and colors into the form of linear expressions and instructions.

In 1986 we completed a full-scale prototype Pixel-Planes system, Pixel-Planes 4 (*Pxpl4*) [Poulton 87, Eyles 88], which renders 39,000 Gouraud-shaded, z-buffered polygons per second (13,000 smooth-shaded interpenetrating spheres/second, 11,000 shadowed polygons/second) on a 512x512 pixel full-color display. While this system was a successful research vehicle and is extremely useful in our department's computer graphics laboratory, it is too large and expensive to be practical outside of a research setting. Its main limitations are:

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- large amount of hardware, often utilized poorly (particularly when rendering small primitives)
- hard limit on the memory available at each pixel (72 bits)
- no access to pixel data by the transformation unit or host computer
- · insufficient front-end computation power

This paper describes its successor, Pixel-Planes 5 (Pxpl5). Pxpl5 uses screen subdivision and multiple small rendering units in a modular, expandable architecture to address the problem of processor utilization. A full-size system is designed to render in excess of one million Phong-shaded triangles per second. Sufficient "front end" power for this level of performance is provided by a MIMD array of general-purpose math-oriented processors. The machine's multiple processors communicate over a high-speed network. Its organization is sufficiently general that it can efficiently render curved surfaces, volume-defined data and CSG-defined objects. In addition it can rapidly perform various image-processing algorithms. Pxpl5's rendering units each are 5 times faster than Pxpl4 and contain more memory per pixel, distributed in a memory hierarchy: 208 bits of fast local storage on its processor-enhanced memory chips, 4K bits of memory per pixel processor in a conventional VRAM "backing store", and a separate frame buffer that refreshes normal and stereo images on a 1280x1024 72Hz display.

2. Background

Raster graphics systems generally contain two distinct parts: a graphics transformation engine that transforms and lights the geometric description of a scene in accordance with the user's viewpoint and a Renderer that paints the transformed scene onto a screen.

Designs for fast transformation units have often cast the series of discrete steps in the transformation process onto a pipeline of processing elements, each of which does one of the steps [Clark 82]. As performance requirements increase, however, simple pipelines begin to experience communication bottlenecks, so designers have turned to multiple pipelines [Runyon 87] or have spread the work at some stages of the pipe across multiple processors [Akeley 88]. Vector organizations offer a simple and effective way to harness the power of multiple processors, and have been used in the fastest current graphics workstations [Apgar 88, Diede 88]. Wide vector organizations may have difficulty with data structures of arbitrary size, such as those that implement the PHIGS+ standard, so at least one commercial offering divides the work across multiple processors operating in MIMD fashion [Torberg 87].

The rendering problem has generally been much more difficult to solve because it requires, in principal, computations for every pixel of every primitive in a scene. To achieve interactive speeds on workstation-class machines, parallel rendering engines have become the rule. These designs must all deal with the memory bandwidth bottleneck at a raster system's frame buffer. Three basic strategies for solving this problem are:

Rendering Pipelines. The rendering problem can also be pipelined over multiple processors. The Hewlett-Packard SRX graphics system [Swanson 86], for example, uses a pipeline of processors implemented in custom VLSI that simultaneously perform 6-axis interpolations for visibility and shading, operating on data in a pixel cache.

The frame buffer bandwidth bottleneck can be ameliorated by writing to the frame buffer only the final colors of the *visible* pixels. This can only be achieved if all the primitives that may affect a pixel are known and considered before that pixel is written. Sorting primitives by screen position minimizes the number that have to be

considered for any one pixel. Sorting first by Y, then by X achieves a scan-line order that has been popular since the late 1960's and is the basis for several types of real-time systems [Watkins 70]. The basic strategy has been updated by several groups recently. The SAGE design [Gharachorloo 88] contained a processor for every pixel on a scan-line. Data for primitives active on a scan-line pass by this array, and visible pixel colors are emitted at video rates; no separate frame buffer is required. Researchers at Schlumberger [Deering 88] recently proposed a system in which visibility and Phong-shading processors in a pipeline are assigned to the *objects* to be rendered on the current scan line. The latter two projects promise future commercial offerings that can render on the order of 1M triangles per second with remarkably little hardware, though designs for the front ends of these systems have yet to be published. These machines have each cast one particular rendering algorithm into hardware, enabling a lower-cost solution but one not intended for internal programming by users. New algorithms cannot easily be mapped onto hardware for scan-line ordered pipelines. Finally, a difficulty with these designs is ensuring graceful performance degradation for scenes with exceptional numbers of primitives crossing a given scan-line.

