

# Microelectronics Circuit Analysis and Design

## Homework(1st)

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9.6 Assume the op-amps in Figure P9.6 are ideal. Find the voltage gain  $A_v = v_O/v_I$  and the input resistance  $R_i$  of each circuit.

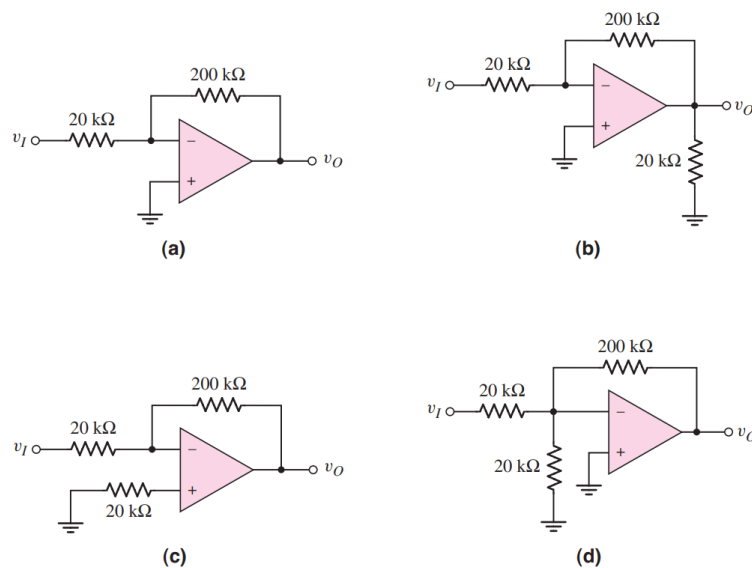


Figure 1: Problem 9.6

Solution:

(a) Actually,  $(v_2 - v_1) \rightarrow 0$ ,  $i_+$ ,  $i_- \rightarrow 0$ , and we have these equations as follow:

$$\begin{cases} \frac{v_I - v_-}{20\text{ k}\Omega} = \frac{v_- - v_O}{200\text{ k}\Omega} \\ v_+ = 0 \end{cases} \Rightarrow \frac{v_O}{v_I} = -10$$

The input resistance  $R_i = \frac{v_I}{\frac{v_I - v_-}{20k\Omega}} = 20k\Omega$

(b)(c)(d) In fact the new resistances of  $20k\Omega$  in Figure (a)(b)(c) don't make differences to their circuits.

So the answers do not change:  $\frac{v_O}{v_I} = -10, R_i = 20k\Omega$

9.14 (a) The input to the circuit shown in Figure P9.14 is  $v_I = -0.20$  V. (i) What is  $v_O$ ? (ii) Determine  $i_2, i_O$ , and  $i_L$ . (b) Repeat part (a) for  $v_I = +0.05$  V. (c) Repeat part (a) for  $v_I = 8\sin\omega t$  mV.

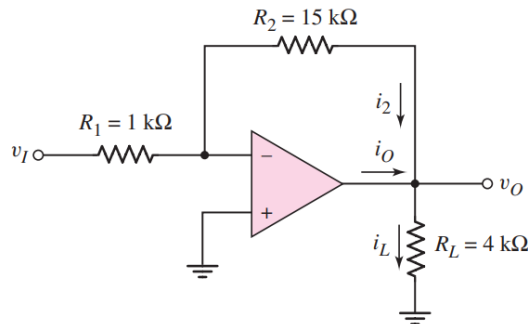


Figure 2: Problem 9.14

Solution:

We provide a general solution in most instances first.

Because of "virtual short", "virtual open" and KCL, we have equations as follow:

$$\begin{cases} \frac{v_I - v_-}{R_1} = \frac{v_- - v_O}{R_2} = i_2 \\ v_+ = v_- = 0 \\ i_O + i_2 = i_L \\ i_L = \frac{v_O}{R_L} \end{cases} \Rightarrow \begin{cases} v_O = -\frac{R_2}{R_1} v_I \\ i_2 = \frac{v_I}{R_1} \\ i_O = \frac{v_O}{R_L} - \frac{v_I}{R_1} \\ i_L = \frac{v_O}{R_L} \end{cases}$$

(a)  $v_O = 3V, i_2 = -0.2mA, i_O = 0.95mA, i_L = 0.75mA$

(b)  $v_O = -0.75V, i_2 = 0.05mA, i_O = -0.2375mA, i_L = -0.1875mA$

(c)  $v_O = -120\sin\omega tV, i_2 = 8\sin\omega tmA, i_O = -38\sin\omega tmA, i_L = -30\sin\omega tmA$

9.37 A summing amplifier can be used as a digital-to-analog converter (DAC). An example of a 4-bit DAC is shown in Figure P9.37. When switch  $S_3$  is connected to the -5 V supply, the most significant bit is  $a_3 = 1$ ; when  $S_3$  is connected to ground, the most significant bit is  $a_3 = 0$ . The same condition applies to the other switches  $S_2, S_1$ , and  $S_0$ , corresponding to bits  $a_2, a_1$ , and  $a_0$ ,

where  $a_o$  is the least significant bit. (a) Show that the output voltage is given by

$$v_O = \frac{R_F}{10} \left[ \frac{a_3}{2} + \frac{a_2}{4} + \frac{a_1}{8} + \frac{a_o}{16} \right] \quad (5)$$

(5) where  $R_F$  is in  $k\Omega$ . (b) Find the value of  $R_F$  such that  $v_O = 2.5V$  when the digital input is  $a_3a_2a_1a_o = 1000$ . (c) Using the results of part (b), find  $v_O$  for: (i)  $a_3a_2a_1a_o = 0001$ , and (ii)  $a_3a_2a_1a_o = 1111$ .

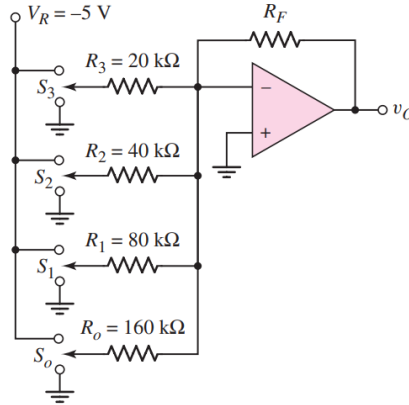


Figure 3: Problem 9.37

Solution:

(a) Because of "virtual short", "virtual open", we have equations as follow:

$$\begin{cases} a_o \frac{v_R - v_-}{R_o} + a_1 \frac{v_R - v_-}{R_1} + a_2 \frac{v_R - v_-}{R_2} + a_3 \frac{v_R - v_-}{R_3} = \frac{v_- - v_O}{R_F} \\ v_+ = v_- = 0 \end{cases}$$

$$\Rightarrow v_O = \frac{R_F}{10} \left[ \frac{a_3}{2} + \frac{a_2}{4} + \frac{a_1}{8} + \frac{a_o}{16} \right] \quad (\text{Maybe there is a problem with this question?})$$

(b) substitute  $v_O = 2.5V$ ,  $a_3a_2a_1a_o = 1000$  into the (5)  $\Rightarrow R_F = 10k\Omega$

(c) Now  $R_F = 10k\Omega$

so (i) substitute  $a_3a_2a_1a_o = 0001$  into the (5)  $\Rightarrow v_O = 0.3125V$

so (ii) substitute  $a_3a_2a_1a_o = 1111$  into the (5)  $\Rightarrow v_O = 4.6875V$