ML/DL for Everyone with PYTORCH

Lecture 3: Gradient Descent



Call for Comments

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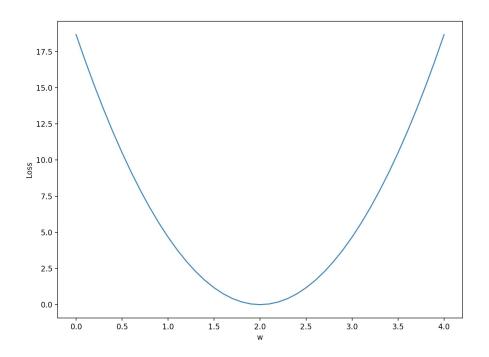
ML/DL for Everyone with PYTORCH

Lecture 3: Gradient Descent



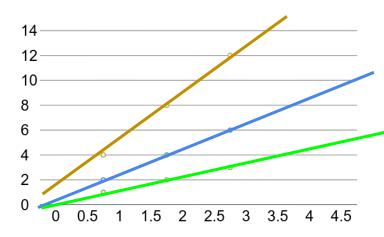
Loss graph

Loss (w=0)	Loss (w=1)	Loss (w=2)	Loss (w=3)	Loss (w=4)
mean=56/3=18.7	mean=14/3=4.7	i mean=0	mean=14/3=4.7	mean=56/3=18.7



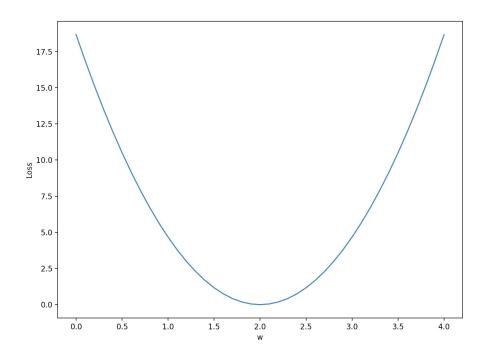
$$loss(w) = rac{1}{N} \sum_{n=1}^{N} (\hat{y_n} - y_n)^2$$

Linear Regression error?



What is the learning: find w that minimizes the loss

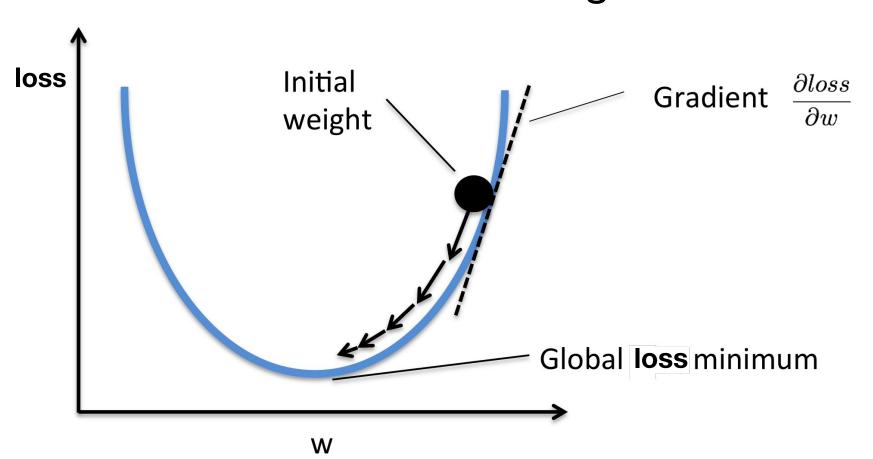
Loss (w=0)	Loss (w=1)	Loss (w=2)	Loss (w=3)	Loss (w=4)
mean=56/3=18.7	mean=14/3=4.7	mean=0	mean=14/3=4.7	mean=56/3=18.7



