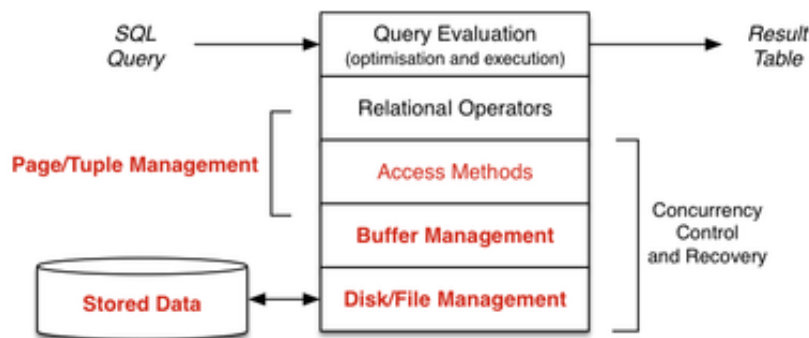


Week 03 Lectures

Pages

Page/Tuple Management

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Some terminology

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Terminology used in these slides ...

- Record = sequence of bytes stored on disk (data for one tuple)
- Tuple = "interpretable" version of a Record in memory
- Page = copy of page from file on disk
- PageId = index of Page within file = **pid**
- $\text{pageOffsetInFile} = \text{pid} * \text{PAGESIZE}$
- TupleId = index of record within page = **tid**
- RecordId = (PageId, TupleId) = **rid**
- $\text{recOffsetInPage} = \text{page.directory}[\text{tid}].\text{offset}$
- Relation = descriptor for open relation

Reminder: Views of Data

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Abstract view: sequence of tuples

Table	<i>tup1, tup2, tup3, tup4, tup5, tup6, tup7, tup8, tup9, tup10, tup11, tup12,</i>
-------	---

Concrete view: sequence of pages

	[0]	[1]	[2]	[3]	
Table	rec1, rec2, rec3	rec4, rec5	rec6, rec7, rec8, rec9	rec10, rec11, rec12

Each *tuple* is represented by a *record* in some *page*

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Page Formats

A Page is simply an array of bytes (`byte[]`).

Want to interpret/manipulate it as a collection of Records.

Typical operations on pages and records:

- `buf = request_page(rel, pid)` ... get page via its PageId
- `rec = get_record(buf, tid)` ... get record from buffer
- `rid = insert_record(rel, pid, rec)` ... add new record
- `update_record(rel, rid, rec)` ... update value of record
- `delete_record(rel, rid)` ... remove record

Note: `rid = (PageId, TupleId)`, `rel` = open relation

Exercise 1: `get_record(rel, rid)`

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Give an implementation of a function

Record `get_record(Relation rel, RecordId rid)`

which takes two parameters

- an open relation descriptor (`rel`)
- a record id (`rid`)

and returns the record corresponding to that `rid`

... Page Formats

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Factors affecting Page formats:

- determined by record size flexibility (fixed, variable)
- how free space within Page is managed
- whether some data is stored outside Page
 - does Page have an associated overflow chain?
 - are large data values stored elsewhere? (e.g. TOAST)
 - can one tuple span multiple Pages?

Implementation of Page operations critically depends on format.

Exercise 2: Fixed-length Records (i)

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How records are managed in Pages ...

- depends on whether records are fixed-length or variable-length

Give examples of table definitions

- which result in fixed-length records
- which result in variable-length records

`create table R (...);`

What are the common features of each type of table?

... Page Formats

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For fixed-length records, use *record slots*.

- *insert*: place new record in first available slot

- *delete*: mark slot as free, or set *xmax*

Page	
Slot[0]	<i>tuple</i>
Slot[1]	<i>free</i>
Slot[2]	<i>tuple</i>
Slot[3]	<i>tuple</i>
Slot[4]	<i>free</i>
Slot[5]	<i>free</i>
<div> <div>1</div> <div>0</div> <div>1</div> <div>1</div> <div>0</div> <div>0</div> </div> <div>[0] [1] [2] [3] [4] [5]</div>	

Page	
Slot[0]	<i>tuple</i>
Slot[1]	<i>xmax != 0</i>
Slot[2]	<i>tuple</i>
Slot[3]	<i>tuple</i>
Slot[4]	<i>xmax != 0</i>
Slot[5]	<i>xmax != 0</i>
Slot[6]	<i>tuple</i>

Exercise 3: Fixed-length Records (ii)

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For the two fixed-length record page formats ...

Implement

- a suitable data structure to represent a Page
- insertion ... `rid = insert_record(rel, pid, rec)`
- deletion ... `delete_record(rel, rid)`

Ignore buffer pool (i.e. use `get_page()` and `put_page()`)

Page Formats

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For variable-length records, must use *record directory*

- `directory[i]` gives location within page of i^{th} record

An important aspect of using record directory

- location of tuple within page can change, tuple index does not change

Issue with variable-length records

- managing space withing the page (esp. after deletions)
- recording used and unused regions of the page

We refer to tuple index within directory as `TupleId tid`

... Page Formats

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Possibilities for handling free-space within block:

- compacted (one region of free space)
- fragmented (distributed free space)

In practice, a combination is useful:

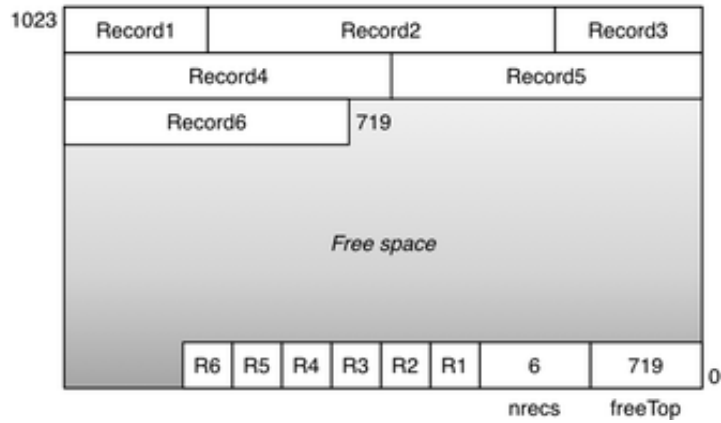
- normally fragmented (cheap to maintain)
- compacted when needed (e.g. record won't fit)

... Page Formats

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Compacted free space ... before inserting record 7

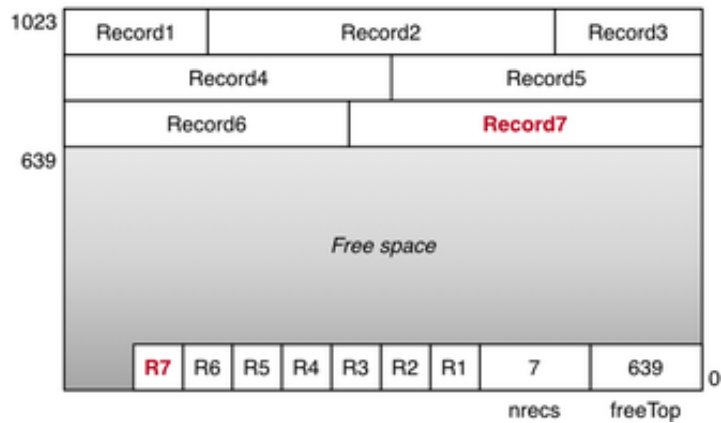
compacted free space



... Page Formats

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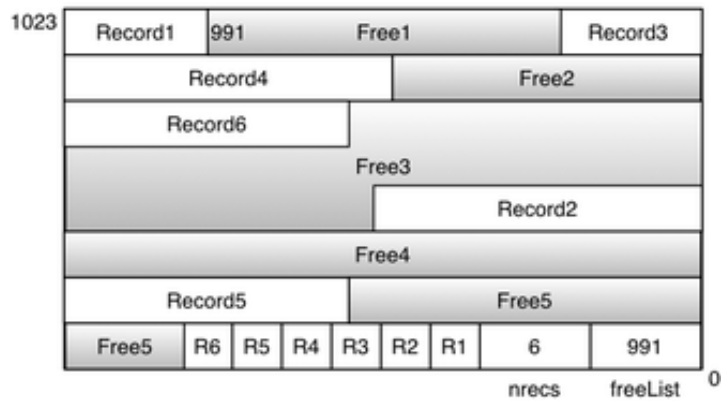
After inserting record 7 (80 bytes) ...



... Page Formats

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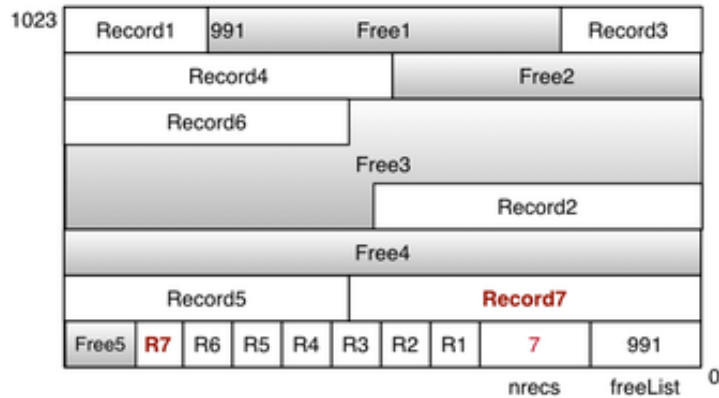
Fragmented free space ... before inserting record 7



... Page Formats

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After inserting record 7 (80 bytes) ...



Exercise 4: Inserting Variable-length Records

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For both of the following page formats

1. variable-length records, with compacted free space
2. variable-length records, with fragmented free space

implement the `insert()` function.

Use the above page format, but also assume:

- page size is 1024 bytes
- tuples start on 4-byte boundaries
- references into page are all 8-bits (1 byte) long
- a function `recSize(rec)` gives size in bytes

Storage Utilisation

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How many records can fit in a page? (denoted c = capacity)

Depends on:

- page size ... typical values: 1KB, 2KB, 4KB, 8KB
- record size ... typical values: 64B, 200B, app-dependent
- page header data ... typically: 4B - 32B
- slot directory ... depends on how many records

每个page都有一个header

We typically consider *average* record size (R)

Given c , $HeaderSize + c * SlotSize + c * R \leq PageSize$

Exercise 5: Space Utilisation

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Consider the following page/record information:

- page size = 1KB = 1024 bytes = 2^{10} bytes
- records: `(w:int, x:varchar(20), y:char(10), z:int)`
- records are all aligned on 4-byte boundaries
- `x` field padded to ensure `z` starts on 4-byte boundary
- each record has 4 field-offsets at start of record (each 1 byte)
- `char(10)` field rounded up to 12-bytes to preserve alignment
- maximum size of `x` values = 20 bytes; average size = 16 bytes
- page has 32-bytes of header information, starting at byte 0
- only insertions, no deletions or updates

Calculate c = average number of records per page.

Overflows

20/77

Sometimes, it may not be possible to insert a record into a page:

1. no free-space fragment large enough
2. overall free-space in page is not large enough
3. the record is larger than the page
4. no more free directory slots in page

当record过大时 这是一种解决办法 另外一种就是toast

For case (1), can first try to compact free-space within the page.

