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# **Sound Field Analysis Toolbox**

## **Readme**

*Release 0.3*

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## 1.1 Requirements

Obviously, you'll need [Python](#). The code has been developed and tested on Python 3.x only. [NumPy](#) and [SciPy](#) are needed for calculations. .. If you also want to plot the resulting sound fields, you'll need [matplotlib](#).

Instead of installing all of them separately, you should probably get a Python distribution that already includes everything, e.g. [Anaconda](#).

## 1.2 How to Get Started

Various jupyter notebooks are located in the root directory/

- **AE1\_IdealPlaneWave.ipynb**: Ideal unity plane wave simulation

## 1.3 Reference

Feel free to check out the full [Reference](#).

## **GENERATORS**

Generators explanation. Module contains various generator functions:

***whiteNoise*** Generate additive White Gaussian noise

***gauss\_grid*** Gauss-Legendre quadrature grid and weights

***lebedev*** Lebedev quadrature grid and weights

***radial\_filter*** Modal radial filter

***radial\_filter\_fullspec*** Modal radial filter over the full spectrum

***sampledWave*** Sampled Wave generator, emulating discrete sampling

***ideal\_wave*** Ideal wave generator, returns spatial fourier coefficients

**sampled\_wave** This file is a wrapper generating the complex pressures at the positions given in 'gridData' for a full spectrum 0-FS/2 Hz (NFFT Bins) wave impinging on the array, emulating discrete sampling.

## PROCESSING

Processing explanation. Functions that act on the Spatial Fourier Coefficients

***FFT*** (Fast) Fourier Transform

***iFFT*** Inverse (Fast) Fourier Transform

***spatFT*** Spatial Fourier Transform

***iSpatFT*** Fast Inverse Spatial Fourier Transform

***PWDecomp*** Plane Wave Decomposition

## **PLOTTING**

Plotting explanation. Plotting functions Helps visualizing spherical microphone data.

## REFERENCE

## 5.1 Generators

Module contains various generator functions:

***whiteNoise*** Generate additive White Gaussian noise

***gauss\_grid*** Gauss-Legendre quadrature grid and weights

***lebedev*** Lebedev quadrature grid and weights

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***sampledWave*** Sampled Wave generator, emulating discrete sampling

***ideal\_wave*** Ideal wave generator, returns spatial fourier coefficients

`sound_field_analysis.gen.gauss_grid(azimuth_nodes=10, colatitude_nodes=5)`

Compute Gauss-Legendre quadrature nodes and weights in the SOFiA/VariSphear data format.

**Parameters** **ELnodes** (*AZnodes*,) – Number of azimuthal / elevation nodes

**Returns** **gridData** – SphericalGrid containing azimuth, colatitude and weights

**Return type** *io.SphericalGrid*

`sound_field_analysis.gen.ideal_wave(order, fs, azimuth, colatitude, array_configuration,  
wavetype='plane', distance=1.0, NFFT=128, delay=0.0, c=343.0)`

Ideal wave generator, returns spatial Fourier coefficients *Pnm* of an ideal wave front hitting a specified array

**Parameters**

- **order** (*int*) – Maximum transform order.
- **fs** (*int*) – Sampling frequency
- **NFFT** (*int*) – Order of FFT (number of bins), should be a power of 2
- **array\_configuration** (*ArrayConfiguration*) – List/Tuple/ArrayConfiguration, see *io.ArrayConfiguration*
- **colatitude** (*azimuth*,) – Azimuth/Colatitude angle of the wave in [RAD]
- **wavetype** ({'plane', 'spherical'}, *optional*) – Select between plane or spherical wave [Default: Plane wave]
- **distance** (*float*, *optional*) – Distance of the source in [m] (for spherical waves only)
- **delay** (*float*, *optional*) – Time Delay in s [default: 0]
- **c** (*float*, *optional*) – Propagation velocity in m/s [Default: 343m/s]

**Warning:** If NFFT is smaller than the time the wavefront needs to travel from the source to the array, the impulse response will be cyclically shifted.

**Returns** **Pnm** – Spatial Fourier Coefficients with nm coeffs in cols and FFT coeffs in rows

**Return type** array of complex floats

`sound_field_analysis.gen.lebedev(max_order=None, degree=None)`

Compute Lebedev quadrature nodes and weights given a maximum stable order. Alternatively, a degree may be supplied.

**Parameters**

- **max\_order** (*int*) – Maximum stable order of the Lebedev grid, [0 ... 11]
- **degree** (*int*, *optional*) – Lebedev Degree, one of {6, 14, 26, 38, 50, 74, 86, 110, 146, 170, 194}

**Returns** **gridData** – Lebedev quadrature positions and weights: [AZ, EL, W]

**Return type** array\_like

`sound_field_analysis.gen.radial_filter(order, freq, array_configuration, amp_maxdB=40)`

Generate modal radial filter of specified order and frequency

**Parameters**

- **order** (*array\_like*) – order of filter
- **freq** (*array\_like*) – Frequency of modal filter
- **array\_configuration** (*ArrayConfiguration*) – List/Tuple/ArrayConfiguration, see `io.ArrayConfiguration`
- **amp\_maxdB** (*int*, *optional*) – Maximum modal amplification limit in dB [Default: 40]

