# HElib Implementing Homomorphic Encryption

Generated by Doxygen 1.8.18

## **Chapter 1**

### HEIib v1.0.2 Documentation

HElib is an open-source ( Apache License v2.0) software library that implements homomorphic encryption (HE). Currently available schemes are the implementations of the Brakerski-Gentry-Vaikuntanathan (BGV) scheme and the Approximate Number scheme of Cheon-Kim-Kim-Song (CKKS), along with many optimizations to make homomorphic evaluation runs faster, focusing mostly on effective use of the Smart-Vercauteren ciphertext packing techniques and the Gentry-Halevi-Smart optimizations.

Articles that describe some aspects of HElib include:

- A (somewhat outdated) design document, Shai Halevi and Victor Shoup, April 2013.
- Algorithms in HElib, Shai Halevi and Victor Shoup, published in CRYPTO 2014.
- Bootstrapping for HElib, Shai Halevi and Victor Shoup, EUROCRYPT 2015.

Since mid-2018 HElib has been under extensive refactoring for *Reliability*, Robustness & Serviceability\*, *Performance*, and most importantly *Usability* for researchers and developers working on HE and its uses.

HElib supports an "assembly language for HE", providing low-level routines (set, add, multiply, shift, etc.), sophisticated automatic noise management, improved BGV bootstrapping, multi-threading, and also support for Ptxt (plaintext) objects which mimics the functionality of Ctxt (ciphertext) objects. See <a href="changes.md">changes.md</a> for more details.

HElib is written in C++14 and uses the NTL mathematical library, over GMP.

HElib is distributed under the terms of the Apache License v2.0.

For code downloads and full installation instructions, visit HElib GitHub Pages.

## **Chapter 2**

## Namespace Index

## 2.1 Namespace List

Here is a list of all namespaces with brief descriptions:

| ft               | ?1 |
|------------------|----|
| elib             | ?? |
| elib::FHEglobals | ?? |
| TL               | ?? |
| d                | 27 |

4 Namespace Index

## **Chapter 3**

## **Hierarchical Index**

## 3.1 Class Hierarchy

This inheritance list is sorted roughly, but not completely, alphabetically:

6 Hierarchical Index

| $\label{lem:helib::decode_pa_impl} \textbf{helib::decode\_pa\_impl} < type > \  \   \dots \dots$   |      |
|--|------|
| $\label{localization} \begin{split} & \text{helib::deep\_clone} < X > \dots & \dots & \dots & \dots & \dots \\ & \text{helib::DoubleCRT} & \dots & \dots & \dots & \dots & \dots & \dots \\ & & & & & & &$   |      |
| helib::CtxtPart  |      |
| helib::DynamicCtxtPowers   |      |
| helib::encode_pa_impl< type >  |      |
| helib::EncryptedArray  |      |
| helib::EncryptedArrayBase  |      |
| helib::EncryptedArrayCx  |      |
| helib::EncryptedArrayDerived< type >   |      |
| helib::equals_pa_impl< type >  |      |
| helib::EvalMap   |      |
| helib::Exception   |      |
| helib::InvalidArgument   |      |
| helib::LogicError  |      |
| helib::OutOfRangeError   | ??   |
| helib::RuntimeError  |      |
| helib::fhe stats record  | . ?? |
| helib::FHEtimer  | . ?? |
| helib::FlowEdge  | . ?? |
| $\verb helib::frobeniusAutomorph_pa_impl  < type > $   |      |
| helib::FullBinaryTree  |      |
| helib::GenDescriptor   |      |
| $\label{lem:helib::general_range} \textbf{helib::general\_range} < T > \ \dots \dots$  |      |
| helib::GeneralAutomorphPrecon  |      |
| helib::GeneralAutomorphPrecon_BSGS   |      |
| helib::GeneralAutomorphPrecon_FULL   |      |
| helib::GeneralAutomorphPrecon_UNKNOWN  |      |
| helib::GeneralBenesNetwork   |      |
| helib::GeneratorTrees  |      |
| helib::half_FFT  |      |
| HighLvlTimingData  |      |
| helib::HyperCube < T >   |      |
| helib::HyperCube < long >  |      |
| helib::ColPerm   |      |
| helib::IndexMap< T >   |      |
| helib::IndexMap< NTL::vec_long >   |      |
| $\label{local-policy} \begin{split} &\text{helib::IndexMapInit} < T > \dots \\ &\text{helib::IndexMapInit} < NTL:: vec\_long > \dots $ |      |
|  |      |
| helib::DoubleCRTHelper   |      |
| helib::IndexSet  | . ?? |
| helib::InvalidArgument   | ??   |
| helib::IndexSet::iterator  |      |
| helib::general_range < T >::iterator   | . ?? |
| helib::KeySwitch   |      |
| helib::LabeledEdge   |      |
| helib::LabeledVertex   | . ?? |
| logic_error  |      |
| helib::LogicError  |      |
| LowLvlTimingData   |      |
| helib::MappingData< type >   |      |
| helib::MatMul1D  |      |
| helib::MatMul1D_partial< type >  |      |
| helib::MatMul1D_derived< type >  |      |
| helib::RandomMatrix< type >  | ??   |

3.1 Class Hierarchy 7

| helib::RandomMultiMatrix< type >   |   |           |
|--|---|-----------|
| helib::MatMulFullHelper< type >  |   |           |
| helib::MatMul1D_derived_impl< type >   |   |           |
| helib::MatMul1DExec_construct< type >  |   | ??        |
| helib::MatMulFullExec_construct< type >::MatMulDimComp   | 1 | ??        |
| helib::MatMulExecBase  | 1 | ??        |
| helib::BlockMatMul1DExec   |   | ??        |
| helib::BlockMatMulFullExec   |   |           |
| helib::MatMul1DExec  |   |           |
| helib::MatMulFullExec  |   |           |
| helib::MatMulFull  |   |           |
|  |   |           |
| helib::MatMulFull_derived< type >  |   |           |
| helib::RandomFullMatrix< type >  | 1 | ??        |
| helib::MatMulFullExec_construct< type >  | 1 | ??        |
| helib::ModuliSizes   |   | ??        |
| helib::mul_BlockMatMul1D_impl< type >  |   | ??        |
| helib::mul_BlockMatMulFull_impl< type >  |   | ??        |
| helib::mul_MatMul1D_impl< type >   |   | ??        |
| helib::mul_MatMulFull_impl< type >   |   | ??        |
| helib::mul_pa_impl< type >   |   | ??        |
| MyClass  |   | ??        |
| helib::negate_pa_impl< type >  |   | <br>??    |
| OtherTimingData  |   | <br>??    |
| out of range   |   |           |
| helib::OutOfRangeError   |   | 22        |
|  |   |           |
| helib::PAlgebra  |   |           |
| helib::PAlgebraMod   |   |           |
| helib::PAlgebraModBase   |   |           |
| helib::PAlgebraModCx   | 1 | ??        |
| helib::PAlgebraModDerived< type >  |   | ??        |
| helib::PermNetLayer  | 1 | ??        |
| helib::PermNetwork   | 1 | ??        |
| helib::PGFFT   |   | ??        |
| helib::PlaintextArray  |   | ??        |
| helib::PlaintextArrayBase  |   | ??        |
| helib::PlaintextArrayDerived< type >   |   | ??        |
| helib::PolyMod   |   | · ·<br>?? |
| helib::PolyModRing   |   | : :<br>?? |
| , and the second |   |           |
| helib::PowerfulConversion  |   | ??        |
| helib::PowerfulDCRT  |   | ??        |
| helib::PowerfulTranslationIndexes  |   | ??        |
| helib::PrimeGenerator  |   | ??        |
| helib::print_pa_impl< type >   |   | ??        |
| $helib::PtrMatrix < T > \dots \dots$   |   | ??        |
| helib::PtrMatrix_PtPtrVector< T >  |   |           |
| helib::PtrMatrix_ptVec< T >  | 1 | ??        |
| helib::PtrMatrix_ptvector< T >   |   |           |
| helib::PtrMatrix_Vec< T >  | 1 | ??        |
| helib::PtrMatrix_vector< T >   | 1 | ??        |
| helib::PtrVector< T >  | 1 | ??        |
| helib::PtrVector Singleton< T >  |   | 22        |
| helib::PtrVector_slice< T >  |   |           |
| helib::PtrVector VecPt< T >  |   |           |
| helib::PtrVector_VecT< T >   |   |           |
| helib::PtrVector_vectorPt< T >   |   |           |
| helib::PtrVector_vectorT< T >  |   |           |
| HelibF (I vectol_vector I < 1 >  | : | "         |

8 Hierarchical Index

| nelib::Ptxt                      | ?? |
|----------------------------------|----|
| nelib::PubKey                    | ?? |
| helib::SecKey                    | ?? |
| nelib::PubKeyHack                | ?? |
| nelib::quarter_FFT               | ?? |
| nelib::random_pa_impl< type >    | ?? |
| nelib::RandomState               | ?? |
| nelib::RecryptData               |    |
| helib::ThinRecryptData           |    |
| nelib::replicate_pa_impl< type > | ?? |
| nelib::ReplicateHandler          | ?? |
| helib::ExplicitReplicator        | ?? |
| ReplicateDummy                   |    |
| ReplicateTester                  |    |
| nelib::rotate_pa_impl< type >    |    |
| untime error                     |    |
| helib::RuntimeError              | ?? |
| nelib::ScratchCell               | ?? |
| nelib::shallow_clone < X >       | ?? |
| nelib::shift_pa_impl< type >     |    |
| nelib::SKHandle                  |    |
| StopReplicate                    |    |
| nelib::sub_pa_impl< type >       | ?? |
| nelib::SubDimension              | ?? |
| nelib::ThinEvalMap               | ?? |
| TimingData                       | ?? |
| nelib::TreeNode< T >             | ?? |
| ZZ_pXModulus                     |    |
| helib::ZZ_pXModulus1             | ?? |
| nelib::zz_pXModulus1             | ?? |

## **Chapter 4**

## **Class Index**

### 4.1 Class List

Here are the classes, structs, unions and interfaces with brief descriptions:

| helib::add_pa_impl< type >   | ??  |
|--|-----|
| A class representing the logic of the order of bit products when adding two integers | ??  |
| helib::PGFFT::aligned allocator< T >   | ??  |
| helib::applyPerm_pa_impl< type >   | ??  |
| helib::ArgMap  |     |
|  | ??  |
| Basic class for arg parsing. Example use:  | ??  |
| helib::ArgMap::ArgProcessor  |     |
| helib::BasicAutomorphPrecon  |     |
| Pre-computation to speed many automorphism on the same ciphertext                    | ??  |
| helib::BGV   |     |
| Type for BGV scheme, to be used as template parameter                                | ??  |
| helib::BipartitleGraph   |     |
| A bipartite flow graph   | ??  |
| helib::BlockMatMul1D   | ??  |
| helib::BlockMatMul1D_derived< type >   | ??  |
| helib::BlockMatMul1D_derived_impl< type >  | ??  |
| helib::BlockMatMul1D_partial< type >   | ??  |
| helib::BlockMatMul1DExec   | ??  |
| helib::BlockMatMul1DExec_construct< type >   | ??  |
| helib::BlockMatMulFullExec_construct< type >::BlockMatMulDimComp                     | ??  |
| helib::BlockMatMulFull   | ??  |
| helib::BlockMatMulFull derived< type >   | ??  |
| helib::BlockMatMulFullExec   | ??  |
| helib::BlockMatMulFullExec_construct< type >   | ??  |
| helib::BlockMatMulFullHelper< type >   | ??  |
| helib::CKKS  |     |
| Type for CKKS scheme, to be used as template parameter                               | ??  |
| helib::Cmodulus  |     |
| Provides FFT and iFFT routines modulo a single-precision prime                       | ??  |
| helib::ColPerm   | • • |
| Permuting a single dimension (column) of a hypercube                                 | ??  |
| helib::ConstCubeSlice < T >  |     |
|  | 21  |
| ••   |     |
| helib::ConstMultiplier   | 11  |

10 Class Index

| helib::ConstMultiplier_DoubleCRT  | ??  |
|---|-----|
| helib::ConstMultiplier_zzX  | ??  |
| helib::ConstMultiplierCache   | ??  |
| helib::Context  |     |
| Maintaining the parameters  | ??  |
| helib::Ctxt   |     |
| A Ctxt object holds a single ciphertext   | ??  |
| helib::CtxtPart   |     |
| One entry in a ciphertext std::vector   | ??  |
| helib::CubeSignature  | ??  |
| Holds a vector of dimensions for a hypercube and some additional data                               | "   |
| A lower-dimension slice of a hypercube  | ??  |
| helib::DAGnode  | 11  |
| A node in an addition-DAG structure   | ??  |
| helib::decode_pa_impl< type >   | ??  |
| helib::deep_clone< X >  | • • |
| Deep copy: initialize with clone  | ??  |
| helib::DoubleCRT  | • • |
| Implementing polynomials (elements in the ring R Q) in double-CRT form                              | ??  |
| helib::DoubleCRTHelper  |     |
| A helper class to enforce consistency within an DoubleCRTHelper object                              | ??  |
| helib::DynamicCtxtPowers  |     |
| Store powers of X, compute them dynamically as needed   | ??  |
| helib::encode_pa_impl< type >   | ??  |
| helib::EncryptedArray   |     |
| A simple wrapper for a smart pointer to an EncryptedArrayBase. This is the interface that higher-   |     |
| level code should use   | ??  |
| helib::EncryptedArrayBase   |     |
| Virtual class for data-movement operations on arrays of slots                                       | ??  |
| helib::EncryptedArrayCx   |     |
| A different derived class to be used for the approximate-numbers scheme                             | ??  |
| helib::EncryptedArrayDerived< type >  |     |
| Derived concrete implementation of EncryptedArrayBase   | ??  |
| helib::equals_pa_impl< type >   | ??  |
| helib::EvalMap  |     |
| Class that provides the functionality for the linear transforms used in boostrapping. The con-      |     |
| structor is invoked with three arguments:   | ??  |
| helib::Exception  |     |
| Base class that other HElib exception classes inherit from  | ??  |
| helib::ExplicitReplicator   |     |
| An implementation of ReplicateHandler that explicitly returns all the replicated ciphertexts in one |     |
| big vector  | ??  |
| helib::fhe_stats_record   | ??  |
| helib::FHEtimer   |     |
| A simple class to accumulate time   | ??  |
| helib::FlowEdge   | ??  |
| An edge in a flow graph   |     |
| helib::frobeniusAutomorph_pa_impl< type >   | ??  |
| helib::FullBinaryTree  A simple implementation of full binary trees (each non-leaf has 2 children)  | ??  |
| helib::GenDescriptor  | 11  |
| ·   | ??  |
| A minimal description of a generator for the purpose of building tree                               | ??  |
| helib::General_range< r >   | ??  |
| helib::GeneralAutomorphPrecon_BSGS  | ??  |
| helib::GeneralAutomorphPrecon_FULL  | ??  |
| helib::GeneralAutomorphPrecon_FOLL helib::GeneralAutomorphPrecon_UNKNOWN                            | ??  |
| TrelibGeneral/Automorphi/Frecon_Oraniovalv  | " " |

4.1 Class List

| helib::GeneralBenesNetwork   |    |
|--|----|
| Implementation of generalized Benes Permutation Network  | ?? |
| helib::GeneratorTrees  |    |
| A std::vector of generator trees, one per generator in Zm*/(p)   | ?? |
| helib::half_FFT  | ?? |
| HighLvlTimingData  | ?? |
| helib::HyperCube< T >  | •  |
| A multi-dimensional cube   | ?? |
|  | •  |
| helib::IndexMap< T >   | ~  |
| IndexMap <t> implements a generic map indexed by a dynamic index set</t>   | ?? |
| helib::IndexMapInit< T >   |    |
| Initializing elements in an IndexMap   | ?? |
| helib::IndexSet  |    |
| A dynamic set of non-negative integers   | ?? |
| helib::InvalidArgument   |    |
| Inherits from Exception and std::invalid_argument  | ?? |
| helib::IndexSet::iterator  | ?? |
| helib::general_range< T >::iterator  | ?? |
| helib::KeySwitch   |    |
| Key-switching matrices   | ?? |
| helib::LabeledEdge   |    |
| A generic directed edge in a graph with some labels  | ?? |
| helib::LabeledVertex   | •  |
| A generic node in a graph with some labels   | ?? |
|  |    |
| helib::LogicError  | ~  |
| Inherits from Exception and std::logic_error   | ?? |
| LowLvlTimingData   | ?? |
| helib::MappingData< type >   |    |
| Auxiliary structure to support encoding/decoding slots   | ?? |
| helib::MatMul1D  | ?? |
| helib::MatMul1D_derived< type >  | ?? |
| helib::MatMul1D_derived_impl< type >   | ?? |
| helib::MatMul1D_partial< type >  | ?? |
| helib::MatMul1DExec  | ?? |
| helib::MatMul1DExec_construct< type >  | ?? |
| helib::MatMulFullExec_construct< type >::MatMulDimComp   | ?? |
| helib::MatMulExecBase  | ?? |
| helib::MatMulFull  | ?? |
| helib::MatMulFull_derived< type >  | ?? |
|  | ?? |
| helib::MatMulFullExec  |    |
| helib::MatMulFullExec_construct< type >  | ?? |
| helib::MatMulFullHelper< type >  | ?? |
| helib::ModuliSizes   |    |
| A helper class to map required modulo-sizes to primeSets   | ?? |
| $\label{lockMatMul1D_impl} \\ \text{helib::mul\_BlockMatMul1D\_impl} < \text{type} > \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $               | ?? |
| $helib:: mul\_BlockMatMulFull\_impl < type > \dots $ | ?? |
| helib::mul_MatMul1D_impl< type >   | ?? |
| helib::mul_MatMulFull_impl< type >   | ?? |
| helib::mul_pa_impl < type >  | ?? |
| MyClass  | ?? |
| helib::negate_pa_impl< type >  | ?? |
| OtherTimingData  | ?? |
| helib::OutOfRangeError   | •  |
| Inherits from Exception and std::out_of_range  | ?? |
| · — — •  |    |
| helib::PAlgebra  | ٠. |
| The structure of (Z/mZ)* /(p)  | ?? |
| helib::PAlgebraMod   |    |
| The structure of Z[X]/(Phi_m(X), p)  | ?? |

12 Class Index

| helib::PAlgebraModBase   |     |
|--|-----|
| Virtual base class for PAlgebraMod   | ??  |
| helib::PAlgebraModCx   | ??  |
| helib::PAlgebraModDerived< type >  |     |
| A concrete instantiation of the virtual class  | ??  |
| helib::PermNetLayer  |     |
| The information needed to apply one layer of a permutation network                               | ??  |
| helib::PermNetwork   |     |
| A full permutation network   | ??  |
| helib::PGFFT   | ??  |
|  | ??  |
| helib::PlaintextArray  |     |
| helib::PlaintextArrayBase  | ??  |
| helib::PlaintextArrayDerived< type >   | ??  |
| helib::PolyMod   |     |
| An object that contains an NTL:: ZZX polynomial along with a coefficient modulus p2r and a       |     |
| polynomial modulus G   | ??  |
| helib::PolyModRing   |     |
| Lightweight type for describing the structure of a single slot of the plaintext space            | ??  |
| helib::PowerfulConversion  |     |
| Conversion between powerful representation in R_m/(q) and zz_pX                                  | ??  |
| helib::PowerfulDCRT  | • • |
|  | ??  |
| Conversion between powerful representation, DoubleCRT, and ZZX                                   | "   |
| helib::PowerfulTranslationIndexes  |     |
| Holds index tables for translation between powerful and zz_pX                                    | ??  |
| helib::PrimeGenerator  | ??  |
| helib::print_pa_impl< type >   | ??  |
| helib::PtrMatrix< T >  |     |
| An abstract class for an array of PtrVectors   | ??  |
| helib::PtrMatrix PtPtrVector< T >  |     |
| An implementation of PtrMatrix using vector< PtrVector <t>*&gt;</t>                              | ??  |
| helib::PtrMatrix_ptVec< T >  |     |
| An implementation of PtrMatrix using Vec< Vec <t>*&gt;</t>                                       | ??  |
| •  | 11  |
| helib::PtrMatrix_ptvector< T >   |     |
| An implementation of PtrMatrix using vector< vector <t>*&gt;</t>                                 | ??  |
| helib::PtrMatrix_Vec< T >  |     |
| An implementation of PtrMatrix using Vec< Vec <t>&gt;</t>  | ??  |
| helib::PtrMatrix_vector< T >   |     |
| An implementation of PtrMatrix using vector< vector <t>&gt;</t>                                  | ??  |
| helib::PtrVector< T >  |     |
| Abstract class for an array of objects   | ??  |
| helib::PtrVector_Singleton< T >  |     |
| An implementation of PtrVector from a single T object  | ??  |
| · · · · · · · · · · · · · · · · · · ·  | • • |
| helib::PtrVector_slice < T >   | 20  |
| An implementation of PtrVector as a slice of another PtrVector                                   | ??  |
| helib::PtrVector_VecPt< T >  |     |
| An implementation of PtrVector using Vec <t*></t*>   | ??  |
| helib::PtrVector_VecT< T >   |     |
| An implementation of PtrVector using Vec <t></t>   | ??  |
| helib::PtrVector_vectorPt< T >   |     |
| An implementation of PtrVector using vector <t*></t*>  | ??  |
| helib::PtrVector_vectorT< T >  |     |
| An implementation of PtrVector using vector <t></t>  | ??  |
| helib::Ptxt  |     |
| An object that mimics the functionality of the Ctxt object, and acts as a convenient entry point |     |
|  | 20  |
| for inputting/encoding data which is to be encrypted   | ??  |
| helib::PubKey  |     |
| The public key   | ??  |
| helib::PubKeyHack  | ??  |

4.1 Class List

| helib::quarter_FFT  | ??  |
|---|-----|
| $\verb helib::random_pa_impl  < type > \dots $  | ??  |
| $\label{lockMatrix} \mbox{helib::RandomBlockMatrix} < \mbox{type} > \ \ \ldots \ \ \ \ldots \$ | ??  |
| helib::RandomFullBlockMatrix< type >  | ??  |
| $\label{lem:helib::RandomFullMatrix} \\ \text{helib::RandomFullMatrix} < \\ \text{type} > \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ $   | ??  |
| $helib:: Random Matrix < type > \dots $   | ??  |
| $\label{lem:helib::RandomMultiBlockMatrix} \textbf{kupe} > \dots $  | ??  |
| $\label{lem:helib::RandomMultiMatrix} \textbf{helib::RandomMultiMatrix} < \textbf{type} > \dots $   | ??  |
| helib::RandomState  |     |
| Facility for "restoring" the NTL PRG state  | ??  |
| helib::RecryptData  |     |
| A structure to hold recryption-related data inside the Context  | ??  |
| helib::replicate_pa_impl< type >  | ??  |
| ReplicateDummy  | ??  |
| helib::ReplicateHandler   |     |
| An abstract class to handle call-backs to get the output of replicate   | ??  |
| ReplicateTester   | ??  |
| helib::rotate_pa_impl< type >   | ??  |
| helib::RuntimeError   |     |
| Inherits from Exception and std::runtime_error  | ??  |
| helib::ScratchCell  | ~   |
| A class to help manage the allocation of temporary Ctxt objects   | ??  |
| helib::SecKey   | ~   |
| The secret key  | ??  |
| helib::shallow_clone< X >   | ~   |
| Shallow copy: initialize with copy constructor  | ??  |
| helib::shift_pa_impl< type >  | ??  |
| helib::SKHandle   | ??  |
| A handle, describing the secret-key element that "matches" a part, of the form $s^{\wedge}r(X^{\wedge}t)$   |     |
| StopReplicate   | ??  |
| helib::SubDimension   | •   |
| A node in a tree relative to some generator   | ??  |
| helib::ThinEvalMap  | • • |
| Class that provides the functionality for the linear transforms used in "thin" boostrapping, where  |     |
| slots are assumed to contain constants. The interface is exactly the same as for EvalMap, except  |     |
| that the constructor does not have a normal_basis parameter   | ??  |
| helib::ThinRecryptData  | •   |
| Same as above, but for "thin" bootstrapping, where the slots are assumed to contain constants   | ??  |
| TimingData  | ??  |
| helib::TreeNode< T >  |     |
| A node in a full binary tree  | ??  |
| helib::ZZ pXModulus1  |     |
| Placeholder for pXModulusno optimizations   | ??  |
| helib::zz pXModulus1  |     |
| Auxiliary classes to facilitate faster reduction mod Phi_m(X) when the input has degree less than   |     |
| m   | ??  |

14 Class Index

## **Chapter 5**

## File Index

### 5.1 File List

Here is a list of all files with brief descriptions:

| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/apiAttributes.h .     | ?? |
|--|----|
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/ArgMap.h              |    |
| Easier arg parsing   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/assertions.h          |    |
| Various assertion functions for use within HElib. These are meant as a replacement for C-style         |    |
| asserts, which (undesirably) exit the process without giving the opportunity to clean up and shut      |    |
| down gracefully. Instead, these functions will throw an exception if their conditions are violated     | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/binaryArith.h         |    |
| Implementing integer addition, multiplication in binary representation                                 | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/binaryCompare.h       |    |
| Implementing integer comparison in binary representation   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/binio.h               | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/bluestein.h           |    |
| Declaration of BluesteinFFT(x, n, root, powers, powers_aux, Rb):                                       | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/clonedPtr.h           |    |
| Implementation of smart pointers with "deep cloning" semantics   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/CModulus.h            |    |
| Supports forward and backward length-m FFT transformations   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/Context.h             |    |
| Keeps the parameters of an instance of the cryptosystem  | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/CtPtrs.h              |    |
| Unified interface for vector of pointers to ciphertexts  | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/Ctxt.h                |    |
| Declarations of a BGV-type ciphertext and key-switching matrices                                       | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/debugging.h           |    |
| Debugging utilities  | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/DoubleCRT.h           |    |
| Integer polynomials (elements in the ring R_Q) in double-CRT form $\ldots \ldots \ldots \ldots \ldots$ | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/EncryptedArray.h      |    |
| Data-movement operations on encrypted arrays of slots  | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/EvalMap.h             |    |
| Implementing the recryption linear transformations   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/exceptions.h          |    |
| Various HElib-specific exception types   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/FHE.h                 |    |
| Deprecated entry point header for HElib (legacy alias of helib.h)                                      | ?? |

16 File Index

| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/fhe_stats.h   | ??       |
|--|----------|
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/helib.h   |          |
| Entry point header for HElib   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/hypercube.h   | -00      |
| Hypercubes and their slices  | ??       |
| Implementation of a map indexed by a dynamic set of integers   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/IndexSet.h  | • •      |
| A dynamic set of integers  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/intraSlot.h   |          |
| Packing/unpacking of mod-p integers in GF(p $^{\wedge}$ d) slots   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/keys.h  |          |
| Declaration of public key  |          |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/keySwitching.h  | ??       |
| Declaration of key switching matrices  |          |
| // Jacys/Dysicate/FLIF LIFIib Dance Dublic staging/bomane vd 0.0// IFIib/inglyde/balib/matching b  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/matching.h  Classes and functions for max-flow in a generic graph                                   | ??       |
| /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/matmul.h  | "        |
| Some matrix / linear algenra stuff   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/multicore.h   |          |
| Support for multi-threaded implementations   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/norms.h   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/NumbTh.h  |          |
| Miscellaneous utility functions  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/PAlgebra.h  |          |
| Declarations of the classes PAlgebra   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/permutations.h  | -00      |
| Permutations over Hypercubes and their slices  | ??<br>?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/PGFFT.h /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/polyEval.h | "        |
| Homomorphic Polynomial Evaluation  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/PolyMod.h   | ••       |
| Underlying slot type structure of BGV ptxts  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/PolyModRing.h   |          |
| Definition of the plaintext slot algebraic ring  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/powerful.h  |          |
| The "powerful basis" of a cyclotomic ring  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/primeChain.h  |          |
| Handling the chain of moduli   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/PtrMatrix.h   |          |
| Convenience class templates providing a unified interface for a matrix of objects, returning point-  | 22       |
| ers to these objects   | ??       |
| Convenience class templates providing a unified interface for a collection of objects, returning   |          |
| pointers to these objects  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/Ptxt.h  | • •      |
| Plaintext object parameterised on CKKS and BGV schemes. Also contains definition of CKKS   |          |
| and BGV structs  | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/randomMatrices.h  |          |
| Implementation of random matrices of various forms, used for testing   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/range.h   | ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/recryption.h  |          |
| Define some data structures to hold recryption data  | ??       |

5.1 File List

| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/replicate.h       |
|--|
| Procedures for replicating a ciphertext slot across a full ciphertext                              |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/sample.h ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/tableLookup.h     |
| Code for homomorphic table lookup and fixed-point functions  |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/timing.h          |
| Utility functions for measuring time   |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/include/helib/zzX.h ??          |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/BenesNetwork.cpp ??         |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/binaryArith.cpp             |
| Implementing integer addition, multiplication in binary representation                             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/binaryCompare.cpp           |
| Implementing integer comparison in binary representation   |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/binio.cpp ??                |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/bluestein.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/CModulus.cpp ??             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Context.cpp ??              |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Ctxt.cpp                    |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/debugging.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/DoubleCRT.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/EaCx.cpp ??                 |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/EncryptedArray.cpp ??       |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/eqtesting.cpp               |
| Useful functions for equality testing??  |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/EvalMap.cpp ??              |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/extractDigits.cpp ??        |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/fhe_stats.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/hypercube.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/IndexSet.cpp ??             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/intraSlot.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/keys.cpp                    |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/keySwitching.cpp            |
| A few strategies for generating key-switching matrices   |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/matching.cpp ??             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/matmul.cpp ??               |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/norms.cpp ??                |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/NumbTh.cpp ??               |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/OptimizePermutations.cpp ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/PAlgebra.cpp ??             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/PermNetwork.cpp ??          |
| /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/permutations.cpp ??         |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/PGFFT.cpp ??                |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/polyEval.cpp ??             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/PolyMod.cpp ??              |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/PolyModRing.cpp ??          |
| /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/powerful.cpp ??             |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/primeChain.cpp              |
| Handling the chain of moduli   |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Ptxt.cpp                    |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/randomMatrices.cpp          |
| Implementation of random matrices of various forms build functions, used for testing ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/recryption.cpp ??           |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/replicate.cpp ??            |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/sample.cpp ??               |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/tableLookup.cpp             |
| Code for homomorphic table lookup and fixed-point functions  |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_approxNums.cpp ??      |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_Bin_IO.cpp ??          |
|  |

18 File Index

| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_binaryArith.cpp       | ?? |
|---|----|
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_binaryCompare.cpp .   | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_bootstrapping.cpp     | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_EaCx.cpp              | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_EvalMap.cpp           | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_extractDigits.cpp     | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_fatboot.cpp           | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_General.cpp           | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_intraSlot.cpp         | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_IO.cpp                | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_matmul.cpp            | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_PAlgebra.cpp          | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_Permutations.cpp      | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_PGFFT.cpp             | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_PolyEval.cpp          | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_Powerful.cpp          | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_PtrVector.cpp         | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_Replicate.cpp         | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_tableLookup.cpp       | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_thinboot.cpp          | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_ThinBootstrapping.cpp |    |
| ??  |    |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_ThinEvalMap.cpp       | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/Test_Timing.cpp            | ?? |
| /Users/Projects/FHE_HElib_Repos_Public_staging/homenc_v1.0.2/HElib/src/timing.cpp                 | ?? |
| /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/zzX.cpp                    | ?? |

## **Chapter 6**

## **Namespace Documentation**

### 6.1 Fft Namespace Reference

#### **Functions**

- void transform (std::vector < lcx > &vec)
- void inverseTransform (std::vector< lcx > &vec)
- void transformRadix2 (std::vector < lcx > &vec)
- void transformBluestein (std::vector< lcx > &vec)
- void convolve (const std::vector< lcx > &vecx, const std::vector< lcx > &vecy, std::vector< lcx > &vecout)

### 6.1.1 Function Documentation

#### 6.1.1.1 convolve()

### 6.1.1.2 inverseTransform()

#### 6.1.1.3 transform()

```
void Fft::transform ( std::vector < \ lcx \ > \ \& \ vec \ )
```

#### 6.1.1.4 transformBluestein()

```
void Fft::transformBluestein ( std::vector < lcx > \& vec )
```

#### 6.1.1.5 transformRadix2()

```
void Fft::transformRadix2 ( {\tt std::vector} < {\tt lcx} \, > \, \& \, \, vec \, )
```

### 6.2 helib Namespace Reference

#### **Namespaces**

• FHEglobals

#### **Classes**

- class add\_pa\_impl
- class AddDAG

A class representing the logic of the order of bit products when adding two integers.

- class applyPerm\_pa\_impl
- class ArgMap

Basic class for arg parsing. Example use:

• class BasicAutomorphPrecon

Pre-computation to speed many automorphism on the same ciphertext.

• struct BGV

Type for BGV scheme, to be used as template parameter.

· class BipartitleGraph

A bipartite flow graph.

- class BlockMatMul1D
- · class BlockMatMul1D\_derived
- struct BlockMatMul1D\_derived\_impl
- class BlockMatMul1D\_partial
- class BlockMatMul1DExec
- struct BlockMatMul1DExec\_construct
- class BlockMatMulFull
- · class BlockMatMulFull derived
- · class BlockMatMulFullExec

- struct BlockMatMulFullExec construct
- class BlockMatMulFullHelper
- struct CKKS

Type for CKKS scheme, to be used as template parameter.

class Cmodulus

Provides FFT and iFFT routines modulo a single-precision prime.

class ColPerm

Permuting a single dimension (column) of a hypercube.

· class ConstCubeSlice

A constant lower-dimension slice of a hypercube.

- struct ConstMultiplier
- struct ConstMultiplier DoubleCRT
- struct ConstMultiplier zzX
- · struct ConstMultiplierCache
- · class Context

Maintaining the parameters.

· class Ctxt

A Ctxt object holds a single ciphertext.

· class CtxtPart

One entry in a ciphertext std::vector.

· class CubeSignature

Holds a vector of dimensions for a hypercube and some additional data.

· class CubeSlice

A lower-dimension slice of a hypercube.

class DAGnode

A node in an addition-DAG structure.

- · class decode\_pa\_impl
- · class deep clone

Deep copy: initialize with clone.

class DoubleCRT

Implementing polynomials (elements in the ring R\_Q) in double-CRT form.

· class DoubleCRTHelper

A helper class to enforce consistency within an DoubleCRTHelper object.

class DynamicCtxtPowers

Store powers of X, compute them dynamically as needed.

- class encode\_pa\_impl
- class EncryptedArray

A simple wrapper for a smart pointer to an EncryptedArrayBase. This is the interface that higher-level code should use.

class EncryptedArrayBase

virtual class for data-movement operations on arrays of slots

class EncryptedArrayCx

A different derived class to be used for the approximate-numbers scheme.

class EncryptedArrayDerived

Derived concrete implementation of EncryptedArrayBase.

- class equals\_pa\_impl
- class EvalMap

Class that provides the functionality for the linear transforms used in boostrapping. The constructor is invoked with three arguments:

class Exception

Base class that other HElib exception classes inherit from.

· class ExplicitReplicator

An implementation of ReplicateHandler that explicitly returns all the replicated ciphertexts in one big vector.

- struct fhe\_stats\_record
- · class FHEtimer

A simple class to accumulate time.

class FlowEdge

An edge in a flow graph.

- · class frobeniusAutomorph pa impl
- class FullBinaryTree

A simple implementation of full binary trees (each non-leaf has 2 children)

· class GenDescriptor

A minimal description of a generator for the purpose of building tree.

- · class general range
- class GeneralAutomorphPrecon
- class GeneralAutomorphPrecon\_BSGS
- class GeneralAutomorphPrecon FULL
- class GeneralAutomorphPrecon\_UNKNOWN
- · class GeneralBenesNetwork

Implementation of generalized Benes Permutation Network.

· class GeneratorTrees

A std::vector of generator trees, one per generator in Zm\*/(p)

- · struct half FFT
- · class HyperCube

A multi-dimensional cube.

class IndexMap

IndexMap<T> implements a generic map indexed by a dynamic index set.

class IndexMapInit

Initializing elements in an IndexMap.

class IndexSet

A dynamic set of non-negative integers.

class InvalidArgument

Inherits from Exception and std::invalid\_argument.

class KeySwitch

Key-switching matrices.

class LabeledEdge

A generic directed edge in a graph with some labels.

· class LabeledVertex

A generic node in a graph with some labels.

class LogicError

Inherits from Exception and std::logic\_error.

· class MappingData

Auxiliary structure to support encoding/decoding slots.

- class MatMul1D
- · class MatMul1D derived
- struct MatMul1D derived impl
- class MatMul1D\_partial
- class MatMul1DExec
- struct MatMul1DExec\_construct
- class MatMulExecBase
- class MatMulFull
- · class MatMulFull derived
- class MatMulFullExec
- struct MatMulFullExec\_construct

- class MatMulFullHelper
- · class ModuliSizes

A helper class to map required modulo-sizes to primeSets.

- struct mul BlockMatMul1D impl
- struct mul\_BlockMatMulFull\_impl
- struct mul\_MatMul1D\_impl
- struct mul\_MatMulFull\_impl
- · class mul\_pa\_impl
- · class negate pa impl
- class OutOfRangeError

Inherits from Exception and std::out\_of\_range.

• class PAlgebra

The structure of (Z/mZ)\* /(p)

class PAlgebraMod

The structure of  $Z[X]/(Phi_m(X), p)$ 

• class PAlgebraModBase

Virtual base class for PAlgebraMod.

- class PAlgebraModCx
- class PAlgebraModDerived

A concrete instantiation of the virtual class.

class PermNetLayer

The information needed to apply one layer of a permutation network.

class PermNetwork

A full permutation network.

- class PGFFT
- class PlaintextArray
- · class PlaintextArrayBase
- class PlaintextArrayDerived
- class PolyMod

An object that contains an NTL: : ZZX polynomial along with a coefficient modulus p2r and a polynomial modulus G.

struct PolyModRing

Lightweight type for describing the structure of a single slot of the plaintext space.

· class PowerfulConversion

Conversion between powerful representation in R\_m/(q) and zz\_pX.

class PowerfulDCRT

Conversion between powerful representation, DoubleCRT, and ZZX.

• class PowerfulTranslationIndexes

Holds index tables for translation between powerful and zz\_pX.

- struct PrimeGenerator
- class print\_pa\_impl
- struct PtrMatrix

An abstract class for an array of PtrVectors.

struct PtrMatrix\_PtPtrVector

An implementation of PtrMatrix using vector< PtrVector<T>\*>

struct PtrMatrix ptVec

An implementation of PtrMatrix using Vec< Vec<T>\*>

struct PtrMatrix\_ptvector

An implementation of PtrMatrix using vector< vector< T>\*>

• struct PtrMatrix Vec

An implementation of PtrMatrix using Vec< Vec<T>>

struct PtrMatrix\_vector

An implementation of PtrMatrix using vector< vector< T>>

struct PtrVector

Abstract class for an array of objects.

• struct PtrVector\_Singleton

An implementation of PtrVector from a single T object.

• struct PtrVector\_slice

An implementation of PtrVector as a slice of another PtrVector.

struct PtrVector VecPt

An implementation of PtrVector using Vec<T\*>

struct PtrVector\_VecT

An implementation of PtrVector using Vec<T>

struct PtrVector\_vectorPt

An implementation of PtrVector using vector< T\*>

• struct PtrVector\_vectorT

An implementation of PtrVector using vector<T>

· class Ptxt

An object that mimics the functionality of the Ctxt object, and acts as a convenient entry point for inputting/encoding data which is to be encrypted.

class PubKey

The public key.

- struct PubKeyHack
- struct quarter\_FFT
- · class random\_pa\_impl
- · class RandomBlockMatrix
- · class RandomFullBlockMatrix
- · class RandomFullMatrix
- class RandomMatrix
- · class RandomMultiBlockMatrix
- class RandomMultiMatrix
- class RandomState

Facility for "restoring" the NTL PRG state.

class RecryptData

A structure to hold recryption-related data inside the Context.

- class replicate\_pa\_impl
- class ReplicateHandler

An abstract class to handle call-backs to get the output of replicate.

- · class rotate\_pa\_impl
- class RuntimeError

Inherits from Exception and std::runtime\_error.

class ScratchCell

A class to help manage the allocation of temporary Ctxt objects.

· class SecKey

The secret key.

class shallow\_clone

Shallow copy: initialize with copy constructor.

- class shift\_pa\_impl
- class SKHandle

A handle, describing the secret-key element that "matches" a part, of the form  $s^{\wedge}r(X^{\wedge}t)$ .

- class sub\_pa\_impl
- class SubDimension

A node in a tree relative to some generator.

class ThinEvalMap

Class that provides the functionality for the linear transforms used in "thin" boostrapping, where slots are assumed to contain constants. The interface is exactly the same as for EvalMap, except that the constructor does not have a normal\_basis parameter.

· class ThinRecryptData

Same as above, but for "thin" bootstrapping, where the slots are assumed to contain constants.

class TreeNode

A node in a full binary tree.

class zz\_pXModulus1

Auxiliary classes to facilitate faster reduction mod Phi\_m(X) when the input has degree less than m.

class ZZ pXModulus1

placeholder for pXModulus ...no optimizations

### **Typedefs**

- typedef PtrVector < Ctxt > CtPtrs
- typedef PtrVector\_VecT< Ctxt > CtPtrs\_VecCt
- typedef PtrVector vectorT< Ctxt > CtPtrs vectorCt
- typedef PtrVector VecPt< Ctxt > CtPtrs VecPt
- $\bullet \ \ typedef \ PtrVector\_vectorPt < Ctxt > CtPtrs\_vectorPt \\$
- typedef PtrVector\_slice < Ctxt > CtPtrs\_slice
- typedef PtrMatrix < Ctxt > CtPtrMat
- typedef PtrMatrix\_Vec< Ctxt > CtPtrMat\_VecCt
- typedef PtrMatrix\_vector< Ctxt > CtPtrMat\_vectorCt
- typedef PtrMatrix\_ptVec< Ctxt > CtPtrMat\_ptVecCt
- typedef PtrMatrix\_ptvector< Ctxt > CtPtrMat\_ptvectorCt
- typedef std::shared\_ptr< DoubleCRT > DCRTptr
- typedef std::shared\_ptr< NTL::ZZX > ZZXptr
- typedef std::complex< double > cx\_double
- typedef std::unordered map< long, FlowEdge > FNeighborList
- typedef std::vector< FNeighborList > FlowGraph
- typedef std::unordered\_multimap< long, LabeledEdge > LNeighborList
- typedef long LONG
- typedef NTL::Vec< long > Permut

A simple permutation is just a vector with p[i]=\pi\_i.

- typedef FullBinaryTree< SubDimension > OneGeneratorTree
- typedef NTL::Vec< long > zzX
- typedef std::pair< long, long > Nodeldx
- template < class T >
   using aligned\_vector = PGFFT::aligned\_vector < T >
- typedef complex< double > cmplx\_t
- · typedef long double Idbl

#### **Enumerations**

enum PA\_tag { PA\_GF2\_tag, PA\_zz\_p\_tag, PA\_cx\_tag }

#### **Functions**

- template<typename ExceptionTy = ::helib::LogicError, typename T = void> void assertTrue (const T &value, const std::string &message)
- template < typename ExceptionTy = ::helib::LogicError, typename T = void> void assertFalse (T value, const std::string &message)
- template<typename ExceptionTy = ::helib::LogicError, typename T = void>
   void assertEq (const T &a, const T &b, const std::string &message)
- template < typename ExceptionTy = ::helib::LogicError, typename T = void> void assertNeq (const T &a, const T &b, const std::string &message)
- template<typename ExceptionTy = ::helib::LogicError, typename T = void> void assertNotNull (const T &p, const std::string &message)
- template<typename ExceptionTy = ::helib::OutOfRangeError, typename T = void>
   void assertInRange (const T &elem, const T &min, const T &max, const std::string &message, bool right\_
   inclusive=false)
- std::vector< long > longToBitVector (long num, long bitSize)

Returns a number as a vector of bits with LSB on the left.

void binaryCond (CtPtrs &output, const Ctxt &cond, const CtPtrs &trueValue, const CtPtrs &falseValue)

Implementation of output = cond \* trueValue + (1 - cond) \* falseValue.

void binaryMask (CtPtrs &binaryNums, const Ctxt &mask)

Zeroes the slots of binaryNums where the corresponding slot of mask is 0.

void concatBinaryNums (CtPtrs &output, const CtPtrs &a, const CtPtrs &b)

Concatenates two binary numbers into a single CtPtrs object. E.g. If a=10111, b=00101 then output = 1011100101.

void splitBinaryNums (CtPtrs &leftSplit, CtPtrs &rightSplit, const CtPtrs &input)

Splits a single binary number into two binary numbers leftSplit and rightSplit.

• void leftBitwiseShift (CtPtrs &output, const CtPtrs &input, const long shamt)

Left shift input by shamt.

void bitwiseRotate (CtPtrs &output, const CtPtrs &input, long rotamt)

Rotate input by rotamt.

void bitwiseXOR (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise XOR between 1hs and rhs.

· void bitwiseOr (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise OR between 1hs and rhs.

void bitwiseAnd (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise AND between 1hs and rhs.

void bitwiseAnd (CtPtrs &output, const CtPtrs &input, const std::vector < long > mask)

Compute a bitwise AND between input and a std::vector<long>.

· void bitwiseNot (CtPtrs &output, const CtPtrs &input)

Compute a bitwise NOT of input.

void addTwoNumbers (CtPtrs &sum, const CtPtrs &lhs, const CtPtrs &rhs, long sizeLimit=0, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Adds two numbers in binary representation where each ciphertext of the input vector contains a bit.

void negateBinary (CtPtrs &negation, const CtPtrs &input)

Negates a number in binary 2's complement representation.

void subtractBinary (CtPtrs &difference, const CtPtrs &lhs, const CtPtrs &rhs, std::vector < zzX > \*unpack ← SlotEncoding=nullptr)

Subtracts rhs from 1hs where 1hs, rhs are in 2's complement.

• long fifteenOrLess4Four (const CtPtrs &out, const CtPtrs &in, long sizeLimit=4)

Add together up to fifteen {0,1} integers, producing a 4-bit counter.

void addManyNumbers (CtPtrs &sum, CtPtrMat &numbers, long sizeLimit=0, std::vector < zzX > \*unpack ← SlotEncoding=nullptr)

Sum an arbitrary amount of numbers in binary representation.

void multTwoNumbers (CtPtrs &product, const CtPtrs &lhs, const CtPtrs &rhs, bool rhsTwos
 — Complement=false, long sizeLimit=0, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Multiply two numbers in binary representation where each ciphertext of the input vector contains a bit.

 void decryptBinaryNums (std::vector < long > &pNums, const CtPtrs &eNums, const SecKey &sKey, const EncryptedArray &ea, bool twosComplement=false, bool allSlots=true)

Decrypt the binary numbers that are encrypted in eNums.

• void packedRecrypt (const CtPtrs &a, const CtPtrs &b, std::vector< zzX > \*unpackSlotEncoding)

Function for packed recryption to recrypt multiple numbers.

 void compareTwoNumbers (CtPtrs &max, CtPtrs &min, Ctxt &mu, Ctxt &ni, const CtPtrs &a, const CtPtrs &b, bool twosComplement=false, std::vector< zzX > \*unpackSlotEncoding=nullptr)

Compares two integers in binary a, b. Returns max(a, b), min(a, b) and indicator bits mu=(a>b) and ni=(a<b)

void compareTwoNumbers (Ctxt &mu, Ctxt &ni, const CtPtrs &a, const CtPtrs &b, bool twos
 Complement=false, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Compares two integers in binary a, b. Returns only indicator bits mu=(a>b) and ni=(a<b).

- int readEyeCatcher (std::istream &str, const char \*expect)
- void writeEyeCatcher (std::ostream &str, const char \*eye)
- void write\_ntl\_vec\_long (std::ostream &str, const NTL::vec\_long &vl, long intSize=BINIO\_64BIT)
- void read\_ntl\_vec\_long (std::istream &str, NTL::vec\_long &vl)
- long read raw int (std::istream &str)
- int read\_raw\_int32 (std::istream &str)
- void write\_raw\_int (std::ostream &str, long num)
- void write raw int32 (std::ostream &str, int num)
- void write raw double (std::ostream &str, const double d)
- double read\_raw\_double (std::istream &str)
- void write\_raw\_xdouble (std::ostream &str, const NTL::xdouble xd)
- NTL::xdouble read\_raw\_xdouble (std::istream &str)
- void write\_raw\_ZZ (std::ostream &str, const NTL::ZZ &zz)
- void read\_raw\_ZZ (std::istream &str, NTL::ZZ &zz)
- $\bullet \ \ template {<} typename \ T >$

void write raw vector (std::ostream &str, const std::vector< T > &v)

- template<> void write\_raw\_vector< long > (std::ostream &str, const std::vector< long > &v)
- template<> void write\_raw\_vector< double > (std::ostream &str, const std::vector< double > &v)
- template<typename T >

void read\_raw\_vector (std::istream &str, std::vector< T > &v, T &init)

 $\bullet \ \ template {<} typename \ T >$ 

 $\label{eq:condition} \mbox{void read\_raw\_vector} \mbox{ (std::istream \&str, std::vector} < \mbox{T} > \&\mbox{v)}$ 

- template<> void read\_raw\_vector< long > (std::istream &str, std::vector< long > &v)
- template<> void read raw vector< double > (std::istream &str, std::vector< double > &v)
- template<typename T >

void read\_raw\_vector (std::istream &str, std::vector < T > &v, const Context &context)

void BluesteinInit (long n, const NTL::zz\_p &root, NTL::zz\_pX &powers, NTL::Vec< NTL::mulmod\_precon\_t > &powers\_aux, NTL::fftRep &Rb)

initialize bluestein

• void BluesteinFFT (NTL::zz\_pX &x, long n, const NTL::zz\_p &root, const NTL::zz\_pX &powers, const NTL ∴: ::Vec < NTL::mulmod\_precon\_t > &powers\_aux, const NTL::fftRep &Rb)

apply bluestein

• template<typename X , typename Cloner >

 $void \ swap \ (cloned\_ptr < X, \ Cloner > \&x, \ cloned\_ptr < X, \ Cloner > \&y)$ 

• template<typename X , typename Cloner >

void swap (copied\_ptr< X, Cloner > &x, copied\_ptr< X, Cloner > &y)

• long FindM (long k, long nBits, long c, long p, long d, long s, long chosen\_m, bool verbose=false)

Returns smallest parameter m satisfying various constraints:

void writeContextBase (std::ostream &s, const Context &context)

write [m p r gens ords] data

void readContextBase (std::istream &s, unsigned long &m, unsigned long &p, unsigned long &r, std::vector<
long > &gens, std::vector< long > &ords)

read [m p r gens ords] data, needed to construct context

- std::unique\_ptr< Context > buildContextFromAscii (std::istream &str)
- void writeContextBaseBinary (std::ostream &str, const Context &context)

write [m p r gens ords] data

- void writeContextBinary (std::ostream &str, const Context &context)
- void readContextBaseBinary (std::istream &s, unsigned long &m, unsigned long &p, unsigned long &r, std
   ::vector < long > &gens, std::vector < long > &ords)

read [m p r gens ords] data, needed to construct context

- std::unique\_ptr< Context > buildContextFromBinary (std::istream &str)
- void readContextBinary (std::istream &str, Context &context)
- void buildModChain (Context &context, long nBits, long nDgts=3, bool willBeBootstrappable=false, long sk
   Hwt=0, long resolution=3, long bitsInSpecialPrimes=0)
- void endBuildModChain (Context &context)
- void packedRecrypt (const CtPtrs &cPtrs, const std::vector< zzX > &unpackConsts, const EncryptedArray &ea)
- void packedRecrypt (const CtPtrs & array, const std::vector < zzX > & unpackConsts, const EncryptedArray & ea, long belowLvl)
- void packedRecrypt (const CtPtrMat &m, const std::vector< zzX > &unpackConsts, const EncryptedArray &ea, long belowLvl=LONG MAX)
- long findMinBitCapacity (const CtPtrs &v)
- long findMinBitCapacity (const CtPtrMat &m)
- long findMinBitCapacity (std::initializer\_list< const CtPtrs \* > list)
- void innerProduct (Ctxt &result, const CtPtrs &v1, const CtPtrs &v2)
- Ctxt innerProduct (const CtPtrs &v1, const CtPtrs &v2)
- std::ostream & operator << (std::ostream &s, const SKHandle &handle)
- std::istream & operator>> (std::istream &s, CtxtPart &p)
- std::ostream & operator<< (std::ostream &s, const CtxtPart &p)</li>
- void totalProduct (Ctxt &out, const std::vector< Ctxt > &v)
- void incrementalProduct (std::vector < Ctxt > &v)
- void innerProduct (Ctxt &result, const std::vector < Ctxt > &v1, const std::vector < Ctxt > &v2)
- Ctxt innerProduct (const std::vector < Ctxt > &v1, const std::vector < Ctxt > &v2)
- void innerProduct (Ctxt &result, const std::vector< Ctxt > &v1, const std::vector< DoubleCRT > &v2)

Compute the inner product of a vectors of ciphertexts and a constant vector.

- Ctxt innerProduct (const std::vector < Ctxt > &v1, const std::vector < DoubleCRT > &v2)
- void innerProduct (Ctxt &result, const std::vector < Ctxt > &v1, const std::vector < NTL::ZZX > &v2)
- Ctxt innerProduct (const std::vector < Ctxt > &v1, const std::vector < NTL::ZZX > &v2)
- void CheckCtxt (const Ctxt &c, const char \*label)

print to cerr some info about ciphertext

void extractDigits (std::vector < Ctxt > &digits, const Ctxt &c, long r=0)

Extract the mod-p digits of a mod-p<sup>^</sup> r ciphertext.

- void extractDigits (std::vector < Ctxt > &digits, const Ctxt &c, long r, bool shortCut)
- void extendExtractDigits (std::vector < Ctxt > &digits, const Ctxt &c, long r, long e)
- void setupDebugGlobals (SecKey \*debug\_key, const std::shared\_ptr< const EncryptedArray > &debug\_ea, NTL::ZZX debug\_ptxt=NTL::ZZX{})

Setup function for setting up the global debug variables.

• void cleanupDebugGlobals ()

Cleanup function for clearing the global debug variables.

- void decryptAndPrint (std::ostream &s, const Ctxt &ctxt, const SecKey &sk, const EncryptedArray &ea, long flags=0)
- NTL::xdouble embeddingLargestCoeff (const Ctxt &ctxt, const SecKey &sk)
- double realToEstimatedNoise (const Ctxt &ctxt, const SecKey &sk)

- void checkNoise (const Ctxt &ctxt, const SecKey &sk, const std::string &msg, double thresh=10.0)
- bool decryptAndCompare (const Ctxt &ctxt, const SecKey &sk, const EncryptedArray &ea, const PlaintextArray &pa)
- void rawDecrypt (NTL::ZZX &plaintxt, const std::vector< NTL::ZZX > &zzParts, const DoubleCRT &sKey, long q=0)
- template<typename VEC >
  - std::ostream & printVec (std::ostream &s, const VEC &v, long nCoeffs=40)
- std::ostream & printZZX (std::ostream &s, const NTL::ZZX &poly, long nCoeffs=40)
- void conv (DoubleCRT &d, const NTL::ZZX &p)
- void conv (NTL::ZZX &p, const DoubleCRT &d)
- NTL::ZZX to ZZX (const DoubleCRT &d)
- template<typename RX , typename RXModulus >
   void plaintextAutomorph (RX &bb, const RX &a, long k, long m, const RXModulus &PhimX)
- template<typename RX , typename type >
   void plaintextAutomorph (RX &b, const RX &a, long i, long j, const EncryptedArrayDerived< type > &ea)
- EncryptedArrayBase \* buildEncryptedArray (const Context &context, const PAlgebraMod &alMod, const N

  TL::ZZX &G=NTL::ZZX::zero())

A "factory" for building EncryptedArrays.

- std::ostream & operator<< (std::ostream &s, const PlaintextArray &pa)</li>
- void rotate (const EncryptedArray &ea, PlaintextArray &pa, long k)
- void shift (const EncryptedArray &ea, PlaintextArray &pa, long k)
- void encode (const EncryptedArray &ea, PlaintextArray &pa, const std::vector < long > &array)
- void encode (const EncryptedArray &ea, PlaintextArray &pa, const std::vector < NTL::ZZX > &array)
- void encode (const EncryptedArray &ea, PlaintextArray &pa, long val)
- void encode (const EncryptedArray &ea, PlaintextArray &pa, const NTL::ZZX &val)
- void random (const EncryptedArray &ea, PlaintextArray &pa)
- void decode (const EncryptedArray &ea, std::vector< long > &array, const PlaintextArray &pa)
- void decode (const EncryptedArray &ea, std::vector < NTL::ZZX > &array, const PlaintextArray &pa)
- bool equals (const EncryptedArray &ea, const PlaintextArray &pa, const PlaintextArray &other)
- bool equals (const EncryptedArray &ea, const PlaintextArray &pa, const std::vector < long > &other)
- bool equals (const EncryptedArray &ea, const PlaintextArray &pa, const std::vector< NTL::ZZX > &other)
- void add (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void sub (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void mul (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void negate (const EncryptedArray &ea, PlaintextArray &pa)
- void frobeniusAutomorph (const EncryptedArray &ea, PlaintextArray &pa, long j)
- void frobeniusAutomorph (const EncryptedArray &ea, PlaintextArray &pa, const NTL::Vec< long > &vec)
- void applyPerm (const EncryptedArray &ea, PlaintextArray &pa, const NTL::Vec< long > &pi)
- void power (const EncryptedArray &ea, PlaintextArray &pa, long e)
- void runningSums (const EncryptedArray &ea, Ctxt &ctxt)

A ctxt that encrypts  $(x_1,...,x_n)$  is replaced by an encryption of  $(y_1,...,y_n)$ , where  $y_i = sum_{j \le i}x_j$ .

- void print\_stats (std::ostream &s)
- const std::vector< double > \* fetch\_saved\_values (const char \*)
- std::ostream & operator<< (std::ostream &s, const CubeSignature &sig)</li>
- template<typename T >

 $\mbox{void getHyperColumn (NTL::Vec< T > \&v, const \ \mbox{ConstCubeSlice} < T > \&s, \ \mbox{long pos)} \label{eq:constCubeSlice}$ 

template < typename T >
 void setHyperColum

template<typename T >

 $\label{eq:const} \mbox{void setHyperColumn (const NTL::Vec< T > \&v, const CubeSlice< T > \&s, long pos, const T \&val)} \\$ 

• template<typename T >

void print3D (const HyperCube < T > &c)

• template<typename T >

bool operator== (const IndexMap< T > &map1, const IndexMap< T > &map2)

Comparing maps, by comparing all the elements.

• template<typename T >

bool operator!= (const IndexMap< T > &map1, const IndexMap< T > &map2)

IndexSet operator (const IndexSet &s, const IndexSet &t)

unior

IndexSet operator& (const IndexSet &s, const IndexSet &t)

intersection

IndexSet operator<sup>∧</sup> (const IndexSet &s, const IndexSet &t)

exclusive-or

IndexSet operator/ (const IndexSet &s, const IndexSet &t)

set minus

- std::ostream & operator<< (std::ostream &str, const IndexSet &set)</li>
- std::istream & operator>> (std::istream &str, IndexSet &set)
- long card (const IndexSet &s)

Functional cardinality.

- bool empty (const IndexSet &s)
- bool operator<= (const IndexSet &s1, const IndexSet &s2)</li>

Is s1 subset or equal to s2.

bool operator< (const IndexSet &s1, const IndexSet &s2)</li>

Is s1 strict subset of s2.

bool operator>= (const IndexSet &s1, const IndexSet &s2)

Is s2 subset or equal to s2.

bool operator> (const IndexSet &s1, const IndexSet &s2)

Is s2 strict subset of s1.

bool disjoint (const IndexSet &s1, const IndexSet &s2)

Functional disjoint.

- void buildUnpackSlotEncoding (std::vector< zzX > &unpackSlotEncoding, const EncryptedArray &ea)
- void unpack (const CtPtrs &unpacked, const Ctxt &packed, const EncryptedArray &ea, const std::vector
   zzX > &unpackSlotEncoding)
- long unpack (const CtPtrs &unpacked, const CtPtrs &packed, const EncryptedArray &ea, const std::vector
   zzX > &unpackSlotEncoding)
- void repack (Ctxt &packed, const CtPtrs &unpacked, const EncryptedArray &ea)
- long repack (const CtPtrs &packed, const CtPtrs &unpacked, const EncryptedArray &ea)
- void unpackSlots (std::vector< unsigned long > &value, PlaintextArray &pa, const EncryptedArray &ea)
- void unpackSlots (std::vector< unsigned long > &value, NTL::ZZX &pa, const EncryptedArray &ea)
- void packConstant (zzX &result, unsigned long data, long nbits, const EncryptedArray &ea)
- void packConstants (zzX &result, const std::vector< unsigned long > &data, long nbits, const EncryptedArray &ea)
- void writePubKeyBinary (std::ostream &str, const PubKey &pk)
- void readPubKeyBinary (std::istream &str, PubKey &pk)
- void writeSecKeyBinary (std::ostream &str, const SecKey &sk)
- void readSecKeyBinary (std::istream &str, SecKey &sk)
- double RLWE (DoubleCRT &c0, DoubleCRT &c1, const DoubleCRT &s, long p, NTL::ZZ \*prgSeed=nullptr)
- double RLWE1 (DoubleCRT &c0, const DoubleCRT &c1, const DoubleCRT &s, long p)

Same as RLWE, but assumes that c1 is already chosen by the caller.

- std::ostream & operator<< (std::ostream &str, const KeySwitch &matrix)</li>
- long maximum\_flow (FlowGraph &fg, long src, long sink)
- void traceMap (Ctxt &ctxt)
- void mul (PlaintextArray &pa, const MatMul1D &mat)
- void mul (PlaintextArray &pa, const BlockMatMul1D &mat)
- void mul (PlaintextArray &pa, const MatMulFull &mat)
- void mul (PlaintextArray &pa, const BlockMatMulFull &mat)
- long sumOfCoeffs (const zzX &f)
- NTL::ZZ sumOfCoeffs (const NTL::ZZX &f)

- NTL::ZZ sumOfCoeffs (const DoubleCRT &f)
- template<typename T >

double largestCoeff (const NTL::Vec< T > &f)

The L-infinity norm of an element (in coefficient representation)

• template<typename T >

double largestCoeff (const std::vector< T > &f)

- NTL::ZZ largestCoeff (const NTL::ZZX &f)
- NTL::ZZ largestCoeff (const NTL::Vec< NTL::ZZ > &f)
- NTL::ZZ largestCoeff (const DoubleCRT &f)
- double coeffsL2NormSquared (const zzX &f)

The L2-norm of an element (in coefficient representation)

- NTL::xdouble coeffsL2NormSquared (const NTL::ZZX &f)
- NTL::xdouble coeffsL2NormSquared (const DoubleCRT &f)
- double coeffsL2Norm (const zzX &f)
- NTL::xdouble coeffsL2Norm (const NTL::ZZX &f)
- NTL::xdouble coeffsL2Norm (const DoubleCRT &f)
- double embeddingLargestCoeff (const zzX &f, const PAlgebra &palg)
- double embeddingLargestCoeff (const std::vector< double > &f, const PAlgebra &palg)
- void embeddingLargestCoeff\_x2 (double &norm1, double &norm2, const std::vector< double > &f1, const std::vector< double > &f2, const PAlgebra &palg)
- NTL::xdouble embeddingLargestCoeff (const NTL::ZZX &f, const PAlgebra &palg)
- void CKKS canonicalEmbedding (std::vector < cx double > &v, const zzX &f, const PAlgebra &palg)
- void CKKS\_canonicalEmbedding (std::vector < cx\_double > &v, const NTL::ZZX &f, const PAlgebra &palg)
- void CKKS\_canonicalEmbedding (std::vector< cx\_double > &v, const std::vector< double > &f, const PAlgebra &palg)
- void CKKS\_embedInSlots (zzX &f, const std::vector < cx\_double > &v, const PAlgebra &palg, double scaling)
- bool setDryRun (bool toWhat=true)
- bool isDryRun ()
- void setAutomorphVals (std::set< long > \*aVals)
- bool isSetAutomorphVals ()
- void recordAutomorphVal (long k)
- void setAutomorphVals2 (std::set< long > \*aVals)
- bool isSetAutomorphVals2 ()
- void recordAutomorphVal2 (long k)
- long bitSetToLong (long bits, long bitSize)

Considers bits as a vector of bits and returns the value it represents when interpreted as a n-bit 2's complement number, where n is given by bitSize.

• long mcMod (long a, long b)

Routines for computing mathematically correct mod and div.

- long mcDiv (long a, long b)
- long balRem (long a, long q)
- double fsquare (double x)

Return the square of a number as a double.

• long multOrd (long p, long m)

Return multiplicative order of p modulo m, or 0 if GCD(p, m) = 1.

- void ppsolve (NTL::vec\_zz\_pE &x, const NTL::mat\_zz\_pE &A, const NTL::vec\_zz\_pE &b, long p, long r)

  Prime power solver.
- void ppsolve (NTL::vec\_GF2E &x, const NTL::mat\_GF2E &A, const NTL::vec\_GF2E &b, long p, long r)

A version for GF2: must have p == 2 and r == 1.

• void ppInvert (NTL::mat\_zz\_p &X, const NTL::mat\_zz\_p &A, long p, long r)

Compute the inverse mod  $p^{\wedge}r$  of an  $n \times n$  matrix.

- void ppInvert (NTL::mat zz pE &X, const NTL::mat zz pE &A, long p, long r)
- void ppInvert (NTL::mat GF2 &X, const NTL::mat GF2 &A, UNUSED long p, UNUSED long r)
- void ppInvert (NTL::mat\_GF2E &X, const NTL::mat\_GF2E &A, UNUSED long p, UNUSED long r)

- void buildLinPolyMatrix (NTL::mat\_zz\_pE &M, long p)
- void buildLinPolyMatrix (NTL::mat\_GF2E &M, long p)
- void buildLinPolyCoeffs (NTL::vec\_zz\_pE &C, const NTL::vec\_zz\_pE &L, long p, long r)

Combination of buildLinPolyMatrix and ppsolve.

void buildLinPolyCoeffs (NTL::vec\_GF2E &C, const NTL::vec\_GF2E &L, long p, long r)

A version for GF2: must be called with p == 2 and r == 1.

void applyLinPoly (NTL::zz\_pE &beta, const NTL::vec\_zz\_pE &C, const NTL::zz\_pE &alpha, long p)

Apply a linearized polynomial with coefficient vector C.

• void applyLinPoly (NTL::GF2E &beta, const NTL::vec\_GF2E &C, const NTL::GF2E &alpha, long p)

A version for GF2: must be called with p == 2 and r == 1.

• double log2 (const NTL::xdouble &x)

Base-2 logarithm.

void factorize (std::vector < long > &factors, long N)

Factoring by trial division, only works for N<2<sup>\(\)</sup>{60}, only the primes are recorded, not their multiplicity.

- void factorize (std::vector < NTL::ZZ > &factors, const NTL::ZZ &N)
- void factorize (NTL::Vec< NTL::Pair< long, long >> &factors, long N)

Factoring by trial division, only works for  $N<2^{\wedge}$  {60} primes and multiplicities are recorded.

void pp\_factorize (std::vector< long > &factors, long N)

Prime-power factorization.

void phiN (long &phiN, std::vector< long > &facts, long N)

Compute Phi(N) and also factorize N.

- void phiN (NTL::ZZ &phiN, std::vector< NTL::ZZ > &facts, const NTL::ZZ &N)
- long phi N (long N)

Compute Phi(N).

- long findGenerators (std::vector< long > &gens, std::vector< long > &ords, long m, long p, const std
   ::vector< long > &candidates=std::vector< long >())
- void FindPrimitiveRoot (NTL::zz\_p &r, unsigned long e)

Find e-th root of unity modulo the current modulus.

- void FindPrimitiveRoot (NTL::ZZ\_p &r, unsigned long e)
- long mobius (long n)

Compute mobius function (naive method as n is small).

• NTL::ZZX Cyclotomic (long N)

Compute cyclotomic polynomial.

• NTL::ZZX makeIrredPoly (long p, long d)

Return a degree-d irreducible polynomial mod p.

long primroot (long N, long phiN)

Find a primitive root modulo N.

• long ord (long N, long p)

Compute the highest power of p that divides N.

- bool is2power (long m)
- NTL::ZZX RandPoly (long n, const NTL::ZZ &p)
- void MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long q, bool abs)
- void MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long g)
- NTL::ZZX MulMod (const NTL::ZZX &f, long a, long q, bool abs)
- NTL::ZZX MulMod (const NTL::ZZX &f, long a, long q)
- void balanced\_MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long q)
- template<typename T1 , typename T2 >

void convert (T1 &x1, const T2 &x2)

A generic template that resolves to NTL's conv routine.

- template<typename T1 , typename T2 >

void convert (std::vector< T1 > &v1, const std::vector< T2 > &v2)

generic vector conversion routines

```
• template<typename T1 , typename T2 >
  void convert (std::vector< T1 > &v1, const NTL::Vec< T2 > &v2)
• template<typename T1 , typename T2 >
  void convert (NTL::Vec< T1 > &v1, const std::vector< T2 > &v2)

    template<typename T >

  void convert (std::vector < T > &v1, const std::vector < T > &v2)
      Trivial type conversion, useful for generic code.
• template<typename T1 , typename T2 >
  T1 convert (const T2 &v2)
• template<typename T >
  std::vector < T > vector replicate (const T &a, long n)

    template<typename T >

  std::vector< T > Vec replicate (const T &a, long n)

    long computeProd (const NTL::Vec< long > &vec)

     returns \prod_d vec[d]

    long computeProd (const std::vector< long > &vec)

    void mul (std::vector < NTL::ZZX > &x, const std::vector < NTL::ZZX > &a, long b)

    void div (std::vector < NTL::ZZX > &x, const std::vector < NTL::ZZX > &a, long b)

    void add (std::vector< NTL::ZZX > &x, const std::vector< NTL::ZZX > &a, const std::vector< NTL::ZZX >

  &b)

    long is_in (long x, int *X, long sz)

     Finds whether x is an element of the set X of size sz, Returns -1 it not and the location if true.

    long CRTcoeff (long p, long q, bool symmetric=false)

     Returns a CRT coefficient: x = (0 \mod p, 1 \mod q). If symmetric is set then x \ln [-pq/2, pq/2), else x \ln [0,pq)

    template < class zzvec >

  bool intVecCRT (NTL::vec_ZZ &vp, const NTL::ZZ &p, const zzvec &vq, long q)
     Incremental integer CRT for vectors.

    template<typename T, bool maxFlag>

  long argminmax (std::vector< T > &v)
     Find the index of the (first) largest/smallest element.
• template<typename T >
  long argmax (std::vector< T > &v)
• template<typename T >
  long argmin (std::vector< T > &v)

    long argmax (std::vector < long > &v, bool(*moreThan)(long, long))

     A variant with a specialized comparison function (*moreThan)(a,b) returns the comparison a>b.

    bool closeToOne (const NTL::xdouble &x, long p)

    std::pair< long, long > rationalApprox (double x, long denomBound=0)

    std::pair< NTL::ZZ, NTL::ZZ > rationalApprox (NTL::xdouble x, NTL::xdouble denomBound=NTL←

  ::xdouble(0.0))

    void seekPastChar (std::istream &str, int cc)

     Advance the input stream beyond white spaces and a single instance of the char cc.
• template<typename T >
  void reverse (NTL::Vec< T > &v, long lo, long hi)
     Reverse a vector in place.
• template<typename T >
  void rotate (NTL::Vec< T > &v, long k)
     Rotate a vector in place using swaps.
• template<typename T >
  long lsize (const std::vector< T > &v)
     Size of STL vector as a long (rather than unsigned long)
• template<typename T >
  void killVec (std::vector< T > &vec)
     NTL/std compatibility.
```

```
• template<typename T >
  void killVec (NTL::Vec< T > &vec)
• template<typename T >
  void setLengthZero (std::vector< T > &vec)

    template<typename T >

  void setLengthZero (NTL::Vec< T > &vec)
• template<typename T >
  long lsize (const NTL::Vec< T > &v)
template<typename T >
  void resize (NTL::Vec< T > &v, long sz, const T &val)

    template<typename T >

  void resize (std::vector< T > &v, long sz, const T &val)
• template<typename T >
  void resize (NTL::Vec< T > &v, long sz)
• template<typename T >
  void resize (std::vector< T > &v, long sz)
• template<typename T1 , typename T2 >
  bool sameObject (const T1 *p1, const T2 *p2)
      Testing if two vectors point to the same object.

    void ModComp (NTL::ZZX &res, const NTL::ZZX &g, const NTL::ZZX &h, const NTL::ZZX &f)

     Modular composition of polynomials: res = g(h) \mod f.

    long polyEvalMod (const NTL::ZZX &poly, long x, long p)

     Evaluates a modular integer polynomial, returns poly(x) mod p.

    void interpolateMod (NTL::ZZX &poly, const NTL::vec_long &x, const NTL::vec_long &y, long p, long e=1)

     Interpolate polynomial such that poly(x[i] \mod p) = y[i] \pmod{p^e} It is assumed that the points x[i] are all distinct modulo
• long divc (long a, long b)
     returns ceiling(a/b); assumes a >=0, b>0, a+b <= MAX_LONG

    void rem (NTL::zz_pX &r, const NTL::zz_pX &a, const zz_pXModulus1 &ff)

template<typename T >
  std::ostream & operator << (std::ostream &s, std::vector < T > v)
• template<typename T >
  std::istream & operator>> (std::istream &s, std::vector< T > &v)
template<typename T >
  std::string vecToStr (const std::vector< T > &v)
• template<typename T >
 NTL::Vec< T> atoVec (const char *a)
• template<typename T >
  std::vector < T > atovector (const char *a)

    void TofftRep trunc (NTL::fftRep &y, const NTL::zz pX &x, long k, UNUSED long len, long lo, long hi)

    void TofftRep_trunc (NTL::fftRep &y, const NTL::zz_pX &x, long k, long len)

• template<typename T , typename P , typename... Args>
  void make_lazy (const NTL::Lazy< T, P > &obj, Args &&... args)
• template<typename T , typename P , typename F , typename... Args>
  void make_lazy_with_fun (const NTL::Lazy< T, P > &obj, F f, Args &&... args)

    void Warning (const char *msg)

    void Warning (const std::string &msg)

    PAlgebraModBase * buildPAlgebraMod (const PAlgebra &zMStar, long r)

      Builds a table, of type PA\_GF2 if p == 2 and r == 1, and PA\_zz\_p otherwise.
• bool comparePAlgebra (const PAlgebra &palg, unsigned long m, unsigned long p, unsigned long r, const
  std::vector< long > &gens, const std::vector< long > &ords)
     returns true if the palg parameters match the rest, false otherwise

    double calcPolyNormBnd (long m)

    template<typename T >
```

void applyPermToVec (NTL::Vec< T > &out, const NTL::Vec< T > &in, const Permut &p1)

Apply a permutation to a std::vector, out[i]=in[p1[i]] (NOT in-place)

• template<typename T >

void applyPermToVec (std::vector< T > &out, const std::vector< T > &in, const Permut &p1)

template<typename T >

void applyPermsToVec (NTL::Vec< T > &out, const NTL::Vec< T > &in, const Permut &p2, const Permut &p1)

Apply two permutations to a std::vector out[i]=in[p2[p1[i]]] (NOT in-place)

• template<typename T >

void applyPermsToVec (std::vector < T > &out, const std::vector < T > &in, const Permut &p2, const Permut &p1)

• void randomPerm (Permut &perm, long n)

A random size-n permutation.

- std::ostream & operator<< (std::ostream &s, const ColPerm &p)</li>
- void breakPermByDim (std::vector< ColPerm > &out, const Permut &pi, const CubeSignature &sig)

Takes a permutation pi over m-dimensional cube  $C=Z_{n1} \times ... \times Z_{m}$  and expresses pi as a product pi =  $rho_{m}$  {2m-1} o ... o  $rho_{n}$  o  $rho_{n}$  where each  $rho_{n}$  is a column permutation along one dimension. Specifically for i < m, the permutations  $rho_{n}$  and  $rho_{n}$  permute the i'th dimension.

void polyEval (Ctxt &ret, NTL::ZZX poly, const Ctxt &x, long k=0)

Evaluate a cleartext polynomial on an encrypted input.

void polyEval (Ctxt &ret, const NTL::Vec< Ctxt > &poly, const Ctxt &x)

Evaluate an encrypted polynomial on an encrypted input.

- std::ostream & operator<< (std::ostream &s, const ModuliSizes::Entry &e)</li>
- std::istream & operator>> (std::istream &s, ModuliSizes::Entry &e)
- void write (std::ostream &s, const ModuliSizes::Entry &e)
- void read (std::istream &s, ModuliSizes::Entry &e)
- template<typename T >

long Isize (const PtrMatrix< T > &v)

 $\bullet \ \ template {<} typename \ T >$ 

void resize (PtrMatrix< T > &v, long newSize)

• template<typename T >

void setLengthZero (PtrMatrix< T > &v)

• template<typename T >

const T \* ptr2nonNull (std::initializer\_list< const PtrVector< T > \* > list)

• template<typename T >

long Isize (const PtrVector< T > &v)

 $\bullet \ \ template {<} typename \ T >$ 

void setLengthZero (PtrVector< T > &v)

• template<typename T >

void resize (PtrVector< T > &v, long newSize, const T &val)

template<typename T >

void resize (PtrVector< T > &v, long newSize, const T \*val)

• template<typename V1 , typename V2 >

void vecCopy (V1 &v1, const V2 &v2, long sizeLimit=0)

• template<typename V , typename T >

void vecCopy (V &v1, const PtrVector< T > &v2, long sizeLimit=0)

template<typename V , typename T >

void vecCopy (PtrVector< T > &v1, const V &v2, long sizeLimit=0)

• template<typename T >

void vecCopy (PtrVector< T > &v1, const PtrVector< T > &v2, long sizeLimit=0)

- template<typename From , typename Scheme >

std::vector< typename Scheme::SlotType > convertDataToSlotVector (const std::vector< From > &data, const Context &context)

Converts std::vector<From> to std::vector<Scheme::SlotType>.

• template<typename Scheme >

void innerProduct (Ptxt< Scheme > &result, const std::vector< Ptxt< Scheme >> &first\_vec, const std↔ ::vector< Ptxt< Scheme >> &second vec)

Free function that computes the inner product of two vectors of Ptxt.

- MatMul1D \* buildRandomMatrix (const EncryptedArray &ea, long dim)
- MatMul1D \* buildRandomMultiMatrix (const EncryptedArray &ea, long dim)
- BlockMatMul1D \* buildRandomBlockMatrix (const EncryptedArray &ea, long dim)
- BlockMatMul1D \* buildRandomMultiBlockMatrix (const EncryptedArray &ea, long dim)
- MatMulFull \* buildRandomFullMatrix (const EncryptedArray &ea)
- BlockMatMulFull \* buildRandomFullBlockMatrix (const EncryptedArray &ea)
- general\_range< long > range (long n)
- general range< long > range (long m, long n)
- void replicate (const EncryptedArray &ea, Ctxt &ctx, long pos)

The value in slot #pos is replicated in all other slots. On an n-slot ciphertext, this algorithm performs O(log n) 1D rotations.

void replicate0 (const EncryptedArray &ea, Ctxt &ctxt, long pos)

A lower-level routine. Same as replicate, but assumes all slots are zero except slot #pos.

- void replicateAll (const EncryptedArray &ea, const Ctxt &ctxt, ReplicateHandler \*handler, long recBound=64, RepAuxDim \*repAuxPtr=nullptr)
- void replicateAll (std::vector< Ctxt > &v, const EncryptedArray &ea, const Ctxt &ctxt, long recBound=64, RepAuxDim \*repAuxPtr=nullptr)
- template<typename Scheme >

void replicateAll (std::vector < Ptxt < Scheme >> &v, const EncryptedArray &, const Ptxt < Scheme > &ptxt)

Generate a vector of plaintexts with each slot replicated in each plaintext.

- void replicateAllOrig (const EncryptedArray &ea, const Ctxt &ctxt, ReplicateHandler \*handler, RepAux \*rep
   — AuxPtr=nullptr)
- void replicate (const EncryptedArray &ea, PlaintextArray &pa, long i)
- template<typename Scheme >

void replicate (const EncryptedArray &, Ptxt< Scheme > &ptxt, long i)

Replicate single slot of a Ptxt object across all of its slots.

- void sampleSmall (zzX &poly, long n, double prob=0.5)
- void sampleSmall (NTL::ZZX &poly, long n, double prob=0.5)
- void sampleHWt (zzX &poly, long n, long Hwt=100)

Sample a degree-(n-1) poly as above, with only Hwt nonzero coefficients.

- void sampleHWt (NTL::ZZX &poly, long n, long Hwt=100)
- void sampleGaussian (zzX &poly, long n, double stdev)

Sample polynomials with Gaussian coefficients.

- void sampleGaussian (NTL::ZZX &poly, long n, double stdev)
- void sampleUniform (zzX &poly, long n, long B=100)

Sample a degree-(n-1) ZZX, with coefficients uniform in [-B,B].

- void sampleUniform (NTL::ZZX &poly, long n, const NTL::ZZ &B=NTL::ZZ(100L))
- void sampleGaussian (std::vector< double > &dvec, long n, double stdev)

Choose a vector of continuous Gaussians.

- double sampleHWt (zzX &poly, const Context &context, long Hwt=100)
- double sampleHWtBounded (zzX &poly, const Context &context, long Hwt=100)
- double sampleHWtBoundedEffectiveBound (const Context &context, long Hwt=100)
- double sampleSmall (zzX &poly, const Context &context)
- double sampleSmallBounded (zzX &poly, const Context &context)
- double sampleGaussian (zzX &poly, const Context &context, double stdev)
- double sampleGaussianBounded (zzX &poly, const Context &context, double stdev)
- double sampleUniform (zzX &poly, const Context &context, long B=100)
- NTL::xdouble sampleUniform (NTL::ZZX &poly, const Context &context, const NTL::ZZ &B=NTL::ZZ(100L))
- void reduceModPhimX (zzX &poly, const PAlgebra &palg)
- const NTL::zz\_pXModulus & getPhimXMod (const PAlgebra &palg)
- void computeAllProducts (CtPtrs &products, const CtPtrs &array, std::vector < zzX > \*unpackSlot ← Encoding=nullptr)

- void tableLookup (Ctxt &out, const std::vector< zzX > &table, const CtPtrs &idx, std::vector< zzX > \*unpackSlotEncoding=nullptr)
- void tableWriteIn (const CtPtrs &table, const CtPtrs &idx, std::vector < zzX > \*unpackSlotEncoding=nullptr)
- void buildLookupTable (std::vector< zzX > &T, std::function< double(double)> f, long nbits\_in, long scale\_in, long sign\_in, long nbits\_out, long scale\_out, long sign\_out, const EncryptedArray &ea)

Built a table-lookup for a function in fixed-point representation.

- void registerTimer (FHEtimer \*timer)
- · unsigned long GetTimerClock ()
- void setTimersOn ()
- void setTimersOff ()
- bool areTimersOn ()
- const FHEtimer \* getTimerByName (const char \*name)
- void resetAllTimers ()
- void printAllTimers (std::ostream &str=std::cerr)

Print the value of all timers to stream.

- bool printNamedTimer (std::ostream &str, const char \*name)
- bool IsZero (const zzX &a)
- void clear (zzX &a)
- void convert (NTL::zz\_pX &x, const zzX &a)
- void add (zzX &res, const zzX &a, const zzX &b)
- zzX operator+ (const zzX &a, const zzX &b)
- zzX & operator+= (zzX &a, const zzX &b)
- void div (zzX &res, const zzX &a, long b)
- zzX operator/ (const zzX &a, long b)
- zzX & operator/= (zzX &a, long b)
- void mul (zzX &res, const zzX &a, long b)
- zzX operator\* (const zzX &a, long b)
- zzX & operator\*= (zzX &a, long b)
- void normalize (zzX &f)
- void MulMod (zzX &res, const zzX &a, const zzX &b, const PAlgebra &palg)
- zzX MulMod (const zzX &a, const zzX &b, const PAlgebra &palg)
- zzX balanced\_zzX (const NTL::zz\_pX &f)
- zzX balanced zzX (const NTL::GF2X &f)
- long defaultPmiddle (long delta)
- long defaultQmiddle (long delta)
- void runningSums (CtPtrs &v)
- void compareTwoNumbersImplementation (CtPtrs &max, CtPtrs &min, Ctxt &mu, Ctxt &ni, const CtPtrs &aa, const CtPtrs &bb, bool twosComplement, std::vector< zzX > \*unpackSlotEncoding, bool cmp\_only)
- void BluesteinFFT (NTL::zz\_pX &x, long n, UNUSED const NTL::zz\_p &root, const NTL::zz\_pX &powers, const NTL::Vec< NTL::mulmod\_precon\_t > &powers\_aux, const NTL::fftRep &Rb)
- NTL::zz\_pContext BuildContext (long p, long maxroot)
- std::ostream & operator<< (std::ostream &str, const Context &context)</li>
- std::istream & operator>> (std::istream &str, Context &context)
- NTL::ZZX getG (const EncryptedArray &ea)
- void addSomePrimes (Ctxt &c)
- void computeIntervalForMul (double &lo, double &hi, const Ctxt &ctxt1, const Ctxt &ctxt2)
- void computeIntervalForSqr (double &lo, double &hi, const Ctxt &ctxt)
- std::istream & operator>> (std::istream &str, SKHandle &handle)
- std::ostream & operator<< (std::ostream &str, const Ctxt &ctxt)
- std::istream & operator>> (std::istream &str, Ctxt &ctxt)
- double log2\_realToEstimatedNoise (const Ctxt &ctxt, const SecKey &sk)
- template DoubleCRT & DoubleCRT::Op< DoubleCRT::AddFun > (const DoubleCRT &other, AddFun fun, bool matchIndexSets)
- template DoubleCRT & DoubleCRT::Op< DoubleCRT::SubFun > (const DoubleCRT &other, SubFun fun, bool matchIndexSets)

- template DoubleCRT & DoubleCRT::Op < DoubleCRT::MulFun > (const NTL::ZZ &num, MulFun fun)
- template DoubleCRT & DoubleCRT::Op< DoubleCRT::AddFun > (const NTL::ZZ &num, AddFun fun)
- template DoubleCRT & DoubleCRT::Op < DoubleCRT::SubFun > (const NTL::ZZ &num, SubFun fun)
- template DoubleCRT & DoubleCRT::Op < DoubleCRT::MulFun > (const NTL::ZZX &poly, MulFun fun)
- template DoubleCRT & DoubleCRT::Op < DoubleCRT::AddFun > (const NTL::ZZX &poly, AddFun fun)
- template DoubleCRT & DoubleCRT::Op < DoubleCRT::SubFun > (const NTL::ZZX &poly, SubFun fun)
- std::ostream & operator<< (std::ostream &str, const DoubleCRT &d)</li>
- std::istream & operator>> (std::istream &str, DoubleCRT &d)
- void totalSums (const EncryptedArray &ea, Ctxt &ctxt)
- void applyLinPoly1 (const EncryptedArray &ea, Ctxt &ctxt, const std::vector < NTL::ZZX > &C)
- void applyLinPolyMany (const EncryptedArray &ea, Ctxt &ctxt, const std::vector < std::vector < NTL::ZZX >> &Cvec)
- template<typename P >
   void applyLinPolyLL (Ctxt &ctxt, const std::vector< P > &encodedC, long d)
- template void applyLinPolyLL (Ctxt &ctxt, const std::vector< zzX > &encodedC, long d)
- template void applyLinPolyLL (Ctxt &ctxt, const std::vector< NTL::ZZX > &encodedC, long d)
- template void applyLinPolyLL (Ctxt &ctxt, const std::vector < DoubleCRT > &encodedC, long d)
- void print (const EncryptedArray &ea, std::ostream &s, const PlaintextArray &pa)
- void mapTo01 (const EncryptedArray &ea, Ctxt &ctxt)
- template<typename Scheme > void mapTo01 (const EncryptedArray &, Ptxt< Scheme > &ptxt)
- template void mapTo01 (const EncryptedArray &, Ptxt< BGV > &ptxt)
- template void mapTo01 (const EncryptedArray &, Ptxt< CKKS > &ptxt)
- void fastPower (Ctxt &ctxt, long d)
- void incrementalZeroTest (Ctxt \*res[], const EncryptedArray &ea, const Ctxt &ctxt, long n)
- void RelaxedInv (NTL::Mat< NTL::zz p > &x, const NTL::Mat< NTL::zz p > &a)
- void RelaxedInv (NTL::Mat< NTL::GF2 > &x, const NTL::Mat< NTL::GF2 > &a)
- void TraceMap (NTL::GF2X &w, const NTL::GF2X &a, long d, const NTL::GF2XModulus &F, const NTL::GF2X &b)
- template void getHyperColumn (NTL::Vec< long > &v, const ConstCubeSlice< long > &s, long pos)
- $\bullet \ \ \text{template void setHyperColumn (const NTL::Vec< long>\&v, const \ \ \ \ \text{CubeSlice} < long>\&s, long \ pos)\\$
- template void setHyperColumn (const NTL::Vec< long > &v, const CubeSlice< long > &s, long pos, const long &val)
- template void print3D (const HyperCube < long > &c)
- template void getHyperColumn (NTL::Vec< NTL::zz\_p > &v, const ConstCubeSlice< NTL::zz\_p > &s, long pos)
- template void setHyperColumn (const NTL::Vec< NTL::zz\_p > &v, const CubeSlice< NTL::zz\_p > &s, long pos)
- template void setHyperColumn (const NTL::Vec< NTL::zz\_p > &v, const CubeSlice< NTL::zz\_p > &s, long pos, const NTL::zz\_p &val)
- template void print3D (const HyperCube < NTL::zz\_p > &c)
- std::ostream & operator<< (std::ostream &str, const PubKey &pk)</li>
- std::istream & operator>> (std::istream &str, PubKey &pk)
- std::ostream & operator<< (std::ostream &str, const SecKey &sk)</li>
- std::istream & operator>> (std::istream &str, SecKey &sk)
- void printFlow (FlowGraph &fg)
- std::shared\_ptr< GeneralAutomorphPrecon > buildGeneralAutomorphPrecon (const Ctxt &ctxt, long dim, const EncryptedArray &ea)
- template<typename RX >
  - $std::shared\_ptr < ConstMultiplier > build\_ConstMultiplier \ (const \ RX \ \&poly)$
- template<typename RX , typename type >
   std::shared\_ptr< ConstMultiplier > build\_ConstMultiplier (const RX &poly, long dim, long amt, const EncryptedArrayDerived< type > &ea)
- void MulAdd (Ctxt &x, const std::shared ptr< ConstMultiplier > &a, const Ctxt &b)
- void DestMulAdd (Ctxt &x, const std::shared\_ptr< ConstMultiplier > &a, Ctxt &b)

- void GenBabySteps (std::vector< std::shared\_ptr< Ctxt >> &v, const Ctxt &ctxt, long dim, bool clean)
- template < typename zp , typename zz > void FindPrimRootT (zp &root, unsigned long e)
- template bool intVecCRT (NTL::vec\_ZZ &, const NTL::ZZ &, const NTL::vec\_ZZ &, long)
- template bool intVecCRT (NTL::vec ZZ &, const NTL::ZZ &, const NTL::vec long &, long)
- template bool intVecCRT (NTL::vec ZZ &, const NTL::ZZ &, const NTL::Vec < NTL::zz p > &, long)
- void removeDups (std::list< long > &x, bool \*aux)
- void addOffset (std::list< long > &x, long offset, long n, bool \*aux, UNUSED bool good=false)
- long reducedCount (const std::list< long > &x, long n, bool \*aux)
- void buildBenesCostTable (long n, long k, bool good, NTL::Vec< NTL::Vec< long >> &tab)
- std::ostream & operator<< (std::ostream &s, LongNodePtr p)</li>
- BenesMemoEntry optimalBenesAux (long i, long budget, long nlev, const NTL::Vec< NTL::Vec< long >> &costTab, BenesMemoTable &memoTab)
- void optimalBenes (long n, long budget, bool good, long &cost, LongNodePtr &solution)
- void print (std::ostream &s, SplitNodePtr p, bool first)
- std::ostream & operator<< (std::ostream &s, SplitNodePtr p)</li>
- long length (GenNodePtr ptr)
- std::ostream & operator<< (std::ostream &s, GenNodePtr p)</li>
- LowerMemoEntry optimalLower (long order, bool good, long budget, long mid, LowerMemoTable &lower

   MemoTable)
- UpperMemoEntry optimalUpperAux (const NTL::Vec< GenDescriptor > &vec, long i, long budget, long mid, UpperMemoTable &upperMemoTable, LowerMemoTable &lowerMemoTable)
- template<typename RX > bool poly comp (const RX &a, const RX &b)
- bool less\_than (NTL::GF2 a, NTL::GF2 b)
- bool less\_than (NTL::zz\_p a, NTL::zz\_p b)
- bool less\_than (const NTL::GF2X &a, const NTL::GF2X &b)
- bool less\_than (const NTL::zz\_pX &a, const NTL::zz\_pX &b)
- bool less than (const NTL::GF2E &a, const NTL::GF2E &b)
- bool less\_than (const NTL::zz\_pE &a, const NTL::zz\_pE &b)
- bool less\_than (const NTL::GF2EX &a, const NTL::GF2EX &b)
- bool less than (const NTL::zz pEX &a, const NTL::zz pEX &b)
- bool comparePAlgebra (const PAlgebra &palg, unsigned long m, unsigned long p, UNUSED unsigned long r, const std::vector< long > &gens, const std::vector< long > &ords)
- template < typename T > void PAlgebraLift (const NTL::ZZX &phimx, const T &lfactors, T &factors, T &crtc, long r)
- void EDF (NTL::vec\_zz\_pX &v, const NTL::zz\_pX &f, long d)
- NTL::zz\_pEX FrobeniusMap (const NTL::zz\_pEXModulus &F)
   void InvModpr (NTL::zz\_pX &S, const NTL::zz\_pX &F, const NTL::zz\_pX &G, long p, long r)
- template<> void PAlgebraLift (const NTL::ZZX &phimx, const NTL::vec\_zz\_pX &lfactors, NTL::vec\_zz\_pX &ractors, NTL::vec\_zz\_pX &crtc, long r)
- std::ostream & operator<< (std::ostream &s, const PermNetwork &net)</li>
- template void applyPermToVec< long > (NTL::Vec< long > &out, const NTL::Vec< long > &in, const Permut &p1)
- template void applyPermToVec< long > (std::vector< long > &out, const std::vector< long > &in, const Permut &p1)
- template void applyPermToVec< NTL::ZZX > (std::vector< NTL::ZZX > &out, const std::vector< NTL::ZZX > &in, const Permut &p1)
- template void applyPermsToVec< long > (NTL::Vec< long > &out, const NTL::Vec< long > &in, const Permut &p2, const Permut &p1)
- template void applyPermsToVec< long > (std::vector< long > &out, const std::vector< long > &in, const Permut &p2, const Permut &p1)
- void breakPermTo3 (const HyperCube < long > &pi, long dim, ColPerm &rho1, HyperCube < long > &rho2, ColPerm &rho3)
- void ComputeOneGenMapping (Permut &genMap, const OneGeneratorTree &T)

to a single generator tree

- std::ostream & operator<< (std::ostream &s, const SubDimension &sd)</li>
- std::ostream & operator<< (std::ostream &s, const GeneratorTrees &trees)</li>
- std::istream & operator>> (std::istream &is, PolyMod &poly)
- std::ostream & operator<< (std::ostream &os, const PolyMod &poly)</li>
- std::ostream & operator<< (std::ostream &os, const PolyModRing &ring)</li>
- void computeDivVec (NTL::Vec< long > &divVec, long m, const NTL::Vec< long > &powVec)
- void computeInvVec (NTL::Vec< long > &invVec, const NTL::Vec< long > &divVec, const NTL::Vec< long > &powVec)
- bool operator> (const ModuliSizes::Entry &a, const ModuliSizes::Entry &b)
- std::ostream & operator<< (std::ostream &s, const ModuliSizes &szs)</li>
- std::istream & operator>> (std::istream &s, ModuliSizes &szs)
- void addSmallPrimes (Context &context, long resolution, long cpSize)

Add small primes to get target resolution.

- long ctxtPrimeSize (long nBits)
- void addCtxtPrimes (Context &context, long nBits, long targetSize)
- template<typename Scheme >

Scheme::SlotType randomSlot (const Context &context)

- template<> BGV::SlotType randomSlot< BGV > (const Context &context)
- template<> CKKS::SlotType randomSlot< CKKS > (UNUSED const Context &context)
- void extractDigitsPacked (Ctxt &ctxt, long botHigh, long r, long ePrime, const std::vector< NTL::ZZX > &unpackSlotEncoding)
- void extractDigitsThin (Ctxt &ctxt, long botHigh, long r, long ePrime)
- · double boundRoundingNoise (UNUSED long m, long phim, long p2r, double epsilon)
- bool timer compare (const FHEtimer \*a, const FHEtimer \*b)

### **Variables**

- Context \* activeContext = nullptr
- SecKey \* dbgKey = nullptr
- std::shared\_ptr< const EncryptedArray > dbgEa = nullptr
- NTL::ZZX dbg ptxt
- bool fhe\_stats = false
- int fhe\_test\_force\_bsgs = 0
- int fhe test force hoist = 0
- · const long double PI
- const double erfc\_inverse []
- · long thinRecrypt initial level
- long fhe\_force\_chen\_han = 0
- long printFlag
- NTL\_THREAD\_LOCAL bool replicateVerboseFlag = false
- int fhe\_watcher = 0
- const unsigned long CLOCK\_SCALE = (unsigned long)CLOCKS\_PER\_SEC

# Strategies for generating key-switching matrices

These functions are implemented in KeySwitching.cpp

• long KSGiantStepSize (long D)

Function that returns number of baby steps. Used to keep this and matmul routines "in sync".

• void addAllMatrices (SecKey &sKey, long keyID=0)

Maximalistic approach: generate matrices  $s(X^{\wedge}e)->s(X)$  for all e in Zm\*.

void addFewMatrices (SecKey &sKey, long keyID=0)

Generate matrices so every  $s(X^{\wedge} e)$  can be reLinearized in at most two steps.

void addSome1DMatrices (SecKey &sKey, long bound=HELIB KEYSWITCH THRESH, long keyID=0)

Generate some matrices of the form  $s(X^{\hat{}}\{g^{\hat{}}i\})->s(X)$ , but not all. For a generator g whose order is larger than bound, generate only enough matrices for the giant-step/baby-step procedures (2\*sqrt(ord(g))) of them).

void add1DMatrices (SecKey &sKey, long keyID=0)

Generate all matrices  $s(X^{g^{i}})-s(X)$  for generators g of Zm\* /(p) and i<ord(g). If g has different orders in Zm\* and Zm\* /(p) then generate also matrices of the form  $s(X^{g^{i}})-s(X)$ 

- void addBSGS1DMatrices (SecKey &sKey, long keyID=0)
- void addSomeFrbMatrices (SecKey &sKey, long bound=HELIB\_KEYSWITCH\_THRESH, long keyID=0)

Generate all/some Frobenius matrices of the form  $s(X^{\wedge}\{p^{\wedge}i\})->s(X)$ 

- void addFrbMatrices (SecKey &sKey, long keyID=0)
- void addBSGSFrbMatrices (SecKey &sKey, long keyID=0)
- void addMinimal1DMatrices (SecKey &sKey, long keyID=0)

These routines just add a single matrix (or two, for bad dimensions)

- void addMinimalFrbMatrices (SecKey &sKey, long keyID=0)
- void addMatrices4Network (SecKey &sKey, const PermNetwork &net, long keyID=0)
- void addTheseMatrices (SecKey &sKey, const std::set < long > &automVals, long keyID=0)

Generate specific key-switching matrices, described by the given set.

void PolyRed (NTL::ZZX &out, const NTL::ZZX &in, long q, bool abs=false)

Reduce all the coefficients of a polynomial modulo q.

