Word representations

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Introduction

 Traditional way to represent words as atomic symbols with a unique integer is associated with each word:

Equivalent to represent words as 1-hot vectors:

```
\begin{array}{lll} \mathsf{movie} &=& [1,0,0,0,0] \\ \mathsf{hotel} &=& [0,1,0,0,0] \\ & \dots \\ \mathsf{art} &=& [0,0,0,0,1] \end{array}
```

Introduction

- Implicit assumption: word vectors are an orthonormal basis
 - orthogonal $(x^Ty = 0)$
 - normalized $(x^T x = 1)$
- Problem: Not very informative:
 - Weird to consider "movie" and "movies" as independent entities
 - Or to consider all words equidistant:

$$\|dog - cat\| = \|dog - moon\|$$

Introduction

- Reminder:
 - Word types are element of the vocabulary
 - Word tokens are instances of word types in text
- Here, we want representations for word types

Feature based representation

- Solution: represent words with hand crafted features and relations
- Example of potential features:
 - Morphology: prefix, suffix, stem...
 - Grammar: part of speech, gender, number,...
 - Shape: capitalization, digit, hyphen
- Example of potential relations:
 - synonyms,
 - hypernyms,
 - antonyms...

WordNet

- Lexical database for English (and other) language(s)
- Word types are grouped into synonym sets: synsets ${\tt S09293800} = \{ \textit{ Earth, earth, world, globe } \}$
- Polysemous words: assigned to different synsets ${\tt S14867162} = \{ \textit{ earth, ground } \}$
- Contains glosses for synsets:
 the 3rd planet from the sun; the planet we live on
- Noun/verb synsets: organized in hierarchy, capturing IS-A relation apple IS-A fruit

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- X is a holonym of Y if Y is a part of X:
 car is a holonym of wheel

Limitations of feature based representation

- Requires (a lot of) human annotations
- Subjectivity of the annotators
- does not adapt to new words (languages are not stationary!):

Mocktail, Guac, Fave, Biohacking

were added to Merriam-Webster in 2018

- Existing online taxonomy like WordNet are not always very precise:
 - "Good" synonyms: skillful, practiced, proficient, adept

Distributional hypothesis

"You shall know a word by the company it keeps" Firth (1957)

• Meaning of a word: set of contexts in which it occurs in texts

He handed her her glass of bardiwac.

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- The drinks were delicious: blood-red bardiwac as well as light, sweet Rhenish.
- → bardiwac is a heavy red alcoholic beverage made from grapes

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- count how many times each target word occurs in this context
- build vectors out of (a function of) these context occurrence counts

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- Distributional hypothesis: bridging assumption from distributional representation to semantic representation

- Define what is the context of a word
- count how many times each target word occurs in a certain context
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The whole document

A window of surrounding words

A window of surrounding words after preprocessing

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Source: Foundations of Distributional Semantic Models, Stefan Evert and Alessandro Lenci, 2009.

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The co-occurrence matrix

	leash	walk	run	owner	pet	barked
dog	3	5	2	5	3	2
cat	0	3	3	2	3	0
lion	0	3	2	0	1	0
light	0	0	0	0	0	0
bark	1	0	0	2	1	0
car	0	0	1	3	0	0

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Distributional word representation in a nutshell

- Define what is the context of a word
- count how many times each target word occurs in a certain context
- build vectors out of (a function of) these context occurrence counts

- Goal: Build word vectors from occurence count with their context
- We focus on context as a fixed size window around the word
- Distance between vectors should reflect "similarity" between words
- We use the cosine similarity:

$$\cos(\mathbf{x}, \mathbf{y}) = \frac{\mathbf{x}^{\top} \mathbf{y}}{\|\mathbf{x}\| \|\mathbf{y}\|}$$

	leash	walk	run	owner	pet	barked	the
dog	3	5	2	5	3	2	8
cat	0	3	3	2	3	0	9
lion	0	3	2	0	1	0	6
light	0	0	0	0	0	0	5
bark	1	0	0	2	1	0	0
car	0	0	1	3	0	0	3

ullet Naive approach: takes the row of the co-occurence matrix $oldsymbol{M}$

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Naive approach: takes the row of the co-occurence matrix M

