

Jan 28, 2021

Welcome to CMPE258 I

First Day of the Class

Harry LI, github/hualili/opencv/deep-learning-2020S

20-2021S Email: hualili@sjsu.edu

Office Hours M.W. 4:30-5:30 PM.

Zoom Based

(650) 400-1116 Text Only

On-Line Material

github/hualili

CANVAS

Homework Assignment

Collect Submission of Homework

Write/Submit Pseudo Code (Brief Summary) Report

1 page

Note, Post a

Sample on github Latex

3. Homework Submission

if Submission (Including Semester Long team Projects).

Action 2: Form 4-person Team

By Feb 14 week; work has to Individual/Encourage team Discussion.

Grading Policy: { Mid: 30%
Homework: 30%
Final: 40%

x Introduction

Neural Nets

Biological System
Human Brain

Neurons (Cells)

Note: Python 3. Python Virtual Environment

3 major Areas { Handwritten Nerals
Recognition MNIST

{ Time Series Prediction LSTM

{ C.V. ROI.
Deep NN

Subjects

③ FaceNet, ResNet

④ Deep Reinforcement Learning

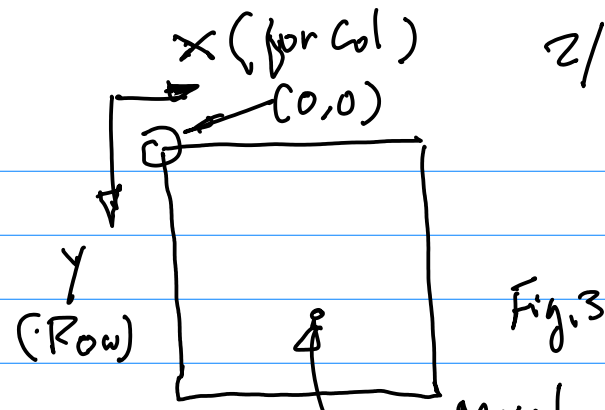
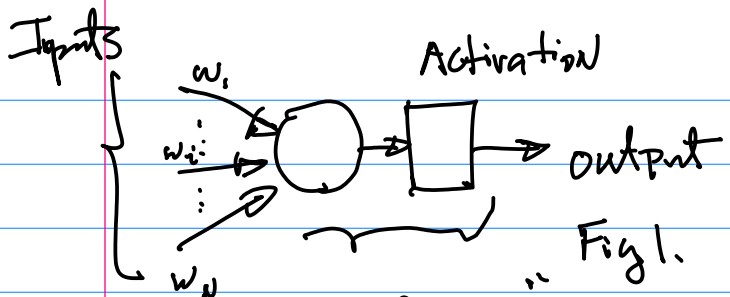
DRL
Action - Policy - Reward

Virtual Box
and O.S.

U.B. (Free)

Native O.S.

Note: Python 3. Python Virtual Environment



Prof. Carver Mead — "Silicon Brain"
Intel Processor ~1992-94, ↓

Note: 1° "Scanning" ~ Resolution
From L to R, top to B
"L2R, T2B"

~1994-95 "Father of VLSI"
Autonomous System ↓

2° Resolution 1024 x 768

2005-2006 Stanford Group + Google
Self Driving Market Hung

No. of column No. of Row
M x N → 1024 x 768
Column X Row y

2013 Alex Net (Deep Convolutional Neural Network)
CUDA GPU Architecture

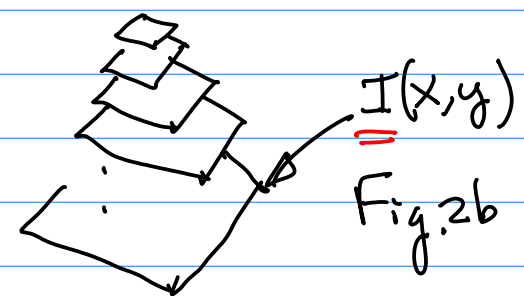
Recently: FaceNet, ResNet
Time Series Analysis (LSTM)
Deep Reinforcement

