

**Abstract**—Simultaneous Wireless Information and Power Transfer (SWIPT) is severely restricted by the low power level of the receive Radio-Frequency (RF) signal. To tackle this problem, we introduce Intelligent Reflecting Surface (IRS) that brings a high passive beamforming gain to compensate the propagation loss and boost the energy efficiency with a low power consumption. This paper investigates an IRS-aided Orthogonal Frequency Division Multiplexing (OFDM) SWIPT system based on practical nonlinear harvester model, where a multi-antenna Access Point (AP) transmits information and energy simultaneously to a single-antenna user under the assist of IRS. We aim to maximize the Rate-Energy (R-E) region via jointly optimizing the transmit waveform at the AP, the phase shifts at the IRS, and the splitting ratio at the user. The problem is formulated as current maximization problem subject to rate constraint, and we propose an low-complexity alternating algorithm to obtain suboptimal solutions iteratively. Numerical results demonstrated that dedicated power signal is beneficial to multicarrier SWIPT, while IRS brings significant R-E region enlargement over benchmark schemes when properly configured.

## I. INTRODUCTION

### A. Simultaneous Wireless Information and Power Transfer

With the great advance in communication performance (throughput, latency, outage), the main challenge of wireless network has come to energy supply. Most existing mobile devices are powered by batteries that require frequent charging or replacement, which leads to high maintenance cost and thus restricts the scale of networks. Although solar energy and inductive coupling has become popular alternatives, the former depends on the environment while the latter has a very short operation range. Simultaneous Wireless Information and Power Transfer (SWIPT) is a promising solution to connect and power mobile devices via electromagnetic (EM) waves in the Radio-Frequency (RF) band. It provides low power (in  $\mu\text{W}$  level) but broad coverage (up to hundreds of meters) [1] in a sustainable and controllable manner. The decreasing trend in electronic power consumption also boosts the paradigm shift from dedicated power source to Wireless Power Transfer (WPT) and SWIPT.

The concept of SWIPT were first cast in [2], where the authors investigated the Rate-Energy (R-E) tradeoff for a flat Gaussian channel and some discrete channels. Two practical receiver structures were then proposed in [3], namely Time Switching (TS) that switches between Energy Harvesting (EH) and Information Decoding (ID) modes, and Power Splitting (PS) that splits the received signal into individual components. On top of this, [4] characterized the R-E region for a Multiple-Input Multiple-Output (MIMO) broadcast system under TS and PS setup. Information and power beamforming was then considered in multiuser Multi-Input Single-Output (MISO) systems to maximize the Weighted Sum-Power (WSP) subjective to Signal-to-Interference-plus-Noise Ratio (SINR) constraints [5]. Motivated by this, [6] investigated fundamental transceiver modules, information and power scheduling, and interference management for SWIPT systems. However, [7] pointed out that the Radio Frequency-to-Direct Current (RF-to-DC) conversion efficiency depends on the harvester input power level, which also suggested a parametric harvester

model based on curve fitting and proposed an iterative resource allocation algorithm. From another perspective, [8], [9] demonstrated that multisine waveform is more suitable for WPT as it outperforms single tone in both operation range and RF-to-DC efficiency. [10] derived a tractable nonlinear harvester model based on the Taylor expansion of diode I-V characteristics and proposed an adaptive waveform optimization algorithm to maximize the output DC current under rate constraints. Simulation and experiments demonstrated the benefit of modelling rectifier nonlinearity in system design [11], [12]. The work was extended to SWIPT in [13] where a superposition of modulated information waveform and multi-sine power waveform is optimized to enlarge the R-E region. In contrast, [14] suggested an adaptive dual-mode SWIPT, which alternates between single-tone transmission that exploits conventional modulation for high-rate applications and multi-sine transmission that encodes the information in the Peak-to-Average Ratio (PAPR) for power-demanding applications. By assuming On-Off-Keying (OOK) where bit 1 carries energy, [15] compared unary and Run-Length-Limited (RLL) code in terms of rate vs battery overflow/underflow probability, and adapted conventional modulation schemes to ensure WPT is only activated at the points with large offset. Also, a learning approach [16] demonstrated that the offset of the power symbol is positively correlated to the harvester energy constraint, while the information symbols are symmetrically distributed around the origin. It confirmed that the superposed waveform is feasible to enlarge R-E region when considering rectifier nonlinearity. SWIPT was also explored in the network design. [17] proposed a cooperative SWIPT Non-Orthogonal Multiple Access (NOMA) protocol with three user selection schemes such that the strong user assists the EH of the weak user. In [18], SWIPT based on Rate Splitting (RS) was formulated as a Weighted Sum-Rate (WSR) maximization problem subject to total harvested energy constraint for separated Information Receivers (IRs) and Energy Receivers (ERs).

### B. Intelligent Reflecting Surface

Intelligent Reflecting Surface (IRS) adapts the wireless environment to increase spectrum and energy efficiency. In practice, an IRS consists of multiple individual reflecting elements that adjust the amplitude and phase of the incident signal through passive beamforming. Different from relay and backscatter communication, IRS assists the primary transmission without any active components, leading to low power consumption and no thermal noise added to the reflected signal. Compared with the linear increase in Amplify-and-Forward (AF) relay, the received power scales quadratically with the number of reflectors [19], since more reflectors boost the power collected by IRS and increase the array gain in its equal gain transmission.

