

M0 @PGPname^{†1}

^{†1} transfer to end for full

time at day 01 tuesday, month 02 february, year 2011, hour 10:00 before noon,
at place court 505

time at day 01 tuesday, month 02 february, year 2011, hour 23:59 after noon,
at place <http://mathim.com/ct>

touch last of data at day 31 monday, month 01 january, year 2011, hour 15:58
after noon

Short: (on CHIC 05) how duality?

1. Import. Import reference for all for now until far time:

[tourlakis1] author_George Tourlakis_ short_Lectures in Logic and Set Theory_
refer_Cambridge University Press, (2003), Volume 1, Cambridge studies in advanced mathematics 82_

[tourlakis2] author_George Tourlakis_ short_Lectures in Logic and Set Theory_
refer_Cambridge University Press, (2003), Volume 2, Cambridge studies in advanced mathematics 83_

[aigner1] author_Martin Aigner_ short_Combinatorial Theory_ refer_Springer,
(1997), reprint from (1979), Classics in Mathematics_

[aigner2] author_Martin Aigner_ short_Discrete mathematics_ refer_Springer, (2007),
trans-write from (2004), American Mathematical Society_

[aigner3] author_Martin Aigner_ short_A Course in Enumeration_ refer_Springer,
(2007), Graduate Texts in Mathematics 238_

[borceux1] author_Francis Borceux_ short_Handbook of Categorical Algebra 1_
refer_Cambridge University Press, (1994), Encyclopedia Of Mathematics And Its Applications 50_

[borceux2] author_Francis Borceux_ short_Handbook of Categorical Algebra 2_
refer_Cambridge University Press, (1994), Encyclopedia Of Mathematics And Its Applications 51_

[borceux3] author_Francis Borceux_ short_Handbook of Categorical Algebra 3_
refer_Cambridge University Press, (1994), Encyclopedia Of Mathematics And Its Applications 52_

[gelfand] author_Sergei Izrailevich Gelfand, Yuri I. Manin_ short_Methods of Homological Algebra_ refer_Springer, (2003), Second Edition, Springer Monographs in Mathematics_

[goerss] author_Paul G. Goerss, John F. Jardine_ short_Simplicial Homotopy Theory_ refer_Birkhauser, (2009), Modern Birkhauser Classics_

2. Normal.

2.1. Prophecy. (Thm 1.3.3, ref [borceux1]) Behold internalized Set-valued functor $F : \mathcal{A} \rightarrow \text{Set}$. Deduce a contrast

$$\text{Nat}(\mathcal{A}[\#, -], F) \quad \text{against} \quad F\#$$

as internalization, with commutability in variable F .

Deduce. Behold $f : A \rightarrow B$ and $\gamma : F \Rightarrow G$, deduce, for all $\alpha : \mathcal{A}(A, -) \Rightarrow F$,

$$\begin{aligned} Gf(\gamma_A(\alpha_A(1_A))) &= Gf \circ \gamma_A \circ \alpha_A(1_A) \\ &= \gamma_B \circ \alpha_B \circ \mathcal{A}(A, f)(1_A) \\ &= \gamma_B \circ \alpha_B \circ \mathcal{A}(f, B)(1_B) \\ &= (\gamma \circ (\alpha \circ \mathcal{A}(f, -)))_B(1_B) . \end{aligned}$$

■

3. Duality

3.1. Prophecy. (Ex 1.10.3.b, 1.10.3.d, ref [borceux1]) There is duality $\text{Set}(-, 2) : \text{Set} \rightarrow \text{CBA}$ with link $2 \in \text{Set}, \in \text{CBA}$.

There is duality $\text{FAB}(-, U) : \text{FAB} \rightarrow \text{FAB}$ with link $U \in \text{FAB}, \in \text{FAB}$.

3.2. Prophecy. Behold \mathcal{A} small. Deduce $\text{Fun}(\mathcal{A}, \text{Set})$ is a category of dualities, is the duality for \mathcal{A} .

Deduce. Protos, deduce (Prop 1.5.2, ref [borceux1]) the functor $Y^* : \mathcal{A}^{\text{op}} \rightarrow \text{Fun}(\mathcal{A}, \text{Set})$, $\# \mapsto \mathcal{A}(\#, -)$ is full faithful.