Interlaced Processors. As first suggested a decade ago [Fuchs 77, 79, Clark 80], the frame buffer memory can be divided into groups of memory chips, each with its own rendering processor, in an interlaced fashion (each processor-with-memory handles every nth pixel on every mth row). The rendering task is distributed evenly across the multiple processors, so the effective bandwidth into the frame buffer increases by a factor of $m \cdot n$. This idea is the basis of several of the most effective current raster graphics systems [Akeley 88, Apgar 88]. Some of these systems, however, are again becoming limited by the bandwidth of commercial DRAMs [Whitton 84]. With increasing numbers of processors operating in SIMD fashion, processor utilization begins to suffer because fewer processors are able to operate on visible pixels, the "write efficiency" problem discussed in [Deering 88]. Raising the performance of interlaced processors by an order of magnitude will probably require more complex organizations or new memory devices.

Processor-Enhanced Memories. Much higher memory bandwidth can be obtained by combining some processing circuitry on the same chip with dense memory circuits. The most widely used example of a "smart" memory is the Video RAM (VRAM), introduced by Texas Instruments. Its only enhancement is a second, serial-access port into the frame buffer memory; nevertheless these parts have had a great impact on graphics system design. The SLAM system, described some years ago in [Demetrescu 85], combines a 2D frame buffer memory with an on-chip parallel 1D span computation unit; it appears to offer excellent performance for some 2D applications but requires external processing to divide incoming primitives into scanline slices. Recently NEC announced a commercial version of an enhanced VRAM that performs many common functions needed in 2D windowing systems. This approach has been the focus of our work since 1980; in the Pixel-Planes architecture we have attempted to remove the memory bottleneck by performing essentially all pixeloriented rendering tasks within the frame buffer memory system itself.

The architecture we will describe below employs a MIMD array of processors in its transformation unit and seeks to make more effective use of the processor-enhanced memory approach.

3. Project Goals

We wanted Pixel-Planes 5 to be a platform for research in graphics algorithms, applications and architectures, and a testbed for refinements that would enhance the cost effectiveness of the approach. To this end, we adopted the following goals:



- Fast Polygon Rendering. Despite all the interest in higherorder primitives and rendering techniques, faster polygon rendering is still the most often expressed need for many applications: 3D medical imaging, scientific visualization, 'virtual worlds' research. We therefore set a goal of rendering 1 million z-buffered Phong-shaded triangles per second, assuming the average triangle's area is 100 pixels and that it is embedded in a triangle strip. We wanted to achieve this rate without using any special structures for rendering just triangles — we wanted a system for much more than triangles.
- Generality. For the system to be an effective base for algorithm development, it needed to have a simple, general structure whose power was readily accessible to the algorithm developer programming in a high-level language. We wanted it to have sufficient generality for rendering curved surfaces, volume data, objects described with Constructive Solid Geometry, for rendering scenes using the radiosity lighting model, and (we hoped) for a variety of other 3D graphics tasks that we have not yet considered. It was essential that the system support a PHIGS+ -like environment for application programmers not interested in the system's low-level details. Further, the hardware platform should be flexible to allow experiments in hardware architectures.
- Packaging. A high-performance configuration that met our primary performance goals should fit within a workstation cabinet with no unusual power requirements. We also wanted a system that could be modularly built and flexibly configured to trade cost for performance. The system should drive a 1280x1024 display at >60Hz, and be able to update full scene images at >20 frames/second.

4. Parallel Rendering by Screen-space Subdivision

We now describe the scheme we use in Pxpl5 to attain high levels of performance in a compact, modular, expandable machine. Our previous work has depended on a single, large computing surface of SIMD parallel processors operating on the entire screen space. In the new architecture, we instead have one or more small SIMD engines, called Renderers, that operate on small, separate 128x128-pixel patches in a virtual pixel space. Virtual patches can be assigned on the fly to any actual patch of the display screen. The system achieves considerable speedup by simultaneously processing graphics primitives that fall entirely within different patches on the screen.

The principal cost of this screen-space subdivision scheme is that the primitives handled in the transformation engine must be sorted into "bins" corresponding to each patch-sized region of the screen space. Primitives that fall into more than one region are placed into the bins for all such regions. The simplest (though expensive) way to support these bins is to provide additional storage in the transformation engine for the entire, sorted list of output primitives. Once transformed, sorted, and stored, a new scene is rendered by assigning all available Renderers to patches on the screen and dispatching to these Renderers primitives from their corresponding bins. When a Renderer completes a patch, it can discard its z-buffer and all other pixel values besides colors; pixel color values are transferred from on-chip pixel memory to the secondary storage system, or "backing store", described below. The Renderer is then assigned to the next patch to be processed. This process is illustrated in Figure 1 for a system configured with only four Renderers.

