Chapter 3: The Logic of Types, Part II Disjunction types

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Tuples with names: "case classes"

- Pair of values: val a: (Int, String) = (123, "xyz")
- For convenience, we can define a name for this type:
 type MyPair = (Int, String); val a: MyPair = (123, "xyz")
- We can define a name for each value and also for the type:

```
case class MySocks(size: Double, color: String)
val a: MySocks = MySocks(10.5, "white")
```

Case classes can be nested:

```
case class BagOfSocks(socks: MySocks, count: Int)
val bag = BagOfSocks(MySocks(10.5, "white"), 6)
```

Parts of the case class can be accessed by name:
 val c: String = bag.socks.color

- Parts can be given in any order by using names:
 val y = MySocks(color = "black", size = 11.0)
- Default values can be defined for parts:

```
case class Shirt(color: String = "blue", hasHoles: Boolean = false)
val sock = Shirt(hasHoles = true)
```

Tuples with one element and with zero elements

- A tuple type expression (Int, String) is special syntax for parameterized type Tuple2[Int, String]
- Case class with no parts is called a "case object"
- What are tuples with one element or with zero elements?
 - ► There is no TupleO it is a special type called Unit

Tuples	Case classes
(123, "xyz"): Tuple2[Int, String]	case class A(x: Int, y: String)
(123,): Tuple1[Int]	case class B(z: Int)
(): Unit	case object C

- Case classes can have one or more type parameters:
 case class Pairs [A, B] (left: A, right: B, count: Int)
- The "Tuple" types could be defined by this code: case class Tuple2[A, B] (_1: A, _2: B)

Pattern-matching syntax for case classes

Scala allows pattern matching in two places:

- val pattern = ... (value assignment)
- case pattern ⇒ ... (partial function)

Examples with case classes:

```
val a = MySocks(10.5, "white")
val MySocks(x, y) = a
val f: BagOfSocks⇒Int = { case BagOfSocks(MySocks(s, c), z)⇒...}
def f(b: BagOfSocks): String = b match {
   case BagOfSocks(MySocks(s, c), z) ⇒ c
}
```

• Note: s, c, z are defined as pattern variables of correct types

Disjunction types

- Motivational examples:
 - ▶ The roots of a quadratic equation are either a pair, or one, or none
 - ▶ Binary search gives either a found value and an index, or nothing
 - ► Computations that give a value or an error with a text message
 - ► Computer game states: several kinds of rooms, types players, etc.
 - ★ Each kind of room may have different sets of properties
- We would like to be able to represent disjunctions of sets
 - ► A value that is either (Complex, Complex) or Complex or empty ()
 - ► A value that is either (Int, Int) or empty ()
 - ► A value that is either an Int value or a String error message
 - ▶ A value that is one case class out of a number of case classes
- Disjunction types represent such values as types

Disjunction type: Either[A, B]

Example: Either[String, Int] (may be used for error reporting)

- Represents a value that is either a String or an Int (but not both)
- Example values: Left("blah") or Right(123)
- Use pattern matching to distinguish "left" from "right":

```
def logError(x: Either[String, Int]): Int = x match {
  case Left(error) ⇒ println(s"Got error: $error"); -1
  case Right(res) ⇒ res
} // Left("blah") and Right(123) are possible values of type Either[String, Int]
```

- Now logError(Right(123)) returns 123 while logError(Left("bad result")) prints the error and returns -1
- The case expression chooses among possible values of a given type
 - Note the similarity with this code:

```
def f(x: Int): Int = x match {
  case 0 ⇒ println(s"error: must be nonzero"); -1
  case 1 ⇒ println(s"error: must be greater than 1"); -1
  case res ⇒ res
} // 0 and 1 are possible values of type Int
```

More general disjunction types: trait + case classes

A future version of Scala 3 has a short syntax for disjunction types:

- type MyIntOrStr = Int | String
- more generally, type MyType = List[Int] | (Int, Boolean) | MySocks
 - ► Some libraries (scalaz, cats, shapeless) also provide shorter syntax

```
For now, in Scala 2, we use the "long syntax":
```

```
(specify names for each case and for each part, use "trait" / "extends")
```

```
sealed trait MyType
final case class HaveListInt(x: List[Int]) extends MyType
final case class HaveIntBool(s: Int, b: Boolean) extends MyType
final case class HaveSocks(socks: MySocks) extends MyType
```

Pattern-matching example:

```
val x: MyType = if (...) HaveSocks(...) else HaveListInt(...) ... // some other code here x match { case HaveListInt(1st) \Rightarrow ... case HaveIntBool(p, q) \Rightarrow ... case HaveSocks(s) \Rightarrow ...
```

The most often used disjunction type: Option[T]

A simple implementation:

```
sealed trait Option[T]
final case class Some[T](t: T) extends Option[T]
final case object None extends Option[Nothing]
```

Pattern-matching example:

```
def saveDivide(x: Double, y: Double): Option[Double] = {
   if (y == 0) None else Some(x / y)
// Example usage:
val result = safeDivide(1.0, q) match {
   case Some(x) ⇒ previousResult * x
   case None ⇒ previousResult // provide a default value
}
```

Many Scala library functions return an Option[T]

- find, headOption, reduceOption, get (for Map[K, V]), lift for Array[T]
 - ► Note: Option[T] is "collection-like": has map, flatMap, filter, exists...

Worked examples

- What problems can we solve now?
 - Represent values from disjoint sets as a single type
 - Use such values in collections safely
- Define a disjunction type DayOfWeek representing the seven days.
- Modify DayOfWeek so that the values additionally represent a restaurant name and total amount for Fridays and a wake-up time on Saturdays.
- Define a disjunction type RootsOfQuadratic that represents real-valued roots of the equation $x^2 + bx + c = 0$ for arbitrary real b, c. (The cases of interest are: no real roots; two equal roots; two unequal roots.) Implement solve2: ((Double, Double)) \Rightarrow RootsOfQuadratic.
- Define a function rootAverage: RootsOfQuadratic ⇒ Option[Double]
 that computes the average value of all real roots, returning None if the
 average is undefined.
- Generate 100 random coefficients b, c (uniformly distributed between
 −1 and 1) and compute the mean of rootAverage for them.
- Implement def f[A, B]: (Option[A], Option[B]) ⇒ Option[(A, B)]

Exercises II

- Define a disjunction type CellState representing the visual state of one cell in the "Minesweeper" game: A cell can be either closed, or display a bomb, or be open and display the number of neighbor bombs.
- ② Define a function from Seq[Seq[CellState]] to Int, counting the total number of cells with 0 neighbor bombs shown.
- Opening a disjunction type RootOfLinear representing all possibilities for the solution of the equation ax + b = 0 for arbitrary real a, b. (The cases of interest are: no roots; one root; all x are roots.) Implement the solution as a function solve1: ((Double, Double)) ⇒ RootOfLinear.
- Given a Seq[(Double, Double)] containing pairs (a, b) of the coefficients of ax + b = 0, use solve1 to produce a Seq[Double] containing the roots of that equation when a unique root exists.
- Opening by Define fully parametric functions having these types:
 - def f1[A, B]: Option[(A, B)] ⇒ (Option[A], Option[B])
 - ② def f2[A, B]: Either[A,B] ⇒ (Option[A], Option[B])
 - ② def f3[A,B,C]: Either[A, Either[B,C]] ⇒ Either[Either[A,B], C]