3° Color Image Vector
Color Space (r, g, b)
Primitive Color

Computer Vision
Retina of Photo Receptors
~10 layers.
110 ~ 120 million P.R.
Eye Optic N. (Brain Cells)
~ 1 million

r — red;
g — green;
b — blue

Fig. 2a
Image Pyramid



color cube
Fig. 4
(0,0,0) Black (1,1,1) White
grey scale as Traveling from (0,0,0) towards (1,1,1)

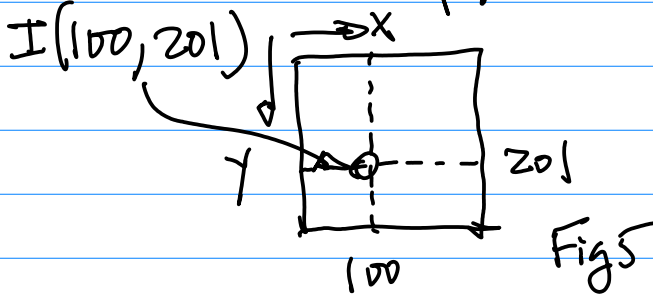
Highest Red $(r, g, b) = (1, g, b)$

" Green $(r, g, b) = (r, 1, b)$

" Blue $(r, g, b) = (r, g, 1)$

$I(x, y)$ Intensity in terms of (r, g, b)

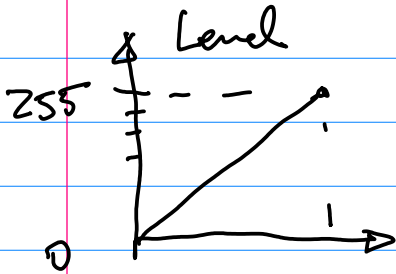
① Location on the Image Plane



r : 8 bit $[0, 255]$ ($2^8 = 256$)

g, b : 8 bit, " "

Pixel Depth (BPP: Bit Per Pixel) Quantization Level

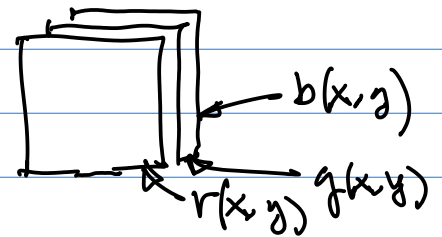


For 8 bit

GrayScale Image

$$I(x, y)_g = \frac{1}{3} [r(x, y) + g(x, y) + b(x, y)] \dots (1)$$

r, g, b . Convert Color Image to GrayScale Image



Example: Suppose an $I(x, y)$ is given below,

0	2	3	10	0
0	2	3	0	0
0	2	3	0	0
0	2	3	0	0
0	2	3	0	0

$M \times N$

Action 3. Enable OpenCV

.... Display A "Jpg"

Color Image \rightarrow From your Smart

Feb 4th, CMPE258

Today's Topics: 1^o Convolution, Two Dimensional Convolution; 2^o Intro to Neural Network

Note: 1^o Installation of Python, OpenCV, and T.F.

Python { 2.7
3.5 or higher

Anaconda — Python Distribution \rightarrow Python Virtual Environment

OpenCV 4.2 Version 3.0 or higher

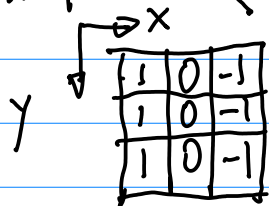
T.F. Keras (API)

Given a digital image

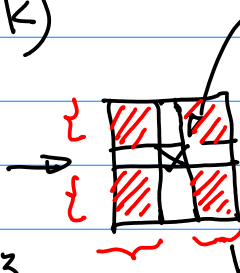
$$I(x, y) \rightarrow r(x, y), g(x, y), b(x, y)$$

Perform Convolution on $I(x,y)$

Convolution kernel (mask)