**Returns** **dn** – Vector of modal frequency domain filter of shape [nOrders x nFreq]

**Return type** array\_like

`sound_field_analysis.gen.radial_filter_fullspec(max_order, NFFT, fs, array_configuration, amp_maxdB=40)`

Generate NFFT/2 + 1 modal radial filter of orders 0:max\_order for frequencies 0:fs/2, wraps `radial_filter()`

**Parameters**

- **max\_order** (*int*) – Maximum order
- **NFFT** (*int*) – Order of FFT (number of bins), should be a power of 2.
- **fs** (*int*) – Sampling frequency
- **array\_configuration** (*ArrayConfiguration*) – List/Tuple/ArrayConfiguration, see `io.ArrayConfiguration`
- **amp\_maxdB** (*int*, *optional*) – Maximum modal amplification limit in dB [Default: 40]

**Returns** **dn** – Vector of modal frequency domain filter of shape [max\_order + 1 x NFFT / 2 + 1]

**Return type** array\_like



`sound_field_analysis.gen.sampled_wave` (*order*, *fs*, *NFFT*, *array\_configuration*, *gridData*, *wave\_azimuth*, *wave\_colatitude*, *wavetype*='plane', *c*=343, *distance*=1.0, *limit\_order*=85)

Returns the frequency domain data of an ideal wave as recorded by a provided array.

#### Parameters

- **fs** (*int*) – Sampling frequency
- **NFFT** (*int*) – Order of FFT (number of bins), should be a power of 2.
- **array\_configuration** (*ArrayConfiguration*) – List/Tuple/ArrayConfiguration, see `io.ArrayConfiguration`
- **gridData** (*SphericalGrid*) – List/Tuple/gauss\_grid, see `io.SphericalGrid`
- **wave\_colatitude** (*wave\_azimuth*,) – Direction of incoming wave in radians [0-2pi].
- **wavetype** ({'plane', 'spherical'}, *optional*) – Type of the wave. [Default: plane]
- **c** (*float*, *optional*) – Speed of sound in [m/s] [Default: 343 m/s]
- **distance** (*float*, *optional*) – Distance of the source in [m] (For spherical waves only)
- **limit\_order** (*int*, *optional*) – Sets the limit for wave generation

**Warning:** If NFFT is smaller than the time the wavefront needs to travel from the source to the array, the impulse response will be cyclically shifted (cyclic convolution).

**Returns** **Pnm** – Spatial fourier coefficients of resampled sound field

**Return type** `array_like`

`sound_field_analysis.gen.spherical_noise` (*azimuth\_grid*, *colatitude\_grid*, *order\_max*=8, *spherical\_harmonic\_bases*=None)

Returns band-limited random weights on a spherical surface

#### Parameters

- **colatitude\_grid** (*azimuth\_grid*,) – Grids holding azimuthal and colatitudinal angles
- **order\_max** (*int*, *optional*) – Spherical order limit [Default: 8]

**Returns** **noisy\_weights** – Noisy weights

**Return type** `array_like`, `complex`

`sound_field_analysis.gen.whiteNoise` (*fftData*, *noiseLevel*=80)

Adds White Gaussian Noise of approx. 16dB crest to a FFT block.

#### Parameters

- **fftData** (*array of complex floats*) – Input `fftData` block (e.g. from F/D/T or S/W/G)
- **noiseLevel** (*int*, *optional*) – Average noise Level in dB [Default: -80dB]

**Returns** **noisyData** – Output `fftData` block including white gaussian noise

**Return type** `array of complex floats`

## 5.2 Processing

Functions that act on the Spatial Fourier Coefficients

**FFT** (Fast) Fourier Transform

**iFFT** Inverse (Fast) Fourier Transform

**spatFT** Spatial Fourier Transform

**iSpatFT** Fast Inverse Spatial Fourier Transform

**PWDecomp** Plane Wave Decomposition

`sound_field_analysis.process.BEMA (Pnm, ctSig, dn, transition, avgBandwidth, fade=True)`

BEMA Spatial Anti-Aliasing - NOT YET IMPLEMENTED

### Parameters

- **Pnm** (*array\_like*) – Spatial Fourier coefficients
- **ctSig** (*array\_like*) – Signal of the center microphone
- **dn** (*array\_like*) – Radial filters for the current array configuration
- **transition** (*int*) – Highest stable bin, approx:  $\text{transition} = (\text{NFFT}/\text{FS} + 1) * (\text{N} * \text{c}) / (2 * \pi * \text{r})$
- **avgBandwidth** (*int*) – Averaging Bandwidth in oct
- **fade** (*bool, optional*) – Fade over if True, else hard cut {false} [Default: True]

**Returns** **Pnm** – Alias-free spatial Fourier coefficients

**Return type** *array\_like*

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**Note:** This was presented at the 2012 AES convention, see<sup>1</sup>.

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### References

`sound_field_analysis.process.FFT (time_signals, fs=None, NFFT=None, oversampling=1, first_sample=0, last_sample=None)`

Real-valued Fast Fourier Transform.

