

CMPE 258 Midterm Exam Version A
2021S (close book, close notes)

First Name: _____ **Last Name:** _____
Student ID: _____ **Email:** _____ **(Total 30 points)**

Honor Code: All students agree, individually and collectively, that they will not give or receive unpermitted aid during examinations. Engaging in such unpermitted actions is considered cheating. By my signature, I affirm that I have adhered to the spirit of the Honor Code.

Signature: _____ Date: _____

Please Read: instructions for Zoon based online exam.

1. this is an one hour exam, starting from 3:00 and last till 4:00;
2. use cellphone to scan your papers, save them as pdf file, then you must convert it zip file;
3. Submit the zip file on line before 4:15, late submission will make the paper disqualified; After 4:15 no submission will be accepted (based on the time stamp of the submission). Thank you and stay safe.

There are total 3 questions in this midterm, and the questions **start next page**.

QUESTION 1 (10 points) Based on the project of NIST Convolutional Neural Network for handwritten digits recognition, answer the following questions:

1.1 (2 pts) Describe MNIST CNN architecture by using C1 for the 1st convolutional layer, M1 for the 1st max pooling layer, etc., based on the Tensorflow model.summary() output (as shown in the figure below), and explain why the output shape of the convolution is 26x26 while the input image is 28x28?

1.2 (3 pts) Suppose an image layer $I(x,y)$ is given in the following figure and a 3x3 Laplace of Gaussian (LoG) kernel is to be utilized to perform convolution. Find the kernel coefficients $LoG(x,y)$, assuming $\sigma=1$ (Note: the formula for $LoG(x,y)$ is given in the Appendix, and $LoG(0,1)=LoG(0,-1)$, and $LoG(0,1)=LoG(1,0)$, so the computation can be simplified)?

1.3 (4 pts) Compute 2D convolution by using LoG kernel at image plane location (2,2), assuming the origin of the image at top left hand corner is (1,1).

1.4 (1 pt) First Write a line of python code using TF Keras to save a trained MNIST model, then write a line of python code to load the trained MNIST model.

2	0	0	10
0	2	0	10
0	0	0	10
1	1	0	10

```
>>> model.summary()
```

Layer (type)	Output Shape	Param #
conv2d_1 (Conv2D)	(None, 26, 26, 32)	320
max_pooling2d_1 (MaxPooling2D)	(None, 13, 13, 32)	0
conv2d_2 (Conv2D)	(None, 11, 11, 64)	18496
max_pooling2d_2 (MaxPooling2D)	(None, 5, 5, 64)	0
conv2d_3 (Conv2D)	(None, 3, 3, 64)	36928
flatten_1 (Flatten)	(None, 576)	0
dense_1 (Dense)	(None, 64)	36928
dense_2 (Dense)	(None, 10)	650
Total params: 93,322		
Trainable params: 93,322		
Non-trainable params: 0		

QUESTION 2 (10 points). Gradient descent technique is applied to train Neural Networks, use this technique to answer the following questions:

2.1 (3 pts) Suppose a feed forward NN is given in the figure below with an activation function $f(\cdot)$, for each neuron output, find

$h_1 = ?$

$h_2 = ?$

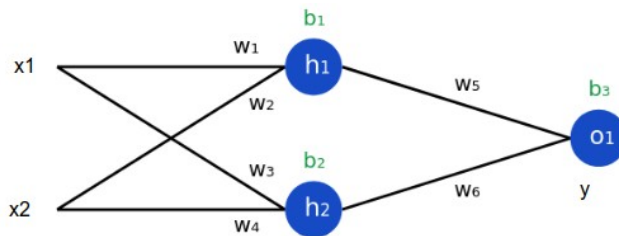
$o_1 = ?$

2.2 (1 pt) What is the weight w_i update equation based on gradient descent technique?

Define a loss function as MSE (Mean Square Error shown below), choose Sigmoid activation function (See Appendix);

2.3 (5 pts) Find the updated w_1 by using gradient descent technique, assuming $x_1=1$, $x_2=-1$, and all the w 's are at the initial value 0.5.

2.4 (1 pt) Using Taylor expansion up to the first linear term (see Appendix) to explain why gradient descent technique will lead to the reduction of the loss function. (Note you can use a simplified two dimension case, such as x_1 and x_2 , for your analysis and explanation).