Problems with using the co-occurence matrix **M** directly:

- Co-occurence matrix norm is proportional to corpus size
- Entries associated with frequent words dominate the matrix
- Sensitive to small changes in counts of rare words

• An alternative context weighting is the Mutual Information (MI):

$$MI(i,j) = \log p(i,j) - \log p(i) - \log p(j)$$

- In our case $p(i,j) = \mathbf{M}_{i,j}/n$ and $p(i) = \sum_{ij} \mathbf{M}_{ij}/n$
- The resulting matrix is called the Pointwise Mutual Information (PMI) matrix.

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- → Normalized vector by word counts:

$$\mathbf{Q}_{ij} = rac{\mathbf{P}_{ij}}{\mathbf{P}_{j}\mathbf{P}_{i}}$$
 where $\mathbf{P}_{i} = \sum_{j} \mathbf{P}_{ij} = \sum_{j} \mathbf{P}_{ji}$

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- Sensitive to small changes in counts of rare words
- → take the log to smooth high frequencies:

$$\mathbf{R}_{ij} = \log \mathbf{Q}_{ij}$$

This is the PMI matrix!

Limitations of PMI

• Word pairs with p(a, b) < p(a)p(b) lead to instability in MI

Example

- with context size = 3: p("a","the") << p("a")p("the")
- p("a") = 0.1, p("the") = 0.2
- $p("a","the") = 10^{-5} \rightarrow MI("a","the") = -7.6$
- $p("a","the") = 10^{-9} \rightarrow MI("a","the") = -16.8$
- Small error in estimation of rare events are blown out by log
- Impacts the similarities between words
- An alternative is the Positive PMI (Bullinaria and Levy, 2007):

$$PPMI(x, y) = \max(PMI(x, y), 0)$$

Dimensionality reduction

- The word vectors are the rows of the PMI matrix
- The size of word vector is the size of the vocabulary
- Problems:
 - Requires lot of memory: needs to store in sparse matrix all non-zero co-occurence.
 - large dimensional vectors are hard to handle (e.g. in a text classifier)
 - cannot compare word vectors estimated on 2 different corpora unless they have exactly the same vocabulary!
- Solution: build vectors with fixed predefined size from the PMI matrix

Dimensionality reduction

- PMI does not differentiate between words and context: symmetric matrix
- However PMI matrix **M** is not positive definite
- We build a similarity matrix between words as: $\mathbf{S} = \mathbf{M}\mathbf{M}^T$
- **S** is a symmetric positive definite matrix that measure similarity between words based on PMI
- **Goal** Find a $n \times d$ dimensional matrix \mathbf{X}_d such that:

$$\mathbf{X}_d = \operatorname{argmin}_{\mathbf{Y}} \|\mathbf{S} - \mathbf{Y} \mathbf{Y}^T\|_2^2$$

- X_d's row are word vectors that explain most of the variance of S, and thus M
- Solution: truncated Singular Value Decomposition (SVD)

Truncated Singular Value Decomposition (SVD)

• The SVD of a matrix **A** is:

$$A = U\Sigma V^T$$

where Σ is a diagonal matrix with the singular values, and ${\bf U}$ and ${\bf V}$ are orthonormal basis.

The truncated SVD is:

$$\mathbf{A}_d = \mathbf{U}_d \mathbf{\Sigma}_d \mathbf{V}_d^T$$

 Σ_d is the diagonal matrix formed with the d largest singular value. \mathbf{U}_d is the matrix formed by the d columns of \mathbf{U} corresponding to the d largest singular value.