The general idea of multiple independent groups of pixel processors operating on disjoint parts of the display screen was described in several of our earlier publications as "buffered" Pixel-Planes. What

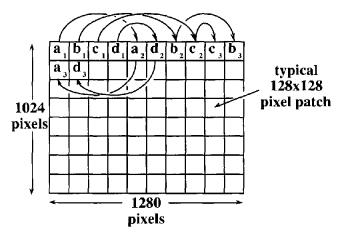


Figure 1: Rendering process for a Pxpl5 system with 4 Renderers. 1280x1024 screen is divided into 80 128x128 patches. Patches are processed in raster order. Renderers a-d are assigned initially to the first four patches. Renderer a completes first, and is assigned to the next available patch. Next Renderer d completes its first patch and is assigned to the next available patch, and so forth.

is new about this implementation is the idea of flexibly mapping small virtual pixel spaces onto the screen space. It allows useful systems to be built with any number of small rendering units, permits cost/performance to be traded nearly linearly, and can render into a window of arbitrary size with only linear time penalty.

The virtual pixel approach is supported in the Pxpl5 implementation by a memory hierarchy, whose elements are: (1) 208 bits of fast SRAM associated on-chip with each pixel processor; (2) a "backing store" built from VRAMs, tightly linked to the custom logic-enhanced memory chips; (3) a conventional VRAM frame buffer. The backing store consists of an array of VRAMs, each connected via its video port to one of our custom memory chips; 1MB VRAMs provide 4Kbits of storage per pixel. The backing store memory is available through the VRAM random I/O port to the rest of the system, which can read and write pixel values in the conventional way. A Renderer uses this memory to save and retrieve pixel values, effectively allowing "context switches" when the Renderer ceases operations on one patch and moves to another. A typical context switch takes about 0.4 msec, the time to render a hundred or so primitives, and can be fully overlapped with pixel processing.

In the simple multi-Renderer scheme described above, the backing store is used to store pixel color values for patches of the screen as the Renderer completes them. When the entire image has been rendered, each of these regions is transferred in a block to the (double-buffered) display memory in the Frame Buffer, from which the display is refreshed.

5. Architectural Overview

The major elements of *Pxpl5* are:

- Graphics Processors (GPs), floating point engines, each with considerable local code and data storage.
- Renderers, each a small SIMD array of pixel processors with its own controller.
- Frame Buffer, double-buffered, built from conventional Video RAMs, from which the video display is refreshed.





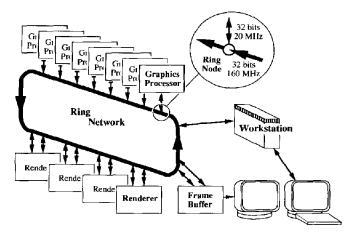


Figure 2: Pxpl5 block diagram.

- Host Interface, which supports communications to/from a UNIX workstation.
- Ring Network to interconnect the various processors in a flexible way.

5.1 Ring Network

Pxpl5's multi-processor architecture, motivated by the desire to support a variety of graphics tasks, requires a capable communications network. Rather than build several specialized communications busses to support different types of traffic between system elements, we instead provide a single, flexible, very high performance network connecting all parts of the system.

At rendering rates of 1M primitives per second, moving object descriptions from the GPs to the Renderers requires up to 40 million 32-bit words/second (40 MW/sec), even for relatively simple rendering algorithms. Simultaneously, pixel values must be moved from the Renderers to the Frame Buffer at rates up to 40 MW/sec, for real-time interactive applications. At the suggestion of J. William Poduska of Stellar Computer, Inc., we explored technology and protocols for fast ring networks, and eventually settled on a multi-channel token ring. Ring networks have many advantages over busses in high-speed digital systems. They require only point-to-point communication, thus reducing signal propagation and power consumption problems, while allowing a relatively simple communication protocol. Their major disadvantage, long latency, is not acceptable for many computing systems, but is okay here.

Our network can support eight simultaneous messages, each at 20 MW/sec for a total bandwidth of 160 MW/sec. To avoid deadlock, each transmitting device gains exclusive access first to its intended receiver, then to one of the 8 data channels, before it transmits its data packet. Each Ring Node is a circuit composed of commercial MSI bus-oriented data parts and field-programmable controllers. (At the expense of an expensive development cycle, the Ring Network could be reduced to one or a few ASICs.) The controllers operate at 20MHz, while data is moved at 40MHz (to save wires). Each client processor in the system has one or more of these Nodes, which provides to the client a 20 MW/sec port onto the Ring network.

