

QUESTION #11

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RED - BLACK TREE

How to insert a value in a red - black tree.

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TREES

## Solution

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If Tree is a non-empty tree :

1. Use the BST insert algorithm to add K to the tree
2. Color the node containing K red
3. Restore red-black tree properties(if necessary)

To restore the violated property, we use:

- 3.1. Recolouring
- 3.2. Rotation(Left, Right, Double)

Two cases based on color of Uncle(sibling of parent node)

- 3.3.1. If Uncle is red, we do recoloring
- 3.3.2. If Uncle is black, we do rotation and/or recoloring

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NERVING INTO  
DATA STRUCTURES

## Solution

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Now, Let  $x$  be the newly inserted node

If  $x$ 's Uncle is red and  $x$ 's parent is not black

1. Change the color of the parent and uncle as black
2. Change color of grandparent as red
3. Make  $x$ 's grandparent as the new  $x$ .
4. Repeat above steps on new  $x$ .

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NERVING INTO  
DATA STRUCTURES

## Solution

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If x's uncle is black and x's parent is not black then there can be four configurations for x

1. Left Left Case(parent is left child of grand parent and x is left child of parent)
  - 1.1 Right rotate grandparent
  - 1.2 Swap colors of parent and grandparent
2. Left Right Case(parent is left child of grandparent and x is right child of parent)
  - 2.1 Left rotate parent
  - 2.2 Apply Left Left Case(1)
3. Right Right Case (parent is right child of grand parent and x is right child of parent)
  - 3.1 Left rotate grandparent
  - 3.2 Swap colors of parent and grandparent
4. Right Left Case (parent is right child of grand parent and x is left child of parent)
  - 4.1 Right rotate parent
  - 4.2 Apply Right Right Case(3)