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## 1.1. Contest

### 1.1.1. Makefile

```
1 .PRECIOUS: ./p%
3 %: p%
    ulimit -s unlimited && ./$<
p%: p%.cpp
    g++ -o $@ $< -std=c++17 -Wall -Wextra -Wshadow \
7    -fsanitize=address,undefined</pre>
```

## 1.2. How Did We Get Here?

#### 1.2.1. Macros

Use vectorizations and math optimizations at your own peril. For gcc≥9, there are [[likely]] and [[unlikely]] attributes. Call gcc with -fopt-info-optimized-missed-optall for optimization info.

# 1.2.2. Fast I/O

```
struct scanner {
    static constexpr size_t LEN = 32 << 20;
    char *buf, *buf_ptr, *buf_end;
    scanner()</pre>
```

```
: buf(new char[LEN]), buf_ptr(buf + LEN),
          buf_end(buf + LEN) {}
   ~scanner() { delete[] buf; }
   char getc() {
  if (buf_ptr == buf_end) [[unlikely]]
       buf_end = buf + fread_unlocked(buf, 1, LEN, stdin),
buf_ptr = buf;
     return *(buf_ptr++);
   char seek(char del) {
     char c;
     while ((c = getc()) < del) {}</pre>
     return c;
   void read(int &t) {
     bool neg = false;
     char c = seek('-');
if (c == '-') neg = true, t = 0;
else t = c ^ '0';
     while ((c = getc()) >= '0') t = t * 10 + (c ^ '0');
     if (neg) t = -t;
};
struct printer {
   static constexpr size_t CPI = 21, LEN = 32 << 20;</pre>
   char *buf, *buf_ptr, *buf_end, *tbuf;
char *int_buf, *int_buf_end;
   printer()
       : buf(new char[LEN]), buf_ptr(buf),
buf_end(buf + LEN), int_buf(new char[CPI + 1]()),
int_buf_end(int_buf + CPI - 1) {}
   ~printer() {
     flush()
     delete[] buf, delete[] int_buf;
     fwrite_unlocked(buf, 1, buf_ptr - buf, stdout);
     buf_pt_r = buf;
   void write_(const char &c) {
     *buf_ptr = c;
     if (++buf_ptr == buf_end) [[unlikely]]
       flush():
   void write_(const char *s) {
     for (; *s != '\0'; ++s) write_(*s);
  void write(int x) {
  if (x < 0) write_('-'), x = -x;</pre>
     if (x == 0) [[unlikely]]
       return write_('0');
     for (tbuf = int_buf_end; x != 0; --tbuf, x /= 10)
  *tbuf = '0' + char(x % 10);
     write_(++tbuf);
};
```

# 1.2.3. constexpr

59

```
Some default limits in gcc (7.x - trunk):

• constexpr recursion depth: 512
• constexpr loop iteration per function: 262\,144
• constexpr operation count per function: 33\,554\,432
• template recursion depth: 900 (gcc might segfault first)
```

```
1 constexpr array<int, 10> fibonacci{[] {
    array<int, 10> a{};
    a[0] = a[1] = 1;
    for (int i = 2; i < 10; i++) a[i] = a[i - 1] + a[i - 2];
    return a;
  }()};
  static_assert(fibonacci[9] == 55, "CE");
9
  template <typename F, typename INT, INT... S>
  constexpr void for_constexpr(integer_sequence<INT, S...>,
                            F &&func)
11
    int _[] = {(func(integral_constant<INT, S>{}), 0)...};
13
  template <typename... T> void print_tuple(tuple<T...> t) {
    17
  }
```

# 1.2.4. Bump Allocator

```
// global bump allocator
char mem[256 << 20]; // 256 MB
size_t rsp = sizeof mem;
void *operator new(size_t s) {</pre>
```

```
assert(s < rsp); // MLE
     return (void *)&mem[rsp -= s];
   void operator delete(void *) {}
   // bump allocator for STL / pbds containers
   char mem[256 << 20];</pre>
   size_t rsp = sizeof mem;
   template <typename T> struct bump {
13
     typedef T value_type;
     bump() {}
     template <typename U> bump(U, ...) {}
     T *allocate(size_t n) {
       rsp -= n * sizeof(T);
rsp &= 0 - alignof(T);
       return (T *)(mem + rsp);
     void deallocate(T *, size_t n) {}
23 };
```