Inspired by the advance in real-time reconfigurable metamaterials [20], [21] introduced a programmable metasurface that steers or polarizes the EM wave at specific frequency to mitigate signal attenuation. At the same time, [22] constructed an adjustable reflect array that ensures reliable millimeter-wave (mmWave) communication based on a beam-searching

algorithm to reduce indoor signal blockage. Motivated by this, [23], [19] introduced an IRS-assisted MISO system and proposed a beamforming algorithm that jointly optimizes the precoder at the Access Point (AP) and the phase shifts at the IRS to maximize Signal-to-Noise Ratio (SNR). The active and passive beamforming problem was extended to the discrete phase shift case [24] and the multiuser case [25]. In [26], channel estimation for Time-Division Duplex (TDD) systems was carried through a two-stage Minimum Mean Squared Error (MMSE)-based protocol that sequentially estimates the cascaded channel of each IRS element with the others switched off. Starting from the impedance equation, [27] investigated the influence of phase shift on the reflection amplitude and proposed a parametric IRS model via curve fitting. Recent research also explored the opportunity of integrating IRS with Orthogonal Frequency-Division Multiplexing (OFDM) systems. [28] exploited spatial correlation to reduce estimation overhead and design complexity by assuming adjacent elements share a common reflection coefficient. On top of this, group-based OFDM channel estimation was investigated in [29]. By adjusting IRS over time slots, [30] introduced artificial diversity within coherence time and investigated resource allocation and IRS configuration per Resource Block (RB). Real-time high-definition video transmission was performed over a prototype constructed with Positive Intrinsic-Negative (PIN) diodes, which demonstrated the feasibility and benefit of IRS at GHz and mmWave frequency [31].

Most existing papers assume a Frequency-Flat (FF) IRS where all elements reflect different frequencies equally. Although Frequency-Selective Surface (FSS) has received much attention for wideband communications, it is prohibitive since active FSS requires RF-chains [32], [5] while passive FSS has fixed physical characteristics and unable to adjust channel adaptively [33].

### C. IRS-aided SWIPT

The effective channel enhancement and low power consumption of IRS are expected to bring more opportunities to SWIPT. Based on linear harvester model and energy interference, [34] proved that at most one energy beam is required to maximize the WSP subject to SINR constraints. The fairness issue was then considered in [35], which maximize the minimum output power on the assumption of perfect energy interference cancellation. [36] proposed a novel penalty-based algorithm, whose inner layer employs Block Coordinate Descent (BCD) method to update precoders, phase shifts and auxiliary variables while the outer layer updates the penalty coefficients. It demonstrated that Line-of-Sight (LoS) links can boost the harvested power, as the rank-deficient channels are highly correlated and a single energy stream can satisfy the energy constraints of all ERs. In [37], the WSR maximization of MIMO SWIPT was first transformed to Weighted Minimum Mean Square Error (WMMSE) problem then solved by BCD with low-complexity iterative algorithms. However, most existing IRS-SWIPT papers focus on narrow-band transmission over linear harvester model.

### D. Objective and Methodology

In this paper, we study an IRS-aided broadband downlink MISO SWIPT system where the IRS assists the information and energy transmission of a single user. A multicarrier unmodulated power waveform (deterministic multisine) is superposed to a multicarrier modulated information waveform (e.g. OFDM) to boost the energy transfer efficiency without introducing additional interference. The transmit waveform, IRS phase shift and receive splitting ratio are jointly optimized to maximize the R-E tradeoff. Different from previous research, this paper focus on broadband SWIPT and investigates the fundamental impact of harvester nonlinearity on IRS design. We transform the R-E region characterization problem into multiple current maximization problems subject to different rate constraints. To reduce the design complexity, we propose an Alternating Optimization (AO) algorithm that updates the channel and transceiver iteratively based on Semidefinite Relaxation (SDR) and Geometric Programming (GP) technique. Numerical results showed that SDR is tight and the proposed algorithm can find a stationary point for all tested channel realizations. We demonstrate that dedicated power waveform boosts the energy transmission efficiency, such that TS and PS are preferred for low-rate and high-rate applications respectively. Also, IRS brings a significant channel amplification thus R-E enhancement especially when located near the transmitter/receiver, and the performance loss compared with ideal Frequency-Selective (FS) IRS decreases as the number of reflectors increases.

## II. SYSTEM MODEL

Consider an IRS-aided SWIPT system where a  $M$ -antenna transmitter delivers information and power simultaneously, through a  $L$ -reflector IRS, to a single-antenna user over  $N$  orthogonal subbands. We assume a total bandwidth  $B$  with evenly-spaced subbands centered at frequency  $f_n$  ( $n = 1, \dots, N$ ). Perfect Channel State Information (CSI) with negligible training overhead is assumed to explore the analytical upper-bound of the proposed design. A quasi-static block fading channel model is considered for all links, and we focus on one particular block where the channels are approximately unchanged. Two practical co-located receiver architectures are compared in terms of R-E region. Specifically, TS divides each time slot into orthogonal data and energy slots and performs a time sharing between WPT and Wireless Information Transfer (WIT). In comparison, PS splits the received signal into individual ID and EH streams such that the splitting ratio  $\rho$  is coupled with waveform and IRS design. Perfect synchronization is assumed among the three parties in both scenarios, and signals reflected by IRS for two and more times are omitted.

### A. Transmit Signal

Denote  $\tilde{x}_{I,n}(t)$  as the information symbol transmitted over subband  $n$ , which follows a capacity-achieving i.i.d. Circular Symmetric Complex Gaussian (CSCG) distribution with zero

mean and unit variance  $\tilde{x}_{I,n} \sim \mathcal{CN}(0, 1)$ . The superposed transmit signal on antenna  $m$  ( $m = 1, \dots, M$ ) at time  $t$  is

$$x_m(t) = \Re \left\{ \sum_{n=1}^N (w_{I,n,m} \tilde{x}_{I,n}(t) + w_{P,n,m}) e^{j2\pi f_n t} \right\} \quad (1)$$

where  $w_{I/P,n,m}$  denotes the weight on the information and power signal transmitted by antenna  $m$  at subband  $n$ . Define  $\mathbf{w}_{I/P,n} = [w_{I/P,n,1}, \dots, w_{I/P,n,M}]^T \in \mathbb{C}^{M \times 1}$  by stacking up weights across all antennas. Therefore, the transmit information and power signals write as

$$\mathbf{x}_I(t) = \Re \left\{ \sum_{n=1}^N \mathbf{w}_{I,n} \tilde{x}_{I,n}(t) e^{j2\pi f_n t} \right\} \quad (2)$$

$$\mathbf{x}_P(t) = \Re \left\{ \sum_{n=1}^N \mathbf{w}_{P,n} e^{j2\pi f_n t} \right\} \quad (3)$$