- void PolyRed (NTL::ZZX &out, const NTL::ZZX &in, const NTL::ZZ &g, bool abs=false)
- void PolyRed (NTL::ZZX &F, long q, bool abs=false)
- void PolyRed (NTL::ZZX &F, const NTL::ZZ &g, bool abs=false)
- void vecRed (NTL::Vec< NTL::ZZ > &out, const NTL::Vec< NTL::ZZ > &in, long q, bool abs)
- void vecRed (NTL::Vec < NTL::ZZ > &out, const NTL::Vec < NTL::ZZ > &in, const NTL::ZZ &q, bool abs)

### Some enhanced conversion routines

- void convert (long &x1, const NTL::GF2X &x2)
- void convert (long &x1, const NTL::zz\_pX &x2)
- void convert (NTL::vec\_zz\_pE &X, const std::vector< NTL::ZZX > &A)
- void convert (NTL::mat zz pE &X, const std::vector< std::vector< NTL::ZZX >> &A)
- void convert (std::vector< NTL::ZZX > &X, const NTL::vec zz pE &A)
- void convert (std::vector < NTL::ZZX >> &X, const NTL::mat\_zz\_pE &A)
- void convert (NTL::Vec< long > &out, const NTL::ZZX &in)
- void convert (NTL::Vec< long > &out, const NTL::zz\_pX &in, bool symmetric=true)
- void convert (NTL::Vec< long > &out, const NTL::GF2X &in)
- void convert (NTL::ZZX &out, const NTL::Vec< long > &in)
- void convert (NTL::GF2X &out, const NTL::Vec< long > &in)
- double boundFreshNoise (long m, long phim, double sigma, double epsilon=9e-13)
- double boundRoundingNoise (long m, long phim, long p2r, double epsilon=9e-13)

## 6.2.1 Typedef Documentation

# 6.2.1.1 aligned\_vector

```
template<class T >
using helib::aligned_vector = typedef PGFFT::aligned_vector<T>
```

# 6.2.1.2 cmplx\_t

typedef complex<double> helib::cmplx\_t

## 6.2.1.3 CtPtrMat

typedef PtrMatrix<Ctxt> helib::CtPtrMat

# 6.2.1.4 CtPtrMat\_ptVecCt

typedef PtrMatrix\_ptVec<Ctxt> helib::CtPtrMat\_ptVecCt

# 6.2.1.5 CtPtrMat\_ptvectorCt

 ${\tt typedef\ PtrMatrix\_ptvector}{<\tt Ctxt}{\gt helib::CtPtrMat\_ptvectorCt}$ 

# 6.2.1.6 CtPtrMat\_VecCt

typedef PtrMatrix\_Vec<Ctxt> helib::CtPtrMat\_VecCt

# 6.2.1.7 CtPtrMat\_vectorCt

typedef PtrMatrix\_vector<Ctxt> helib::CtPtrMat\_vectorCt

# 6.2.1.8 CtPtrs

typedef PtrVector<Ctxt> helib::CtPtrs

# 6.2.1.9 CtPtrs\_slice

typedef PtrVector\_slice<Ctxt> helib::CtPtrs\_slice

# 6.2.1.10 CtPtrs\_VecCt

typedef PtrVector\_VecT<Ctxt> helib::CtPtrs\_VecCt

## 6.2.1.11 CtPtrs\_VecPt

typedef PtrVector\_VecPt<Ctxt> helib::CtPtrs\_VecPt

# 6.2.1.12 CtPtrs\_vectorCt

typedef PtrVector\_vectorT<Ctxt> helib::CtPtrs\_vectorCt

## 6.2.1.13 CtPtrs\_vectorPt

typedef PtrVector\_vectorPt<Ctxt> helib::CtPtrs\_vectorPt

# 6.2.1.14 cx\_double

typedef std::complex< double > helib::cx\_double

# 6.2.1.15 DCRTptr

typedef std::shared\_ptr<DoubleCRT> helib::DCRTptr

# 6.2.1.16 FlowGraph

typedef std::vector<FNeighborList> helib::FlowGraph

## 6.2.1.17 FNeighborList

typedef std::unordered\_map<long, FlowEdge> helib::FNeighborList

#### 6.2.1.18 Idbl

typedef long double helib::ldbl

# 6.2.1.19 LNeighborList

typedef std::unordered\_multimap<long, LabeledEdge> helib::LNeighborList

### 6.2.1.20 LONG

typedef long helib::LONG

## 6.2.1.21 Nodeldx

typedef std::pair<long, long> helib::NodeIdx

# 6.2.1.22 OneGeneratorTree

typedef FullBinaryTree<SubDimension> helib::OneGeneratorTree

# 6.2.1.23 Permut

```
typedef NTL::Vec<long> helib::Permut
```

A simple permutation is just a vector with  $p[i]=\pi_i$ .

#### 6.2.1.24 zzX

```
typedef NTL::Vec<long> helib::zzX
```

# 6.2.1.25 ZZXptr

```
typedef std::shared_ptr<NTL::ZZX> helib::ZZXptr
```

# 6.2.2 Enumeration Type Documentation

# 6.2.2.1 PA\_tag

```
enum helib::PA_tag
```

### Enumerator

| PA_GF2_tag  |  |
|-------------|--|
| PA_zz_p_tag |  |
| PA_cx_tag   |  |

# 6.2.3 Function Documentation

# **6.2.3.1 add()** [1/3]

## 6.2.3.2 add() [2/3]

## 6.2.3.3 add() [3/3]

```
void helib::add (
          zzX & res,
          const zzX & a,
          const zzX & b)
```

### 6.2.3.4 add1DMatrices()

Generate all matrices  $s(X^{g^{i}})-s(X)$  for generators g of Zm\*/(p) and i< ord(g). If g has different orders in Zm\* and Zm\*/(p) then generate also matrices of the form  $s(X^{g^{i}}-i)>s(X)$ 

### 6.2.3.5 addAllMatrices()

Maximalistic approach: generate matrices  $s(X^{\wedge}e)$ ->s(X) for all e in Zm\*.

# 6.2.3.6 addBSGS1DMatrices()

## 6.2.3.7 addBSGSFrbMatrices()

# 6.2.3.8 addCtxtPrimes()

# 6.2.3.9 addFewMatrices()

Generate matrices so every  $s(X^{\wedge}e)$  can be reLinearized in at most two steps.

# 6.2.3.10 addFrbMatrices()

## 6.2.3.11 addManyNumbers()

Sum an arbitrary amount of numbers in binary representation.

| Parameters         |         |
|--------------------|---------|
| sum                | result  |
|                    | of the  |
|                    | sum-    |
|                    | ma-     |
|                    | tion.   |
| numbers            | values  |
|                    | of      |
|                    | which   |
|                    | to      |
|                    | sum.    |
| sizeLimit          | number  |
|                    | of bits |
|                    | to      |
|                    | com-    |
|                    | pute    |
|                    | on,     |
|                    | taken   |
|                    | from    |
|                    | the     |
|                    | least   |
|                    | signif- |
|                    | icant   |
|                    | end.    |
| unpackSlotEncoding | vector  |
|                    | of con- |
|                    | stants  |
|                    | for un- |
|                    | pack-   |
|                    | ing, as |
|                    | used    |
|                    | in      |
|                    | boot-   |
|                    | strap-  |
|                    | ping.   |

Calculates the sum of many numbers using the 3-for-2 method.

# 6.2.3.12 addMatrices4Network()

# 6.2.3.13 addMinimal1DMatrices()

These routines just add a single matrix (or two, for bad dimensions)

#### 6.2.3.14 addMinimalFrbMatrices()

### 6.2.3.15 addOffset()

```
void helib::addOffset (
    std::list< long > & x,
    long offset,
    long n,
    bool * aux,
    UNUSED bool good = false )
```

## 6.2.3.16 addSmallPrimes()

Add small primes to get target resolution.

#### 6.2.3.17 addSome1DMatrices()

Generate some matrices of the form  $s(X^{g^i})->s(X)$ , but not all. For a generator g whose order is larger than bound, generate only enough matrices for the giant-step/baby-step procedures (2\*sqrt(ord(g)) of them).

# 6.2.3.18 addSomeFrbMatrices()

Generate all/some Frobenius matrices of the form  $s(X^{\hat{}}\{p^{\hat{}}i\})->s(X)$ 

## 6.2.3.19 addSomePrimes()

# 6.2.3.20 addTheseMatrices()

Generate specific key-switching matrices, described by the given set.

# 6.2.3.21 addTwoNumbers()

Adds two numbers in binary representation where each ciphertext of the input vector contains a bit.

Add two integers in binary representation.

| raiailleteis |         |
|--------------|---------|
| sum          | result  |
|              | of the  |
|              | addi-   |
|              | tion    |
|              | opera-  |
|              | tion.   |
| lhs          | left    |
|              | hand    |
|              | side of |
|              | the ad- |
|              | dition. |
| rhs          | right   |
|              | hand    |
|              | side of |
|              | the ad- |
|              | dition. |

| raiailieteis       |         |
|--------------------|---------|
| sizeLimit          | number  |
|                    | of bits |
|                    | to      |
|                    | com-    |
|                    | pute    |
|                    | on,     |
|                    | taken   |
|                    | from    |
|                    | the     |
|                    | least   |
|                    | signif- |
|                    | icant   |
|                    | end.    |
| unpackSlotEncoding | vector  |
|                    | of con- |
|                    | stants  |
|                    | for un- |
|                    | pack-   |
|                    | ing, as |
|                    | used    |
|                    | in      |
|                    | boot-   |
|                    | strap-  |
|                    | ping.   |

# 6.2.3.22 applyLinPoly() [1/2]

```
void helib::applyLinPoly (
          NTL::GF2E & beta,
          const NTL::vec_GF2E & C,
          const NTL::GF2E & alpha,
          long p )
```

A version for GF2: must be called with p == 2 and r == 1.

# 6.2.3.23 applyLinPoly() [2/2]

Apply a linearized polynomial with coefficient vector C.

NTL's current smallint modulus,  $zz_p::modulus()$ , is assumed to be  $p^r$ , for p prime, r >= 1 integer.

## 6.2.3.24 applyLinPoly1()

# 6.2.3.25 applyLinPolyLL() [1/4]

## 6.2.3.26 applyLinPolyLL() [2/4]

# 6.2.3.27 applyLinPolyLL() [3/4]

## 6.2.3.28 applyLinPolyLL() [4/4]

## 6.2.3.29 applyLinPolyMany()

## 6.2.3.30 applyPerm()

#### 6.2.3.31 applyPermsToVec() [1/2]

```
template<typename T >
void helib::applyPermsToVec (
    NTL::Vec< T > & out,
    const NTL::Vec< T > & in,
    const Permut & p2,
    const Permut & p1 )
```

Apply two permutations to a std::vector out[i]=in[p2[p1[i]]] (NOT in-place)

## 6.2.3.32 applyPermsToVec() [2/2]

## 6.2.3.33 applyPermsToVec < long >() [1/2]

```
template void helib::applyPermsToVec< long > (
    NTL::Vec< long > & out,
    const NTL::Vec< long > & in,
    const Permut & p2,
    const Permut & p1 )
```

### 6.2.3.34 applyPermsToVec < long >() [2/2]

```
template void helib::applyPermsToVec< long > (
    std::vector< long > & out,
    const std::vector< long > & in,
    const Permut & p2,
    const Permut & p1 )
```

## 6.2.3.35 applyPermToVec() [1/2]

Apply a permutation to a std::vector, out[i]=in[p1[i]] (NOT in-place)

## 6.2.3.36 applyPermToVec() [2/2]

# **6.2.3.37** applyPermToVec< long >() [1/2]

## 6.2.3.38 applyPermToVec < long >() [2/2]

```
template void helib::applyPermToVec< long > ( std::vector< long > & out, const std::vector< long > & in, const Permut & p1)
```

## 6.2.3.39 applyPermToVec< NTL::ZZX >()

```
template void helib::applyPermToVec< NTL::ZZX > ( std::vector< NTL::ZZX > & out, const std::vector< NTL::ZZX > & in, const Permut & p1)
```

## 6.2.3.40 areTimersOn()

```
bool helib::areTimersOn ( ) [inline]
```

### 6.2.3.41 argmax() [1/2]

```
long helib::argmax (  {\tt std::vector} < {\tt long} > \& \ v, \\  {\tt bool(*)(long, long)} \ {\tt moreThan} \ ) \ \ [inline]
```

A variant with a specialized comparison function (\*moreThan)(a,b) returns the comparison a>b.

## 6.2.3.42 argmax() [2/2]

```
template<typename T > long helib::argmax (  {\tt std::vector} < {\tt T} > {\tt \&} \ v \ )
```

### 6.2.3.43 argmin()

```
template<typename T > long helib::argmin (  std::vector < T > \& \ v \ )
```

## 6.2.3.44 argminmax()

```
template<typename T , bool maxFlag> long helib::argminmax (  {\tt std::vector} < {\tt T} > {\tt \&} \ v \ )
```

Find the index of the (first) largest/smallest element.

These procedures are roughly just simpler variants of std::max\_element and std::min\_element. argmin/argmax are implemented as a template, so the code must be placed in the header file for the compiler to find it. The class T must have an implementation of operator> and operator< for this template to work.

# **Template Parameters**

```
maxFlag A boolean value: true - argmax, false - argmin
```

## 6.2.3.45 assertEq()

Function throwing an exception of type ExceptionTy if the two arguments are not equal.

# **Template Parameters**

| ExceptionTy | type of the exception thrown.        |
|-------------|--------------------------------------|
| T           | type of the elements to be compared. |

#### **Parameters**

| а       | the first element to be compared.  |
|---------|--|
| b       | the sec-ond ele-ment to be compared.                                     |
| message | the mes- sage of the excep- tion raised if the two values are not equal. |

# **Exceptions**

Note

ExceptionTy first and T defaulted to void so that one can specify only ExceptionTy, letting T be inferred from the argument passed.

### 6.2.3.46 assertFalse()

Function throwing an exception of type ExceptionTy if the condition is true.

## **Template Parameters**

| ExceptionTy | type of the exception thrown.                         |
|-------------|---|
| T           | type of the condition being checked (must be a bool). |

### **Parameters**

| value   | the      |
|---------|----------|
|         | con-     |
|         | dition   |
|         | being    |
|         | checked. |
| message | the      |
|         | mes-     |
|         | sage     |
|         | of the   |
|         | excep-   |
|         | tion     |
|         | raised   |
|         | if the   |
|         | condi-   |
|         | tion is  |
|         | true.    |

# **Exceptions**

| ExceptionTy | exception if condition is true. |
|-------------|---------------------------------|
|-------------|---------------------------------|

## Note

ExceptionTy first and T defaulted to void so that one can specify only ExceptionTy, letting T be inferred from the argument passed.

# 6.2.3.47 assertInRange()

Function throwing an exception of type ExceptionTy if the element is in the range [min,max) or [min, max]

# **Template Parameters**

| ExceptionTy | type of the exception thrown.           |
|-------------|---|
| T           | type of the element (and of the range). |

| ne el-  |
|---------|
| ment    |
| be      |
| ested.  |
| ne left |
| de      |
| f the   |
| ange    |
| al-     |
| ays     |
| ıclu-   |
| ve).    |
| ne      |
| ght     |
| de      |
| f the   |
| ange    |
| de-     |
| ult     |
| xclu-   |
| ve).    |
| ne      |
| ies-    |
| age     |
| f the   |
| хсер-   |
| on      |
| aised   |
| the     |
| le-     |
| nent    |
| not     |
| the     |
|         |
|         |

| right_inclusive | flag    |
|-----------------|---------|
|                 | spec-   |
|                 | ifying  |
|                 | if the  |
|                 | right   |
|                 | side is |
|                 | inclu-  |
|                 | sive    |
|                 | (de-    |
|                 | fault   |
|                 | false). |
|                 | 1 7,-   |

## **Exceptions**

|  | ExceptionTy | exception if elem is not in the range | l |
|--|-------------|---------------------------------------|---|
|--|-------------|---------------------------------------|---|

# Note

ExceptionTy first and T defaulted to void so that one can specify only ExceptionTy, letting T be inferred from the argument passed.

# 6.2.3.48 assertNeq()

Function throwing an exception of type ExceptionTy if the two arguments are equal.

# **Template Parameters**

| ExceptionTy | type of the exception thrown.        |
|-------------|--------------------------------------|
| T           | type of the elements to be compared. |

| а | the       |
|---|-----------|
|   | first el- |
|   | ement     |
|   | to be     |
|   | com-      |
|   | pared.    |

| b       | the    |
|---------|--------|
|         | sec-   |
|         | ond    |
|         | ele-   |
|         | ment   |
|         | to be  |
|         | com-   |
|         | pared. |
| message | the    |
|         | mes-   |
|         | sage   |
|         | of the |
|         | excep- |
|         | tion   |
|         | raised |
|         | if the |
|         | two    |
|         | values |
|         | are    |
|         | equal. |

# **Exceptions**

| ceptionTy exception if the tw | o values are equal. |
|-------------------------------|---------------------|
|-------------------------------|---------------------|

# Note

ExceptionTy first and T defaulted to void so that one can specify only ExceptionTy, letting T be inferred from the argument passed.

# 6.2.3.49 assertNotNull()

Function throwing an exception of type ExceptionTy if the argument is nullptr.

# **Template Parameters**

| ExceptionTy | type of the exception thrown. |
|-------------|-------------------------------|
| T           | type of the element.          |

| р       | the element to be tested.  |
|---------|--|
| message | the mes- sage of the excep- tion raised if the ele- ment is nullptr. |

#### **Exceptions**

| ExceptionTy | exception if p is nullptr. |
|-------------|----------------------------|
|-------------|----------------------------|

#### Note

ExceptionTy first and T defaulted to void so that one can specify only ExceptionTy, letting T be inferred from the argument passed.

# 6.2.3.50 assertTrue()

Function throwing an exception of type ExceptionTy if the condition is false.

## **Template Parameters**

| ExceptionTy | type of the exception thrown.                         |
|-------------|---|
| Т           | type of the condition being checked (must be a bool). |

| value | the      |
|-------|----------|
|       | con-     |
|       | dition   |
|       | being    |
|       | checked. |

| message | the     |
|---------|---------|
|         | mes-    |
|         | sage    |
|         | of the  |
|         | excep-  |
|         | tion    |
|         | raised  |
|         | if the  |
|         | condi-  |
|         | tion is |
|         | false.  |

#### **Exceptions**

ExceptionTy | exception if condition is false.

#### Note

ExceptionTy first and T defaulted to void so that one can specify only ExceptionTy, letting T be inferred from the argument passed.

# 6.2.3.51 atoVec()

# 6.2.3.52 atovector()

# 6.2.3.53 balanced\_MulMod()

Multiply the polynomial f by the integer a modulo q output coefficients are balanced (appropriately randomized for even q)

## 6.2.3.54 balanced\_zzX() [1/2]

# 6.2.3.55 balanced\_zzX() [2/2]

## 6.2.3.56 balRem()

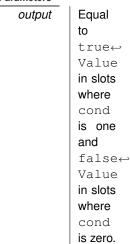
```
long helib::balRem ( \label{long a, long q } \log \ q \ ) \quad \mbox{[inline]}
```

Return balanced remainder. Assumes a in [0, q) and returns balanced remainder in (-q/2, q/2]

## 6.2.3.57 binaryCond()

Implementation of output = cond \* trueValue + (1 - cond) \* falseValue.

Implementation of output = cond ? trueValue : falseValue.



| i didilicicio |          |
|---------------|----------|
| cond          | The      |
|               | condi-   |
|               | tion,    |
|               | namely   |
|               | a        |
|               | Ctxt     |
|               | con-     |
|               | taining  |
|               | ele-     |
|               | ments    |
|               | of       |
|               | {0,1} in |
|               | each     |
|               | slot.    |
| trueValue     | Value    |
|               | of       |
|               | output   |
|               | wher-    |
|               | ever     |
|               | cond     |
|               | is one.  |
| falseValue    | Value    |
|               | of       |
|               | output   |
|               | wher-    |
|               | ever     |
|               | cond     |
|               | is zero. |

## Note

trueValue, falseValue and output must have the same size.

# 6.2.3.58 binaryMask()

Zeroes the slots of  ${\tt binaryNums}$  where the corresponding slot of  ${\tt mask}$  is 0.

Apply mask across the vector of bits slot-wise.

| binaryNums | Input     |
|------------|-----------|
|            | bits on   |
|            | which     |
|            | to        |
|            | mask      |
|            | (this is  |
|            | done      |
|            | in        |
|            | place).   |
| mask       | Encrypted |
|            | mask      |
|            | indi-     |
|            | cating    |
|            | de-       |
|            | sired     |
|            | slots.    |

# 6.2.3.59 bitSetToLong()

Considers bits as a vector of bits and returns the value it represents when interpreted as a n-bit 2's complement number, where n is given by bitSize.

| bits    | The     |
|---------|---------|
|         | value   |
|         | con-    |
|         | taining |
|         | the     |
|         | bits    |
|         | to be   |
|         | rein-   |
|         | ter-    |
|         | preted. |
| bitSize | The     |
|         | num-    |
|         | ber of  |
|         | bits to |
|         | use,    |
|         | taken   |
|         | from    |
|         | the     |
|         | least   |
|         | signif- |
|         | icant   |
|         | end of  |
|         | bits.   |

#### Returns

The value of the reinterpreted number as a long.

# 6.2.3.60 bitwiseAnd() [1/2]

Compute a bitwise AND between input and a std::vector<long>.

Compute a bitwise AND between input and mask.

## **Parameters**

|        | _       |
|--------|---------|
| output | Equal   |
|        | to the  |
|        | output  |
|        | of the  |
|        | AND     |
|        | opera-  |
|        | tion.   |
| input  | Number  |
|        | to A←   |
|        | ND.     |
| mask   | Number  |
|        | to A←   |
|        | ND      |
|        | with    |
|        | input.  |
|        | This    |
|        | should  |
|        | be a    |
|        | vector  |
|        | of ele- |
|        | ments   |
|        | of      |
|        | {0,1}.  |

## Note

The size of output and input must be the same.

# 6.2.3.61 bitwiseAnd() [2/2]

```
const CtPtrs & lhs,
const CtPtrs & rhs )
```

Compute a bitwise AND between  ${\tt lhs}$  and  ${\tt rhs}$ .

| output | Result<br>of bit-<br>wise<br>lhs<br>AND |
|--------|---|
|        | rhs.                                    |
| lhs    | Left                                    |
|        | operand                                 |
|        | to the                                  |
|        | AND                                     |
|        | opera-                                  |
|        | tion.                                   |
| rhs    | Right                                   |
|        | operand                                 |
|        | to the                                  |
|        | AND                                     |
|        | opera-                                  |
|        | tion.                                   |

## Note

output, 1hs and rhs must all have the same size.

# 6.2.3.62 bitwiseNot()

Compute a bitwise NOT of input.

## **Parameters**

| output | Result of bit-flipping input.                   |
|--------|---|
| input  | Binary<br>num-<br>ber to<br>be bit-<br>flipped. |

# Note

The size of output and input must be the same.

# 6.2.3.63 bitwiseOr()

Compute a bitwise OR between lhs and rhs.

#### **Parameters**

| output | Result  |
|--------|---------|
|        | of bit- |
|        | wise    |
|        | lhs     |
|        | OR      |
|        | rhs.    |
| lhs    | Left    |
|        | operand |
|        | to the  |
|        | OR      |
|        | opera-  |
|        | tion.   |
| rhs    | Right   |
|        | operand |
|        | to the  |
|        | OR      |
|        | opera-  |
|        | tion.   |

## Note

output, lhs and rhs must all have the same size.

# 6.2.3.64 bitwiseRotate()

Rotate input by rotamt.

Rotate binary numbers by rotamt.

| output                   | Rotated  |
|--------------------------|----------|
| ,                        | result.  |
| input                    | The      |
|                          | num-     |
|                          | ber      |
|                          | to be    |
|                          | bitwise- |
| Generated by Drodygierd. |          |

| rotamt | The       |
|--------|-----------|
|        | amount    |
|        | by        |
|        | which     |
|        | to ro-    |
|        | tate      |
|        | input.    |
|        | May       |
|        | be        |
|        | nega-     |
|        | tive for  |
|        | opposite- |
|        | direction |
|        | rota-     |
|        | tions.    |

#### Note

For positive rotamt arguments, this rotates towards the most-significant end (i.e. the same direction as leftBitwiseShift).

The size of output and input must be the same.

# 6.2.3.65 bitwiseXOR()

Compute a bitwise XOR between lhs and rhs.

| output | Result  |
|--------|---------|
|        | of bit- |
|        | wise    |
|        | lhs     |
|        | XOR     |
|        | rhs.    |
| lhs    | Left    |
|        | operand |
|        | to the  |
|        | XOR     |
|        | opera-  |
|        | tion.   |
| rhs    | Right   |
|        | operand |
|        | to the  |
|        | XOR     |
|        | opera-  |
|        | tion.   |

Note

output, lhs and rhs must all have the same size.

### 6.2.3.66 BluesteinFFT() [1/2]

```
void helib::BluesteinFFT (
        NTL::zz_pX & x,
        long n,
        const NTL::zz_p & root,
        const NTL::zz_pX & powers,
        const NTL::Vec< NTL::mulmod_precon_t > & powers_aux,
        const NTL::fftRep & Rb )
```

apply bluestein

## 6.2.3.67 BluesteinFFT() [2/2]

```
void helib::BluesteinFFT (
        NTL::zz_pX & x,
        long n,
        UNUSED const NTL::zz_p & root,
        const NTL::zz_pX & powers,
        const NTL::Vec< NTL::mulmod_precon_t > & powers_aux,
        const NTL::fftRep & Rb )
```

## 6.2.3.68 BluesteinInit()

initialize bluestein

### 6.2.3.69 boundFreshNoise()

Helper functions, return a bound B such that for random noise terms we have  $Pr[|canonicalEmbed(noise)|_{\infty}] > B] < epsilon.$  (The default is epsilon =  $2^{-40}$ .)

### 6.2.3.70 boundRoundingNoise() [1/2]

```
double helib::boundRoundingNoise ( long \ m, \\ long \ phim, \\ long \ p2r, \\ double \ epsilon = 9e-13 )
```

### 6.2.3.71 boundRoundingNoise() [2/2]

## 6.2.3.72 breakPermByDim()

Takes a permutation pi over m-dimensional cube  $C=Z_{n1} x...x Z_{nm}$  and expresses pi as a product pi = rho\_ $\leftarrow$  {2m-1} o ... o rho\_2 o rho\_1 where each rho\_i is a column permutation along one dimension. Specifically for i<m, the permutations rho\_i and rho\_{2(m-1)-i} permute the i'th dimension.

### 6.2.3.73 breakPermTo3()

## 6.2.3.74 build\_ConstMultiplier() [1/2]

### 6.2.3.75 build\_ConstMultiplier() [2/2]

## 6.2.3.76 buildBenesCostTable()

```
void helib::buildBenesCostTable ( \log n, \log k, \operatorname{bool} good, \operatorname{NTL}::\operatorname{Vec}<\operatorname{NTL}::\operatorname{Vec}<\operatorname{long}>> \& tab )
```

### 6.2.3.77 BuildContext()

```
\label{eq:ntl::zz_pContext} $$\operatorname{NTL}::zz_pContext \ helib::BuildContext \ ($$long $p$, $$long $maxroot \ )$$
```

## 6.2.3.78 buildContextFromAscii()

```
\begin{tabular}{ll} \tt std::unique\_ptr< Context > helib::buildContextFromAscii ( & std::istream & str ) \end{tabular}
```

### 6.2.3.79 buildContextFromBinary()

```
\begin{tabular}{ll} \tt std::unique\_ptr< Context > helib::buildContextFromBinary ( & std::istream & str ) \end{tabular}
```

## 6.2.3.80 buildEncryptedArray()

A "factory" for building EncryptedArrays.

### 6.2.3.81 buildGeneralAutomorphPrecon()

### 6.2.3.82 buildLinPolyCoeffs() [1/2]

A version for GF2: must be called with p == 2 and r == 1.

### 6.2.3.83 buildLinPolyCoeffs() [2/2]

```
void helib::buildLinPolyCoeffs (
          NTL::vec_zz_pE & C,
          const NTL::vec_zz_pE & L,
          long p,
          long r )
```

Combination of buildLinPolyMatrix and ppsolve.

Obtain the linearized polynomial coefficients from a vector L representing the action of a linear map on the standard basis for zz\_pE over zz\_p.

NTL's current smallint modulus, zz p::modulus(), is assumed to be  $p^r$ , for p prime, r >= 1 integer.

### 6.2.3.84 buildLinPolyMatrix() [1/2]

## 6.2.3.85 buildLinPolyMatrix() [2/2]

```
void helib::buildLinPolyMatrix ( \label{eq:ntl:mat_zz_pe} \mbox{NTL}::\mbox{mat_zz_pE \& $M$,} \\ \mbox{long $p$ )}
```

### 6.2.3.86 buildLookupTable()

```
void helib::buildLookupTable (
    std::vector< zzX > & T,
    std::function< double(double)> f,
    long nbits_in,
    long scale_in,
    long sign_in,
    long nbits_out,
    long scale_out,
    long sign_out,
    const EncryptedArray & ea )
```

Built a table-lookup for a function in fixed-point representation.

@function buildLookupTable FIXED-POINT CONVENTIONS: Fixed-point numbers are specified by a triple (nbits,scale,signed). Such a number is represented as an integer x with nbits bits. If signed == 1, then x is treated as a signed integer in 2's compliment; otherwise it is as an unsigned integer. The value represented by x is  $x*2^{s}$  (scale).

The buildLookupTable function builds a lookup table T, which can be used in conjunction with the tableLookup function above. The size of T will be  $2^{n}$  hbits\_in}. For every signed integer x with bit-size 'nbits\_in', we will have  $T[x] = f(x * 2^{s} - x) * 2^{-s} = f(x * 2^{s} -$ 

SATURATED ARITHMETIC: Applications of f that return a result that is too large to represent in the output format will be converted to the maximum representable value. Similarly, Applications of f that return a result that is too small will be converted to the minimal representable value. (This applies also to applications of f that return infinites, NaNs will just be mapped to zero.) For this to work correctly, you should be working with standard IEEE arithmetic...which will be the case on almost all platforms.

#### **EXAMPLE**:

buildLookupTable(T, [](double x){ return 1/x;}, nbits\_in, scale\_in, nbits\_out, scale\_out, sign\_out, ea) will build a lookup table for inversion.

### 6.2.3.87 buildModChain()

### 6.2.3.88 buildPAlgebraMod()

Builds a table, of type PA\_GF2 if p == 2 and r == 1, and PA\_zz\_p otherwise.

### 6.2.3.89 buildRandomBlockMatrix()

## 6.2.3.90 buildRandomFullBlockMatrix()

### 6.2.3.91 buildRandomFullMatrix()

## 6.2.3.92 buildRandomMatrix()

## 6.2.3.93 buildRandomMultiBlockMatrix()

## 6.2.3.94 buildRandomMultiMatrix()

### 6.2.3.95 buildUnpackSlotEncoding()

## 6.2.3.96 calcPolyNormBnd()

```
double helib::calcPolyNormBnd ( long m)
```

## 6.2.3.97 card()

Functional cardinality.

### 6.2.3.98 CheckCtxt()

print to cerr some info about ciphertext

### 6.2.3.99 checkNoise()

### 6.2.3.100 CKKS\_canonicalEmbedding() [1/3]

```
void helib::CKKS_canonicalEmbedding (
    std::vector< cx_double > & v,
    const NTL::ZZX & f,
    const PAlgebra & palg )
```

### 6.2.3.101 CKKS\_canonicalEmbedding() [2/3]

```
void helib::CKKS_canonicalEmbedding (  \verb|std::vector| < cx_double > \& v, \\ const std::vector| < double > \& f, \\ const PAlgebra & palg )
```

### 6.2.3.102 CKKS\_canonicalEmbedding() [3/3]

```
void helib::CKKS_canonicalEmbedding (
    std::vector< cx_double > & v,
    const zzX & f,
    const PAlgebra & palg )
```

Computes canonical embedding. Requires p==-1 and m== $2^k$  where  $k \ge 2$  and f.length() < m/2. Sets v[m/4-1-i] = DFT[palg.ith\_rep(i)] for i in range(m/4), where DFT[j] = f(W^j) for j in range(m), and W = exp(-2\*pi\*I/m).

### 6.2.3.103 CKKS embedInSlots()

```
void helib::CKKS_embedInSlots (
    zzX & f,
    const std::vector< cx_double > & v,
    const PAlgebra & palg,
    double scaling )
```

Requires p==-1 and m== $2^k$  where k >=2. Computes the inverse of canonical embedding, scaled by scaling and then rounded to nearest integer.

### 6.2.3.104 cleanupDebugGlobals()

```
void helib::cleanupDebugGlobals ( ) [inline]
```

Cleanup function for clearing the global debug variables.

## 6.2.3.105 clear()

```
void helib::clear (
          zzX & a ) [inline]
```

# 6.2.3.106 closeToOne()

```
bool helib::closeToOne (  {\tt const\ NTL::xdouble\ \&\ x,}   {\tt long\ p\ )} \quad [{\tt inline}]
```

## 6.2.3.107 coeffsL2Norm() [1/3]

### 6.2.3.108 coeffsL2Norm() [2/3]

## 6.2.3.109 coeffsL2Norm() [3/3]

```
double helib::coeffsL2Norm ( {\tt const~zzX~\&~f~)} \quad [{\tt inline}]
```

## 6.2.3.110 coeffsL2NormSquared() [1/3]

### 6.2.3.111 coeffsL2NormSquared() [2/3]

## 6.2.3.112 coeffsL2NormSquared() [3/3]

```
double helib::coeffsL2NormSquared ( {\tt const\ zzX\ \&\ f\ )}
```

The L2-norm of an element (in coefficient representation)

### 6.2.3.113 comparePAlgebra() [1/2]

returns true if the palg parameters match the rest, false otherwise

## 6.2.3.114 comparePAlgebra() [2/2]

## 6.2.3.115 compareTwoNumbers() [1/2]

Compares two integers in binary a, b. Returns max(a, b), min(a, b) and indicator bits mu=(a>b) and ni=(a<b)

#### **Parameters**

| max | Maximum                   |
|-----|---------------------------|
|     | of a                      |
|     | and b.                    |
| min | Minimum                   |
|     | of a                      |
|     | and b.                    |
| mu  | Indicator                 |
|     | bits                      |
|     | mu=(a>b).                 |
| ni  | Indicator                 |
|     | bits                      |
|     | ni=(a <b).< td=""></b).<> |

| а                  | First     |
|--------------------|-----------|
|                    | num-      |
|                    | ber to    |
|                    | com-      |
|                    | pare.     |
| b                  | Second    |
|                    | num-      |
|                    | ber to    |
|                    | com-      |
|                    | pare.     |
| twosComplement     | When      |
|                    | set to    |
|                    | true,     |
|                    | the       |
|                    | inputs    |
|                    | are       |
|                    | signed    |
|                    | inte-     |
|                    | gers      |
|                    | in 2's    |
|                    | com-      |
|                    | ple-      |
|                    | ment.     |
|                    | If set to |
|                    | false     |
|                    | (de-      |
|                    | fault),   |
|                    | un-       |
|                    | signed    |
|                    | com-      |
|                    | pari-     |
|                    | son is    |
|                    | per-      |
|                    | formed.   |
| unpackSlotEncoding | Vector    |
|                    | of con-   |
|                    | stants    |
|                    | for un-   |
|                    | pack-     |
|                    | ing, as   |
|                    | used      |
|                    | in        |
|                    | boot-     |
|                    | strap-    |
|                    | ping.     |

### Note

If a=b then mu=ni=0

# 6.2.3.116 compareTwoNumbers() [2/2]

```
void helib::compareTwoNumbers (
    Ctxt & mu,
    Ctxt & ni,
    const CtPtrs & a,
    const CtPtrs & b,
    bool twosComplement = false,
    std::vector< zzX > * unpackSlotEncoding = nullptr )
```

Compares two integers in binary a, b. Returns only indicator bits mu=(a>b) and ni=(a<b).

## Parameters

| Parameters     |                 |
|----------------|-----------------|
| mu             | Indicator bits  |
|                | mu=(a>b).       |
| ni             | Indicator       |
|                | bits            |
|                | ni=(a < b).     |
| а              | First           |
|                | num-            |
|                | ber to          |
|                | com-            |
|                | pare.           |
| b              | Second          |
|                | num-            |
|                | ber to          |
|                | com-            |
|                | pare.           |
| twosComplement | When            |
|                | set to          |
|                | true,           |
|                | the             |
|                | inputs          |
|                | are             |
|                | signed          |
|                | inte-           |
|                | gers            |
|                | in 2's          |
|                | com-            |
|                | ple-            |
|                | ment.           |
|                | If set to       |
|                | false           |
|                | (de-            |
|                | fault),         |
|                | un-<br>signed   |
|                | com-            |
|                | 1               |
|                | pari-<br>son is |
|                | per-            |
|                | formed.         |
|                | iornieu.        |

| unpackSlotEncoding | Vector  |
|--------------------|---------|
|                    | of con- |
|                    | stants  |
|                    | for un- |
|                    | pack-   |
|                    | ing, as |
|                    | used    |
|                    | in      |
|                    | boot-   |
|                    | strap-  |
|                    | ping.   |

### Note

If a=b then mu=ni=0

### 6.2.3.117 compareTwoNumbersImplementation()

### 6.2.3.118 computeAllProducts()

For an n-size array, compute the  $2^n$  products products  $[j] = \frac{i \cdot j_{i=1}}{array[i]} \times \frac{i \cdot j_{i=1}}{array[i]}$ 

## 6.2.3.119 computeDivVec()

### 6.2.3.120 computeIntervalForMul()

### 6.2.3.121 computeIntervalForSqr()

## 6.2.3.122 computeInvVec()

## 6.2.3.123 ComputeOneGenMapping()

to a single generator tree

### 6.2.3.124 computeProd() [1/2]

returns \prod\_d vec[d]

## 6.2.3.125 computeProd() [2/2]

```
long helib::computeProd ( {\tt const \ std::vector} < {\tt long} \ > \& \ \textit{vec} \ )
```

# 6.2.3.126 concatBinaryNums()

Concatenates two binary numbers into a single CtPtrs object. E.g. If a=10111, b=00101 then output = 1011100101.

Concatenate two binary numbers into a single CtPtrs object.

### **Parameters**

| output | Equal       |
|--------|-------------|
|        | to the      |
|        | con-        |
|        | cate-       |
|        | nation      |
|        | <b>of</b> a |
|        | and b.      |
| а      | First       |
|        | num-        |
|        | ber to      |
|        | сору        |
|        | into        |
|        | output.     |
| b      | Second      |
|        | num-        |
|        | ber to      |
|        | con-        |
|        | cate-       |
|        | nate to     |
|        | a.          |

### Note

The size of output must be of size a.size() + b.size().

## 6.2.3.127 conv() [1/2]

## 6.2.3.128 conv() [2/2]

```
void helib::conv (
         NTL::ZZX & p,
         const DoubleCRT & d ) [inline]
```

# 6.2.3.129 convert() [1/18]

## 6.2.3.130 convert() [2/18]

```
void helib::convert ( \label{eq:long & x1, const NTL::GF2X & x2 ) [inline]}
```

# 6.2.3.131 convert() [3/18]

# 6.2.3.132 convert() [4/18]

```
void helib::convert (
          NTL::GF2X & out,
          const NTL::Vec< long > & in )
```

## 6.2.3.133 convert() [5/18]

### 6.2.3.134 convert() [6/18]

```
void helib::convert (
          NTL::Vec< long > & out,
          const NTL::GF2X & in )
```

## 6.2.3.135 convert() [7/18]

```
void helib::convert (
          NTL::Vec< long > & out,
          const NTL::zz_pX & in,
          bool symmetric = true )
```

## 6.2.3.136 convert() [8/18]

```
void helib::convert (
     NTL::Vec< long > & out,
     const NTL::ZZX & in )
```

# 6.2.3.137 convert() [9/18]

### 6.2.3.138 convert() [10/18]

# 6.2.3.139 convert() [11/18]

### 6.2.3.140 convert() [12/18]

## 6.2.3.141 convert() [13/18]

```
void helib::convert (
          std::vector< NTL::ZZX > & X,
          const NTL::vec_zz_pE & A)
```

### 6.2.3.142 convert() [14/18]

```
void helib::convert (
          std::vector< std::vector< NTL::ZZX >> & X,
          const NTL::mat_zz_pE & A )
```

## 6.2.3.143 convert() [15/18]

```
template<typename T > void helib::convert ( std::vector < T > \& v1, \\ const std::vector < T > \& v2)
```

Trivial type conversion, useful for generic code.

### 6.2.3.144 convert() [16/18]

```
template<typename T1 , typename T2 > void helib::convert ( std::vector < T1 > \& v1, \\ const NTL::Vec < T2 > \& v2 )
```

# 6.2.3.145 convert() [17/18]

```
template<typename T1 , typename T2 > void helib::convert (  std::vector < T1 > \& v1, \\ const std::vector < T2 > \& v2 )
```

generic vector conversion routines

### 6.2.3.146 convert() [18/18]

A generic template that resolves to NTL's conv routine.

### 6.2.3.147 convertDataToSlotVector()

Converts std::vector<From> to std::vector<Scheme::SlotType>.

#### **Template Parameters**

| From   | Type of the element in the input vector.               |
|--------|--|
| Scheme | The encryption scheme to be used, must be BGV or CKKS. |

## **Parameters**

| data | Vec | ctor |
|------|-----|------|
|      | to  | be   |
|      | cor | 1-   |
|      | ver | ted. |

# Returns

Vector of converted values of type Scheme::SlotType.

### Note

Only exists for BGV and CKKS.

### 6.2.3.148 CRTcoeff()

```
long helib::CRTcoeff ( long \ p, \\ long \ q, \\ bool \ symmetric = false ) \ [inline]
```

Returns a CRT coefficient: x = (0 mod p, 1 mod q). If symmetric is set then x \in [-pq/2, pq/2), else x \in [0,pq)

### 6.2.3.149 ctxtPrimeSize()

# 6.2.3.150 Cyclotomic()

```
NTL::ZZX helib::Cyclotomic ( long N)
```

Compute cyclotomic polynomial.

## 6.2.3.151 decode() [1/2]

### 6.2.3.152 decode() [2/2]

# 6.2.3.153 decryptAndCompare()

# 6.2.3.154 decryptAndPrint()

```
void helib::decryptAndPrint (
    std::ostream & s,
    const Ctxt & ctxt,
    const SecKey & sk,
    const EncryptedArray & ea,
    long flags = 0 )
```

# 6.2.3.155 decryptBinaryNums()

```
void helib::decryptBinaryNums (
    std::vector< long > & pNums,
    const CtPtrs & eNums,
    const SecKey & sKey,
    const EncryptedArray & ea,
    bool twosComplement = false,
    bool allSlots = true )
```

Decrypt the binary numbers that are encrypted in eNums.

## **Parameters**

| Parameters |           |
|------------|-----------|
| pNums      | vector    |
|            | to de-    |
|            | crypt     |
|            | the       |
|            | binary    |
|            | num-      |
|            | bers      |
|            | into.     |
| eNums      | encrypted |
|            | binary    |
|            | num-      |
|            | bers of   |
|            | which     |
|            | to        |
|            | be de-    |
|            | crypted.  |
| sKey       | secret    |
|            | key       |
|            | used      |
|            | for de-   |
|            | cryp-     |
|            | tion.     |
| ea         | encrypted |
|            | array     |
|            | that      |
|            | holds     |
|            | neces-    |
|            | sary      |
|            | infor-    |
|            | mation    |
|            | for de-   |
|            | cryp-     |
|            | tion.     |

| twosComplement | when              |
|----------------|-------------------|
| twoocomplement | set to            |
|                | true,             |
|                | the               |
|                | num-              |
|                | ber               |
|                | to de-            |
|                | crypt             |
|                | is a              |
|                | signed            |
|                | -                 |
|                | integer<br>in 2's |
|                |                   |
|                | com-              |
|                | ple-              |
| "01 :          | ment.             |
| allSlots       | when              |
|                | set to            |
|                | false,            |
|                | return            |
|                | only              |
|                | the               |
|                | sub-              |
|                | cube              |
|                | with in-          |
|                | dex=0             |
|                | in the            |
|                | last              |
|                | dimen-            |
|                | sion              |
|                | within            |
|                | each              |
|                | cipher-           |
|                | text.             |

The bits are encrypted in a bit-sliced manner. Namely, encNums[0] contains the LSB of all the numbers, enc—Nums[1] the next bits from all, etc. If twosComplement==true then the number is interpreted as a signed integer in 2's-complement representation. If allSlots==false then we only return the subcube with index i=0 in the last dimension within each ciphertext. Namely, the bit for the j'th counter is found in slot of index j\*sizeOf(lastDim).

# 6.2.3.156 defaultPmiddle()

## 6.2.3.157 defaultQmiddle()

## 6.2.3.158 DestMulAdd()

## 6.2.3.159 disjoint()

Functional disjoint.

# 6.2.3.160 div() [1/2]

```
void helib::div (  \verb|std::vector< NTL::ZZX| > \& x, \\ const std::vector< NTL::ZZX| > \& a, \\ long b )
```

# 6.2.3.161 div() [2/2]

```
void helib::div (
    zzX & res,
    const zzX & a,
    long b )
```

## 6.2.3.162 divc()

```
long helib::divc (
          long a,
          long b ) [inline]
```

returns ceiling(a/b); assumes a >=0, b>0, a+b <= MAX\_LONG

### 

### 

## 

# $\textbf{6.2.3.166} \quad \textbf{DoubleCRT::Op} < \textbf{DoubleCRT::MulFun} > \textbf{()} \ \ \texttt{[1/2]}$

# $\textbf{6.2.3.167} \quad \textbf{DoubleCRT::Op}{<} \ \textbf{DoubleCRT::MulFun} > \textbf{()} \ \ \textbf{[2/2]}$

## 6.2.3.168 DoubleCRT::Op < DoubleCRT::SubFun >() [1/3]

### 

## 

### 6.2.3.171 EDF()

## 6.2.3.172 embeddingLargestCoeff() [1/4]

## 6.2.3.173 embeddingLargestCoeff() [2/4]

## 6.2.3.174 embeddingLargestCoeff() [3/4]

### 6.2.3.175 embeddingLargestCoeff() [4/4]

Computing the L-infinity norm of the canonical embedding Assumed: deg(f) < phi(m).

## 6.2.3.176 embeddingLargestCoeff\_x2()

### 6.2.3.177 empty()

```
bool helib::empty ( {\tt const\ IndexSet\ \&\ s\ )} \quad [{\tt inline}]
```

# 6.2.3.178 encode() [1/4]

### 6.2.3.179 encode() [2/4]

### 6.2.3.180 encode() [3/4]

### 6.2.3.181 encode() [4/4]

## 6.2.3.182 endBuildModChain()

## 6.2.3.183 equals() [1/3]

## 6.2.3.184 equals() [2/3]

### 6.2.3.185 equals() [3/3]

# 6.2.3.186 extendExtractDigits()

### 6.2.3.187 extractDigits() [1/2]

```
void helib::extractDigits (
          std::vector< Ctxt > & digits,
          const Ctxt & c,
          long r,
          bool shortCut ) [inline]
```

## 6.2.3.188 extractDigits() [2/2]

```
void helib::extractDigits ( std::vector < Ctxt > \& \ digits, const \ Ctxt \& \ c, long \ r = 0 \ )
```

Extract the mod-p digits of a mod-p^r ciphertext.

extractDigits returns in the slots of digits[j] the j'th-lowest digits from the integers in the slots of the input. Namely, the i'th slot of digits[j] contains the j'th digit in the p-base expansion of the integer in the i'th slot of the \*this.

If r==0 then it is set to c.effectiveR(). It is assumed that the slots of \*this contains integers mod  $p^r$ , i.e., that only the free terms are nonzero. If that assumptions does not hold then the result will not be a valid ciphertext anymore.

The "shortcut" flag is deprecated, it often leads to catastrophic failure in the noise estimate. Calling the function with shortcut=true has not effect, except printing a warning message to cerr.

The output ciphertext digits[j] contains the j'th digit in the base-p expansion of the input, and its plaintext space is modulo  $p^{r}$ . All the ciphertexts in the output are at the same level.

## 6.2.3.189 extractDigitsPacked()

# 6.2.3.190 extractDigitsThin()

### 6.2.3.191 factorize() [1/3]

Factoring by trial division, only works for  $N<2^{60}$  primes and multiplicities are recorded.

## 6.2.3.192 factorize() [2/3]

```
void helib::factorize ( \label{eq:std:vector} \texttt{std::vector} < \ \texttt{long} \ > \ \& \ \textit{factors}, \\ \ \ \texttt{long} \ \textit{N} \ )
```

Factoring by trial division, only works for N<2^{60}, only the primes are recorded, not their multiplicity.

### 6.2.3.193 factorize() [3/3]

```
void helib::factorize ( {\tt std::vector} < {\tt NTL::ZZ} \ > \& \ factors, \\ {\tt const} \ {\tt NTL::ZZ} \ \& \ N \ )
```

### 6.2.3.194 fastPower()

### 6.2.3.195 fetch\_saved\_values()

## 6.2.3.196 fifteenOrLess4Four()

Add together up to fifteen {0,1} integers, producing a 4-bit counter.

| out       | 4-bit<br>counter<br>to be<br>out- |
|-----------|-----------------------------------|
|           | putted.                           |
| in        | bits                              |
|           | to be                             |
|           | counted.                          |
| sizeLimit | number                            |
|           | of bits                           |
|           | to                                |
|           | com-                              |
|           | pute                              |
|           | on,                               |
|           | taken                             |
|           | from                              |
|           | the                               |
|           | least                             |
|           | signif-                           |
|           | icant                             |
|           | end.                              |

### Returns

number of output bits that are not identically zero (i.e. != null).

Adding fifteen input bits, getting a 4-bit counter. Some of the input pointers may be null, but output pointers must point to allocated Ctxt objects. If sizeLimit<4, only that many bits are computed (taken from the least significant end).

## 6.2.3.197 findGenerators()

```
long helib::findGenerators (
    std::vector< long > & gens,
    std::vector< long > & ords,
    long m,
    long p,
    const std::vector< long > & candidates = std::vector<long>() )
```

Returns in gens a generating set for Zm\*/

, and in ords the order of these generators. Return value is the order of p in  $\mbox{Zm}\ast.$ 

### 6.2.3.198 FindM()

```
long helib::FindM (
        long k,
        long nBits,
        long c,
        long p,
        long d,
        long s,
        long chosen_m,
        bool verbose = false )
```

Returns smallest parameter m satisfying various constraints:

| Parameters |                |
|------------|----------------|
| k          | security       |
|            | param-         |
|            | eter           |
| L          | number         |
|            | of lev-        |
|            | els            |
| С          | number         |
|            | of             |
|            | columns        |
|            | in key         |
|            | switch-        |
|            | ing            |
|            | matri-         |
|            | ces            |
| p          | characteristic |
|            | of             |
|            | plain-         |
|            | text           |
|            | space          |
| d          | embedding      |
|            | degree         |
|            | (d             |
|            | ==0 or         |
|            | d==1           |
|            | => no          |
|            | con-           |
|            | straint)       |
| s          | at             |
|            | least          |
|            | that           |
|            | many           |
|            | plain-         |
|            | text           |
|            | slots          |

| i didilictors |             |
|---------------|-------------|
| chosen_m      | preselected |
|               | value       |
|               | of m (0     |
|               | => not      |
|               | prese-      |
|               | lected)     |
|               | Fails       |
|               | with an     |
|               | error       |
|               | mes-        |
|               | sage        |
|               | if no       |
|               | suit-       |
|               | able        |
|               | m is        |
|               | found       |
|               | prints      |
|               | an          |
|               | infor-      |
|               | mative      |
|               | mes-        |
|               | sage        |
|               | if ver-     |
|               | bose        |
|               | == true     |

# 6.2.3.199 findMinBitCapacity() [1/3]

# 6.2.3.200 findMinBitCapacity() [2/3]

```
long helib::findMinBitCapacity ( {\tt const~CtPtrs~\&~v~)} \quad [{\tt inline}]
```

# 6.2.3.201 findMinBitCapacity() [3/3]

### 6.2.3.202 FindPrimitiveRoot() [1/2]

Find e-th root of unity modulo the current modulus.

## 6.2.3.203 FindPrimitiveRoot() [2/2]

```
void helib::FindPrimitiveRoot (  \mbox{NTL}:: \mbox{ZZ\_p \& } r, \\ \mbox{unsigned long e } )
```

### 6.2.3.204 FindPrimRootT()

# 6.2.3.205 frobeniusAutomorph() [1/2]

### 6.2.3.206 frobeniusAutomorph() [2/2]

### 6.2.3.207 FrobeniusMap()

```
\label{eq:ntl::zz_pex} $$ NTL::zz_pEX \ helib::FrobeniusMap ($$ const NTL::zz_pEXModulus & $F$ )
```

### 6.2.3.208 fsquare()

```
double helib::fsquare ( double x ) [inline]
```

Return the square of a number as a double.

## 6.2.3.209 GenBabySteps()

```
void helib::GenBabySteps (
         std::vector< std::shared_ptr< Ctxt >> & v,
         const Ctxt & ctxt,
         long dim,
         bool clean )
```

### 6.2.3.210 getG()

## 6.2.3.211 getHyperColumn() [1/3]

```
template void helib::getHyperColumn (  \mbox{NTL}::\mbox{Vec}<\mbox{long}>\mbox{\&}\ v, \\ \mbox{const}\mbox{ConstCubeSlice}<\mbox{long}>\mbox{\&}\ s, \\ \mbox{long}\ pos\ )
```

# 6.2.3.212 getHyperColumn() [2/3]

### 6.2.3.213 getHyperColumn() [3/3]

getHyperColumn reads out a (multi-dimensional) column from a slice. The parameter pos specifies the position of the column, which must be in the range  $0 \le pos \le s.getProd(1)$ . The vector v is filled with values whose coordinate in the lower dimensional subcube is equal to pos. The length of v will be set to s.getDim(0).

## 6.2.3.214 getPhimXMod()

### 6.2.3.215 getTimerByName()

### 6.2.3.216 GetTimerClock()

```
unsigned long helib::GetTimerClock ( )
```

### 6.2.3.217 incrementalProduct()

```
void helib::incrementalProduct ( {\tt std::vector} < {\tt Ctxt} \ > \ \& \ v \ )
```

For i=n-1...0, set v[i]=prod\_{i<=i} v[j] This implementation uses depth log n and (nlog n)/2 products

### 6.2.3.218 incrementalZeroTest()

### 6.2.3.219 innerProduct() [1/9]

## 6.2.3.220 innerProduct() [2/9]

## 6.2.3.221 innerProduct() [3/9]

## 6.2.3.222 innerProduct() [4/9]

# 6.2.3.223 innerProduct() [5/9]

### 6.2.3.224 innerProduct() [6/9]

#### 6.2.3.225 innerProduct() [7/9]

Compute the inner product of a vectors of ciphertexts and a constant vector.

#### 6.2.3.226 innerProduct() [8/9]

#### 6.2.3.227 innerProduct() [9/9]

Free function that computes the inner product of two vectors of Ptxt.

#### **Parameters**

| The     |
|---------|
| The     |
| output  |
| Ptxt    |
| that    |
| will    |
| hold    |
| the     |
| result. |
| The     |
| first   |
| input   |
| vec-    |
| tor of  |
| plain-  |
| texts.  |
| The     |
| sec-    |
| ond     |
| input   |
| vec-    |
| tor of  |
| plain-  |
| texts.  |
|         |

Note

If the two vector sizes differ, the shorter vector will be padded with zeroes.

# 6.2.3.228 interpolateMod()

Interpolate polynomial such that  $poly(x[i] \mod p) = y[i] \pmod{p^e}$  It is assumed that the points x[i] are all distinct modulo p.

### 6.2.3.229 intVecCRT() [1/4]

```
template bool helib::intVecCRT (
          NTL::vec_ZZ & ,
          const NTL::ZZ & ,
          const NTL::Vec< NTL::zz_p > & ,
          long )
```

# 6.2.3.230 intVecCRT() [2/4]

#### 6.2.3.231 intVecCRT() [3/4]

```
template bool helib::intVecCRT (
          NTL::vec_ZZ & ,
          const NTL::ZZ & ,
          const NTL::vec_ZZ & ,
          long )
```

#### 6.2.3.232 intVecCRT() [4/4]

Incremental integer CRT for vectors.

Expects co-primes p,q with q odd, and such that all the entries in v1 are in [-p/2,p/2). Returns in v1 the CRT of vp mod p and vq mod q, as integers in [-pq/2, pq/2). Uses the formula:

$$CRT(vp, p, vq, q) = vp + [(vq - vp) * p^{-1}]_q * p,$$

where [...]\_q means reduction to the interval [-q/2,q/2). Notice that if q is odd then this is the same as reducing to [-(q-1)/2,(q-1)/2], which means that [...]\_q \* p is in [-p(q-1)/2, p(q-1)/2], and since vp is in [-p/2,p/2) then the sum is indeed in [-pq/2,pq/2).

Return true is both vectors are of the same length, false otherwise

### 6.2.3.233 InvModpr()

#### 6.2.3.234 is2power()

```
bool helib::is2power ( long \ \textit{m} \ ) \quad [inline]
```

# 6.2.3.235 is\_in()

```
long helib::is_in ( \log x, int * X, \log sz )
```

Finds whether x is an element of the set X of size sz, Returns -1 it not and the location if true.

#### 6.2.3.236 isDryRun()

```
bool helib::isDryRun ( ) [inline]
```

### 6.2.3.237 isSetAutomorphVals()

```
bool helib::isSetAutomorphVals ( ) [inline]
```

### 6.2.3.238 isSetAutomorphVals2()

```
bool helib::isSetAutomorphVals2 ( ) [inline]
```

#### 6.2.3.239 IsZero()

# 6.2.3.240 killVec() [1/2]

# 6.2.3.241 killVec() [2/2]

```
template<typename T > void helib::killVec ( std::vector < T > \& \ vec \ )
```

NTL/std compatibility.

# 6.2.3.242 KSGiantStepSize()

```
long helib::KSGiantStepSize ( long \ {\it D} \ )
```

Function that returns number of baby steps. Used to keep this and matmul routines "in sync".

#### 6.2.3.243 largestCoeff() [1/5]

```
NTL::ZZ helib::largestCoeff ( {\tt const\ DoubleCRT\ \&\ f\ )}
```

#### 6.2.3.244 largestCoeff() [2/5]

```
NTL::ZZ helib::largestCoeff ( {\tt const\ NTL::Vec<\ NTL::ZZ\ >\ \&\ f\ )}
```

# 6.2.3.245 largestCoeff() [3/5]

The L-infinity norm of an element (in coefficient representation)

# 6.2.3.246 largestCoeff() [4/5]

```
NTL::ZZ helib::largestCoeff ( {\tt const\ NTL::ZZX\ \&\ f\ )}
```

### 6.2.3.247 largestCoeff() [5/5]

### 6.2.3.248 leftBitwiseShift()

Left shift input by shamt.

Shift binary numbers to the left by shamt

#### **Parameters**

| output | Shifted  |  |
|--------|----------|--|
|        | result.  |  |
| input  | The      |  |
|        | num-     |  |
|        | ber      |  |
|        | to be    |  |
|        | shifted. |  |
| shamt  | The      |  |
|        | num-     |  |
|        | ber to   |  |
|        | bits to  |  |
|        | shift    |  |
|        | by.      |  |

#### Note

This is a left shift only, i.e. the bits are moved to the most-significant end.

shamt must be positive.

The size of output and input must be the same.

### 6.2.3.249 length()

# 6.2.3.250 less\_than() [1/8]

# 6.2.3.251 less\_than() [2/8]

# 6.2.3.252 less\_than() [3/8]

# 6.2.3.253 less\_than() [4/8]

# 6.2.3.254 less\_than() [5/8]

# 6.2.3.255 less\_than() [6/8]

# 6.2.3.256 less\_than() [7/8]

### 6.2.3.257 less\_than() [8/8]

#### 6.2.3.258 log2()

Base-2 logarithm.

# 6.2.3.259 log2\_realToEstimatedNoise()

# 6.2.3.260 longToBitVector()

Returns a number as a vector of bits with LSB on the left.

# **Parameters**

| num     | Number  |  |
|---------|---------|--|
|         | to be   |  |
|         | con-    |  |
|         | verted. |  |
| bitSize | Number  |  |
|         | of bits |  |
|         | of the  |  |
|         | input   |  |
|         | and     |  |
|         | output. |  |
|         |         |  |

# Returns

Bit vector representation of num.

Note

bitSize must be non-negative.

#### 6.2.3.261 Isize() [1/4]

#### 6.2.3.262 Isize() [2/4]

#### 6.2.3.263 Isize() [3/4]

#### 6.2.3.264 Isize() [4/4]

Size of STL vector as a long (rather than unsigned long)

### 6.2.3.265 make\_lazy()

This should go in NTL some day... Just call as make\_lazy(obj, ...) to initialize a lazy object via a call to a constructor T(...)

### 6.2.3.266 make\_lazy\_with\_fun()

This should go in NTL some day... Just call as make\_lazy(obj, f, ....) to initialize a lazy object via a call to f(\*obj, ...)

# 6.2.3.267 makeIrredPoly()

```
NTL::ZZX helib::makeIrredPoly ( \label{eq:problem} \log \ p, \label{eq:problem} \log \ d \ )
```

Return a degree-d irreducible polynomial mod p.

# 6.2.3.268 mapTo01() [1/4]

# 6.2.3.269 mapTo01() [2/4]

# 6.2.3.270 mapTo01() [3/4]

# 6.2.3.271 mapTo01() [4/4]

#### 6.2.3.272 maximum\_flow()

Remove from the graph all the flow-zero edges for (long i=0; i<(long)fg.size(); i++) { FNeighborList::iterator it1=fg[i].begin(); do { FNeighborList::iterator it2 = it1; it1++; // increment the iterator before potentially erasing the edge if (it2->second.flow == 0) fg[i].erase(it2); } while (it1 != fg[i].end()); }

Remove from the graph all the flow-zero edges for (long i=0; i<(long)fg.size(); i++) { FNeighborList::iterator it1=fg[i].begin(); do { FNeighborList::iterator it2 = it1; it1++; // increment the iterator before potentially erasing the edge if (it2->second.flow == 0) fg[i].erase(it2); } while (it1 != fg[i].end()); }

#### 6.2.3.273 mcDiv()

```
long helib::mcDiv (
          long a,
          long b )
```

#### 6.2.3.274 mcMod()

```
long helib::mcMod (
          long a,
          long b )
```

Routines for computing mathematically correct mod and div.

mcDiv(a, b) = floor(a / b), mcMod(a, b) = a - b\*mcDiv(a, b); in particular, mcMod(a, b) is 0 or has the same sign as b

#### 6.2.3.275 mobius()

```
long helib::mobius ( long n)
```

Compute mobius function (naive method as n is small).

#### 6.2.3.276 ModComp()

```
void helib::ModComp (
    NTL::ZZX & res,
    const NTL::ZZX & g,
    const NTL::ZZX & h,
    const NTL::ZZX & f)
```

Modular composition of polynomials:  $res = g(h) \mod f$ .

```
6.2.3.277 mul() [1/7]
```

```
void helib::mul (
            const EncryptedArray & ea,
            PlaintextArray & pa,
            const PlaintextArray & other )
6.2.3.278 mul() [2/7]
void helib::mul (
            PlaintextArray & pa,
            const BlockMatMul1D & mat )
6.2.3.279 mul() [3/7]
void helib::mul (
           PlaintextArray & pa,
            const BlockMatMulFull & mat )
6.2.3.280 mul() [4/7]
void helib::mul (
            PlaintextArray & pa,
            const MatMul1D & mat )
6.2.3.281 mul() [5/7]
void helib::mul (
            PlaintextArray & pa,
            const MatMulFull & mat )
6.2.3.282 mul() [6/7]
void helib::mul (
            std::vector< NTL::ZZX > & x,
            const std::vector< NTL::ZZX > & a,
            long b )
```

# 6.2.3.283 mul() [7/7]

# 6.2.3.284 MulAdd()

#### 6.2.3.285 MulMod() [1/6]

# 6.2.3.286 MulMod() [2/6]

#### 6.2.3.287 MulMod() [3/6]

#### 6.2.3.288 MulMod() [4/6]

```
void helib::MulMod (
     NTL::ZZX & out,
     const NTL::ZZX & f,
     long a,
     long q ) [inline]
```

# 6.2.3.289 MulMod() [5/6]

```
void helib::MulMod (
     NTL::ZZX & out,
     const NTL::ZZX & f,
     long a,
     long q,
     bool abs )
```

### 6.2.3.290 MulMod() [6/6]

```
void helib::MulMod (
    zzX & res,
    const zzX & a,
    const zzX & b,
    const PAlgebra & palg )
```

#### 6.2.3.291 multOrd()

```
long helib::multOrd ( \label{eq:problem} \mbox{long } p, \\ \mbox{long } m \mbox{ )}
```

Return multiplicative order of p modulo m, or 0 if GCD(p, m) != 1.

#### 6.2.3.292 multTwoNumbers()

```
void helib::multTwoNumbers (
    CtPtrs & product,
    const CtPtrs & lhs,
    const CtPtrs & rhs,
    bool rhsTwosComplement = false,
    long sizeLimit = 0,
    std::vector< zzX > * unpackSlotEncoding = nullptr )
```

Multiply two numbers in binary representation where each ciphertext of the input vector contains a bit.

# **Parameters**

| Parameters         |  |
|--------------------|--|
| product            | result   |
| JP. 0 22 22 1      | of the   |
|                    | mul-   |
|                    |  |
|                    | tipli-   |
|                    | cation   |
|                    | opera-   |
|                    | tion.  |
| lhs                | left   |
|                    | hand   |
|                    | side   |
|                    | of the   |
|                    | multi-   |
|                    |  |
|                    | plica-   |
|                    | tion.  |
| rhs                | right  |
|                    | hand   |
|                    | side   |
|                    | of the   |
|                    | multi-   |
|                    | plica-   |
|                    | tion.  |
|                    |  |
| rhsTwosComplement  | flag to  |
|                    | state  |
|                    | the  |
|                    | multi-   |
|                    | plier is   |
|                    | poten-   |
|                    | tially   |
|                    | nega-  |
|                    | tive.  |
| sizeLimit          | number   |
| SIZGLIIIII         | of bits  |
|                    |  |
|                    | to   |
|                    | com-   |
|                    | pute   |
|                    | on,  |
|                    | taken  |
|                    | from   |
|                    | the  |
|                    | least  |
|                    | signif-  |
|                    |  |
|                    | _  |
|                    | icant  |
|                    | icant<br>end.  |
| unpackSlotEncoding | icant  |
| unpackSlotEncoding | icant<br>end.  |
| unpackSlotEncoding | icant<br>end.<br>vector  |
| unpackSlotEncoding | icant end. vector of con-                                      |
| unpackSlotEncoding | icant end. vector of constants for un-                         |
| unpackSlotEncoding | icant end. vector of constants for unpack-                     |
| unpackSlotEncoding | icant end. vector of constants for unpacking, as               |
| unpackSlotEncoding | icant end. vector of constants for unpacking, as used          |
| unpackSlotEncoding | icant end. vector of constants for unpacking, as used in       |
| unpackSlotEncoding | icant end. vector of constants for unpacking, as used          |
| unpackSlotEncoding | icant end. vector of constants for unpacking, as used in       |
| unpackSlotEncoding | icant end. vector of constants for unpacking, as used in boot- |

# 6.2.3.293 negate()

# 6.2.3.294 negateBinary()

Negates a number in binary 2's complement representation.

### **Parameters**

| negation | Reference |  |
|----------|-----------|--|
|          | to the    |  |
|          | negated   |  |
|          | num-      |  |
|          | ber       |  |
|          | that      |  |
|          | will be   |  |
|          | popu-     |  |
|          | lated.    |  |
| input    | Number    |  |
|          | to be     |  |
|          | negated.  |  |

#### Note

input will be treated as a number in 2's complement. input must not alias negation.

#### 6.2.3.295 normalize()

```
void helib::normalize (
    zzX & f )
```

#### 6.2.3.296 operator"!=()

# 6.2.3.297 operator&()

intersection

# 6.2.3.298 operator\*()

#### 6.2.3.299 operator\*=()

```
zzX& helib::operator*= (
          zzX & a,
          long b ) [inline]
```

# 6.2.3.300 operator+()

### 6.2.3.301 operator+=()

```
zzX& helib::operator+= (
          zzX & a,
          const zzX & b ) [inline]
```

# 6.2.3.302 operator/() [1/2]

set minus

# 6.2.3.303 operator/() [2/2]

# 6.2.3.304 operator/=()

```
zzX& helib::operator/= (
          zzX & a,
          long b ) [inline]
```

# 6.2.3.305 operator<()

```
bool helib::operator< ( {\tt const\ IndexSet\ \&\ s1,} {\tt const\ IndexSet\ \&\ s2\ )}
```

Is s1 strict subset of s2.

# 6.2.3.306 operator << () [1/23]

### **Parameters**

| os   | Output     |  |
|------|------------|--|
|      | std↔       |  |
|      | ::ostream. |  |
| poly | PolyMod    |  |
|      | object     |  |
|      | to be      |  |
|      | writ-      |  |
|      | ten.       |  |

#### Returns

Input std::ostream post writing.

#### Note

p2r and G are not serialised, see note of operator>>.

# 6.2.3.307 operator <<() [2/23]

#### **Parameters**

| os   | Output      |
|------|-------------|
|      | std↔        |
|      | ::ostream.  |
| ring | PolyModRing |
|      | object      |
|      | to be       |
|      | writ-       |
|      | ten.        |

#### Returns

Input std::ostream post writing.

# 6.2.3.308 operator << () [3/23]

# 6.2.3.309 operator << () [4/23]

# 6.2.3.310 operator << () [5/23]

# 6.2.3.311 operator<<() [6/23]

#### 6.2.3.312 operator << () [7/23]

# 6.2.3.313 operator << () [8/23]

# 6.2.3.314 operator <<() [9/23]

# 6.2.3.315 operator <<() [10/23]

#### 6.2.3.316 operator << () [11/23]

# 6.2.3.317 operator <<() [12/23]

# 6.2.3.318 operator << () [13/23]

#### 6.2.3.319 operator << () [14/23]

### 6.2.3.320 operator << () [15/23]

# 6.2.3.321 operator << () [16/23]

```
template<typename T > std::ostream& helib::operator<< ( std::ostream \& s, \\ std::vector< T > v )
```

# 6.2.3.322 operator <<() [17/23]

# 6.2.3.323 operator << () [18/23]

# 6.2.3.324 operator <<() [19/23]

# 6.2.3.325 operator <<() [20/23]

# 6.2.3.326 operator <<() [21/23]

# 6.2.3.327 operator << () [22/23]

#### 6.2.3.328 operator << () [23/23]

#### 6.2.3.329 operator<=()

Is s1 subset or equal to s2.

#### 6.2.3.330 operator==()

Comparing maps, by comparing all the elements.

# 6.2.3.331 operator>() [1/2]

Is s2 strict subset of s1.

### 6.2.3.332 operator>() [2/2]

#### 6.2.3.333 operator>=()

Is s2 subset or equal to s2.

# 6.2.3.334 operator>>() [1/12]

#### **Parameters**

| is   | Input       |
|------|-------------|
|      | std↩        |
|      | ::istream.  |
| poly | Destination |
|      | PolyMod     |
|      | object.     |

#### Returns

```
Input std::istream post reading.
```

#### Note

```
poly must be constructed with an appropriate p2r and G BEFORE calling this function. For example, polyMod my_poly(p2r, G); std::cin > my_poly;
```

#### 6.2.3.335 operator>>() [2/12]

# 6.2.3.336 operator>>() [3/12]

#### 6.2.3.337 operator>>() [4/12]

#### 6.2.3.338 operator>>() [5/12]

#### 6.2.3.339 operator>>() [6/12]

# 6.2.3.340 operator>>() [7/12]

# 6.2.3.341 operator>>() [8/12]

# 6.2.3.342 operator>>() [9/12]

# 6.2.3.343 operator>>() [10/12]

### 6.2.3.344 operator>>() [11/12]

# 6.2.3.345 operator>>() [12/12]

### 6.2.3.346 operator^()

exclusive-or

# 6.2.3.347 operator" | ()

union

#### 6.2.3.348 optimalBenes()

# 6.2.3.349 optimalBenesAux()

```
BenesMemoEntry helib::optimalBenesAux ( long \ i, \\ long \ budget, \\ long \ nlev, \\ const \ NTL::Vec< \ NTL::Vec< \ long >> \& \ costTab, \\ BenesMemoTable \& \ memoTab \ )
```

#### 6.2.3.350 optimalLower()

# 6.2.3.351 optimalUpperAux()

#### 6.2.3.352 ord()

```
long helib::ord ( \log \ \textit{N,} \\ \log \ \textit{p} \ )
```

Compute the highest power of p that divides N.

# 6.2.3.353 packConstant()

```
void helib::packConstant (
    zzX & result,
    unsigned long data,
    long nbits,
    const EncryptedArray & ea )
```

#### 6.2.3.354 packConstants()

# 6.2.3.355 packedRecrypt() [1/4]

# 6.2.3.356 packedRecrypt() [2/4]

Function for packed recryption to recrypt multiple numbers.

#### **Parameters**

| а                  | first in-                     |
|--------------------|-------------------------------|
|                    | put of                        |
|                    | which                         |
|                    | to re-                        |
|                    | crypt.                        |
| b                  | second                        |
|                    | input                         |
|                    | of                            |
|                    | which                         |
|                    | to re-                        |
|                    | crypt.                        |
| unpackSlotEncoding | vector                        |
|                    | of con-                       |
|                    | stants                        |
|                    | for un-                       |
|                    | pack-                         |
|                    | ing, as                       |
|                    | used                          |
|                    | in                            |
|                    | boot-                         |
|                    | strap-                        |
|                    | ping.                         |
|                    | used<br>in<br>boot-<br>strap- |

# 6.2.3.357 packedRecrypt() [3/4]

#### 6.2.3.358 packedRecrypt() [4/4]

#### 6.2.3.359 PAlgebraLift() [1/2]

#### 6.2.3.360 PAlgebraLift() [2/2]

#### 6.2.3.361 phi\_N()

```
long helib::phi_N ( long N )
```

Compute Phi(N).

# 6.2.3.362 phiN() [1/2]

```
void helib::phiN ( long \ \& \ phiN, std::vector < \ long \ > \ \& \ facts, long \ N \ )
```

Compute Phi(N) and also factorize N.

#### 6.2.3.363 phiN() [2/2]

```
void helib::phiN (
         NTL::ZZ & phiN,
         std::vector< NTL::ZZ > & facts,
         const NTL::ZZ & N )
```

# 6.2.3.364 plaintextAutomorph() [1/2]

# 6.2.3.365 plaintextAutomorph() [2/2]

#### 6.2.3.366 poly\_comp()

#### 6.2.3.367 polyEval() [1/2]

Evaluate an encrypted polynomial on an encrypted input.

# **Parameters**

| out | res  | to hold<br>the<br>return<br>value     |
|-----|------|---------------------------------------|
| in  | poly | the degree-d poly-nomial to evalu-ate |
| in  | х    | the point on which to evaluate        |

# 6.2.3.368 polyEval() [2/2]

Evaluate a cleartext polynomial on an encrypted input.

# **Parameters**

| out | res  | to hold<br>the<br>return<br>value     |
|-----|------|---------------------------------------|
| in  | poly | the degree-d poly-nomial to evalu-ate |
| in  | х    | the point on which to evaluate        |

#### **Parameters**

| in | k | optional  |
|----|---|-----------|
|    |   | opti-     |
|    |   | miza-     |
|    |   | tion      |
|    |   | param-    |
|    |   | eter,     |
|    |   | de-       |
|    |   | faults    |
|    |   | to        |
|    |   | sqrt(d/2) |
|    |   | rounded   |
|    |   | up or     |
|    |   | down      |
|    |   | to a      |
|    |   | power     |
|    |   | of two    |

# 6.2.3.369 polyEvalMod()

Evaluates a modular integer polynomial, returns poly(x) mod p.

# 6.2.3.370 PolyRed() [1/4]

```
void helib::PolyRed (
          NTL::ZZX & F,
           const NTL::ZZ & q,
          bool abs = false ) [inline]
```

# 6.2.3.371 PolyRed() [2/4]

#### 6.2.3.372 PolyRed() [3/4]

```
void helib::PolyRed (
    NTL::ZZX & out,
    const NTL::ZZX & in,
    const NTL::ZZ & q,
    bool abs = false )
```

#### 6.2.3.373 PolyRed() [4/4]

Reduce all the coefficients of a polynomial modulo q.

When abs=false reduce to interval (-q/2,...,q/2), when abs=true reduce to [0,q). When abs=false and q=2, maintains the same sign as the input.

#### 6.2.3.374 power()

### 6.2.3.375 pp\_factorize()

```
void helib::pp_factorize ( std::vector < long > \& factors, \\ long N )
```

Prime-power factorization.

# 6.2.3.376 ppInvert() [1/4]

#### 6.2.3.377 ppInvert() [2/4]

### 6.2.3.378 ppInvert() [3/4]

Compute the inverse mod  $p^r$  of an n x n matrix.

NTL's current smallint modulus  $zz_p::modulus()$  is assumed to be  $p^r$  for p prime, r >= 1 integer. For the  $zz_pE$  variant also  $zz_pE::modulus()$  must be initialized. An error is raised if A is not invertible mod p.

### 6.2.3.379 ppInvert() [4/4]

# 6.2.3.380 ppsolve() [1/2]

A version for GF2: must have p == 2 and r == 1.

#### 6.2.3.381 ppsolve() [2/2]

Prime power solver.

A is an n x n matrix, b is a length n (row) vector, this function finds a solution for the matrix-vector equation x A = b. An error is raised if A is not invertible mod p.

NTL's current smallint modulus,  $zz_p::modulus()$ , is assumed to be  $p^r$ , for p prime, r >= 1 integer.

#### 6.2.3.382 primroot()

```
long helib::primroot (
          long N,
          long phiN )
```

Find a primitive root modulo N.

#### 6.2.3.383 print() [1/2]

#### 6.2.3.384 print() [2/2]

# 6.2.3.385 print3D() [1/3]

# 6.2.3.386 print3D() [2/3]

# 6.2.3.387 print3D() [3/3]

### 6.2.3.388 print\_stats()

```
void helib::print_stats ( std::ostream \ \& \ s \ )
```

# 6.2.3.389 printAllTimers()

Print the value of all timers to stream.

# 6.2.3.390 printFlow()

# 6.2.3.391 printNamedTimer()

#### 6.2.3.392 printVec()

#### 6.2.3.393 printZZX()

#### 6.2.3.394 ptr2nonNull()

#### 6.2.3.395 random()

### 6.2.3.396 randomPerm()

A random size-n permutation.

### 6.2.3.397 randomSlot()

## $\textbf{6.2.3.398} \quad \textbf{randomSlot} < \textbf{BGV} > \textbf{()}$

```
{\tt template}{<>}
BGV::SlotType helib::randomSlot< BGV > (
            const Context & context )
6.2.3.399 randomSlot< CKKS >()
template<>
CKKS::SlotType helib::randomSlot< CKKS > (
            UNUSED const Context & context )
6.2.3.400 RandPoly()
NTL::ZZX helib::RandPoly (
            long n,
            const NTL::ZZ & p )
6.2.3.401 range() [1/2]
general_range<long> helib::range (
            long m_{r}
            long n ) [inline]
6.2.3.402 range() [2/2]
general_range<long> helib::range (
            long n ) [inline]
```

## 6.2.3.403 rationalApprox() [1/2]

```
std::pair< long, long > helib::rationalApprox ( double x, long denomBound = 0 )
```

#### 6.2.3.404 rationalApprox() [2/2]

#### 6.2.3.405 rawDecrypt()

#### 6.2.3.406 read()

#### 6.2.3.407 read\_ntl\_vec\_long()

#### 6.2.3.408 read\_raw\_double()

#### 6.2.3.409 read\_raw\_int()

#### 6.2.3.410 read\_raw\_int32()

### 6.2.3.411 read\_raw\_vector() [1/3]

## 6.2.3.412 read\_raw\_vector() [2/3]

### 6.2.3.413 read\_raw\_vector() [3/3]

### 6.2.3.414 read\_raw\_vector< double >()

### 6.2.3.415 read\_raw\_vector< long >()

#### 6.2.3.416 read\_raw\_xdouble()

### 6.2.3.417 read\_raw\_ZZ()

#### 6.2.3.418 readContextBase()

```
void helib::readContextBase (
    std::istream & s,
    unsigned long & m,
    unsigned long & p,
    unsigned long & r,
    std::vector< long > & gens,
    std::vector< long > & ords )
```

read [m p r gens ords] data, needed to construct context

read [m p r] data, needed to construct context

#### 6.2.3.419 readContextBaseBinary()

```
void helib::readContextBaseBinary (
    std::istream & s,
    unsigned long & m,
    unsigned long & p,
    unsigned long & r,
    std::vector< long > & gens,
    std::vector< long > & ords )
```

read [m p r gens ords] data, needed to construct context

#### 6.2.3.420 readContextBinary()

### 6.2.3.421 readEyeCatcher()

### 6.2.3.422 readPubKeyBinary()

```
void helib::readPubKeyBinary ( std::istream \ \& \ str, PubKey \ \& \ pk \ )
```

### 6.2.3.423 readSecKeyBinary()

### 6.2.3.424 realToEstimatedNoise()

### 6.2.3.425 recordAutomorphVal()

```
void helib::recordAutomorphVal ( long \ k \ ) \quad [inline]
```

### 6.2.3.426 recordAutomorphVal2()

```
void helib::recordAutomorphVal2 ( \log \ k \ ) \quad [inline]
```

### 6.2.3.427 reducedCount()

### 6.2.3.428 reduceModPhimX()

### 6.2.3.429 registerTimer()

### 6.2.3.430 RelaxedInv() [1/2]

### 6.2.3.431 RelaxedInv() [2/2]

### 6.2.3.432 rem()

#### 6.2.3.433 removeDups()

```
void helib::removeDups (  \mbox{std::list} < \mbox{long} > \& \ x \mbox{,} \\ \mbox{bool} * \mbox{aux} )
```

#### 6.2.3.434 repack() [1/2]

#### 6.2.3.435 repack() [2/2]

### 6.2.3.436 replicate() [1/3]

```
template<typename Scheme > void helib::replicate ( const EncryptedArray & , Ptxt< Scheme > & ptxt, long i)
```

Replicate single slot of a Ptxt object across all of its slots.

### **Template Parameters**

Scheme | Encryption scheme used (must be BGV or CKKS).

### **Parameters**

| ptxt | Plaintext |  |
|------|-----------|--|
|      | on        |  |
|      | which     |  |
|      | to do     |  |
|      | the       |  |
|      | repli-    |  |
|      | cation.   |  |

#### **Parameters**

| i | Position |  |
|---|----------|--|
|   | of the   |  |
|   | slot to  |  |
|   | repli-   |  |
|   | cate.    |  |

#### Returns

Reference to \*this post replication.

### 6.2.3.437 replicate() [2/3]

The value in slot #pos is replicated in all other slots. On an n-slot ciphertext, this algorithm performs  $O(\log n)$  1D rotations.

#### 6.2.3.438 replicate() [3/3]

### 6.2.3.439 replicate0()

A lower-level routine. Same as replicate, but assumes all slots are zero except slot #pos.

#### 6.2.3.440 replicateAll() [1/3]

replicateAll uses a hybrid strategy, combining the O(log n) strategy of the replicate method, with an O(1) strategy, which is faster but introduces more noise. This tradeoff is controlled by the parameter recBound:

- recBound < 0: recursion to depth |recBound| (faster, noisier)</li>
- recBound ==0: no recursion (slower, less noise)
- recBound > 0: the recursion depth is chosen heuristically, but is capped at recBound

The default value for recBound is 64, this ensures that the choice is based only on the heuristic, which will introduce noise corresponding to  $O(\log \log n)$  levels of recursion, but still gives an algorithm that theoretically runs in time O(n).

#### 6.2.3.441 replicateAll() [2/3]

```
void helib::replicateAll (
    std::vector< Ctxt > & v,
    const EncryptedArray & ea,
    const Ctxt & ctxt,
    long recBound = 64,
    RepAuxDim * repAuxPtr = nullptr )
```

return the result as a std::vector of ciphertexts, mostly useful for debugging purposes (for real parameters would take a lot of memory)

### 6.2.3.442 replicateAll() [3/3]

Generate a vector of plaintexts with each slot replicated in each plaintext.

#### **Template Parameters**

Scheme | Encryption scheme used (must be BGV or CKKS).

#### **Parameters**

| V    | Vector    |
|------|-----------|
|      | of        |
|      | repli-    |
|      | cated     |
|      | plain-    |
|      | text      |
|      | slots.    |
| ptxt | Plaintext |
|      | whose     |
|      | slots     |
|      | will be   |
|      | repli-    |
|      | cated.    |

The order of the return vector agrees with the order of the slots. i.e. the ith plaintext in the return value is a replication of \*this[i].

### 6.2.3.443 replicateAllOrig()

This function is obsolete, and is kept for historical purposes only. It was a first attempt at implementing the O(1)-amortized algorithm, but is less efficient than the function above.

### 6.2.3.444 resetAllTimers()

```
void helib::resetAllTimers ( )
```

### 6.2.3.445 resize() [1/7]

## 6.2.3.446 resize() [2/7]

## **6.2.3.447** resize() [3/7]

## 6.2.3.448 resize() [4/7]

## 6.2.3.449 resize() [5/7]

## 6.2.3.450 resize() [6/7]

```
template<typename T > void helib::resize ( std::vector < T > \& \ v \text{,} \\ long \ sz \ )
```

### 6.2.3.451 resize() [7/7]

#### 6.2.3.452 reverse()

Reverse a vector in place.

#### 6.2.3.453 RLWE()

Choose random c0,c1 such that c0+s\*c1 = p\*e for a short e Returns a high-probability bound on the L-infty norm of the canonical embedding

#### 6.2.3.454 RLWE1()

Same as RLWE, but assumes that c1 is already chosen by the caller.

### 6.2.3.455 rotate() [1/2]

### 6.2.3.456 rotate() [2/2]

Rotate a vector in place using swaps.

### 6.2.3.457 runningSums() [1/2]

A ctxt that encrypts  $(x_1,...,x_n)$  is replaced by an encryption of  $(y_1,...,y_n)$ , where  $y_i=sum_{j\leq i}x_j$ .

#### 6.2.3.458 runningSums() [2/2]

### 6.2.3.459 sameObject()

Testing if two vectors point to the same object.

### 6.2.3.460 sampleGaussian() [1/4]

### 6.2.3.461 sampleGaussian() [2/4]

```
void helib::sampleGaussian (  std::vector < \ double \ > \& \ dvec, \\ long \ n, \\ double \ stdev \ )
```

Choose a vector of continuous Gaussians.

#### 6.2.3.462 sampleGaussian() [3/4]

```
double helib::sampleGaussian (
    zzX & poly,
    const Context & context,
    double stdev )
```

#### 6.2.3.463 sampleGaussian() [4/4]

```
void helib::sampleGaussian (
    zzX & poly,
    long n,
    double stdev)
```

Sample polynomials with Gaussian coefficients.

### 6.2.3.464 sampleGaussianBounded()

```
double helib::sampleGaussianBounded (
    zzX & poly,
    const Context & context,
    double stdev )
```

### 6.2.3.465 sampleHWt() [1/3]

#### 6.2.3.466 sampleHWt() [2/3]

### 6.2.3.467 sampleHWt() [3/3]

```
void helib::sampleHWt (
    zzX & poly,
    long n,
    long Hwt = 100 )
```

Sample a degree-(n-1) poly as above, with only Hwt nonzero coefficients.

#### 6.2.3.468 sampleHWtBounded()

```
double helib::sampleHWtBounded (
    zzX & poly,
    const Context & context,
    long Hwt = 100 )
```

### 6.2.3.469 sampleHWtBoundedEffectiveBound()

## 6.2.3.470 sampleSmall() [1/3]

### 6.2.3.471 sampleSmall() [2/3]

```
double helib::sampleSmall (
          zzX & poly,
          const Context & context )
```

#### 6.2.3.472 sampleSmall() [3/3]

Sample a degree-(n-1) poly, with -1/0/+1 coefficients. Each coefficients is +-1 with probability prob/2 each, and 0 with probability 1-prob. By default, pr[nonzero]=1/2.

### 6.2.3.473 sampleSmallBounded()

#### 6.2.3.474 sampleUniform() [1/4]

### 6.2.3.475 sampleUniform() [2/4]

```
void helib::sampleUniform (
         NTL::ZZX & poly,
         long n,
         const NTL::ZZ & B = NTL::ZZ(100L) )
```

### 6.2.3.476 sampleUniform() [3/4]

#### 6.2.3.477 sampleUniform() [4/4]

Sample a degree-(n-1) ZZX, with coefficients uniform in [-B,B].

### 6.2.3.478 seekPastChar()

Advance the input stream beyond white spaces and a single instance of the char cc.

#### 6.2.3.479 setAutomorphVals()

```
void helib::setAutomorphVals ( {\tt std::set} < {\tt long} \, > * \, {\tt aVals} \, \, ) \quad [{\tt inline}]
```

#### 6.2.3.480 setAutomorphVals2()

```
void helib::setAutomorphVals2 ( std::set < long > * aVals ) \quad [inline] \\
```

### 6.2.3.481 setDryRun()

```
bool helib::setDryRun (
                bool toWhat = true ) [inline]
```

### 6.2.3.482 setHyperColumn() [1/6]

```
template void helib::setHyperColumn (  {\rm const~NTL}:: {\tt Vec} < {\tt long} > \& \ v, \\ {\tt const~CubeSlice} < {\tt long} > \& \ s, \\ {\tt long} \ pos \ )
```

#### 6.2.3.483 setHyperColumn() [2/6]

### 6.2.3.484 setHyperColumn() [3/6]

#### 6.2.3.485 setHyperColumn() [4/6]

#### 6.2.3.486 setHyperColumn() [5/6]

setHyperColumn does the reverse of getHyperColumn, setting the column to the given vector

### 6.2.3.487 setHyperColumn() [6/6]

this version of setHyperColumn implicitly pads v with a default value, if v is too short

### 6.2.3.488 setLengthZero() [1/4]

#### 6.2.3.489 setLengthZero() [2/4]

### 6.2.3.490 setLengthZero() [3/4]

### 6.2.3.491 setLengthZero() [4/4]

```
template<typename T > void helib::setLengthZero ( std::vector< T > \& \ vec \ )
```

### 6.2.3.492 setTimersOff()

```
void helib::setTimersOff ( ) [inline]
```

### 6.2.3.493 setTimersOn()

```
void helib::setTimersOn ( ) [inline]
```

#### 6.2.3.494 setupDebugGlobals()

Setup function for setting up the global debug variables.

Note

Works only if HELIB\_DEBUG is defined. It does not do anything otherwise

#### 6.2.3.495 shift()

### 6.2.3.496 splitBinaryNums()

Splits a single binary number into two binary numbers leftSplit and rightSplit.

Split a binary number into two separate binary numbers.

### **Parameters**

| leftSplit  | Left<br>hand<br>side<br>of the<br>split.  |
|------------|---|
| rightSplit | Right<br>hand<br>side<br>of the<br>split. |
| input      | Binary<br>num-<br>ber<br>to be<br>split.  |

#### Note

The size of leftSplit and rightSplit must sum to the size of input.

The location of the split is defined by the sizes of leftSplit and rightSplit.

## 6.2.3.497 sub()

### 6.2.3.498 subtractBinary()

Subtracts rhs from lhs where lhs, rhs are in 2's complement.

### **Parameters**

| difference         | Reference<br>to the<br>differ-<br>ence<br>post<br>sub-<br>trac- |
|--------------------|---|
| lhs                | tion.<br>Left   |
| 1113               | hand  |
|                    | side of   |
|                    | sub-  |
|                    | trac-   |
|                    | tion.   |
| rhs                | Right   |
|                    | hand  |
|                    | side of   |
|                    | sub-  |
|                    | trac-   |
|                    | tion.   |
| unpackSlotEncoding | vector  |
|                    | of con-   |
|                    | stants  |
|                    | for un-   |
|                    | pack-   |
|                    | ing, as   |
|                    | used  |
|                    | in  |
|                    | boot-   |
|                    | strap-  |
|                    | pina.   |

Generated by Doxygen

Note

lhs and rhs must have the same size.

## 6.2.3.499 sumOfCoeffs() [1/3]

```
NTL::ZZ helib::sumOfCoeffs ( {\tt const\ DoubleCRT\ \&\ f\ )}
```

### 6.2.3.500 sumOfCoeffs() [2/3]

### 6.2.3.501 sumOfCoeffs() [3/3]

### 6.2.3.502 swap() [1/2]

#### 6.2.3.503 swap() [2/2]

#### 6.2.3.504 tableLookup()

The input is a plaintext table T[] and an array of encrypted bits I[], holding the binary representation of an index i into T. The output is the encrypted value T[i].

### 6.2.3.505 tableWriteIn()

The input is an encrypted table T[] and an array of encrypted bits I[], holding the binary representation of an index i into T. This function increments by one the entry T[i].

#### 6.2.3.506 timer\_compare()

#### 6.2.3.507 to\_ZZX()

```
NTL::ZZX helib::to_ZZX (

const DoubleCRT & d ) [inline]
```

### 6.2.3.508 TofftRep\_trunc() [1/2]

#### 6.2.3.509 TofftRep\_trunc() [2/2]

```
void helib::TofftRep_trunc (
    NTL::fftRep & y,
    const NTL::zz_pX & x,
    long k,
    UNUSED long len,
    long lo,
    long hi ) [inline]
```

### 6.2.3.510 totalProduct()

### 6.2.3.511 totalSums()

### 6.2.3.512 traceMap()

### 6.2.3.513 TraceMap()

#### 6.2.3.514 unpack() [1/2]

### 6.2.3.515 unpack() [2/2]

### 6.2.3.516 unpackSlots() [1/2]

## 6.2.3.517 unpackSlots() [2/2]

```
void helib::unpackSlots (
          std::vector< unsigned long > & value,
          PlaintextArray & pa,
          const EncryptedArray & ea )
```

### 6.2.3.518 Vec\_replicate()

#### 6.2.3.519 vecCopy() [1/4]

### 6.2.3.520 vecCopy() [2/4]

#### 6.2.3.521 vecCopy() [3/4]

#### 6.2.3.522 vecCopy() [4/4]

### 6.2.3.523 vecRed() [1/2]

```
void helib::vecRed (
          NTL::Vec< NTL::ZZ > & out,
          const NTL::Vec< NTL::ZZ > & in,
          const NTL::ZZ & q,
          bool abs )
```

### 6.2.3.524 vecRed() [2/2]

#### 6.2.3.525 vector\_replicate()

#### 6.2.3.526 vecToStr()

### 6.2.3.527 Warning() [1/2]

```
void helib::Warning ( {\tt const~char~*~\it msg~)} \quad [{\tt inline}]
```

### 6.2.3.528 Warning() [2/2]

#### 6.2.3.529 write()

### 6.2.3.530 write\_ntl\_vec\_long()

### 6.2.3.531 write\_raw\_double()

### 6.2.3.532 write\_raw\_int()

### 6.2.3.533 write\_raw\_int32()

### 6.2.3.534 write\_raw\_vector()

```
template<typename T > void helib::write_raw_vector ( std::ostream \ \& \ str, const \ std::vector< T > \& \ v \ )
```

## $\textbf{6.2.3.535} \quad \textbf{write\_raw\_vector} < \textbf{double} > \textbf{()}$

### 6.2.3.536 write\_raw\_vector< long >()

### 6.2.3.537 write\_raw\_xdouble()

### 6.2.3.538 write\_raw\_ZZ()

### 6.2.3.539 writeContextBase()

```
void helib::writeContextBase (  \texttt{std::ostream \& } s, \\  \texttt{const Context \& } context \ ) \\
```

write [m p r gens ords] data

write [m p r] data

### 6.2.3.540 writeContextBaseBinary()

write [m p r gens ords] data

### 6.2.3.541 writeContextBinary()

### 6.2.3.542 writeEyeCatcher()

### 6.2.3.543 writePubKeyBinary()

### 6.2.3.544 writeSecKeyBinary()

#### 6.2.4 Variable Documentation

### 6.2.4.1 activeContext

```
Context * helib::activeContext = nullptr
```

### 6.2.4.2 CLOCK\_SCALE

```
const unsigned long helib::CLOCK_SCALE = (unsigned long)CLOCKS_PER_SEC
```

### 6.2.4.3 dbg\_ptxt

NTL::ZZX helib::dbg\_ptxt

#### 6.2.4.4 dbgEa

```
std::shared_ptr< const EncryptedArray > helib::dbgEa = nullptr
```

#### 6.2.4.5 dbgKey

```
SecKey * helib::dbgKey = nullptr
```

### 6.2.4.6 erfc\_inverse

```
const double helib::erfc_inverse[]
```

#### Initial value:

 $= \{0,$ 

```
0.6744897501960817432,
1.1503493803760081782,
1.5341205443525463117,
1.8627318674216514554,
2.1538746940614562129,
2.4175590162365050618,
2.6600674686174596585,
2.8856349124267571473,
3.0972690781987844623,
3.2971933456919633418,
3.4871041041144311068,
3.6683292851213230192,
3.8419306855019108708,
4.0087725941685849622,
4.1695693233491057549,
4.3249190408260462571,
4.4753284246542033544,
4.6212310014992471565,
4.7630010342678139569,
4.9009642079631930118}
```

### 6.2.4.7 fhe\_force\_chen\_han

```
long helib::fhe_force_chen_han = 0
```

### 6.2.4.8 fhe\_stats

```
bool helib::fhe_stats = false
```

### 6.2.4.9 fhe\_test\_force\_bsgs

```
int helib::fhe_test_force_bsgs = 0
```

#### 6.2.4.10 fhe\_test\_force\_hoist

```
int helib::fhe_test_force_hoist = 0
```

#### 6.2.4.11 fhe\_watcher

```
int helib::fhe_watcher = 0
```

### 6.2.4.12 PI

const long double helib::PI

#### Initial value:

3.1415926535897932384626433832795028841971693993751058209749445923078164L

#### 6.2.4.13 printFlag

long helib::printFlag

#### 6.2.4.14 replicateVerboseFlag

NTL\_THREAD\_LOCAL bool helib::replicateVerboseFlag = false

## 6.2.4.15 thinRecrypt\_initial\_level

long helib::thinRecrypt\_initial\_level

## 6.3 helib::FHEglobals Namespace Reference

### **Variables**

• bool dryRun = false

A dry-run flag The dry-run option disables most operations, to save time. This lets us quickly go over the evaluation of a circuit and estimate the resulting noise magnitude, without having to actually compute anything.

std::set< long > \* automorphVals = nullptr

A list of required automorphisms When non-nullptr, causes Ctxt::smartAutomorphism to just record the requested automorphism rather than actually performing it. This can be used to get a list of needed automorphisms for certain operations and then generate all these key-switching matrices. Should only be used in conjunction with dryRun=true.

std::set< long > \* automorphVals2 = nullptr

### 6.3.1 Variable Documentation

### 6.3.1.1 automorphVals

```
std::set< long > * helib::FHEglobals::automorphVals = nullptr
```

A list of required automorphisms When non-nullptr, causes Ctxt::smartAutomorphism to just record the requested automorphism rather than actually performing it. This can be used to get a list of needed automorphisms for certain operations and then generate all these key-switching matrices. Should only be used in conjunction with dryRun=true.

#### 6.3.1.2 automorphVals2

```
std::set< long > * helib::FHEglobals::automorphVals2 = nullptr
```

#### 6.3.1.3 dryRun

```
bool helib::FHEglobals::dryRun = false
```

A dry-run flag The dry-run option disables most operations, to save time. This lets us quickly go over the evaluation of a circuit and estimate the resulting noise magnitude, without having to actually compute anything.

## 6.4 NTL Namespace Reference

## 6.5 std Namespace Reference

# **Chapter 7**

# **Class Documentation**

## 7.1 helib::add\_pa\_impl< type > Class Template Reference

### **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const PlaintextArray &other)

#### 7.1.1 Member Function Documentation

#### 7.1.1.1 apply()

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

## 7.2 helib::AddDAG Class Reference

A class representing the logic of the order of bit products when adding two integers.

178 Class Documentation

#### **Public Member Functions**

```
· void init (const CtPtrs &a, const CtPtrs &b)
```

Build a plan to add a and b.

- AddDAG (const CtPtrs &a, const CtPtrs &b)
- void apply (CtPtrs &sum, const CtPtrs &a, const CtPtrs &b, long sizeLimit=0)

Perform the actual addition.

long lowLvl () const

Returns the lowest level in this DAG.

• DAGnode \* findP (long i, long j) const

Returns a pointer to the a 'p' node of index (i,j)

DAGnode \* findQ (long i, long j) const

Returns a pointer to the a 'q' node of index (i,j)

### 7.2.1 Detailed Description

A class representing the logic of the order of bit products when adding two integers.

Given two input arrays a[], b[], we build a DAG with each node representing a term either of the form  $p_{i,j} = \prod \prod \prod_{t=j}^i (a[t]+b[t])$ , or of the form  $q_{i,j} = (a[j]*b[j]) * \prod_{t=j+1}^i (a[t]+b[t])$ . The source nodes are of the forms a[i]\*b[i] and a[i]\*b[i], and each non-source node has exactly two parents, whose product yields that node.

When building the DAG, we keep the level of each node as high as possible. For example we can set  $q_{i,j}=p_{\leftarrow}\{i,k\}*q_{k-1,j}$  or  $q_{i,j}=p_{i,k+1}*q_{k,j}$  (among other options), and we choose the option that results in the highest level. In addition, we try to minimize the number of nodes in the DAG that actually need to be computed while adding the two numbers (subject to still consuming as few levels as possible).

#### 7.2.2 Constructor & Destructor Documentation

#### 7.2.2.1 AddDAG()

#### 7.2.3 Member Function Documentation

#### 7.2.3.1 apply()

Perform the actual addition.

Apply the DAG to actually compute the sum.

#### 7.2.3.2 findP()

Returns a pointer to the a 'p' node of index (i,j)

#### 7.2.3.3 findQ()

Returns a pointer to the a 'q' node of index (i,j)

#### 7.2.3.4 init()

Build a plan to add a and b.

### 7.2.3.5 lowLvl()

```
long helib::AddDAG::lowLvl ( ) const [inline]
```

Returns the lowest level in this DAG.