#### 1.3. Tools

# 1.3.1. Floating Point Binary Search

```
union di {
    double d;
    ull i;
};

bool check(double);
// binary search in [L, R) with relative error 2^-eps
double binary_search(double L, double R, int eps) {
    di l = {L}, r = {R}, m;
    while (r.i - l.i > 1LL << (52 - eps)) {
        m.i = (l.i + r.i) >> 1;
        if (check(m.d)) r = m;
        else l = m;
}
return l.d;
}
```

# 1.3.2. SplitMix64

```
using ull = unsigned long long;
inline ull splitmix64(ull x) {

// change to `static ull x = SEED;` for DRBG
ull z = (x += 0x9E3779B97F4A7C15);

z = (z ^ (z >> 30)) * 0xBF58476D1CE4E5B9;
z = (z ^ (z >> 27)) * 0x94D049BB133111EB;

return z ^ (z >> 31);
}
```

### 1.3.3. <random>

#### 1.4. Algorithms

# 1.4.1. Bit Hacks

```
// next permutation of x as a bit sequence
ull next_bits_permutation(ull x) {
  ull c = _builtin_ctzll(x), r = x + (1 << c);
  return (r ^ x) >> (c + 2) | r;
}

// iterate over all (proper) subsets of bitset s

void subsets(ull s) {
  for (ull x = s; x;) { --x &= s; /* do stuff */ }
}
```

## 1.4.2. Aliens Trick

```
// min dp[i] value and its i (smallest one)
pll get_dp(int cost);
l aliens(int k, int l, int r) {
    while (l != r) {
        int m = (l + r) / 2;
        auto [f, s] = get_dp(m);
        if (s = k) return f - m * k;
        if (s < k) r = m;
        else l = m + 1;
    }
return get_dp(l).first - l * k;
}</pre>
```

#### 1.4.3. Hilbert Curve

#### 1.4.4. Infinite Grid Knight Distance

```
1  ll get_dist(ll dx, ll dy) {
    if (++(dx = abs(dx)) > ++(dy = abs(dy))) swap(dx, dy);
    if (dx == 1 && dy == 2) return 3;
    if (dx == 3 && dy == 3) return 4;
    ll lb = max(dy / 2, (dx + dy) / 3);
    return ((dx ^ dy ^ lb) & 1) ? ++lb : lb;
    }
```

#### 2. Data Structures

#### 2.1. GNU PBDS

```
1 #include <ext/pb_ds/assoc_container.hpp>
#include <ext/pb_ds/priority_queue.hpp>
3 #include <ext/pb_ds/tree_policy.hpp>
   using namespace __gnu_pbds;
   // useful tags: rb_tree_tag, splay_tree_tag
11
   template <typename T> struct myhash {
    size_t operator()(T x) const; // splitmix, bswap(x*R), ...
13
   };
// most of std::unordered_map, but faster (needs good hash)
15
   template <typename T, typename U = null_type>
   using hash_table = gp_hash_table<T, U, myhash<T>>;
   // most std::priority_queue + modify, erase, split, join
   using heap = priority_queue<int, std::less<>>;
21
   // useful tags: pairing_heap_tag, binary_heap_tag,
                     (rc_)?binomial_heap_tag, thin_heap_tag
```

## 2.2. Segment Tree (ZKW)

```
struct segtree {
      using T = int;
T f(T a, T b) { return a + b; } // any monoid operation
                                                // identity element
       static constexpr T ID = \theta;
       vector<T> v;
       segtree(int n_{-}): n(n_{-}), v(2 * n, ID) {}
       segtree(vector<T> &a): n(a.size()), v(2 * n, ID) {
         copy_n(a.begin(), n, v.begin() + n);
for (int i = n - 1; i > 0; i--)
 9
            v[i] = f(v[i * 2], v[i * 2 + 1]);
11
      void update(int i, T x) {
  for (v[i += n] = x; i /= 2;)
    v[i] = f(v[i * 2], v[i * 2 + 1]);
13
15
17
       T query(int l, int r) {
         T tl = ID, tr = ID;
         for (l += n, r += n; l < r; l /= 2, r /= 2) {
   if (l & 1) tl = f(tl, v[l++]);
19
            if (r \& 1) tr = f(v[--r], tr);
         return f(tl, tr);
25 };
```

