

Best response Polytopes

$(A, B) \in \mathbb{R}^{2 \times 2}$

row player best response polytope:

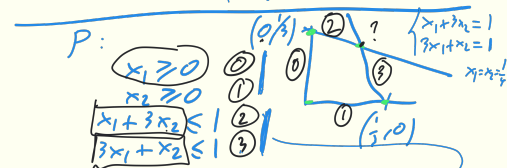
$$P = \{x \in \mathbb{R}^2 \mid x \geq 0, x_1 + 3x_2 \leq 1, 3x_1 + x_2 \leq 1\}$$

col player best response polytope:

$$Q = \{y \in \mathbb{R}^2 \mid y \geq 0, y_1 \leq 1, y_2 \leq 1\}$$

$A = \begin{pmatrix} 1 & -1 \\ -1 & 1 \end{pmatrix}$   $B = \begin{pmatrix} -1 & 1 \\ 1 & -1 \end{pmatrix}$

$A = \begin{pmatrix} 3 & 1 \\ 1 & 3 \end{pmatrix}$   $B = \begin{pmatrix} 1 & 3 \\ 3 & 1 \end{pmatrix}$



$(0,0)$   $\{0, 1\}$  "12 or 15"

$(\frac{1}{4}, \frac{1}{4})$   $\{1, 3\}$

$(0, \frac{1}{3})$   $\{0, 2, 4\}$

$(\frac{1}{3}, 0)$   $\{2, 3\}$

$P = \{x \in \mathbb{R}^2 \mid x \geq 0, x_1 + 3x_2 \leq 1, 3x_1 + x_2 \leq 1\}$

$A = \begin{pmatrix} 3 & 1 \\ 1 & 3 \end{pmatrix}$   $Q = \{y \in \mathbb{R}^2 \mid y_1 \leq 1, y_2 \leq 1, y \geq 0\}$



$(0,0)$   $\{2, 3\}$

$(\frac{1}{3}, 0)$   $\{0, 3\}$

$(0, \frac{1}{3})$   $\{1, 2\}$

$(\frac{1}{4}, \frac{1}{4})$   $\{0, 1\}$

$\{0, 2, 3\}$

$\left\{ \begin{pmatrix} 1 & 1 \\ 4 & 4 \end{pmatrix}, \begin{pmatrix} 1 & 1 \\ 4 & 4 \end{pmatrix} \right\}$  is fully labelled

$\left\{ \begin{pmatrix} 1 & 1 \\ 2 & 2 \end{pmatrix}, \begin{pmatrix} 1 & 1 \\ 2 & 2 \end{pmatrix} \right\}$  is a Nash equilibria