

MODULE TITLE	Mathematical Biology and Ecology	CREDIT VALUE	15
MODULE CODE	МТН3006	MODULE CONVENER	Prof Marc Goodfellow (Coordinator)
<b>DURATION: TERM</b>	1	2	3
<b>DURATION: WEEKS</b>	11 weeks	0	0
Number of Students Taking	g Module (anticipated)	90	

### **DESCRIPTION** - summary of the module content

This module will give you the opportunity to learn how mathematics may be applied to the biosciences in order to quantitatively model biological processes, from molecular processes at work within living cells up to the behaviour of populations and demographic phenomena. The subject matter has been selected so as to give a wide-ranging overview of the role applied mathematics has to play in the biological disciplines. You will build and analyse models (typically as differential equations or iterated maps) using real world examples from nature. Examples that may be studied within the module include: the population dynamics of insects, animals or fish, competitive exclusion of species, the behaviour of the chemical reactions kinetics that power living cells and mechanisms of biological pattern formation from reaction-diffusion equations.

Pre-requisite module: MTH2003 or equivalent

### AIMS - intentions of the module

This module is designed to illustrate the application of mathematics to the biological science, and emphasises realistic situations throughout. These include: population dynamics and stage-structured population models incorporating complex demographies. They also include harvesting models; competitive exclusion of species; reaction kinetics; biological waves; diffusion-driven instabilities and the effects of geometry on pattern formation in animals. On this module, you will learn how to use core applied mathematics techniques, such as differential equation modelling and matrix algebra. However, no previous biological knowledge will be assumed.

### INTENDED LEARNING OUTCOMES (ILOs) (see assessment section below for how ILOs will be assessed)

On successful completion of this module, you should be able to:

### Module Specific Skills and Knowledge:

1 Appreciate how mathematics can be usefully employed in various aspects of the life sciences;

### Discipline Specific Skills and Knowledge:

- 2 Understand the role of mathematical modelling in real-life situations;
- 3 Recognise how many aspects of applied mathematics learned in earlier modules have practical uses;
- 4 Develop considerable expertise in using analytical and numerical techniques to explore mathematical models, including the use of appropriate software (e.g. MATLAB, Python, R etc.)
- 5 Formulate simple models;

Guided Independent Study

Coursework

**DETAILS OF SUMMATIVE ASSESSMENT** 

- 6 Study adeptly the resulting equations;
- 7 Draw conclusions about likely behaviours.

### Personal and Key Transferable/ Employment Skills and Knowledge:

8 Display enhanced numerical and computational skills via the suite of practical exercises that accompany the formal lecture work;

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**Written Exams** 

- 9 Show enhanced literature searching and library skills in order to investigate various phenomena discussed;
- 10 Demonstrate enhanced time management and organisational abilities.

### SYLLABUS PLAN - summary of the structure and academic content of the module

- Continuous models for a single species; analysis of models using linear stability theory; Hysteresis effects; harvesting a single natural population; discrete models and cobwebbing; discrete logistic growth and the route to chaos;
- Two-dimensional models; introduction to simple phase plane analysis; realistic models for various cases (e.g. predator-prey interactions) and the principles of competitive exclusion and mutualism;
- Introduction to population projection models; geometric growth, stable stage structures and reproductive value for stage-structured ecological populations; asymptotic analysis and transient bounds;
- Tools for analysing PPMs; sensitivity and elasticity; use of transfer function analysis to achieve exact perturbations; applications to managed conservation strategies; reaction kinetics and the law of mass action;
- Enzyme-substrate kinetics; Michaelis-Menten theory and activation/inhibition phenomena;
- Reaction-diffusion problems and biological waves; the Fisher equation; Turing instabilities and diffusion-driven instabilities in two-component systems; generation of patterning by domain geometry; minimal domains for stable pattern formation

# LEARNING AND TEACHING LEARNING ACTIVITIES AND TEACHING METHODS (given in hours of study time) Scheduled Learning & Teaching Activities 33.00 Guided Independent Study 117.00 Placement / Study Abroad 0.00 DETAILS OF LEARNING ACTIVITIES AND TEACHING METHODS Category Hours of study time Description Scheduled Learning and Teaching Activities 33 Lectures, example classes