We have developed a low-level message-passing operating system for the ring devices called the Ring Operating System (ROS). It provides device control routines as well as hardware independent communication. In addition, ROS controls the loading and initialization of programs and data.

5.2 Graphics Processors

The performance goals we have set require sustained computation rates in the "front end" of several hundred MFlops, feasible today only in parallel or vector architectures. We elected to build a MIMD transformation unit; this organization handles PHIGS+-like variable data structures better than would a vector unit, and supports the "bins" needed for our screen subdivision multi-Renderer.

Much of the system's complexity is hidden by ROS; the programming model is therefore relatively simple. Load sharing is accomplished by dividing a database across the GPs, generally with each GP running the same code. Since the GPs are programmable in the C language, users have access to the machine's full capability without needing to write microcode.

5.3 Renderer

Section 4 describes the essentials of the Renderer design, whose block diagram is shown in Figure 3. It is based on a logic-enhanced memory chip built using 1.6 micron CMOS technology and operating at 40MHz bit-serial instruction rates. In addition to 256 pixel processing elements, each with 208 bits of static memory, the chip contains a quadratic expression evaluator (QEE) that produces the value Ax+By+C+Dx²+Exy+Fy² simultaneously at each pixel x,y from global inputs A,B,C,D,E,F[Goldfeather 86]. Quadratic expressions, while not essential for polygon rendering, are very useful for rendering curved surfaces and for computing a spherical radiosity lighting model (see Section 7.6).

A major design issue for the Renderer was choosing the size of the processor array. The effectiveness of the screen-space subdivision scheme for parallel rendering is determined in part by the frequency with which primitives must be processed in more than one region, and this in turn depends on the size of the Renderer's patch. On one hand, economy of use of the fairly expensive custom chips of the processor array and the need to leverage performance by dividing the rendering work across as many processors as possible argue for smaller Renderer patches. A large Renderer patch, on the other hand, reduces the likelihood that primitives will need to be processed more than once. We elected a 128x128 Renderer size; it is fairly efficient for small primitives, and its hardware conveniently fits on a reasonable size printed circuit board.

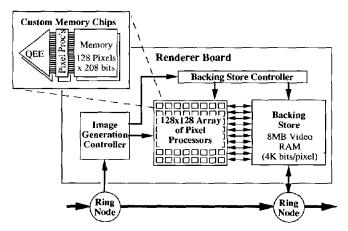


Figure 3: Block diagram of a *Pxpl5* Renderer. Pixel processor array implemented in 64 custom chips, each with 2 columns of 128 pixel processors-with-memory and a quadratic expression evaluator.





5.4 Frame Buffer and Host Interface

The Frame Buffer is built in a fairly conventional way using Video RAMs. It supports a 1280x1024-pixel, 72Hz refresh-rate display, 24-bit true color and a color lookup table. Display modes include stereo (alternating frames) and a hardware 2x zoom. The Frame Buffer is accessed through two Ring Nodes, to provide an aggregate bandwidth of 40 MW/sec into the buffer, allowing up to 24Hz updates for full-size images. *Pxpl5* is hosted by a Sun 4 workstation. Host communication is via programmed I/O, providing up to 4 MBytes/sec bandwidth between *Pxpl5* and its host.

5.5 Performance

Since the transformation engine in *Pxpl5* is based on the same processor used in *Pxpl4*, we estimate, based on the earlier machine's performance, that a GP can process on the order of 30,000 Phongshaded triangles per second; 32 GPs are therefore required to meet our performance goal. A single Renderer has a raw performance of about 150,000 Phong-shaded triangles per second; actual performance is reduced somewhat by inefficiencies resulting from primitives that must be processed in more than one patch. Simulations predict an actual performance of around 100,000 triangles/sec, so a configuration to meet the performance goals will require 8-10 Renderers.

6. PPHIGS Graphics Library

Pxpl5 may be programmed at various levels. We anticipate users ranging from application programmers, who simply desire a fast rendering platform with a PHIGS+-style interface [van Dam 88], to algorithm prototypers, who need access to the Renderer's low-level pixel operations and may depart from the PHIGS+ paradigm. To meet these disparate needs, several layers of support software are required. Program initialization and message passing between processors are handled by the Ring Operating System (ROS). A local variation of PHIGS+ (Pixel-Planes PHIGS or PPHIGS) provides a high-level interface for users desiring portable code. This section describes PPHIGS.