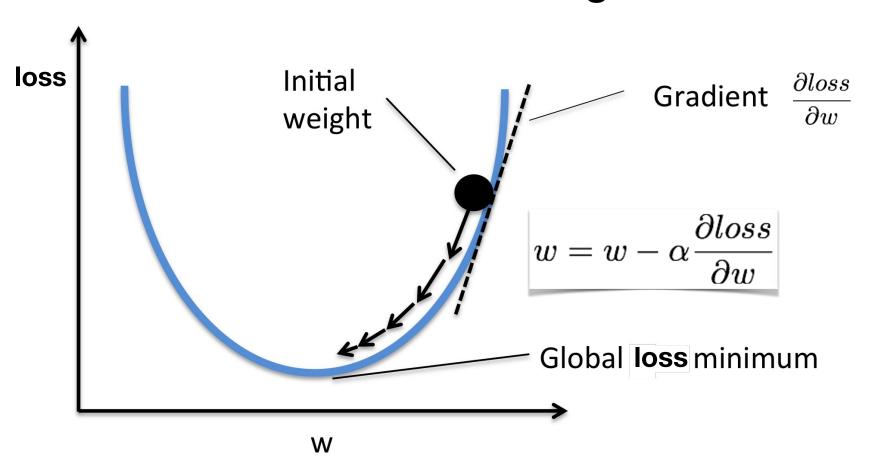
$$loss(w) = rac{1}{N} \sum_{n=1}^{N} (\hat{y_n} - y_n)^2$$

$$\operatorname{arg\,min}_{w} loss(w)$$

Gradient descent algorithm



Gradient descent algorithm



Derivative

$$loss = (\hat{y} - y)^2 = (x * w - y)^2$$

$$w = w - \alpha \frac{\partial loss}{\partial w}$$

Derivative

$$loss = (\hat{y} - y)^2 = (x * w - y)^2$$

$$w = w - \alpha \frac{\partial loss}{\partial w}$$

$$\frac{\partial loss}{\partial w} = ?$$

Derivative $loss = (\hat{y} - y)^2 = (x * w - y)^2$

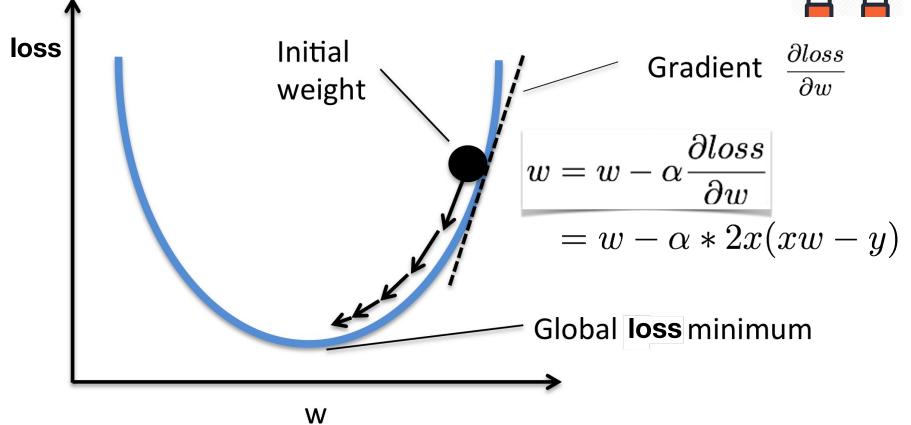
$$\frac{\partial loss}{\partial w} = ?$$

Derivative $loss = (\hat{y} - y)^2 = (x * w - y)^2$

$$\frac{\partial loss}{\partial w} = ? \\ \frac{(xw-y)^2}{\text{Simplify Roots/zeros}} \\ \frac{\frac{\mathrm{d}}{\mathrm{d}w}[f(w)]}{\frac{\mathrm{d}}{\mathrm{d}w}[f(w)]} = f'(w) = \\ \\ \frac{\frac{\mathrm{d}}{\mathrm{d}w}[f(w)] = f'(w)}{\frac{\mathrm{d}}{\mathrm{d}w}[(xw-y)^2]} \\ = 2(xw-y) \cdot \frac{\mathrm{d}}{\mathrm{d}w}[xw-y] \\ = 2\left(x \cdot \frac{\mathrm{d}}{\mathrm{d}w}[w] + \frac{\mathrm{d}}{\mathrm{d}w}[-y]\right)(xw-y) \\ = 2x(xw-y) \\ = 2x(xw-y) \\ = 2x(xw-y)$$

Let's implement!