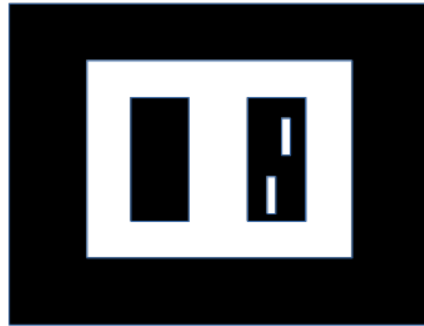


$$\text{MSE} = \frac{1}{n} \sum_{i=1}^n (Y_i - \hat{Y}_i)^2$$

QUESTION 3 (10 points). Based on the design for handwritten digits recognition, answer the following questions:

3.1 (2 pts) Design an implementation technique by providing step by step detailed flow chart for handwritten digits recognition?

3.2 (2 pts) Find a contour (2 pts) of the image below by using CV_RETR_TREE algorithm.



3.3 (3 pts) Find \bar{x} of the following binary image during the localization of ROI operation;

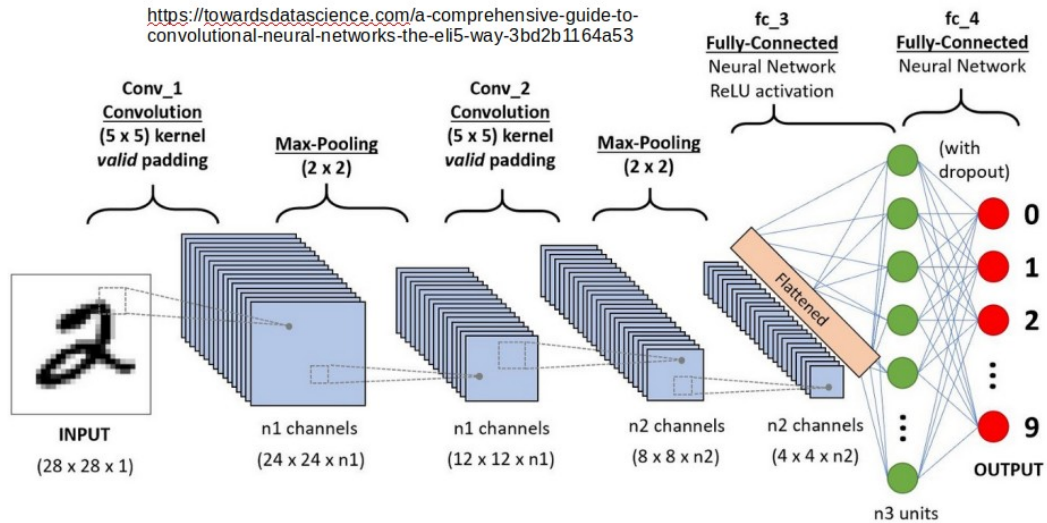
3.4 (3 pts) In order to find orientation of the object given in the following binary image, compute α (see Appendix).

1			
	1		

APPENDIX A. CNN Architecture

Illustration of A CNN for Digits Recognition

<https://towardsdatascience.com/a-comprehensive-guide-to-convolutional-neural-networks-the-eli5-way-3bd2b1164a53>



Harry Li, Ph.D., 2018

Orientation

Moments:

$$M_{pq} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} x^p y^q f(x, y) dx dy$$

Central Moments:

$$\mu_{pq} = \int_{-\infty}^{\infty} \int_{-\infty}^{\infty} (x - \bar{x})^p (y - \bar{y})^q f(x, y) dx dy$$

$$\tan 2\phi \triangleq \frac{b}{a-c}$$

$$\begin{aligned} a &= \iint_{\mathcal{R}} (x - \bar{x})^2 B(x, y) dx dy \dots (2) \\ b &= \iint_{\mathcal{R}} 2(x - \bar{x})(y - \bar{y}) B(x, y) dx dy \dots (3) \\ c &= \iint_{\mathcal{R}} (y - \bar{y})^2 B(x, y) dx dy \dots (4) \end{aligned}$$

APPENDIX B. LoG(x,y) kernel

$$\nabla^2 G(x, y) = \frac{x^2 y^2 - 2b^2}{\sqrt{\pi} b^5} e^{-\frac{x^2 y^2}{2b^2}}$$

APPENDIX C. Sigmoid Activation Function and Example for Gradient Descent Based Training Formula

Note: for the Sigmoid activation function $S(x)$, we have

$$S(x) = \frac{1}{1 + e^{-x}} = \frac{e^x}{e^x + 1} \quad (3)$$

Its derivative is

$$S'(x) = \frac{e^{-x}}{(1 + e^{-x})^2} = f(x) * (1 - f(x))$$

$$w_1 \leftarrow w_1 - \eta \frac{\partial L}{\partial w_1} \quad (4)$$

APPENDIX D.

$$f(x_1, x_2) \simeq f(a, b) + \frac{\partial f}{\partial x_1}(x_1 - a) + \frac{\partial f}{\partial x_2}(x_2 - b)$$

(END)