

Logic programming and types: An introduction to Mercury

Sergei Winitzki

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Logic programming as a DSL for logic puzzles (Prolog)

*All jumping creatures are green. All small jumping creatures are martians.
All green martians are intelligent.*

Ngtrks is small and green. Pgvdrk is a jumping martian.

Who is intelligent? (inspired by S. Lem, *Invasion from Aldebaran*)

```
small(ngtrks). green(ngtrks).  
martian(pgvdrk). jumping(pgvdrk).  
green(X) :- jumping(X).  
martian(X) :- small(X), jumping(X).  
intelligent(X) :- green(X), martian(X).  
?- intelligent(X).  
X = pgvdrk
```

- The runtime will perform a backtracking search for a proof
- Classical logic limited to Horn clauses = executable program

Mercury in a nutshell: a Prolog dialect with static types

- Mercury borrows these from Prolog: logical variables, predicates, rules
- Syntax and semantics is very close to Prolog
- Data structures: list, queue, hash map
- Flexible mode system, type checking, mode and type inference
- Polymorphic types and type classes, type quantifiers
- Termination analysis for predicates
- Functions as a primitive, on par with predicates
- Higher-order functions and higher-order predicates
- Compilation to C, Java, Erlang, .NET
 - ▶ Interop and type-level compatibility with these environments

Modes, determinism, types, I/O

- Predicate arguments must have **types**, **modes**, and **determinism**
- “Martians” requires a declaration of modes & determinism for `main`:

```
pred main(io::di, io::uo) is cc_multi.
```
- Input/output: Special syntax `!IO` means a pair of `io` (“world”) values
- Proof search may backtrack - the goal `intelligent(X)` may fail, so:

```
main(!IO) :- ( if intelligent(X) then write(X, !IO)
               else write_string("No solution", !IO) ).
```
- Determinism: `det`, `semidet`, `multi`, `nondet`, `failure`, `cc_multi`, `cc_nondet`
- Predefined modes: `in`, `out`, `di`, `uo`
 - ▶ A **mode** describes what happens to an LV during proof search:

```
:- mode out == (free >> ground).
:- mode uo == (free >> unique).
:- mode di == (unique >> dead).
```
 - ▶ User-defined modes are possible

Example: integer factorial

- Implementation as a predicate:

```
:- pred fact(int::in, int::out) is det.  
fact(N,F) :- ( if N <= 1 then F = 1 else fact(N-1, A), F = A*N ).
```

- Implementation as a function:

```
:- func fct(int) = int.  
fct(N) = ( if N <= 1 then 1 else N*fct(N-1) ).
```

- The generated code is *identical* in both cases!
 - However, predicates are **not** “functions returning Boolean”
- Type/mode/determinism are inferred and statically checked
- Order of goals* is inferred from modes rather than from code!

```
:- pred fact(int::in, int::out) is det.  
fact(N,F) :- ( if N <= 1 then F = 1 else F = A*N, fact(N-1, A) ).
```

Functions and expressions

- Functions are deterministic predicates with “in-out” mode
- Expressions are syntactic sugar for goals involving functions
- Hence, the general syntax for functions:
`fname(Arg1, Arg2, ...) = Result :- goal, goal, ..., Result = ...`
- “Lambda” predicate terms and function terms:

```
F1 = ( pred(N::in, X::out) is det :- fact(N, X) ).
```

```
F2 = fact . % same value as F1 by  $\eta$ -equivalence
```

```
F3 = ( func(N) = X :- X = fct(N) ).
```

```
F4 = fct. % same value as F3 by  $\eta$ -equivalence
```

- Higher-order predicates:
`map(fact, [1,3,5], Res)` will unify `Res` with `[1,6,120]`
 - ▶ Declaring higher-order predicate modes is verbose and complicated

Algebraic types and polymorphism

- Primitive types: `char`, `int`, `float`, `string`

- ▶ No “symbol literals” as in Prolog

- Predicate types, function types

- ▶ Type syntax: `pred(int::in, int::out)` and `func(int) = int`

- Tuples, unions

```
:- type mytype3 ---> point({int,int},string); ok(string); failed.
```

```
:- type list(T) ---> []; [ T | list(T) ]. % special syntax
```

```
:- type tree(T) ---> leaf; branch(tree(T), T, tree(T)).
```

- Records with accessors

```
:- type employee ---> employee(name :: string, id :: int).
```

```
X = employee(...), if X ^ name = "myself" then ...
```

Example: “reversible computation”

- Convert integers between unary encoding and native representation

```
:- type unary ---> z; s(unary). %   z;  s(z);  s(s(z));  etc.
:- pred unary_int(unary, int).
:- mode unary_int(in, out). % is det.
:- mode unary_int(out, in). % is multi.
unary_int(C, N) :- (
    C = z, N = 0 ;
    C = s(B), N = M+1, unary_int(B, M)
% goals will be reordered here depending on mode!
).
```

- The same code can unify `unary_int(s(s(z)), N)` or `unary_int(C, 3)`
 - ▶ Determinism and mode of predicates is inferred from use!
 - ▶ *Different code* is compiled for each declared mode of `unary_int(C, N)`

Type classes à la Haskell

• ***

Existential types

• ***

Limitations of Mercury

- No higher-order type constructors (e.g. cannot define “traversable functor” parameterized by “applicative functor”)
- No row polymorphism for records
- No partially instantiated values (e.g. difference lists)

Summary

- How to unite "logic programming" and "functional programming"
- Mercury = Prolog + modes + types
- Features of the Mercury programming language ([online link](#))