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	4.2 Dijkstra.cpp	9	9	<pre>int bit[N][N]; #define lb(x) (x &amp; -x)</pre>	
	4.3 Dinic.cpp	10	11	<pre>void upd(int i, int j, int v) {</pre>	
	4.4 MaximumFlow.cpp	10	13	<pre>for(; j &lt; N; j += lb(j))   for(int k = i; k &lt; N; k += lb(k)) bit[k][j] += v;</pre>	
	4.5 SCC.cpp	10		}	
	4.6 VBCC.cpp	10	15	int qry2(int i, int j) {	
	4.7 one-degree-cycle(CSES Planets Cycles).cpp	11	17	<pre>int ans = 0; for(; j; j -= lb(j))</pre>	
			10	<pre>for(int k = i; k; k -= lb(k)) ans += bit[k][j];</pre>	
5	<b>DP</b> 5.1 CHO.cpp	11		<b>}</b>	
	5.2 Li-Chao-SegmentTree.cpp	11 11	21	int qry(int y1, int x1, int y2, int x2) {	٠,٠١
	5.3 SOSDP.cpp	12	23	return qry2(y2, x2) - qry2(y2, x1 - 1) - qry2(y1 - 1, x qry2(y1 - 1, x1 - 1);	(2)
	o.o bobbi.cpp			1	
6	Geometry	<b>12</b>	25	<pre>int main() {    int n, q, i = 1, j, y, x;</pre>	
	6.1 164253Version.cpp	12	27	for(scanf("%d %d", &n, &q); getchar(), i <= n; ++i)	
	6.2 ConvexHull.cpp	12	20	for(j = 1; j <= n; ++j)	
	6.3 Inside.cpp	13		TOT(: 0:) 3	
	6.4 Intersect.cpp	13	31	scanf("%d", &i);	
	6.5 MinimumEuclideanDistance.cpp	13	33	if(i == 1) scanf("%d%d", &i, &j),	
7	Tree	13	-	upd(i, j, 1 - 2 * qry(i, j, i, j));	
	7.1 HeavyLightDecomposition(modify-and-query-on-path).cpp	13	35		
	7.2 LCA.cpp	14	37	scanf("%d%d%d%d", &i, &j, &y, &x), printf("%d\n", qry(i, j, y, x));	
_	26		20	}	
8	Misc 8.1 BigNum(luoguP1005).cpp	14 14	39	}	
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		10	4		
9		15	1	#define int long long	
	9.1 BIT.cpp	15	3	using namespace std;	
	9.2 DSU.cpp	15	5	int n, q;	
	9.3 Treap.cpp	15		struct node {	
	9.4 Treap 但可以多個數縮點 (疑似爛的).cpp	17	7		
	9.5 區間插線段單點查詢李超 (是爛的).cpp	18	9	<pre>int rv() { return data + tag; } };</pre>	
	9.6 單點修改動態開點線段樹.cpp	18	, .		
	9.7 單點修改無懶標線段樹.cpp	19	11	node tree[20000005]; int a[200005];	
	9.8 懶標線段樹.cpp	19	13	<pre>int now = 1;</pre>	
	9.9 純直線單點查詢李超.cpp	19		<pre>int mx = 10000000005;</pre>	

```
void push(int index) {
         if(!tree[index].lson) {
17
             tree[index].lson = ++now;
19
         if(!tree[index].rson) {
              tree[index].rson = ++now;
21
         int lson = tree[index].lson;
23
         int rson = tree[index].rson;
         tree[lson].tag += tree[index].tag;
tree[rson].tag += tree[index].tag;
25
         tree[index].data = tree[index].rv();
27
         tree[index].tag = 0;
29
   }
   void modify(int l, int r, int L, int R, int val, int index) {
   if(l == L && r == R) {
31
33
              tree[index].tag += val;
         int mid = (l + r) >> 1;
37
         push(index);
         int lson = tree[index].lson;
int rson = tree[index].rson;
39
         if(R <= mid) {
         modify(l, mid, L, R, val, lson);
} else if(L > mid) {
             modify(mid + 1, r, L, R, val, rson);
         } else ·
45
              modify(l, mid, L, mid, val, lson);
              modify(mid + 1, r, mid + 1, R, val, rson);
         tree[index].data = tree[lson].rv() + tree[rson].rv();
   }
49
   int query(int l, int r, int L, int R, int index) {
   // cout << L << " " << R << "\n";
   if(l == L && r == R) {</pre>
51
53
              return tree[index].rv();
55
         int mid = (l + r) >> 1;
         push(index);
         int lson = tree[index].lson;
int rson = tree[index].rson;
         if(R <= mid) {</pre>
              return query(l, mid, L, R, lson);
              return query(mid + 1, r, L, R, rson);
         return query(l, mid, L, mid, lson) +
67
                 query(mid + 1, r, mid + 1, R, rson);
    }
69
    signed main() {
         ios::sync_with_stdio(0);
         cin.tie(0);
73
         cout.tie(0);
         cin >> n >> q;
for(int i = 1; i <= n; i++) {
75
              cin >> a[i];
              modify(1, mx, a[i], a[i], 1, 1);
79
         while(q--) {
              char mode;
              int x, y;
cin >> mode;
if(mode == '?') {
81
83
                   cin >> x >> y;
                   cout << query(1, mx, x, y, 1) << "\n";</pre>
              } else {
                   cin >> x >> y;
                  modify(1, mx, a[x], a[x], -1, 1);
a[x] = y;
                   modify(1, mx, a[x], a[x], 1, 1);
              }
91
         }
93 }
```

# 1.3. PbdsGpHashTable.cpp

```
ull operator()(ull x) const {
13
            static const ull FIXED_RANDOM =
                 (ull)make_unique<char>().get() ^
15
                 chrono::high_resolution_clock::now()
                     .time_since_epoch()
17
                     .count();
            // static const ull FIXED_RANDOM=mt();
// static const ull
19
            // FIXED_RANDOM=chrono::steady_clock::now()
            // .time_since_epoch().count()
21
            return splitmix64(x + FIXED_RANDOM);
23
   };
25 /*
   gp_hash_table<ull,ull,myhash> gp;
   gp[x]=y;
   if(gp.find(x)!=gp.end())cout<<gp[x];</pre>
29 gp.count(); //CE
```

#### 1.4. PbdsPriorityQueue.cpp

```
1
    __gnu_pbds::priority_queue<int> pq;
/*
    push(x); //return iterator
5    pop() top() join(pq2) erase(iter) modify(iter,x)
*/
```

## 1.5. PbdsRope.cpp

```
using namespace __gnu_cxx;

/*
rope<int> r;
r.erase(pos,k); //r=r.[0,pos)+r.[pos+k,r.length());
push_back(x) pop_back() insert(pos,x) clear() find(x)

lower_bound(all(r),x) upper_bound //same as vector
r.length(); //same as .length
r.replace(pos,len=r.length(),x); //r.[pos,pos+len)=x;
r.substr(pos,x); //return r.[pos,pos+x);
rope<char> s="official_beautiful_fruit";
cout<<s; //it's legal

*/</pre>
```

#### 1.6. PbdsTree.cpp

### 1.7. PersistentSegmentTree.cpp

```
1 // cses Range Queries and Copies
   using namespace std;
   #define LL long long
 5 #define pii pair<int, int>
   #define N 200005
   #define F first
   #define S second
          ver = 1;
   int n,
   LL a[N];
   struct Seg {
LL v = 0;
11
   struct Seg *l = NULL, *r = NULL;
#define M (L + R >> 1)
13
       static const void init(Seg *node, int L = 1, int R = n) {
           if(L == R) {
               node->v = a[L];
17
                return;
19
            node->l = new Seg();
21
            init(node->l, L, M);
           node->r = new Seg();
init(node->r, M + 1, R);
23
            node -> v = node -> l -> v + node -> r -> v;
25
       27
            if(L == R) {
               node -> v = v;
```

```
31
            if(x \ll M)
33
                node->l = new Seg(*node->l),
                upd(node->l, x, v, L, M);
35
                node \rightarrow r = new Seg(*node \rightarrow r)
           upd(node->r, x, v, M + 1, R);
node->v = node->l->v + node->r->v;
37
39
       41
            if(l <= L && R <= r) return node->v;
           43
45
   } * tree[N];
int main() {
49
       ios::sync_with_stdio(0);
       cin.tie(0)
51
       cout.tie(0);
       int q, i = 1, j, k;
for(cin >> n >> q; i <= n; ++i) cin >> a[i];
tree[1] = new Seg();
53
55
       Seg::init(tree[1]);
       for(; q--;) {
    cin >> i >> k;
            if(i == 1)
               cin >> i >> j, Seg::upd(tree[k], i, j);
            else if(i == 2)
                cin >> i >> j,
                    cout << Seg::qry(tree[k], i, j) << "\n";</pre>
                tree[++ver] = new Seg(*tree[k]);
65
67 }
```

## 1.8. Treap.cpp

```
#define pii pair<int, int>
    struct node {
           int tag = 0;
           int sum = 0;
           int prio = rand();
           int lson = 0;
           int rson = 0;
           int si = 0:
           int val = 0;
    node treap[400005];
11
    int cnt = 0;
    int root = 0;
     void update(int index) {
           int lson = treap[index].lson;
           int rson = treap[index].rson;
17
           treap[index].si = treap[lson].si + treap[rson].si + 1;
treap[index].sum = treap[lson].sum;
treap[index].sum += treap[rson].sum;
19
           treap[index].sum += treap[index].val;
21
    void push(int index) {
   if(!treap[index].tag) return;
   swap(treap[index].lson, treap[index].rson);
   int lson = treap[index].lson;
   int rson = treap[index].rson;
   int rson = treap[index].rson;
23
25
           treap[lson].tag ^= 1;
treap[rson].tag ^= 1;
treap[index].tag = 0;
29
31
    }
    pii split(int rk, int index) {
33
           if(!index) return \{0, 0\};
           push(index);
           int lson = treap[index].lson;
int rson = treap[index].rson;
37
           if(rk <= treap[lson].si) {</pre>
39
                 pii temp = split(rk, lson);
                 treap[index].lson = temp.second;
41
                 update(index);
                 return {temp.first, index};
                 pii temp = split(rk - treap[lson].si - 1, rson);
treap[index].rson = temp.first;
                 update(index);
                 return {index, temp.second};
    }
49
51 int merge(int x, int y) {
    if(!x && !y) return 0;
```

```
if(!x && y) return y;
        if(x && !y) return x;
55
        push(x);
        push(y);
57
        if(treap[x].prio < treap[y].prio) {</pre>
             treap[x].rson = merge(treap[x].rson, y);
59
             update(x);
            return x;
61
        } else {
            treap[y].lson = merge(x, treap[y].lson);
63
             update(y);
            return y;
65
        }
   }
67
   void insert(int x, int v) {
   pii temp = split(x - 1, root);
69
71
        treap[cnt].val = v;
        update(cnt);
temp.first = merge(temp.first, cnt);
73
        root = merge(temp.first, temp.second);
75
   int query(int l, int r) {
  pii R = split(r, root);
  pii L = split(l - 1, R.first);
79
        int ret = treap[L.second].sum;
        R.first = merge(L.first, L.second);
81
        root = merge(R.first, R.second);
83
        return ret;
   }
85
       void modify(int l, int r) {
87
89
        R.first = merge(L.first, L.second);
91
        root = merge(R.first, R.second);
   }
```

#### 2. Math

#### 2.1. CRT.cpp

```
1
    #define int long long
 3
    using namespace std;
 5
    int a[15];
   int b[15];
    int mul = 1;
    void exgcd(int a, int b, int &x, int &y) {
11
         if(b == 0) {
              x = 1:
              y = 0;
13
              return:
15
         exgcd(b, a % b, y, x);
y -= (a / b) * x;
17
19
    int inv(int a, int p) {
21
         int x, y;
         exgcd(a, p, x, y);
23
    }
25
    int ans = 0;
27
    signed main() {
         cin >> n;
for(int i = 1; i <= n; i++) {
   cin >> a[i] >> b[i];
   mul *= a[i];
29
31
33
         for(int i = 1; i <= n; i++) {
    ans += inv(mul / a[i], a[i]) * (mul / a[i]) % mul *</pre>
35
                       b[i] % mul;
37
               ans %= mul;
39
         ans = (ans + mul) % mul;
         cout << ans;
41 }
```

#### 2.2. CountPrimes.cpp

```
using namespace std;
using i64 = long long;
```

```
i64 count_pi(i64 N) {
          if(N <= 1) return 0;
int v = sqrt(N + 0.5);</pre>
          int n_4 = sqrt(v + 0.5);
int T = min((int)sqrt(n_4) * 2, n_4);
int K = pow(N, 0.625) / log(N) * 2;
           K = max(K, v);
           K = min < i64 > (K, N);
11
          int B = N / K;
B = N / (N / B);
13
           B = min < i64 > (N / (N / B), K);
15
          vector<i64> l(v + 1);
vector<int> s(K + 1);
vector<bool> e(K + 1);
          vector<int> w(K + 1);
for(int i = 1; i <= v; ++i) l[i] = N / i - 1;
for(int i = 1; i <= v; ++i) s[i] = i - 1;</pre>
19
21
           const auto div = [](i64 n, int d) \rightarrow int {
23
                return double(n) / d;
25
           int p;
          int p;
for(p = 2; p <= T; ++p)
    if(s[p] != s[p - 1]) {
        i64 M = N / p;
        int t = v / p, t0 = s[p - 1];
}</pre>
27
                       for(int i = v, j = t; j >= p; --j)
  for(int l = j * p; i >= l; --i)
    s[i] -= s[j] - t0;
                       for(int i = p * p; i <= K; i += p) e[i] = 1;
39
           e[1] = 1;
           int cnt = 1;
          vector<int> roughs(B + 1);
for(int i = 1; i <= B; ++i)</pre>
41
          if(!e[i]) roughs[cnt++] = i;
roughs[cnt] = 0x7fffffff;
43
          for(int i = 1; i <= K; ++i) w[i] = e[i] + w[i - 1];
for(int i = 1; i <= K; ++i) s[i] = w[i] - w[i - (i & -i)];</pre>
47
           const auto query = [8](int x) \rightarrow int {
                 int sum = x;
while(x) sum -= s[x], x ^= x & -x;
49
                 return sum;
51
53
           const auto add = [\delta](int x) \rightarrow void {
                e[x] = 1:
                 while(x <= K) ++s[x], x += x \delta -x;
55
           cnt = 1;
           for(; p <= n_4; ++p)</pre>
                 if(!e[p]) {
                       i64 q = i64(p) * p, M = N / p;
while(cnt < q) w[cnt] = query(cnt), cnt++;
                       int t1 = B / p, t2 = min<i64>(B, M / q),
                             t0 = query(p - 1);
                       int id = 1, i = 1;
for(; i <= t1; i = roughs[++id])</pre>
                       l[i] -= l[i * p] - t0;
for(; i <= t2; i = roughs[++id])
                             l[i] -= query(div(M, i)) - t0;
                               i <= B; i = roughs[++id])
69
                             l[i] = w[div(M, i)] - t0;
                       for(int i = q; i <= K; i += p)</pre>
                             if(!e[i]) add(i);
73
          while(cnt <= v) w[cnt] = query(cnt), cnt++;</pre>
           vector<int> primes;
          primes.push_back(1);
for(int i = 2; i <= v; ++i)
    if(!e[i]) primes.push_back(i);
l[1] += i64(w[v] + w[n_4] - 1) * (w[v] - w[n_4]) / 2;
for(int i = w[n_4] + 1; i <= w[B]; ++i)</pre>
81
          83
85
                 int q = primes[i];
i64 M = N / q;
int e = w[M / q];
                 if(e <= i) break;
                 l[1] += e - i;
                 i64 t = 0;
                 int m = w[sqrt(M + 0.5)];
93
                 for(int k = i + 1; k <= m; ++k)</pre>
                t += w[div(M, primes[k])];
l[1] += 2 * t - (i + m) * (m - i);
95
          }
```

```
97 return l[1];
}
```

## 2.3. FFT.cpp

```
using namespace std;
    inline int read() {
          int ans = 0;
char c = getchar();
while(!isdigit(c)) c = getchar();
          while(isdigit(c)) {
                ans = ans * 10 + c - '0';
                c = getchar();
11
          return ans:
    typedef complex<double> comp:
    const int MAXN = 1000005;
    const comp I(0, 1);
    const double PI = acos(-1);
comp A[MAXN * 3], B[MAXN * 3], tmp[MAXN * 3], ans[MAXN * 3];
     void fft(comp F[], int N, int sgn = 1) {
          if(N == 1) return;
          23
          comp cur = 1, step = exp(2 * PI / N * sgn * I);
          for(int k = 0; k < N / 2; k++)
    tmp[k] = G[k] + cur * H[k];</pre>
27
                tmp[k + N / 2] = G[k] - cur * H[k];
29
                cur *= step;
31
          memcpy(F, tmp, sizeof(comp) * N);
    int main() {
33
          int n = read(), m = read(), N = 1 << __lg(n + m + 1) + 1;
for(int i = 0; i <= n; ++i) A[i] = read();
for(int i = 0; i <= m; ++i) B[i] = read();
fft(A, N), fft(B, N);
for(int i = 0; i < N; ++i) ans[i] = A[i] * B[i];
fft(an N = 1);</pre>
35
37
          fft(ans, N, -1);
for(int i = 0; i <= n + m; ++i)
    printf("%d ", int(ans[i].real() / N + 0.1));</pre>
39
41
          return 0;
43 }
```

