

CS4402 Constraint Programming

The B0mbastic Modelling Problem

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1 Introduction

B0mbastic is a Capcom video game which involves pushing dice on a grid into certain configurations In this practical we take an abstraction of this game, modelling it in Essence Prime using the Savile Row tool and writing constraints to the problem.

The model and constraints are then run against a set of parameter files with different processing options in Savile Row to evaluate the performance of the model and explore the effects of heuristics and optimisations of the tool.

2 Design and Implementation

An initial model was created to pass all tests from the given parameter files with little thought for efficiency. Afterwards, small changes were made to try and optimise the model and improve the time taken and reduce the number of solver nodes to search.

2.1 Initial model

2.1.1 Initial and goal states

There are three sets of state variables that need to be set up as the initial states: the avatar's position, the locations of the blocks and the cells of the grid.

```
$ Avatar's initial position
    avatarCurrentRow[0] = avatarInitRow,
    avatarCurrentCol[0] = avatarInitCol,
    $ Initial locations for blocks
5
6
    forall block : int(1..numBlocks) .
       blocksCurrentRow[0,block] = blocksInitRow[block] /\
8
       blocksCurrentCol[0,block] = blocksInitCol[block],
9
10
   $ Initial cells of grid
11
    forall row: int(1..r).
12
       forall col : int(1..c)
13
           gridCurrent[0,row,col] = gridInit[row,col],
```

Listing 1: Constraints for setting initial state variables

This sets all current decision variables for step 0 based on the given init parameter variables. All further constraints will be based on these current matrices and their values. Next is the constraint for the goal state.

```
1  $ All blocks are in a goal
2  forall block : int(1..numBlocks) .
3   exists goal : int(1..numBlocks) .
```

```
blocksCurrentRow[steps,block] = blocksGoalRow[goal] /\
blocksCurrentCol[steps,block] = blocksGoalCol[goal],
```

Listing 2: Constraints for the goal state

Because it does not matter which blocks is pushed into which goal, we can say that for every block there must exist a goal it is in. This combined with the constraint that blocks cannot be in the same position means each block must be in a different goal.

2.1.2 Invalid states

Next are the constraints for invalid states of the game. This restricts the model to not have states such as having the avatar and a block be in the same position.

```
$ Avatar current row/col cannot be on dead cells
1
2
    forall step : int(0..steps) .
3
       forall row : int(1..r)
4
           forall col : int(1..c) .
5
               gridCurrent[step,row,col] = 0
                  -> avatarCurrentRow[step] != row \/
6
7
                     avatarCurrentCol[step] != col,
8
9
10
    $ Blocks and avatar cannot share same cell
    forall step : int(0..steps) .
11
12
       forall block : int(1..numBlocks) .
13
           avatarCurrentRow[step] != blocksCurrentRow[step,block] \/
14
           avatarCurrentCol[step] != blocksCurrentCol[step,block],
15
    $ Block cannot be on dead cells
16
17
    forall step : int(0..steps) .
18
       forall block : int(1..numBlocks) .
19
           forall row: int(1..r).
20
           forall col : int(1..c) .
21
               gridCurrent[step,row,col] = 0
22
                  -> blocksCurrentRow[step,block] != row \/
23
                     blocksCurrentCol[step,block] != col,
24
25
    $ Blocks cannot share same cell
26
    forall step : int(0..steps) .
27
       forall checkBlock : int(1..numBlocks) .
28
           forall otherBlock : int(1..numBlocks) .
29
               checkBlock != otherBlock ->
30
                  blocksCurrentRow[step, checkBlock] !=
                       blocksCurrentRow[step, otherBlock] \/
31
                  blocksCurrentCol[step, checkBlock] !=
                       blocksCurrentCol[step, otherBlock],
```

Listing 3: Constraints to prevent invalid game states

All these constraints are quite similar and simply deal with not allowing the avatar or any blocks to share position or be in dead cells. An \vee is used instead of an \wedge because TODO

2.1.3 Movement

Now for movement. We need to ensure that if the avatarCurrentRow and avatarCurrentCol have different positions in different steps (i.e the avatar has moved its position), then moveRol and moveCol must be updated. Furthermore, the movement cannot be more than one step vertically or horizontally and not diagonally and there cannot be no movement every turn.

```
$ Update moveRow/moveCol for avatar movement
forall step: int(1..steps).

moveRow[step] = avatarCurrentRow[step] - avatarCurrentRow[step-1]
//
moveCol[step] = avatarCurrentCol[step] - avatarCurrentCol[step-1],
```

Listing 4: Updating moveRow and moveCol

Updating moveRow and moveCol works as the game grid is indexed in order both row-wise and column-wise. To explain easily, we can rearrange the formula to be as follows:

```
1 avatarCurrentRow[step] = moveRow[step] + avatarCurrentRow[step-1]
2 avatarCurrentCol[step] = moveCol[step] + avatarCurrentCol[step-1]
```

This intuitively says that the avatar's current position is its previous position plus the value of its movement. This works the same for a negative value of moveRow/moveCol as that is just moving in the other direction.

