

## I. SYSTEM MODEL

Consider an IRS-aided multiuser SISO SWIPT system where the IRS not only assists the primal transmission but also retrieves Channel State Information (CSI) and harvests energy for its own operation. The single-antenna transmitter delivers information and power simultaneously, through the  $L$ -reflector IRS, to  $K$  single-antenna users over  $N$  orthogonal subbands. It is assumed that the IRS performs channel estimation in the first subframe and supports information and power transfer in the second subframe [1]. Due to the passive characteristics of IRS, we consider a Time-Division Duplexing (TDD) protocol where the CSI can be obtained by exploiting channel reciprocity. Perfect CSI is assumed at the AP and IRS to investigate the analytical upper-bound of the proposed system. The signals reflected by IRS for two and more times are assumed negligible and thus not considered. A quasi-static frequency-selective model is used for both the AP-user and AP-IRS-user links where the channels are assumed unchanged within each transmission frame. A superposition of multicarrier modulated and unmodulated waveforms, both transmitted on the same frequency bands, are designed adaptively to maximize the rate-energy tradeoff [2]. Note that although Frequency Selective Surface (FSS) has received much attention for wideband communications, active FSS requires RF-chains thus becomes prohibitive in IRS [3], [4]. Since passive FSS is not reconfigurable with fixed physical characteristics [5], we assume a frequency-flat IRS with same reflection coefficients for all subbands. Two practical receiver architectures proposed in [6], namely Time Switching (TS) and Power Splitting (PS), are investigated for the co-located information decoder and energy harvester. In the TS strategy, each transmission subframe is further divided into orthogonal data and energy slots with duration ratio  $(1 - \alpha)$  and  $\alpha$  respectively. Hence, the achievable rate-energy region can be obtained through a direct time sharing between wireless power transfer (WPT) with  $\alpha = 1$  and wireless information transfer (WIT) with  $\alpha = 0$ . The adjustment of  $\alpha$  has no impact on the transmit waveform and IRS elements design, since they are optimized individually in data and energy slots. In comparison, the PS scheme splits the received signal into data and energy streams with power ratio  $(1 - \rho)$  and  $\rho$ . As  $\rho$  is coupled with waveform and IRS design, we investigate the rate-energy region by placing different rate constraints and optimizing waveform, PS ratio and reflectors accordingly. Perfect synchronization is assumed among the three parties in both scenario.

### A. Transmitted Signal

1) *Modulated Information Waveform:* Assume the carrier are evenly spaced with equal bandwidth  $B_s$  such that the frequency of the  $n$ -th subband is  $f_n = f_0 + (n - 1)\Delta f$  ( $n = 1, \dots, N$ ). The information symbol  $\tilde{x}_{I,n}$  on subband  $n$  is a capacity-achieving i.i.d. Circular Symmetric Complex Gaussian (CSCG) variable with zero mean and unit variance (i.e.  $\tilde{x}_{I,n} \sim \mathcal{CN}(0, 1)$ ). Denote  $w_{I,n} = s_{I,n}e^{j\phi_{I,n}}$  as the information weight on the  $n$ -th subcarrier with magnitude  $s_{I,n}$  and phase  $\phi_{I,n}$ , the corresponding modulated symbol can be

expressed as  $x_{I,n} = \tilde{s}_{I,n}e^{j\tilde{\phi}_{I,n}}$ , with  $\tilde{s}_{I,n} = s_{I,n}|\tilde{x}_{I,n}|$  and  $\tilde{\phi}_{I,n} = \phi_{I,n} + \angle\tilde{x}_{I,n}$ , which also follows zero-mean CSCG distribution with variance equal to the subcarrier power (i.e.  $x_{I,n} \sim \mathcal{CN}(0, s_{I,n}^2)$ ). Therefore, the transmit information waveform at time  $t$  writes as

$$\begin{aligned} x_I(t) &= \sum_{n=1}^N \tilde{s}_{I,n}(t) \cos(2\pi f_n t + \tilde{\phi}_{I,n}(t)) \\ &= \Re \left\{ \sum_{n=1}^N x_{I,n}(t) e^{j2\pi f_n t} \right\} \\ &= \Re \left\{ \sum_{n=1}^N w_{I,n} \tilde{x}_{I,n}(t) e^{j2\pi f_n t} \right\} \end{aligned} \quad (1)$$

