

05-D

二叉树

二叉树实现

Anyone who loves his father or mother more than me is not worthy of me; anyone who loves his son or daughter more than me is not worthy of me.

邓俊辉

deng@tsinghua.edu.cn

BinNode模板类

❖ #define BinNodePosi(T) BinNode<T>* //节点位置

❖ template <typename T> **struct** BinNode {

BinNodePosi(T) parent, lc, rc; //父亲、孩子

T data; int height; int size(); //高度、子树规模

BinNodePosi(T) insertAsLC(T const &); //作为左孩子插入新节点

BinNodePosi(T) insertAsRC(T const &); //作为右孩子插入新节点

BinNodePosi(T) succ(); // (中序遍历意义下) 当前节点的直接后继

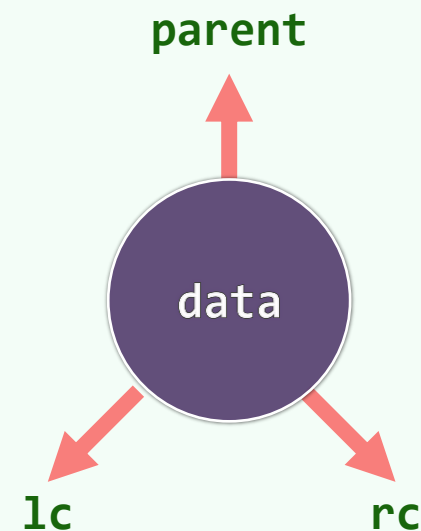
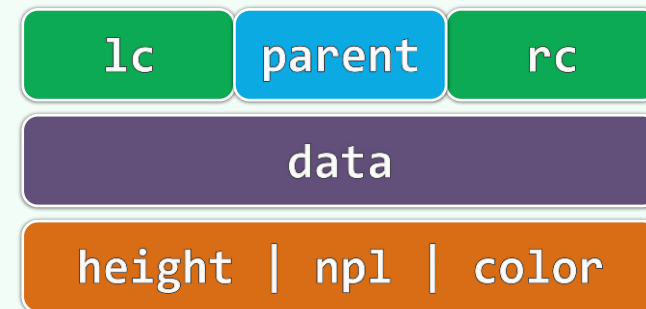
template <typename VST> void travLevel(VST &); //子树层次遍历

template <typename VST> void travPre(VST &); //子树先序遍历

template <typename VST> void travIn(VST &); //子树中序遍历

template <typename VST> void travPost(VST &); //子树后序遍历

};



BinNode接口实现

❖ `template <typename T> BinNodePosi(T) BinNode<T>::insertAsLC(T const & e)`

`{ return lc = new BinNode(e, this); }`

❖ `template <typename T> BinNodePosi(T) BinNode<T>::insertAsRC(T const & e)`

`{ return rc = new BinNode(e, this); }`

❖ `template <typename T>`

`int BinNode<T>::size() { //后代总数，亦即以其为根的子树的规模`

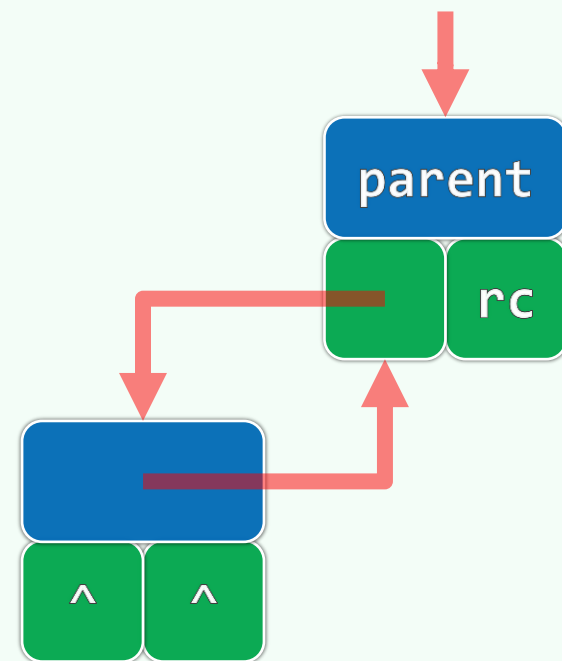
`int s = 1; //计入本身`

`if (lc) s += lc->size(); //递归计入左子树规模`

`if (rc) s += rc->size(); //递归计入右子树规模`

`return s;`

`} //O(n = |size|)`



BinTree模板类

```
template <typename T> class BinTree {  
protected:  
    int _size; //规模  
    BinNodePosi(T) _root; //根节点  
    virtual int updateHeight( BinNodePosi(T) x ); //更新节点x的高度  
    void updateHeightAbove( BinNodePosi(T) x ); //更新x及祖先的高度  
public:  
    int size() const { return _size; } //规模  
    bool empty() const { return !_root; } //判空  
    BinNodePosi(T) root() const { return _root; } //树根  
    /* ... 子树接入、删除和分离接口；遍历接口 ... */  
}
```