### Parameters

- **time\_signals** (*TimeSignal/tuple/object*) – Time-domain signals to be transformed. If of length 2, fs is assumed as the second element, otherwise fs has to be specified.
- **fs** (*int, optional*) – Sampling frequency - only optional if a TimeSignal or tuple/array containing fs is passed
- **NFFT** (*int, optional*) – Number of frequency bins. Resulting array will have size  $\text{NFFT}/2 + 1$  Default: Next power of 2
- **oversampling** (*int, optional*) – Oversamples the incoming signal to increase frequency resolution [Default: 1]
- **firstSample** (*int, optional*) – First time domain sample to be included. [Default: 0]
- **lastSample** (*int, optional*) – Last time domain sample to be included. [Default: -1]

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<sup>1</sup> B. Bernschütz, “Bandwidth Extension for Microphone Arrays”, AES Convention 2012, Convention Paper 8751, 2012. <http://www.aes.org/e-lib/browse.cfm?elib=16493>

**Returns**

- **fftData** (*ndarray*) – Frequency-domain data
- **f** (*ndarray*) – Frequency scale

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**Note:** An oversampling\*NFFT point Fourier Transform is applied to the time domain data, where NFFT is the next power of two of the number of samples. Time-windowing can be used by providing a `first_sample` and `last_sample` index.

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`sound_field_analysis.process.convolve(A, B, FFT=None)`

Convolve two arrays A & B row-wise. One or both can be one-dimensional for SIMO/SISO convolution

**Parameters**

- **B** (*A,* ) – Data to perform the convolution on of shape [Nsignals x NSamples]
- **FFT** (*bool, optional*) – Selects whether time or frequency domain convolution is applied. Default: On if Nsamples > 500 for both

**Returns out** – Array containing row-wise, linear convolution of A and B

**Return type** array

`sound_field_analysis.process.iFFT(Y, output_length=None, window=False)`

Inverse real-valued Fourier Transform

**Parameters**

- **Y** (*array\_like*) – Frequency domain data [Nsignals x Nbins]
- **output\_length** (*int, optional*) – Length of returned time-domain signal (Default:  $2 \times \text{len}(Y) + 1$ )
- **win** (*boolean, optional*) – Weights the resulting time-domain signal with a Hann

**Returns y** – Reconstructed time-domain signal

**Return type** array\_like

`sound_field_analysis.process.iSpatFT(spherical_coefficients, position_grid, order_max=None, spherical_harmonic_bases=None)`

Inverse spatial Fourier Transform

**Parameters**

- **spherical\_coefficients** (*array\_like*) – Spatial Fourier coefficients with columns representing frequency bins
- **position\_grid** (*array\_like or io.SphericalGrid*) – Azimuth/Colatitude angles of spherical coefficients
- **order\_max** (*int, optional*) – Maximum transform order [Default: highest available order]

**Returns P** – Sound pressures with frequency bins in columns and angles in rows

**Return type** array\_like

`sound_field_analysis.process.plane_wave_decomp(order, wave_direction, field_coeffs, radial_filter, weights=None)`

Plane wave decomposition

**Parameters**

- **order** (*int*) – Decomposition order

- **wave\_direction** (*array\_like*) – Direction of plane wave as [azimuth, colatitude] pair. `io.SphericalGrid` is used internally
- **field\_coeffs** (*array\_like*) – Spatial fourier coefficients
- **radial\_filter** (*array\_like*) – Radial filters
- **weights** (*array\_like, optional*) – Weighting function. Either scalar, one per directions or of dimension (nKR\_bins x nDirections). [Default: None]

**Returns** **Y** – Matrix of the decomposed wavefield with kr bins in rows

**Return type** matrix of floats

`sound_field_analysis.process.rfi(dn, kernelDownScale=2, highPass=0.0)`

R/F/I Radial Filter Improvement [NOT YET IMPLEMENTED!]

#### Parameters

- **dn** (*array\_like*) – Analytical frequency domain radial filters (e.g. `gen.radFilter()`)
- **kernelDownScale** (*int, optional*) – Downscale factor for the filter kernel [Default: 2]
- **highPass** (*float, optional*) – Highpass Filter from 0.0 (off) to 1.0 (maximum kr) [Default: 0.0]

#### Returns

- **dn** (*array\_like*) – Improved radial filters
- **kernelSize** (*int*) – Filter kernel size (total)
- **latency** (*float*) – Approximate signal latency due to the filters

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**Note:** This function improves the FIR radial filters from `gen.radFilter()`. The filters are made causal and are windowed in time domain. The DC components are estimated. The R/F/I module should always be inserted to the filter path when treating measured data even if no use is made of the included kernel downscaling or highpass filters.

Do NOT use R/F/I for single open sphere filters (e.g. `simulations`).

**IMPORTANT** Remember to choose a `fft-oversize` factor (`.FFT()`) being large enough to cover all filter latencies and reponse slopes. Otherwise undesired cyclic convolution artifacts may appear in the output signal.