2) *Unmodulated Power Waveform:* As suggested in [2], [7], we use deterministic multisine waveform to boost the harvested energy. It has no randomness over time and the equivalent input power symbol  $\tilde{x}_{P,n}$  is a constant (i.e.  $\tilde{x}_{P,n} = 1$ ). Therefore, the power weight  $w_{P,n} = s_{P,n}e^{j\phi_{P,n}}$  represents the complex-valued sinewave (i.e.  $x_{P,n}(t) = w_{P,n}$ ) in the baseband (BB). The transmit power waveform at time  $t$  is given by

$$\begin{aligned} x_P(t) &= \sum_{n=1}^N s_{P,n}(t) \cos(2\pi f_n t + \phi_{P,n}(t)) \\ &= \Re \left\{ \sum_{n=1}^N x_{P,n}(t) e^{j2\pi f_n t} \right\} \\ &= \Re \left\{ \sum_{n=1}^N w_{P,n} e^{j2\pi f_n t} \right\} \end{aligned} \quad (2)$$

3) *Superposed Waveform:* At time  $t$ , a superposition of the information and power waveform at subband  $n$  writes as

$$\begin{aligned} x_n(t) &= x_{I,n}(t) + x_{P,n}(t) \\ &= w_{I,n} \tilde{x}_{I,n}(t) + w_{P,n} \end{aligned} \quad (3)$$

Hence, the transmitted signal is summed over all subbands

$$\begin{aligned} x(t) &= x_I(t) + x_P(t) \\ &= \Re \left\{ \sum_{n=1}^N (w_{I,n} \tilde{x}_{I,n}(t) + w_{P,n}) e^{j2\pi f_n t} \right\} \end{aligned} \quad (4)$$

### B. Composite Channel Model

Denote the baseband equivalent channels from the AP to users, from the AP to the IRS, and from the IRS to users as  $\mathbf{H}_D \in \mathbb{C}^{K \times N}$ ,  $\mathbf{H}_I \in \mathbb{C}^{L \times N}$ , and  $\mathbf{H}_R \in \mathbb{C}^{K \times NL}$  respectively. Specifically, the frequency response of direct and reflective links at subband  $n$  are  $\mathbf{h}_{D,n} = [h_{D,1,n}, \dots, h_{D,K,n}]^T \in \mathbb{C}^{K \times 1}$  and  $\mathbf{H}_{R,n} = [\mathbf{h}_{R,n,1}, \dots, \mathbf{h}_{R,n,L}] \in \mathbb{C}^{K \times L}$  with  $\mathbf{h}_{R,n,l} = [h_{R,1,n,l}, \dots, h_{R,K,n,l}]^T \in \mathbb{C}^{K \times 1}$ . Similarly, the  $n$ -th incident channel matrix writes as  $\mathbf{h}_{I,n} = [h_{I,n,1}, \dots, h_{I,n,L}]^T \in \mathbb{C}^{L \times 1}$ . We also denote the direct and reflective links of user  $k$  as  $\mathbf{h}_{D,k} = [h_{D,k,1}, \dots, h_{D,k,N}] \in \mathbb{C}^{1 \times N}$  and  $\mathbf{h}_{R,k} = [h_{R,k,1}, \dots, h_{R,k,N}] \in \mathbb{C}^{1 \times NL}$  with  $\mathbf{h}_{R,k,n} = [h_{R,k,n,1}, \dots, h_{R,k,n,L}] \in \mathbb{C}^{1 \times L}$ . Therefore, it

holds that  $\mathbf{H}_D = [\mathbf{h}_{D,1}, \dots, \mathbf{h}_{D,N}] = [\mathbf{h}_{D,1}^T, \dots, \mathbf{h}_{D,N}^T]^T$ ,  $\mathbf{H}_I = [\mathbf{h}_{I,1}, \dots, \mathbf{h}_{I,N}]$ , and  $\mathbf{H}_R = [\mathbf{H}_{R,1}, \dots, \mathbf{H}_{R,N}] = [\mathbf{h}_{R,1}^T, \dots, \mathbf{h}_{R,N}^T]^T$ . Element  $l$  of the IRS receives a superposed waveform through the multipath channel and redistributes it by adjusting the amplitude reflection coefficient  $\beta_l \in [0, 1]$  and phase shift  $\theta_l \in [0, 2\pi)$ . Each passive reflector absorbs a small portion  $(1 - \beta_l)$  of the signal to support CSI decoding and impedance matching. We construct a diagonal subband-wise IRS matrix by collecting the reflection coefficients onto the diagonal entries such that  $\mathbf{\Theta}_0 = \text{diag}(\beta_1 e^{j\theta_1}, \dots, \beta_L e^{j\theta_L}) \in \mathbb{C}^{L \times L}$ . With the assumption of frequency-flat reflection, the IRS matrix is formed by stacking  $\mathbf{\Theta}_0$  over  $N$  subbands as  $\mathbf{\Theta} = [\mathbf{\Theta}_0^T, \dots, \mathbf{\Theta}_0^T]^T \in \mathbb{C}^{NL \times L}$ . The IRS-aided extra link can be modeled as a concatenation of the AP-IRS channel, the IRS reflection matrix, and the IRS-user channel. Both direct and AP-IRS-user link contributes to the composite channel  $\mathbf{H} \in \mathbb{C}^{K \times N}$  as