Listing 5: Prevent diagonal movement and force movement every turn

The second constraint restricts both diagonal movement and forces the avatar to move every turn. This works because the absolute value of moveRow and moveCol is how much the avatar has moved by. To move diagonally, the sum of moveRow and moveCol must be at least 2, as one has to move at least one row and column. Additionally, the avatar must move every turn with this constraint as the sum is equal to 1, so moveRow and moveCol cannot both be 0 on each turn. This also constrains the avatar to only move a distance of 1 each turn.

Next, the blocks must be pushed by the avatar must be moved. To do this, two constraints were used.

```
$ If block has moved, avatar must have moved into block's previous
        location
2
    forall step : int(1..steps) .
3
       forall block : int(1..numBlocks) .
4
           blocksCurrentRow[step-1,block] != blocksCurrentRow[step,block] \/
5
           blocksCurrentCol[step-1,block] != blocksCurrentCol[step,block] ->
               avatarCurrentRow[step] = blocksCurrentRow[step-1,block] /\
               avatarCurrentCol[step] = blocksCurrentCol[step-1,block],
8
9
    $ If avatar moved into block, block move same direction
   forall step : int(1..steps) .
10
       forall block : int(1..numBlocks) .
11
           avatarCurrentRow[step] = blocksCurrentRow[step-1,block] /\
12
13
           avatarCurrentCol[step] = blocksCurrentCol[step-1,block] ->
14
               blocksCurrentRow[step,block] = blocksCurrentRow[step-1,block]
                   + moveRow[step] /\
15
               blocksCurrentCol[step,block] = blocksCurrentCol[step-1,block]
                   + moveCol[step],
```

Listing 6: Constraints for moving blocks

The first checks if a block has moved on the next step. If the block has moved, then the avatar must have moved into the block's old position as that is the only way blocks can move. However, just this constraint is not enough as it doesn't say anything about how to move the block. The second constraint moves the block by adding moveRow and moveCol to blocksCurrentRow and blocksCurrentCol respectively. This works as moveRow and moveCol directly represent the direction of the avatar's movement and blocks must be pushed in the same direction. We do not have to worry about pushing blocks into dead cells as previous constraints do not allow that to happen.

2.1.4 Grid and ice

Finally, we have to make sure than none of the grid changes unless it is ice and it was stepped on.

```
$ Grid O and 2s always stay the same
1
2
    forall step : int(1..steps) .
3
       forall row : int(1..r)
4
           forall col : int(1..c) .
5
               gridCurrent[step-1,row,col] != 1 ->
6
                   gridCurrent[step,row,col] = gridCurrent[step-1,row,col],
8
    $ Ice becomes dead cell
    forall step : int(1..steps) .
10
       forall row: int(1..r).
11
           forall col : int(1..c) .
12
               avatarCurrentRow[step-1] = row /\
13
               avatarCurrentCol[step-1] = col /\
```

```
14 gridCurrent[step-1,row,col] = 1 ->
15 gridCurrent[step,row,col] = 0,
```

Listing 7: Constraints for grid cells

The first constraint here ensures 0s and 2s never change, however this doesn't take into account the 1s that need to stay the same as long as the avatar has not stepped on them yet.

Listing 8: Additional constraint to prevent ice cells from changing

For this constraint, in addition to the grid of the previous step having to be an ice cell (gridCurrent[step-1,row,col] = 1), the avatar must also not have stepped on the cell in the previous turn. Only then should the ice cells stay the same.

2.2 Model improvements

After some testing and initial results, improvements to the original model were made that substantially reduced the number of solver nodes.

2.2.1 Direct row/col

In a few cases, the constraints in the initial model had to loop through all steps, rows and columns, for example to check the avatar is not on a dead cell. This could be simplified to directly use the avatar's current row and column as an index rather than check every combination of step, row and col.

```
$ Avatar current row/col cannot be on dead cells
1
2
    forall step : int(0..steps) .
3
       forall row: int(1..r).
4
           forall col: int(1..c).
5
               gridCurrent[step,row,col] = 0 ->
6
                  avatarCurrentRow[step] != row \/
7
                  avatarCurrentCol[step] != col,
8
9
    $ Optimisation
10
    forall step : int (0..steps) .
11
       gridCurrent[step, avatarCurrentRow[step], avatarCurrentCol[step]] !=
```

Listing 9: Example of optimising number of constraints by directly indexing with avatarCurrentRow and avatarCurrentCol.