Data, Model, Loss, and Gradient



```
x_{data} = [1.0, 2.0, 3.0]
y data = [2.0, 4.0, 6.0]
w = 1.0 # a random quess: random value
# our model forward pass
def forward(x):
   return x * w
# Loss function
def loss(x, y):
   y pred = forward(x)
   return (y pred - y) * (y pred - y)
```

```
# compute gradient
def gradient(x, y): # d_loss/d_w
   return 2 * x * (x * w - y)
```

2x(xw-y)

Training: updating weight



```
x_{data} = [1.0, 2.0, 3.0]
y data = [2.0, 4.0, 6.0]
w = 1.0 # a random guess: random value
                                        # Before training
# our model forward pass
def forward(x):
   return x * w
                                        # Training Loop
# Loss function
def loss(x, y):
   y pred = forward(x)
   return (y pred - y) * (y pred - y)
# compute gradient
def gradient(x, y): # d_loss/d_w
                                        # After training
   return 2 * x * (x * w - y)
```

```
print("predict (before training)", 4, forward(4))
for epoch in range(100):
  for x_val, y_val in zip(x_data, y_data):
      grad = gradient(x val, y val)
      w = w - 0.01 * grad
      print("\tgrad: ", x val, y val, grad)
       l = loss(x val, y val)
  print("progress:", epoch, "w=", w, "loss=", 1)
print("predict (after training)", "4 hours", forward(4))
```

```
predict (before training) 4 4.0
      grad: 1.0 2.0 -2.0
      grad: 2.0 4.0 -7.84
      grad: 3.0 6.0 -16.23
progress: 0 w= 1.26 loss= 4.92
      grad: 1.0 2.0 -1.48
      grad: 2.0 4.0 -5.8
      grad: 3.0 6.0 -12.0
progress: 1 w= 1.45 loss= 2.69
      grad: 1.0 2.0 -1.09
      grad: 2.0 4.0 -4.29
      grad: 3.0 6.0 -8.87
progress: 2 w= 1.6 loss= 1.47
      grad: 1.0 2.0 -0.81
      grad: 2.0 4.0 -3.17
      grad: 3.0 6.0 -6.56
progress: 7 w= 1.91 loss= 0.07
      grad: 1.0 2.0 -0.18
      grad: 2.0 4.0 -0.7
      grad: 3.0 6.0 -1.45
progress: 8 w= 1.93 loss= 0.04
      grad: 1.0 2.0 -0.13
      grad: 2.0 4.0 -0.52
      grad: 3.0 6.0 -1.07
progress: 9 w= 1.95 loss= 0.02
predict (after training) 4 hours 7.80
```

Output

(from gradient numeric computation)



```
# Before training
print("predict (before training)", 4, forward(4))
# Training Loop
for epoch in range(100):
   for x_val, y_val in zip(x_data, y_data):
       grad = gradient(x val, y val)
       w = w - 0.01 * grad
       print("\tgrad: ", x_val, y_val, grad)
       1 = loss(x val, y val)
  print("progress:", epoch, "w=", w, "loss=", 1)
# After training
print("predict (after training)", "4 hours", forward(4))
```

Exercise 3-1: compute gradient

$$\hat{y} = x^2 w_2 + x w_1 + b$$
$$loss = (\hat{y} - y)^2$$

$$\frac{\partial loss}{\partial w_1} = ?$$

$$\frac{\partial loss}{\partial w_2} = ?$$

Exercise 3-2: implement

$$\hat{y} = x^2 w_2 + x w_1 + b$$
$$loss = (\hat{y} - y)^2$$

$$\frac{\partial loss}{\partial w_1} = ?$$

$$\frac{\partial loss}{\partial w_2} = ?$$



Lecture 4: Back-propagation