## 2.4. FWT.cpp

## 2.5. Gaussian-Jordan.cpp

```
#define int long long
   using namespace std;
   int n;
double a[105][105];
   void gaussian(double a[105][105], int n, int m) {
         int curi = 0;
         for(int j = 0; j < m; j++) \{
              int i;
13
              for(i = curi; i < n; i++) {</pre>
                   if(a[i][j]) {
15
                        break;
                   }
17
              if(a[i][j] == 0) continue;
for(int k = 0; k < m; k++) {
    swap(a[i][k], a[curi][k]);</pre>
19
21
              for(int k = m - 1; k >= j; k--) {
                   a[curi][k] /= a[curi][j];
23
```

```
for(int i = 0; i < n; ++i) {</pre>
                   if(i != curi) {
                       for(int k = m - 1; k >= j; k--) {
    a[i][k] -= a[curi][k] * a[i][j];
27
29
                   }
31
              curi++;
33
    }
   2.6.
         Generator.cpp
    #define int long long
    using namespace std;
```

```
int t;
    int n, d;
    bitset<1000005> exist;
    bitset<1000005> vis;
    vector<int> prime;
    int phi[1000005];
11
    void init() {
   phi[1] = 1;
   for(int i = 2; i <= 1000000; i++) {</pre>
13
               if(!vis[i]) {
15
                     prime.push_back(i);
phi[i] = i - 1;
17
                for(int j : prime) {
                     if(i * j > 1000000) break;
vis[i * j] = 1;
if(i % j == 0) {
                           phi[i * j] = phi[i] * j;
                           phi[i * j] = phi[i] * phi[j];
27
                }
29
          exist[2] = exist[4] = 1;
          for(int i : prime) {
    if(i == 2) continue;
    for(int j = i; j <= 1000000; j *= i) {
        exist[j] = 1;
        if(j * 2 <= 1000000) {</pre>
31
33
35
                           exist[j << 1] = 1;
                     }
37
                }
39
          }
    }
41
    vector<int> factors(int x) {
          vector<int> v;
for(int i = 1; i * i <= x; i++) {
    if(x % i == 0) {</pre>
43
45
                     v.push_back(i);
if(i * i != x)
                           v.push_back(x / i);
49
                }
          return v;
53
    }
    int f(int x, int y, int mod) {
55
          int ret = 1;
          while(y) {
57
                if(y & 1) {
59
                     ret *= x:
                     ret %= mod;
               }
61
               x *= x:
               x %= mod;
63
                y >>= 1;
65
          return (ret % mod + mod) % mod;
    }
67
    vector<int> findroot(int x) {
          vector<int> ret;
          if(!exist[x]) return ret;
          int phix = phi[x];
73
          vector<int> fact = factors(phix);
          int fst;
          for(int i = 1;; i++) {
75
               if(_gcd(i, x) != 1) continue;
bool ok = 1;
for(int j : fact) {
   if(j != phix && f(i, j, x) == 1) {
77
79
                           ok = 0:
```

```
break:
                       }
 83
                  if(ok) {
 85
                       fst = i;
                       break;
 87
                 }
           int now = fst;
// cout << fst <<"\n";
for(int i = 1; i <= phix; i++) {
    if(__gcd(i, phix) == 1) {</pre>
 89
 91
                       ret.push_back(now);
 93
 95
                 now *= fst;
                 now %= x;
 97
            return ret;
 99
     signed main() {
           ios::sync_with_stdio(0);
103
            cin.tie(0);
            cout.tie(0);
           init();
105
            cin >> t;
107
           while(t--) {
                 cin >> n >> d;
vector<int> v = findroot(n);
109
                  sort(v.begin(), v.end());
                  cout << v.size() << "\n"
111
                 for(int i = 0; i < v.size(); i++) {
   if(i % d == d - 1) {
      cout << v[i] << " ";</pre>
113
115
                  cout << "\n";
117
           }
119 }
```

#### 2.7. Inv.cpp

```
int exgcd(int a, int b, int 8x, int 8y) {
  if(b == 0) {
 1
             x = 1;
              y = 0;
              return a;
 5
         int d = exgcd(b, a % b, y, x);
         y -= x * (a / b);
 9
         return d;
11
    int inv(int a, int p) {
         int x, y;
exgcd(a, p, x, y);
return (x % p + p) % p;
13
15
```

#### 2.8. Lucas.cpp

```
1
    int fact[100005]:
    int p;
 3
    void init() {
   fact[0] = 1;
 5
         for(int i = 1; i <= p; i++) {
    fact[i] = fact[i - 1] * i % p;</pre>
 9 }
int inv(int x, int p) {
   if(x == 1) return 1;
          return (p - p / x) * inv(p % x, p) % p;
13
    }
15
    int c(int x, int y, int p) {
   if(x < y) return 0;
   int k = fact[x] * inv(fact[y], p) % p;</pre>
17
19
          return k * inv(fact[x - y], p) % p;
21
    int lucas(int x, int y, int p) {
23
          if(x == 0) return 1;
          return lucas(x / p, y / p, p) % p * c(x % p, y % p, p) % p;
25 }
```

## 2.9. Matrix.cpp

```
#define int long long
3 using namespace std;
```

```
template <class T> T extgcd(T a, T b, T &x, T &y) {
                  if(!b) {
                                                                                                                                                                       99
                           x = 1;
y = 0;
                                                                                                                                                                     101
                            return a;
                                                                                                                                                                     103
                  T ans = extgcd(b, a \% b, y, x);
                      -= a / b * x;
                                                                                                                                                                     105
13
                 return ans:
       }
                                                                                                                                                                     107
15
       template <class T> T modeq(T a, T b, T p) {
                                                                                                                                                                     109
                 T x, y, d = extgcd(a, p, x, y);
if(b % d) return 0;
return ((b / d * x) % p + p) % p;
17
                                                                                                                                                                     111
19
       }
                                                                                                                                                                     113
21
       template <class T> class Matrix {
                                                                                                                                                                     115
                 static const T MOD = 10000000007;
23
                                                                                                                                                                     117
                  vector<vector<T>> v;
                                                                                                                                                                     119
27
                  Matrix(int n, int m, int identity) {
                            v = vector<vector<T>>(n, vector<T>(m, 0));
                                                                                                                                                                     121
29
                            if(identity)
                                      for(int i = 0, k = min(n, m); i < k; ++i)
                                                                                                                                                                     123
31
                                                v[i][i] = 1;
                                                                                                                                                                     125
                 Matrix(Matrix &b) { v = b.v; }
33
                  void in(int l = 0, int m = -1, int u = 0, int n = -1) {
                                                                                                                                                                     127
                            if(n < 0) n = v.size();
if(m < 0) m = v[0].size();
35
                                                                                                                                                                     129
                            for(int i = u; i < n; ++i)
    for(int j = l; j < m; ++j) scanf("%lld", &v[i][j]);131</pre>
37
39
                  Matrix(int n, int m) {
                                                                                                                                                                     133
                            v = vector<vector<T>>(n, vector<T>(m, 0));
41
                                                                                                                                                                     135
43
                 void out(int l = 0, int m = -1, int u = 0, int n = -1) {
   if(n < 0) n = v.size();
   if(m < 0) m = v[0].size();</pre>
                                                                                                                                                                     137
45
                                                                                                                                                                     139
                            for(int i = u; i < n; ++i)
    for(int j = l; j < m; ++j)
        printf("%lld%c", v[i][j], " \n"[j == m - 1]);</pre>
47
                                                                                                                                                                     141
49
                                                                                                                                                                     143
                  Matrix operator=(Matrix &b) {
51
                            v = b.v;
                                                                                                                                                                     145
                            return *this;
53
                                                                                                                                                                     147
                  Matrix operator+(Matrix &b) {
                            Matrix ans(*this);
                                                                                                                                                                     149
                            int n = v.size(), m = v[0].size();
                            for(int i = 0; i < n; ++i)
  for(int j = 0; j < m; ++j) {
    ans.v[i][j] += b.v[i][j];</pre>
                                                                                                                                                                     151
59
                                                                                                                                                                     153
61
                                                if(MOD) {
                                                          if(ans.v[i][j] < 0)
                                                                                                                                                                     155
                                                                    ans.v[i][j]
                                                                              (ans.v[i][j] % MOD + MOD) % MOD;
65
                                                          if(ans.v[i][j] >= MOD) ans.v[i][j] %= MOD;
                                                }
                                                                                                                                                                     159
67
                                     }
                            return ans;
                                                                                                                                                                     161
69
                  Matrix operator+(T x) {
                                                                                                                                                                     163
                            Matrix ans(*this);
71
                            int n = v.size(), m = v[0].size();
for(int i = 0; i < n; ++i)
    for(int j = 0; j < m; ++j) {
        ans.v[i][j] += x;
        reconstruction</pre>
                                                                                                                                                                     165
73
                                                                                                                                                                     167
75
                                                if(MOD) {
                                                                                                                                                                     169
                                                         if(ans.v[i][j] < 0)
                                                                    ans.v[i][j]
                                                                                                                                                                     171
                                                                              (ans.v[i][j] % MOD + MOD) % MOD;
                                                          if(ans.v[i][j] >= MOD) ans.v[i][j] %= MOD; 173
81
                                                                                                                                                                     175
83
                            return ans:
                                                                                                                                                                     177
                  Matrix operator-(Matrix &b) {
                            Matrix ans(*this);
                                                                                                                                                                     179
                            int n = v.size(), m = v[0].size();
for(int i = 0; i < n; ++i)
    for(int j = 0; j < m; ++j) {
        ans.v[i][j] -= b.v[i][j];
        if(int) = if(i
                                                                                                                                                                     181
89
                                                                                                                                                                     183
                                                if(MOD) {
91
                                                          if(ans.v[i][j] < 0)
                                                                                                                                                                     185
93
                                                                    ans.v[i][j] =
                                                                              (ans.v[i][j] % MOD + MOD) % MOD;
95
                                                          if(ans.v[i][j] >= MOD) ans.v[i][j] %= MOD;
                                                }
```

```
return ans;
Matrix operator-(T x) {
     Matrix ans(*this);
     int n = v.size(), m = v[0].size();
     for(int i = 0; i < n; ++i)
for(int j = 0; j < m; ++j) {
                ans.v[i][j] -= x;
                if(MOD) {
                     if(ans.v[i][j] < 0)
                          ans.v[i][j]
                                (ans.v[i][j] % MOD + MOD) % MOD;
                     if(ans.v[i][j] >= MOD) ans.v[i][j] %= MOD;
          }
     return ans:
Matrix operator+=(Matrix &b) {
     if(MOD) {
                     if(v[i][j] < 0)
                           \bar{v}[\bar{i}][\bar{j}] = (v[i][j] \% MOD + MOD) \% MOD;
                     if(v[i][j] >= MOD) v[i][j] %= MOD;
     return *this;
Matrix operator+=(T x) {
     int n = v.size(), m = v[0].size();
     for(int i = 0; i < n; ++i)
    for(int j = 0; j < m; ++j) {</pre>
               v[i][j] += x;
                if(MOD) {
                     if(v[i][j] < 0)
                          v[i][j] = (v[i][j] \% MOD + MOD) \% MOD;
                     if(v[i][j] >= MOD) v[i][j] %= MOD;
                }
          }
     return *this;
Matrix operator -= (Matrix &b) {
     int n = v.size(), m = v[0].size();
for(int i = 0; i < n; ++i)
    for(int j = 0; j < m; ++j) {
        v[i][j] -= b.v[i][j];
        refuse | feet | feet | feet |
        v[i][j] | feet | feet |
        v[i][j];</pre>
                if(MOD) {
                     if(v[i][j] < 0)
                           v[i][j] = (v[i][j] % MOD + MOD) % MOD;
                     if(v[i][j] >= MOD) v[i][j] %= MOD;
     return *this;
Matrix operator-=(T x) {
     int n = v.size(), m = v[0].size();
for(int i = 0; i < n; ++i)</pre>
          for(int j = 0; j < m; ++j) {
    v[i][j] -= x;
                          v[i][\bar{j}] = (v[i][j] \% MOD + MOD) \% MOD;
                     if(v[i][j] >= MOD) v[i][j] %= MOD;
          }
     return *this;
Matrix operator*(Matrix &b) {
     int n = v.size()
     int p = b.v.size();
int m = b.v[0].size();
     Matrix ans(n, m, 0);
for(int i = 0; i < n; ++i)
  for(int k = 0; k < p; ++k)
    for(int j = 0; j < m; +-i)</pre>
                     ans.v[i][j] += v[i][k] * b.v[k][j];
                     if(MOD) {
                          if(ans.v[i][i] < 0)
                                ans.v[i][j] =
                                     (ans.v[i][j] % MOD + MOD) % MOD;
                           if(ans.v[i][j] >= MOD)
                                ans.v[i][j] %= MOD;
                     }
     return ans:
Matrix operator*(T x) {
     Matrix ans(*this);
     int n = v.size(), m = v[0].size();
for(int i = 0; i < n; ++i)</pre>
```

191

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255

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259

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263

265

267

269

271

273

279

281

```
for(int j = 0; j < m; ++j) {
    ans.v[i][j] *= x;</pre>
              if(MOD) {
                                                                   285
                  if(ans.v[i][j] < 0)
                       ans.v[i][j]
                                                                   287
                           (ans.v[i][j] % MOD + MOD) % MOD;
                  if(ans.v[i][j] >= MOD) ans.v[i][j] %= MOD; 289
                                                                   291
    return ans;
                                                                   293
Matrix operator*=(Matrix &b) {
    int n = v.size();
int p = b.v.size();
                                                                   295
     int m = b.v[0].size();
                                                                   297
    299
                                                                   301
                  if(MOD) {
                                                                   303
                       if(ans.v[i][j] < 0)
                           ans.v[i][j]
                                                                   305
                       (ans.v[i][j] % MOD + MOD) % MOD;
if(ans.v[i][j] >= MOD)
                           ans.v[i][j] %= MOD;
                                                                   309
     v = ans.v;
                                                                   311
    return *this;
                                                                   313
Matrix operator*=(T x) {
     int n = v.size(), m = v[0].size();
     for(int i = 0; i < n; ++i)
         for(int j = 0; j < m; ++j) {
              v[i][j] *= x;
              if(MOD) {
                  if(v[i][j] < 0)
    v[i][j] = (v[i][j] % MOD + MOD) % MOD;</pre>
                  if(v[i][j] >= MOD) v[i][j] %= MOD;
              }
         }
    return *this:
                                                                     q
Matrix operator/(T x) {
    Matrix ans(*this);
                                                                    11
    13
              if(MOD) {
                  ans.v[i][j] *= modeq(x, (T)1, (T)MOD);
                  if(ans.v[i][j] < 0)
                                                                    17
                       ans.v[i][j] =
                            (ans.v[i][j] % MOD + MOD) % MOD;
                                                                    19
                  if(ans.v[i][j] >= MOD) ans.v[i][j] %= MOD;
              } else
                                                                    21
                  ans.v[i][j] /= x;
         }
                                                                    23
    return ans;
                                                                    25
Matrix operator/=(T x) {
     int n = v.size(), m = v[0].size();
for(int i = 0; i < n; ++i)</pre>
                                                                    27
         for(int j
                    = 0; j < m; ++j) {
                                                                    29
             if(MOD) {
    v[i][j] *= modeq(x, (T)1, (T)MOD);
                  if(v[i][j] < 0)
                       v[i][j] = (v[i][j] \% MOD + MOD) \% MOD;
                                                                    33
                  if(v[i][j] >= MOD) v[i][j] %= MOD;
              } else
                                                                    35
                  v[i][j] /= x;
         }
                                                                    37
    return *this;
                                                                    39
Matrix operator%=(T p) {
    int n = v.size(), m = v[0].size();
    for(int i = 0; i < n; ++i)
        for(int j = 0; j < m; ++j)</pre>
             if(v[i][j] >= p) v[i][j] %= p;
    return *this:
void gaussian() {
     int curi = 0;
     int n = v.size();
     int m = v[0].size();
                                                                     5
     for(int j = 0; j < m; j++) {
         for(i = curi; i < n; i++) {</pre>
                                                                     9
              if(MOD)
                  v[i][j] %= MOD;
                                                                    11
              if(v[i][j]) {
                  break:
```

```
if(i >= n) {
                     continue;
                if(v[i][j] == 0) continue;
               for(int k = θ; k < m; k++) {
    swap(v[i][k], v[curi][k]);</pre>
                for(int k = m - 1; k >= j; k--) {
                     if(MOD) {
                          v[curi][k] *=
                          modeq(v[curi][j], (T)1, (T)MOD);
v[curi][k] = (v[curi][k] % MOD + MOD) % MOD;
                     } else
                          v[curi][k] /= v[curi][j];
                for(int i = 0; i < n; ++i) {
                     if(i != curi) {
                          for(int k = m - 1; k >= j; k--) {
   v[i][k] -= v[curi][k] * v[i][j];
                               if(MOD) {
                                     v[i][k]
                                          (v[i][k] % MOD + MOD) % MOD;
                                }
                          }
                     }
                curi++;
          }
     }
};
```

