

# Microelectronics Circuit Analysis and Design

## Homework(8th)

Yuejin Xie U202210333

Oct 10th, 2023

- 5.24 (a) For the circuit in Figure P5.24, determine  $V_B$  and  $I_E$  such that  $V_B = V_C$ . Assume  $\beta = 90$ .  
 (b) What value of  $V_B$  results in  $V_{CE} = 2V$ ?

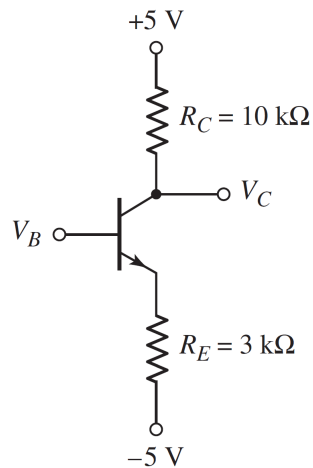


Figure 1: Problem 5.24

Solution:

- (a) Assume the BJT works in the forward-active region:

$$\begin{cases} I_C = \frac{5 - V_C}{R_C} \\ I_E = \frac{V_B - V_{BE(on)} - (-5)}{R_E} \\ I_E = \frac{1 + \beta}{\beta} I_C \\ V_B = V_C \end{cases} \Rightarrow \begin{cases} V_B = -2.14V \\ I_E = 0.72mA \end{cases}$$

(b) Obviously, the BJT work in the active region, so we have equation:

$$\begin{cases} V_C - V_B + V_{BE(on)} = V_{CE} \\ I_C = \frac{5 - V_C}{R_C} \\ I_E = \frac{V_B - V_{BE(on)} - (-5)}{R_E} \\ I_E = \frac{1 + \beta}{\beta} I_C \end{cases} \Rightarrow \begin{cases} V_B = -2.44\text{V} \\ I_E = 0.62\text{mA} \end{cases}$$

5.43 The common-emitter current gain of the transistor in Figure P5.43 is  $\beta = 80$ . Plot the voltage transfer characteristics over the range  $0 \leq V_I \leq 5\text{V}$ .

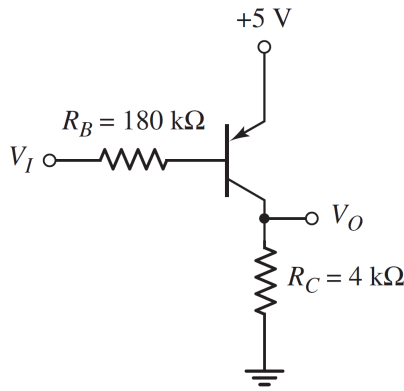


Figure 2: Problem 5.43

Solution:

It's a PNP BJT

case 1:  $V_I \in (4.3, 5)$ ,  $V_{EB} < 0.7\text{V}$ , the B-E junction isn't conducted,  $I_E = 0$ ,  $V_O = 0$

case 2: When BJT works in saturation region(at sat-point),  $V_{EC} = 0.2\text{V}$ ,  $V_O = 4.8\text{V}$ ,  $V_I = 5 - V_{EC(ON)} - \frac{V_O}{\beta R_C} R_B = 1.6\text{V}$ , so when  $V_I < 1.6\text{V}$ ,  $V_O = 4.8\text{V}$

case 3:  $V_I \in [1.6, 4.3]$ , the BJT works in the active region:

$$\frac{V_O}{R_C} = \beta \frac{5 - V_{BE(ON)} - V_I}{R_B} \Rightarrow V_O = -\frac{16}{9} V_I + \frac{344}{45}$$

5.70 For the circuit in Figure P5.70, let  $R_C = 2.2\text{k}\Omega$ ,  $R_E = 2\text{k}\Omega$ ,  $R_1 = 10\text{k}\Omega$ ,  $R_2 = 20\text{k}\Omega$ , and  $\beta = 60$ . (a) Find  $R_{TH}$  and  $V_{TH}$  for the base circuit. (b) Determine  $I_{BQ}$ ,  $I_{CQ}$ ,  $V_E$ , and  $V_C$ .