### B. Composite Channel

At subband  $n$ , denote the AP-user direct channel as  $\mathbf{h}_{D,n}^H \in \mathbb{C}^{1 \times M}$ , AP-IRS incident channel as  $\mathbf{H}_{I,n} \in \mathbb{C}^{L \times M}$ , and IRS-user reflective channel as  $\mathbf{h}_{R,n}^H \in \mathbb{C}^{1 \times L}$ . At the IRS, element  $l$  ( $l = 1, \dots, L$ ) redistributes the incoming signal by adjusting the reflection amplitude  $\gamma_l \in [0, 1]$  and phase shift  $\theta_l \in [0, 2\pi)$ <sup>1</sup>. On top of this, the IRS matrix collects the reflection coefficients onto the main diagonal entries as  $\mathbf{\Theta} = \text{diag}(\gamma_1 e^{j\theta_1}, \dots, \gamma_L e^{j\theta_L}) \in \mathbb{C}^{L \times L}$ . The extra link introduced by IRS can be modeled as a concatenation of the AP-IRS channel, IRS reflection, and IRS-user channel. On top of this, the total composite channel is formed by adding the IRS-aided extra channel to the AP-user direct channel as

$$\mathbf{h}_n^H = \mathbf{h}_{D,n}^H + \mathbf{h}_{R,n}^H \mathbf{\Theta} \mathbf{H}_{I,n} = \mathbf{h}_{D,n}^H + \phi^H \mathbf{V}_n \quad (4)$$

where  $\phi = [\gamma_1 e^{j\theta_1}, \dots, \gamma_L e^{j\theta_L}]^H \in \mathbb{C}^{L \times 1}$  and  $\mathbf{V}_n = \text{diag}(\mathbf{h}_{R,n}^H) \mathbf{H}_{I,n} \in \mathbb{C}^{L \times M}$ . Note that the Hermitian transpose in the definition of  $\phi$  makes its entries complex conjugate of the diagonal entries of  $\mathbf{\Theta}$ .

### C. Receive Signal

At the single-antenna receiver, the total received signal  $y(t) = y_I(t) + y_P(t)$  captures the contribution of information and power components over  $N$  subbands, where

$$y_I(t) = \Re \left\{ \sum_{n=1}^N \mathbf{h}_n^H \mathbf{w}_{I,n} \tilde{x}_{I,n}(t) e^{j2\pi f_n t} \right\} \quad (5)$$

$$y_P(t) = \Re \left\{ \sum_{n=1}^N \mathbf{h}_n^H \mathbf{w}_{P,n} e^{j2\pi f_n t} \right\} \quad (6)$$

<sup>1</sup>To investigate the performance upper bound of IRS, we suppose the reflection coefficient is maximized  $\gamma_l = 1 \forall l$  while the phase shift is a continuous variable over  $[0, 2\pi)$ .

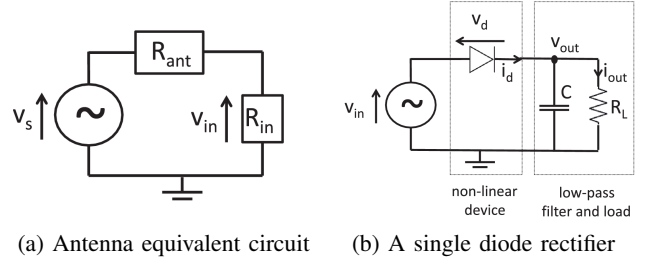


Fig. 1: Rectenna circuit

### D. Information Decoder

A major benefit of the proposed waveform is that the determined power waveform creates no interference to the information waveform. Therefore, the achievable rate writes as

$$\begin{aligned} R(\mathbf{w}_I, \phi, \rho) &= \sum_{n=1}^N \log_2 \left( 1 + \frac{(1-\rho) |\mathbf{h}_n^H \mathbf{w}_{I,n}|^2}{\sigma_n^2} \right) \\ &= \sum_{n=1}^N \log_2 \left( 1 + \frac{(1-\rho) |(\mathbf{h}_{D,n}^H + \phi^H \mathbf{V}_n) \mathbf{w}_{I,n}|^2}{\sigma_n^2} \right) \end{aligned} \quad (7)$$

where  $\sigma_n^2$  is the variance of the total noise (RF-band and RF-to-baseband conversion) on tone  $n$ . Rate 7 is achievable with either waveform cancellation or translated demodulation [38].

### E. Energy Harvester

In this section, we briefly revisit a tractable nonlinear rectenna model that relates the harvester output DC current to the received waveform [10], [38]. Fig. 1a illustrates the equivalent circuit of a lossless antenna, where the incoming signal creates an voltage source  $v_s(t)$  and the antenna has an impedance  $R_{\text{ant}}$ . Let  $R_{\text{in}}$  be the total input impedance of the rectifier and matching network. Assume the voltage across matching network is negligible and the RF-band noise is too small to harvest. When perfectly matched ( $R_{\text{in}} = R_{\text{ant}}$ ) with power splitting ratio  $\rho$ , the rectifier input voltage is  $v_{\text{in}}(t) = y(t) \sqrt{\rho R_{\text{ant}}}$ .

Rectifiers consist of nonlinear components as diode and capacitor to produce DC and store energy [39], [40]. Consider a simplified rectifier in Fig. 1b where a single series diode is followed by a low-pass filter with load. Denote  $v_d(t) = v_{\text{in}}(t) - v_{\text{out}}(t)$  as the voltage across the diode where  $v_{\text{out}}(t)$  is the output voltage across the load. A Taylor expansion of the diode characteristic equation  $i_d(t) = i_s (e^{v_d(t)/n'v_t} - 1)$  (with  $i_s$  the reverse bias saturation current,  $n'$  the diode ideality factor,  $v_t$  the thermal voltage) around a quiescent operating point  $v_d = a$  writes as  $i_d(t) = \sum_{i=0}^{\infty} k'_i (v_d(t) - a)^i$ , where  $k'_0 = i_s (e^{a/n'v_t} - 1)$  and  $k'_i = i_s e^{a/n'v_t} / i! (n'v_t)^i$ ,  $i = 1, \dots, \infty$ . Note that this small signal expansion model is only valid for the non-linear operation region, and the I-V relationship would be linear if the diode behavior is dominated by the load [10]. Also, an ideal low-pass filter with steady-state response can provide a constant  $v_{\text{out}}$  that depends on the

peak of  $v_{\text{in}}(t)$  [41]. Therefore, a proper choice of the operating voltage drop is  $a = \mathcal{E}\{v_d(t)\} = -v_{\text{out}}$  such that

$$i_d(t) = \sum_{i=0}^{\infty} k'_i \rho^{i/2} R_{\text{ant}}^{i/2} y(t)^i \quad (8)$$

