

Kalkulus

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A.

$$1. \int x^8 dx = \frac{1}{9} x^{9} + C$$

$$2. \int \frac{1}{x^6} dx = \int x^{-6} dx$$

$$= \frac{1}{-6+1} x^{-6+1} + C$$

$$= -\frac{1}{5} x^{-5} + C$$

$$= -\frac{1}{5} \cdot \frac{1}{x^5} + C$$

$$= -\frac{1}{5x^5} + C$$

$$3. \int \sqrt[3]{x^6} dx = \int x^{\frac{6}{3}} dx = \int x^2 dx$$

$$= \frac{1}{2+1} x^{2+1} + C$$

$$= \frac{1}{3} x^3 + C$$

$$= \frac{1}{3} \cdot \frac{x^3}{1} + C$$

$$= \frac{1}{3} x^3 + C$$

$$4. \int \frac{1}{t} dt = \int \frac{1}{t} dt$$

$$= 4 \ln |t| + C$$

$$5. \int (x^3 - 3x - 9) dx = \frac{1}{4} x^{3+1} - 3 \frac{1}{1+1} x^{1+1} - 9 \cdot \frac{1}{0+1} x^{0+1} + C$$

$$= \frac{1}{4} x^4 - 3 \frac{1}{2} x^2 - 9x + C$$

$$= \frac{1}{4} x^4 - \frac{3}{2} x^2 - 9x + C$$

$$6. \int (2-y^2)^2 dy = \int 4 - 4y^2 + y^4 dy$$

$$= 4 \frac{1}{0+1} y^{0+1} - 4 \frac{1}{2+1} y^{2+1} + \frac{1}{4+1} y^{4+1} + C$$

$$= 4x - \frac{4}{3} y^3 + \frac{1}{5} y^5 + C$$

B.

$$7. \int 2x(x^2+1)^2 dx = \int 2x \cdot U^2 \cdot \frac{dU}{2x} \quad \left\{ \begin{array}{l} U = x^2 + 1 \\ \frac{dU}{dx} = 2x \\ dx = \frac{dU}{2x} \end{array} \right.$$

$$= \int U^2 dU$$

$$= \frac{1}{3} U^3 + C$$

$$= \frac{1}{3} (x^2+1)^3 + C$$

$$8. \int \frac{\sin \sqrt{x}}{\sqrt{x}} dx = \int \sin U \cdot 2 du$$

$$= 2 \int \sin U du$$

$$= -2 \cos U + C$$

$$= -2 \cos \sqrt{x} + C$$

$$U = \sqrt{x}$$

$$\frac{dU}{dx} = \frac{1}{2\sqrt{x}}$$

$$2dU = \frac{dx}{\sqrt{x}}$$

$$9. \int \cos^3 x \sin x dx = \int U^2 \cdot 3 \sin x \cdot \frac{dU}{3 \sin x} = -\int U^2 dU$$

$$= -\frac{1}{3} U^3 + C$$

$$= -\frac{1}{3} \cos^3 x + C$$

$$U = \cos x$$

$$\frac{dU}{dx} = -\sin x$$

$$dx = \frac{dU}{-\sin x}$$

$$10. \int \frac{3x dx}{\sqrt{4x^2+7}} = \int \frac{3x \cdot \frac{dx}{2x}}{\sqrt{4x^2+7}}$$

$$= \int \frac{3}{2} \cdot \frac{dx}{\sqrt{4x^2+7}}$$

$$U = 4x^2 + 7$$

$$\frac{dU}{dx} = 8x$$

$$dx = \frac{dU}{8x}$$

$$= \frac{3}{2} \cdot \frac{1}{\sqrt{U}} \cdot \frac{dU}{8x}$$

$$= \frac{3}{16} \cdot \frac{1}{\sqrt{U}} dU$$

$$= \frac{3}{16} \cdot 2 \sqrt{U} + C$$

$$= \frac{3}{8} \sqrt{4x^2+7} + C$$