Dimensionality reduction

- Since **S** is definite positive, $\forall i, \ \lambda_i(\mathbf{S}) \geq 0$
- Apply SVD to S, the matrix of word vectors is:

$$\mathbf{X}_d = \mathbf{U}_d(\Sigma_d)^{1/2}$$

- Each row of X_d is a word vector
- **S** and **M** gives same matrix \mathbf{U}_d and \mathbf{V}_d , and $(\lambda_i(\mathbf{S}))_i = (\lambda_i(\mathbf{M}))_i^2$

Different examples of distributional word representation

We have seen one instance of word vector, but we can vary many parameters:

Linguistic parameters

pre-processing and linguistic annotation - raw text, stemming, POS tagging and lemmatisation, (dependency) parsing, semantically relevant patterns

choice of context - document, sentence, window, dependency relations, etc.

Mathematical parameters

matrix column and row entries - words, document id context weighting (w) - log-frequency, association scores, entropy, etc.

measuring similarity (s) - cosine similarity, Euclidean, Manhattan, Minkowski (p-norm)

dimensionality reduction (r) - feature selection, SVD projection (PCA), random indexing

Source: Foundations of Distributional Semantic Models. Stefan Evert and Alessandro Lenci, 2009.

Different examples of distributional word representation

Latent Semantic Analysis (Landauer and Dumais, 1997)

context documents

matrix word× document id

w log term frequency and term entropy in the corpus

s cosine

r SVD

Hyperspace Analogue to Language (Lund and Burgess, 1996)

context triangular window-based with position as context-typing

function

matrix word× word

w frequency

s Minkowski metric

r dimensions with the highest variance

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Distributional word representation: in a nutshell

- Define what is the context of a word
- count how many times each target word occurs in this context
- → co-occurence matrix M
 - build vectors out of (a function of) these context occurrence counts
- \rightarrow Similarity matrix $\mathbf{S} = \phi(\mathbf{M})$ (e.g., PMI)
 - Reduce dimensionality with SVD
- o matrix of word representation: $\mathbf{X} = \operatorname{argmin}_{\mathbf{Y} \in \mathbb{R}^{n \times d}} \|\mathbf{S} \mathbf{Y} \mathbf{Y}^T\|_2^2$

Limitations of this approach

- Building the co-occurrence matrix: $O(V^2)$ in memory (e.g. on Common Crawl: $V=2\mathrm{M}$)
- Complexity of truncated SVD: $O(d^2V)$
- Inefficient to build a large matrix and reduce it later: Can we do both simultaneously?

Continuous word representations

Learning distributed word representation

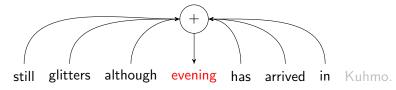
- Directly learning low dimensional vectors
- Moving from count based statistics to machine learning
- Key idea 1 (Collobert and Weston, 2008)
 learning distributed word vectors as a discriminative problem
- Key idea 2 (Mikolov et al., 2013a)
 efficient online training to scale to large dataset
- State-of-the-art model: word2vec by Mikolov et al. (2013a)

Word2vec: the skipgram and cbow models

- word2vec: context is a fixed size window around the word
- Skipgram predict context from the word



Continuous Bag of Word (Cbow) predict word from the context



Word2vec: word vectors as a discriminative problem

• Given a vocabulary of V words and a dataset of N tokens:

$$(w_1,...,w_N) \in \{1,...,V\}^N$$

- Each word i in the vocabulary is associated with a word vector $\mathbf{x}_i \in \mathbb{R}^d$ and a context vector $\mathbf{y}_i \in \mathbb{R}^d$, with d << V
- Denote by X the matrix with the i-th row equal to x; (same for Y)