By discarding non-DC components, taking expectation over symbol distribution, and truncating 8 to the  $n_0$ -th order, we approximate the average output DC current for a given channel as

$$i_{\text{out}}(t) = \mathcal{A}\{i_d(t)\} \approx \sum_{i=0}^{\infty} k'_i \rho^{i/2} R_{\text{ant}}^{i/2} \mathcal{E}\{\mathcal{A}\{y(t)^i\}\} \quad (9)$$

With the assumption of evenly spaced frequencies, it holds that  $\mathcal{A}\{y(t)^i\} = 0$  for odd  $i$  thus the related terms has no contribution to DC components. However,  $k'_i$  is still a function of  $i_{\text{out}}$ , and [10] proved that maximizing a truncated  $i_{\text{out}}$  is equivalent to maximizing a monotonic function

$$z(\mathbf{w}_I, \mathbf{w}_P, \phi, \rho) = \sum_{\substack{i \text{ even}, i \geq 2}}^{n_0} k_i \rho^{i/2} R_{\text{ant}}^{i/2} \mathcal{E}\{\mathcal{A}\{y(t)^i\}\} \quad (10)$$

where  $k_i = i_s / i! (nv_t)^i$ . It can be observed that the traditional linear harvester model, where the output DC power equals the sum of the power harvested on each frequency, is a special case of 10 with  $n_0 = 2$ . However, due to the coupling among different frequencies, some high-order terms also cancel out non-DC components thus contribute to the output DC power. In other words, even terms with  $i \geq 4$  account for the nonlinear behavior of the diode. For simplicity, we choose  $n_0 = 4$  to investigate fundamental nonlinearity and let  $\beta_2 = k_2 R_{\text{ant}}$ ,  $\beta_4 = k_4 R_{\text{ant}}^2$ . Note that  $\mathcal{E}\{|\tilde{x}_{I,n}|^2\} = 1$  but  $\mathcal{E}\{|\tilde{x}_{I,n}|^4\} = 2$  can be interpreted as a modulation gain on the nonlinear terms of the output DC current.

Similar to [42], we further stack up channel and waveform vectors over all subbands to define  $\mathbf{h} = [\mathbf{h}_1^H, \dots, \mathbf{h}_N^H]^H \in \mathbb{C}^{MN \times 1}$ ,  $\mathbf{w}_{I/P} = [\mathbf{w}_{I/P,1}^H, \dots, \mathbf{w}_{I/P,N}^H]^H \in \mathbb{C}^{MN \times 1}$ . Moreover, let  $\mathbf{W}_{I/P,n}$  keep the  $n$ -th ( $n = -N + 1, \dots, N - 1$ ) block diagonal of  $\mathbf{W}_{I/P} = \mathbf{w}_{I/P} \mathbf{w}_{I/P}^H$  and null the remaining entries. On top of this,  $z$  is reduced to 11 with DC terms expressed in 12 – 15.

#### F. Rate-Energy Region

Define the achievable R-E region as

$$C_{R_{\text{ID}}-I_{\text{EH}}}(P) \triangleq \left\{ (R_{\text{ID}}, I_{\text{EH}}) : R_{\text{ID}} \leq R, I_{\text{EH}} \leq z, \frac{1}{2} (\|\mathbf{w}_I\|^2 + \|\mathbf{w}_P\|^2) \leq P \right\} \quad (16)$$

where  $P$  is the average transmit power budget and the coefficient  $1/2$  converts the maximum power of sine waves to the average power.

### III. PROBLEM FORMULATION

We characterize the R-E region through multiple current maximization problems subject to transmit power, IRS magnitude, and different rate constraints

$$\max_{\mathbf{w}_I, \mathbf{w}_P, \phi, \rho} z(\mathbf{w}_I, \mathbf{w}_P, \phi, \rho) \quad (17a)$$

$$\text{s.t.} \quad \frac{1}{2} (\|\mathbf{w}_I\|^2 + \|\mathbf{w}_P\|^2) \leq P, \quad (17b)$$

$$R(\mathbf{w}_I, \phi, \rho) \geq \bar{R}, \quad (17c)$$

$$|\phi_l| = 1, \quad l = 1, \dots, L, \quad (17d)$$

$$0 \leq \rho \leq 1 \quad (17e)$$

Problem 17 is intricate with coupled variables involved in non-convex objective function 17a and rate constraint 17c. To reduce the design complexity, we propose an suboptimal AO algorithm that iteratively updates the IRS phase shift and transmit waveform together with receive splitting ratio until convergence.

