CMPE 258 Midterm Exam Version A 2021S (close book, close notes)

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receive unpermitted aid during examinations. Engaging in such unpermitted actions a considered cheating. By my signature, I affirm that I have adhered to the spirit of the Honor Code.	sidered cheatin	_			
Signature:Date:	nature:		Date	e:	

Please Read: instructions for Zoon based online exam.

- 1. this is an one hour exam, starting from 3:00 and last till 4:00;
- 2. use cellphone to scan your papers, save them as pdf file, then you must convert it zip file;
- 3. Submit the zip file on line before 4:15, late submission will make the paper disqualified; After 4:15 no submission will be accepted (based on the time stamp of the submission). Thank you and stay safe.

There are total 3 questions in this midterm, and the questions **start next page**.

QUESTION 1 (10 points) Based on the project of NIST Convolutional Neural Network for handwritten digits recognition, answer the following questions:

- 1.1 (2 pts) Describe MNIST CNN architecture by using C1 for the 1st convolutional layer, M1 for the 1st max pooling layer, etc., based on the Tensorflow model.summary() output (as shown in the figure below), and explain why the output shape of the convolution is 26x26 while the input image is 28x28?
- 1.2 (3 pts) Suppose an image layer I(x,y) is given in the following figure and a 3x3 Laplace of Gaussian (LoG) kernel is to be utilized to perform convolution. Find the kernel coefficients LoG(x,y), assuming sigma=1 (Note: the formula for LoG(x,y) is given in the Appendix, and LoG(0,1)=LoG(0,-1), and LoG(0,1)=LoG(1,0), so the computation can be simplified)?
- 1.3 (4 pts) Compute 2D convolution by using LoG kernel at image plane location (2,2), assuming the origin of the image at top left hand corner is (1,1).
- 1.4 (1 pt) First Write a line of python code using TF Keras to save a trained MNIST model, then write a line of python code to load the trained MNIST model.

Gnv after as we	Architecture: CI-MI-CZ-M- olntion Kemelsize is 3x3. Convolution lost the top 4: 1) as left & Right Col. So. mes 2bx2b (olf(0,0) = -Z Lobf(1,0): Lobf(1,1)	Hence I(Xy) Buttom Row, He size 28x28 = LOG(DI)=-1e-2	2 0 0 1	0 2 0 1	0 0 0 0	10 10 10 10	h51)
	Layer (type)	Output Shape		Par	am #		,
	conv2d_1 (Conv2D)	(None, 26, 26, 32)		326)		
	max_pooling2d_1 (MaxPooling2	(None, 13, 13, 32)		0			
	conv2d_2 (conv2b)	(None, 11, 11, 64)		184	96	$\overline{}$	
	max_pooling2d_2 (MaxPooling2			0	120		
	conv2d_3 (Conv2D) (None, 3, 3, 64)			369			
	flatten_1 (Flatten) (None, 576)			Θ			
	dense_1 (Dense)	(None, 64)	36928				
	dense_2 (Dense) (None, 10)			656			
13	Total params: 93,322 Trainable params: 93,322 Non-trainable params: 0 $(X,Y) \times I(X,Y) = Z$ $X = 1 = Z$ $X = 1 = Z$ $X = 1 = Z$	*Lob(-1,-1)+0+)*Lob(-1,0)+2*)*Lob(-1,1)+0*	lob/ Lol Lob	(0,-1) x(0,0) r(0,1)	+0+)+0+	tloby tlob	(1,-1) r(1,0) r(1,1)

 $= 2 + lok(1,1) + 2 + lok(0,0) = 2 + lok(1,1) + 2 + \frac{2}{E_1} = -\frac{1}{\sqrt{E_1}}$

QUESTION 2 (10 points). Gradient descent technique is applied to train Neural Networks, use this technique to answer the following questions:

2.1 (3 pts) Suppose a feed forward NN is given in the figure below with an activation

function f(), for each neuron output, find
$$h_1 = f(x_1 w_1 + x_2 w_2 + b_1)$$
, $f_{r_2} = f(x_1 w_3 + x_2 w_4 + b_2)$

$$h_2 = f(x_1 w_1 + x_2 w_2 + b_1)$$

$$h_3 = f(x_1 w_3 + x_2 w_4 + b_2)$$

$$h_4 = f(x_1 w_3 + x_2 w_4 + b_3)$$

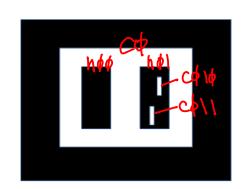
$$h_5 = f(x_1 w_3 + x_2 w_4 + b_3)$$

- 2.2 (1 pt) What is the weight w i update equation based on gradient descent technique? Define a loss function as MSE (Mean Square Error shown below), choose Sigmoid activation function (See Appendix);
- 2.3 (5 pts) Find the updated w1 by using gradient descent technique, assuming x1=1, x2=-1, and all the w's are at the initial value 0.5.
- 2.4 (1 pt) Using Taylor expansion up to the first linear term (see Appendix) to explain why gradient descent technique will lead to the reduction of the loss function. (Note you can use a simplified two dimension case, such as x1 and x2, for your analysis and explanation).