**HIGHPASS** If HPF is on (`highPass>0`) the radial filter kernel is downscaled by a factor of two. Radial Filters and HPF share the available taps and the latency keeps constant. Be careful using very small signal blocks because there may remain too few taps. Observe the filters by plotting their spectra and impulse responses. > Be very carefull if  $NFFT/\max(kr) < 25$  > Do not use R/F/I if  $NFFT/\max(kr) < 15$

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`sound_field_analysis.process.sfe(Pnm_kra, kra, krb, problem='interior')`

S/F/E Sound Field Extrapolation. CURRENTLY WIP

#### Parameters

- **Pnm\_kra** (*array\_like*) – Spatial Fourier Coefficients (e.g. from `spatFT()`)
- **kra, krb** (*array\_like*) –  $k * r_a/r_b$  vector
- **problem** (*string{'interior', 'exterior'}*) – Select between interior and exterior problem [Default: interior]

`sound_field_analysis.process.spatFT(data, position_grid, order_max=10, spherical_harmonic_bases=None)`

Spatial Fourier Transform

#### Parameters

- **data** (*array\_like*) – Data to be transformed, with signals in rows and frequency bins in columns
- **order\_max** (*int, optional*) – Maximum transform order (Default: 10)
- **position\_grid** (*array\_like or io.SphericalGrid*) – Azimuths/Colatitudes/Gridweights of spatial sampling points

**Returns** **Pnm** – Spatial Fourier Coefficients with nm coeffs in rows and FFT bins in columns

**Return type** *array\_like*

`sound_field_analysis.process.spatFT_LSF(data, position_grid, order_max, spherical_harmonic_bases=None)`

Returns spherical harmonics coefficients least square fitted to provided data

#### Parameters

- **data** (*array\_like, complex*) – Data to be fitted to
- **position\_grid** (*array\_like, or io.SphericalGrid*) – Azimuth / colatitude data locations
- **order\_max** (*int*) – Maximum order N of fit

**Returns** **coefficients** – Fitted spherical harmonic coefficients (indexing:  $n^2 + n + m + 1$ )

**Return type** *array\_like, float*

`sound_field_analysis.process.wdr(Pnm, xAngle, yAngle, zAngle)`

W/D/R Wigner-D Rotation - NOT YET IMPLEMENTED

#### Parameters

- **Pnm** (*array\_like*) – Spatial Fourier coefficients
- **yAngle, zAngle** (*xAngle,*) – Rotation angle around the x/y/z-Axis

**Returns** **PnmRot** – Rotated spatial Fourier coefficients

**Return type** *array\_like*

## 5.3 Plotting

Plotting functions Helps visualizing spherical microphone data.

`sound_field_analysis.plot.genFlat(vizMTX)`

Returns trace of flat surface with intensity as surface elevation and color

**Parameters** **vizMTX** (*array\_like*) – Matrix holding spherical data for visualization

**Returns** **T** – Trace of desired surface

**Return type** *plotly\_trace*

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#### Todo

Fix orientation and axis limits

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`sound_field_analysis.plot.genShape(vizMTX)`

Returns trace of shape with intensity as radial extension

**Parameters** **vizMTX** (*array\_like*) – Matrix holding spherical data for visualization

**Returns** **T** – Trace of desired shape

**Return type** *plotly\_trace*

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**Todo**Fix camera position

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`sound_field_analysis.plot.genSphCoords()`

Generates cartesian (x,y,z) and spherical (theta, phi) coordinates of a sphere :returns: **coords** – holds cartesian (x,y,z) and spherical (theta, phi) coordinates :rtype: named tuple

`sound_field_analysis.plot.genSphere(vizMTX)`

Returns trace of sphere with intensity as surface color

**Parameters** **vizMTX** (*array\_like*) – Matrix holding spherical data for visualization

**Returns** **T** – Trace of desired sphere

**Return type** `plotly_trace`

`sound_field_analysis.plot.genVisual(vizMTX, style='shape', normalize=True, logScale=False)`

Returns desired trace after cleaning the data

**Parameters**

- **vizMTX** (*array\_like*) – Matrix holding spherical data for visualization
- **style** (*string* {'shape', 'sphere', 'flat'}, *optional*) – Style of visualization. [Default: 'Shape']
- **normalize** (*Bool*, *optional*) – Toggle normalization of data to [-1 ... 1] [Default: True]

**Returns** **T** – Trace of desired visualization

**Return type** `plotly_trace`

`sound_field_analysis.plot.layout_2D(type=None, title=None)``sound_field_analysis.plot.makeFullMTX(Pnm, dn, kr, viz_order=None)`

Generates visualization matrix for a set of spatial fourier coefficients over all kr :param Pnm: Spatial Fourier Coefficients (e.g. from S/T/C) :type Pnm: *array\_like* :param dn: Modal Radial Filters (e.g. from M/F) :type dn: *array\_like* :param kr: kr-vector :type kr: *array\_like* :param viz\_order: Order of the spatial fourier tplane\_wave\_decompransform [Default: Highest available] :type viz\_order: *int*, *optional*

**Returns** **vizMtx** – Computed visualization matrix over all kr

**Return type** *array\_like*

`sound_field_analysis.plot.makeMTX(spat_coeffs, radial_filter, kr_IDX, viz_order=None, stepsize_deg=1)`

Returns a plane wave decomposition over a full sphere

**Parameters**

- **spat\_coeffs** (*array\_like*) – Spatial fourier coefficients
- **radial\_filter** (*array\_like*) – Modal radial filters
- **kr\_IDX** (*int*) – Index of kr to be computed
- **viz\_order** (*int*, *optional*) – Order of the spatial fourier transform [Default: Highest available]
- **stepsize\_deg** (*float*, *optional*) – Integer Factor to increase the resolution. [Default: 1]

**Returns** **mtxData** – Plane wave decomposition (frequency domain)

**Return type** *array\_like*

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**Note:** The file generates a Matrix of 181x360 pixels for the visualisation with visualize3D() in 1[deg] Steps (65160 plane waves).