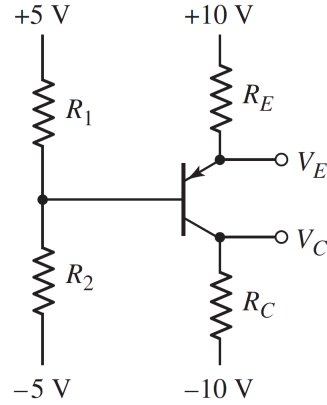


Figure 3: Problem 5.70

Solution:

$$(a) V_{TH} = V^- + \frac{R_2}{R_1 + R_2}(V^+ - V^-) = \frac{5}{3}V, R_{TH} = R_1 || R_2 = \frac{20}{3}k\Omega$$

(b) Equation is as follow:

$$(1 + \beta)I_B R_E + V_{BE(ON)} + I_B R_{TH} + V_{TH} = 10 \Rightarrow I_B = 0.0593mA$$

$$\therefore I_C = \beta I_B = 3.56mA, V_E = V_S - I_E R_E = 2.76V, V_C = -10V + I_C R_C = -2.17V$$

6.8 The parameters of each transistor in the circuits shown in Figure P6.8 are  $\beta = 130$ ,  $V_A = 80V$ , and  $I_{CQ} = 0.2mA$ . Determine the output resistance  $R_o$  for each circuit.

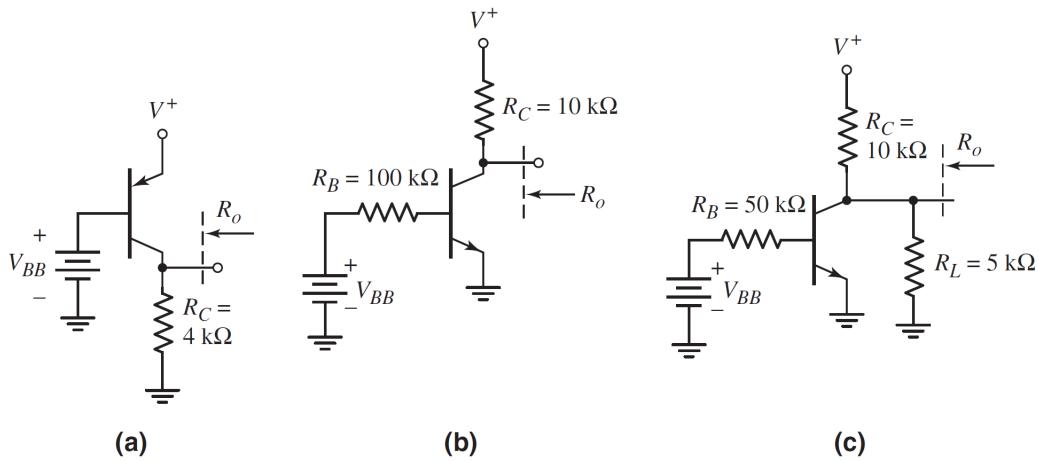


Figure 4: Problem 6.8

Solution:

$$r_o = \frac{V_A}{I_{CQ}} = 400\text{k}\Omega$$

$$(a) R_o = r_o || R_C = 3.96\text{k}\Omega$$

$$(b) R_o = r_o || R_C = 9.76\text{k}\Omega$$

$$(c) R_o = r_o || R_L || R_C = 3.31\text{k}\Omega$$

6.18 The signal source in Figure P6.18 is  $v_s = 5 \sin \omega t \text{ mV}$ . The transistor parameters are  $\beta = 120$  and  $V_A = \infty$ . (a) (i) Design the circuit such that  $I_{CQ} = 0.25 \text{ mA}$  and  $V_{CEQ} = 3 \text{ V}$ . (ii) Find the small-signal voltage gain  $A_v = v_o/v_s$ . (iii) Find  $v_o(t)$ . (b) Repeat part (a) for  $R_S = 0$ .

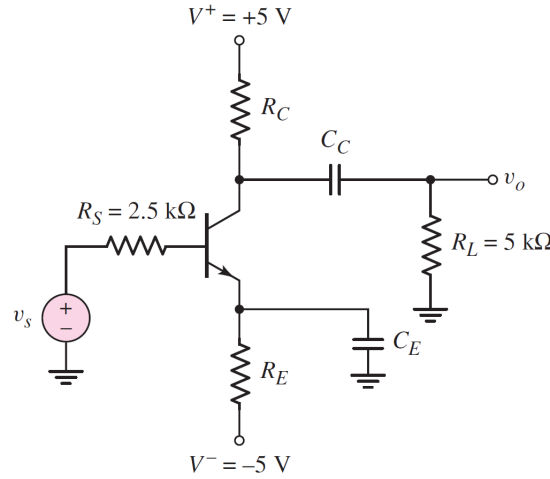


Figure 5: Problem 6.18

Solution:

(a)(i)  $I_{BQ} = \frac{I_{CQ}}{\beta} = 0.00661 \text{ mA}$ , then because of KVL, we have equation:

$$\begin{cases} I_{BQ}R_S + V_{BEON} + (\beta + 1)I_B R_E = 0 - V^- \\ I_C R_C + V_{CEQ} + (\beta + 1)I_B = V^+ - V^- \end{cases} \Rightarrow \begin{cases} R_C = 10.9\text{k}\Omega \\ R_E = 17.0\text{k}\Omega \end{cases}$$

$$(ii) A_v = \frac{-g_m \left( \frac{r_\pi}{R_S + r_\pi} \cdot v_s \right) (R_L || R_C)}{v_s} = -27.5$$

$$(iii) v_o(t) = A_v v_s = -0.14 \sin \omega t \text{ V}$$

(b)(i) because of KVL, we have equation:

$$\begin{cases} \beta I_{BQ} R_C + V_{CEQ} + (\beta + 1)I_B R_E = V^+ - V^- \\ V_{BEON} + (\beta + 1)I_B R_E = 0 - V^- \end{cases} \Rightarrow \begin{cases} R_C = 10.8\text{k}\Omega \\ R_E = 17.1\text{k}\Omega \end{cases}$$

$$(ii) A_v = \frac{-g_m(\cdot v_s)(R_L || R_C)}{v_s} = -32.9$$

$$(iii) v_o(t) = A_v v_s = -0.16 \sin \omega t \text{ V}$$

6.33 For the circuit in Figure P6.15, let  $\beta = 100$ ,  $V_A = \infty$ ,  $R_E = 12.9 \text{ k}\Omega$ , and  $R_C = 6 \text{ k}\Omega$ . Determine the maximum undistorted swing in the output voltage if the total instantaneous C–E voltage is to remain in the range  $1 \leq v_{CE} \leq 9 \text{ V}$  and if the total instantaneous collector current is to remain greater or equal to  $50 \mu \text{ A}$ .

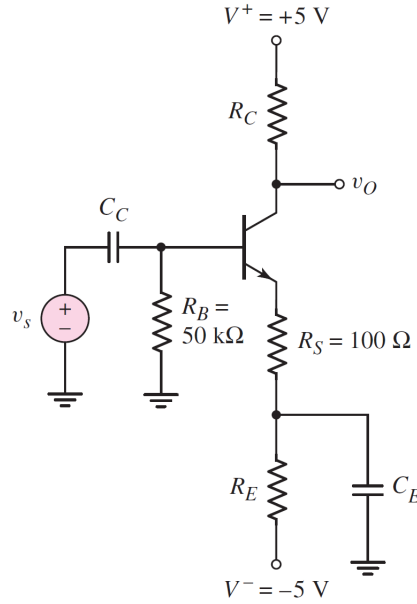


Figure 6: Problem 6.33

Solution:

First, we solve out Q-point:

because of KVL, we have equation:

$$I_B R_B + V_{BE(ON)} + (\beta + 1) I_B (R_E + R_S) = 0 - V^- \Rightarrow I_B = 0.00315 \text{ mA}$$

$$\therefore I_C = 0.315 \text{ mA}, I_E = 0.319 \text{ mA}, V_{CEQ} = (V^+ - V^-) - I_C R_C - I_E (R_E + R_S) = 3.96 \text{ V}$$

Second, AC circuit Load Line Analysis:

$$AC - slope = -\frac{1}{R_C || R_S} = -\frac{1}{6.1} \Rightarrow 315 \mu \text{ A} - 50 \mu \text{ A} = \Delta i_{CE(\max)} = -\frac{1}{6.1} \Delta v_{CE(\max)}$$

$$\Rightarrow \Delta v_{CE(\max)} = 1.62 \text{ V} \Rightarrow v_{CE(\min)} = 2.34 \text{ V} > 1 \text{ V}$$

Third, calculate the max undistorted swing:

$$V_{pp(\max)} = 2 \Delta v_{CE(\max)} = 3.24 \text{ V}$$

6.39 For the circuit in Figure P6.24, the transistor parameters are  $\beta = 100$  and  $V_A = \infty$ . (a) Determine the maximum undistorted swing in the output voltage if the total instantaneous E–C voltage is to remain in the range  $1 \leq v_{EC} \leq 9\text{V}$ . (b) Using the results of part (a), determine the range of collector current.