3x3



Center of the kernel

pixel of Interest

$$\textcircled{2} f(i,j) g(x-i, y-j)$$

$$\textcircled{3} g(x-i, y-j)$$

Shift

$$g(1-i, 1-j)$$

$$g(2-i, 1-j)$$

$$g(2-i, 2-j)$$

Ref: [2020s] ... 2D Convolution

From 1D Case, given a function $f(x)$ and a kernel $g(x)$

$$\int_{\Omega} f(u) g(x-u) du \quad \dots (1)$$

$$\sum_{i \in \Omega} f(i) g(x-i) \quad \dots (2)$$

Now, 2D Case

$$\iint_{\phi} f(u,v) g(x-u, y-v) du dv \quad \dots (3)$$

$$\sum_j \sum_i f(i,j) g(x-i, y-j) \quad \dots (4)$$

Image

Kernel

Index of pixel location

$$\text{Kernel } g(x,y) \rightarrow g(-x, -y)$$

① Flip



a) Flips the Kernel

b) $g(x,y) = g(-x, -y)$ if Symmetric

$$\begin{aligned} & f(0,0) * 1 + f(1,0) * 0 + \\ & f(2,0) * (-1) + \\ & f(0,1) * 1 + f(1,1) * 0 + \\ & f(2,1) * (-1) + \end{aligned}$$

and so on ...

Summary: 2D Convolution consists of shift-product-summation

Compute 2D Convolution:

Step 1. Place the kernel @

the initial condition, e.g.,

the top left hand corner

of the image, in such a way

its boundary rows and

columns are aligned with

the image boundary row

and column.

$$f(0,2) \times 1 + f(1,2) \times 0 + f(2,2) \times (-1)$$

$$= 0 \times 1 + 2 \times 0 + 3 \times (-1) +$$

$$0 \times 1 + 2 \times 0 + 3 \times (-1) +$$

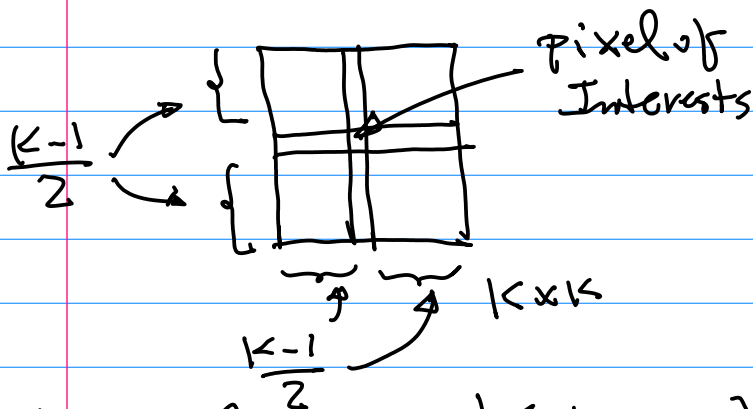
$$0 \times 1 + 2 \times 0 + 3 \times (-1)$$

$$= -3 - 3 - 3 = -9$$

Note: This convolution resulted in a new processed image plane

$I_{\text{new}}(x, y)$ whose Rows is less than the original image,
 No. of Rows = Original No. of Rows - 2

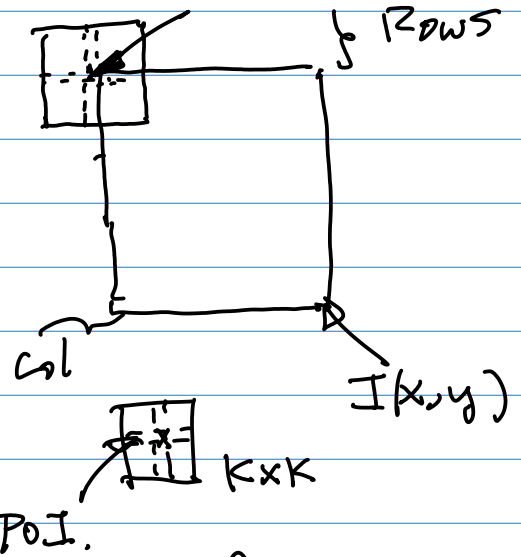
for 3×3 kernel, for $K \times K$ kernel (K is odd Number), in this case
 No. of Rows Reduced by $2 \times \left(\frac{K-1}{2}\right)$
 $= K-1$.



Homework (Exercise — No Submission)

Based on the given $I(x, y)$ Image from PPT @ github, Perform hand Calculation of 2D Convolution

Note follow the example in Class.



Consider Neural Networks.