## 2.10. MillerRabin.cpp

```
uint128 t
   #define uLL
    template <class T, class POW>
    void fastpow(T x, POW n, POW p, T & ans) {
         for(; n; n >>= 1) {
              if(n & 1) {
                   ans *= x;
                   ans %= p;
              }
              x *= x;
              x \%= p;
   /* 輸入 x,n,p,ans 會將 ans 修改為 x<sup>n</sup>%p
對整數/矩陣/不要求精度的浮點 皆有效
模板第一個型別是 x,ans 第二個是 n,p(應該放 LL 或
                                                             int128)*/
   uLL pri[7] = {2, 325, 9375, 28178, 450775, 9780504, 1795265022}; /*2^64*/// int p[3]={2,7,61}; /*2^32*/
   bool check(const uLL x, const uLL p) {
         uLL d = x - 1, ans =
         fastpow(p, d, x, ans);
if(ans != 1) return 1;
         for(; !(d & 1);) {
              d >>= 1;
              ans = 1;
              fastpow(p, d, x, ans);
if(ans == x - 1)
                  return 0;
              else if(ans != 1)
                   return 1;
         return 0;
    bool miller_rabin(const uLL x) {
         if(x == 1) return \theta;
         for(auto e : pri) {
              if(e >= x) return 1;
              if(check(x, e)) return 0;
         return 1;
41 }
```

#### 2.11. Mu.cpp

```
vector<int> prime;
bitset<1000005> vis;
int n;
int mu[1000005];
void init() {
    for(int i = 2; i <= n; i++) {
        if(!vis[i]) {
            prime.push_back(i);
            mu[i] = -1;
    }
    for(int p : prime) {
        if(i * p > n) break;
```

```
vis[i * p] = 1;
if(i % p == 0) {
    mu[i * p] = 0;
15
17
                             break;
                       } else {
                             mu[i * p] = mu[i] * mu[p];
19
21
                 }
           }
23 }
```

#### 2.12. NTT.cpp

```
#define ll long long
      using namespace std;
     const int MAXN = 1000005;
const int MOD = 998244353, G = 3;
int rev[MAXN * 3];
      int qpow(int x, int y) {
              int ret = 1;
              while(y) {
11
                      if(y & 1) {
                             ret *= x
13
                             ret %= MOD;
15
                      x *= x;
                      x %= MOD;
17
                      y >>= 1;
19
              return ret;
21 }
      void ntt(int F[], int N, int sgn) {
23
              int bit = _lg(N);
for(int i = 0; i < N; ++i) {
   rev[i] = (rev[i >> 1] >> 1) | ((i & 1) << (bit - 1));</pre>
25
27
                      if(i < rev[i]) swap(F[i], F[rev[i]]);</pre>
             for(int l = 1, t = 1; l < N; l <<= 1, t++) {
    int step = qpow(G, ((MOD - 1) >> t) * sgn + MOD - 1);
    for(int i = 0; i < N; i += l << 1)
        for(int k = i, cur = 1; k < i + l; ++k) {
            int g = F[k], h = (ll)F[k + l] * cur % MOD;
            F[k] = (g + h) % MOD;
            F[k + l] = ((g - h) % MOD + MOD) % MOD;
            cur = (ll)cur * step % MOD;
}</pre>
29
31
33
35
                              }
37
              if(sgn == -1) {
39
                      int invN = qpow(N, MOD - 2);
for(int i = 0; i < N; ++i) F[i] = (ll)F[i] * invN % MOD;</pre>
41
43
     }
```

#### 2.13. PollardRho.cpp

```
using namespace std;
     #define LL long long
     #define uLL __uint128_t
#define sub(a, b) ((a) < (b) ? (b) - (a) : (a) - (b))
template <class T, class POW>
void fastpow(T x, POW n, POW p, T & ans) {
    for(; n; n >>= 1) {
        if(n & 1) {
                           ans *= x:
                           ans %= p;
11
                    }
                    x *= x;
13
                    x %= p;
15
     /*input x, n, p, ans, will modify ans to x ^n % p the first is x, ans and the second is n, p (LL or __int128)
19
      450775, 9780504, 1795265022}; /*2<sup>6</sup>64*/
// int p[3]={2,7,61};/*2<sup>32*</sup>/
bool check(conet
     uLL pri[7] = \{2,
21
23
     bool check(const uLL x, const uLL p) {
             uLL d = x - 1, ans = 1;
            fastpow(p, d, x, ans);
if(ans!= 1) return 1;
for(; !(d & 1);) {
    d >>= 1;
25
27
                    ans = 1
                    fastpow(p, d, x, ans);
if(ans == x - 1)
31
                           return 0:
                    else if(ans != 1)
                           return 1;
```

```
return 0;
37
    bool miller_rabin(const uLL x) {
39
         if(x == 1) return \theta;
         for(auto e : pri) {
41
              if(e >= x) return 1;
              if(check(x, e)) return 0;
43
         return 1;
45
   }
    template <class T> T gcd(T a, T b) {
         if(!a) return b;
if(!b) return a;
47
         if(a \delta b \delta 1) return gcd(sub(a, b), min(a, b)); if(a \delta 1) return gcd(a, b >> 1); if(b \delta 1) return gcd(a >> 1, b);
49
51
         return gcd(a >> 1, b >> 1) << 1:
53 }
    /*gcd(a.b) denote gcd(a.0) = a*/
   mt19937 rnd(time(0));
template <class T> T f(T x, T c, T mod) {
    return (((uLL)x) * x % mod + c) % mod;
55
57
   template <class T> T rho(T n) {
59
         T \mod = n, x = rnd() \% \mod, c = rnd() \% (\mod - 1) + 1,
61
               1;
         for(T i = 2, j = 2, d = x;; ++i) {
              x = f(x, c, mod);
p = ((uLL)p) * sub(x, d) % mod;
63
65
              if(i % 127
                           == 0 && gcd(p, n) != 1) return gcd(p, n);
              if(i == j) {
                   j <<= 1, d = x;
67
                   if(gcd(p, n) != 1) return gcd(p, n);
69
71 }
    template <class T> T pollard_rho(T n) {
73
         if(miller_rabin(n)) return n;
         T p = n;
75
         while(p == n) p = rho(n);
         return max(pollard_rho(p), pollard_rho(n / p));
77
   }
    int main() {
79
         LL t, n, ans;
         for(cin >> t; t--;) {
    cin >> n;
81
              ans = pollard_rho(n);
83
              if(ans == n)
                  puts("Prime");
              else
85
                   printf("%lld\n", ans);
87
         }
   }
```

#### 2.14. XorBasis.cpp

```
#pragma GCC optimize(
          'Ofast,fast-math,unroll-loops,no-stack-protector")
   using namespace std;
#define ll long long
    #define V vector
    #define pb push_back
    #define all(x) \bar{x}.begin(), x.end()
    ll f(ll'k, ll now = 0, ll p = v.size() - 1, ll ans = 0) {
         if(k<sub>_</sub> >= 1 << p) {
11
              k -= 1 << p;
13
              ans = max(ans, ans ^ v[now]);
         } else
              ans = min(ans, ans ^ v[now]);
15
         if(!p) return ans;
return f(k, now + 1, p - 1, ans);
17
19
   int main() {
         ios::sync_with_stdio(\theta);
21
         cin.tie(0);
         cout.tie(0);
23
         ll n, k;
         cin >> n >> k;
         for(ll x, i = 0; i < n; ++i) {</pre>
25
              cin >> x;
              for(ll &e : v) x = min(x, x ^ e);
27
              if(x) v.pb(x);
29
         sort(all(v), greater<ll>());
         ll t = n - v.size(), a = k >> t,
b = k & ((1 << min(t, 20LL)) - 1), i = 0;</pre>
31
         for(; a--; ++i)
    for(ll j = 1 << t, p = f(i); j--;) cout << p << " ";
for(i = f(i); b--;) cout << i << " ";</pre>
33
35
```

### 3. String

## 3.1. Booth.cpp

```
#define V vector
                                                                                                          41
     string booth(string s) {
           s += s;
                                                                                                          43
           int n = s.size(), k = 0;
           V<int> f(n, -1);
for(int i = 1; i < n; ++i) {
   int j = f[i - k - 1];</pre>
                                                                                                          45
                                                                                                          47
                 for(; j >= 0 && s[j + k + 1] != s[i]; j = f[j])
    if(s[i] < s[j + k + 1]) k = i - j - 1;
if(s[i] != s[j + k + 1]) {
    if(s[i] < s[k]) k = i;</pre>
                                                                                                          49
11
                        f[i - k] = -1;
13
                 } else
                                                                                                          53
                        f[i - k] = j + 1;
15
           return s.substr(k, s.size() >> 1);
17
    }
                                                                                                          57
     //給出循環排列後最小字典序的解
```

## 3.2. KMP.cpp

```
string s, t;
int pmt[1000005];
   if(t[j] == t[i]) j++;
            pmt[i] = j;
11
   }
13
   int kmp(string s) {
       int ret = 0;
for(int i = 0, j = 0; i < s.size(); i++) {
    while(j && s[i] ^ t[j]) {
15
17
                j = pmt[j - 1];
19
            if(s[i] == t[j]) {
21
                j++;
            if(j == t.size()) {
23
                ret++
                j = pmt[j - 1];
25
27
        return ret;
29
   }
```

#### 3.3. LongestPalindrome.cpp

```
#define int long long
   using namespace std;
    string t;
    int d[2000005];
   int ans = 0;
   signed main() {
11
        cin >> t;
13
        n = t.size();
        for(int i = 0; i < 2 * n + 1; i++) {
    if(i & 1 ^ 1) {
15
                 s += '0';
             } else {
17
                 s += t[i / 2];
19
        n = s.size();
21
        d[0] = 1;
        for(int i = 0, l = 0, r = 0; i < n; i++) {
23
             if(i > r) {
                 d[i] = 1;
                 bool a = i + d[i] < n;
bool b = i - d[i] >= 0;
27
          bool c = (s[i + d[i]] == s[i - d[i]];
29
          while (a && b && c) {
                      d[i]++;
a = i + d[i] < n;
31
                      b = i - d[i] >= 0;
                      c = ([i + d[i]] == s[i - d[i]]);
33
          l = i - d[i] + 1;
35
```

```
r = i + d[i] - 1;
37
              } else {
                   int j = l + r - i;
if(j - d[j] + 1 > l) {
39
                         d[i] = d[j];
                    } else {
                         d[i] = r - i + 1;
                         a = i + d[i] < n;
b = i - d[i] >= 0;
                         c = (s[i + d[i]] == s[i - d[i]]);
                         while(a && b && c) {
                              d[i]++;
a = i + d[i] < n;
b = i - d[i] >= 0;
                              c = (s[i + d[i]] == s[i - d[i]]);
51
                         i = i - d[i] + 1;

r = i + d[i] - 1;
                    }
55
               // cout << d[i] << " ";
              if(d[i] > d[ans]) {
                    ans = i;
59
         for(int i = ans - d[ans] + 1; i < ans + d[ans]; i++) {
   if(s[i] ^ '0') {</pre>
61
                    cout << s[i];
63
65
         }
   }
```

#### 3.4. **Z.**cpp

```
1
    #define int long long
    using namespace std;
 5
    string s, t;
    int ans = 0;
    int z[2000005]:
    signed main() {
11
          ios::sync_with_stdio(0);
          cin.tie(0);
13
          cout.tie(0);
          cin >> s >> t;
s = t + '0' +
15
          int n, m;
17
          n = s.size();
          m = t.size();
          for(int i = 0, l = 0, r = 0; i < n; i++) {
    if(z[i - l] < r - i + 1) {
        z[i] = z[i - l];
    }</pre>
19
21
                } else {
                     z[i] = max(r - i + 1, (int)\theta);

while(i + z[i] < n \delta\delta s[i + z[i]] == s[z[i]]) {
23
25
                          z[i]++;
                     l = i;
r = i + z[i] - 1;
27
                     if(z[i] == m) {
29
                           ans++;
31
                }
33
          cout << ans;
35 }
```

## 4. Graph

## 4.1. 2-SAT(CSES Planets Cycles).cpp

```
#define int long long
using namespace std;

int n, m;
vector<int> v[200005];
int d[200005];
int low[200005];
int now = 0;
int now = 0;
int scc[200005];
stack<int> s;
int op[200005];
vector<int> v2[200005];
int ind[200005];
queue<int> q;
int ans[200005];
```

```
int no(int x) {
          if(x > m) return x - m;
          return x + m;
 21
23
     void dfs(int x) {
          d[x] = low[x] = ++cnt;
25
          s.push(x);
for(int i : v[x]) {
   if(scc[i]) continue;
 27
 29
                if(d[i]) -
                     low[x] = min(low[x], d[i]);
                } else {
 31
                    dfs(i);
                     low[x] = min(low[x], low[i]);
33
35
          if(d[x] == low[x]) {
37
               now++
               while(!s.empty()) {
                     int k = s.top();
 39
                    s.pop();
scc[k] = now;
if(k == x) break;
 41
 43
               }
 45
     }
     signed main() {
          ios::sync_with_stdio(0);
 49
          cin.tie(0);
          cout.tie(0);
          cin >> n >>
          while(n--) {
 53
               char a, b;
               int x, y;

cin >> a >> x >> b >> y;

if(a == '-') x = no(x);

if(b == '-') y = no(y);
 57
               v[no(x)].push_back(y);
 59
                v[no(y)].push_back(x);
          for(int i = 1; i <= 2 * m; i++) {
    if(!d[i]) {</pre>
 61
 63
                    dfs(i);
 65
          for(int i = 1; i <= m; i++) {
    if(scc[i] ^ scc[i + m]) {
        op[scc[i]] = scc[i + m]</pre>
 67
                     op[scc[i + m]] = scc[i];
                } else {
                     cout << "IMPOSSIBLE";</pre>
                     exit(0);
          75
 79
                          ind[scc[i]]++;
                     }
81
               }
          for(int i = 1; i <= now; i++) {
    if(!ind[i]) {</pre>
83
                    q.push(i);
85
87
          while(!q.empty()) {
               int k = q.front();
q.pop();
89
               if(!ans[k]) {
    ans[k] = :
 91
                     ans[op[k]] = 2;
 93
 95
                for(int i : v2[k]) {
                     ind[i]-
                     if(!ind[i]) {
                          q.push(i);
 99
          for(int i = 1; i <= m; i++) {
               if(ans[scc[i]] == 1) {
    cout << "+ ";
103
105
               } else {
                     cout << "- ";
107
          }
109 }
```