If still insufficient space, we need an alternative solution ...

... Overflows

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File organisation determines how cases (2)..(4) are handled.

If records may be inserted anywhere that there is free space

- cases (2) and (4) can be handled by making a new page
- case (3) requires either spanned records or "overflow file"

If file organisation determines record placement (e.g. hashed file)

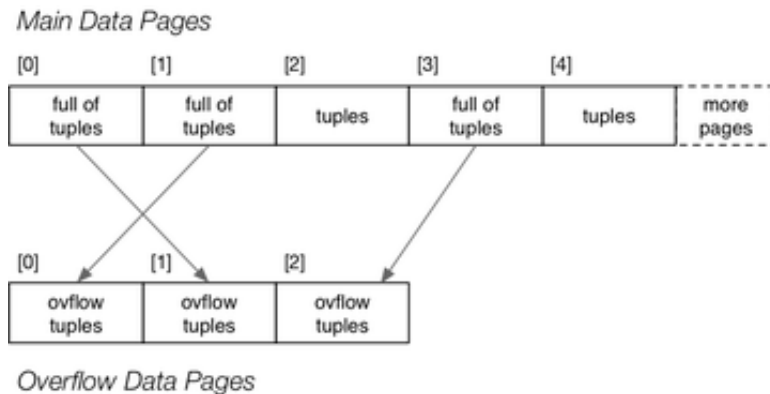
- cases (2) and (4) require an "overflow page"
- case (3) requires an "overflow file"

With overflow pages, *rid* structure may need modifying (*rel, page, ovfl, rec*)

... Overflows

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Overflow pages for full buckets in a hashed file:

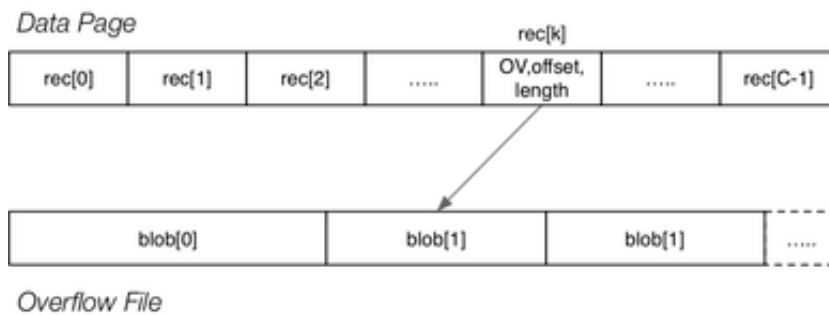


... Overflows

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Overflow file for very large records and BLOBs:

large data item



PostgreSQL Page Representation

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Functions: `src/backend/storage/page/*.c`

Definitions: `src/include/storage/bufpage.h`

Each page is 8KB (default `BLCKSZ`) and contains:

- header (free space pointers, flags, xact data)
- array of (offset,length) pairs for tuples in page
- free space region (between array and tuple data)
- actual tuples themselves (inserted from end towards start)
- (optionally) region for special data (e.g. index data)

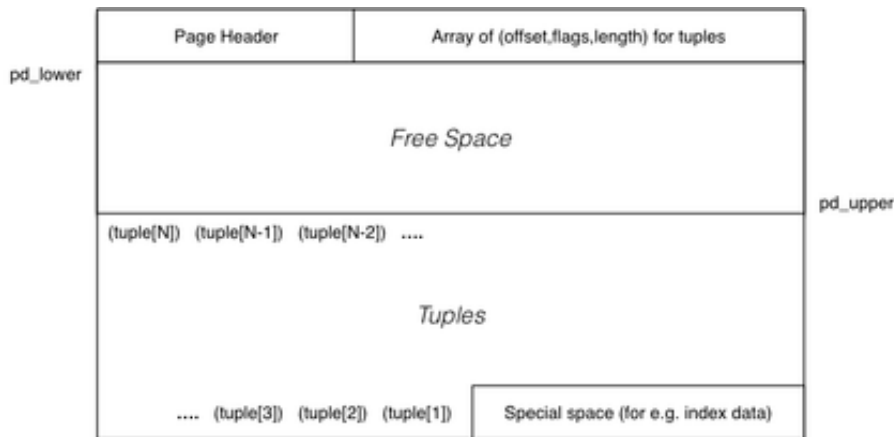
Large data items are stored in separate (TOAST) files (implicit)

Also supports ~SQL-standard BLOBs (explicit large data items)

... PostgreSQL Page Representation

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PostgreSQL page layout:



... PostgreSQL Page Representation

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Page-related data types:

```
// a Page is simply a pointer to start of buffer
typedef Pointer Page;

// indexes into the tuple directory
typedef uint16 LocationIndex;

// entries in tuple directory (line pointer array)
typedef struct ItemIdData
{
    unsigned lp_off:15, // tuple offset from start of page
            lp_flags:2, // unused, normal, redirect, dead
            lp_len:15;  // length of tuple (bytes)
} ItemIdData;
```

... PostgreSQL Page Representation

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Page-related data types: (cont)

```
typedef struct PageHeaderData (simplified)
{
    ...
    uint16 pd_checksum; // checksum
    uint16 pd_flags;    // flag bits (e.g. free, full, ...
    LocationIndex pd_lower; // offset to start of free space
    LocationIndex pd_upper; // offset to end of free space
    LocationIndex pd_special; // offset to start of special space
    uint16 pd_pagesize_version;
    ItemIdData pd_linp[1]; // beginning of line pointer array
} PageHeaderData;

typedef PageHeaderData *PageHeader;
```

... PostgreSQL Page Representation

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Operations on Pages:

```
void PageInit(Page page, Size pageSize, ...)
```

- initialize a Page buffer to empty page
- in particular, sets `pd_lower` and `pd_upper`

```
OffsetNumber PageAddItem(Page page,
                          Item item, Size size, ...)
```

- insert one tuple (or index entry) into a Page
- fails if: not enough free space, too many tuples

```
void PageRepairFragmentation(Page page)
```

- compact tuple storage to give one large free space region

... PostgreSQL Page Representation

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PostgreSQL has two kinds of pages:

- *heap pages* which contain tuples
- *index pages* which contain index entries

Both kinds of page have the same page layout.