Other constraints of this pattern, such as checking a block on a dead cell were all changed the same way.

3 Experimentation

The constraint models were tested on the given parameter files and the results of the .info files taken. Except for the very first parameter file, the parameter files come in pairs of the same "problem". We will refer to these as the same problem as the grid, blocks and goals are all the same, with the only difference between the instances being the number of steps the avatar can take. The first of each pair always has not enough steps to find a solution while the second of the pair does. For example, files 2_2 and 2_3 are the same problem as they are identical except for the number of steps. This feature will be important remember for our analysis.

The results of running the instances in Savile Row will be displayed and analysed to test differences in optimisation and heuristic options in Savile Row and how the efficiency of the models and the characteristics of problem instances relate to each other. Finally, new instances were created and tested TODO

3.1 Methodology

For the experiments with optimisation and heuristic options in Savile Row, both the initial model and improved model were used. This lets us see if any options can improve the efficiency of the models without manually refining the constraints.

The time taken by the solver is not the only metric to look at, as it is not the same on every run and dependent on the load and speed of the computer running the experiment. The number of solver nodes will also be used as a metric of how well the models perform since this number will always stay the same for the same model and problem instance.

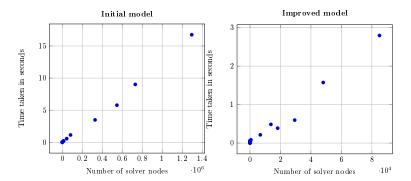


Figure 1: Number of solver nodes plotted against time for both initial and improved models. We can see a strong linear relationship between the time taken and number of solver nodes. This shows both are equivalent metrics for measuring the performance of our model.

To run the experiments, a simple python script was written to run Savile Row automatically with various options and the results gathered. The two fields SolverTotalTime and SolverNodes from the .info file are used as the time taken and number of solver nodes respectively.

3.2 Results

From running both models against all given parameter files, we can see a simple pattern which applies to both the initial model and the improved one. As the problem instances become more complicated, the number of solver nodes and the time taken both increase. The improved model performs much better, taking less time and less nodes, but the pattern is the same.

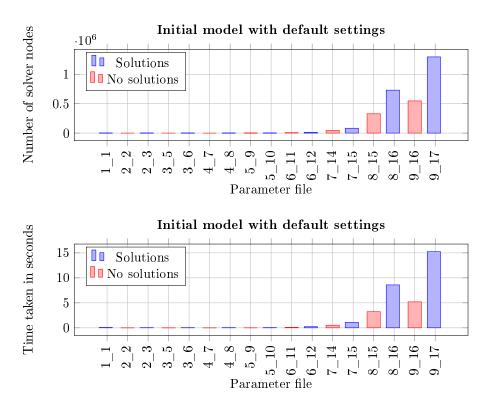


Figure 2: Number of solver nodes and time taken on all given parameters for the initial model. The two different coloured bars represent parameters which either had a solution, or the solver found no solutions.

At first glance, it appears that the instances with solutions always take more time and nodes than an instance of the same problem with no solution. This is not intuitive as logically having no solution means the solver must search through all nodes before stopping while having a solution means a solver can stop on the first solution found (TODO Savile Row default all solutions?). However, it is unfair to make this comparison because the instance with solutions always contain one more step compared to their counterparts. We shall revisit this issue later by defining instances with multiple solutions and running different flags on Savile Row.

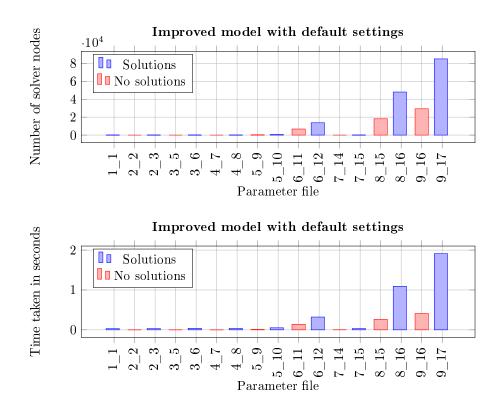


Figure 3: Number of solver nodes and time taken on all given parameters for the improved model

The improved model follows almost the same pattern as initial model, but the number of solver nodes and time taken is decreased significantly. For example the instance 9_17 took over 15 seconds and 1 million solver nodes for the initial model while the improved model only took 2 seconds and 85000 nodes. Interestingly, problem 7 is easier for the improved model to solve.