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`sound_field_analysis.plot.normalizeMTX (MTX, logScale=False)`

Normalizes a matrix to [0 ... 1]

**Parameters**

- **MTX** (*array\_like*) – Matrix to be normalized
- **logScale** (*bool*) – Toggle conversion logScale [Default: False]

**Returns** MTX – Normalized Matrix

**Return type** array\_liked

`sound_field_analysis.plot.plot2D (data, title=None, viz_type=None, fs=None)`

Visualize 2D data using plotly.

**Parameters**

- **data** (*array\_like*) – Data to be plotted, separated along the first dimension (rows).
- **title** (*string*) – Add title to be displayed on plot
- **type** (*string*{None, 'time', 'linFFT', 'logFFT'}) – Type of data to be displayed. [Default: None]
- **fs** (*int*) – Sampling rate in Hz. [Default: 44100]

`sound_field_analysis.plot.plot3D (vizMTX, style='shape', layout=None, colorize=True, logScale=False)`

Visualize matrix data, such as from makeMTX(Pnm, dn)

**Parameters**

- **vizMTX** (*array\_like*) – Matrix holding spherical data for visualization
- **style** (*string*{'shape', 'sphere', 'flat'}, *optional*) – Style of visualization. [Default: 'shape']
- **normalize** (*Bool*, *optional*) – Toggle normalization of data to [-1 ... 1] [Default: True]

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**Todo**

Colorization, contour plot

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`sound_field_analysis.plot.plot3Dgrid (rows, cols, viz_data, style, normalize=True)`

`sound_field_analysis.plot.prepare_2D_traces (data, viz_type=None, fs=None)`

`sound_field_analysis.plot.prepare_2D_x (L, viz_type=None, fs=None)`

`sound_field_analysis.plot.showTrace (trace, layout=None, title=None)`

Wrapper around plotlys offline .plot() function

**Parameters**

- **trace** (*plotly\_trace*) – Plotly generated trace to be displayed offline
- **colorize** (*Bool*, *optional*) – Toggles bw / colored plot [Default: True]

**Returns** fig – JSON representation of generated figure

**Return type** plotly\_fig\_handle

`sound_field_analysis.plot.sph2cartMTX (vizMTX)`

Converts the spherical vizMTX data to named tuple contaibubg .xs/.ys/.zs

**Parameters** **vizMTX** (*array\_like*) – [180 x 360] matrix that hold amplitude information over phi and theta

**Returns** **V** – Contains .xs, .ys, .zs cartesian coordinates

**Return type** `named_tuple`

## 5.4 Sphericals

Collection of spherical helper functions:

**sph\_harm** More robust spherical harmonic coefficients

**spbessel / dspbessel** Spherical Bessel and derivative

**spneumann / dspneumann** Spherical Neumann (Bessel 2nd kind) and derivative

**sphankel / dsphankel** Spherical Hankel (second kind) and derivative

**cart2sph / sph2cart** Convert cartesian to spherical coordinates and vice versa

**sound\_field\_analysis.sph.array\_extrapolation** (*order, freqs, array\_configuration, normalize=True*)

Factor that relate signals recorded on a sphere to it's center. In the rigid configuration, a scatter\_radius that is different to the array radius may be set.

**Parameters**

- **order** (*int*) – Order
- **freqs** (*array\_like*) – Frequencies
- **array\_configuration** (*ArrayConfiguration*) – List/Tuple/ArrayConfiguration, see `io.ArrayConfiguration`
- **normalize** (*Bool, optional*) – Normalize by  $4 * \pi * 1j^{**} \text{order}$  (Default: True)

**Returns** **b** – Coefficients of shape [nOrder x nFreqs]

**Return type** `array, complex`

**sound\_field\_analysis.sph.besselj** (*n, z*)

Bessel function of first kind of order n at kr. Wraps `scipy.special.jn(n, z)`.

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **J** – Values of Bessel function of order n at position z

**Return type** `array_like`

**sound\_field\_analysis.sph.bn\_dual\_open\_omni** (*n, kr1, kr2*)

**sound\_field\_analysis.sph.bn\_open\_cardioid** (*n, krm*)

**sound\_field\_analysis.sph.bn\_open\_omni** (*n, krm*)

**sound\_field\_analysis.sph.bn\_rigid\_cardioid** (*n, krm, krs*)

**sound\_field\_analysis.sph.bn\_rigid\_omni** (*n, krm, krs*)

**sound\_field\_analysis.sph.cart2sph** (*x, y, z*)

Converts cartesian coordinates x, y, z to spherical coordinates az, el, r.