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/binaryArith.cpp

# 7.3 helib::PGFFT::aligned\_allocator< T > Class Template Reference

```
#include <PGFFT.h>
```

# **Public Types**

• using value\_type = T

#### **Public Member Functions**

```
    aligned_allocator () noexcept
    template < class U >
        aligned_allocator (aligned_allocator < U > const &) noexcept
    value_type * allocate (std::size_t n)
    void deallocate (value_type *p, std::size_t) noexcept
    template < class U >
        bool operator == (aligned_allocator < U > const &) noexcept
    template < class U >
        bool operator! = (aligned_allocator < U > const &y) noexcept
```

# 7.3.1 Member Typedef Documentation

#### 7.3.1.1 value\_type

```
template<class T >
using helib::PGFFT::aligned_allocator< T >::value_type = T
```

#### 7.3.2 Constructor & Destructor Documentation

#### 7.3.2.1 aligned\_allocator() [1/2]

```
template<class T >
helib::PGFFT::aligned_allocator< T >::aligned_allocator ( ) [inline], [noexcept]
```

# 7.3.2.2 aligned\_allocator() [2/2]

# 7.3.3 Member Function Documentation

#### 7.3.3.1 allocate()

#### 7.3.3.2 deallocate()

#### 7.3.3.3 operator"!=()

#### 7.3.3.4 operator==()

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PGFFT.h

# 7.4 helib::applyPerm\_pa\_impl< type > Class Template Reference

#### **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const NTL::Vec< long > &pi)

# 7.4.1 Member Function Documentation

#### 7.4.1.1 apply()

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.5 helib::ArgMap Class Reference

Basic class for arg parsing. Example use:

```
#include <ArgMap.h>
```

#### **Classes**

struct ArgProcessor

# **Public Types**

• enum Separator { Separator::COLON, Separator::EQUALS, Separator::WHITESPACE }

#### **Public Member Functions**

template<typename T >

```
ArgMap & arg (const std::string &name, T &value)
```

Add a new argument description Adds a new argument description with value of type T. Throws helib::RuntimeError if the arg key is duplicated or if the storing variable is used more than once.

• template<typename T >

```
ArgMap & arg (const std::string &name, T &value, const std::string &doc)
```

Add a new argument with docs Adds a new argument description with value of type T and docs. Throws helib::RuntimeError if the arg key is duplicated or if the storing variable is used more than once.

• template<typename T >

```
ArgMap & arg (const std::string &name, T &value, const std::string &doc, const char *info)
```

Add a new argument with docs and default description Adds a new argument description with value of type T, with docs and default description. Throws helib::RuntimeError if the arg key is duplicated or if the storing variable is used more than once.

template<typename C >

ArgMap & dots (C &container, const char \*name)

Adds variable number of positional arg types after defined arg types are exhausted. These are treated as optional.

ArgMap & parse (int argc, char \*\*argv)

Parse the argv array Parse the argv array If it fails or -h is an argument it prints the usage and exits the program.

ArgMap & parse (const std::string &filepath)

Parse the configuration/parameters file Parsing a configuration file only functions with named arguments Parse the config file Throws RuntimeError on failure.

ArgMap & optional ()

Swaps to optional arg mode (default) Swaps to optional arg mode. Following arguments will be considered optional.

ArgMap & required ()

Swaps to required arg mode Swaps to required arg mode. Following arguments will be considered required.

ArgMap & toggle (bool t=true)

Swaps to toggle arg type Swaps to required arg mode. Following arguments will be considered of toggle type.

ArgMap & named ()

Swaps to named arg type (default) Swaps to required arg mode. Following arguments will be considered of named type.

ArgMap & positional ()

Swaps to positional arg type Swaps to required arg mode. Following arguments will be considered of positional type.

ArgMap & helpArgs (const std::initializer\_list< std::string > s)

Provide custom help toggle args. (defaults are "-h", "--help") Overwrite default help toggle args to custom ones for parsing.

- ArgMap & helpArgs (const std::string s)
- ArgMap & diagnostics (std::ostream &ostrm=std::cout)

Turns on diagnostics printout when parsing Swaps to required arg mode. Following arguments will be considered of positional type.

ArgMap & separator (Separator s)

Sets the key-value separator Sets the named args key-value pair separator character.

ArgMap & note (const std::string &s)

Adds a note to usage Adds a note to the arg usage description.

• void usage (const std::string &msg="") const

Print usage and exit Prints the usage and exits the program.

std::string doc () const

Return arg docs Returns the argument documentation as a string.

# 7.5.1 Detailed Description

#### Basic class for arg parsing. Example use:

```
// Variables to be set by command line.
                                                      // default values.
long p = 2;
long m = 19;
bool t = false;
bool f = true;
std::string k = "Hello World";
                                                      // (*) marks default.
ArgMap()
  .required()
                                                      // set args to required.
  .positional()
    .arg("p", p, "doc for p") //
.arg("m", m, "doc for m", "undefined") // special default info.
                                                      // swap to optional args (*).
  .optional()
  .named()
                                                      // named args (*) e.g.k=v.
  .separator(ArgMap::Separator::WHITESPACE) // change separator to
.arg("-k", k, "doc for k", "") // whitespace ('=' is (*)).
.note("an extra note") // no default value info.
  .toggle()
.arg("-t", t, "doc for t", "")
                                                      // add extra doc/note.
                                                     // toggle flag sets bool true.
  .toggle(false)
                                                      // toggle flag sets bool false.
  .arg("-f", f, "doc for f", "")
.helpArgs({"--myhelp"})
                                                      // changes default help flags
                                                      // (*) is {"-h", "--help"}.
  .parse(argc, argv);
                                                      // parses and overwrites values
```

#### 7.5.2 Member Enumeration Documentation

#### 7.5.2.1 Separator

```
enum helib::ArgMap::Separator [strong]
```

#### Enumerator

| COLON      |  |
|------------|--|
| EQUALS     |  |
| WHITESPACE |  |

# 7.5.3 Member Function Documentation

# 7.5.3.1 arg() [1/3]

Add a new argument description Adds a new argument description with value of type T. Throws helib::RuntimeError if the arg key is duplicated or if the storing variable is used more than once.

# **Template Parameters**

| Τ | The type of the argument |
|---|--------------------------|
|---|--------------------------|

#### **Parameters**

| name  | The     |
|-------|---------|
|       | argu-   |
|       | ment    |
|       | name    |
|       | (key)   |
| value | a vari- |
|       | able    |
|       | where   |
|       | the     |
|       | argu-   |
|       | ment    |
|       | will be |
|       | stored. |
|       | Also    |
|       | used    |
|       | as      |
|       | default |
|       | value   |

#### Returns

A reference to the modified ArgMap object

#### 7.5.3.2 arg() [2/3]

Add a new argument with docs Adds a new argument description with value of type T and docs. Throws helib::RuntimeError if the arg key is duplicated or if the storing variable is used more than once.

# **Template Parameters**

| The type of the argument |  |
|--------------------------|--|
|--------------------------|--|

# **Parameters**

| name  | The         |
|-------|-------------|
|       | argu-       |
|       | ment        |
|       | name        |
|       | (key)       |
| value | a vari-     |
|       | able        |
|       | where       |
|       | the         |
|       | argu-       |
|       | ment        |
|       | will be     |
|       | stored.     |
|       | Also        |
|       | used        |
|       | as          |
|       | default     |
|       | value       |
| doc1  | Description |
|       | of the      |
|       | argu-       |
|       | ment        |
|       | used        |
|       | when        |
|       | dis-        |
|       | playing     |
|       | usage       |

#### Returns

A reference to the modified ArgMap object

# 7.5.3.3 arg() [3/3]

```
template<typename T >
ArgMap & helib::ArgMap::arg (
```

```
const std::string & name,
T & value,
const std::string & doc,
const char * info )
```

Add a new argument with docs and default description Adds a new argument description with value of type T, with docs and default description. Throws helib::RuntimeError if the arg key is duplicated or if the storing variable is used more than once.

# **Template Parameters**

#### **Parameters**

| Parameter    | 'S               |
|--------------|------------------|
| name         | The              |
|              | argu-            |
|              | ment             |
|              | name             |
|              | (key)            |
| value        | a vari-          |
|              | able             |
|              | where            |
|              | the              |
|              | argu-            |
|              | ment             |
|              | will be          |
|              | stored.          |
|              | Also             |
|              | used             |
|              | as               |
|              | default          |
|              | value            |
| doc1         | Description      |
|              | of the           |
|              | argu-            |
|              | ment             |
|              | used             |
|              | when<br>dis-     |
|              |                  |
|              | playing<br>usage |
| : <b>(</b> - | _                |
| info         | The              |
|              | default<br>value |
|              | de-              |
|              | scrip-           |
|              | tion             |
|              | (ig-             |
|              | nored            |
|              | if               |
|              | nullptr          |
|              | or "")           |
|              | J. ,             |

#### Returns

A reference to the modified ArgMap object

# 7.5.3.4 diagnostics()

Turns on diagnostics printout when parsing Swaps to required arg mode. Following arguments will be considered of positional type.

# Returns

A reference to the ArgMap object

#### 7.5.3.5 doc()

```
std::string helib::ArgMap::doc ( ) const [inline]
```

Return arg docs Returns the argument documentation as a string.

#### Returns

the argument documentation string

# 7.5.3.6 dots()

Adds variable number of positional arg types after defined arg types are exhausted. These are treated as optional.

#### **Parameters**

| container | holds   |
|-----------|---------|
|           | the     |
|           | vari-   |
|           | able    |
|           | posi-   |
|           | tional  |
|           | args.   |
|           | It must |
|           | have a  |
|           | push←   |
|           | _back   |
|           | method  |
|           | for in- |
|           | sertion |

#### Returns

A reference to the ArgMap object

# 7.5.3.7 helpArgs() [1/2]

```
ArgMap & helib::ArgMap::helpArgs ( {\tt const \ std::initializer\_list< \ std::string > s \ )} \quad [inline]
```

Provide custom help toggle args. (defaults are "-h", "--help") Overwrite default help toggle args to custom ones for parsing.

Returns

A reference to the ArgMap object

#### 7.5.3.8 helpArgs() [2/2]

# 7.5.3.9 named()

```
ArgMap & helib::ArgMap::named ( ) [inline]
```

Swaps to named arg type (default) Swaps to required arg mode. Following arguments will be considered of named type.

Returns

A reference to the ArgMap object

#### 7.5.3.10 note()

```
ArgMap & helib::ArgMap::note ( {\tt const\ std::string\ \&\ s\ )} \quad [{\tt inline}]
```

Adds a note to usage Adds a note to the arg usage description.

#### **Parameters**

| s | The    |
|---|--------|
|   | note   |
|   | string |

#### Returns

A reference to the ArgMap object

# 7.5.3.11 optional()

```
ArgMap & helib::ArgMap::optional ( ) [inline]
```

Swaps to optional arg mode (default) Swaps to optional arg mode. Following arguments will be considered optional.

#### Returns

A reference to the ArgMap object

# 7.5.3.12 parse() [1/2]

Parse the configuration/parameters file Parsing a configuration file only functions with named arguments Parse the config file Throws RuntimeError on failure.

#### **Parameters**

|          | _      |
|----------|--------|
| filepath | the    |
|          | config |
|          | file   |
|          | path   |

### Returns

A reference to the ArgMap object

#### 7.5.3.13 parse() [2/2]

Parse the argv array Parse the argv array If it fails or -h is an argument it prints the usage and exits the program.

#### **Parameters**

| argc | number<br>of en-<br>tries in<br>argv              |
|------|---|
| argv | array<br>con-<br>taining<br>the<br>argu-<br>ments |

#### Returns

A reference to the ArgMap object

#### 7.5.3.14 positional()

```
ArgMap & helib::ArgMap::positional ( ) [inline]
```

Swaps to positional arg type Swaps to required arg mode. Following arguments will be considered of positional type.

#### Returns

A reference to the ArgMap object

# 7.5.3.15 required()

```
ArgMap & helib::ArgMap::required ( ) [inline]
```

Swaps to required arg mode Swaps to required arg mode. Following arguments will be considered required.

#### Returns

A reference to the ArgMap object

# 7.5.3.16 separator()

Sets the key-value separator Sets the named args key-value pair separator character.

# **Parameters**

#### Returns

A reference to the ArgMap object

# 7.5.3.17 toggle()

Swaps to toggle arg type Swaps to required arg mode. Following arguments will be considered of toggle type.

#### Returns

A reference to the ArgMap object

# 7.5.3.18 usage()

Print usage and exit Prints the usage and exits the program.

#### **Parameters**

| msg | An       |
|-----|----------|
|     | addi-    |
|     | tional   |
|     | mes-     |
|     | sage     |
|     | to print |
|     | before   |
|     | show-    |
|     | ing      |
|     | usage    |

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/ArgMap.h

# 7.6 helib::ArgMap::ArgProcessor Struct Reference

#include <ArgMap.h>

#### **Public Member Functions**

- virtual ~ArgProcessor ()=default
- virtual ArgType getArgType ()=0
- virtual bool process (const std::string &s)=0

#### 7.6.1 Constructor & Destructor Documentation

#### 7.6.1.1 ∼ArgProcessor()

virtual helib::ArgMap::ArgProcessor::~ArgProcessor ( ) [virtual], [default]

# 7.6.2 Member Function Documentation

# 7.6.2.1 getArgType()

virtual ArgType helib::ArgMap::ArgProcessor::getArgType ( ) [pure virtual]

#### 7.6.2.2 process()

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/ArgMap.h

# 7.7 helib::BasicAutomorphPrecon Class Reference

Pre-computation to speed many automorphism on the same ciphertext.

#### **Public Member Functions**

- BasicAutomorphPrecon (const Ctxt &\_ctxt)
- std::shared ptr< Ctxt > automorph (long k) const

# 7.7.1 Detailed Description

Pre-computation to speed many automorphism on the same ciphertext.

The expensive part of homomorphic automorphism is breaking the ciphertext parts into digits. The usual setting is we first rotate the ciphertext parts, then break them into digits. But when we apply many automorphisms it is faster to break the original ciphertext into digits, then rotate the digits (as opposed to first rotate, then break). An BasicAutomorphPrecon object breaks the original ciphertext and keeps the digits, then when you call automorph is only needs to apply the native automorphism and key switching to the digits, which is fast(er).

# 7.7.2 Constructor & Destructor Documentation

#### 7.7.2.1 BasicAutomorphPrecon()

#### 7.7.3 Member Function Documentation

#### 7.7.3.1 automorph()

```
\label{lem:std:shared_ptr} $$ std::shared_ptr<Ctxt> helib::BasicAutomorphPrecon::automorph ( long $k$ ) const [inline]
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

#### 7.8 helib::BGV Struct Reference

Type for BGV scheme, to be used as template parameter.

```
#include <Ptxt.h>
```

# **Public Types**

```
    using SlotType = PolyMod
    Slot type used for BGV plaintexts: helib::PolyMod i.e. an integer polynomial modulo p<sup>r</sup> and G.
```

# 7.8.1 Detailed Description

Type for BGV scheme, to be used as template parameter.

# 7.8.2 Member Typedef Documentation

#### 7.8.2.1 SlotType

```
using helib::BGV::SlotType = PolyMod
```

Slot type used for BGV plaintexts: helib::PolyMod i.e. an integer polynomial modulo p^r and G.

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ptxt.h

# 7.9 helib::BipartitleGraph Class Reference

A bipartite flow graph.

```
#include <matching.h>
```

# **Public Member Functions**

- void addEdge (long from, long to, long label, long color=0)
- void partitionToMatchings ()
- void printout ()

#### **Public Attributes**

• std::vector< LabeledVertex > left

# 7.9.1 Detailed Description

A bipartite flow graph.

# 7.9.2 Member Function Documentation

#### 7.9.2.1 addEdge()

#### 7.9.2.2 partitionToMatchings()

```
void helib::BipartitleGraph::partitionToMatchings ( )
```

# 7.9.2.3 printout()

```
void helib::BipartitleGraph::printout ( )
```

# 7.9.3 Member Data Documentation

#### 7.9.3.1 left

std::vector<LabeledVertex> helib::BipartitleGraph::left

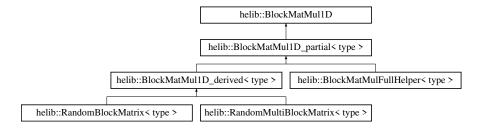
The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matching.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matching.cpp

# 7.10 helib::BlockMatMul1D Class Reference

#include <matmul.h>

Inheritance diagram for helib::BlockMatMul1D:



# **Public Types**

typedef BlockMatMul1DExec ExecType

#### **Public Member Functions**

- virtual ∼BlockMatMul1D ()
- virtual const EncryptedArray & getEA () const =0
- virtual long getDim () const =0

# 7.10.1 Member Typedef Documentation

#### 7.10.1.1 ExecType

typedef BlockMatMul1DExec helib::BlockMatMul1D::ExecType

# 7.10.2 Constructor & Destructor Documentation

#### 7.10.2.1 ~BlockMatMul1D()

virtual helib::BlockMatMullD::~BlockMatMullD ( ) [inline], [virtual]

#### 7.10.3 Member Function Documentation

#### 7.10.3.1 getDim()

```
virtual long helib::BlockMatMul1D::getDim ( ) const [pure virtual]
```

Implemented in helib::BlockMatMulFullHelper< type >, helib::RandomMultiBlockMatrix< type >, and helib::RandomBlockMatrix< type

#### 7.10.3.2 getEA()

```
virtual const EncryptedArray& helib::BlockMatMullD::getEA ( ) const [pure virtual]
```

Implemented in helib::BlockMatMulFullHelper< type >, helib::RandomMultiBlockMatrix< type >, and helib::RandomBlockMatrix< type

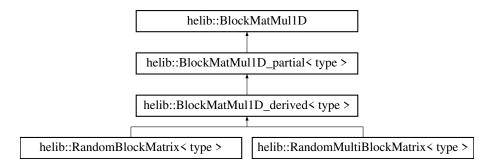
The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

# 7.11 helib::BlockMatMul1D\_derived< type > Class Template Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::BlockMatMul1D\_derived< type >:



#### **Public Member Functions**

- virtual bool multipleTransforms () const =0
- virtual bool get (mat R &out, long i, long j, long k) const =0
- bool processDiagonal (std::vector< RX > &poly, long i, const EncryptedArrayDerived< type > &ea) const override

#### **Additional Inherited Members**

#### 7.11.1 Member Function Documentation

#### 7.11.1.1 get()

Implemented in helib::RandomMultiBlockMatrix< type >.

#### 7.11.1.2 multipleTransforms()

```
template<typename type >
virtual bool helib::BlockMatMul1D_derived< type >::multipleTransforms ( ) const [pure virtual]
```

Implemented in helib::RandomMultiBlockMatrix< type >, and helib::RandomBlockMatrix< type >.

# 7.11.1.3 processDiagonal()

Implements helib::BlockMatMul1D\_partial< type >.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.12 helib::BlockMatMul1D\_derived\_impl< type > Struct Template Reference

## **Static Public Member Functions**

- static bool processDiagonal1 (std::vector< RX > &poly, long i, const EncryptedArrayDerived< type > &ea, const BlockMatMul1D\_derived< type > &mat)
- static bool processDiagonal2 (std::vector< RX > &poly, long idx, const EncryptedArrayDerived< type > &ea, const BlockMatMul1D derived< type > &mat)
- static bool processDiagonal (std::vector< RX > &poly, long i, const EncryptedArrayDerived< type > &ea, const BlockMatMul1D\_derived< type > &mat)

#### 7.12.1 Member Function Documentation

#### 7.12.1.1 processDiagonal()

#### 7.12.1.2 processDiagonal1()

#### 7.12.1.3 processDiagonal2()

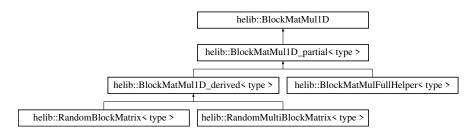
The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.13 helib::BlockMatMul1D\_partial< type > Class Template Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::BlockMatMul1D\_partial< type >:



#### **Public Member Functions**

virtual bool processDiagonal (std::vector< RX > &poly, long i, const EncryptedArrayDerived< type > &ea)
 const =0

#### **Additional Inherited Members**

#### 7.13.1 Member Function Documentation

#### 7.13.1.1 processDiagonal()

```
template<typename type > virtual bool helib::BlockMatMullD_partial< type >::processDiagonal ( std::vector< RX > & poly, long i, const EncryptedArrayDerived< type > & ea ) const [pure virtual]
```

 $Implemented \ in \ helib:: Block Mat Mul Full Helper < type >, \ and \ helib:: Block Mat Mul 1 D\_derived < type >.$ 

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

# 7.14 helib::BlockMatMul1DExec Class Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::BlockMatMul1DExec:



#### **Public Member Functions**

- BlockMatMul1DExec (const BlockMatMul1D &mat, bool minimal=false)
- · void mul (Ctxt &ctxt) const override
- void upgrade () override
- const EncryptedArray & getEA () const override

# **Public Attributes**

- const EncryptedArray & ea
- long dim
- long D
- long d
- · bool native
- long strategy
- ConstMultiplierCache cache
- ConstMultiplierCache cache1

#### 7.14.1 Constructor & Destructor Documentation

# 7.14.1.1 BlockMatMul1DExec()

#### 7.14.2 Member Function Documentation

#### 7.14.2.1 getEA()

```
const EncryptedArray& helib::BlockMatMullDExec::getEA ( ) const [inline], [override], [virtual]
```

Implements helib::MatMulExecBase.

# 7.14.2.2 mul()

Implements helib::MatMulExecBase.

# 7.14.2.3 upgrade()

```
void helib::BlockMatMullDExec::upgrade ( ) [inline], [override], [virtual]
```

Implements helib::MatMulExecBase.

# 7.14.3 Member Data Documentation

# 7.14.3.1 cache

ConstMultiplierCache helib::BlockMatMullDExec::cache

#### 7.14.3.2 cache1

ConstMultiplierCache helib::BlockMatMullDExec::cache1

# 7.14.3.3 D

long helib::BlockMatMul1DExec::D

# 7.14.3.4 d

long helib::BlockMatMul1DExec::d

#### 7.14.3.5 dim

long helib::BlockMatMullDExec::dim

#### 7.14.3.6 ea

const EncryptedArray& helib::BlockMatMullDExec::ea

# 7.14.3.7 native

bool helib::BlockMatMul1DExec::native

#### 7.14.3.8 strategy

```
long helib::BlockMatMul1DExec::strategy
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.15 helib::BlockMatMul1DExec\_construct< type > Struct Template Reference

#### **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, const BlockMatMul1D &mat\_basetype, std
 ::vector< std::shared\_ptr< ConstMultiplier >> &vec, std::vector< std::shared\_ptr< ConstMultiplier >>
 &vec1, long strategy)

#### 7.15.1 Member Function Documentation

#### 7.15.1.1 apply()

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/matmul.cpp

# 7.16 helib::BlockMatMulFullExec\_construct< type >::BlockMatMulDimComp Struct Reference

#### **Public Member Functions**

- BlockMatMulDimComp (const EncryptedArrayDerived< type > \*\_ea)
- bool operator() (long i, long j)

# **Public Attributes**

• const EncryptedArrayDerived< type > \* ea

# 7.16.1 Constructor & Destructor Documentation

# 7.16.1.1 BlockMatMulDimComp()

#### 7.16.2 Member Function Documentation

#### 7.16.2.1 operator()()

#### 7.16.3 Member Data Documentation

#### 7.16.3.1 ea

```
template<typename type >
const EncryptedArrayDerived<type>* helib::BlockMatMulFullExec_construct< type >::BlockMat \cdot
MulDimComp::ea
```

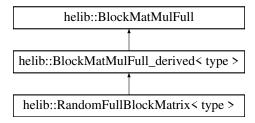
The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.17 helib::BlockMatMulFull Class Reference

#include <matmul.h>

Inheritance diagram for helib::BlockMatMulFull:



# **Public Types**

typedef BlockMatMulFullExec ExecType

#### **Public Member Functions**

- virtual ∼BlockMatMulFull ()
- virtual const EncryptedArray & getEA () const =0

# 7.17.1 Member Typedef Documentation

#### 7.17.1.1 ExecType

 ${\tt typedef~BlockMatMulFullExec~helib::BlockMatMulFull::ExecType}$ 

#### 7.17.2 Constructor & Destructor Documentation

# 7.17.2.1 $\sim$ BlockMatMulFull()

virtual helib::BlockMatMulFull::~BlockMatMulFull ( ) [inline], [virtual]

#### 7.17.3 Member Function Documentation

#### 7.17.3.1 getEA()

```
virtual const EncryptedArray& helib::BlockMatMulFull::getEA ( ) const [pure virtual]
Implemented in helib::RandomFullBlockMatrix< type >.
```

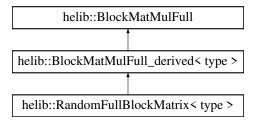
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

# 7.18 helib::BlockMatMulFull\_derived< type > Class Template Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::BlockMatMulFull derived< type >:



#### **Public Member Functions**

virtual bool get (mat\_R &out, long i, long j) const =0

#### **Additional Inherited Members**

#### 7.18.1 Member Function Documentation

# 7.18.1.1 get()

Implemented in helib::RandomFullBlockMatrix< type >.

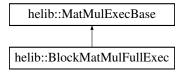
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

# 7.19 helib::BlockMatMulFullExec Class Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::BlockMatMulFullExec:



#### **Public Member Functions**

- BlockMatMulFullExec (const BlockMatMulFull &mat, bool minimal=false)
- · void mul (Ctxt &ctxt) const override
- void upgrade () override
- const EncryptedArray & getEA () const override
- long rec\_mul (Ctxt &acc, const Ctxt &ctxt, long dim, long idx) const

#### **Public Attributes**

- · const EncryptedArray & ea
- bool minimal
- std::vector< long > dims
- std::vector< BlockMatMul1DExec > transforms

# 7.19.1 Constructor & Destructor Documentation

#### 7.19.1.1 BlockMatMulFullExec()

#### 7.19.2 Member Function Documentation

# 7.19.2.1 getEA()

```
const EncryptedArray& helib::BlockMatMulFullExec::getEA ( ) const [inline], [override], [virtual]
Implements helib::MatMulExecBase.
```

# 7.19.2.2 mul()

Implements helib::MatMulExecBase.

#### 7.19.2.3 rec\_mul()

# 7.19.2.4 upgrade()

```
void helib::BlockMatMulFullExec::upgrade ( ) [inline], [override], [virtual]
```

Implements helib::MatMulExecBase.

# 7.19.3 Member Data Documentation

#### 7.19.3.1 dims

```
std::vector<long> helib::BlockMatMulFullExec::dims
```

# 7.19.3.2 ea

```
const EncryptedArray& helib::BlockMatMulFullExec::ea
```

#### 7.19.3.3 minimal

bool helib::BlockMatMulFullExec::minimal

#### 7.19.3.4 transforms

```
std::vector<BlockMatMul1DExec> helib::BlockMatMulFullExec::transforms
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.20 helib::BlockMatMulFullExec\_construct< type > Struct Template Reference

#### Classes

struct BlockMatMulDimComp

#### **Static Public Member Functions**

- static long rec\_mul (long dim, long idx, const std::vector< long > &idxes, std::vector< BlockMatMul1DExec > &transforms, bool minimal, const std::vector< long > &dims, const EncryptedArray &ea\_basetype, const EncryptedArrayDerived< type > &ea, const BlockMatMulFull\_derived< type > &mat)
- static void apply (const EncryptedArrayDerived< type > &ea, const EncryptedArray &ea\_basetype, const BlockMatMulFull &mat\_basetype, std::vector< BlockMatMul1DExec > &transforms, bool minimal, std← ::vector< long > &dims)

# 7.20.1 Member Function Documentation

# 7.20.1.1 apply()

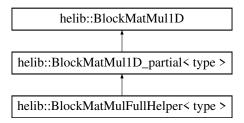
#### 7.20.1.2 rec\_mul()

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.21 helib::BlockMatMulFullHelper< type > Class Template Reference

Inheritance diagram for helib::BlockMatMulFullHelper< type >:



#### **Public Member Functions**

- BlockMatMulFullHelper (const EncryptedArray &\_ea\_basetype, const BlockMatMulFull\_derived< type > &
   — mat, const std::vector< long > &\_init\_idxes, long \_dim)
- bool processDiagonal (std::vector< RX > &poly, long offset, const EncryptedArrayDerived< type > &ea)
  const override
- const EncryptedArray & getEA () const override
- long getDim () const override

#### **Public Attributes**

- const EncryptedArray & ea\_basetype
- const BlockMatMulFull\_derived< type > & mat
- std::vector< long > init\_idxes
- long dim

## **Additional Inherited Members**

### 7.21.1 Constructor & Destructor Documentation

#### 7.21.1.1 BlockMatMulFullHelper()

#### 7.21.2 Member Function Documentation

# 7.21.2.1 getDim()

```
template<typename type >
long helib::BlockMatMulFullHelper< type >::getDim ( ) const [inline], [override], [virtual]
```

Implements helib::BlockMatMul1D.

#### 7.21.2.2 getEA()

```
template<typename type >
const EncryptedArray& helib::BlockMatMulFullHelper< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::BlockMatMul1D.

#### 7.21.2.3 processDiagonal()

Implements helib::BlockMatMul1D\_partial< type >.

#### 7.21.3 Member Data Documentation

#### 7.21.3.1 dim

```
template<typename type >
long helib::BlockMatMulFullHelper< type >::dim
```

#### 7.21.3.2 ea\_basetype

```
template<typename type >
const EncryptedArray& helib::BlockMatMulFullHelper< type >::ea_basetype
```

#### 7.21.3.3 init idxes

```
template<typename type >
std::vector<long> helib::BlockMatMulFullHelper< type >::init_idxes
```

#### 7.21.3.4 mat

```
template<typename type >
const BlockMatMulFull_derived<type>& helib::BlockMatMulFullHelper< type >::mat
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.22 helib::CKKS Struct Reference

Type for CKKS scheme, to be used as template parameter.

```
#include <Ptxt.h>
```

# **Public Types**

```
    using SlotType = std::complex < double >
    Slot type used for CKKS plaintexts: std::complex < double >.
```

# 7.22.1 Detailed Description

Type for CKKS scheme, to be used as template parameter.

# 7.22.2 Member Typedef Documentation

#### 7.22.2.1 SlotType

```
using helib::CKKS::SlotType = std::complex<double>
```

Slot type used for CKKS plaintexts: std::complex<double>.

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ptxt.h

# 7.23 helib::Cmodulus Class Reference

Provides FFT and iFFT routines modulo a single-precision prime.

```
#include <CModulus.h>
```

#### **Public Member Functions**

• Cmodulus ()

Default constructor.

- Cmodulus (const Cmodulus &other)
- Cmodulus (const PAlgebra &zms, long qq, long rt)

Constructor.

• Cmodulus & operator= (const Cmodulus &other)

Copy assignment operator.

- const PAlgebra & getZMStar () const
- unsigned long getM () const
- unsigned long getPhiM () const
- long getQ () const
- NTL::mulmod\_t getQInv () const
- long getRoot () const
- const zz\_pXModulus1 & getPhimX () const
- · void restoreModulus () const

Restore NTL's current modulus.

- void FFT (NTL::vec\_long &y, const NTL::ZZX &x) const
- void FFT (NTL::vec\_long &y, const zzX &x) const
- void FFT aux (NTL::vec long &y, NTL::zz pX &tmp) const
- void iFFT (NTL::zz\_pX &x, const NTL::vec\_long &y) const

#### Static Public Member Functions

- static NTL::zz\_pX & getScratch\_zz\_pX ()
- static NTL::Vec< long > & getScratch\_vec\_long ()
- static NTL::fftRep & getScratch\_fftRep (long k)

# 7.23.1 Detailed Description

Provides FFT and iFFT routines modulo a single-precision prime.

On initialization, it initializes NTL's zz\_pContext for this q and computes a 2m-th root of unity r mod q and also  $r^{-1}$  mod q. Thereafter this class provides FFT and iFFT routines that converts between time & frequency domains. Some tables are computed the first time that each directions is called, which are then used in subsequent computations.

The "time domain" polynomials are represented as ZZX, which are reduced modulo Phi\_m(X). The "frequency domain" are just vectors of integers (vec long), that store only the evaluation in primitive m-th roots of unity.

#### 7.23.2 Constructor & Destructor Documentation

# 7.23.2.1 Cmodulus() [1/3]

```
helib::Cmodulus::Cmodulus ( ) [inline]
```

Default constructor.

#### 7.23.2.2 Cmodulus() [2/3]

```
helib::Cmodulus::Cmodulus (

const Cmodulus & other ) [inline]
```

#### 7.23.2.3 Cmodulus() [3/3]

Constructor.

Note

Specify m and q, and optionally also the root if q == 0, then the current context is used

#### 7.23.3 Member Function Documentation

## 7.23.3.1 FFT() [1/2]

## 7.23.3.2 FFT() [2/2]

## 7.23.3.3 FFT\_aux()

## 7.23.3.4 getM()

```
unsigned long helib::Cmodulus::getM ( ) const [inline]
```

## 7.23.3.5 getPhiM()

```
unsigned long helib::Cmodulus::getPhiM ( ) const [inline]
```

### 7.23.3.6 getPhimX()

```
const zz_pXModulus1& helib::Cmodulus::getPhimX ( ) const [inline]
```

## 7.23.3.7 getQ()

```
long helib::Cmodulus::getQ ( ) const [inline]
```

## 7.23.3.8 getQlnv()

```
NTL::mulmod_t helib::Cmodulus::getQInv ( ) const [inline]
```

### 7.23.3.9 getRoot()

```
long helib::Cmodulus::getRoot ( ) const [inline]
```

## 7.23.3.10 getScratch\_fftRep()

## 7.23.3.11 getScratch\_vec\_long()

```
\label{eq:ntl:vec_long} $$ NTL::Vec< long > \& helib::Cmodulus::getScratch_vec_long () [static] $$
```

## 7.23.3.12 getScratch\_zz\_pX()

```
NTL::zz_pX & helib::Cmodulus::getScratch_zz_pX ( ) [static]
```

### 7.23.3.13 getZMStar()

```
const PAlgebra& helib::Cmodulus::getZMStar ( ) const [inline]
```

## 7.23.3.14 iFFT()

#### 7.23.3.15 operator=()

Copy assignment operator.

#### 7.23.3.16 restoreModulus()

```
void helib::Cmodulus::restoreModulus ( ) const [inline]
```

Restore NTL's current modulus.

The documentation for this class was generated from the following files:

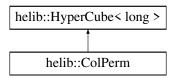
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/CModulus.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/CModulus.cpp

## 7.24 helib::ColPerm Class Reference

Permuting a single dimension (column) of a hypercube.

```
#include <permutations.h>
```

Inheritance diagram for helib::ColPerm:



## **Public Member Functions**

- ColPerm (const CubeSignature &\_sig)
- long getPermDim () const
- void setPermDim (long \_dim)
- · void makeExplicit (Permut &out) const
- long getShiftAmounts (Permut &out) const
- void getBenesShiftAmounts (NTL::Vec< Permut > &out, NTL::Vec< bool > &idID, const NTL::Vec< long > &benesLvls) const
- void printout (std::ostream &s)

A test/debugging method.

## 7.24.1 Detailed Description

Permuting a single dimension (column) of a hypercube.

ColPerm is derived from a HyperCube<long>, and it uses the cube object to store the actual permutation data. The interpretation of this data, however, depends on the data member dim.

The cube is partitioned into columns of size n = getDim(dim): a single column consists of the n entries whose indices i have the same coordinates in all dimensions other than dim. The entries in any such column form a permutation on [0..n).

For a given ColPerm perm, one way to access each column is as follows: for slice\_index = [0..perm.getProd(0, dim)) CubeSlice slice(perm, slice\_index, dim) for col\_index = [0..perm.getProd(dim+1)) getHyperColumn(column, slice, col\_index)

Another way is to use the getCoord and addCoord methods.

For example, permuting a 2x3x2 cube along dim=1 (the 2nd dimension), we could have the data std::vector as [ 1 1 0 2 2 0 2 0 1 1 0 2 ]. This means the four columns are permuted by the permutations [ 1 0 2 ] [ 1 2 0 ] [ 2 1 0 ] [ 0 1 2 ]. Written explicitly, we get: [ 2 3 0 5 4 1 10 7 8 9 6 11 ].

Another representation that we provide is by "shift amount": how many slots each element needs to move inside its small permutation. For the example above, this will be: [1-10][2-1-1][20-2][000] so we write the permutation as [11-110-22000-20].

#### 7.24.2 Constructor & Destructor Documentation

## 7.24.2.1 ColPerm()

```
helib::ColPerm::ColPerm (

const CubeSignature & _sig ) [inline], [explicit]
```

## 7.24.3 Member Function Documentation

### 7.24.3.1 getBenesShiftAmounts()

Get multiple layers of a Benes permutation network. Returns in out[i][j] the shift amount to move item j in the i'th layer. Also isID[i]=true if the i'th layer is the identity (i.e., contains only 0 shift amounts).

#### 7.24.3.2 getPermDim()

```
long helib::ColPerm::getPermDim ( ) const [inline]
```

#### 7.24.3.3 getShiftAmounts()

For each position in the data std::vector, compute how many slots it should be shifted inside its small permutation. Returns zero if all the shift amounts are zero, nonzero values otherwise.

#### 7.24.3.4 makeExplicit()

### 7.24.3.5 printout()

```
void helib::ColPerm::printout (  std::ostream \ \& \ s \ ) \quad [inline]
```

A test/debugging method.

## 7.24.3.6 setPermDim()

The documentation for this class was generated from the following files:

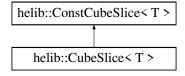
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/permutations.cpp

# 7.25 helib::ConstCubeSlice < T > Class Template Reference

A constant lower-dimension slice of a hypercube.

```
#include <hypercube.h>
```

Inheritance diagram for helib::ConstCubeSlice< T >:



#### **Public Member Functions**

ConstCubeSlice (const HyperCube < T > &\_cube)

initialize the slice to the full cube

- ConstCubeSlice (const NTL::Vec< T > & data, const CubeSignature & sig)
- ConstCubeSlice (const ConstCubeSlice &bigger, long i, long \_dimOffset=1)
- ConstCubeSlice (const HyperCube< T > &\_cube, long i, long \_dimOffset=1)
- · const CubeSignature & getSig () const

const ref to signature

• long getSize () const

total size

long getNumDims () const

number of dimensions

long getDim (long d) const

size of dimension d

• long getProd (long d) const

product of sizes of dimensions d, d+1, ...

• long getProd (long from, long to) const

product of sizes of dimensions from, from+1, ..., to-1

• long getCoord (long i, long d) const

get coordinate in dimension d of index i

long addCoord (long i, long d, long offset) const

add offset to coordinate in dimension d of index i

• long numSlices (long d=1) const

number of slices

• long sliceSize (long d=1) const

size of one slice

• long numCols () const

number of columns

• const T & at (long i) const

read-only reference to element at position i, with bounds check

const T & operator[] (long i) const

read-only reference to element at position i, without bounds check

#### 7.25.1 Detailed Description

template < typename T > class helib::ConstCubeSlice < T >

A constant lower-dimension slice of a hypercube.

A ConstCubeSlice acts like a pointer to a lower dimensional constant subcube of a hypercube. It is initialized using a reference to a hypercube, which must remain alive during the lifetime of the slice, to prevent dangling pointers. The subclass CubeSlice works also with non-constant cubes and subcubes.

In addition, for greater flexibility, a "slice" may be initialized with a vector and a signature, rather than a cube

### 7.25.2 Constructor & Destructor Documentation

#### 7.25.2.1 ConstCubeSlice() [1/4]

initialize the slice to the full cube

### 7.25.2.2 ConstCubeSlice() [2/4]

### 7.25.2.3 ConstCubeSlice() [3/4]

initialize the slice to point to the i-th subcube (with some given dimension offset) of the cube pointed to by \_cube or bigger.

## 7.25.2.4 ConstCubeSlice() [4/4]

## 7.25.3 Member Function Documentation

## 7.25.3.1 addCoord()

add offset to coordinate in dimension d of index i

### 7.25.3.2 at()

```
\label{template} $$\operatorname{T\& helib::ConstCubeSlice} \subset T > :: at ($$\log i$) const [inline]
```

read-only reference to element at position i, with bounds check

## 7.25.3.3 getCoord()

get coordinate in dimension d of index i

#### 7.25.3.4 getDim()

```
\label{template} $$ template < typename T > $$ long helib::ConstCubeSlice < T >::getDim ( $$ long $d$ ) const [inline] $$
```

size of dimension d

## 7.25.3.5 getNumDims()

```
template<typename T >
long helib::ConstCubeSlice< T >::getNumDims ( ) const [inline]
```

number of dimensions

#### 7.25.3.6 getProd() [1/2]

product of sizes of dimensions d, d+1, ...

## 7.25.3.7 getProd() [2/2]

product of sizes of dimensions from, from+1, ..., to-1

## 7.25.3.8 getSig()

```
template<typename T >
const CubeSignature& helib::ConstCubeSlice< T >::getSig ( ) const [inline]
```

const ref to signature

## 7.25.3.9 getSize()

```
\label{template} $$ template < typename T > $$ long helib::ConstCubeSlice < T >::getSize ( ) const [inline]
```

total size

### 7.25.3.10 numCols()

```
template<typename T >
long helib::ConstCubeSlice< T >::numCols ( ) const [inline]
```

number of columns

### 7.25.3.11 numSlices()

number of slices

#### 7.25.3.12 operator[]()

read-only reference to element at position i, without bounds check

### 7.25.3.13 sliceSize()

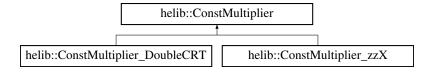
size of one slice

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/hypercube.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/hypercube.cpp

# 7.26 helib::ConstMultiplier Struct Reference

Inheritance diagram for helib::ConstMultiplier:



### **Public Member Functions**

- virtual ∼ConstMultiplier ()
- virtual void mul (Ctxt &ctxt) const =0
- virtual std::shared\_ptr< ConstMultiplier > upgrade (const Context &context) const =0

#### 7.26.1 Constructor & Destructor Documentation

#### 7.26.1.1 ∼ConstMultiplier()

```
\label{thm:constMultiplier::} \verb|\| ConstMultiplier::| \verb|\| ConstMultiplier|| ( ) [inline], [virtual] |
```

#### 7.26.2 Member Function Documentation

### 7.26.2.1 mul()

Implemented in helib::ConstMultiplier\_zzX, and helib::ConstMultiplier\_DoubleCRT.

### 7.26.2.2 upgrade()

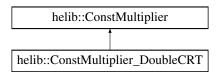
Implemented in helib::ConstMultiplier zzX.

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.27 helib::ConstMultiplier\_DoubleCRT Struct Reference

Inheritance diagram for helib::ConstMultiplier\_DoubleCRT:



#### **Public Member Functions**

- ConstMultiplier\_DoubleCRT (const DoubleCRT &\_data, double \_sz)
- · void mul (Ctxt &ctxt) const override
- std::shared\_ptr< ConstMultiplier > upgrade (UNUSED const Context &context) const override

### **Public Attributes**

- DoubleCRT data
- double sz

## 7.27.1 Constructor & Destructor Documentation

## 7.27.1.1 ConstMultiplier\_DoubleCRT()

### 7.27.2 Member Function Documentation

### 7.27.2.1 mul()

Implements helib::ConstMultiplier.

## 7.27.2.2 upgrade()

### 7.27.3 Member Data Documentation

### 7.27.3.1 data

```
DoubleCRT helib::ConstMultiplier_DoubleCRT::data
```

## 7.27.3.2 sz

```
double helib::ConstMultiplier_DoubleCRT::sz
```

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.28 helib::ConstMultiplier\_zzX Struct Reference

Inheritance diagram for helib::ConstMultiplier\_zzX:

```
helib::ConstMultiplier
helib::ConstMultiplier_zzX
```

### **Public Member Functions**

- ConstMultiplier\_zzX (const zzX &\_data)
- void mul (Ctxt &ctxt) const override
- std::shared\_ptr< ConstMultiplier > upgrade (const Context &context) const override

## **Public Attributes**

• zzX data

## 7.28.1 Constructor & Destructor Documentation

### 7.28.1.1 ConstMultiplier\_zzX()

### 7.28.2 Member Function Documentation

## 7.28.2.1 mul()

Implements helib::ConstMultiplier.

#### 7.28.2.2 upgrade()

Implements helib::ConstMultiplier.

#### 7.28.3 Member Data Documentation

#### 7.28.3.1 data

```
zzX helib::ConstMultiplier_zzX::data
```

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.29 helib::ConstMultiplierCache Struct Reference

```
#include <matmul.h>
```

## **Public Member Functions**

• void upgrade (const Context &context)

## **Public Attributes**

std::vector< std::shared\_ptr< ConstMultiplier >> multiplier

## 7.29.1 Member Function Documentation

## 7.29.1.1 upgrade()

### 7.29.2 Member Data Documentation

#### 7.29.2.1 multiplier

std::vector<std::shared\_ptr<ConstMultiplier> > helib::ConstMultiplierCache::multiplier

The documentation for this struct was generated from the following files:

- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

## 7.30 helib::Context Class Reference

Maintaining the parameters.

#include <Context.h>

#### **Public Member Functions**

- double noiseBoundForUniform (double magBound, long degBound) const
- NTL::xdouble noiseBoundForUniform (NTL::xdouble magBound, long degBound) const
- · double noiseBoundForMod (long modulus, long degBound) const
- double noiseBoundForGaussian (double sigma, long degBound) const
- · double noiseBoundForSmall (double prob, long degBound) const
- double noiseBoundForHWt (long hwt, UNUSED long degBound) const
- double stdDevForRecryption (long skHwt=0) const

NOTE: this is a bit heuristic. See design document for details.

- double boundForRecryption (long skHwt=0) const
- void setModSizeTable ()
- Context (unsigned long m, unsigned long p, unsigned long r, const std::vector< long > &gens=std::vector< long > (), const std::vector< long > &ords=std::vector< long > ())
- void makeBootstrappable (const NTL::Vec< long > &mvec, long skWht=0, bool build\_cache=false, bool alsoThick=true)
- · bool isBootstrappable () const
- IndexSet fullPrimes () const
- IndexSet allPrimes () const
- IndexSet getCtxtPrimes (long nprimes) const
- · long BPL () const
- bool operator== (const Context &other) const
- bool operator!= (const Context &other) const
- long ithPrime (unsigned long i) const

The ith small prime in the modulus chain.

· const Cmodulus & ithModulus (unsigned long i) const

Cmodulus object corresponding to ith small prime in the chain.

• long numPrimes () const

Total number of small prime in the chain.

• bool isZeroDivisor (const NTL::ZZ &num) const

Is num divisible by any of the primes in the chain?

· bool inChain (long p) const

Is p already in the chain?

double logOfPrime (unsigned long i) const

Returns the natural logarithm of the ith prime.

double logOfProduct (const IndexSet &s) const

Returns the natural logarithm of productOfPrimes(s)

· double securityLevel () const

An estimate for the security-level.

• void AddSmallPrime (long q)

Just add the given prime to the chain.

- void AddCtxtPrime (long q)
- void AddSpecialPrime (long q)
- void productOfPrimes (NTL::ZZ &p, const IndexSet &s) const

The product of all the primes in the given set.

• NTL::ZZ productOfPrimes (const IndexSet &s) const

#### **Public Attributes**

· PAlgebra zMStar

The structure of Zm\*.

PAlgebraMod alMod

The structure of  $Z[X]/(Phi_m(X),p^{\wedge}r)$ 

• std::shared\_ptr< const EncryptedArray > ea

A default EncryptedArray.

- std::shared\_ptr< const PowerfulDCRT > pwfl\_converter
- std::shared\_ptr< PolyModRing > slotRing

The structure of a single slot of the plaintext space.

NTL::xdouble stdev

sqrt(variance) of the LWE error (default=3.2)

- double scale
- IndexSet ctxtPrimes
- IndexSet specialPrimes
- IndexSet smallPrimes
- ModuliSizes modSizes

A helper table to map required modulo-sizes to primeSets.

std::vector< IndexSet > digits

The set of primes for the digits.

ThinRecryptData rcData

Bootstrapping-related data in the context.

## Friends

- void writeContextBinary (std::ostream &str, const Context &context)
- void readContextBinary (std::istream &str, Context &context)

#### I/O routines

To write out all the data associated with a context, do the following:

```
writeContextBase(str, context);
str « context;
```

The first function call writes out just [m p r gens ords], which is the data needed to invoke the context constructor.

The second call writes out all other information, including the stdev field, the prime sequence (including which primes are "special"), and the digits info.

To read in all the data associated with a context, do the following:

```
unsigned long m, p, r;
std::vector<long> gens, ords;
readContextBase(str, m, p, r, gens, ords);
Context context(m, p, r, gens, ords);
str » context;
```

The call to readContextBase just reads the values m, p, r and the set of generators in Zm\*/(p) and their order. Then, after constructing the context, the >> operator reads in and attaches all other information.

- void writeContextBase (std::ostream &str, const Context &context)
   write [m p r] data
- std::ostream & operator<< (std::ostream &str, const Context &context)

  Write all other data.
- void readContextBase (std::istream &str, unsigned long &m, unsigned long &p, unsigned long &r, std
   ::vector < long > &gens, std::vector < long > &ords)

read [m p r] data, needed to construct context

std::istream & operator>> (std::istream &str, Context &context)

read all other data associated with context

## 7.30.1 Detailed Description

Maintaining the parameters.

#### 7.30.2 Constructor & Destructor Documentation

#### 7.30.2.1 Context()

```
helib::Context::Context (
        unsigned long m,
        unsigned long p,
        unsigned long r,
        const std::vector< long > & gens = std::vector<long>(),
        const std::vector< long > & ords = std::vector<long>() )
```

## 7.30.3 Member Function Documentation

#### 7.30.3.1 AddCtxtPrime()

## 7.30.3.2 AddSmallPrime()

```
void helib::Context::AddSmallPrime ( long q)
```

Just add the given prime to the chain.

### 7.30.3.3 AddSpecialPrime()

```
void helib::Context::AddSpecialPrime ( \log \ q \ )
```

## 7.30.3.4 allPrimes()

```
IndexSet helib::Context::allPrimes ( ) const [inline]
```

## 7.30.3.5 boundForRecryption()

```
double helib::Context::boundForRecryption ( long \ skHwt \ = \ 0 \ ) \ const \ [inline]
```

## 7.30.3.6 BPL()

```
long helib::Context::BPL ( ) const [inline]
```

## 7.30.3.7 fullPrimes()

```
IndexSet helib::Context::fullPrimes ( ) const [inline]
```

### 7.30.3.8 getCtxtPrimes()

## 7.30.3.9 inChain()

Is p already in the chain?

#### 7.30.3.10 isBootstrappable()

```
bool helib::Context::isBootstrappable ( ) const [inline]
```

#### 7.30.3.11 isZeroDivisor()

Is num divisible by any of the primes in the chain?

### 7.30.3.12 ithModulus()

```
\begin{tabular}{ll} \begin{tabular}{ll} const $C modulus \& helib::Context::ithModulus ( \\ & unsigned long $i$ ) const [inline] \end{tabular}
```

Cmodulus object corresponding to ith small prime in the chain.

## 7.30.3.13 ithPrime()

The ith small prime in the modulus chain.

## 7.30.3.14 logOfPrime()

Returns the natural logarithm of the ith prime.

### 7.30.3.15 logOfProduct()

Returns the natural logarithm of productOfPrimes(s)

#### 7.30.3.16 makeBootstrappable()

#### 7.30.3.17 noiseBoundForGaussian()

Assume the polynomial  $f(x) = sum_{i} < k$   $f_i x^i$  is chosen so that each  $f_i$  is chosen uniformly and independently from N(0, sigma^2), and that k = degBound. This returns a bound B such that the L-infty norm of the canonical embedding exceeds B with probability at most epsilon.

### 7.30.3.18 noiseBoundForHWt()

Assume the polynomial  $f(x) = sum_{i} = sum_{$ 

#### 7.30.3.19 noiseBoundForMod()

Assume the polynomial  $f(x) = sum_{i} < k$   $f_i x^i$  is chosen so that each  $f_i$  is chosen uniformly and independently from the from the set of balanced residues modulo the given modulus. This returns a bound B such that the L-infty norm of the canonical embedding exceeds B with probability at most epsilon.

### 7.30.3.20 noiseBoundForSmall()

Assume the polynomial  $f(x) = sum_{i} < k$   $f_i x^i$  is chosen so that each  $f_i$  is zero with probability 1-prob, 1 with probability prob/2, and -1 with probability prob/2. This returns a bound B such that the L-infty norm of the canonical embedding exceeds B with probability at most epsilon.

#### 7.30.3.21 noiseBoundForUniform() [1/2]

erfc(scale/sqrt(2)) \* phi(m) should be less than some negligible parameter epsilon. The default value of 10 should be good enough for most applications. NOTE:  $-\log(\text{erfc}(8/\text{sqrt}(2)))/\log(2) = 49.5 -\log(\text{erfc}(10/\text{sqrt}(2)))/\log(2) = 75.$  8  $-\log(\text{erfc}(11/\text{sqrt}(2)))/\log(2) = 91.1 -\log(\text{erfc}(12/\text{sqrt}(2)))/\log(2) = 107.8$  The way this is used is as follows. If we have a normal random variable X with variance  $\operatorname{sigma}^2$ , then the probability that that X lies outside the interval [-scale\*sigma, scale\*sigma] is  $\operatorname{delta}=\operatorname{erfc}(\operatorname{scale/sqrt}(2))$ . We will usually apply the union bound to a vector of phi(m) such random variables (one for each primitive m-th root of unity), so that the probability that that the L-infty norm exceeds scale\*sigma is at most epsilon=phim\*delta. Thus, scale\*sigma will be used as a high-probability bound on the L-infty norm of such vectors. Assume the polynomial  $f(x) = \sup_{i=1}^{\infty} i \le i$  is chosen so that each  $f_i$  is chosen uniformly and independently from the interval [-magBound, magBound], and that  $k = \deg Bound$ . This returns a bound B such that the L-infty norm of the canonical embedding exceeds B with probability at most epsilon.

#### 7.30.3.22 noiseBoundForUniform() [2/2]

#### 7.30.3.23 numPrimes()

```
long helib::Context::numPrimes ( ) const [inline]
```

Total number of small prime in the chain.

#### 7.30.3.24 operator"!=()

#### 7.30.3.25 operator==()

```
bool helib::Context::operator== (
    const Context & other ) const
```

#### 7.30.3.26 productOfPrimes() [1/2]

### 7.30.3.27 productOfPrimes() [2/2]

The product of all the primes in the given set.

## 7.30.3.28 securityLevel()

```
double helib::Context::securityLevel ( ) const [inline]
```

An estimate for the security-level.

### 7.30.3.29 setModSizeTable()

```
void helib::Context::setModSizeTable ( ) [inline]
```

### 7.30.3.30 stdDevForRecryption()

```
double helib::Context::stdDevForRecryption ( long skHwt = 0 ) const [inline]
```

NOTE: this is a bit heuristic. See design document for details.

This computes a high probability bound on the L-infty norm of x0+s\*x1 in the pwrfl basis, assuming is chosen with coeffs in the pwrfl basis uniformly and independently dist'd over [-1/2,1/2], x0 has arbitrary coeffs over [-1/2,1/2] in the pwrfl basis, and assuming s is chosen with skHwt nonzero coeffs mod  $X^m-1$  in the power basis (uniformly and independently over  $\{-1,1\}$ ). The bound should be satisfied with probability epsilon. NOTE: this is still valid even when m is a power of 2

## 7.30.4 Friends And Related Function Documentation

### 7.30.4.1 operator <<

Write all other data.

### 7.30.4.2 operator>>

```
std::istream& operator>> (
          std::istream & str,
          Context & context ) [friend]
```

read all other data associated with context

#### 7.30.4.3 readContextBase

```
void readContextBase (
    std::istream & str,
    unsigned long & m,
    unsigned long & p,
    unsigned long & r,
    std::vector< long > & gens,
    std::vector< long > & ords ) [friend]
```

read [m p r] data, needed to construct context

### 7.30.4.4 readContextBinary

#### 7.30.4.5 writeContextBase

```
void writeContextBase (
          std::ostream & str,
          const Context & context ) [friend]
```

write [m p r] data

#### 7.30.4.6 writeContextBinary

### 7.30.5 Member Data Documentation

#### 7.30.5.1 alMod

```
PAlgebraMod helib::Context::alMod
```

The structure of  $Z[X]/(Phi_m(X),p^r)$ 

#### 7.30.5.2 ctxtPrimes

```
IndexSet helib::Context::ctxtPrimes
```

The "ciphertext primes" are the "normal" primes that are used to represent the public encryption key and ciphertexts. These are all "large" single=precision primes, or bit-size roughly NTL\_SP\_SIZE bits.

### 7.30.5.3 digits

```
std::vector<IndexSet> helib::Context::digits
```

The set of primes for the digits.

The different columns in any key-switching matrix contain encryptions of multiplies of the secret key, sk, B1\*sk, B2\*B1\*sk, B3\*B2\*B1\*sk,... with each Bi a product of a few "non-special" primes in the chain. The digits data member indicate which primes correspond to each of the Bi's. These are all IndexSet objects, whose union is the subset ctxtPrimes.

The number of Bi's is one less than the number of columns in the key switching matrices (since the 1st column encrypts sk, without any Bi's), but we keep in the digits std::vector also an entry for the primes that do not participate in any Bi (so digits.size() is the same as the number of columns in the key switching matrices). See section 3.1.6 in the design document (key-switching).

## 7.30.5.4 ea

std::shared\_ptr<const EncryptedArray> helib::Context::ea

A default EncryptedArray.

### 7.30.5.5 modSizes

ModuliSizes helib::Context::modSizes

A helper table to map required modulo-sizes to primeSets.

## 7.30.5.6 pwfl\_converter

std::shared\_ptr<const PowerfulDCRT> helib::Context::pwfl\_converter

### 7.30.5.7 rcData

ThinRecryptData helib::Context::rcData

Bootstrapping-related data in the context.

### 7.30.5.8 scale

double helib::Context::scale

## 7.30.5.9 slotRing

std::shared\_ptr<PolyModRing> helib::Context::slotRing

The structure of a single slot of the plaintext space.

This will be  $Z[X]/(G(x),p^{\wedge}r)$  for some irreducible factor G of Phi\_m(X).

#### 7.30.5.10 smallPrimes

```
IndexSet helib::Context::smallPrimes
```

Yet a third set of primes, aimed at allowing modulus-switching with higher resolution. These are somewhat smaller single-precision primes, of size from NTL\_SP\_SIZE-20 to NTL\_SP\_SIZE-1.

#### 7.30.5.11 specialPrimes

```
IndexSet helib::Context::specialPrimes
```

A disjoint set of primes, used for key switching. See section 3.1.6 in the design document (key-switching). These too are "large" single=precision primes, or bit-size close to NTL\_SP\_SIZE bits.

### 7.30.5.12 stdev

NTL::xdouble helib::Context::stdev

sqrt(variance) of the LWE error (default=3.2)

#### 7.30.5.13 zMStar

PAlgebra helib::Context::zMStar

The structure of Zm\*.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Context.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Context.cpp
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/primeChain.cpp

## 7.31 helib::Ctxt Class Reference

A Ctxt object holds a single ciphertext.

#include <Ctxt.h>

#### **Public Member Functions**

- Ctxt (const PubKey &newPubKey, long newPtxtSpace=0)
- Ctxt (const Ctxt &other)=default
- Ctxt (ZeroCtxtLike\_type, const Ctxt &ctxt)
- void DummyEncrypt (const NTL::ZZX &ptxt, double size=-1.0)
- Ctxt & operator= (const Ctxt & other)
- bool operator== (const Ctxt &other) const
- bool operator!= (const Ctxt &other) const
- bool equalsTo (const Ctxt &other, bool comparePkeys=true) const
- · void write (std::ostream &str) const
- void read (std::istream &str)

#### Ciphertext arithmetic

```
• void negate ()
```

- Ctxt & operator+= (const Ctxt & other)
- Ctxt & operator-= (const Ctxt & other)
- void addCtxt (const Ctxt &other, bool negative=false)
- void multLowLvl (const Ctxt &other, bool destructive=false)
- Ctxt & operator\*= (const Ctxt &other)
- void automorph (long k)
- Ctxt & operator>>= (long k)
- void complexConj ()
- void smartAutomorph (long k)

automorphism with re-linearization

· void frobeniusAutomorph (long j)

applies the automorphism  $p^{\wedge}j$  using smartAutomorphism

Ctxt & operator+= (const Ptxt< BGV > &other)

Plus equals operator with a BGV Ptxt.

Ctxt & operator-= (const Ptxt < BGV > &other)

Minus equals operator with a BGV Ptxt.

Ctxt & operator\*= (const Ptxt< BGV > &other)

Times equals operator with a BGV Ptxt.

Ctxt & operator+= (const Ptxt< CKKS > &other)

Plus equals operator with a CKKS Ptxt.

Ctxt & operator= (const Ptxt< CKKS > &other)

Minus equals operator with a CKKS Ptxt.

Ctxt & operator\*= (const Ptxt< CKKS > &other)

Times equals operator with a CKKS Ptxt.

Ctxt & operator\*= (const NTL::ZZX &poly)

Times equals operator with a ZZX.

• Ctxt & operator\*= (const long scalar)

Times equals operator with a long.

- void addConstant (const DoubleCRT &dcrt, double size=-1.0)
- void addConstant (const NTL::ZZX &poly, double size=-1.0)
- $\bullet \ \ \text{template}{<} \text{typename Scheme} >$

void addConstant (const Ptxt< Scheme > &ptxt)

Add a BGV plaintext to this Ctxt.

- void addConstant (const NTL::ZZ &c)
- void addConstantCKKS (std::pair< long, long >)

add a rational number in the form a/b, a,b are long

- void addConstantCKKS (double x)
- void addConstantCKKS (const DoubleCRT &dcrt, NTL::xdouble size=NTL::xdouble(-1.0), NTL::xdouble factor=NTL::xdouble(-1.0))
- void addConstantCKKS (const NTL::ZZX &poly, NTL::xdouble size=NTL::xdouble(-1.0), NTL::xdouble factor=NTL::xdouble(-1.0))
- void addConstantCKKS (const std::vector< std::complex< double >> &ptxt)
- void addConstantCKKS (const Ptxt< CKKS > &ptxt)

Add a CKKS plaintext to this Ctxt. void addConstantCKKS (const NTL::ZZ &c) void multByConstant (const DoubleCRT &dcrt, double size=-1.0) void multByConstant (const NTL::ZZX &poly, double size=-1.0) void multByConstant (const zzX &poly, double size=-1.0) void multByConstant (const NTL::ZZ &c) template<typename Scheme > void multByConstant (const Ptxt< Scheme > &ptxt) Multiply a BGV plaintext to this Ctxt. void multByConstantCKKS (double x) multiply by a rational number or floating point void multByConstantCKKS (std::pair< long, long > num) void multByConstantCKKS (const DoubleCRT &dcrt, NTL::xdouble size=NTL::xdouble(-1.0), NTL::xdouble factor=NTL::xdouble(-1.0), double roundingErr=-1.0) void multByConstantCKKS (const NTL::ZZX &poly, NTL::xdouble size=NTL::xdouble(-1.0), NTL::xdouble factor=NTL::xdouble(-1.0), double roundingErr=-1.0) void multByConstantCKKS (const Ptxt< CKKS > &ptxt) Multiply a CKKS plaintext to this Ctxt. void multByConstantCKKS (const std::vector< std::complex< double >> &ptxt) void xorConstant (const DoubleCRT &poly, UNUSED double size=-1.0) void xorConstant (const NTL::ZZX &poly, double size=-1.0) void nxorConstant (const DoubleCRT &poly, UNUSED double size=-1.0) void nxorConstant (const NTL::ZZX &poly, double size=-1.0) void divideByP () void multByP (long e=1) void divideBy2 () void extractBits (std::vector < Ctxt > &bits, long nBits2extract=0) void multiplyBy (const Ctxt &other) void multiplyBy2 (const Ctxt &other1, const Ctxt &other2) • void square ()

#### Ciphertext maintenance

void cube ()void power (long e)

void reducePtxtSpace (long newPtxtSpace)

Reduce plaintext space to a divisor of the original plaintext space.

- void hackPtxtSpace (long newPtxtSpace)
- void bumpNoiseBound (double factor)

raise ciphertext to some power

- void reLinearize (long keyldx=0)
- void cleanUp ()
- void blindCtxt (const NTL::ZZX &poly)

Add a high-noise encryption of the given constant.

NTL::xdouble modSwitchAddedNoiseBound () const

Estimate the added noise.

void modUpToSet (const IndexSet &s)

Modulus-switching up (to a larger modulus). Must have primeSet <= s, and s must contain either all the special primes or none of them.

void modDownToSet (const IndexSet &s)

Modulus-switching down (to a smaller modulus). mod-switch down to primeSet \intersect s, after this call we have primeSet <=s. s must contain either all special primes or none of them.

void bringToSet (const IndexSet &s)

make the primeSet equal to newPrimeSet, via modUpToSet and modDownToSet

- double naturalSize () const
- IndexSet naturalPrimeSet () const

"natural size" is size before squaring

void dropSmallAndSpecialPrimes ()

the corresponding primeSet

double capacity () const

returns the "capacity" of a ciphertext, which is the log of the ratio of the modulus to the noise bound

- long bitCapacity () const
  - the capacity in bits, returned as an integer
- double logOfPrimeSet () const
  - returns the log of the prime set
- double rawModSwitch (std::vector < NTL::ZZX > &zzParts, long toModulus) const
  - Special-purpose modulus-switching for bootstrapping.
- void evalPoly (const NTL::ZZX &poly)
  - compute the power  $X, X^{\wedge}2, ..., X^{\wedge}n$

### **Utility methods**

- · void clear ()
- bool isEmpty () const

Is this an empty ciphertext without any parts.

bool inCanonicalForm (long keyID=0) const

A canonical ciphertext has (at most) handles pointing to (1.s)

bool isCorrect () const

Would this ciphertext be decrypted without errors?

- const Context & getContext () const
- const PubKey & getPubKey () const
- const IndexSet & getPrimeSet () const
- long getPtxtSpace () const
- const NTL::xdouble & getNoiseBound () const
- const NTL::xdouble & getRatFactor () const
- const NTL::xdouble & getPtxtMag () const
- void setPtxtMag (const NTL::xdouble &z)
- long getKeyID () const
- bool isCKKS () const
- · long effectiveR () const
- double log\_of\_ratio () const

Returns log(noiseBound) - log(q)

#### **Static Public Member Functions**

• static void equalizeRationalFactors (Ctxt &c1, Ctxt &c2)

#### **Friends**

- class PubKey
- · class SecKey
- · class BasicAutomorphPrecon
- std::istream & operator>> (std::istream &str, Ctxt &ctxt)
- std::ostream & operator<< (std::ostream &str, const Ctxt &ctxt)</li>

## 7.31.1 Detailed Description

A Ctxt object holds a single ciphertext.

The class Ctxt includes a std::vector<CtxtPart>: For a Ctxt c, c[i] is the i'th ciphertext part, which can be used also as a DoubleCRT object (since CtxtPart is derived from DoubleCRT). By convention, c[0], the first CtxtPart object in the std::vector, has skHndl that points to 1 (i.e., it is just added in upon decryption, without being multiplied by anything). We maintain the invariance that all the parts of a ciphertext are defined relative to the same set of primes.

A ciphertext contains also pointers to the general parameters of this FHE instance and the public key, and a high-probability bound on the noise magnitude (kept in the noiseBound data member). The noise bound is a bound on the l-infinity norm of the canonical embedding of the noise polynomial, namely its evaluation in roots of the ring polynomial (which are the complex primitive roots of unity). The noise bound is added on addition, multiplied on multiplications, remains unchanged for automorphism, and is roughly scaled down by mod-switching with some added factor, and similarly scaled up by key-switching with some added factor.

### 7.31.2 Constructor & Destructor Documentation

## 7.31.2.1 Ctxt() [1/3]

### 7.31.2.2 Ctxt() [2/3]

## 7.31.2.3 Ctxt() [3/3]

## 7.31.3 Member Function Documentation

## 7.31.3.1 addConstant() [1/4]

Add a constant polynomial. If provided, size should be a high-probability bound on the L-infty norm of the canonical embedding Otherwise, for the DoubleCRT variant, a bound based on the assumption that the coefficients are uniformly and independently distributed over [-ptxtSpace/2, ptxtSpace/2]. For the other variants, explicit bounds are computed (if not CKKS).

### 7.31.3.2 addConstant() [2/4]

```
void helib::Ctxt::addConstant ( const NTL::ZZ & c )
```

### 7.31.3.3 addConstant() [3/4]

### 7.31.3.4 addConstant() [4/4]

## Add a BGV plaintext to this Ctxt.

#### **Parameters**

| ptxt | Plaintext |
|------|-----------|
|      | Ptxt      |
|      | object    |
|      | with      |
|      | which     |
|      | to add.   |

### 7.31.3.5 addConstantCKKS() [1/7]

## 7.31.3.6 addConstantCKKS() [2/7]

```
void helib::Ctxt::addConstantCKKS ( const NTL::ZZ & c )
```

### 7.31.3.7 addConstantCKKS() [3/7]

## 7.31.3.8 addConstantCKKS() [4/7]

```
void helib::Ctxt::addConstantCKKS ( {\tt const\ Ptxt} < {\tt CKKS} \ > \& \ ptxt \ )
```

Add a CKKS plaintext to this Ctxt.

### **Parameters**

| ptxt | Plaintext |
|------|-----------|
|      | Ptxt      |
|      | object    |
|      | with      |
|      | which     |
|      | to add.   |

## 7.31.3.9 addConstantCKKS() [5/7]

```
void helib::Ctxt::addConstantCKKS ( {\tt const \ std::vector< \ std::complex< \ double >> \& \ ptxt \ )}
```

### 7.31.3.10 addConstantCKKS() [6/7]

## 7.31.3.11 addConstantCKKS() [7/7]

```
void helib::Ctxt::addConstantCKKS ( {\tt std::pair} < {\tt long, long} > {\tt num} \ )
```

add a rational number in the form a/b, a,b are long

## 7.31.3.12 addCtxt()

## 7.31.3.13 automorph()

```
void helib::Ctxt::automorph ( \log \ k \ )
```

### 7.31.3.14 bitCapacity()

```
long helib::Ctxt::bitCapacity ( ) const [inline]
```

the capacity in bits, returned as an integer

### 7.31.3.15 blindCtxt()

Add a high-noise encryption of the given constant.

## 7.31.3.16 bringToSet()

make the primeSet equal to newPrimeSet, via modUpToSet and modDownToSet

## 7.31.3.17 bumpNoiseBound()

## 7.31.3.18 capacity()

```
double helib::Ctxt::capacity ( ) const [inline]
```

returns the "capacity" of a ciphertext, which is the log of the ratio of the modulus to the noise bound

### 7.31.3.19 cleanUp()

```
void helib::Ctxt::cleanUp ( )
```

### 7.31.3.20 clear()

```
void helib::Ctxt::clear ( ) [inline]
```

### 7.31.3.21 complexConj()

```
void helib::Ctxt::complexConj ( )
```

#### 7.31.3.22 cube()

```
void helib::Ctxt::cube ( ) [inline]
```

#### 7.31.3.23 divideBy2()

```
void helib::Ctxt::divideBy2 ( )
```

### 7.31.3.24 divideByP()

```
void helib::Ctxt::divideByP ( )
```

Divide a ciphertext by p, for plaintext space  $p^r$ , r>1. It is assumed that the ciphertext encrypts a polynomial which is zero mod p. If this is not the case then the result will not be a valid ciphertext anymore. As a side-effect, the plaintext space is reduced from  $p^r$  to  $p^r$  to  $p^r$  to  $p^r$ .

### 7.31.3.25 dropSmallAndSpecialPrimes()

```
void helib::Ctxt::dropSmallAndSpecialPrimes ( )
```

the corresponding primeSet

drop all smallPrimes and specialPrimes, adding ctxtPrimes as necessary to ensure that the scaled noise is above the modulus-switching added noise term.

### 7.31.3.26 DummyEncrypt()

Dummy encryption, just encodes the plaintext in a Ctxt object If provided, size should be a high-probability bound on the L-infty norm of the canonical embedding

### 7.31.3.27 effectiveR()

```
long helib::Ctxt::effectiveR ( ) const [inline]
```

### 7.31.3.28 equalizeRationalFactors()

### 7.31.3.29 equalsTo()

### 7.31.3.30 evalPoly()

compute the power  $X, X^{\hat{}}2,...,X^{\hat{}}n$ 

Evaluate the cleartext poly on the encrypted ciphertext

### 7.31.3.31 extractBits()

### 7.31.3.32 frobeniusAutomorph()

```
void helib::Ctxt::frobeniusAutomorph ( \log \ j \ )
```

applies the automorphism  $p^{\wedge}j$  using smartAutomorphism

## 7.31.3.33 getContext()

```
const Context& helib::Ctxt::getContext ( ) const [inline]
```

## 7.31.3.34 getKeyID()

```
long helib::Ctxt::getKeyID ( ) const
```

#### 7.31.3.35 getNoiseBound()

```
const NTL::xdouble& helib::Ctxt::getNoiseBound ( ) const [inline]
```

## 7.31.3.36 getPrimeSet()

```
const IndexSet& helib::Ctxt::getPrimeSet ( ) const [inline]
```

## 7.31.3.37 getPtxtMag()

```
const NTL::xdouble& helib::Ctxt::getPtxtMag ( ) const [inline]
```

## 7.31.3.38 getPtxtSpace()

```
long helib::Ctxt::getPtxtSpace ( ) const [inline]
```

### 7.31.3.39 getPubKey()

```
const PubKey& helib::Ctxt::getPubKey ( ) const [inline]
```

# 7.31.3.40 getRatFactor()

```
const NTL::xdouble& helib::Ctxt::getRatFactor ( ) const [inline]
```

# 7.31.3.41 hackPtxtSpace()

#### 7.31.3.42 inCanonicalForm()

```
bool helib::Ctxt::inCanonicalForm ( long \ keyID = 0 \ ) \ const \ [inline]
```

A canonical ciphertext has (at most) handles pointing to (1,s)

### 7.31.3.43 isCKKS()

```
bool helib::Ctxt::isCKKS ( ) const [inline]
```

### 7.31.3.44 isCorrect()

```
bool helib::Ctxt::isCorrect ( ) const [inline]
```

Would this ciphertext be decrypted without errors?

### 7.31.3.45 isEmpty()

```
bool helib::Ctxt::isEmpty ( ) const [inline]
```

Is this an empty ciphertext without any parts.

#### 7.31.3.46 log\_of\_ratio()

```
double helib::Ctxt::log_of_ratio ( ) const [inline]
```

Returns log(noiseBound) - log(q)

# 7.31.3.47 logOfPrimeSet()

```
double helib::Ctxt::logOfPrimeSet ( ) const [inline]
```

returns the log of the prime set

#### 7.31.3.48 modDownToSet()

Modulus-switching down (to a smaller modulus). mod-switch down to primeSet \intersect s, after this call we have primeSet<=s. s must contain either all special primes or none of them.

### 7.31.3.49 modSwitchAddedNoiseBound()

```
NTL::xdouble helib::Ctxt::modSwitchAddedNoiseBound ( ) const
```

Estimate the added noise.

### 7.31.3.50 modUpToSet()

Modulus-switching up (to a larger modulus). Must have primeSet  $\leq$ = s, and s must contain either all the special primes or none of them.

### 7.31.3.51 multByConstant() [1/5]

Multiply-by-constant. If the size is not given, for the DCRT variant, we use a high probability bound assuming "random" coefficients mod ptxtSpace, while for the other variants, we use explicitly computed bounds (if not CKKS).

# 7.31.3.52 multByConstant() [2/5]

```
void helib::Ctxt::multByConstant ( {\tt const~NTL::ZZ~\&~C~)}
```

# 7.31.3.53 multByConstant() [3/5]

# 7.31.3.54 multByConstant() [4/5]

Multiply a BGV plaintext to this Ctxt.

#### **Parameters**

| ptxt | Plaintext |
|------|-----------|
|      | Ptxt      |
|      | object    |
|      | with      |
|      | which     |
|      | to mul-   |
|      | tiply.    |

# 7.31.3.55 multByConstant() [5/5]

# 7.31.3.56 multByConstantCKKS() [1/6]

# 7.31.3.57 multByConstantCKKS() [2/6]

### 7.31.3.58 multByConstantCKKS() [3/6]

```
void helib::Ctxt::multByConstantCKKS ( {\tt const\ Ptxt} < {\tt CKKS} \ > \& \ ptxt \ )
```

Multiply a CKKS plaintext to this Ctxt.

#### **Parameters**

| ptxt | Plaintext |
|------|-----------|
|      | Ptxt      |
|      | object    |
|      | poly-     |
|      | nomial    |
|      | with      |
|      | which     |
|      | to mul-   |
|      | tiply.    |

### 7.31.3.59 multByConstantCKKS() [4/6]

# 7.31.3.60 multByConstantCKKS() [5/6]

```
\begin{tabular}{ll} \beg
```

multiply by a rational number or floating point

# 7.31.3.61 multByConstantCKKS() [6/6]

# 7.31.3.62 multByP()

Multiply ciphertext by  $p^e$ , for plaintext space  $p^r$ . This also has the side-effect of increasing the plaintext space to  $p^f$ r+e.

### 7.31.3.63 multiplyBy()

# 7.31.3.64 multiplyBy2()

# 7.31.3.65 multLowLvI()

# 7.31.3.66 naturalPrimeSet()

```
IndexSet helib::Ctxt::naturalPrimeSet ( ) const
```

"natural size" is size before squaring

#### 7.31.3.67 naturalSize()

```
double helib::Ctxt::naturalSize ( ) const
```

# 7.31.3.68 negate()

```
void helib::Ctxt::negate ( )
```

# 7.31.3.69 nxorConstant() [1/2]

# 7.31.3.70 nxorConstant() [2/2]

# 7.31.3.71 operator"!=()

```
bool helib::Ctxt::operator!= (
     const Ctxt & other ) const [inline]
```

# 7.31.3.72 operator\*=() [1/5]

# 7.31.3.73 operator\*=() [2/5]

Times equals operator with a long.

### **Parameters**

| scalar | Constant |
|--------|----------|
|        | by       |
|        | which    |
|        | to mul-  |
|        | tiply.   |

# Returns

Reference to \*this post multiplication.

# 7.31.3.74 operator\*=() [3/5]

Times equals operator with a  $\mbox{ZZX}.$ 

#### **Parameters**

| poly | Element |
|------|---------|
|      | by      |
|      | which   |
|      | to mul- |
|      | tiply.  |

# Returns

Reference to \*this post multiplication.

# 7.31.3.75 operator\*=() [4/5]

```
Ctxt & helib::Ctxt::operator*= (  \mbox{const Ptxt} < \mbox{BGV} > \mbox{\& other} \mbox{ )}
```

Times equals operator with a BGV Ptxt.

| other | Right   |
|-------|---------|
|       | hand    |
|       | side of |
|       | multi-  |
|       | plica-  |
|       | tion.   |

#### Returns

reference to \*this post multiplication.

# 7.31.3.76 operator\*=() [5/5]

Times equals operator with a CKKS Ptxt.

#### **Parameters**

| other | Right   |
|-------|---------|
|       | hand    |
|       | side of |
|       | multi-  |
|       | plica-  |
|       | tion.   |

### Returns

Reference to \*this post multiplication.

# 7.31.3.77 operator+=() [1/3]

# 7.31.3.78 operator+=() [2/3]

```
Ctxt & helib::Ctxt::operator+= (  \mbox{const Ptxt} < \mbox{BGV} > \mbox{\& other} \mbox{ )}
```

Plus equals operator with a BGV Ptxt.

| other | Right   |
|-------|---------|
|       | hand    |
|       | side of |
|       | addi-   |
|       | tion.   |

#### Returns

Reference to \*this post addition.

# 7.31.3.79 operator+=() [3/3]

Plus equals operator with a CKKS Ptxt.

#### **Parameters**

| other | Right   |
|-------|---------|
|       | hand    |
|       | side of |
|       | addi-   |
|       | tion.   |

#### Returns

Reference to \*this post addition.

# 7.31.3.80 operator-=() [1/3]

# 7.31.3.81 operator-=() [2/3]

Minus equals operator with a BGV Ptxt.

| i di dilicto | 13      |
|--------------|---------|
| other        | Right   |
|              | hand    |
|              | side of |
|              | sub-    |
|              | trac-   |
|              | tion.   |

#### Returns

Reference to \*this post subtraction.

# 7.31.3.82 operator-=() [3/3]

Minus equals operator with a CKKS Ptxt.

#### **Parameters**

| other | Right   |
|-------|---------|
|       | hand    |
|       | side of |
|       | sub-    |
|       | trac-   |
|       | tion.   |

### Returns

Reference to \*this post subtraction.

# 7.31.3.83 operator=()

# 7.31.3.84 operator==()

### 7.31.3.85 operator>>=()

```
Ctxt& helib::Ctxt::operator>>= (
    long k ) [inline]
```

#### 7.31.3.86 power()

raise ciphertext to some power

### 7.31.3.87 rawModSwitch()

Special-purpose modulus-switching for bootstrapping.

Mod-switch to an externally-supplied modulus. The modulus need not be in the moduli-chain in the context, and does not even need to be a prime. The ciphertext \*this is not affected, instead the result is returned in the zzParts std::vector, as a std::vector of ZZX'es. Returns an estimate for the scaled noise (not including the additive mod switching noise)

### 7.31.3.88 read()

#### 7.31.3.89 reducePtxtSpace()

Reduce plaintext space to a divisor of the original plaintext space.

### 7.31.3.90 reLinearize()

#### 7.31.3.91 setPtxtMag()

# 7.31.3.92 smartAutomorph()

```
void helib::Ctxt::smartAutomorph ( long k )
```

automorphism with re-linearization

### 7.31.3.93 square()

```
void helib::Ctxt::square ( ) [inline]
```

### 7.31.3.94 write()

```
void helib::Ctxt::write ( {\tt std::ostream~\&~str~)~const}
```

#### 7.31.3.95 xorConstant() [1/2]

Convenience method: XOR and nXOR with arbitrary plaintext space: a xor b = a+b-2ab = a + (1-2a)\*b, a nxor b = 1-a-b+2ab = (b-1)(2a-1)+a

#### 7.31.3.96 xorConstant() [2/2]

### 7.31.4 Friends And Related Function Documentation

### 7.31.4.1 BasicAutomorphPrecon

```
friend class BasicAutomorphPrecon [friend]
```

#### 7.31.4.2 operator <<

```
std::ostream& operator<< (
          std::ostream & str,
          const Ctxt & ctxt ) [friend]</pre>
```

# 7.31.4.3 operator>>

### 7.31.4.4 PubKey

```
friend class PubKey [friend]
```

#### 7.31.4.5 SecKey

```
friend class SecKey [friend]
```

The documentation for this class was generated from the following files:

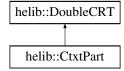
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ctxt.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Ctxt.cpp
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/polyEval.cpp

# 7.32 helib::CtxtPart Class Reference

One entry in a ciphertext std::vector.

```
#include <Ctxt.h>
```

Inheritance diagram for helib::CtxtPart:



### **Public Member Functions**

- bool operator== (const CtxtPart &other) const
- bool operator!= (const CtxtPart &other) const
- CtxtPart (const Context &\_context, const IndexSet &s)
- CtxtPart (const Context &\_context, const IndexSet &s, const SKHandle &otherHandle)
- CtxtPart (const DoubleCRT &other)
- CtxtPart (const DoubleCRT & other, const SKHandle & otherHandle)
- void read (std::istream &str)
- void write (std::ostream &str) const

### **Public Attributes**

· SKHandle skHandle

The handle is a public data member.

# 7.32.1 Detailed Description

One entry in a ciphertext std::vector.

A ciphertext part consists of a polynomial (element of the ring R\_Q) and a handle to the corresponding secret-key polynomial.

### 7.32.2 Constructor & Destructor Documentation

### 7.32.2.1 CtxtPart() [1/4]

### 7.32.2.2 CtxtPart() [2/4]

### 7.32.2.3 CtxtPart() [3/4]

# 7.32.2.4 CtxtPart() [4/4]

### 7.32.3 Member Function Documentation

# 7.32.3.1 operator"!=()

# 7.32.3.2 operator==()

#### 7.32.3.3 read()

# 7.32.3.4 write()

# 7.32.4 Member Data Documentation

#### 7.32.4.1 skHandle

SKHandle helib::CtxtPart::skHandle

The handle is a public data member.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ctxt.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Ctxt.cpp

# 7.33 helib::CubeSignature Class Reference

Holds a vector of dimensions for a hypercube and some additional data.

#include <hypercube.h>

#### **Public Member Functions**

- CubeSignature ()
- void initSignature (const long \_dims[], long \_ndims)
- template<typename VecType > void initSignature (const VecType &\_dims)
- CubeSignature (const long dims[], long ndims)
- CubeSignature (const NTL::Vec< long > &\_dims)
- CubeSignature (const std::vector< long > &\_dims)
- long getNumDims () const

number of dimensions

· long getSize () const

total size of cube

• long getDim (long d) const

size of dimension d

• long getProd (long d) const

product of sizes of dimensions d, d+1, ...

• long getProd (long from, long to) const

product of sizes of dimensions from, from+1, ..., to-1

• long getCoord (long i, long d) const

get coordinate in dimension d of index i

long addCoord (long i, long d, long offset) const

add offset to coordinate in dimension d of index i

template<typename VecType >

bool incrementCoords (VecType &v) const

• template<typename VecType>

void getAllCoords (VecType &v, long i) const

• template<typename VecType >

long assembleCoords (VecType &v) const

• long numSlices (long d=1) const

number of slices

long sliceSize (long d=1) const

size of one slice

• long numCols () const

number of columns

- std::pair< long, long > breakIndexByDim (long idx, long dim) const
- long assembleIndexByDim (std::pair< long, long > idx, long dim) const

The inverse of breakIndexByDim.

### **Friends**

• std::ostream & operator<< (std::ostream &s, const CubeSignature &sig)

# 7.33.1 Detailed Description

Holds a vector of dimensions for a hypercube and some additional data.

### 7.33.2 Constructor & Destructor Documentation

### 7.33.2.1 CubeSignature() [1/4]

```
helib::CubeSignature::CubeSignature ( ) [inline]
```

### 7.33.2.2 CubeSignature() [2/4]

# 7.33.2.3 CubeSignature() [3/4]

```
helib::CubeSignature::CubeSignature ( {\tt const\ NTL::Vec<\ long\ >\ \&\ \_dims\ )} \quad [inline]
```

### 7.33.2.4 CubeSignature() [4/4]

# 7.33.3 Member Function Documentation

### 7.33.3.1 addCoord()

add offset to coordinate in dimension d of index i

#### 7.33.3.2 assembleCoords()

reconstruct index from its coordinates VecType is either std::vector<intType> or NTL:Vec<intType>

#### 7.33.3.3 assembleIndexByDim()

```
long helib::CubeSignature::assembleIndexByDim ( {\tt std::pair} < {\tt long, \ long} > idx, \\ {\tt long \ } dim \ ) \ {\tt const}
```

The inverse of breakIndexByDim.

### 7.33.3.4 breakIndexByDim()

Break an index into the hypercube to index of the dimension-dim subcube and index inside that subcube.

# 7.33.3.5 getAllCoords()

```
template<typename VecType > void helib::CubeSignature::getAllCoords ( \mbox{VecType \& } v, \\ \mbox{long } i \mbox{ ) const [inline]}
```

get the coordinates of index i in all dimensions. VecType is either std::vector<intType> or NTL:Vec<intType>

# 7.33.3.6 getCoord()

get coordinate in dimension d of index i

# 7.33.3.7 getDim()

size of dimension d

### 7.33.3.8 getNumDims()

```
long helib::CubeSignature::getNumDims ( ) const [inline]
```

number of dimensions

# 7.33.3.9 getProd() [1/2]

product of sizes of dimensions d, d+1, ...

# 7.33.3.10 getProd() [2/2]

product of sizes of dimensions from, from+1, ..., to-1

### 7.33.3.11 getSize()

```
long helib::CubeSignature::getSize ( ) const [inline]
```

total size of cube

# 7.33.3.12 incrementCoords()

Increment the coordinates to point to next index, returning false if already at maximum value. VecType is either std::vector<intType> or NTL:Vec<intType>

### 7.33.3.13 initSignature() [1/2]

# 7.33.3.14 initSignature() [2/2]

# 7.33.3.15 numCols()

```
long helib::CubeSignature::numCols ( ) const [inline]
```

number of columns

### 7.33.3.16 numSlices()

```
long helib::CubeSignature::numSlices ( long \ d = 1 \ ) \ const \ [inline]
```

number of slices

#### 7.33.3.17 sliceSize()

```
long helib::CubeSignature::sliceSize ( long \ d = 1 \ ) \ const \ [inline]
```

size of one slice

### 7.33.4 Friends And Related Function Documentation

### 7.33.4.1 operator <<

The documentation for this class was generated from the following files:

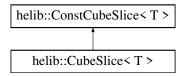
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/hypercube.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/hypercube.cpp

# 7.34 helib::CubeSlice< T > Class Template Reference

A lower-dimension slice of a hypercube.

```
#include <hypercube.h>
```

Inheritance diagram for helib::CubeSlice< T >:



### **Public Member Functions**

- CubeSlice (HyperCube < T > &\_cube)
- CubeSlice (NTL::Vec< T > &\_data, const CubeSignature &\_sig)
- CubeSlice (const CubeSlice < T > &bigger, long i, long \_dimOffset=1)
- CubeSlice (HyperCube< T > &\_cube, long i, long \_dimOffset=1)
- void copy (const ConstCubeSlice < T > &other) const
- T & at (long i) const
- T & operator[] (long i) const

# 7.34.1 Detailed Description

```
template<typename T> class helib::CubeSlice< T>
```

A lower-dimension slice of a hypercube.

### 7.34.2 Constructor & Destructor Documentation

### 7.34.2.1 CubeSlice() [1/4]

### 7.34.2.2 CubeSlice() [2/4]

# 7.34.2.3 CubeSlice() [3/4]

### 7.34.2.4 CubeSlice() [4/4]

### 7.34.3 Member Function Documentation

#### 7.34.3.1 at()

```
\label{template} $$ \ensuremath{\mbox{T\& helib::CubeSlice} \ T > ::at (} $$ \ensuremath{\mbox{long} \ i \ ) \ const \ [inline] $$ $$ $$
```

#### 7.34.3.2 copy()

```
\label{template} $$ \ensuremath{\sf template}$ \ensuremath{\sf template}$
```

### 7.34.3.3 operator[]()

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/hypercube.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/hypercube.cpp

# 7.35 helib::DAGnode Class Reference

A node in an addition-DAG structure.

#### **Public Member Functions**

- DAGnode (Nodeldx ii, bool qq, long lvl, long chl=0, DAGnode \*pt1=nullptr, DAGnode \*pt2=nullptr)
- DAGnode (DAGnode &&other)
- std::string nodeName () const

# **Public Attributes**

- Nodeldx idx
- bool isQ
- long level
- std::atomic\_long childrenLeft
- DAGnode \* parent1
- DAGnode \* parent2
- std::mutex ct\_mtx
- Ctxt \* ct

# 7.35.1 Detailed Description

A node in an addition-DAG structure.

# 7.35.2 Constructor & Destructor Documentation

### 7.35.2.1 DAGnode() [1/2]

### 7.35.2.2 DAGnode() [2/2]

```
helib::DAGnode::DAGnode (

DAGnode && other ) [inline]
```

# 7.35.3 Member Function Documentation

#### 7.35.3.1 nodeName()

```
std::string helib::DAGnode::nodeName ( ) const [inline]
```

# 7.35.4 Member Data Documentation

# 7.35.4.1 childrenLeft

std::atomic\_long helib::DAGnode::childrenLeft

#### 7.35.4.2 ct

Ctxt\* helib::DAGnode::ct

# 7.35.4.3 ct\_mtx

std::mutex helib::DAGnode::ct\_mtx

### 7.35.4.4 idx

NodeIdx helib::DAGnode::idx

#### 7.35.4.5 isQ

bool helib::DAGnode::isQ

# 7.35.4.6 level

long helib::DAGnode::level

# 7.35.4.7 parent1

DAGnode\* helib::DAGnode::parent1

#### 7.35.4.8 parent2

```
DAGnode * helib::DAGnode::parent2
```

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/binaryArith.cpp

# 7.36 helib::decode\_pa\_impl< type > Class Template Reference

### **Static Public Member Functions**

template<typename T >
 static void apply (const EncryptedArrayDerived< type > &ea, std::vector< T > &array, const PlaintextArray &pa)

#### 7.36.1 Member Function Documentation

### 7.36.1.1 apply()

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.37 helib::deep\_clone < X > Class Template Reference

Deep copy: initialize with clone.

```
#include <clonedPtr.h>
```

#### **Static Public Member Functions**

```
    static X * apply (const X *x)
```

# 7.37.1 Detailed Description

```
template<typename X> class helib::deep_clone< X>
```

Deep copy: initialize with clone.

**Template Parameters** 

X The class to which this points

#### 7.37.2 Member Function Documentation

#### 7.37.2.1 apply()

The documentation for this class was generated from the following file:

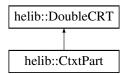
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/clonedPtr.h

# 7.38 helib::DoubleCRT Class Reference

Implementing polynomials (elements in the ring R\_Q) in double-CRT form.

```
#include <DoubleCRT.h>
```

Inheritance diagram for helib::DoubleCRT:



#### **Public Member Functions**

- DoubleCRT (const DoubleCRT &other)=default
- DoubleCRT (const NTL::ZZX &poly, const Context &\_context, const IndexSet &indexSet)
   Initializing DoubleCRT from a ZZX polynomial.
- DoubleCRT (const zzX &poly, const Context &\_context, const IndexSet &indexSet)

Same as above, but with zzX's.

• DoubleCRT (const Context &\_context, const IndexSet &indexSet)

Also specify the IndexSet explicitly.

- DoubleCRT & operator= (const DoubleCRT & other)
- DoubleCRT & operator= (const zzX &poly)
- DoubleCRT & operator= (const NTL::ZZX &poly)
- DoubleCRT & operator= (const NTL::ZZ &num)
- DoubleCRT & operator= (const long num)
- $\bullet \ \mathsf{long} \ \mathsf{getOneRow} \ (\mathsf{NTL} :: \mathsf{Vec} {<} \ \mathsf{long} \ {>} \ \mathsf{\&row}, \ \mathsf{long} \ \mathsf{idx}, \ \mathsf{bool} \ \mathsf{positive=false}) \ \mathsf{const}$

Get one row of a polynomial.

- long getOneRow (NTL::zz\_pX &row, long idx) const
- void toPoly (NTL::ZZX &p, const IndexSet &s, bool positive=false) const

Recovering the polynomial in coefficient representation. This yields an integer polynomial with coefficients in [-P/2,P/2], unless the positive flag is set to true, in which case we get coefficients in [0,P-1] (P is the product of all moduli used). Using the optional IndexSet param we compute the polynomial reduced modulo the product of only the primes in that set.

- void toPoly (NTL::ZZX &p, bool positive=false) const
- bool operator== (const DoubleCRT & other) const
- bool operator!= (const DoubleCRT &other) const
- DoubleCRT & SetZero ()
- DoubleCRT & SetOne ()
- NTL::xdouble breakIntoDigits (std::vector < DoubleCRT > &dgts) const

Break into n digits, according to the primeSets in context.digits. See Section 3.1.6 of the design document (relinearization) Returns the sum of the canonical embedding of the digits.

void addPrimes (const IndexSet &s1, NTL::ZZX \*poly\_p=0)

Expand the index set by s1. It is assumed that s1 is disjoint from the current index set. If poly\_p != 0, then \*poly\_p will first be set to the result of applying toPoly.

double addPrimesAndScale (const IndexSet &s1)

Expand index set by s1, and multiply by Prod\_{q in s1}. s1 is disjoint from the current index set, returns log(product).

void removePrimes (const IndexSet &s1)

Remove s1 from the index set.

void setPrimes (const IndexSet &s1)

@ brief make prime set equal to s1

- · const Context & getContext () const
- const IndexMap< NTL::vec long > & getMap () const
- const IndexSet & getIndexSet () const
- void randomize (const NTL::ZZ \*seed=nullptr)

Fills each row i with random ints mod pi, uses NTL's PRG.

• double sampleSmall ()

Coefficients are -1/0/1, Prob[0]=1/2.

- double sampleSmallBounded ()
- double sampleHWt (long Hwt)

Coefficients are -1/0/1 with pre-specified number of nonzeros.

- · double sampleHWtBounded (long Hwt)
- double sampleGaussian (double stdev=0.0)

Coefficients are Gaussians Return a high probability bound on L-infty norm of canonical embedding.

- double sampleGaussianBounded (double stdev=0.0)
- double sampleUniform (long B)

Coefficients are uniform in [-B..B].

- NTL::xdouble sampleUniform (const NTL::ZZ &B)
- void scaleDownToSet (const IndexSet &s, long ptxtSpace, NTL::ZZX &delta)
- void FFT (const NTL::ZZX &poly, const IndexSet &s)
- void FFT (const zzX &poly, const IndexSet &s)
- void reduce () const
- void read (std::istream &str)
- · void write (std::ostream &str) const

#### **Arithmetic operation**

Only the "destructive" versions are used, i.e., a += b is implemented but not a + b.

- DoubleCRT & Negate (const DoubleCRT & other)
- DoubleCRT & Negate ()
- DoubleCRT & operator+= (const DoubleCRT & other)

```
• DoubleCRT & operator+= (const NTL::ZZX &poly)
• DoubleCRT & operator+= (const NTL::ZZ &num)

    DoubleCRT & operator+= (long num)

    DoubleCRT & operator-= (const DoubleCRT & other)

    DoubleCRT & operator-= (const NTL::ZZX &poly)

    DoubleCRT & operator-= (const NTL::ZZ &num)

    DoubleCRT & operator-= (long num)

    DoubleCRT & operator++ ()

• DoubleCRT & operator-- ()

    void operator++ (int)

· void operator-- (int)

    DoubleCRT & operator*= (const DoubleCRT & other)

    DoubleCRT & operator*= (const NTL::ZZX &poly)

    DoubleCRT & operator*= (const NTL::ZZ &num)

    DoubleCRT & operator*= (long num)

    void Add (const DoubleCRT & other, bool matchIndexSets=true)

    void Sub (const DoubleCRT &other, bool matchIndexSets=true)

    void Mul (const DoubleCRT & other, bool matchIndexSets=true)

    DoubleCRT & operator/= (const NTL::ZZ &num)

    DoubleCRT & operator/= (long num)

    void Exp (long k)

      Small-exponent polynomial exponentiation.

    void automorph (long k)

      Apply the automorphism F(X) --> F(X^{\wedge} k) (with gcd(k,m)=1)

    DoubleCRT & operator>>= (long k)

    void complexConj ()
```

#### **Friends**

std::ostream & operator<< (std::ostream &s, const DoubleCRT &d)</li>

Compute the complex conjugate, the same as automorph(m-1)

std::istream & operator>> (std::istream &s, DoubleCRT &d)

### 7.38.1 Detailed Description

Implementing polynomials (elements in the ring R\_Q) in double-CRT form.

Double-CRT form is a matrix of L rows and phi(m) columns. The i'th row contains the FFT of the element wrt the ith prime, i.e. the evaluations of the polynomial at the primitive mth roots of unity mod the ith prime. The polynomial thus represented is defined modulo the product of all the primes in use.

The list of primes is defined by the data member indexMap. indexMap.getIndexSet() defines the set of indices of primes associated with this DoubleCRT object: they index the primes stored in the associated Context.

Arithmetic operations are computed modulo the product of the primes in use and also modulo  $Phi_m(X)$ . Arithmetic operations can only be applied to DoubleCRT objects relative to the same context, trying to add/multiply objects that have different Context objects will raise an error.

### 7.38.2 Constructor & Destructor Documentation

# 7.38.2.1 DoubleCRT() [1/4]

# 7.38.2.2 DoubleCRT() [2/4]

Initializing DoubleCRT from a ZZX polynomial.

| raiailieteis |           |   |
|--------------|-----------|---|
| poly         | The       |   |
|              | ring el-  |   |
|              | ement     |   |
|              | itself,   |   |
|              | zero      |   |
|              | if not    |   |
|              | speci-    |   |
|              | fied      |   |
| _context     | The       |   |
|              | con-      |   |
|              | text      |   |
|              | for this  |   |
|              | DoubleCR1 | Γ |
|              | object,   |   |
|              | use       |   |
|              | "cur-     |   |
|              | rent      |   |
|              | active    |   |
|              | con-      |   |
|              | text"     |   |
|              | if not    |   |
|              | speci-    |   |
|              | fied      |   |
| indexSet     | Which     |   |
|              | primes    |   |
|              | to use    |   |
|              | for this  |   |
|              | object,   |   |
|              | if not    |   |
|              | spec-     |   |
|              | ified     |   |
|              | then      |   |
|              | use       |   |
|              | all of    |   |
|              | them      |   |

#### 7.38.2.3 DoubleCRT() [3/4]

Same as above, but with zzX's.

### 7.38.2.4 DoubleCRT() [4/4]

Also specify the IndexSet explicitly.

# 7.38.3 Member Function Documentation

### 7.38.3.1 Add()

### 7.38.3.2 addPrimes()

Expand the index set by s1. It is assumed that s1 is disjoint from the current index set. If poly\_p != 0, then \*poly\_p will first be set to the result of applying toPoly.

# 7.38.3.3 addPrimesAndScale()

Expand index set by s1, and multiply by Prod\_{q in s1}. s1 is disjoint from the current index set, returns log(product).

### 7.38.3.4 automorph()

```
void helib::DoubleCRT::automorph ( long k )
```

Apply the automorphism  $F(X) --> F(X^{\wedge}k)$  (with gcd(k,m)=1)

# 7.38.3.5 breakIntoDigits()

```
\label{eq:ntl::mouble} $$ NTL::xdouble helib::DoubleCRT::breakIntoDigits ( $$ std::vector< DoubleCRT > & dgts ) const
```

Break into n digits,according to the primeSets in context.digits. See Section 3.1.6 of the design document (relinearization) Returns the sum of the canonical embedding of the digits.

#### 7.38.3.6 complexConj()

```
void helib::DoubleCRT::complexConj ( )
```

Compute the complex conjugate, the same as automorph(m-1)

# 7.38.3.7 Exp()

```
void helib::DoubleCRT::Exp ( \label{eq:long_k} \mbox{long } k \mbox{ )}
```

Small-exponent polynomial exponentiation.

# 7.38.3.8 FFT() [1/2]

# 7.38.3.9 FFT() [2/2]

```
void helib::DoubleCRT::FFT (  {\tt const~zzX~\&~poly,}   {\tt const~IndexSet~\&~s~)}
```

# 7.38.3.10 getContext()

```
const Context& helib::DoubleCRT::getContext ( ) const [inline]
```

#### 7.38.3.11 getIndexSet()

```
const IndexSet& helib::DoubleCRT::getIndexSet ( ) const [inline]
```

# 7.38.3.12 getMap()

```
const IndexMap<NTL::vec_long>& helib::DoubleCRT::getMap ( ) const [inline]
```

# 7.38.3.13 getOneRow() [1/2]

Get one row of a polynomial.

### 7.38.3.14 getOneRow() [2/2]

# 7.38.3.15 Mul()

```
7.38.3.16 Negate() [1/2]
```

```
DoubleCRT& helib::DoubleCRT::Negate ( ) [inline]
```

# 7.38.3.17 Negate() [2/2]

### 7.38.3.18 operator"!=()

### 7.38.3.19 operator\*=() [1/4]

# 7.38.3.20 operator\*=() [2/4]

# 7.38.3.21 operator\*=() [3/4]

# 7.38.3.22 operator\*=() [4/4]

```
7.38.3.23 operator++() [1/2]
```

```
DoubleCRT& helib::DoubleCRT::operator++ ( ) [inline]
```

### 7.38.3.24 operator++() [2/2]

```
void helib::DoubleCRT::operator++ (
          int ) [inline]
```

### 7.38.3.25 operator+=() [1/4]

### 7.38.3.26 operator+=() [2/4]

### 7.38.3.27 operator+=() [3/4]

# 7.38.3.28 operator+=() [4/4]

# 7.38.3.29 operator--() [1/2]

```
DoubleCRT& helib::DoubleCRT::operator-- ( ) [inline]
```

```
7.38.3.30 operator--() [2/2]
```

### 7.38.3.31 operator-=() [1/4]

### 7.38.3.32 operator-=() [2/4]

### 7.38.3.33 operator-=() [3/4]

### 7.38.3.34 operator-=() [4/4]

# 7.38.3.35 operator/=() [1/2]

# 7.38.3.36 operator/=() [2/2]

# 7.38.3.37 operator=() [1/5]

#### 7.38.3.38 operator=() [2/5]

# 7.38.3.39 operator=() [3/5]

#### 7.38.3.40 operator=() [4/5]

#### 7.38.3.41 operator=() [5/5]

# 7.38.3.42 operator==()

# 7.38.3.43 operator>>=()

# 7.38.3.44 randomize()

Fills each row i with random ints mod pi, uses NTL's PRG.

# 7.38.3.45 read()

#### 7.38.3.46 reduce()

```
void helib::DoubleCRT::reduce ( ) const [inline]
```

# 7.38.3.47 removePrimes()

Remove s1 from the index set.

# 7.38.3.48 sampleGaussian()

```
double helib::DoubleCRT::sampleGaussian ( double stdev = 0.0 )
```

Coefficients are Gaussians Return a high probability bound on L-infty norm of canonical embedding.

# 7.38.3.49 sampleGaussianBounded()

```
double helib::DoubleCRT::sampleGaussianBounded ( double stdev = 0.0 )
```

# 7.38.3.50 sampleHWt()

Coefficients are -1/0/1 with pre-specified number of nonzeros.

# 7.38.3.51 sampleHWtBounded()

# 7.38.3.52 sampleSmall()

```
double helib::DoubleCRT::sampleSmall ( )
```

Coefficients are -1/0/1, Prob[0]=1/2.

Sampling routines: Each of these return a high probability bound on L-infty norm of canonical embedding

# 7.38.3.53 sampleSmallBounded()

```
double helib::DoubleCRT::sampleSmallBounded ( )
```

# 7.38.3.54 sampleUniform() [1/2]

# 7.38.3.55 sampleUniform() [2/2]

```
double helib::DoubleCRT::sampleUniform ( long B )
```

Coefficients are uniform in [-B..B].

# 7.38.3.56 scaleDownToSet()

#### 7.38.3.57 SetOne()

```
DoubleCRT& helib::DoubleCRT::SetOne ( ) [inline]
```

# 7.38.3.58 setPrimes()

@ brief make prime set equal to s1

# 7.38.3.59 SetZero()

```
DoubleCRT& helib::DoubleCRT::SetZero ( ) [inline]
```

### 7.38.3.60 Sub()

# 7.38.3.61 toPoly() [1/2]

#### 7.38.3.62 toPoly() [2/2]

Recovering the polynomial in coefficient representation. This yields an integer polynomial with coefficients in [-P/2,P/2], unless the positive flag is set to true, in which case we get coefficients in [0,P-1] (P is the product of all moduli used). Using the optional IndexSet param we compute the polynomial reduced modulo the product of only the primes in that set.

# 7.38.3.63 write()

```
void helib::DoubleCRT::write ( std::ostream \ \& \ str \ ) \ const
```

#### 7.38.4 Friends And Related Function Documentation

# 7.38.4.1 operator <<

#### 7.38.4.2 operator>>

The documentation for this class was generated from the following files:

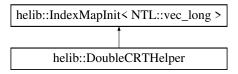
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/DoubleCRT.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/DoubleCRT.cpp

# 7.39 helib::DoubleCRTHelper Class Reference

A helper class to enforce consistency within an DoubleCRTHelper object.

