

> Lab - 1 | 22 January 2026

↳ 6 cells hidden

> Lab - 2 | 29 January 2026

↳ 14 cells hidden

✓ Lab - 3 | 05 February 2026

Forward Pass + Backpropagation

```
import numpy as np
import matplotlib.pyplot as plt

# ----- Input & Target -----
x1, x2 = 0.6, 0.1
y = 1

# ----- Initial Parameters -----
w1, w2, b = 0.2, -0.3, 0.4
lr = 0.1

# ----- Sigmoid Function -----
def sigmoid(z):
    return 1 / (1 + np.exp(-z))

# ----- Forward Pass -----
z = w1 * x1 + w2 * x2 + b
y_pred = sigmoid(z)

# Error BEFORE update
error = abs(y - y_pred)

# ----- Backpropagation -----
dL_dy_pred = y_pred - y
dy_pred_dz = y_pred * (1 - y_pred)
dL_dz = dL_dy_pred * dy_pred_dz
```

```

dL_dw1 = dL_dz * x1
dL_dw2 = dL_dz * x2
dL_db = dL_dz

# ----- Parameter Update -----
w1 -= lr * dL_dw1
w2 -= lr * dL_dw2
b -= lr * dL_db

print("----- Updated Parameters -----")
print(f"w1: {w1:.4f}, w2: {w2:.4f}, b: {b:.4f}")
print(f"Prediction Error (before update): {error:.4f}")
print("-----")

# ----- Visualization -----
labels = ['Weight 1 (w1)', 'Weight 2 (w2)', 'Bias (b)', 'Error']
values = [w1, w2, b, error]
colors = ['royalblue', 'tomato', 'seagreen', 'gold'] # Different colors

plt.figure(figsize=(8, 5))
bars = plt.bar(labels, values, color=colors)

plt.title('Parameters & Prediction Error After One Update')
plt.ylabel('Value')
plt.grid(axis='y', linestyle='--', alpha=0.7)

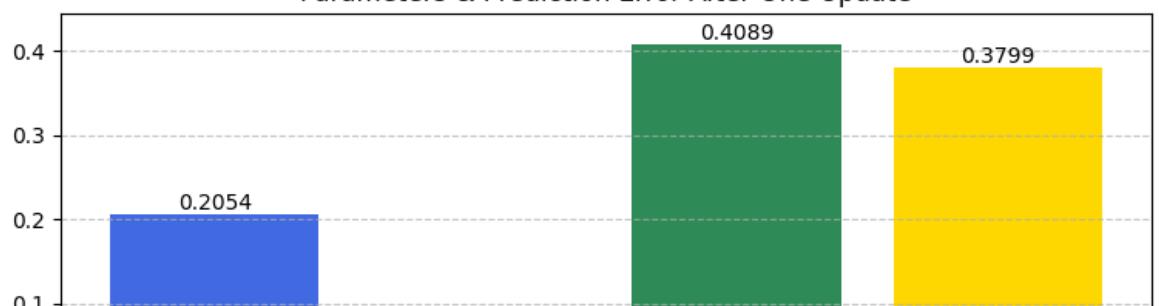
# Add value labels on bars
for bar in bars:
    height = bar.get_height()
    plt.text(bar.get_x() + bar.get_width()/2, height,
              f'{height:.4f}', ha='center',
              va='bottom' if height >= 0 else 'top')

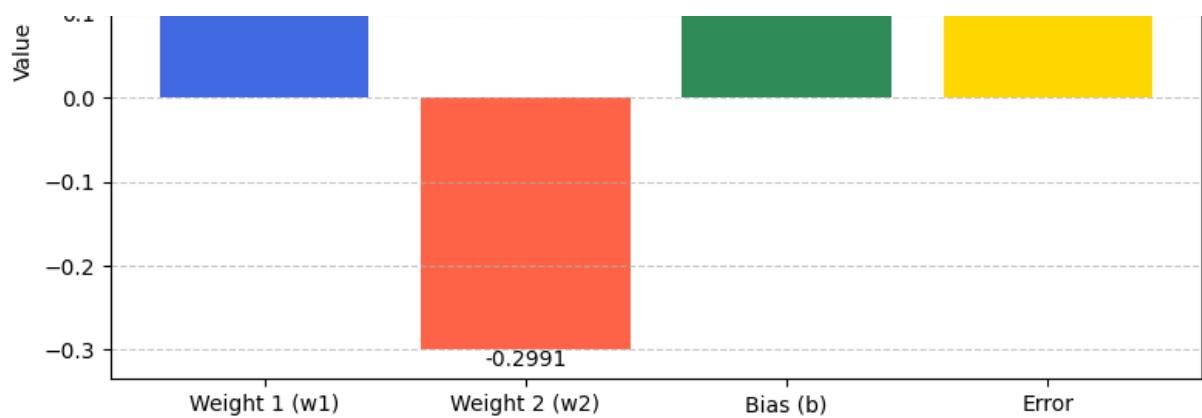
plt.tight_layout()
plt.show()

```

----- Updated Parameters -----
w1: 0.2054, w2: -0.2991, b: 0.4089
Prediction Error (before update): 0.3799

Parameters & Prediction Error After One Update





Perceptron using sigmoid activation to learn the AND logic gate using gradient descent

```
import numpy as np
import matplotlib.pyplot as plt

X = np.array([
    [0,0],
    [0,1],
    [1,0],
    [1,1]
])
y = np.array([0,0,0,1])

learning_rates = [0.01, 0.1, 0.5, 0.8] # 4 different LRs
epochs = 1000

def sigmoid(z):
    return 1/(1+np.exp(-z))

plt.figure(figsize=(10,6))

for lr in learning_rates:
    # Reset weights for each LR
    w = np.array([0.1, 0.2], dtype=float)
    b = 0.3

    errors_per_epoch = []
```

```
for epoch in range(epochs):
    total_absolute_error = 0

    for i in range(len(X)):
        z = np.dot(X[i], w) + b
        y_pred = sigmoid(z)

        total_absolute_error += abs(y[i] - y_pred)

        dz = y_pred - y[i]
        dw = dz * X[i]
        db = dz

        w -= lr * dw
        b -= lr * db

    errors_per_epoch.append(total_absolute_error)

plt.plot(errors_per_epoch, label=f"LR = {lr}")

plt.title("Effect of Learning Rate on Training Error (AND Gate)")
plt.xlabel("Epoch")
plt.ylabel("Total Absolute Error")
plt.legend()
plt.grid(True)
plt.show()
```