#### A. IRS Phase Shift

In this section, the IRS phase shift  $\phi$  is optimized for any given waveform  $\mathbf{w}_{I/P}$  and splitting ratio  $\rho$ . We observe that

$$\begin{aligned} |\mathbf{h}_n^H \mathbf{w}_{I,n}|^2 &= \mathbf{w}_{I,n}^H \mathbf{h}_n \mathbf{h}_n^H \mathbf{w}_{I,n} \\ &= \mathbf{w}_{I,n}^H (\mathbf{h}_{D,n} + \mathbf{V}_n^H \phi) (\mathbf{h}_{D,n}^H + \phi^H \mathbf{V}_n) \mathbf{w}_{I,n} \\ &= \mathbf{w}_{I,n}^H \mathbf{M}_n^H \Phi \mathbf{M}_n \mathbf{w}_{I,n} \\ &= \text{Tr}(\mathbf{M}_n \mathbf{w}_{I,n} \mathbf{w}_{I,n}^H \mathbf{M}_n^H \Phi) \\ &= \text{Tr}(\mathbf{C}_n \Phi) \end{aligned} \quad (18)$$

where  $t$  is an auxiliary variable with unit modulus,  $\mathbf{M}_n = [\mathbf{V}_n^H, \mathbf{h}_{D,n}^H]^H \in \mathbb{C}^{(L+1) \times M}$ ,  $\phi = [\phi^H, t]^H \in \mathbb{C}^{(L+1) \times 1}$ ,  $\Phi = \phi \phi^H \in \mathbb{C}^{(L+1) \times (L+1)}$ ,  $\mathbf{C}_n = \mathbf{M}_n \mathbf{w}_{I,n} \mathbf{w}_{I,n}^H \mathbf{M}_n^H \in \mathbb{C}^{(L+1) \times (L+1)}$ . Similarly, we define  $t_{I/P,n}$  ( $n = -N + 1, \dots, N - 1$ ) as

$$\begin{aligned} t_{I/P,n} &= \mathbf{h}^H \mathbf{W}_{I/P,n} \mathbf{h} \\ &= \text{Tr}(\mathbf{h} \mathbf{h}^H \mathbf{W}_{I/P,n}) \\ &= \text{Tr}((\mathbf{h}_D + \mathbf{V}^H \phi) (\mathbf{h}_D^H + \phi^H \mathbf{V}) \mathbf{W}_{I/P,n}) \\ &= \text{Tr}(\mathbf{M}^H \Phi \mathbf{M} \mathbf{W}_{I/P,n}) \\ &= \text{Tr}(\mathbf{M} \mathbf{W}_{I/P,n} \mathbf{M}^H \Phi) \\ &= \text{Tr}(\mathbf{C}_{I/P,n} \Phi) \end{aligned} \quad (19)$$

where  $\mathbf{h}_D = [\mathbf{h}_{D,1}^H, \dots, \mathbf{h}_{D,N}^H]^H \in \mathbb{C}^{MN \times 1}$ ,  $\mathbf{V} = [\mathbf{V}_1, \dots, \mathbf{V}_N] \in \mathbb{C}^{L \times MN}$ ,  $\mathbf{M} = [\mathbf{V}^H, \mathbf{h}_D]^H \in \mathbb{C}^{(L+1) \times MN}$ ,  $\mathbf{C}_{I/P,n} = \mathbf{M} \mathbf{W}_{I/P,n} \mathbf{M}^H \in \mathbb{C}^{(L+1) \times (L+1)}$ . Therefore, the rate and objective expressions 7 and 11 rewrites as 20 and 21, respectively.

$$R(\Phi) = \sum_n \log_2 \left( 1 + \frac{(1-\rho) \text{Tr}(\mathbf{C}_n \Phi)}{\sigma_n^2} \right) \quad (20)$$

$$\begin{aligned}
z(\Phi) = & \frac{1}{2}\beta_2\rho(t_{I,0} + t_{P,0}) \\
& + \frac{3}{8}\beta_4\rho^2\left(2t_{I,0}^2 + \sum_{n=-N+1}^{N-1} t_{P,n}t_{P,n}^*\right) \\
& + \frac{3}{2}\beta_4\rho^2 t_{I,0}t_{P,0}
\end{aligned} \quad (21)$$

To maximize non-concave expression 21, we use first-order Taylor expansion to approximate its second-order terms. Based on the variables optimized at iteration  $i-1$ , the local approximation at iteration  $i$  suggests [43]

$$(t_{I,0}^{(i)})^2 \geq 2t_{I,0}^{(i)}t_{I,0}^{(i-1)} - (t_{I,0}^{(i-1)})^2 \quad (22)$$

$$t_{P,n}^{(i)}(t_{P,n}^{(i)})^* \geq 2\Re\left\{t_{P,n}^{(i)}(t_{P,n}^{(i-1)})^*\right\} - t_{P,n}^{(i-1)}(t_{P,n}^{(i-1)})^* \quad (23)$$

$$\begin{aligned}
t_{I,0}^{(i)}t_{P,0}^{(i)} &= \frac{1}{4}(t_{I,0}^{(i)} + t_{P,0}^{(i)})^2 - \frac{1}{4}(t_{I,0}^{(i)} - t_{P,0}^{(i)})^2 \\
&\geq \frac{1}{2}(t_{I,0}^{(i)} + t_{P,0}^{(i)})(t_{I,0}^{(i-1)} + t_{P,0}^{(i-1)}) \\
&\quad - \frac{1}{4}(t_{I,0}^{(i-1)} + t_{P,0}^{(i-1)})^2 - \frac{1}{4}(t_{I,0}^{(i)} - t_{P,0}^{(i)})^2
\end{aligned} \quad (24)$$

which provide lower bounds to the corresponding terms in 21. At iteration  $i$ , the approximated objection function  $\tilde{z}(\Phi^{(i)})$  is detailed in 25. Hence, problem 17 is transformed to

$$\max_{\Phi} \tilde{z}(\Phi) \quad (26a)$$

$$\text{s.t.} \quad R(\Phi) \geq \bar{R}, \quad (26b)$$

$$\Phi_{l,l} = 1, \quad l = 1, \dots, L+1, \quad (26c)$$

$$\Phi \succeq 0, \quad (26d)$$

$$\text{rank}(\Phi) = 1 \quad (26e)$$

Problem 26 is not a standard Semidefinite Programming (SDP) due to the rate constraint 26b. Therefore, even if we relax the rank constraint 26e to formulate a convex problem, there is no guarantee that the optimal rank-1 solution  $\bar{\Phi}^*$  extracted from  $\Phi^*$  is a stationary point of the original problem 17. In Section [TODO], we numerically show that  $\Phi^*$  is rank-1 for all tested channel realizations so that the performance loss is insignificant.