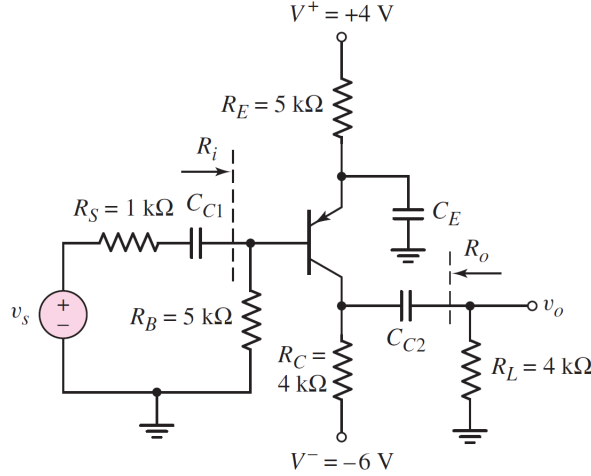


Figure 7: Problem 6.39

Solution:

(a) First, find Q-point:

$$(\beta + 1)I_{BQ}R_E + V_{BE}(ON) + I_{BQ}R_B = V^+ \Rightarrow I_{BQ} = 0.00647\text{mA}$$

$$\therefore I_{CQ} = 0.647\text{mA}, V_{ECQ} = (V^+ - V^-) - (\beta + 1)R_E - I_{CQ}R_C = 4.18\text{V}$$

Second, AC circuit Load Line Analysis:

$$AC - slope = -\frac{1}{R_C || R_L} = -\frac{1}{2\text{k}\Omega} \Rightarrow 0.647\text{mA} = \Delta i_{CE(\max)} = -\frac{1}{2\text{k}\Omega} \Delta v_{CE(\max)}$$

$$\Rightarrow \Delta v_{CE(\max)} = 1.294\text{V} \Rightarrow v_{CE(\min)} = V_{CEQ} - \Delta v_{CE(\max)} > 1\text{V}$$

Third, calculate the max undistorted swing:

$$V_{pp(\max)} = 2\Delta v_{CE(\max)} = 2.59\text{V}$$

(b) the answer is obviously:  $i_C \in (0, 1.294]\text{mA}$

6.65 Consider the circuit shown in Figure P6.69. The transistor has parameters  $\beta = 120$  and  $V_A = \infty$ . (a) Determine the quiescent  $V_{CEQ}$ . (b) Determine the small-signal voltage gain  $A_v = v_o/v_s$ .

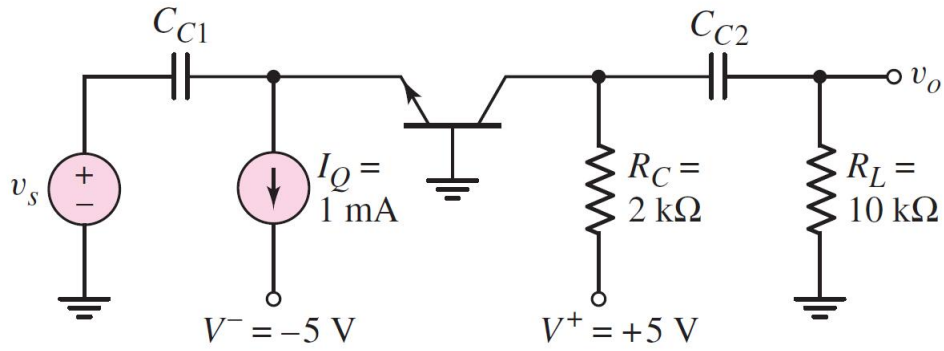


Figure 8: Problem 6.65

Solution:

(a) Because of KCL, we have equation:

$$\begin{cases} I_{BQ} + \beta I_{BQ} = I_Q \\ \beta I_{BQ} R_C + V_{CEQ} = V^+ - (-V_{BE(ON)}) \end{cases} \Rightarrow \begin{cases} I_{BQ} = 0.0083 \text{ mA} \\ V_{CEQ} = 3.72 \text{ V} \end{cases}$$

$$(b) A_v = \frac{-g_m V_\pi (R_C || R_L)}{v_s} = g_m (R_C || R_L) = 63.6$$