$$\mathbf{H} = \mathbf{H}_D + \mathbf{H}_R \mathbf{\Theta} \mathbf{H}_I \quad (5)$$

whose  $(k, n)$ -th entry

$$h_{k,n} = h_{D,n,k} + \mathbf{h}_{R,k} \mathbf{\Theta} \mathbf{h}_{I,n} \quad (6)$$

represents the overall channel gain of user  $k$  at subband  $n$ . Hence, the  $n$ -th subchannel  $\mathbf{h}_n \in \mathbb{C}^{K \times 1}$  is

$$\mathbf{h}_n = \mathbf{h}_{D,n} + \mathbf{H}_R \mathbf{\Theta} \mathbf{h}_{I,n} \quad (7)$$

It is interesting to notice that the total frequency response at subband  $n$  depends on the reflective channel across all  $N$  subbands such that the frequency selectivity only comes from the direct and incident links. From another perspective, the composite channel  $\mathbf{h}_k \in \mathbb{C}^{1 \times N}$  for user  $k$  writes as

$$\mathbf{h}_k = \mathbf{h}_{D,k} + \mathbf{h}_{R,k} \mathbf{\Theta} \mathbf{H}_I \quad (8)$$

Therefore, we have  $\mathbf{H} = [\mathbf{h}_1, \dots, \mathbf{h}_N] = [\mathbf{h}_1^T, \dots, \mathbf{h}_N^T]^T$ .

### C. Received Signal

The RF signal received by user  $k$  captures the contribution of information and power waveforms through both direct and reflective links as

$$\begin{aligned} y_k(t) &= y_{I,k}(t) + y_{P,k}(t) \\ &= \Re \left\{ \sum_{n=1}^N (w_{I,n} \tilde{x}_{I,n}(t) + w_{P,n}) h_{k,n} e^{j2\pi f_n t} \right\} \end{aligned} \quad (9)$$

### D. Information Decoder

One major benefit of using proposed waveform is that the deterministic power term  $y_{P,k}(t)$  bears no information and creates no interference to the modulated information term  $y_{I,k}(t)$ . Therefore, the achievable rate of user  $k$  is expressed as

$$I_k(\mathbf{w}_I, \mathbf{\Theta}, \rho) = \sum_{n=1}^N \log_2 \left( 1 + \frac{(1 - \rho) |\mathbf{h}_{k,n} \mathbf{w}_{I,n}|^2}{\sigma_n^2} \right) \quad (10)$$

=?

where  $\sigma_n^2$  is the sum variance of the Gaussian noise at the RF-band and those introduced during the RF-to-BB conversion on subband  $n$ . A significant conclusion in [2] indicates that the rate 10 is always achievable with or without waveform cancellation, by subtracting the deterministic power component or constructing a translated codebook.

### E. Energy Harvester

Although the power term  $y_{P,k}(t)$  have no impact on communication, both  $y_{I,k}(t)$  and  $y_{P,k}(t)$  contribute to energy delivery in different manner. Consider the nonlinear diode model based on the Taylor expansion of a small signal model [2], [7], which highlights the dependency between the harvester output DC current and the received waveform by

$$i_{\text{out},k} \approx \sum_{i=0}^{\infty} k'_i R_{\text{ant}}^{i/2} \mathcal{E} \{ y_k(t)^i \} \quad (11)$$

where  $k'_i$  depends on  $i_{\text{out},k}$  and diode characteristics,  $R_{\text{ant}}$  is the impedance of receive antenna. With the assumption of evenly spaced frequencies,  $\mathcal{E} \{ y(t)^i \} = 0$  for odd  $i$  which has no contribution to DC components. [7] also demonstrated that to maximize  $i_{\text{out},k}$ , it suffices to maximize the monotonic target function truncated to the  $n_0$  order

$$\begin{aligned} z_{DC,k} &= \sum_{i \text{ even}, i \geq 2}^{n_0} k'_i R_{\text{ant}}^{i/2} \mathcal{E} \{ y_k(t)^i \} \\ &= \sum_{i \text{ even}, i \geq 2}^{n_0} k'_i R_{\text{ant}}^{i/2} \mathcal{E} \{ y_{P,k}(t)^i \} \\ &\quad + \sum_{i \text{ even}, i \geq 2}^{n_0} k'_i R_{\text{ant}}^{i/2} \mathcal{E} \{ \mathcal{A} \{ y_{I,k}(t)^i \} \} \end{aligned} \quad (12)$$

where  $k_i = i_s / i! (n v_t)^i$ ,  $i_s$  is saturation current,  $n$  is diode ideality factor,  $v_t$  is thermal voltage.

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