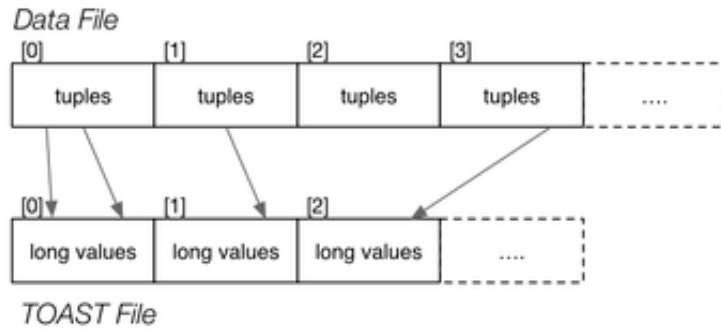
One important difference:

- index entries tend to be smaller than tuples
- can typically fit more index entries per page

TOAST Files

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Each data file has a corresponding TOAST file (if needed)



Tuples in data pages contain rids for long values

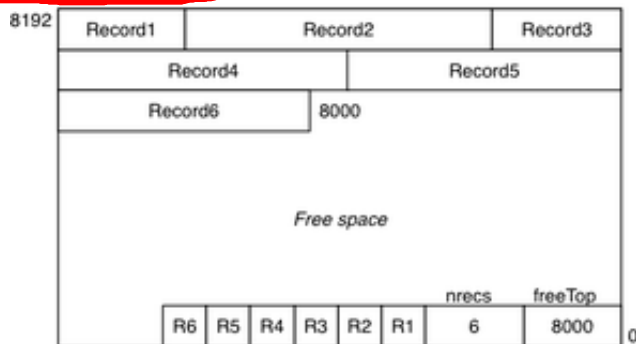
TOAST = The Oversized Attribute Storage Technique

Tuples

Tuples

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Each page contains a collection of tuples



What do tuples contain? How are they structured internally?

Records vs Tuples

33/77

A table is defined by a collection of attributes (*schema*), e.g.

```
create table Employee (
  id integer primary key, name varchar(20),
  job varchar(10), dept number(4)
);
```

Tuple = collection of attribute values for such a schema, e.g.

(33357462, 'Neil Young', 'Musician', 0277)

Record = sequence of bytes, containing data for one tuple, e.g.

01101001	11001100	01010101	00111100	10100011	01011111	01011010
----------	----------	----------	----------	----------	----------	----------

Bytes need to be interpreted relative to schema to get tuple

Operations on Records

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Common operation on records ... access record via RecordId:

```
Record get_record(Relation rel, RecordId rid) {
  (pid,tid) = rid;
  Page *buf = request_page(rel, pid);
  return get_record(buf, tid);
}
```

Gives a sequence of bytes, which needs to be interpreted, e.g.

```
Relation rel = ... // relation schema
Record rec = get_record(rel,rid)
Tuple t = makeTuple(rel,rec)
```

Once we have a tuple, we can access individual attributes/fields

Operations on Tuples

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Once we have a record, we need to interpret it as a tuple ...

```
Tuple t = makeTuple(rel, rec)
```

- convert record to tuple data structure for relation `rel`

Once we have a tuple, we want to examine its contents ...

```
Typ getTypField(Tuple t, int fno)
```

- extract the `fno`'th field from a `Tuple` as a value of type `Typ`

```
E.g. int x = getIntField(t,1), char *s = getStrField(t,2)
```

Scanning

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Access methods typically involve *iterators*, e.g.

```
Scan s = start_scan(Relation r, ...)
```

- commence a scan of relation `r`
- Scan may include condition to implement WHERE-clause
- Scan holds data on progress through file (e.g. current page)

```
Tuple next_tuple(Scan s)
```

- return `Tuple` immediately following last accessed one
- returns `NULL` if no more `Tuples` left in the relation

Example Query

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Example: simple scan of a table ...

```
select name from Employee
```

implemented as:

```
DB db = openDatabase("myDB");
Relation r = openRel(db, "Employee");
Scan s = start_scan(r);
Tuple t; // current tuple
while ((t = next_tuple(s)) != NULL)
{
    char *name = getStrField(t,2);
    printf("%s\n", name);
}
```

Exercise 6: Implement next_tuple()

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Consider the following possible `Scan` data structure

```
typedef struct {
    Relation rel;
    Page *curPage; // Page buffer
    int curPID; // current pid
    int curTID; // current tid
} ScanData;
```

Assume tuples are indexed 0..nTuples(p)

Assume pages are indexed 0..nPages(rel)

Implement the `Tuple next_tuple(Scan)` function

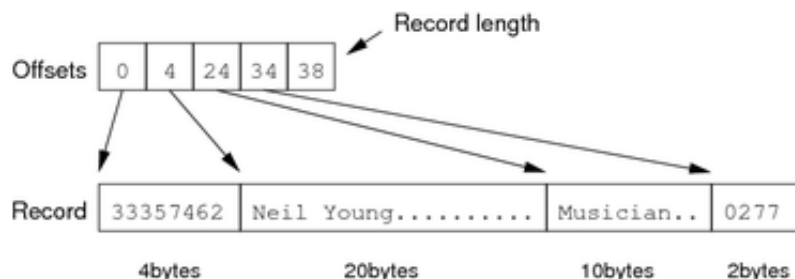
P.S. What's in a `Relation` object?