Skipgram as a discriminative problem

- **Skipgram** predicts each word c in context C_n of n-th token
- Discriminate between correct word in the context against the rest of the vocabulary
- Frame as a minimization problem:

$$\min_{\mathbf{X} \in \mathbb{R}^{V \times d}, \ \mathbf{Y} \in \mathbb{R}^{V \times d}} \quad \frac{1}{N} \sum_{n=0}^{N} \left[\frac{1}{|C_n|} \sum_{c \in C_n} \ell(\mathbf{x}_{w_n}, \mathbf{y}_c) \right]$$

where:

$$\ell(\mathbf{x}, \mathbf{y}) = -\mathbf{x}^T \mathbf{y} + \log \left(\sum_{k=1}^V \exp(\mathbf{y}_k^T \mathbf{x}) \right)$$

is the negative log-softmax function

Cbow as a discriminative problem

- Chow predicts the word associated with the n-th token based on its context Cn
- The context is represented as a Bag-of-Word (BoW)
- Discriminate between the correct word and the rest of the vocabulary
- Frame as a minimization problem:

$$\min_{\mathbf{X} \in \mathbb{R}^{V \times d}, \ \mathbf{Y} \in \mathbb{R}^{V \times d}} \quad \frac{1}{N} \sum_{n=0}^{N} \ell \left(\underbrace{\frac{1}{|C_n|} \sum_{c \in C_n} \mathbf{x}_c, \mathbf{y}_{w_n}}_{\text{Context BoW}} \right)$$

where ℓ is the negative log-softmax

Optimization of word2vec

Gradient descent

$$\mathbf{X}_{t+1} \leftarrow \mathbf{X}_t - \alpha_t \frac{1}{N} \sum_{n=1}^{N} \sum_{c \in C_n} \nabla_{\mathbf{X}} \ell(\mathbf{x}_{w_n}, \mathbf{y}_c)$$

 \rightarrow Requires a pass over dataset for one gradient: O(N)

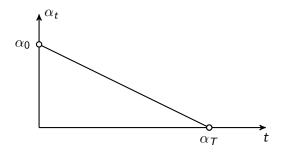
Stochastic gradient descent with predefined sequential scheduler

- loop over the N tokens in dataset, take gradient step at each token
- Repeat process for E epoch. Total number of iteration T = NE
- t-th update:

$$\mathbf{X}_{t+1} \leftarrow \mathbf{X}_t - \alpha_t \nabla_{\mathbf{X}} \sum_{c \in C_n} \ell(\mathbf{x}_{w_n}, \mathbf{y}_c)$$

with
$$n = t/N$$

Optimization of word2vec



Learning rate scheduler $(\alpha_t)_t$

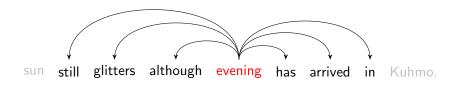
• set α_0 and number of iteration T:

$$\alpha_t = \left(1 - \frac{t}{T}\right)\alpha_0$$

Optimization of word2vec

Hogwild parallelizes this process over *P* processes:

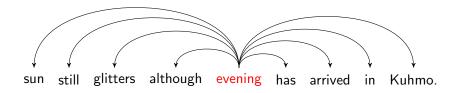
- split dataset in P subsets.
- Read P subsets in parallel.
- Share parameters between processes
- Each process compute a gradient per token and update shared parameters.
- → Update parameters sequentially and in parallel.



- Instead of fixing the window size $|C_n|$, sample it
- Uniform sample w in $\{1, \ldots, w_{max}\}$ and $C_n = 2w$



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- Computing softmax over the whole vocabulary is slow O(V)
- \rightarrow Replace it by negative sampling
 - **Negative sampling** (Skipgram) sample K << V words N_n that does not appear in the context of \mathbf{x}_n and replace softmax by sum of 1-versus-all losses:

$$\ell(\mathbf{x}_{w_n}, \mathbf{y}_c) \leftarrow \sigma(\mathbf{x}_{w_n}, \mathbf{y}_c) + \frac{1}{K} \sum_{k \in N_n} \sigma(-\mathbf{x}_{w_n}, \mathbf{y}_k)$$

where $\sigma(\mathbf{x}, \mathbf{y}) = \log(1 + \exp(-\mathbf{x}^T \mathbf{y}))$ is the negative log-sigmoid function

 Important to sample negatives based on word frequency to match dataset distribution:

$$p_{\text{negative}}(w) \propto \text{freq}^{0.75}(w)$$

Same for cbow

Word2vec: efficient distributed training

- Word frequency in corpora follows a Zipf distribution
- **Zipf distribution** ranked by frequency, each word is *x* times less frequent than previous one.

