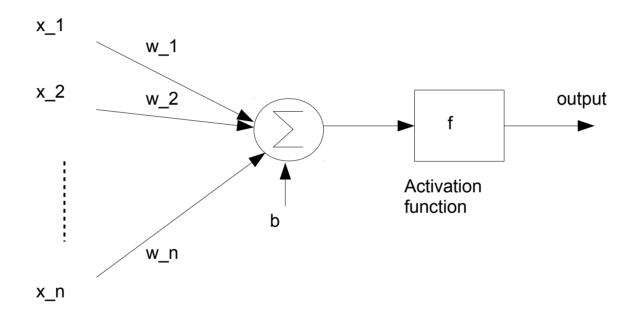
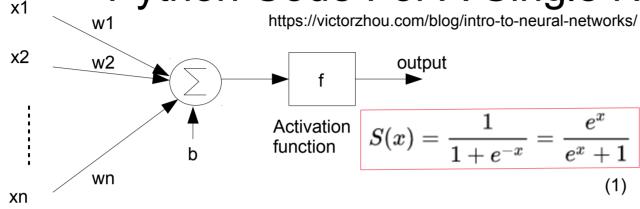
Intro-python-for-nn-2019-2-28.odp Version 2.0 last update Feb. 8, 2022

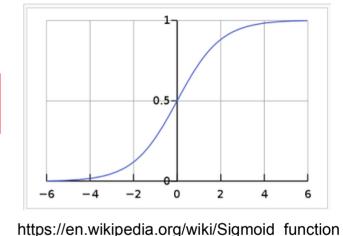
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Neural Network Basic Building Block



Python Code For A Single Neuron





Note: 1. define activation function mathematical function

def sigmoid(x): # Our activation function: $f(x) = 1 / (1 + e^{-(-x)})$ return 1 / (1 + np.exp(-x)) A sigmoid function is a mathematical function having a characteristic "S"-shaped curve

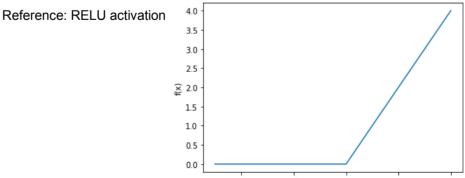
Reference: for further discussion on Sigmoid https://deepai.org/machine-learning-glossary-and-terms/sigmoid-function

2. define a single neuron

class Neuron:

def __init__(self, weights, bias):
 self.weights = weights
 self.bias = bias

def feedforward(self, inputs):
 # Weight inputs, add bias, then use the activation function
 total = np.dot(self.weights, inputs) + self.bias
 return sigmoid(total)



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Python Classes Example

https://www.tutorialspoint.com/python3/python_classes_objects.htm

```
Create a python class with keyword class, then the name of the class, then : sign

class ClassName:
   'Optional class documentation string'
   class_suite
```

1. The class has a documentation string, which can be accessed via ClassName. doc . .

```
class Employee:
    'Common base class for all employees'
    empCount = 0
    def __init__(self, name, salary):
        self.name = name
        self.salary = salary
        Employee.empCount += 1

def displayCount(self):
    print ("Total Employee %d" % Employee.empCount)
    def displayEmployee(self):
        print ("Name : ", self.name, ", Salary: ", self.salary)
```

- 2. class variable whose value is shared among all the instances of a in this class.
- 3. The first method __init__() is a special method, which is called class constructor or initialization method that Python calls when you create a new instance of this class.
- 4. You declare other class methods like normal functions with the exception that the first argument to each method is self. Python adds the self argument to the list for you; you do not need to include it when you call the methods.