### 4.2. Dijkstra.cpp

```
1 vector<pair<int, int>> v[100005], v2[100005];
    vector<edge> es;
    int dis1[100005];
     int dis2[100005];
    bitset<100005> vis1, vis2;
    void dijkstra(int x, int *dis, vector<pair<int, int>> *v,
          bitset<100005> &vis) {
priority_queue<pair<int, int>, vector<pair<int, int>>,
 9
                                greater<pair<int, int>>>
11
          memset(dis, 0x3f, sizeof(dis1));
13
          vis.reset();
          dis[x] = 0;
          pq.push({0, x});
while(!pq.empty()) {
15
17
                pair<int, int> now = pq.top();
                pq.pop();
if(vis[now.second]) continue;
19
                if(vis[inow.second] = 1;
for(auto [i, w] : v[now.second]) {
    if(vis[i]) continue;
    if(dis[now.second] + w < dis[i]) {
        dis[i] = dis[now.second] + w;
        result/fiel[i] ;]).</pre>
21
23
25
                            pq.push({dis[i], i});
                      }
27
                }
          }
29 }
```

```
4.3. Dinic.cpp
 1
    using namespace std;
   #define ll long long
    const ll inf = 8e18;
    #define N 505
    #define pb push_back
    struct pp {
         int from, to;
 9
        ll flow;
int t, lvl[N], p[N];
vector<int> g[N];
vector<ppe edge;</pre>
    int bfs(int s) {
        15
17
             for(int e : g[u]) {
    int v = edge[e].to;
    if(lvl[v] || !edge[e].flow) continue;
    lvl[v] = lvl[u] + 1;
19
21
                  q.push(v);
             }
23
         return lvl[t];
25
27
   ll dfs(int u, ll f = inf) {
         if(u == t || !f) return f;
29
        ll ans = 0;
        for(int &i = p[u]; i < g[u].size(); ++i) {
   pp &e = edge[g[u][i]], &b = edge[g[u][i] ^ 1];
   if(lvl[e.to] == lvl[u] + 1) {</pre>
31
                  ll c = dfs(e.to, min(e.flow, f));
33
                  e.flow -= c;
                  b.flow += c;
35
                  f -= c;
37
                  ans += c:
             }
39
        return ans;
41
    ll dinic(int s) {
43
         ll ans = 0;
         for(; bfs(s); memset(lvl, 0, sizeof lvl))
              for(ll k; k = (memset(p, 0, sizeof(p)), dfs(s));)
45
47
         return ans;
49
   int main() {
         ios::sync_with_stdio(0);
51
         cin.tie(0);
         cout.tie(0);
53
         int n, m, cnt = 0;
         for(cin >> n >> m; m--;) {
55
             int u, v;
             ll f;
cin >> u >> v >> f;
57
              g[u].pb(cnt++);
59
              g[v].pb(cnt++);
```

```
edge.pb({u, v, f});
edge.pb({v, u, 0});
                                                                                                     dfs(i);
                                                                                  19
                                                                                                     low[x] = min(low[x], low[i]);
63
         cout << dinic(1);</pre>
                                                                                  21
65 }
                                                                                           if(d[x] == low[x]) {
                                                                                  23
                                                                                                while(!s.empty())
         MaximumFlow.cpp
                                                                                  25
                                                                                                     int k = s.top();
                                                                                                     s.pop();
   #define int long long
                                                                                  27
                                                                                                     scc[k] = now;
                                                                                                     if(k == x) break;
 3
   using namespace std;
                                                                                  29
                                                                                                }
                                                                                           }
   int n, m;
                                                                                  31 }
    vector<int> v[1005];
    int head[1005];
    int c[1005][1005];
                                                                                     4.6.
                                                                                            VBCC.cpp
   int lv[1005];
   int ans = 0;
11
                                                                                      using namespace std;
   bool bfs() {
   memset(head, 0, sizeof(head));
                                                                                      #define pb push_back
13
                                                                                      #define pii pair<int, int>
        memset(lv, 0, sizeof(lv));
                                                                                     #define N 100005
15
         queue<int> q;
                                                                                      vector<int> adj[N], bcc[N];
                                                                                      stack<int> st;
int dfn[N], low[N], tag, bc, root;
         q.push(1);
         while(!q.empty()) {
17
                                                                                      bitset<N> ap;
             int now = q.front();
                                                                                      void dfs(int now, int par = -1) {
19
              q.pop();
              if(now == n) continue;
                                                                                  11
                                                                                           st.push(now)
             for(int i : v[now]) {
   if(i != 1 && c[now][i] && !lv[i]) {
        lv[i] = !v[now] + 1;
                                                                                           low[now] = dfn[now] = ++tag;
21
                                                                                           int f = 0;
                                                                                  13
                                                                                           for(int e : adj[now] | views::reverse) {
   if(e == par) continue;
   if(!dfn[e]) {
23
                       q.push(i);
                                                                                  15
25
                  }
                                                                                                     dfs(e, now), low[now] = min(low[now], low[e]);
if(low[e] >= dfn[now]) {
             }
                                                                                  17
         return lv[n];
                                                                                  19
                                                                                                          if(++f > 1 | | now != root) ap[now] = 1;
29
   }
                                                                                                          ++bc;
                                                                                                          for(; st.top() != now; st.pop())
   bcc[bc].pb(st.top());
                                                                                  21
   int dfs(int x, int flow) {
   int ret = 0;
31
                                                                                  23
                                                                                                          bcc[bc].pb(now);
         if(x == n) return flow;
         for(int i = head[x]; i < v[x].size(); i++) {</pre>
                                                                                  25
                                                                                                } else
35
              int y = v[x][i];
                                                                                                     low[now] = min(low[now], dfn[e]);
              head[x] = 
                                                                                  27
              if(c[x][y] 88 lv[y] == lv[x] + 1) {
37
                  int d = dfs(y, min(flow, c[x][y]));
flow -= d;
                                                                                  29
                                                                                      int main() {
39
                                                                                           int n, m, u, v;
                  c[x][y] -= d;
c[y][x] += d;
                                                                                  31
                                                                                           cin >> n >> m;
41
                                                                                           vector<pii> g(m);
                  ret += d:
                                                                                  33
                                                                                           for(auto &[u, v] : g)
                                                                                           cin >> u >> v, adj[u].pb(v), adj[v].pb(u);
for(root = 1; root <= n; ++root)</pre>
             }
43
                                                                                  35
        return ret;
45
                                                                                                if(!dfn[u]) dfs(root);
                                                                                           int ans = 0;
for(int i :: views::iota(1) | views::take(n))
                                                                                  37
47
                                                                                           if(ap[i]) ++ans;
cout << ans << "\n";
for(int i : views::iota(1) | views::take(n))
    if(ap[i]) cout << i << " ";</pre>
   signed main() {
                                                                                  39
49
         cin >> n >> m;
         while(m--) {
                                                                                  41
             int x, y, z;
cin >> x >> y >> z;
                                                                                  43 }
             if(c[x][y] || c[y][x]) {
    c[x][y] += z;
                                                                                            one-degree-cycle(CSES Planets Cycles).cpp
55
                  continue:
57
             v[x].push_back(y);
                                                                                      #define int long long
             v[y].push_back(x);
                                                                                      using namespace std;
59
             c[x][y] = z;
                                                                                      int n, q;
int a[200005];
61
         while(bfs()) {
             ans += dfs(1, INT_MAX);
                                                                                      int r[200005];
63
                                                                                      int d[200005];
         cout << ans;
                                                                                      int cycle[200005];
65 }
                                                                                      int len[200005];
                                                                                      int cnt = 0;
                                                                                      vector<int> v[200005];
   4.5. SCC.cpp
                                                                                      bitset<200005> vis1;
                                                                                  13
   int n, m;
                                                                                      bitset<200005> vis2;
    vector<int> v[100005];
    int d[100005];
                                                                                      void findcycle(int x) {
    int low[100005];
                                                                                  17
                                                                                           while(!vis1[x]) {
   int cnt = 0;
                                                                                                vis1[x] = 1;
    stack<int> s
                                                                                  19
                                                                                                x = a[x];
   int scc[100005];
   int now = 0:
                                                                                  21
                                                                                           cnt++
                                                                                           cycle[x] = cnt;
   void dfs(int x) {
    d[x] = low[x] = ++cnt;
                                                                                           r[x] = 0;
                                                                                  23
                                                                                           len[cnt] = 1;
11
        s.push(x);
for(int i : v[x]) {
                                                                                           int temp = a[x];
while(temp ^ x) {
    r[temp] = len[cnt];
                                                                                  25
13
                                                                                  27
              if(scc[i]) continue;
15
              if(d[i])
                                                                                                len[cnt]++:
                  low[x] = min(low[x], d[i]);
                                                                                                cycle[temp] = cnt;
```

```
temp = a[temp];
31
        }
   }
33
   void dfs(int x) {
35
        if(vis2[x]) return;
        vis2[x] = 1;
for(int i : v[x]) {
            dfs(i);
39
   }
41
   void dfs2(int x) {
   if(cycle[x] || d[x]) return;
43
        dfs2(a[x]);
        d[x] = d[a[x]] + 1;
r[x] = r[a[x]];
45
47
        cycle[x] = cycle[a[x]];
   }
49
   signed main() {
        ios::sync_with_stdio(0);
51
        cin.tie(0);
        cout.tie(0);
        for(int i = 1; i <= n; i++) {
            cin >> a[i];
57
             v[i].push_back(a[i]);
            v[a[i]].push_back(i);
59
        for(int i = 1;
                         i <= n; i++) {
            if(!vis2[i]) {
61
                 findcycle(i);
                 dfs(i);
63
65
        for(int i = 1; i <= n; i++) {
            if(!cycle[i] && !r[i]) {
67
                 dfs2(i);
69
                         i <= n; i++) {
        for(int i = 1:
71
            cout << d[i] + len[cycle[i]] << " ";
73
   }
```

#### 5. DP

#### 5.1. CHO.cpp

```
struct line {
         int a. b:
         int y(int x) { return a * x + b; }
    };
 5
    struct CHO {
         deque<line> dq;
         int intersect(line x, line y) {
  int d1 = x.b - y.b;
  int d2 = y.a - x.a;
 9
              return d1 / d2;
         bool check(line x, line y, line z) {
13
              int I12 = intersect(x, y);
int I23 = intersect(y, z);
15
              return I12 < I23;
17
         void insert(int a, int b) {
   if(!dq.empty() && a == dq.back().a) return;
19
              while(dq.size() >= 2 &&
                     !check(dq[dq.size() - 2], dq[dq.size() - 1],
21
23
                   dq.pop_back();
25
              dq.push_back({a, b});
27
         void update(int x) {
              while(dq.size() >= 2 && dq[0].y(x) >= dq[1].y(x)) {
29
                   dq.pop_front();
31
         int query(int x) {
33
              update(x);
              return dq.front().y(x);
35
    };
```

#### 5.2. Li-Chao-SegmentTree.cpp

```
1 struct line {
   int a, b = 10000000000000;
```

```
int y(int x) { return a * x + b; }
   };
 5
   line tree[4000005];
   int n, x;
int s[200005];
int f[200005];
 9
   int dp[200005];
11
    void update(line ins, int l = 1, int r = 1e6, int index = 1) {
        if(l == r) {
   if(ins.y(l) < tree[index].y(l)) {</pre>
13
                  tree[index] = ins;
15
17
             return;
         int mid = (l + r) >> 1;
if(tree[index].a < ins.a) swap(tree[index], ins);</pre>
19
         if(tree[index].y(mid) > ins.y(mid)) {
             swap(tree[index], ins);
             update(ins, l, mid, index << 1);</pre>
25
             update(ins, mid + 1, r, index \ll 1 | 1);
27
   }
29
   int query(int x, int l = 1, int r = 1000000, int index = 1) {
         int cur = tree[index].y(x);
31
         if(l == r) {
             return cur;
33
        int mid = (l + r) >> 1;
if(x <= mid) {</pre>
35
             return min(cur, query(x, l, mid, index << 1));</pre>
37
         } else {
             return min(cur, query(x, mid + 1, r, index << 1 | 1));</pre>
39
        }
   }
```

### 5.3. SOSDP.cpp

```
for(int i = 0; i < 20; ++i)
    for(int j = i; j < N; ++j)
    if(j >> i & 1) dp[j] += dp[j ^ (1 << i)]; // subset
for(int i = 0; i < 20; ++i)
    for(int j = 0; j < N; ++j)
    if(!(j >> i & 1))
        dp2[j] += dp2[j | (1 << i)]; // superset</pre>
```

#### 6. Geometry

## 6.1. 164253Version.cpp

```
1
    using namespace std;
 3
    #define ll long long
    #define pb push_back
   #define pll pair<int,</pre>
    #define pdd pair<double, double>
   #define pll pair<ll, ll>
    #define F first
   #define S second
    #define eps 1e-6
11 int sign(double x) {
         return fabs(x) < eps ? 0 : x > 0 ? 1 : -1;
13
    int sign(ll x) { return !x ? 0 : x > 0 ? 1 : -1; }
   template <typename T1, typename T2>
    istream &operator>>(istream &s, pair<T1, T2> &p) {
         auto δ[a, b] = p;
s >> a >> b;
17
19
         return s;
    template <typename T1, typename T2>
    ostream &operator<<(ostream &s, const pair<T1, T2> p) {
         auto &[a, b] = p;
s << a << " " << b;
23
25
         return s;
   pll operator+(const pll a, const pll b) {
   return {a.F + b.F, a.S + b.S};
27
29
    pll operator-(const pll a, const pll b) {
   return {a.F - b.F, a.S - b.S};
31
   pll operator-(const pll a) { return {-a.F, -a.S}; }
pll operator*(const pll a, const pll b) {
   return {(ll)a.F * b.F, (ll)a.S * b.S};
33
35
   pdd operator/(const pll a, const double x) {
   return {a.F / x, a.S / x};
37
39 }
```

```
pdd operator*(const pll a, const double x) {
    return {a.F * x, a.S * x};
 41
                                                                                  135
     pdd operator*(const double x, const pll a) {
 43
          return {a.F * x, a.S * x};
                                                                                  137
      //沒有標示幾個 vector 的都是對三個點做事,以第一個點為參考點
    ll len2(pll p) {
          return (ll)p.F * p.F + (ll)p.S * p.S;
    } // 1 vector
     double len(pll p) { return sqrt((double)len2(p)); }
    ll cross(pil a, pil b) {
    return (ll)a.F * b.S - (ll)a.S * b.F;
 51
       // 2 vector
     ll cross(pll p1, pll p2, pll p3) {
    return cross(p2 - p1, p3 - p1);
 55
    59
       //(b-a) dot (c-a)
    15
    bool btw(pll p1, pll p2, pll p3) {
    return ori(p3, p1, p2) == 0 88 dot(p3, p1, p2) <= 0;
} // r2 britant f = 0 88 dot(p3, p1, p2) <= 0;
                                                                                   17
    } // p3 bwteen p1,p2
bool banana(pll p1, pll p2, pll p3,
pll p4) { //問兩線段是否香蕉
                                                                                   19
          if(btw(p1, p2, p3) || btw(p1, p2, p4) || btw(p3, p4, p1) |
                                                                                  21
             btw(p3, p4, p2))
return true;
                                                                                   23
          return ori(p1, p2, p3) * ori(p1, p2, p4) < 0 δδ ori(p3, p4, p1) * ori(p3, p4, p2) < 0;
                                                                                   25
    pdd banana_point(pll p1, pll p2, pll p3,
pll p4) { //分點,算的是無限延伸直線的交點
//平行的時候 undefined
                                                                                   27
                                                                                   29
          return cross(p2 - p1, p4 - p1) /
                  (double)cross(p2 - p1, p4 - p3) * p3 - cross(p2 - p1, p3 - p1) /
 79
                                                                                   31
                       (double)cross(p2 - p1, p4 - p3) * p4;
                                                                                   33
    pdd proj(pll p1, pll p2, pll p3) {
    return dot(p1, p2, p3) / (double)len2(p2 - p1) * (p2 - p1);
 83
                                                                                   35
     87
          return min(len(p3 - p1), len(p3 - p2));
return abs(cross(p1, p2, p3)) / len(p2 - p1);
 89
 91
     il area2(vector<pll> &v) { //傳入一個多邊形照順序的點集
//起點要出現兩次,回傳兩倍面積
//注意是兩倍才可以 ll 避免浮點數
 93
 95
          int n = v.size() - 1:
          for(int i = 0; i < n; ++i) ans += cross(v[i], v[i + 1]);
 97
          return abs(ans);
 99
     11
101
                                  //{-1:in, 0:on, 1:out}
                                                                                   13
          int n = v.size() - 1, ans = 1;
for(int i = 0; i < n; ++i)</pre>
103
                                                                                   15
              if(btw(v[i], v[i + 1], p)) return 0;
(int i = 0; i < n; ++i)
105
               if(banana(v[i], v[i + 1], p, {(ll)2e9 + 7, p.S + 1LL}))
                            -1;
          //對於任意 p 到 \{W, p.S+1\} //的向量中不會有整數點存在,其中需要滿足 \{W, p.S+1\}
109
          //必須很遠,保證在多邊形外
          return ans;
113
     void solve() {
115
          cin >> n:
117
          vector<pll> v(n);
          for(pll &e : v) cin >> e;
119
          v.pb(v[0]);
                                                                                   11
          ll ans = area2(v) + 2, ans2 = 0;
for(int i = 0; i < n; ++i) {
   if(v[i].F == v[i + 1].F)</pre>
121
                                                                                   13
               ans2 += abs(v[i].S - v[i + 1].S);
else if(v[i].S == v[i + 1].S)
123
                                                                                   15
                   ans2 += abs(v[i].F - v[i + 1].F);
125
                                                                                   17
                   ans2 += gcd(abs(v[i].F - v[i + 1].F),
abs(v[i].S - v[i + 1].S));
127
                                                                                   19
129
                                                                                   21
          cout << (ans - ans2) / 2 << " " << ans2;
131
     int main() {
```

```
int t = 1;
// cin>>t;
for(; t--;) {
    solve();
}
```

#### 6.2. ConvexHull.cpp

```
#define int long long
#define fastio
     ios_base::sync_with_stdio(0);
     cin.tie(0):
     cout.tie(0);
using namespace std;
template <typename T>
pair<T, T> operator-(pair<T, T> a, pair<T, T> b) {
     return make_pair(a.first - b.first, a.second - b.second);
template <typename T> T cross(pair<T, T> a, pair<T, T> b) {
     return a.first * b.second - a.second * b.first;
template <typename T>
vector<pair<T, T>> getCH(vector<pair<T, T>> v) {
     int n = v.size();
     sort(v.begin(), v.end());
vector<pair<T, T>> hull;
for(int i = 0; i < 2; i++) {
   int t = hull.size();
   for(int);</pre>
          for(auto x : v) {
    while(hull.size() - t >= 2 &&
                      cross(hull[hull.size() - 1] -
                             hull[hull.size() - 2],
x - hull[hull.size() - 2]) <= 0)
                    hull.pop_back();
              hull.push_back(x);
          hull.pop_back();
          reverse(v.begin(), v.end());
     return hull;
```

## 6.3. Inside.cpp

```
int inside(point p) {
    int ans = 0;
    for(int i = 1; i <= n; i++) {
        if(onseg(a[i], a[i + 1], {p.x, p.y})) {
            return -1;
        }
        if(intersect({p.x, p.y}, {INF, p.y}, a[i], a[i + 1])) {
            ans ^= 1;
        }
        point temp = a[i].y > a[i + 1].y ? a[i] : a[i + 1];
        if(temp.y == p.y && temp.x > p.x) {
            ans ^= 1;
        }
    }
    return ans;
}
```