Secondo, given $F : \mathcal{A} \rightarrow \text{Set}$, deduce the category of (universal|non-universal) **coreflections** (copairs) of F along Y^* ,

$$\{\mathcal{A}(A, -) : A \in \mathcal{A}^{\text{op}}\} / F \cong \text{Elts}(\text{Nat}(\mathcal{A}[\#, -], F)) \cong \text{Elts}(F)^{\text{op}} .$$

Then deduce (Thm 2.15.6, ref [borceux1]) the **colimit**

$$\begin{aligned} (F, (\alpha : \mathcal{A}(A, -) \Rightarrow F)_{(A, \alpha) \in \text{Elts}(F)^{\text{op}}}) \\ = \text{colim}_{(A, \alpha : \mathcal{A}(A, -) \Rightarrow F) \in \text{Elts}(F)^{\text{op}}} \mathcal{A}(A, -) \end{aligned}$$

Tertio, given any $Z : \mathcal{A}^{\text{op}} \rightarrow \mathcal{C}$ with \mathcal{C} has small colimits, deduce Z has **extension** W along Y^* with value on F as

$$\begin{aligned} (W(F), (\sigma_{(A,\alpha)}^F : ZA \rightarrow W(F))_{(A,\alpha:\mathcal{A}(A,-)\Rightarrow F) \in \text{Elts}(F)^{\text{op}}}) \\ = \text{colim}_{(A,\alpha:\mathcal{A}(A,-)\Rightarrow F) \in \text{Elts}(F)^{\text{op}}} ZA \end{aligned}$$

and $(\sigma_{(A,1_{\mathcal{A}(A,-)}:\mathcal{A}(A,-)\Rightarrow\mathcal{A}(A,-))}^{\mathcal{A}(A,-)})_{A \in \mathcal{A}^{\text{op}}} : Z \Rightarrow WY^*$ is iso. ■

4. Back to normal.

4.1. Prophecy. (Prop 4.5.14, ref [borceux1]) Behold \mathcal{A} small. Write full subcategory $i : \{\mathcal{A}(A, -) : A \in \mathcal{A}\} \subseteq \text{Fun}(\mathcal{A}, \text{Set})$. Deduce the functor (in larger Grothendieck universe)

$$F \longmapsto \text{Nat}(i(\#), F)$$

is full faithful.

Deduce. Given $\Xi_{\mathcal{A}(A,-)} : \text{Nat}(\mathcal{A}(A, -), F) \rightarrow \text{Nat}(\mathcal{A}(A, -), G)$ commutable transformation in variable $\mathcal{A}(A, -)$, get another cocone $(\Xi_{\mathcal{A}(A,-)}(\alpha) : \mathcal{A}(A, -) \Rightarrow G)_{(A,\alpha:\mathcal{A}(A,-)\Rightarrow F) \in \text{Elts}(F)^{\text{op}}}$ of shape $\text{Elts}(F)^{\text{op}}$ on diagram $(\mathcal{A}(A, -))_{(A,\alpha:\mathcal{A}(A,-)\Rightarrow F) \in \text{Elts}(F)^{\text{op}}}$ at tip G , thus get unique $\gamma : F \Rightarrow G$ with $\gamma \circ \alpha = \Xi_{\mathcal{A}(A,-)}(\alpha)$ for all $(A, \alpha : \mathcal{A}(A, -) \Rightarrow F) \in \text{Elts}(F)^{\text{op}}$. ■

5. ?[\mathcal{A} algebraic | localic]

5.1. Reductions:

5.2. pre-Prophecy. (Prop 6.1.2, Prop 6.1.4, ref [borceux1]) Behold \mathcal{A} with finite limits. Deduce the reduction (hold that whole commutability of filtered colimits with finite limits is not lacked)

$$F : \mathcal{A} \rightarrow \text{Set} \text{ preserves finite limits} \iff \text{Elts}(F)^{\text{op}} \text{ is finitely-filtered}$$

(“ \rightarrow ” holds \mathcal{A} with finite limits) and the reduction to $\text{Fun}(\mathcal{A}, \text{Set})$:

$$\begin{aligned} F : \mathcal{A} \rightarrow \mathcal{B} \text{ preserves finite limits} \\ \iff \forall B \in \mathcal{B} \quad \text{Elts}(\mathcal{B}(B, F-)) : \mathcal{A} \rightarrow \text{Set})^{\text{op}} \text{ is finitely-filtered} \end{aligned}$$

(“ \rightarrow ” holds \mathcal{A} with finite limits).

5.3. pre-Prophecy. (Exe 3.9.2, ref [borceux1]) Deduce the reduction to $\text{Fun}(\mathcal{A}, \text{Set})$:

$$\begin{aligned} F : \mathcal{A} \rightarrow \mathcal{B} \text{ has a left adjoint} \\ \iff \forall B \in \mathcal{B}, \quad \mathcal{B}(B, F-) : \mathcal{A} \rightarrow \text{Set} \text{ is representable} \\ \text{(some orthogonality) } \theta_{-,B} : \mathcal{A}(|G|B, -) \cong \mathcal{B}(B, F-) . \end{aligned}$$

5.4. \mathcal{A} algebraic:

5.5. Prophecy. (Ex 5.2.2.c, ref [borceux2]) If \mathcal{A} small with finite limits (saturated), able to name $\text{Lex}(\mathcal{A}, \text{Set})$ locally finitely-presentable.

