







What is the Generalized Linear Model (GLM)?

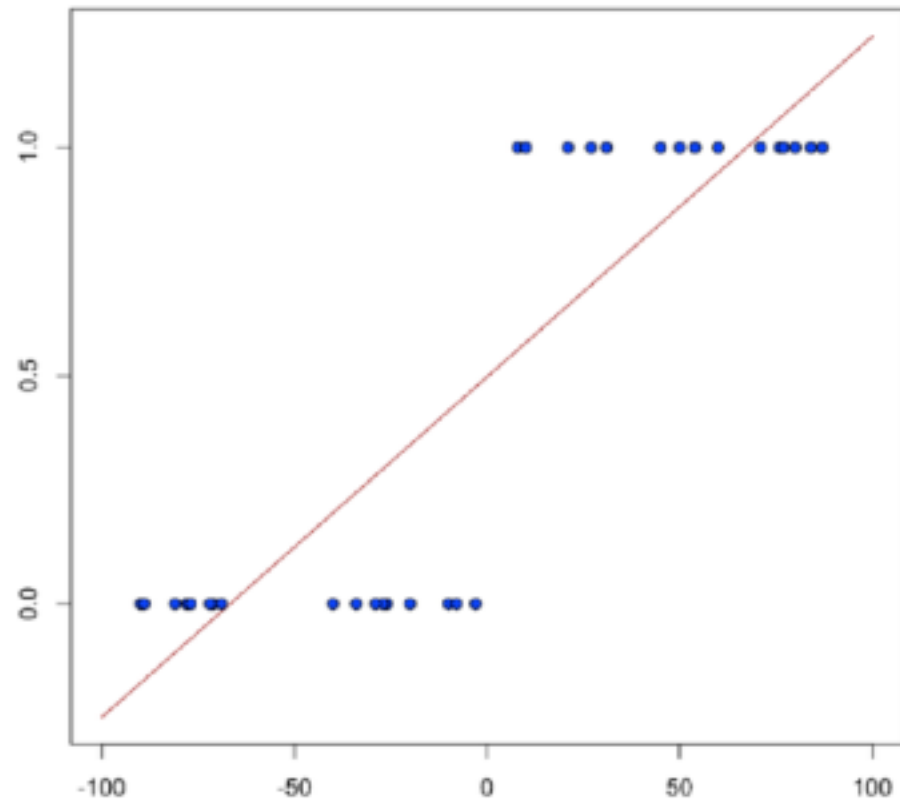
- Class of models that relate  $X$  (inputs) to  $Y$  (output)
- Allows for a unification of models that have errors of the following form:
  - Normal (Gaussian)
  - Poisson
  - Gamma
  - Tweedie
  - Binomial (Logistic)
  - Multinomial
- MLE is found by iteratively reweighted least squares

$$E(Y) = \mu = g^{-1}(x\beta)$$

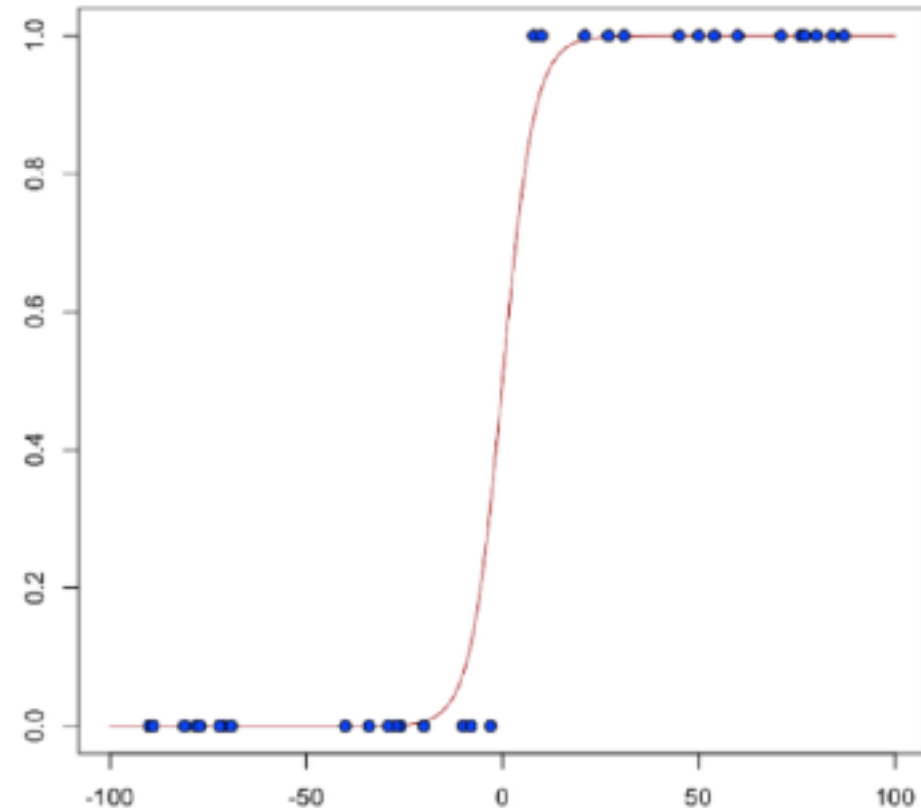
$$\text{var}(\mathbf{Y}) \equiv \mathbf{V}(\boldsymbol{\mu}) \equiv \mathbf{V}(\mathbf{g}^{-1}(\mathbf{X}\boldsymbol{\theta})).$$

# Same predictors, different family and link functions

Linear Regression fit  
(family=gaussian, link = identity)



Logistic Regression fit  
(family=binomial, link = logit)





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$$E(\mathbf{Y}) = \boldsymbol{\mu} = g^{-1}(\mathbf{X}\boldsymbol{\beta})$$

$$\text{Var}(\mathbf{Y}) = V(\boldsymbol{\mu}) = V(g^{-1}(\mathbf{X}\boldsymbol{\beta})).$$

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