# Getting the Timing Right: Leveraging Category Inter-purchase Times to Improve Recommender Systems

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## **ABSTRACT**

In the marketing domain, models of grocery buying behavior consider purchase incidence as a key dimension. However, in recommender systems, timing is often subsumed under contextual information and has received little attention yet. For this reason, we analyze the relation between the timing of a recommendation and its acceptance across different product categories. Our study is based on a real-world deployment of an in-store recommendation system in the brick-and-mortar grocery industry. We base our analysis on transaction data of more than 100,000 unique users and more than four million product recommendations. Our findings suggest that the success of a recommendation significantly depends on the inter-purchase time within the respective category. Different sensitivities across product categories further stress the importance of timing and its interplay with category characteristics within the context of recommender systems. The insights gained in this study enable retailers to improve scheduling recommendations and target promotions more efficiently.

## **CCS Concepts**

•Information systems  $\rightarrow$  Computational advertising; Data mining; Data analytics; •Applied computing  $\rightarrow$  Online shopping;

## **Keywords**

inter-purchase times; category; retail; fast moving consumer goods

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RecSys '16, September 15 - 19, 2016, Boston, MA, USA

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DOI: http://dx.doi.org/10.1145/2959100.2959184

### 1. INTRODUCTION

Customer purchase decisions, both online and in-store, are to a great extent influenced by recommendations. They might be proactively inquired by customers seeking advice or provided by retailers leveraging their customers' past browsing or purchasing behaviors. In the latter scenario, a customer's interest in buying in a particular category at a particular time is not evident and needs to be inferred indirectly, a task often performed by automated recommender systems [2]. Consequently, recommender systems need to solve two questions in order to provide meaningful recommendations: First, whether or not to recommend a product and second, when to recommend it—thus, getting the timing right [12]. In contrast to common retailer promotions, personalized recommendations enable the promotion of specific products based on individual product and time preferences.

In this paper, the success of a recommendation—as indicated by the redemption of personalized in-store priceoff promotions—is modeled as a function of category interpurchase times. We find that inter-purchase times significantly influence the acceptance of recommendations with the effect depending on the respective product category. Particularly, in many fast moving categories, there is an optimal point in time for a product recommendation. Thus, incorporating category inter-purchase times can improve the accuracy of recommendations by up to 6 %<sup>1</sup>. Furthermore, we show that the optimal point in time for a recommendation does not coincide with average category inter-purchase times. Thus, recommendations can influence individual interpurchase times. Our findings contribute to the efficiency of personalized promotions and their successful implementation within recommendation schedules.

### 2. RELATED WORK

Traditionally, research on recommender systems has focused on developing distinct approaches for recommending products or services to users. For this reason, content-based [10], collaborative-filtering [8] and hybrid approaches

 $<sup>^{1}\</sup>mathrm{As}$  measured by the increase of correctly classified redemptions.

[4] have been advanced, incorporating information of the current system user, of similar peers or a combination of both. Yet, independently of the underlying approach, recommender systems have traditionally aimed at answering what to recommend to whom [12]. More recently, research has begun to further leverage context as a multidimensional feature. Such context-aware recommender systems incorporate all kinds of contextual information, depending on the dimension of the respective problem [1]. When a recommender system is used in a commercial context, it should ideally benefit both customers and retailers. While the former improve or facilitate their decision making [8], the latter can improve targeting and exploit cross- and up-selling opportunities [12]. Grocery purchase decisions are usually modeled as consisting of three dimensions, purchase incidence, brand choice and purchase quantity [7, 3]. Hence, customer purchases simultaneously cover the questions when to buy in a certain product category, which brand to buy and how much to buy. First, purchase volumes are assumed to be driven by household size, inventory levels, consumption rates as well as price promotions [7, 3]. The second dimension, brand choice, coincides with the main purpose of recommender systems and thus has been extensively covered in the respective literature [8]. The decision whether or not to buy a certain brand is driven by the entire product attributes including price. Finally, the last dimension describes the timing of a purchase which depends on consumption rates, inventory levels and in-store or price promotions [7, 3]. From a retailer perspective, recommendations are personalized promotions that allow for a precise targeting of single customers and can thus be used in order to influence any of the three dimensions of the customer purchase decision. Retailers can try to influence the timing of a purchase by providing customers with recommendations. The aspired purchase acceleration increases sales if customers do not only engage in stockpiling but adapt their consumption levels accordingly [9]. This is eventually dependent on the underlying product category and its characteristics. Moreover, well-timed promotional recommendations might encourage store switching. Customers would be expected to relocate purchases from competitors' stores to the focus retailer [11]. Thus, the timing of recommendations should receive a greater amount of attention in research on recommender systems, especially in industries where products are regularly re-bought and categories are characterized by distinct purchasing cycles.

