# Elm-style Functional Reactive Programming demystified

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SF Types, Theorems, and Programming Languages

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## What is "functional reactive programming"

#### FRP has little to do with...

- event-driven state machines
- message-passing concurrency and "actors"
- distributed computing on massively parallel load-balanced clusters
- ma/reduce, the "reactive manifesto", (insert latest fad here)...

#### FRP is...

- pure functions using temporal types as primitives
  - (temporal type pprox lazy stream of events)

# Transformational vs. reactive programs

Transformational programs	Reactive programs
example: pdflatex elm_talk.tex	example: any GUI program, OS
start, run, then stop	keep running indefinitely
read some input, write some output	wait for signals, send messages
execution: sequential, parallel	"main run loop" + concurrency
difficulty: algorithms	signal/response sequences
specification: classical logic?	classical temporal logic?
verification: proof of correctness?	model checking?
synthesis: extract code from proof?	temporal logic synthesis?
type theory: intuitionistic logic	intuitionistic <i>temporal</i> logic

### Difficulties in reactive programming

- Input signals may come at unpredictable times
  - ▶ Imperative updates are difficult to keep in the correct order
  - Flow of events becomes difficult to understand
- Asynchronous (out-of-order) callback structures are difficult to maintain
- Inverted control ("the system will call you") obscures the flow of data
- Some concurrency is usually required (e.g. background tasks)
  - Explicit multithreaded code is hard

#### Motivation for FRP

- Reactive programs work on infinite sequences of input/output values
- Main idea: make infinite sequences implicit, as a new "temporal" type
  - ightharpoonup (Elm) Signal lpha an infinite sequence of values of type lpha
  - ightharpoonup alternatively, a value of type lpha that "changes with time"
- Reactive programs are pure functions
  - lacktriangle a GUI is a pure function of type Signal Inputs ightarrow Signal View
  - lacktriangle a Web server is a pure function Signal Request ightarrow Signal Response
  - ▶ all mutation is **implicit** in Signal  $\alpha$ ; our code is 100% immutable
    - ★ instead of updating an x:Int, we define a temporal value of type Signal Int
  - asynchronous behavior is implicit: our code has no callbacks
  - concurrency / parallelism is implicit
    - ★ (the runtime needs to provide the required scheduling of events)

### Elm primitives

Reactive programs work with infinite sequences of input/output values

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### Part 2. Temporal logic and FRP

- Reminder (Curry-Howard): temporal logic expressions will be our types
- We only need to control the order of events: no hard real-time requirements
- How to understand temporal logic:
  - ▶ classical propositional logic ≈ Boolean arithmetic
  - ▶ intuitionistic propositional logic ≈ same but without true / false dichotomy
  - lacktriangle (linear-time) temporal logic pprox Boolean arithmetic for *infinite sequences*
  - ightharpoonup intuitionistic temporal logic pprox same but without true / false dichotomy
- In other words:
  - a temporal type represents a single infinite sequence of values

#### Boolean arithmetic: notation

- Classical propositional (Boolean) logic: T, F,  $a \lor b$ ,  $a \land b$ ,  $\neg a$ ,  $a \to b$
- A notation better adapted to school-level arithmetic: 1, 0, a+b, ab, a'
- ullet The only "new rule" is 1+1=1
- Define  $a \rightarrow b = a' + b$
- Some identities:

$$0a = 0$$
,  $1a = a$ ,  $a + 0 = a$ ,  $a + 1 = 1$ ,  
 $a + a = a$ ,  $aa = a$ ,  $a + a' = 1$ ,  $aa' = 0$ ,  
 $(a + b)' = a'b'$ ,  $(ab)' = a' + b'$ ,  $(a')' = a$   
 $a(b + c) = ab + ac$ ,  $(a + b)(a + c) = a + bc$ 

### Boolean arithmetic: example

Of the three suspects A, B, C, only one is guilty of a crime. Suspect A says: "B did it". Suspect B says: "C is innocent." The guilty one is lying, the innocent ones tell the truth.

$$\phi = \left(ab'c' + a'bc' + a'b'c\right)\left(a'b + ab'\right)\left(b'c' + bc\right)$$

**Simplify**: expand the brackets, omit aa', bb', cc', replace aa = a etc.:

$$\phi = ab'c' + 0 + 0 = ab'c'$$

The guilty one is A.