5.6. Prophecy. (Prop 3.8.12, Thm 5.2.7, ref [borceux2]) If \mathcal{M} locally finitely-presentable category (for example, of algebras $\text{Mod}_{\mathcal{T}}$ with $\mathcal{T} = \{T^0, T^1, \dots, T^n, \dots\}$ non-saturated), deduce small, stable under finite limits (saturated, dense) \mathcal{A} with \mathcal{A}^{op} equivalent to the full subcategory of \mathcal{M} of all finitely-presentable objects and with \mathcal{M} is equivalent to $\text{Lex}(\mathcal{A}, \text{Set})$.

5.7. \mathcal{A} localic:

5.8. Prophecy. (Sec 3.3, Prop 3.4.16, ref [borceux3]) Behold \mathcal{A} small. If \mathcal{A} localic with (transfinitely built Grothendieck saturated) coverings \mathcal{L} , deduce able to name flat (exact) orthogonal subcategory $\Sigma\Sigma \dashv i : \text{Sh}(\mathcal{A}^{\text{op}}, \mathcal{L}) \subseteq \text{Fun}(\mathcal{A}^{\text{op}}, \text{Set})$ with $\eta_F^C : F(C) \subseteq \Sigma(F)(C) = \text{colim}_{R \in \mathcal{L}(C)} \text{Nat}(R, F)$ and with $(\Sigma\Sigma(\mathcal{A}(\#, A)))_{A \in \mathcal{A}}$ family of finitely-presentable generators in $\text{Sh}(\mathcal{A}, \mathcal{L})$.

5.9. Prophecy. (Prop 3.5.4, ref [borceux3]) Behold \mathcal{A} small. If \mathcal{M} flat (exact) orthogonal subcategory of $\text{Fun}(\mathcal{A}^{\text{op}}, \text{Set})$, deduce localic \mathcal{A} with (Grothendieck saturated) coverings \mathcal{L} with $\mathcal{M} = \text{Sh}(\mathcal{A}, \mathcal{L})$.

5.10. Search|query|question. ?[coherence in functor categories], then ?[algebraic|localic].

6. Other, non-ordered.

6.1. Th. 2.8.1. limits = products + equalizers: Given \mathcal{D} small, diagram $F : \mathcal{D} \rightarrow \mathcal{C}$ and product $(p'_D : \prod_{D \in \mathcal{D}_0} FD \rightarrow FD)_{D \in \mathcal{D}_0}$, deduce $(M, (p'_D m : M \rightarrow FD)_{D \in \mathcal{D}_0})$ is cone on $F \xleftarrow{\quad} (M, m : M \rightarrow \prod_{D \in \mathcal{D}_0} FD)$ is cone on parallel pair $\langle p'_{t(f)} \rangle_{f \in \mathcal{D}_1}, \langle Ff \circ p'_{s(f)} \rangle_{f \in \mathcal{D}_1} : \prod_{D \in \mathcal{D}_0} FD \rightrightarrows \prod_{f \in \mathcal{D}_1} F(t(f))$.

6.2. Prop. 2.8.2. finite limits = 1 + binary products + equalizers, and binary products + equalizers = binary products + pullbacks.

6.3. Prop. 2.9.4. $\mathcal{C}(C, -)$ preserves limits: Given diagram $F : \mathcal{D} \rightarrow \mathcal{C}$ and $q_D(m) : C \rightarrow FD$ commutable in variable D , deduce factorization through limit $(p_D : L \rightarrow FD)_{D \in \mathcal{D}}$ of F as $\forall m \quad q_D(m) : C \xrightarrow{\exists! q(m)} L \xrightarrow{p_D} FD$.

6.4. Prop. 2.9.9. $F : \mathcal{A} \subseteq \mathcal{B}$ full faithful \rightarrow “ $\exists!$ ” is liftable, so reflects limitativeness of cones in \mathcal{A} .

6.5. Sec 2.10. Absolute colimitativeness = colimitativeness is equational enough for all functors.

6.6. Sec 2.11. Final functors = concentration|reduction of whole limitativeness to limitativeness on the final part of any diagram.