#### 6.4. Intersect.cpp

```
struct point {
    int x, y;
    point operator+(point b) { return {x + b.x, y + b.y}; }
    point operator-(point b) { return {x - b.x, y - b.y}; }
    int operator*(point b) { return x * b.x + y * b.y; }
    int operator^(point b) { return x * b.x + y * b.y; }
};

bool onseg(point x, point y, point z) {
    return ((x - z) ^ (y - z)) == 0 && (x - z) * (y - z) <= 0;
}

int dir(point x, point y) {
    int k = x ^ y;
    if(k == 0) return 0;
    if(k > 0) return 1;
    return -1;
}

bool intersect(point x, point y, point z, point w) {
    if(onseg(x, y, z) || onseg(x, y, w)) return 1;
    if(onseg(z, w, x) || onseg(z, w, y)) return 1;
    if(dir(y - x, z - x) * dir(y - x, w - x) == -1 &&
```

```
return query(L, R, l, mid, index << 1);</pre>
            dir(z - w, x - w) * dir(z - w, y - w) == -1) {
25
             return 1;
                                                                                37
                                                                                         if(L > mid) {
27
         return 0;
                                                                                              return query(L, R, mid + 1, r, index << 1 | 1);</pre>
                                                                                39
                                                                                         return max(query(L, mid, l, mid, index << 1),
                                                                                 41
                                                                                                      query(mid + 1, R, mid + 1, r, index << 1 | 1));
   6.5. MinimumEuclideanDistance.cpp
                                                                                    }
                                                                                 43
                                                                                    void modify(int x, int val, int l = 1, int r = n,
    #define int long long
                                                                                         int index = 1) {
if(l == r) {
                                                                                45
    #define pii pair<int, int>
    using namespace std;
                                                                                47
                                                                                              tree[index] = val;
                                                                                              return:
                                                                                49
    vector<pair<int, int>> v;
                                                                                         int mid = (l + r) >> 1;
if(x <= mid) {</pre>
   set<pair<int, int>> s;
int dd = LONG_LONG_MAX;
                                                                                51
                                                                                              modify(x, val, l, mid, index << 1);</pre>
                                                                                         } else {
                                                                                 53
   modify(x, val, mid + 1, r, index << 1 | 1);
13
                                                                                         tree[index] = max(tree[index << 1], tree[index << 1 | 1]);</pre>
                                                                                57
    signed main() {
                                                                                    void dfs(int x, int pre) {
17
         ios::sync_with_stdio(0);
                                                                                         si[x] = 1;
         cin.tie(0);
                                                                                 61
                                                                                         for(int i : v[x]) {
         cout.tie(0);
19
                                                                                              if(i == pre) continue;
                                                                                 63
         for(int i = 0; i < n; i++) {
21
                                                                                              d[i] = d[x] + 1;
             int x, y;
cin >> x >> y;
x += 1000000000;
                                                                                65
                                                                                              dfs(i, x);
23
                                                                                              si[x] += si[i];
                                                                                67
25
             v.push_back({x, y});
                                                                                    }
                                                                                69
         sort(v.begin(), v.end());
27
                                                                                    void dfs2(int x, int pre, int t) {
        int l = 0;
for(int i = 0; i < n; i++) {</pre>
                                                                                71
                                                                                         tp[x] = t;
st[x] = ++cnt;
29
             int d = ceil(sqrt(dd));
while(l < i && v[i].first - v[l].first > d) {
                                                                                         int ma = 0;
                                                                                73
31
                                                                                         for(int i : v[x]) {
    if(i == pre) continue;
    if(si[i] > si[ma]) {
                  s.erase({v[l].second, v[l].first});
                                                                                75
33
                                                                                                  ma = i;
                                                                                77
             auto x = s.lower_bound({v[i].second - d, 0});
35
             auto y = s.upper_bound({v[i].second + d, 0});
for(auto it = x; it != y; it++) {
    dd = min(dd, dis({it->second, it->first}, v[i]));
37
                                                                                         if(!ma) return;
                                                                                         dfs2(ma, x, t);
for(int i : v[x]) {
39
             s.insert({v[i].second, v[i].first});
                                                                                              if(i == pre || i == ma) {
                                                                                 83
41
                                                                                                   continue:
         cout << dd;
                                                                                 85
43 }
                                                                                              dfs2(i, x, i);
                                                                                87
                                                                                         }
                                                                                    }
         Tree
                                                                                 89
                                                                                    int f(int x, int y) {
                                                                                         int ret = 0;
while(tp[x] ^ tp[y]) {
          HeavyLightDecomposition(modify-and-query-
                                                                                91
          on-path).cpp
                                                                                              if(d[tp[x]] < d[tp[y]]) {
                                                                                 93
                                                                                                   swap(x, y);
                                                                                95
    #define int long long
   using namespace std;
                                                                                              ret = max(ret, query(st[tp[x]], st[x]));
                                                                                97
                                                                                              x = p[tp[x]];
    int tree[800005];
                                                                                99
                                                                                         if(d[x] > d[y]) swap(x, y);
                                                                                         ret = max(ret, query(st[x], st[y]));
   int n, q;
int a[200005]
                                                                                         return ret;
                                                                               101
    int st[200005];
                                                                               103
    int tp[200005];
                                                                                    signed main() {
    int p[200005];
                                                                               105
                                                                                         ios::sync_with_stdio(0);
    int cnt = 0:
    int d[200005]:
                                                                                         cin.tie(0);
   int si[200005];
vector<int> v[200005];
                                                                               107
                                                                                         cout.tie(0);
                                                                                         cin >> n >> q;
for(int i = 1; i <= n; i++) {
15
    int b[200005];
                                                                               109
                                                                                              cin >> a[i];
17
    void build(int l = 1, int r = n, int index = 1) {
                                                                               111
19
        if(l == r) {
                                                                                         for(int i = 1; i < n; i++) {
                                                                                              int x, y;
cin >> x >> y;
             tree[index] = b[l];
                                                                               113
21
                                                                               115
                                                                                              v[x].push_back(y);
        int mid = (l + r) >> 1;
build(l, mid, index << 1);</pre>
23
                                                                                              v[y].push_back(x);
                                                                               117
25
         build(mid + 1, r, index << 1 | 1);
                                                                                         dfs(1, 0);
                                                                                         dfs2(1, 0, 1);
for(int i = 1; i <= n; i++) {
    b[st[i]] = a[i];</pre>
         tree[index] = max(tree[index << 1], tree[index << 1 | 1]); 119</pre>
27
   }
   int query(int L, int R, int l = 1, int r = n, int index = 1) {
   if(L == l && r == R) {
29
                                                                                         build();
                                                                               123
                                                                                         while(q--) {
             return tree[index];
31
                                                                                              int mode, x, y;
cin >> mode >> x >> y;
if(mode == 1) {
                                                                               125
        int mid = (l + r) >> 1;
if(R <= mid) {</pre>
33
                                                                               127
```

modify(st[x], y);

```
129
               } else {
                     cout << f(x, y) << " ";
                                                                                       13
131
                                                                                                      len = 0;
                                                                                        15
133 }
                                                                                                 num(LL x) {
                                                                                        17
                                                                                                      len = 0;
    7.2. LCA.cpp
                                                                                        19
     #define int long long
                                                                                       21
                                                                                                 num operator=(LL x) {
  3
     using namespace std;
                                                                                       23
     int n, q;
int a[200005][21];
                                                                                                      len = 0;
                                                                                       25
     int d[200005];
                                                                                       27
                                                                                                      return *this;
     vector<int> v[200005];
     void init() {
                                                                                       29
                                                                                                 num max(const num &b) {
          for(int j = 1; j < 21; j++) {
    for(int i = 1; i <= n; i++) {
        a[i][j] = a[a[i][j - 1]][j - 1];
}</pre>
 11
                                                                                       31
 13
                                                                                       33
 15
                                                                                        35
     }
                                                                                                      num c;
 17
     void dfs(int x, int pre) {
   for(int i : v[x]) {
      if(i == pre) {
                                                                                       37
                                                                                                      LL x = 0;
 19
                                                                                       39
 21
                    continue:
                                                                                       41
                                                                                                           c.p[i] %= base;
 23
               a[i][0] = x;
               d[i] = d[x] + 1;
                                                                                       43
                                                                                                      return c;
 25
               dfs(i, x);
                                                                                       45
     }
                                                                                                 num operator*(LL b) {
 27
                                                                                       47
                                                                                                      num c;
c.len = len;
     int lca(int x, int y) {
    while(d[x] ^ d[y]) {
        if(d[x] < d[y]) {</pre>
 29
                                                                                        49
 31
                                                                                       51
                    swap(x, y);
 33
                                                                                        53
               int k =
                            _lg(d[x] - d[y]);
               x = a[x][k];
 35
                                                                                        55
 37
          if(x == y) {
                                                                                       57
               return x;
                                                                                           } dp[N][N], ans;
 39
          for(int i = 20; i >= 0; i--) {
                                                                                       59
               if(a[x][i] != a[y][i]) {
    x = a[x][i];
 41
                                                                                        61
                                                                                                 s << a.p[a.len - 1];
                     y = a[y][i];
 43
                                                                                       63
                                                                                                      if(!a.p[i])
               }
                                                                                                          s << "000000000";
 45
                                                                                                      else {
                                                                                       65
          return a[x][0];
 47
     }
                                                                                       67
                                                                                                           s << a.p[i];
 49
     signed main() {
                                                                                       69
                                                                                                      }
          ios::sync_with_stdio(0);
          cin.tie(0);
                                                                                        71
                                                                                                 return s;
          cout.tie(0);
          cin >> n >> q;
for(int i = 1; i < n; i++) {
                                                                                        73
                                                                                           LL a[N];
                                                                                            int main() {
               int x, y;
cin >> x >> y
                                                                                        75
                                                                                                 ios::sync_with_stdio(0);
                                                                                                 cin.tie(0);
 57
               v[x].push_back(y);
                                                                                       77
                                                                                                 cout.tie(0);
               v[y].push_back(x);
                                                                                                 int n, m, i, j;
 59
                                                                                       79
          dfs(1, 0);
init();
 61
                                                                                       81
          while(q--) {
               int x, y;
cin >> x >> y;
int k = lca(x, y);
cout << (d[x] + d[y] - 2 * d[k]) << "\n";
                                                                                       83
 65
                                                                                       85
 67
          }
                                                                                       87
     }
                                                                                       89
                                                                                                      ans = ans + dp[0][m - 1];
           Misc
                                                                                       91
                                                                                                 cout << ans;
    8.1. BigNum(luoguP1005).cpp
                                                                                       93 }
```

```
1 //洛谷 P1005
  using namespace std;
  #define N 85
  #define LL long long
  #define pii pair<int, int>
#define F first
  #define S second
  struct num {
      const static LL base = 1000000000LL; // base 1e9
```

```
LL p[505], len;
       num() {
              memset(p, 0, sizeof(p));
              memset(p, 0, sizeof(p));
              for(p[len++] = x; p[len - 1] >= base; ++len)
    p[len] = p[len - 1] / base, p[len - 1] %= base;
              memset(p, 0, sizeof(p));
              for(p[len++] = x; p[len - 1] >= base; ++len)
    p[len] = p[len - 1] / base, p[len - 1] %= base;
             if(len != b.len) return len > b.len ? *this : b;
for(int i = len; i--;)
    if(p[i] != b.p[i]) return p[i] > b.p[i] ? *this : b;
       num operator+(const num &b) {
              for(LL &i = c.len; i < len || i < b.len; ++i) {
   c.p[i] = p[i] + b.p[i] + x;
   x = c.p[i] / base;</pre>
              if(x) c.p[c.len++] = x;
              LL x = 0;
for(LL i = 0; i < len; ++i) {
                    c.p[i] = p[i] * b + x;
x = c.p[i] / base;
c.p[i] %= base;
              for(; x; x /= base) c.p[c.len++] = x % base;
ostream &operator<<(ostream &s, num a) {
   if(!a.len) return s << "0";
       for(int i = a.len - 1; i--;) {
                    for(int k = 10; k * a.p[i] < (LL)1e9; k *= 10)
    s << _"0";</pre>
       for(cin >> n >> m; n--;) {
   for(i = 0; i < m; ++i) cin >> a[i];
   for(i = 0; i < m; ++i)
      for(j = 0; j < m; ++j) dp[i][j] = 0;</pre>
             for(i = 0; i < m; ++i) dp[i][i] = a[i] << 1;

for(j = 1; j < m; ++j)

for(i = 0; i + j < m; ++i)

dp[i][i + j] =
                                  (dp[i][i + j
                                                       - 1] + a[i + j])
                                        \max(dp[i + 1][i + j] + a[i]) *
```

## 8.2. Tri-search.cpp

```
using namespace std;
int n;
double a[15], x, y;
double get(double x) {
    double ret = 0;
```

```
for(int i = 0; i <= n; i++) {
   ret += k * a[i];</pre>
11
                 k *= x;
13
           return -ret;
    }
15
    template <class T> T bi_search(T l, T r, T end) {
   if(!check(r - end)) return r - end;
   for(; r - l > end;) {
      T mid = (l + r) / 2;
   if(shear(-int))
17
19
                 if(check(mid))
21
                      r = mid;
                 else
                       l = mid;
23
25
           return l;
     /*check gives 000000001111 find the last 0*/
     template <class T> T tri_search(T l, T r, T end) {
29
           T midl, midr;
for(;;) {
31
                midl = (l + r) / 2;
midr = (midl + r) / 2;
if(midr - midl < end) break;
33
                 if(get(midr) > get(midl))
35
                      r = midr;
                 else
37
                      l = midl;
39
          for(; r - l > end;) {
    midl = (l + r) / 2;
    if(get(r) > get(l))
41
                      r = midl;
43
                 else
                       l = midl;
45
47
           return l;
49
     /*get gives the value, find the minimum*/
           cin >> n >> x >> y;
for(int i = n; i >= 0; i--) {
                 cin >> a[i];
55
           cout << fixed << setprecision(7)</pre>
5.7
                  << tri_search<double>(x, y, 1e-7);
     }
```

## AnotherVersionDataStructure

#### 9.1. BIT.cpp

```
template <class T> class BIT { \#define\ lb(x)\ ((x)\ \delta\ -(x))
   #define N (int)2e5 + 5
      public:
        T bit[N] = \{0\};
        void update(T x, T v) {
             for(; x < N; x += lb(x)) bit[x] += v;
 9
        T qry(T x) {
             T ans = 0;
             for(; x; \dot{x} -= lb(x)) ans += bit[x];
             return ans;
   #undef lb
   #undef N
15
17 /*1based bit update 預設是加值 */
```

### 9.2. DSU.cpp

```
template <class T> class Dsu {
   #define N 2000005
      public:
         T dsu[N], size[N];
Dsu(T n) {
    for(; n; --n) dsu[n] = n, size[n] = 1;
         T qry(T x) {
9
              if(dsu[x] == x) return x;
              return dsu[x] = qry(dsu[x]);
11
         void merge(T a, T b) {
13
              a = qry(a);
              b = qry(b);
if(a == b) return;
if(size[a] < size[b])
15
```

```
dsu[a] = b, size[b] += size[a];
          else
19
              dsu[b] = a, size[a] += size[b];
21 #undef N
23 /*1based 初始化為 dsu[x]=x 路徑壓縮 + 啟發式合併 */
```