```
#include <DoubleCRT.h>
```

Inheritance diagram for helib::DoubleCRTHelper:



# **Public Member Functions**

- DoubleCRTHelper (const Context &context)
- virtual void init (NTL::vec\_long &v)

the init method ensures that all rows have the same size

 virtual IndexMapInit < NTL::vec\_long > \* clone () const clone allocates a new object and copies the content

# 7.39.1 Detailed Description

A helper class to enforce consistency within an DoubleCRTHelper object.

See Section 2.6.2 of the design document (IndexMap)

# 7.39.2 Constructor & Destructor Documentation

# 7.39.2.1 DoubleCRTHelper()

# 7.39.3 Member Function Documentation

# 7.39.3.1 clone()

```
virtual IndexMapInit<NTL::vec_long>* helib::DoubleCRTHelper::clone ( ) const [inline], [virtual]
clone allocates a new object and copies the content
```

#### 7.39.3.2 init()

the init method ensures that all rows have the same size

Implements helib::IndexMapInit< NTL::vec long >.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/DoubleCRT.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/DoubleCRT.cpp

# 7.40 helib::DynamicCtxtPowers Class Reference

Store powers of X, compute them dynamically as needed.

```
#include <polyEval.h>
```

#### **Public Member Functions**

- DynamicCtxtPowers (const Ctxt &c, long nPowers)
- Ctxt & getPower (long e)

Returns the e'th power, computing it as needed.

• Ctxt & at (long i)

dp.at(i) and dp[i] both return the i+1st power

- Ctxt & operator[] (long i)
- const std::vector < Ctxt > & getVector () const
- long size () const
- bool isPowerComputed (long i)

# 7.40.1 Detailed Description

Store powers of X, compute them dynamically as needed.

# 7.40.2 Constructor & Destructor Documentation

# 7.40.2.1 DynamicCtxtPowers()

# 7.40.3 Member Function Documentation

# 7.40.3.1 at()

dp.at(i) and dp[i] both return the i+1st power

# 7.40.3.2 getPower()

Returns the e'th power, computing it as needed.

# 7.40.3.3 getVector()

```
const std::vector<Ctxt>& helib::DynamicCtxtPowers::getVector ( ) const [inline]
```

# 7.40.3.4 isPowerComputed()

```
\label{eq:bool} \bool helib:: DynamicCtxtPowers:: is PowerComputed ( \\ long i) [inline]
```

# 7.40.3.5 operator[]()

### 7.40.3.6 size()

```
long helib::DynamicCtxtPowers::size ( ) const [inline]
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/polyEval.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/polyEval.cpp

# 7.41 helib::encode pa impl< type > Class Template Reference

# **Static Public Member Functions**

- static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const std::vector< long > &array)

# 7.41.1 Member Function Documentation

#### 7.41.1.1 apply() [1/2]

# 7.41.1.2 apply() [2/2]

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.42 helib::EncryptedArray Class Reference

A simple wrapper for a smart pointer to an EncryptedArrayBase. This is the interface that higher-level code should use.

```
#include <EncryptedArray.h>
```

#### **Public Member Functions**

```
    EncryptedArray (const Context &context, const NTL::ZZX &G=NTL::ZZX(1, 1))
```

constructor: G defaults to the monomial X, PAlgebraMod from context

EncryptedArray (const Context &context, const PAlgebraMod & alMod)

constructor: G defaults to F0, PAlgebraMod explicitly given

- EncryptedArray & operator= (const EncryptedArray & other)
- template<typename type >

const EncryptedArrayDerived< type > & getDerived (type) const

downcast operator example: const EncryptedArrayDerived<PA\_GF2>& rep = ea.getDerived(PA\_GF2());

const EncryptedArrayCx & getCx () const

#### Direct access to EncryptedArrayBase methods

- PA\_tag getTag () const
- template < template < typename > class T, typename... Args > void dispatch (Args &&... args) const
- const Context & getContext () const
- const PAlgebraMod & getAlMod () const
- const PAlgebra & getPAlgebra () const
- long getDegree () const
- · void rotate (Ctxt &ctxt, long k) const
- · void shift (Ctxt &ctxt, long k) const
- void rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const
- void shift1D (Ctxt &ctxt, long i, long k) const
- void badDimensionAutomorphCorrection (Ctxt &ctxt, long i, long amt) const
- template<typename PTXT , typename ARRAY >

void encode (PTXT &ptxt, const ARRAY &array) const

- void encodeUnitSelector (zzX &ptxt, long i) const
- template<typename PTXT , typename ARRAY >

void decode (ARRAY & array, const PTXT & ptxt) const

template<typename T >

void random (std::vector< T > &array) const

template<typename T >

void encrypt (Ctxt &ctxt, const PubKey &pKey, const T &ptxt) const

• template<typename T >

void decrypt (const Ctxt &ctxt, const SecKey &sKey, T &ptxt) const

- void buildLinPolyCoeffs (std::vector < NTL::ZZX > &C, const std::vector < NTL::ZZX > &L) const
- void restoreContext () const
- void restoreContextForG () const
- · long size () const
- · long dimension () const
- · long sizeOfDimension (long i) const
- long nativeDimension (long i) const
- · long coordinate (long i, long k) const
- long addCoord (long i, long k, long offset) const
- template<typename U >

void rotate1D (std::vector< U > &out, const std::vector< U > &in, long i, long offset) const rotate an array by offset in the i'th dimension (output should not alias input)

# 7.42.1 Detailed Description

A simple wrapper for a smart pointer to an EncryptedArrayBase. This is the interface that higher-level code should use.

# 7.42.2 Constructor & Destructor Documentation

# 7.42.2.1 EncryptedArray() [1/2]

constructor: G defaults to the monomial X, PAlgebraMod from context

# 7.42.2.2 EncryptedArray() [2/2]

constructor: G defaults to F0, PAlgebraMod explicitly given

# 7.42.3 Member Function Documentation

# 7.42.3.1 addCoord()

# 7.42.3.2 badDimensionAutomorphCorrection()

# 7.42.3.3 buildLinPolyCoeffs()

```
void helib::EncryptedArray::buildLinPolyCoeffs ( std::vector < NTL::ZZX \ > \ \& \ C, const \ std::vector < NTL::ZZX \ > \ \& \ L \ ) \ const \ [inline]
```

# 7.42.3.4 coordinate()

```
long helib::EncryptedArray::coordinate ( \label{eq:long_i} \log \ i \text{,} \label{eq:long_k} \log \ k \text{ ) const [inline]}
```

# 7.42.3.5 decode()

#### 7.42.3.6 decrypt()

#### 7.42.3.7 dimension()

```
long helib::EncryptedArray::dimension ( ) const [inline]
```

# 7.42.3.8 dispatch()

# 7.42.3.9 encode()

# 7.42.3.10 encodeUnitSelector()

# 7.42.3.11 encrypt()

# 7.42.3.12 getAlMod()

```
const PAlgebraMod& helib::EncryptedArray::getAlMod ( ) const [inline]
```

# 7.42.3.13 getContext()

```
const Context& helib::EncryptedArray::getContext ( ) const [inline]
```

# 7.42.3.14 getCx()

```
const EncryptedArrayCx& helib::EncryptedArray::getCx ( ) const [inline]
```

# 7.42.3.15 getDegree()

```
long helib::EncryptedArray::getDegree ( ) const [inline]
```

# 7.42.3.16 getDerived()

downcast operator example: const EncryptedArrayDerived<PA\_GF2>& rep = ea.getDerived(PA\_GF2());

# 7.42.3.17 getPAlgebra()

```
const PAlgebra& helib::EncryptedArray::getPAlgebra ( ) const [inline]
```

# 7.42.3.18 getTag()

```
PA_tag helib::EncryptedArray::getTag ( ) const [inline]
```

# 7.42.3.19 nativeDimension()

#### 7.42.3.20 operator=()

# 7.42.3.21 random()

# 7.42.3.22 restoreContext()

```
void helib::EncryptedArray::restoreContext ( ) const [inline]
```

# 7.42.3.23 restoreContextForG()

```
void helib::EncryptedArray::restoreContextForG ( ) const [inline]
```

#### 7.42.3.24 rotate()

# 7.42.3.25 rotate1D() [1/2]

# 7.42.3.26 rotate1D() [2/2]

rotate an array by offset in the i'th dimension (output should not alias input)

# 7.42.3.27 shift()

# 7.42.3.28 shift1D()

### 7.42.3.29 size()

```
long helib::EncryptedArray::size ( ) const [inline]
```

#### 7.42.3.30 sizeOfDimension()

```
long helib::EncryptedArray::sizeOfDimension ( long \ i \ ) \ const \ [inline]
```

The documentation for this class was generated from the following file:

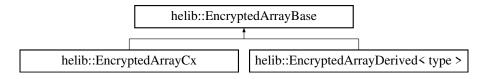
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/EncryptedArray.h

# 7.43 helib::EncryptedArrayBase Class Reference

virtual class for data-movement operations on arrays of slots

```
#include <EncryptedArray.h>
```

Inheritance diagram for helib::EncryptedArrayBase:



# **Public Member Functions**

- virtual ∼EncryptedArrayBase ()
- virtual EncryptedArrayBase \* clone () const =0
- virtual PA\_tag getTag () const =0
- virtual const Context & getContext () const =0
- virtual const PAlgebra & getPAlgebra () const =0
- virtual long getDegree () const =0
- virtual long getP2R () const =0
- virtual void rotate (Ctxt &ctxt, long k) const =0

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

virtual void shift (Ctxt &ctxt, long k) const =0

Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)

virtual void rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const =0

right-rotate k positions along the i'th dimension

• virtual void shift1D (Ctxt &ctxt, long i, long k) const =0

Right shift k positions along the i'th dimension with zero fill.

• virtual void badDimensionAutomorphCorrection (Ctxt &ctxt, long i, long amt) const =0

Correct an automorphism in a bad dimension.

virtual void buildLinPolyCoeffs (std::vector < NTL::ZZX > &C, const std::vector < NTL::ZZX > &L) const =0
 Linearized polynomials. L describes a linear map M by describing its action on the standard power basis: M(x<sup>^</sup> j mod G) = (L[j] mod G), for j = 0..d-1. The result is a coefficient std::vector C for the linearized polynomial representing M: a polynomial h in Z/(p<sup>^</sup> r)[X] of degree < d is sent to.</p>

- virtual void restoreContext () const
- virtual void restoreContextForG () const
- · long size () const

Total size (# of slots) of hypercube.

• long dimension () const

Number of dimensions of hypercube.

· long sizeOfDimension (long i) const

Size of given dimension.

• bool nativeDimension (long i) const

Is rotations in given dimension a "native" operation?

• long coordinate (long i, long k) const

returns coordinate of index k along the i'th dimension

long addCoord (long i, long k, long offset) const

adds offset to index k in the i'th dimension

• template<typename U >

void rotate1D (std::vector< U > &out, const std::vector< U > &in, long i, long offset) const

rotate an array by offset in the i'th dimension (output should not alias input)

# **Encoding/decoding methods**

- virtual void encode (zzX &ptxt, const std::vector< long > &array) const =0
- virtual void encode (NTL::ZZX &ptxt, const std::vector< long > &array) const =0
- virtual void encode (zzX &ptxt, const std::vector < zzX > &array) const =0
- virtual void encode (zzX &ptxt, const PlaintextArray &array) const =0
- virtual void encode (NTL::ZZX &ptxt, const std::vector< NTL::ZZX > &array) const =0
- virtual void encode (NTL::ZZX &ptxt, const PlaintextArray &array) const =0
- void encode (zzX &ptxt, const std::vector< NTL::ZZX > &array) const
- virtual void decode (std::vector < long > &array, const NTL::ZZX &ptxt) const =0
- virtual void decode (std::vector < NTL::ZZX > &array, const NTL::ZZX &ptxt) const =0
- virtual void decode (PlaintextArray & array, const NTL::ZZX &ptxt) const =0
- virtual void random (std::vector< long > &array) const =0
- virtual void random (std::vector< NTL::ZZX > &array) const =0

- long decode1Slot (const NTL::ZZX &ptxt, long i) const
- void decode1Slot (NTL::ZZX &slot, const NTL::ZZX &ptxt, long i) const
- virtual void encodeUnitSelector (zzX &ptxt, long i) const =0

Encodes a std::vector with 1 at position i and 0 everywhere else.

#### Encoding+encryption/decryption+decoding

- template<typename PTXT >
   void encrypt (Ctxt &ctxt, const PubKey &key, const PTXT &ptxt) const
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector < long > &ptxt) const =0
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector < NTL::ZZX > &ptxt) const =0
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, PlaintextArray &ptxt) const =0
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector< double > &ptxt) const =0
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector< cx double > &ptxt) const =0
- long decrypt1Slot (const Ctxt &ctxt, const SecKey &sKey, long i) const
- void decrypt1Slot (NTL::ZZX &slot, const Ctxt &ctxt, const SecKey &sKey, long i) const

# 7.43.1 Detailed Description

virtual class for data-movement operations on arrays of slots

An object ea of type EncryptedArray stores information about an Context context, and a monic polynomial G. If context defines parameters m, p, and r, then ea is a helper abject that supports encoding/decoding and encryption/decryption of std::vectors of plaintext slots over the ring  $(Z/(p^{\wedge}r)[X])/(G)$ .

The polynomial G should be irreducible over  $Z/(p^{r})$  (this is not checked). The degree of G should divide the multiplicative order of p modulo m (this is checked). Currently, the following restriction is imposed:

```
either r == 1 or deg(G) == 1 or G == factors[0].
```

ea stores objects in the polynomial ring  $Z/(p^{\wedge}r)[X]$ .

Just as for the class PAlgebraMod, if p == 2 and r == 1, then these polynomials are represented as GF2X's, and otherwise as  $zz_pX$ 's. Thus, the types of these objects are not determined until run time. As such, we need to use a class hierarchy, which mirrors that of PAlgebraMod, as follows.

EncryptedArrayBase is a virtual class

EncryptedArrayDerived<type> is a derived template class, where type is either PA\_GF2 or PA\_zz\_p.

The class EncryptedArray is a simple wrapper around a smart pointer to an EncryptedArrayBase object: copying an EncryptedArray object results is a "deep copy" of the underlying object of the derived class.

### 7.43.2 Constructor & Destructor Documentation

# 7.43.2.1 ~EncryptedArrayBase()

virtual helib::EncryptedArrayBase::~EncryptedArrayBase ( ) [inline], [virtual]

# 7.43.3 Member Function Documentation

# 7.43.3.1 addCoord()

```
long helib::EncryptedArrayBase::addCoord ( long \ i, \\ long \ k, \\ long \ offset \ ) \ const \ [inline]
```

adds offset to index k in the i'th dimension

# 7.43.3.2 badDimensionAutomorphCorrection()

Correct an automorphism in a bad dimension.

#### **Parameters**

| i didiiio | ici 3     |
|-----------|-----------|
| ctxt      | Ctxt      |
|           | to per-   |
|           | form      |
|           | the       |
|           | cor-      |
|           | rection   |
|           | on.       |
| i         | Dimension |
|           | of        |
|           | which     |
|           | to cor-   |
|           | rect.     |
| amt       | Exponent  |
|           | of the    |
|           | auto-     |
|           | mor-      |
|           | phism.    |

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

### 7.43.3.3 buildLinPolyCoeffs()

```
virtual void helib::EncryptedArrayBase::buildLinPolyCoeffs ( std::vector < NTL::ZZX > \& C, \\ const std::vector < NTL::ZZX > \& L ) const [pure virtual]
```

Linearized polynomials. L describes a linear map M by describing its action on the standard power basis:  $M(x^{\hat{}})$  mod G) = (L[j] mod G), for j = 0..d-1. The result is a coefficient std::vector C for the linearized polynomial representing M: a polynomial h in  $Z/(p^{\hat{}})[X]$  of degree < d is sent to.

$$//!M(h(X) \bmod G) = \sum_{i=0}^{d-1} (C[j] \cdot h(X^{p^j})) \bmod G).//!$$

Implemented in helib::EncryptedArrayDerived< type >.

#### 7.43.3.4 clone()

```
virtual EncryptedArrayBase* helib::EncryptedArrayBase::clone () const [pure virtual]
```

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

#### 7.43.3.5 coordinate()

```
long helib::EncryptedArrayBase::coordinate ( \label{eq:long_i} \log \ i \text{,} \label{eq:long_k} \log \ k \text{ ) const [inline]}
```

returns coordinate of index k along the i'th dimension

# 7.43.3.6 decode() [1/3]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.7 decode() [2/3]

Implemented in helib::EncryptedArrayDerived< type >.

#### 7.43.3.8 decode() [3/3]

Implemented in helib::EncryptedArrayDerived< type >.

#### 7.43.3.9 decode1Slot() [1/2]

```
long helib::EncryptedArrayBase::decode1Slot ( const NTL::ZZX & ptxt, long i ) const [inline]
```

#### 7.43.3.10 decode1Slot() [2/2]

# 7.43.3.11 decrypt() [1/5]

Implemented in helib::EncryptedArrayDerived< type >.

#### 7.43.3.12 decrypt() [2/5]

Implemented in helib::EncryptedArrayCx.

# 7.43.3.13 decrypt() [3/5]

Implemented in helib::EncryptedArrayCx.

# 7.43.3.14 decrypt() [4/5]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.15 decrypt() [5/5]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.16 decrypt1Slot() [1/2]

# 7.43.3.17 decrypt1Slot() [2/2]

# 7.43.3.18 dimension()

```
long helib::EncryptedArrayBase::dimension ( ) const [inline]
```

Number of dimensions of hypercube.

#### 7.43.3.19 encode() [1/7]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.20 encode() [2/7]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.21 encode() [3/7]

 $Implemented \ in \ helib:: Encrypted Array Derived < type >.$ 

### 7.43.3.22 encode() [4/7]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.23 encode() [5/7]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.24 encode() [6/7]

# 7.43.3.25 encode() [7/7]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.26 encodeUnitSelector()

Encodes a std::vector with 1 at position i and 0 everywhere else.

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.27 encrypt()

#### 7.43.3.28 getContext()

```
virtual const Context& helib::EncryptedArrayBase::getContext ( ) const [pure virtual]
Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.
```

# 7.43.3.29 getDegree()

```
virtual long helib::EncryptedArrayBase::getDegree ( ) const [pure virtual]
```

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.30 getP2R()

```
virtual long helib::EncryptedArrayBase::getP2R ( ) const [pure virtual]
```

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.31 getPAlgebra()

```
virtual const PAlgebra& helib::EncryptedArrayBase::getPAlgebra ( ) const [pure virtual]
```

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.32 getTag()

```
virtual PA_tag helib::EncryptedArrayBase::getTag ( ) const [pure virtual]
```

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

### 7.43.3.33 nativeDimension()

```
bool helib::EncryptedArrayBase::nativeDimension ( \log \ i \ ) \ {\tt const} \ \ [{\tt inline}]
```

Is rotations in given dimension a "native" operation?

#### 7.43.3.34 random() [1/2]

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.35 random() [2/2]

Implemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.36 restoreContext()

```
virtual void helib::EncryptedArrayBase::restoreContext ( ) const [inline], [virtual]
```

Reimplemented in helib::EncryptedArrayDerived< type >.

# 7.43.3.37 restoreContextForG()

```
virtual void helib::EncryptedArrayBase::restoreContextForG ( ) const [inline], [virtual]
```

Reimplemented in helib::EncryptedArrayDerived< type >.

#### 7.43.3.38 rotate()

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.39 rotate1D() [1/2]

right-rotate k positions along the i'th dimension

#### **Parameters**

| Parameters |         |
|------------|---------|
| dc         | means   |
|            | "don't  |
|            | care",  |
|            | which   |
|            | means   |
|            | that    |
|            | the     |
|            | caller  |
|            | guar-   |
|            | antees  |
|            | that    |
|            | only    |
|            | zero    |
|            | ele-    |
|            | ments   |
|            | rotate  |
|            | off the |
|            | end     |
|            | - this  |
|            | allows  |
|            | for     |
|            | some    |
|            | opti-   |
|            | miza-   |
|            | tions   |
|            | that    |
|            | would   |
|            | not     |
|            | other-  |
|            | wise    |
|            | be      |
|            | possi-  |
|            | ble     |

 $Implemented \ in \ helib:: Encrypted Array Cx, \ and \ helib:: Encrypted Array Derived < type >.$ 

# 7.43.3.40 rotate1D() [2/2]

rotate an array by offset in the i'th dimension (output should not alias input)

# 7.43.3.41 shift()

Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

# 7.43.3.42 shift1D()

Right shift k positions along the i'th dimension with zero fill.

Implemented in helib::EncryptedArrayCx, and helib::EncryptedArrayDerived< type >.

#### 7.43.3.43 size()

```
long helib::EncryptedArrayBase::size ( ) const [inline]
```

Total size (# of slots) of hypercube.

#### 7.43.3.44 sizeOfDimension()

```
long helib::EncryptedArrayBase::sizeOfDimension ( \label{eq:long} \mbox{long $i$ ) const [inline]}
```

Size of given dimension.

The documentation for this class was generated from the following file:

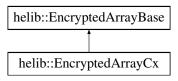
 $\bullet \ / Users/Projects/FHE\_HE Lib\_Repos\_Public\_staging/homenc\_v1.0.2/HE Lib/include/he Lib/Encrypted Array.h$ 

# 7.44 helib::EncryptedArrayCx Class Reference

A different derived class to be used for the approximate-numbers scheme.

```
#include <EncryptedArray.h>
```

Inheritance diagram for helib::EncryptedArrayCx:



#### **Public Member Functions**

- double encodei (zzX &ptxt, long precision=-1) const
- EncryptedArrayCx (const Context & context)
- EncryptedArrayCx (const Context &\_context, const PAlgebraModCx &\_alMod)
- EncryptedArrayBase \* clone () const override
- const zzX & getiEncoded () const
- PA tag getTag () const override
- const Context & getContext () const override
- · const PAlgebra & getPAlgebra () const override
- · long getDegree () const override
- void rotate (Ctxt &ctxt, long k) const override

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

void shift (Ctxt &ctxt, long k) const override

Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)

void rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const override

right-rotate k positions along the i'th dimension

void shift1D (Ctxt &ctxt, long i, long k) const override

Right shift k positions along the i'th dimension with zero fill.

- long getP2R () const override
- void encode (UNUSED zzX &ptxt, UNUSED const std::vector < long > &array) const override
   Unimplemented encode function for BGV. It will always throw helib::LogicError.
- void encode (UNUSED NTL::ZZX &ptxt, UNUSED const std::vector< long > &array) const override
   Unimplemented encode function for BGV. It will always throw helib::LogicError.
- void encode (UNUSED zzX &ptxt, UNUSED const std::vector < zzX > &array) const override
   Unimplemented encode function for BGV. It will always throw helib::LogicError.
- void encode (UNUSED zzX &ptxt, UNUSED const PlaintextArray &array) const override
- Unimplemented encode function for BGV. It will always throw helib::LogicError.

   void encode (UNUSED NTL::ZZX &ptxt, UNUSED const std::vector< NTL::ZZX > &array) const override
- Unimplemented encode function for BGV. It will always throw helib::LogicError.
- void encode (UNUSED NTL::ZZX &ptxt, UNUSED const PlaintextArray &array) const override
   Unimplemented encode function for BGV. It will always throw helib::LogicError.
- void decode (UNUSED std::vector < long > &array, UNUSED const NTL::ZZX &ptxt) const override
   Unimplemented decode function for BGV. It will always throw helib::LogicError.
- void decode (UNUSED std::vector < NTL::ZZX > & array, UNUSED const NTL::ZZX &ptxt) const override
   Unimplemented decode function for BGV. It will always throw helib::LogicError.
- void decode (UNUSED PlaintextArray & array, UNUSED const NTL::ZZX &ptxt) const override

Unimplemented decode function for BGV. It will always throw helib::LogicError.

void random (UNUSED std::vector < NTL::ZZX > & array) const override

Unimplemented random function for BGV. It will always throw helib::LogicError.

void decrypt (UNUSED const Ctxt &ctxt, UNUSED const SecKey &sKey, UNUSED std::vector < long > &ptxt)
 const override

Unimplemented decrypt function for BGV. It will always throw helib::LogicError.

Unimplemented decrypt function for BGV. It will always throw helib::LogicError.

 void decrypt (UNUSED const Ctxt &ctxt, UNUSED const SecKey &sKey, UNUSED PlaintextArray &ptxt) const override

Unimplemented decrypt function for BGV. It will always throw helib::LogicError.

void buildLinPolyCoeffs (UNUSED std::vector< NTL::ZZX > &C, UNUSED const std::vector< NTL::ZZX > &L) const override

Unimplemented buildLinPolyCoeffs function for BGV. It will always throw helib::LogicError.

- double encode (zzX &ptxt, const std::vector< cx\_double > &array, double useThisSize, long precision=-1)
- double encode (zzX &ptxt, const std::vector< double > &array, double useThisSize, long precision=-1) const
- double encode (zzX &ptxt, const std::vector < long > &array, double useThisSize, long precision=-1) const
- template<typename Scheme >

double encode (zzX &out, const Ptxt< Scheme > &ptxt, double useThisSize, long precision=-1) const Encode a Ptxt object into a zzX.

- double encode (zzX &ptxt, double aSingleNumber, double useThisSize=-1, long precision=-1) const
- template<typename PTXT >

double encode (NTL::ZZX &ptxt, const PTXT &pt, double useThisSize=-1, long precision=-1) const

- void encryptOneNum (Ctxt &ctxt, const PubKey &key, double num, double useThisSize=-1, long precision=-1)
   const
- $\bullet \ \ \text{template}{<} \text{typename PTXT} >$

void encrypt (Ctxt &ctxt, const PubKey &key, const PTXT &ptxt, double useThisSize, long precision=-1) const

• template<typename PTXT >

void encrypt (Ctxt &ctxt, const PubKey &key, const PTXT &ptxt) const

void encodeUnitSelector (zzX &ptxt, long i) const override

Encodes a std::vector with 1 at position i and 0 everywhere else.

- double encodeRoundingError () const
- long encodeScalingFactor (long precision=-1, double roundErr=-1.0) const
- void decode (std::vector< cx\_double > &array, const zzX &ptxt, double scaling) const
- void decode (std::vector< cx\_double > &array, const NTL::ZZX &ptxt, double scaling) const
- void decode (std::vector< double > &array, const zzX &ptxt, double scaling) const
- void decode (std::vector< double > &array, const NTL::ZZX &ptxt, double scaling) const
- void random (std::vector < cx\_double > &array, double rad=1.0) const
- void random (std::vector< double > &array, double rad=1.0) const
- void random (std::vector < long > &array) const override
- void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector < cx double > &ptxt) const override
- void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector< double > &ptxt) const override
- template<typename Scheme >

void decrypt (const Ctxt &ctxt, const SecKey &sKey, Ptxt< Scheme > &ptxt) const

Decrypt ciphertext to a plaintext relative to a specific scheme.

- void extractRealPart (Ctxt &c) const
- template<typename Scheme >

void extractRealPart (Ptxt< Scheme > &p) const

Extract the real part of a CKKS plaintext.

template<typename Scheme >

void extractImPart (Ptxt< Scheme > &p) const

Extract the imaginary part of a CKKS plaintext.

- void extractImPart (Ctxt &c, DoubleCRT \*dcrt=nullptr) const
- · void badDimensionAutomorphCorrection (Ctxt &ctxt, long i, long k) const override

Correct an automorphism in a bad dimension.

#### Linearized polynomials for EncryptedArrayCx

buildLinPolyCoeffs returns in C two encoded constants such that the linear transformation(s) defined as L(1) = 0 oneImage and L(i) = 0 ilmage can be computed as: L(x) = C[0]\*x + C[1]\*conjugate(x). Once C is computed, we can apply this L to a ciphertext by calling applyLinPolyLL(ctxt, C, 2). Alternatively, we can convert C to a vector of two DoubleCRT objects, then call applyLinPolyLL(ctxt, dcrtVec, 2). This lets us compute the DoubleCRT object just once, then use them many times.

void buildLinPolyCoeffs (std::vector< zzX > &C, const cx\_double &oneImage, const cx\_double &iImage, long precision=0) const

First variant: same linear transformation in all the slots.

void buildLinPolyCoeffs (std::vector< zzX > &C, const std::vector< cx\_double > &oneImages, const std
 ::vector< cx\_double > &iImages, long precision=0) const

Second variant: different linear transformation in each slots.

#### **Static Public Member Functions**

- static double roundedSize (double x)
- static void convert (std::vector< cx double > &out, const std::vector< double > &in)
- static void convert (std::vector< double > &out, const std::vector< cx double > &in)
- static void convert (std::vector< cx\_double > &out, const std::vector< long > &in)
- static void convert (std::vector < long > &out, const std::vector < cx\_double > &in)

# 7.44.1 Detailed Description

A different derived class to be used for the approximate-numbers scheme.

# 7.44.2 Constructor & Destructor Documentation

# 7.44.2.1 EncryptedArrayCx() [1/2]

#### 7.44.2.2 EncryptedArrayCx() [2/2]

# 7.44.3 Member Function Documentation

# 7.44.3.1 badDimensionAutomorphCorrection()

Correct an automorphism in a bad dimension.

#### **Parameters**

| ctxt | Ctxt      |
|------|-----------|
|      | to per-   |
|      | form      |
|      | the       |
|      | cor-      |
|      | rection   |
|      | on.       |
| i    | Dimension |
|      | of        |
|      | which     |
|      | to cor-   |
|      | rect.     |
| amt  | Exponent  |
|      | of the    |
|      | auto-     |
|      | mor-      |
|      | phism.    |

Implements helib::EncryptedArrayBase.

# 7.44.3.2 buildLinPolyCoeffs() [1/3]

```
void helib::EncryptedArrayCx::buildLinPolyCoeffs (
    std::vector< zzX > & C,
    const cx_double & oneImage,
    const cx_double & iImage,
    long precision = 0 ) const
```

First variant: same linear transformation in all the slots.

# 7.44.3.3 buildLinPolyCoeffs() [2/3]

```
void helib::EncryptedArrayCx::buildLinPolyCoeffs (
    std::vector< zzX > & C,
    const std::vector< cx_double > & oneImages,
    const std::vector< cx_double > & iImages,
    long precision = 0 ) const
```

Second variant: different linear transformation in each slots.

# 7.44.3.4 buildLinPolyCoeffs() [3/3]

Unimplemented buildLinPolyCoeffs function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| С | Unused. |
|---|---------|
| L | Unused. |

#### 7.44.3.5 clone()

```
EncryptedArrayBase* helib::EncryptedArrayCx::clone ( ) const [inline], [override], [virtual]
```

Implements helib::EncryptedArrayBase.

### 7.44.3.6 convert() [1/4]

# 7.44.3.7 convert() [2/4]

#### 7.44.3.8 convert() [3/4]

# 7.44.3.9 convert() [4/4]

# 7.44.3.10 decode() [1/7]

```
void helib::EncryptedArrayCx::decode (
    std::vector< cx_double > & array,
    const NTL::ZZX & ptxt,
    double scaling ) const [inline]
```

# 7.44.3.11 decode() [2/7]

```
void helib::EncryptedArrayCx::decode (
    std::vector< cx_double > & array,
    const zzX & ptxt,
    double scaling ) const
```

# 7.44.3.12 decode() [3/7]

```
void helib::EncryptedArrayCx::decode (
    std::vector< double > & array,
    const NTL::ZZX & ptxt,
    double scaling ) const [inline]
```

# 7.44.3.13 decode() [4/7]

```
void helib::EncryptedArrayCx::decode (
    std::vector< double > & array,
    const zzX & ptxt,
    double scaling ) const [inline]
```

# 7.44.3.14 decode() [5/7]

Unimplemented decode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| array | Unused. |
|-------|---------|
| ptxt  | Unused. |

# 7.44.3.15 decode() [6/7]

Unimplemented decode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| array | Unused. |
|-------|---------|
| ptxt  | Unused. |

#### 7.44.3.16 decode() [7/7]

Unimplemented decode function for BGV. It will always throw helib::LogicError.

# **Parameters**

| array | Unused. |
|-------|---------|
| ptxt  | Unused. |

# 7.44.3.17 decrypt() [1/6]

Decrypt ciphertext to a plaintext relative to a specific scheme.

# **Template Parameters**

Scheme | Encryption scheme to be used (either BGV or CKKS).

# **Parameters**

| raiaiiiete |              |
|------------|--------------|
| ctxt       | Ciphertext   |
|            | to de-       |
|            | crypt.       |
| sKey       | Secret       |
|            | key          |
|            | to be        |
|            | used         |
|            | for de-      |
|            | cryp-        |
|            | tion.        |
| ptxt       | Plaintext    |
|            | into         |
|            | which        |
|            | to de-       |
|            | crypt.       |
|            | De-          |
|            | crypt a      |
|            | Ctxt         |
|            | cipher-      |
|            | text         |
|            | object       |
|            | to a         |
|            | Ptxt         |
|            | plain-       |
|            | text         |
|            | one<br>rela- |
|            | tive to      |
|            | a spe-       |
|            | cific        |
|            | scheme.      |
|            | Scrienie.    |

# 7.44.3.18 decrypt() [2/6]

Implements helib::EncryptedArrayBase.

# 7.44.3.19 decrypt() [3/6]

Implements helib::EncryptedArrayBase.

#### 7.44.3.20 decrypt() [4/6]

Unimplemented decrypt function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ctxt | Unused. |
|------|---------|
| sKey | Unused. |
| ptxt | Unused. |

## 7.44.3.21 decrypt() [5/6]

Unimplemented decrypt function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ctxt | Unused. |
|------|---------|
| sKey | Unused. |
| ptxt | Unused. |

#### 7.44.3.22 decrypt() [6/6]

Unimplemented decrypt function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ctxt | Unused. |
|------|---------|
| sKey | Unused. |
| ptxt | Unused. |

## 7.44.3.23 encode() [1/12]

## 7.44.3.24 encode() [2/12]

Unimplemented encode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ptxt  | Unused. |
|-------|---------|
| array | Unused. |

# 7.44.3.25 encode() [3/12]

Unimplemented encode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ptxt  | Unused. |
|-------|---------|
| array | Unused. |

## 7.44.3.26 encode() [4/12]

Unimplemented encode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ptxt  | Unused. |
|-------|---------|
| array | Unused. |

## 7.44.3.27 encode() [5/12]

Unimplemented encode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ptxt  | Unused. |
|-------|---------|
| array | Unused. |

## 7.44.3.28 encode() [6/12]

Unimplemented encode function for BGV. It will always throw helib::LogicError.

# **Parameters**

| ptxt  | Unused. |
|-------|---------|
| array | Unused. |

## 7.44.3.29 encode() [7/12]

Unimplemented encode function for BGV. It will always throw helib::LogicError.

#### **Parameters**

| ptxt  | Unused. |
|-------|---------|
| array | Unused. |

## 7.44.3.30 encode() [8/12]

```
template<typename Scheme >
double helib::EncryptedArrayCx::encode (
    zzX & out,
    const Ptxt< Scheme > & ptxt,
    double useThisSize,
    long precision = -1 ) const [inline]
```

Encode a Ptxt object into a zzX.

## **Template Parameters**

| Scheme | Encryption scheme to be used (either BGV or CKKS). |
|--------|--|
|--------|--|

## **Parameters**

| out         | Polynomia |
|-------------|-----------|
|             | to en-    |
|             | code      |
|             | into.     |
| ptxt        | Plaintext |
|             | Ptxt      |
|             | object    |
|             | to en-    |
|             | code.     |
| useThisSize | Size to   |
|             | use.      |
| precision   | Precision |
|             | to use.   |

## Returns

The scaling factor used in the encoding routine.

# 7.44.3.31 encode() [9/12]

```
double helib::EncryptedArrayCx::encode (
    zzX & ptxt,
    const std::vector< cx_double > & array,
    double useThisSize,
    long precision = -1 ) const
```

## 7.44.3.32 encode() [10/12]

```
double helib::EncryptedArrayCx::encode (
    zzX & ptxt,
    const std::vector< double > & array,
    double useThisSize,
    long precision = -1 ) const [inline]
```

## 7.44.3.33 encode() [11/12]

```
double helib::EncryptedArrayCx::encode (
    zzX & ptxt,
    const std::vector< long > & array,
    double useThisSize,
    long precision = -1 ) const [inline]
```

# 7.44.3.34 encode() [12/12]

```
double helib::EncryptedArrayCx::encode (
    zzX & ptxt,
    double aSingleNumber,
    double useThisSize = -1,
    long precision = -1 ) const
```

## 7.44.3.35 encodei()

#### 7.44.3.36 encodeRoundingError()

```
\verb|double| helib:: EncryptedArrayCx:: encodeRoundingError () const [inline]|
```

## 7.44.3.37 encodeScalingFactor()

## 7.44.3.38 encodeUnitSelector()

Encodes a std::vector with 1 at position i and 0 everywhere else.

Implements helib::EncryptedArrayBase.

## 7.44.3.39 encrypt() [1/2]

## 7.44.3.40 encrypt() [2/2]

## 7.44.3.41 encryptOneNum()

## 7.44.3.42 extractImPart() [1/2]

Note: If called with dcrt==nullptr, extractImPart will perform FFT's when encoding i as a DoubleCRT object. If called with dcrt!=nullptr, it assumes that dcrt points to an object that encodes i.

# 7.44.3.43 extractImPart() [2/2]

Extract the imaginary part of a CKKS plaintext.

## **Template Parameters**

| Scheme | Encryption scheme to be used (must be CKKS). |
|--------|--|
|--------|--|

#### **Parameters**

| р | Plaintext |
|---|-----------|
|   | on        |
|   | which     |
|   | to op-    |
|   | erate.    |

## 7.44.3.44 extractRealPart() [1/2]

## 7.44.3.45 extractRealPart() [2/2]

Extract the real part of a CKKS plaintext.

## **Template Parameters**

| 3 | Scheme | Encryption scheme to be used (must be CKKS). |
|---|--------|--|
|---|--------|--|

## **Parameters**



# 7.44.3.46 getContext()

```
\verb|const Context@helib::EncryptedArrayCx::getContext ( ) const [inline], [override], [virtual]| \\
```

## 7.44.3.47 getDegree()

```
long helib::EncryptedArrayCx::getDegree ( ) const [inline], [override], [virtual]
Implements helib::EncryptedArrayBase.
```

#### 7.44.3.48 getiEncoded()

```
const zzX & helib::EncryptedArrayCx::getiEncoded ( ) const
```

## 7.44.3.49 getP2R()

```
long helib::EncryptedArrayCx::getP2R ( ) const [inline], [override], [virtual]
```

Implements helib::EncryptedArrayBase.

## 7.44.3.50 getPAlgebra()

```
const PAlgebra& helib::EncryptedArrayCx::getPAlgebra ( ) const [inline], [override], [virtual]
Implements helib::EncryptedArrayBase.
```

# 7.44.3.51 getTag()

```
PA_tag helib::EncryptedArrayCx::getTag ( ) const [inline], [override], [virtual]
```

Implements helib::EncryptedArrayBase.

## 7.44.3.52 random() [1/4]

```
void helib::EncryptedArrayCx::random (  std::vector < cx\_double > \& array, \\ double \ rad = 1.0 \ ) \ const
```

#### 7.44.3.53 random() [2/4]

```
void helib::EncryptedArrayCx::random (  std::vector < double > \& \ array, \\ double \ rad = 1.0 \ ) \ const \ [inline]
```

## 7.44.3.54 random() [3/4]

Implements helib::EncryptedArrayBase.

## 7.44.3.55 random() [4/4]

Unimplemented random function for BGV. It will always throw helib::LogicError.

#### **Parameters**

```
array Unused.
```

#### 7.44.3.56 rotate()

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

Implements helib::EncryptedArrayBase.

#### 7.44.3.57 rotate1D()

right-rotate k positions along the i'th dimension

#### **Parameters**

| Parameters |         |  |
|------------|---------|--|
| dc         | means   |  |
|            | "don't  |  |
|            | care",  |  |
|            | which   |  |
|            | means   |  |
|            | that    |  |
|            | the     |  |
|            | caller  |  |
|            | guar-   |  |
|            | antees  |  |
|            | that    |  |
|            | only    |  |
|            | zero    |  |
|            | ele-    |  |
|            | ments   |  |
|            | rotate  |  |
|            | off the |  |
|            | end     |  |
|            | - this  |  |
|            | allows  |  |
|            | for     |  |
|            | some    |  |
|            | opti-   |  |
|            | miza-   |  |
|            | tions   |  |
|            | that    |  |
|            | would   |  |
|            | not     |  |
|            | other-  |  |
|            | wise    |  |
|            | be      |  |
|            | possi-  |  |
|            | ble     |  |

Implements helib::EncryptedArrayBase.

## 7.44.3.58 roundedSize()

## 7.44.3.59 shift()

Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)

#### 7.44.3.60 shift1D()

Right shift k positions along the i'th dimension with zero fill.

Implements helib::EncryptedArrayBase.

The documentation for this class was generated from the following files:

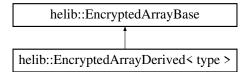
- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/EncryptedArray.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EaCx.cpp

# 7.45 helib::EncryptedArrayDerived< type > Class Template Reference

Derived concrete implementation of EncryptedArrayBase.

```
#include <EncryptedArray.h>
```

Inheritance diagram for helib::EncryptedArrayDerived< type >:



## **Public Member Functions**

- EncryptedArrayDerived (const Context &\_context, const RX &\_G, const PAlgebraMod &\_tab)
- EncryptedArrayDerived (const EncryptedArrayDerived &other)
- EncryptedArrayDerived & operator= (const EncryptedArrayDerived &other)
- virtual EncryptedArrayBase \* clone () const override
- virtual PA\_tag getTag () const override
- template < typename > class T, typename... Args > void dispatch (Args &&... args) const
- const RX & getG () const
- const NTL::Mat< R > & getNormalBasisMatrix () const
- const NTL::Mat< R > & getNormalBasisMatrixInverse () const
- · void initNormalBasisMatrix () const
- · virtual void restoreContext () const override
- virtual void restoreContextForG () const override
- virtual const Context & getContext () const override
- virtual const PAlgebra & getPAlgebra () const override
- virtual long getDegree () const override
- const PAlgebraModDerived< type > & getTab () const
- virtual void rotate (Ctxt &ctxt, long k) const override

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

- virtual void shift (Ctxt &ctxt, long k) const override
  - Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)
- virtual void rotate1D (Ctxt &ctxt, long i, long k, bool dc=false) const override
  - right-rotate k positions along the i'th dimension
- virtual void badDimensionAutomorphCorrection (Ctxt &ctxt, long i, long k) const override
  - Correct an automorphism in a bad dimension.
- long getP2R () const override
- template<typename U >
  - void rotate1D (std::vector < U > &out, const std::vector < U > &in, long i, long offset) const
- virtual void shift1D (Ctxt &ctxt, long i, long k) const override
  - Right shift k positions along the i'th dimension with zero fill.

Unimplemented decrypt function for CKKS. It will always throw helib::LogicError.

void decrypt (UNUSED const Ctxt &ctxt, UNUSED const SecKey &sKey, UNUSED std::vector < cx\_double > &ptxt) const override

Unimplemented decrypt function for CKKS. It will always throw helib::LogicError.

- virtual void encode (NTL::ZZX &ptxt, const std::vector< long > &array) const override
- virtual void encode (zzX &ptxt, const std::vector< long > &array) const override
- virtual void encode (NTL::ZZX &ptxt, const std::vector < NTL::ZZX > &array) const override
- virtual void encode (zzX &ptxt, const std::vector< zzX > &array) const override
- virtual void encode (NTL::ZZX &ptxt, const PlaintextArray &array) const override
- · virtual void encode (zzX &ptxt, const PlaintextArray &array) const override
- virtual void encodeUnitSelector (zzX &ptxt, long i) const override

Encodes a std::vector with 1 at position i and 0 everywhere else.

- virtual void decode (std::vector< long > &array, const NTL::ZZX &ptxt) const override
- virtual void decode (std::vector < NTL::ZZX > &array, const NTL::ZZX &ptxt) const override
- virtual void decode (PlaintextArray & array, const NTL::ZZX &ptxt) const override
- virtual void decode (PlaintextArray & array, const zzX &ptxt) const
- virtual void random (std::vector < long > &array) const override
- virtual void random (std::vector < NTL::ZZX > &array) const override
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector < long > &ptxt) const override
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector < NTL::ZZX > &ptxt) const override
- virtual void decrypt (const Ctxt &ctxt, const SecKey &sKey, PlaintextArray &ptxt) const override
- virtual void buildLinPolyCoeffs (std::vector< NTL::ZZX > &C, const std::vector< NTL::ZZX > &L) const over-ride

Linearized polynomials. L describes a linear map M by describing its action on the standard power basis:  $M(x^{\hat{}})$  mod G) = (L[j] mod G), for j = 0..d-1. The result is a coefficient std::vector C for the linearized polynomial representing M: a polynomial h in  $Z/(p^{\hat{}})$ [X] of degree X is sent to.

- void encode (zzX &ptxt, const std::vector< RX > &array) const
- void decode (std::vector< RX > &array, const zzX &ptxt) const
- void encode (NTL::ZZX &ptxt, const std::vector< RX > &array) const
- void decode (std::vector< RX > &array, const NTL::ZZX &ptxt) const
- void encode (RX &ptxt, const std::vector< RX > &array) const
- void decode (std::vector < RX > &array, const RX &ptxt) const
- void random (std::vector < RX > &array) const
- void decrypt (const Ctxt &ctxt, const SecKey &sKey, std::vector< RX > &ptxt) const
- virtual void buildLinPolyCoeffs (std::vector < RX > &C, const std::vector < RX > &L) const

#### 7.45.1 Detailed Description

template < typename type > class helib::EncryptedArrayDerived < type >

Derived concrete implementation of EncryptedArrayBase.

# 7.45.2 Constructor & Destructor Documentation

## 7.45.2.1 EncryptedArrayDerived() [1/2]

#### 7.45.2.2 EncryptedArrayDerived() [2/2]

## 7.45.3 Member Function Documentation

## 7.45.3.1 badDimensionAutomorphCorrection()

Correct an automorphism in a bad dimension.

#### Parameters

|      | phism.        | Generated by Doxygen |
|------|---------------|----------------------|
|      | auto-<br>mor- |                      |
|      | of the        |                      |
| amt  | Exponent      |                      |
|      | rect.         |                      |
|      | to cor-       |                      |
|      | which         |                      |
|      | of            |                      |
| i    | Dimension     | i<br>M               |
|      | on.           |                      |
|      | rection       |                      |
|      | cor-          |                      |
|      | the           |                      |
|      | form          |                      |
|      | to per-       |                      |
| ctxt | Ctxt          |                      |

Implements helib::EncryptedArrayBase.

#### 7.45.3.2 buildLinPolyCoeffs() [1/2]

Linearized polynomials. L describes a linear map M by describing its action on the standard power basis:  $M(x^{\hat{}})$  mod G) = (L[j] mod G), for j = 0..d-1. The result is a coefficient std::vector C for the linearized polynomial representing M: a polynomial h in  $Z/(p^{\hat{}})$ [X] of degree < d is sent to.

$$//!M(h(X) \bmod G) = \sum_{i=0}^{d-1} (C[j] \cdot h(X^{p^j})) \bmod G).//!$$

Implements helib::EncryptedArrayBase.

#### 7.45.3.3 buildLinPolyCoeffs() [2/2]

## 7.45.3.4 clone()

```
template<typename type >
virtual EncryptedArrayBase* helib::EncryptedArrayDerived< type >::clone ( ) const [inline],
[override], [virtual]
```

Implements helib::EncryptedArrayBase.

## 7.45.3.5 decode() [1/7]

#### 7.45.3.6 decode() [2/7]

## 7.45.3.7 decode() [3/7]

Implements helib::EncryptedArrayBase.

#### 7.45.3.8 decode() [4/7]

Implements helib::EncryptedArrayBase.

## 7.45.3.9 decode() [5/7]

## 7.45.3.10 decode() [6/7]

#### 7.45.3.11 decode() [7/7]

## 7.45.3.12 decrypt() [1/6]

Implements helib::EncryptedArrayBase.

## 7.45.3.13 decrypt() [2/6]

Implements helib::EncryptedArrayBase.

#### 7.45.3.14 decrypt() [3/6]

Implements helib::EncryptedArrayBase.

## 7.45.3.15 decrypt() [4/6]

#### 7.45.3.16 decrypt() [5/6]

Unimplemented decrypt function for CKKS. It will always throw helib::LogicError.

#### **Parameters**

| ctxt | Unused. |
|------|---------|
| sKey | Unused. |
| ptxt | Unused. |

## 7.45.3.17 decrypt() [6/6]

Unimplemented decrypt function for CKKS. It will always throw helib::LogicError.

#### **Parameters**

| ctxt | Unused. |
|------|---------|
| sKey | Unused. |
| ptxt | Unused. |

#### 7.45.3.18 dispatch()

# 7.45.3.19 encode() [1/9]

#### 7.45.3.20 encode() [2/9]

Implements helib::EncryptedArrayBase.

#### 7.45.3.21 encode() [3/9]

Implements helib::EncryptedArrayBase.

#### 7.45.3.22 encode() [4/9]

## 7.45.3.23 encode() [5/9]

#### 7.45.3.24 encode() [6/9]

#### 7.45.3.25 encode() [7/9]

Implements helib::EncryptedArrayBase.

## 7.45.3.26 encode() [8/9]

## 7.45.3.27 encode() [9/9]

Implements helib::EncryptedArrayBase.

## 7.45.3.28 encodeUnitSelector()

Encodes a std::vector with 1 at position i and 0 everywhere else.

Implements helib::EncryptedArrayBase.

## 7.45.3.29 getContext()

```
template<typename type >
virtual const Context& helib::EncryptedArrayDerived< type >::getContext ( ) const [inline],
[override], [virtual]
```

#### 7.45.3.30 getDegree()

```
template<typename type >
virtual long helib::EncryptedArrayDerived< type >::getDegree ( ) const [inline], [override],
[virtual]
```

Implements helib::EncryptedArrayBase.

## 7.45.3.31 getG()

```
template<typename type >
const RX& helib::EncryptedArrayDerived< type >::getG ( ) const [inline]
```

## 7.45.3.32 getNormalBasisMatrix()

```
template<typename type >
const NTL::Mat<R>& helib::EncryptedArrayDerived< type >::getNormalBasisMatrix ( ) const [inline]
```

## 7.45.3.33 getNormalBasisMatrixInverse()

## 7.45.3.34 getP2R()

```
template<typename type >
long helib::EncryptedArrayDerived< type >::getP2R ( ) const [inline], [override], [virtual]
```

Implements helib::EncryptedArrayBase.

## 7.45.3.35 getPAlgebra()

```
template<typename type >
virtual const PAlgebra& helib::EncryptedArrayDerived< type >::getPAlgebra ( ) const [inline],
[override], [virtual]
```

#### 7.45.3.36 getTab()

```
template<typename type >
const PAlgebraModDerived<type>& helib::EncryptedArrayDerived< type >::getTab ( ) const [inline]
```

## 7.45.3.37 getTag()

```
template<typename type >
virtual PA_tag helib::EncryptedArrayDerived< type >::getTag ( ) const [inline], [override],
[virtual]
```

Implements helib::EncryptedArrayBase.

#### 7.45.3.38 initNormalBasisMatrix()

```
template<typename type >
void helib::EncryptedArrayDerived< type >::initNormalBasisMatrix
```

#### 7.45.3.39 operator=()

## 7.45.3.40 random() [1/3]

Implements helib::EncryptedArrayBase.

## 7.45.3.41 random() [2/3]

#### 7.45.3.42 random() [3/3]

#### 7.45.3.43 restoreContext()

```
template<typename type >
virtual void helib::EncryptedArrayDerived< type >::restoreContext ( ) const [inline], [override],
[virtual]
```

Reimplemented from helib::EncryptedArrayBase.

#### 7.45.3.44 restoreContextForG()

```
template<typename type >
virtual void helib::EncryptedArrayDerived< type >::restoreContextForG ( ) const [inline],
[override], [virtual]
```

Reimplemented from helib::EncryptedArrayBase.

#### 7.45.3.45 rotate()

Right rotation as a linear array. E.g., rotating ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(n 1 2 ... n-1)

Implements helib::EncryptedArrayBase.

#### 7.45.3.46 rotate1D() [1/2]

right-rotate k positions along the i'th dimension

#### **Parameters**

| dc means "don't care", which means that the caller guar- antees that only zero ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi- ble | 'aram | eters                  |
|--|-------|------------------------|
| care", which means that the caller guarantees that only zero elements rotate off the end — this allows for some optimizations that would not otherwise be possi-                               | dc    | means                  |
| which means that the caller guarantees that only zero elements rotate off the end — this allows for some optimizations that would not otherwise be possi-                                      |       | "don't                 |
| means that the caller guarantees that only zero elements rotate off the end — this allows for some optimizations that would not otherwise be possi-  |       | · · · · ·              |
| that the caller guar- antees that only zero ele- ments rotate off the end — this allows for some opti- miza- tions that would not other- wise be possi-  |       | which                  |
| the caller guar- antees that only zero ele- ments rotate off the end — this allows for some opti- miza- tions that would not other- wise be possi-   |       | means                  |
| caller guar- antees that only zero ele- ments rotate off the end  - this allows for some opti- miza- tions that would not other- wise be possi-  |       | that                   |
| guarantees that only zero ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-  |       | the                    |
| antees that only zero ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-  |       | caller                 |
| that only zero ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-   |       | guar-                  |
| only zero ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-  |       | antees                 |
| zero ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-   |       | that                   |
| ele- ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-  |       | only                   |
| ments rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-   |       | zero                   |
| rotate off the end - this allows for some opti- miza- tions that would not other- wise be possi-   |       | ele-                   |
| off the end  - this allows for some optimizations that would not otherwise be possi-   |       | ments                  |
| end - this allows for some opti- miza- tions that would not other- wise be possi-  |       | rotate                 |
| - this allows for some optimizations that would not otherwise be possi-  |       | off the                |
| allows for some opti- miza- tions that would not other- wise be possi-   |       | end                    |
| for some optimizations that would not otherwise be possi-  |       | <ul><li>this</li></ul> |
| some opti- miza- tions that would not other- wise be possi-  |       | allows                 |
| opti- miza- tions that would not other- wise be possi-   |       | for                    |
| miza-<br>tions<br>that<br>would<br>not<br>other-<br>wise<br>be<br>possi-   |       | some                   |
| tions that would not other- wise be possi-   |       |                        |
| that would not other- wise be possi-   |       |                        |
| would<br>not<br>other-<br>wise<br>be<br>possi-   |       | tions                  |
| not<br>other-<br>wise<br>be<br>possi-  |       |                        |
| other-<br>wise<br>be<br>possi-   |       | would                  |
| wise<br>be<br>possi-   |       |                        |
| be<br>possi-   |       |                        |
| possi-   |       |                        |
| l .  |       |                        |
| ble  |       |                        |
|  |       | ble                    |

Implements helib::EncryptedArrayBase.

# 7.45.3.47 rotate1D() [2/2]

#### 7.45.3.48 shift()

Non-cyclic right shift with zero fill E.g., shifting ctxt=Enc(1 2 3 ... n) by k=1 gives Enc(0 1 2... n-1)

Implements helib::EncryptedArrayBase.

## 7.45.3.49 shift1D()

Right shift k positions along the i'th dimension with zero fill.

Implements helib::EncryptedArrayBase.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/EncryptedArray.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.46 helib::equals\_pa\_impl< type > Class Template Reference

#### **Static Public Member Functions**

- static void apply (const EncryptedArrayDerived< type > &ea, bool &res, const PlaintextArray &pa, const PlaintextArray &other)
- static void apply (const EncryptedArrayDerived< type > &ea, bool &res, const PlaintextArray &pa, const std::vector< long > &other)
- static void apply (const EncryptedArrayDerived< type > &ea, bool &res, const PlaintextArray &pa, const std::vector< NTL::ZZX > &other)

#### 7.46.1 Member Function Documentation

#### 7.46.1.1 apply() [1/3]

## 7.46.1.2 apply() [2/3]

#### 7.46.1.3 apply() [3/3]

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.47 helib::EvalMap Class Reference

Class that provides the functionality for the linear transforms used in boostrapping. The constructor is invoked with three arguments:

```
#include <EvalMap.h>
```

#### **Public Member Functions**

- EvalMap (const EncryptedArray &\_ea, bool minimal, const NTL::Vec< long > &mvec, bool \_invert, bool build\_cache, bool normal\_basis=true)
- void upgrade ()
- · void apply (Ctxt &ctxt) const

## 7.47.1 Detailed Description

Class that provides the functionality for the linear transforms used in boostrapping. The constructor is invoked with three arguments:

- an EncryptedArray object ea
- · an integer vector mvec
- a boolean flag invert The mvec vector specifies the factorization of m to use in the "powerful basis" decomposition.

If the invert flag is false, the forward transformation is used. This transformation views the slots as being packed with powerful-basis coefficients and performs a multi-point polynomial evaluation. This is the second transformation used in bootstrapping.

If invert flag is true, the inverse transformation is used. In addition, the current implementation folds into the inverse transformation a transformation that moves the coefficients in each slot into a normal-basis representation, which helps with the unpacking procedure.

The constructor precomputes certain values, and the linear transformation itself is effected using the apply method.

Note that the factorization in mvec must correspond to the generators used in PAlgebra. The best way to ensure this is to directly use the output of the program in params.cpp: that program computes values for mvec (to be used here), and gens and ords (to be used in initialization of the Context).

## 7.47.2 Constructor & Destructor Documentation

## 7.47.2.1 EvalMap()

#### 7.47.3 Member Function Documentation

## 7.47.3.1 apply()

## 7.47.3.2 upgrade()

```
void helib::EvalMap::upgrade ( )
```

The documentation for this class was generated from the following files:

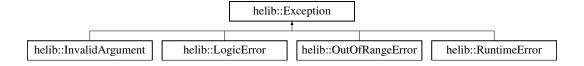
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/EvalMap.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EvalMap.cpp

# 7.48 helib::Exception Class Reference

Base class that other HElib exception classes inherit from.

```
#include <exceptions.h>
```

Inheritance diagram for helib::Exception:



## **Public Member Functions**

- virtual ∼Exception ()=default
- virtual const char \* what () const noexcept=0

## **Protected Member Functions**

• Exception ()=default

# 7.48.1 Detailed Description

Base class that other HElib exception classes inherit from.

## 7.48.2 Constructor & Destructor Documentation

## 7.48.2.1 $\sim$ Exception()

```
virtual helib::Exception::~Exception ( ) [virtual], [default]
```

#### 7.48.2.2 Exception()

```
helib::Exception::Exception ( ) [protected], [default]
```

#### 7.48.3 Member Function Documentation

#### 7.48.3.1 what()

```
virtual const char* helib::Exception::what ( ) const [pure virtual], [noexcept]
```

Implemented in helib::InvalidArgument, helib::RuntimeError, helib::OutOfRangeError, and helib::LogicError.

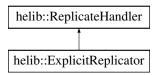
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/exceptions.h

# 7.49 helib::ExplicitReplicator Class Reference

An implementation of ReplicateHandler that explicitly returns all the replicated ciphertexts in one big vector.

Inheritance diagram for helib::ExplicitReplicator:



## **Public Member Functions**

- ExplicitReplicator (std::vector < Ctxt > &\_v)
- virtual void handle (const Ctxt &ctxt)

## 7.49.1 Detailed Description

An implementation of ReplicateHandler that explicitly returns all the replicated ciphertexts in one big vector.

This is useful mostly for debugging purposes, for real parameters it would take a lot of memory.

# 7.49.2 Constructor & Destructor Documentation

## 7.49.2.1 ExplicitReplicator()

```
\label{eq:helib::explicitReplicator::explicitReplicator (} $$ std::vector< Ctxt > \& v ) [inline]
```

#### 7.49.3 Member Function Documentation

## 7.49.3.1 handle()

Implements helib::ReplicateHandler.

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/replicate.cpp

# 7.50 helib::fhe\_stats\_record Struct Reference

```
#include <fhe_stats.h>
```

#### **Public Member Functions**

- fhe\_stats\_record (const char \*\_name)
- void update (double val)
- void save (double val)

## **Public Attributes**

- const char \* name
- · long count
- double sum
- double max
- std::vector< double > saved\_values

## **Static Public Attributes**

static std::vector< fhe\_stats\_record \* > map

## 7.50.1 Constructor & Destructor Documentation

## 7.50.1.1 fhe\_stats\_record()

# 7.50.2 Member Function Documentation

## 7.50.2.1 save()

## 7.50.2.2 update()

# 7.50.3 Member Data Documentation

#### 7.50.3.1 count

long helib::fhe\_stats\_record::count

# 7.50.3.2 map

```
std::vector<fhe_stats_record*> helib::fhe_stats_record::map [static]
```

## 7.50.3.3 max

double helib::fhe\_stats\_record::max

#### 7.50.3.4 name

const char\* helib::fhe\_stats\_record::name

## 7.50.3.5 saved\_values

std::vector<double> helib::fhe\_stats\_record::saved\_values

#### 7.50.3.6 sum

double helib::fhe\_stats\_record::sum

The documentation for this struct was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/fhe\_stats.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/fhe\_stats.cpp

# 7.51 helib::FHEtimer Class Reference

A simple class to accumulate time.

#include <timing.h>

## **Public Member Functions**

- FHEtimer (const char \*\_name, const char \*\_loc)
- void reset ()
- double getTime () const
- long getNumCalls () const

## **Public Attributes**

- const char \* name
- const char \* loc
- HELIB\_atomic\_ulong counter
- HELIB\_atomic\_long numCalls

## 7.51.1 Detailed Description

A simple class to accumulate time.

# 7.51.2 Constructor & Destructor Documentation

## 7.51.2.1 FHEtimer()

## 7.51.3 Member Function Documentation

## 7.51.3.1 getNumCalls()

```
long helib::FHEtimer::getNumCalls ( ) const
```

## 7.51.3.2 getTime()

```
double helib::FHEtimer::getTime ( ) const
```

## 7.51.3.3 reset()

```
void helib::FHEtimer::reset ( )
```

## 7.51.4 Member Data Documentation

# 7.51.4.1 counter

```
HELIB_atomic_ulong helib::FHEtimer::counter
```

# 7.51.4.2 loc

```
const char* helib::FHEtimer::loc
```

## 7.51.4.3 name

```
const char* helib::FHEtimer::name
```

#### 7.51.4.4 numCalls

```
HELIB_atomic_long helib::FHEtimer::numCalls
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/timing.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/timing.cpp

# 7.52 helib::FlowEdge Class Reference

An edge in a flow graph.

```
#include <matching.h>
```

## **Public Member Functions**

• FlowEdge (long c=0, long f=0)

#### **Public Attributes**

- · long capacity
- · long flow

# 7.52.1 Detailed Description

An edge in a flow graph.

## 7.52.2 Constructor & Destructor Documentation

## 7.52.2.1 FlowEdge()

```
helib::FlowEdge::FlowEdge ( long \ c \ = \ 0 \, , long \ f \ = \ 0 \ ) \quad [inline] \, , \ [explicit]
```

## 7.52.3 Member Data Documentation

## 7.52.3.1 capacity

long helib::FlowEdge::capacity

## 7.52.3.2 flow

```
long helib::FlowEdge::flow
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matching.h

# 7.53 helib::frobeniusAutomorph\_pa\_impl< type > Class Template Reference

# **Static Public Member Functions**

- static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, long j)
- static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const NTL::Vec< long > &vec)

#### 7.53.1 Member Function Documentation

## 7.53.1.1 apply() [1/2]

#### 7.53.1.2 apply() [2/2]

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.54 helib::FullBinaryTree Class Reference

A simple implementation of full binary trees (each non-leaf has 2 children)

```
#include <permutations.h>
```

#### **Public Member Functions**

- FullBinaryTree (long \_aux=0)
- FullBinaryTree (const T &d, long \_aux=0)
- void putDataInRoot (const T &d)
- long size ()
- TreeNode< T > & operator[] (long i)
- const TreeNode< T > & operator[] (long i) const
- TreeNode< T > & at (long i)
- const TreeNode< T > & at (long i) const
- T & DataOfNode (long i)
- · const T & DataOfNode (long i) const
- long getAuxKey () const
- void setAuxKey (long \_aux)
- long getNleaves () const
- long firstLeaf () const
- long nextLeaf (long i) const
- long prevLeaf (long i) const
- long lastLeaf () const
- long rootldx () const
- long parentldx (long i) const
- · long leftChildldx (long i) const
- long rightChildldx (long i) const
- void printout (std::ostream &s, long idx=0) const
- long addChildren (long prntldx, const T &leftData, const T &rightData)
- void collapseToRoot ()

Remove all nodes in the tree except for the root.

## 7.54.1 Detailed Description

A simple implementation of full binary trees (each non-leaf has 2 children)

## 7.54.2 Constructor & Destructor Documentation

## 7.54.2.1 FullBinaryTree() [1/2]

#### 7.54.2.2 FullBinaryTree() [2/2]

## 7.54.3 Member Function Documentation

## 7.54.3.1 addChildren()

If the parent is a leaf, add to it to children with the given data, else just update the data of the two children of this parent. Returns the index of the left child, the right-child index is one more than the left-child index.

#### 7.54.3.2 at() [1/2]

## 7.54.3.3 at() [2/2]

## 7.54.3.4 collapseToRoot()

```
void helib::FullBinaryTree::collapseToRoot ( ) [inline]
```

Remove all nodes in the tree except for the root.

## 7.54.3.5 DataOfNode() [1/2]

```
T& helib::FullBinaryTree::DataOfNode ( \log \ i \ ) \quad [inline]
```

## 7.54.3.6 DataOfNode() [2/2]

```
\begin{tabular}{ll} \begin{tabular}{ll} const T& helib::FullBinaryTree::DataOfNode ( \\ long $i$ ) const [inline] \end{tabular}
```

## 7.54.3.7 firstLeaf()

```
long helib::FullBinaryTree::firstLeaf ( ) const [inline]
```

## 7.54.3.8 getAuxKey()

```
long helib::FullBinaryTree::getAuxKey ( ) const [inline]
```

## 7.54.3.9 getNleaves()

```
long helib::FullBinaryTree::getNleaves ( ) const [inline]
```

## 7.54.3.10 lastLeaf()

```
long helib::FullBinaryTree::lastLeaf ( ) const [inline]
```

## 7.54.3.11 leftChildldx()

## 7.54.3.12 nextLeaf()

```
long helib::FullBinaryTree::nextLeaf ( \log i \text{ ) const [inline]}
```

## 7.54.3.13 operator[]() [1/2]

#### 7.54.3.14 operator[]() [2/2]

## 7.54.3.15 parentldx()

## 7.54.3.16 prevLeaf()

## 7.54.3.17 printout()

## 7.54.3.18 putDataInRoot()

## 7.54.3.19 rightChildldx()

## 7.54.3.20 rootldx()

```
long helib::FullBinaryTree::rootIdx ( ) const [inline]
```

## 7.54.3.21 setAuxKey()

## 7.54.3.22 size()

```
long helib::FullBinaryTree::size ( ) [inline]
```

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h

# 7.55 helib::GenDescriptor Class Reference

A minimal description of a generator for the purpose of building tree.

```
#include <permutations.h>
```

## **Public Member Functions**

- GenDescriptor (long \_order, bool \_good, long gen=0)
- GenDescriptor ()

## **Public Attributes**

- long genldx
- long order
- bool good

## 7.55.1 Detailed Description

A minimal description of a generator for the purpose of building tree.

## 7.55.2 Constructor & Destructor Documentation

## 7.55.2.1 GenDescriptor() [1/2]

## 7.55.2.2 GenDescriptor() [2/2]

```
\verb|helib::GenDescriptor::GenDescriptor ( ) [inline]|\\
```

## 7.55.3 Member Data Documentation

## 7.55.3.1 genldx

```
long helib::GenDescriptor::genIdx
```

## 7.55.3.2 good

```
bool helib::GenDescriptor::good
```

#### 7.55.3.3 order

```
long helib::GenDescriptor::order
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h

# 7.56 helib::general\_range< T > Class Template Reference

```
#include <range.h>
```

#### **Classes**

· class iterator

## **Public Member Functions**

- iterator begin () const
- iterator end () const
- general\_range (T begin, T end)

## 7.56.1 Constructor & Destructor Documentation

## 7.56.1.1 general\_range()

## 7.56.2 Member Function Documentation

## 7.56.2.1 begin()

```
template<typename T >
iterator helib::general_range< T >::begin ( ) const [inline]
```

#### 7.56.2.2 end()

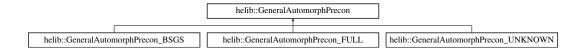
```
template<typename T >
iterator helib::general_range< T >::end ( ) const [inline]
```

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/range.h

# 7.57 helib::GeneralAutomorphPrecon Class Reference

Inheritance diagram for helib::GeneralAutomorphPrecon:



#### **Public Member Functions**

- virtual ∼GeneralAutomorphPrecon ()
- virtual std::shared\_ptr< Ctxt > automorph (long i) const =0

## 7.57.1 Constructor & Destructor Documentation

#### 7.57.1.1 ∼GeneralAutomorphPrecon()

```
virtual helib::GeneralAutomorphPrecon::~GeneralAutomorphPrecon ( ) [inline], [virtual]
```

## 7.57.2 Member Function Documentation

## 7.57.2.1 automorph()

```
\label{local_virtual} \begin{tabular}{ll} virtual & std::shared_ptr<Ctxt> & helib::GeneralAutomorphPrecon::automorph ( & long $i$ ) const [pure virtual] \end{tabular}
```

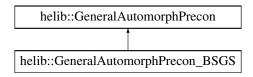
Implemented in helib::GeneralAutomorphPrecon\_BSGS, helib::GeneralAutomorphPrecon\_FULL, and helib::GeneralAutomorphPreco

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.58 helib::GeneralAutomorphPrecon\_BSGS Class Reference

Inheritance diagram for helib::GeneralAutomorphPrecon\_BSGS:



#### **Public Member Functions**

- GeneralAutomorphPrecon\_BSGS (const Ctxt &\_ctxt, long \_dim, const EncryptedArray &ea)
- std::shared ptr< Ctxt > automorph (long i) const override

## 7.58.1 Constructor & Destructor Documentation

## 7.58.1.1 GeneralAutomorphPrecon BSGS()

## 7.58.2 Member Function Documentation

## 7.58.2.1 automorph()

```
\begin{tabular}{ll} {\tt std::shared\_ptr<Ctxt>} & helib::GeneralAutomorphPrecon\_BSGS::automorph ( \\ & long $i$ ) const [inline], [override], [virtual] \end{tabular}
```

Implements helib::GeneralAutomorphPrecon.

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.59 helib::GeneralAutomorphPrecon\_FULL Class Reference

Inheritance diagram for helib::GeneralAutomorphPrecon FULL:

```
helib::GeneralAutomorphPrecon
helib::GeneralAutomorphPrecon_FULL
```

#### **Public Member Functions**

- GeneralAutomorphPrecon\_FULL (const Ctxt &\_ctxt, long \_dim, const EncryptedArray &ea)
- std::shared ptr< Ctxt > automorph (long i) const override

## 7.59.1 Constructor & Destructor Documentation

#### 7.59.1.1 GeneralAutomorphPrecon\_FULL()

## 7.59.2 Member Function Documentation

#### 7.59.2.1 automorph()

```
\begin{tabular}{ll} {\tt std::shared\_ptr<Ctxt>} & helib::GeneralAutomorphPrecon\_FULL::automorph ( \\ & long $i$ ) const [inline], [override], [virtual] \end{tabular}
```

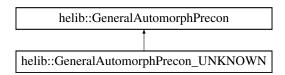
Implements helib::GeneralAutomorphPrecon.

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

## 7.60 helib::GeneralAutomorphPrecon UNKNOWN Class Reference

Inheritance diagram for helib::GeneralAutomorphPrecon\_UNKNOWN:



#### **Public Member Functions**

- GeneralAutomorphPrecon\_UNKNOWN (const Ctxt &\_ctxt, long \_dim, const EncryptedArray &ea)
- std::shared\_ptr< Ctxt > automorph (long i) const override

#### 7.60.1 Constructor & Destructor Documentation

#### 7.60.1.1 GeneralAutomorphPrecon\_UNKNOWN()

#### 7.60.2 Member Function Documentation

#### 7.60.2.1 automorph()

```
\label{local_state} $$ std::shared_ptr<Ctxt> helib::GeneralAutomorphPrecon_UNKNOWN::automorph ( long $i$ ) const [inline], [override], [virtual]
```

Implements helib::GeneralAutomorphPrecon.

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

## 7.61 helib::GeneralBenesNetwork Class Reference

Implementation of generalized Benes Permutation Network.

```
#include <permutations.h>
```

## **Public Member Functions**

- long getDepth () const
- long getSize () const
- long getNumLevels () const
- const NTL::Vec< short > & getLevel (long i) const
- long levelToDepthMap (long i) const
- long shamt (long i) const
- GeneralBenesNetwork (const Permut &perm)
- bool testNetwork (const Permut &perm) const

#### **Static Public Member Functions**

- static long depth (long n)
- static long levelToDepthMap (UNUSED long n, long k, long i)
- static long shamt (long n, long k, long i)

## 7.61.1 Detailed Description

Implementation of generalized Benes Permutation Network.

#### 7.61.2 Constructor & Destructor Documentation

## 7.61.2.1 GeneralBenesNetwork()

#### 7.61.3 Member Function Documentation

## 7.61.3.1 depth()

```
static long helib::GeneralBenesNetwork::depth ( long n ) [inline], [static]
```

computes recursion depth k for generalized Benes network of size n. the actual number of levels in the network is 2\*k-1

## 7.61.3.2 getDepth()

```
long helib::GeneralBenesNetwork::getDepth ( ) const [inline]
```

#### 7.61.3.3 getLevel()

```
\label{lem:const_NTL} $$\operatorname{NTL}::\operatorname{Vec}_s\operatorname{hort}_k $$ helib::\operatorname{GeneralBenesNetwork}::\operatorname{getLevel} ($$ long $i$ ) const [inline]
```

## 7.61.3.4 getNumLevels()

```
long helib::GeneralBenesNetwork::getNumLevels ( ) const [inline]
```

#### 7.61.3.5 getSize()

```
long helib::GeneralBenesNetwork::getSize ( ) const [inline]
```

## 7.61.3.6 levelToDepthMap() [1/2]

```
long helib::GeneralBenesNetwork::levelToDepthMap ( long \ i \ ) \ const \ \ [inline]
```

## 7.61.3.7 levelToDepthMap() [2/2]

 $maps \ a \ level \ number \ i = 0..2*k-2 \ to \ a \ recursion \ depth \ d = 0..k-1 \ using \ the \ formula \ d = (k-1)-\left|(k-1)-i\right|$ 

## 7.61.3.8 shamt() [1/2]

```
long helib::GeneralBenesNetwork::shamt ( \log \ i \ ) \ {\tt const} \ \ [{\tt inline}]
```

## 7.61.3.9 shamt() [2/2]

shift amount for level number i=0..2\*k-2 using the formula ceil( floor( $n/2^{\circ}d$ ) / 2), where d = levelToDepthMap(i)

#### 7.61.3.10 testNetwork()

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/BenesNetwork.cpp

## 7.62 helib::GeneratorTrees Class Reference

A std::vector of generator trees, one per generator in Zm\*/(p)

```
#include <permutations.h>
```

#### **Public Member Functions**

- · GeneratorTrees ()
- long numLayers () const
- long numTrees () const
- long getSize () const
- OneGeneratorTree & operator[] (long i)
- const OneGeneratorTree & operator[] (long i) const
- OneGeneratorTree & at (long i)
- const OneGeneratorTree & at (long i) const
- OneGeneratorTree & getGenTree (long i)
- const OneGeneratorTree & getGenTree (long i) const
- const Permut & mapToCube () const
- const Permut & mapToArray () const
- Permut & mapToCube ()
- Permut & mapToArray ()
- long mapToCube (long i) const
- long mapToArray (long i) const
- void getCubeDims (NTL::Vec< long > &dims) const
- void getCubeSubDims (NTL::Vec< long > &dims) const
- long buildOptimalTrees (const NTL::Vec< GenDescriptor > &vec, long depthBound)
- void ComputeCubeMapping ()

Computes permutations mapping between linear array and the cube.

#### **Friends**

• std::ostream & operator<< (std::ostream &s, const GeneratorTrees &t)

## 7.62.1 Detailed Description

A std::vector of generator trees, one per generator in Zm\*/(p)

#### 7.62.2 Constructor & Destructor Documentation

#### 7.62.2.1 GeneratorTrees()

```
helib::GeneratorTrees::GeneratorTrees ( ) [inline]
```

#### 7.62.3 Member Function Documentation

## 7.62.3.1 at() [1/2]

#### 7.62.3.2 at() [2/2]

```
const OneGeneratorTree& helib::GeneratorTrees::at ( long \ i \ ) \ const \ [inline]
```

#### 7.62.3.3 buildOptimalTrees()

Compute the trees corresponding to the "optimal" way of breaking a permutation into dimensions, subject to some constraints. Returns the cost (# of 1D shifts) of this solution. Returns NTL\_MAX\_LONG if no solution

## 7.62.3.4 ComputeCubeMapping()

```
void helib::GeneratorTrees::ComputeCubeMapping ( )
```

Computes permutations mapping between linear array and the cube.

If the cube dimensions (i.e., leaves of tree) are n1,n2,...,nt and N=\prod\_j n\_j is the size of the cube, then an integer i can be represented in either the mixed base of the n\_j's or in "CRT basis" relative to the leaves: Namely either i = \sum\_{j <=t} i\_j \* \prod\_{k>j} n\_k, or i = \sum\_leaf i'\_leaf \* leaf.e mod N.

The breakPermByDim procedure expects its input in the mixed-base representation, and the maps are used to convert back and forth. Specifically, let (i'\_1,...,i'\_t) be the CRT representation of i in this cube, and  $j = \sum_{i=1}^{t} i'_j * \pmod{k} n_k$ , then we have map2cube[i]=i and map2array[j]=i.

## 7.62.3.5 getCubeDims()

```
void helib::GeneratorTrees::getCubeDims ( \label{eq:ntl:vec} {\tt NTL::Vec} < {\tt long} > {\tt \&} \ {\tt dims} \ ) \ {\tt const}
```

Get the "crude" cube dimensions corresponding to the vector of trees, the ordered vector with one dimension per tree

## 7.62.3.6 getCubeSubDims()

```
void helib::GeneratorTrees::getCubeSubDims ( \label{eq:ntl:vec} {\tt NTL::Vec} < {\tt long} ~ \& ~ {\it dims} ~) ~ {\tt const}
```

Get the "fine" cube dimensions corresponding to the vector of trees, the ordered vector with one dimension per leaf in all the trees.

# 7.62.3.7 getGenTree() [1/2]

```
OneGeneratorTree& helib::GeneratorTrees::getGenTree ( long i ) [inline]
```

## 7.62.3.8 getGenTree() [2/2]

```
\begin{tabular}{ll} \begin{tabular}{ll} const & OneGeneratorTree \& & helib::GeneratorTrees::getGenTree & long $i$ ) const & [inline] \\ \end{tabular}
```

## 7.62.3.9 getSize()

```
long helib::GeneratorTrees::getSize ( ) const [inline]
```

## 7.62.3.10 mapToArray() [1/3]

```
Permut& helib::GeneratorTrees::mapToArray ( ) [inline]
```

## 7.62.3.11 mapToArray() [2/3]

```
const Permut& helib::GeneratorTrees::mapToArray ( ) const [inline]
```

```
7.62.3.12 mapToArray() [3/3]
```

```
long helib::GeneratorTrees::mapToArray ( \label{eq:const} \mbox{long $i$ ) const [inline]}
```

## 7.62.3.13 mapToCube() [1/3]

```
Permut& helib::GeneratorTrees::mapToCube ( ) [inline]
```

## 7.62.3.14 mapToCube() [2/3]

```
const Permut& helib::GeneratorTrees::mapToCube ( ) const [inline]
```

## 7.62.3.15 mapToCube() [3/3]

## 7.62.3.16 numLayers()

```
long helib::GeneratorTrees::numLayers ( ) const [inline]
```

## 7.62.3.17 numTrees()

```
long helib::GeneratorTrees::numTrees ( ) const [inline]
```

## 7.62.3.18 operator[]() [1/2]

#### 7.62.3.19 operator[]() [2/2]

```
const OneGeneratorTree& helib::GeneratorTrees::operator[] ( long \ i \ ) \ const \ [inline]
```

#### 7.62.4 Friends And Related Function Documentation

## 7.62.4.1 operator <<

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/OptimizePermutations.cpp
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/permutations.cpp

# 7.63 helib::half\_FFT Struct Reference

```
#include <PAlgebra.h>
```

## **Public Member Functions**

• half\_FFT (long m)

#### **Public Attributes**

- PGFFT fft
- std::vector< std::complex< double > > pow

## 7.63.1 Constructor & Destructor Documentation

#### 7.63.1.1 half\_FFT()

## 7.63.2 Member Data Documentation

#### 7.63.2.1 fft

```
PGFFT helib::half_FFT::fft
```

## 7.63.2.2 pow

```
std::vector<std::complex<double> > helib::half_FFT::pow
```

The documentation for this struct was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PAlgebra.cpp

# 7.64 HighLvlTimingData Class Reference

## **Public Member Functions**

• HighLvlTimingData (long \_lvl=-1)

## **Public Attributes**

- long lvl
- double rotate
- · double shift
- double permute
- · double matmul
- · double replicate
- double repIAII

## 7.64.1 Constructor & Destructor Documentation

## 7.64.1.1 HighLvlTimingData()

```
\label{eq:highLvlTimingData::HighLvlTimingData} \mbox{ (} \\ \mbox{long } \_lvl = -1 \mbox{ ) [inline], [explicit]}
```

## 7.64.2 Member Data Documentation

# 7.64.2.1 |v| long HighLvlTimingData::lvl

double HighLvlTimingData::matmul

## 7.64.2.3 permute

7.64.2.2 matmul

double HighLvlTimingData::permute

#### 7.64.2.4 repIAII

double HighLvlTimingData::replAll

## 7.64.2.5 replicate

double HighLvlTimingData::replicate

## 7.64.2.6 rotate

double HighLvlTimingData::rotate

## 7.64.2.7 shift

double HighLvlTimingData::shift

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Timing.cpp

# 7.65 helib::HyperCube < T > Class Template Reference

A multi-dimensional cube.

```
#include <hypercube.h>
```

#### **Public Member Functions**

```
    HyperCube (const HyperCube &other)=default
```

HyperCube (const CubeSignature &\_sig)

initialize a HyperCube with a CubeSignature

HyperCube & operator= (const HyperCube < T > & other)

assignment: signatures must be the same

bool operator== (const HyperCube< T > &other) const

equality testing: signatures must be the same

- bool operator!= (const HyperCube< T > &other) const
- const CubeSignature & getSig () const

const ref to signature

- NTL::Vec< T > & getData ()
- const NTL::Vec< T > & getData () const

read-only ref to data vector

• long getSize () const

total size of cube

long getNumDims () const

number of dimensions

· long getDim (long d) const

size of dimension d

long getProd (long d) const

product of sizes of dimensions d, d+1, ...

• long getProd (long from, long to) const

product of sizes of dimensions from, from+1, ..., to-1

long getCoord (long i, long d) const

get coordinate in dimension d of index i

· long addCoord (long i, long d, long offset) const

add offset to coordinate in dimension d of index i

• long numSlices (long d=1) const

number of slices

• long sliceSize (long d=1) const

size of one slice

• long numCols () const

number of columns

• T & at (long i)

reference to element at position i, with bounds check

• T & operator[] (long i)

reference to element at position i, without bounds check

· const T & at (long i) const

read-only reference to element at position i, with bounds check

const T & operator[] (long i) const

read-only reference to element at position i, without bounds check

void rotate1D (long i, long k)

rotate k positions along the i'th dimension

• void shift1D (long i, long k)

Shift k positions along the i'th dimension with zero fill.

## 7.65.1 Detailed Description

```
template < typename T> class helib::HyperCube < T>
```

A multi-dimensional cube.

Such an object is initialized with a CubeSignature: a reference to the signature is stored with the cube, and so the signature must remain alive during the lifetime of the cube, to prevent dangling pointers.

#### 7.65.2 Constructor & Destructor Documentation

## 7.65.2.1 HyperCube() [1/2]

## 7.65.2.2 HyperCube() [2/2]

initialize a HyperCube with a CubeSignature

## 7.65.3 Member Function Documentation

## 7.65.3.1 addCoord()

add offset to coordinate in dimension d of index i

## 7.65.3.2 at() [1/2]

reference to element at position i, with bounds check

## 7.65.3.3 at() [2/2]

read-only reference to element at position i, with bounds check

## 7.65.3.4 getCoord()

get coordinate in dimension d of index i

## 7.65.3.5 getData() [1/2]

```
\label{template} $$ \template< typename T > $$ \template< T > ::getData ( ) [inline] $$
```

read/write ref to the data vector. Note that the length of data is fixed upon construction, so it cannot be changed through this ref.

#### 7.65.3.6 getData() [2/2]

```
template<typename T >
const NTL::Vec<T>& helib::HyperCube< T >::getData ( ) const [inline]
```

read-only ref to data vector

## 7.65.3.7 getDim()

size of dimension d

## 7.65.3.8 getNumDims()

```
template<typename T >
long helib::HyperCube< T >::getNumDims ( ) const [inline]
```

number of dimensions

## 7.65.3.9 getProd() [1/2]

```
\label{template} $$ template < typename T > $$ long helib::HyperCube < T >::getProd ( long $d$) const [inline]
```

product of sizes of dimensions d, d+1, ...

## 7.65.3.10 getProd() [2/2]

product of sizes of dimensions from, from+1, ..., to-1

# 7.65.3.11 getSig()

```
template<typename T >
const CubeSignature& helib::HyperCube< T >::getSig ( ) const [inline]
```

const ref to signature

# 7.65.3.12 getSize()

```
template<typename T >
long helib::HyperCube< T >::getSize ( ) const [inline]
```

total size of cube

## 7.65.3.13 numCols()

```
template<typename T >
long helib::HyperCube< T >::numCols ( ) const [inline]
```

number of columns

#### 7.65.3.14 numSlices()

number of slices

## 7.65.3.15 operator"!=()

## 7.65.3.16 operator=()

assignment: signatures must be the same

#### 7.65.3.17 operator==()

equality testing: signatures must be the same

#### 7.65.3.18 operator[]() [1/2]

reference to element at position i, without bounds check

## 7.65.3.19 operator[]() [2/2]

read-only reference to element at position i, without bounds check

## 7.65.3.20 rotate1D()

rotate k positions along the i'th dimension

## 7.65.3.21 shift1D()

Shift k positions along the i'th dimension with zero fill.

#### 7.65.3.22 sliceSize()

```
template<typename T > long helib::HyperCube< T >::sliceSize ( long d = 1 ) const [inline]
```

size of one slice

The documentation for this class was generated from the following files:

- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/hypercube.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/hypercube.cpp

# 7.66 helib::IndexMap< T > Class Template Reference

IndexMap<T> implements a generic map indexed by a dynamic index set.

```
#include <IndexMap.h>
```

## **Public Member Functions**

IndexMap ()

The empty map.

IndexMap (IndexMapInit < T > \*\_init)

A map with an initialization object. This associates a method for initializing new elements in the map. When a new index j is added to the index set, an object t of type T is created using the default constructor for T, after which the function\_init->init(t) is called (t is passed by reference). To use this feature, you need to derive a subclass of Index $\leftarrow$  MapInit<T> that defines the init function. This "helper object" should be created using operator new, and the pointer is "exclusively owned" by the map object.

· const IndexSet & getIndexSet () const

Get the underlying index set.

T & operator[] (long j)

Access functions: will raise an error if j does not belong to the current index set.

- const T & operator[] (long j) const
- void insert (long j)

Insert indexes to the IndexSet. Insertion will cause new T objects to be created, using the default constructor, and possibly initialized via the IndexMapInit < T > pointer.

- · void insert (const IndexSet &s)
- void remove (long j)

Delete indexes from IndexSet, may cause objects to be destroyed.

- · void remove (const IndexSet &s)
- void clear ()

## 7.66.1 Detailed Description

```
template<typename T> class helib::IndexMap< T>
```

IndexMap<T> implements a generic map indexed by a dynamic index set.

Additionally, it allows new elements of the map to be initialized in a flexible manner.

## 7.66.2 Constructor & Destructor Documentation

## 7.66.2.1 IndexMap() [1/2]

```
template<typename T >
helib::IndexMap< T >::IndexMap ( )
```

The empty map.

## 7.66.2.2 IndexMap() [2/2]

A map with an initialization object. This associates a method for initializing new elements in the map. When a new index j is added to the index set, an object t of type T is created using the default constructor for T, after which the function \_init->init(t) is called (t is passed by reference). To use this feature, you need to derive a subclass of IndexMapInit<T> that defines the init function. This "helper object" should be created using operator new, and the pointer is "exclusively owned" by the map object.

#### 7.66.3 Member Function Documentation

#### 7.66.3.1 clear()

```
template<typename T >
void helib::IndexMap< T >::clear ( ) [inline]
```

## 7.66.3.2 getIndexSet()

```
template<typename T >
const IndexSet& helib::IndexMap< T >::getIndexSet ( ) const [inline]
```

Get the underlying index set.

## 7.66.3.3 insert() [1/2]

## 7.66.3.4 insert() [2/2]

Insert indexes to the IndexSet. Insertion will cause new T objects to be created, using the default constructor, and possibly initialized via the IndexMapInit<T> pointer.

## 7.66.3.5 operator[]() [1/2]

Access functions: will raise an error if j does not belong to the current index set.

## 7.66.3.6 operator[]() [2/2]

## 7.66.3.7 remove() [1/2]

#### 7.66.3.8 remove() [2/2]

```
template<typename T >
void helib::IndexMap< T >::remove (
          long j ) [inline]
```

Delete indexes from IndexSet, may cause objects to be destroyed.

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/IndexMap.h

# 7.67 helib::IndexMapInit< T > Class Template Reference

Initializing elements in an IndexMap.

```
#include <IndexMap.h>
```

## **Public Member Functions**

• virtual void init (T &)=0

Initialization function, override with initialization code.

virtual IndexMapInit< T > \* clone () const =0

Cloning a pointer, override with code to create a fresh copy.

virtual ∼IndexMapInit ()

## 7.67.1 Detailed Description

```
template<typename T> class helib::IndexMapInit< T>
```

Initializing elements in an IndexMap.

## 7.67.2 Constructor & Destructor Documentation

#### 7.67.2.1 ∼IndexMapInit()

```
template<typename T >
virtual helib::IndexMapInit< T >::~IndexMapInit ( ) [inline], [virtual]
```

## 7.67.3 Member Function Documentation

#### 7.67.3.1 clone()

```
template<typename T >
virtual IndexMapInit<T>* helib::IndexMapInit< T >::clone ( ) const [pure virtual]
```

Cloning a pointer, override with code to create a fresh copy.

#### 7.67.3.2 init()

Initialization function, override with initialization code.

Implemented in helib::DoubleCRTHelper.

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/IndexMap.h

## 7.68 helib::IndexSet Class Reference

A dynamic set of non-negative integers.

```
#include <IndexSet.h>
```

#### **Classes**

· class iterator

#### **Public Member Functions**

- IndexSet ()
- IndexSet (long low, long high)
- IndexSet (long j)
- · long first () const

Returns the first element, 0 if the set is empty.

· long last () const

Returns the last element, -1 if the set is empty.

long next (long j) const

Returns the next element after j, if any; otherwise j+1.

- long prev (long j) const
- long card () const

The cardinality of the set.

• bool contains (long j) const

Returns true iff the set contains j.

· bool contains (const IndexSet &s) const

Returns true iff the set contains s.

bool disjointFrom (const IndexSet &s) const

Returns true iff the set is disjoint from s.

- bool operator== (const IndexSet &s) const
- bool operator!= (const IndexSet &s) const
- void clear ()

Set to the empty set.

· void insert (long j)

Add j to the set.

• void remove (long j)

Remove j from the set.

void insert (const IndexSet &s)

Add s to the set (union)

void remove (const IndexSet &s)

Remove s from the set (set minus)

• void retain (const IndexSet &s)

Retains only those elements that are also in s (intersection)

• bool isInterval () const

Is this set a contiguous interval?

- void read (std::istream &str)
- · void write (std::ostream &str) const
- iterator begin () const
- iterator end () const

#### **Static Public Member Functions**

• static const IndexSet & emptySet ()

Read-only access to an empty set.

## 7.68.1 Detailed Description

A dynamic set of non-negative integers.

```
You can iterate through a set as follows:
```

```
for (long i = s.first(); i <= s.last(); i = s.next(i)) ...
for (long i = s.last(); i >= s.first(); i = s.prev(i)) ...
```

## 7.68.2 Constructor & Destructor Documentation

#### 7.68.2.1 IndexSet() [1/3]

```
helib::IndexSet::IndexSet () [inline]
```

## 7.68.2.2 IndexSet() [2/3]

## 7.68.2.3 IndexSet() [3/3]

## 7.68.3 Member Function Documentation

## 7.68.3.1 begin()

```
iterator helib::IndexSet::begin ( ) const [inline]
```

## 7.68.3.2 card()

```
long helib::IndexSet::card ( ) const [inline]
```

The cardinality of the set.

# 7.68.3.3 clear()

```
void helib::IndexSet::clear ( )
```

Set to the empty set.

## 7.68.3.4 contains() [1/2]

Returns true iff the set contains s.

## 7.68.3.5 contains() [2/2]

```
bool helib::IndexSet::contains ( \log \ j \ ) \ const
```

Returns true iff the set contains j.

## 7.68.3.6 disjointFrom()

Returns true iff the set is disjoint from s.

## 7.68.3.7 emptySet()

```
const IndexSet & helib::IndexSet::emptySet ( ) [static]
```

Read-only access to an empty set.

## 7.68.3.8 end()

```
iterator helib::IndexSet::end ( ) const [inline]
```

## 7.68.3.9 first()

```
long helib::IndexSet::first ( ) const [inline]
```

Returns the first element, 0 if the set is empty.

## 7.68.3.10 insert() [1/2]

Add s to the set (union)

## 7.68.3.11 insert() [2/2]

```
void helib::IndexSet::insert ( long \ j \ )
```

Add j to the set.

## 7.68.3.12 isInterval()

```
bool helib::IndexSet::isInterval ( ) const [inline]
```

Is this set a contiguous interval?

## 7.68.3.13 last()

```
long helib::IndexSet::last ( ) const [inline]
```

Returns the last element, -1 if the set is empty.

## 7.68.3.14 next()

```
long helib::IndexSet::next ( long \ j \ ) \ const
```

Returns the next element after j, if any; otherwise j+1.

## 7.68.3.15 operator"!=()

## 7.68.3.16 operator==()

#### 7.68.3.17 prev()

```
long helib::IndexSet::prev ( long j ) const
```

## 7.68.3.18 read()

#### 7.68.3.19 remove() [1/2]

Remove s from the set (set minus)

## 7.68.3.20 remove() [2/2]

```
void helib::IndexSet::remove ( long \ j \ )
```

Remove j from the set.

## 7.68.3.21 retain()

Retains only those elements that are also in s (intersection)

## 7.68.3.22 write()

The documentation for this class was generated from the following files:

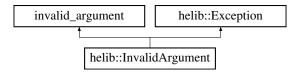
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/IndexSet.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/IndexSet.cpp

# 7.69 helib::InvalidArgument Class Reference

Inherits from Exception and std::invalid\_argument.

