

Polytopes

$$\mathcal{P} = \left\{ \sum_{i=1}^K \lambda_i v_i \in \mathbb{R}^K \mid \begin{array}{l} \sum_{i=1}^K \lambda_i = 1 \\ \lambda_i \geq 0 \\ v_i \in V \end{array} \right\}$$

$$V = \left\{ (0,0), \left(\frac{1}{2}, 0\right), \left(\frac{1}{2}, \frac{1}{4}\right), \left(0, \frac{1}{4}\right) \right\}$$

$$\lambda = \left(\frac{1}{4}, 0, \frac{1}{2}, \frac{1}{4} \right)$$

$$v = \frac{1}{4}(0,0) + 0\left(\frac{1}{2}, 0\right) + \frac{1}{2}\left(\frac{1}{2}, \frac{1}{4}\right) + \frac{1}{4}\left(0, \frac{1}{4}\right)$$

$$= \left(\frac{1}{4}, \frac{1}{8} + \frac{1}{2} \right) \in \mathcal{P}$$