### 9.3. Treap.cpp

```
1 // treap 模板 洛谷 P3369 【模板】普通平衡树
    using namespace std;
    #define pnn pair<node *, node *>
   #define F first
    #define S second
   mt19937 mt(hash<string>()("official_beautiful_fruit"));
    struct node {
         node *l, *r;
 9
         int val, sz;
        int mx, mn, sum;
int rev_tag, add_tag;
11
13
         node(int x)
              : val(x), l(\theta), r(\theta), sz(1), rev_tag(\theta), add_tag(\theta), mx(x), mn(x), sum(x) {}
         node(node *tr)
             : val(tr->val), l(tr->l), r(tr->r), sz(tr->sz),
  rev_tag(tr->rev_tag), add_tag(tr->add_tag),
  mx(tr->mx), mn(tr->mn) {}
17
19
         void pull() {
21
             sz = 1;
mx = mn = sum = val;
23
              if(l)
                   sz += l->sz, mx = max(mx, l->mx),
mn = min(mn, l->mn), sum += l->sum;
25
              if(r)
27
                   sz += r->sz, mx = max(mx, r->mx),
                                   mn = min(mn, r->mn), sum += r->sum;
29
         void push() {
             if(rev_tag) swap(l, r);
if(l) l->add_tag += add_tag, l->rev_tag ^= rev_tag;
if(r) r->add_tag += add_tag, r->rev_tag ^= rev_tag;
31
33
              mx += add_tag;
              mn += add_tag;
35
              sum += add_tag;
37
              add_tag = 0;
              rev_tag = 0;
39
   void debug(node *tr) {
41
         if(!tr) return;
         tr->push();
43
         tr->pull();
        debug(tr->l);
cout << tr->val << " ";</pre>
45
47
         debug(tr->r);
49
   void debug2(node *tr) {
         if(!tr) return;
         tr->push();
51
         tr->pull();
         cout << tr->val << " ";
53
         debug2(tr->l);
55
         debug2(tr->r);
57
   int sz(node *tr) { return tr ? tr->sz : 0; }
    node *merge(node *a, node *b) {
         if(!a || !b) return a ?: b;
         a->push();
61
         b->push();
         if(mt() % (sz(a) + sz(b)) < sz(a)) {
63
             a->r = merge(a->r, b);
              a->pull();
65
              return a;
67
         b->l = merge(a, b->l);
         b->pull();
69
         return b;
   pnn split(node *tr, int v) { //(-inf,v],(v,inf)
    if(!tr) return {0, 0};
71
73
         tr->push();
         if(tr->val_- <= v) {
             auto [l, r] = split(tr->r, v);
tr->r = l;
75
              tr->pull();
77
             return {tr, r};
79
         auto [l, r] = split(tr->l, v);
81
         tr->l = r:
         tr->pull();
83
         return {l, tr};
```

```
pnn splitsz(node *tr, int k) { //[rk.1,rk.k],(rk.k,rk.n]
    if(!tr || sz(tr) <= k) return {tr, 0};</pre>
 87
              ->push();
           if(k <= sz(tr->l)) {
                auto [l, r] = splitsz(tr->l, k);
 89
                tr->1 = r
 91
                tr->pull();
          return {l, tr};
} else if(k <= sz(tr->l) + 1) {
 93
                auto r = tr -> r;
 95
                tr->r = 0
                tr->pull();
                return {tr, r};
           } else {
                auto [l, r] = splitsz(tr->r, k - (sz(tr->l) + 1));
tr->r = l;
 99
                tr->pull();
101
                return {tr, r};
103
     node *insert(node *tr, int v) {
   auto [l, r] = split(tr, v);
105
           return merge(merge(l, new node(v)), r);
     node *insertkth(node *tr, int k) {
   auto [l, r] = splitsz(tr, k -
109
111
           return merge(merge(l, new node(0)),
                           r); // new node 拿來區間操作初始化
113
     node *eraseall(node *tr, int v) {
          auto [l, r] = split(tr, v
115
           return merge(l, split(r, v).S);
117
     node *eraseone(node *tr, int v) {
119
          auto [l, r] = split(tr, v - 1)
           return merge(l, splitsz(r, 1).S);
121
     node *erasekth(node *tr, int k) {
123
          auto [l, r] = splitsz(tr, k
           return merge(l, splitsz(r, k).S);
125
     int rnk(node *tr, int v) {
127
          if(!tr) return 0;
           if(tr->val <= v) return sz(tr->l) + 1 + rnk(tr->r, v);
129
           return rnk(tr->l, v);
131
     int kth(node *&tr, int k) {
          auto [l, x] = splitsz(tr, k - 1);
auto [m, r] = splitsz(x, 1);
133
           if(!m) return 0;
135
           int ans = m->val;
           tr = merge(merge(l, m), r);
137
          return ans:
     int count(node *&tr, int L, int R) { // count[L,R]
    auto [l, x] = split(tr, L - 1);
    auto [m, r] = split(x, R);
    int ans = m->sz; //看要改啥
139
141
           tr = merge(merge(l, m), r);
143
          return ans;
145
     int countkth(node *8tr, int L, int R) { // count[rk.L,rk.R]
    auto [l, x] = splitsz(tr, L - 1);
           auto [m, r] = splitsz(x, R - L);
           int ans = m->sum; //
149
           tr = merge(merge(l, m), r);
151
           return ans;
     int prev(node *&tr, int v) {
153
          auto [x, r] = split(tr, v - 1);
auto [l, m] = splitsz(x, sz(x) - 1);
155
           int ans = m->val;
157
           tr = merge(merge(l, m), r);
           return ans;
159
     int next(node *&tr, int v) {
          auto [l, x] = split(tr, v);
auto [m, r] = splitsz(x, 1);
int ans = m->val;
161
163
           tr = merge(merge(l, m), r);
165
          return ans;
     int qry(node *&tr, int L, int R) { // qry[L,R] auto [x, r] = splitsz(tr, R); auto [l, m] = splitsz(x, L - 1); int ans - m > cum: //季電池中
167
169
           int ans = m->sum;
           tr = merge(merge(l, m), r);
171
           return ans;
173
     void modify(node *&tr, int L, int R, int v) { // modify[L,R]
          auto [x, r] = splitsz(tr, R);
auto [l, m] = splitsz(x, L - 1);
```

```
m->val += v;
         m->add_tag += v;
         m->rev_tag = 1; //看要改啥
179
         tr = merge(merge(l, m), r);
181
    int main() {
183
         int t;
         node *tr = 0;
185
         for(cin >> t; t--;) {
             int op, x;
cin >> op >> x;
187
             switch(op) {
189
             case 1:
                 tr = insert(tr, x);
191
                 break;
             case 2:
193
                 tr = eraseone(tr, x);
                 break;
195
             case 3:
                 cout << rnk(tr, x - 1) + 1 << "\n";
197
199
                  cout << kth(tr, x) << "\n";</pre>
                 break;
201
             case 5:
                 cout << prev(tr, x) << "\n";
203
                 break;
             case 6:
205
                 cout << next(tr, x) << "\n";
                 break;
207
             }
         }
209 }
```

## **9.4.** Treap 但可以多個數縮點 (疑似爛的).cpp

```
1 // treap 模板 洛谷 P3369 【模板】普通平衡树
 3
   using namespace std;
   #define pnn pair<node *, node *>
#define F first
    #define S second
   #define int long long
   mt19937 mt(hash<string>()("official_beautiful_fruit"));
   struct node {
        int val, sz;
11
        int mx, mn, sum, num;
13
        int rev_tag, add_tag;
        15
        mx(_val), mn(_val), rev_tag(0), add_tag(0) {}
node(node *tr)
17
             : val(tr->val), l(tr->l), r(tr->r), sz(tr->sz) {}
        void pull() {
19
             sz = 1:
             mx = mn = sum = num;
21
             if(1)
23
                 sz += l->sz, mx = max(mx, l->mx),
                                mn = min(mn, l->mn), sum += l->sum;
25
                 sz += r->sz, mx = max(mx, r->mx),
mn = min(mn, r->mn), sum += r->sum;
27
29
        void push() {
             if(rev_tag) swap(l, r);
if(l) l->add_tag += add_tag, l->rev_tag ^= rev_tag;
31
             if(r) r->add_tag += add_tag, r->rev_tag ^= rev_tag;
33
             mx += add_tag;
             mn += add_tag;
             sum += add_tag;
35
             add_tag = 0;
37
             rev_tag = 0;
39
    void debug(node *tr) {
41
        if(!tr) return;
        debug(tr->l);
        cout << tr->val << " ";
43
        debug(tr->r);
45
    void debug2(node *tr) {
        if(!tr) return;
cout << tr->val << " ";</pre>
47
        debug2(tr->l);
49
        debug2(tr->r);
51
   int sz(node *tr) { return tr ? tr->sz : 0; }
node *merge(node *a, node *b) {
   if(!a || !b) return a ?: b;
53
        if(mt() % (sz(a) + sz(b)) < sz(a)) {
   a->r = merge(a->r, b);
55
57
             a->pull();
```

```
59
           b->l = merge(a, b->l);
 61
           b->pull();
           return b:
     }
 63
     pnn split(node *tr, int v) { //(-inf,v],(v,inf)
    if(!tr) return {0, 0};
 65
           tr->push();
           if(tr->val <= v) {
 67
                auto [l, r] = split(tr->r, v);
tr->r = l;
 69
                tr->pull();
 71
                return {tr, r};
           auto [l, r] = split(tr->l, v);
 73
           tr -> l = r
           tr->pull();
 75
           return {l, tr};
     }
     pnn splitsz(node *tr, int k) { //[rk.1,rk.k],(rk.k,rk.n]
    if(!tr || sz(tr) <= k) return {tr, 0};</pre>
           tr->push();
 81
           if(k <= sz(tr->l)) {
                auto [l, r] = splitsz(tr->l, k);
tr->l = r;
 83
                tr->pull();
           return {l, tr};
} else if(k <= sz(tr->l) + 1) {
                auto r = tr->r;
                tr->r = 0;
                tr->pull();
 89
                return {tr, r};
           } else {
 91
                auto [l, r] = splitsz(tr->r, k - (sz(tr->l) + 1)); tr->r=l;
 93
                tr->pull();
 95
                return {tr, r};
 97
     node *insert(node *tr, int val = 0, int num = 1) {
   auto [l, r] = split(tr, val);
 99
           return merge(merge(l, new node(val, num)), r);
101
     }
     103
105
     107
           return merge(l, split(r, v).S);
109
     node *eraseone(node *tr, int v) {
    auto [l, r] = split(tr, v - 1);
    return mana(l, splits;(n, 1));
111
           return merge(l, splitsz(r, 1).S);
113
115
     node *erasekth(node *tr, int k) {
          auto [l, r] = splitsz(tr, k - 1);
return merge(l, splitsz(r, k).S);
117
119
     int rnk(node *tr, int v) {
           if(!tr) return 0;
           if(tr->val <= v) return sz(tr->l) + 1 + rnk(tr->r, v);
           return rnk(tr->l, v);
123
     int kth(node *&tr, int k) {
    auto [l, x] = splitsz(tr, k - 1);
    auto [m, r] = splitsz(x, 1);
125
           if(!m) return 0;
127
           int ans = m->val;
129
           tr = merge(merge(l, m), r);
           return ans;
131
     int count(node *&tr, int L, int R) { // count[L,R]
auto [l, x] = split(tr, L - 1);
auto [m, r] = split(x, R);
int ans = m->sum; //看要改啥
133
135
           tr = merge(merge(l, m), r);
137
           return ans:
     int countkth(node *8tr, int L, int R) { // count[rk.L,rk.R]
    auto [l, x] = splitsz(tr, L - 1);
    auto [m, r] = splitsz(x, R - L);
    int ans = m->sum; //看要改啥
139
141
           tr = merge(merge(l, m), r);
143
           return ans;
145
     int prev(node *&tr, int v) {
          auto [x, r] = split(tr, v - 1);
auto [l, m] = splitsz(x, sz(x) - 1);
147
           int ans = m->val;
           tr = merge(merge(l, m), r);
```

```
return ans:
153 int next(node *&tr, int v) {
           auto [l, x] = split(tr, v);
           auto [m, r] = splitsz(x, 1);
int ans = m->val;
155
157
           tr = merge(merge(l, m), r);
           return ans:
159
     int qry(node *&tr, int L, int R) { // qry[L,R]
          auto [l, x] = splitsz(tr, L - 1);
auto [m, r] = splitsz(x, R);
161
163
           int ans = m->sum;
           tr = merge(merge(l, m), r);
165
           return ans:
     void modify(node *&tr, int L, int R, int v) { // modify[L,R]
   auto [l, x] = splitsz(tr, L - 1);
   auto [m, r] = splitsz(x, R);
167
169
          m->val += v;
m->add_tag += v; //看要改啥
171
           tr = merge(merge(l, m), r);
173
     }
      signed main() {
175
           vector<node *> tr(2);
          177
179
           for(; m--;) {
                int op = -1, p = -1, x = -1, y = -1; scanf("%lld", &op);
181
183
                if(!op) {
                     scanf("%lld%lld%lld", &p, &x, &y);
auto [l, tmp] = split(tr[p], x - 1);
185
                      auto [m, r] = split(tmp, y);
187
                     tr[p] = merge(l, r);
                     tr.push_back(m)
                } else if(op == 1) {
    scanf("%lld%lld", &p, &x);
    // cout<<kth(tr[x],1)<<"\n";//break;
    auto [l, r] = split(tr[p], kth(tr[x], 1));
    tr[p] = merge(merge(l, tr[x]), r);
}</pre>
189
191
193
                } else
195
                     switch(op) {
                     case 2:
197
                           scanf("%lld%lld", &p, &x, &y);
                           tr[p] = insert(tr[p], y, x);
199
                           break:
                     case 3:
                           scanf("%lld%lld", &p, &x, &y);
201
                           printf("%lld\n", count(tr[p], x, y));
203
                           break;
                      case 4:
                          scanf(<mark>"%lld%lld"</mark>, &p, &x);
printf("%lld\n", kth(tr[p], x));
205
207
209
```

#### 9.5. 區間插線段單點查詢李超 (是爛的).cpp

```
1 // luogu P4097 區間插線段李超
  3
     using namespace std;
     #define N 50005
     struct Line {
            double a, b;
            int l, r, id; // ax+b{l<=x<=r}</pre>
           Int (, r, iu, // ax*b[t--x--1]
Line(double _a = -1e6, double _b = -1, int _l = 1,
    int _r = N, int _id = 0)
    : a(_a), b(_b), l(_l), r(_r), id(_id) {}
double operator()(int x) { return a * x + b; }
      } line[N];
13
    int seg[N << 2];</pre>
    #define lid (id << 1)
#define rid (id << 1 | 1)
#define M (L + R >> 1)
15
     #define eps 1e-6
     void ins(int l, int L = 1, int R = N, int id = 1) {
    // cout<<"ins{"<<line[l].a<<","<<li>line[l].b<<","<<liline[l].l<<","
    // "<<R<<"\n";</pre>
19
            if(line[l].r < L || R < line[l].l) return;</pre>
21
            if(L == R)
                  if(line[l](M) - line[seg[id]](M) > eps) seg[id] = l;
23
                  return:
25
            if(line[l].l <= M && M <= line[l].r &&
27
                 line[l](M) - line[seg[id]](M) > eps)
            swap(1, seg[id]);
if(line[l].l <= L && R <= line[l].r) {
   if(line[l].a - line[seg[id]].a > eps)
29
```

```
ins(l, M + 1, R, rid);
            else
33
                ins(l, L, M, lid);
35
        /*if(line[l].a>line[seg[id]].a)*/ ins(l, M + 1, R, rid);
        /*else */ ins(l, L, M, lid);
37
39
        if(L == R) return seg[id];
41
        int k = (x \le M ? qry(x, L, M, lid)
       43
45
47
49
        if(not_seg) return k;
       return line[k](x) - line[seg[id]](x) > eps ? k : seg[id];
51
   int main() {
53
        int n, ans = 0, p = 1;
        for(cin >> n; n--;) {
55
            int op;
            cin >> op;
            if(op) {
                int x0, y0, x1, y1;
cin >> x0 >> y0 >> x1 >> y1;
                x0 = (x0 + ans - 1) \% 39989 + 1;

y0 = (y0 + ans - 1) \% 1000000000 + 1;
                x1 = (x1 + ans - 1) % 39989 + 1;
y1 = (y1 + ans - 1) % 1000000000 + 1;
                if(x0 > x1) swap(x0, x1), swap(y0, y1);
// cout<<"?"<<((double)y1-y0)/(x1-x0)<<"</pre>
                    "<<y0-x0*((double)y1-y0)/(x1-x0)<<"\n";
                if(x0 != x1)
                     x0, x1, p);
                     line[p] = Line(0, max(y0, y1), x0, x1, p);
                ins(p);
            ++p;
} else {
                int k;
cin >> k;
                k = (k + ans - 1) \% 39989 + 1;
                cout << (ans = qry(k)) << "\n";
81
        // cout<<qry(9)<<"\n";
```

#### 9.6. 單點修改動態開點線段樹.cpp

```
using namespace std;
   #define N 200005
#define M int m = l + r >> 1
   #define MAX 1000000000
   int a[N];
   typedef struct node {
       struct node *l, *r;
       int val;
   void check(node *tree, int flag) {
11
       if(flag && !tree->r)
13
            tree->r = (node *)malloc(sizeof(struct node)),
            tree->r->val = 0;
       else if(!flag && !tree->l)
tree->l = (node *)malloc(sizeof(struct node)),
17
            tree->l->val = 0;
19
   void upd(int pos, int val, int l, int r, node *tree) {
       tree->val += val;
21
       if(l == r) return;
23
       if(pos > m)
           check(tree, 1), upd(pos, val, m + 1, r, tree->r);
25
            check(tree, 0), upd(pos, val, l, m, tree->l);
27
   int qry(int a, int b, int l, int r, node *tree) {
   if(!tree) return θ;
29
       if(a <= l && r <= b) return tree->val;
31
       33
35
   }
```

```
37 | int main() {
                                                                                                                                                                                                                                                                                                                                                                                                                                    int n, q, i = 1, x;
                                                                                                                                                                                                                                                                                                                                                                                         39
                                                                                                                                                                                                                                                                                                                                                                                                                                     node *root = (node *)malloc(sizeof(struct node));
                                                                                                                                                                                                                                                                                                                                                                                                                                     root->val = 0;
                                                                                                                                                                                                                                                                                                                                                                                                                                    for(scanf("%d %d", &n, &q); i <= n; ++i)
getchar(), scanf("%d", a + i),
                                                                                                                                                                                                                                                                                                                                                                                          41

}
int qry(int x, int L = 1, int R = N, int id = 1) {
    // cout<<"qry"<<x<<"{"<<li>"<<li>"<<li>"", "<<li>", "<</li>", ", ", qry(2,2,1,n,1),qry(3,3,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1),qry(5,1,n,1,n,1),qry(5,1,n,1,n,1),qry(5,1,n,1,n,1),qry(5,1,n,1,n,1
                                                                                                                                                                                                                                                                                                                                                                                                                                                            getchar();
                                                                                                                                                                                                                                                                                                                                                                                          47
                                                                                                                                                                                                                                                                                                                                                                                                                                                            char c = getchar();
scanf(" %d %d", &x, &i);
if(c == '!')
                                                                                                                                                                                                                                                                                                                                                                                          49
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                   upd(a[x], -1, 1, MAX, root),
a[x] = i, upd(i, 1, 1, MAX, root);
                                                                                                                                                                                                                                                                                                                                                                                         51
                                                                                                                                                                                                                                                                                                                                                                                         53
                                                                                                                                                                                                                                                                                                                                                                                                                                                                                    printf("%d\n", qry(x, i, 1, MAX, root));
                                                                                                                                                                                                                                                                                                                                                                                                                                   }
                                                                                                                                                                                                                                                                                                                                                                                          55
                                                                                                                                                                                                                                                                                                                                                                                                            }
```