PPHIGS makes the hardware appear to the "high-level" graphics programmer very much like any other graphics system: the programmer's code (running on the host) makes calls to the graphics system to build and modify a hierarchical data structure. This structure is traversed by the PPHIGS system to create the image on the screen.

6.1 Database Distribution

Since the applications programming library is based on PHIGS, it allows the programmer to create a display list that is a directed acyclic graph of structures. These structures contain elements that are either graphics primitives, state-changing commands, or calls to execute other structures. To take advantage of the multiple graphics processors in *Pxpl5*, we must distribute the database structure graph across the graphics processors in a way that balances the computational load, even in the presence of editing and changes in view. In order to achieve this we must balance the load across GPs for each structure. When a structure is created, some of the primitives are placed on each GP. If the object goes out of view or a new instance is created, the load will remain balanced.

In PHIGS, as in most structured display list systems, child structures inherit information from their parents such as transformation matrices and colors. These state-changing commands as well as structure execution calls must be replicated on each GP since each structure is distributed across multiple GPs. This replication should not be a problem, since we expect the majority of structure elements to be

graphics primitives and not state-changing ones. We have devised other distribution schemes for applications that violate this assumption.

6.2 The Rendering Process

The rendering process is controlled by a designated graphics processor, the master GP, or MGP. By exchanging messages with other GPs and sending commands to other modules when necessary, the MGP synchronizes operations throughout the system.

Before discussing the steps in the rendering process, we first want to emphasize the distinction between pixel operations that take place on a per primitive basis, such as z comparison and storage, and those that can be deferred until the end of all primitive processing or *end-of-frame*. Shading calculations from intermediate values stored at the pixels, for instance, need only be performed once per pixel, rather than once per primitive (assuming there is sufficient pixel storage to hold the intermediate values until end-of-frame). During end-of-frame the final colors can be computed in parallel from the stored values of the visible portions of every polygon that falls within the 128x128 pixel region. For expensive lighting and shading models, such as Phong shading and textures, this speedup is dramatic.

The major steps in the rendering process are:

- The application program running on the host edits the database using PPHIGS library routines and transmits these changes to the GPs
- Application requests a new frame. Host sends this request to the MGP, which relays it to the other GPs.
- The GPs interpret the database, generating Renderer commands for each graphics primitive. These commands are placed into the local bins corresponding to the screen regions where the primitive lies. Each GP has a bin for every 128x128 pixel region in the window being rendered.
- The GPs send bins containing commands to Renderers. The Renderers execute commands and compute intermediate results.
- The GP sending the final bin to a Renderer also sends end-offrame commands for the region. The Renderers execute these commands and compute final pixel values from the intermediate results.
- 6. The Renderers send computed pixels to the frame buffer.
- 7. When all regions have been received, the frame buffer swaps banks and displays the newly-computed frame.

The MGP assigns Renderers to screen regions while the frame is being rendered. It communicates a Renderer assignment to the GPs by sending a message to one GP, which sends its associated bin, and then forwards the message to the next GP, which does the same. At the end, the message is sent back to the MGP, indicating that all the bins have been processed. This method ensures that at most one GP attempts to transmit to a Renderer at a given time. This prevents blocked transmissions, which would slow throughput.

The steps of the rendering process can be overlapped in several ways; at maximum throughput, several frames may be in progress at once. This requires that the bin memory be double buffered. If a GP runs out of bin memory it must send some of its bin data to a Renderer to free up memory. The MGP handles synchronization to keep the frames properly separated [Ellsworth 89].

7. Rendering Algorithms

We now discuss various rendering algorithms in turn. Some of these have been published before, in which case, we review their applica-





bility to *Pxpl5* and give performance estimates. We also report new techniques for efficiently displaying procedural textures and conic spline-defined fonts, for calculating radiosity form-factors, and for displaying volume-defined images at interactive rates.

7.1 Phong Shading

Since *Pxpl5* can evaluate quadratic expressions directly, we can implement Phong shading using Bishop and Wiemer's Fast Phong Shading technique [Bishop 86]. However, the power of the pixel processors allows us to compute the Phong lighting model [Phong 73] directly. This means that the graphics processors do not have to do the extensive computation necessary to compute the quadratic coefficients. We feel that this approach will be faster and more general.

As polygons and other primitives are processed, the x, y, and z components of the surface normal are stored in all the pixels where the primitive is visible. For polygons this is done by simple linear interpolation of each component. When all the primitives for a region have been processed, the pixel-parallel end-of-frame operations are performed. First, the normal vector is normalized by dividing by the square root of its length, which is computed using a Newton iteration; then the color for each pixel is computed using the standard Phong lighting model.

