

## ROTATE-SCALE-TRANSLATE (RST)

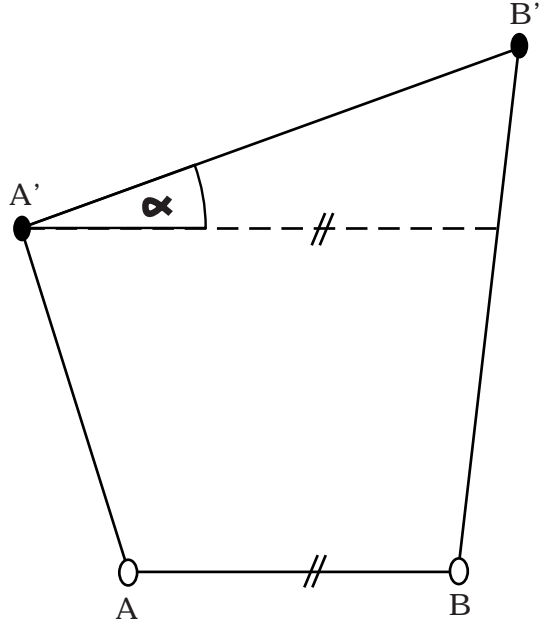


FIGURE 1. Two touch Rotate-Scale-Translate (RST) algorithm

The two touch RST algorithm: the initial two touch points  $A$  and  $B$  are dragged to the current two touch points  $A'$  and  $B'$ . From these four points we can calculate rotation, scaling and translation as follows. First, the rotation angle  $\alpha$  is defined by the angle between  $AB$  and  $A'B'$ .  $\alpha$  is calculated using the dot product:  $AB \cdot A'B' = |AB||A'B'| \cos \alpha$ . The scale factor is calculated from the ratio of the lengths of  $A'B'$  and  $AB$ . For rotation as well as for scaling, the centre of transformation is  $A$ . This plays a role only from the algorithmic point of view. For the user, it does not make a difference whether  $A$  is held fixed or  $B$  or even both touch points are dragged simultaneously. Translation is specified by the vector  $AA'$ . Once calculated, the three transformations can be accumulated into one transformation matrix.