## 2.3. Wavelet Matrix

```
#pragma GCC target("popcnt,bmi2")
#include <immintrin.h>

// T is unsigned. You might want to compress values first
template <typename T> struct wavelet_matrix {
    static_assert(is_unsigned_v<T>, "only unsigned T");
struct bit_vector {
```

```
static constexpr uint W = 64;
         uint n, cnt0;
         vector ull> bits;
         vector<uint> sum;
11
         bit_vector(uint n_)
              : n(n_{-}), bits(n / W + 1), sum(n / W + 1) {}
13
         void build() {
           for (uint j = 0; j != n / W; ++j)
  sum[j + 1] = sum[j] + _mm_popcnt_u64(bits[j]);
15
           cnt0 = rank0(n):
17
        void set_bit(uint i) { bits[i / W] |= 1ULL << i % W; }
bool operator[](uint i) const {</pre>
19
           return !!(bits[i / W] & 1ULL << i % W);</pre>
21
         uint rank1(uint i) const {
  return sum[i / W] +
23
                    _mm_popcnt_u64(_bzhi_u64(bits[i / W], i % W));
25
         uint rank0(uint i) const { return i - rank1(i); }
27
      };
29
      vector<bit_vector> b;
      wavelet_matrix(const vector<T> &a) : n(a.size()) {
         lg
33
          _lg(max(*max_element(a.begin(), a.end()), T(1))) + 1;
         b.assign(lg, n);
         vector<T> cur = a, nxt(n);
35
         for (int h = lg; h--;) {
           for (uint i = 0; i < n; ++i)
37
              if (cur[i] & (T(1) << h)) b[h].set_bit(i);</pre>
39
           b[h].build();
           int il = 0, ir = b[h].cnt0;
for (uint i = 0; i < n; ++i)
   nxt[(b[h][i] ? ir : il)++] = cur[i];</pre>
41
43
           swap(cur, nxt);
45
      T operator[](uint i) const {
         for (int h = lg; h--;)
49
           if (b[h][i])
              i += b[h].cnt0 - b[h].rank0(i), res |= T(1) << h;
           else i = b[h].rank0(i);
51
         return res:
53
      // query k-th smallest (0-based) in a[l, r)
55
      T kth(uint l, uint r, uint k) const {
         T res = 0;
         for (int h = lg; h--;) {
  uint tl = b[h].rank0(l), tr = b[h].rank0(r);
57
           if (k >= tr - tl) {
59
              k -= tr - tl;
              l += b[h].cnt0 - tl;
61
              r += b[h].cnt0 - tr;
              res |= T(1) << h;
           } else l = tl, r = tr;
         return res;
      // count of i in [l, r) with a[i] < u</pre>
      uint count(uint l, uint r, T u) const {
  if (u >= T(1) << lg) return r - l;</pre>
        uint res = 0;
for (int h = lg; h--;) {
    uint tl = b[h].rank0(l), tr = b[h].rank0(r);
71
           if (u δ (T(1) << h)) {
             l += b[h].cnt0 - tl;
              r += b[h].cnt0 - tr;
              res += tr - tl;
           } else l = tl, r = tr;
79
         return res;
81
```