Supervised Learning

Reference: 20-20215-2

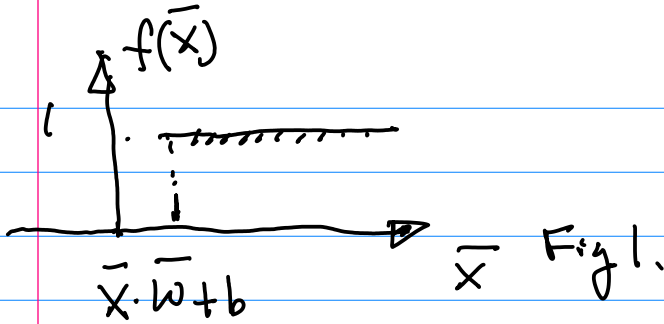
Example: \bar{x}
 Input (x_1, x_2, \dots, x_n)
 Weights (w_1, w_2, \dots, w_n)
 $\bar{x} \cdot \bar{w} = (x_1, x_2, \dots, x_n) \cdot (w_1, w_2, \dots, w_n)$

$$= x_1 w_1 + x_2 w_2 + \dots + x_n w_n + \dots + x_n w_n$$

$$= \sum_{i=1}^n x_i w_i \quad \dots (1)$$

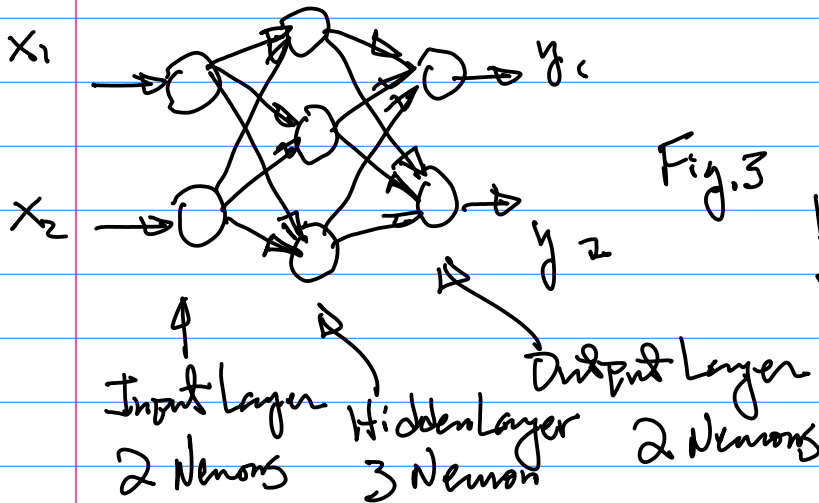
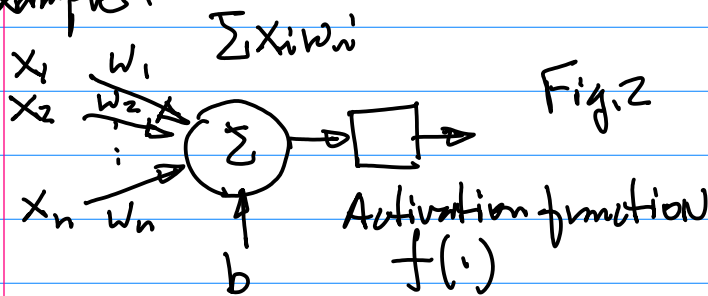
Define Transfer function $f(\cdot)$ as follows

$$f(\bar{x}) = \begin{cases} 1 & \sum_{i=1}^n x_i w_i + b > 0 \\ 0 & \text{o/w} \end{cases} \quad \dots (2)$$



Consider a Simple Feedforward NN

Example:



Feed Forward

Have Training Dataset ϕ or Ω

Two Classes C_1, C_2 Representing 2 Patterns

Feature Vector $X = (x_1, x_2)$, up to N_1 of them

N_1, N_2 do not have to be equal; up to N_2 for C_2

$$w_i = w_i + \Delta w_i = w_i + \eta (d - y) x_i$$

updated Current ~

Rate

Training (Learning)

desired output

Actual output

1. A Single Neuron

Block Diagram

Notation

$$\bar{x} = (x_1, \dots, x_n)$$

$$y = f(\bar{x}) = f(x_1, x_2, \dots, x_n)$$

Activation function

$$2. S(x) = \frac{1}{1 + e^{-x}}$$

Sigmoid

Feb 11,

Today's Topics: 1° Introduction to NN; 2° Coding (Python)

Examples.