#### 9.7. 單點修改無懶標線段樹.cpp

```
1 template <class T> class Seg {
   #define lid id << 1
   #define rid id << 1 |
   #define M (L + R >> 1)
   #define N 200005
 5
      public:
        T a[N], seg[N << 2];
        Seg() {
             for(int i = 1; i <= n; ++i) cin >> a[i];
             init();
11
        T update(int pos, int val, int L = 1, int R = n,
    int id = 1) {
13
             if(L == R) return seg[id] = val;
15
             if(pos > M)
                 return seg[id] = seg[lid]
17
                                     update(pos, val, M + 1, R, rid);
             return seg[id] = update(pos, val, L, M, lid) + seg[rid];
19
        T qry(int l, int r, int L = 1, int R = n, int id = 1) {
   if(l <= L && R <= r) return seg[id];</pre>
21
             if(L == R) return seg[id];
23
             int M = L + R >> 1;
             if(l > M) return qry(l, r, M + 1, R, rid);
             if(r <= M) return qry(l, r, L, M, lid);
return qry(l, M, L, M, lid) +</pre>
25
27
                     qry(M + 1, r, M + 1, R, rid);
        }
29
      private:
        T init(int l = 1, int r = n, int id = 1) {
31
            if(l == r) return seg[id] = a[l];
int m = l + r >> 1;
33
             return seg[id] = init(l, m, lid) + init(m + 1, r, rid);
35
    #undef lid
   #undef rid
37
    #undef N
   /*1based 陣列 1based id 單點修改 預設維護區間和 */
```

## 9.8. 懶標線段樹.cpp

```
1 struct Seg {
    #define lid (id << 1)
#define rid ((id << 1) | 1)
    #define M (L + R >> 1)
#define N 200005
          LL seg[N << 2], tag[N << 2];
          void inline addtag(int id, LL v, int L, int R) {
    seg[id] += v * (R - L + 1);
                tag[id] += v;
          void inline push(int id, int L, int R) {
   addtag(lid, tag[id], L, M);
   addtag(rid, tag[id], M + 1, R);
11
13
                tag[id] = 0;
15
          void inline pull(int id) { seg[id] = seg[lid] + seg[rid]; }
          void init(int L = 1, int R = n, int id = 1) {
17
                if(L == R) {
                     seg[id] = 0;
19
                     tag[id] = 0;
21
                     return;
               init(L, M, lid);
init(M + 1, R, rid);
23
                pull(id);
25
```

```
if(l <= L && R <= r) {
29
                      addtag(id, v, L, R);
31
                push(id, L, R);
if(r <= M)</pre>
33
                upd(l, r, v, L, M, lid);
else if(M + 1 <= l)
    upd(l, r, v, M + 1, R, rid);</pre>
35
37
                else
                     upd(l, M, v, L, M, lid),
upd(M + 1, r, v, M + 1, R, rid);
39
                pull(id);
41
          LL qry(int l, int r, int L = 1, int R = n, int id = 1) {
    if(l <= L && R <= r) return seg[id];
43
               push(id, L, R);
if(r <= M) return qry(l, r, L, M, lid);
if(M + 1 <= l) return qry(l, r, M + 1, R, rid);
return qry(l, M, L, M, lid) +</pre>
45
                          qry(M + 1, r, M + 1, R, rid);
49
          }
    } seg;
    /*1based 陣列 1based id 區間修改 預設維護區間和 */
```

## 9.9. 純直線單點查詢李超.cpp

```
// luogu P4254 李超
   using namespace std;
   #define N 50005
   struct Line {
        double a, b; // ax+b
        double operator()(int x) { return a * x + b; }
} seg[N << 2];</pre>
   | seglN << \( \sigma \);
| #define lid (id << 1)
| #define rid (id << 1 | 1)
| #define M (L + R >> 1)
   void ins(Line l, int L = 1, int R = N, int id = 1) {
   if(L == R) {
15
            if(seg[id].a < 0 || l(M) > seg[id](M)) seg[id] = l;
            return:
        if(l(M) > seg[id](M)) swap(l, seg[id]);
19
        if(l.a > seg[id].a)
            ins(l, M + 1, R, rid);
21
        else
23
            ins(l, L, M, lid);
   double qry(int x, int L = 1, int R = N, int id = 1) {
        if(L == R) return seg[id](x);
        if(x <= M) return max(qry(x, L, M, lid), seg[id](x));</pre>
        return max(seg[id](x), qry(x, M + 1, R, rid));
29
   int main() {
        int n;
        for(cin >> n; n--;) {
            string s;
33
            cin >> s;
if(s[0] == 'Q') {
35
                 int x;
37
                 cin >> x:
                 cout << \max(0, ((int)(qry(x) * 100)) / 10000)
39
                       << "\n";
            } else {
                 double s, p;
cin >> s >> p
41
                 ins(Line(p, s));
43
            }
45
        }
   }
```

## 10. AnotherVersionMath

## 10.1. CRT(luoguVersion).cpp

## 10.2. PollardRho.cpp

```
1
    using namespace std;
    #define LL long long
    #define uLL __uint128_t
    #define sub(a, b) ((a) < (b) ? (b) - (a) : (a) - (b))
    template <class T, class POW>
void fastpow(T x, POW n, POW p, T & ans) {
          for(; n; n >>= 1) {
                if(n & 1) {
                      ans *= x;
                      ans %= p;
11
13
                x *= x;
                x \%= p;
15
    /* 輸入 x,n,p,ans 會將 ans 修改為 x^n%p
對整數/矩陣/不要求精度的浮點 皆有效
模板中個型別是 x,ans 第二個是 n,p(應該放 LL 或
17
                                                                       int128)*/
    ull pri[7] = {2, 325, 9375, 28178, 450775, 9780504, 1795265022}; /*2^64*/
// int p[3]={2,7,61};/*2^32*/
bool check(const ull x, const ull p) {
    ull d = x - 1, ans = 1;
21
          fastpow(p, d, x, ans);
if(ans != 1) return 1;
for(; !(d δ 1);) {
                d >>= 1;
                 ans = 1;
29
                 fastpow(p, d, x, ans);
                 if(ans == x
31
                     return 0;
33
                 else if(ans != 1)
                      return 1;
35
          return 0:
37
     bool miller_rabin(const uLL x) {
39
           if(x == 1) return 0;
           for(auto e : pri) {
   if(e >= x) return 1;
41
                if(check(x, e)) return 0;
43
          return 1:
    }
45
     template <class T> T gcd(T a, T b) {
          if(!a) return b;
if(!b) return a;
47
          if(a & b & 1) return gcd(sub(a, b), min(a, b));

if(a & 1) return gcd(a, b >> 1);

if(b & 1) return gcd(a >> 1, b);

return gcd(a >> 1, b >> 1) << 1;
49
51
    /*gcd(a,b) 默認 gcd(a,0)=a*/
mt19937 rnd(time(0));
template <class T> T f(T x, T c, T mod) {
55
          return (((uLL)x) * x % mod + c) % mod;
59
    template <class T> T rho(T n) {
          T \mod = n, x = rnd() \% \mod, c = rnd() \% (\mod - 1) + 1,
61
           for(T i = 2, j = 2, d = x;; ++i) {
  x = f(x, c, mod), p = ((uLL)p) * sub(x, d) % mod;
  if(i % 127 == 0 && gcd(p, n) != 1) return gcd(p, n);
63
                if(i == j) {
                       j <<= 1, d = x;
67
                      if(gcd(p, n) != 1) return gcd(p, n);
                }
69
71
    template <class T> T pollard_rho(T n) {
          if(miller_rabin(n)) return n;
73
          while(p == n) p = rho(n);
return max(pollard_rho(p), pollard_rho(n / p));
75
77
    int main() {
          LL t, n, ans;
for(cin >> t; t--;) {
79
                cin >> n:
                 ans = pollard_rho(n);
81
                if(ans == n)
                     puts("Prime");
83
                 else
85
                      printf("%lld\n", ans);
          }
87 }
```

#### 10.3. 快速幕.cpp

```
1 template <class T, class POW>
```

```
void fastpow(T x, POW n, POW p, T &ans) {
          for(; n; n >>= 1) {
    if(n & 1) {
                     ans *= x;
                     ans %= p;
               x *= x;
               x %= p;
    }
11
    ,/* 輸入 x,n,p,ans 會將 ans 修改為 x^n%p
對整數/矩陣/不要求精度的浮點 皆有效
模板第一個型別是 x,ans 第二個是 n,p(應該放 LL 或 __int128)*/
```

# 10.4. 數論.cpp

```
template <class T> T extgcd(T a, T b, T &x, T &y) {
          if(!b) {
               x = 1;
                y = 0;
                return a:
          T ans = extgcd(b, a \% b, y, x);
          y -= a / b * x;
          return ans:
    /*extgcd(a,b,x,y)=ax+by,x 跟 y 是會被修改的參數 */
11
    template <class T> T modeq(T a, T b, T p) {
          T x, y, d = extgcd(a, p, x, y);
if(b % d) return 0;
return ((b / d * x) % p + p) % p;
13
15
    /*x=modeq(a,b,n),ax=b(mod n),0<=x< n
    modeq(a,1,n) 相當於求 a 在 mod n 下的逆元 */
    template <class T> T gcd(T a, T b) {
19
          if(!a) return b;
          if(!b) return a;
          if(a \delta b \delta 1) return gcd(abs(a - b), min(a, b));
          if(a & 1) return gcd(a, b >> 1);
if(b & 1) return gcd(a >> 1, b);
23
          return gcd(a >> 1, b >> 1) << 1;
27
     /*gcd(a,b) 默認 gcd(a,0)=a*
    ll crt(V<ll> &p, V<ll> &a) {
29
          ll n = 1, ans = 0, k = a.size();
                                                                                                  11
          for(ll &e : p) n *= e;
for(int i = 0; i < k; ++i)</pre>
31
                                                                                                  13
                ans = (ans + a[i] * n / p[i] % n *
33
                                         modeq(n / p[i], 1LL, p[i]) % n) %
                                                                                                  15
          return (ans % n + n) % n;
35
                                                                                                  17
    /*(a+b)^p \equiv a+b \equiv a^p+b^p \pmod{p} (小費馬)
                                                                                                  19
    (p-1)! \equiv -1 \pmod{p} (風爾遼定理)

v(n) := n + p的冪次, (n)_p := \frac{n}{p^v(n)},
                                                                                                  21
    s(n) := p進制下n的所有位數和 v(n!) = \sum_{i=1}^{\infty} \bigcup_{p=1}^{n} \left( 執壤得定理\right)
                                                                                                  23
                                                                                                  25
    v(\binom{n}{m}) = \frac{s(n)+s(m-n)-s(m)}{p-1} (庫默爾定理)
    v(\binom{n}{m_1, m_2, \dots m_k}) \stackrel{i}{=}
                                                                                                  27
    \sum_{i=1}^{k} \frac{s(mi)-s(n)}{s(mi)} (庫默爾定理推廣)
45
                                                                                                  29
    1
47
          (n!)_p\equiv-1^{\lfloor\frac{n}{p}\rfloor}
                                                                                                  31
49
    1/
                                                                                                  33
          ((\floor\frac{n}{p}\rfloor)!)_p((n\p)!)\pmod p
    \]
                                                                                                  35
    打階乘表 + 迭代這條式子可以 O(p + log_p(n)) (mod 下階乘)
    打階乘表 + 数代這條式子可以 O(p + log_p(n)) \binom{n}{m} \equiv \frac{((n+m)!)p}{(n!)p(m!)p} p^{v(n+m)-v(n)-v(m)} \pmod{p^q} 把 p 從 C(n,m) 裡面隔離掉了 就能用上面的 (n!)_p + 模逆元 \pmod{r} 下下乘推廣至二項式
53
                                                                                                  37
                                                                                                  39
    ((p^q)!)_p \equiv \pm 1 \pmod p^q (威爾遜定理推廣)
                                                                                                  41
57
59
          \binom{n}{m}\equiv\binom{\lfloor\frac{n}{p}\rfloor}
                                                                                                  43
    \]
    \lfloor \frac{m}{p} \rfloor \binom{n \% p}{m \% p} \pmod{p} (lucas 定理) 打階乘表跟模逆元表 + 迭代這條式子可以 O(p + log_p(n))
                                                                                                  45
61
                                                                                                  47
       p 進制下任何一位 i 滿足 n_i < m_i 則
      \binom{n_i}{m_i}\%p = 0
                                                                                                  49
   則因 \binom{n}{m} = \prod_{i=0}^{\max(\log_p(a),\log_p(b))}
則因 \binom{n_i}{m_i}%p 導致 \binom{n}{m}%p = 0
設 p = 2 則有 \binom{n}{m} 是奇數的充要條件為二進制下每一位
n < m (lucas 定理可由此生成函數做法得到
不依賴小費馬 對多項式也成立 根據上述
                      \max(\log_p(a), \log_p(b))
                                                                                                  51
                                                                                                  53
    \binom{n}{m}%k 可將 k 做唯一質數分解
個別做完再做 crt 得到結果 (exlucas 定理)
                                                                                                  55
71
    1/
                                                                                                  57
73
           卡特蘭數 C(0)=C(1)=1.n>1 時 C(n)=\sum {k=0}^{n-1}C(k)C(n-1-k)=
    \]
```

```
\binom{\binom{r}{r-1}}{n+1} 同時 n 對括號的合法放置數即是 C(n) 若有任意 k 種括號可選 則
 77
    C(n)k^n
     模逆元表 p=i*(p/i)+p%i,-p%i=i*(p/i),inv(i)=-(p/i)*inv(p%i)*/
 79  LL fracp[N], invp[N];
void fracp_init(LL p) {
    fracp[0] = 1;
          for(int i = 1; i < p; ++i) fracp[i] = fracp[i - 1] * i % p;</pre>
 83 }
     void invp_init(LL p) {
    invp[0] = invp[1] = 1;
    for(int i = 2; i < p; ++i)
        invp[i] = p - (p / i * invp[p % i]) % p;</pre>
 89
     /* 階乘表跟模逆元表 之後可以考慮改一下長相 */
     template <class T> T lucas(T n, T m, T p) {
 91
          if(!m) return 1;
          if(m > n | | m % p > n % p) return 0;
          return lucas(n / p, m / p, p) * fracp[n % p] % p * invp[fracp[n % p - m % p]] % p * invp[fracp[m % p]] %
 93
 95
    /*lucas(n,m,p)=C(n,m)%p 要求要帶階乘表跟模逆元表
97
      * O(p+log_p(n))*/
 99
     /* 米勒拉賓質數 2,325,9375,28178,450775,9780504,1795265022*/
     /*crt 質數
101 (2^16)+1 65537 3
     7*17*(2^23)+1 998244353 3
1255*(2^20)+1 1315962881 3
     51*(2^25)+1 1711276033 29
105 */
```

```
10.5. 篩法.cpp
1 // 待加入分塊節
   template <class T> class Prime {
   #define N (int)1e8 + 9
      public:
         vector<T> list, factor;
         Prime(T n) {
               eular(n);
               // eratosthenes(n);
// sqrt_sieve
               // factorize(n);
         void show() {
               for(T e : list) printf("%lld ", e);
putchar('\n');
      private:
         bitset<N> notprime; // 1e8<2^27=128MB
         void eular(T n) {
               for(T i = 2; i <= n; ++i) {
    if(!notprime[i]) list.emplace_back(i);</pre>
                     const T k = n / i;
for(T j : list) {
                           if(j > k) break;
                           notprime[i * j] = 1;
                           if(!(i % j)) break;
                     }
               }
         void eratosthenes(T n) {
  for(T i = 2; i <= n; ++i) {
    if(!notprime[i]) list.emplace_back(i);</pre>
                     const T k = n / i;
for(T j : list) {
                           if(j > k) break;
                           notprime[i * j] = 1;
if(!(i % j)) break;
                     }
               }
         void sqrt_sieve(T n) {
    for(T i = 2; i <= n; ++i) {</pre>
                     bool isprime = 1;
                     for(T j : list) {
   if(j > i / j) break;
   if(!(i % j)) {
                                 isprime = 0;
                                 break;
                     if(isprime) list.emplace_back(i);
               }
         void factorize(T n) {
               factor = vector<T>(n);
               factor = vector(i)(i);
if(list.empty()) eular(n);
for(T j : list) factor[j] = j;
for(T i = 2; i <= n; ++i) {
    const T k = n / i;</pre>
```