# 3. Graph

## 3.1. Strongly Connected Components

```
struct TarjanScc {
   int n, step;
   vector<int> time, low, instk, stk;
   vector<vector<int>> e, scc;
   TarjanScc(int n_)
        : n(n_), step(0), time(n), low(n), instk(n), e(n) {}
   void add_edge(int u, int v) { e[u].push_back(v); }
   void dfs(int x) {
      time[x] = low[x] = ++step;
}
```

```
stk.push_back(x);
        instk[x] = 1;
for (int y : e[x])
11
          if (!time[y]) {
13
            dfs(y);
low[x] = min(low[x], low[y]);
15
          } else if (instk[y]) {
            low[x] = min(low[x], time[y]);
17
19
        if (time[x] == low[x]) {
          scc.emplace_back();
21
          for (int y = -1; y != x;) {
            y = stk.back();
            stk.pop_back();
instk[y] = 0;
23
             scc.back().push_back(y);
25
27
      void solve() {
        for (int i = 0; i < n; i++)
31
          if (!time[i]) dfs(i);
        reverse(scc.begin(), scc.end());
33
   };
```

#### 4. Math

# 4.1. Number Theory

#### 4.1.1. Mod Struct

A list of safe primes: 26003,27767,28319,28979,29243,29759,30467910927547,919012223,947326223,990669467,1007939579,1019126699929760389146037459,975500632317046523,989312547895528379

```
\begin{array}{c|ccccc} \text{NTT prime } p & p-1 & \text{primitive root} \\ 65537 & 1 \ll 16 & 3 \\ 998244353 & 119 \ll 23 & 3 \\ 2748779069441 & 5 \ll 39 & 3 \\ 1945555039024054273 & 27 \ll 56 & 5 \end{array}
```

```
template <typename T> struct M {
  static T MOD; // change to constexpr if already known
 3
       T v;
M(): v(0) {}
       M(T x) {
    v = (-MOD <= x 88 x < MOD) ? x : x % MOD;
 5
          if (v < 0) v += MOD;
 9
       explicit operator T() const { return v; }
       bool operator==(const M &b) const { return v == b.v;
       bool operator!=(const M &b) const { return v != b.v; }
       M operator-() { return M(-v); }
       M operator*(M b) { return M(v + b.v); }
M operator*(M b) { return M(v - b.v); }
M operator*(M b) { return M(v - b.v); }
M operator*(M b) { return M((__int128)v * b.v % MOD); }
M operator/(M b) { return *this * (b ^ (MOD - 2)); }
friend M operator^(M a, ll b) {
13
15
17
          M ans(1);
19
           for (; b; b >>= 1, a *= a)
             if (b & 1) ans *= a;
21
          return ans:
23
       friend M \deltaoperator+=(M \deltaa, M b) { return a = a + b; }
       friend M Soperator-=(M Sa, M b) { return a = a - b; }
friend M Soperator*=(M Sa, M b) { return a = a * b; }
       friend M &operator/=(M &a, M b) { return a = a / b; }
27
    };
    using Mod = M<int>;
    template <> int Mod::MOD = 1'000'000'007;
     int &MOD = Mod::MOD;
```

## 4.1.2. Miller-Rabin

Requires: Mod Struct

```
1  // checks if Mod::MOD is prime
bool is_prime() {
3    if (MOD < 2 || MOD % 2 == 0) return MOD == 2;
    Mod A[] = {2, 7, 61}; // for int values (< 2^31)
5    // ll: 2, 325, 9375, 28178, 450775, 9780504, 1795265022
    int s = __builtin_ctzll(MOD - 1), i;
6    for (Mod a : A) {
        Mod x = a ^ (MOD >> s);
6    for (i = 0; i < s && (x + 1).v > 2; i++) x *= x;
        if (i && x != -1) return 0;
11    }
12    return 1;
13 }
```

## 4.1.3. Extended GCD

```
1  // returns (p, q, g): p * a + q * b == g == gcd(a, b)
  // g is not guaranteed to be positive when a < 0 or b < 0
3  tuple<ll, ll, ll> extgcd(ll a, ll b) {
    ll s = 1, t = 0, u = 0, v = 1;
    while (b) {
        ll q = a / b;
        swap(a -= q * b, b);
        swap(s -= q * t, t);
        swap(u -= q * v, v);
    }
11  return {s, u, a};
}
```

## 4.1.4. Chinese Remainder Theorem

# 4.2. Combinatorics

#### 4.2.1. Matroid Intersection

This template assumes 2 weighted matroids of the same type, and that removing an element is much more expensive than checking if one can be added. Remember to change the implementation details.