Action 1: Form 4-Person Team. Submit your team member information By Friday 5:00 pm.

Subject: CMPE258 First Last Name of the group Coordinator

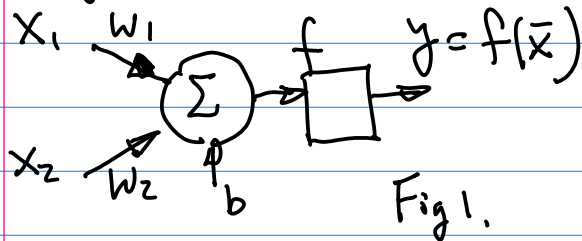
First, Last Name, Last 4 Digits of your SID; E-mail Contact information;

Homework 1: Due A week from Today; Submission to CANVAS.

Consider Dense Feedforward NN From the PPT.

3. Python Implementation

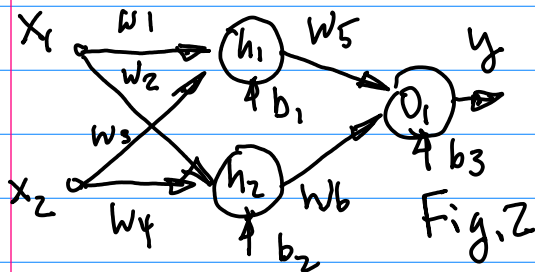
Create A template for your program header,



$$x_1 = 2, x_2 = 3, w_1 = 0, w_2 = 1.$$

$$b = 4, f(x) = \text{Sigmoid}(x)$$

4. Feedforward NN



5. Data Set \rightarrow Pre-processing
to allow Activation
function to Better
handle the input values

Supervised Learning

Data \rightarrow Its Categories Known

Labeling Images/Videos \rightarrow
Annotation.

ImageNet \sim 1.4 million Test
Images

6. Loss Function \rightarrow Objective
Function
Subset
SuperSet

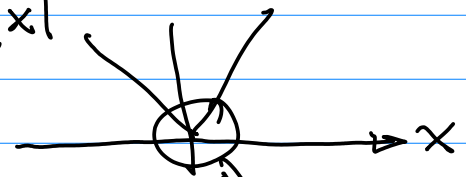


$y_{\text{true}}, y_{\text{pred}}$ — Notation &
meaning
gives the information
for which Category
the data belongs to

7 Use squared difference to
handle potential error (Loss)

Cancellations due to opposite Signs

Note: Be Careful Not Absolute
value! $|x|$



No derivatives
at this point.

8. Define Loss
function

\downarrow
Behavior of Loss
Function

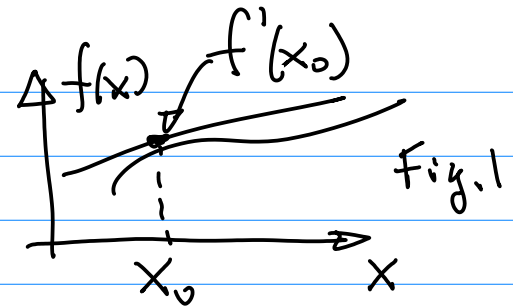
Gradient gives the
fastest increase
of the error

\rightarrow Minimize the
Loss/error
function
in the
negative
direction
of the gradient

q, Denote the Loss as

$$L(W, b) = \sum (y_{\text{true}} - y_{\text{pred}})^2 \dots (2)$$

$b = (b_1, b_2, \dots, b_m)$
 $W = (w_1, w_2, \dots, w_n)$
 $m \neq n$



$$f'(x_0) > 0 \Rightarrow f(x_0 + \Delta x) - f(x_0) > 0 \dots (2)$$

CMPE258 Feb 18

Reference: 1° Training Algorithm
(PART I) 2° OpenCV — Preprocessing

Increase

$$f'(x_0) < 0 \Rightarrow f(x_0 + \Delta x) - f(x_0) < 0 \dots (2^*)$$

Objectives: Deep Convolutional NN
[Deep Reinforcement Learning

$$f(x) = \text{Basic Building Block}_0 + \text{BBB}_1 + \text{BBB}_2 + \text{BBB}_3 + \dots$$