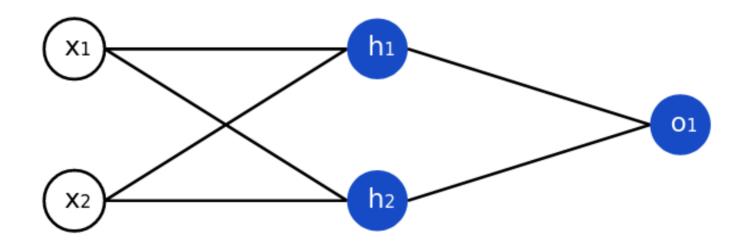
Feed Forward NN

https://victorzhou.com/blog/intro-to-neural-networks/

Input Layer

Hidden Layer

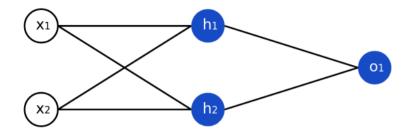
Output Layer



Python Code for Feed Forward NN

https://victorzhou.com/blog/intro-to-neural-networks/

Input Layer Hidden Layer Output Layer



```
def init (self):
  weights = np.array([0, 1])
  bias = 0
  # The Neuron class here is from the previous section
  self.h1 = Neuron(weights, bias)
  self.h2 = Neuron(weights, bias)
  self.o1 = Neuron(weights, bias)
 def feedforward(self, x):
  out h1 = self.h1.feedforward(x)
  out h2 = self.h2.feedforward(x)
  # The inputs for o1 are the outputs from h1 and h2
  out o1 = self.o1.feedforward(np.array([out h1, out h2]))
  return out o1
network = OurNeuralNetwork()
x = np.array([2, 3])
print(network.feedforward(x))
```

Data Set and Prepare for Training

https://victorzhou.com/blog/intro-to-neural-networks/

Example: Collecting data for training

Name Weight (lb	. ,	• , ,	Gender F M M	Name	Weight (minus 135)	Height (minus 66)	Gender	
Alice Bob	133 160	65 72			Alice	-2	-1 ´	1
Charlie	152	70			Bob	25	6	0
Diana	120	60	F		Charlie	17	4	0
210.10	0		•		Diana	-15	-6	1
Signs	Mii	Mna	Sign					

Note: to reduce the mean value of the data, so it will have balanced distribution for both positive and negative side, it is good for the activation function to handle

Signs	Mij	Mpq	Sign
V1	133	65	Stop
V2	160	72	Right
V3	152	70	Right
V4	120	60	Stop

Define Loss Function

https://victorzhou.com/blog/intro-to-neural-networks/

$$ext{MSE} = rac{1}{n} \sum_{i=1}^n (y_{true} - y_{pred})^2$$
 The Mean Square Error Function as a loss function, very often it is also defined as objective function, e.g., minimize the loss function becomes objective function, as shown below step by step.
$$y_{true} - y_{pred}$$
 $(y_{true} - y_{pred})^2$ $\sum_{i=1}^n (y_{true} - y_{pred})^2$ $\sum_{i=1}^n (y_{true} - y_{pred})^2$ $\sum_{i=1}^n (y_{true} - y_{pred})^2$

Define Loss Function

https://victorzhou.com/blog/intro-to-neural-networks/

$$\mathrm{MSE} = \frac{1}{n} \sum_{i=1}^{n} (y_{true} - y_{pred})^2 \qquad \text{The Mean Square Error Function as a loss function, very often it is also defined as objective function, e.g., minimize the loss function becomes objective function, as shown below step by step. \\ y_{true} - y_{pred} \qquad \qquad \qquad \underset{\text{def mse_loss(y_true, y_pred):}}{\underset{\text{feature}}{\text{import numpy as np} \atop \text{def mse_loss(y_true, y_pred):}}} \\ (y_{true} - y_{pred})^2 \qquad \qquad \qquad \qquad \sum_{i=1}^{n} (y_{true} - y_{pred})^2 \\ \qquad \qquad \qquad \qquad \sum_{i=1}^{n} (y_{true} - y_{pred})^2 \qquad \qquad \qquad \qquad \qquad \qquad \\ \text{Exp}\left[\sum_{i=1}^{n} (y_{true} - y_{pred})^2\right]$$

Compute Loss Function

https://victorzhou.com/blog/intro-to-neural-networks/

Example: Given the following y_{true} and y_{pred}, compute the MSE

Name	y_{true}	y_{pred}	(y_{true} - y_{pred})^2
Alice	1	0	1
Bob	0	0	0
Charlie	0	0	0
Diana	1	0	1

$$MSE = \frac{1}{4}(1+0+0+1) = \boxed{0.5}$$

```
import numpy as np
def mse_loss(y_true, y_pred):
    # y_true and y_pred are numpy arrays of the same length.
    return ((y_true - y_pred) ** 2).mean()
y_true = np.array([1, 0, 0, 1])
y_pred = np.array([0, 0, 0, 0])
print(mse_loss(y_true, y_pred)) # 0.5
```

Loss Function and Learning

https://victorzhou.com/blog/intro-to-neural-networks/

Loss function is a very important function to realize training, and to link the minimization of error to the NN weights.