Fixed-length Records

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Encoding scheme for fixed-length records:

- record format (length + offsets) stored in catalogue
- data values stored in fixed-size slots in data pages



Since record format is frequently used at query time, should be in memory.

Variable-length Records

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Some encoding schemes for variable-length records:

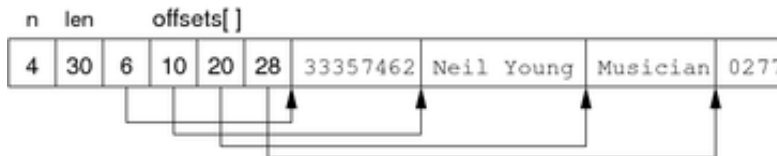
- Prefix each field by length



- Terminate fields by delimiter



- Array of offsets



Converting Records to Tuples

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A Record is an array of bytes (byte[])

- representing the data values from a typed Tuple

A Tuple is a collection of named, typed values (cf. C struct)

Information on how to interpret the bytes as typed values

- will be contained in schema data in DBMS catalogue
- may be stored in the header for the data file
- may be stored partly in the record and partly in the schema

For variable-length records, some formatting info ...

- must be stored in the record or in the page directory

... Converting Records to Tuples

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DBMSs typically define a fixed set of field types, e.g.

DATE, FLOAT, INTEGER, NUMBER(*n*), VARCHAR(*n*), ...

This determines implementation-level data types:

DATE	time_t
FLOAT	float, double
INTEGER	int, long
NUMBER(<i>n</i>)	int[] (?)
VARCHAR(<i>n</i>)	char[]

... Converting Records to Tuples

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A Tuple could be defined as

- a list of field descriptors for a record instance
(where a FieldDesc gives (offset, length, type) information)
- along with a reference to the Record data

```
typedef struct {
    ushort    nfields; // number of fields/attrs
    ushort    data_off; // offset in struct for data
    FieldDesc fields[]; // field descriptions
    Record    data; // pointer to record in buffer
} Tuple;
```

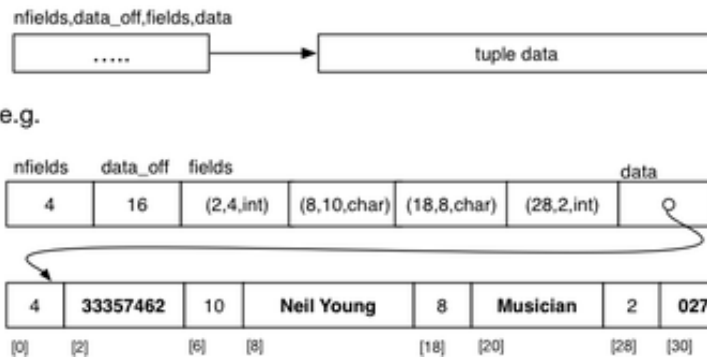
Fields are derived from relation descriptor + record instance data.

... Converting Records to Tuples

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Tuple data could be

- a pointer to bytes stored elsewhere in memory



... Converting Records to Tuples

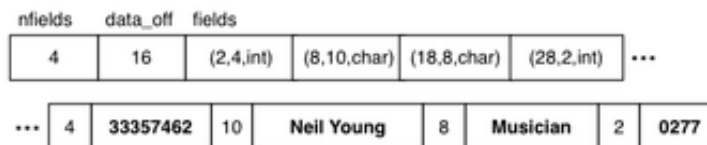
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Or, tuple data could be ...

- appended to Tuple struct (used widely in PostgreSQL)



e.g.



Exercise 7: How big is a FieldDesc?

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FieldDesc = (offset,length,type), where

- offset = offset of field within record data
- length = length (in bytes) of field
- type = data type of field

If pages are 8KB in size, how many bits are needed for each?

E.g.



PostgreSQL Tuples

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Definitions: `include/postgres.h`, `include/access/*tup*.h`

Functions: `backend/access/common/*tup*.c` e.g.

- `HeapTuple heap_form_tuple(desc,values[],isnull[])`
- `heap_deform_tuple(tuple,desc,values[],isnull[])`

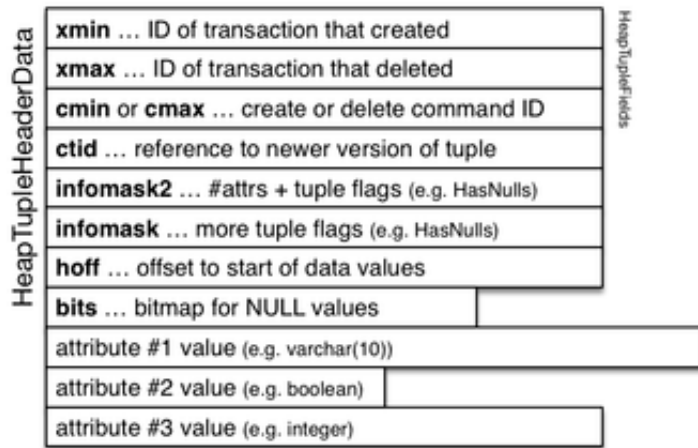
PostgreSQL defines tuples via:

- a contiguous chunk of memory
- starting with a header giving e.g. #fields, nulls
- followed by the data values (as sequence of Datum)

... PostgreSQL Tuples

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Tuple structure:



... PostgreSQL Tuples

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Tuple-related data types:

```
// representation of a data value
typedef uintptr_t Datum;
```

The actual data value:

- may be stored in the `Datum` (e.g. `int`)
- may have a header with length (for varlen attributes)
- may be stored in a TOAST file

... PostgreSQL Tuples

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Tuple-related data types: (cont)

```
// TupleDesc: schema-related information for HeapTuples

typedef struct tupleDesc
{
    int          natts;           // number of attributes in the tuple
    Form_pg_attribute *attrs;
    // attrs[N] is a pointer to description of attribute N+1
    TupleConstr *constr;         // constraints, or NULL if none
    Oid          tdtypeid;       // composite type ID for tuple type
    int32        tdtypmod;       // typmod for tuple type
    bool         tdhasoid;       // does tuple have oid attribute?
    int          tdrefcount;     // reference count (-1 if not counting)
} *TupleDesc;
```

... PostgreSQL Tuples

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`HeapTupleData` contains information about a stored tuple

```
typedef HeapTupleData *HeapTuple;
```

```
typedef struct HeapTupleData
{
    uint32        t_len;         // length of *t_data
    ItemPointerData t_self;      // SelfItemPointer
    Oid           t_tableOid;    // table the tuple came from
    HeapTupleHeader t_data;      // -> tuple header and data
} HeapTupleData;
```

`HeapTupleHeader` is a pointer to a location in a buffer

... PostgreSQL Tuples

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PostgreSQL stores a single block of data for tuple

- containing a tuple header, followed by data byte[]

```
typedef struct HeapTupleHeaderData // simplified
{
    HeapTupleFields t_heap;
    ItemPointerData t_ctid;       // TID of this tuple or newer version
    uint16          t_infomask2;  // #attributes + flags
    uint16          t_infomask;   // flags e.g. has_null, has_varwidth
    uint8           t_hoff;       // sizeof header incl. bitmap+padding
    // above is fixed size (23 bytes) for all heap tuples
    bits8           t_bits[1];    // bitmap of NULLs, variable length
    // OID goes here if HEAP_HASOID is set in t_infomask
    // actual data follows at end of struct
} HeapTupleHeaderData;
```

... PostgreSQL Tuples

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Tuple-related data types: (cont)

```
typedef struct HeapTupleFields // simplified
{
    TransactionId t_xmin; // inserting xact ID
    TransactionId t_xmax; // deleting or locking xact ID
    union {
        CommandId t_cid; // inserting or deleting command ID
        TransactionId t_xvac; // old-style VACUUM FULL xact ID
    } t_field3;
} HeapTupleFields;
```

Note that not all system fields from stored tuple appear

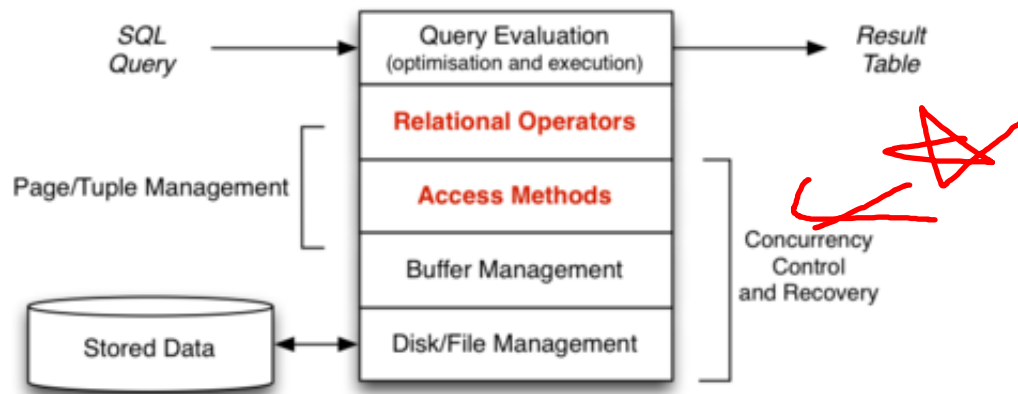
- oid is stored after the tuple header, if used
- both xmin/xmax are stored, but only one of cmin/cmax

Implementing Relational Operations

DBMS Architecture (revisited)

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Implementation of relational operations in DBMS:



Relational Operations

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DBMS core = relational engine, with implementations of

- selection, projection, join, set operations
- scanning, sorting, grouping, aggregation, ...

In this part of the course:

- examine methods for implementing each operation
- develop cost models for each implementation
- characterise when each method is most effective

Terminology reminder:

- tuple = collection of data values under some schema = record
- page = block = collection of tuples + management data = i/o unit
- relation = table = file = collection of tuples

... Relational Operations

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Two "dimensions of variation":

- which relational operation (e.g. Sel, Proj, Join, Sort, ...)
- which access-method (e.g. file struct: heap, indexed, hashed, ...)

Each query method involves an operator and a file structure:

- e.g. primary-key selection on hashed file
- e.g. primary-key selection on indexed file
- e.g. join on ordered heap files (sort-merge join)
- e.g. join on hashed files (hash join)
- e.g. two-dimensional range query on R-tree indexed file

As well as query costs, consider update costs (insert/delete).