Higher order terms

- (1) Handwritten Digits Recognition MNIST
- (2) Facial Recognition (3) Deep Reinforcement Learning (4) LSTM Time Series Data

Note: 1° Minimization Optimization, Maximization.

$$f \rightarrow \frac{1}{f} \text{ min } \rightarrow \frac{1}{f} \text{ max}$$

$$g \rightarrow \frac{1}{g} \text{ max } \rightarrow \frac{1}{g} \text{ min}$$

2° Taylor Expansion

Basic Building Blocks to Build A Given function $f(x)$ provided it has derivatives up to order K .

$$\lim_{\Delta x \rightarrow 0} \frac{\Delta f(x)}{\Delta x} = f'(x) = \frac{d}{dx} f(x) \dots (1)$$

$$\Delta x \rightarrow \Delta f \rightarrow \frac{\Delta f}{\Delta x} \rightarrow \frac{\Delta f}{\Delta x} \Big|_{\Delta x \rightarrow 0}$$

BBB₀ 1st One Constant
BBB₁ 2nd one Linear

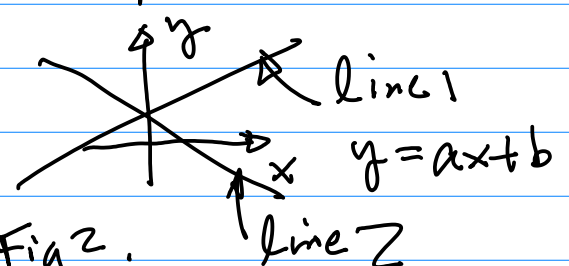


Fig 2.

BBB₂ 3rd 2nd order quadratic

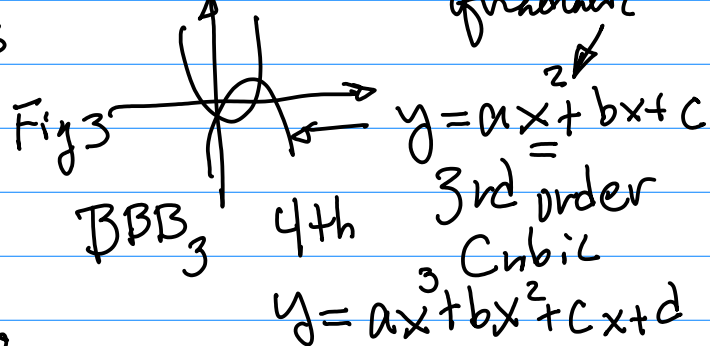


Fig 3

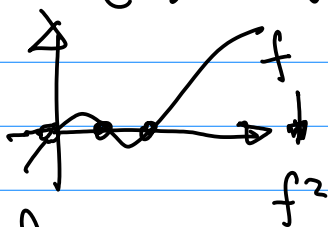
BBB₃ 4th 3rd order Cubic
 $y = ax^3 + bx^2 + cx + d$

$$f(x) = f(x_0) + \frac{f'(x_0)}{1!}(x-x_0) + \frac{f''(x_0)}{2!}(x-x_0)^2 + \dots \quad (3^*) \quad \text{Fig 4}$$

$$f(x_i^{n+1}) - f(x_i^n) < 0 \quad \dots (5)$$

$$\Delta x_i^n = ?$$

Root Finding
Minimization



3° For N-Dimensional Case

$$w_1, w_2, \dots, w_N; b_1, b_2, \dots, b_m$$

$$N = N_1 + M$$

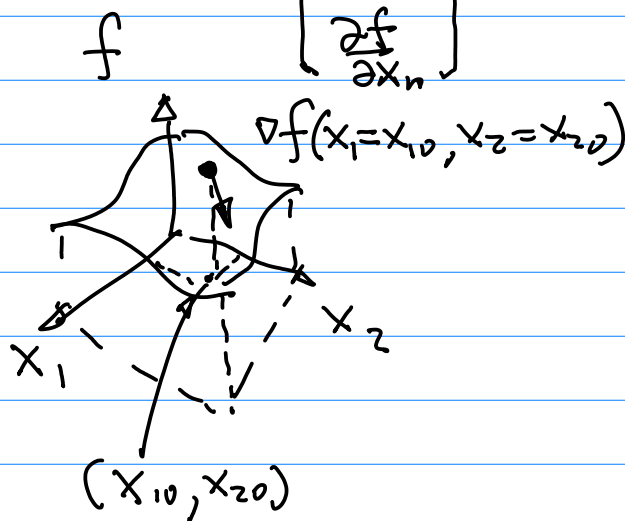
Rewrite b_1, b_2, \dots, b_m as w_i
 $i = N_1 + 1, N_1 + 2, \dots, N_1 + M$