# 3. METHOD AND DATA

To analyze the influence of category-specific inter-purchase times on the success of recommendations, an empirical study of transaction and recommendation data has been conducted at a brick-and-mortar grocery retailer. The results of the empirical analysis address the following questions: (1) Is there a category-specific optimal point in time for a product recommendation? (2) Can recommendations be used to influence individual inter-purchase times? (3) Does incorporating inter-purchase times have a positive effect on the redemption of a recommendation?

The studied in-store recommendation system provides customers with personalized product recommendations in the form of tailored price promotions. Customers can receive these personalized recommendations when they enter the store by scanning their loyalty card at special in-store kiosk terminals. The terminal prints a list of tailored price promo-

tions, in the form of individual discounts on selected products, for every customer. Price promotions are chosen from a specific set of currently active campaigns, which retailers and manufacturers can define to target specific consumers. The specific underlying algorithm is subject to our partner's secrecy. Campaigns are assigned using a dynamic scoring model estimating redemption probabilities based on a similiarty measure between a user's historic shopping baskets, the promoted products and an individual price-off derived from user heterogeneity in price sensitivity. Inter-purchase times are not considered in the scoring algorithm. Campaigns are then assigned to users maximizing total expected revenue constrained to specific campaign goal fulfillment criteria and filters. At the checkout promotions are automatically redeemed when the customer's loyalty card is scanned. As the loyalty program is completely anonymous, no demographics are available. In the following, we analyze transaction data that was collected in 2015 over a period of two months in more than 100 stores in a big European city. Our sample includes more than 100,000 unique users as well as more than four million product recommendations, out of which we analyze more than 500,000. The categorization is provided by a large market research organization. We limit our analysis to the top ten most recommended campaigns in our sample and pick four fast-moving categories which are regularly purchased—namely bread, cola, milk and curd. These are used for an examination of our proposed research questions. This allows us to identify and illustrate different patterns in the adoption and timing of recommendations.

# 3.1 Category Redemption Rates and Inter-purchase Times

To quantify the impact of inter-purchase times on category level redemptions, we conduct a linear regression of category redemption rates (abbreviated as RR) on the predictor "time since the last category purchase" (subsequently abbreviated as TSLP). In order to account for a potentially nonlinear relationship, we add a quadratic and cubic term of our TSLP variable to the regression. We hypothesize that for most categories c there is an optimal point in time for a recommendation that will correspond to the average category inter-purchase time. We expect recommendations made much earlier (low TSLP) to be penalized as customers inventory will not be low enough to induce another category purchase. Furthermore, we also expect lower redemption rates for customers that have not made purchases in the respective category for a long time (high TSLP). These could either have purchased at a competitor's store or become uninterested in the category itself.

$$RR_c(TSLP) = k_{c,0} + k_{c,1} \cdot TSLP + k_{c,2} \cdot TSLP^2$$

$$+k_{c,3} \cdot TSLP^3$$
(1)

Table 1 summarizes the results of the regression described in equation 1 for our four selected categories, while Figure 1 illustrates the corresponding fitted redemption rates. Apart from the category cola, all categories exhibit a characteristic inverse u-shape, indicating the existence of an optimal point in time for a category recommendation. For milk and curd, average inter-purchase times without promotion are higher than the optimal points in time for a recommendation. Thus, in these categories recommendations might trigger purchase acceleration. In the case of the category

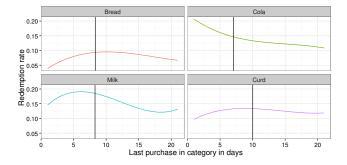


Figure 1: Comparing fitted redemption rates to avg. category inter-purchase times without promotions

cola, this effect might even be so strong that redemptions are highest right after a category purchase.