 $\label{eq:example:proba} \text{Example: proba(the)} = 0.1, \; \text{proba(a)} = 0.05, \; \text{proba(is)} = 0.025....$

- ightarrow a subset of vocabulary (pprox 2k words) covers > 80% of dataset
- \rightarrow 80% of training spent on learning 2k word vectors out of 2M
 - discard words during training based on frequency ($t \in [10^{-5}, 10^{-3}]$):

$$p(exttt{discard} \mid w) = \max\left(0, 1 - \sqrt{\frac{t}{ ext{freq}(w)}}\right)$$

Example of nearest neighbors

Trained on 1B tokens from Wikipedia, dimension 300

moon	score	talking	score	blue	score
mars	0.615	discussing	0.663	red	0.704
moons	0.611	telling	0.657	yellow	0.677
lunar	0.602	joking	0.632	purple	0.676
sun	0.602	thinking	0.627	green	0.655
venus	0.583	talked	0.624	pink	0.612

Word vector analogies

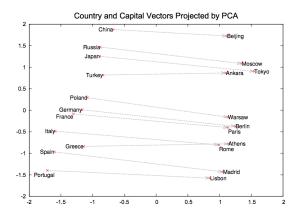


Figure 2: Two-dimensional PCA projection of the 1000-dimensional Skip-gram vectors of countries and their capital cities. The figure illustrates ability of the model to automatically organize concepts and learn implicitly the relationships between them, as during the training we did not provide any supervised information about what a capital city means.

Credit: Mikolov et al. (2013)



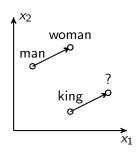
Analogies as intrinsic evaluation of word representation

Word vector analogies:

$$king - man + woman = ?$$

- Frame as a retrieval problem:
- \rightarrow Normalize word embeddings $\mathbf{x}_i \leftarrow \mathbf{x}_i / \|\mathbf{x}_i\|$
- \rightarrow Find the closest vectors w.r.t. I_2 distance:

$$\mathbf{x}_d = \operatorname{argmax}_i (\mathbf{x}_c + \mathbf{x}_a - \mathbf{x}_b)^{\top} \mathbf{x}_i$$



Analogies as intrinsic evaluation of word representation

Semantic analogies:

currency:

```
• capital-common-countries:
Athens: Greece: Helsinki: Finland
```

Japan : yen :: Sweden : krona

• family:
 father : mother :: uncle : aunt

- Syntactic analogies:
 - gram2-opposite: logical: illogical:: clear: unclear
 - gram3-comparative: strong : stronger :: good : better
 - gram5-present-participle: think: thinking:: listen: listening

Analogies as intrinsic evaluation of word representation

	PPMI	PPMI+SVD	Skipgram
Analogies	.552	.554	.694

Figure: Accuracy on the analogy dataset of Mikolov et al. (2013b)

Source: Levy et al. (2015).

Impact of dimension

	100	200	300	400
Semantic	73.7	80.8	82.2	82.6
Syntactic	69.6	74.4	75.0	74.8
Total	71.2	76.9	77.8	77.9

Figure: Accuracy on the analogy dataset of Mikolov et al. (2013b)

• Take home message:

dimension 300 is good enough for most applications

Extensions

Extensions: GloVe (Pennington et al., 2014)

 GloVe (Global Vector) is a word2vec model trained with a different loss:

$$\min_{X,Y,b} \quad \sum_{i, j \in V} f(C_{ij}) \left(\mathbf{x}_i^T \mathbf{y}_j + b_i + b_j - \log C_{ij}\right)^2$$