```
#include <exceptions.h>
```

Inheritance diagram for helib::InvalidArgument:



## **Public Member Functions**

- InvalidArgument (const std::string &what\_arg)
- InvalidArgument (const char \*what\_arg)
- virtual ∼InvalidArgument ()
- virtual const char \* what () const noexcept override

## **Additional Inherited Members**

## 7.69.1 Detailed Description

Inherits from Exception and std::invalid\_argument.

## 7.69.2 Constructor & Destructor Documentation

## 7.69.2.1 InvalidArgument() [1/2]

## 7.69.2.2 InvalidArgument() [2/2]

#### 7.69.2.3 ~InvalidArgument()

```
virtual helib::InvalidArgument::~InvalidArgument ( ) [inline], [virtual]
```

#### 7.69.3 Member Function Documentation

#### 7.69.3.1 what()

```
virtual const char* helib::InvalidArgument::what ( ) const [inline], [override], [virtual],
[noexcept]
```

Implements helib::Exception.

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/exceptions.h

#### 7.70 helib::IndexSet::iterator Class Reference

```
#include <IndexSet.h>
```

#### **Public Member Functions**

- long operator\* () const
- iterator & operator++ ()
- bool operator== (const iterator &other) const
- bool operator!= (const iterator &other) const

#### **Protected Member Functions**

• iterator (const IndexSet &s, long i)

#### **Friends**

class IndexSet

#### 7.70.1 Constructor & Destructor Documentation

#### 7.70.1.1 iterator()

#### 7.70.2 Member Function Documentation

#### 7.70.2.1 operator"!=()

#### 7.70.2.2 operator\*()

```
long helib::IndexSet::iterator::operator* ( ) const [inline]
```

#### 7.70.2.3 operator++()

```
iterator& helib::IndexSet::iterator::operator++ ( ) [inline]
```

#### 7.70.2.4 operator==()

#### 7.70.3 Friends And Related Function Documentation

#### 7.70.3.1 IndexSet

```
friend class IndexSet [friend]
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/IndexSet.h

# 7.71 helib::general\_range< T >::iterator Class Reference

```
#include <range.h>
```

#### **Public Member Functions**

- T operator\* () const
- iterator & operator++ ()
- bool operator== (const iterator &other) const
- bool operator!= (const iterator &other) const

#### **Protected Member Functions**

• iterator (T start)

#### **Friends**

· class general\_range

#### 7.71.1 Constructor & Destructor Documentation

#### 7.71.1.1 iterator()

#### 7.71.2 Member Function Documentation

#### 7.71.2.1 operator"!=()

#### 7.71.2.2 operator\*()

```
template<typename T >
T helib::general_range< T >::iterator::operator* ( ) const [inline]
```

#### 7.71.2.3 operator++()

```
template<typename T >
iterator& helib::general_range< T >::iterator::operator++ ( ) [inline]
```

#### 7.71.2.4 operator==()

#### 7.71.3 Friends And Related Function Documentation

#### 7.71.3.1 general\_range

```
template<typename T >
friend class general_range [friend]
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/range.h

### 7.72 helib::KeySwitch Class Reference

Key-switching matrices.

```
#include <keySwitching.h>
```

#### **Public Member Functions**

- KeySwitch (long sPow=0, long xPow=0, long fromID=0, long toID=0, long p=0)
- KeySwitch (const SKHandle &\_fromKey, long fromID=0, long toID=0, long p=0)
- bool operator== (const KeySwitch &other) const
- bool operator!= (const KeySwitch &other) const
- · unsigned long NumCols () const
- bool isDummy () const
- void verify (SecKey &sk)

A debugging method.

void readMatrix (std::istream &str, const Context &context)

Read a key-switching matrix from input.

• void read (std::istream &str, const Context &context)

Raw IO.

· void write (std::ostream &str) const

#### **Static Public Member Functions**

static const KeySwitch & dummy ()
 returns a dummy static matrix with toKeyId == -1

#### **Public Attributes**

- SKHandle fromKey
- long toKeyID
- long ptxtSpace
- std::vector< DoubleCRT > b
- NTL::ZZ prgSeed
- NTL::xdouble noiseBound

#### 7.72.1 Detailed Description

Key-switching matrices.

There are basically two approaches for how to do key-switching: either decompose the mod-q ciphertext into bits (or digits) to make it low-norm, or perform the key-switching operation mod Q>>q. The tradeoff is that when decomposing the (coefficients of the) ciphertext into t digits, we need to increase the size of the key-switching matrix by a factor of t (and the running time similarly grows). On the other hand if we do not decompose at all then we need to work modulo  $Q>q^{\wedge}2$ , which means that the bitsize of our largest modulus q0 more than doubles (and hence also the parameter m more than doubles). In general if we decompose into digits of size B then we need to work with Q>q\*B.)

The part of the spectrum where we expect to find the sweet spot is when we decompose the ciphertext into digits of size  $B=q0^{1/t}$  for some small constant t (maybe t=2,3 or so). This means that our largest modulus has to be  $Q>q0^{1+1/t}$ , which increases also the parameter m by a factor (1+1/t). It also means that for key-switching in the top levels we would break the ciphertext to t digits, hence the key-switching matrix will have t columns.

A key-switch matrix W[s'->s] converts a ciphertext-part with respect to secret-key polynomial s' into a canonical ciphertext (i.e. a two-part ciphertext with respect to (1,s)). The matrix W is a 2-by-t matrix of DoubleCRT objects. The bottom row are just (pseudo)random elements. Then for column j, if the bottom element is aj then the top element is set as bj =  $P*Bj*s' + p*ej - s*aj \mod P*q0$ , where p is the plaintext space (i.e. 2 or  $2^{\land}r$ , or 1 for CKKS) and Bj is the product of the digits-sizes corresponding to columns 0...i-1. (For example if we have digit sizes 3,5,7

then B0=1, B1=3, B2=15 and B3=105.) Also, q0 is the product of all the "ciphertext primes" and P is roughly the product of all the special primes. (Actually, for BGV, if Q is the product of all the special primes then  $P=Q*(Q^{-1})$  mod p).)

In this implementation we save some space, by keeping only a PRG seed for generating the pseudo-random elements, rather than the elements themselves.

To convert a ciphertext part R, we break R into digits  $R = sum_j$  Bj Rj, then set  $(q0,q1)^{\wedge}T = sum_j$  Rj \* column-j. Note that we have  $<(1,s),(q0,q1)>= sum_j$  Rj\*(s\*aj - s\*aj + p\*ej +P\*Bj\*s') = P \* sum\_j Bj\*Rj \* s' + p sum\_j Rj\*ej = P \* R \* s' + p\*a-small-element (mod P\*q0) where the last element is small since the ej's are small and |Rj| < B. Note that if the ciphertext is encrypted relative to plaintext space p' and then key-switched with matrices W relative to plaintext space p, then we get a mew ciphertext with noise p'\*small+p\*small, so it is valid relative to plaintext space GCD(p',p).

The matrix W is defined modulo Q>t\*B\*sigma\*q0 (with sigma a bound on the size of the ej's), and Q is the product of all the small primes in our moduli chain. However, if p is much smaller than B then is is enough to use W mod Qi with Qi a smaller modulus, Q>p\*sigma\*q0. Also note that if p<Br then we will be using only first r columns of the matrix W.

#### 7.72.2 Constructor & Destructor Documentation

#### 7.72.2.1 KeySwitch() [1/2]

```
helib::KeySwitch::KeySwitch (
    long sPow = 0,
    long xPow = 0,
    long fromID = 0,
    long toID = 0,
    long p = 0 ) [explicit]
```

#### 7.72.2.2 KeySwitch() [2/2]

```
helib::KeySwitch::KeySwitch (
    const SKHandle & _fromKey,
    long fromID = 0,
    long toID = 0,
    long p = 0 ) [explicit]
```

#### 7.72.3 Member Function Documentation

returns a dummy static matrix with toKeyId == -1

#### 7.72.3.1 dummy()

```
const KeySwitch & helib::KeySwitch::dummy ( ) [static]
```

#### 7.72.3.2 isDummy()

```
bool helib::KeySwitch::isDummy ( ) const
```

#### 7.72.3.3 NumCols()

```
unsigned long helib::KeySwitch::NumCols ( ) const
```

#### 7.72.3.4 operator"!=()

#### 7.72.3.5 operator==()

#### 7.72.3.6 read()

Raw IO.

#### 7.72.3.7 readMatrix()

Read a key-switching matrix from input.

#### 7.72.3.8 verify()

A debugging method.

#### 7.72.3.9 write()

#### 7.72.4 Member Data Documentation

#### 7.72.4.1 b

```
std::vector<DoubleCRT> helib::KeySwitch::b
```

#### 7.72.4.2 fromKey

```
SKHandle helib::KeySwitch::fromKey
```

#### 7.72.4.3 noiseBound

NTL::xdouble helib::KeySwitch::noiseBound

#### 7.72.4.4 prgSeed

NTL::ZZ helib::KeySwitch::prgSeed

#### 7.72.4.5 ptxtSpace

long helib::KeySwitch::ptxtSpace

#### 7.72.4.6 toKeyID

```
long helib::KeySwitch::toKeyID
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/keySwitching.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/keySwitching.cpp

# 7.73 helib::LabeledEdge Class Reference

A generic directed edge in a graph with some labels.

```
#include <matching.h>
```

#### **Public Member Functions**

• LabeledEdge (long f, long t, long l=0, long c=0)

#### **Public Attributes**

- long from
- · long to
- long label
- · long color

#### 7.73.1 Detailed Description

A generic directed edge in a graph with some labels.

#### 7.73.2 Constructor & Destructor Documentation

#### 7.73.2.1 LabeledEdge()

```
\label{eq:labeledEdge::LabeledEdge} \begin{tabular}{ll} $\log f, \\ $\log t, \\ $\log t, \\ $\log c = 0, \\ \end{tabular}
```

#### 7.73.3 Member Data Documentation

#### 7.73.3.1 color

long helib::LabeledEdge::color

#### 7.73.3.2 from

long helib::LabeledEdge::from

#### 7.73.3.3 label

long helib::LabeledEdge::label

#### 7.73.3.4 to

long helib::LabeledEdge::to

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matching.h

#### 7.74 helib::LabeledVertex Class Reference

A generic node in a graph with some labels.

#include <matching.h>

#### **Public Member Functions**

- LabeledVertex (long n, long l=0)
- void addEdge (long nn, long l=0, long c=0)
- void addNeighbor (long nn, long l=0, long c=0)

#### **Public Attributes**

- long name
- long label
- LNeighborList neighbors

#### 7.74.1 Detailed Description

A generic node in a graph with some labels.

#### 7.74.2 Constructor & Destructor Documentation

#### 7.74.2.1 LabeledVertex()

```
\label{labeledVertex:LabeledVertex} \mbox{$($ long $n,$} \mbox{$long $l=0$) [inline], [explicit]}
```

#### 7.74.3 Member Function Documentation

#### 7.74.3.1 addEdge()

```
void helib::LabeledVertex::addEdge ( long \ nn, \\ long \ 1 = 0, \\ long \ c = 0 \ ) \ [inline]
```

#### 7.74.3.2 addNeighbor()

```
void helib::LabeledVertex::addNeighbor ( long \ nn, \\ long \ long \ long \ long \ c = 0 ) \ [inline]
```

#### 7.74.4 Member Data Documentation

#### 7.74.4.1 label

```
long helib::LabeledVertex::label
```

#### 7.74.4.2 name

long helib::LabeledVertex::name

#### 7.74.4.3 neighbors

```
LNeighborList helib::LabeledVertex::neighbors
```

The documentation for this class was generated from the following file:

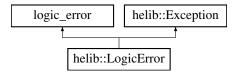
/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matching.h

# 7.75 helib::LogicError Class Reference

Inherits from Exception and std::logic\_error.

```
#include <exceptions.h>
```

Inheritance diagram for helib::LogicError:



#### **Public Member Functions**

- LogicError (const std::string &what\_arg)
- LogicError (const char \*what\_arg)
- virtual ~LogicError ()
- virtual const char \* what () const noexcept override

#### **Additional Inherited Members**

#### 7.75.1 Detailed Description

Inherits from Exception and std::logic\_error.

#### 7.75.2 Constructor & Destructor Documentation

#### 7.75.2.1 LogicError() [1/2]

#### 7.75.2.2 LogicError() [2/2]

#### 7.75.2.3 ~LogicError()

```
virtual helib::LogicError::~LogicError ( ) [inline], [virtual]
```

#### 7.75.3 Member Function Documentation

#### 7.75.3.1 what()

```
virtual const char* helib::LogicError::what ( ) const [inline], [override], [virtual], [noexcept]
Implements helib::Exception.
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/exceptions.h

### 7.76 LowLvlTimingData Class Reference

#### **Public Member Functions**

• LowLvlTimingData (long \_lvl=-1)

#### **Public Attributes**

- long lvl
- double addConst
- double add
- double multConst
- · double mult
- double multBy2
- double autoNative
- double autoTypical
- double innerProd

#### 7.76.1 Constructor & Destructor Documentation

#### 7.76.1.1 LowLvlTimingData()

```
\label{lowLvlTimingData::LowLvlTimingData} \mbox{ (} \\ \mbox{long } \_lvl \ = \ -1 \ ) \ \mbox{ [inline], [explicit]}
```

#### 7.76.2 Member Data Documentation

#### 7.76.2.1 add

double LowLvlTimingData::add

#### 7.76.2.2 addConst

double LowLvlTimingData::addConst

#### 7.76.2.3 autoNative

double LowLvlTimingData::autoNative

#### 7.76.2.4 autoTypical

double LowLvlTimingData::autoTypical

#### 7.76.2.5 innerProd

double LowLvlTimingData::innerProd

#### 7.76.2.6 Ivl

long LowLvlTimingData::lvl

#### 7.76.2.7 mult

double LowLvlTimingData::mult

#### 7.76.2.8 multBy2

double LowLvlTimingData::multBy2

#### 7.76.2.9 multConst

double LowLvlTimingData::multConst

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Timing.cpp

# 7.77 helib::MappingData < type > Class Template Reference

Auxiliary structure to support encoding/decoding slots.

#include <PAlgebra.h>

#### **Public Member Functions**

- const RX & getG () const
- long getDegG () const
- void restoreContextForG () const

#### **Friends**

class PAlgebraModDerived< type >

#### 7.77.1 Detailed Description

```
template<typename type> class helib::MappingData< type >
```

Auxiliary structure to support encoding/decoding slots.

#### 7.77.2 Member Function Documentation

#### 7.77.2.1 getDegG()

```
template<typename type >
long helib::MappingData< type >::getDegG ( ) const [inline]
```

#### 7.77.2.2 getG()

```
template<typename type >
const RX& helib::MappingData< type >::getG ( ) const [inline]
```

#### 7.77.2.3 restoreContextForG()

```
template<typename type >
void helib::MappingData< type >::restoreContextForG ( ) const [inline]
```

#### 7.77.3 Friends And Related Function Documentation

#### 7.77.3.1 PAlgebraModDerived< type >

```
template<typename type >
friend class PAlgebraModDerived< type > [friend]
```

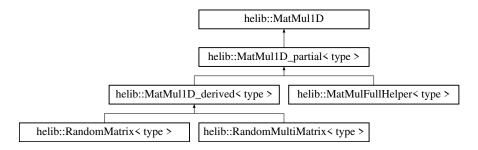
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h

#### 7.78 helib::MatMul1D Class Reference

#include <matmul.h>

Inheritance diagram for helib::MatMul1D:



#### **Public Types**

typedef MatMul1DExec ExecType

#### **Public Member Functions**

- virtual ~MatMul1D ()
- virtual const EncryptedArray & getEA () const =0
- virtual long getDim () const =0

#### 7.78.1 Member Typedef Documentation

#### 7.78.1.1 ExecType

typedef MatMul1DExec helib::MatMul1D::ExecType

#### 7.78.2 Constructor & Destructor Documentation

#### 7.78.2.1 $\sim$ MatMul1D()

virtual helib::MatMullD::~MatMullD ( ) [inline], [virtual]

#### 7.78.3 Member Function Documentation

#### 7.78.3.1 getDim()

```
virtual long helib::MatMullD::getDim ( ) const [pure virtual]
```

Implemented in helib::MatMulFullHelper< type >, helib::RandomMultiMatrix< type >, and helib::RandomMatrix< type >.

#### 7.78.3.2 getEA()

```
virtual const EncryptedArray& helib::MatMullD::getEA ( ) const [pure virtual]
```

Implemented in helib::MatMulFullHelper< type >, helib::RandomMultiMatrix< type >, and helib::RandomMatrix< type >.

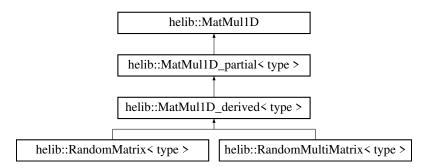
The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

## 7.79 helib::MatMul1D\_derived< type > Class Template Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::MatMul1D\_derived< type >:



#### **Public Member Functions**

- virtual bool multipleTransforms () const =0
- virtual bool get (RX &out, long i, long j, long k) const =0
- void processDiagonal (RX &poly, long i, const EncryptedArrayDerived < type > &ea) const override

#### **Additional Inherited Members**

#### 7.79.1 Member Function Documentation

#### 7.79.1.1 get()

Implemented in helib::RandomMultiMatrix< type >.

#### 7.79.1.2 multipleTransforms()

```
template<typename type >
virtual bool helib::MatMullD_derived< type >::multipleTransforms ( ) const [pure virtual]
```

Implemented in helib::RandomMultiMatrix< type >, and helib::RandomMatrix< type >.

#### 7.79.1.3 processDiagonal()

Implements helib::MatMul1D\_partial< type >.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.80 helib::MatMul1D\_derived\_impl< type > Struct Template Reference

#### **Static Public Member Functions**

- static void processDiagonal1 (RX &poly, long i, const EncryptedArrayDerived< type > &ea, const MatMul1D\_derived< type > &mat)
- static void processDiagonal2 (RX &poly, long idx, const EncryptedArrayDerived< type > &ea, const MatMul1D\_derived< type > &mat)
- static void processDiagonal (RX &poly, long i, const EncryptedArrayDerived< type > &ea, const MatMul1D\_derived< type > &mat)

#### 7.80.1 Member Function Documentation

#### 7.80.1.1 processDiagonal()

#### 7.80.1.2 processDiagonal1()

#### 7.80.1.3 processDiagonal2()

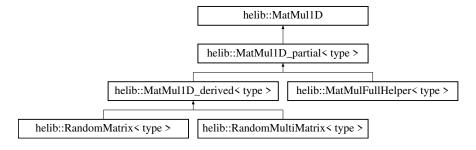
The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.81 helib::MatMul1D\_partial< type > Class Template Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::MatMul1D\_partial< type >:



#### **Public Member Functions**

virtual void processDiagonal (RX &poly, long i, const EncryptedArrayDerived< type > &ea) const =0

#### **Additional Inherited Members**

#### 7.81.1 Member Function Documentation

#### 7.81.1.1 processDiagonal()

Implemented in helib::MatMul1D\_derived< type >, and helib::MatMulFullHelper< type >.

The documentation for this class was generated from the following file:

/Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/matmul.h

# 7.82 helib::MatMul1DExec Class Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::MatMul1DExec:



#### **Public Member Functions**

- MatMul1DExec (const MatMul1D &mat, bool minimal=false)
- · void mul (Ctxt &ctxt) const override
- void upgrade () override
- const EncryptedArray & getEA () const override

#### **Public Attributes**

- const EncryptedArray & ea
- long dim
- long D
- · bool native
- bool minimal
- long g
- ConstMultiplierCache cache
- ConstMultiplierCache cache1

#### 7.82.1 Constructor & Destructor Documentation

#### 7.82.1.1 MatMul1DExec()

#### 7.82.2 Member Function Documentation

#### 7.82.2.1 getEA()

```
const EncryptedArray& helib::MatMullDExec::getEA ( ) const [inline], [override], [virtual]
```

Implements helib::MatMulExecBase.

#### 7.82.2.2 mul()

Implements helib::MatMulExecBase.

#### 7.82.2.3 upgrade()

```
void helib::MatMullDExec::upgrade ( ) [inline], [override], [virtual]
```

Implements helib::MatMulExecBase.

#### 7.82.3 Member Data Documentation

# 7.82.3.1 cache ConstMultiplierCache helib::MatMullDExec::cache 7.82.3.2 cache1 ConstMultiplierCache helib::MatMullDExec::cache1 7.82.3.3 D long helib::MatMul1DExec::D 7.82.3.4 dim long helib::MatMul1DExec::dim 7.82.3.5 ea const EncryptedArray& helib::MatMullDExec::ea 7.82.3.6 g long helib::MatMul1DExec::g

#### 7.82.3.7 minimal

bool helib::MatMul1DExec::minimal

#### 7.82.3.8 native

```
bool helib::MatMullDExec::native
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.83 helib::MatMul1DExec\_construct< type > Struct Template Reference

#### **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, const MatMul1D &mat\_basetype, std::vector< std::shared\_ptr< ConstMultiplier >> &vec, std::vector< std::shared\_ptr< ConstMultiplier >> &vec1, long g)

#### 7.83.1 Member Function Documentation

#### 7.83.1.1 apply()

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/matmul.cpp

# 7.84 helib::MatMulFullExec\_construct< type >::MatMulDimComp Struct Reference

#### **Public Member Functions**

- MatMulDimComp (const EncryptedArrayDerived< type > \*\_ea)
- bool operator() (long i, long j)

#### **Public Attributes**

const EncryptedArrayDerived< type > \* ea

#### 7.84.1 Constructor & Destructor Documentation

#### 7.84.1.1 MatMulDimComp()

#### 7.84.2 Member Function Documentation

#### 7.84.2.1 operator()()

#### 7.84.3 Member Data Documentation

#### 7.84.3.1 ea

```
template<typename type >
const EncryptedArrayDerived<type>* helib::MatMulFullExec_construct< type >::MatMulDimComp::ea
```

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

#### 7.85 helib::MatMulExecBase Class Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::MatMulExecBase:

```
helib::MatMulExecBase

t helib::BlockMatMul1DExec helib::MatMul1DExec helib::MatMulFullExec
```

#### **Public Member Functions**

- virtual ∼MatMulExecBase ()
- virtual const EncryptedArray & getEA () const =0
- virtual void upgrade ()=0
- virtual void mul (Ctxt &ctxt) const =0

#### 7.85.1 Constructor & Destructor Documentation

#### 7.85.1.1 ~MatMulExecBase()

```
virtual helib::MatMulExecBase::~MatMulExecBase ( ) [inline], [virtual]
```

#### 7.85.2 Member Function Documentation

#### 7.85.2.1 getEA()

```
virtual const EncryptedArray& helib::MatMulExecBase::getEA ( ) const [pure virtual]
```

Implemented in helib::BlockMatMulFullExec, helib::MatMulFullExec, helib::BlockMatMul1DExec, and helib::MatMul1DExec.

#### 7.85.2.2 mul()

Implemented in helib::BlockMatMulFullExec, helib::MatMulFullExec, helib::BlockMatMul1DExec, and helib::MatMul1DExec.

#### 7.85.2.3 upgrade()

```
virtual void helib::MatMulExecBase::upgrade ( ) [pure virtual]
```

 $Implemented \ in \ helib:: Block Mat Mul Full Exec, \ helib:: Block Mat Mul 1 D Exec, \ and \ helib:: Mat Mul 1 D Exec.$ 

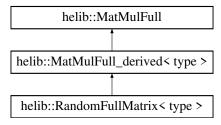
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

#### 7.86 helib::MatMulFull Class Reference

#include <matmul.h>

Inheritance diagram for helib::MatMulFull:



#### **Public Types**

typedef MatMulFullExec ExecType

#### **Public Member Functions**

- virtual ∼MatMulFull ()
- virtual const EncryptedArray & getEA () const =0

#### 7.86.1 Member Typedef Documentation

#### 7.86.1.1 ExecType

typedef MatMulFullExec helib::MatMulFull::ExecType

#### 7.86.2 Constructor & Destructor Documentation

#### 7.86.2.1 ~MatMulFull()

virtual helib::MatMulFull::~MatMulFull ( ) [inline], [virtual]

#### 7.86.3 Member Function Documentation

#### 7.86.3.1 getEA()

```
virtual const EncryptedArray& helib::MatMulFull::getEA ( ) const [pure virtual]
```

Implemented in helib::RandomFullMatrix< type >.

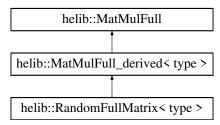
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

# 7.87 helib::MatMulFull\_derived< type > Class Template Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::MatMulFull\_derived< type >:



#### **Public Member Functions**

• virtual bool get (RX &out, long i, long j) const =0

#### **Additional Inherited Members**

#### 7.87.1 Member Function Documentation

#### 7.87.1.1 get()

Implemented in helib::RandomFullMatrix< type >.

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h

#### 7.88 helib::MatMulFullExec Class Reference

```
#include <matmul.h>
```

Inheritance diagram for helib::MatMulFullExec:



#### **Public Member Functions**

- MatMulFullExec (const MatMulFull &mat, bool minimal=false)
- · void mul (Ctxt &ctxt) const override
- void upgrade () override
- const EncryptedArray & getEA () const override
- long rec\_mul (Ctxt &acc, const Ctxt &ctxt, long dim, long idx) const

#### **Public Attributes**

- const EncryptedArray & ea
- bool minimal
- std::vector< long > dims
- std::vector< MatMul1DExec > transforms

#### 7.88.1 Constructor & Destructor Documentation

#### 7.88.1.1 MatMulFullExec()

#### 7.88.2 Member Function Documentation

#### 7.88.2.1 getEA()

```
const EncryptedArray& helib::MatMulFullExec::getEA ( ) const [inline], [override], [virtual]
Implements helib::MatMulExecBase.
```

#### 7.88.2.2 mul()

Implements helib::MatMulExecBase.

#### 7.88.2.3 rec\_mul()

#### 7.88.2.4 upgrade()

```
void helib::MatMulFullExec::upgrade ( ) [inline], [override], [virtual]
```

Implements helib::MatMulExecBase.

#### 7.88.3 Member Data Documentation

#### 7.88.3.1 dims

```
std::vector<long> helib::MatMulFullExec::dims
```

#### 7.88.3.2 ea

```
const EncryptedArray& helib::MatMulFullExec::ea
```

#### 7.88.3.3 minimal

bool helib::MatMulFullExec::minimal

#### 7.88.3.4 transforms

```
std::vector<MatMullDExec> helib::MatMulFullExec::transforms
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/matmul.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.89 helib::MatMulFullExec\_construct< type > Struct Template Reference

#### Classes

struct MatMulDimComp

#### **Static Public Member Functions**

- static long rec\_mul (long dim, long idx, const std::vector< long > &idxes, std::vector< MatMul1DExec > &transforms, bool minimal, const std::vector< long > &dims, const EncryptedArray &ea\_basetype, const EncryptedArrayDerived< type > &ea, const MatMulFull\_derived< type > &mat)
- static void apply (const EncryptedArrayDerived< type > &ea, const EncryptedArray &ea\_basetype, const MatMulFull &mat\_basetype, std::vector< MatMul1DExec > &transforms, bool minimal, std::vector< long > &dims)

#### 7.89.1 Member Function Documentation

#### 7.89.1.1 apply()

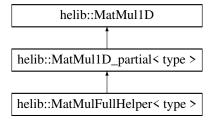
#### 7.89.1.2 rec\_mul()

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.90 helib::MatMulFullHelper< type > Class Template Reference

Inheritance diagram for helib::MatMulFullHelper< type >:



#### **Public Member Functions**

- MatMulFullHelper (const EncryptedArray &\_ea\_basetype, const MatMulFull\_derived< type > &\_mat, const std::vector< long > &\_init\_idxes, long \_dim)
- void processDiagonal (RX &epmat, long offset, const EncryptedArrayDerived < type > &ea) const override
- · const EncryptedArray & getEA () const override
- long getDim () const override

#### **Public Attributes**

- const EncryptedArray & ea\_basetype
- const MatMulFull\_derived< type > & mat
- std::vector< long > init\_idxes
- long dim

#### **Additional Inherited Members**

#### 7.90.1 Constructor & Destructor Documentation

#### 7.90.1.1 MatMulFullHelper()

#### 7.90.2 Member Function Documentation

#### 7.90.2.1 getDim()

```
template<typename type >
long helib::MatMulFullHelper< type >::getDim ( ) const [inline], [override], [virtual]
```

Implements helib::MatMul1D.

#### 7.90.2.2 getEA()

```
template<typename type >
const EncryptedArray& helib::MatMulFullHelper< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::MatMul1D.

#### 7.90.2.3 processDiagonal()

Implements helib::MatMul1D\_partial< type >.

#### 7.90.3 Member Data Documentation

#### 7.90.3.1 dim

```
template<typename type >
long helib::MatMulFullHelper< type >::dim
```

#### 7.90.3.2 ea\_basetype

```
template<typename type >
const EncryptedArray& helib::MatMulFullHelper< type >::ea_basetype
```

#### 7.90.3.3 init\_idxes

```
template<typename type >
std::vector<long> helib::MatMulFullHelper< type >::init_idxes
```

#### 7.90.3.4 mat

```
template<typename type >
const MatMulFull_derived<type>& helib::MatMulFullHelper< type >::mat
```

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

#### 7.91 helib::ModuliSizes Class Reference

A helper class to map required modulo-sizes to primeSets.

```
#include <primeChain.h>
```

#### **Public Types**

• typedef std::pair< double, IndexSet > Entry

#### **Public Member Functions**

- void init (const std::vector< Cmodulus > &chain, const IndexSet &ctxtPrimes, const IndexSet &smallPrimes) initialize helper table for a given chain
- IndexSet getSet4Size (double low, double high, const IndexSet &fromSet, bool reverse) const
- IndexSet getSet4Size (double low, double high, const IndexSet &from1, const IndexSet &from2, bool reverse)
- void read (std::istream &str)
- void write (std::ostream &str) const

#### **Friends**

- std::istream & operator>> (std::istream &s, ModuliSizes &szs)
- std::ostream & operator<< (std::ostream &s, const ModuliSizes &szs)</li>

#### 7.91.1 Detailed Description

A helper class to map required modulo-sizes to primeSets.

#### 7.91.2 Member Typedef Documentation

#### 7.91.2.1 Entry

```
typedef std::pair<double, IndexSet> helib::ModuliSizes::Entry
```

#### 7.91.3 Member Function Documentation

#### 7.91.3.1 getSet4Size() [1/2]

Find a suitable IndexSet of primes whose total size is in the target interval [low,high], trying to minimize the total number of primes dropped from both from1, from2. If no IndexSet exists that fits in the target interval, returns the IndexSet that gives the largest value smaller than low. (or the smallest value greater than low if reverse flag is set).

Find a suitable IndexSet of primes whose total size is in the target interval [low,high], trying to minimize the total number of primes dropped from both from1, from2. If no IndexSet exists that fits in the target interval, returns the IndexSet that gives the largest value smaller than low.

#### 7.91.3.2 getSet4Size() [2/2]

Find a suitable IndexSet of primes whose total size is in the target interval [low,high], trying to minimize the number of primes dropped from fromSet. If no IndexSet exists that fits in the target interval, returns the IndexSet that gives the largest value smaller than low (or the smallest value greater than low if reverse flag is set).

#### 7.91.3.3 init()

initialize helper table for a given chain

#### 7.91.3.4 read()

#### 7.91.3.5 write()

```
void helib::ModuliSizes::write ( {\tt std::ostream~\&~str~)~const}
```

#### 7.91.4 Friends And Related Function Documentation

### $\textbf{7.91.4.1} \quad operator <<$

#### 7.91.4.2 operator>>

```
std::istream& operator>> (
          std::istream & s,
          ModuliSizes & szs ) [friend]
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/primeChain.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/primeChain.cpp

## 7.92 helib::mul\_BlockMatMul1D\_impl< type > Struct Template Reference

#### **Static Public Member Functions**

 static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const BlockMatMul1D &mat basetype)

## 7.92.1 Member Function Documentation

#### 7.92.1.1 apply()

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

# 7.93 helib::mul\_BlockMatMulFull\_impl< type > Struct Template Reference

## **Static Public Member Functions**

 static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const BlockMatMulFull &mat\_basetype)

## 7.93.1 Member Function Documentation

## 7.93.1.1 apply()

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

## 7.94 helib::mul MatMul1D impl< type > Struct Template Reference

## **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const MatMul1D &mat\_←
basetype)

## 7.94.1 Member Function Documentation

#### 7.94.1.1 apply()

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

## 7.95 helib::mul MatMulFull impl< type > Struct Template Reference

## **Static Public Member Functions**

## 7.95.1 Member Function Documentation

## 7.95.1.1 apply()

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/matmul.cpp

## 7.96 helib::mul pa impl< type > Class Template Reference

## **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const PlaintextArray &other)

## 7.96.1 Member Function Documentation

## 7.96.1.1 apply()

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

## 7.97 MyClass Class Reference

## **Public Member Functions**

- MyClass (int i)
- int get () const
- void set (int i)

## 7.97.1 Constructor & Destructor Documentation

## 7.97.1.1 MyClass()

```
\label{eq:myclass} \mbox{MyClass::MyClass (} \\ \mbox{int } i \mbox{)} \mbox{ [inline]}
```

## 7.97.2 Member Function Documentation

#### 7.97.2.1 get()

```
int MyClass::get ( ) const [inline]
```

## 7.97.2.2 set()

```
void MyClass::set ( \quad \text{int } i \text{ ) } \quad [\text{inline}]
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_PtrVector.cpp

## 7.98 helib::negate\_pa\_impl< type > Class Template Reference

#### **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa)

## 7.98.1 Member Function Documentation

## 7.98.1.1 apply()

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

## 7.99 OtherTimingData Class Reference

#### **Public Attributes**

- double init2
- double init4
- double keyGen
- double encode2
- double encode2d
- double encode4
- double encode4d
- · double encrypt
- double decode2
- · double decode4
- double decrypt

## 7.99.1 Member Data Documentation

# 7.99.1.1 decode2 double OtherTimingData::decode2 7.99.1.2 decode4 double OtherTimingData::decode4 7.99.1.3 decrypt double OtherTimingData::decrypt 7.99.1.4 encode2 double OtherTimingData::encode2 7.99.1.5 encode2d double OtherTimingData::encode2d 7.99.1.6 encode4 double OtherTimingData::encode4 7.99.1.7 encode4d

double OtherTimingData::encode4d

#### 7.99.1.8 encrypt

double OtherTimingData::encrypt

## 7.99.1.9 init2

double OtherTimingData::init2

## 7.99.1.10 init4

double OtherTimingData::init4

## 7.99.1.11 keyGen

double OtherTimingData::keyGen

The documentation for this class was generated from the following file:

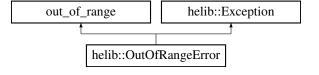
/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Timing.cpp

## 7.100 helib::OutOfRangeError Class Reference

Inherits from Exception and std::out\_of\_range.

```
#include <exceptions.h>
```

Inheritance diagram for helib::OutOfRangeError:



#### **Public Member Functions**

- OutOfRangeError (const std::string &what\_arg)
- OutOfRangeError (const char \*what\_arg)
- virtual ~OutOfRangeError ()
- virtual const char \* what () const noexcept override

## **Additional Inherited Members**

## 7.100.1 Detailed Description

Inherits from Exception and std::out\_of\_range.

#### 7.100.2 Constructor & Destructor Documentation

#### 7.100.2.1 OutOfRangeError() [1/2]

#### 7.100.2.2 OutOfRangeError() [2/2]

## 7.100.2.3 ~OutOfRangeError()

```
\label{lib::outOfRangeError::} \verb|\|OutOfRangeError| ( ) [inline], [virtual] \\
```

## 7.100.3 Member Function Documentation

#### 7.100.3.1 what()

```
virtual const char* helib::OutOfRangeError::what ( ) const [inline], [override], [virtual],
[noexcept]
```

Implements helib::Exception.

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/exceptions.h

## 7.101 helib::PAlgebra Class Reference

```
The structure of (Z/mZ)* /(p)
#include <PAlgebra.h>
```

#### **Public Member Functions**

- PAlgebra (long mm, long pp=2, const std::vector< long > &\_gens=std::vector< long >(), const std::vector< long > & ords=std::vector< long >())
- bool operator== (const PAlgebra &other) const
- bool operator!= (const PAlgebra &other) const
- void printout () const

Prints the structure in a readable form.

- void printAll () const
- long getM () const

Returns m.

· long getP () const

Returns p.

• long getPhiM () const

Returns phi(m)

• long getOrdP () const

The order of p in  $(Z/mZ)^{\wedge}*$ .

• long getNFactors () const

The number of distinct prime factors of m.

• long getRadM () const

getRadM() = prod of distinct prime factors of m

• double getNormBnd () const

max-norm-on-pwfl-basis <= normBnd \* max-norm-canon-embed

double getPolyNormBnd () const

max-norm-on-pwfl-basis <= polyNormBnd \* max-norm-canon-embed

• long getNSlots () const

The number of plaintext slots = phi(m)/ord(p)

long getPow2 () const

if  $m = 2^k$ , then pow2 == k; otherwise, pow2 == 0

const NTL::ZZX & getPhimX () const

The cyclotomix polynomial Phi\_m(X)

void set\_cM (double c)

The "ring constant" cM.

- double get\_cM () const
- long numOfGens () const

The prime-power factorization of m.

• long ZmStarGen (long i) const

the i'th generator in  $(Z/mZ)^{\wedge}*/(p)$  (if any)

• long genToPow (long i, long j) const

the i'th generator to the power j mod m

- long frobeniusPow (long j) const
- · long OrderOf (long i) const

The order of i'th generator (if any)

• long ProdOrdsFrom (long i) const

The product prod\_ $\{j=i\}^{\land}\{n-1\}$  OrderOf(i)

· bool SameOrd (long i) const

Is ord(i'th generator) the same as its order in  $(Z/mZ)^{\wedge}*$ ?

• long FrobPerturb (long i) const

#### Translation between index, representatives, and exponents

• long ith\_rep (long i) const

Returns the i'th element in T.

long indexOfRep (long t) const

Returns the index of t in T.

• bool isRep (long t) const

Is t in T?

long indexInZmstar (long t) const

Returns the index of t in (Z/mZ)\*.

long indexInZmstar unchecked (long t) const

Returns the index of t in (Z/mZ)\* – no range checking.

long repInZmstar\_unchecked (long idx) const

Returns rep whose index is i.

- bool inZmStar (long t) const
- long exponentiate (const std::vector< long > &exps, bool onlySameOrd=false) const

Returns  $prod_i gi^{(k)}$  and m. If onlySameOrd=true, use only generators that have the same order as in  $(Z/mZ)^{(k)}$ .

· long coordinate (long i, long k) const

Returns coordinate of index k along the i'th dimension.

- std::pair< long, long > breakIndexByDim (long idx, long dim) const
- long assembleIndexByDim (std::pair< long, long > idx, long dim) const

The inverse of breakIndexByDim.

long addCoord (long i, long k, long offset) const

adds offset to index k in the i'th dimension

- bool nextExpVector (std::vector < long > &exps) const
- long fftSizeNeeded () const

The largest FFT we need to handle degree-m polynomials.

- const PGFFT & getFFTInfo () const
- const half FFT & getHalfFFTInfo () const
- const quarter\_FFT & getQuarterFFTInfo () const

## 7.101.1 Detailed Description

The structure of (Z/mZ)\*/(p)

A PAlgebra object is determined by an integer m and a prime p, where p does not divide m. It holds information describing the structure of  $(Z/mZ)^{\wedge}*$ , which is isomorphic to the Galois group over  $A = Z[X]/Phi_m(X)$ .

We represent  $(Z/mZ)^*$  as  $(Z/mZ)^*$  = (p) x (g1,g2,...) x (h1,h2,...) where the group generated by g1,g2,... consists of the elements that have the same order in  $(Z/mZ)^*$  as in  $(Z/mZ)^*$  /(p,g\_1,...,g\_{i-1}), and h1,h2,... generate the remaining quotient group  $(Z/mZ)^*$  /(p,g1,g2,...).

We let T subset  $(Z/mZ)^*$  be a set of representatives for the quotient group  $(Z/mZ)^*$  /(p), defined as T={ prod\_i gi^{ei} \* prod\_j hj^{ej} } where the ei's range over 0,1,...,ord(gi)-1 and the ej's range over 0,1,...ord(hj)-1 (these last orders are in  $(Z/mZ)^*$  /(p,g1,g2,...)).

Phi\_m(X) is factored as Phi\_m(X)= prod\_{t in T} F\_t(X) mod p, where the F\_t's are irreducible modulo p. An arbitrary factor is chosen as F\_1, then for each t in T we associate with the index t the factor F\_t(X) = GCD(F\_1(X^t), Phi  $\leftarrow$  \_m(X)).

Note that fixing a representation of the field  $R=(Z/pZ)[X]/F_1(X)$  and letting z be a root of  $F_1$  in R (which is a primitive m-th root of unity in R), we get that  $F_1$  is the minimal polynomial of  $z^{-1/t}$ .

## 7.101.2 Constructor & Destructor Documentation

## 7.101.2.1 PAlgebra()

## 7.101.3 Member Function Documentation

## 7.101.3.1 addCoord()

```
long helib::PAlgebra::addCoord (
                long i,
                long k,
                long offset ) const [inline]
```

adds offset to index k in the i'th dimension

## 7.101.3.2 assembleIndexByDim()

```
long helib::Palgebra::assembleIndexByDim (  std::pair < long, \ long > idx, \\ long \ dim \ ) \ const \ [inline]
```

The inverse of breakIndexByDim.

## 7.101.3.3 breakIndexByDim()

Break an index into the hypercube to index of the dimension-dim subcube and index inside that subcube.

## 7.101.3.4 coordinate()

```
long helib::PAlgebra::coordinate ( \label{eq:palgebra:coordinate} \mbox{long $i$,} \\ \mbox{long $k$ ) const [inline]}
```

Returns coordinate of index k along the i'th dimension.

## 7.101.3.5 exponentiate()

Returns prod\_i gi^{exps[i]} mod m. If onlySameOrd=true, use only generators that have the same order as in  $(Z/mZ)^*$ .

## 7.101.3.6 fftSizeNeeded()

```
long helib::PAlgebra::fftSizeNeeded ( ) const [inline]
```

The largest FFT we need to handle degree-m polynomials.

## 7.101.3.7 frobeniusPow()

```
long helib::PAlgebra::frobeniusPow ( \log \ j \ ) \ {\tt const}
```

## 7.101.3.8 FrobPerturb()

```
long helib::PAlgebra::FrobPerturb ( long \ i \ ) \ const \ [inline]
```

#### 7.101.3.9 genToPow()

```
long helib::PAlgebra::genToPow ( \label{eq:const} \log \ i \, , \label{eq:const} \log \ j \ ) \ \mbox{const}
```

the i'th generator to the power j mod m

## 7.101.3.10 get\_cM()

```
double helib::PAlgebra::get_cM ( ) const [inline]
```

## 7.101.3.11 getFFTInfo()

```
const PGFFT& helib::PAlgebra::getFFTInfo ( ) const [inline]
```

## 7.101.3.12 getHalfFFTInfo()

```
const half_FFT& helib::PAlgebra::getHalfFFTInfo ( ) const [inline]
```

## 7.101.3.13 getM()

```
long helib::PAlgebra::getM ( ) const [inline]
```

Returns m.

## 7.101.3.14 getNFactors()

```
long helib::PAlgebra::getNFactors ( ) const [inline]
```

The number of distinct prime factors of m.

## 7.101.3.15 getNormBnd()

```
double helib::PAlgebra::getNormBnd ( ) const [inline]
```

max-norm-on-pwfl-basis <= normBnd \* max-norm-canon-embed

## 7.101.3.16 getNSlots()

```
long helib::PAlgebra::getNSlots ( ) const [inline]
```

The number of plaintext slots = phi(m)/ord(p)

## 7.101.3.17 getOrdP()

```
long helib::PAlgebra::getOrdP ( ) const [inline]
```

The order of p in  $(Z/mZ)^*$ .

#### 7.101.3.18 getP()

```
long helib::PAlgebra::getP ( ) const [inline]
```

Returns p.

## 7.101.3.19 getPhiM()

```
long helib::PAlgebra::getPhiM ( ) const [inline]
```

Returns phi(m)

## 7.101.3.20 getPhimX()

```
const NTL::ZZX& helib::PAlgebra::getPhimX ( ) const [inline]
```

The cyclotomix polynomial Phi\_m(X)

## 7.101.3.21 getPolyNormBnd()

```
double helib::PAlgebra::getPolyNormBnd ( ) const [inline]
```

max-norm-on-pwfl-basis <= polyNormBnd \* max-norm-canon-embed

## 7.101.3.22 getPow2()

```
long helib::PAlgebra::getPow2 ( ) const [inline]
```

if  $m = 2^k$ , then pow2 == k; otherwise, pow2 == 0

## 7.101.3.23 getQuarterFFTInfo()

```
const quarter_FFT& helib::PAlgebra::getQuarterFFTInfo ( ) const [inline]
```

## 7.101.3.24 getRadM()

```
long helib::PAlgebra::getRadM ( ) const [inline]
getRadM() = prod of distinct prime factors of m
```

## 7.101.3.25 indexInZmstar()

Returns the index of t in (Z/mZ)\*.

## 7.101.3.26 indexInZmstar\_unchecked()

```
long helib::PAlgebra::indexInZmstar_unchecked ( long \ t \ ) \ const \ [inline]
```

Returns the index of t in (Z/mZ)\* – no range checking.

## 7.101.3.27 indexOfRep()

Returns the index of t in T.

## 7.101.3.28 inZmStar()

## 7.101.3.29 isRep()

```
bool helib::PAlgebra::isRep ( \label{eq:long} \mbox{long $t$ ) const [inline]}
```

Is t in T?

## 7.101.3.30 ith\_rep()

```
long helib::PAlgebra::ith_rep ( long \ i \ ) \ const \ [inline]
```

Returns the i'th element in T.

## 7.101.3.31 nextExpVector()

exps is an array of exponents (the dLog of some t in T), this function increment exps lexicographic order, return false if it cannot be incremented (because it is at its maximum value)

## 7.101.3.32 numOfGens()

```
long helib::PAlgebra::numOfGens ( ) const [inline]
```

The prime-power factorization of m.

The number of generators in  $(Z/mZ)^* * /(p)$ 

## 7.101.3.33 operator"!=()

## 7.101.3.34 operator==()

## 7.101.3.35 OrderOf()

```
long helib::PAlgebra::OrderOf ( long \ i \ ) \ const \ [inline]
```

The order of i'th generator (if any)

## 7.101.3.36 printAll()

```
void helib::PAlgebra::printAll ( ) const
```

## 7.101.3.37 printout()

```
void helib::PAlgebra::printout ( ) const
```

Prints the structure in a readable form.

## 7.101.3.38 ProdOrdsFrom()

```
long helib::PAlgebra::ProdOrdsFrom ( long \ i \ ) \ const \ [inline]
```

The product prod\_ ${j=i}^{n-1} OrderOf(i)$ 

## 7.101.3.39 replnZmstar\_unchecked()

Returns rep whose index is i.

## 7.101.3.40 SameOrd()

```
bool helib::PAlgebra::SameOrd ( long \ i \ ) \ const \ \ [inline]
```

Is ord(i'th generator) the same as its order in  $(Z/mZ)^*$ ?

#### 7.101.3.41 set\_cM()

```
void helib::PAlgebra::set_cM ( \label{eq:condition} \mbox{double } c \mbox{ ) [inline]}
```

The "ring constant" cM.

## 7.101.3.42 ZmStarGen()

```
long helib::PAlgebra::ZmStarGen ( \label{eq:long_i} \mbox{long $i$ ) const [inline]}
```

the i'th generator in  $(Z/mZ)^{\wedge}*/(p)$  (if any)

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PAlgebra.cpp

## 7.102 helib::PAlgebraMod Class Reference

```
The structure of Z[X]/(Phi_m(X), p) #include <PAlgebra.h>
```

## **Public Member Functions**

- PAlgebraMod (const PAlgebra &zMStar, long r)
- template<typename type >
   const PAlgebraModDerived< type > & getDerived (type) const
- const PAlgebraModCx & getCx () const
- bool operator== (const PAlgebraMod &other) const
- bool operator!= (const PAlgebraMod &other) const
- PA\_tag getTag () const

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

· const PAlgebra & getZMStar () const

Returns reference to underlying PAlgebra object.

const std::vector< NTL::ZZX > & getFactorsOverZZ () const

Returns reference to the factorization of  $Phi_m(X) \mod p^{\wedge}r$ , but as ZZX's.

• long getR () const

The value r.

• long getPPowR () const

The value  $p^{\wedge}r$ .

· void restoreContext () const

Restores the NTL context for  $p^{\wedge}r$ .

zzX getMask\_zzX (long i, long j) const

## 7.102.1 Detailed Description

The structure of Z[X]/(Phi\_m(X), p)

An object of type PAlgebraMod stores information about a PAlgebra object zMStar, and an integer r. It also provides support for encoding and decoding plaintext slots.

the PAlgebra object zMStar defines  $(Z/mZ)^*/(0)$ , and the PAlgebraMod object stores various tables related to the polynomial ring  $Z/(p^r)[X]$ . To do this most efficiently, if p == 2 and r == 1, then these polynomials are represented as GF2X's, and otherwise as  $zz_pX$ 's. Thus, the types of these objects are not determined until run time. As such, we need to use a class hierarchy, as follows.

- PAlgebraModBase is a virtual class
- PAlgebraModDerived<type> is a derived template class, where type is either PA\_GF2 or PA\_zz\_p.
- The class PAlgebraMod is a simple wrapper around a smart pointer to a PAlgebraModBase object: copying a PAlgebra object results is a "deep copy" of the underlying object of the derived class. It provides dDirect access to the virtual methods of PAlgebraModBase, along with a "downcast" operator to get a reference to the object as a derived type, and also == and != operators.

#### 7.102.2 Constructor & Destructor Documentation

## 7.102.2.1 PAlgebraMod()

## 7.102.3 Member Function Documentation

## 7.102.3.1 getCx()

```
const PAlgebraModCx& helib::PAlgebraMod::getCx ( ) const [inline]
```

## 7.102.3.2 getDerived()

Downcast operator example: const PAlgebraModDerived<PA\_GF2>& rep = alMod.getDerived(PA\_GF2());

## 7.102.3.3 getFactorsOverZZ()

```
const std::vector<NTL::ZZX>& helib::PAlgebraMod::getFactorsOverZZ ( ) const [inline]
```

Returns reference to the factorization of Phi\_m(X) mod  $p^r$ , but as ZZX's.

## 7.102.3.4 getMask\_zzX()

## 7.102.3.5 getPPowR()

```
long helib::PAlgebraMod::getPPowR ( ) const [inline]
```

The value  $p^r$ .

## 7.102.3.6 getR()

```
long helib::PAlgebraMod::getR ( ) const [inline]
```

The value r.

## 7.102.3.7 getTag()

```
PA_tag helib::PAlgebraMod::getTag ( ) const [inline]
```

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

## 7.102.3.8 getZMStar()

```
const PAlgebra& helib::PAlgebraMod::getZMStar ( ) const [inline]
```

Returns reference to underlying PAlgebra object.

### 7.102.3.9 operator"!=()

## 7.102.3.10 operator==()

## 7.102.3.11 restoreContext()

```
void helib::PAlgebraMod::restoreContext ( ) const [inline]
```

Restores the NTL context for  $p^{\wedge}r$ .

The documentation for this class was generated from the following file:

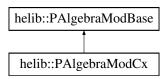
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h

## 7.103 helib::PAlgebraModBase Class Reference

Virtual base class for PAlgebraMod.

```
#include <PAlgebra.h>
```

Inheritance diagram for helib::PAlgebraModBase:



## **Public Member Functions**

- virtual ~PAlgebraModBase ()
- virtual PAlgebraModBase \* clone () const =0
- virtual PA\_tag getTag () const =0

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

• virtual const PAlgebra & getZMStar () const =0

Returns reference to underlying PAlgebra object.

virtual const std::vector< NTL::ZZX > & getFactorsOverZZ () const =0

Returns reference to the factorization of  $Phi_m(X) \mod p^{\wedge}r$ , but as ZZX's.

virtual long getR () const =0

The value r.

• virtual long getPPowR () const =0

The value  $p^{\wedge}r$ .

• virtual void restoreContext () const =0

Restores the NTL context for  $p^{\wedge}r$ .

virtual zzX getMask\_zzX (long i, long j) const =0

## 7.103.1 Detailed Description

Virtual base class for PAlgebraMod.

## 7.103.2 Constructor & Destructor Documentation

#### 7.103.2.1 ∼PAlgebraModBase()

```
virtual helib::PAlgebraModBase::~PAlgebraModBase ( ) [inline], [virtual]
```

## 7.103.3 Member Function Documentation

## 7.103.3.1 clone()

```
virtual PAlgebraModBase* helib::PAlgebraModBase::clone ( ) const [pure virtual]
```

Implemented in helib::PAlgebraModCx.

## 7.103.3.2 getFactorsOverZZ()

```
\label{lem:palgebraModBase::getFactorsOverZZ () const [pure virtual]} % The const of the const
```

Returns reference to the factorization of Phi\_m(X) mod p^r, but as ZZX's.

Implemented in helib::PAlgebraModCx.

## 7.103.3.3 getMask zzX()

```
virtual zzX helib::PAlgebraModBase::getMask_zzX ( long \ i, \\ long \ j \ ) \ const \ [pure virtual]
```

## 7.103.3.4 getPPowR()

```
virtual long helib::PAlgebraModBase::getPPowR ( ) const [pure virtual]
```

The value  $p^r$ .

Implemented in helib::PAlgebraModCx.

## 7.103.3.5 getR()

```
virtual long helib::PAlgebraModBase::getR ( ) const [pure virtual]
```

The value r.

Implemented in helib::PAlgebraModCx.

## 7.103.3.6 getTag()

```
virtual PA_tag helib::PAlgebraModBase::getTag ( ) const [pure virtual]
```

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

Implemented in helib::PAlgebraModCx.

## 7.103.3.7 getZMStar()

```
virtual const PAlgebra& helib::PAlgebraModBase::getZMStar ( ) const [pure virtual]
```

Returns reference to underlying PAlgebra object.

Implemented in helib::PAlgebraModCx.

## 7.103.3.8 restoreContext()

```
virtual void helib::PAlgebraModBase::restoreContext ( ) const [pure virtual]
```

Restores the NTL context for  $p^r$ .

Implemented in helib::PAlgebraModCx.

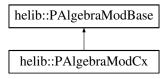
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h

## 7.104 helib::PAlgebraModCx Class Reference

```
#include <PAlgebra.h>
```

Inheritance diagram for helib::PAlgebraModCx:



#### **Public Member Functions**

- PAlgebraModCx (const PAlgebra &palg, long \_r)
- PAlgebraModBase \* clone () const override
- PA\_tag getTag () const override

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

const PAlgebra & getZMStar () const override

Returns reference to underlying PAlgebra object.

• long getR () const override

The value r.

• long getPPowR () const override

The value  $p^{\wedge}r$ .

• void restoreContext () const override

Restores the NTL context for  $p^{\wedge}r$ .

const std::vector< NTL::ZZX > & getFactorsOverZZ () const override

Returns reference to the factorization of Phi\_m(X) mod  $p^{\wedge}$ r, but as ZZX's.

zzX getMask\_zzX (UNUSED long i, UNUSED long j) const override

## 7.104.1 Detailed Description

A different derived class to be used for the approximate-numbers scheme This is mostly a dummy class, but needed since the context always has a PAlgebraMod data member.

### 7.104.2 Constructor & Destructor Documentation

## 7.104.2.1 PAlgebraModCx()

## 7.104.3 Member Function Documentation

## 7.104.3.1 clone()

```
PAlgebraModBase* helib::PAlgebraModCx::clone ( ) const [inline], [override], [virtual]
```

Implements helib::PAlgebraModBase.

## 7.104.3.2 getFactorsOverZZ()

```
const std::vector<NTL::ZZX>& helib::PAlgebraModCx::getFactorsOverZZ ( ) const [inline], [override],
[virtual]
```

Returns reference to the factorization of Phi\_m(X) mod p^r, but as ZZX's.

Implements helib::PAlgebraModBase.

## 7.104.3.3 getMask\_zzX()

## 7.104.3.4 getPPowR()

```
long helib::PAlgebraModCx::getPPowR ( ) const [inline], [override], [virtual]
```

The value  $p^r$ .

Implements helib::PAlgebraModBase.

## 7.104.3.5 getR()

```
long helib::PAlgebraModCx::getR ( ) const [inline], [override], [virtual]
```

The value r.

Implements helib::PAlgebraModBase.

### 7.104.3.6 getTag()

```
PA_tag helib::PAlgebraModCx::getTag ( ) const [inline], [override], [virtual]
```

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

Implements helib::PAlgebraModBase.

## 7.104.3.7 getZMStar()

```
const PAlgebra& helib::PAlgebraModCx::getZMStar ( ) const [inline], [override], [virtual]
```

Returns reference to underlying PAlgebra object.

Implements helib::PAlgebraModBase.

#### 7.104.3.8 restoreContext()

```
void helib::PAlgebraModCx::restoreContext ( ) const [inline], [override], [virtual]
```

Restores the NTL context for  $p^{\uparrow}$ r.

Implements helib::PAlgebraModBase.

The documentation for this class was generated from the following file:

 $\bullet \ / Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h$ 

## 7.105 helib::PAlgebraModDerived< type > Class Template Reference

A concrete instantiation of the virtual class.

```
#include <PAlgebra.h>
```

#### **Public Member Functions**

- PAlgebraModDerived (const PAlgebra &zMStar, long r)
- PAlgebraModDerived (const PAlgebraModDerived &other)
- PAlgebraModDerived & operator= (const PAlgebraModDerived &other)
- virtual PAlgebraModBase \* clone () const override

Returns a pointer to a "clone".

virtual PA\_tag getTag () const override

Returns the type tag: PA GF2 tag or PA zz p tag.

· virtual const PAlgebra & getZMStar () const override

Returns reference to underlying PAlgebra object.

virtual const std::vector< NTL::ZZX > & getFactorsOverZZ () const override

Returns reference to the factorization of Phi\_m(X) mod  $p^{\wedge}r$ , but as ZZX's.

virtual long getR () const override

The value r.

virtual long getPPowR () const override

The value  $p^{\wedge}r$ .

· virtual void restoreContext () const override

Restores the NTL context for  $p^{\wedge}r$ .

· const RXModulus & getPhimXMod () const

Returns reference to an RXModulus representing Phi\_m(X) (mod  $p^{\wedge}r$ )

const vec\_RX & getFactors () const

Returns reference to the factors of Phim\_m(X) modulo  $p^{\wedge}r$ .

· const vec RX & getCrtCoeffs () const

Returns the CRT coefficients: element i contains (prod\_{j!=i} F\_j)^{-1} mod F\_i, where F\_0 F\_1 ... is the factorization of Phi\_m(X) mod  $p^r$ .

const std::vector< std::vector< RX >> & getMaskTable () const

Returns ref to maskTable, which is used to implement rotations (in the EncryptedArray module).

zzX getMask\_zzX (long i, long j) const override

## Embedding in the plaintext slots and decoding back

In all the functions below, G must be irreducible mod p, and the order of G must divide the order of p modulo m (as returned by zMStar.getOrdP()). In addition, when r > 1, G must be the monomial X (RX(1, 1))

void CRT decompose (std::vector< RX > &crt, const RX &H) const

Returns a std::vector crt[] such that  $crt[i] = H \mod Ft$  (with t = T[i])

void CRT reconstruct (RX &H, std::vector< RX > &crt) const

Returns H in  $R[X]/Phi_m(X)$  s.t. for every i < nSlots and t = T[i], we have H = = crt[i] (mod Ft)

void mapToSlots (MappingData < type > &mappingData, const RX &G) const

Compute the maps for all the slots. In the current implementation, we if r > 1, then we must have either deg(G) = 1 or G = factors[0].

- void embedInAllSlots (RX &H, const RX &alpha, const MappingData< type > &mappingData) const
  - Returns H in  $R[X]/Phi_m(X)$  s.t. for every t in T, the element  $Ht = (H \mod Ft)$  in R[X]/Ft(X) represents the same element as alpha in R[X]/G(X).

Returns H in  $R[X]/Phi_m(X)$  s.t. for every t in T, the element  $Ht = (H \mod Ft)$  in R[X]/Ft(X) represents the same element as alphas[i] in R[X]/G(X).

 void decodePlaintext (std::vector< RX > &alphas, const RX &ptxt, const MappingData< type > &mappingData) const

Return an array such that alphas[i] in R[X]/G(X) represent the same element as  $rt = (H \mod Ft)$  in R[X]/Ft(X) where t=T[i].

void buildLinPolyCoeffs (std::vector< RX > &C, const std::vector< RX > &L, const MappingData< type</li>
 > &mappingData) const

Returns a coefficient std::vector C for the linearized polynomial representing M.

## 7.105.1 Detailed Description

```
template < typename type > class helib::PAlgebraModDerived < type >
```

A concrete instantiation of the virtual class.

#### 7.105.2 Constructor & Destructor Documentation

#### 7.105.2.1 PAlgebraModDerived() [1/2]

#### 7.105.2.2 PAlgebraModDerived() [2/2]

## 7.105.3 Member Function Documentation

#### 7.105.3.1 buildLinPolyCoeffs()

Returns a coefficient std::vector C for the linearized polynomial representing M.

For h in  $\mathbb{Z}/(p^{\wedge}r)[X]$  of degree < d,

$$M(h(X) modG) = sum_{i=0}^{d-1}(C[j] modG) * (h(X^{p^j}) modG).$$

G is assumed to be defined in mappingData, with d = deg(G). L describes a linear map M by describing its action on the standard power basis:  $M(x^{\hat{}}j \mod G) = (L[j] \mod G)$ , for j = 0..d-1.

## 7.105.3.2 clone()

```
template<typename type >
virtual PAlgebraModBase* helib::PAlgebraModDerived< type >::clone ( ) const [inline], [override],
[virtual]
```

Returns a pointer to a "clone".

## 7.105.3.3 CRT\_decompose()

Returns a std::vector crt[] such that crt[i] = H mod Ft (with t = T[i])

### 7.105.3.4 CRT\_reconstruct()

Returns H in  $R[X]/Phi_m(X)$  s.t. for every i<nSlots and t=T[i], we have H == crt[i] (mod Ft)

## 7.105.3.5 decodePlaintext()

Return an array such that alphas[i] in R[X]/G(X) represent the same element as  $rt = (H \mod Ft)$  in R[X]/Ft(X) where t=T[i].

The mappingData argument should contain the output of mapToSlots(G).

## 7.105.3.6 embedInAllSlots()

Returns H in  $R[X]/Phi_m(X)$  s.t. for every t in T, the element  $Ht = (H \mod Ft)$  in R[X]/Ft(X) represents the same element as alpha in R[X]/G(X).

Must have deg(alpha) < deg(G). The mappingData argument should contain the output of mapToSlots(G).

## 7.105.3.7 embedInSlots()

Returns H in  $R[X]/Phi_m(X)$  s.t. for every t in T, the element  $Ht = (H \mod Ft)$  in R[X]/Ft(X) represents the same element as alphas[i] in R[X]/G(X).

Must have deg(alpha[i])<deg(G). The mappingData argument should contain the output of mapToSlots(G).

## 7.105.3.8 getCrtCoeffs()

```
template<typename type >
const vec_RX& helib::PAlgebraModDerived< type >::getCrtCoeffs ( ) const [inline]
```

Returns the CRT coefficients: element i contains (prod\_{j!=i} F\_j)^{-1} mod F\_i, where F\_0 F\_1 ... is the factorization of Phi\_m(X) mod  $p^r$ .

#### 7.105.3.9 getFactors()

```
template<typename type >
const vec_RX& helib::PAlgebraModDerived< type >::getFactors ( ) const [inline]
```

Returns reference to the factors of Phim m(X) modulo  $p^{\wedge}r$ .

## 7.105.3.10 getFactorsOverZZ()

```
template<typename type >
virtual const std::vector<NTL::ZZX>& helib::PAlgebraModDerived< type >::getFactorsOverZZ ( )
const [inline], [override], [virtual]
```

Returns reference to the factorization of Phi\_m(X) mod  $p^{\wedge}r$ , but as ZZX's.

## 7.105.3.11 getMask\_zzX()

## 7.105.3.12 getMaskTable()

```
template<typename type >
const std::vector<std::vector<RX> >& helib::PAlgebraModDerived< type >::getMaskTable ( )
const [inline]
```

Returns ref to maskTable, which is used to implement rotations (in the EncryptedArray module).

maskTable[i][j] is a polynomial representation of a mask that is 1 in all slots whose i'th coordinate is at least j, and 0 elsewhere. We have:

## 7.105.3.13 getPhimXMod()

```
template<typename type >
const RXModulus& helib::PAlgebraModDerived< type >::getPhimXMod ( ) const [inline]
```

Returns reference to an RXModulus representing Phi\_m(X) (mod p^r)

#### 7.105.3.14 getPPowR()

```
template<typename type >
virtual long helib::PAlgebraModDerived< type >::getPPowR ( ) const [inline], [override],
[virtual]
```

The value  $p^{r}$ .

## 7.105.3.15 getR()

```
template<typename type >
virtual long helib::PAlgebraModDerived< type >::getR ( ) const [inline], [override], [virtual]
```

The value r.

#### 7.105.3.16 getTag()

```
template<typename type >
virtual PA_tag helib::PAlgebraModDerived< type >::getTag ( ) const [inline], [override],
[virtual]
```

Returns the type tag: PA\_GF2\_tag or PA\_zz\_p\_tag.

### 7.105.3.17 getZMStar()

```
template<typename type >
virtual const PAlgebra& helib::PAlgebraModDerived< type >::getZMStar ( ) const [inline],
[override], [virtual]
```

Returns reference to underlying PAlgebra object.

#### 7.105.3.18 mapToSlots()

Compute the maps for all the slots. In the current implementation, we if r > 1, then we must have either deg(G) == 1 or G == factors[0].

## 7.105.3.19 operator=()

#### 7.105.3.20 restoreContext()

```
template<typename type >
virtual void helib::PAlgebraModDerived< type >::restoreContext ( ) const [inline], [override],
[virtual]
```

Restores the NTL context for p^r.

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PAlgebra.cpp

## 7.106 helib::PermNetLayer Class Reference

The information needed to apply one layer of a permutation network.

```
#include <permutations.h>
```

## **Public Member Functions**

- long getGenIdx () const
- long getE () const
- const NTL::Vec< long > & getShifts () const
- bool isldentity () const

## **Friends**

- class PermNetwork
- std::ostream & operator<< (std::ostream &s, const PermNetwork &net)

## 7.106.1 Detailed Description

The information needed to apply one layer of a permutation network.

## 7.106.2 Member Function Documentation

## 7.106.2.1 getE()

```
long helib::PermNetLayer::getE ( ) const [inline]
```

## 7.106.2.2 getGenIdx()

```
long helib::PermNetLayer::getGenIdx ( ) const [inline]
```

## 7.106.2.3 getShifts()

```
const NTL::Vec<long>& helib::PermNetLayer::getShifts ( ) const [inline]
```

## 7.106.2.4 isldentity()

```
bool helib::PermNetLayer::isIdentity ( ) const [inline]
```

## 7.106.3 Friends And Related Function Documentation

#### 7.106.3.1 operator <<

```
std::ostream& operator<< (
          std::ostream & s,
          const PermNetwork & net ) [friend]</pre>
```

## 7.106.3.2 PermNetwork

```
friend class PermNetwork [friend]
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h

## 7.107 helib::PermNetwork Class Reference

A full permutation network.

```
#include <permutations.h>
```

## **Public Member Functions**

- PermNetwork ()
- PermNetwork (const Permut &pi, const GeneratorTrees &trees)
- · long depth () const
- void buildNetwork (const Permut &pi, const GeneratorTrees &trees)
- void applyToCtxt (Ctxt &c, const EncryptedArray &ea) const

Apply network to permute a ciphertext.

• void applyToCube (HyperCube < long > &v) const

Apply network to array, used mostly for debugging.

- void applyToPtxt (NTL::ZZX &p, const EncryptedArray &ea) const
  - Apply network to plaintext polynomial, used mostly for debugging.
- const PermNetLayer & getLayer (long i) const

### Friends

std::ostream & operator<< (std::ostream &s, const PermNetwork &net)</li>

## 7.107.1 Detailed Description

A full permutation network.

## 7.107.2 Constructor & Destructor Documentation

## 7.107.2.1 PermNetwork() [1/2]

```
helib::PermNetwork::PermNetwork ( ) [inline]
```

## 7.107.2.2 PermNetwork() [2/2]

## 7.107.3 Member Function Documentation

#### 7.107.3.1 applyToCtxt()

Apply network to permute a ciphertext.

## 7.107.3.2 applyToCube()

```
void helib::PermNetwork::applyToCube ( \label{eq:hyperCube} \mbox{HyperCube} < \mbox{long} > \& \ v \ \mbox{) const}
```

Apply network to array, used mostly for debugging.

## 7.107.3.3 applyToPtxt()

Apply network to plaintext polynomial, used mostly for debugging.

## 7.107.3.4 buildNetwork()

Take as input a permutation pi and the trees of all the generators, and prepares the permutation network for this pi

## 7.107.3.5 depth()

```
long helib::PermNetwork::depth ( ) const [inline]
```

#### 7.107.3.6 getLayer()

## 7.107.4 Friends And Related Function Documentation

## 7.107.4.1 operator <<

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PermNetwork.cpp

## 7.108 helib::PGFFT Class Reference

```
#include <PGFFT.h>
```

## Classes

· class aligned\_allocator

## **Public Types**

```
    template < class T >
        using aligned_vector = std::vector < T, aligned_allocator < T > >
```

## **Public Member Functions**

```
• PGFFT (long n)
```

- void apply (const std::complex< double > \*src, std::complex< double > \*dst) const
- void apply (std::complex < double > \*v) const
- PGFFT (const PGFFT &)=delete
- PGFFT (PGFFT &&)=delete
- PGFFT & operator= (const PGFFT &)=delete
- PGFFT & operator= (PGFFT &&)=delete

## **Static Public Member Functions**

```
• static bool simd_enabled ()
```

- static void \* aligned\_allocate (std::size\_t n, std::size\_t nelts)
- static void aligned\_deallocate (void \*p)

## 7.108.1 Member Typedef Documentation

## 7.108.1.1 aligned\_vector

```
template<class T >
using helib::PGFFT::aligned_vector = std::vector<T,aligned_allocator<T> >
```

## 7.108.2 Constructor & Destructor Documentation

## 7.108.2.1 PGFFT() [1/3]

```
\label{eq:posterior} \mbox{helib::PGFFT::PGFFT (} \\ \mbox{long } n \mbox{ ) } \mbox{ [explicit]}
```

## 7.108.2.2 PGFFT() [2/3]

## 7.108.2.3 PGFFT() [3/3]

# 7.108.3 Member Function Documentation

# 7.108.3.1 aligned\_allocate()

## 7.108.3.2 aligned\_deallocate()

# 7.108.3.3 apply() [1/2]

# 7.108.3.4 apply() [2/2]

# 7.108.3.5 operator=() [1/2]

## 7.108.3.6 operator=() [2/2]

```
PGFFT& helib::PGFFT::operator= (
          PGFFT && ) [delete]
```

## 7.108.3.7 simd\_enabled()

```
bool helib::PGFFT::simd_enabled ( ) [static]
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PGFFT.h
- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/PGFFT.cpp

# 7.109 helib::PlaintextArray Class Reference

```
#include <EncryptedArray.h>
```

## **Public Member Functions**

- PlaintextArray (const EncryptedArray &ea)
- PlaintextArray (const PlaintextArray &other)
- PlaintextArray & operator= (const PlaintextArray &other)
- template<typename type >
   std::vector< typename type::RX > & getData ()
- template<typename type >
   const std::vector< typename type::RX > & getData () const
- void print (std::ostream &s) const

# 7.109.1 Constructor & Destructor Documentation

#### 7.109.1.1 PlaintextArray() [1/2]

## 7.109.1.2 PlaintextArray() [2/2]

#### 7.109.2 Member Function Documentation

#### 7.109.2.1 getData() [1/2]

```
template<typename type >
std::vector<typename type::RX>& helib::PlaintextArray::getData ( ) [inline]
```

## 7.109.2.2 getData() [2/2]

```
template<typename type >
const std::vector<typename type::RX>& helib::PlaintextArray::getData ( ) const [inline]
```

## 7.109.2.3 operator=()

#### 7.109.2.4 print()

```
void helib::PlaintextArray::print ( {\tt std::ostream~\&~s~)~const~[inline]}
```

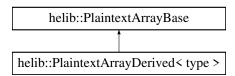
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/EncryptedArray.h

# 7.110 helib::PlaintextArrayBase Class Reference

```
#include <EncryptedArray.h>
```

Inheritance diagram for helib::PlaintextArrayBase:



# **Public Member Functions**

- virtual ~PlaintextArrayBase ()
- virtual void print (std::ostream &s) const =0

# 7.110.1 Constructor & Destructor Documentation

# 7.110.1.1 ~PlaintextArrayBase()

```
virtual helib::PlaintextArrayBase::~PlaintextArrayBase ( ) [inline], [virtual]
```

## 7.110.2 Member Function Documentation

## 7.110.2.1 print()

Implemented in helib::PlaintextArrayDerived< type >.

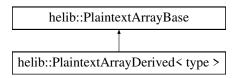
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/EncryptedArray.h

# 7.111 helib::PlaintextArrayDerived< type > Class Template Reference

```
#include <EncryptedArray.h>
```

Inheritance diagram for helib::PlaintextArrayDerived< type >:



#### **Public Member Functions**

virtual void print (std::ostream &s) const

## **Public Attributes**

std::vector< RX > data

#### 7.111.1 Member Function Documentation

## 7.111.1.1 print()

```
template<typename type > virtual void helib::PlaintextArrayDerived< type >::print ( std::ostream & s ) const [inline], [virtual]
```

Implements helib::PlaintextArrayBase.

## 7.111.2 Member Data Documentation

#### 7.111.2.1 data

```
template<typename type >
std::vector<RX> helib::PlaintextArrayDerived< type >::data
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/EncryptedArray.h

# 7.112 helib::PolyMod Class Reference

An object that contains an NTL:: ZZX polynomial along with a coefficient modulus p2r and a polynomial modulus G.

```
#include <PolyMod.h>
```

# **Public Member Functions**

• PolyMod ()

Default constructor.

PolyMod (const std::shared\_ptr< PolyModRing > &ringDescriptor)

No-data constructor.

PolyMod (long input, const std::shared\_ptr< PolyModRing > &ringDescriptor)

Constant constructor.

• PolyMod (const std::vector< long > &input, const std::shared\_ptr< PolyModRing > &ringDescriptor)

Coefficient vector constructor.

PolyMod (const NTL::ZZX &input, const std::shared\_ptr< PolyModRing > &ringDescriptor)

Polynomial constructor.

• PolyMod (const PolyMod &input)=default

Default copy constructor.

PolyMod (PolyMod &&input) noexcept=default

Default move constructor.

∼PolyMod ()=default

Default destructor.

• PolyMod & operator= (const PolyMod &input)=default

Assignment operator.

PolyMod & operator= (PolyMod &&input)=default

default move assignment operator

PolyMod & operator= (long input)

long assignment operator, creates a constant polynomial mod G and p2r.

PolyMod & operator= (const std::vector < long > &input)

std::vector<long> assignment operator, creates a polynomial mod G and p2r.

PolyMod & operator= (const std::initializer\_list< long > &input)

std::initializer\_list<long> assignment operator, creates a polynomial mod G and p2r.

PolyMod & operator= (const NTL::ZZX &input)

NTL:: ZZX assignment operator, creates a polynomial mod G and p2r.

operator long () const

Explicit conversion to a long.

operator std::vector< long > () const

Explicit conversion to std::vector<long> (coefficient vector).

operator NTL::ZZX () const

Explicit conversion to an NTL:: ZZX.

• bool isValid () const

Gets the validity of this. This will be false iff this was default constructed.

· long getp2r () const

Get current  $p^{\wedge}r$  value.

• NTL::ZZX getG () const

Get current G value.

• NTL::ZZX getData () const

Getter function that returns the data of PolyMod as an NTL::ZZX.

bool operator== (const PolyMod &rhs) const

Equals operator between two PolyMod objects.

• bool operator== (long rhs) const

Equals operator between a PolyMod and a long.

bool operator== (const std::vector< long > &rhs) const

Equals operator between two PolyMod objects.

bool operator== (const NTL::ZZX &rhs) const

Equals operator between two PolyMod objects.

• template<typename T >

bool operator!= (T &&rhs) const

Not equals operator.

PolyMod & negate ()

Negate function.

· PolyMod operator- () const

Unary minus operator.

• PolyMod operator\* (const PolyMod &rhs) const

Infix multiplication operator.

• PolyMod operator\* (long rhs) const

Infix multiplication operator with long.

PolyMod operator\* (const NTL::ZZX &rhs) const

Infix multiplication operator with NTL:: ZZX.

 PolyMod operator+ (const PolyMod &rhs) const Infix plus operator.

PolyMod operator+ (long rhs) const

Infix plus operator with long.

PolyMod operator+ (const NTL::ZZX &rhs) const

Infix plus operator with NTL:: ZZX.

PolyMod operator- (const PolyMod &rhs) const

Infix minus operator.

• PolyMod operator- (long rhs) const

Infix minus operator with long.

PolyMod operator- (const NTL::ZZX &rhs) const

Infix minus operator with NTL:: ZZX.

• PolyMod & operator\*= (const PolyMod &otherPoly)

Times equals operator with PolyMod rhs.

PolyMod & operator\*= (long scalar)

Times equals operator with long rhs.

PolyMod & operator\*= (const NTL::ZZX &otherPoly)

Times equals operator with NTL:: ZZX rhs.

PolyMod & operator+= (const PolyMod &otherPoly)

Plus equals operator with PolyMod rhs.

PolyMod & operator+= (long scalar)

Plus equals operator with long rhs.

PolyMod & operator+= (const NTL::ZZX &otherPoly)

Plus equals operator with NTL:: ZZX rhs.

PolyMod & operator-= (const PolyMod &otherPoly)

Minus equals operator with PolyMod rhs.

• PolyMod & operator-= (long scalar)

Minus equals operator with long rhs.

PolyMod & operator= (const NTL::ZZX &otherPoly)

Minus equals operator with NTL:: ZZX rhs.

#### **Friends**

- std::istream & operator>> (std::istream &is, PolyMod &poly)
   Input shift operator.
- std::ostream & operator<< (std::ostream &os, const PolyMod &poly)</li>

Output shift operator.

## 7.112.1 Detailed Description

An object that contains an NTL:: ZZX polynomial along with a coefficient modulus p2r and a polynomial modulus C

A PolyMod object can be considered to be an element of  $\mathbb{Z}_{p^r}[x]/G$  where  $p^r$  and G are the passed-in parameters p2r and G.

This allows for inter-PolyMod operations with the modulo operations performed automatically.

#### General usage:

helib::PolyMod poly(input\_data, p2r, G);

Calling an operation on a default constructed PolyMod will throw an helib::LogicError.

# 7.112.2 Constructor & Destructor Documentation

# 7.112.2.1 PolyMod() [1/7]

```
helib::PolyMod::PolyMod ( )
```

Default constructor.

Note

PolyMod objects constructed using this are marked as invalid. If used for any operation whether directly on a PolyMod or via another object such as Ptxt this will produce an error.

## 7.112.2.2 PolyMod() [2/7]

No-data constructor.

#### **Parameters**

| ringDescriptor | Descriptor |
|----------------|------------|
| ringbessripter | object     |
|                | for the    |
|                |            |
|                | plain-     |
|                | text       |
|                | ring.      |
|                | Con-       |
|                | tains      |
|                | p^r        |
|                | and G      |
|                | which      |
|                | are        |
|                | to be      |
|                | used       |
|                | for        |
|                | mod-       |
|                | ular       |
|                | reduc-     |
|                | tion.      |

## Note

This constructor does not take in input data but can be assigned data later via operator=.

# 7.112.2.3 PolyMod() [3/7]

# Constant constructor.

#### **Parameters**

| rarameters     |  |
|----------------|--|
| input          | Input data as a long.  |
| ringDescriptor | Descriptor object for the plaintext ring. Contains p^r and G which are to be used for modular reduction. |

# Note

This constructor accepts input data as a long and converts it into an NTL:: ZZX polynomial.

# 7.112.2.4 PolyMod() [4/7]

Coefficient vector constructor.

# **Parameters**

| i arameters    |            |
|----------------|------------|
| input          | Input      |
|                | data       |
|                | as a       |
|                | vec-       |
|                | tor of     |
|                | long       |
|                | (the       |
|                | i'th el-   |
|                | ement      |
|                | of the     |
|                | vector     |
|                | corre-     |
|                | sponds     |
|                | to the     |
|                | coef-      |
|                | ficient    |
|                | of x^i).   |
| ringDescriptor | Descriptor |
|                | object     |
|                | for the    |
|                | plain-     |
|                | text       |
|                | ring.      |
|                | Con-       |
|                | tains      |
|                | p^r        |
|                | and G      |
|                | which      |
|                | are        |
|                | to be      |
|                | used       |
|                | for        |
|                | mod-       |
|                | ular       |
|                | reduc-     |
|                | tion.      |
|                |            |

# Note

This constructor accepts input data as a std::vector < long> and converts it into an NTL::ZZX polynomial.

# 7.112.2.5 PolyMod() [5/7]

Polynomial constructor.

# **Parameters**

| input          | Input data as an NTL← :: Z← ZX.  |
|----------------|--|
| ringDescriptor | Descriptor object for the plaintext ring. Contains p^r and G which are to be used for modular reduction. |

#### Note

This constructor accepts input data as an NTL::  ${\tt ZZX}$ .

# 7.112.2.6 PolyMod() [6/7]

Default copy constructor.

# **Parameters**

| input | PolyMod |
|-------|---------|
|       | object  |
|       | that is |
|       | copied. |

# 7.112.2.7 PolyMod() [7/7]

Default move constructor.

# 7.112.2.8 ∼PolyMod()

```
helib::PolyMod::~PolyMod ( ) [default]
```

Default destructor.

# 7.112.3 Member Function Documentation

## 7.112.3.1 getData()

```
NTL::ZZX helib::PolyMod::getData ( ) const
```

Getter function that returns the data of PolyMod as an NTL:: ZZX.

# 7.112.3.2 getG()

```
NTL::ZZX helib::PolyMod::getG ( ) const
```

Get current G value.

Returns

The current G value in use.

# 7.112.3.3 getp2r()

```
long helib::PolyMod::getp2r ( ) const
```

Get current  $p^{\wedge}r$  value.

Returns

The current p^r value in use.

#### 7.112.3.4 isValid()

```
bool helib::PolyMod::isValid ( ) const
```

Gets the validity of this. This will be false iff this was default constructed.

#### Returns

true if this is valid, false otherwise.

#### 7.112.3.5 negate()

```
PolyMod & helib::PolyMod::negate ( )
```

Negate function.

Returns

Reference to \*this post negation.

## 7.112.3.6 operator long()

```
helib::PolyMod::operator long ( ) const [explicit]
```

Explicit conversion to a long.

Note

This function returns only the constant term even if the polynomial contains higher order terms.

## 7.112.3.7 operator NTL::ZZX()

```
helib::PolyMod::operator NTL::ZZX ( ) const [explicit] 
Explicit conversion to an NTL::ZZX.
```

## 7.112.3.8 operator std::vector< long >()

```
helib::PolyMod::operator std::vector< long > ( ) const [explicit]
```

Explicit conversion to std::vector<long> (coefficient vector).

## 7.112.3.9 operator"!=()

Not equals operator.

## **Parameters**

| rhs | Right-  |
|-----|---------|
|     | hand    |
|     | side of |
|     | com-    |
|     | pari-   |
|     | son.    |

## Returns

true if not equal, false otherwise

#### Note

Simply forwards to the correct operator == method.

# 7.112.3.10 operator\*() [1/3]

Infix multiplication operator with NTL:: ZZX.

#### **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | multi-  |
|     | plica-  |
|     | tion.   |

#### Returns

Product of the two objects.

# 7.112.3.11 operator\*() [2/3]

Infix multiplication operator.

## **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | multi-  |
|     | plica-  |
|     | tion.   |

## Returns

Product of the two PolyMod objects.

# 7.112.3.12 operator\*() [3/3]

Infix multiplication operator with long.

# **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | multi-  |
|     | plica-  |
|     | tion.   |

## Returns

Product of the two values.

# 7.112.3.13 operator\*=() [1/3]

Times equals operator with  $\mathtt{NTL}$  :  $\mathtt{ZZX}$  rhs.

## **Parameters**

| otherPoly | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | multi-  |
|           | plica-  |
|           | tion.   |

#### Returns

Reference to \*this post multiplication.

# 7.112.3.14 operator\*=() [2/3]

Times equals operator with PolyMod rhs.

## **Parameters**

| otherPoly | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | multi-  |
|           | plica-  |
|           | tion.   |

## Returns

Reference to \*this post multiplication.

# 7.112.3.15 operator\*=() [3/3]

Times equals operator with long rhs.

#### **Parameters**

|        | _       |
|--------|---------|
| scalar | Right   |
|        | hand    |
|        | side of |
|        | multi-  |
|        | plica-  |
|        | tion.   |

## Returns

Reference to \*this post multiplication.

# 7.112.3.16 operator+() [1/3]

Infix plus operator with NTL::ZZX.

## **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | addi-   |
|     | tion.   |

## Returns

Sum of the two objects.

# 7.112.3.17 operator+() [2/3]

Infix plus operator.

## Parameters

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | addi-   |
|     | tion.   |

## Returns

Sum of the two PolyMod objects.

# 7.112.3.18 operator+() [3/3]

Infix plus operator with long.

## **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | addi-   |
|     | tion.   |

# Returns

Sum of the two values.

# 7.112.3.19 operator+=() [1/3]

Plus equals operator with NTL:: ZZX rhs.

#### **Parameters**

| otherPoly | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | addi-   |
|           | tion.   |

# Returns

Reference to  $\verb|*this|$  post addition.

# 7.112.3.20 operator+=() [2/3]

Plus equals operator with PolyMod rhs.

## **Parameters**

| i ai ai i i o to i o |         |
|----------------------|---------|
| otherPoly            | Right   |
|                      | hand    |
|                      | side of |
|                      | addi-   |
|                      | tion.   |

#### Returns

Reference to \*this post addition.

# 7.112.3.21 operator+=() [3/3]

Plus equals operator with long rhs.

#### **Parameters**

| scalar | Right   |
|--------|---------|
|        | hand    |
|        | side of |
|        | addi-   |
|        | tion.   |

#### Returns

Reference to \*this post addition.

# 7.112.3.22 operator-() [1/4]

```
PolyMod helib::PolyMod::operator- ( ) const
```

Unary minus operator.

## Returns

Negation of the PolyMod.

# 7.112.3.23 operator-() [2/4]

Infix minus operator with NTL::ZZX.

# **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | sub-    |
|     | trac-   |
|     | tion.   |

## Returns

Difference of the two objects.

# 7.112.3.24 operator-() [3/4]

Infix minus operator.

# **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | sub-    |
|     | trac-   |
|     | tion.   |

## Returns

Difference of the two PolyMod objects.

# 7.112.3.25 operator-() [4/4]

Infix minus operator with long.

# **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | sub-    |
|     | trac-   |
|     | tion.   |

#### Returns

Difference of the two values.

# 7.112.3.26 operator-=() [1/3]

Minus equals operator with NTL:: ZZX rhs.

## **Parameters**

| otherPoly | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | sub-    |
|           | trac-   |
|           | tion.   |

## Returns

Reference to \*this post subtraction.

# 7.112.3.27 operator-=() [2/3]

Minus equals operator with PolyMod rhs.

#### **Parameters**

| otherPoly | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | sub-    |
|           | trac-   |
|           | tion.   |

## Returns

Reference to \*this post subtraction.

# 7.112.3.28 operator-=() [3/3]

Minus equals operator with long rhs.

## **Parameters**

| scalar | Right   |
|--------|---------|
|        | hand    |
|        | side of |
|        | sub-    |
|        | trac-   |
|        | tion.   |

## Returns

Reference to \*this post subtraction.

# 7.112.3.29 operator=() [1/6]

 $\mathtt{NTL}: \mathtt{ZZX}$  assignment operator, creates a polynomial mod G and p2r.

# **Parameters**

```
input Polynomial.
```

# 7.112.3.30 operator=() [2/6]

Assignment operator.

#### **Parameters**

| input | Another |
|-------|---------|
|       | PolyMod |
|       | to      |
|       | сору.   |

# 7.112.3.31 operator=() [3/6]

 $\verb|std::initializer_list<| long>| assignment operator, creates a polynomial mod G and p2r.$ 

## **Parameters**

| input | coefficient |
|-------|-------------|
|       | vector      |
|       | as an       |
|       | initial-    |
|       | izer        |
|       | list of     |
|       | long        |
|       | (the        |
|       | i'th el-    |
|       | ement       |
|       | of the      |
|       | vector      |
|       | corre-      |
|       | sponds      |
|       | to the      |
|       | coef-       |
|       | ficient     |
|       | of x^i).    |

# 7.112.3.32 operator=() [4/6]

std::vector<long> assignment operator, creates a polynomial mod G and p2r.

## **Parameters**

| input | Coefficien  |
|-------|-------------|
|       | vec-        |
|       | tor of      |
|       | long        |
|       | (the        |
|       | i'th el-    |
|       | ement       |
|       | of the      |
|       | vector      |
|       | corre-      |
|       | sponds      |
|       | to the      |
|       | coef-       |
|       | ficient     |
|       | of $x^i$ ). |

# 7.112.3.33 operator=() [5/6]

long assignment operator, creates a constant polynomial mod G and p2r.

## **Parameters**

| input | long   |
|-------|--------|
|       | datum. |

# 7.112.3.34 operator=() [6/6]

default move assignment operator

## 7.112.3.35 operator==() [1/4]

Equals operator between two PolyMod objects.

## **Parameters**

| rhs | Other   |
|-----|---------|
|     | PolyMod |
|     | to      |
|     | com-    |
|     | pare    |
|     | to.     |

#### Returns

true if identical, false otherwise.

# Note

Always returns false when called on invalid PolyMod objects.

## 7.112.3.36 operator==() [2/4]

Equals operator between two PolyMod objects.

## **Parameters**

| rhs | Other   |
|-----|---------|
|     | PolyMod |
|     | to      |
|     | com-    |
|     | pare    |
|     | to.     |

#### Returns

true if PolyMod objects are identical, false otherwise.

## 7.112.3.37 operator==() [3/4]

```
bool helib::PolyMod::operator== ( {\tt const \ std::vector} < \ {\tt long} \ > \ \& \ {\it rhs} \ ) \ {\tt const}
```

Equals operator between two PolyMod objects.

#### **Parameters**

| rhs | Other   |  |
|-----|---------|--|
|     | PolyMod |  |
|     | to      |  |
|     | com-    |  |
|     | pare    |  |
|     | to.     |  |

# Returns

true if identical, false otherwise.

## Note

Always returns false when called on invalid  ${\tt PolyMod}$  objects.

## 7.112.3.38 operator==() [4/4]

Equals operator between a PolyMod and a long.

#### **Parameters**

| rhs | long     |
|-----|----------|
|     | to       |
|     | com-     |
|     | pare     |
|     | the      |
|     | data     |
|     | against. |

## Returns

true if identical, false otherwise.

Note

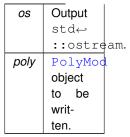
Always returns false when called on invalid PolyMod objects.

# 7.112.4 Friends And Related Function Documentation

## 7.112.4.1 operator <<

Output shift operator.

#### **Parameters**



## Returns

Input std::ostream post writing.

## Note

p2r and G are not serialised, see note of operator>>.

# 7.112.4.2 operator>>

```
std::istream& operator>> (
          std::istream & is,
          PolyMod & poly ) [friend]
```

Input shift operator.

#### **Parameters**

| is   | Input       |
|------|-------------|
|      | std↔        |
|      | ::istream.  |
| poly | Destination |
|      | PolyMod     |
|      | object.     |

#### Returns

Input std::istream post reading.

#### Note

```
poly must be constructed with an appropriate p2r and G BEFORE calling this function. For example, PolyMod my_poly(p2r, G); std::cin > my_poly;
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PolyMod.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PolyMod.cpp

# 7.113 helib::PolyModRing Struct Reference

Lightweight type for describing the structure of a single slot of the plaintext space.

```
#include <PolyModRing.h>
```

# **Public Member Functions**

- PolyModRing ()=delete
- PolyModRing & operator= (const PolyModRing &)=delete
- PolyModRing & operator= (PolyModRing &&)=delete
- PolyModRing (const PolyModRing &other)=default

Copy constructor.

PolyModRing (PolyModRing &&other)=default

Move constructor.

∼PolyModRing ()=default

Destructor.

PolyModRing (long p, long r, const NTL::ZZX &G)

Constructor.

• bool operator== (const PolyModRing &rhs) const noexcept

Equality operator.

bool operator!= (const PolyModRing &rhs) const noexcept

Not-equals operator.

## **Public Attributes**

· const long p

The characteristic of the plaintext space. This should be prime.

· const long r

The power of p used in the plaintext space coefficient modulus.

· const NTL::ZZX G

The irreducible factor of  $Phi_m(X)$  used for the algebra of the individual slots.

· const long p2r

The plaintext space coefficient modulus, equal to  $p^{\wedge}r$ .

#### **Friends**

std::ostream & operator<< (std::ostream &os, const PolyModRing &ring)</li>
 Output shift operator.

# 7.113.1 Detailed Description

Lightweight type for describing the structure of a single slot of the plaintext space.

A single slot of the plaintext space is isomorphic to  $\mathbb{Z}[X]/(G(x),p^r)$  for some irreducible factor G of  $\Phi_m(X)$ , so the main useful members of this struct are p, r, G, and p2r.

The fields of this struct are all const, so they should be determined at the time of construction.

Note

This struct aggregates this often-useful information into a single placeholder for convenience.

## 7.113.2 Constructor & Destructor Documentation

## 7.113.2.1 PolyModRing() [1/4]

```
helib::PolyModRing::PolyModRing ( ) [delete]
```

# 7.113.2.2 PolyModRing() [2/4]

Copy constructor.

# 7.113.2.3 PolyModRing() [3/4]

Move constructor.

# 7.113.2.4 $\sim$ PolyModRing()

```
\verb|helib::PolyModRing::\sim PolyModRing ( ) [default]|\\
```

Destructor.

# 7.113.2.5 PolyModRing() [4/4]

```
\label{eq:polyModRing:polyModRing} \mbox{ ( } & \mbox{long } p, \\ & \mbox{long } r, \\ & \mbox{const NTL::ZZX & $G$ )} \\
```

Constructor.

## Parameters

| р | The     |
|---|---------|
|   | char-   |
|   | acter-  |
|   | istic   |
|   | of the  |
|   | plain-  |
|   | text    |
|   | space.  |
| r | The     |
|   | power   |
|   | of p    |
|   | used    |
|   | in the  |
|   | plain-  |
|   | text    |
|   | space   |
|   | coef-   |
|   | ficient |
|   | modu-   |
|   | lus.    |

## **Parameters**

| G | The     |
|---|---------|
|   | irre-   |
|   | ducible |
|   | fac-    |
|   | tor of  |
|   | Phi←    |
|   | _m(X)   |
|   | used    |
|   | for the |
|   | alge-   |
|   | bra     |
|   | of the  |
|   | indi-   |
|   | vidual  |
|   | slots.  |

p^r will be calculated automatically.

Note

p should be a prime number.

# 7.113.3 Member Function Documentation

# 7.113.3.1 operator"!=()

Not-equals operator.

# 7.113.3.2 operator=() [1/2]

# 7.113.3.3 operator=() [2/2]

# 7.113.3.4 operator==()

Equality operator.

## 7.113.4 Friends And Related Function Documentation

#### 7.113.4.1 operator <<

Output shift operator.

#### **Parameters**

| os   | Output      |
|------|-------------|
|      | std↔        |
|      | ::ostream.  |
| ring | PolyModRing |
|      | object      |
|      | to be       |
|      | writ-       |
|      | ten.        |

# Returns

Input std::ostream post writing.

# 7.113.5 Member Data Documentation

## 7.113.5.1 G

```
const NTL::ZZX helib::PolyModRing::G
```

The irreducible factor of  $Phi_m(X)$  used for the algebra of the individual slots.

#### 7.113.5.2 p

```
const long helib::PolyModRing::p
```

The characteristic of the plaintext space. This should be prime.

#### 7.113.5.3 p2r

```
const long helib::PolyModRing::p2r
```

The plaintext space coefficient modulus, equal to  $p^{\wedge}r$ .

#### 7.113.5.4 r

```
const long helib::PolyModRing::r
```

The power of p used in the plaintext space coefficient modulus.

The documentation for this struct was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PolyModRing.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PolyModRing.cpp

# 7.114 helib::PowerfulConversion Class Reference

Conversion between powerful representation in R\_m/(q) and zz\_pX.

```
#include <powerful.h>
```

#### **Public Member Functions**

- PowerfulConversion ()
- PowerfulConversion (const PowerfulTranslationIndexes &ind)
- void initPConv (const PowerfulTranslationIndexes &ind)
- void restoreModulus () const
- const CubeSignature & getLongSig () const
- · const CubeSignature & getShortSig () const
- long powerfulToPoly (NTL::zz pX &poly, const HyperCube < NTL::zz p > &powerful) const
- $\bullet \ \ long \ polyToPowerful \ (HyperCube < NTL::zz\_p > \&powerful, \ const \ NTL::zz\_pX \ \&poly) \ const$

# 7.114.1 Detailed Description

Conversion between powerful representation in R\_m/(q) and zz\_pX.

Usage pattern is as follows:

// compute tables for index translation PowerfulTranslationIndexes ind(mvec); // mvec is some factorization of m

// ... set the current zz\_p::modulus to something before initializing PowerfulConversion pConv(ind);

// Alternatively use // PowerfulConversion pConv(); pConv.initPConv(ind); // Only the latter call needs zz\_p::modulus to be defined

// A powerful basis is defined wrt same modulus and cube signature HyperCube<zz\_p> powerful(pConv.get ← ShortSig());

// ... some code here to initialize powerful // code can also do other stuff, perhaps changing zz\_p::modulus

pConv.restoreModulus(); // restore zz\_p::modulus zz\_pX poly; // defined relative to the same modulus pConv. powerfulToPoly(poly, powerful);

// ... some more code here, perhaps changing zz\_p::modulus again

pConv.restoreModulus(); // restore zz p::modulus pConv.polyToPowerful(powerful, poly);

## 7.114.2 Constructor & Destructor Documentation

#### 7.114.2.1 PowerfulConversion() [1/2]

```
\verb|helib::PowerfulConversion::PowerfulConversion () [inline]|\\
```

## 7.114.2.2 PowerfulConversion() [2/2]

```
helib::PowerfulConversion::PowerfulConversion (

const PowerfulTranslationIndexes & ind ) [inline], [explicit]
```

#### 7.114.3 Member Function Documentation

## 7.114.3.1 getLongSig()

```
const CubeSignature& helib::PowerfulConversion::getLongSig ( ) const [inline]
```

## 7.114.3.2 getShortSig()

```
const CubeSignature& helib::PowerfulConversion::getShortSig ( ) const [inline]
```

## 7.114.3.3 initPConv()

#### 7.114.3.4 polyToPowerful()

#### 7.114.3.5 powerfulToPoly()

The conversion routines return the value of the modulus q. It is assumed that the modulus is already set before calling them

# 7.114.3.6 restoreModulus()

```
void helib::PowerfulConversion::restoreModulus ( ) const [inline]
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/powerful.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/powerful.cpp

# 7.115 helib::PowerfulDCRT Class Reference

Conversion between powerful representation, DoubleCRT, and ZZX.

```
#include <powerful.h>
```

#### **Public Member Functions**

- PowerfulDCRT (const Context &\_context, const NTL::Vec< long > &mvec)
- const PowerfulTranslationIndexes & getIndexTranslation () const
- const PowerfulConversion & getPConv (long i) const
- void dcrtToPowerful (NTL::Vec< NTL::ZZ > &powerful, const DoubleCRT &dcrt) const
- void ZZXtoPowerful (NTL::Vec< NTL::ZZ > &powerful, const NTL::ZZX &poly) const
- void powerfulToZZX (NTL::ZZX &poly, const NTL::Vec< NTL::ZZ > &powerful) const

# 7.115.1 Detailed Description

Conversion between powerful representation, DoubleCRT, and ZZX.

## 7.115.2 Constructor & Destructor Documentation

#### 7.115.2.1 PowerfulDCRT()

## 7.115.3 Member Function Documentation

#### 7.115.3.1 dcrtToPowerful()

## 7.115.3.2 getIndexTranslation()

```
const PowerfulTranslationIndexes& helib::PowerfulDCRT::getIndexTranslation ( ) const [inline]
```

#### 7.115.3.3 getPConv()

```
 \begin{tabular}{ll} {\tt const} & {\tt PowerfulConversion\& helib::PowerfulDCRT::getPConv (} \\ & {\tt long} & i \end{tabular} ) & {\tt const} & [{\tt inline}] \\ \end{tabular}
```

#### 7.115.3.4 powerfulToZZX()

#### 7.115.3.5 ZZXtoPowerful()

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/powerful.h
- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/powerful.cpp

# 7.116 helib::PowerfulTranslationIndexes Class Reference

Holds index tables for translation between powerful and zz\_pX.