**sound\_field\_analysis.sph.dspbessel** (*n, kr*)

Derivative of spherical Bessel (first kind) of order n at kr

**Parameters**



- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **J'** – Derivative of spherical Bessel

**Return type** complex float

`sound_field_analysis.sph.dsphankel1(n, kr)`

Derivative spherical Hankel (first kind) of order n at kr

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **dhn1** – Derivative of spherical Hankel function hn' (second kind)

**Return type** complex float

`sound_field_analysis.sph.dsphankel2(n, kr)`

Derivative spherical Hankel (second kind) of order n at kr

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **dhn2** – Derivative of spherical Hankel function hn' (second kind)

**Return type** complex float

`sound_field_analysis.sph.dspneumann(n, kr)`

Derivative spherical Neumann (Bessel second kind) of order n at kr

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **Yv'** – Derivative of spherical Neumann (Bessel second kind)

**Return type** complex float

`sound_field_analysis.sph.hankel1(n, z)`

Bessel function of third kind (Hankel function) of order n at kr. Wraps `scipy.special.hankel1(n, z)`

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **H1** – Values of Hankel function of order n at position z

**Return type** array\_like

`sound_field_analysis.sph.hankel2(n, z)`

Bessel function of third kind (Hankel function) of order n at kr. Wraps `scipy.special.hankel2(n, z)`

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **H2** – Values of Hankel function of order n at position z

**Return type** array\_like

`sound_field_analysis.sph.kr(f, radius, temperature=20)`

Return kr vector for given f and array radius

**Parameters**

- **f** (*array\_like*) – Frequencies to calculate the kr for
- **radius** (*float*) – Radius of array
- **temperature** (*float, optional*) – Room temperature in degree Celcius [Default: 20]

**Returns** **kr** –  $2 * \pi * f / c(\text{temperature}) * r$

**Return type** *array\_like*

`sound_field_analysis.sph.kr_full_spec(fs, radius, NFFT, temperature=20)`

Returns full spectrum kr

**Parameters**

- **fs** (*int*) – Sampling rate in Hertz
- **radius** (*float*) – Radius
- **NFFT** (*int*) – Number of frequency bins
- **temperature** (*float, optional*) – Temperature in degree Celcius (Default: 20 C)

**Returns** **kr** – kr vector of length NFFT/2 + 1 spanning the frequencies of 0:fs/2

**Return type** *array\_like*

`sound_field_analysis.sph.mnArrays(nMax)`

Returns degrees n and orders m up to nMax.

**Parameters** **nMax** (*int*) – Maximum degree of coefficients to be returned.  $n \geq 0$

**Returns**

- **m** (*int, array\_like*) – 0, -1, 0, 1, -2, -1, 0, 1, 2, ... , -nMax ..., nMax
- **n** (*int, array\_like*) – 0, 1, 1, 1, 2, 2, 2, 2, ... nMax, nMax, nMax

`sound_field_analysis.sph.neumann(n, z)`

Bessel function of second kind (Neumann / Weber function) of order n at kr. Implemented as  $(\text{hankel1}(n, z) - \text{besselj}(n, z)) / 1j$

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **Y** – Values of Hankel function of order n at position z

**Return type** *array\_like*

`sound_field_analysis.sph.spbessel(n, kr)`

Spherical Bessel function (first kind) of order n at kr

**Parameters**

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **J** – Spherical Bessel

**Return type** *complex float*

`sound_field_analysis.sph.sph2cart(az, el, r)`

Converts spherical coordinates az, el, r to cartesian coordinates x, y, z.

`sound_field_analysis.sph.sph_harm(m, n, az, el, type='complex')`

Compute spherical harmonics

**Parameters**

- **m** ((int)) – Order of the spherical harmonic.  $\text{abs}(m) \leq n$
- **n** ((int)) – Degree of the harmonic, sometimes called l.  $n \geq 0$
- **az** ((float)) – Azimuthal (longitudinal) coordinate [0, 2pi], also called Theta.
- **el** ((float)) – Elevation (colatitudinal) coordinate [0, pi], also called Phi.

**Returns** **y\_mn** – Complex spherical harmonic of order m and degree n, sampled at theta = az, phi = el

**Return type** (complex float)

`sound_field_analysis.sph.sph_harm_all (nMax, az, el, type='complex')`

Compute all spherical harmonic coefficients up to degree nMax.

**Parameters**

- **nMax** ((int)) – Maximum degree of coefficients to be returned.  $n \geq 0$
- **az** ((float), array\_like) – Azimuthal (longitudinal) coordinate [0, 2pi], also called Theta.
- **el** ((float), array\_like) – Elevation (colatitudinal) coordinate [0, pi], also called Phi.

**Returns** **y\_mn** – Complex spherical harmonics of degrees n [0 ... nMax] and all corresponding orders m [-n ... n], sampled at [az, el]. dim1 corresponds to az/el pairs, dim2 to order/degree (m, n) pairs like 0/0, -1/1, 0/1, 1/1, -2/2, -1/2 ...

**Return type** (complex float), array\_like

`sound_field_analysis.sph.sph_harm_large (m, n, az, el)`

Compute spherical harmonics for large orders > 84

**Parameters**

- **m** ((int)) – Order of the spherical harmonic.  $\text{abs}(m) \leq n$
- **n** ((int)) – Degree of the harmonic, sometimes called l.  $n \geq 0$
- **az** ((float)) – Azimuthal (longitudinal) coordinate [0, 2pi], also called Theta.
- **el** ((float)) – Elevation (colatitudinal) coordinate [0, pi], also called Phi.