6.7. Prop 2.12.1 Commutability of limits: Behold \mathcal{A} complete and \mathcal{C}, \mathcal{D} small and $F : \mathcal{C} \times \mathcal{D} \rightarrow \mathcal{A}$. Protos, refer to 6.10 below or Sec 2.14 ref [borceux1]. Deduce

$$\begin{aligned} \lim_C \lim_D F(C, D) &= \left(\text{tip} \lim_C \lim_D^{\mathcal{A}} F(C, D), \right. \\ &\quad \left. \text{tip} \lim_C \lim_D^{\mathcal{A}} F(C, D) \xrightarrow[\text{proj}_C^{\lim_D F[-, D]}]{} \lim_D F(C, D) \right) \\ &\xleftarrow{\sim} \left(\lim_D^{\mathcal{A}} \text{tip} \lim_C F(C, D), \right. \\ &\quad \left. \lim_D^{\mathcal{A}} \text{tip} \lim_C F(C, D) \xrightarrow[\lim_D \text{proj}_C^{F(-, D)}]{} \lim_D F(C, D) \right) \end{aligned}$$

with

$$\begin{aligned} &\left(\text{tip} \text{tip} \lim_C \lim_D^{\mathcal{A}} F(C, D), \right. \\ &\text{tip} \text{tip} \lim_C \lim_D^{\mathcal{A}} F(C, D) \xrightarrow[\text{tip} \text{proj}_C^{\lim_D F[-, D]}]{} \text{tip} \lim_D F(C, D) \xrightarrow[\text{proj}_D^{F(C, \#)}]{} F(C, D) \Big) \\ &\xrightarrow{\sim} \left(\text{tip} \lim_C \text{tip} \lim_D F(C, D), \right. \\ &\text{tip} \lim_C \text{tip} \lim_D F(C, D) \xrightarrow[\text{proj}_C^{\text{tip} \lim_D F[-, D]}]{} \text{tip} \lim_D F(C, D) \xrightarrow[\text{proj}_D^{F(C, \#)}]{} F(C, D) \Big) \end{aligned}$$

6.8. Prop 2.13.4 Commutability of finitely-filtered colimits with finite limits for all functors. Behold small filtered \mathcal{C} and finite \mathcal{D} and $F : \mathcal{C} \times \mathcal{D} \rightarrow \text{Set}$. Deduce

$$\begin{aligned} \text{colim}_C \lim_D F(C, D) &= \left(\lim_D F(C, D) \xrightarrow[\text{inj}^{\lim_D F[-, D]}]{} \text{tip} \text{colim}_C \lim_D F(C, D), \right. \\ &\quad \left. \text{tip} \text{colim}_C \lim_D F(C, D) \right) \\ &\xrightarrow{\sim} \left(\lim_D F(C, D) \xrightarrow[\lim_D \text{inj}_C^{F(-, D)}]{} \lim_D \text{tip} \text{colim}_C F(C, D), \right. \\ &\quad \left. \lim_D \text{tip} \text{colim}_C F(C, D) \right) \end{aligned}$$

6.9. Sec 2.14. Universal colimitativeness = preservation of colimitativeness after pullback at the tip.

6.10. Prop 2.15.1 Commutability of evaluation with limit: Hold that evaluation $\text{ev}(?, -)$, with $\text{ev}(F, x) = Fx$, F functor, x object or arrow, is able to act on cones substituted for both variables. Behold $F : \mathcal{D} \rightarrow \text{Fun}(\mathcal{C}, \mathcal{A})$ with \mathcal{C} and \mathcal{D} small. Deduce

$$\left(\lim_{D \in \mathcal{D}} (F(D)) \right) (-) = \lim_{D \in \mathcal{D}} \left(F(D)[-] \right)$$

if any one side is present.

6.11. Prop 2.15.5. $Y_* : - \mapsto \mathcal{C}(\#, -)$ preserves limits.

6.12. Prop 3.3.1. Behold $F : \mathcal{A} \rightarrow \mathcal{B}$ and $B \in \mathcal{B}$. Deduce

$$\exists \alpha : B \rightarrow FL \quad \text{with} \quad \left((L, \alpha), (p_{(A,b)} : (L, \alpha) \rightarrow (A, b))_{(A,b) \in \text{Elts}(\mathcal{B}(B, F-))} \right)$$

if and only if

$$\begin{aligned} \left(L, (p_{(A,b)} : L \rightarrow A)_{(A,b) \in \text{Elts}(\mathcal{B}(B, F-))} \right) & \quad \text{is limit and} \\ \left(FL, (Fp_{(A,b)} : FL \rightarrow FA)_{(A,b) \in \text{Elts}(\mathcal{B}(B, F-))} \right) & \quad \text{is limit.} \end{aligned}$$