When  $\Phi^*$  is rank-1, the optimal phase shift vector  $\bar{\phi}^*$  is obtained by Eigenvalue Decomposition (EVD). Otherwise, a suboptimal solution can be extracted via Gaussian randomization method [44]. Specifically, we perform EVD  $\Phi^* = U\Sigma U^H$ , generate  $Q$  CSCG random vectors  $\mathbf{r}_q \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_{L+1})$ ,  $q = 1, \dots, Q$ , construct the corresponding candidates  $\bar{\phi}_q = e^{j\arg(U\Sigma^{1/2}\mathbf{r}_q)}$ , and choose the one that maximizes the objective function 26a. Finally, the phase shift is retrieved by  $\theta_l = \arg(\phi_l^*/\phi_{L+1}^*)$ ,  $l = 1, \dots, L$ . The algorithm for the phase shift optimization is summarized in Algorithm 1.

$$\begin{aligned}
z(\mathbf{w}_I, \mathbf{w}_P, \phi, \rho) = & \beta_2\rho\left(\mathcal{E}\{\mathcal{A}\{y_I^2(t)\}\} + \mathcal{A}\{y_P^2(t)\}\right) + \beta_4\rho^2\left(\mathcal{E}\{\mathcal{A}\{y_I^4(t)\}\} + \mathcal{A}\{y_P^4(t)\} + 6\mathcal{E}\{\mathcal{A}\{y_I^2(t)\}\}\mathcal{A}\{y_P^2(t)\}\right)
\end{aligned} \quad (11)$$

$$\mathcal{E}\{\mathcal{A}\{y_I^2(t)\}\} = \frac{1}{2}\sum_{n=1}^N (\mathbf{h}_n^H \mathbf{w}_{I,n})(\mathbf{h}_n^H \mathbf{w}_{I,n})^H = \frac{1}{2}\mathbf{h}^H \mathbf{W}_{I,0} \mathbf{h} \quad (12)$$

$$\mathcal{E}\{\mathcal{A}\{y_I^4(t)\}\} = \frac{3}{4}\left(\sum_{n=1}^N (\mathbf{h}_n^H \mathbf{w}_{I,n})(\mathbf{h}_n^H \mathbf{w}_{I,n})^H\right)^2 = \frac{3}{4}(\mathbf{h}^H \mathbf{W}_{I,0} \mathbf{h})^2 \quad (13)$$

$$\mathcal{A}\{y_P^2(t)\} = \frac{1}{2}\sum_{n=1}^N (\mathbf{h}_n^H \mathbf{w}_{P,n})(\mathbf{h}_n^H \mathbf{w}_{P,n})^H = \frac{1}{2}\mathbf{h}^H \mathbf{W}_{P,0} \mathbf{h} \quad (14)$$

$$\begin{aligned}
\mathcal{A}\{y_P^4(t)\} = & \frac{3}{8}\sum_{\substack{n_1, n_2, n_3, n_4 \\ n_1+n_2=n_3+n_4}} (\mathbf{h}_{n_1}^H \mathbf{w}_{P,n_1})(\mathbf{h}_{n_2}^H \mathbf{w}_{P,n_2})(\mathbf{h}_{n_3}^H \mathbf{w}_{P,n_3})(\mathbf{h}_{n_4}^H \mathbf{w}_{P,n_4})^H = \frac{3}{8}\sum_{n=-N+1}^{N-1} (\mathbf{h}^H \mathbf{W}_{P,n} \mathbf{h})(\mathbf{h}^H \mathbf{W}_{P,n} \mathbf{h})^H
\end{aligned} \quad (15)$$

$$\begin{aligned}
\tilde{z}(\Phi^{(i)}) = & \frac{1}{2}\beta_2\rho(t_{I,0}^{(i)} + t_{P,0}^{(i)}) \\
& + \frac{3}{8}\beta_4\rho^2\left(4(t_{I,0}^{(i)})(t_{I,0}^{(i-1)}) - 2(t_{I,0}^{(i-1)})^2 + \sum_{n=-N+1}^{N-1} 2\Re\left\{t_{P,n}^{(i)}(t_{P,n}^{(i-1)})^*\right\} - t_{P,n}^{(i-1)}(t_{P,n}^{(i-1)})^*\right) \\
& + \frac{3}{2}\beta_4\rho^2\left(\frac{1}{2}(t_{I,0}^{(i)} + t_{P,0}^{(i)})(t_{I,0}^{(i-1)} + t_{P,0}^{(i-1)}) - \frac{1}{4}(t_{I,0}^{(i-1)} + t_{P,0}^{(i-1)})^2 - \frac{1}{4}(t_{I,0}^{(i)} - t_{P,0}^{(i)})^2\right)
\end{aligned} \quad (25)$$

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**Algorithm 1** SDR: IRS Phase Shift
 