$$L(w, b)$$

$$L(\underline{w})$$

4° Gradient

$$\nabla f(x) = \begin{bmatrix} \frac{\partial f}{\partial x_1} \\ \frac{\partial f}{\partial x_2} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{bmatrix} \quad \dots (6)$$



Partial Derivatives

One-Dimensional Case $f'(x) = \frac{d}{dx} f(x)$

N-Dimensional Case

$$\frac{\partial}{\partial x_1} f(x_1, x_2, \dots, x_N)$$

$$\frac{\partial}{\partial x_2} f(x_1, x_2, \dots, x_N)$$

...

$$\frac{\partial}{\partial x_N} f(x_1, x_2, \dots, x_N) \quad \dots (4)$$

$(x_1^{n+1}, x_2^{n+1}, \dots, x_n^{n+1})$ New updated Value

Based on Gradient with "—" "

$$-\eta \nabla f = -\eta \begin{bmatrix} \frac{\partial f}{\partial x_1} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{bmatrix}$$

$$\text{Find } x_i^{n+1} = x_i^n + \Delta x_i^n$$

... (7)

$$f(x_1, x_2, \dots, x_n) = f(a_1, a_2, \dots, a_n)$$

$$+ \frac{\partial f}{\partial x_1}(x_1 - a_1) + \frac{\partial f}{\partial x_2}(x_2 - a_2) + \dots + \frac{\partial f}{\partial x_n}(x_n - a_n)$$

$$+ \text{higher Order Term} \dots (8)$$

$$\underline{\text{Let}} \Delta x_1 = -\frac{\partial f}{\partial x_1}, \dots$$

$$\Delta x_n = -\frac{\partial f}{\partial x_n} \dots (11)$$

Remove higher order terms,

$$f(x_1, x_2, \dots, x_n) \approx f(a_1, a_2, \dots, a_n) +$$

$$\frac{\partial f}{\partial x_1}(x_1 - a_1) + \frac{\partial f}{\partial x_2}(x_2 - a_2) + \dots + \frac{\partial f}{\partial x_n}(x_n - a_n) \dots (8x)$$

Substitute eqn (11) Back to Eqn (10)

$$(\Delta x_1, \Delta x_2, \dots, \Delta x_n) \begin{pmatrix} \frac{\partial f}{\partial x_1} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{pmatrix}$$

$$f(x_1, x_2, \dots, x_n) - f(a_1, a_2, \dots, a_n) = \dots$$

" < 0 "

$$= \left(-\frac{\partial f}{\partial x_1}, -\frac{\partial f}{\partial x_2}, \dots, -\frac{\partial f}{\partial x_n} \right) \begin{pmatrix} \frac{\partial f}{\partial x_1} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{pmatrix}$$

$$f(x_1, x_2, \dots, x_n) < f(a_1, a_2, \dots, a_n)$$

... (9) We want

PH =

$$\frac{\partial f}{\partial x_1}(x_1 - a_1) + \frac{\partial f}{\partial x_2}(x_2 - a_2) + \dots + \frac{\partial f}{\partial x_n}(x_n - a_n)$$

$$= - \left[\left(\frac{\partial f}{\partial x_1} \right)^2 + \dots + \left(\frac{\partial f}{\partial x_n} \right)^2 \right] \dots (12)$$

" ≤ 0 "

$$\underbrace{(x_1 - a_1, \dots, x_n - a_n)}_{\Delta x_1 \dots \Delta x_n} \cdot \begin{pmatrix} \frac{\partial f}{\partial x_1} \\ \frac{\partial f}{\partial x_2} \\ \vdots \\ \frac{\partial f}{\partial x_n} \end{pmatrix} \dots (10)$$

from Eqn (11) (Handout, Note 1, pp. 1) Gradient