Simulation indicates that the end-of-frame computation for the Phong lighting model with a single light source consumes around 23,000 Renderer cycles or .57 milliseconds. With full screen resolution of 1024 by 1280 and a 16 Renderer system, the total end-of-frame time is .57msec • (80/16) or 2.85msec per frame. At 24 frames per second this is 6.8 percent of the rendering time.

7.2 Spheres

Pxpl5 can render spheres using the same algorithm as on Pxpl4 [Fuchs 85], but is both faster (taking advantage of the QEE), and can generate higher-quality images (Phong shading with 24-bit color). Phong shading is achieved as follows. The expressions for the coordinates of the surface normal for a sphere are:

$$nx = \frac{x - a}{r}$$

$$ny = \frac{y - b}{r}$$

$$nz = \frac{\sqrt{r^2 - (x - a)^2 - (y - b)^2}}{r'}$$

The expression for nz can be approximated by a parabola:

$$rz = \frac{r^2 - (x - a)^2 - (y - b)^2}{r^2}$$

Then the normals are computed at each pixel by broadcasting two linear expressions and one quadratic expression. Results from simulation indicate that this approximation produces satisfactory shading including the specular highlights. Assuming one light source and 24 frames per second, we estimate the system performance to be 1.8M spheres per second for 100 pixel area spheres and 900K spheres per second for 1600 pixel area spheres.

7.3 Shadows

Pxp/4 was able to generate images with shadows very rapidly—nearly half as fast as images without shadows [Fuchs 85]. Unfortunately we will not achieve similar results with Pxp/5. Since a

polygon's shadow volume will cross many screen regions, the speedup we would get from screen-space subdivision will be greatly reduced. A naive approach would be to send the plane equations for the shadow volume to every region. This would greatly increase both the amount of data that would be sent over the ring and the amount of computation that the Renderers would have to do. A simple optimization would be to have the graphics processors compute which regions could possibly be shadowed by a polygon. We have not yet explored these options in depth. Because of the problems mentioned above, we anticipate increasing use of the fast radiosity technique described in Section 7.6.

7.4 Texture Mapping

We have previously reported a technique to compute the u,v texture coordinates for polygons in perspective [Fuchs 85]. The speed of this technique is limited by the time to broadcast the individual texture values to the pixels. While 64x64 image textures run at interactive rates on Pxpl4 (see Figure 4), a more efficient method for Pxpl5 is to calculate the texture values directly in each pixel. Broadcasting the texture values will be significantly faster on Pxpl5 than on Pxpl4, since texture values can be stored in bins and only broadcast when needed for one or more pixels of a region.

Image-based Textures. We have explored both summed area tables [Crow 84] and mip-maps [Williams 83] for anti-aliasing image



Figure 4: Mandrill mapped onto a plane and hoop on *Pxpl4*. Estimated rendering time on *Pxpl5* is 31 msec.

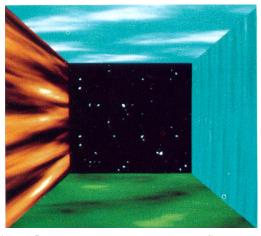


Figure 5: Procedural earth, water, sky, fire and stars textures (simulated). Estimated rendering time on *Pxpl5* is 5.5 milliseconds.



textures. We feel that mip-maps will work best on Pxpl5. During rendering the mip-map interpolation value can be linearly interpolated across the polygon. At end of frame, the mip-map is broadcast to each pixel-processor, and each processor loads the texture elements at its u,v coordinate along with neighboring values for interpolation.

Procedural Textures. We have begun to explore procedural textures, as shown by Perlin [Perlin 85] and Gardner [Gardner 88], for use in *Pxpl5*. We have written a program for *Pxpl4* that allows one to explore in real-time the space of textures possible using Gardner's technique. This program and software written by Douglass Turner were used to create the textures shown in Figure 5.

The two-dimensional Gardner spectral functions are calculated using quadratic approximations for the cosine functions. This requires nine multiplies per term plus one multiply to combine the x and y directions. Different textures for different pixels can be computed simultaneously. The images shown in the figure contains five terms. On Pxpl5 they would require about 15,000 cycles or 360 microseconds using 10 bits of resolution. These procedural methods can be anti-aliased by eliminating high frequency portions of the texture; terms whose wavelength spans less than one pixel are simply not computed [Norton 82].