高度更新

❖ `#define stature(p) ((p) ? (p)->height : -1)` //节点高度——约定空树高度为-1

❖ `template <typename T> //更新节点x高度，具体规则因树不同而异`

```
int BinTree<T>::updateHeight( BinNodePosi(T) x ) {  
    return x->height = 1 + max( stature( x->lc ), stature( x->rc ) );  
} //此处采用常规二叉树规则， $O(1)$ 
```

❖ `template <typename T> //更新v及其历代祖先的高度`

```
void BinTree<T>::updateHeightAbove( BinNodePosi(T) x ) {  
    while (x) { updateHeight(x); x = x->parent; } //可优化  
} // $O( n = \text{depth}(x) )$ 
```

节点插入

❖ template <typename T>

```
BinNodePosi(T) BinTree<T>::insertAsRC( BinNodePosi(T) x, T const & e ) {
```

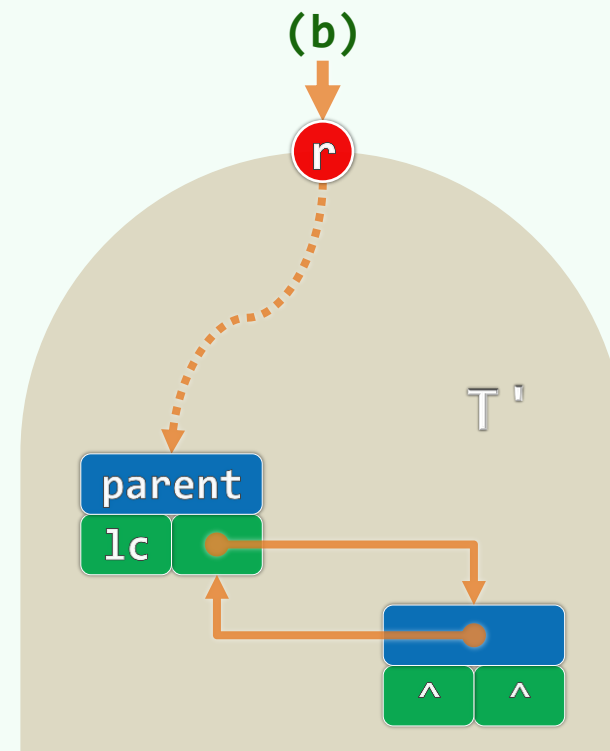
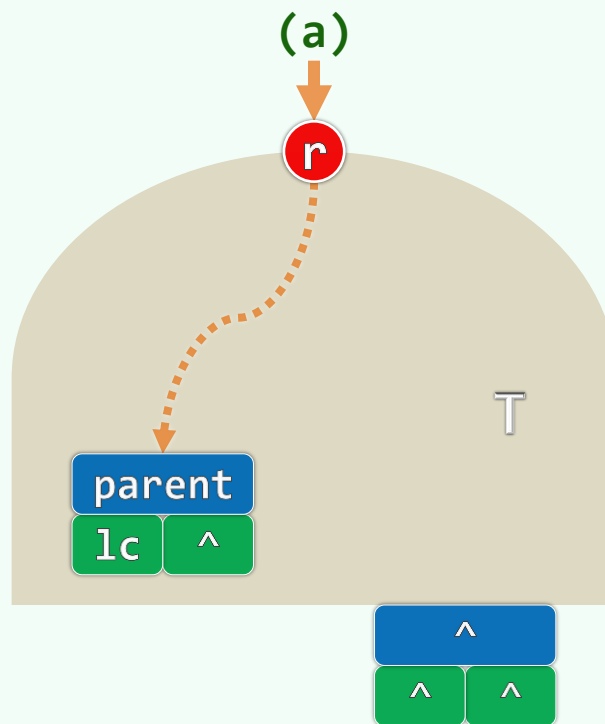
```
    _size++;
```

```
    x->insertAsRC(e);
```

```
    updateHeightAbove(x);
```

```
    return x->rc;
```

```
} //insertAsLC()对称
```