Lecture and assessment preparation; wider reading

**Practical Exams** 

ASSESSMENT							
FORMATIVE ASSESSMENT - for feedback and development purposes; does not count towards module grade							
Form of Assessment	Size of Assessment (e.g. duration/length)	ILOs Assessed	Feedback Method				
Four Coursework Sheets	5-6 questions per sheet	1-10	Feedback sheet and in-class review of model solutions				
SUMMATIVE ASSESS	MENT (% of credit)						

Form of Assessment	% of Credit	Size of Assessment (e.g. duration/length)	ILOs Assessed	Feedback Method
Coursework 1 – based on questions submitted for assessment	10	15 hours	All	Annotated script and written/verbal feedback
Coursework 2 - based on questions submitted for assessment	10	15 hours	All	Annotated script and written/verbal feedback
Written Exam	80	2 hours (Summer)	1-7	Written/Verbal on request, SRS

### **DETAILS OF RE-ASSESSMENT (where required by referral or deferral)**

Original Form of Assessment	Form of Re-assessment	ILOs Re-assessed	Time Scale for Re-reassessment
Written Exam*	Written Exam (2 hours) (10%)	All	August Ref/Def Period
Coursework 1	Coursework 1 (10%)	All	August Ref/Def Period
Coursework 2	Coursework 2 (80%)	All	August ref/Def Period

<sup>\*</sup>Please refer to reassessment notes for details on deferral vs. Referral reassessment

### **RE-ASSESSMENT NOTES**

Deferrals: Reassessment will be by coursework and/or written exam in the deferred element only. For deferred candidates, the module mark will be uncapped.

Referrals: Reassessment will be by a single written exam worth 100% of the module only. As it is a referral, the mark will be capped at 40%.

### **RESOURCES**

INDICATIVE LEARNING RESOURCES - The following list is offered as an indication of the type & level of information that you are expected to consult. Further guidance will be provided by the Module Convener

## ELE - <a href="http://vle.exeter.ac.uk">http://vle.exeter.ac.uk</a> Reading list for this module:

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Type	Author	Title			Edition	Publisher		Year	ISBN	Search
Set	Murray, J.D.	Mathem	atical Biology		2nd	Springer	1	1993	000-3-540- 57204-X	[Library]
Set	Jones, D.S. & Sleeman, B.D.	Different	cial Equations and Mathematical Biolog	у	Electronic	Allen & Unwin	2	2003	000-0-045- 15001-X	[Library]
Set	Fife, P.C.	Mathem	atical Aspects of Reacting and Diffusing	g Systems		Springer	1	1979	000-3-540- 09117-3	[Library]
Set	May, R.M.	Theoreti	cal Ecology. Principles and Applications	5	Electronic	Blackwell Scient Publications	ific 2	2007	000-0-632- 00762-1	[Library]
Set	Alstad, D.	Basic Po	pulus Models of Ecology			Prentice-Hall	2	2001	978-0130212894	[Library]
Set	Caswell, H.	Matrix P	opulation Models: Construction, Analystation	is, and	2nd	Sinauer Associa	tes 2	2001	9780878930937	[Library]
Set	Britton, N.F.	Essentia	l Mathematical Biology			Springer	2	2005	978-1852335366	[Library]
CREE	DIT VALUE		15	ECTS VALUE			7.5			
PRE-	REQUISITE MODULES		MTH2003							
CO-R	EQUISITE MODULES									
NQF	LEVEL (FHEQ)		6	AVAILABLE A	AS DISTAI	NCE LEARNING	No			
ORIG	IN DATE		Tuesday 10 July 2018	LAST REVISI	ON DATE		Thursday 26 Ja	anuar	y 2023	
KEY	WORDS SEARCH		Mathematical Biology; Ecology; Nonlin Algebra; Differential Equations	near Dynamics;	Systems I	Biology; Populatio	on Dynamics; M	/lathei	matical Modelling	; Linear