The ground set is  $0, 1, \ldots, n-1$ , where element i has weight w[i]. For the unweighted version, remove weights and change BF/SPFA to BFS. 11

```
constexpr int N = 100;
   constexpr int INF = 1e9;
   struct Matroid {
                              // represents an independent set
      Matroid(bitset<N>); // initialize from an independent set
      bool can_add(int);
                             // if adding will break independence
      Matroid remove(int); // removing from the set
   auto matroid_intersection(int n, const vector<int> &w) {
      bitset<N> S;
11
      for (int sz = 1; sz <= n; sz++) {</pre>
        Matroid M1(S), M2(S);
13
        vector<vector<pii>>> e(n + 2);
        for (int j = 0; j < n; j++)
          if (!S[j]) {
             if (M1.can_add(j)) e[n].emplace_back(j, -w[j]);
19
             if (M2.can_add(j)) e[j].emplace_back(n + 1, 0);
        for (int i = 0; i < n; i++)
21
          if (S[i]) {
             Matroid T1 = M1.remove(i), T2 = M2.remove(i);
23
             for (int j = 0; j < n; j++)</pre>
               if (!S[j]) {
                 if (T1.can_add(j)) e[i].emplace_back(j, -w[j]);
27
                 if (T2.can_add(j)) e[j].emplace_back(i, w[i]);
29
        vector<pii> dis(n + 2, {INF, 0});
        vector<int> prev(n + 2, -1);
        dis[n] = \{0, 0\};
        // change to SPFA for more speed, if necessary
        bool upd = 1;
        while (upd) {
          upu - v,
for (int u = 0; u < n + 2; u++)
for (auto [v, c] : e[u]) {
   pii x(dis[u].first + c, dis[u].second + 1);
   if (x < dis[v]) dis[v] = x, prev[v] = u, upd = 1;
}</pre>
39
41
        }
43
        if (dis[n + 1].first < INF)</pre>
45
          for (int x = prev[n + 1]; x != n; x = prev[x])
            S.flip(x);
        else break;
49
        // S is the max-weighted independent set with size sz
51
      }
      return S;
53 }
```

# 5. Numeric

#### 5.1. Fast Fourier Transform

```
template <typename T>
    void fft_(int n, vector<T> &a, vector<T> &rt, bool inv) {
       vector<int> br(n);
       for (int i = 1; i < n; i++) {
  br[i] = (i & 1) ? br[i - 1] + n / 2 : br[i / 2] / 2;
 5
           if (br[i] > i) swap(a[i], a[br[i]]);
 7
       for (int len = 2; len <= n; len *= 2)</pre>
           for (int i = 0; i < n; i += len)</pre>
             for (int j = 0; j < len / 2; j++) {
   int pos = n / len * (inv ? len - j : j);
   T u = a[i + j], v = a[i + j + len / 2] * rt[pos];
   a[i + j] = u + v, a[i + j + len / 2] = u - v;</pre>
11
13
       if (T minv = T(1) / T(n); inv)
15
          for (T \delta x : a) x *= minv;
17 }
```

Requires: Mod Struct

```
void ntt(vector<Mod> &a, bool inv, Mod primitive_root) {
    int n = a.size();

    Mod root = primitive_root ^ (MOD - 1) / n;
    vector<Mod> rt(n + 1, 1);
    for (int i = 0; i < n; i++) rt[i + 1] = rt[i] * root;
    fft_(n, a, rt, inv);

}
void fft(vector<complex<double>> &a, bool inv) {
    int n = a.size();
    vector<complex<double>> rt(n + 1);
    double arg = acos(-1) * 2 / n;
    for (int i = 0; i <= n; i++)
        rt[i] = {cos(arg * i), sin(arg * i)};

fft_(n, a, rt, inv);
}</pre>
```