QUESTION 3 (10 points). Based on the design for handwritten digits recognition, answer the following questions:

3.1 (2 pts) Design an implementation technique by providing step by step detailed flow chart for handwritten digits recognition?

3.2 (2 pts) Find a contour (2 pts) of the image belwo by using CV_RETR_TREE algorithm.



3.3 (3 pts) Find x-bar of the following binary image during the localization of ROI operation;

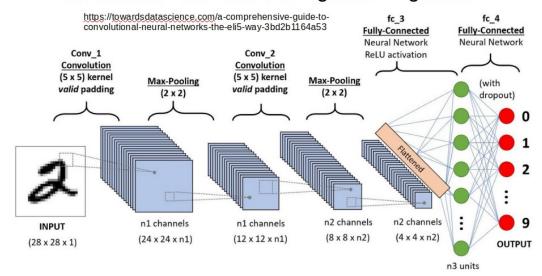
3.4 (3 pts) In order to find orientation of the object given in the following binary image, compute a (see Appendix).

ા બ						
Σ Σ K, β(K1, K2)	1					
X= 4 9 (1)		1				
X= Y & B(K1, K2) Where						
					•	
\(\frac{1}{2} \) \(\frac{1}{	B(K	4, Kz) =	: [. [3	k(1,1)}	-2.B/
K=1 K=1 / K=1 K=1			_=	= ·	+2:1=	1+2:
$= \frac{3}{2} = 1.5$	Not	રઃ સ્ટિ	sto	f B(1	۲۰/K²):	=0)
Now. Countails a						
Σ = (κ, -x) 2β(κ, κz) Wha	re :	22	- (K	,- =	E) B(1	F1, Fz
K=1 K=1 · /	1	احتدالا	1-1		•	. 7

 $\begin{array}{ll}
A = \frac{K_{e} \cdot K_{e} - 1}{2} \\
\frac{1}{2} \cdot \frac{1}{2}$

APPENDIX A. CNN Architecture

Illustration of A CNN for Digits Recognition



Harry Li, Ph.D. 2018

Moments:

$$M_{pq} = \int\limits_{-\infty}^{\infty}\int\limits_{-\infty}^{\infty}x^py^qf(x,y)\,dx\,dy$$

Central Moments:

$$\mu_{pq} = \int\limits_{-\infty}^{\infty}\int\limits_{-\infty}^{\infty}(x-ar{x})^p(y-ar{y})^qf(x,y)\,dx\,dy$$

Orientation

$$\tan 2\phi \stackrel{\triangle}{=} \frac{b}{a-c}$$

$$\alpha = \iint_{\Omega} (X - \bar{X})^{2} B(x, y) dx dy$$

$$b = \iint_{\Omega} 2(x - \bar{X})(y - \bar{y}) B(x, y) dx dy$$

$$c = \iint_{\Omega} (y - \bar{y})^{2} B(x, y) dx dy \dots (4)$$

APPENDIX B. LoG(x,y) kernel

For $|a| \cdot Lo4(0,0) = -\frac{26^2}{E\pi 6^5} = -\frac{2}{E\pi}$ $Lo4(0,1) = -\frac{1}{E\pi} = Lo4(1,0)$ Lo4(1,1) = 0For $|a| \cdot (4 + 1)$

For 1.4: (from Keras import models)
model save ('my. 45')

(from Keras. models import load model)
model=load_model (iny. 45)

APPENDIX C. Sigmoid Activation Function and Example for Gradient Descent Based Training Formula

Note: for the Sigmoid activation function S(x), we have

$$S(x) = \frac{1}{1 + e^{-x}} = \frac{e^x}{e^x + 1} \tag{3}$$

Its derivative is

$$For \frac{e^{-x}}{(1+e^{-x})^2} = f(x) * (1-f(x))$$

$$For \frac{\partial \beta}{\partial x}, h_1 = f(x_1 \omega_1 + x_2 \omega_2 + b_1) = f(0.5 + 0.5 + 0.5 + 0.5) = f(1) \le f(1) \le f(1) = f(1) = \frac{e^{-1}}{(1+e^{-1})^2} = f(1) = f$$

APPENDIX D.

For 2.4 Let
$$f(x_1, x_2) \simeq f(a, b) + \frac{\partial f}{\partial x_1}(x_1 - a) + \frac{\partial f}{\partial x_2}(x_2 - b)$$
 ... (1)

For 2.4 Let $f(x_1, x_2)$ be a loss function, $f(x_1, x_2)$ is a new updated function (simparing to $f(a_1b)$, 50,

One-step for $f(x_1, x_2) - f(a_1b) < 0$, the updated independent variable $f(x_1, x_2) - f(a_1b) < 0$, which leads to $\left(\frac{\partial f}{\partial x_1}\right)^2 \left(\frac{\partial f}{\partial x_2}\right)^2 < 0$

(END) Hence, $f(x_1, x_2) \neq f(a_1b)$.