**Returns**

- **y\_mn** ((complex float)) – Complex spherical harmonic of order m and degree n, sampled at theta = az, phi = el
- $Y_{n,m}(\theta, \phi) = ((n - m)! * (2l + 1)) / (4\pi * (l + m))^{0.5} * \exp(i m \phi) * P_n^m(\cos(\theta))$
- **as per** <http://dlmf.nist.gov/14.30>
- $P_m(z)$  is the associated Legendre function of the first kind, like `scipy.special.lpmv`
- `scipy.special.lpmn` calculates  $P(0...m, 0...n)$  and its derivative but won't return +inf at high orders

`sound_field_analysis.sph.sphankel1 (n, kr)`

Spherical Hankel (first kind) of order n at kr

**Parameters**

- **n** (array\_like) – Order
- **kr** (array\_like) – Argument

**Returns** **hn1** – Spherical Hankel function hn (first kind)

**Return type** complex float

`sound_field_analysis.sph.sphankel12` (*n*, *kr*)

Spherical Hankel (second kind) of order *n* at *kr*

#### Parameters

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **hn2** – Spherical Hankel function *hn* (second kind)

**Return type** complex float

`sound_field_analysis.sph.spherical_extrapolation` (*order*, *array\_configuration*,  
*k\_mic*, *k\_scatter*=None,  
*k\_dual*=None)

Factor that relate signals recorded on a sphere to it's center.

#### Parameters

- **order** (*int*) – Order
- **array\_configuration** (*ArrayConfiguration*) – List/Tuple/ArrayConfiguration, see `io.ArrayConfiguration`
- **k\_mic** (*array\_like*) – K vector for microphone array
- **k\_scatter** (*array\_like*, *optional*) – K vector for scatterer (Default: same as *k\_mic*)

**Returns** **b**

**Return type** array, complex

`sound_field_analysis.sph.spneumann` (*n*, *kr*)

Spherical Neumann (Bessel second kind) of order *n* at *kr*

#### Parameters

- **n** (*array\_like*) – Order
- **kr** (*array\_like*) – Argument

**Returns** **Yv** – Spherical Neumann (Bessel second kind)

**Return type** complex float

## 5.5 I/O

Input-Output functions

**class** `sound_field_analysis.io.ArrayConfiguration`

Tuple of type `ArrayConfiguration`

#### Parameters

- **array\_radius** (*float*) – Radius of array
- **array\_type** (*{'open', 'rigid'}*) – Type array
- **transducer\_type** (*{'omni', 'cardioid'}*) – Type of transducer,
- **scatter\_radius** (*float*, *optional*) – Radius of scatterer, required for *array\_type* == 'rigid'. (Default: equal to *array\_radius*)
- **dual\_radius** (*float*, *optional*) – Radius of second array, required for *array\_type* == 'dual'

**class** `sound_field_analysis.io.ArraySignal`

Tuple of type `ArraySignal`

**Parameters**

- **signals** (*TimeSignal*) – Holds time domain signals and sampling frequency fs
- **grid** (*SphericalGrid*) – Location grid of all time domain signals
- **configuration** (*ArrayConfiguration*) – Information on array configuration
- **temperature** (*array\_like, optional*) – Temperature in room or at each sampling position

**class** `sound_field_analysis.io.SphericalGrid`

Tuple of type *SphericalGrid*

**Parameters**

- **Colatitude** (*Azimuth,*) –
- **Weights** (*Radius,*) –

**class** `sound_field_analysis.io.TimeSignal`

Tuple of type *TimeSignal*

**Parameters**

- **signal** (*array\_like*) – Array of signals of shape [nSignals x nSamples]
- **fs** (*int*) – Sampling frequency
- **delay** (*float*) –

`sound_field_analysis.io.empty_time_signal` (*no\_of\_signals, signal\_length*)

Returns an empty np rec array that has the proper data structure

**Parameters**

- **no\_of\_signals** (*int*) – Number of signals to be stored in the recarray
- **signal\_length** (*int*) – Length of the signals to be stored in the recarray

**Returns**

- **time\_data** (*recarray*) – Structured array with following fields:
- **::** – .signal [Channels X Samples] .fs Sampling frequency in [Hz] .azimuth Azimuth of sampling points .colatitude Colatitude of sampling points .radius Array radius in [m] .grid\_weights Weights of quadrature .air\_temperature Average temperature in [C]

`sound_field_analysis.io.load_time_signal` (*filename*)

Convenience function to load saved np data structures

**Parameters** **filename** (*string*) – File to load

**Returns**

- **time\_data** (*recarray*) – Structured array with following fields:
- **::** – .IR [Channels X Samples] .fs Sampling frequency in [Hz] .azimuth Azimuth of sampling points .colatitude Colatitude of sampling points .radius Array radius in [m] .grid\_weights Weights of quadrature .air\_temperature Average temperature in [C]

`sound_field_analysis.io.read_miro_struct` (*file\_name, channel='irChOne', transducer\_type='omni', scatter\_radius=None*)

Reads miro matlab files.