7.5 Fonts

Herve Tardif has been developing methods for rapidly rendering fonts. Conic splines, as advocated by several researchers [Pavlidis 83, Pratt 85], are particularly well suited for rendering by Pxpl5; with the OEE in the processor-enhanced memories. Pxpl5 can directly scan convert conic section, from which characters are defined. Initially, a character is represented by a sequence of straight line segments and arcs of conics joined together in the plane. As suggested by Pratt, each arc of a conic is in turn represented by three points M, N, P and a scalar S which measures the departure of the conic from a parabola (Figure 6). Hence, a letter can be represented either by a simple closed polygon or, for letters with holes, two or more polygons. The character is initially converted into the difference between its unique convex hull and the discrepancy with that hull. (Holes are treated the same as other discrepancies.) The process is repeated if the discrepancy region(s) are concave. This process amounts to building a tree whose leaves are convex regions and nodes are set operators [Tor 84]. A character is rendered by traversing its corresponding tree, scan converting each convex region in turn. Since conic sections are invariant under projective maps, this technique can also be applied to the rendering of planar characters embedded in a 3D environment.

Performance estimates have been obtained from a conic representation of a Times Roman font given to us courtesy of Michael Shantz of Sun Microsystems. The average number of convex polygons per character in this set is 8.12, the average number of straight edges per polygon is 4.13, and the average number of conics per character is



Figure 6: Conic font constructed by regions bounded by lines and conic sections.

8.4. This indicates that the average character can be scan-converted with 36 linear coefficients and 8.4 quadratic coefficients. This suggests that each Renderer can scan-convert over 20,000 letters per second. Assuming each character falls into an average of 1.4 rendering regions, 16 Renderers can draw over 225,000 letters per second. The GPs will have difficulty keeping up with this rendering rate, but they can eache coefficients in 2D applications.

7.6 Fast Radiosity

The realism of indoor scenes is greatly enhanced by the radiosity lighting model [Goral 84, Cohen 85], where the lighting contribution due to diffuse interreflection is taken into account. We believe that Pixel-Planes 5 can be used to speed up the calculations needed to compute radiosity. Initial implementations of radiosity required the lighting of all polygons in a scene to be computed before an image is displayed, and this requires many minutes even for simple scenes. The progressive radiosity method [Cohen 88] allows images of progressively better quality to be displayed as light is being distributed through the scene, thus making radiosity more attractive for interactive applications. The most time-consuming step of this process is in computing the form-factors of a polygon patch, that is, how much a patch "sees" of other patches in the scene. This means that a separate visibility calculation must be performed from each patch in a scene. Two common methods used to compute formfactors are tracing rays from a patch and z-buffer rendering onto five image planes that form a hemi-cube at each patch.

We could use Pxpl5's Renderers to compute the five z-buffer images needed for each hemi-cube and then bring this information back to the GPs where the rest of the radiosity calculation can be performed. The quadratic expression tree offers another possibility: one zbuffered image will suffice for the visibility calculation at a patch if the polygons are projected onto a hemisphere. Figure 8 illustrates how the edges of a polygon become sections of ellipses when projected onto a hemisphere and from there onto a plane. To compute such a projected image each edge of a polygon in the scene is scanned using the quadratic expression tree, and then a depth value is computed either by using an approximate depth or by storing special constants at each pixel [Goldfeather 89]. An identifying number for the polygon is stored at all pixels where the polygon is visible. A completed hemisphere image is sent to a GP which uses the image to compute the form-factors, and then this information is used to compute the colors at vertices of the patches in the scene. A radiositylit scene is then displayed by the regular scan conversion procedure and by interpolating the vertex colors across each polygon patch. Since the resolution within a single Renderer appears to be more than adequate for each projected image, multiple Renderers can be used independently. Each Renderer should be able to process about 100,000 quadrilaterals per second.

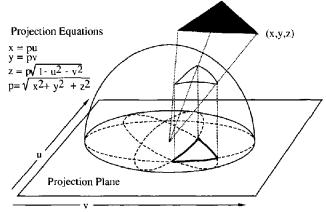


Figure 7: Hemispherical projection of a triangle.





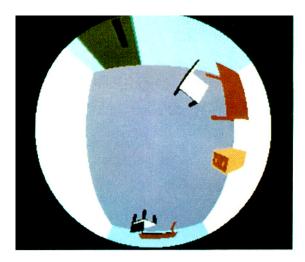




Figure 8: (a) Hemispherical projection of Tebbs and Turk's office, generated on the *Pxpl5* simulator. Estimated rendering time on *Pxpl5* is 2.8 milliseconds. (b) Standard view of the same room as in (a), displayed on *Pxpl4* (radiosity software described in [Airey 89]). The viewpoint in (a) is from the light fixture near the door.