```
#include <powerful.h>
```

# **Public Member Functions**

PowerfulTranslationIndexes (const NTL::Vec< long > &mv)

## **Public Attributes**

- long m
- long phim
- NTL::Vec< long > mvec
- NTL::Vec < long > phivec
- NTL::Vec< long > divvec
- NTL::Vec< long > invvec
- CubeSignature longSig
- CubeSignature shortSig
- NTL::Vec< long > polyToCubeMap
- NTL::Vec< long > cubeToPolyMap
- $\bullet \ \, \mathsf{NTL} \\ \mathsf{::Vec} \\ < \mathsf{long} \\ > \\ \mathsf{shortToLongMap} \\ \\ \\ \mathsf{ong} \\ \mathsf{ong}$
- NTL::Vec< NTL::ZZX > cycVec
- NTL::ZZX phimX

# 7.116.1 Detailed Description

Holds index tables for translation between powerful and zz\_pX.

# 7.116.2 Constructor & Destructor Documentation

# 7.116.2.1 PowerfulTranslationIndexes()

```
helib::PowerfulTranslationIndexes::PowerfulTranslationIndexes ( const NTL::Vec< long > & mv )
```

### 7.116.3 Member Data Documentation

# 7.116.3.1 cubeToPolyMap

NTL::Vec<long> helib::PowerfulTranslationIndexes::cubeToPolyMap

### 7.116.3.2 cycVec

NTL::Vec<NTL::ZZX> helib::PowerfulTranslationIndexes::cycVec

#### 7.116.3.3 divvec

 $\verb|NTL::Vec<long>| helib::PowerfulTranslationIndexes::divvec|$ 

### 7.116.3.4 invvec

NTL::Vec<long> helib::PowerfulTranslationIndexes::invvec

### 7.116.3.5 longSig

CubeSignature helib::PowerfulTranslationIndexes::longSig

# 7.116.3.6 m

long helib::PowerfulTranslationIndexes::m

### 7.116.3.7 mvec

NTL::Vec<long> helib::PowerfulTranslationIndexes::mvec

# 7.116.3.8 phim

long helib::PowerfulTranslationIndexes::phim

# 7.116.3.9 phimX

NTL::ZZX helib::PowerfulTranslationIndexes::phimX

# 7.116.3.10 phivec

NTL::Vec<long> helib::PowerfulTranslationIndexes::phivec

# 7.116.3.11 polyToCubeMap

 $\verb|NTL::Vec<long>| helib::PowerfulTranslationIndexes::polyToCubeMap| \\$ 

# 7.116.3.12 shortSig

CubeSignature helib::PowerfulTranslationIndexes::shortSig

# 7.116.3.13 shortToLongMap

```
NTL::Vec<long> helib::PowerfulTranslationIndexes::shortToLongMap
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/powerful.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/powerful.cpp

# 7.117 helib::PrimeGenerator Struct Reference

### **Public Member Functions**

- PrimeGenerator (long \_len, long \_m)
- long next ()

### **Public Attributes**

- long len
- long m
- long k
- long t

# 7.117.1 Constructor & Destructor Documentation

# 7.117.1.1 PrimeGenerator()

# 7.117.2 Member Function Documentation

# 7.117.2.1 next()

```
long helib::PrimeGenerator::next ( ) [inline]
```

# 7.117.3 Member Data Documentation

# 7.117.3.1 k

```
long helib::PrimeGenerator::k
```

### 7.117.3.2 len

```
long helib::PrimeGenerator::len
```

# 7.117.3.3 m

```
long helib::PrimeGenerator::m
```

### 7.117.3.4 t

```
long helib::PrimeGenerator::t
```

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/primeChain.cpp

# 7.118 helib::print\_pa\_impl< type > Class Template Reference

# **Static Public Member Functions**

• static void apply (const EncryptedArrayDerived< type > &ea, std::ostream &s, const PlaintextArray &pa)

### 7.118.1 Member Function Documentation

# 7.118.1.1 apply()

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.119 helib::PtrMatrix< T > Struct Template Reference

An abstract class for an array of PtrVectors.

```
#include <PtrMatrix.h>
```

Inheritance diagram for helib::PtrMatrix< T >:

```
helib::PtrMatrix T >
helib::PtrMatrix_PtPtrVector< T > helib::PtrMatrix_ptVec< T > helib::PtrMatrix_ptVector< T > helib::PtrMatrix_vector< T >
```

### **Public Member Functions**

- virtual PtrVector< T > & operator[] (long)=0
- virtual const PtrVector< T > & operator[] (long) const =0
- virtual long size () const =0
- virtual void resize (long newSize)
- virtual ∼PtrMatrix ()
- virtual const T \* ptr2nonNull () const

# 7.119.1 Detailed Description

```
template<typename T> struct helib::PtrMatrix< T>
```

An abstract class for an array of PtrVectors.

# 7.119.2 Constructor & Destructor Documentation

# 7.119.2.1 $\sim$ PtrMatrix()

```
template<typename T >
virtual helib::PtrMatrix< T >::~PtrMatrix ( ) [inline], [virtual]
```

# 7.119.3 Member Function Documentation

### 7.119.3.1 operator[]() [1/2]

Implemented in helib::PtrMatrix\_PtPtrVector< T >, helib::PtrMatrix\_ptvector< T >, helib::PtrMatrix\_vector< T >, helib::PtrMatrix\_ptVec< T >, and helib::PtrMatrix\_vector< T >.

# 7.119.3.2 operator[]() [2/2]

 $Implemented \ in \ helib::PtrMatrix\_PtPtrVector < T>, \ helib::PtrMatrix\_ptvector < T>, \ helib::PtrMatrix\_ptVector < T>, \ helib::PtrMatrix\_ptVector < T>, \ helib::PtrMatrix\_ptVector < T>.$ 

### 7.119.3.3 ptr2nonNull()

```
template<typename T >
virtual const T* helib::PtrMatrix< T >::ptr2nonNull ( ) const [inline], [virtual]
```

# 7.119.3.4 resize()

# 7.119.3.5 size()

```
template<typename T >
virtual long helib::PtrMatrix< T >::size ( ) const [pure virtual]
```

 $Implemented \ in \ helib::PtrMatrix\_PtPtrVector < T>, \ helib::PtrMatrix\_ptvector < T>, \ helib::PtrMatrix\_vector < T>, \ helib::PtrMatrix\_ptVec < T>, \ helib::PtrMatrix\_vector < T>.$ 

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrMatrix.h

# 7.120 helib::PtrMatrix\_PtPtrVector< T > Struct Template Reference

An implementation of PtrMatrix using vector< PtrVector<T>\*>

Inheritance diagram for helib::PtrMatrix\_PtPtrVector< T >:

```
helib::PtrMatrix< T >
helib::PtrMatrix_PtPtrVector< T >
```

### **Public Member Functions**

- PtrMatrix\_PtPtrVector (std::vector< PtrVector< T > \* > &mat)
- PtrVector< T > & operator[] (long i) override
- const PtrVector< T > & operator[] (long i) const override
- long size () const override

# **Public Attributes**

std::vector< PtrVector< T > \* > & rows

# 7.120.1 Detailed Description

```
template < typename T > struct helib::PtrMatrix_PtPtrVector < T >
```

An implementation of PtrMatrix using vector< PtrVector<T>\*>

# 7.120.2 Constructor & Destructor Documentation

### 7.120.2.1 PtrMatrix\_PtPtrVector()

# 7.120.3 Member Function Documentation

### 7.120.3.1 operator[]() [1/2]

### 7.120.3.2 operator[]() [2/2]

### 7.120.3.3 size()

```
template<typename T >
long helib::PtrMatrix_PtPtrVector< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrMatrix < T >.
```

### 7.120.4 Member Data Documentation

#### 7.120.4.1 rows

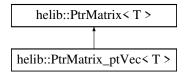
```
template<typename T >
std::vector<PtrVector<T>*>& helib::PtrMatrix_PtPtrVector< T >::rows
```

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/binaryArith.cpp

# 7.121 helib::PtrMatrix\_ptVec< T > Struct Template Reference

```
An implementation of PtrMatrix using Vec< Vec<T>* > #include <math><PtrMatrix.h> Inheritance diagram for helib::PtrMatrix ptVec< T>:
```



# **Public Member Functions**

- PtrMatrix ptVec (NTL::Vec< NTL::Vec< T > \* > &mat)
- PtrVector< T > & operator[] (long i) override
- const PtrVector< T > & operator[] (long i) const override
- long size () const override

### **Public Attributes**

- NTL::Vec< NTL::Vec< T > \* > & buffer
- std::vector < PtrVector VecT < T > > rows

# 7.121.1 Detailed Description

```
\label{template} \begin{split} & \text{template}\!<\!\text{typename T}\!> \\ & \text{struct helib::PtrMatrix\_ptVec}\!<\!\text{T}> \end{split}
```

An implementation of PtrMatrix using Vec< Vec<T>\*>

# 7.121.2 Constructor & Destructor Documentation

# 7.121.2.1 PtrMatrix\_ptVec()

# 7.121.3 Member Function Documentation

# 7.121.3.1 operator[]() [1/2]

Implements helib::PtrMatrix< T >.

### 7.121.3.2 operator[]() [2/2]

 $Implements \ helib:: PtrMatrix < T>.$ 

### 7.121.3.3 size()

```
template<typename T >
long helib::PtrMatrix_ptVec< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrMatrix< T >.
```

# 7.121.4 Member Data Documentation

# 7.121.4.1 buffer

```
template<typename T >
NTL::Vec<NTL::Vec<T>*>& helib::PtrMatrix_ptVec< T >::buffer
```

# 7.121.4.2 rows

```
template<typename T >
std::vector<PtrVector_VecT<T> > helib::PtrMatrix_ptVec< T >::rows
```

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrMatrix.h

# 7.122 helib::PtrMatrix\_ptvector< T > Struct Template Reference

```
An implementation of <a href="PtrMatrix">PtrMatrix</a> using vector< <a href="Vector<T>*></a>
```

```
#include <PtrMatrix.h>
```

Inheritance diagram for helib::PtrMatrix\_ptvector< T >:

```
helib::PtrMatrix < T >
helib::PtrMatrix_ptvector < T >
```

# **Public Member Functions**

- PtrMatrix\_ptvector (std::vector< std::vector< T > \* > &mat)
- PtrVector< T > & operator[] (long i) override
- const PtrVector< T > & operator[] (long i) const override
- long size () const override

### **Public Attributes**

- std::vector< std::vector< T > \* > & buffer
- std::vector
   PtrVector
   vectorT
   rows

# 7.122.1 Detailed Description

```
template<typename T> struct helib::PtrMatrix_ptvector< T>
```

An implementation of PtrMatrix using vector< vector<T>\*>

# 7.122.2 Constructor & Destructor Documentation

# 7.122.2.1 PtrMatrix\_ptvector()

# 7.122.3 Member Function Documentation

# 7.122.3.1 operator[]() [1/2]

Implements helib::PtrMatrix< T >.

### 7.122.3.2 operator[]() [2/2]

Implements helib::PtrMatrix< T >.

# 7.122.3.3 size()

```
template<typename T >
long helib::PtrMatrix_ptvector< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrMatrix< T >.
```

# 7.122.4 Member Data Documentation

# 7.122.4.1 buffer

```
\label{template} $$ \ensuremath{\texttt{template}}$ $$ \ensuremath{\texttt{template}
```

# 7.122.4.2 rows

```
template<typename T >
std::vector<PtrVector_vectorT<T> > helib::PtrMatrix_ptvector< T >::rows
```

The documentation for this struct was generated from the following file:

 $\bullet \ / Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrMatrix.h \\$ 

# 7.123 helib::PtrMatrix\_Vec< T > Struct Template Reference

```
An implementation of PtrMatrix using Vec< Vec<T>>
```

```
#include <PtrMatrix.h>
```

Inheritance diagram for helib::PtrMatrix\_Vec< T >:

```
helib::PtrMatrix < T >
helib::PtrMatrix_Vec < T >
```

# **Public Member Functions**

- PtrMatrix\_Vec (NTL::Vec< NTL::Vec< T >> &mat)
- PtrVector< T > & operator[] (long i) override
- const PtrVector< T > & operator[] (long i) const override
- long size () const override
- void resize (long newSize) override

### **Public Attributes**

- NTL::Vec< NTL::Vec< T > > & buffer
- std::vector< PtrVector $\_$ VecT< T >> rows

# 7.123.1 Detailed Description

```
\label{template} \begin{split} & \text{template}\!<\!\text{typename T}\!> \\ & \text{struct helib::PtrMatrix\_Vec}\!<\!\text{T}> \end{split}
```

An implementation of PtrMatrix using Vec< Vec<T>>

# 7.123.2 Constructor & Destructor Documentation

# 7.123.2.1 PtrMatrix\_Vec()

# 7.123.3 Member Function Documentation

### 7.123.3.1 operator[]() [1/2]

Implements helib::PtrMatrix< T >.

# 7.123.3.2 operator[]() [2/2]

### 7.123.3.3 resize()

Reimplemented from helib::PtrMatrix< T >.

# 7.123.3.4 size()

```
template<typename T >
long helib::PtrMatrix_Vec< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrMatrix< T >.
```

# 7.123.4 Member Data Documentation

### 7.123.4.1 buffer

```
template<typename T >
NTL::Vec<NTL::Vec<T> >& helib::PtrMatrix_Vec< T >::buffer
```

#### 7.123.4.2 rows

```
template<typename T >
std::vector<PtrVector_VecT<T> > helib::PtrMatrix_Vec< T >::rows
```

The documentation for this struct was generated from the following file:

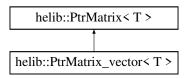
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrMatrix.h

# 7.124 helib::PtrMatrix\_vector< T > Struct Template Reference

An implementation of PtrMatrix using vector< vector<T>>

```
#include <PtrMatrix.h>
```

Inheritance diagram for helib::PtrMatrix\_vector< T >:



# **Public Member Functions**

- PtrMatrix\_vector (std::vector< std::vector< T >> &mat)
- PtrVector< T > & operator[] (long i) override
- const PtrVector< T > & operator[] (long i) const override
- long size () const override
- void resize (long newSize) override

### **Public Attributes**

- std::vector< std::vector< T >> & buffer
- std::vector< PtrVector\_vectorT< T >> rows

# 7.124.1 Detailed Description

```
template<typename T> struct helib::PtrMatrix_vector< T>
```

An implementation of PtrMatrix using vector< vector<T>>

# 7.124.2 Constructor & Destructor Documentation

### 7.124.2.1 PtrMatrix\_vector()

# 7.124.3 Member Function Documentation

# 7.124.3.1 operator[]() [1/2]

# 7.124.3.2 operator[]() [2/2]

Implements helib::PtrMatrix< T >.

# 7.124.3.3 resize()

Reimplemented from helib::PtrMatrix< T >.

### 7.124.3.4 size()

```
template<typename T >
long helib::PtrMatrix_vector< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrMatrix< T >.
```

### 7.124.4 Member Data Documentation

### 7.124.4.1 buffer

```
template<typename T >
std::vector<std::vector<T> >& helib::PtrMatrix_vector< T >::buffer
```

#### 7.124.4.2 rows

```
template<typename T >
std::vector<PtrVector_vectorT<T> > helib::PtrMatrix_vector< T >::rows
```

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrMatrix.h

# 7.125 helib::PtrVector< T > Struct Template Reference

Abstract class for an array of objects.

```
#include <PtrVector.h>
```

Inheritance diagram for helib::PtrVector< T >:



# **Public Member Functions**

- virtual T \* operator[] (long) const =0
- virtual long size () const =0
- virtual void resize (long newSize, UNUSED const PtrVector \*another=nullptr)
- virtual ∼PtrVector ()
- bool isSet (long i) const
- virtual long numNonNull (long first=0, long last=LONG\_MAX) const
- virtual const T \* ptr2nonNull () const

# 7.125.1 Detailed Description

```
template<typename T> struct helib::PtrVector< T>
```

Abstract class for an array of objects.

# 7.125.2 Constructor & Destructor Documentation

# 7.125.2.1 ∼PtrVector()

```
\label{template} $$ template < typename T > $$ virtual helib::PtrVector < T >:: \sim PtrVector ( ) [inline], [virtual] $$
```

# 7.125.3 Member Function Documentation

#### 7.125.3.1 isSet()

# 7.125.3.2 numNonNull()

Reimplemented in helib::PtrVector\_slice< T >, helib::PtrVector\_vectorT< T >, and helib::PtrVector\_vector\_VecT< T >.

# 7.125.3.3 operator[]()

Implemented in helib::PtrVector\_Singleton < T >, helib::PtrVector\_slice < T >, helib::PtrVector\_vectorT < T >, helib::PtrVector\_vector\_VecT < T >, helib::PtrVector\_vec

# 7.125.3.4 ptr2nonNull()

```
template<typename T >
virtual const T* helib::PtrVector< T >::ptr2nonNull ( ) const [inline], [virtual]
```

Reimplemented in helib::PtrVector\_slice< T >, and helib::PtrVector\_vecT< T >.

### 7.125.3.5 resize()

Reimplemented in helib::PtrVector\_vectorPt< T >, and helib::PtrVector\_VecPt< T >.

#### 7.125.3.6 size()

```
\label{template} $$ template < typename T > $$ virtual long helib::PtrVector < T >::size ( ) const [pure virtual]
```

 $Implemented \ \ in \ \ helib::PtrVector\_Singleton < T>, \ \ helib::PtrVector\_slice < T>, \ \ helib::PtrVector\_vector T < T>, \ helib::PtrVector\_vector T < T>, \ \ helib::PtrVector\_vector T < T>, \ \ and \ \ helib::PtrVector\_Vec T < T>.$ 

The documentation for this struct was generated from the following file:

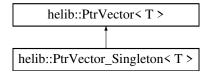
/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrVector.h

# 7.126 helib::PtrVector\_Singleton < T > Struct Template Reference

An implementation of PtrVector from a single T object.

```
#include <PtrVector.h>
```

Inheritance diagram for helib::PtrVector Singleton< T >:



### **Public Member Functions**

- PtrVector\_Singleton (const T \*\_v)
- T \* operator[] (long i) const override
- long size () const override

# **Public Attributes**

const T \* v

# 7.126.1 Detailed Description

```
template<typename T> struct helib::PtrVector_Singleton< T>
```

An implementation of PtrVector from a single T object.

# 7.126.2 Constructor & Destructor Documentation

# 7.126.2.1 PtrVector\_Singleton()

# 7.126.3 Member Function Documentation

### 7.126.3.1 operator[]()

Implements helib::PtrVector< T >.

# 7.126.3.2 size()

```
template<typename T >
long helib::PtrVector_Singleton< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrVector< T >.
```

# 7.126.4 Member Data Documentation

### 7.126.4.1 v

```
template<typename T >
const T* helib::PtrVector_Singleton< T >::v
```

The documentation for this struct was generated from the following file:

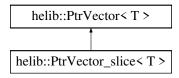
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrVector.h

# 7.127 helib::PtrVector\_slice < T > Struct Template Reference

An implementation of PtrVector as a slice of another PtrVector.

```
#include <PtrVector.h>
```

Inheritance diagram for helib::PtrVector\_slice < T >:



# **Public Member Functions**

- PtrVector\_slice (const PtrVector\_slice < T > &slice, long from, long \_sz=-1)
- PtrVector\_slice (const PtrVector< T > &\_orig, long from, long \_sz=-1)
- T \* operator[] (long i) const override
- long size () const override
- · long numNonNull (long first=0, long last=LONG MAX) const override
- const T \* ptr2nonNull () const override

### **Public Attributes**

- const PtrVector< T > & orig
- long start
- long sz

# 7.127.1 Detailed Description

```
template<typename T> struct helib::PtrVector_slice< T>
```

An implementation of PtrVector as a slice of another PtrVector.

# 7.127.2 Constructor & Destructor Documentation

### 7.127.2.1 PtrVector\_slice() [1/2]

# 7.127.2.2 PtrVector\_slice() [2/2]

# 7.127.3 Member Function Documentation

### 7.127.3.1 numNonNull()

Reimplemented from helib::PtrVector< T >.

# 7.127.3.2 operator[]()

Implements helib::PtrVector< T >.

# 7.127.3.3 ptr2nonNull()

```
template<typename T >
const T* helib::PtrVector_slice< T >::ptr2nonNull ( ) const [inline], [override], [virtual]
```

Reimplemented from helib::PtrVector< T >.

### 7.127.3.4 size()

```
\label{template} $$ template < typename T > $$ long helib::PtrVector\_slice < T >::size ( ) const [inline], [override], [virtual] $$ $$ $$
```

Implements helib::PtrVector< T >.

# 7.127.4 Member Data Documentation

# 7.127.4.1 orig

```
template<typename T >
const PtrVector<T>& helib::PtrVector_slice< T >::orig
```

#### 7.127.4.2 start

```
template<typename T >
long helib::PtrVector_slice< T >::start
```

### 7.127.4.3 sz

```
template<typename T >
long helib::PtrVector_slice< T >::sz
```

The documentation for this struct was generated from the following file:

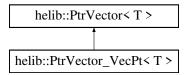
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrVector.h

# 7.128 helib::PtrVector\_VecPt< T > Struct Template Reference

An implementation of PtrVector using Vec<T\*>

```
#include <PtrVector.h>
```

Inheritance diagram for helib:: $PtrVector\_VecPt < T >$ :



# **Public Member Functions**

- PtrVector\_VecPt (NTL::Vec< T \* > &\_v)
- T \* operator[] (long i) const override
- long size () const override
- void resize (long newSize, UNUSED const PtrVector< T > \*another=nullptr) override

# **Public Attributes**

```
• NTL::Vec< T * > & v
```

# 7.128.1 Detailed Description

```
template < typename T > struct helib::PtrVector_VecPt < T >
```

An implementation of PtrVector using Vec<T\*>

# 7.128.2 Constructor & Destructor Documentation

# 7.128.2.1 PtrVector\_VecPt()

```
\label{template} $$ \text{template}$$ $$ \text{typename T} > $$ \text{helib}::PtrVector\_VecPt ( } $$ NTL::Vec< T * > & _v ) [inline]
```

# 7.128.3 Member Function Documentation

# 7.128.3.1 operator[]()

Implements helib::PtrVector< T >.

# 7.128.3.2 resize()

Reimplemented from helib::PtrVector< T >.

### 7.128.3.3 size()

```
template<typename T >
long helib::PtrVector_VecPt< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrVector< T >.
```

### 7.128.4 Member Data Documentation

### 7.128.4.1 v

```
template<typename T >
NTL::Vec<T*>& helib::PtrVector_VecPt< T >::v
```

The documentation for this struct was generated from the following file:

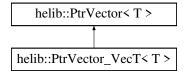
/Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/PtrVector.h

# 7.129 helib::PtrVector\_VecT< T > Struct Template Reference

An implementation of PtrVector using Vec<T>

```
#include <PtrVector.h>
```

Inheritance diagram for helib::PtrVector\_VecT< T >:



# **Public Member Functions**

- PtrVector\_VecT (NTL::Vec< T > &\_v)
- T \* operator[] (long i) const override
- long size () const override
- void resize (long newSize, const PtrVector < T > \*another) override
- · long numNonNull (long first=0, long last=LONG\_MAX) const override
- const T \* ptr2nonNull () const override

# **Public Attributes**

NTL::Vec< T > & v

# 7.129.1 Detailed Description

```
template < typename T > struct helib::PtrVector_VecT < T >
```

An implementation of PtrVector using Vec<T>

# 7.129.2 Constructor & Destructor Documentation

# 7.129.2.1 PtrVector\_VecT()

### 7.129.3 Member Function Documentation

### 7.129.3.1 numNonNull()

Reimplemented from helib::PtrVector< T >.

# 7.129.3.2 operator[]()

Implements helib::PtrVector< T >.

### 7.129.3.3 ptr2nonNull()

```
template<typename T >
const T* helib::PtrVector_VecT< T >::ptr2nonNull ( ) const [inline], [override], [virtual]
```

Reimplemented from helib::PtrVector< T >.

#### 7.129.3.4 resize()

# 7.129.3.5 size()

```
template<typename T >
long helib::PtrVector_VecT< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrVector< T >.
```

# 7.129.4 Member Data Documentation

# 7.129.4.1 v

```
template<typename T >
NTL::Vec<T>& helib::PtrVector_VecT< T >::v
```

The documentation for this struct was generated from the following file:

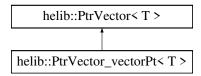
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrVector.h

# 7.130 helib::PtrVector\_vectorPt< T > Struct Template Reference

An implementation of PtrVector using vector<T\*>

```
#include <PtrVector.h>
```

Inheritance diagram for helib::PtrVector\_vectorPt< T >:



# **Public Member Functions**

- PtrVector\_vectorPt (std::vector< T \* > &\_v)
- T \* operator[] (long i) const override
- long size () const override
- void resize (long newSize, UNUSED const PtrVector< T > \*another=nullptr) override

# **Public Attributes**

```
• std::vector< T * > & v
```

# 7.130.1 Detailed Description

```
\label{template} \mbox{typename T} > \\ \mbox{struct helib::PtrVector\_vectorPt} < \mbox{T} > \\
```

An implementation of PtrVector using vector<T\*>

# 7.130.2 Constructor & Destructor Documentation

# 7.130.2.1 PtrVector\_vectorPt()

# 7.130.3 Member Function Documentation

# 7.130.3.1 operator[]()

Implements helib::PtrVector< T >.

# 7.130.3.2 resize()

Reimplemented from helib::PtrVector< T >.

### 7.130.3.3 size()

```
template<typename T >
long helib::PtrVector_vectorPt< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrVector< T >.
```

### 7.130.4 Member Data Documentation

#### 7.130.4.1 v

```
template<typename T >
std::vector<T*>& helib::PtrVector_vectorPt< T >::v
```

The documentation for this struct was generated from the following file:

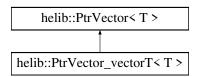
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrVector.h

# 7.131 helib::PtrVector\_vectorT< T > Struct Template Reference

An implementation of PtrVector using vector<T>

```
#include <PtrVector.h>
```

Inheritance diagram for helib::PtrVector\_vectorT< T >:



### **Public Member Functions**

- PtrVector\_vectorT (std::vector< T > &\_v)
- T \* operator[] (long i) const override
- long size () const override
- void resize (long newSize, const PtrVector< T > \*another) override
- long numNonNull (long first=0, long last=LONG\_MAX) const override

# **Public Attributes**

std::vector< T > & v

# 7.131.1 Detailed Description

```
template < typename T > struct helib::PtrVector_vectorT < T >
```

An implementation of PtrVector using vector<T>

# 7.131.2 Constructor & Destructor Documentation

# 7.131.2.1 PtrVector\_vectorT()

# 7.131.3 Member Function Documentation

### 7.131.3.1 numNonNull()

Reimplemented from helib::PtrVector< T >.

# 7.131.3.2 operator[]()

Implements helib::PtrVector< T >.

# 7.131.3.3 resize()

# 7.131.3.4 size()

```
template<typename T >
long helib::PtrVector_vectorT< T >::size ( ) const [inline], [override], [virtual]
Implements helib::PtrVector< T >.
```

# 7.131.4 Member Data Documentation

#### 7.131.4.1 v

```
template<typename T >
std::vector<T>& helib::PtrVector_vectorT< T >::v
```

The documentation for this struct was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PtrVector.h

# 7.132 helib::Ptxt Class Reference

An object that mimics the functionality of the Ctxt object, and acts as a convenient entry point for inputting/encoding data which is to be encrypted.

```
#include <Ctxt.h>
```

# **Public Types**

using SlotType = typename Scheme::SlotType
 Alias for type to be stored in the slots.

### **Public Member Functions**

• Ptxt ()

Default constructor results in invalid Ptxt object which throws if used.

Ptxt (const Context &context)

Context only constructor, defaults all slots to 0.

Ptxt (const Context &context, const SlotType &value)

Single slot constructor, set all slots to value.

template<typename U = Scheme, std::enable\_if\_t< std::is\_same< U, BGV >::value > \* = nullptr>
 Ptxt (const Context &context, const NTL::ZZX &value)

BGV plaintext polynomial constructor, set all slots to the value polynomial.

Ptxt (const Context &context, const std::vector < SlotType > &data)

Slot vector constructor.

• template<typename T > Ptxt (const Context &context, const std::vector< T > &data) Generic slot vector constructor. Ptxt (const Ptxt < Scheme > &other)=default Default copy constructor. Ptxt (Ptxt < Scheme > &&other) noexcept=default Default move constructor. Ptxt< Scheme > & operator= (const Ptxt< Scheme > &v)=default Copy assignment operator with other Ptxt. Ptxt< Scheme > & operator= (Ptxt< Scheme > &&v) noexcept=default Move assignment operator with other Ptxt. ∼Ptxt ()=default Default destructor. • bool isValid () const Check if a Ptxt is valid. • size t size () const Returns the size (number of slots) of a Ptxt. · long Isize () const Returns the size (number of slots) of a Ptxt as long. void setData (const std::vector< SlotType > &data) Set the data. void setData (const SlotType &value) Set the data replicating the input on all slots. • template<typename T = Scheme, typename std::enable\_if\_t< std::is\_same< T, BGV >::value > \* = nullptr> void setData (const NTL::ZZX &value) Set the Ptxt data replicating the input polynomial on all slots. • template<typename T = Scheme, typename std::enable\_if\_t< std::is\_same< T, BGV >::value > \* = nullptr> void decodeSetData (const NTL::ZZX &data) Set the Ptxt slots using values from decoding data to slot representation. • void clear () Sets all slots to 0. Ptxt< Scheme > & random () Populate slots with random data. const std::vector < SlotType > & getSlotRepr () const Get the data held in the slots as a std::vector<SlotType>. NTL::ZZX getPolyRepr () const Converts the slot data in this to its single polynomial representation. SlotType & operator[] (long i) Square bracket accessor operator. SlotType operator[] (long i) const const square bracket accessor operator. SlotType & at (long i) at accessor operator. SlotType at (long i) const const at accessor operator. bool operator== (const Ptxt< Scheme > &other) const Equals operator between two Ptxt objects. bool operator!= (const Ptxt< Scheme > &other) const Not equals operator between two Ptxt objects. Ptxt< Scheme > operator\* (const Ptxt< Scheme > &rhs) const

Infix multiplication operator.

```
    Ptxt< Scheme > operator+ (const Ptxt< Scheme > &rhs) const

     Infix addition operator.
• Ptxt< Scheme > operator- (const Ptxt< Scheme > &rhs) const
     Infix subtraction operator.

    Ptxt< Scheme > & operator*= (const Ptxt< Scheme > &otherPtxt)

      Times equals operator with another Ptxt.

    Ptxt< Scheme > & operator*= (const SlotType &scalar)

      Times equals operator with a single SlotType.
• template<typename Scalar >
  Ptxt< Scheme > & operator*= (const Scalar &scalar)
      Times equals operator with a scalar.

    Ptxt< Scheme > & operator+= (const Ptxt< Scheme > &otherPtxt)

     Plus equals operator with another Ptxt.

    Ptxt< Scheme > & operator+= (const SlotType &scalar)

     Plus equals operator with a single SlotType.

    template<typename Scalar >

  Ptxt< Scheme > & operator+= (const Scalar &scalar)
     Plus equals operator with a scalar.

    Ptxt< Scheme > & operator= (const Ptxt< Scheme > &otherPtxt)

     Minus equals operator with another Ptxt.

    Ptxt< Scheme > & operator= (const SlotType &scalar)

     Minus equals operator with a single SlotType.

    template<typename Scalar >

  Ptxt < Scheme > & operator-= (const Scalar &scalar)
     Minus equals operator with a scalar.

    Ptxt< Scheme > & negate ()

     Negate a Ptxt.
• template<typename T = Scheme, typename Scalar, typename std::enable_if_t< std::is_same< T, BGV >::value > * = nullptr>
  Ptxt < Scheme > & addConstant (const Scalar &scalar)
     Add a constant to a BGV Ptxt.
• template<typename T = Scheme, typename Scalar, typename std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
  Ptxt< Scheme > & addConstantCKKS (const Scalar &scalar)
     Add a constant to a CKKS Ptxt.

    Ptxt< Scheme > & multiplyBy (const Ptxt< Scheme > &otherPtxt)

     Multiplication function between two Ptxt objects.

    Ptxt < Scheme > & multiplyBy2 (const Ptxt &otherPtxt1, const Ptxt &otherPtxt2)

     Multiplication function between three Ptxt objects.

    Ptxt< Scheme > & square ()

     Square operation on a Ptxt.

    Ptxt< Scheme > & cube ()

     Cube operation on a Ptxt.

    Ptxt< Scheme > & power (long e)

     Power operation to raise a Ptxt to an arbitrary non-negative power.

    Ptxt< Scheme > & rotate (long amount)

     Rotate slots right by specified amount (slot i goes to slot i+1 mod size).

    Ptxt< Scheme > & rotate1D (long dim, long amount)

     Rotate slots right by specified amount along a specific dimension.

    Ptxt< Scheme > & shift (long amount)

     Shifts slots right by specified amount with 0 fill (slot i goes to slot i+1 mod size).

    Ptxt< Scheme > & shift1D (long dim, long amount)

     Shift slots right in one dimension of the hypercube structure with 0 fill.
```

```
    Ptxt< Scheme > & automorph (long k)

      Apply the automorphism a(X) \rightarrow a(X^{\wedge}k) \mod Phi_m(X).
• template<typename T = Scheme, std::enable_if_t< std::is_same< T, BGV >::value > * = nullptr>
  Ptxt < Scheme > & frobeniusAutomorph (long j)
      Apply the frobenius automorphism a(X) -> a(X^{\wedge}(p^{\wedge}j)) \mod Phi_m(X).

    Ptxt< Scheme > & replicate (long pos)

      Replicate single slot across all slots.

    std::vector< Ptxt< Scheme > > replicateAll () const

      Generate a vector of plaintexts with each slot replicated in each plaintext.
• template<typename T = Scheme, std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
  Ptxt < Scheme > & complexConj ()
      Apply complex conjugate of complex numbers in slots of a CKKS Ptxt object.
template<typename T = Scheme, std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
  Ptxt< Scheme > real () const
      Extract the real part of a CKKS plaintext.
• template<typename T = Scheme, std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
  Ptxt< Scheme > imag () const
      Extract the imaginary part of a CKKS plaintext.

    Ptxt< Scheme > & runningSums ()

      Compute the running sum (each slot is the sum of the previous slots).

    Ptxt< Scheme > & totalSums ()

      Compute the total sum (each slot contains the total sum of every slot).

    Ptxt< Scheme > & incrementalProduct ()

      Compute the incremental product (each slot is the product of the previous slots).

    Ptxt< Scheme > & totalProduct ()

      Compute the total product (each slot contains the total product of every slot).

    Ptxt< Scheme > & mapTo01 ()

      Map all non-zero slots to 1, keeping zero slots as zero.

    PolyMod convertToSlot (const Context &context, long slot)

    std::complex < double > convertToSlot (const Context &, long slot)

• template<typename Scheme >
  Ptxt ()
template<typename Scheme >
  Ptxt (const Context &context)
• template<typename Scheme >
  Ptxt (const Context &context, const SlotType &value)

    void setData (const NTL::ZZX &value)

    Ptxt (const Context &context, const NTL::ZZX &value)

template<typename Scheme >
  Ptxt (const Context &context, const std::vector < SlotType > &data)
• template<typename Scheme >
  void setData (const std::vector< SlotType > &data)

    template<typename Scheme >

  void setData (const SlotType &value)

    void decodeSetData (const NTL::ZZX &data)

    NTL::ZZX getPolyRepr () const

      BGV specialisation of the getPolyRepr function.

    NTL::ZZX getPolyRepr () const

      CKKS specialisation of the getPolyRepr function.
template<typename Scheme >
  Ptxt< Scheme > & operator*= (const Ptxt< Scheme > &otherPtxt)
template<typename Scheme >
  Ptxt< Scheme > & operator*= (const SlotType &scalar)
```

```
template<typename Scheme >
Ptxt< Scheme > & operator+= (const Ptxt< Scheme > & otherPtxt)
template<typename Scheme >
Ptxt< Scheme > & operator+= (const SlotType &scalar)
template<typename Scheme >
Ptxt< Scheme > & operator-= (const Ptxt< Scheme > & otherPtxt)
template<typename Scheme >
Ptxt< Scheme > & operator-= (const SlotType &scalar)
Ptxt< Scheme > & operator-= (const SlotType &scalar)
Ptxt< BGV > & automorph (long k)
Ptxt< CKKS > & automorph (long k)
Ptxt< BGV > & frobeniusAutomorph (long j)
Ptxt< CKKS > & complexConj ()
Ptxt< CKKS > real () const
Ptxt< CKKS > imag () const
```

#### Static Public Member Functions

static SlotType convertToSlot (const Context &context, long slot)
 Conversion function from long to SlotType.

#### **Friends**

```
    std::istream & operator>> (std::istream &is, Ptxt< Scheme > &ptxt)
        Input shift operator.

    std::ostream & operator<< (std::ostream &os, const Ptxt< Scheme > &ptxt)
        Output shift operator.
```

### 7.132.1 Detailed Description

An object that mimics the functionality of the Ctxt object, and acts as a convenient entry point for inputting/encoding data which is to be encrypted.

 ${\tt Ptxt} \ \ \text{is templated on Scheme, which may be CKKS or BGV}.$ 

In the BGV case, Ptxt can be considered to be an element of  $\mathbb{Z}_p[x]/\Phi(m)$  viewed as a vector of slots with values each in  $\mathbb{Z}_p[x]/G$  where G is one of the irreducible factors of  $\Phi(m)$ , and all operations are performed entry-wise.

# General usage:

```
helib::Ptxt<BGV> p1(bgv_context, data);
helib::Ptxt<BGV> p2(bgv_context, data);
p1 += p2;
std::cout « p1 « std::endl;
```

Internally, Ptxt objects store their data as a std::vector<helib::PolyMod>, where PolyMod is a convenience type representing an element of the above ring,  $\mathbb{Z}_p[x]/G$ . The PolyMod type can be easily converted via static\_cast to more convenient types such as long and NTL::ZZX.

In the CKKS case, the slot type is std::complex<double>, and has sensible operator overloads supporting operations with other Ptxt<CKKS>, Ctxt, and std::complex<double> objects, as well as performing all operations slot-wise.

A large number of operator overloads are defined so that Ptxt objects should easily inter-operate, as well as providing interoperability with other logically compatible types e.g. long and NTL:: ZZX in the BGV case,  $std \leftarrow ::complex < double > in the CKKS case, and helib::Ctxt in both cases.$ 

# 7.132.2 Member Typedef Documentation

# 7.132.2.1 SlotType

```
using helib::Ptxt::SlotType = typename Scheme::SlotType
```

Alias for type to be stored in the slots.

```
std::complex<double> for CKKS, helib::PolyMod for BGV.
```

# 7.132.3 Constructor & Destructor Documentation

# 7.132.3.1 Ptxt() [1/13]

```
helib::Ptxt::Ptxt ( )
```

Default constructor results in invalid Ptxt object which throws if used.

# 7.132.3.2 Ptxt() [2/13]

Context only constructor, defaults all slots to 0.

### **Parameters**

| context | Context |
|---------|---------|
|         | to use. |

# 7.132.3.3 Ptxt() [3/13]

Single slot constructor, set all slots to value.

#### **Parameters**

| context | Context |
|---------|---------|
|         | to use. |
| value   | Value   |
|         | to set  |
|         | all     |
|         | slots   |
|         | to.     |

## 7.132.3.4 Ptxt() [4/13]

BGV plaintext polynomial constructor, set all slots to the value polynomial.

#### **Parameters**

| context | Context    |
|---------|------------|
|         | to use.    |
| data    | Polynomial |
|         | to be      |
|         | con-       |
|         | verted     |
|         | into       |
|         | slot       |
|         | repre-     |
|         | senta-     |
|         | tion.      |

### Note

Only exists for BGV.

## 7.132.3.5 Ptxt() [5/13]

Slot vector constructor.

#### **Parameters**

| context | Context |
|---------|---------|
|         | to use. |

## **Parameters**

| data | Data    |
|------|---------|
|      | to pop- |
|      | ulate   |
|      | the     |
|      | slots.  |

# 7.132.3.6 Ptxt() [6/13]

Generic slot vector constructor.

### **Parameters**

| context | Context |
|---------|---------|
|         | to use. |
| data    | Data    |
|         | to pop- |
|         | ulate   |
|         | the     |
|         | slots,  |
|         | must    |
|         | be      |
|         | con-    |
|         | vert-   |
|         | ible to |
|         | Slot↩   |
|         | Type.   |

## 7.132.3.7 Ptxt() [7/13]

```
\label{eq:ptxt:ptxt} \begin{tabular}{ll} helib::Ptxt::Ptxt ( & const Ptxt < Scheme > & other ) & [default] \end{tabular}
```

Default copy constructor.

## **Parameters**

| other | Ptxt   |
|-------|--------|
|       | object |
|       | to     |
|       | сору.  |

### 7.132.3.8 Ptxt() [8/13]

Default move constructor.

#### **Parameters**

| other | Ptxt  |
|-------|-------|
|       | to    |
|       | сору. |

## 7.132.3.9 ∼Ptxt()

```
\verb|helib::Ptxt::\sim Ptxt ( ) [default]
```

Default destructor.

## 7.132.3.10 Ptxt() [9/13]

```
template<typename Scheme >
helib::Ptxt::Ptxt ( )
```

# 7.132.3.11 Ptxt() [10/13]

### 7.132.3.12 Ptxt() [11/13]

### 7.132.3.13 Ptxt() [12/13]

## 7.132.3.14 Ptxt() [13/13]

## 7.132.4 Member Function Documentation

## 7.132.4.1 addConstant()

Add a constant to a BGV Ptxt.

#### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | added   |
|        | across  |
|        | all     |
|        | slots.  |

### Returns

Reference to \*this post scalar addition.

## 7.132.4.2 addConstantCKKS()

Add a constant to a CKKS Ptxt.

### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | added   |
|        | across  |
|        | all     |
|        | slots.  |

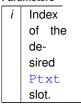
### Returns

Reference to \*this post scalar addition.

### 7.132.4.3 at() [1/2]

at accessor operator.

## **Parameters**



#### Returns

Reference to the data held at slot i.

## Note

throws if i is out of range.

## 7.132.4.4 at() [2/2]

const at accessor operator.

### **Parameters**

| i | Index  |  |
|---|--------|--|
|   | of the |  |
|   | de-    |  |
|   | sired  |  |
|   | Ptxt   |  |
|   | slot.  |  |

### Returns

Copy of the data held at slot i.

#### Note

throws if i is out of range.

# 7.132.4.5 automorph() [1/3]

```
\label{eq:ptxt} $$ Ptxt<Scheme>& helib::Ptxt::automorph ($$ long $k$ )
```

Apply the automorphism  $a(X) -> a(X^{\wedge}k) \mod Phi_m(X)$ .

## **Parameters**

| k | Exponent |  |
|---|----------|--|
|   | of the   |  |
|   | auto-    |  |
|   | mor-     |  |
|   | phism    |  |
|   | to       |  |
|   | apply.   |  |

### Returns

Reference to \*this post automorphism application.

#### Note

k must be an element of Zm\*

# 7.132.4.6 automorph() [2/3]

```
Ptxt< BGV > & helib::Ptxt< BGV >::automorph ( long k )
```

## 7.132.4.7 automorph() [3/3]

#### 7.132.4.8 clear()

```
void helib::Ptxt::clear ( )
```

Sets all slots to 0.

### 7.132.4.9 complexConj() [1/2]

```
template<typename T = Scheme, std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
Ptxt<Scheme>& helib::Ptxt::complexConj ( )
```

Apply complex conjugate of complex numbers in slots of a CKKS Ptxt object.

Returns

Reference to \*this post complex conjugation.

Note

Only valid for the CKKS scheme.

## 7.132.4.10 complexConj() [2/2]

```
Ptxt< CKKS > & helib::Ptxt< CKKS >::complexConj ( )
```

### 7.132.4.11 convertToSlot() [1/3]

### 7.132.4.12 convertToSlot() [2/3]

## 7.132.4.13 convertToSlot() [3/3]

Conversion function from long to SlotType.

#### **Parameters**

|         | _       |
|---------|---------|
| context | Context |
|         | which   |
|         | may     |
|         | be      |
|         | needed  |
|         | to ex-  |
|         | tract   |
|         | alge-   |
|         | braic   |
|         | info.   |
| slot    | Datum   |
|         | to be   |
|         | con-    |
|         | verted  |
|         | to a    |
|         | Slot↩   |
|         | Type.   |

#### Returns

Converted slot.

#### 7.132.4.14 cube()

```
Ptxt< Scheme > & helib::Ptxt::cube ( )
```

Cube operation on a Ptxt.

#### Returns

Reference to \*this post cube operation.

## 7.132.4.15 decodeSetData() [1/2]

## 7.132.4.16 decodeSetData() [2/2]

Set the Ptxt slots using values from decoding data to slot representation.

#### **Parameters**

| data | Polynomial |
|------|------------|
|      | to be      |
|      | de-        |
|      | coded      |
|      | and        |
|      | con-       |
|      | verted     |
|      | into       |
|      | slot       |
|      | data.      |

#### Note

Only works in the  ${\tt BGV}$  case.

### 7.132.4.17 frobeniusAutomorph() [1/2]

Apply the frobenius automorphism  $a(X) -> a(X^{\wedge}(p^{\wedge}j)) \mod Phi_m(X)$ .

### **Parameters**

| j | Ex  | <br>ponent |
|---|-----|------------|
|   | of  | the        |
|   | au  | to-        |
|   | mc  | r-         |
|   | phi | ism        |
|   | to  |            |
|   | ар  | ply.       |

#### Returns

Reference to  $\verb|*this|$  post frobenius automorphism application.

#### Note

Only valid for the BGV scheme.

## 7.132.4.18 frobeniusAutomorph() [2/2]

```
\label{eq:bgv}  \mbox{Ptxt} < \mbox{BGV} > \mbox{$\&$ helib::Ptxt} < \mbox{BGV} > \mbox{$::$ frobenius Automorph} \mbox{ (} \\ \mbox{long } j \mbox{\ )}
```

## 7.132.4.19 getPolyRepr() [1/3]

```
NTL::ZZX helib::Ptxt< BGV >::getPolyRepr ( ) const
```

BGV specialisation of the getPolyRepr function.

### Returns

Single encoded polynomial.

Note

Only enabled for the BGV scheme.

## 7.132.4.20 getPolyRepr() [2/3]

```
NTL::ZZX helib::Ptxt< CKKS >::getPolyRepr ( ) const
```

CKKS specialisation of the getPolyRepr function.

### Returns

Single encoded polynomial.

Note

Only enabled for the CKKS scheme.

## 7.132.4.21 getPolyRepr() [3/3]

```
NTL::ZZX helib::Ptxt::getPolyRepr ( ) const
```

Converts the slot data in this to its single polynomial representation.

Returns

Single encoded polynomial.

Note

 $\mathtt{NTL}$ :  $\mathtt{ZZX}$  representation loses some precision in the  $\mathtt{CKKS}$  case.

#### 7.132.4.22 getSlotRepr()

```
\verb|const| std::vector<| typename | Ptxt<| Scheme | >::SlotType > & helib::Ptxt::getSlotRepr () | const| | cons
```

Get the data held in the slots as a std::vector<SlotType>.

#### Returns

Constant reference to the slot vector.

#### 7.132.4.23 imag() [1/2]

```
template<typename T = Scheme, std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
Ptxt<Scheme> helib::Ptxt::imag ( ) const
```

Extract the imaginary part of a CKKS plaintext.

#### Returns

New plaintext containing the imaginary part of each slot.

#### Note

Only valid for the CKKS scheme.

### 7.132.4.24 imag() [2/2]

```
Ptxt< CKKS > helib::Ptxt< CKKS >::imag ( ) const
```

# 7.132.4.25 incrementalProduct()

```
Ptxt< Scheme > & helib::Ptxt::incrementalProduct ( )
```

Compute the incremental product (each slot is the product of the previous slots).

#### Returns

Reference to \*this post multiplication.

## 7.132.4.26 isValid()

```
bool helib::Ptxt::isValid ( ) const
```

Check if a Ptxt is valid.

### Returns

true if valid, false otherwise.

## 7.132.4.27 lsize()

```
long helib::Ptxt::lsize ( ) const
```

Returns the size (number of slots) of a Ptxt as long.

#### Returns

Number of slots of the Ptxt.

## 7.132.4.28 mapTo01()

```
Ptxt< Scheme > & helib::Ptxt::mapTo01 ( )
```

Map all non-zero slots to 1, keeping zero slots as zero.

### Returns

Reference to \*this post mapping.

## 7.132.4.29 multiplyBy()

Multiplication function between two Ptxt objects.

### **Parameters**

| otherPtxt | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | multi-  |
|           | plica-  |
|           | tion.   |

### Returns

Reference to \*this post multiplication.

#### Note

This function is equivalent to operator \*=.

# 7.132.4.30 multiplyBy2()

Multiplication function between three Ptxt objects.

#### **Parameters**

| otherPtxt1 | First   |
|------------|---------|
|            | Ptxt    |
|            | to mul- |
|            | tiply   |
|            | with.   |
| otherPtxt2 | Second  |
|            | Ptxt    |
|            | to mul- |
|            | tiply   |
|            | with.   |

#### Returns

Reference to \*this post multiplication.

# 7.132.4.31 negate()

```
Ptxt< Scheme > & helib::Ptxt::negate ( )
```

Negate a Ptxt.

#### Returns

Reference to \*this post negation.

# 7.132.4.32 operator"!=()

```
bool helib::Ptxt::operator!= ( {\tt const\ Ptxt}< {\tt Scheme}\ >\ \&\ other\ )\ {\tt const}
```

Not equals operator between two Ptxt objects.

### **Parameters**

| other | Ptxt |
|-------|------|
|       | to   |
|       | com- |
|       | pare |
|       | to.  |

#### Returns

true if differ, false otherwise.

# 7.132.4.33 operator\*()

Infix multiplication operator.

### **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | multi-  |
|     | plica-  |
|     | tion.   |

## Returns

Product of the two Ptxt objects.

### 7.132.4.34 operator\*=() [1/5]

### 7.132.4.35 operator\*=() [2/5]

Times equals operator with another Ptxt.

#### **Parameters**

| otherPtxt | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | multi-  |
|           | plica-  |
|           | tion.   |

### Returns

Reference to \*this post multiplication.

## 7.132.4.36 operator\*=() [3/5]

Times equals operator with a scalar.

# **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | added   |
|        | across  |
|        | all     |
|        | slots.  |

#### Returns

Reference to \*this post scalar multiplication.

# 7.132.4.37 operator\*=() [4/5]

## 7.132.4.38 operator\*=() [5/5]

Times equals operator with a single SlotType.

### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | multi-  |
|        | plied   |
|        | across  |
|        | all     |
|        | slots.  |

### Returns

Reference to \*this post multiplication.

# 7.132.4.39 operator+()

Infix addition operator.

# **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | addi-   |
|     | tion.   |

#### Returns

Sum of the two Ptxt objects.

### 7.132.4.40 operator+=() [1/5]

### 7.132.4.41 operator+=() [2/5]

Plus equals operator with another Ptxt.

#### **Parameters**

| otherPtxt | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | addi-   |
|           | tion.   |

#### Returns

Reference to \*this post addition.

## 7.132.4.42 operator+=() [3/5]

Plus equals operator with a scalar.

### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | added   |
|        | across  |
|        | all     |
|        | slots.  |

#### Returns

Reference to \*this post scalar addition.

## 7.132.4.43 operator+=() [4/5]

### 7.132.4.44 operator+=() [5/5]

Plus equals operator with a single SlotType.

### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | added   |
|        | across  |
|        | all     |
|        | slots.  |

### Returns

Reference to \*this post addition.

## 7.132.4.45 operator-()

Infix subtraction operator.

### **Parameters**

| rhs | Right   |
|-----|---------|
|     | hand    |
|     | side of |
|     | sub-    |
|     | trac-   |
|     | tion.   |

#### Returns

Difference of the two Ptxt objects.

## 7.132.4.46 operator-=() [1/5]

### 7.132.4.47 operator-=() [2/5]

Minus equals operator with another Ptxt.

### **Parameters**

| otherPtxt | Right   |
|-----------|---------|
|           | hand    |
|           | side of |
|           | sub-    |
|           | trac-   |
|           | tion.   |

#### Returns

Reference to \*this post subtraction.

## 7.132.4.48 operator-=() [3/5]

Minus equals operator with a scalar.

### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | sub-    |
|        | tracted |
|        | across  |
|        | all     |
|        | slots.  |

### Returns

Reference to \*this post scalar subtraction.

## 7.132.4.49 operator-=() [4/5]

### 7.132.4.50 operator-=() [5/5]

Minus equals operator with a single  ${\tt SlotType}.$ 

### **Parameters**

| scalar | Element |
|--------|---------|
|        | to be   |
|        | sub-    |
|        | tracted |
|        | across  |
|        | all     |
|        | slots.  |

### Returns

Reference to \*this post subtraction.

# 7.132.4.51 operator=() [1/2]

```
\label{limits} $$ Ptxt<Scheme>& helib::Ptxt::operator= ( \\ const Ptxt< Scheme > & v ) \quad [default] $$
```

Copy assignment operator with other Ptxt.

### **Parameters**

| other | Ptxt  |
|-------|-------|
|       | to    |
|       | сору. |

# 7.132.4.52 operator=() [2/2]

```
\label{lem:ptxt} $$ Ptxt<Scheme>& helib::Ptxt::operator= ( \\  Ptxt<Scheme>&& v ) [default], [noexcept] $$
```

Move assignment operator with other Ptxt.

### **Parameters**

| other | Ptxt  |
|-------|-------|
|       | to    |
|       | сору. |

### 7.132.4.53 operator==()

Equals operator between two Ptxt objects.

#### **Parameters**

| other | Ptxt |
|-------|------|
|       | to   |
|       | com- |
|       | pare |
|       | to.  |

### Returns

true if identical, false otherwise.

### 7.132.4.54 operator[]() [1/2]

```
Ptxt< Scheme >::SlotType & helib::Ptxt::operator[] ( \log i )
```

Square bracket accessor operator.

# **Parameters**

```
i Index
of the
de-
sired
Ptxt
slot.
```

#### Returns

Reference to the data held at slot i.

## 7.132.4.55 operator[]() [2/2]

const square bracket accessor operator.

### **Parameters**

```
i Index of the desired Ptxt slot.
```

### Returns

Copy of the data held at slot i.

## 7.132.4.56 power()

Power operation to raise a Ptxt to an arbitrary non-negative power.

# **Parameters**

| е | Exponent |
|---|----------|
|   | to       |
|   | raise    |
|   | the      |
|   | Ptxt     |
|   | by.      |

# Returns

Reference to \*this post raising to the power e.

## 7.132.4.57 random()

```
Ptxt< Scheme > & helib::Ptxt::random ( )
```

Populate slots with random data.

#### Returns

Reference to \*this post population.

## 7.132.4.58 real() [1/2]

```
template<typename T = Scheme, std::enable_if_t< std::is_same< T, CKKS >::value > * = nullptr>
Ptxt<Scheme> helib::Ptxt::real ( ) const
```

Extract the real part of a CKKS plaintext.

#### Returns

New plaintext containing the real part of each slot.

#### Note

Only valid for the CKKS scheme.

### 7.132.4.59 real() [2/2]

```
Ptxt< CKKS > helib::Ptxt< CKKS >::real ( ) const
```

# 7.132.4.60 replicate()

Replicate single slot across all slots.

# **Parameters**

| pos | Position |
|-----|----------|
| POO |          |
|     | of the   |
|     | slot to  |
|     | repli-   |
|     | cate.    |

#### Returns

Reference to \*this post replication.

## 7.132.4.61 replicateAll()

Generate a vector of plaintexts with each slot replicated in each plaintext.

#### Returns

Vector of replicated plaintext slots. The order of the return vector agrees with the order of the slots. i.e. the i-th plaintext in the return value is a replication of \*this[i].

## 7.132.4.62 rotate()

Rotate slots right by specified amount (slot i goes to slot i+1 mod size).

#### **Parameters**

| amount | Number   |
|--------|----------|
|        | of slots |
|        | to ro-   |
|        | tate     |
|        | by.      |

#### Returns

Reference to \*this post rotation.

### 7.132.4.63 rotate1D()

Rotate slots right by specified amount along a specific dimension.

#### **Parameters**

| dim    | Dimension<br>in<br>which<br>to<br>rotate.   |
|--------|---|
| amount | Number<br>of slots<br>to ro-<br>tate<br>by. |

### Returns

Reference to \*this post rotation.

### 7.132.4.64 runningSums()

```
Ptxt< Scheme > & helib::Ptxt::runningSums ( )
```

Compute the running sum (each slot is the sum of the previous slots).

### Returns

Reference to \*this post summation.

## 7.132.4.65 setData() [1/6]

## 7.132.4.66 setData() [2/6]

Set the Ptxt data replicating the input polynomial on all slots.

## **Parameters**

| data | Polynomia |
|------|-----------|
|      | to be     |
|      | repli-    |
|      | cate      |
|      | into      |
|      | slots.    |

### Note

Only works in the BGV case.

## 7.132.4.67 setData() [3/6]

## 7.132.4.68 setData() [4/6]

Set the data replicating the input on all slots.

### **Parameters**

| value | value  |
|-------|--------|
|       | to set |
|       | all    |
|       | slots  |
|       | to.    |

## 7.132.4.69 setData() [5/6]

## 7.132.4.70 setData() [6/6]

Set the data.

### **Parameters**

| data | Vector  |
|------|---------|
|      | of      |
|      | Slot↩   |
|      | Type    |
|      | to pop- |
|      | ulate   |
|      | the     |
|      | slots.  |

## 7.132.4.71 shift()

Shifts slots right by specified amount with 0 fill (slot i goes to slot  $i+1 \mod size$ ).

#### **Parameters**

| . aramotoro |          |
|-------------|----------|
| amount      | Number   |
|             | of slots |
|             | to shift |
|             | by.      |

#### Returns

Reference to \*this post shift.

## 7.132.4.72 shift1D()

Shift slots right in one dimension of the hypercube structure with 0 fill.

#### **Parameters**

|        | Г         |
|--------|-----------|
| dim    | Dimension |
|        | in        |
|        | which     |
|        | to        |
|        | shift.    |
| amount | Amount    |
|        | by        |
|        | which     |
|        | to        |
|        | shift.    |

### Returns

Reference to \*this post shift.

### 7.132.4.73 size()

```
size_t helib::Ptxt::size ( ) const
```

Returns the size (number of slots) of a Ptxt.

#### Returns

Number of slots of the Ptxt.

## 7.132.4.74 square()

```
Ptxt< Scheme > & helib::Ptxt::square ( )
```

Square operation on a Ptxt.

## Returns

Reference to \*this post squaring.

## 7.132.4.75 totalProduct()

```
Ptxt< Scheme > & helib::Ptxt::totalProduct ( )
```

Compute the total product (each slot contains the total product of every slot).

#### Returns

Reference to \*this post multiplication.

## 7.132.4.76 totalSums()

```
Ptxt< Scheme > & helib::Ptxt::totalSums ( )
```

Compute the total sum (each slot contains the total sum of every slot).

#### Returns

Reference to \*this post summation.

## 7.132.5 Friends And Related Function Documentation

## 7.132.5.1 operator <<

Output shift operator.

#### **Parameters**

| os   | Output  |     |
|------|---------|-----|
|      | std↩    |     |
|      | ::ostre | am. |
| ptxt | Ptxt    |     |
|      | object  |     |
|      | to be   |     |
|      | writ-   |     |
|      | ten.    |     |

#### Returns

Input std::ostream post writing.

### Note

Ptxt context is not serialised, see note of operator>>.

#### 7.132.5.2 operator>>

Input shift operator.

#### **Parameters**

| is   | Input      |     |
|------|------------|-----|
|      | std←       |     |
|      | ::istre    | am. |
| ptxt | Destinatio | n   |
|      | Ptxt       |     |
|      | object.    |     |

#### Returns

Input std::istream post reading.

## Note

ptxt must be constructed with an appropriate context **BEFORE** calling this function. For example,  $ptxt my_ptxt(context)$ ;  $ptxt my_ptxt(context)$ ;  $ptxt my_ptxt(context)$ ;

The documentation for this class was generated from the following files:

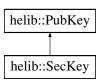
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ctxt.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ptxt.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Ptxt.cpp

# 7.133 helib::PubKey Class Reference

The public key.

#include <keys.h>

Inheritance diagram for helib::PubKey:



### **Public Member Functions**

• PubKey ()

This constructor thorws run-time error if activeContext=nullptr.

- PubKey (const Context &\_context)
- PubKey (const PubKey &other)

Copy constructor.

virtual ∼PubKey ()=default

Default destructor.

• virtual void clear ()

Clear all public-key data.

- bool operator== (const PubKey &other) const
- bool operator!= (const PubKey &other) const
- · const Context & getContext () const
- long getPtxtSpace () const
- bool keyExists (long keyID) const
- double getSKeyBound (long keyID=0) const

The size of the secret key.

• bool isReachable (long k, long keyID=0) const

Is it possible to re-linearize the automorphism  $X \to X^k$  See Section 3.2.2 in the design document (KeySwitchMap)

void setKeySwitchMap (long keyId=0)

Compute the reachability graph of key-switching matrices See Section 3.2.2 in the design document (KeySwitchMap)

long getKSStrategy (long dim) const

get KS strategy for dimension dim dim == -1 is Frobenius

void setKSStrategy (long dim, int val)

set KS strategy for dimension dim dim == -1 is Frobenius

- long Encrypt (Ctxt &ciphertxt, const NTL::ZZX &plaintxt, long ptxtSpace, bool highNoise) const
- long Encrypt (Ctxt &ciphertxt, const zzX &plaintxt, long ptxtSpace, bool highNoise) const
- void CKKSencrypt (Ctxt &ciphertxt, const NTL::ZZX &plaintxt, double ptxtSize=1.0, double scaling=0.0) const
- void CKKSencrypt (Ctxt &ciphertxt, const zzX &plaintxt, double ptxtSize=1.0, double scaling=0.0) const
- virtual long Encrypt (Ctxt &ciphertxt, const NTL::ZZX &plaintxt, long ptxtSpace=0) const
- virtual long Encrypt (Ctxt &ciphertxt, const zzX &plaintxt, long ptxtSpace=0) const
- template<typename Scheme >

long Encrypt (Ctxt &ciphertxt, const Ptxt< Scheme > &plaintxt, long ptxtSpace=0) const

Encrypts a plaintext into a ciphertext.

- bool isCKKS () const
- bool isBootstrappable () const
- void reCrypt (Ctxt &ctxt) const
- void thinReCrypt (Ctxt &ctxt) const
- friend void ::helib::writePubKeyBinary (std::ostream &str, const PubKey &pk)
- friend void ::helib::readPubKeyBinary (std::istream &str, PubKey &pk)
- void hackPtxtSpace (long p2r)
- template<> long Encrypt (Ctxt &ciphertxt, const Ptxt< BGV > &plaintxt, long ptxtSpace) const
- template<> long Encrypt (Ctxt &ciphertxt, const Ptxt< CKKS > &plaintxt, UNUSED long ptxtSpace) const

#### Find key-switching matrices

- const std::vector < KeySwitch > & keySWlist () const
- const KeySwitch & getKeySWmatrix (const SKHandle &from, long toID=0) const

Find a key-switching matrix by its indexes. If no such matrix exists it returns a dummy matrix with toKeyID==-1.

- const KeySwitch & getKeySWmatrix (long fromSPower, long fromXPower, long fromID=0, long toID=0)
- bool haveKeySWmatrix (const SKHandle &from, long toID=0) const
- bool haveKeySWmatrix (long fromSPower, long fromXPower, long fromID=0, long toID=0) const
- const KeySwitch & getAnyKeySWmatrix (const SKHandle &from) const

Is there a matrix from this key to any base key?

- bool haveAnyKeySWmatrix (const SKHandle &from) const
- const KeySwitch & getNextKSWmatrix (long fromXPower, long fromID=0) const

Get the next matrix to use for multi-hop automorphism See Section 3.2.2 in the design document.

#### **Static Public Member Functions**

static long ePlusR (long p)

## **Friends**

- class SecKey
- std::ostream & operator<< (std::ostream &str, const PubKey &pk)</li>
- std::istream & operator>> (std::istream &str, PubKey &pk)

# 7.133.1 Detailed Description

The public key.

## 7.133.2 Constructor & Destructor Documentation

```
7.133.2.1 PubKey() [1/3]
```

```
helib::PubKey::PubKey ( )
```

This constructor thorws run-time error if activeContext=nullptr.

## 7.133.2.2 PubKey() [2/3]

### 7.133.2.3 PubKey() [3/3]

```
helib::PubKey::PubKey (

const PubKey & other )
```

Copy constructor.

# 7.133.2.4 $\sim$ PubKey()

```
virtual helib::PubKey::~PubKey ( ) [virtual], [default]
```

Default destructor.

#### 7.133.3 Member Function Documentation

### 7.133.3.1 CKKSencrypt() [1/2]

### 7.133.3.2 CKKSencrypt() [2/2]

## 7.133.3.3 clear()

```
void helib::PubKey::clear ( ) [virtual]
```

Clear all public-key data.

Reimplemented in helib::SecKey.

### 7.133.3.4 Encrypt() [1/7]

Encrypts plaintext, result returned in the ciphertext argument. When called with highNoise=true, returns a ciphertext with noise level approximately q/8. For BGV, ptxtSpace is the intended plaintext space, which cannot be co-prime with pubEncrKey.ptxtSpace. The returned value is the plaintext-space for the resulting ciphertext, which is  $G \leftarrow CD(ptxtSpace, pubEncrKey.ptxtSpace)$ . For CKKS, ptxtSpace is a bound on the size of the complex plaintext elements that are encoded in ptxt (before scaling), it is assumed that they are scaled by context.alMod.encode  $\leftarrow$  ScalingFactor(). The returned value is the same as the argument ptxtSpace.

# 7.133.3.5 Encrypt() [2/7]

Reimplemented in helib::SecKey.

### 7.133.3.6 Encrypt() [3/7]

## 7.133.3.7 Encrypt() [4/7]

### 7.133.3.8 Encrypt() [5/7]

Encrypts a plaintext into a ciphertext.

### **Template Parameters**

Scheme | Encryption scheme used (must be BGV or CKKS).

#### **Parameters**

| ciphertxt | Ciphertext |
|-----------|------------|
|           | into       |
|           | which      |
|           | to en-     |
|           | crypt.     |
| plaintxt  | Plaintext  |
|           | to en-     |
|           | crypt.     |

#### Returns

Plaintext space.

## 7.133.3.9 Encrypt() [6/7]

# 7.133.3.10 Encrypt() [7/7]

Reimplemented in helib::SecKey.

#### 7.133.3.11 ePlusR()

```
static long helib::PubKey::ePlusR ( \log \ p \ ) \quad [\mathrm{static}]
```

### 7.133.3.12 getAnyKeySWmatrix()

Is there a matrix from this key to any base key?

### 7.133.3.13 getContext()

```
const Context & helib::PubKey::getContext ( ) const
```

## 7.133.3.14 getKeySWmatrix() [1/2]

Find a key-switching matrix by its indexes. If no such matrix exists it returns a dummy matrix with toKeyID==-1.

### 7.133.3.15 getKeySWmatrix() [2/2]

## 7.133.3.16 getKSStrategy()

get KS strategy for dimension dim dim == -1 is Frobenius

#### 7.133.3.17 getNextKSWmatrix()

Get the next matrix to use for multi-hop automorphism See Section 3.2.2 in the design document.

## 7.133.3.18 getPtxtSpace()

```
long helib::PubKey::getPtxtSpace ( ) const
```

## 7.133.3.19 getSKeyBound()

The size of the secret key.

## 7.133.3.20 hackPtxtSpace()

## 7.133.3.21 haveAnyKeySWmatrix()

## 7.133.3.22 haveKeySWmatrix() [1/2]

## 7.133.3.23 haveKeySWmatrix() [2/2]

## 7.133.3.24 isBootstrappable()

```
bool helib::PubKey::isBootstrappable ( ) const
```

## 7.133.3.25 isCKKS()

```
bool helib::PubKey::isCKKS ( ) const
```

## 7.133.3.26 isReachable()

```
bool helib::PubKey::isReachable ( long \ k, \\ long \ keyID = 0 ) const
```

Is it possible to re-linearize the automorphism  $X -> X^{\wedge}k$  See Section 3.2.2 in the design document (KeySwitchMap)

## 7.133.3.27 keyExists()

## 7.133.3.28 keySWlist()

```
const std::vector< KeySwitch > & helib::PubKey::keySWlist ( ) const
```

## 7.133.3.29 operator"!=()

## 7.133.3.30 operator==()

#### 7.133.3.31 reCrypt()

## 7.133.3.32 setKeySwitchMap()

Compute the reachability graph of key-switching matrices See Section 3.2.2 in the design document (KeySwitch← Map)

#### 7.133.3.33 setKSStrategy()

set KS strategy for dimension dim dim == -1 is Frobenius

## 7.133.3.34 thinReCrypt()

## 7.133.3.35 void ::helib::readPubKeyBinary()

## 7.133.3.36 void ::helib::writePubKeyBinary()

```
\label{eq:helib::writePubKeyBinary} $$ \text{helib::writePubKeyBinary (} $$ std::ostream & str, $$ const PubKey & pk )$
```

## 7.133.4 Friends And Related Function Documentation

## 7.133.4.1 operator <<

## 7.133.4.2 operator>>

```
std::istream& operator>> (  std::istream \& str, \\ PubKey \& pk ) \quad [friend]
```

## 7.133.4.3 SecKey

```
friend class SecKey [friend]
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/keys.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/keys.cpp
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/recryption.cpp

# 7.134 helib::PubKeyHack Struct Reference

#### **Public Attributes**

- const Context & context
- Ctxt pubEncrKey
- std::vector< long > skHwts
- std::vector< KeySwitch > keySwitching
- std::vector< std::vector< long > > keySwitchMap
- NTL::Vec< int > KS\_strategy
- · long recryptKeyID
- Ctxt recryptEkey

## 7.134.1 Member Data Documentation

#### 7.134.1.1 context

```
const Context& helib::PubKeyHack::context
```

## 7.134.1.2 keySwitching

std::vector<KeySwitch> helib::PubKeyHack::keySwitching

## 7.134.1.3 keySwitchMap

std::vector<std::vector<long> > helib::PubKeyHack::keySwitchMap

#### 7.134.1.4 KS\_strategy

NTL::Vec<int> helib::PubKeyHack::KS\_strategy

## 7.134.1.5 pubEncrKey

Ctxt helib::PubKeyHack::pubEncrKey

The public encryption key is an encryption of 0, relative to the first secret key

## 7.134.1.6 recryptEkey

Ctxt helib::PubKeyHack::recryptEkey

## 7.134.1.7 recryptKeyID

long helib::PubKeyHack::recryptKeyID

#### 7.134.1.8 skHwts

std::vector<long> helib::PubKeyHack::skHwts

The documentation for this struct was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/recryption.cpp

# 7.135 helib::quarter\_FFT Struct Reference

```
#include <PAlgebra.h>
```

## **Public Member Functions**

• quarter\_FFT (long m)

## **Public Attributes**

- PGFFT fft
- std::vector< std::complex< double >> pow1
- std::vector< std::complex< double >> pow2

## 7.135.1 Constructor & Destructor Documentation

```
7.135.1.1 quarter_FFT()
```

#### 7.135.2 Member Data Documentation

## 7.135.2.1 fft

```
PGFFT helib::quarter_FFT::fft
```

## 7.135.2.2 pow1

```
std::vector<std::complex<double> > helib::quarter_FFT::pow1
```

## 7.135.2.3 pow2

```
std::vector<std::complex<double> > helib::quarter_FFT::pow2
```

The documentation for this struct was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/PAlgebra.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/PAlgebra.cpp

# 7.136 helib::random\_pa\_impl< type > Class Template Reference

## **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa)

#### 7.136.1 Member Function Documentation

#### 7.136.1.1 apply()

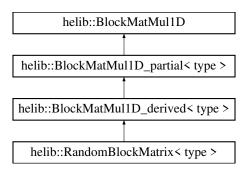
The documentation for this class was generated from the following file:

/Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/src/EncryptedArray.cpp

# 7.137 helib::RandomBlockMatrix< type > Class Template Reference

```
#include <randomMatrices.h>
```

Inheritance diagram for helib::RandomBlockMatrix< type >:



#### **Public Member Functions**

- RandomBlockMatrix (const EncryptedArray &\_ea, long \_dim)
- bool get (mat\_R &out, long i, long j, UNUSED long k) const override
- const EncryptedArray & getEA () const override
- long getDim () const override
- bool multipleTransforms () const override

## **Additional Inherited Members**

## 7.137.1 Constructor & Destructor Documentation

#### 7.137.1.1 RandomBlockMatrix()

#### 7.137.2 Member Function Documentation

## 7.137.2.1 get()

## 7.137.2.2 getDim()

```
template<typename type >
long helib::RandomBlockMatrix< type >::getDim ( ) const [inline], [override], [virtual]
```

Implements helib::BlockMatMul1D.

## 7.137.2.3 getEA()

```
template<typename type >
const EncryptedArray& helib::RandomBlockMatrix< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::BlockMatMul1D.

#### 7.137.2.4 multipleTransforms()

```
template<typename type >
bool helib::RandomBlockMatrix< type >::multipleTransforms ( ) const [inline], [override],
[virtual]
```

Implements helib::BlockMatMul1D\_derived< type >.

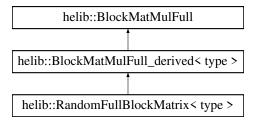
The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/randomMatrices.h

# 7.138 helib::RandomFullBlockMatrix< type > Class Template Reference

```
#include <randomMatrices.h>
```

Inheritance diagram for helib::RandomFullBlockMatrix< type >:



## **Public Member Functions**

- RandomFullBlockMatrix (const EncryptedArray & ea)
- bool get (mat\_R &out, long i, long j) const override
- const EncryptedArray & getEA () const override

#### **Additional Inherited Members**

#### 7.138.1 Constructor & Destructor Documentation

#### 7.138.1.1 RandomFullBlockMatrix()

## 7.138.2 Member Function Documentation

#### 7.138.2.1 get()

Implements helib::BlockMatMulFull\_derived< type >.

#### 7.138.2.2 getEA()

```
template<typename type >
const EncryptedArray& helib::RandomFullBlockMatrix< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::BlockMatMulFull.

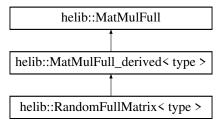
The documentation for this class was generated from the following file:

/Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/randomMatrices.h

# 7.139 helib::RandomFullMatrix< type > Class Template Reference

```
#include <randomMatrices.h>
```

Inheritance diagram for helib::RandomFullMatrix< type >:



## **Public Member Functions**

- RandomFullMatrix (const EncryptedArray &\_ea)
- bool get (RX &out, long i, long j) const override
- const EncryptedArray & getEA () const override

## **Additional Inherited Members**

## 7.139.1 Constructor & Destructor Documentation

#### 7.139.1.1 RandomFullMatrix()

## 7.139.2 Member Function Documentation

#### 7.139.2.1 get()

Implements helib::MatMulFull\_derived< type >.

## 7.139.2.2 getEA()

```
template<typename type >
const EncryptedArray& helib::RandomFullMatrix< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::MatMulFull.

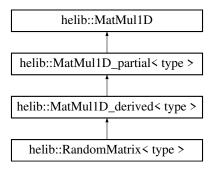
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/randomMatrices.h

# 7.140 helib::RandomMatrix< type > Class Template Reference

```
#include <randomMatrices.h>
```

Inheritance diagram for helib::RandomMatrix< type >:



## **Public Member Functions**

- virtual ∼RandomMatrix ()
- RandomMatrix (const EncryptedArray &\_ea, long \_dim)
- const EncryptedArray & getEA () const override
- bool multipleTransforms () const override
- long getDim () const override
- bool get (RX &out, long i, long j, UNUSED long k) const override

## **Additional Inherited Members**

## 7.140.1 Constructor & Destructor Documentation

## 7.140.1.1 ~RandomMatrix()

```
template<typename type >
virtual helib::RandomMatrix< type >::~RandomMatrix ( ) [inline], [virtual]
```

#### 7.140.1.2 RandomMatrix()

#### 7.140.2 Member Function Documentation

## 7.140.2.1 get()

#### 7.140.2.2 getDim()

```
template<typename type >
long helib::RandomMatrix< type >::getDim ( ) const [inline], [override], [virtual]
```

Implements helib::MatMul1D.

#### 7.140.2.3 getEA()

```
template<typename type >
const EncryptedArray& helib::RandomMatrix< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::MatMul1D.

#### 7.140.2.4 multipleTransforms()

```
template<typename type >
bool helib::RandomMatrix< type >::multipleTransforms ( ) const [inline], [override], [virtual]
```

Implements helib::MatMul1D\_derived< type >.

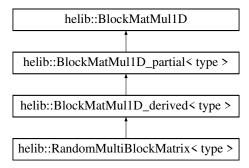
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/randomMatrices.h

# 7.141 helib::RandomMultiBlockMatrix< type > Class Template Reference

```
#include <randomMatrices.h>
```

Inheritance diagram for helib::RandomMultiBlockMatrix< type >:



## **Public Member Functions**

- RandomMultiBlockMatrix (const EncryptedArray &\_ea, long \_dim)
- bool get (mat\_R &out, long i, long j, long k) const override
- · const EncryptedArray & getEA () const override
- long getDim () const override
- bool multipleTransforms () const override

#### **Additional Inherited Members**

## 7.141.1 Constructor & Destructor Documentation

#### 7.141.1.1 RandomMultiBlockMatrix()

#### 7.141.2 Member Function Documentation

## 7.141.2.1 get()

 $Implements\ helib:: Block Mat Mul1D\_derived < type >.$ 

## 7.141.2.2 getDim()

```
template<typename type >
long helib::RandomMultiBlockMatrix< type >::getDim ( ) const [inline], [override], [virtual]
```

Implements helib::BlockMatMul1D.

#### 7.141.2.3 getEA()

```
template<typename type >
const EncryptedArray& helib::RandomMultiBlockMatrix< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::BlockMatMul1D.

## 7.141.2.4 multipleTransforms()

```
template<typename type >
bool helib::RandomMultiBlockMatrix< type >::multipleTransforms ( ) const [inline], [override],
[virtual]
```

Implements helib::BlockMatMul1D\_derived< type >.

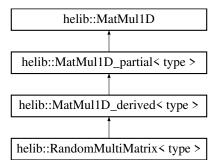
The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/randomMatrices.h

# 7.142 helib::RandomMultiMatrix< type > Class Template Reference

```
#include <randomMatrices.h>
```

Inheritance diagram for helib::RandomMultiMatrix< type >:



## **Public Member Functions**

- virtual ∼RandomMultiMatrix ()
- RandomMultiMatrix (const EncryptedArray &\_ea, long \_dim)
- const EncryptedArray & getEA () const override
- bool multipleTransforms () const override
- long getDim () const override
- bool get (RX &out, long i, long j, long k) const override

## **Additional Inherited Members**

## 7.142.1 Constructor & Destructor Documentation

## 7.142.1.1 ∼RandomMultiMatrix()

```
template<typename type >
virtual helib::RandomMultiMatrix< type >::~RandomMultiMatrix ( ) [inline], [virtual]
```

## 7.142.1.2 RandomMultiMatrix()

## 7.142.2 Member Function Documentation

## 7.142.2.1 get()

Implements helib::MatMul1D\_derived< type >.

## 7.142.2.2 getDim()

```
template<typename type >
long helib::RandomMultiMatrix< type >::getDim ( ) const [inline], [override], [virtual]
```

Implements helib::MatMul1D.

#### 7.142.2.3 getEA()

```
template<typename type >
const EncryptedArray& helib::RandomMultiMatrix< type >::getEA ( ) const [inline], [override],
[virtual]
```

Implements helib::MatMul1D.

#### 7.142.2.4 multipleTransforms()

```
template<typename type >
bool helib::RandomMultiMatrix< type >::multipleTransforms ( ) const [inline], [override],
[virtual]
```

 $Implements\ helib:: MatMul1D\_derived < type >.$ 

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/randomMatrices.h

## 7.143 helib::RandomState Class Reference

Facility for "restoring" the NTL PRG state.

```
#include <NumbTh.h>
```

## **Public Member Functions**

- · RandomState ()
- void restore ()

Restore the PRG state of NTL.

•  $\sim$ RandomState ()

## 7.143.1 Detailed Description

Facility for "restoring" the NTL PRG state.

NTL's random number generation facility is pretty limited, and does not provide a way to save/restore the state of a pseudo-random stream. This class gives us that ability: Constructing a RandomState object uses the PRG to generate 512 bits and stores them. Upon destruction (or an explicit call to restore()), these bits are used to re-set the seed of the PRG. A typical usage of the class is as follows:

## 7.143.2 Constructor & Destructor Documentation

## 7.143.2.1 RandomState()

helib::RandomState::RandomState ( ) [inline]

## 7.143.2.2 ~RandomState()

 $\verb|helib::RandomState:: \sim RandomState ( ) [inline]|$ 

## 7.143.3 Member Function Documentation

## 7.143.3.1 restore()

void helib::RandomState::restore ( ) [inline]

Restore the PRG state of NTL.

The documentation for this class was generated from the following file:

 $\bullet \ / Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/NumbTh.h \\$ 

# 7.144 helib::RecryptData Class Reference

A structure to hold recryption-related data inside the Context.

#include <recryption.h>

Inheritance diagram for helib::RecryptData:



#### **Public Member Functions**

- RecryptData ()
- void init (const Context &context, const NTL::Vec< long > &mvec\_, bool enableThick, long t=0, bool build\_cache=false, bool minimal=false)

Initialize the recryption data in the context.

- bool operator== (const RecryptData &other) const
- bool operator!= (const RecryptData &other) const

#### **Static Public Member Functions**

• static long setAE (long &e, long &ePrime, const Context &context, long t=0)

Helper function for computing the recryption parameters.

## **Public Attributes**

NTL::Vec< long > mvec

Some data members that are only used for I/O.

• long e

partition of m into co-prime factors

- · long ePrime
- long skHwt

Hamming weight of recryption secret key.

std::shared\_ptr< const PAlgebraMod > alMod

for plaintext space p^{e-e'+r}

• std::shared\_ptr< const EncryptedArray > ea

for plaintext space  $p^{\wedge}\{e-e'+r\}$ 

- · bool build cache
- std::shared\_ptr< const EvalMap > firstMap

linear maps

- std::shared\_ptr< const EvalMap > secondMap
- std::shared ptr< const PowerfulDCRT > p2dConv

conversion between ZZX and Powerful

std::vector< NTL::ZZX > unpackSlotEncoding

linPolys for unpacking the slots

#### **Static Public Attributes**

static constexpr long defSkHwt = 100
 default Hamming weight of recryption key

## 7.144.1 Detailed Description

A structure to hold recryption-related data inside the Context.

## 7.144.2 Constructor & Destructor Documentation

## 7.144.2.1 RecryptData()

```
helib::RecryptData::RecryptData ( ) [inline]
```

## 7.144.3 Member Function Documentation

## 7.144.3.1 init()

Initialize the recryption data in the context.

## 7.144.3.2 operator"!=()

## 7.144.3.3 operator==()

## 7.144.3.4 setAE()

```
long helib::RecryptData::setAE (
            long & e,
            long & ePrime,
            const Context & context,
            long t = 0 ) [static]
```

Helper function for computing the recryption parameters.

## 7.144.4 Member Data Documentation

## 7.144.4.1 alMod

```
\label{limited_ptr} $$ std::shared_ptr<const $$PAlgebraMod>$ helib::RecryptData::alMod $$ for plaintext space $p^{e-e'+r}$
```

## 7.144.4.2 build\_cache

```
bool helib::RecryptData::build_cache
```

#### 7.144.4.3 defSkHwt

```
constexpr long helib::RecryptData::defSkHwt = 100 [static], [constexpr]
default Hamming weight of recryption key
```

## 7.144.4.4 e

```
long helib::RecryptData::e partition\ of\ m\ into\ co\mbox{-prime factors} skey\ encrypted\ wrt\ space\ p^{\mbox{-}\{e\mbox{-}e'\mbox{+}r\}}
```

## 7.144.4.5 ea

```
\label{limited_ptr} $$ std::shared_ptr<const EncryptedArray> helib::RecryptData::ea $$ for plaintext space $p^{e-e'+r}$$
```

## 7.144.4.6 ePrime

```
long helib::RecryptData::ePrime
```

## 7.144.4.7 firstMap

```
std::shared_ptr<const EvalMap> helib::RecryptData::firstMap
```

linear maps

#### 7.144.4.8 mvec

```
NTL::Vec<long> helib::RecryptData::mvec
```

Some data members that are only used for I/O.

## 7.144.4.9 p2dConv

```
std::shared_ptr<const PowerfulDCRT> helib::RecryptData::p2dConv
```

conversion between ZZX and Powerful

## 7.144.4.10 secondMap

```
std::shared_ptr<const EvalMap> helib::RecryptData::secondMap
```

## 7.144.4.11 skHwt

long helib::RecryptData::skHwt

Hamming weight of recryption secret key.

## 7.144.4.12 unpackSlotEncoding

```
std::vector<NTL::ZZX> helib::RecryptData::unpackSlotEncoding
```

linPolys for unpacking the slots

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/recryption.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/recryption.cpp

# 7.145 helib::replicate pa impl< type > Class Template Reference

## **Static Public Member Functions**

• static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, long i)

## 7.145.1 Member Function Documentation

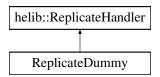
#### 7.145.1.1 apply()

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/replicate.cpp

# 7.146 ReplicateDummy Class Reference

Inheritance diagram for ReplicateDummy:



## **Public Member Functions**

- ReplicateDummy ()
- virtual void handle (const Ctxt &ctxt)

## 7.146.1 Constructor & Destructor Documentation

## 7.146.1.1 ReplicateDummy()

```
ReplicateDummy::ReplicateDummy ( ) [inline]
```

## 7.146.2 Member Function Documentation

## 7.146.2.1 handle()

Implements helib::ReplicateHandler.

The documentation for this class was generated from the following file:

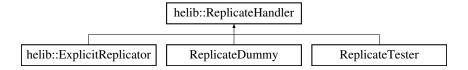
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Timing.cpp

# 7.147 helib::ReplicateHandler Class Reference

An abstract class to handle call-backs to get the output of replicate.

```
#include <replicate.h>
```

Inheritance diagram for helib::ReplicateHandler:



## **Public Member Functions**

- virtual void handle (const Ctxt &ctxt)=0
- virtual ∼ReplicateHandler ()
- virtual bool earlyStop (long d, long k, long prodDim)

# 7.147.1 Detailed Description

An abstract class to handle call-backs to get the output of replicate.

#### 7.147.2 Constructor & Destructor Documentation

## 7.147.2.1 ~ReplicateHandler()

```
\label{limits} \mbox{ virtual helib::ReplicateHandler::$$\sim$$ ReplicateHandler ( ) [inline], [virtual] $$
```

## 7.147.3 Member Function Documentation

## 7.147.3.1 earlyStop()

```
virtual bool helib::ReplicateHandler::earlyStop ( long \ d, \\ long \ k, \\ long \ prodDim \ ) \ [inline], [virtual]
```

#### 7.147.3.2 handle()

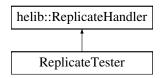
Implemented in helib::ExplicitReplicator, ReplicateDummy, and ReplicateTester.

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/replicate.h

# 7.148 ReplicateTester Class Reference

Inheritance diagram for ReplicateTester:



## **Public Member Functions**

- ReplicateTester (const SecKey &\_sKey, const EncryptedArray &\_ea, const PlaintextArray &\_pa, long \_B)
- virtual void handle (const Ctxt &ctxt)

## **Public Attributes**

- const SecKey & sKey
- const EncryptedArray & ea
- const PlaintextArray & pa
- long B
- double t\_last
- double t\_total
- long pos
- bool error

## 7.148.1 Constructor & Destructor Documentation

## 7.148.1.1 ReplicateTester()

## 7.148.2 Member Function Documentation

## 7.148.2.1 handle()

Implements helib::ReplicateHandler.

## 7.148.3 Member Data Documentation

## 7.148.3.1 B

long ReplicateTester::B

## 7.148.3.2 ea

const EncryptedArray& ReplicateTester::ea

## 7.148.3.3 error

bool ReplicateTester::error

#### 7.148.3.4 pa

const PlaintextArray& ReplicateTester::pa

#### 7.148.3.5 pos

long ReplicateTester::pos

#### 7.148.3.6 sKey

const SecKey& ReplicateTester::sKey

## 7.148.3.7 t\_last

double ReplicateTester::t\_last

## 7.148.3.8 t\_total

double ReplicateTester::t\_total

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Replicate.cpp

# 7.149 helib::rotate\_pa\_impl< type > Class Template Reference

# **Static Public Member Functions**

• static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, long k)

## 7.149.1 Member Function Documentation

## 7.149.1.1 apply()

The documentation for this class was generated from the following file:

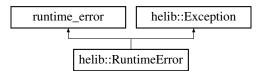
/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

## 7.150 helib::RuntimeError Class Reference

Inherits from Exception and std::runtime\_error.

```
#include <exceptions.h>
```

Inheritance diagram for helib::RuntimeError:



## **Public Member Functions**

- RuntimeError (const std::string &what\_arg)
- RuntimeError (const char \*what\_arg)
- virtual ∼RuntimeError ()
- virtual const char \* what () const noexcept override

## **Additional Inherited Members**

## 7.150.1 Detailed Description

Inherits from Exception and std::runtime\_error.

## 7.150.2 Constructor & Destructor Documentation

#### 7.150.2.1 RuntimeError() [1/2]

#### 7.150.2.2 RuntimeError() [2/2]

## 7.150.2.3 ∼RuntimeError()

```
virtual helib::RuntimeError::~RuntimeError ( ) [inline], [virtual]
```

#### 7.150.3 Member Function Documentation

## 7.150.3.1 what()

```
virtual const char* helib::RuntimeError::what ( ) const [inline], [override], [virtual], [noexcept]
Implements helib::Exception.
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/exceptions.h

## 7.151 helib::ScratchCell Class Reference

A class to help manage the allocation of temporary Ctxt objects.

## **Public Member Functions**

- ScratchCell (const Ctxt &c)
- ScratchCell (ScratchCell &&other)

## **Public Attributes**

- std::atomic\_bool used
- $std::unique\_ptr < Ctxt > ct$

# 7.151.1 Detailed Description

A class to help manage the allocation of temporary Ctxt objects.

## 7.151.2 Constructor & Destructor Documentation

## 7.151.2.1 ScratchCell() [1/2]

## 7.151.2.2 ScratchCell() [2/2]

## 7.151.3 Member Data Documentation

## 7.151.3.1 ct

```
std::unique_ptr<Ctxt> helib::ScratchCell::ct
```

## 7.151.3.2 used

```
std::atomic_bool helib::ScratchCell::used
```

The documentation for this class was generated from the following file:

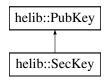
/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/binaryArith.cpp

# 7.152 helib::SecKey Class Reference

The secret key.

#include <keys.h>

Inheritance diagram for helib::SecKey:



## **Public Member Functions**

- SecKey ()=delete
- ∼SecKey () override=default
- SecKey (const Context &\_context)
- bool operator== (const SecKey &other) const
- bool operator!= (const SecKey &other) const
- · void clear () override

Clear all secret-key data.

- long ImportSecKey (const DoubleCRT &sKey, double bound, long ptxtSpace=0, long maxDegKswitch=3)
- long GenSecKey (long hwt=0, long ptxtSpace=0, long maxDegKswitch=3)
- void GenKeySWmatrix (long fromSPower, long fromXPower, long fromKeyIdx=0, long toKeyIdx=0, long ptxt
   Space=0)
- void Decrypt (NTL::ZZX &plaintxt, const Ctxt &ciphertxt) const
- template<typename Scheme >

void Decrypt (Ptxt< Scheme > &plaintxt, const Ctxt &ciphertxt) const

Decrypt a ciphertext into a plaintext.

void Decrypt (NTL::ZZX &plaintxt, const Ctxt &ciphertxt, NTL::ZZX &f) const

Debugging version, returns in f the polynomial before reduction modulo the ptxtSpace.

• long skEncrypt (Ctxt &ctxt, const NTL::ZZX &ptxt, long ptxtSpace, long skldx) const

Symmetric encryption using the secret key.

- long skEncrypt (Ctxt &ctxt, const zzX &ptxt, long ptxtSpace, long skldx) const
- long Encrypt (Ctxt &ciphertxt, const NTL::ZZX &plaintxt, long ptxtSpace=0) const override
- long Encrypt (Ctxt &ciphertxt, const zzX &plaintxt, long ptxtSpace=0) const override
- long genRecryptData ()

Generate bootstrapping data if needed, returns index of key.

- friend void ::helib::writeSecKeyBinary (std::ostream &str, const SecKey &sk)
- friend void ::helib::readSecKeyBinary (std::istream &str, SecKey &sk)
- template<> void Decrypt (Ptxt< BGV > &plaintxt, const Ctxt &ciphertxt) const
- template<> void Decrypt (Ptxt< CKKS > &plaintxt, const Ctxt &ciphertxt) const

## **Public Attributes**

std::vector < DoubleCRT > sKeys

## **Friends**

- std::ostream & operator<< (std::ostream &str, const SecKey &sk)
- std::istream & operator>> (std::istream &str, SecKey &sk)

## **Additional Inherited Members**

# 7.152.1 Detailed Description

The secret key.

## 7.152.2 Constructor & Destructor Documentation

```
7.152.2.1 SecKey() [1/2]
```

```
helib::SecKey::SecKey ( ) [delete]
```

## 7.152.2.2 ∼SecKey()

```
\verb|helib::SecKey::\sim SecKey ( ) [override], [default]|\\
```

## 7.152.2.3 SecKey() [2/2]

## 7.152.3 Member Function Documentation

## 7.152.3.1 clear()

```
void helib::SecKey::clear ( ) [override], [virtual]
```

Clear all secret-key data.

Reimplemented from helib::PubKey.

## 7.152.3.2 Decrypt() [1/5]

## 7.152.3.3 Decrypt() [2/5]

Debugging version, returns in f the polynomial before reduction modulo the ptxtSpace.

## 7.152.3.4 Decrypt() [3/5]

```
template<>
void helib::SecKey::Decrypt (
          Ptxt< BGV > & plaintxt,
          const Ctxt & ciphertxt ) const
```

#### 7.152.3.5 Decrypt() [4/5]

## 7.152.3.6 Decrypt() [5/5]

Decrypt a ciphertext into a plaintext.

#### **Template Parameters**

Scheme | Encryption scheme used (must be BGV or CKKS).

#### **Parameters**

| plaintxt  | Plaintext  |
|-----------|------------|
|           | into       |
|           | which      |
|           | to de-     |
|           | crypt.     |
| ciphertxt | Ciphertext |
|           | to de-     |
|           | crypt.     |

#### 7.152.3.7 Encrypt() [1/2]

Reimplemented from helib::PubKey.

# 7.152.3.8 Encrypt() [2/2]

Reimplemented from helib::PubKey.

## 7.152.3.9 GenKeySWmatrix()

Generate a key-switching matrix and store it in the public key. The i'th column of the matrix encrypts from Key\* $\leftarrow$  B1\*B2\*...\*B{i-1}\*Q under to Key, relative to the largest modulus (i.e., all primes) and plaintext space p. Q is the product of special primes, and the Bi's are the products of primes in the i'th digit. The plaintext space defaults to  $2^{\wedge}r$ , as defined by context.mod2r.

#### 7.152.3.10 genRecryptData()

```
long helib::SecKey::genRecryptData ( )
```

Generate bootstrapping data if needed, returns index of key.

## 7.152.3.11 GenSecKey()

Key generation: This procedure generates a single secret key, pushes it onto the sKeys list using ImportSecKey from above.

## 7.152.3.12 ImportSecKey()

We allow the calling application to choose a secret-key polynomial by itself, then insert it into the SecKey object, getting the index of that secret key in the sKeys list. If this is the first secret-key for this object then the procedure below also generates a corresponding public encryption key. It is assumed that the context already contains all parameters.

#### 7.152.3.13 operator"!=()

#### 7.152.3.14 operator==()

## 7.152.3.15 skEncrypt() [1/2]

Symmetric encryption using the secret key.

## 7.152.3.16 skEncrypt() [2/2]

## 7.152.3.17 void ::helib::readSecKeyBinary()

## 7.152.3.18 void ::helib::writeSecKeyBinary()

## 7.152.4 Friends And Related Function Documentation

#### 7.152.4.1 operator <<

```
std::ostream& operator<< (
          std::ostream & str,
          const SecKey & sk ) [friend]</pre>
```

#### 7.152.4.2 operator>>

```
std::istream& operator>> (  std::istream \& str, \\ SecKey \& sk ) \quad [friend]
```

#### 7.152.5 Member Data Documentation

#### 7.152.5.1 sKeys

```
std::vector<DoubleCRT> helib::SecKey::sKeys
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/keys.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/keys.cpp

# 7.153 helib::shallow\_clone < X > Class Template Reference

Shallow copy: initialize with copy constructor.

```
#include <clonedPtr.h>
```

#### **Static Public Member Functions**

```
    static X * apply (const X *x)
```

# 7.153.1 Detailed Description

```
template < typename X> class helib::shallow_clone < X >
```

Shallow copy: initialize with copy constructor.

#### **Template Parameters**

X The class to which this points

#### 7.153.2 Member Function Documentation

#### 7.153.2.1 apply()

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/clonedPtr.h

# 7.154 helib::shift\_pa\_impl< type > Class Template Reference

#### **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, long k)

#### 7.154.1 Member Function Documentation

#### 7.154.1.1 apply()

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.155 helib::SKHandle Class Reference

A handle, describing the secret-key element that "matches" a part, of the form  $s^{\wedge}r(X^{\wedge}t)$ .

```
#include <Ctxt.h>
```

#### **Public Member Functions**

- SKHandle (long newPowerOfS=0, long newPowerOfX=1, long newSecretKeyID=0)
- void setBase (long newSecretKeyID=-1)

```
Set powerOfS=powerOfX=1.
```

• bool isBase (long ofKeyID=0) const

```
Is powerOfS==powerOfX==1?
```

• void setOne (long newSecretKeyID=-1)

Set powerOfS=0, powerOfX=1.

• bool isOne () const

```
Is powerOfS==0?
```

- bool operator== (const SKHandle &other) const
- bool operator!= (const SKHandle &other) const
- long getPowerOfS () const
- long getPowerOfX () const
- long getSecretKeyID () const
- bool mul (const SKHandle &a, const SKHandle &b)

Computes the "product" of two handles.

- void read (std::istream &str)
- · void write (std::ostream &str) const

#### **Friends**

- · class Ctxt
- std::istream & operator>> (std::istream &s, SKHandle &handle)

# 7.155.1 Detailed Description

A handle, describing the secret-key element that "matches" a part, of the form  $s^{\wedge}r(X^{\wedge}t)$ .

#### 7.155.2 Constructor & Destructor Documentation

# 7.155.2.1 SKHandle()

#### 7.155.3 Member Function Documentation

#### 7.155.3.1 getPowerOfS()

```
long helib::SKHandle::getPowerOfS ( ) const [inline]
```

# 7.155.3.2 getPowerOfX()

```
long helib::SKHandle::getPowerOfX ( ) const [inline]
```

#### 7.155.3.3 getSecretKeyID()

```
long helib::SKHandle::getSecretKeyID ( ) const [inline]
```

#### 7.155.3.4 isBase()

Is powerOfS==powerOfX==1?

#### 7.155.3.5 isOne()

```
bool helib::SKHandle::isOne ( ) const [inline]
```

Is powerOfS==0?

#### 7.155.3.6 mul()

Computes the "product" of two handles.

The key-ID's and powers of X must match, else an error state arises, which is represented using a key-ID of -1 and returning false. Also, note that inputs may alias outputs.

To determine if the resulting handle can be re-linearized using some key-switching matrices from the public key, use the method pubKey.haveKeySWmatrix(handle,handle.secretKeyID), from the class PubKey in keys.h

# 7.155.3.7 operator"!=()

```
bool helib::SKHandle::operator!= (
          const SKHandle & other ) const [inline]
```

# 7.155.3.8 operator==()

#### 7.155.3.9 read()

```
void helib::SKHandle::read (
          std::istream & str )
```

### 7.155.3.10 setBase()

Set powerOfS=powerOfX=1.

#### 7.155.3.11 setOne()

Set powerOfS=0, powerOfX=1.

