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## 1. Misc

### 1.1. Contest

#### 1.1.1. Makefile

```
1 .PRECIOUS: ./p%
3 %: p%
   ulimit -s unlimited && ./<
5 p%: p%.cpp
   g++ -o $@ $< -std=c++17 -Wall -Wextra -Wshadow \
   -fsanitize=address,undefined
```

#### 1.1.2. Default Code

```
1 #include <bits/stdc++.h>
3 #define pb      push_back
   #define eb      emplace_back
5 #define F      first
   #define S      second
7 #define SZ(v)   ((int)(v).size())
   #define ALL(v)  (v).begin(), (v).end()
9 #define MEM(a, b) memset(a, b, sizeof a)
   #define unpair(p) (p).F][p).S
11
   using namespace std;
13 using ll = long long;
   using ld = long double;
15 using LL = __int128;
   using pii = pair<int, int>;
17 using pll = pair<ll, ll>;
19 int main() { ios::sync_with_stdio(0), cin.tie(0); }
```

### 1.2. How Did We Get Here?

#### 1.2.1. Macros

Use vectorizations and math optimizations at your own peril.  
For gcc $\geq 9$ , there are `[[likely]]` and `[[unlikely]]` attributes.  
Call gcc with `-fopt-info-optimized-missed-optall` for optimization info.

```
1 #define _GLIBCXX_DEBUG      1 // for debug mode
   #define _GLIBCXX_SANITIZE_VECTOR 1 // for asan on vectors
3 #pragma GCC optimize("O3", "unroll-loops")
   #pragma GCC optimize("fast-math")
5 #pragma GCC target("avx,avx2,abm,bmi,bmi2") // tip: `lscpu`
   // before a loop
7 #pragma GCC unroll 16 // 0 or 1 -> no unrolling
   #pragma GCC ivdep
```

#### 1.2.2. constexpr

Some default limits in gcc (7.x - trunk):

- constexpr recursion depth: 512
- constexpr loop iteration per function: 262144
- constexpr operation count per function: 33554432
- template recursion depth: 900 (gcc *might* segfault first)

```
1 constexpr array<int, 10> fibonacci{[] {
   array<int, 10> a{};
3   a[0] = a[1] = 1;
   for (int i = 2; i < 10; i++) a[i] = a[i - 1] + a[i - 2];
5   return a;
   }()};
7 static_assert(fibonacci[9] == 55, "CE");
9
10 template <typename F, typename INT, INT... S>
   constexpr void for_constexpr(integer_sequence<INT, S...>,
11                               F &&func) {
12     int _[] = {(func(integer_constant<INT, S>{}), 0)...};
13 }
   // example
15 template <typename... T> void print_tuple(tuple<T...> t) {
   for_constexpr(make_index_sequence<sizeof...(T)>{}),
17                 [&](auto i) { cout << get<i>(t) << '\n'; });
2   }
2 }
```

#### 1.2.3. Bump Allocator

```
2 // global bump allocator
2 char mem[256 << 20]; // 256 MB
3 size_t rsp = sizeof mem;
2 void *operator new(size_t s) {
2     assert(s < rsp); // MLE
2     return (void *)&mem[rsp -= s];
7 }
   void operator delete(void *) {}
9
   // bump allocator for STL / pbd's containers
11 char mem[256 << 20];
   size_t rsp = sizeof mem;
13 template <typename T> struct bump {
   typedef T value_type;
15     bump() {}
   template <typename U> bump(U, ...) {}
17     T *allocate(size_t n) {
       rsp -= n * sizeof(T);
19     rsp &= 0 - alignof(T);
       return (T *) (mem + rsp);
21     }
   void deallocate(T *, size_t n) {}
23 };
```

### 1.3. Tools

#### 1.3.1. Floating Point Binary Search

```
1 union di {
   double d;
3   ull i;
   };
5 bool check(double);
   // binary search in [L, R) with relative error 2^-eps
7 double binary_search(double L, double R, int eps) {
   di l = {L}, r = {R}, m;
9   while (r.i - l.i > 1LL << (52 - eps)) {
       m.i = (l.i + r.i) >> 1;
11     if (check(m.d)) r = m;
       else l = m;
13   }
   return l.d;
15 }
```

#### 1.3.2. SplitMix64

```
1 using ull = unsigned long long;
   inline ull splitmix64(ull x) {
3     // change to `static ull x = SEED;` for DRBG
       ull z = (x += 0x9E3779B97F4A7C15);
5     z = (z ^ (z >> 30)) * 0xBF58476D1CE4E5B9;
       z = (z ^ (z >> 27)) * 0x94D049BB133111EB;
7     return z ^ (z >> 31);
   }
```

#### 1.3.3. <random>

```
1 #ifdef __unix__
   random_device rd;
3 mt19937_64 RNG(rd());
   #else
5     const auto SEED = chrono::high_resolution_clock::now()
       .time_since_epoch()
7     .count();
   mt19937_64 RNG(SEED);
9 #endif
   // random uint_fast64_t: RNG();
11 // uniform random of type T (int, double, ...) in [l, r]:
   // uniform_int_distribution<T> dist(l, r); dist(RNG);
```

## 1.4. Algorithms

### 1.4.1. Bit Hacks

```
1 // next permutation of x as a bit sequence
ull next_bits_permutation(ull x) {
3     ull c = __builtin_ctzll(x), r = x + (1 << c);
        return (r ^ x) >> (c + 2) | r;
5 }
// iterate over all (proper) subsets of bitset s
7 void subsets(ull s) {
    for (ull x = s; x;) { --x &= s; /* do stuff */ }
9 }
```