Table 1: Summary of regression results

	Dependent variable:					
	RR					
	Bread	Cola	Milk	Curd		
$\overline{TSLP}$	0.016*** (0.005)	$-0.017^{***}$ $(0.005)$	0.025*** (0.005)	0.013*** (0.004)		
$TSLP^2$	$-0.001^{**}$ $(0.001)$	0.001* (0.001)	$-0.003^{***}$ $(0.001)$	$-0.001^{**}$ $(0.0004)$		
$TSLP^3$	$0.00002 \\ (0.00002)$	-0.00002 $(0.00002)$	0.0001*** (0.00002)	$0.00003^* \ (0.00001)$		
Constant	$0.024^*$ $(0.013)$	0.223*** (0.014)	0.123*** (0.014)	0.085*** (0.010)		
	0.625 0.559 9.445***	0.843 0.816 30.540***	0.823 0.792 26.386***	0.543 0.462 6.725***		
Note:	*p<0.1; **p<0.05; ***p<0.01					

# 3.2 Changes in Individual Inter-purchase

In order to determine whether recommendations have an influence on individual category inter-purchase times, we split individual purchases, distinguishing category purchases that are affected by promotions from those that are not. In a first scenario, purchases are only affected by promotions when a promotion is redeemed during that particular purchase. In a second case, we also account for stockpiling, by including the purchase directly following a purchase on promotion into the promotion sample. In this way, we determine average inter-purchase times with and without promotional redemptions, considering only those customers for whom both inter-purchase times can be calculated. Using two-sided Kolmogorov-Smirnov tests (p<0.05), we analyze the average inter-purchase times in both scenarios. In the

first case, we find significant differences in average interpurchase times for all categories. In the second scenario, accounting for stockpiling, we find significant differences in average inter-purchase times for all categories except for curd, where customers might engage in stockpiling when redeeming a promotion.

## 3.3 Improving Redemption Classification

In order to test the validity of our findings we randomly split our data in an estimation and validation sample (2:1) and then train two different logistic regressions to predict coupon redemptions. First, the standard model only uses the scoring values (SCORE) provided by our research partner as a predictor, also accounting for the magnitude of the individual price discount. Second, the extended model additionally includes a variable that indicates the deviation of the TSLP variable from the optimal recommendation time, derived in our previous regression model. We allow the coefficient of this feature to vary depending on whether the recommendation was provided too early  $(d_{early})$  or too late  $(d_{late})$ . We analyze whether the incorporation of the optimal recommendation time leads to an improvement in the prediction of coupon redemptions. The standard model, implemented by our research partner, will serve as a baseline.

Table 2: Summary of classification estimation and validation results

	Dependent variable:					
	Redemption					
	Milk		Cola			
	Standard	Extended	Standard	Extended		
SCORE	1.440*** (0.045)	1.344*** (0.045)	2.672*** (0.207)	2.476*** (0.207)		
$d_{early}$		$-0.040^{***}$ $(0.011)$				
$d_{late}$		$-0.014^{***}$ $(0.001)$		$-0.014^{***}$ $(0.001)$		
Constant	$-2.116^{***}$ $(0.019)$	$-1.825^{***}$ $(0.026)$	$-2.401^{***}$ $(0.026)$	$-1.953^{***}$ $(0.030)$		
Observations LL AIC	30,881 $-11,770$ $23,545$	30,881 $-11,559$ $23,126$	$   \begin{array}{r}     33,032 \\     -10,762 \\     21,529   \end{array} $	$   \begin{array}{r}     33,032 \\     -10,471 \\     20,949   \end{array} $		
Recall	0.123	0.141	0.035	0.061		
Precision	0.524	(+14.6 %) 0.540 (+3.1 %)	0.339	(+74 %) 0.345 (+1.8 %)		
Prevalence	0.136	0.136	0.090	0.090		
Balanced Accuracy	0.553	0.561	0.514	0.524		
Note:	*p<0.1; **p<0.05; ***p<0.01					

