

## Q2 2 Prep

Heap as an array

$i$ 's left child =  $2i+1$

$i$ 's right child =  $2i+2$

$i$ 's parent =  $(i-1)/2$

Each level is inserted

level at a time

Kahn's (Topological Sort)

- Add indegree of 0 to queue
- Remove from queue and decrement neighbours indegrees  
add to sorted result

Prim's (MST)

- Add random node to visited
- From visited pick minimum edge weight
- Add minimum edge neighbor to visited

Kruskal's (MST)

- Pick minimum weight edge and add to MST solution
- If minimum weight edge connecting two nodes in same tree then ignore

Dijkstra's (Shortest Path)

- Start at start node and add to visited
- Pick shortest path that leads to node not in visited, <sup>update value for node</sup>
- Check adjacent edge of unvisited node to check for shorter path, update value for the unvisited node.
- (a) write distance from source, not local distance



## Problems with Dijkstra's:

1. Doing updates is unnecessary. Compare edges in terms of weight + shortest distance to that edge
2. Fails if there are negative weights

Bellman Ford is Dijkstra's modified for negative weight edges.

Longest path in graph is  $V-1$  length, otherwise there is cycle

$A^*$  is general case of Dijkstra's.

1. add heuristic function value to each edge weight
2. Do Dijkstra's, with heuristics applied to weights

## Floyd-Warshall (Shortest Distance)

dist is a  $V \times V$  matrix initialized to  $\infty$

for each edge  $(u, v)$

$$\text{dist}[u][v] = \text{weight of } (u, v)$$

for each vertex  $v$

$$\text{dist}[v][v] = 0$$

for  $k, 1$  to  $V$

for  $i, 1$  to  $V$

for  $j, 1$  to  $V$

$$\text{if } \text{dist}[i][j] > \text{dist}[i][k] + \text{dist}[k][j]$$

$$\text{dist}[i][j] = \text{dist}[i][k] + \text{dist}[k][j]$$