**Parameters**

- **matFile** (*filepath*) – Path to file that has been exported as a struct
- **channel** (*string, optional*) – Channel that holds required signals. Default: 'irChOne'

- **transducer\_type** (*{omni, cardoid}*, *optional*) – Sets the type of transducer used in the recording. Default: omni
- **scatter\_radius** (*float*, *option*) – Radius of the scatterer. Default: None

**Returns** **array\_signal** – Tuple containing a TimeSignal *signal*, SphericalGrid *grid*, ArrayConfiguration *configuration* and the air temperature

**Return type** *ArraySignal*

`sound_field_analysis.io.read_wavefile(filename)`

Reads in wavefiles and returns data [Nsig x Nsamples] and fs :param filename, string: Filename of wave file to be read

**Returns**

- *data, array\_like* – Data of dim [Nsig x Nsamples]
- *fs, int* – Sampling frequency of read data

`sound_field_analysis.io.write_SSR_IRs(filename, time_data_l, time_data_r)`

Takes two time signals and writes out the horizontal plane as HRIRs for the SoundScapeRenderer

**Parameters**

- **filename** (*string*) – filename to write to
- **time\_data\_l** (*time\_data\_l*,) – time\_data arrays for left/right channel.

## 5.6 lebedev

Generate Lebedev grid and coefficients This module only exposes the function `lebGrid = lebedev.genGrid(degree)`.

lebGrid is a named tuple containing the coordinates .x, .y, .z and the weights .w Possible degrees: 6, 14, 26, 38, 50, 74, 86, 110, 146, 170, 194

Adapted from Richard P. Mullers Python version, [https://github.com/gabrielelanaro/pyquante/blob/master/Data/lebedev\\_write.py](https://github.com/gabrielelanaro/pyquante/blob/master/Data/lebedev_write.py) C version: Dmitri Laikov F77 version: Christoph van Wuelen, <http://www.ccl.net>

Users of this code are asked to include reference [1] in their publications, and in the user- and programmers-manuals describing their codes.

[1] V.I. Lebedev, and D.N. Laikov ‘A quadrature formula for the sphere of the 131st algebraic order of accuracy’ Doklady Mathematics, Vol. 59, No. 3, 1999, pp. 477-481.

`sound_field_analysis.lebedev.genGrid(n)`

Returns Lebedev coefficients of n'th degree

**Parameters** **n** (*int{6, 14, 26, 38, 50, 74, 86, 110, 146, 170, 194}*) – Lebedev degree

**Returns** **lebGrid** – lebGrid is a named tuple containing .x, .y, .z and .w

**Return type** named tuple

## 5.7 Utilities

Miscellaneous utility functions

`sound_field_analysis.utils.current_time()`

`sound_field_analysis.utils.db(data, power=False)`

Convenience function to calculate the  $20 \cdot \log_{10}(\text{abs}(x))$

**Parameters**

- **data** (*array\_like*) – signals to be converted to db
- **power** (*boolean*) – data is a power signal and only needs factor 10

**Returns** **db** –  $20 * \log_{10}(\text{abs}(\text{data}))$

**Return type** *array\_like*

`sound_field_analysis.utils.deg2rad(deg)`  
Converts from degree [0 ... 360] to radiant [0 ... 2 pi]

`sound_field_analysis.utils.env_info()`  
Guess environment based on `sys.modules`.

**Returns** **env** – Guesed environment

**Return type** `string`{ 'jupyter\_notebook', 'ipython\_terminal', 'terminal' }

`sound_field_analysis.utils.frq2kr(target_frequency, freq_vector)`  
Returns the kr bin closest to the target frequency

**Parameters**

- **fTarget** (*float*) – Target frequency
- **fVec** (*array\_like*) – Array containing the available frequencys

**Returns** **krTarget** – kr bin closest to target frequency

**Return type** *int*

`sound_field_analysis.utils.interleave_channels(left_channel, right_channel, style=None)`

Interleave left and right channels. Style == 'SSR' checks if we total 360 channels

`sound_field_analysis.utils.nearest_to_value(array, target_val)`  
Returns nearest value inside an array

`sound_field_analysis.utils.nearest_to_value_IDX(array, target_val)`  
Returns nearest value inside an array

`sound_field_analysis.utils.nearest_to_value_logical_IDX(array, target_val)`  
Returns logical indices of nearest values inside array

`sound_field_analysis.utils.progress_bar(curIDX, maxIDX=None, description='Progress')`

Display a spinner or a progress bar

**Parameters**

- **curIDX** (*int*) – Current position in the loop
- **maxIDX** (*int, optional*) – Number of iterations. Will force a spinner if set to None. [Default: None]
- **description** (*string, optional*) – Clarify what's taking time

`sound_field_analysis.utils.rad2deg(rad)`  
Converts from radiant [0 ... 2 pi] to degree [0 ... 360]

`sound_field_analysis.utils.scalar_broadcast_match(a, b)`  
Returns arguments as `np.array`, if one is a scalar it will broadcast the other one's shape.

`sound_field_analysis.utils.simple_resample(data, original_fs, target_fs)`  
Wrap `scipy.signal.resample` with a simpler API

`sound_field_analysis.utils.stack(vector_1, vector_2)`  
Stacks two 2D vectors along the same-sized dimension or the smaller one

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