We report the quality of our models on the hidden evaluation set for the two categories with the best model fit

<sup>&</sup>lt;sup>2</sup>It should further be noted that purchase volumes are not accounted for as we only focus on purchase incidence.

in our previous regression analysis: milk and cola. Table 1 summarizes the results of our classification model which will further be discussed with respect to the classification metrics precision and recall.<sup>3</sup> The standard model provides similar results for milk as obtained in previous studies within the retailing industry regarding the classification metrics [6]. The extended model, which incorporates the distance to the optimal recommendation time, improves precision by 3.1 % and recall by 14.6 % compared to the standard model. For the category cola, we can increase recall by 74 \%, however, precision can only be marginally increased by 1.8 %. We believe that our extended model can only marginally improve the correct classification in the second category due to the monotonous relationship between TSLP and overall redemption rates as indicated in Figure 1 and Table 1. Furthermore, we get similar precision improvements for the remaining two categories (bread 6.6 % and curd 2.4 %).

#### 4. CONCLUSION AND FUTURE WORK

Purchase incidence is a key pillar of every customer choice decision [7, 3]. Yet, so far it has only received marginal attention in the context of recommender systems. However, as commercial recommendations aim at influencing customer choices [2], purchase incidence should be incorporated when a recommendation is made. For this reason, we have analyzed customer data from an in-store recommendation system at a brick-and-mortar grocery retailer that provides customers with tailored price promotions. Our findings support the view that recommender systems should not only focus on the product or service to recommend but also on the timing of the recommendation [12]. Regarding the first research question we find that in many fast moving categories, there exists an optimal point in time for a recommendation which maximizes its acceptance among customers. In particular, we show that considering this optimum and categoryspecific individual inter-purchase times, has a positive effect on the success of recommendations, increasing precision by up to 6 %. Thus, answering the third research question, incorporating this additional information improves recommender systems. Moreover, we find that the optimal point in time for a recommendation precedes the average category inter-purchase time for most categories, indicating accelerated category purchases. Finally, regarding the second research question, we find that recommendations can influence individual inter-purchase times.

Altogether, the findings we present in this paper emphasize the importance of incorporating category-specific interpurchase times when making product recommendations. Yet, the data we have used for our analyses is limited to only four categories and two months. It would be worthwhile to analyze a larger number of categories and to extend the observation period in order to capture seasonality and model dynamic inter-purchase times. Furthermore, as we do not use scanner data but transaction data of a single retailer, we cannot directly account for category purchases at competitors' stores and for inventory building. However, in further analyses deviations from predicted parametric interpurchase times could help to indicate consumers' shopping

Recall: Number of instances in which coupon redemption was correctly predicted divided by all observed redemptions.

at other retailers [5]. This individual risk could be modeled using identifiers based on past purchases and category characteristics. Additionally, it should be noted that in our particular case, recommendations are combined with individual price discounts. Therefore, an analysis of the profitability a recommendation should further consider customers purchase decisions in the absence of a discount. Finally, these opportunities for further research will help to improve the timing of recommendations and design recommender systems that better address the needs of individual customers while leveraging category-specific inter-purchase times.

### 5. ACKNOWLEDGMENTS

We want to thank our research partner, who decided to remain anonymous, for providing us with the data sample.

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<sup>&</sup>lt;sup>3</sup>Precision: Number of instances in which coupon redemption was correctly predicted divided by all instances in which coupon redemption was predicted.