9

```
for(T j : list) {
        if(j > k) break;
        factor[i * j] = j;
        if(!(i % j)) break;
}

63        if(!(i % j)) break;
}

65     }

#undef N
};

67     /*Prime prime(n) 建立打好 1~n 質數表的物件
prime.list(一個 vector) 是質數表
        可修改 define N 決定歐節/埃飾上限
        可在建構子選擇篩法 有歐節/埃飾/根號暴力搜
prime.factorize(n) 用歐節方式得到 1~n 所有數的最小質因數
        可在 factor(一個 vector) 上一路回溯 logn 得到一個數的質因數分解
        做 n 個數質因數分解共花 nlogn
show() 會以空格隔開 顯示所有 list 內的元素 有尾空格尾換行
printf 裡面用%lld 視情況換為%d 或 cout*/
```

## 11. Another Version String

## 11.1. KMP (2).cpp

```
1 #define V vector

V<int> kmp(string s) {

    int n = s.size();

    V<int> f(n);

    for(int i = 1; i < n; ++i) {

        int j = f[i - 1];

        for(; j > 0 && s[j] != s[i];) j = f[j - 1];

        f[i] = j + (s[j] == s[i]);

    }

    return f;

11 }

// kmp(s+"#"+t) 得到的陣列中,f[i]=s.size() 的格子代表 t

13 // 中匹配到 s 的結尾位置
```

### 11.2. KMP.cpp

#### 11.3. Manacher (2).cpp

```
#define T(x) ((x)&1 ? s[(x) >> 1] :
   int ex(string &s, int l, int r, int n) {
        int i = \bar{0};
while(l - i >= 0 && r + i < n && T(l - i) == T(r + i)) ++i;
 5
         return i:
   int manacher(string s, int n) {
        n = 2 * n + 1;
         int mx = 0;
         int center = 0;
11
         vector<int> r(n);
         int ans = 1;
13
         r[0] = 1;
         for(int i = 1; i < n; i++) {
   int ii = center - (i - center);</pre>
15
              int len = mx - i + 1;
              if(i > mx) {
                  r[i] = ex(s, i, i, n);
             center = i;
    mx = i + r[i] - 1;
} else if(r[ii] == len) {
19
21
                  r[i] = len + ex(s, i - len, i + len, n);
23
                  center = i:
```

```
mx = i + r[i] - 1;
} else {
    r[i] = min(r[ii], len);
}
ans = max(ans, r[i]);
}
return ans - 1;
}
```

#### 11.4. Manacher.cpp

```
1 #define V vector
     string manacher(string t) {
           int n = t.size() << 1 | 1;
string s(n, '#');
for(int i = 0, m = t.size(); i < m; ++i)
        s[i << 1 | 1] = t[i];</pre>
 5
            V<int> p(n);
           _ p[i] >= 0 öö i + p[i] < s[i - p[i]] == s[i + p[i]];) ++p[i];
11
13
                   if(i + p[i] > r) r = i + p[i], m = i;
15
            int k = 0:
            string ans = "";
for(int i = 0; i < n; ++i)
17
            if(p[i] > p[k]) k = i;
for(int r = k + p[k], l = k - p[k]; ++l < r;)
if(s[l] != '#') ans += s[l];</pre>
19
21
            return ans;

      23
      // manacher(s) 給出 s

      // 中的最長回文,若有多個則給字典序最小的,p[i] = 以 i

      25
      // 為中心的最大回文半徑,所有字之間和頭尾都加上 '#'
```

## 11.5. Z.cpp

```
class Z {
1
     public:
       vector<int> z:
       Z(string s) {
            z = vector<int>(s.size());
5
            for(int l = 0, i = 1; i < n; ++i) {
    if(l + z[l] >= i)
                    z[i] = min(z[l] + l - i, z[i - l]);
                while(i + z[i] < n \delta \delta s[z[i]] == s[i + z[i]])
                     ++z[i]:
                if(i + z[i] > l + z[l]) l = i;
11
            }
13
       }
  };
// Z(s+"#"+t) 得到的陣列中,f[i]=s.size() 的格子代表 t
   // 中匹配到 s 的開頭位置
```

### 12. Another Version Graph

#### 12.1. Dijkstra.cpp

```
1 // cses Shortest Routes I
 3
   using namespace std;
    #define N 100005
   #define LL long long
#define pii pair<int, int>
   #define pil pair<LL, LL>
#define F first
   #define S second
   #define pb push_back
#define DE if(1)
11
    #define INF (LL)1e16
   vector<pil> adj[N];
13
    LL d[N];
15
   bitset<N> vis;
    int main() {
17
         int n, m, u, v;
19
         priority_queue<pil, vector<pil>, greater<pil>> q;
        for(cin >> n >> m; m--;)
cin >> u >> v >> c, adj[u].pb({v, c});
21
         q.push({0, 1});
        d[1] = 0;
23
        for(u = 2; u <= n; ++u) d[u] = INF;
for(; !q.empty(); q.pop()) {
    if(vis[q.top().S]) continue;</pre>
25
27
              vis[q.top().S] = 1
             29
                       q.push({d[e.F], e.F});
31
```

```
33
              }
35
         for(u = 1; u <= n; ++u) printf("%lld ", d[u]);</pre>
   12.2. SCC.cpp
    using namespace std;
    #define pb push_back
#define pii pair<int, int>
#define N 100005
    vector<int> adj[N];
    stack<int> st;
int dfn[N], low[N], tag, scc[N], scchead[N], sc;
    bitset<N> in;
    void dfs(int now, int par = -1) {
         st.push(now);
         in[now] = 1;
low[now] = dfn[now] = ++tag;
13
         for(int e : adj[now]) {
   if(e == par) continue;
15
               if(!dfn[e])
17
                    dfs(e, now), low[now] = min(low[now], low[e]);
               else if(in[e])
                    low[now] = min(low[now], dfn[e]);
19
21
         if(dfn[now] == low[now]) {
              for(; st.top() != now; st.pop())
    scc[st.top()] = sc, in[st.top()] = 0;
23
               st.pop();
25
              scc[now] = sc;
in[now] = 0;
scchead[sc] = now;
29
31
    int main() {
         int n, m, u, v;
         cin >> n >> m;
         vector<pii> g(m);
         for(auto &[u, v] : g)
         cin >> u >> v, adj[u].pb(v), adj[v].pb(u);
for(u = 1; u <= n; ++u)
              if(!dfn[u]) dfs(u);
39
         int ans = 0;
         for(auto 8[u, v] : g)
         if(scc[u] != scc[v]) ++ans; //=eBCC
cout << ans << "\n";</pre>
         for(auto &[u, v] : g)
	if(scc[u] != scc[v]) cout << u << " " << v << "\n";
43
45 }
```

### **12.3. cses** 有向圖基環樹森林**.cpp**

```
// cses Planets Queries II 基環樹森林模板
    using namespace std;
    #define N 200005
    #define pb push_back
   #derine pb pusn_Dack
// int cyc[i]=1~n 代表 i 屬於哪顆樹
// bitset incyc[i]=0/1 代表 i 是否在環上
// int len[k]=1~n 代表第 k 棵樹的環長度
// int num[i]=1~n 如果 incyc[i] 代表的是在環上的編號
// 否則代表的是環上最近的點的編號 int dis[i]=0~n-1
// 代表到環上最近點的距離 若 i 在環上則為 0
    int tag = 1, cyc[N], len[N], num[N], dis[N], nxt[N][19];
    bitset<N> vis, incyc;
    vector<int> path;
    void dfs(int now)
15
         if(vis[now]) {
17
              int i = 1:
               for(int k; k = path.back(), path.pop_back(),
                             k != now && !path.empty();
19
                    ++i) {
                    cyc(k) = tag;
21
                    incyc[k] = 1;
                    num[k] = i;
              cyc[now] = tag;
               incyc[now] = 1;
               len[tag] = i;
29
               ++tag;
              return;
31
         vis[now] = 1;
         path.pb(now);
33
         if(!cyc[nxt[now][0]]) dfs(nxt[now][0]);
35
         if(cyc[now]) return;
         cyc[now] = cyc[nxt[now][0]];
         num[now] = num[nxt[now][0]];
```

```
dis[now] = dis[nxt[now][0]] + 1;
39 }
    int jmp(int a, int x) {
    for(int k = 19; k--;)
41
              for(; 1 << k <= x;) x -= 1 << k, a = nxt[a][k];
43
         return a;
45
    int main() {
         ios::sync_with_stdio(0);
47
         cin.tie(0)
         cout.tie(0);
         for(int k = 1; k < 19; ++k)
for(int k = 1; k < 19; ++k)
for(i = 1; i <= n; ++i)
    nxt[i][k] = nxt[nxt[i][k - 1]][k - 1];
for(i = 1; i <= n; ++i)
    nxt[i][k] = nxt[nxt[i][k - 1]][k - 1];</pre>
49
51
53
              if(!cyc[i]) path.clear(), dfs(i);
55
         for(; q--;) {
    cin >> u >> v;
57
              if(cyc[u] == cyc[v]) {
59
                   if(incyc[v])
                        61
                                             len[cyc[u]]
                   63
                        jmp(u, dis[u] - dis[v]) == v)
cout << dis[u] - dis[v] << "\n";</pre>
65
67
                   else
                        cout << "-1\n";
69
              } else
                   cout << "-1\n";
71
         }
    }
```

## 13. Another Version Geometry

## 13.1. DynamicHull.cpp

```
1 struct Line {
         mutable int a, b, r;
         bool operator<(const Line &o) const { return a < o.a; }</pre>
 3
         bool operator<(const int o) const { return r < o; }</pre>
 5 };
   struct DynamicHull : multiset<Line, less<>> {
   inline int Div(int a, int b) {
     return a / b - ((a ^ b) < 0 88 a % b);</pre>
 7
 9
11
          inline bool intersect(iterator x, iterator y) {
               if(y == end()) {
                    x->r = inf;
13
                    return false:
15
               if(x->a == y->a)
                    x->r = (x->b) > (y->b) ? inf : -inf;
17
               else
19
                    x->r = Div((y->b) - (x->b), (x->a) - (y->a));
               return (x->r) >= (y->r);
21
          void Insert(int a, int b) {
              auto y = insert({a, b, 0}), z = next(y), x = y;
while(intersect(y, z)) z = erase(z);
if(x != begin() && intersect(--x, y))
23
25
               intersect(x, y = erase(y));
while((y = x) != begin() && ((--x)->r) >= (y->r))
27
                    intersect(x, erase(y));
29
          int query(int x) const {
               auto l = *lower_bound(x);
31
               return (l.a) *\bar{x} + (l.b);
33
    };
```

## 14. Another Version Tree

#### 14.1. LCA.cpp

```
#define N 100005
#define LG 15
int dep[N], par[N][LG], sub[N];
vector<int> g[N];

void dfs(int now = 1, int pre = 0) {
    dep[now] = dep[pre] + 1;
    par[now][0] = pre;
    sub[now] = 1;
    for(int e : g[now])
        if(e != pre) dfs(e, now), sub[now] += sub[e];

11 }
```

```
int jmp(int x, int k) {
 13
           for(int i = LG; i--;)
               for(; k >= 1 << i; k -= 1 << i) x = par[x][i];
                                                                                         107
 15
           return x;
                                                                                         109
     int lca(int a, int b)
           if(dep[a] > dep[b]) swap(a, b);
                                                                                         111
 19
           b = jmp(b, dep[b] - dep[a]);
          if(a == b) return a;
for(int i = LG; i--;)
    for(; par[a][i] != par[b][i]; b = par[b][i])
                                                                                         113
 21
                                                                                         115
 23
                     a = par[a][i];
          return par[a][0];
                                                                                         117
     }
25
     int main() {
                                                                                         119
          int n;
cin >> n;
27
                                                                                         121
 29
           for(int i = n, u, v; --i;)
                cin >> u >> v, g[u].pb(v), g[v].pb(u);
                                                                                         123
           dfs();
 31
          for(int i = 1; i < LG; ++i)
    for(int j = 1; j <= n; ++j)
        par[j][i] = par[par[j][i - 1]][i - 1];</pre>
                                                                                         125
 33
                                                                                         127
 35
           int k = lca(1, n);
                                                                                         129
     //點編號 1~n,建的無向圖但改 dfs
     //就能變有向,改有向記得邊要反著建 dep[n] 代表 n 的深度 (1
// base),par[i][j] 代表 i 往上 1<<j 步的祖先是誰,不存在則是
                                                                                         131
     // 0,sub[i] 代表 i 的子樹大小 jmp(i,j) 代表 i 往上 j
                                                                                         133
                                                                                         135
     #pragma GCC optimize(
           "Ofast,fast-math,unroll-loops,no-stack-protector")
                                                                                         137
 45
     using namespace std;
                                                                                         139
 47
     #define ll long long
     #define pb push_back
#define N 200005
                                                                                         141
     #define pii pair<int, int>
#define V vector
                                                                                         143
 51
     #define inf 1000000007
                                                                                         145
     #define M 200005
     #define LG 18
                                                                                         147
     #define pii pair<int, int>
     #define ppp pair<pii, pii>
char buf[1 << 22], *p1, *p2;</pre>
                                                                                         149
     int p[12];
                                                                                         151
 59
     #define gc()
          (p1 == p2 &&
                                                                                         153
61
                      (p2 = (p1 = buf) + fread(buf, 1, 1 << 22, stdin),
                       p1 == p2)
                                                                                         155
                 ? E0F
                  : *p1+
                                                                                         157
 65
     inline int gi() {
          int x = 0;
                                                                                         159
           for(char c; '0' <= (c = gc()) && c <= '9'; x += c - '0')
 67
               x *= 10;
                                                                                         161
 69
          return x;
                                                                                         163 }
     inline void pi(int x, char c = ' ') {
   if(!x) putchar('0');
   int i = 0;
 71
 73
          for(; x; x /= 10) p[i++] = x % 10;
for(; i--;) putchar(p[i] + '0');
 75
           putchar(c);
     int main() {
          cin.tie(\theta)->sync_with_stdio(\theta);
          int n, m, q;
cin >> n >> m >> q;
 81
           vector<ppp> g(m);
           bitset<M> ans;
           vector<vector<pii>>> adj(n + 1, vector<pii>());
           for(int i = 0; i < m; ++i) {
auto δ[p1, p2] = g[i];
 85
                auto \delta[w, idx] = p1;
87
               auto δ[u, v] = p2;
89
                cin >> u >> v >> w;
                idx = i:
91
           sort(g.begin(), g.end());
          vector<ll> dsu(n + 1, -1);
auto qry = [8dsu](auto qry, int x) -> int {
    return dsu[x] < 0 ? x : dsu[x] = qry(qry, dsu[x]);</pre>
93
95
          auto upd = [8dsu, 8qry](int u, int v) -> void {
    if(dsu[u = qry(qry, u)] > dsu[v = qry(qry, v)])
97
               swap(u, v);
dsu[u] += dsu[v];
dsu[v] = u;
99
101
          for(auto δ[p1, p2] : g) {
    auto δ[w, idx] = p1;
103
```

```
vector<vector<int>> par(n + 1, vector<int>(LG)),
     mx(n + 1, vector<int>(LG));
vector<int> dep(n + 1);
auto dfs = [8par, 8mx, 8dep, 8adj](auto dfs, int now,
                                           int p = 0
                                           int \dot{w} = 0) -> void {
     par[now][0] = p;
     mx[now][0] = w;
dep[now] = dep[p] + 1;
for(auto &[e, w] : adj[now])
    if(e != p) dfs(dfs, e, now, w);
max(mx[j][i - 1], mx[par[j][i - 1]][i - 1]);
auto lca = [&par, &dep](int u, int v) -> int {
   if(dep[u] > dep[v]) swap(u, v);
     for(int i = LG; i--;)
    if((1 << i) δ (dep[v] - dep[u])) v = par[v][i];
     if(u == v) return u;
     for(int i = LG; i--;)
    if(par[u][i] != p
                             par[v][i])
              u = par[u][i], v = par[v][i];
     return par[u][0];
auto path = [\delta par, \delta mx, \delta dep](int k, int x) \rightarrow int {
     int ans = 0;
     for(int i = LG; i--;)
          if((1 << i) & (dep[x] - dep[k]))
              ans = max(ans, mx[x][i]), x = par[x][i];
     return ans;
for(auto δ[p1, p2] : g) {
    auto δ[w, idx] = p1;
    auto δ[u, v] = p2;
    int k = lca(u, v);
     ans[idx] = max(path(k, u), path(k, v)) >= w;
for(int i = 0; i < m; ++i)
cout << i << " "
           << (const char[2][5]){"NO\n", "YES\n"}[ans[i]];
cout << "\n";
for(int k; q--;) {
    cin >> k;
     int flag = 1;
     for(int x; k--;) {
          if(!ans[x - 1]) flag = 0;
     cout << (const char[2][5]){"NO\n", "YES\n"}[flag];</pre>
```