... Relational Operations

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SQL vs DBMS engine

- **select ... from R where C**
 - find relevant tuples (satisfying C) in file(s) of R
- **insert into R values(...)**

- place new tuple in some page of a file of R
- **delete from R where C**
 - find relevant tuples and "remove" from file(s) of R
- **update R set ... where C**
 - find relevant tuples in file(s) of R and "change" them

Cost Models

Cost Models

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An important aspect of this course is

- analysis of cost of various query methods

Cost can be measured in terms of

- *Time Cost*: total time taken to execute method, or
- *Page Cost*: number of pages read and/or written

Primary assumptions in our cost models:

- memory (RAM) is "small", fast, byte-at-a-time
- disk storage is very large, slow, page-at-a-time

... Cost Models

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Since *time cost* is affected by many factors

- speed of i/o devices (fast/slow disk, SSD)
- load on machine

we do not consider time cost in our analyses.

For comparing methods, *page cost* is better

- identifies workload imposed by method
- BUT is clearly affected by buffering

Estimating costs with multiple concurrent ops and buffering is difficult!!

Additional assumption: every page request leads to some i/o

... Cost Models

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In developing cost models, we also assume:

- a relation is a set of r tuples, with average size R bytes
- the tuples are stored in b data pages on disk
- each page has size B bytes and contains up to c tuples
- the tuples which answer query q are contained in b_q pages
- data is transferred disk \leftrightarrow memory in whole pages
- cost of disk \leftrightarrow memory transfer T_{rw} is very high



... Cost Models

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Our cost models are "rough" (based on assumptions)

But do give an $O(x)$ feel for how expensive operations are.

Example "rough" estimation: how many piano tuners in Sydney?

- Sydney has = 4 000 000 people
- Average household size = 3 \therefore 1 300 000 households
- Let's say that 1 in 10 households owns a piano
- Therefore there are = 130 000 pianos
- Say people get their piano tuned every 2 years (on average)
- Say a tuner can do 2/day, 250 working-days/year
- Therefore 1 tuner can do 500 pianos per year
- Therefore Sydney would need = $130000/2/500 = 130$ tuners

Actual number of tuners in Yellow Pages = 120

Example borrowed from Alan Fekete at Sydney University.

Query Types

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Type	SQL	RelAlg	a.k.a.
Scan	<code>select * from R</code>	R	-

Proj	select x, y from R	$Proj[x, y]R$	-
Sort	select * from R order by x	$Sort[x]R$	ord
Sel_1	select * from R where $id = k$	$Sel[id=k]R$	one
Sel_n	select * from R where $a = k$	$Sel[a=k]R$	-
$Join_1$	select * from R, S where $R.id = S.r$	$R Join[id=r] S$	-

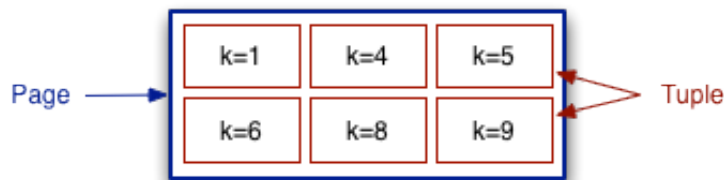
Different query classes exhibit different query processing behaviours.

Example File Structures

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When describing file structures

- use a large box to represent a *page*
- use either a small box or *tuple* (or *rec*) to represent a *tuple*
- sometimes refer to tuples via their *key*
 - mostly, *key* corresponds to the notion of "primary key"
 - sometimes, *key* means "search key" in selection condition



... Example File Structures

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Consider three simple file structures:

- *heap file* ... tuples added to any page which has space
- *sorted file* ... tuples arranged in file in key order
- *hash file* ... tuples placed in pages using hash function

All files are composed of b primary blocks/pages



Some records in each page may be marked as "deleted".

Exercise 8: Operation Costs

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For each of the following file structures

- determine #page-reads + #page-writes for each operation

You can assume the existence of a file header containing

- values for r, R, b, B, c
- index of first page with free space (and a free list)

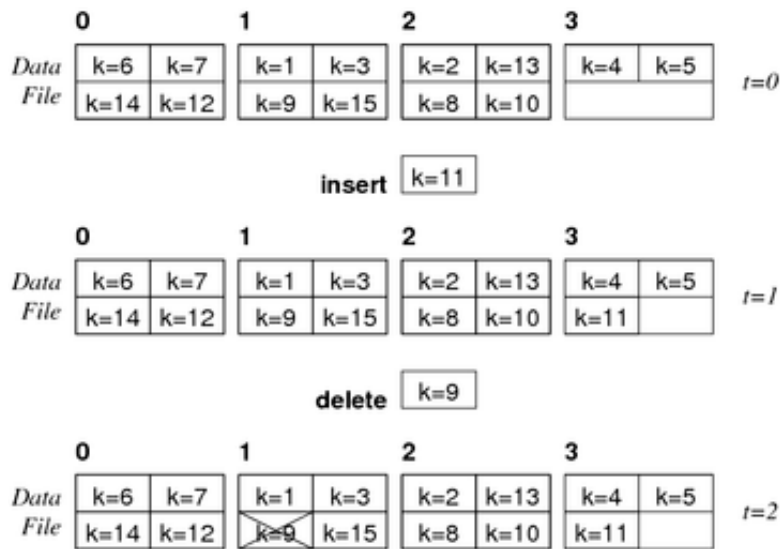
Assume also

- each page contains a header and directory as well as tuples
- no buffering (worst case scenario)