❖ x接入后，祖先的高度**可能增加**，其余节点**必然不变**

子树接入

```
template <typename T>
```

```
BinNodePosi(T) BinTree<T>::attachAsRC( BinNodePosi(T) x, BinTree<T>* & S ) {
```

```
    if ( x->rc = S->_root )
```

```
        x->rc->parent = x;
```

```
    _size += S->_size;
```

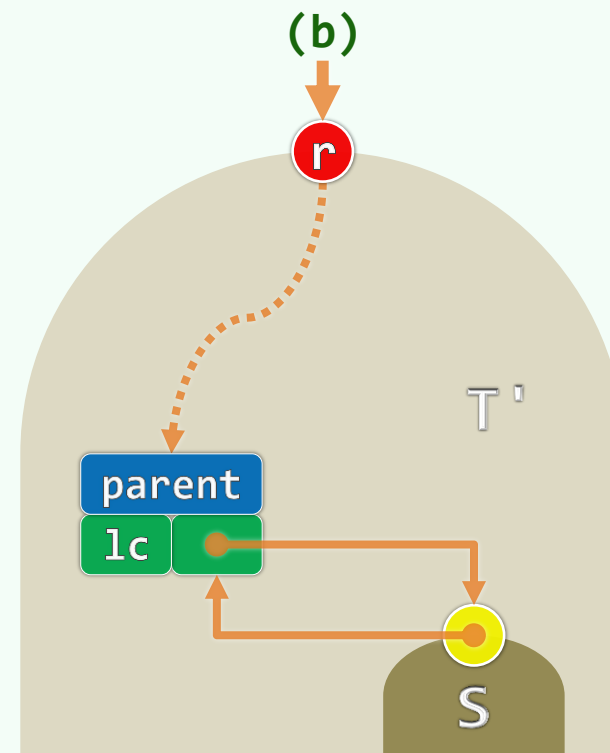
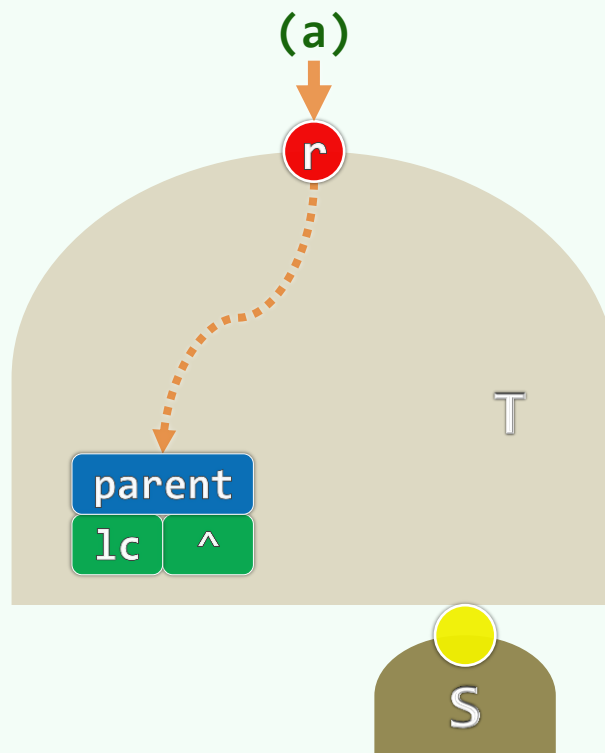
```
    updateHeightAbove(x);
```

```
    S->_root = NULL; S->_size = 0;
```

```
    release(S); S = NULL;
```

```
    return x;
```

```
} //attachAsLC()对称
```



子树删除

```
❖ template <typename T> int BinTree<T>::remove( BinNodePosi(T) x ) {  
    FromParentTo( * x ) = NULL;  
    updateHeightAbove( x->parent ); //更新祖先高度 ( 其余节点亦不变 )  
    int n = removeAt(x); _size -= n; return n;  
}
```

```
❖ template <typename T> static int removeAt( BinNodePosi(T) x ) {  
    if ( ! x ) return 0;  
    int n = 1 + removeAt( x->lc ) + removeAt( x->rc );  
    release(x->data); release(x); return n;  
}
```


子树分离

```
template <typename T> BinTree<T>* BinTree<T>::secede( BinNodePosi(T) x ) {  
  
    FromParentTo( * x ) = NULL;  
  
    updateHeightAbove( x->parent );  
  
    // 以上与BinTree<T>::remove()一致；以下还需对分离出来的子树重新封装  
  
    BinTree<T> * S = new BinTree<T>; //创建空树  
  
    S->_root = x; x->parent = NULL; //新树以x为根  
  
    S->_size = x->size(); _size -= S->_size; //更新规模  
  
    return S; //返回封装后的子树  
  
}
```