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1: Input  $\beta_2, \beta_4, \mathbf{h}_D, \mathbf{h}_I, \mathbf{h}_R, \mathbf{w}_I, \mathbf{w}_P, \rho, \sigma_n, \bar{R}, Q, \epsilon$ 
2: Construct  $\mathbf{M}, \mathbf{M}_n, \mathbf{C}_n$  for  $n = 1, \dots, N$ ,  $\mathbf{C}_{I/P,n}$  for  $n = -N + 1, \dots, N - 1$ 
3: Initialize  $i \leftarrow 0, \Phi^{(0)}, t_{I/P,n}^{(0)}, n = -N + 1, \dots, N - 1$ 
4: repeat
5:    $i \leftarrow i + 1$ 
6:   Obtain  $\Phi^{(i)}, t_{I/P,n}^{(i)}$  by solving problem 26
7:   Compute  $z^{(i)}$  by 21
8: until  $|(z^{(i)} - z^{(i-1)})/z^{(i)}| \leq \epsilon$ 
9: Set  $\Phi^* = \Phi^{(i)}$ 
10: if  $\text{rank}(\Phi^*) = 1$  then
11:   Obtain  $\bar{\phi}^*$  by  $\Phi^* = \bar{\phi}^* (\bar{\phi}^*)^H$ 
12: else
13:   Obtain  $\mathbf{U}, \Sigma$  by  $\Phi^* = \mathbf{U} \Sigma \mathbf{U}^H$ 
14:   Generate  $\mathbf{r}_q \sim \mathcal{CN}(\mathbf{0}, \mathbf{I}_{L+1})$ ,  $q = 1, \dots, Q$ 
15:   Construct  $\bar{\phi}_q = e^{j \arg(\mathbf{U} \Sigma^{1/2} \mathbf{r}_q)}$ ,  $\Phi_q = \bar{\phi}_q \bar{\phi}_q^H$ 
16:   Set  $q^* = \arg \max_q z(\Phi_q)$ ,  $\bar{\phi}^* = \bar{\phi}_{q^*}$ 
17: end if
18: Set  $\theta_l^* = \arg(\phi_l^* / \phi_{L+1}^*)$ ,  $l = 1, \dots, L$ 
19: Output  $\theta_l^*$ 

```

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### B. Waveform and Splitting Ratio

Next, we jointly optimize both information and power waveforms  $\mathbf{w}_{I/P}$  together with splitting ratio  $\rho$  for any given IRS phase shift  $\phi$ . As pointed out in [38], the waveform design in frequency and spatial domain can be decoupled without performance loss, and the optimal spatial weight is given by Maximum-Ratio Transmission (MRT) beamformer

$$\mathbf{w}_{I/P,n} = s_{I/P,n} \frac{\mathbf{h}_n^H}{\|\mathbf{h}_n\|} \quad (27)$$

That is to say, it is only necessary to determine the amplitudes  $s_{I/P,n}$  at different tones for single-user MISO SWIPT, and the original waveform optimization with  $2MN$  variables is converted into a power allocation problem with  $2N$  nonnegative real variables. Let  $\mathbf{s}_{I/P} = [s_{I/P,1}, \dots, s_{I/P,N}]^T \in \mathbb{C}^{N \times 1}$ . At subband  $n$ , the effective channel gain is given by  $\|\mathbf{h}_n\|$  and the power allocated to the modulated and unmodulated waveform are given by  $s_{I,n}^2$  and  $s_{P,n}^2$ , respectively. With such a beamformer selection, we have  $\mathbf{h}_n^H \mathbf{w}_{I,n} = |\mathbf{h}_n^H \mathbf{w}_{I,n}| = \|\mathbf{h}_n\| s_{I,n}$  such that the rate and objective expressions 7 and 11 reduces to 28 and 29.

$$R(\mathbf{s}_I, \rho) = \log_2 \left( \prod_{n=1}^N \left( 1 + \frac{(1-\rho)\|\mathbf{h}_n\|^2 s_{I,n}^2}{\sigma_n^2} \right) \right) \quad (28)$$

Therefore, 17 is reduced to an amplitude optimization problem

$$\max_{\mathbf{s}_I, \mathbf{s}_P, \rho} z(\mathbf{s}_I, \mathbf{s}_P, \rho) \quad (30a)$$

$$\text{s.t.} \quad \frac{1}{2} (\|\mathbf{s}_I\|^2 + \|\mathbf{s}_P\|^2) \leq P, \quad (30b)$$

$$R(\mathbf{s}_I, \rho) \geq \bar{R} \quad (30c)$$

Since problem 30 involves the production of nonnegative real variables, we introduce auxiliary variables  $t', \bar{\rho}$  and transform it into a reversed GP

$$\min_{\mathbf{s}_I, \mathbf{s}_P, \rho, \bar{\rho}, t'} \frac{1}{t'} \quad (31a)$$

$$\text{s.t.} \quad \frac{1}{2} (\|\mathbf{s}_I\|^2 + \|\mathbf{s}_P\|^2) \leq P, \quad (31b)$$

$$\frac{t'}{z(\mathbf{s}_I, \mathbf{s}_P, \rho)} \leq 1, \quad (31c)$$

$$\frac{2\bar{R}}{\prod_{n=1}^N \left( 1 + \bar{\rho} \|\mathbf{h}_n\|^2 s_{I,n}^2 / \sigma_n^2 \right)} \leq 1, \quad (31d)$$

$$\rho + \bar{\rho} \leq 1 \quad (31e)$$

It is observed that the denominators of 31c, 31d are posynomials [45], and we further express them in a compact form

$$z(\mathbf{s}_I, \mathbf{s}_P, \rho) = \sum_{m_P} g_{m_P}(\mathbf{s}_I, \mathbf{s}_P, \rho) \quad (32)$$

$$1 + \frac{\bar{\rho} \|\mathbf{h}_n\|^2 s_{I,n}^2}{\sigma_n^2} = \sum_{m_{I,n}} g_{m_{I,n}}(s_{I,n}, \bar{\rho}) \quad (33)$$

where  $m_P, m_{I,n}$  are the number of monomials in the corresponding posynomials (obviously  $m_{I,n} = 2$ ). It is suggested in [38], [46] that posynomials 32 and 33 can be upper bounded by Arithmetic Mean-Geometric Mean (AM-GM) inequality such that problem 31 is equivalent to

$$\begin{aligned} \min_{\mathbf{s}_I, \mathbf{s}_P, \rho, \bar{\rho}, t'} \quad & \frac{1}{t'} \\ \text{s.t.} \quad & \frac{1}{2} (\|\mathbf{s}_I\|^2 + \|\mathbf{s}_P\|^2) \leq P, \\ & t' \prod_{m_P} \left( \frac{g_{m_P}(\mathbf{s}_I, \mathbf{s}_P, \rho)}{\gamma_{m_P}} \right)^{-\gamma_{m_P}} \leq 1, \\ & 2\bar{R} \prod_n \prod_{m_{I,n}} \left( \frac{g_{m_{I,n}}(s_{I,n}, \bar{\rho})}{\gamma_{m_{I,n}}} \right)^{-\gamma_{m_{I,n}}} \leq 1, \\ & \rho + \bar{\rho} \leq 1 \end{aligned} \quad (34)$$

where  $\gamma_{m_P}, \gamma_{m_{I,n}} \geq 0$ ,  $\sum_{m_P} \gamma_{m_P} = \sum_{m_{I,n}} \gamma_{m_{I,n}} = 1$ . The tightness of the AM-GM inequality depends on  $\{\gamma_{m_P}, \gamma_{m_{I,n}}\}$  that require successive update, and a feasible choice at iteration  $i$  is [38]

$$\gamma_{m_P}^{(i)} = \frac{g_{m_P}(\mathbf{s}_I^{(i-1)}, \mathbf{s}_P^{(i-1)}, \rho^{(i-1)})}{z(\mathbf{s}_I^{(i-1)}, \mathbf{s}_P^{(i-1)}, \rho^{(i-1)})} \quad (35)$$

$$\gamma_{m_{I,n}}^{(i)} = \frac{g_{m_{I,n}}(s_{I,n}^{(i-1)}, \bar{\rho}^{(i-1)})}{1 + \bar{\rho}^{(i-1)} \|\mathbf{h}_n\|^2 (s_{I,n}^{(i-1)})^2 / \sigma_n^2} \quad (36)$$

$\mathbf{s}_I, \mathbf{s}_P, \rho$  are updated iteratively until convergence and the GP algorithm is summarized in Algorithm 2. It is also known as a inner approximation algorithm that only provides a KKT solution [47].

### C. R-E Region Characterization

To characterize the R-E region, we initialize the algorithm to WPT mode and increase the rate constraint gradually to

**Algorithm 2** GP: Waveform and Splitting Ratio

---