- $(b_i)_{i \in V}$ are scalars to learn
- C_{ii} co-occurence counts of words i and j in same context
- f reweighting function:

$$f(C) = \min\left(1, \left(C/C_{cutoff}\right)^{3/4}\right)$$

similar to discount factor of word2vec



Extensions: fastText (Bojanowski et al., 2017)

• Represent a word as bag of character *n*-grams:

$$skiing = \{ \text{ `skiing\$, `ski, skii, kiin, iing ing\$} \}$$

• \mathcal{G}_w is the set of *n*-grams appearing in word w.

$$s(w,c) = \sum_{g \in \mathcal{G}_w} \mathbf{g}^{\top} \mathbf{c}.$$

(It includes the word w in the set of n-grams)

- Advantage 1 Get word vectors for out-of-vocabulary words using subwords!
- Advantage 2 Generalize well to text with typos or agglutinative languages

Technical details of fastText

- *n*-grams between 3 and 6 characters
- Hashing to map n-grams to integers in 1 to K
- Same training / sampling procedure as in word2vec
- \rightarrow Less than 2× slower than word2vec skipgram!

Experiments – word analogy (A is to B as C is to ?)

All models trained on Wikipedia:

		sg	cbow	ours
Cs	Semantic Syntactic	25.7 52.8	27.6 55.0	27.5 77.8
DE	Semantic Syntactic	66.5 44.5	66.8 45.0	62.3 56.4
En	Semantic Syntactic	78.5 70.1	78.2 69.9	77.8 74.9
Іт	Semantic Syntactic	52.3 51.5	54.7 51.8	52.3 62.7

Table: Accuracy of our model and baselines on word analogy tasks for Czech, German, English and Italian. We report results for semantic and syntactic analogies separately.

Further Extensions

 Position vectors multiply input word vectors of cbow by position vectors (Mnih and Kavukcuoglu, 2013):

$$\mathbf{h}_C = \frac{1}{|P|} \sum_{p \in P} \mathbf{d}_p \odot \mathbf{x}_{n+c}$$

 \mathbf{d}_p =learnable position vectors. \odot = pointwise multiplication.

Reminder, regular cbow:

$$\mathbf{h}_C = \frac{1}{|P|} \sum_{n \in P} \mathbf{x}_{n+c}$$

Further Extensions

 Phrase vectors pre-processing of dataset to convert with probability, bigrams with high MI into token (Mikolov et al., 2013b):

New York
$$\rightarrow$$
 New_York

Repeat process:

New York University → New_York_University

• Score to merge two tokens:

$$score(w_i, w_j) = \frac{count(w_i w_j) - \delta}{count(w_i) \times count(w_i)}$$

where δ is a discount factor to prevent phrases of infrequent words

→ These extensions are in new fastText vectors (Mikolov et al., 2017)

Evaluation of these extensions

	Semantic	Syntactic	Total
cbow	79	73	76
${\sf cbow} + {\sf phrases}$	82	78	80
${\sf cbow} + {\sf phrases} + {\sf position}$	87	82	85

Models trained on Common Crawl (Mikolov et al., 2017)

Impact of training data

Wikipedia: high quality but small

28 languages with more than 100M tokens

• Hindi: only 39M tokens

Crawl: noisy but larger and more domains

Preprocessing: language id / deduplication / tokenization

anguage	wiki	crawl	language	wiki
German	1.3B	65B	Italian	0.7B
rench	1.1B	68B	Polish	0.4B
apanese	1.0B	92B	Portuguese	0.4B
Russian	0.8B	102B	Chinese	0.4B
Spanish	0.8B	72B	Czech	0.2B

Table: Dataset sizes (number of tokens) for Wikipedia and Crawl.