### 1.4.2. Aliens Trick

```
1 // min dp[i] value and its i (smallest one)
pll get_dp(int cost);
3 ll aliens(int k, int l, int r) {
    while (l != r) {
5         int m = (l + r) / 2;
        auto [f, s] = get_dp(m);
7         if (s == k) return f - m * k;
        if (s < k) r = m;
9         else l = m + 1;
    }
11    return get_dp(l).first - l * k;
}
```

### 1.4.3. Hilbert Curve

```
1 ll hilbert(ll n, int x, int y) {
    ll res = 0;
3     for (ll s = n / 2; s; s >>= 1) {
        int rx = !(x & s), ry = !(y & s);
5         res += s * s * ((3 * rx) ^ ry);
        if (ry == 0) {
7             if (rx == 1) x = s - 1 - x, y = s - 1 - y;
            swap(x, y);
9         }
    }
11    return res;
}
```

## 2. Math

### 2.1. Number Theory

#### 2.1.1. Mod Struct

A list of safe primes: 26003, 27767, 28319, 28979, 29243, 29759, 30467, 910927547, 919012223, 947326223, 990669467, 1007939579, 1019126699, 929760389146037459, 975500632317046523, 989312547895528379

NTT prime $p$	$p - 1$	primitive root
65537	$1 \ll 16$	3
998244353	$119 \ll 23$	3
2748779069441	$5 \ll 39$	3
1945555039024054273	$27 \ll 56$	5

```
1 template <typename T> struct M {
    static T MOD; // change to constexpr if already known
    T v;
3     M() : v(0) {}
    M(T x) {
5         v = (-MOD <= x && x < MOD) ? x : x % MOD;
        if (v < 0) v += MOD;
7     }
    explicit operator T() const { return v; }
    bool operator==(const M &b) const { return v == b.v; }
11    bool operator!=(const M &b) const { return v != b.v; }
    M operator-() { return M(-v); }
    M operator+(M b) { return M(v + b.v); }
13    M operator-(M b) { return M(v - b.v); }
    M operator*(M b) { return M((__int128)v * b.v % MOD); }
15    M operator/(M b) { return *this * (b ^ (MOD - 2)); }
    friend M operator^(M a, ll b) {
17        M ans(1);
        for (; b >>= 1, a *= a)
19            if (b & 1) ans *= a;
        return ans;
21    }
    friend M &operator+=(M &a, M b) { return a = a + b; }
    friend M &operator-=(M &a, M b) { return a = a - b; }
23    friend M &operator*=(M &a, M b) { return a = a * b; }
    friend M &operator/=(M &a, M b) { return a = a / b; }
25 };
using Mod = M<int>;
27 template <> int Mod::MOD = 1'000'000'007;
int &MOD = Mod::MOD;
```

### 2.1.2. Miller-Rabin

Requires: Mod Struct

```
1 // checks if Mod::MOD is prime
bool is_prime() {
3     if (MOD < 2 || MOD % 2 == 0) return MOD == 2;
    Mod A[] = {2, 7, 61}; // for int values (< 2^31)
5     // ll: 2, 325, 9375, 28178, 450775, 9780504, 1795265022
    int s = __builtin_ctzll(MOD - 1), i;
7     for (Mod a : A) {
        Mod x = a ^ (MOD >> s);
9         for (i = 0; i < s && (x + 1).v > 2; i++) x *= x;
        if (i && x != -1) return 0;
11    }
    return 1;
13 }
```

## 2.2. Combinatorics

### 2.2.1. Matroid Intersection

This template assumes 2 weighted matroids of the same type, and that removing an element is much more expensive than checking if one can be added. **Remember to change the implementation details.**

The ground set is  $0, 1, \dots, n - 1$ , where element  $i$  has weight  $w[i]$ . For the unweighted version, remove weights and change BF/SPFA to BFS.

```
1 constexpr int N = 100;
constexpr int INF = 1e9;
3
5 auto matroid_intersection(int n, const vector<int> &w) {
    bitset<N> S;
7     for (int sz = 1; sz <= n; sz++) {
        Matroid M1(S), M2(S);
9
        vector<vector<pii>> e(n);
        for (int j = 0; j < n; j++)
11            if (!S[j]) {
                if (M1.can_add(j)) e[n].emplace_back(j, -w[j]);
13                if (M2.can_add(j)) e[j].emplace_back(n + 1, 0);
            }
15        for (int i = 0; i < n; i++)
            if (S[i]) {
17                Matroid T1 = M1.remove(i), T2 = M2.remove(i);
                for (int j = 0; j < n; j++)
19                    if (!S[j]) {
                        if (T1.can_add(j)) e[i].emplace_back(j, -w[j]);
21                        if (T2.can_add(j)) e[j].emplace_back(i, w[i]);
                    }
23            }
25        vector<pii> dis(n + 2, {INF, 0});
        vector<int> prev(n + 2, -1);
27        dis[n] = {0, 0};
        // change to SPFA for more speed, if necessary
29        bool upd = 1;
        while (upd) {
31            upd = 0;
            for (int u = 0; u < n; u++)
33                for (auto [v, c] : e[u]) {
                    pii x(dis[u].first + c, dis[u].second + 1);
35                    if (x < dis[v]) dis[v] = x, prev[v] = u, upd = 1;
                }
37        }
39        if (dis[n + 1].first < INF)
            for (int x = prev[n + 1]; x != n; x = prev[x])
41                S.flip(x);
            else break;
43        // S is the max-weighted independent set with size sz
45    }
    return S;
47 }
```