3.2.1 Optimisations

To find out more about Savile Row and our models, we can specify the level of optimisation.

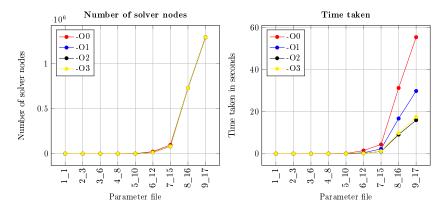


Figure 4: Comparing the effect of optimisation flags on the number of nodes and time taken on the initial model for parameter files with solutions. See appendix TODO for full results.

An interesting result from using different optimisation flags in is the effect it has on the performance of the model. Although it was shown earlier that the number of solver nodes and the time taken by the solver are very similar metrics for measuring the performance of the model, the optimisation flags have a much greater effect on the time taken compared to the number of nodes the solver has to search. With optimisations, the number of solver nodes only decreased by a small fraction. For many parameter files, this number did not change between the three levels of optimisation. However for the time taken by the solver, the time almost halved for most parameter files when comparing -00 and -01. The time again decreased significantly for -02, though there is little difference between -02 and -03.

This shows that parts of the optimisation may be optimising Savile Row like a program, similar to how optimisation flags work in compilers like gcc rather than optimising it as a constraint solver. These optimisations would work well for most general programs, speeding up the run time but does little to improve our model from a constraint programming point of view. That is not to say the optimisations have no effect at all on the constraints. Figure 5 shows that for some parameter files, the optimisation does well enough to eliminate many solver nodes. For example in problems 4 and 7, the -01 optimisation is able to eliminate all but 1 solver node. From the difference shown between the initial model and improved model, it can be seen that the optimisations have a stronger effect on the better model for lowering the number of solver nodes This shows it is important to have a well defined model as optimisations are not enough to overcome an inefficient model and are also more effective for good models.

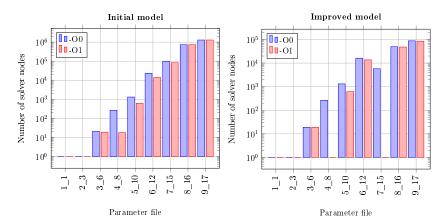


Figure 5: Effect of optimisation flags on number of solver nodes for parameter files with solutions.

3.2.2 Heuristics

Another option to look at is the heuristics that Essence Prime provides. As these are heuristics that must be specified in the model (in BOmbastic.eprime), we are interested to see how they may affect the number of solver nodes searched by the model. Most of the problem instances follow a similar pattern for how they are affected by different heuristics. We shall focus our attention on the 9_17 problem instance as it is the most difficult problem - takes the longest time and most solver nodes.

From figure 6, the most interesting heuristics to take note of are sdf and srf. When using the sdf heuristic, we can see there is a large difference for its effect on the initial model and improved model. With optimisation flags, the heuristic causes the model to perform worse than without any optimisation for the initial model, but it performs exceedingly well for the improved model only with optimisations on. It is impossible to say without knowing what the heuristics do how the models are actually affected, but the more concise constraints of the improved model are likely part of the cause.

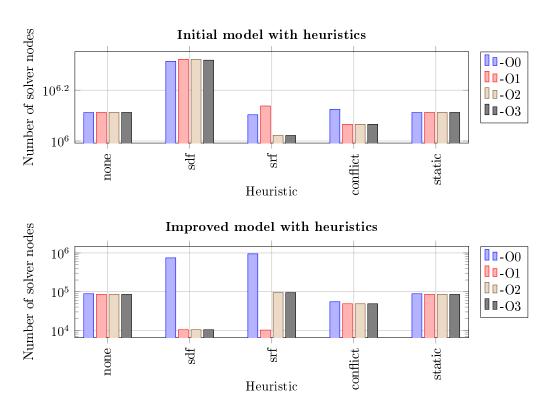


Figure 6: Effect of different heuristics on problem instance 9_17

It should also be noted that in the case of sdf and srf that using the heuristics without optimisations performs worse than not using the heuristics with no optimisations. This suggests some kind of relationship between how the heuristics and optimisations complement or contrast each other. Perhaps the heuristics create a lot of equivalent or symmetrical nodes that optimisations can easily simplify, but over-complicates the search if not simplified.

3.3 Custom instances

4 Conclusion and evaluation

5 Appendix

References

[1] Bombastic (video game). URL: https://en.wikipedia.org/wiki/Bombastic_(video_game).