### 5.2. Fast Walsh-Hadamard Transform

Requires: Mod Struct

```
void fwht(vector<Mod> &a, bool inv) {
    int n = a.size();

    for (int d = 1; d < n; d <<= 1)
        for (int m = 0; m < n; m++)
        if (!(m & d)) {
            inv ? a[m] -= a[m | d] : a[m] += a[m | d]; // AND
            inv ? a[m | d] -= a[m] : a[m | d] += a[m]; // OR
            Mod x = a[m], y = a[m | d]; // XOR
            a[m] = x + y, a[m | d] = x - y; // XOR
        }

if (Mod iv = Mod(1) / n; inv) // XOR
        for (Mod &i : a) i *= iv; // XOR
}</pre>
```

## 6. Geometry

## 6.1. Point

```
1 template <typename T> struct P {
       T \times y;
P(T \times y = 0, T y = 0) : x(x), y(y) {}
 3
       bool operator<(const P &p) const
          return tie(x, y) < tie(p.x, p.y);</pre>
       bool operator==(const P &p) const {
          return tie(x, y) == tie(p.x, p.y);
 9
       P operator-() const { return {-x, -y}; }
       P operator+(P p) const { return {x + p.x, y + p.y}; }
P operator-(P p) const { return {x - p.x, y - p.y}; }
P operator+(T d) const { return {x + d, y + d}; }
P operator/(T d) const { return {x + d, y + d}; }
P operator/(T d) const { return {x / d, y / d}; }
11
13
       T dist2() const { return x * x + y * y;
15
       double len() const { return sqrt(dist2()); }
       P unit() const { return *this / len(); }
friend T dot(P a, P b) { return a.x * b.x + a.y * b.y; }
17
       friend T cross(P a, P b) { return a.x * b.y - a.y * b.x; }
19
       friend T cross(P a, P b, P o) {
          return cross(a - o, b - o);
23 };
    using pt = P<ll>;
```

#### 6.1.1. Quarternion

```
constexpr double PI = 3.141592653589793;
constexpr double EPS = 1e-7;
    struct Q {
      using T = double;
      T x, y, z, r; Q(T r = \theta) : x(\theta), y(\theta), z(\theta), r(r) {} Q(T x, T y, T z, T r = \theta) : x(x), y(y), z(z), r(r) {} friend bool operator==(const Q &a, const Q &b) {
 9
         return (a - b).abs2() <= EPS;</pre>
11
      friend bool operator!=(const Q &a, const Q &b) {
         return !(a == b);
13
      Q operator-() { return Q(-x, -y, -z, -r); } Q operator+(const Q &b) const {
15
         return Q(x + b.x, y + b.y, z + b.z, r + b.r);
17
      Q operator-(const Q &b) const {
         return Q(x - b.x, y - b.y, z - b.z, r - b.r);
19
      Q operator*(const T &t) const {
21
         return Q(x * t, y * t, z * t, r * t);
23
      Q operator*(const Q &b) const {
         25
27
                    r * b.z + x * b.y - y * b.x + z * b.r
                    r * b.r - x * b.x - y * b.y - z * b.z);
29
       Q operator/(const Q &b) const { return *this * b.inv(); }
31
       T abs2() const { return r * r + x * x + y * y + z * z; }
      T len() const { return sqrt(abs2()); }
      Q conj() const { return Q(-x, -y, -z, r); } Q unit() const { return *this * (1.0 / len()); } Q inv() const { return conj() * (1.0 / abs2()); } friend T dot(Q a, Q b) {
35
         return a.x * b.x + a.y * b.y + a.z * b.z;
37
39
       friend Q cross(Q a, Q b) {
         return Q(a.y * b.z - a.z * b.y, a.z * b.x - a.x * b.z,
a.x * b.y - a.y * b.x);
41
      friend Q rotation_around(Q axis, T angle) {
  return axis.unit() * sin(angle / 2) + cos(angle / 2);
43
45
       Q rotated_around(Q axis, T angle) {
47
         Q u = rotation_around(axis, angle);
         return u * *this / u;
49
       friend Q rotation between(Q a, Q b) {
         a = a.unit(), b = b.unit();
if (a == -b) {
51
53
           // degenerate case
           Q ortho = abs(a.y) > EPS ? cross(a, Q(1, 0, 0))
55
                                            : cross(a, Q(0, 1, 0));
           return rotation_around(ortho, PI);
57
         return (a * (a + b)).conj();
59
```