Impact of training data

Model	Dataset	Analogy	Similarity (RW)	QA
GloVe	Wiki + news	72	0.38	77.7
GloVe	Crawl	75	0.50	78.8
fastText	Wiki + news	87	0.52	78.9
fastText	Crawl	85	0.58	79.8

Results from Mikolov et al. (2017). **Analogy:** accuracy on the Google analogy dataset. **Similarity (RW):** Spearman rank correlation on the Stanford Rare Word dataset. **QA:** F1 score on the SQuAD question answering dataset. Pre-trained word vectors were used to initialize the lookup table of the RNN DrQA model from Chen et al. (2017).

Bias in word vectors

Based on four sets of words:

```
Math: {math, algebra, geometry, calculus, equations, numbers, ...}

Arts: {poetry, art, dance, literature, novel, symphony, drama, ...}

Male: {male, man, boy, brother, he, him, his, son}

Female: {female, woman, girl, sister, she, her, hers, daughter}
```

- Target words: Math and Arts
- Attributes: Male and Female
- Objective: determine if math is more associated to male or female

• Based on reaction time to classify word into category:

Math		Arts
	geometry	

Based on reaction time to classify word into category:

Math Female		Arts Male
	dance	

• Based on reaction time to classify word into category:

Math Male		Arts Female
	de vere	
	dance	

Based on reaction time to classify word into category:

Math Male		Arts Female
	dance	

• Compare reaction time of pairings:

Math/Male and Arts/Female v.s.
Math/Female and Arts/Male

Word embedding association test

Caliskan, Bryson, Narayanan (2017)

- Replicate implicit assocition test with word vectors
- Objective: measure strength of association of four sets of words
- Given a word w and two sets of attribute A and B:

$$s(w, A, B) = \frac{1}{\operatorname{card}(A)} \sum_{a \in A} \cos(w, a) - \frac{1}{\operatorname{card}(B)} \sum_{b \in B} \cos(w, b)$$

measure association of w to attribute.

• Then, given two sets of word X and Z of equal size

$$s(X,Z,A,B) = \sum_{x \in X} s(x,A,B) - \sum_{z \in Z} s(z,A,B)$$

Experiments

Caliskan, Bryson, Narayanan (2017)

- Replicate humans implicit association test results
- Word vectors trained with word2vec on 100B news tokens
- Example of biases:

target words	attributes	р
Flowers vs insects	Pleasant vs unpleasant	10^{-7}
Instruments vs weapons	Pleasant vs unpleasant	10^{-7}
EurAm. vs AfrAm. names	Pleasant vs unpleasant	10^{-8}
Male vs female names	Career vs family	10^{-3}
Science vs arts	Male vs female terms	10^{-2}

Experiments

Caliskan, Bryson, Narayanan (2017)

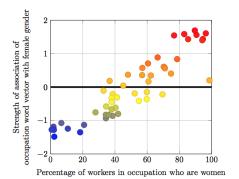


Figure 1: Occupation-gender association. Pearson's correlation coefficient $\rho=0.90$ with $p\text{-value}<10^{-18}$.

Credit: Caliskan, Bryson, Narayanan (2017)

Bias in word vectors

- Word vectors: capture the biases from the data
- Human biases in data implies human biases in word vectors
- Choice of training data: big impact on biases!
- Careful when using word vectors: biased classifier/system
- But, might be useful to study biases in large corpora!

Limitations

• Antonyms:

small	score	fast	score	bad	score
large tiny	0.807 0.798	Fast super-fast	0.668 0.646	good terrible	0.751 0.731
smallish	0.730	slow	0.619	horrible	0.718
smalll largish	0.722 0.693	faster quick	0.603 0.578	lousy baaaad	0.708 0.702

• High similarity:

car	score
cars	0.733
vehicle	0.727
automobile	0.702
Car	0.659
truck	0.647

car	score
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Features of Similarity

Amos Tversky Hebrew University Jerusalem, Israel

- Tversky (1977): metric assumption of human similarity?
- Human similarity: no symmetry

Human similarity: no triangular inequality

$$d(ball, moon) + d(moon, light) \le d(ball, light)$$

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