Operation Costs Example

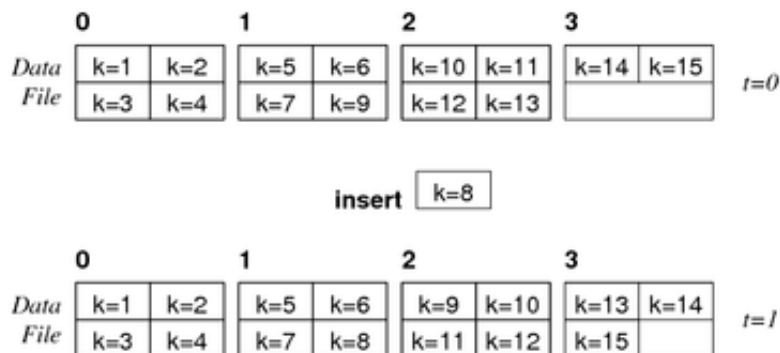
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Heap file with $b = 4, c = 4$:



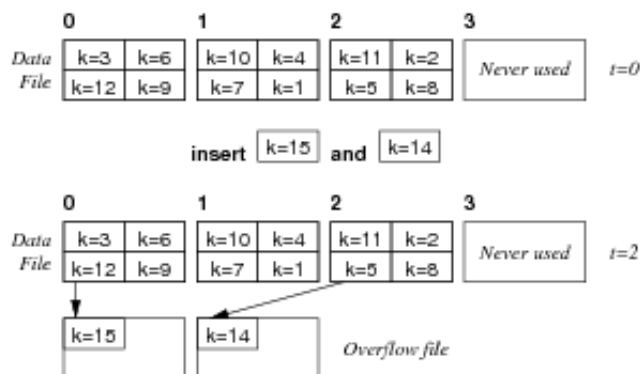
... Operation Costs Example

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Sorted file with $b = 4$, $c = 4$:

... Operation Costs Example

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Hashed file with $b = 3$, $c = 4$, $h(k) = k \% 3$ 

Scanning

Scanning

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Consider the query:

```
select * from Rel;
```

Operational view:

```
for each page P in file of relation Rel {
  for each tuple t in page P {
    add tuple t to result set
  }
}
```

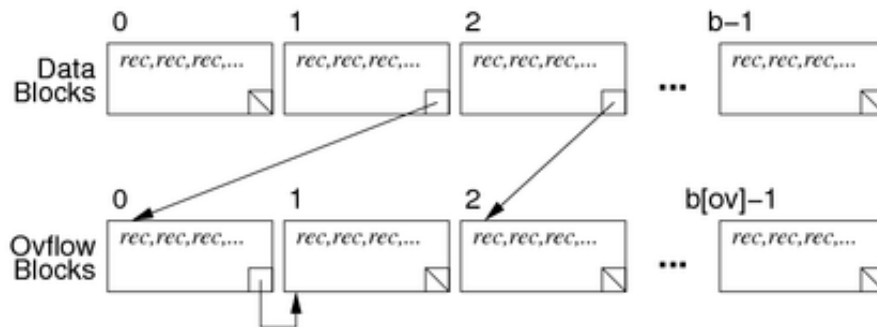

Cost: read every data page once

Time Cost = $b \cdot T_p$ Page Cost = b

... Scanning

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Scan implementation when file has overflow pages, e.g.



... Scanning

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In this case, the implementation changes to:

```
for each page P in file of relation T {
  for each tuple t in page P {
    add tuple t to result set
  }
  for each overflow page V of page P {
    for each tuple t in page V {
      add tuple t to result set
    }
  }
}
```

Cost: read each data and overflow page once

Cost = $b + b_{ov}$

where b_{ov} = total number of overflow pages

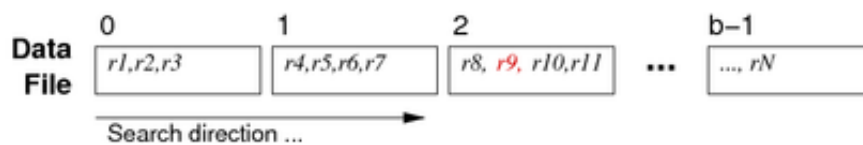
Selection via Scanning

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Consider a *one* query like:

```
select * from Employee where id = 762288;
```

In an unordered file, search for matching tuple requires:



Guaranteed at most one answer; but could be in any page.

... Selection via Scanning

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Overview of scan process:

```
for each page P in relation Employee {
  for each tuple t in page P {
    if (t.id == 762288) return t
  }
}
```

Cost analysis for *one* searching in unordered file

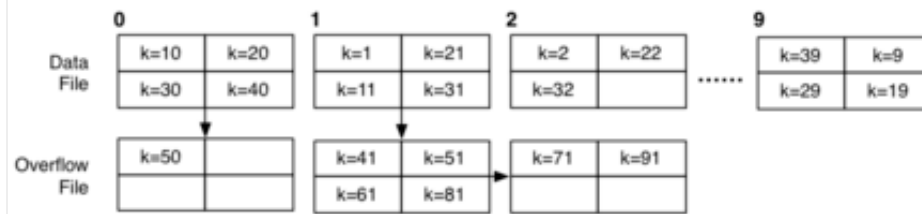
- best case: read one page, find tuple
- worst case: read all b pages, find in last (or don't find)
- average case: read half of the pages ($b/2$)

Page Costs: $Cost_{avg} = b/2$ $Cost_{min} = 1$ $Cost_{max} = b$

Exercise 9: Cost of Search in Hashed File

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Consider the hashed file structure $b = 10$, $c = 4$, $h(k) = k \% 10$



Describe how the following queries

```
select * from R where k = 51;
select * from R where k > 50;
```

might be solved in a file structure like the above ($h(k) = k \% b$).

Estimate the minimum and maximum cost (as #pages read)

Produced: 20 Jun 2019