7.7 Volume Rendering

One example of *Pxpl5's* generality is its ability to perform volume rendering. Marc Levoy plans to implement a version of the algorithm described in [Levoy 89a, 89b]. To briefly summarize the algorithm: We begin with a 3D array of scalar-valued voxels. We first classify and shade the array based on the function value and its gradient to yield a color and an opacity for each voxel. Parallel viewing rays are then traced into the array from an observer position. Each ray is divided into equally spaced sample intervals, and a color and opacity is computed at the center of each interval by tri-linearly interpolating from the colors and opacities of the nearest eight voxels. The resampled colors and opacities are then composited in front-to-back order to yield a color for the ray.

For *Pxpl5*, we propose to store the function value and gradient for several voxels in the backing store of each pixel processor. The processor then performs classification and shading calculations for all voxels in its backing store. The time to apply a monochrome Phong shading model at a single voxel using a pixel processor is about 1 msec. For a 256x256x256 voxel dataset, each pixel processor

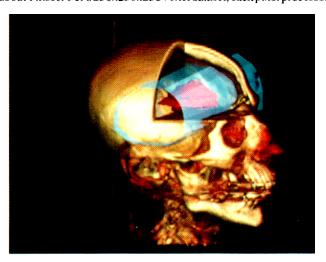


Figure 9: Volume-rendered head from CT data, generated by Marc Levoy on a Sun 4. Estimated rendering time on *Pxpl5* is 1 second.

would be assigned 64 voxels, so the time required to classify and shade the entire dataset would be about 64 msec.

The GPs perform the ray-tracing to generate the image. They are each assigned a set of rays and request sets of voxels from the pixel processors as necessary. The GPs perform the tri-linear interpolation and compositing operations, then transmit the resulting pixel colors to the frame buffer for display. Hierarchical subdivision techniques can be used to reduce the amount of data that must be sent to each graphics processor.

The frame rate we expect from this system depends on which parameters change from frame to frame. Preliminary estimates suggest that for changes in observer position alone, we will be able to generate a sequence of slightly coarse images at 10 frames per second and a sequence of images of the quality of Figure 9 at 1 frame per second.

7.8 Rendering CSG-defined Objects

We and others have developed algorithms to directly render Constructive Solid Geometry (CSG) defined objects on graphics systems with deep frame buffers [Jansen 87, Rossignac 86, Goldfeather 88]. On *Pxpl4* we developed a CSG modeler that displays small datasets at interactive rates.

Pxpl5 provides several opportunities to increase CSG rendering speed: the QEE on Pxpl5 renders curved-surfaced primitives without breaking them into polygonal facets; having more bits per pixel allows surfaces that are used multiple times to be stored and re-used, rather than being re-rendered, greatly increasing performance; finally, the screen-subdivision technique advocated in [Jansen 87] provides a way to take advantage of Pxpl5's multiple Renderers. Pxpl4 interactively renders CSG objects with dozens of primitives (Figure 10). We expect Pxpl5 to interactively render objects with hundreds of primitives.

7.9 Transparency

Several methods for rendering transparent surfaces are possible, given the generality and power of *Pxpl5*. The most promising is to enhance the bin sorting in each GP to generate twice as many bins, one for transparent and another for opaque primitives for each region. The transparent primitives are rendered after all the opaque ones. Since we expect relatively few transparent polygons, each of the



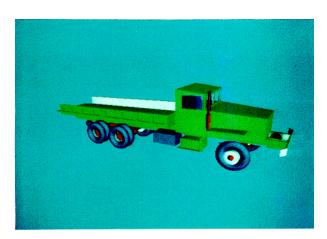


Figure 10: CSG-modeled truck generated on *Pxpl4*. Estimated rendering time on *Pxpl5* is 40 milliseconds.

"transparent" bins can be sorted from back to front and rendered by simple composition. For difficult cases, in which a cluster of transparent polygons cannot be sorted in z (as in a basket-weave of transparent strips), multiple z values can be stored at each pixel to control the compositing step. With this approach, difficult primitives may need to be sent to Renderers several times to ensure correct blending.

8. Current Status of Pxpl5 (April 1989)

Of the three custom CMOS VLSI chips being designed, the backingstore interface chip is being tested and the processor-enhanced memory chip is in fabrication. Layout of the third chip, the Renderer controller, is nearly complete. Detailed simulation of the board-level logic design is well along, and PCBs are being designed. A small version of the Ring Network with a pair of Graphics Processors is expected to become operational by late summer, with a complete system running by year's end. On the software front, a high-level language porting base is running simple code. The Renderer simulator is yielding useful images.

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