# 7.155.3.12 write()

# 7.155.4 Friends And Related Function Documentation

#### 7.155.4.1 Ctxt

```
friend class Ctxt [friend]
```

#### 7.155.4.2 operator>>

```
std::istream& operator>> (
          std::istream & s,
          SKHandle & handle ) [friend]
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ctxt.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Ctxt.cpp

# 7.156 StopReplicate Class Reference

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Replicate.cpp

# 7.157 helib::sub\_pa\_impl< type > Class Template Reference

# **Static Public Member Functions**

static void apply (const EncryptedArrayDerived< type > &ea, PlaintextArray &pa, const PlaintextArray &other)

#### 7.157.1 Member Function Documentation

#### 7.157.1.1 apply()

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EncryptedArray.cpp

# 7.158 helib::SubDimension Class Reference

A node in a tree relative to some generator.

```
#include <permutations.h>
```

#### **Public Member Functions**

- SubDimension (long sz=0, bool gd=false, long ee=0, const NTL::Vec< long > &bns1=dummyBenes, const NTL::Vec< long > &bns2=dummyBenes)
- long totalLength () const

#### **Public Attributes**

- long size
- bool good
- long e
- NTL::Vec< long > frstBenes
- NTL::Vec< long > scndBenes

# **Friends**

std::ostream & operator<< (std::ostream &s, const SubDimension &tree)</li>

# 7.158.1 Detailed Description

A node in a tree relative to some generator.

#### 7.158.2 Constructor & Destructor Documentation

#### 7.158.2.1 SubDimension()

```
helib::SubDimension::SubDimension ( long \ sz = 0, \\ bool \ gd = false, \\ long \ ee = 0, \\ const \ NTL::Vec< long > & bns1 = dummyBenes, \\ const \ NTL::Vec< long > & bns2 = dummyBenes ) [inline], [explicit]
```

# 7.158.3 Member Function Documentation

# 7.158.3.1 totalLength()

```
long helib::SubDimension::totalLength ( ) const [inline]
```

# 7.158.4 Friends And Related Function Documentation

#### 7.158.4.1 operator <<

```
std::ostream& operator<< (
          std::ostream & s,
          const SubDimension & tree ) [friend]</pre>
```

# 7.158.5 Member Data Documentation

#### 7.158.5.1 e

long helib::SubDimension::e

#### 7.158.5.2 frstBenes

NTL::Vec<long> helib::SubDimension::frstBenes

# 7.158.5.3 good

bool helib::SubDimension::good

#### 7.158.5.4 scndBenes

NTL::Vec<long> helib::SubDimension::scndBenes

#### 7.158.5.5 size

```
long helib::SubDimension::size
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE HElib Repos Public staging/homenc v1.0.2/HElib/include/helib/permutations.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/permutations.cpp

# 7.159 helib::ThinEvalMap Class Reference

Class that provides the functionality for the linear transforms used in "thin" boostrapping, where slots are assumed to contain constants. The interface is exactly the same as for EvalMap, except that the constructor does not have a normal\_basis parameter.

```
#include <EvalMap.h>
```

#### **Public Member Functions**

- ThinEvalMap (const EncryptedArray &\_ea, bool minimal, const NTL::Vec< long > &mvec, bool \_invert, bool build\_cache)
- void upgrade ()
- · void apply (Ctxt &ctxt) const

# 7.159.1 Detailed Description

Class that provides the functionality for the linear transforms used in "thin" boostrapping, where slots are assumed to contain constants. The interface is exactly the same as for EvalMap, except that the constructor does not have a normal\_basis parameter.

#### 7.159.2 Constructor & Destructor Documentation

# 7.159.2.1 ThinEvalMap()

#### 7.159.3 Member Function Documentation

#### 7.159.3.1 apply()

#### 7.159.3.2 upgrade()

```
void helib::ThinEvalMap::upgrade ( )
```

The documentation for this class was generated from the following files:

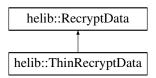
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/EvalMap.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/EvalMap.cpp

# 7.160 helib::ThinRecryptData Class Reference

Same as above, but for "thin" bootstrapping, where the slots are assumed to contain constants.

```
#include <recryption.h>
```

Inheritance diagram for helib::ThinRecryptData:



#### **Public Member Functions**

• void init (const Context &context, const NTL::Vec< long > &mvec\_, bool alsoThick, long t=0, bool build\_cache=false, bool minimal=false)

Initialize the recryption data in the context.

# **Public Attributes**

- std::shared\_ptr< const ThinEvalMap > coeffToSlot linear maps
- std::shared ptr< const ThinEvalMap > slotToCoeff

#### **Additional Inherited Members**

# 7.160.1 Detailed Description

Same as above, but for "thin" bootstrapping, where the slots are assumed to contain constants.

#### 7.160.2 Member Function Documentation

#### 7.160.2.1 init()

Initialize the recryption data in the context.

#### 7.160.3 Member Data Documentation

#### 7.160.3.1 coeffToSlot

```
\verb|std::shared_ptr<const|| ThinEvalMap>| helib::ThinRecryptData::coeffToSlot|| thinEvalMap>| thinEvalMap>| thinEvalMap>| thinEvalMap>|| thinEval
```

linear maps

#### 7.160.3.2 slotToCoeff

```
std::shared_ptr<const ThinEvalMap> helib::ThinRecryptData::slotToCoeff
```

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/recryption.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/recryption.cpp

# 7.161 TimingData Class Reference

# **Public Member Functions**

• TimingData (long \_m=-1)

# **Public Attributes**

- long m
- long phim
- long nSlots
- long p
- vector< LowLvlTimingData > lowLvl
- HighLvlTimingData highLvl
- OtherTimingData other

# 7.161.1 Constructor & Destructor Documentation

# 7.161.1.1 TimingData()

```
TimingData::TimingData ( long \_m = -1 ) \quad [inline], \; [explicit]
```

#### 7.161.2 Member Data Documentation

#### 7.161.2.1 highLvl

HighLvlTimingData TimingData::highLvl

#### 7.161.2.2 lowLvl

vector<LowLvlTimingData> TimingData::lowLvl

#### 7.161.2.3 m

long TimingData::m

#### 7.161.2.4 nSlots

long TimingData::nSlots

#### 7.161.2.5 other

OtherTimingData TimingData::other

#### 7.161.2.6 p

long TimingData::p

# 7.161.2.7 phim

long TimingData::phim

The documentation for this class was generated from the following file:

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/Test\_Timing.cpp

# 7.162 helib::TreeNode< T > Class Template Reference

A node in a full binary tree.

#include <permutations.h>

#### **Public Member Functions**

- TreeNode ()
- TreeNode (const T &d)
- T & getData ()
- const T & getData () const
- long getParent () const
- long getLeftChild () const
- long getRightChild () const
- long getPrev () const
- long getNext () const

# **Friends**

• class FullBinaryTree< T >

# 7.162.1 Detailed Description

```
template < typename T> class helib::TreeNode < T>
```

A node in a full binary tree.

These nodes are in a std::vector, so we use indexes rather than pointers

# 7.162.2 Constructor & Destructor Documentation

# 7.162.2.1 TreeNode() [1/2]

```
template<typename T >
helib::TreeNode ( ) [inline]
```

# 7.162.2.2 TreeNode() [2/2]

#### 7.162.3 Member Function Documentation

#### 7.162.3.1 getData() [1/2]

```
template<typename T >
T& helib::TreeNode< T >::getData ( ) [inline]
```

#### 7.162.3.2 getData() [2/2]

```
template<typename T >
const T& helib::TreeNode< T >::getData ( ) const [inline]
```

#### 7.162.3.3 getLeftChild()

```
template<typename T >
long helib::TreeNode< T >::getLeftChild ( ) const [inline]
```

# 7.162.3.4 getNext()

```
template<typename T >
long helib::TreeNode< T >::getNext ( ) const [inline]
```

#### 7.162.3.5 getParent()

```
template<typename T >
long helib::TreeNode< T >::getParent ( ) const [inline]
```

# 7.162.3.6 getPrev()

```
template<typename T >
long helib::TreeNode< T >::getPrev ( ) const [inline]
```

#### 7.162.3.7 getRightChild()

```
template<typename T >
long helib::TreeNode< T >::getRightChild ( ) const [inline]
```

# 7.162.4 Friends And Related Function Documentation

#### 7.162.4.1 FullBinaryTree < T >

```
template<typename T >
friend class FullBinaryTree< T > [friend]
```

The documentation for this class was generated from the following file:

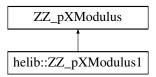
• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/permutations.h

# 7.163 helib::ZZ\_pXModulus1 Class Reference

placeholder for pXModulus ...no optimizations

```
#include <NumbTh.h>
```

Inheritance diagram for helib::ZZ\_pXModulus1:



# **Public Member Functions**

- ZZ\_pXModulus1 (UNUSED long \_m, const NTL::ZZ\_pX &\_f)
- const NTL::ZZ\_pXModulus & upcast () const

# 7.163.1 Detailed Description

placeholder for pXModulus ...no optimizations

#### 7.163.2 Constructor & Destructor Documentation

#### 7.163.2.1 ZZ pXModulus1()

#### 7.163.3 Member Function Documentation

# 7.163.3.1 upcast()

```
const NTL::ZZ_pXModulus& helib::ZZ_pXModulus1::upcast ( ) const [inline]
```

The documentation for this class was generated from the following file:

• /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/NumbTh.h

# 7.164 helib::zz\_pXModulus1 Class Reference

Auxiliary classes to facilitate faster reduction mod Phi\_m(X) when the input has degree less than m.

```
#include <NumbTh.h>
```

#### **Public Member Functions**

- zz\_pXModulus1 (long \_m, const NTL::zz\_pX &\_f)
- const NTL::zz pXModulus & upcast () const

#### **Public Attributes**

```
• long m
```

- NTL::zz\_pX f
- long n
- · bool specialLogic
- long k
- long k1
- NTL::fftRep R0
- NTL::fftRep R1
- NTL::zz\_pXModulus fm

# 7.164.1 Detailed Description

Auxiliary classes to facilitate faster reduction mod Phi\_m(X) when the input has degree less than m.

# 7.164.2 Constructor & Destructor Documentation

#### 7.164.2.1 zz\_pXModulus1()

#### 7.164.3 Member Function Documentation

#### 7.164.3.1 upcast()

```
\verb|const NTL::zz_pXModulus\&| helib::zz_pXModulus1::upcast () const [inline]| \\
```

# 7.164.4 Member Data Documentation

#### 7.164.4.1 f

NTL::zz\_pX helib::zz\_pXModulus1::f

# 7.164.4.2 fm

NTL::zz\_pXModulus helib::zz\_pXModulus1::fm

#### 7.164.4.3 k

long helib::zz\_pXModulus1::k

#### 7.164.4.4 k1

long helib::zz\_pXModulus1::k1

#### 7.164.4.5 m

long helib::zz\_pXModulus1::m

#### 7.164.4.6 n

long helib::zz\_pXModulus1::n

# 7.164.4.7 R0

NTL::fftRep helib::zz\_pXModulus1::R0

#### 7.164.4.8 R1

NTL::fftRep helib::zz\_pXModulus1::R1

### 7.164.4.9 specialLogic

bool helib::zz\_pXModulus1::specialLogic

The documentation for this class was generated from the following files:

- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/NumbTh.h
- /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/NumbTh.cpp

# **Chapter 8**

# **File Documentation**

- 8.1 mainpage.dox File Reference
- 8.2 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/
  HElib/include/helib/apiAttributes.h File
  Reference

# **Namespaces**

helib

#### **Macros**

- #define UNUSED
- 8.2.1 Macro Definition Documentation

#### 8.2.1.1 UNUSED

# 8.3 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/ HElib/include/helib/ArgMap.h File Reference

#### Easier arg parsing.

```
#include <iostream>
#include <iomanip>
#include <forward_list>
#include <initializer list>
#include <set>
#include <unordered_map>
#include <algorithm>
#include <functional>
#include <string>
#include <sstream>
#include <fstream>
#include <cctype>
#include <memory>
#include <vector>
#include <tuple>
#include <type_traits>
#include <regex>
#include <helib/assertions.h>
```

#### **Classes**

class helib::ArgMap

Basic class for arg parsing. Example use:

struct helib::ArgMap::ArgProcessor

# **Namespaces**

helib

#### 8.3.1 Detailed Description

Easier arg parsing.

# 8.4 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/ HElib/include/helib/assertions.h File Reference

Various assertion functions for use within HElib. These are meant as a replacement for C-style asserts, which (undesirably) exit the process without giving the opportunity to clean up and shut down gracefully. Instead, these functions will throw an exception if their conditions are violated.

```
#include <helib/exceptions.h>
```

#### **Namespaces**

· helib

#### **Functions**

- template<typename ExceptionTy = ::helib::LogicError, typename T = void>
   void helib::assertTrue (const T &value, const std::string &message)
- template < typename ExceptionTy = ::helib::LogicError, typename T = void> void helib::assertFalse (T value, const std::string &message)
- template < typename ExceptionTy = ::helib::LogicError, typename T = void>
   void helib::assertEq (const T &a, const T &b, const std::string &message)
- template<typename ExceptionTy = ::helib::LogicError, typename T = void>
   void helib::assertNeq (const T &a, const T &b, const std::string &message)
- template < typename ExceptionTy = ::helib::LogicError, typename T = void > void helib::assertNotNull (const T &p, const std::string &message)
- template<typename ExceptionTy = ::helib::OutOfRangeError, typename T = void>
   void helib::assertInRange (const T &elem, const T &min, const T &max, const std::string &message, bool
   right inclusive=false)

# 8.4.1 Detailed Description

Various assertion functions for use within HElib. These are meant as a replacement for C-style asserts, which (undesirably) exit the process without giving the opportunity to clean up and shut down gracefully. Instead, these functions will throw an exception if their conditions are violated.

```
General usage is of the form:
```

```
helib::assertEq(my_variable, 51, "my_variable must equal 5!");
```

Most of these functions will result in an helib::LogicError being thrown if their conditions are violated, except for assertInRange, which will throw an helib::OutOfRange. However, if one wishes to throw some other helib exception, one can specify it as a template argument as follows. For example:

```
\label{lem:helib::assertTrue} $$ helib::InvalidArgument>(some\_var > 0, "some\_var must be positive!");
```

The full set of helib exceptions can be found in exceptions.h.

# 8.5 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/ HElib/include/helib/binaryArith.h File Reference

Implementing integer addition, multiplication in binary representation.

```
#include <helib/EncryptedArray.h>
#include <helib/CtPtrs.h>
```

#### **Namespaces**

helib

#### **Functions**

std::vector < long > helib::longToBitVector (long num, long bitSize)

Returns a number as a vector of bits with LSB on the left.

void helib::binaryCond (CtPtrs &output, const Ctxt &cond, const CtPtrs &trueValue, const CtPtrs &falseValue)

Implementation of output = cond \* trueValue + (1 - cond) \* falseValue.

void helib::binaryMask (CtPtrs &binaryNums, const Ctxt &mask)

Zeroes the slots of binaryNums where the corresponding slot of mask is 0.

void helib::concatBinaryNums (CtPtrs &output, const CtPtrs &a, const CtPtrs &b)

Concatenates two binary numbers into a single CtPtrs object. E.g. If a=10111, b=00101 then output = 1011100101.

void helib::splitBinaryNums (CtPtrs &leftSplit, CtPtrs &rightSplit, const CtPtrs &input)

Splits a single binary number into two binary numbers <code>leftSplit</code> and <code>rightSplit</code>.

void helib::leftBitwiseShift (CtPtrs &output, const CtPtrs &input, const long shamt)

Left shift input by shamt.

void helib::bitwiseRotate (CtPtrs &output, const CtPtrs &input, long rotamt)

Rotate input by rotamt.

• void helib::bitwiseXOR (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise XOR between 1hs and rhs.

void helib::bitwiseOr (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise OR between 1hs and rhs.

· void helib::bitwiseAnd (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise AND between 1hs and rhs.

void helib::bitwiseAnd (CtPtrs &output, const CtPtrs &input, const std::vector < long > mask)

Compute a bitwise AND between input and a std::vector<long>.

void helib::bitwiseNot (CtPtrs &output, const CtPtrs &input)

Compute a bitwise NOT of input.

void helib::addTwoNumbers (CtPtrs &sum, const CtPtrs &lhs, const CtPtrs &rhs, long sizeLimit=0, std
 ::vector < zzX > \*unpackSlotEncoding=nullptr)

Adds two numbers in binary representation where each ciphertext of the input vector contains a bit.

• void helib::negateBinary (CtPtrs &negation, const CtPtrs &input)

Negates a number in binary 2's complement representation.

 void helib::subtractBinary (CtPtrs &difference, const CtPtrs &lhs, const CtPtrs &rhs, std::vector< zzX > \*unpackSlotEncoding=nullptr)

Subtracts rhs from 1hs where 1hs, rhs are in 2's complement.

• long helib::fifteenOrLess4Four (const CtPtrs &out, const CtPtrs &in, long sizeLimit=4)

Add together up to fifteen {0,1} integers, producing a 4-bit counter.

 void helib::addManyNumbers (CtPtrs &sum, CtPtrMat &numbers, long sizeLimit=0, std::vector< zzX > \*unpackSlotEncoding=nullptr)

Sum an arbitrary amount of numbers in binary representation.

void helib::multTwoNumbers (CtPtrs &product, const CtPtrs &lhs, const CtPtrs &rhs, bool rhsTwos
 —
 Complement=false, long sizeLimit=0, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Multiply two numbers in binary representation where each ciphertext of the input vector contains a bit.

 void helib::decryptBinaryNums (std::vector< long > &pNums, const CtPtrs &eNums, const SecKey &sKey, const EncryptedArray &ea, bool twosComplement=false, bool allSlots=true)

Decrypt the binary numbers that are encrypted in eNums.

• void helib::packedRecrypt (const CtPtrs &a, const CtPtrs &b, std::vector< zzX > \*unpackSlotEncoding)

Function for packed recryption to recrypt multiple numbers.

# 8.5.1 Detailed Description

Implementing integer addition, multiplication in binary representation.

/Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/binaryCompare.h

# File Reference 8.6 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/← HElib/include/helib/binaryCompare.h File Reference

Implementing integer comparison in binary representation.

```
#include <helib/EncryptedArray.h>
#include <helib/CtPtrs.h>
```

#### **Namespaces**

· helib

#### **Functions**

 void helib::compareTwoNumbers (CtPtrs &max, CtPtrs &min, Ctxt &mu, Ctxt &ni, const CtPtrs &a, const CtPtrs &b, bool twosComplement=false, std::vector< zzX > \*unpackSlotEncoding=nullptr)

```
Compares two integers in binary a, b. Returns max(a, b), min(a, b) and indicator bits mu=(a>b) and ni=(a<b)
```

void helib::compareTwoNumbers (Ctxt &mu, Ctxt &ni, const CtPtrs &a, const CtPtrs &b, bool twos
 — Complement=false, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Compares two integers in binary a, b. Returns only indicator bits mu=(a>b) and ni=(a<b).

#### 8.6.1 Detailed Description

Implementing integer comparison in binary representation.

# 8.7 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/ HElib/include/helib/binio.h File Reference

```
#include <iostream>
#include <vector>
#include <type_traits>
#include <NTL/xdouble.h>
#include <NTL/vec_long.h>
```

#### **Namespaces**

helib

#### **Macros**

- #define BINIO 32BIT 4
- #define BINIO 48BIT 6
- #define BINIO 64BIT 8
- #define BINIO EYE SIZE 4
- #define BINIO\_EYE\_CONTEXTBASE\_BEGIN "|BS["
- #define BINIO EYE CONTEXTBASE END "]BS|"
- #define BINIO EYE CONTEXT BEGIN "|CN["
- #define BINIO\_EYE\_CONTEXT\_END "]CN|"
- #define BINIO\_EYE\_CTXT\_BEGIN "|CX["
- #define BINIO EYE CTXT END "]CX|"
- #define BINIO\_EYE\_PK\_BEGIN "|PK["
- #define BINIO EYE PK END "]PK|"
- #define BINIO EYE SK BEGIN "|SK["
- #define BINIO EYE SK END "]SK|"
- #define BINIO\_EYE\_SKM\_BEGIN "|KM["
- #define BINIO\_EYE\_SKM\_END "]KM|"

#### **Functions**

- int helib::readEyeCatcher (std::istream &str, const char \*expect)
- void helib::writeEyeCatcher (std::ostream &str, const char \*eye)
- void helib::write\_ntl\_vec\_long (std::ostream &str, const NTL::vec\_long &vl, long intSize=BINIO 64BIT)
- void helib::read\_ntl\_vec\_long (std::istream &str, NTL::vec\_long &vl)
- long helib::read\_raw\_int (std::istream &str)
- int helib::read raw int32 (std::istream &str)
- void helib::write\_raw\_int (std::ostream &str, long num)
- void helib::write raw int32 (std::ostream &str, int num)
- void helib::write\_raw\_double (std::ostream &str, const double d)
- double helib::read\_raw\_double (std::istream &str)
- void helib::write raw xdouble (std::ostream &str, const NTL::xdouble xd)
- NTL::xdouble helib::read raw xdouble (std::istream &str)
- void helib::write\_raw\_ZZ (std::ostream &str, const NTL::ZZ &zz)
- void helib::read\_raw\_ZZ (std::istream &str, NTL::ZZ &zz)
- template<typename T >
  - void helib::write\_raw\_vector (std::ostream &str, const std::vector< T > &v)
- template<> void helib::write\_raw\_vector< long > (std::ostream &str, const std::vector< long > &v)
- template<> void helib::write\_raw\_vector< double > (std::ostream &str, const std::vector< double > &v)
- template<typename T >
- void helib::read\_raw\_vector (std::istream &str, std::vector < T > &v, T &init)
- template<typename T >
  - void helib::read\_raw\_vector (std::istream &str, std::vector< T > &v)
- template<> void helib::read\_raw\_vector< long > (std::istream &str, std::vector< long > &v)
- template<> void helib::read\_raw\_vector< double > (std::istream &str, std::vector< double > &v)
- template<typename T >
  - void helib::read\_raw\_vector (std::istream &str, std::vector< T > &v, const Context &context)

#### 8.7.1 Macro Definition Documentation

# 8.7.1.1 BINIO\_32BIT

#define BINIO\_32BIT 4

# 8.7.1.2 BINIO\_48BIT

#define BINIO\_48BIT 6

# 8.7.1.3 BINIO\_64BIT

#define BINIO\_64BIT 8

#### 8.7.1.4 BINIO\_EYE\_CONTEXT\_BEGIN

#define BINIO\_EYE\_CONTEXT\_BEGIN "|CN["

# 8.7.1.5 BINIO\_EYE\_CONTEXT\_END

#define BINIO\_EYE\_CONTEXT\_END "]CN|"

# 8.7.1.6 BINIO\_EYE\_CONTEXTBASE\_BEGIN

#define BINIO\_EYE\_CONTEXTBASE\_BEGIN "|BS["

# 8.7.1.7 BINIO\_EYE\_CONTEXTBASE\_END

#define BINIO\_EYE\_CONTEXTBASE\_END "]BS|"

# 8.7.1.8 BINIO\_EYE\_CTXT\_BEGIN

#define BINIO\_EYE\_CTXT\_BEGIN "|CX["]

# 8.7.1.9 BINIO\_EYE\_CTXT\_END

#define BINIO\_EYE\_CTXT\_END "]CX|"

# 8.7.1.10 BINIO\_EYE\_PK\_BEGIN

#define BINIO\_EYE\_PK\_BEGIN "|PK["

# 8.7.1.11 BINIO\_EYE\_PK\_END

#define BINIO\_EYE\_PK\_END "]PK|"

# 8.7.1.12 BINIO\_EYE\_SIZE

#define BINIO\_EYE\_SIZE 4

#### 8.7.1.13 BINIO EYE SK BEGIN

#define BINIO\_EYE\_SK\_BEGIN "|SK["

# 8.7.1.14 BINIO\_EYE\_SK\_END

#define BINIO\_EYE\_SK\_END "]SK|"

# 8.7.1.15 BINIO\_EYE\_SKM\_BEGIN

#define BINIO\_EYE\_SKM\_BEGIN "|KM["

# 8.7.1.16 BINIO\_EYE\_SKM\_END

 $\verb|#define BINIO_EYE_SKM_END "]KM|"$ 

# 8.8 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/ HElib/include/helib/bluestein.h File Reference

declaration of BluesteinFFT(x, n, root, powers, powers aux, Rb):

#include <helib/NumbTh.h>

#### **Namespaces**

helib

#### **Functions**

void helib::BluesteinInit (long n, const NTL::zz\_p &root, NTL::zz\_pX &powers, NTL::Vec< NTL::mulmod\_
 precon\_t > &powers\_aux, NTL::fftRep &Rb)

initialize bluestein

void helib::BluesteinFFT (NTL::zz\_pX &x, long n, const NTL::zz\_p &root, const NTL::zz\_pX &powers, const NTL::Vec< NTL::mulmod\_precon\_t > &powers\_aux, const NTL::fftRep &Rb)

apply bluestein

# 8.8.1 Detailed Description

declaration of BluesteinFFT(x, n, root, powers, powers\_aux, Rb):

Compute length-n FFT of the coefficient-vector of x (in place) If the degree of x is less than n then it treats the top coefficients as 0, if the degree of x is more than n then the extra coefficients are ignored. Similarly, if the top entries in x are zeros then x will have degree smaller than n. The argument root is a 2n-th root of unity, namely  $\frac{1}{2} \left( \frac{1}{2} \left$ 

The inverse-FFT is obtained just by calling BluesteinFFT(...  $root^{-1}$ ), but this procedure is *NOT SCALED*, so BluesteinFFT(x,n,root,...) and then BluesteinFFT(x,n,root^{-1},...) will result in x = n \* x\_original

The values powers, powers\_aux, and Rb must be precomputed by first calling BluesteinInit(n, root, powers, powers aux, Rb).

# 8.9 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/ HElib/include/helib/clonedPtr.h File Reference

Implementation of smart pointers with "deep cloning" semantics.

#### **Classes**

class helib::deep\_clone< X >

Deep copy: initialize with clone.

class helib::shallow\_clone< X >

Shallow copy: initialize with copy constructor.

# **Namespaces**

helib

#### **Macros**

- #define CLONED\_PTR\_TEMPLATE\_MEMBERS(CLONED\_PTR\_TYPE)
- #define CLONED PTR DECLARE(CLONED PTR TYPE, CLONED PTR INIT)

#### **Functions**

```
    template < typename X , typename Cloner > void helib::swap (cloned_ptr< X, Cloner > &x, cloned_ptr< X, Cloner > &y)
```

template < typename X, typename Cloner > void helib::swap (copied\_ptr < X, Cloner > &x, copied\_ptr < X, Cloner > &y)

# 8.9.1 Detailed Description

Implementation of smart pointers with "deep cloning" semantics.

Based (loosely) on code from

```
http://github.com/yonat/smart_ptr/blob/master/cloned_ptr.h
```

#### 8.9.2 Macro Definition Documentation

#### 8.9.2.1 CLONED PTR DECLARE

#### 8.9.2.2 CLONED\_PTR\_TEMPLATE\_MEMBERS

#### Value:

```
template <typename Y>
CLONED_PTR_TYPE(const CLONED_PTR_TYPE<Y>& r)
{
  copy(r.ptr);
}
template <typename Y>
CLONED_PTR_TYPE& operator=(const CLONED_PTR_TYPE<Y>& r)
{
  if (this != &r) {
    delete ptr;
    copy(r.ptr);
  }
  return *this;
}
```

# 8.10 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/CModulus.h File Reference

Supports forward and backward length-m FFT transformations.

```
#include <helib/NumbTh.h>
#include <helib/PAlgebra.h>
#include <helib/bluestein.h>
#include <helib/clonedPtr.h>
```

#### **Classes**

· class helib::Cmodulus

Provides FFT and iFFT routines modulo a single-precision prime.

# **Namespaces**

• helib

# 8.10.1 Detailed Description

Supports forward and backward length-m FFT transformations.

This is a wrapper around the bluesteinFFT routines, for one modulus q.

# 8.11 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/Context.h File Reference

Keeps the parameters of an instance of the cryptosystem.

```
#include <helib/PAlgebra.h>
#include <helib/CModulus.h>
#include <helib/IndexSet.h>
#include <helib/recryption.h>
#include <helib/primeChain.h>
#include <helib/powerful.h>
#include <helib/apiAttributes.h>
#include <NTL/Lazy.h>
```

#### Classes

· class helib::Context

Maintaining the parameters.

# **Namespaces**

helib

#### **Functions**

• long helib::FindM (long k, long nBits, long c, long p, long d, long s, long chosen\_m, bool verbose=false)

Returns smallest parameter m satisfying various constraints:

• void helib::writeContextBase (std::ostream &s, const Context &context)

write [m p r gens ords] data

void helib::readContextBase (std::istream &s, unsigned long &m, unsigned long &p, unsigned long &r, std
 ::vector< long > &gens, std::vector< long > &ords)

read [m p r gens ords] data, needed to construct context

- std::unique ptr< Context > helib::buildContextFromAscii (std::istream &str)
- void helib::writeContextBaseBinary (std::ostream &str, const Context &context)

write [m p r gens ords] data

- void helib::writeContextBinary (std::ostream &str, const Context &context)
- void helib::readContextBaseBinary (std::istream &s, unsigned long &m, unsigned long &p, unsigned long &r, std::vector< long > &gens, std::vector< long > &ords)

read [m p r gens ords] data, needed to construct context

- std::unique\_ptr< Context > helib::buildContextFromBinary (std::istream &str)
- void helib::readContextBinary (std::istream &str, Context &context)
- void helib::buildModChain (Context &context, long nBits, long nDgts=3, bool willBeBootstrappable=false, long skHwt=0, long resolution=3, long bitsInSpecialPrimes=0)
- · void helib::endBuildModChain (Context &context)

#### **Variables**

• Context \* helib::activeContext = nullptr

#### 8.11.1 Detailed Description

Keeps the parameters of an instance of the cryptosystem.

# 8.12 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/CtPtrs.h File Reference

Unified interface for vector of pointers to ciphertexts.

```
#include <initializer_list>
#include <helib/Ctxt.h>
#include <helib/PtrVector.h>
#include <helib/PtrMatrix.h>
```

#### **Namespaces**

· helib

# **Typedefs**

- typedef PtrVector< Ctxt > helib::CtPtrs
- typedef PtrVector VecT< Ctxt > helib::CtPtrs VecCt
- typedef PtrVector\_vectorT< Ctxt > helib::CtPtrs\_vectorCt
- typedef PtrVector VecPt< Ctxt > helib::CtPtrs VecPt
- typedef PtrVector vectorPt< Ctxt > helib::CtPtrs vectorPt
- typedef PtrVector\_slice < Ctxt > helib::CtPtrs\_slice
- typedef PtrMatrix < Ctxt > helib::CtPtrMat
- typedef PtrMatrix\_Vec< Ctxt > helib::CtPtrMat\_VecCt
- typedef PtrMatrix vector< Ctxt > helib::CtPtrMat vectorCt
- typedef PtrMatrix\_ptVec< Ctxt > helib::CtPtrMat\_ptVecCt
- typedef PtrMatrix\_ptvector< Ctxt > helib::CtPtrMat\_ptvectorCt

#### **Functions**

- void helib::packedRecrypt (const CtPtrs &cPtrs, const std::vector < zzX > &unpackConsts, const Encrypted ← Array &ea)
- void helib::packedRecrypt (const CtPtrs & array, const std::vector < zzX > & unpackConsts, const Encrypted ← Array & ea, long belowLvl)
- void helib::packedRecrypt (const CtPtrMat &m, const std::vector < zzX > &unpackConsts, const Encrypted ←
   Array &ea, long belowLvl=LONG\_MAX)
- long helib::findMinBitCapacity (const CtPtrs &v)
- long helib::findMinBitCapacity (const CtPtrMat &m)
- long helib::findMinBitCapacity (std::initializer\_list< const CtPtrs \* > list)
- void helib::innerProduct (Ctxt &result, const CtPtrs &v1, const CtPtrs &v2)
- Ctxt helib::innerProduct (const CtPtrs &v1, const CtPtrs &v2)

#### 8.12.1 Detailed Description

Unified interface for vector of pointers to ciphertexts.

# 8.13 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/Ctxt.h File Reference

Declarations of a BGV-type ciphertext and key-switching matrices.

```
#include <cfloat>
#include <helib/DoubleCRT.h>
#include <helib/apiAttributes.h>
```

#### **Classes**

· class helib::Ptxt

An object that mimics the functionality of the Ctxt object, and acts as a convenient entry point for inputting/encoding data which is to be encrypted.

· class helib::SKHandle

A handle, describing the secret-key element that "matches" a part, of the form  $s^{\wedge}r(X^{\wedge}t)$ .

class helib::CtxtPart

One entry in a ciphertext std::vector.

class helib::Ctxt

A Ctxt object holds a single ciphertext.

#### **Namespaces**

helib

#### **Functions**

- std::ostream & helib::operator<< (std::ostream &s, const SKHandle &handle)
- std::istream & helib::operator>> (std::istream &s, CtxtPart &p)
- std::ostream & helib::operator<< (std::ostream &s, const CtxtPart &p)</li>
- void helib::totalProduct (Ctxt &out, const std::vector< Ctxt > &v)
- void helib::incrementalProduct (std::vector < Ctxt > &v)
- void helib::innerProduct (Ctxt &result, const std::vector < Ctxt > &v1, const std::vector < Ctxt > &v2)
- Ctxt helib::innerProduct (const std::vector < Ctxt > &v1, const std::vector < Ctxt > &v2)
- void helib::innerProduct (Ctxt &result, const std::vector< Ctxt > &v1, const std::vector< DoubleCRT > &v2)
   Compute the inner product of a vectors of ciphertexts and a constant vector.
- Ctxt helib::innerProduct (const std::vector < Ctxt > &v1, const std::vector < DoubleCRT > &v2)
- void helib::innerProduct (Ctxt &result, const std::vector < Ctxt > &v1, const std::vector < NTL::ZZX > &v2)
- Ctxt helib::innerProduct (const std::vector< Ctxt > &v1, const std::vector< NTL::ZZX > &v2)
- void helib::CheckCtxt (const Ctxt &c, const char \*label)

print to cerr some info about ciphertext

void helib::extractDigits (std::vector< Ctxt > &digits, const Ctxt &c, long r=0)

Extract the mod-p digits of a mod-p $^{\wedge}$ r ciphertext.

- void helib::extractDigits (std::vector < Ctxt > &digits, const Ctxt &c, long r, bool shortCut)
- void helib::extendExtractDigits (std::vector< Ctxt > &digits, const Ctxt &c, long r, long e)

#### 8.13.1 Detailed Description

Declarations of a BGV-type ciphertext and key-switching matrices.

A ciphertext is a std::vector of "ciphertext parts", each part consists of a polynomial (element of polynomial ring R\_Q) and a "handle" describing the secret-key polynomial that this part multiplies during decryption. For example:

- A "canonical" ciphertext has two parts, the first part multiplies 1 and the second multiplies the "base" secret key s.
- When you multiply two canonical ciphertexts you get a 3-part ciphertext, with parts corresponding to 1, s, and s<sup>2</sup>
- When you apply automorphism  $X->X^{\wedge}t$  to a generic ciphertext, then

- the part corresponding to 1 still remains wrt 1
- every other part corresponding to some s' will now be corresponding to the polynomial  $s'(X^{\wedge}t)$  mod Phi m(X)

This type of representation lets you in principle add ciphertexts that are defined with respect to different keys:

- For parts of the two ciphertexts that point to the same secret-key polynomial, you just add the two Double-CRT polynomials
- Parts in one ciphertext that do not have counter-part in the other ciphertext will just be included in the result intact. For example, you have the ciphertexts C1 = (a relative to 1, b relative to s) C2 = (u relative to 1, v relative to s) Then their sum will be C1+C2 = (a+u relative to 1, b relative to s, v relative to s)

Similarly, in principle you can also multiply arbitrary ciphertexts, even ones that are defined with respect to different keys, and the result will be defined with respect to the tensor product of the two keys.

The current implementation is more restrictive, however. It requires that a ciphertext has one part wrt 1, that for every r>=1 there is at most one part wrt to  $s^r(X^t)$  (for some t), and that the r's are consecutive. For example you cannot have parts wrt  $(1,s,s^3)$  without having a part wrt  $s^2$ .

It follows that you can only add/multiply ciphertexts if one of the two lists of handles is a prefix of the other. For example, one can add a ciphertext wrt  $(1,s(X^2))$  to another wrt  $(1,s(X^2),s^2(X^2))$ , but not to another ciphertext wrt (1,s).

# 8.14 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/debugging.h File Reference

#### debugging utilities

```
#include <iostream>
#include <string>
#include <NTL/ZZX.h>
#include <helib/NumbTh.h>
```

# **Namespaces**

helib

#### **Macros**

- #define FLAG PRINT ZZX 1
- #define FLAG PRINT POLY 2
- #define FLAG PRINT VEC 4 /\* decode to ZZX \*/
- #define FLAG PRINT DVEC 8 /\* decode to double float \*/
- #define FLAG\_PRINT\_XVEC 16 /\* decode to complex numbers \*/

#### **Functions**

void helib::setupDebugGlobals (SecKey \*debug\_key, const std::shared\_ptr< const EncryptedArray > &debug ea, NTL::ZZX debug ptxt=NTL::ZZX{})

Setup function for setting up the global debug variables.

· void helib::cleanupDebugGlobals ()

Cleanup function for clearing the global debug variables.

- void helib::decryptAndPrint (std::ostream &s, const Ctxt &ctxt, const SecKey &sk, const EncryptedArray &ea, long flags=0)
- NTL::xdouble helib::embeddingLargestCoeff (const Ctxt &ctxt, const SecKey &sk)
- double helib::realToEstimatedNoise (const Ctxt &ctxt, const SecKey &sk)
- void helib::checkNoise (const Ctxt &ctxt, const SecKey &sk, const std::string &msg, double thresh=10.0)
- bool helib::decryptAndCompare (const Ctxt &ctxt, const SecKey &sk, const EncryptedArray &ea, const PlaintextArray &pa)
- void helib::rawDecrypt (NTL::ZZX &plaintxt, const std::vector < NTL::ZZX > &zzParts, const DoubleCRT &s ← Key, long q=0)
- template<typename VEC >
   std::ostream & helib::printVec (std::ostream &s, const VEC &v, long nCoeffs=40)
- std::ostream & helib::printZZX (std::ostream &s, const NTL::ZZX &poly, long nCoeffs=40)

#### **Variables**

- SecKey \* helib::dbgKey = nullptr
- std::shared\_ptr< const EncryptedArray > helib::dbgEa = nullptr
- NTL::ZZX helib::dbg\_ptxt

# 8.14.1 Detailed Description

debugging utilities

#### 8.14.2 Macro Definition Documentation

# 8.14.2.1 FLAG\_PRINT\_DVEC

#define FLAG\_PRINT\_DVEC 8 /\* decode to double float \*/

# 8.14.2.2 FLAG\_PRINT\_POLY

#define FLAG\_PRINT\_POLY 2

#### 8.14.2.3 FLAG\_PRINT\_VEC

```
\#define FLAG_PRINT_VEC 4 /* decode to ZZX */
```

# 8.14.2.4 FLAG\_PRINT\_XVEC

```
#define FLAG_PRINT_XVEC 16 /* decode to complex numbers */
```

#### 8.14.2.5 FLAG\_PRINT\_ZZX

```
#define FLAG_PRINT_ZZX 1
```

# 8.15 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/DoubleCRT.h File Reference

Integer polynomials (elements in the ring R\_Q) in double-CRT form.

```
#include <helib/zzX.h>
#include <helib/NumbTh.h>
#include <helib/IndexMap.h>
#include <helib/timing.h>
```

#### **Classes**

• class helib::DoubleCRTHelper

A helper class to enforce consistency within an DoubleCRTHelper object.

· class helib::DoubleCRT

Implementing polynomials (elements in the ring  $R\_Q$ ) in double-CRT form.

# **Namespaces**

helib

# **Typedefs**

- typedef std::shared\_ptr< DoubleCRT > helib::DCRTptr
- $\bullet \ \ typedef \ std::shared\_ptr< NTL::ZZX > \\ \underline{helib::ZZXptr}$

#### **Functions**

- void helib::conv (DoubleCRT &d, const NTL::ZZX &p)
- void helib::conv (NTL::ZZX &p, const DoubleCRT &d)
- NTL::ZZX helib::to\_ZZX (const DoubleCRT &d)

# 8.15.1 Detailed Description

Integer polynomials (elements in the ring R Q) in double-CRT form.

# 8.16 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/EncryptedArray.h File Reference

Data-movement operations on encrypted arrays of slots.

```
#include <exception>
#include <cmath>
#include <complex>
#include <NTL/Lazy.h>
#include <NTL/pair.h>
#include <NTL/SmartPtr.h>
#include <helib/DoubleCRT.h>
#include <helib/Context.h>
#include <helib/Ctxt.h>
#include <helib/Keys.h>
```

# Classes

· class helib::EncryptedArrayBase

virtual class for data-movement operations on arrays of slots

class helib::EncryptedArrayDerived< type >

 ${\it Derived concrete implementation of } {\it Encrypted Array Base}.$ 

class helib::EncryptedArrayCx

A different derived class to be used for the approximate-numbers scheme.

· class helib::EncryptedArray

A simple wrapper for a smart pointer to an EncryptedArrayBase. This is the interface that higher-level code should use.

- · class helib::PlaintextArrayBase
- class helib::PlaintextArrayDerived< type >
- · class helib::PlaintextArray

#### **Namespaces**

helib

- #define PA BOILER
- #define CPA BOILER

## **Typedefs**

typedef std::complex < double > helib::cx\_double

#### **Functions**

- template<typename RX, typename RXModulus >
   void helib::plaintextAutomorph (RX &bb, const RX &a, long k, long m, const RXModulus &PhimX)
- template<typename RX, typename type >
   void helib::plaintextAutomorph (RX &b, const RX &a, long i, long j, const EncryptedArrayDerived< type >
   &ea)
- EncryptedArrayBase \* helib::buildEncryptedArray (const Context &context, const PAlgebraMod &alMod, const NTL::ZZX &G=NTL::ZZX::zero())

A "factory" for building EncryptedArrays.

- std::ostream & helib::operator<< (std::ostream &s, const PlaintextArray &pa)
- void helib::rotate (const EncryptedArray &ea, PlaintextArray &pa, long k)
- void helib::shift (const EncryptedArray &ea, PlaintextArray &pa, long k)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, const std::vector < long > &array)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, const std::vector < NTL::ZZX > &array)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, long val)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, const NTL::ZZX &val)
- void helib::random (const EncryptedArray &ea, PlaintextArray &pa)
- void helib::decode (const EncryptedArray &ea, std::vector < long > &array, const PlaintextArray &pa)
- void helib::decode (const EncryptedArray &ea, std::vector < NTL::ZZX > &array, const PlaintextArray &pa)
- bool helib::equals (const EncryptedArray &ea, const PlaintextArray &pa, const PlaintextArray &other)
- bool helib::equals (const EncryptedArray &ea, const PlaintextArray &pa, const std::vector < long > &other)
- bool helib::equals (const EncryptedArray &ea, const PlaintextArray &pa, const std::vector< NTL::ZZX > &other)
- void helib::add (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void helib::sub (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void helib::mul (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void helib::negate (const EncryptedArray &ea, PlaintextArray &pa)
- void helib::frobeniusAutomorph (const EncryptedArray &ea, PlaintextArray &pa, long j)
- void helib::frobeniusAutomorph (const EncryptedArray &ea, PlaintextArray &pa, const NTL::Vec < long > &vec)
- void helib::applyPerm (const EncryptedArray &ea, PlaintextArray &pa, const NTL::Vec < long > &pi)
- void helib::power (const EncryptedArray &ea, PlaintextArray &pa, long e)
- void helib::runningSums (const EncryptedArray &ea, Ctxt &ctxt)

A ctxt that encrypts  $(x_1,...,x_n)$  is replaced by an encryption of  $(y_1,...,y_n)$ , where  $y_i=sum_{j\leq i}x_j$ .

## 8.16.1 Detailed Description

Data-movement operations on encrypted arrays of slots.

### 8.16.2 Macro Definition Documentation

### 8.16.2.1 CPA\_BOILER

```
#define CPA_BOILER
```

#### Value:

```
const PAlgebraModDerived<type>& tab = ea.getTab();
UNUSED const RX& G = ea.getG();
UNUSED long n = ea.size();
UNUSED long d = ea.getDegree();
const std::vector<RX>& data = pa.getData<type>();
RBak bak;
bak.save();
tab.restoreContext();
```

### 8.16.2.2 HELIB\_MORE\_UNWRAPARGS

### 8.16.2.3 PA\_BOILER

```
#define PA_BOILER
```

#### Value:

```
const PAlgebraModDerived<type>& tab = ea.getTab();
UNUSED const RX& G = ea.getG();
UNUSED long n = ea.size();
UNUSED long d = ea.getDegree();
std::vector<RX>& data = pa.getData<type>();
RBak bak;
bak.save();
tab.restoreContext();
```

# 8.17 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/EvalMap.h File Reference

Implementing the recryption linear transformations.

```
#include <helib/EncryptedArray.h>
#include <helib/matmul.h>
```

## **Classes**

· class helib::EvalMap

Class that provides the functionality for the linear transforms used in boostrapping. The constructor is invoked with three arguments:

class helib::ThinEvalMap

Class that provides the functionality for the linear transforms used in "thin" boostrapping, where slots are assumed to contain constants. The interface is exactly the same as for EvalMap, except that the constructor does not have a normal\_basis parameter.

## **Namespaces**

helib

## 8.17.1 Detailed Description

Implementing the recryption linear transformations.

# 8.18 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/exceptions.h File Reference

Various HElib-specific exception types.

```
#include <exception>
#include <stdexcept>
#include <sstream>
```

## **Classes**

· class helib::Exception

Base class that other HElib exception classes inherit from.

class helib::LogicError

Inherits from Exception and std::logic\_error.

• class helib::OutOfRangeError

Inherits from Exception and std::out\_of\_range.

class helib::RuntimeError

Inherits from Exception and std::runtime\_error.

· class helib::InvalidArgument

Inherits from Exception and std::invalid\_argument.

## **Namespaces**

## 8.18.1 Detailed Description

Various HElib-specific exception types.

This is largely a mirror image of the standard library exceptions, with the added ancestor of Exception. This allows one to distinguish between general exceptions and those specifically thrown by HElib. For example:

```
try {
    // Some code including calls to HElib
}
catch(const Exception& err) {
    // HElib error handling
}
catch(const std::exception& err) {
    // Generic error handling
```

To make sure that this is a pattern that can be used, we should only throw exceptions derived from Exception wherever possible.

# 8.19 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_⊸ v1.0.2/HElib/include/helib/FHE.h File Reference

Deprecated entry point header for HElib (legacy alias of helib.h)

```
#include <helib/helib.h>
```

# 8.19.1 Detailed Description

Deprecated entry point header for HElib (legacy alias of helib.h)

# 8.20 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/fhe\_stats.h File Reference

```
#include <vector>
#include <iostream>
```

## **Classes**

· struct helib::fhe\_stats\_record

# **Namespaces**

### **Macros**

- #define HELIB\_STATS\_UPDATE(name, val)
- #define HELIB\_STATS\_SAVE(name, val)

## **Functions**

- void helib::print\_stats (std::ostream &s)
- const std::vector< double > \* helib::fetch\_saved\_values (const char \*)

#### **Variables**

• bool helib::fhe\_stats = false

## 8.20.1 Macro Definition Documentation

## 8.20.1.1 HELIB\_STATS\_SAVE

#### Value:

```
do {
  if (fhe_stats) {
    static fhe_stats_record _local_stats_record(name);
    _local_stats_record.save(val);
  }
} while (0)
```

## 8.20.1.2 HELIB\_STATS\_UPDATE

## Value:

```
do {
  if (fhe_stats) {
    static fhe_stats_record _local_stats_record(name);
    _local_stats_record.update(val);
  }
} while (0)
```

# 8.21 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/helib.h File Reference

Entry point header for HElib.

```
#include <helib/DoubleCRT.h>
#include <helib/Context.h>
#include <helib/Ctxt.h>
#include <helib/keySwitching.h>
#include <helib/keys.h>
#include <helib/EncryptedArray.h>
#include <helib/Ptxt.h>
```

## 8.21.1 Detailed Description

Entry point header for HElib.

# 8.22 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/hypercube.h File Reference

Hypercubes and their slices.

```
#include <helib/NumbTh.h>
```

#### **Classes**

· class helib::CubeSignature

Holds a vector of dimensions for a hypercube and some additional data.

class helib::HyperCube< T >

A multi-dimensional cube.

class helib::ConstCubeSlice< T >

A constant lower-dimension slice of a hypercube.

class helib::CubeSlice< T >

A lower-dimension slice of a hypercube.

## **Namespaces**

#### **Functions**

```
• std::ostream & helib::operator<< (std::ostream &s, const CubeSignature &sig)
```

```
    template<typename T >
        void helib::getHyperColumn (NTL::Vec< T > &v, const ConstCubeSlice< T > &s, long pos)
```

```
    template<typename T >
        void helib::setHyperColumn (const NTL::Vec< T > &v, const CubeSlice< T > &s, long pos)
```

```
 \begin{tabular}{ll} \bullet & template < typename T > \\ & void & helib::setHyperColumn (const NTL::Vec < T > \&v, const CubeSlice < T > \&s, long pos, const T \&val) \\ \end{tabular}
```

```
    template < typename T > void helib::print3D (const HyperCube < T > &c)
```

# 8.22.1 Detailed Description

Hypercubes and their slices.

# 8.23 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/IndexMap.h File Reference

Implementation of a map indexed by a dynamic set of integers.

```
#include <helib/IndexSet.h>
#include <helib/clonedPtr.h>
```

#### **Classes**

```
    class helib::IndexMapInit< T >
        Initializing elements in an IndexMap.
```

class helib::IndexMap< T >

 $\textit{IndexMap}{<}\textit{T}{>}\textit{implements a generic map indexed by a dynamic index set}.$ 

# **Namespaces**

helib

#### **Functions**

```
    template<typename T >
        bool helib::operator== (const IndexMap< T > &map1, const IndexMap< T > &map2)
        Comparing maps, by comparing all the elements.
    template<typename T >
        bool helib::operator!= (const IndexMap< T > &map1, const IndexMap< T > &map2)
```

## 8.23.1 Detailed Description

Implementation of a map indexed by a dynamic set of integers.

# 8.24 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/IndexSet.h File Reference

A dynamic set of integers.

#include <helib/NumbTh.h>

#### **Classes**

· class helib::IndexSet

A dynamic set of non-negative integers.

· class helib::IndexSet::iterator

## **Namespaces**

· helib

### **Functions**

- IndexSet helib::operator (const IndexSet &s, const IndexSet &t)
- IndexSet helib::operator& (const IndexSet &s, const IndexSet &t)
- IndexSet helib::operator<sup>∧</sup> (const IndexSet &s, const IndexSet &t)
- IndexSet helib::operator/ (const IndexSet &s, const IndexSet &t)
- std::ostream & helib::operator<< (std::ostream &str, const IndexSet &set)
- std::istream & helib::operator>> (std::istream &str, IndexSet &set)
- long helib::card (const IndexSet &s)

Functional cardinality.

set minus

- bool helib::empty (const IndexSet &s)
- bool helib::operator<= (const IndexSet &s1, const IndexSet &s2)</li>

Is s1 subset or equal to s2.

• bool helib::operator< (const IndexSet &s1, const IndexSet &s2)

Is s1 strict subset of s2.

• bool helib::operator>= (const IndexSet &s1, const IndexSet &s2)

Is s2 subset or equal to s2.

bool helib::operator> (const IndexSet &s1, const IndexSet &s2)

Is s2 strict subset of s1.

bool helib::disjoint (const IndexSet &s1, const IndexSet &s2)

Functional disjoint.

## 8.24.1 Detailed Description

A dynamic set of integers.

# 8.25 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/intraSlot.h File Reference

Packing/unpacking of mod-p integers in GF(p^d) slots.

```
#include <NTL/BasicThreadPool.h>
#include <helib/Context.h>
#include <helib/EncryptedArray.h>
#include <helib/Ctxt.h>
#include <helib/CtPtrs.h>
```

## **Namespaces**

helib

#### **Functions**

- void helib::buildUnpackSlotEncoding (std::vector < zzX > &unpackSlotEncoding, const EncryptedArray &ea)
- void helib::unpack (const CtPtrs &unpacked, const Ctxt &packed, const EncryptedArray &ea, const std
   ::vector < zzX > &unpackSlotEncoding)
- long helib::unpack (const CtPtrs &unpacked, const CtPtrs &packed, const EncryptedArray &ea, const std

  ::vector< zzX > &unpackSlotEncoding)
- void helib::repack (Ctxt &packed, const CtPtrs &unpacked, const EncryptedArray &ea)
- long helib::repack (const CtPtrs &packed, const CtPtrs &unpacked, const EncryptedArray &ea)
- void helib::unpackSlots (std::vector< unsigned long > &value, PlaintextArray &pa, const EncryptedArray &ea)
- void helib::unpackSlots (std::vector< unsigned long > &value, NTL::ZZX &pa, const EncryptedArray &ea)
- void helib::packConstant (zzX &result, unsigned long data, long nbits, const EncryptedArray &ea)
- void helib::packConstants (zzX &result, const std::vector< unsigned long > &data, long nbits, const EncryptedArray &ea)

## 8.25.1 Detailed Description

Packing/unpacking of mod-p integers in  $GF(p^{\wedge}d)$  slots.

# 8.26 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/keys.h File Reference

· Declaration of public key

#include <helib/keySwitching.h>

#### **Classes**

class helib::PubKey
 The public key.

 class helib::SecKey
 The secret key.

## **Namespaces**

helib

#### **Macros**

- #define HELIB KSS UNKNOWN (0)
- #define HELIB\_KSS\_FULL (1)
- #define HELIB\_KSS\_BSGS (2)
- #define HELIB\_KSS\_MIN (3)

#### **Functions**

- void helib::writePubKeyBinary (std::ostream &str, const PubKey &pk)
- void helib::readPubKeyBinary (std::istream &str, PubKey &pk)
- void helib::writeSecKeyBinary (std::ostream &str, const SecKey &sk)
- void helib::readSecKeyBinary (std::istream &str, SecKey &sk)
- double helib::RLWE1 (DoubleCRT &c0, const DoubleCRT &c1, const DoubleCRT &s, long p)

Same as RLWE, but assumes that c1 is already chosen by the caller.

## 8.26.1 Detailed Description

- · Declaration of public key
- · Declaration of secret key

Copyright IBM Corporation 2019 All rights reserved.

### 8.26.2 Macro Definition Documentation

## 8.26.2.1 HELIB\_KSS\_BSGS

#define HELIB\_KSS\_BSGS (2)

## 8.26.2.2 HELIB\_KSS\_FULL

#define HELIB\_KSS\_FULL (1)

## 8.26.2.3 HELIB\_KSS\_MIN

#define HELIB\_KSS\_MIN (3)

#### 8.26.2.4 HELIB\_KSS\_UNKNOWN

#define HELIB\_KSS\_UNKNOWN (0)

# 8.27 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/keySwitching.h File Reference

· Declaration of key switching matrices

```
#include <climits>
#include <helib/DoubleCRT.h>
#include <helib/Context.h>
#include <helib/Ctxt.h>
```

## Classes

· class helib::KeySwitch

Key-switching matrices.

## **Namespaces**

helib

# **Functions**

std::ostream & helib::operator<< (std::ostream &str, const KeySwitch &matrix)</li>

## Strategies for generating key-switching matrices

These functions are implemented in KeySwitching.cpp

• #define HELIB KEYSWITCH THRESH (50)

Constant defining threshold above which a baby-set/giant-step strategy is used.

• #define HELIB KEYSWITCH MIN THRESH (8)

Constant defining threshold above which a single giant step matrix is added even in HELIB\_KSS\_MIN mode. This helps in the matmul routines.

long helib::KSGiantStepSize (long D)

Function that returns number of baby steps. Used to keep this and matmul routines "in sync".

void helib::addAllMatrices (SecKey &sKey, long keyID=0)

Maximalistic approach: generate matrices  $s(X^{\wedge} e) -> s(X)$  for all e in Zm\*.

void helib::addFewMatrices (SecKey &sKey, long keyID=0)

Generate matrices so every  $s(X^{\wedge}e)$  can be reLinearized in at most two steps.

void helib::addSome1DMatrices (SecKey &sKey, long bound=HELIB\_KEYSWITCH\_THRESH, long keyID=0)

Generate some matrices of the form  $s(X^{\land}\{g^{\land}i\})->s(X)$ , but not all. For a generator g whose order is larger than bound, generate only enough matrices for the giant-step/baby-step procedures (2\*sqrt(ord(g))of them).

void helib::add1DMatrices (SecKey &sKey, long keyID=0)

Generate all matrices  $s(X^{g^{i}})-s(X)$  for generators g of Zm\*/(p) and i< ord(g). If g has different orders in Zm\* and Zm\*/(p) then generate also matrices of the form  $s(X^{g^{i}})-s(X)$ 

- void helib::addBSGS1DMatrices (SecKey &sKey, long keyID=0)
- void helib::addSomeFrbMatrices (SecKey &sKey, long bound=HELIB\_KEYSWITCH\_THRESH, long keyID=0)

Generate all/some Frobenius matrices of the form  $s(X^{\wedge}\{p^{\wedge}i\})->s(X)$ 

- void helib::addFrbMatrices (SecKey &sKey, long keyID=0)
- void helib::addBSGSFrbMatrices (SecKey &sKey, long keyID=0)
- void helib::addMinimal1DMatrices (SecKey &sKey, long keyID=0)

These routines just add a single matrix (or two, for bad dimensions)

- void helib::addMinimalFrbMatrices (SecKey &sKey, long keyID=0)
- void helib::addMatrices4Network (SecKey &sKey, const PermNetwork &net, long keyID=0)
- void helib::addTheseMatrices (SecKey &sKey, const std::set < long > &automVals, long keyID=0)

Generate specific key-switching matrices, described by the given set.

### 8.27.1 Detailed Description

- · Declaration of key switching matrices
- Other key switching-related free functions

Copyright IBM Corporation 2019 All rights reserved.

#### 8.27.2 Macro Definition Documentation

## 8.27.2.1 HELIB\_KEYSWITCH\_MIN\_THRESH

#define HELIB\_KEYSWITCH\_MIN\_THRESH (8)

Constant defining threshold above which a single giant step matrix is added even in HELIB\_KSS\_MIN mode. This helps in the matmul routines.

#### 8.27.2.2 HELIB KEYSWITCH THRESH

#define HELIB\_KEYSWITCH\_THRESH (50)

Constant defining threshold above which a baby-set/giant-step strategy is used.

# 8.28 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/matching.h File Reference

Classes and functions for max-flow in a generic graph.

#include <helib/NumbTh.h>

## Classes

· class helib::FlowEdge

An edge in a flow graph.

• class helib::LabeledEdge

A generic directed edge in a graph with some labels.

· class helib::LabeledVertex

A generic node in a graph with some labels.

· class helib::BipartitleGraph

A bipartite flow graph.

# **Namespaces**

helib

# **Typedefs**

- typedef std::unordered\_map< long, FlowEdge > helib::FNeighborList
- typedef std::vector< FNeighborList > helib::FlowGraph
- $\bullet \ \ typedef \ std:: unordered\_multimap < long, \ Labeled \ Edge > helib:: LNeighbor List$

### **Functions**

· long helib::maximum\_flow (FlowGraph &fg, long src, long sink)

## 8.28.1 Detailed Description

Classes and functions for max-flow in a generic graph.

# 8.29 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/matmul.h File Reference

some matrix / linear algenra stuff

#include <helib/EncryptedArray.h>

#### Classes

- · class helib::MatMulFull
- class helib::MatMulFull\_derived< type >
- class helib::BlockMatMulFull
- class helib::BlockMatMulFull\_derived< type >
- · class helib::MatMul1D
- class helib::MatMul1D partial< type >
- class helib::MatMul1D\_derived< type >
- class helib::BlockMatMul1D
- class helib::BlockMatMul1D\_partial< type >
- class helib::BlockMatMul1D\_derived< type >
- struct helib::ConstMultiplierCache
- class helib::MatMulExecBase
- class helib::MatMul1DExec
- class helib::BlockMatMul1DExec
- · class helib::MatMulFullExec
- · class helib::BlockMatMulFullExec

## **Namespaces**

· helib

### **Functions**

- void helib::traceMap (Ctxt &ctxt)
- void helib::mul (PlaintextArray &pa, const MatMul1D &mat)
- void helib::mul (PlaintextArray &pa, const BlockMatMul1D &mat)
- void helib::mul (PlaintextArray &pa, const MatMulFull &mat)
- void helib::mul (PlaintextArray &pa, const BlockMatMulFull &mat)

#### **Variables**

- int helib::fhe\_test\_force\_bsgs = 0
- int helib::fhe test force hoist = 0

# 8.29.1 Detailed Description

some matrix / linear algenra stuff

# 8.30 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/multicore.h File Reference

Support for multi-threaded implementations.

# **Namespaces**

helib

#### **Macros**

- #define HELIB\_atomic\_long long
- #define HELIB\_atomic\_ulong unsigned long
- #define HELIB\_MUTEX\_TYPE int
- #define HELIB\_MUTEX\_GUARD(mx) ((void)mx)

## 8.30.1 Detailed Description

Support for multi-threaded implementations.

### 8.30.2 Macro Definition Documentation

## 8.30.2.1 HELIB\_atomic\_long

#define HELIB\_atomic\_long long

### 8.30.2.2 HELIB\_atomic\_ulong

#define HELIB\_atomic\_ulong unsigned long

#### 8.30.2.3 HELIB MUTEX GUARD

### 8.30.2.4 HELIB\_MUTEX\_TYPE

#define HELIB\_MUTEX\_TYPE int

# 8.31 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/norms.h File Reference

```
#include <vector>
#include <complex>
#include <NTL/ZZX.h>
#include <NTL/xdouble.h>
#include <helib/zzX.h>
```

## **Namespaces**

helib

### **Functions**

- long helib::sumOfCoeffs (const zzX &f)
- NTL::ZZ helib::sumOfCoeffs (const NTL::ZZX &f)
- NTL::ZZ helib::sumOfCoeffs (const DoubleCRT &f)
- template<typename T >
   double helib::largestCoeff (const NTL::Vec< T > &f)

The L-infinity norm of an element (in coefficient representation)

- template < typename T > double helib::largestCoeff (const std::vector < T > &f)
- NTL::ZZ helib::largestCoeff (const NTL::ZZX &f)
- NTL::ZZ helib::largestCoeff (const NTL::Vec< NTL::ZZ > &f)
- NTL::ZZ helib::largestCoeff (const DoubleCRT &f)
- double helib::coeffsL2NormSquared (const zzX &f)

The L2-norm of an element (in coefficient representation)

- NTL::xdouble helib::coeffsL2NormSquared (const NTL::ZZX &f)
- NTL::xdouble helib::coeffsL2NormSquared (const DoubleCRT &f)
- double helib::coeffsL2Norm (const zzX &f)
- NTL::xdouble helib::coeffsL2Norm (const NTL::ZZX &f)
- NTL::xdouble helib::coeffsL2Norm (const DoubleCRT &f)
- double helib::embeddingLargestCoeff (const zzX &f, const PAlgebra &palg)
- double helib::embeddingLargestCoeff (const std::vector< double > &f, const PAlgebra &palg)
- void helib::embeddingLargestCoeff\_x2 (double &norm1, double &norm2, const std::vector< double > &f1, const std::vector< double > &f2, const PAlgebra &palg)
- NTL::xdouble helib::embeddingLargestCoeff (const NTL::ZZX &f, const PAlgebra &palg)
- void helib::CKKS canonicalEmbedding (std::vector< cx double > &v, const zzX &f, const PAlgebra &palg)
- void helib::CKKS\_canonicalEmbedding (std::vector< cx\_double > &v, const NTL::ZZX &f, const PAlgebra &palg)
- void helib::CKKS\_canonicalEmbedding (std::vector< cx\_double > &v, const std::vector< double > &f, const PAlgebra &palg)
- void helib::CKKS\_embedInSlots (zzX &f, const std::vector< cx\_double > &v, const PAlgebra &palg, double scaling)

## 8.31.1 Detailed Description

· computing various norms of ring elements

# 8.32 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/NumbTh.h File Reference

Miscellaneous utility functions.

```
#include <vector>
#include <set>
#include <cmath>
#include <complex>
#include <string>
#include <climits>
#include <iostream>
#include <fstream>
#include <istream>
#include <sstream>
#include <ctime>
#include <memory>
#include <unordered_map>
#include <NTL/version.h>
#include <NTL/ZZ.h>
#include <NTL/ZZX.h>
#include <NTL/ZZ p.h>
#include <NTL/ZZ pX.h>
#include <NTL/xdouble.h>
#include <NTL/mat_GF2.h>
#include <NTL/mat_GF2E.h>
#include <NTL/GF2XFactoring.h>
#include <NTL/mat_lzz_p.h>
#include <NTL/mat_lzz_pE.h>
```

```
#include <NTL/lzz_pXFactoring.h>
#include <NTL/GF2EX.h>
#include <NTL/lzz_pEX.h>
#include <NTL/FFT.h>
#include <helib/range.h>
#include <helib/assertions.h>
#include <helib/apiAttributes.h>
```

#### **Classes**

· class helib::RandomState

Facility for "restoring" the NTL PRG state.

class helib::zz\_pXModulus1

Auxiliary classes to facilitate faster reduction mod Phi m(X) when the input has degree less than m.

class helib::ZZ pXModulus1

placeholder for pXModulus ...no optimizations

## **Namespaces**

- · helib
- · helib::FHEglobals

#### **Macros**

• #define ERFC\_INVERSE\_SIZE (long(sizeof(erfc\_inverse) / sizeof(erfc\_inverse[0])))

# **Typedefs**

· typedef long helib::LONG

#### **Functions**

- bool helib::setDryRun (bool toWhat=true)
- bool helib::isDryRun ()
- void helib::setAutomorphVals (std::set< long > \*aVals)
- bool helib::isSetAutomorphVals ()
- void helib::recordAutomorphVal (long k)
- void helib::setAutomorphVals2 (std::set< long > \*aVals)
- bool helib::isSetAutomorphVals2 ()
- void helib::recordAutomorphVal2 (long k)
- long helib::bitSetToLong (long bits, long bitSize)

Considers bits as a vector of bits and returns the value it represents when interpreted as a n-bit 2's complement number, where n is given by bitSize.

• long helib::mcMod (long a, long b)

Routines for computing mathematically correct mod and div.

- long helib::mcDiv (long a, long b)
- long helib::balRem (long a, long q)
- double helib::fsquare (double x)

Return the square of a number as a double.

• long helib::multOrd (long p, long m)

Return multiplicative order of p modulo m, or 0 if GCD(p, m) != 1.

void helib::ppsolve (NTL::vec\_zz\_pE &x, const NTL::mat\_zz\_pE &A, const NTL::vec\_zz\_pE &b, long p, long r)

Prime power solver.

- void helib::ppsolve (NTL::vec\_GF2E &x, const NTL::mat\_GF2E &A, const NTL::vec\_GF2E &b, long p, long r)

  A version for GF2: must have p == 2 and r == 1.
- void helib::ppInvert (NTL::mat\_zz\_p &X, const NTL::mat\_zz\_p &A, long p, long r)

Compute the inverse mod  $p^{\wedge}r$  of an  $n \times n$  matrix.

- void helib::ppInvert (NTL::mat\_zz\_pE &X, const NTL::mat\_zz\_pE &A, long p, long r)
- void helib::ppInvert (NTL::mat GF2 &X, const NTL::mat GF2 &A, UNUSED long p, UNUSED long r)
- void helib::ppInvert (NTL::mat GF2E &X, const NTL::mat GF2E &A, UNUSED long p, UNUSED long r)
- void helib::buildLinPolyMatrix (NTL::mat\_zz\_pE &M, long p)
- void helib::buildLinPolyMatrix (NTL::mat GF2E &M, long p)
- void helib::buildLinPolyCoeffs (NTL::vec\_zz\_pE &C, const NTL::vec\_zz\_pE &L, long p, long r)

Combination of buildLinPolyMatrix and ppsolve.

• void helib::buildLinPolyCoeffs (NTL::vec\_GF2E &C, const NTL::vec\_GF2E &L, long p, long r)

A version for GF2: must be called with p == 2 and r == 1.

• void helib::applyLinPoly (NTL::zz\_pE &beta, const NTL::vec\_zz\_pE &C, const NTL::zz\_pE &alpha, long p)

Apply a linearized polynomial with coefficient vector C.

• void helib::applyLinPoly (NTL::GF2E &beta, const NTL::vec GF2E &C, const NTL::GF2E &alpha, long p)

A version for GF2: must be called with p == 2 and r == 1.

double helib::log2 (const NTL::xdouble &x)

Base-2 logarithm.

void helib::factorize (std::vector< long > &factors, long N)

Factoring by trial division, only works for  $N<2^{\hat{}}$  {60}, only the primes are recorded, not their multiplicity.

- void helib::factorize (std::vector< NTL::ZZ > &factors, const NTL::ZZ &N)
- void helib::factorize (NTL::Vec< NTL::Pair< long, long >> &factors, long N)

Factoring by trial division, only works for  $N<2^{\wedge}$  {60} primes and multiplicities are recorded.

void helib::pp\_factorize (std::vector < long > &factors, long N)

Prime-power factorization.

void helib::phiN (long &phiN, std::vector< long > &facts, long N)

Compute Phi(N) and also factorize N.

- void helib::phiN (NTL::ZZ &phiN, std::vector< NTL::ZZ > &facts, const NTL::ZZ &N)
- long helib::phi\_N (long N)

Compute Phi(N).

- long helib::findGenerators (std::vector< long > &gens, std::vector< long > &ords, long m, long p, const std::vector< long > &candidates=std::vector< long >())
- void helib::FindPrimitiveRoot (NTL::zz\_p &r, unsigned long e)

Find e-th root of unity modulo the current modulus.

- void helib::FindPrimitiveRoot (NTL::ZZ p &r, unsigned long e)
- long helib::mobius (long n)

Compute mobius function (naive method as n is small).

NTL::ZZX helib::Cyclotomic (long N)

Compute cyclotomic polynomial.

• NTL::ZZX helib::makeIrredPoly (long p, long d)

Return a degree-d irreducible polynomial mod p.

long helib::primroot (long N, long phiN)

Find a primitive root modulo N.

• long helib::ord (long N, long p)

Compute the highest power of p that divides N.

bool helib::is2power (long m)

NTL::ZZX helib::RandPoly (long n, const NTL::ZZ &p)

```
    void helib::MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long q, bool abs)

    void helib::MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long q)

    NTL::ZZX helib::MulMod (const NTL::ZZX &f, long a, long q, bool abs)

    NTL::ZZX helib::MulMod (const NTL::ZZX &f, long a, long q)

    void helib::balanced_MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long q)

• template<typename T1 , typename T2 >
  void helib::convert (T1 &x1, const T2 &x2)
      A generic template that resolves to NTL's conv routine.
• template<typename T1 , typename T2 >
  void helib::convert (std::vector< T1 > &v1, const std::vector< T2 > &v2)
      generic vector conversion routines
• template<typename T1 , typename T2 >
  void helib::convert (std::vector < T1 > &v1, const NTL::Vec < T2 > &v2)

    template<typename T1, typename T2 >

  void helib::convert (NTL::Vec< T1 > &v1, const std::vector< T2 > &v2)

    template<typename T >

  void helib::convert (std::vector< T > &v1, const std::vector< T > &v2)
      Trivial type conversion, useful for generic code.

    template<typename T1 , typename T2 >

  T1 helib::convert (const T2 &v2)
• template<typename T >
  std::vector< T > helib::vector_replicate (const T &a, long n)

    template<typename T >

  std::vector< T > helib::Vec_replicate (const T &a, long n)

    long helib::computeProd (const NTL::Vec< long > &vec)

      returns \prod d vec[d]

    long helib::computeProd (const std::vector < long > &vec)

    void helib::mul (std::vector< NTL::ZZX > &x, const std::vector< NTL::ZZX > &a, long b)

    void helib::div (std::vector < NTL::ZZX > &x, const std::vector < NTL::ZZX > &a, long b)

    void helib::add (std::vector < NTL::ZZX > &x, const std::vector < NTL::ZZX > &a, const std::vector < NTL</li>

  ::ZZX > \&b)
• long helib::is_in (long x, int *X, long sz)
      Finds whether x is an element of the set X of size sz, Returns -1 it not and the location if true.

    long helib::CRTcoeff (long p, long q, bool symmetric=false)

      Returns a CRT coefficient: x = (0 \mod p, 1 \mod q). If symmetric is set then x \ln [-pq/2, pq/2), else x \ln [0,pq)

    template < class zzvec >

  bool helib::intVecCRT (NTL::vec_ZZ &vp, const NTL::ZZ &p, const zzvec &vq, long q)
      Incremental integer CRT for vectors.

    template<typename T, bool maxFlag>

  long helib::argminmax (std::vector < T > &v)
      Find the index of the (first) largest/smallest element.

    template<typename T >

  long helib::argmax (std::vector< T > &v)

    template<typename T >

  long helib::argmin (std::vector< T > &v)

    long helib::argmax (std::vector< long > &v, bool(*moreThan)(long, long))

      A variant with a specialized comparison function (*moreThan)(a,b) returns the comparison a>b.

    bool helib::closeToOne (const NTL::xdouble &x, long p)

• std::pair< long, long > helib::rationalApprox (double x, long denomBound=0)

    std::pair < NTL::ZZ, NTL::ZZ > helib::rationalApprox (NTL::xdouble x, NTL::xdouble denomBound=NTL←

  ::xdouble(0.0))

    void helib::seekPastChar (std::istream &str, int cc)
```

```
Advance the input stream beyond white spaces and a single instance of the char cc.
• template<typename T >
  void helib::reverse (NTL::Vec< T > &v, long lo, long hi)
     Reverse a vector in place.
template<typename T >
  void helib::rotate (NTL::Vec< T > &v, long k)
     Rotate a vector in place using swaps.

    template<tvpename T >

  long helib::lsize (const std::vector< T > &v)
     Size of STL vector as a long (rather than unsigned long)
• template<typename T >
  void helib::killVec (std::vector< T > &vec)
     NTL/std compatibility.
• template<typename T >
  void helib::killVec (NTL::Vec< T > &vec)
• template<typename T >
  void helib::setLengthZero (std::vector< T > &vec)
template<typename T >
  void helib::setLengthZero (NTL::Vec< T > &vec)
• template<typename T >
  long helib::lsize (const NTL::Vec< T > &v)
• template<typename T >
  void helib::resize (NTL::Vec< T > &v, long sz, const T &val)
• template<typename T >
  void helib::resize (std::vector< T > &v, long sz, const T &val)
• template<typename T >
  void helib::resize (NTL::Vec< T > &v, long sz)
• template<typename T >
  void helib::resize (std::vector< T > &v, long sz)
• template<typename T1 , typename T2 >
  bool helib::sameObject (const T1 *p1, const T2 *p2)
      Testing if two vectors point to the same object.

    void helib::ModComp (NTL::ZZX &res, const NTL::ZZX &g, const NTL::ZZX &h, const NTL::ZZX &f)

     Modular composition of polynomials: res = g(h) \mod f.

    long helib::polyEvalMod (const NTL::ZZX &poly, long x, long p)

     Evaluates a modular integer polynomial, returns poly(x) mod p.

    void helib::interpolateMod (NTL::ZZX &poly, const NTL::vec_long &x, const NTL::vec_long &y, long p, long

  e=1)
     Interpolate polynomial such that poly(x[i] \mod p) = y[i] \pmod{p^e} It is assumed that the points x[i] are all distinct modulo

    long helib::divc (long a, long b)

     returns ceiling(a/b); assumes a >=0, b>0, a+b <= MAX_LONG

    void helib::rem (NTL::zz pX &r, const NTL::zz pX &a, const zz pXModulus1 &ff)

    template<typename T >

  std::ostream & helib::operator<< (std::ostream &s, std::vector< T > v)

    template<typename T >

  std::istream & helib::operator>> (std::istream &s, std::vector< T > &v)
• template<typename T >
 std::string helib::vecToStr (const std::vector< T > &v)

    template<typename T >

 NTL::Vec< T > helib::atoVec (const char *a)
• template<typename T >
  std::vector < T > helib::atovector (const char *a)

    void helib::TofftRep_trunc (NTL::fftRep &y, const NTL::zz_pX &x, long k, UNUSED long len, long lo, long hi)
```

- void helib::TofftRep\_trunc (NTL::fftRep &y, const NTL::zz\_pX &x, long k, long len)
- template < typename T, typename P, typename... Args > void helib::make\_lazy (const NTL::Lazy < T, P > &obj, Args &&... args)
- template<typename T, typename P, typename F, typename... Args>
   void helib::make\_lazy\_with\_fun (const NTL::Lazy< T, P > &obj, F f, Args &&... args)
- void helib::Warning (const char \*msg)
- void helib::Warning (const std::string &msg)

#### **Variables**

- · const long double helib::PI
- bool helib::FHEglobals::dryRun = false

A dry-run flag The dry-run option disables most operations, to save time. This lets us quickly go over the evaluation of a circuit and estimate the resulting noise magnitude, without having to actually compute anything.

std::set< long > \* helib::FHEglobals::automorphVals = nullptr

A list of required automorphisms When non-nullptr, causes Ctxt::smartAutomorphism to just record the requested automorphism rather than actually performing it. This can be used to get a list of needed automorphisms for certain operations and then generate all these key-switching matrices. Should only be used in conjunction with dryRun=true.

- std::set< long > \* helib::FHEglobals::automorphVals2 = nullptr
- const double helib::erfc\_inverse []
- void helib::PolyRed (NTL::ZZX &out, const NTL::ZZX &in, long q, bool abs=false)

Reduce all the coefficients of a polynomial modulo q.

- void helib::PolyRed (NTL::ZZX &out, const NTL::ZZX &in, const NTL::ZZ &q, bool abs=false)
- void helib::PolyRed (NTL::ZZX &F, long q, bool abs=false)
- void helib::PolyRed (NTL::ZZX &F, const NTL::ZZ &q, bool abs=false)
- void helib::vecRed (NTL::Vec < NTL::ZZ > &out, const NTL::Vec < NTL::ZZ > &in, long q, bool abs)
- void helib::vecRed (NTL::Vec< NTL::ZZ > &out, const NTL::Vec< NTL::ZZ > &in, const NTL::ZZ &q, bool abs)

#### Some enhanced conversion routines

- void helib::convert (long &x1, const NTL::GF2X &x2)
- void helib::convert (long &x1, const NTL::zz pX &x2)
- void helib::convert (NTL::vec\_zz\_pE &X, const std::vector< NTL::ZZX > &A)
- void helib::convert (NTL::mat\_zz\_pE &X, const std::vector< std::vector< NTL::ZZX >> &A)
- void helib::convert (std::vector < NTL::ZZX > &X, const NTL::vec\_zz\_pE &A)
- void helib::convert (std::vector < std::vector < NTL::ZZX >> &X, const NTL::mat zz pE &A)
- void helib::convert (NTL::Vec< long > &out, const NTL::ZZX &in)
- void helib::convert (NTL::Vec < long > &out, const NTL::zz\_pX &in, bool symmetric=true)
- void helib::convert (NTL::Vec< long > &out, const NTL::GF2X &in)
- void helib::convert (NTL::ZZX &out, const NTL::Vec< long > &in)
- void helib::convert (NTL::GF2X &out, const NTL::Vec< long > &in)

#### 8.32.1 Detailed Description

Miscellaneous utility functions.

#### 8.32.2 Macro Definition Documentation

#### 8.32.2.1 ERFC INVERSE SIZE

```
#define ERFC_INVERSE_SIZE (long(sizeof(erfc_inverse) / sizeof(erfc_inverse[0])))
```

# 8.33 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/PAlgebra.h File Reference

Declarations of the classes PAlgebra.

```
#include <exception>
#include <utility>
#include <vector>
#include <complex>
#include <helib/NumbTh.h>
#include <helib/zzX.h>
#include <helib/hypercube.h>
#include <helib/PGFFT.h>
#include <helib/ClonedPtr.h>
#include <helib/apiAttributes.h>
```

#### **Classes**

- struct helib::half\_FFT
- struct helib::quarter\_FFT
- class helib::PAlgebra

The structure of (Z/mZ)\* /(p)

· class helib::PAlgebraModBase

Virtual base class for PAlgebraMod.

class helib::PAlgebraModDerived< type >

A concrete instantiation of the virtual class.

class helib::MappingData< type >

Auxiliary structure to support encoding/decoding slots.

 $\bullet \ \ {\it class\ helib::} {\it PAlgebraModDerived}{< type} >$ 

A concrete instantiation of the virtual class.

- class helib::PAlgebraModCx
- · class helib::PAlgebraMod

The structure of  $Z[X]/(Phi_m(X), p)$ 

#### **Namespaces**

### **Macros**

#define PA\_INJECT(typ)

#### **Enumerations**

enum helib::PA\_tag { helib::PA\_GF2\_tag, helib::PA\_zz\_p\_tag, helib::PA\_cx\_tag }

#### **Functions**

- PAlgebraModBase \* helib::buildPAlgebraMod (const PAlgebra &zMStar, long r)
   Builds a table, of type PA\_GF2 if p == 2 and r == 1, and PA\_zz\_p otherwise.
- bool helib::comparePAlgebra (const PAlgebra &palg, unsigned long m, unsigned long p, unsigned long r, const std::vector< long > &gens, const std::vector< long > &ords)

returns true if the palg parameters match the rest, false otherwise

double helib::calcPolyNormBnd (long m)

## 8.33.1 Detailed Description

Declarations of the classes PAlgebra.

#### 8.33.2 Macro Definition Documentation

## 8.33.2.1 PA\_INJECT

```
#define PA_INJECT( typ )
```

### Value:

```
static const PA_tag tag = typ::tag;
typedef typename typ::R R;
typedef typename typ::RX RX;
typedef typename typ::RX MX;
typedef typename typ::RXModulus RXModulus;
typedef typename typ::REABA RBak;
typedef typename typ::RContext RContext;
typedef typename typ::RE RE;
typedef typename typ::RE RE;
typedef typename typ::MT RE MT.
typedef typename typ::MT.
typedef typename typ::MT.
typedef typename typ::REX REX;
typedef typename typ::REBak REBak;
typedef typename typ::REBak REBak;
typedef typename typ::Vec_REX Vec_REX;
typedef typename typ::MT.
typedef typename type:MT.
typedef typename typename type:MT.
typedef typename typename type:MT.
typedef typename type:MT.
typedef typename typename type:MT.
typedef typename typ
```

# 8.34 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/permutations.h File Reference

Permutations over Hypercubes and their slices.

```
#include <helib/PAlgebra.h>
#include <helib/matching.h>
#include <helib/hypercube.h>
#include <helib/apiAttributes.h>
```

#### **Classes**

· class helib::ColPerm

Permuting a single dimension (column) of a hypercube.

· class helib::GeneralBenesNetwork

Implementation of generalized Benes Permutation Network.

· class helib::FullBinaryTree

A simple implementation of full binary trees (each non-leaf has 2 children)

class helib::TreeNode< T >

A node in a full binary tree.

• class helib::FullBinaryTree

A simple implementation of full binary trees (each non-leaf has 2 children)

· class helib::GenDescriptor

A minimal description of a generator for the purpose of building tree.

• class helib::SubDimension

A node in a tree relative to some generator.

class helib::GeneratorTrees

A std::vector of generator trees, one per generator in Zm\*/(p)

· class helib::PermNetLayer

The information needed to apply one layer of a permutation network.

class helib::PermNetwork

A full permutation network.

## **Namespaces**

helib

## **Typedefs**

 $\bullet \ \ \mathsf{typedef} \ \mathsf{NTL} \\ \mathsf{::Vec} \\ < \mathsf{long} \\ > \\ \mathsf{helib} \\ \mathsf{::Permut} \\$ 

A simple permutation is just a vector with p[i]=\pi\_i.

 $\bullet \ \ type def \ Full Binary Tree < SubDimension > helib:: One Generator Tree \\$ 

#### **Functions**

```
    template<typename T >
        void helib::applyPermToVec (NTL::Vec< T > &out, const NTL::Vec< T > &in, const Permut &p1)
        Apply a permutation to a std::vector, out[i]=in[p1[i]] (NOT in-place)
```

template<typename T >
 void helib::applyPermToVec (std::vector< T > &out, const std::vector< T > &in, const Permut &p1)

template<typename T >
 void helib::applyPermsToVec (NTL::Vec< T > &out, const NTL::Vec< T > &in, const Permut &p2, const
 Permut &p1)

Apply two permutations to a std::vector out[i]=in[p2[p1[i]]] (NOT in-place)

- template<typename T >
   void helib::applyPermsToVec (std::vector< T > &out, const std::vector< T > &in, const Permut &p2, const Permut &p1)
- void helib::randomPerm (Permut &perm, long n)

A random size-n permutation.

- std::ostream & helib::operator<< (std::ostream &s, const ColPerm &p)</li>
- void helib::breakPermByDim (std::vector< ColPerm > &out, const Permut &pi, const CubeSignature &sig)

Takes a permutation pi over m-dimensional cube  $C=Z_{n1} \times ... \times Z_{m}$  and expresses pi as a product pi =  $rho_{m}$  {2m-1} o ... o  $rho_{n}$  o  $rho_{n}$  where each  $rho_{n}$  is a column permutation along one dimension. Specifically for i < m, the permutations  $rho_{n}$  i and  $rho_{n}$  {2(m-1)-i} permute the i'th dimension.

# 8.34.1 Detailed Description

Permutations over Hypercubes and their slices.

# 8.35 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/PGFFT.h File Reference

```
#include <vector>
#include <complex>
```

#### Classes

- · class helib::PGFFT
- class helib::PGFFT::aligned\_allocator< T >

### **Namespaces**

# 8.36 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/polyEval.h File Reference

Homomorphic Polynomial Evaluation.

```
#include <helib/Context.h>
#include <helib/Ctxt.h>
```

#### **Classes**

· class helib::DynamicCtxtPowers

Store powers of X, compute them dynamically as needed.

## **Namespaces**

· helib

### **Functions**

void helib::polyEval (Ctxt &ret, NTL::ZZX poly, const Ctxt &x, long k=0)

Evaluate a cleartext polynomial on an encrypted input.

void helib::polyEval (Ctxt &ret, const NTL::Vec< Ctxt > &poly, const Ctxt &x)

Evaluate an encrypted polynomial on an encrypted input.

## 8.36.1 Detailed Description

Homomorphic Polynomial Evaluation.

# 8.37 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/PolyMod.h File Reference

Underlying slot type structure of BGV ptxts.

```
#include <NTL/ZZX.h>
#include <vector>
#include <memory>
#include <helib/PolyModRing.h>
```

### **Classes**

· class helib::PolyMod

An object that contains an NTL: : ZZX polynomial along with a coefficient modulus p2r and a polynomial modulus G.

## **Namespaces**

· helib

# 8.37.1 Detailed Description

Underlying slot type structure of BGV ptxts.

# 8.38 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/PolyModRing.h File Reference

Definition of the plaintext slot algebraic ring.

```
#include <NTL/ZZX.h>
#include <NTL/ZZ_p.h>
#include <vector>
```

## **Classes**

• struct helib::PolyModRing

Lightweight type for describing the structure of a single slot of the plaintext space.

## **Namespaces**

• helib

## 8.38.1 Detailed Description

Definition of the plaintext slot algebraic ring.

# 8.39 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/powerful.h File Reference

The "powerful basis" of a cyclotomic ring.

```
#include <helib/NumbTh.h>
#include <helib/clonedPtr.h>
#include <helib/bluestein.h>
#include <helib/hypercube.h>
#include <helib/DoubleCRT.h>
#include <helib/Context.h>
```

#### **Classes**

• class helib::PowerfulTranslationIndexes

Holds index tables for translation between powerful and zz pX.

· class helib::PowerfulConversion

Conversion between powerful representation in R\_m/(q) and zz\_pX.

· class helib::PowerfulDCRT

Conversion between powerful representation, DoubleCRT, and ZZX.

# **Namespaces**

• helib

# 8.39.1 Detailed Description

The "powerful basis" of a cyclotomic ring.

# 8.40 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/primeChain.h File Reference

handling the chain of moduli

```
#include <vector>
#include <helib/IndexSet.h>
```

#### **Classes**

· class helib::ModuliSizes

A helper class to map required modulo-sizes to primeSets.

## **Namespaces**

helib

#### **Functions**

- std::ostream & helib::operator<< (std::ostream &s, const ModuliSizes::Entry &e)</li>
- std::istream & helib::operator>> (std::istream &s, ModuliSizes::Entry &e)
- void helib::write (std::ostream &s, const ModuliSizes::Entry &e)
- void helib::read (std::istream &s, ModuliSizes::Entry &e)

## 8.40.1 Detailed Description

handling the chain of moduli

# 8.41 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/PtrMatrix.h File Reference

Convenience class templates providing a unified interface for a matrix of objects, returning pointers to these objects.

```
#include <initializer_list>
#include <helib/PtrVector.h>
```

#### **Classes**

```
    struct helib::PtrMatrix< T >
```

An abstract class for an array of PtrVectors.

struct helib::PtrMatrix Vec< T >

An implementation of PtrMatrix using Vec< Vec<T>>

struct helib::PtrMatrix\_ptVec< T >

An implementation of PtrMatrix using Vec< Vec<T>\*>

struct helib::PtrMatrix\_vector< T >

An implementation of PtrMatrix using vector< vector< T>>

struct helib::PtrMatrix\_ptvector< T >

An implementation of PtrMatrix using vector< vector< T>\*>

## **Namespaces**

#### **Functions**

```
    template<typename T >
        long helib::Isize (const PtrMatrix< T > &v)
    template<typename T >
        void helib::resize (PtrMatrix< T > &v, long newSize)
    template<typename T >
        void helib::setLengthZero (PtrMatrix< T > &v)
    template<typename T >
        const T * helib::ptr2nonNull (std::initializer list< const PtrVector< T > * > list)
```

## 8.41.1 Detailed Description

Convenience class templates providing a unified interface for a matrix of objects, returning pointers to these objects.

# 8.42 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/PtrVector.h File Reference

Convenience class templates providing a unified interface for a collection of objects, returning pointers to these objects.

```
#include <stdexcept>
#include <climits>
#include <vector>
#include <NTL/vector.h>
#include <helib/assertions.h>
#include <helib/apiAttributes.h>
```

## Classes

## **Namespaces**

helib

### **Functions**

```
• template<typename T >
  long helib::lsize (const PtrVector< T > &v)
• template<typename T >
  void helib::setLengthZero (PtrVector< T > &v)
• template<typename T >
 void helib::resize (PtrVector< T > &v, long newSize, const T &val)
• template<typename T >
 void helib::resize (PtrVector< T > &v, long newSize, const T *val)

    template<typename V1 , typename V2 >

 void helib::vecCopy (V1 &v1, const V2 &v2, long sizeLimit=0)
• template<typename V , typename T >
 void helib::vecCopy (V &v1, const PtrVector< T > &v2, long sizeLimit=0)
• template<typename V, typename T >
  void helib::vecCopy (PtrVector< T > &v1, const V &v2, long sizeLimit=0)

    template<typename T >

  void helib::vecCopy (PtrVector< T > &v1, const PtrVector< T > &v2, long sizeLimit=0)
```

## 8.42.1 Detailed Description

Convenience class templates providing a unified interface for a collection of objects, returning pointers to these objects.

# 8.43 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/include/helib/Ptxt.h File Reference

Plaintext object parameterised on CKKS and BGV schemes. Also contains definition of CKKS and BGV structs.

```
#include <type_traits>
#include <vector>
#include <algorithm>
#include <numeric>
#include <iomanip>
#include <helib/Context.h>
#include <helib/EncryptedArray.h>
#include <helib/assertions.h>
#include <helib/PolyMod.h>
```

#### Classes

struct helib::CKKS

Type for CKKS scheme, to be used as template parameter.

struct helib::BGV

Type for BGV scheme, to be used as template parameter.

class helib::Ptxt

An object that mimics the functionality of the Ctxt object, and acts as a convenient entry point for inputting/encoding data which is to be encrypted.

helib

#### **Functions**

template < typename From , typename Scheme >
 std::vector < typename Scheme::SlotType > helib::convertDataToSlotVector (const std::vector < From >
 &data, const Context &context)

Converts std::vector<From> to std::vector<Scheme::SlotType>.

template<typename Scheme >
 void helib::innerProduct (Ptxt< Scheme > &result, const std::vector< Ptxt< Scheme >> &first\_vec, const std::vector< Ptxt< Scheme >> &second\_vec)

Free function that computes the inner product of two vectors of Ptxt.

## 8.43.1 Detailed Description

Plaintext object parameterised on CKKS and BGV schemes. Also contains definition of CKKS and BGV structs.

# 8.44 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_→ v1.0.2/HElib/include/helib/randomMatrices.h File Reference

implementation of random matrices of various forms, used for testing

```
#include <helib/matmul.h>
#include <NTL/BasicThreadPool.h>
```

#### **Classes**

- class helib::RandomMatrix< type >
- class helib::RandomMultiMatrix< type >
- $\bullet \ \, {\it class helib::} \\ {\it RandomBlockMatrix} < {\it type} >$
- class helib::RandomMultiBlockMatrix< type >
- class helib::RandomFullMatrix< type >
- class helib::RandomFullBlockMatrix< type >

#### **Namespaces**

helib

## **Functions**

- MatMul1D \* helib::buildRandomMatrix (const EncryptedArray &ea, long dim)
- MatMul1D \* helib::buildRandomMultiMatrix (const EncryptedArray &ea, long dim)
- BlockMatMul1D \* helib::buildRandomBlockMatrix (const EncryptedArray &ea, long dim)
- BlockMatMul1D \* helib::buildRandomMultiBlockMatrix (const EncryptedArray &ea, long dim)
- MatMulFull \* helib::buildRandomFullMatrix (const EncryptedArray &ea)
- BlockMatMulFull \* helib::buildRandomFullBlockMatrix (const EncryptedArray &ea)

# 8.44.1 Detailed Description

implementation of random matrices of various forms, used for testing

# 8.45 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/range.h File Reference

### **Classes**

- class helib::general\_range< T >
- class helib::general\_range< T >::iterator

## **Namespaces**

helib

### **Functions**

- general\_range < long > helib::range (long n)
- general\_range < long > helib::range (long m, long n)

# 8.46 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/recryption.h File Reference

Define some data structures to hold recryption data.

```
#include <helib/NumbTh.h>
```

### **Classes**

· class helib::RecryptData

A structure to hold recryption-related data inside the Context.

· class helib::ThinRecryptData

Same as above, but for "thin" bootstrapping, where the slots are assumed to contain constants.

## **Namespaces**

#### **Macros**

• #define HELIB\_MIN\_CAP\_FRAC (2.0 / 3.0)

# **Variables**

- long helib::thinRecrypt\_initial\_level
- long helib::fhe\_force\_chen\_han = 0
- long helib::printFlag

## 8.46.1 Detailed Description

Define some data structures to hold recryption data.

## 8.46.2 Macro Definition Documentation

## 8.46.2.1 HELIB\_MIN\_CAP\_FRAC

```
#define HELIB_MIN_CAP_FRAC (2.0 / 3.0)
```

# 8.47 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/include/helib/replicate.h File Reference

Procedures for replicating a ciphertext slot across a full ciphertext.

```
#include <helib/EncryptedArray.h>
#include <helib/Ptxt.h>
```

### **Classes**

· class helib::ReplicateHandler

An abstract class to handle call-backs to get the output of replicate.

### **Namespaces**

#### **Functions**

void helib::replicate (const EncryptedArray &ea, Ctxt &ctx, long pos)

The value in slot #pos is replicated in all other slots. On an n-slot ciphertext, this algorithm performs O(log n) 1D rotations.

void helib::replicate0 (const EncryptedArray &ea, Ctxt &ctxt, long pos)

A lower-level routine. Same as replicate, but assumes all slots are zero except slot #pos.

- void helib::replicateAll (const EncryptedArray &ea, const Ctxt &ctxt, ReplicateHandler \*handler, long rec
   — Bound=64, RepAuxDim \*repAuxPtr=nullptr)
- void helib::replicateAll (std::vector< Ctxt > &v, const EncryptedArray &ea, const Ctxt &ctxt, long rec
   — Bound=64, RepAuxDim \*repAuxPtr=nullptr)
- template<typename Scheme >
   void helib::replicateAll (std::vector< Ptxt< Scheme >> &v, const EncryptedArray &, const Ptxt< Scheme >
   &ptxt)

Generate a vector of plaintexts with each slot replicated in each plaintext.

- void helib::replicateAllOrig (const EncryptedArray &ea, const Ctxt &ctxt, ReplicateHandler \*handler, RepAux \*repAuxPtr=nullptr)
- void helib::replicate (const EncryptedArray &ea, PlaintextArray &pa, long i)
- template<typename Scheme >

```
void helib::replicate (const EncryptedArray &, Ptxt< Scheme > &ptxt, long i)
```

Replicate single slot of a Ptxt object across all of its slots.

#### **Variables**

• NTL THREAD LOCAL bool helib::replicateVerboseFlag = false

## 8.47.1 Detailed Description

Procedures for replicating a ciphertext slot across a full ciphertext.

This module implements a recursive, O(1)-amortized algorithm for replications. On an input ciphertext that encrypts  $(x_1, ..., x_n)$ , we generate the n encrypted std::vectors  $(x_1, ..., x_n)$ ,  $..., (x_n, ..., x_n)$ , in that order.

To process the output std::vectors, a "call back" mechanism is used (so that we do not need to generate them all, and instead can return them one by one). For this purpose, the caller should pass a pointer to a class derived from the purely abstract class ReplicateHandler.

The replication procedures are meant to be used for linear algebra operation where a matrix-std::vector multiplication can be implemented for example by replicating each entry of the std::vector as a stand-alone ciphertext, then use the SIMD operations on these ciphertexts.

# 8.48 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/sample.h File Reference

```
#include <vector>
#include <NTL/xdouble.h>
#include <NTL/ZZX.h>
#include <NTL/ZZ_pX.h>
#include <helib/zzX.h>
```

### **Namespaces**

helib

### **Functions**

- void helib::sampleSmall (zzX &poly, long n, double prob=0.5)
- void helib::sampleSmall (NTL::ZZX &poly, long n, double prob=0.5)
- void helib::sampleHWt (zzX &poly, long n, long Hwt=100)

Sample a degree-(n-1) poly as above, with only Hwt nonzero coefficients.

- void helib::sampleHWt (NTL::ZZX &poly, long n, long Hwt=100)
- void helib::sampleGaussian (zzX &poly, long n, double stdev)

Sample polynomials with Gaussian coefficients.

- void helib::sampleGaussian (NTL::ZZX &poly, long n, double stdev)
- void helib::sampleUniform (zzX &poly, long n, long B=100)

Sample a degree-(n-1) ZZX, with coefficients uniform in [-B,B].

- void helib::sampleUniform (NTL::ZZX &poly, long n, const NTL::ZZ &B=NTL::ZZ(100L))
- void helib::sampleGaussian (std::vector< double > &dvec, long n, double stdev)

Choose a vector of continuous Gaussians.

- double helib::sampleHWt (zzX &poly, const Context &context, long Hwt=100)
- double helib::sampleHWtBounded (zzX &poly, const Context &context, long Hwt=100)
- double helib::sampleHWtBoundedEffectiveBound (const Context &context, long Hwt=100)
- double helib::sampleSmall (zzX &poly, const Context &context)
- double helib::sampleSmallBounded (zzX &poly, const Context &context)
- double helib::sampleGaussian (zzX &poly, const Context &context, double stdev)
- double helib::sampleGaussianBounded (zzX &poly, const Context &context, double stdev)
- double helib::sampleUniform (zzX &poly, const Context &context, long B=100)
- NTL::xdouble helib::sampleUniform (NTL::ZZX &poly, const Context &context, const NTL::ZZ &B=NTL::← ZZ(100L))
- void helib::reduceModPhimX (zzX &poly, const PAlgebra &palg)
- const NTL::zz\_pXModulus & helib::getPhimXMod (const PAlgebra &palg)
- double helib::boundFreshNoise (long m, long phim, double sigma, double epsilon=9e-13)
- double helib::boundRoundingNoise (long m, long phim, long p2r, double epsilon=9e-13)

# 8.48.1 Detailed Description

· implementing various sampling routines

# 8.49 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/tableLookup.h File Reference

Code for homomorphic table lookup and fixed-point functions.

```
#include <functional>
#include <helib/EncryptedArray.h>
#include <helib/CtPtrs.h>
```

# **Namespaces**

helib

### **Functions**

- void helib::computeAllProducts (CtPtrs &products, const CtPtrs &array, std::vector< zzX > \*unpackSlot←
   Encoding=nullptr)
- void helib::tableLookup (Ctxt &out, const std::vector< zzX > &table, const CtPtrs &idx, std::vector< zzX > \*unpackSlotEncoding=nullptr)
- void helib::tableWriteIn (const CtPtrs &table, const CtPtrs &idx, std::vector< zzX > \*unpackSlot ← Encoding=nullptr)
- void helib::buildLookupTable (std::vector< zzX > &T, std::function< double(double)> f, long nbits\_in, long scale\_in, long sign\_in, long nbits\_out, long scale\_out, long sign\_out, const EncryptedArray &ea)

Built a table-lookup for a function in fixed-point representation.

## 8.49.1 Detailed Description

Code for homomorphic table lookup and fixed-point functions.

