FK kinematics of 2 and 3 link finger

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Forward Kinematics of 1 Finger

As 2 link manipulator DH table:

i	θ	d	a	α
1	θ_1	0	L_1	0
2	θ_2	0	L_2	0

$${}^{0}T_{1} = \begin{bmatrix} c_{1} & -s_{1} & 0 & 0 \\ s_{1} & c_{1} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & L_{1} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$${}^{1}T_{2} = \begin{bmatrix} c_{2} & -s_{2} & 0 & 0 \\ s_{2} & c_{2} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & L_{2} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$(1)$$

$${}^{1}T_{2} = \begin{bmatrix} c_{2} & -s_{2} & 0 & 0 \\ s_{2} & c_{2} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & L_{2} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 (2)

Forward Kinematics:
$${}^{0}T_{2} = \begin{bmatrix} c_{12} & -s_{12} & 0 & L_{1}c_{1} + L_{2}c_{12} \\ s_{12} & c_{12} & 0 & L_{1}s_{1} + L_{2}s_{12} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 (3)

As 3 link manipulator DH table:

i	θ	d	a	α
1	θ_1	0	L_1	0
2	θ_2	0	L_2	0
3	θ_3	0	L_3	0

$${}^{2}T_{3} = \begin{bmatrix} c_{3} & -s_{3} & 0 & 0 \\ s_{3} & c_{3} & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \cdot \begin{bmatrix} 1 & 0 & 0 & L_{3} \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
(4)

Forward Kinematics:
$${}^{0}T_{3} = \begin{bmatrix} c_{123} & -s_{123} & 0 & L_{1}c_{1} + L_{2}c_{12} + L_{3}c_{123} \\ s_{123} & -c_{123} & 0 & L_{1}s_{1} + L_{2}s_{12} + L_{3}s_{123} \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
 (5)

2 Images