Define a loss function as a function of NN parameters, e.g., weights and bias

$$L(w_i, b_j) = \sum_{i=1}^{n} (y_{true} - y_{pred})^2$$
 (1)

Note y_{pred} is a function of NN parameters w_i, so it can be written as y_{pred} (w_i, b_j).

Example: b₁

w₁

h₁

w₂

b₃

w₄

h₂

w₆

y

From the NN given in this example

We can write loss function with respect to the parameters as follows

 $L(w_i, b_j)$, for I = 1,...,6 and for j = 1,2,3. So from Fig. 1 we have:

$$y_{pred} = o_1 = f(w_5 h_1 + w_6 h_2 + b_3)$$
 (2)

Where h1 can be written as

$$h_1 = f(w_1x_1 + w_2x_2 + b_1) \tag{3}$$

Note: we will introduce more generalized notations from equations (1) to (3), for now we will stay with this notation

Remark 1: To minimize loss function with respect to the variables w and b according

Steepest Gradient Descent Algorithm

https://github.com/hualili/opencv/blob/master/deep-learning-2020S/20-2021S-4gradient-descent-final-2021-2-8.pdf

Lecture Note 1 on Gradient Descent

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Abstract—In this lecture note, we give a gradient descent example for its applications in Neural Networks (NN), e.g., the concept of the negative gradient $-\nabla f$ follows the direction of steepest descent.

I. INTRODUCTION

In this lecture note, we give a gradient descent example for Neural Networks (NN) applications. In particular, the basic concept of the negative gradient $-\nabla f$ follows the direction of steepest descent of a given function f which can be an error function.

II. PARTIAL DERIVATIVE VS. GRADIENT

Given a scalar-valued multivariable functions, e.g. the function with a multidimensional input $x_1, x_2, ..., x_n$, and a onedimensional output as $y = f(x_1, x_2, ..., x_i)$, where $f: \mathbb{R}^n \to$ R. The partial derivative of $f(x_1, x_2, ..., x_n)$ with respect to x_i for i = 1, 2, ..., n:

$$\frac{\partial f}{\partial x_i} = \lim_{\delta x \to 0} \frac{f(x_1, \dots, x_i + \delta x_i, \dots, x_n) - f(x_1, \dots, x_i, \dots, x_n)}{\delta x_i}$$

IV. GREDIENT STEEPEST DESCENT FOR MINIMIZATION

Now, let's define f as an error function, and we would like to minimize it. So we can try to change its inputs (x_1, x_2) by iteration steps:

$$(x_1^{k+1}, x_2^{k+1}) = (x_1^k, x_2^k) + (-\eta \nabla f)$$
 (5)

which will reduce the function value f. To verify this, write f in terms of Taylar expansion as follows

$$f(x_1, x_2) \simeq f(a, b) + \frac{\partial f}{\partial x_1}(x_1 - a) + \frac{\partial f}{\partial x_2}(x_2 - b)$$
 (6)

use simplified notation for the partial derivative f_{x_1} and f_{x_2} , we have

$$f(x_1, x_2) \simeq f(a, b) + f_{x_1}(a, b) * (x_1 - a) + f_{x_2}(a, b) * (x_2 - b)$$
(7)

 $\frac{\partial f}{\partial x_{i}} = \lim_{\delta x \to 0} \frac{f(x_{1}, ..., x_{i} + \delta x_{i}, ..., x_{n}) - f(x_{1}, ..., x_{i}, ..., x_{n})}{\delta x_{i}} \qquad \text{we want to update } (x_{1}^{k}, x_{2}^{k}) \text{ to } (x_{1}^{k+1}, x_{2}^{k+1}) \text{ such that } f(x_{1}^{k+1}, x_{2}^{k+1}) < f(x_{1}^{k}, x_{2}^{k}). \text{ From equation (6), replace } (x_{1}, x_{2}) \text{ by } (x_{1}^{k+1}, x_{2}^{k+1}), \text{ and let } (x_{1}^{k}, x_{2}^{k}) = (a, b), \text{ so we have}}$