```

1: Input  $\beta_2, \beta_4, \mathbf{h}, P, \sigma_n, \bar{R}, \epsilon$ 
2: Initialize  $i \leftarrow 0, \mathbf{s}_{I/P}^{(0)}, \rho^{(0)}$ 
3: repeat
4:    $i \leftarrow i + 1$ 
5:   Update  $\{\gamma_{m_P}, \gamma_{m_{I,n}}\}$  by 35, 36
6:   Obtain  $\mathbf{s}_{I/P}^{(i)}, \rho^{(i)}$  by solving problem 34
7:   Compute  $z^{(i)}$  by 29
8: until  $|(z^{(i)} - z^{(i-1)})/z^{(i)}| \leq \epsilon$ 
9: Retrieve  $\mathbf{w}_{I/P}^*$  by 27
10: Output  $\mathbf{w}_{I/P}^*, \rho^*$ 

```

---

obtain  $S$  boundary points. At each point, information and power waveform are initialized to WIT and WPT solutions.

1) *WIT*: Consider a rate maximization problem with given information waveform  $\mathbf{w}_I$  as

$$\max_{\Phi} \sum_n \log_2 \left( 1 + \frac{\text{Tr}(\mathbf{C}_n \Phi)}{\sigma_n^2} \right) \quad (37a)$$

$$\text{s.t. } \Phi_{l,l} = 1, \quad l = 1, \dots, L+1, \quad (37b)$$

$$\Phi \succeq 0, \quad (37c)$$

$$\text{rank}(\Phi) = 1 \quad (37d)$$

Problem 37 can be solved after SDR, and a best solution  $\bar{\Phi}^*$  can be obtained via Gaussian randomization method.  $\phi^*$  can be recovered by  $\phi_l^* = \phi_l^*/\phi_{L+1}^*$ ,  $l = 1, \dots, L$  and  $\mathbf{h}$  can be constructed by 4. On top of this, the optimal information waveform can be obtained by Maximum-Ratio Transmission (MRT). The IRS phase shift and information waveform are updated iteratively until convergence.

2) *WPT*: The current maximization problem can be solved by setting  $\rho = 1$ , removing the rate constraint in problem 26 and ?? then solving them iteratively.

3) *R-E Sample*: We propose a two-layer AO algorithm to maximize the R-E region where the outer loop updates the phase shifts and the inner loop updates the splitting ratio and waveform until convergence. It is summarized in Algorithm 3.

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**Algorithm 3** Outer Loop: Phase Shift, Waveform and Splitting Ratio

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```

1: Input  $\beta_2, \beta_4, \mathbf{h}_D, \mathbf{h}_I, \mathbf{h}_R, P, Q, S, \epsilon, \sigma_n \forall n$ 
2: Initialize  $i \leftarrow 0, \phi^{(0)}, \mathbf{h}^{(0)}, \mathbf{w}_{I/P}^{(0)}$  by WIT/WPT solutions
3: Obtain splitting ratio  $\rho^{(0)}$  and waveform  $\mathbf{w}_{I/P}^{(0)}$  by GP (Algorithm 2) or inner loop (Algorithm ??)
4: repeat
5:    $i \leftarrow i + 1$ 
6:   Update IRS phase shift  $\phi^{(i)}$  by Algorithm 1
7:   Update composite channel  $\mathbf{h}^{(i)}$  by 4
8:   Update splitting ratio  $\rho^{(i)}$  and waveform  $\mathbf{w}_{I/P}^{(i)}$  by GP (Algorithm 2) or inner loop (Algorithm ??)
9: until  $|(z^{(i)} - z^{(i-1)})/z^{(i)}| \leq \epsilon$ 
10: Output  $\mathbf{w}_{I/P}^*, \rho^*, R^*, z^*$ 

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$$\begin{aligned}
z(\mathbf{s}_I, \mathbf{s}_P, \rho) = & \frac{1}{2} \beta_2 \rho \sum_{n=1}^N \|\mathbf{h}_n\|^2 (s_{I,n}^2 + s_{P,n}^2) \\
& + \frac{3}{8} \beta_4 \rho^2 \left( 2 \sum_{n_1, n_2} \prod_{j=1}^2 \|\mathbf{h}_{n_j}\|^2 s_{I,n_j}^2 + \sum_{\substack{n_1, n_2, n_3, n_4 \\ n_1 + n_2 = n_3 + n_4}} \prod_{j=1}^4 \|\mathbf{h}_{n_j}\| s_{I,n_j} \right) \\
& + \frac{3}{2} \beta_4 \rho^2 \left( \sum_{n_1, n_2} \|\mathbf{h}_{n_1}\|^2 s_{I,n_1}^2 \|\mathbf{h}_{n_2}\|^2 s_{P,n_2}^2 \right)
\end{aligned} \quad (29)$$

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