# 8.50 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/timing.h File Reference

Utility functions for measuring time.

```
#include <helib/NumbTh.h>
#include <helib/multicore.h>
```

#### Classes

· class helib::FHEtimer

A simple class to accumulate time.

### **Namespaces**

helib

# **Macros**

- #define HELIB STRINGIFY(x) #x
- #define HELIB\_TOSTRING(x) HELIB\_STRINGIFY(x)
- #define HELIB AT FILE ":" HELIB TOSTRING( LINE )
- #define HELIB\_stringify\_aux(s) #s
- #define HELIB stringify(s) HELIB stringify aux(s)
- #define HELIB TIMER START
- #define HELIB\_TIMER\_STOP \_local\_auto\_timer.stop()
- #define HELIB\_NTIMER\_START(n)
- #define HELIB\_NTIMER\_STOP(n) \_named\_local\_auto\_timer##n.stop();

### **Functions**

- void helib::registerTimer (FHEtimer \*timer)
- unsigned long helib::GetTimerClock ()
- void helib::setTimersOn ()
- void helib::setTimersOff ()
- bool helib::areTimersOn ()
- const FHEtimer \* helib::getTimerByName (const char \*name)
- void helib::resetAllTimers ()
- void helib::printAllTimers (std::ostream &str=std::cerr)

Print the value of all timers to stream.

bool helib::printNamedTimer (std::ostream &str, const char \*name)

# 8.50.1 Detailed Description

Utility functions for measuring time.

This module contains some utility functions for measuring the time that various methods take to execute. To use it, we insert the macro HELIB\_TIMER\_START at the beginning of the method(s) that we want to time and HELIB — \_\_TIMER\_STOP at the end, then the main program needs to call the function setTimersOn() to activate the timers and setTimersOff() to pause them. To obtain the value of a given timer (in seconds), the application can use the function getTime4func(const char \*fncName), and the function printAllTimers() prints the values of all timers to an output stream.

Using this method we can have at most one timer per method/function, and the timer is called by the same name as the function itself (using the built-in macro \_\_func\_\_). We can also use the "lower level" methods startFH  $\leftarrow$  Etimer(name), stopFHEtimer(name), and resetFHEtimer(name) to add timers with arbitrary names (not necessarily associated with functions).

### 8.50.2 Macro Definition Documentation

### 8.50.2.1 HELIB\_AT

```
#define HELIB_AT __FILE__ ":" HELIB_TOSTRING(__LINE__)
```

# 8.50.2.2 HELIB\_NTIMER\_START

### Value:

```
static helib::FHEtimer _named_local_timer##n(#n, HELIB_AT);
helib::auto_timer _named_local_auto_timer##n(&_named_local_timer##n)
```

# 8.50.2.3 HELIB\_NTIMER\_STOP

# 8.50.2.4 HELIB\_stringify

```
\label{eq:continuity} \mbox{\#define HELIB\_stringify(} \\ s \ ) \ \mbox{HELIB\_stringify\_aux(s)}
```

### 8.50.2.5 HELIB\_STRINGIFY

```
#define HELIB_STRINGIFY( x ) \#x
```

# 8.50.2.6 HELIB\_stringify\_aux

```
#define HELIB_stringify_aux( s ) #s
```

# 8.50.2.7 HELIB\_TIMER\_START

```
#define HELIB_TIMER_START
```

#### Value:

```
static helib::FHEtimer _local_timer(__func__, HELIB_AT);
helib::auto_timer _local_auto_timer(&_local_timer)
```

# 8.50.2.8 HELIB\_TIMER\_STOP

```
#define HELIB_TIMER_STOP _local_auto_timer.stop()
```

# 8.50.2.9 HELIB\_TOSTRING

# 8.51 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/include/helib/zzX.h File Reference

```
#include <NTL/vector.h>
#include <NTL/lzz_pX.h>
#include <NTL/GF2X.h>
```

# **Namespaces**

helib

# **Typedefs**

typedef NTL::Vec< long > helib::zzX

#### **Functions**

- bool helib::IsZero (const zzX &a)
- void helib::clear (zzX &a)
- void helib::convert (NTL::zz\_pX &x, const zzX &a)
- void helib::add (zzX &res, const zzX &a, const zzX &b)
- zzX helib::operator+ (const zzX &a, const zzX &b)
- zzX & helib::operator+= (zzX &a, const zzX &b)
- void helib::div (zzX &res, const zzX &a, long b)
- zzX helib::operator/ (const zzX &a, long b)
- zzX & helib::operator/= (zzX &a, long b)
- void helib::mul (zzX &res, const zzX &a, long b)
- zzX helib::operator\* (const zzX &a, long b)
- zzX & helib::operator\*= (zzX &a, long b)
- void helib::normalize (zzX &f)
- const NTL::zz\_pXModulus & helib::getPhimXMod (const PAlgebra &palg)
- void helib::reduceModPhimX (zzX &poly, const PAlgebra &palg)
- void helib::MulMod (zzX &res, const zzX &a, const zzX &b, const PAlgebra &palg)
- zzX helib::MulMod (const zzX &a, const zzX &b, const PAlgebra &palg)
- zzX helib::balanced\_zzX (const NTL::zz\_pX &f)
- zzX helib::balanced\_zzX (const NTL::GF2X &f)

# 8.51.1 Detailed Description

• manipulating polynomials with single-precision coefficient It is assumed that the result is also single-precision

# 8.52 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/BenesNetwork.cpp File Reference

```
#include <NTL/lzz_pXFactoring.h>
#include <helib/EncryptedArray.h>
#include <cstdlib>
#include <list>
#include <sstream>
#include <memory>
#include <NTL/vector.h>
#include <helib/NumbTh.h>
#include <helib/permutations.h>
```

# **Namespaces**

• helib

# 8.53 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/binaryArith.cpp File Reference

Implementing integer addition, multiplication in binary representation.

```
#include <numeric>
#include <climits>
#include <map>
#include <algorithm>
#include <stdexcept>
#include <atomic>
#include <mutex>
#include <NTL/BasicThreadPool.h>
#include <helib/binaryArith.h>
```

### **Classes**

· class helib::DAGnode

A node in an addition-DAG structure.

class helib::ScratchCell

A class to help manage the allocation of temporary Ctxt objects.

· class helib::AddDAG

A class representing the logic of the order of bit products when adding two integers.

struct helib::PtrMatrix\_PtPtrVector< T >

An implementation of PtrMatrix using vector< PtrVector<T>\*>

### **Namespaces**

· helib

#### **Macros**

• #define BPL ESTIMATE (30)

# **Typedefs**

typedef std::pair< long, long > helib::Nodeldx

#### **Functions**

- long helib::defaultPmiddle (long delta)
- long helib::defaultQmiddle (long delta)
- void helib::packedRecrypt (const CtPtrs &a, const CtPtrs &b, std::vector < zzX > \*unpackSlotEncoding)

Function for packed recryption to recrypt multiple numbers.

std::vector< long > helib::longToBitVector (long num, long bitSize)

Returns a number as a vector of bits with LSB on the left.

void helib::binaryMask (CtPtrs &binaryNums, const Ctxt &mask)

Zeroes the slots of binaryNums where the corresponding slot of mask is 0.

• void helib::binaryCond (CtPtrs &output, const Ctxt &cond, const CtPtrs &trueValue, const CtPtrs &falseValue)

Implementation of output = cond \* trueValue + (1 - cond) \* falseValue.

void helib::concatBinaryNums (CtPtrs &output, const CtPtrs &a, const CtPtrs &b)

Concatenates two binary numbers into a single CtPtrs object. E.g. If a=10111, b=00101 then output = 1011100101.

• void helib::splitBinaryNums (CtPtrs &leftSplit, CtPtrs &rightSplit, const CtPtrs &input)

Splits a single binary number into two binary numbers leftSplit and rightSplit.

void helib::leftBitwiseShift (CtPtrs &output, const CtPtrs &input, const long shamt)

Left shift input by shamt.

void helib::bitwiseRotate (CtPtrs &output, const CtPtrs &input, long rotamt)

Rotate input by rotamt.

• void helib::bitwiseXOR (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise XOR between 1hs and rhs.

void helib::bitwiseOr (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise OR between 1hs and rhs.

· void helib::bitwiseAnd (CtPtrs &output, const CtPtrs &lhs, const CtPtrs &rhs)

Compute a bitwise AND between 1hs and rhs.

void helib::bitwiseAnd (CtPtrs &output, const CtPtrs &input, const std::vector < long > mask)

Compute a bitwise AND between input and a std::vector<long>.

void helib::bitwiseNot (CtPtrs &output, const CtPtrs &input)

Compute a bitwise NOT of input.

void helib::addTwoNumbers (CtPtrs &sum, const CtPtrs &lhs, const CtPtrs &rhs, long sizeLimit=0, std
 ::vector < zzX > \*unpackSlotEncoding=nullptr)

Adds two numbers in binary representation where each ciphertext of the input vector contains a bit.

void helib::negateBinary (CtPtrs &negation, const CtPtrs &input)

Negates a number in binary 2's complement representation.

 void helib::subtractBinary (CtPtrs &difference, const CtPtrs &lhs, const CtPtrs &rhs, std::vector< zzX > \*unpackSlotEncoding=nullptr)

Subtracts rhs from 1hs where 1hs, rhs are in 2's complement.

 void helib::addManyNumbers (CtPtrs &sum, CtPtrMat &numbers, long sizeLimit=0, std::vector< zzX > \*unpackSlotEncoding=nullptr)

Sum an arbitrary amount of numbers in binary representation.

void helib::multTwoNumbers (CtPtrs &product, const CtPtrs &lhs, const CtPtrs &rhs, bool rhsTwos
 —
 Complement=false, long sizeLimit=0, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Multiply two numbers in binary representation where each ciphertext of the input vector contains a bit.

long helib::fifteenOrLess4Four (const CtPtrs &out, const CtPtrs &in, long sizeLimit=4)

Add together up to fifteen {0,1} integers, producing a 4-bit counter.

 void helib::decryptBinaryNums (std::vector< long > &pNums, const CtPtrs &eNums, const SecKey &sKey, const EncryptedArray &ea, bool twosComplement=false, bool allSlots=true)

Decrypt the binary numbers that are encrypted in eNums.

## 8.53.1 Detailed Description

Implementing integer addition, multiplication in binary representation.

### 8.53.2 Macro Definition Documentation

#### 8.53.2.1 BPL ESTIMATE

```
#define BPL_ESTIMATE (30)
```

# 8.54 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/binaryCompare.cpp File Reference

Implementing integer comparison in binary representation.

```
#include <algorithm>
#include <NTL/BasicThreadPool.h>
#include <helib/binaryArith.h>
```

### **Namespaces**

helib

### Macros

#define BPL\_ESTIMATE (30)

### **Functions**

- void helib::runningSums (CtPtrs &v)
- void helib::compareTwoNumbersImplementation (CtPtrs &max, CtPtrs &min, Ctxt &mu, Ctxt &ni, const CtPtrs &aa, const CtPtrs &bb, bool twosComplement, std::vector< zzX > \*unpackSlotEncoding, bool cmp\_only)
- void helib::compareTwoNumbers (CtPtrs &max, CtPtrs &min, Ctxt &mu, Ctxt &ni, const CtPtrs &a, const CtPtrs &b, bool twosComplement=false, std::vector< zzX > \*unpackSlotEncoding=nullptr)

Compares two integers in binary a, b. Returns max(a, b), min(a, b) and indicator bits mu=(a>b) and ni=(a<b)

void helib::compareTwoNumbers (Ctxt &mu, Ctxt &ni, const CtPtrs &a, const CtPtrs &b, bool twos
 Complement=false, std::vector < zzX > \*unpackSlotEncoding=nullptr)

Compares two integers in binary a, b. Returns only indicator bits mu=(a>b) and ni=(a<b).

## 8.54.1 Detailed Description

Implementing integer comparison in binary representation.

#### 8.54.2 Macro Definition Documentation

### 8.54.2.1 BPL\_ESTIMATE

```
#define BPL_ESTIMATE (30)
```

# 8.55 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/binio.cpp File Reference

```
#include <helib/binio.h>
#include <helib/assertions.h>
#include <cstring>
#include <sys/types.h>
```

### **Namespaces**

### **Functions**

- int helib::readEyeCatcher (std::istream &str, const char \*expect)
- void helib::writeEyeCatcher (std::ostream &str, const char \*eye)
- long helib::read\_raw\_int (std::istream &str)
- int helib::read\_raw\_int32 (std::istream &str)
- void helib::write\_raw\_int (std::ostream &str, long num)
- void helib::write\_raw\_int32 (std::ostream &str, int num)
- void helib::write\_ntl\_vec\_long (std::ostream &str, const NTL::vec\_long &vl, long intSize=BINIO\_64BIT)
- void helib::read\_ntl\_vec\_long (std::istream &str, NTL::vec\_long &vl)
- void helib::write\_raw\_double (std::ostream &str, const double d)
- double helib::read raw double (std::istream &str)
- void helib::write\_raw\_xdouble (std::ostream &str, const NTL::xdouble xd)
- NTL::xdouble helib::read\_raw\_xdouble (std::istream &str)
- void helib::write\_raw\_ZZ (std::ostream &str, const NTL::ZZ &zz)
- void helib::read\_raw\_ZZ (std::istream &str, NTL::ZZ &zz)
- template<> void helib::read raw vector< long > (std::istream &str, std::vector< long > &v)
- template<> void helib::write\_raw\_vector< long > (std::ostream &str, const std::vector< long > &v)
- template<> void helib::read\_raw\_vector< double > (std::istream &str, std::vector< double > &v)
- template<> void helib::write\_raw\_vector< double > (std::ostream &str, const std::vector< double > &v)

# 8.56 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/bluestein.cpp File Reference

```
#include <helib/bluestein.h>
#include <helib/timing.h>
#include <helib/CModulus.h>
#include <helib/apiAttributes.h>
```

### **Namespaces**

helib

## **Macros**

• #define NEW\_BLUE (1)

#### **Functions**

void helib::BluesteinInit (long n, const NTL::zz\_p &root, NTL::zz\_pX &powers, NTL::Vec< NTL::mulmod\_←
 precon\_t > &powers\_aux, NTL::fftRep &Rb)

initialize bluestein

void helib::BluesteinFFT (NTL::zz\_pX &x, long n, UNUSED const NTL::zz\_p &root, const NTL::zz\_pX &powers, const NTL::Vec< NTL::mulmod\_precon\_t > &powers\_aux, const NTL::fftRep &Rb)

### 8.56.1 Macro Definition Documentation

# 8.56.1.1 NEW\_BLUE

#define NEW\_BLUE (1)

# 8.57 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/CModulus.cpp File Reference

```
#include <helib/CModulus.h>
#include <helib/timing.h>
```

# **Namespaces**

helib

# **Functions**

• NTL::zz\_pContext helib::BuildContext (long p, long maxroot)

# 8.58 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Context.cpp File Reference

```
#include <cstring>
#include <algorithm>
#include <helib/Context.h>
#include <helib/EvalMap.h>
#include <helib/powerful.h>
#include <helib/binio.h>
#include <helib/sample.h>
#include <helib/EncryptedArray.h>
#include <helib/PolyModRing.h>
```

# **Namespaces**

### **Functions**

• long helib::FindM (long k, long nBits, long c, long p, long d, long s, long chosen\_m, bool verbose=false)

Returns smallest parameter m satisfying various constraints:

void helib::writeContextBaseBinary (std::ostream &str, const Context &context)

write [m p r gens ords] data

• void helib::readContextBaseBinary (std::istream &s, unsigned long &m, unsigned long &p, unsigned long &r, std::vector< long > &gens, std::vector< long > &ords)

read [m p r gens ords] data, needed to construct context

- std::unique ptr< Context > helib::buildContextFromBinary (std::istream &str)
- void helib::writeContextBinary (std::ostream &str, const Context &context)
- void helib::readContextBinary (std::istream &str, Context &context)
- · void helib::writeContextBase (std::ostream &s, const Context &context)

write [m p r gens ords] data

- std::ostream & helib::operator<< (std::ostream &str, const Context &context)</li>
- void helib::readContextBase (std::istream &s, unsigned long &m, unsigned long &p, unsigned long &r, std
   ::vector< long > &gens, std::vector< long > &ords)

read [m p r gens ords] data, needed to construct context

- std::unique\_ptr< Context > helib::buildContextFromAscii (std::istream &str)
- std::istream & helib::operator>> (std::istream &str, Context &context)
- NTL::ZZX helib::getG (const EncryptedArray &ea)

# 8.59 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_→ v1.0.2/HElib/src/Ctxt.cpp File Reference

```
#include <NTL/BasicThreadPool.h>
#include <helib/binio.h>
#include <helib/timing.h>
#include <helib/Context.h>
#include <helib/Ctxt.h>
#include <helib/keySwitching.h>
#include <helib/EncryptedArray.h>
#include <helib/Ptxt.h>
#include <helib/Ptxt.h>
#include <helib/debugging.h>
#include <helib/norms.h>
#include <helib/fhe_stats.h>
#include <helib/powerful.h>
```

# **Namespaces**

#### **Functions**

- void helib::addSomePrimes (Ctxt &c)
- void helib::computeIntervalForMul (double &lo, double &hi, const Ctxt &ctxt1, const Ctxt &ctxt2)
- void helib::computeIntervalForSqr (double &lo, double &hi, const Ctxt &ctxt)
- std::istream & helib::operator>> (std::istream &str, SKHandle &handle)
- std::ostream & helib::operator<< (std::ostream &s, const CtxtPart &p)</li>
- std::istream & helib::operator>> (std::istream &s, CtxtPart &p)
- std::ostream & helib::operator<< (std::ostream &str, const Ctxt &ctxt)</li>
- std::istream & helib::operator>> (std::istream &str, Ctxt &ctxt)
- void helib::incrementalProduct (std::vector < Ctxt > &v)
- void helib::totalProduct (Ctxt &out, const std::vector < Ctxt > &v)
- void helib::innerProduct (Ctxt &result, const CtPtrs &v1, const CtPtrs &v2)
- void helib::innerProduct (Ctxt &result, const std::vector< Ctxt > &v1, const std::vector< Ctxt > &v2)
- void helib::innerProduct (Ctxt &result, const std::vector< Ctxt > &v1, const std::vector< DoubleCRT > &v2)
   Compute the inner product of a vectors of ciphertexts and a constant vector.
- void helib::innerProduct (Ctxt &result, const std::vector< Ctxt > &v1, const std::vector< NTL::ZZX > &v2)

### **Variables**

• int helib::fhe\_watcher = 0

# 8.60 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/debugging.cpp File Reference

```
#include <NTL/xdouble.h>
#include <helib/debugging.h>
#include <helib/norms.h>
#include <helib/Context.h>
#include <helib/Ctxt.h>
#include <helib/EncryptedArray.h>
```

# **Namespaces**

helib

#### **Functions**

- double helib::realToEstimatedNoise (const Ctxt &ctxt, const SecKey &sk)
- double helib::log2 realToEstimatedNoise (const Ctxt &ctxt, const SecKey &sk)
- void helib::checkNoise (const Ctxt &ctxt, const SecKey &sk, const std::string &msg, double thresh=10.0)
- NTL::xdouble helib::embeddingLargestCoeff (const Ctxt &ctxt, const SecKey &sk)
- void helib::decryptAndPrint (std::ostream &s, const Ctxt &ctxt, const SecKey &sk, const EncryptedArray &ea, long flags=0)
- bool helib::decryptAndCompare (const Ctxt &ctxt, const SecKey &sk, const EncryptedArray &ea, const PlaintextArray &pa)
- void helib::rawDecrypt (NTL::ZZX &plaintxt, const std::vector < NTL::ZZX > &zzParts, const DoubleCRT &s ← Key, long q=0)
- void helib::CheckCtxt (const Ctxt &c, const char \*label)

print to cerr some info about ciphertext

# 8.61 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/DoubleCRT.cpp File Reference

```
#include <NTL/ZZVec.h>
#include <NTL/BasicThreadPool.h>
#include <helib/timing.h>
#include <helib/binio.h>
#include <helib/sample.h>
#include <helib/DoubleCRT.h>
#include <helib/Context.h>
#include <helib/norms.h>
#include <helib/fhe_stats.h>
```

# **Namespaces**

helib

### **Functions**

- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::AddFun > (const DoubleCRT &other, AddFun fun, bool matchIndexSets)
- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::SubFun > (const DoubleCRT &other, SubFun fun, bool matchIndexSets)
- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::MulFun > (const NTL::ZZ &num, MulFun fun)
- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::AddFun > (const NTL::ZZ &num, AddFun fun)
- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::SubFun > (const NTL::ZZ &num, SubFun fun)
- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::MulFun > (const NTL::ZZX &poly, MulFun fun)
- template DoubleCRT & helib::DoubleCRT::Op < DoubleCRT::AddFun > (const NTL::ZZX &poly, AddFun fun)
- template DoubleCRT & helib::DoubleCRT::Op< DoubleCRT::SubFun > (const NTL::ZZX &poly, SubFun fun)
- std::ostream & helib::operator<< (std::ostream &str, const DoubleCRT &d)</li>
- std::istream & helib::operator>> (std::istream &str, DoubleCRT &d)

# 8.62 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/EaCx.cpp File Reference

```
#include <algorithm>
#include <type_traits>
#include <helib/zzX.h>
#include <helib/EncryptedArray.h>
#include <helib/timing.h>
#include <helib/clonedPtr.h>
#include <helib/norms.h>
#include <helib/debugging.h>
#include <helib/apiAttributes.h>
```

# **Namespaces**

helib

# 8.63 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/EncryptedArray.cpp File Reference

```
#include <algorithm>
#include <helib/zzX.h>
#include <helib/EncryptedArray.h>
#include <helib/timing.h>
#include <helib/clonedPtr.h>
#include <helib/norms.h>
```

### **Classes**

- class helib::rotate\_pa\_impl< type >
- class helib::shift\_pa\_impl< type >
- class helib::encode pa impl< type >
- class helib::random pa impl< type >
- class helib::decode\_pa\_impl< type >
- class helib::equals\_pa\_impl< type >
- class helib::add\_pa\_impl< type >
- class helib::sub\_pa\_impl< type >
- class helib::mul pa impl< type >
- class helib::negate\_pa\_impl< type >
- class helib::frobeniusAutomorph\_pa\_impl< type >
- class helib::applyPerm\_pa\_impl< type >
- class helib::print\_pa\_impl< type >

### **Namespaces**

helib

- EncryptedArrayBase \* helib::buildEncryptedArray (const Context &context, const PAlgebraMod &alMod, const NTL::ZZX &G=NTL::ZZX::zero())
  - A "factory" for building EncryptedArrays.
- void helib::runningSums (const EncryptedArray &ea, Ctxt &ctxt)

```
A ctxt that encrypts (x_1,...,x_n) is replaced by an encryption of (y_1,...,y_n), where y_i = sum_{j < i}x_j.
```

- void helib::totalSums (const EncryptedArray &ea, Ctxt &ctxt)
- void helib::applyLinPoly1 (const EncryptedArray &ea, Ctxt &ctxt, const std::vector < NTL::ZZX > &C)
- template<typename P >
   void helib::applyLinPolyLL (Ctxt &ctxt, const std::vector< P > &encodedC, long d)

- template void helib::applyLinPolyLL (Ctxt &ctxt, const std::vector< zzX > &encodedC, long d)
- template void helib::applyLinPolyLL (Ctxt &ctxt, const std::vector < NTL::ZZX > &encodedC, long d)
- template void helib::applyLinPolyLL (Ctxt &ctxt, const std::vector< DoubleCRT > &encodedC, long d)
- void helib::rotate (const EncryptedArray &ea, PlaintextArray &pa, long k)
- void helib::shift (const EncryptedArray &ea, PlaintextArray &pa, long k)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, const std::vector < long > &array)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, const std::vector< NTL::ZZX > &array)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, long val)
- void helib::encode (const EncryptedArray &ea, PlaintextArray &pa, const NTL::ZZX &val)
- void helib::random (const EncryptedArray &ea, PlaintextArray &pa)
- void helib::decode (const EncryptedArray &ea, std::vector< long > &array, const PlaintextArray &pa)
- void helib::decode (const EncryptedArray &ea, std::vector< NTL::ZZX > &array, const PlaintextArray &pa)
- bool helib::equals (const EncryptedArray &ea, const PlaintextArray &pa, const PlaintextArray &other)
- bool helib::equals (const EncryptedArray &ea, const PlaintextArray &pa, const std::vector< long > &other)
- bool helib::equals (const EncryptedArray &ea, const PlaintextArray &pa, const std::vector < NTL::ZZX > &other)
- void helib::add (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void helib::sub (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void helib::mul (const EncryptedArray &ea, PlaintextArray &pa, const PlaintextArray &other)
- void helib::negate (const EncryptedArray &ea, PlaintextArray &pa)
- void helib::frobeniusAutomorph (const EncryptedArray &ea, PlaintextArray &pa, long j)
- void helib::frobeniusAutomorph (const EncryptedArray &ea, PlaintextArray &pa, const NTL::Vec< long > &vec)
- void helib::power (const EncryptedArray &ea, PlaintextArray &pa, long e)
- void helib::applyPerm (const EncryptedArray &ea, PlaintextArray &pa, const NTL::Vec< long > &pi)
- void helib::print (const EncryptedArray &ea, std::ostream &s, const PlaintextArray &pa)

# 8.64 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_v1.0.2/HElib/src/eqtesting.cpp File Reference

Useful functions for equality testing...

```
#include <NTL/lzz_pXFactoring.h>
#include <helib/timing.h>
#include <helib/EncryptedArray.h>
#include <helib/Ptxt.h>
#include <cstdio>
```

#### Namespaces

• helib

- void helib::mapTo01 (const EncryptedArray &ea, Ctxt &ctxt)
- template < typename Scheme > void helib::mapTo01 (const EncryptedArray &, Ptxt < Scheme > &ptxt)
- template void helib::mapTo01 (const EncryptedArray &, Ptxt< BGV > &ptxt)
- template void helib::mapTo01 (const EncryptedArray &, Ptxt< CKKS > &ptxt)
- void helib::fastPower (Ctxt &ctxt, long d)
- void helib::incrementalZeroTest (Ctxt \*res[], const EncryptedArray &ea, const Ctxt &ctxt, long n)

# 8.64.1 Detailed Description

Useful functions for equality testing...

# 8.65 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/EvalMap.cpp File Reference

```
#include <helib/EvalMap.h>
#include <helib/apiAttributes.h>
#include <NTL/lzz_pXFactoring.h>
#include <NTL/GF2XFactoring.h>
```

## **Namespaces**

helib

### **Functions**

- void helib::RelaxedInv (NTL::Mat< NTL::zz\_p > &x, const NTL::Mat< NTL::zz\_p > &a)
- void helib::RelaxedInv (NTL::Mat< NTL::GF2 > &x, const NTL::Mat< NTL::GF2 > &a)
- void helib::TraceMap (NTL::GF2X &w, const NTL::GF2X &a, long d, const NTL::GF2XModulus &F, const NTL::GF2X &b)

# 8.66 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/extractDigits.cpp File Reference

```
#include <NTL/ZZ.h>
#include <NTL/ZZ_p.h>
#include <helib/EncryptedArray.h>
#include <helib/polyEval.h>
#include <helib/debugging.h>
```

### **Namespaces**

helib

- void helib::extractDigits (std::vector< Ctxt > &digits, const Ctxt &c, long r=0)
   Extract the mod-p digits of a mod-p<sup>^</sup> r ciphertext.
- void helib::extendExtractDigits (std::vector< Ctxt > &digits, const Ctxt &c, long r, long e)

# 8.67 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/fhe\_stats.cpp File Reference

```
#include <helib/fhe_stats.h>
#include <helib/multicore.h>
#include <algorithm>
#include <utility>
#include <cstring>
```

### **Namespaces**

helib

### **Functions**

- · void helib::print\_stats (std::ostream &s)
- const std::vector< double > \* helib::fetch\_saved\_values (const char \*)

# 8.68 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/hypercube.cpp File Reference

```
#include <helib/hypercube.h>
#include <iomanip>
#include <NTL/lzz_p.h>
```

### **Namespaces**

helib

- template<typename T >
   void helib::getHyperColumn (NTL::Vec< T > &v, const ConstCubeSlice< T > &s, long pos)
- $\begin{tabular}{ll} & \textbf{template}\xspace < \textbf{typename}\xspace\xspace T > \textbf{s}, \textbf{long pos)} \\ & \textbf{void helib::setHyperColumn}\xspace\xspace\xspace\xspace\xspace\xspace\xspace volume} & \textbf{typerColumn}\xspace\xs$
- $\begin{tabular}{ll} \bullet & template < typename T > \\ void & helib::setHyperColumn (const NTL::Vec < T > \&v, const CubeSlice < T > \&s, long pos, const T \&val) \\ \end{tabular}$
- template<typename T > void helib::print3D (const HyperCube< T > &c)
- template void helib::getHyperColumn (NTL::Vec< long > &v, const ConstCubeSlice< long > &s, long pos)
- template void helib::setHyperColumn (const NTL::Vec< long > &v, const CubeSlice< long > &s, long pos)
- template void helib::setHyperColumn (const NTL::Vec< long > &v, const CubeSlice< long > &s, long pos, const long &val)

- template void helib::print3D (const HyperCube < long > &c)
- template void helib::getHyperColumn (NTL::Vec< NTL::zz\_p > &v, const ConstCubeSlice< NTL::zz\_p > &s, long pos)
- template void helib::setHyperColumn (const NTL::Vec< NTL::zz\_p > &v, const CubeSlice< NTL::zz\_p > &s, long pos)
- template void helib::setHyperColumn (const NTL::Vec< NTL::zz\_p > &v, const CubeSlice< NTL::zz\_p > &s, long pos, const NTL::zz\_p &val)
- template void helib::print3D (const HyperCube < NTL::zz\_p > &c)

# 8.69 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/IndexSet.cpp File Reference

```
#include <helib/IndexSet.h>
#include <helib/binio.h>
```

# **Namespaces**

helib

### **Functions**

- IndexSet helib::operator (const IndexSet &s, const IndexSet &t)
   union
- IndexSet helib::operator& (const IndexSet &s, const IndexSet &t)
   intersection
- IndexSet helib::operator<sup>^</sup> (const IndexSet &s, const IndexSet &t)
   exclusive-or
- IndexSet helib::operator/ (const IndexSet &s, const IndexSet &t)
- long helib::card (const IndexSet &s)

Functional cardinality.

set minus

• bool helib::operator <= (const IndexSet &s1, const IndexSet &s2)

Is s1 subset or equal to s2.

bool helib::operator< (const IndexSet &s1, const IndexSet &s2)</li>

Is s1 strict subset of s2.

• bool helib::operator>= (const IndexSet &s1, const IndexSet &s2)

Is s2 subset or equal to s2.

bool helib::operator> (const IndexSet &s1, const IndexSet &s2)

Is s2 strict subset of s1.

- std::ostream & helib::operator<< (std::ostream &str, const IndexSet &set)</li>
- std::istream & helib::operator>> (std::istream &str, IndexSet &set)

# 8.70 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/intraSlot.cpp File Reference

```
#include <memory>
#include <helib/replicate.h>
#include <helib/intraSlot.h>
```

## **Namespaces**

helib

### **Functions**

- void helib::unpack (const CtPtrs &unpacked, const Ctxt &packed, const EncryptedArray &ea, const std
   ::vector < zzX > &unpackSlotEncoding)
- long helib::unpack (const CtPtrs &unpacked, const CtPtrs &packed, const EncryptedArray &ea, const std

  ::vector< zzX > &unpackSlotEncoding)
- void helib::repack (Ctxt &packed, const CtPtrs &unpacked, const EncryptedArray &ea)
- long helib::repack (const CtPtrs &packed, const CtPtrs &unpacked, const EncryptedArray &ea)
- void helib::packConstant (zzX &result, unsigned long data, long nbits, const EncryptedArray &ea)
- void helib::packConstants (zzX &result, const std::vector< unsigned long > &data, long nbits, const EncryptedArray &ea)
- void helib::unpackSlots (std::vector< unsigned long > &value, PlaintextArray &pa, const EncryptedArray &ea)

# 8.71 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/keys.cpp File Reference

```
#include <queue>
#include <helib/keys.h>
#include <helib/timing.h>
#include <helib/EncryptedArray.h>
#include <helib/Ptxt.h>
#include <helib/binio.h>
#include <helib/sample.h>
#include <helib/norms.h>
#include <helib/apiAttributes.h>
#include <helib/fhe_stats.h>
```

### **Namespaces**

#### **Macros**

• #define DECRYPT\_ON\_PWFL\_BASIS

### **Functions**

- double helib::RLWE1 (DoubleCRT &c0, const DoubleCRT &c1, const DoubleCRT &s, long p)

  Same as RLWE, but assumes that c1 is already chosen by the caller.
- double helib::RLWE (DoubleCRT &c0, DoubleCRT &c1, const DoubleCRT &s, long p, NTL::ZZ \*prg← Seed=nullptr)
- std::ostream & helib::operator<< (std::ostream &str, const PubKey &pk)</li>
- std::istream & helib::operator>> (std::istream &str, PubKey &pk)
- void helib::writePubKeyBinary (std::ostream &str, const PubKey &pk)
- void helib::readPubKeyBinary (std::istream &str, PubKey &pk)
- std::ostream & helib::operator<< (std::ostream &str, const SecKey &sk)
- std::istream & helib::operator>> (std::istream &str, SecKey &sk)
- void helib::writeSecKeyBinary (std::ostream &str, const SecKey &sk)
- void helib::readSecKeyBinary (std::istream &str, SecKey &sk)

### 8.71.1 Macro Definition Documentation

### 8.71.1.1 DECRYPT ON PWFL BASIS

```
#define DECRYPT_ON_PWFL_BASIS
```

# 8.72 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/keySwitching.cpp File Reference

A few strategies for generating key-switching matrices.

```
#include <unordered_set>
#include <NTL/ZZ.h>
#include <helib/permutations.h>
#include <helib/binio.h>
#include <helib/keySwitching.h>
#include <helib/keys.h>
#include <helib/apiAttributes.h>
```

### **Namespaces**

### **Macros**

• #define computeParams(context, m, i)

### **Functions**

std::ostream & helib::operator<< (std::ostream &str, const KeySwitch &matrix)</li>

### Strategies for generating key-switching matrices

These functions are implemented in KeySwitching.cpp

long helib::KSGiantStepSize (long D)

Function that returns number of baby steps. Used to keep this and matmul routines "in sync".

• void helib::addAllMatrices (SecKey &sKey, long keyID=0)

Maximalistic approach: generate matrices  $s(X^{\wedge}e)$ ->s(X) for all e in Zm\*.

void helib::addSome1DMatrices (SecKey &sKey, long bound=HELIB\_KEYSWITCH\_THRESH, long key ← ID=0)

Generate some matrices of the form  $s(X^{\hat{}}\{g^{\hat{}}i\}) > s(X)$ , but not all. For a generator g whose order is larger than bound, generate only enough matrices for the giant-step/baby-step procedures (2\*sqrt(ord(g))) of them).

void helib::add1DMatrices (SecKey &sKey, long keyID=0)

Generate all matrices  $s(X^{g^{i}})-s(X)$  for generators g of Zm\*/(p) and i< ord(g). If g has different orders in Zm\* and Zm\*/(p) then generate also matrices of the form  $s(X^{g^{i}}-i)$ )-s(X)

- void helib::addBSGS1DMatrices (SecKey &sKey, long keyID=0)
- void helib::addSomeFrbMatrices (SecKey &sKey, long bound=HELIB\_KEYSWITCH\_THRESH, long key ← ID=0)

Generate all/some Frobenius matrices of the form  $s(X^{\wedge}\{p^{\wedge}i\})->s(X)$ 

- void helib::addFrbMatrices (SecKey &sKey, long keyID=0)
- void helib::addBSGSFrbMatrices (SecKey &sKey, long keyID=0)
- void helib::addMinimal1DMatrices (SecKey &sKey, long keyID=0)

These routines just add a single matrix (or two, for bad dimensions)

- void helib::addMinimalFrbMatrices (SecKey &sKey, long keyID=0)
- void helib::addMatrices4Network (SecKey &sKey, const PermNetwork &net, long keyID=0)
- void helib::addTheseMatrices (SecKey &sKey, const std::set < long > &automVals, long keyID=0)

Generate specific key-switching matrices, described by the given set.

# 8.72.1 Detailed Description

A few strategies for generating key-switching matrices.

Copyright IBM Corporation 2012 All rights reserved.

### 8.72.2 Macro Definition Documentation

### 8.72.2.1 computeParams

```
#define computeParams(
                context,
                m.
                i)
Value:
  bool native;
  long ord, gi, g2md;
  NTL::mulmod_precon_t g2mdminv;
  if (i == context.zMStar.numOfGens()) { /* Frobenius matrices */
   ord = context.zMStar.getOrdP();
   gi = context.zMStar.getP();
   native = true;
  } else { /* one of the "regular" dimensions */
  ord = context.zMStar.OrderOf(i);
    gi = context.zMStar.ZmStarGen(i);
    native = context.zMStar.SameOrd(i);
   if (!native) {
     g2md = PowerMod(gi, -ord, m); /* g^{-ord} mod m */
      g2mdminv = PrepMulModPrecon(g2md, m);
 NTL::mulmod_precon_t giminv = PrepMulModPrecon(gi, m);
```

# 8.73 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/matching.cpp File Reference

```
#include <helib/matching.h>
#include <queue>
```

# **Namespaces**

helib

### **Functions**

- void helib::printFlow (FlowGraph &fg)
- long helib::maximum\_flow (FlowGraph &fg, long src, long sink)

# 8.74 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/matmul.cpp File Reference

```
#include <cstddef>
#include <tuple>
#include <algorithm>
#include <NTL/BasicThreadPool.h>
#include <helib/matmul.h>
#include <helib/norms.h>
#include <helib/fhe_stats.h>
#include <helib/apiAttributes.h>
```

### **Classes**

· class helib::BasicAutomorphPrecon

Pre-computation to speed many automorphism on the same ciphertext.

- · class helib::GeneralAutomorphPrecon
- · class helib::GeneralAutomorphPrecon UNKNOWN
- · class helib::GeneralAutomorphPrecon FULL
- class helib::GeneralAutomorphPrecon\_BSGS
- · struct helib::ConstMultiplier
- struct helib::ConstMultiplier\_DoubleCRT
- struct helib::ConstMultiplier zzX
- struct helib::MatMul1D derived impl< type >
- struct helib::MatMul1DExec construct< type >
- struct helib::BlockMatMul1D derived impl< type >
- struct helib::BlockMatMul1DExec construct< type >
- class helib::MatMulFullHelper< type >
- struct helib::MatMulFullExec construct< type >
- struct helib::MatMulFullExec construct< type >::MatMulDimComp
- class helib::BlockMatMulFullHelper< type >
- struct helib::BlockMatMulFullExec construct< type >
- struct helib::BlockMatMulFullExec construct< type >::BlockMatMulDimComp
- struct helib::mul\_MatMul1D\_impl< type >
- struct helib::mul\_BlockMatMul1D\_impl< type >
- struct helib::mul\_MatMulFull\_impl< type >
- struct helib::mul BlockMatMulFull impl< type >

# **Namespaces**

· helib

## **Macros**

- #define ALT\_MATMUL (1)
- #define HELIB\_BSGS\_MUL\_THRESH HELIB\_KEYSWITCH\_THRESH
- #define HELIB TRACE THRESH (50)

- std::shared\_ptr< GeneralAutomorphPrecon > helib::buildGeneralAutomorphPrecon (const Ctxt &ctxt, long dim, const EncryptedArray &ea)
- template<typename RX >
- std::shared\_ptr< ConstMultiplier > helib::build\_ConstMultiplier (const RX &poly)

   template<typename RX , typename type >
- std::shared\_ptr< ConstMultiplier > helib::build\_ConstMultiplier (const RX &poly, long dim, long amt, const EncryptedArrayDerived< type > &ea)
- void helib::MulAdd (Ctxt &x, const std::shared\_ptr< ConstMultiplier > &a, const Ctxt &b)
- void helib::DestMulAdd (Ctxt &x, const std::shared\_ptr< ConstMultiplier > &a, Ctxt &b)
- void helib::GenBabySteps (std::vector< std::shared\_ptr< Ctxt >> &v, const Ctxt &ctxt, long dim, bool clean)
- void helib::mul (PlaintextArray &pa, const MatMul1D &mat)
- void helib::mul (PlaintextArray &pa, const BlockMatMul1D &mat)
- void helib::mul (PlaintextArray &pa, const MatMulFull &mat)
- void helib::mul (PlaintextArray &pa, const BlockMatMulFull &mat)
- void helib::traceMap (Ctxt &ctxt)

### 8.74.1 Macro Definition Documentation

### 8.74.1.1 ALT\_MATMUL

#define ALT\_MATMUL (1)

### 8.74.1.2 HELIB\_BSGS\_MUL\_THRESH

#define HELIB\_BSGS\_MUL\_THRESH HELIB\_KEYSWITCH\_THRESH

### 8.74.1.3 HELIB\_TRACE\_THRESH

#define HELIB\_TRACE\_THRESH (50)

# 8.75 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/norms.cpp File Reference

```
#include <complex>
#include <cmath>
#include <algorithm>
#include <helib/NumbTh.h>
#include <helib/DoubleCRT.h>
#include <helib/norms.h>
#include <helib/PAlgebra.h>
#include <helib/fhe_stats.h>
```

# **Namespaces**

helib

### **Macros**

- #define USE\_HALF\_FFT (1)
- #define USE\_QUARTER\_FFT (1)
- #define USE\_TWO\_QUARTERS (0)

### **Functions**

- long helib::sumOfCoeffs (const zzX &f)
- NTL::ZZ helib::sumOfCoeffs (const NTL::ZZX &f)
- NTL::ZZ helib::sumOfCoeffs (const DoubleCRT &f)
- NTL::ZZ helib::largestCoeff (const NTL::ZZX &f)
- NTL::ZZ helib::largestCoeff (const NTL::Vec< NTL::ZZ > &f)
- NTL::ZZ helib::largestCoeff (const DoubleCRT &f)
- double helib::coeffsL2NormSquared (const zzX &f)

The L2-norm of an element (in coefficient representation)

- NTL::xdouble helib::coeffsL2NormSquared (const NTL::ZZX &f)
- NTL::xdouble helib::coeffsL2NormSquared (const DoubleCRT &f)
- double helib::embeddingLargestCoeff (const std::vector< double > &f, const PAlgebra &palg)
- void helib::embeddingLargestCoeff\_x2 (double &norm1, double &norm2, const std::vector< double > &f1, const std::vector< double > &f2, const PAlgebra &palg)
- double helib::embeddingLargestCoeff (const zzX &f, const PAlgebra &palg)
- NTL::xdouble helib::embeddingLargestCoeff (const NTL::ZZX &f, const PAlgebra &palg)
- void helib::CKKS\_canonicalEmbedding (std::vector< cx\_double > &v, const std::vector< double > &f, const PAlgebra &palg)
- void helib::CKKS\_canonicalEmbedding (std::vector< cx\_double > &v, const zzX &f, const PAlgebra &palg)
- void helib::CKKS\_canonicalEmbedding (std::vector< cx\_double > &v, const NTL::ZZX &f, const PAlgebra &palg)
- void helib::CKKS\_embedInSlots (zzX &f, const std::vector< cx\_double > &v, const PAlgebra &palg, double scaling)

## 8.75.1 Detailed Description

· computing various norms of ring elements

# 8.75.2 Macro Definition Documentation

### 8.75.2.1 USE HALF FFT

#define USE\_HALF\_FFT (1)

#### 8.75.2.2 USE QUARTER FFT

#define USE\_QUARTER\_FFT (1)

### 8.75.2.3 USE\_TWO\_QUARTERS

#define USE\_TWO\_QUARTERS (0)

# 8.76 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/NumbTh.cpp File Reference

```
#include <helib/NumbTh.h>
#include <helib/timing.h>
#include <fstream>
#include <cctype>
#include <algorithm>
```

### **Namespaces**

helib

#### **Functions**

• long helib::bitSetToLong (long bits, long bitSize)

Considers bits as a vector of bits and returns the value it represents when interpreted as a n-bit 2's complement number, where n is given by bitSize.

• long helib::mcMod (long a, long b)

Routines for computing mathematically correct mod and div.

- long helib::mcDiv (long a, long b)
- long helib::multOrd (long p, long m)

Return multiplicative order of p modulo m, or 0 if GCD(p, m) = 1.

long helib::computeProd (const NTL::Vec< long > &vec)

returns \prod\_d vec[d]

- long helib::computeProd (const std::vector < long > &vec)
- NTL::ZZX helib::makeIrredPoly (long p, long d)

Return a degree-d irreducible polynomial mod p.

void helib::factorize (std::vector< long > &factors, long N)

Factoring by trial division, only works for  $N<2^{(60)}$ , only the primes are recorded, not their multiplicity.

- void helib::factorize (std::vector < NTL::ZZ > &factors, const NTL::ZZ &N)
- void helib::factorize (NTL::Vec< NTL::Pair< long, long >> &factors, long N)

Factoring by trial division, only works for  $N<2^{\land}\{60\}$  primes and multiplicities are recorded.

void helib::pp\_factorize (std::vector < long > &factors, long N)

Prime-power factorization.

- void helib::phiN (long &phiN, std::vector< long > &facts, long N)

Compute Phi(N) and also factorize N.

- void helib::phiN (NTL::ZZ &phiN, std::vector< NTL::ZZ > &facts, const NTL::ZZ &N)
- long helib::phi\_N (long N)

Compute Phi(N).

- long helib::findGenerators (std::vector< long > &gens, std::vector< long > &ords, long m, long p, const std::vector< long > &candidates=std::vector< long >())
- template<typename zp , typename zz>

void helib::FindPrimRootT (zp &root, unsigned long e)

• void helib::FindPrimitiveRoot (NTL::zz\_p &r, unsigned long e)

Find e-th root of unity modulo the current modulus.

- void helib::FindPrimitiveRoot (NTL::ZZ p &r, unsigned long e)
- long helib::mobius (long n)

Compute mobius function (naive method as n is small).

NTL::ZZX helib::Cyclotomic (long N)

Compute cyclotomic polynomial.

long helib::primroot (long N, long phiN)

Find a primitive root modulo N.

long helib::ord (long N, long p)

Compute the highest power of p that divides N.

- NTL::ZZX helib::RandPoly (long n, const NTL::ZZ &p)
- void helib::MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long g, bool abs)
- void helib::balanced\_MulMod (NTL::ZZX &out, const NTL::ZZX &f, long a, long q)
- long helib::is\_in (long x, int \*X, long sz)

Finds whether x is an element of the set X of size sz, Returns -1 it not and the location if true.

• template<class zzvec >

bool helib::intVecCRT (NTL::vec\_ZZ &vp, const NTL::ZZ &p, const zzvec &vq, long q)

Incremental integer CRT for vectors.

- template bool helib::intVecCRT (NTL::vec\_ZZ &, const NTL::ZZ &, const NTL::vec\_ZZ &, long)
- template bool helib::intVecCRT (NTL::vec ZZ &, const NTL::ZZ &, const NTL::vec long &, long)
- template bool helib::intVecCRT (NTL::vec\_ZZ &, const NTL::ZZ &, const NTL::Vec< NTL::zz\_p > &, long)
- void helib::ModComp (NTL::ZZX &res, const NTL::ZZX &g, const NTL::ZZX &h, const NTL::ZZX &f)

Modular composition of polynomials:  $res = g(h) \mod f$ .

long helib::polyEvalMod (const NTL::ZZX &poly, long x, long p)

Evaluates a modular integer polynomial, returns poly(x) mod p.

void helib::interpolateMod (NTL::ZZX &poly, const NTL::vec\_long &x, const NTL::vec\_long &y, long p, long e=1)

Interpolate polynomial such that  $poly(x[i] \mod p) = y[i] \pmod{p^e}$  It is assumed that the points x[i] are all distinct modulo p.

void helib::seekPastChar (std::istream &str, int cc)

Advance the input stream beyond white spaces and a single instance of the char cc.

- void helib::buildLinPolyMatrix (NTL::mat\_zz\_pE &M, long p)
- void helib::buildLinPolyMatrix (NTL::mat\_GF2E &M, long p)
- $\bullet \ \ \text{void helib::mul} \ (\text{std::vector} < \ \text{NTL::ZZX} > \&x, \ \text{const std::vector} < \ \text{NTL::ZZX} > \&a, \ \text{long b}) \\$
- void helib::div (std::vector < NTL::ZZX > &x, const std::vector < NTL::ZZX > &a, long b)
- void helib::ppsolve (NTL::vec\_zz\_pE &x, const NTL::mat\_zz\_pE &A, const NTL::vec\_zz\_pE &b, long p, long r)

Prime power solver.

- void helib::ppsolve (NTL::vec\_GF2E &x, const NTL::mat\_GF2E &A, const NTL::vec\_GF2E &b, long p, long r)

  A version for GF2: must have p == 2 and r == 1.
- void helib::ppInvert (NTL::mat\_zz\_pE &X, const NTL::mat\_zz\_pE &A, long p, long r)
- void helib::ppInvert (NTL::mat\_zz\_p &X, const NTL::mat\_zz\_p &A, long p, long r)

Compute the inverse mod  $p^{\wedge}r$  of an  $n \times n$  matrix.

void helib::buildLinPolyCoeffs (NTL::vec\_zz\_pE &C, const NTL::vec\_zz\_pE &L, long p, long r)

Combination of buildLinPolyMatrix and ppsolve.

• void helib::buildLinPolyCoeffs (NTL::vec\_GF2E &C, const NTL::vec\_GF2E &L, long p, long r)

A version for GF2: must be called with p == 2 and r == 1.

- void helib::applyLinPoly (NTL::zz\_pE &beta, const NTL::vec\_zz\_pE &C, const NTL::zz\_pE &alpha, long p)

  Apply a linearized polynomial with coefficient vector C.
- void helib::applyLinPoly (NTL::GF2E &beta, const NTL::vec\_GF2E &C, const NTL::GF2E &alpha, long p)

A version for GF2: must be called with p == 2 and r == 1.

- std::pair< long, long > helib::rationalApprox (double x, long denomBound=0)

- void helib::PolyRed (NTL::ZZX &out, const NTL::ZZX &in, const NTL::ZZ &q, bool abs=false)
- void helib::PolyRed (NTL::ZZX &out, const NTL::ZZX &in, long q, bool abs=false)

Reduce all the coefficients of a polynomial modulo q.

- void helib::vecRed (NTL::Vec< NTL::ZZ > &out, const NTL::Vec< NTL::ZZ > &in, long q, bool abs)
- void helib::vecRed (NTL::Vec< NTL::ZZ > &in, const NTL::ZZ > &in, const NTL::ZZ &q, bool abs)

#### Some enhanced conversion routines

- void helib::convert (NTL::vec zz pE &X, const std::vector< NTL::ZZX > &A)
- void helib::convert (NTL::mat\_zz\_pE &X, const std::vector< std::vector< NTL::ZZX >> &A)
- void helib::convert (std::vector < NTL::ZZX > &X, const NTL::vec\_zz\_pE &A)
- void helib::convert (std::vector< std::vector< NTL::ZZX >> &X, const NTL::mat zz pE &A)
- void helib::convert (NTL::Vec< long > &out, const NTL::ZZX &in)
- void helib::convert (NTL::Vec< long > &out, const NTL::zz\_pX &in, bool symmetric=true)
- void helib::convert (NTL::Vec< long > &out, const NTL::GF2X &in)
- void helib::convert (NTL::ZZX &out, const NTL::Vec< long > &in)
- void helib::convert (NTL::GF2X &out, const NTL::Vec< long > &in)

# 8.77 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/OptimizePermutations.cpp File Reference

```
#include <cstdlib>
#include <list>
#include <sstream>
#include <memory>
#include <NTL/vector.h>
#include <helib/NumbTh.h>
#include <helib/EncryptedArray.h>
#include <helib/permutations.h>
#include <helib/apiAttributes.h>
```

### **Namespaces**

### **Functions**

- void helib::removeDups (std::list< long > &x, bool \*aux)
- void helib::addOffset (std::list< long > &x, long offset, long n, bool \*aux, UNUSED bool good=false)
- long helib::reducedCount (const std::list< long > &x, long n, bool \*aux)
- void helib::buildBenesCostTable (long n, long k, bool good, NTL::Vec< NTL::Vec< long >> &tab)
- std::ostream & helib::operator<< (std::ostream &s, LongNodePtr p)</li>
- BenesMemoEntry helib::optimalBenesAux (long i, long budget, long nlev, const NTL::Vec< NTL::Vec< long
   <p>>> &costTab, BenesMemoTable &memoTabl)
- void helib::optimalBenes (long n, long budget, bool good, long &cost, LongNodePtr &solution)
- void helib::print (std::ostream &s, SplitNodePtr p, bool first)
- std::ostream & helib::operator<< (std::ostream &s, SplitNodePtr p)</li>
- long helib::length (GenNodePtr ptr)
- std::ostream & helib::operator<< (std::ostream &s, GenNodePtr p)</li>
- LowerMemoEntry helib::optimalLower (long order, bool good, long budget, long mid, LowerMemoTable &lowerMemoTable)
- UpperMemoEntry helib::optimalUpperAux (const NTL::Vec< GenDescriptor > &vec, long i, long budget, long mid, UpperMemoTable &upperMemoTable, LowerMemoTable &lowerMemoTable)

# 8.78 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_← v1.0.2/HElib/src/PAlgebra.cpp File Reference

```
#include <algorithm>
#include <cmath>
#include <helib/PAlgebra.h>
#include <helib/hypercube.h>
#include <helib/timing.h>
#include <NTL/ZZXFactoring.h>
#include <NTL/GF2EXFactoring.h>
#include <NTL/lzz_pEXFactoring.h>
#include <NTL/BasicThreadPool.h>
#include <mutex>
```

### **Namespaces**

helib

- template<typename RX >
   bool helib::poly\_comp (const RX &a, const RX &b)
- bool helib::less\_than (NTL::GF2 a, NTL::GF2 b)
- bool helib::less\_than (NTL::zz\_p a, NTL::zz\_p b)
- bool helib::less\_than (const NTL::GF2X &a, const NTL::GF2X &b)
- bool helib::less\_than (const NTL::zz\_pX &a, const NTL::zz\_pX &b)
- bool helib::less\_than (const NTL::GF2E &a, const NTL::GF2E &b)
- bool helib::less\_than (const NTL::zz\_pE &a, const NTL::zz\_pE &b)
- bool helib::less\_than (const NTL::GF2EX &a, const NTL::GF2EX &b)
- bool helib::less\_than (const NTL::zz\_pEX &a, const NTL::zz\_pEX &b)

- double helib::calcPolyNormBnd (long m)
- bool helib::comparePAlgebra (const PAlgebra &palg, unsigned long m, unsigned long p, UNUSED unsigned long r, const std::vector< long > &gens, const std::vector< long > &ords)
- $\bullet \ \ \mathsf{PAlgebraModBase} * \mathsf{helib} \\ \vdots \\ \mathsf{buildPAlgebraMod} \ (\mathsf{const} \ \mathsf{PAlgebra} \ \& \mathsf{zMStar}, \\ \mathsf{long} \ \mathsf{r})$

```
Builds a table, of type PA\_GF2 if p == 2 and r == 1, and PA\_zz\_p otherwise.
```

- template<typename T >
  - void helib::PAlgebraLift (const NTL::ZZX &phimx, const T &lfactors, T &factors, T &crtc, long r)
- void helib::EDF (NTL::vec zz pX &v, const NTL::zz pX &f, long d)
- NTL::zz pEX helib::FrobeniusMap (const NTL::zz pEXModulus &F)
- void helib::InvModpr (NTL::zz\_pX &S, const NTL::zz\_pX &F, const NTL::zz\_pX &G, long p, long r)
- template<> void helib::PAlgebraLift (const NTL::ZZX &phimx, const NTL::vec\_zz\_pX &lfactors, NTL::vec \_ zz\_pX &factors, NTL::vec\_zz\_pX &crtc, long r)

# 8.79 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/PermNetwork.cpp File Reference

```
#include <NTL/ZZ.h>
#include <helib/Context.h>
#include <helib/Ctxt.h>
#include <helib/permutations.h>
#include <helib/EncryptedArray.h>
```

### **Namespaces**

helib

### **Functions**

std::ostream & helib::operator<< (std::ostream &s, const PermNetwork &net)</li>

# 8.80 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/permutations.cpp File Reference

```
#include <helib/permutations.h>
```

### **Namespaces**

### **Functions**

template<typename T >
 void helib::applyPermToVec (NTL::Vec< T > &out, const NTL::Vec< T > &in, const Permut &p1)
 Apply a permutation to a std::vector, out[i]=in[p1[i]] (NOT in-place)

• template<typename T >

void helib::applyPermToVec (std::vector< T > &out, const std::vector< T > &in, const Permut &p1)

template<typename T >

void helib::applyPermsToVec (NTL::Vec< T > &out, const NTL::Vec< T > &in, const Permut &p2, const Permut &p1)

Apply two permutations to a std::vector out[i]=in[p2[p1[i]]] (NOT in-place)

- template<typename T >
  - void helib::applyPermsToVec (std::vector< T >&out, const std::vector< T >&in, const Permut &p2, const Permut &p1)
- template void helib::applyPermToVec< long > (NTL::Vec< long > &out, const NTL::Vec< long > &in, const Permut &p1)
- template void helib::applyPermToVec< long > (std::vector< long > &out, const std::vector< long > &in, const Permut &p1)
- template void helib::applyPermToVec< NTL::ZZX > (std::vector< NTL::ZZX > &out, const std::vector< N ← TL::ZZX > &in, const Permut &p1)
- template void helib::applyPermsToVec< long > (NTL::Vec< long > &out, const NTL::Vec< long > &in, const Permut &p2, const Permut &p1)
- template void helib::applyPermsToVec< long > (std::vector< long > &out, const std::vector< long > &in, const Permut &p2, const Permut &p1)
- void helib::randomPerm (Permut &perm, long n)

A random size-n permutation.

- void helib::breakPermTo3 (const HyperCube < long > &pi, long dim, ColPerm &rho1, HyperCube < long > &rho2, ColPerm &rho3)
- void helib::breakPermByDim (std::vector< ColPerm > &out, const Permut &pi, const CubeSignature &sig)

  Takes a permutation pi over m-dimensional cube C=Z\_{n1} x...x Z\_{nm} and expresses pi as a product pi = rho\_←

lakes a permutation pi over m-dimensional cube  $C=Z_{n1} \times ... \times Z_{nm}$  and expresses pi as a product pi =  $rho\_ \leftarrow \{2m-1\} \circ ... \circ rho\_2 \circ rho\_1$  where each  $rho\_i$  is a column permutation along one dimension. Specifically for i < m, the permutations  $rho\_i$  and  $rho\_\{2(m-1)-i\}$  permute the i'th dimension.

void helib::ComputeOneGenMapping (Permut &genMap, const OneGeneratorTree &T)

to a single generator tree

- std::ostream & helib::operator<< (std::ostream &s, const ColPerm &p)</li>
- std::ostream & helib::operator<< (std::ostream &s, const SubDimension &sd)
- std::ostream & helib::operator<< (std::ostream &s, const GeneratorTrees &trees)</li>

# 8.81 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/PGFFT.cpp File Reference

```
#include <helib/PGFFT.h>
#include <cassert>
#include <cstdlib>
#include <limits>
```

#### Namespaces

### **Macros**

```
#define PGFFT_USE_TRUNCATED_BLUE (1)
#define PGFFT_USE_EXPLICIT_MUL (1)
#define RESTRICT
#define PGFFT_FFT_RDUP (4)
#define fwd_butterfly(xx0, xx1, w)
```

- #define fwd\_butterfly0(xx0, xx1)
- #define inv butterfly0(xx0, xx1)
- #define inv\_butterfly(xx0, xx1, w)
- #define PGFFT\_NEW\_FFT\_THRESH (10)
- #define PGFFT\_BRC\_THRESH (11)
- #define PGFFT\_BRC\_Q (5)
- #define PGFFT\_STRATEGY\_NULL (0)
- #define PGFFT\_STRATEGY\_POW2 (1)
- #define PGFFT STRATEGY BLUE (2)
- #define PGFFT\_STRATEGY\_TBLUE (3)

# **Typedefs**

```
    template < class T >
        using helib::aligned_vector = PGFFT::aligned_vector < T >
```

- typedef complex < double > helib::cmplx\_t
- typedef long double helib::ldbl

# 8.81.1 Macro Definition Documentation

# 8.81.1.1 fwd\_butterfly

#### Value:

# 8.81.1.2 fwd\_butterfly0

# 8.81.1.3 inv\_butterfly

```
#define inv_butterfly(  xx0, \\ xx1, \\ w )
```

### Value:

# 8.81.1.4 inv\_butterfly0

```
#define inv_butterfly0( xx0, xx1)
```

### Value:

# 8.81.1.5 PGFFT\_BRC\_Q

```
#define PGFFT_BRC_Q (5)
```

# 8.81.1.6 PGFFT\_BRC\_THRESH

#define PGFFT\_BRC\_THRESH (11)

# 8.81.1.7 PGFFT\_FFT\_RDUP

#define PGFFT\_FFT\_RDUP (4)

# 8.81.1.8 PGFFT\_NEW\_FFT\_THRESH

#define PGFFT\_NEW\_FFT\_THRESH (10)

### 8.81.1.9 PGFFT\_STRATEGY\_BLUE

#define PGFFT\_STRATEGY\_BLUE (2)

# 8.81.1.10 PGFFT\_STRATEGY\_NULL

#define PGFFT\_STRATEGY\_NULL (0)

## 8.81.1.11 PGFFT STRATEGY POW2

#define PGFFT\_STRATEGY\_POW2 (1)

# 8.81.1.12 PGFFT\_STRATEGY\_TBLUE

#define PGFFT\_STRATEGY\_TBLUE (3)

# 8.81.1.13 PGFFT\_USE\_EXPLICIT\_MUL

#define PGFFT\_USE\_EXPLICIT\_MUL (1)

### 8.81.1.14 PGFFT\_USE\_TRUNCATED\_BLUE

```
#define PGFFT_USE_TRUNCATED_BLUE (1)
```

### 8.81.1.15 RESTRICT

#define RESTRICT

# 8.82 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/polyEval.cpp File Reference

```
#include <helib/Context.h>
#include <helib/polyEval.h>
```

## **Namespaces**

helib

### **Functions**

- void helib::polyEval (Ctxt &ret, const NTL::Vec< Ctxt > &poly, const Ctxt &x) Evaluate an encrypted polynomial on an encrypted input.
- void helib::polyEval (Ctxt &ret, NTL::ZZX poly, const Ctxt &x, long k=0)

Evaluate a cleartext polynomial on an encrypted input.

# 8.83 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/PolyMod.cpp File Reference

```
#include <helib/PolyMod.h>
#include <helib/exceptions.h>
#include <NTL/ZZX.h>
#include <NTL/ZZ_p.h>
#include <vector>
```

### **Namespaces**

# **Functions**

- std::istream & helib::operator>> (std::istream &is, PolyMod &poly)
- std::ostream & helib::operator<< (std::ostream &os, const PolyMod &poly)

# 8.84 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/PolyModRing.cpp File Reference

#include <helib/PolyModRing.h>

# **Namespaces**

· helib

# **Functions**

• std::ostream & helib::operator<< (std::ostream &os, const PolyModRing &ring)

# 8.85 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/powerful.cpp File Reference

#include <helib/powerful.h>

# **Namespaces**

• helib

# **Functions**

- void helib::computeDivVec (NTL::Vec< long > &divVec, long m, const NTL::Vec< long > &powVec)
- void helib::computeInvVec (NTL::Vec< long > &invVec, const NTL::Vec< long > &divVec, const NTL::Vec< long > &powVec)

# 8.86 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/primeChain.cpp File Reference

handling the chain of moduli

```
#include <climits>
#include <cmath>
#include <algorithm>
#include <helib/primeChain.h>
#include <helib/Context.h>
#include <helib/sample.h>
#include <helib/binio.h>
```

### Classes

· struct helib::PrimeGenerator

# **Namespaces**

helib

### **Functions**

- bool helib::operator> (const ModuliSizes::Entry &a, const ModuliSizes::Entry &b)
- std::ostream & helib::operator<< (std::ostream &s, const ModuliSizes::Entry &e)
- std::istream & helib::operator>> (std::istream &s, ModuliSizes::Entry &e)
- void helib::write (std::ostream &s, const ModuliSizes::Entry &e)
- void helib::read (std::istream &s, ModuliSizes::Entry &e)
- std::ostream & helib::operator<< (std::ostream &s, const ModuliSizes &szs)
- std::istream & helib::operator>> (std::istream &s, ModuliSizes &szs)
- void helib::addSmallPrimes (Context &context, long resolution, long cpSize)

Add small primes to get target resolution.

- long helib::ctxtPrimeSize (long nBits)
- void helib::addCtxtPrimes (Context &context, long nBits, long targetSize)
- · void helib::endBuildModChain (Context &context)
- void helib::buildModChain (Context &context, long nBits, long nDgts=3, bool willBeBootstrappable=false, long skHwt=0, long resolution=3, long bitsInSpecialPrimes=0)

# 8.86.1 Detailed Description

handling the chain of moduli

# 8.87 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Ptxt.cpp File Reference

```
#include <random>
#include <helib/Ptxt.h>
#include <helib/apiAttributes.h>
```

# **Namespaces**

helib

### **Functions**

- template < typename Scheme >
   Scheme::SlotType helib::randomSlot (const Context & context)
- template<> BGV::SlotType helib::randomSlot< BGV > (const Context &context)
- template<> CKKS::SlotType helib::randomSlot< CKKS > (UNUSED const Context &context)

# 8.88 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/randomMatrices.cpp File Reference

implementation of random matrices of various forms build functions, used for testing

```
#include <helib/randomMatrices.h>
```

# **Namespaces**

helib

# **Functions**

- MatMul1D \* helib::buildRandomMatrix (const EncryptedArray &ea, long dim)
- MatMul1D \* helib::buildRandomMultiMatrix (const EncryptedArray &ea, long dim)
- BlockMatMul1D \* helib::buildRandomBlockMatrix (const EncryptedArray &ea, long dim)
- BlockMatMul1D \* helib::buildRandomMultiBlockMatrix (const EncryptedArray &ea, long dim)
- MatMulFull \* helib::buildRandomFullMatrix (const EncryptedArray &ea)
- BlockMatMulFull \* helib::buildRandomFullBlockMatrix (const EncryptedArray &ea)

# 8.88.1 Detailed Description

implementation of random matrices of various forms build functions, used for testing

# 8.89 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/recryption.cpp File Reference

```
#include <NTL/BasicThreadPool.h>
#include <helib/recryption.h>
#include <helib/EncryptedArray.h>
#include <helib/EvalMap.h>
#include <helib/powerful.h>
#include <helib/CtPtrs.h>
#include <helib/intraSlot.h>
#include <helib/norms.h>
#include <helib/sample.h>
#include <helib/debugging.h>
#include <helib/fhe_stats.h>
```

### **Classes**

struct helib::PubKeyHack

# **Namespaces**

helib

# **Macros**

- #define DROP BEFORE THIN RECRYPT
- #define THIN\_RECRYPT\_NLEVELS (3)

### **Functions**

- void helib::extractDigitsPacked (Ctxt &ctxt, long botHigh, long r, long ePrime, const std::vector < NTL::ZZX > &unpackSlotEncoding)
- void helib::extractDigitsThin (Ctxt &ctxt, long botHigh, long r, long ePrime)
- void helib::packedRecrypt (const CtPtrs &cPtrs, const std::vector < zzX > &unpackConsts, const Encrypted ← Array &ea)
- void helib::packedRecrypt (const CtPtrs & array, const std::vector < zzX > & unpackConsts, const Encrypted ← Array & ea, long belowLvI)
- void helib::packedRecrypt (const CtPtrMat &m, const std::vector < zzX > &unpackConsts, const Encrypted ←
   Array &ea, long belowLvl=LONG\_MAX)

# 8.89.1 Macro Definition Documentation

# 8.89.1.1 DROP\_BEFORE\_THIN\_RECRYPT

#define DROP\_BEFORE\_THIN\_RECRYPT

### 8.89.1.2 THIN RECRYPT NLEVELS

#define THIN\_RECRYPT\_NLEVELS (3)

# 8.90 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/replicate.cpp File Reference

```
#include <helib/replicate.h>
#include <helib/timing.h>
#include <helib/clonedPtr.h>
```

### **Classes**

· class helib::ExplicitReplicator

An implementation of ReplicateHandler that explicitly returns all the replicated ciphertexts in one big vector.

- class helib::replicate\_pa\_impl< type >

# **Namespaces**

helib

# **Functions**

• void helib::replicate (const EncryptedArray &ea, Ctxt &ctx, long pos)

The value in slot #pos is replicated in all other slots. On an n-slot ciphertext, this algorithm performs O(log n) 1D rotations.

• void helib::replicate0 (const EncryptedArray &ea, Ctxt &ctxt, long pos)

A lower-level routine. Same as replicate, but assumes all slots are zero except slot #pos.

- void helib::replicateAllOrig (const EncryptedArray &ea, const Ctxt &ctxt, ReplicateHandler \*handler, RepAux \*repAuxPtr=nullptr)
- void helib::replicateAll (const EncryptedArray &ea, const Ctxt &ctxt, ReplicateHandler \*handler, long rec
   — Bound=64, RepAuxDim \*repAuxPtr=nullptr)
- void helib::replicateAll (std::vector< Ctxt > &v, const EncryptedArray &ea, const Ctxt &ctxt, long rec
   — Bound=64, RepAuxDim \*repAuxPtr=nullptr)
- void helib::replicate (const EncryptedArray &ea, PlaintextArray &pa, long i)

# 8.91 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/sample.cpp File Reference

```
#include <vector>
#include <NTL/ZZX.h>
#include <NTL/ZZ_pX.h>
#include <NTL/BasicThreadPool.h>
#include <helib/NumbTh.h>
#include <helib/Context.h>
#include <helib/sample.h>
#include <helib/norms.h>
#include <helib/apiAttributes.h>
#include <helib/powerful.h>
```

# **Namespaces**

· helib

### **Functions**

- void helib::sampleHWt (zzX &poly, long n, long Hwt=100)
  - Sample a degree-(n-1) poly as above, with only Hwt nonzero coefficients.
- void helib::sampleHWt (NTL::ZZX &poly, long n, long Hwt=100)
- void helib::sampleSmall (zzX &poly, long n, double prob=0.5)
- void helib::sampleSmall (NTL::ZZX &poly, long n, double prob=0.5)
- void helib::sampleGaussian (std::vector< double > &dvec, long n, double stdev)

Choose a vector of continuous Gaussians.

void helib::sampleGaussian (zzX &poly, long n, double stdev)

Sample polynomials with Gaussian coefficients.

- void helib::sampleGaussian (NTL::ZZX &poly, long n, double stdev)
- void helib::sampleUniform (zzX &poly, long n, long B=100)

Sample a degree-(n-1) ZZX, with coefficients uniform in [-B,B].

- void helib::sampleUniform (NTL::ZZX &poly, long n, const NTL::ZZ &B=NTL::ZZ(100L))
- double helib::sampleHWt (zzX &poly, const Context &context, long Hwt=100)
- double helib::sampleHWtBoundedEffectiveBound (const Context &context, long Hwt=100)
- double helib::sampleHWtBounded (zzX &poly, const Context &context, long Hwt=100)
- double helib::sampleSmall (zzX &poly, const Context &context)
- double helib::sampleSmallBounded (zzX &poly, const Context &context)
- double helib::sampleGaussian (zzX &poly, const Context &context, double stdev)
- double helib::sampleGaussianBounded (zzX &poly, const Context &context, double stdev)
- double helib::sampleUniform (zzX &poly, const Context &context, long B=100)
- NTL::xdouble helib::sampleUniform (NTL::ZZX &poly, const Context &context, const NTL::ZZ &B=NTL::← ZZ(100L))
- double helib::boundRoundingNoise (UNUSED long m, long phim, long p2r, double epsilon)
- double helib::boundFreshNoise (long m, long phim, double sigma, double epsilon=9e-13)

# 8.92 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/tableLookup.cpp File Reference

Code for homomorphic table lookup and fixed-point functions.

```
#include <limits>
#include <cmath>
#include <cstdlib>
#include <stdexcept>
#include <NTL/BasicThreadPool.h>
#include <helib/intraSlot.h>
#include <helib/tableLookup.h>
```

# **Namespaces**

helib

### **Functions**

- void helib::computeAllProducts (CtPtrs &products, const CtPtrs &array, std::vector< zzX > \*unpackSlot←
   Encoding=nullptr)
- void helib::tableLookup (Ctxt &out, const std::vector< zzX > &table, const CtPtrs &idx, std::vector< zzX > \*unpackSlotEncoding=nullptr)
- void helib::tableWriteIn (const CtPtrs &table, const CtPtrs &idx, std::vector< zzX > \*unpackSlot← Encoding=nullptr)
- void helib::buildLookupTable (std::vector< zzX > &T, std::function< double(double)> f, long nbits\_in, long scale in, long sign in, long nbits out, long scale out, long sign out, const EncryptedArray &ea)

Built a table-lookup for a function in fixed-point representation.

# 8.92.1 Detailed Description

Code for homomorphic table lookup and fixed-point functions.

# 8.93 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_approxNums.cpp File Reference

```
#include <NTL/ZZ.h>
#include <algorithm>
#include <complex>
#include <helib/norms.h>
#include <helib/helib.h>
#include <helib/debugging.h>
#include <helib/ArgMap.h>
```

### **Functions**

- double calcMaxDiff (const vector < cx double > &v1, const vector < cx double > &v2)
- double calcMaxRelDiff (const vector< cx\_double > &v1, const vector< cx\_double > &v2)
- bool cx\_equals (const vector< cx\_double > &v1, const vector< cx\_double > &v2, double epsilon)
- void testBasicArith (const PubKey &publicKey, const SecKey &secretKey, const EncryptedArrayCx &ea, double epsilon)
- void testComplexArith (const PubKey &publicKey, const SecKey &secretKey, const EncryptedArrayCx &ea, double epsilon)
- void testRotsNShifts (const PubKey &publicKey, const SecKey &secretKey, const EncryptedArrayCx &ea, double epsilon)
- void debugCompare (const EncryptedArrayCx &ea, const SecKey &sk, vector < cx\_double > &p, const Ctxt &c, double epsilon)
- void negateVec (vector< cx double > &p1)
- void add (vector < cx double > &to, const vector < cx double > &from)
- void sub (vector < cx\_double > &to, const vector < cx\_double > &from)
- void mul (vector < cx double > &to, const vector < cx double > &from)
- void rotate (vector < cx double > &p, long amt)
- void testGeneralOps (const PubKey &publicKey, const SecKey &secretKey, const EncryptedArrayCx &ea, double epsilon, long nRounds)
- int main (int argc, char \*argv[])

### **Variables**

bool verbose =false

# 8.93.1 Function Documentation

# 8.93.1.1 add()

```
void add ( \label{eq:cx_double} \mbox{ vector} < \mbox{ cx_double } > \& \mbox{ to,} \\ \mbox{ const vector} < \mbox{ cx_double } > \& \mbox{ from })
```

# 8.93.1.2 calcMaxDiff()

```
double calcMaxDiff (  \mbox{const vector} < \mbox{cx\_double} > \& v1, \\ \mbox{const vector} < \mbox{cx\_double} > \& v2 )
```

# 8.93.1.3 calcMaxRelDiff()

```
double calcMaxRelDiff (  \mbox{const vector} < \mbox{cx\_double} > \& \ v1, \\ \mbox{const vector} < \mbox{cx\_double} > \& \ v2 \ )
```

# 8.93.1.4 cx\_equals()

```
bool cx_equals (  \mbox{const vector} < \mbox{cx\_double} > \& v1, \\ \mbox{const vector} < \mbox{cx\_double} > \& v2, \\ \mbox{double } \mbox{epsilon} \mbox{) [inline]}
```

# 8.93.1.5 debugCompare()

### 8.93.1.6 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.93.1.7 mul()

```
void mul ( \label{eq:cx_double} \mbox{vector} < \mbox{cx_double} > \& \mbox{\it to}, \mbox{const vector} < \mbox{cx_double} > \& \mbox{\it from })
```

# 8.93.1.8 negateVec()

```
void negateVec ( \label{eq:cx_double} \mbox{vector} < \mbox{cx\_double} > \mbox{\& $p1$ })
```

# 8.93.1.9 rotate()

```
void rotate ( \label{eq:cx_double} \mbox{vector} < \mbox{cx\_double} > \& \ p \mbox{,} \\ \mbox{long amt } \mbox{)}
```

# 8.93.1.10 sub()

```
void sub ( \label{eq:cx_double} \mbox{vector} < \mbox{cx_double} > \& \mbox{\it to}, \mbox{const vector} < \mbox{cx_double} > \& \mbox{\it from })
```

# 8.93.1.11 testBasicArith()

# 8.93.1.12 testComplexArith()

# 8.93.1.13 testGeneralOps()

### 8.93.1.14 testRotsNShifts()

# 8.93.2 Variable Documentation

### 8.93.2.1 verbose

```
bool verbose =false
```

# 8.94 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_Bin\_IO.cpp File Reference

```
#include <cassert>
#include <cstring>
#include <fstream>
#include <utility>
#include <unistd.h>
#include <NTL/ZZX.h>
#include <NTL/vector.h>
#include <helib/helib.h>
#include <helib/ArgMap.h>
#include <helib/debugging.h>
```

# **Functions**

- bool isLittleEndian ()
- void cleanupFiles (const char \*file)
- template<class... Files> void cleanupFiles (const char \*file, Files... files)
- long compareFiles (string filename1, string filename2)
- int main (int argc, char \*argv[])

# 8.94.1 Function Documentation

# 8.94.1.1 cleanupFiles() [1/2]

# 8.94.1.2 cleanupFiles() [2/2]

# 8.94.1.3 compareFiles()

### 8.94.1.4 isLittleEndian()

```
bool isLittleEndian ( )
```

# 8.94.1.5 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.95 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_binaryArith.cpp File Reference

```
#include <iostream>
#include <cassert>
#include <fstream>
#include <vector>
#include <cmath>
#include <algorithm>
#include <NTL/BasicThreadPool.h>
#include <helib/helib.h>
#include <helib/intraSlot.h>
#include <helib/binaryArith.h>
#include <helib/ArgMap.h>
```

# **Functions**

- void test15for4 (SecKey &secKey)
- void testProduct (SecKey &secKey, long bitSize1, long bitSize2, long outSize, bool bootstrap=false)
- void testAdd (SecKey &secKey, long bitSize1, long bitSize2, long outSize, bool bootstrap=false)
- int main (int argc, char \*argv[])

# 8.95.1 Function Documentation

### 8.95.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.95.1.2 test15for4()

# 8.95.1.3 testAdd()

# 8.95.1.4 testProduct()

# 8.96 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_binaryCompare.cpp File Reference

```
#include <iostream>
#include <cassert>
#include <fstream>
#include <vector>
#include <cmath>
#include <algorithm>
#include <NTL/BasicThreadPool.h>
#include <helib/helib.h>
#include <helib/intraSlot.h>
#include <helib/binaryArith.h>
#include <helib/binaryCompare.h>
#include <helib/ArgMap.h>
```

### **Functions**

- void testCompare (SecKey &secKey, long bitSize, bool bootstrap=false)
- int main (int argc, char \*argv[])

# 8.96.1 Function Documentation

# 8.96.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.96.1.2 testCompare()

# 8.97 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_bootstrapping.cpp File Reference

```
#include <NTL/ZZ.h>
#include <NTL/fileio.h>
#include <NTL/BasicThreadPool.h>
#include <cassert>
#include <helib/EncryptedArray.h>
#include <helib/EvalMap.h>
#include <helib/powerful.h>
#include <helib/matmul.h>
#include <helib/ArgMap.h>
#include <helib/ArgMap.h>
#include <helib/debugging.h>
```

### **Macros**

- #define num\_mValues (sizeof(mValues)/(14\*sizeof(long)))
- #define OUTER REP (1)
- #define INNER REP (1)

# **Functions**

- void TestIt (long idx, long p, long r, long L, long c, long skHwt, int build\_cache=0)
- int main (int argc, char \*argv[])

# 8.97.1 Macro Definition Documentation

# 8.97.1.1 INNER\_REP

```
#define INNER_REP (1)
```

### 8.97.1.2 num mValues

#define num\_mValues (sizeof(mValues)/(14\*sizeof(long)))

# 8.97.1.3 OUTER\_REP

#define OUTER\_REP (1)

# 8.97.2 Function Documentation

# 8.97.2.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.97.2.2 TestIt()

# 8.98 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_EaCx.cpp File Reference

```
#include <NTL/ZZ.h>
#include <cassert>
#include <helib/norms.h>
#include <helib/EncryptedArray.h>
#include <helib/ArgMap.h>
```

### **Functions**

• int main (int argc, char \*argv[])

# **Variables**

• bool noPrint = true

# 8.98.1 Function Documentation

### 8.98.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

### 8.98.2 Variable Documentation

### 8.98.2.1 noPrint

```
bool noPrint = true
```

# 8.99 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_EvalMap.cpp File Reference

```
#include <NTL/BasicThreadPool.h>
#include <cassert>
#include <helib/EvalMap.h>
#include <helib/hypercube.h>
#include <helib/powerful.h>
#include <helib/ArgMap.h>
```

# **Namespaces**

- std
- NTL

# **Functions**

- void TestIt (long p, long r, long c, long \_k, long L, Vec< long > &mvec, Vec< long > &gens, Vec< long > &ords, long useCache)
- int main (int argc, char \*argv[])

# 8.99.1 Function Documentation

# 8.99.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.99.1.2 TestIt()

# 8.100 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_extractDigits.cpp File Reference

```
#include <NTL/ZZ.h>
#include <helib/EncryptedArray.h>
#include <helib/polyEval.h>
#include <helib/debugging.h>
#include <helib/ArgMap.h>
```

# **Functions**

• int main (int argc, char \*argv[])

# 8.100.1 Function Documentation

# 8.100.1.1 main()

```
int main (
                int argc,
                char * argv[] )
```

# 8.101 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_fatboot.cpp File Reference

```
#include <NTL/ZZ.h>
#include <NTL/fileio.h>
#include <NTL/BasicThreadPool.h>
#include <cassert>
#include <helib/EncryptedArray.h>
#include <helib/EvalMap.h>
#include <helib/powerful.h>
#include <helib/matmul.h>
#include <helib/debugging.h>
#include <helib/fhe_stats.h>
#include <helib/ArgMap.h>
```

### **Macros**

- #define OUTER REP (1)
- #define INNER\_REP (1)

# **Functions**

- void TestIt (long p, long r, long L, long c, long skHwt, int build\_cache=0)
- int main (int argc, char \*argv[])

# **Variables**

· long printFlag

### 8.101.1 Macro Definition Documentation

### 8.101.1.1 INNER\_REP

#define INNER\_REP (1)

### 8.101.1.2 OUTER REP

#define OUTER\_REP (1)

# 8.101.2 Function Documentation

# 8.101.2.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.101.2.2 TestIt()

# 8.101.3 Variable Documentation

# 8.101.3.1 printFlag

long printFlag

# 8.102 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_General.cpp File Reference

```
#include <NTL/ZZ.h>
#include <NTL/BasicThreadPool.h>
#include <helib/helib.h>
#include <NTL/lzz_pXFactoring.h>
#include <cassert>
#include <cstdio>
#include <helib/ArgMap.h>
#include <helib/fhe_stats.h>
```

# **Macros**

• #define debugCompare(ea, sk, p, c)

# **Functions**

- void TestIt (long R, long p, long r, long d, long c, long k, long w, long L, long m, const Vec< long > &gens, const Vec< long > &ords)
- int main (int argc, char \*\*argv)

# 8.102.1 Macro Definition Documentation

# 8.102.1.1 debugCompare

# 8.102.2 Function Documentation

# 8.102.2.1 main()

```
int main ( \label{eq:int_argc} \text{int } \textit{argc,} \label{eq:char_argv} \text{char } ** \textit{argv} \text{)}
```

# 8.102.2.2 TestIt()

# 8.103 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_intraSlot.cpp File Reference

```
#include <helib/intraSlot.h>
#include <helib/ArgMap.h>
```

# **Functions**

• int main (int argc, char \*\*argv)

# **Variables**

• bool verbose = false

# 8.103.1 Function Documentation

### 8.103.1.1 main()

```
int main (
          int argc,
          char ** argv )
```

# 8.103.2 Variable Documentation

### 8.103.2.1 verbose

bool verbose = false

# 8.104 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_IO.cpp File Reference

```
#include <cassert>
#include <fstream>
#include <unistd.h>
#include <NTL/ZZX.h>
#include <NTL/vector.h>
#include <helib/helib.h>
#include <helib/ArgMap.h>
```

# **Macros**

• #define N\_TESTS 3

# **Functions**

- void checkCiphertext (const Ctxt &ctxt, const ZZX &ptxt, const SecKey &sk)
- int main (int argc, char \*argv[])

# 8.104.1 Macro Definition Documentation

# 8.104.1.1 N TESTS

```
#define N_TESTS 3
```

# 8.104.2 Function Documentation

# 8.104.2.1 checkCiphertext()

# 8.104.2.2 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.105 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_matmul.cpp File Reference

```
#include <helib/matmul.h>
#include <NTL/BasicThreadPool.h>
#include <helib/fhe_stats.h>
#include <helib/randomMatrices.h>
#include <helib/ArgMap.h>
```

# **Functions**

- template<class Matrix >
  bool DoTest (const Matrix &mat, const EncryptedArray &ea, const SecKey &secretKey, bool minimal, bool verbose)
- void Testlt (Context &context, long dim, bool verbose, long full, long block)
- int main (int argc, char \*argv[])

# **Variables**

• int ks\_strategy = 0

# 8.105.1 Function Documentation

# 8.105.1.1 DoTest()

# 8.105.1.2 main()

```
int main (
                      int argc,
                      char * argv[] )
```

# 8.105.1.3 TestIt()

# 8.105.2 Variable Documentation

### 8.105.2.1 ks\_strategy

```
int ks\_strategy = 0
```

# 8.106 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_PAlgebra.cpp File Reference

```
#include <cassert>
#include <string>
#include <sstream>
#include <NTL/ZZ.h>
#include <helib/NumbTh.h>
#include <helib/Context.h>
#include <helib/ArgMap.h>
```

# **Functions**

• int main (int argc, char \*argv[])

# 8.106.1 Function Documentation

### 8.106.1.1 main()

```
int main (
                      int argc,
                      char * argv[] )
```

# 8.107 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_Permutations.cpp File Reference

```
#include <NTL/ZZ.h>
#include <helib/NumbTh.h>
#include <helib/timing.h>
#include <helib/permutations.h>
#include <helib/EncryptedArray.h>
#include <helib/ArgMap.h>
```

# **Functions**

- void testCtxt (long m, long p, long widthBound=0, long L=0, long r=1)
- void testCube (Vec< GenDescriptor > &vec, long widthBound)
- int main (int argc, char \*argv[])

# 8.107.1 Function Documentation

# 8.107.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.107.1.2 testCtxt()

```
void testCtxt ( long \ m, \\ long \ p, \\ long \ widthBound = 0, \\ long \ L = 0, \\ long \ r = 1 )
```

# 8.107.1.3 testCube()

# 8.108 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_PGFFT.cpp File Reference

```
#include <helib/PGFFT.h>
#include <iostream>
#include <cstdlib>
#include <ctime>
#include <algorithm>
#include <cmath>
#include <cstddef>
#include <cstdint>
#include <stdexcept>
#include #include #include #include 
#include 
#include 
#include #include #include #include 
#include #include #include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#include 
#inc
```

# **Namespaces**

• Fft

# **Typedefs**

- typedef long double Idbl
- typedef std::complex < |dbl > |cx
- typedef complex< double > cmplx\_t

# **Functions**

- void Fft::transform (std::vector < lcx > &vec)
- void Fft::inverseTransform (std::vector < lcx > &vec)
- void Fft::transformRadix2 (std::vector< lcx > &vec)
- void Fft::transformBluestein (std::vector< lcx > &vec)
- void Fft::convolve (const std::vector< lcx > &vecx, const std::vector< lcx > &vecy, std::vector< lcx > &vecy,
- int main ()

# 8.108.1 Typedef Documentation

# 8.108.1.1 cmplx\_t

typedef complex<double> cmplx\_t

# 8.108.1.2 lcx

typedef std::complex<ldbl> lcx

### 8.108.1.3 Idbl

typedef long double ldbl

# 8.108.2 Function Documentation

# 8.108.2.1 main()

```
int main ( )
```

# 8.109 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_PolyEval.cpp File Reference

```
#include <NTL/ZZ.h>
#include <helib/polyEval.h>
#include <helib/EncryptedArray.h>
#include <helib/ArgMap.h>
#include <helib/debugging.h>
```

# **Functions**

- bool testEncrypted (long d, const EncryptedArray &ea, const SecKey &secretKey)
- void testIt (long d, long k, long p, long r, long m, long L, bool isMonic=false)
- int main (int argc, char \*argv[])

### 8.109.1 Function Documentation

# 8.109.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

### 8.109.1.2 testEncrypted()

```
bool testEncrypted ( \log \ d, {\rm const} \ {\tt EncryptedArray} \ \& \ ea, {\tt const} \ {\tt SecKey} \ \& \ secretKey \ )
```

# 8.109.1.3 testIt()

```
void testIt (
            long d,
            long k,
            long p,
            long r,
            long m,
            long L,
            bool isMonic = false )
```

# 8.110 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_Powerful.cpp File Reference

```
#include <helib/hypercube.h>
#include <helib/powerful.h>
#include <helib/Context.h>
#include <helib/ArgMap.h>
```

# **Functions**

- void testSimpleConversion (const Vec< long > &mvec)
- void testHighLvlConversion (const Context &context, const Vec< long > &mvec)
- int main (int argc, char \*argv[])

### 8.110.1 Function Documentation

# 8.110.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.110.1.2 testHighLvlConversion()

# 8.110.1.3 testSimpleConversion()

```
void testSimpleConversion ( {\tt const\ Vec<\ long\ >\ \&\ mvec\ )}
```

# 8.111 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ ∨1.0.2/HElib/src/Test\_PtrVector.cpp File Reference

```
#include <cassert>
#include <iostream>
#include <NTL/tools.h>
#include <helib/NumbTh.h>
#include <helib/PtrVector.h>
#include <helib/PtrMatrix.h>
```

### **Classes**

· class MyClass

# **Typedefs**

- typedef PtrVector< MyClass > MyPtrVec
- typedef PtrVector VecT< MyClass > MyPtrVec Vec
- typedef PtrVector VecPt
   MyClass > MyPtrVec VecPt
- typedef PtrVector\_vectorT< MyClass > MyPtrVec\_vector
- typedef PtrVector\_vectorPt< MyClass > MyPtrVec\_vectorPt
- typedef PtrVector slice < MyClass > MyPtrVec slice
- typedef PtrMatrix < MyClass > MyPtrMat
- typedef PtrMatrix\_Vec< MyClass > MyPtrMat\_Vec
- typedef PtrMatrix\_ptVec< MyClass > MyPtrMat\_ptVec
- typedef PtrMatrix\_vector< MyClass > MyPtrMat\_vector
- typedef PtrMatrix\_ptvector < MyClass > MyPtrMat\_ptvector

### **Functions**

- template < typename T2 > bool compPointers (const MyPtrVec &a, T2 &b)
- void test1 (MyClass array[], int length, const MyPtrVec &ptrs)
- void test2 (MyClass \*array[], int length, const MyPtrVec &ptrs)
- void printPtrVector (const MyPtrVec &ptrs)
- void test3 (MyPtrVec &ptrs)
- template<typename T > void test4 (const MyPtrMat &mat, const T &array)
- template<typename T > void test5 (const MyPtrMat &mat, const T &array)
- int main ()

| Variables | Va | ria | bl | es |
|-----------|----|-----|----|----|
|-----------|----|-----|----|----|

• bool verbose = false

# 8.111.1 Typedef Documentation

# 8.111.1.1 MyPtrMat

typedef PtrMatrix<MyClass> MyPtrMat

# 8.111.1.2 MyPtrMat\_ptVec

typedef PtrMatrix\_ptVec<MyClass> MyPtrMat\_ptVec

# 8.111.1.3 MyPtrMat\_ptvector

typedef PtrMatrix\_ptvector<MyClass> MyPtrMat\_ptvector

# 8.111.1.4 MyPtrMat\_Vec

typedef PtrMatrix\_Vec<MyClass> MyPtrMat\_Vec

# 8.111.1.5 MyPtrMat\_vector

typedef PtrMatrix\_vector<MyClass> MyPtrMat\_vector

# 8.111.1.6 MyPtrVec

typedef PtrVector<MyClass> MyPtrVec

# 8.111.1.7 MyPtrVec\_slice

```
typedef PtrVector_slice<MyClass> MyPtrVec_slice
```

# 8.111.1.8 MyPtrVec\_Vec

```
typedef PtrVector_VecT<MyClass> MyPtrVec_Vec
```

# 8.111.1.9 MyPtrVec\_VecPt

```
typedef PtrVector_VecPt<MyClass> MyPtrVec_VecPt
```

# 8.111.1.10 MyPtrVec\_vector

```
typedef PtrVector_vectorT<MyClass> MyPtrVec_vector
```

# 8.111.1.11 MyPtrVec\_vectorPt

```
typedef PtrVector_vectorPt<MyClass> MyPtrVec_vectorPt
```

# 8.111.2 Function Documentation

# 8.111.2.1 compPointers()

# 8.111.2.2 main()

```
int main ( )
```

# 8.111.2.3 printPtrVector()

# 8.111.2.4 test1()

# 8.111.2.5 test2()

# 8.111.2.6 test3()

```
void test3 ( \label{eq:MyPtrVec & ptrs} \mbox{MyPtrVec & ptrs )}
```

# 8.111.2.7 test4()

# 8.111.2.8 test5()

# 8.111.3 Variable Documentation

### 8.111.3.1 verbose

```
bool verbose = false
```

# 8.112 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_Replicate.cpp File Reference

```
#include <cassert>
#include <NTL/lzz_pXFactoring.h>
#include <helib/helib.h>
#include <helib/replicate.h>
#include <helib/ArgMap.h>
```

# **Classes**

- class StopReplicate
- class ReplicateTester

# **Functions**

- void TestIt (long m, long p, long r, long d, long L, long bnd, long B)
- int main (int argc, char \*argv[])

# 8.112.1 Function Documentation

### 8.112.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.112.1.2 TestIt()

```
void TestIt (
    long m,
    long p,
    long r,
    long d,
    long L,
    long bnd,
    long B)
```

# 8.113 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_tableLookup.cpp File Reference

```
#include <iostream>
#include <cassert>
#include <NTL/BasicThreadPool.h>
#include <helib/intraSlot.h>
#include <helib/tableLookup.h>
#include <helib/ArgMap.h>
```

# **Functions**

- void testLookup (const SecKey &sKey, long insize, long outsize)
- void testWritein (const SecKey &sKey, long insize, long nTests)
- int main (int argc, char \*argv[])

# 8.113.1 Function Documentation

# 8.113.1.1 main()

```
int main (
                int argc,
                 char * argv[] )
```

# 8.113.1.2 testLookup()

# 8.113.1.3 testWritein()

# 8.114 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_thinboot.cpp File Reference

```
#include <NTL/BasicThreadPool.h>
#include <helib/helib.h>
#include <helib/matmul.h>
#include <helib/debugging.h>
#include <helib/fhe_stats.h>
#include <helib/ArgMap.h>
#include <algorithm>
#include <cmath>
#include <string>
```

# **Functions**

- void TestIt (long p, long r, long L, long c, long skHwt, int build\_cache=0)
- int main (int argc, char \*argv[])

# 8.114.1 Function Documentation

# 8.114.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.114.1.2 TestIt()

# File Reference 8.115 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_ThinBootstrapping.cpp File Reference

```
#include <NTL/BasicThreadPool.h>
#include <cassert>
#include <helib/helib.h>
#include <helib/matmul.h>
#include <helib/debugging.h>
#include <helib/ArgMap.h>
```

# **Macros**

- #define num\_mValues (sizeof(mValues)/(14\*sizeof(long)))
- #define OUTER REP (1)

# **Functions**

- void Testlt (long idx, long p, long r, long L, long c, long skHwt, int build\_cache=0)
- int main (int argc, char \*argv[])

# 8.115.1 Macro Definition Documentation

### 8.115.1.1 num\_mValues

```
#define num_mValues (sizeof(mValues)/(14*sizeof(long)))
```

### 8.115.1.2 OUTER\_REP

```
#define OUTER_REP (1)
```

### 8.115.2 Function Documentation

# 8.115.2.1 main()

```
int main (
                      int argc,
                      char * argv[] )
```

# 8.115.2.2 TestIt()

```
void TestIt (
            long idx,
            long p,
            long r,
            long L,
            long c,
            long skHwt,
            int build_cache = 0 )
```

# 8.116 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_ThinEvalMap.cpp File Reference

```
#include <cassert>
#include <helib/helib.h>
#include <helib/EvalMap.h>
#include <NTL/BasicThreadPool.h>
#include <helib/ArgMap.h>
```

# **Functions**

- void TestIt (long p, long r, long c, long \_k, long w, long L, Vec< long > &mvec, Vec< long > &gens, Vec< long > &ords, long useCache)
- int main (int argc, char \*argv[])

# 8.116.1 Function Documentation

# 8.116.1.1 main()

```
int main (
          int argc,
          char * argv[] )
```

# 8.116.1.2 TestIt()

# 8.117 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/Test\_Timing.cpp File Reference

```
#include <cassert>
#include <cstdio>
#include <memory>
#include <NTL/ZZ.h>
#include <NTL/BasicThreadPool.h>
#include <helib/helib.h>
#include <helib/matmul.h>
#include <helib/replicate.h>
#include <helib/permutations.h>
#include <helib/ArgMap.h>
#include <helib/debugging.h>
#include <helib/randomMatrices.h>
```

### **Classes**

- class LowLvlTimingData
- class HighLvlTimingData
- class OtherTimingData
- class TimingData
- class ReplicateDummy

# **Macros**

• #define numTests 11

### **Functions**

- void timeInit (long m, long p, long r, long d, long L, long nTests)
- long rotationAmount (const EncryptedArray &ea, const PubKey &publicKey, bool onlyWithMatrix)
- void timeOps (const EncryptedArray &ea, const PubKey &publicKey, Ctxt &ret, const vector < Ctxt > &c, ZZX &p, long nTests, LowLvlTimingData &td)
- void timeHighLvI (const EncryptedArray &ea, const PubKey &publicKey, Ctxt &ret, const vector< Ctxt > &c, GeneratorTrees &trees, long nTests, HighLvITimingData &td)
- void Timelt (long m, long p, TimingData &data, bool high=false)
- void printTimeData (TimingData &td)
- int main (int argc, char \*argv[])

### 8.117.1 Macro Definition Documentation

### 8.117.1.1 numTests

#define numTests 11

# 8.117.2 Function Documentation

# 8.117.2.1 main()

```
int main (
                      int argc,
                      char * argv[] )
```

# 8.117.2.2 printTimeData()

# 8.117.2.3 rotationAmount()

# 8.117.2.4 timeHighLvI()

# 8.117.2.5 timeInit()

```
void timeInit (
    long m,
    long p,
    long r,
    long d,
    long L,
    long nTests )
```

### 8.117.2.6 Timelt()

cannot test high-level routines at level <8

# 8.117.2.7 timeOps()

# 8.118 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/timing.cpp File Reference

```
#include <algorithm>
#include <utility>
#include <cstring>
#include <ctime>
#include <helib/timing.h>
```

# **Namespaces**

helib

# **Functions**

- unsigned long helib::GetTimerClock ()
- bool helib::timer\_compare (const FHEtimer \*a, const FHEtimer \*b)
- void helib::registerTimer (FHEtimer \*timer)
- void helib::resetAllTimers ()
- void helib::printAllTimers (std::ostream &str=std::cerr)

Print the value of all timers to stream.

- const FHEtimer \* helib::getTimerByName (const char \*name)
- bool helib::printNamedTimer (std::ostream &str, const char \*name)

# **Variables**

• const unsigned long helib::CLOCK\_SCALE = (unsigned long)CLOCKS\_PER\_SEC

# 8.119 /Users/Projects/FHE\_HElib\_Repos\_Public\_staging/homenc\_ v1.0.2/HElib/src/zzX.cpp File Reference

```
#include <mutex>
#include <map>
#include <helib/PAlgebra.h>
#include <helib/timing.h>
#include <helib/zzX.h>
```

# **Namespaces**

· helib

# **Functions**

- void helib::MulMod (zzX &res, const zzX &a, const zzX &b, const PAlgebra &palg)
- void helib::add (zzX &res, const zzX &a, const zzX &b)
- void helib::mul (zzX &res, const zzX &a, long b)
- void helib::div (zzX &res, const zzX &a, long b)
- void helib::normalize (zzX &f)
- const NTL::zz\_pXModulus & helib::getPhimXMod (const PAlgebra &palg)
- void helib::reduceModPhimX (zzX &poly, const PAlgebra &palg)
- zzX helib::balanced\_zzX (const NTL::zz\_pX &f)
- zzX helib::balanced\_zzX (const NTL::GF2X &f)

# 8.119.1 Detailed Description

• manipulating polynomials with single-precision coefficient It is assumed that the result is also single-precision