6.13. Prop 3.4.1. Behold $G \dashv F : \mathcal{A} \rightarrow \mathcal{B}$ with $\varepsilon : GF \rightarrow 1_{\mathcal{A}}$. Deduce

$$\begin{aligned} F \text{ full faithful} & \rightarrow F\varepsilon_A \circ FF^{-1}\eta_{FA} = F1_A \text{ and} \\ & F(F^{-1}\eta_{FA} \circ \varepsilon_A) \circ \eta_{FA} = \eta_{FA}, \\ & \leftrightarrow \varepsilon_A \text{ iso} \end{aligned}$$

and

$$\varepsilon \text{ iso} \rightarrow F_{A,A'} = \theta_{A',FA} \circ \mathcal{A}(\varepsilon_A, A') \text{ bijection.}$$

6.14. Prop 3.5.3. Behold $r \dashv i : \mathcal{A} \subseteq \mathcal{B}$ full faithful. Deduce if $H : \mathcal{D} \rightarrow \mathcal{A}$ and $(L, (p_D : L \rightarrow HD)_{D \in \mathcal{D}})$ limit in \mathcal{B} , then the iso $\eta_L^{-1} : rL \rightarrow L$ is held as factorization, then reflect limitativeness in \mathcal{B} to limitativeness in \mathcal{A} .

6.15. Prop 3.5.4. Behold $r \dashv i : \mathcal{A} \subseteq \mathcal{B}$ full faithful. Deduce if $H : \mathcal{D} \rightarrow \mathcal{A}$ and $(L, (s_D : HD \rightarrow L)_{D \in \mathcal{D}})$ colimit in \mathcal{B} , then reflect colimitative cocone in \mathcal{B} to get $(rL, (rs_D \circ \varepsilon_{HD}^{-1} : HD \xrightarrow{\sim} rHD \rightarrow rL)_{D \in \mathcal{D}})$ colimitative cocone in \mathcal{A} .

6.16. Prop 3.7.5. Behold $F : \mathcal{A} \rightarrow 1$ and $G : \mathcal{A} \rightarrow \mathcal{C}$, arbitrary \mathcal{A} . Hold $\text{Fun}(1, \mathcal{C}) = \left(\{\Delta L : L \in \mathcal{C}\}, \{\Delta f \mid f : L \rightarrow L' \text{ in } \mathcal{C}\} \right)$. Deduce colimitative cocone $(\Delta L, \alpha : G \rightarrow \Delta L)$ on G is left Kan extension of G along F .

6.17. Prop 3.7.6. Deduce

$$F : \mathcal{A} \rightarrow \mathcal{B} \text{ (of small categories) has right adjoint } G$$

$$\longleftrightarrow \quad \forall L : \mathcal{A} \rightarrow \mathcal{C} \quad \text{Lan}_F L \text{ exists and } L \circ \text{Lan}_F 1_{\mathcal{A}} = \text{Lan}_F L$$

because of rewrite

$$(\exists G)(\exists \eta : 1_{\mathcal{A}} \rightarrow GF) \left(\forall A \quad (FA, \eta_A) \text{ initial pair of } A \text{ along } G \right),$$

$$\longleftrightarrow \quad \exists (G, \eta : 1_{\mathcal{A}} \rightarrow GF) \left((G, \eta) \text{ is initial pair of } 1_{\mathcal{A}} \text{ along } {}^*F \text{ and} \right.$$

$$\left. \forall L : \mathcal{A} \rightarrow \mathcal{C} \quad (LG, L\eta) \text{ is initial pair of } L \text{ along } {}^*F \right).$$

6.18. Th. 3.7.2. Behold $F : \mathcal{A} \rightarrow \mathcal{B}$, $G : \mathcal{A} \rightarrow \mathcal{C}$ with \mathcal{A} small, \mathcal{C} cocomplete. Deduce left Kan extension K of G as $(KB, (s_{(A,b)}^B : GA \rightarrow KB)_{(A,b) \in \text{Els}(\mathcal{B}(F\#, B))})$ colimit on $(GA)_{(A,b) \in \text{Els}(\mathcal{B}(F\#, B))}$ with $(s_{(A,1_{FA})}^{FA} : GA \rightarrow KFA)_{A \in \mathcal{A}} : G \Rightarrow KF$. If F full faithful, deduce $((A, 1_{FA}), (p_{(A',b)} : (A', b) \rightarrow (A, b))_{(A',b) \in \text{Els}(\mathcal{B}(F\#, FA))})$ is terminal and $s_{(A,1_{FA})}^{FA} = Gp_{(A,1_{FA})} = 1_{GA}$ is iso.

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