## Propositional linear-time temporal logic (LTL)

We work with infinite boolean sequences ("linear time")
 Boolean operations:

$$a = [a_0, a_1, a_2, ...];$$
  $b = [b_0, b_1, b_2, ...];$   $a + b = [a_0 + b_0, a_1 + b_1, ...];$   $a' = [a'_0, a'_1, ...];$   $ab = [a_0 b_0, a_1 b_1, ...]$ 

**Temporal** operations:

(Next) 
$$\mathbf{N}a = [a_1, a_2, ...]$$
  
(Sometimes)  $\mathbf{F}a = [a_0 + a_1 + a_2 + ..., a_1 + a_2 + ..., ...]$   
(Always)  $\mathbf{G}a = [a_0 a_1 a_2 a_3 ..., a_1 a_2 a_3 ..., a_2 a_3 ..., ...]$ 

Other notation (from modal logic):

$$Na \equiv \bigcirc a$$
;  $Fa \equiv \lozenge a$ ;  $Ga \equiv \Box a$ 

• Weak Until: pUq = p' holds from now on until q first becomes true

$$pUq = q + pN(q + pN(q + ...))$$

### Temporal logic redux

- LTL as type theory: do we use  $\mathbf{N}\alpha$ ,  $\mathbf{F}\alpha$ ,  $\mathbf{G}\alpha$  as new types?
- Are they to be functors, monads, ...?
- What is the operational semantics? (I.e., how to compile this?)

### Interpreting values typed by LTL

- What does it mean to have a value x of type, say,  $\mathbf{G}(\alpha \to \alpha \mathbf{U}\beta)$  ??
  - ▶  $x : \mathbf{N}\alpha$  means that  $x : \alpha$  will be available *only* at the *next* time tick  $(x \text{ is a deferred value} \text{ of type } \alpha)$
  - $x : \mathbf{F}\alpha$  means that  $x : \alpha$  will be available at *some* future tick(s) (x is an **event** of type  $\alpha$ )
  - $x : \mathbf{G}\alpha$  means that a (different) value  $x : \alpha$  is available at *every* tick (x is an **infinite stream** of type  $\alpha$ )
  - $x: \alpha \mathbf{U}\beta$  means a **finite stream** of  $\alpha$  that may end with a  $\beta$
- Some temporal axioms of intuitionistic LTL:

### Elm as an FRP language

ullet  $\lambda$ -calculus with type  ${f G}lpha$ , primitives map2, foldp, async

map2 : 
$$(\alpha \to \beta \to \gamma) \to \mathbf{G}\alpha \to \mathbf{G}\beta \to \mathbf{G}\gamma$$
 foldp :  $(\alpha \to \beta \to \beta) \to \beta \to \mathbf{G}\alpha \to \mathbf{G}\beta$  async :  $\mathbf{G}\alpha \to \mathbf{G}\alpha$ 

- (map2 makes **G** an applicative functor)
- async is a special scheduling instruction
- Limitations:
  - ▶ Cannot have a type  $G(G\alpha)$ , also not using N or F
  - Cannot construct temporal values by hand
  - ► This language is an *incomplete* Curry-Howard image of LTL!
  - ▶ I work after the boss comes by and until the phone rings:
     let after\_until w (b,r) = (w or b) and not r in
     foldp after\_until false (boss, phone)



### Conclusions and outlook

- LTL is not a good fit as a specification language for reactive programs
- LTL synthesis from specification is theoretical, not practical
- FRP tries to make specification closer to implementation
- There are some languages that implement FRP in various ad hoc ways
- The ideal is not (yet) reached

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#### **Abstract**

In my day job, most bugs come from imperatively implemented reactive programs. Temporal Logic and FRP are declarative approaches that promise to solve my problems. I will briefly review the motivations behind and the connections between temporal logic and FRP.

FRP can be defined as a  $\lambda$ -calculus with types given by a (limited subset of) propositional intuitionistic LTL. Although the Elm language uses a subset of LTL, it achieves high expressivity for GUI programming. I discuss the current limitations of Elm and outline some possible extensions.

My talk will be largely self-contained and should be understandable to anyone familiar with Curry-Howard and functional programming.

### Suggested reading

- E. Czaplicki, S. Chong. Asynchronous FRP for GUIs. (2013)
- E. Czaplicki. Concurrent FRP for functional GUI (2012).
- M. F. Dam. Lectures on temporal logic. Slides: Syntax and semantics of LTL, A Hilbert-style proof system for LTL
- E. Bainomugisha, et al. A survey of reactive programming (2013).
- W. Jeltsch. Temporal logic with Until, Functional Reactive Programming with processes, and concrete process categories. (2013).
- A. Jeffrey. LTL types FRP. (2012).
- D. Marchignoli. Natural deduction systems for temporal logic. (2002). See Chapter 2 for a natural deduction system for modal and temporal logics.