CITY UNIVERSITY OF HONG KONG

Department of Management Sciences

Module code & title: GE2262 Business Statistics

Session : Examination (Semester B, 2021-2022)

Time allowed : 9:30–11:50 am (2 hours for the examination, 20 minutes for file submission)

This paper has *EIGHT* pages (including this cover page, and three pages of Formulae and statistical tables).

Instructions to students:

1. This paper consists of FOUR questions.

- 2. Answer ALL questions.
- 3. For each question, show sufficient working.
- 4. Display all non-integer numeric values to 3 decimal places unless specified.
- 5. Formulae and statistical tables are provided at the end of this paper.
- 6. Write your answers on paper, take photo for each page of your answer script, combine them together to one pdf file and upload the pdf file to CANVAS before May 5, 11:50 am. Please name your file using your student ID and course code (eg 5******_GE2262.pdf) and remember to write your SID on the answer script.

This is an open-book examination. Students can refer to the teaching materials of this course provided in CANVAS during the examination.

Materials, aids and instruments permitted to be used during examination:

Only university approved calculator is permitted. Computer software such as Excel is not permitted.

Materials other than those stated above are not permitted. Candidates will be subject to disciplinary action if any unauthorized materials or aids are found on them.

Academic honesty pledge

"I pledge that the answers in this test/examination are my own and that I will not seek or obtain an unfair advantage in producing these answers. Specifically,

- ❖ I will not plagiarize (copy without citation) from any source;
- ❖ I will not communicate or attempt to communicate with any other person during the test/examination; neither will I give or attempt to give assistance to another student taking the test/examination; and
- ❖ I will use only approved devices (e.g., calculators) and/or approved device models.
- ❖ I understand that any act of academic dishonesty can lead to disciplinary action."

Please reaffirm the honesty pledge by writing "I pledge to follow the Rules on Academic Honesty and understand that violations may lead to severe penalties" onto the first test/examination answer sheet.

GE2262 Business Statistics Formula Sheet & Statistical Tables

Formula Sheet

1.
$$\mu = \frac{1}{N} \sum X_i ; \qquad \sigma^2 = \frac{1}{N} \sum (X_i - \mu)^2$$
$$\overline{X} = \frac{1}{n} \sum X_i ; \qquad s^2 = \frac{1}{n-1} \sum (X_i - \overline{X})^2$$

2.
$$P(A \text{ or } B) = P(A) + P(B) - P(A \text{ and } B)$$
;
 $P(A \text{ and } B) = P(A \mid B)P(B)$; $P(A \mid B) = \frac{P(A \text{ and } B)}{P(B)}$

3a.
$$\mu = E(X) = \sum X_i P(X_i)$$
; $\sigma^2 = Var(X) = \sum (X_i - \mu)^2 P(X_i)$

3b. If
$$X \sim Bin(n, p)$$
, then (a) $P(X = k) = \frac{n!}{k!(n-k)!} p^k (1-p)^{n-k}$

(b)
$$\mu = E(X) = np$$
; $Var(X) = np(1-p)$

3c. If
$$X \sim N(\mu, \sigma^2)$$
, then $Z = \frac{X - \mu}{\sigma} \sim N(0, 1^2)$

4. If
$$\overline{X} \sim N(\mu, (\frac{\sigma}{\sqrt{n}})^2)$$
, then $Z = \frac{\overline{X} - \mu}{\frac{\sigma}{\sqrt{n}}} \sim N(0, 1^2)$

5.
$$\overline{X} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$$
; $\overline{X} \pm t_{\frac{\alpha}{2}, n-1} \frac{s}{\sqrt{n}}$; $E = z_{\alpha/2} \frac{\sigma}{\sqrt{n}}$

6.
$$Z = \frac{\overline{X} - \mu}{\frac{\sigma}{\sqrt{n}}} ; \qquad t = \frac{\overline{X} - \mu}{\frac{s}{\sqrt{n}}}$$

7. If
$$\hat{p} \sim N(p, \frac{p(1-p)}{n})$$
, then $Z = \frac{\hat{p}-p}{\sqrt{\frac{p(1-p)}{n}}} \sim N(0,1^2)$;

$$\hat{p} \pm z_{\alpha/2} \sqrt{\frac{\hat{p}(1-\hat{p})}{n}} \; ; \; E = z_{\alpha/2} \sqrt{\frac{p(1-p)}{n}}$$

8.
$$S_{XY} = \frac{\sum_{i=1}^{n} (X_{i} - \overline{X})(Y_{i} - \overline{Y})}{n-1}; S_{X} = \sqrt{\frac{\sum_{i=1}^{n} (X_{i} - \overline{X})^{2}}{n-1}}; S_{Y} = \sqrt{\frac{\sum_{i=1}^{n} (Y_{i} - \overline{Y})^{2}}{n-1}}; r_{XY} = \frac{S_{XY}}{S_{X}S_{Y}}; R^{2} = 1 - \frac{SSE}{SST}$$
For $Y = \beta_{0} + \beta_{1}X + \varepsilon$, $b_{1} = \frac{\sum_{i=1}^{n} (X_{i} - \overline{X})(Y_{i} - \overline{Y})}{\sum_{i=1}^{n} (X_{i} - \overline{X})^{2}}; b_{0} = \overline{Y} - b_{1}\overline{X}$ $b_{1} \pm t_{\frac{\alpha}{2}, n-2}S_{b_{1}}$

The Cumulative Standardized Normal Distribution



zed Normal Distribution	r the cumulative standardized normal	

Z	0.00	0.01	0.02	0.03	0.0	0.05	90.0	0.07	0.08	60.0
9.0	0.000000001	01								
-5.5	0.000000019	19								
-5.0	0.000000287	87								
4.5	0.000003398	86								
4.0	0.000031671	71								
9.6	0.00005	0.00005	0.00004	0.00004	0.00004	0.00004	0.00004	0.00004	0.00003	0.00003
-3.8	0.00007	0.00007	0.00007	0.00006	0.0000	0.00000	0.00006	0.00005	0.00005	0.00005
-3.7	0.00011	0.00010	0.00010	0.00010	0.0000	0.0000	0.00008	0.00008	0.00008	0.00008
-3.6	0.00016	0.00015	0.00015	0.00014	0.00014	0.00013	0.00013	0.00012	0.00012	0.00011
-3.5	0.00023	0.00022	0.00022	0.00021	0.00020	0.00019	0.00019	0.00018	0.00017	0.00017
-3.4	0.00034	0.00032	0.00031	0.00030	0.00029	0.00028	0.00027	0.00026	0.00025	0.00024
-3.3	0.00048	0.00047	0.00045	0.00043	0.00042	0.00040	0.00039	0.00038	0.00036	0.00035
-3.2	0.00069	0.00066	0.00064	0.00062	09000.0	0.00058	0.00056	0.00054	0.00052	0.00050
-3.1	0.00097	0.00094	0.00000	0.00087	0.00084	0.00082	0.00079	0.00076	0.00074	0.00071
-3.0	0.00135	0.00131	0.00126	0.00122	0.00118	0.00114	0.00111	0.00107	0.00103	0.00100
-2.9	0.0019	0.0018	0.0018	0.0017	0.0016	0.0016	0.0015	0.0015	0.0014	0.0014
-2.8	0.0026	0.0025	0.0024	0.0023	0.0023	0.0022	0.0021	0.0021	0.0020	0.0019
-2.7	0.0035	0.0034	0.0033	0.0032	0.0031	0.0030	0.0029	0.0028	0.0027	0.0026
-2.6	0.0047	0.0045	0.0044	0.0043	0.0041	0.0040	0.0039	0.0038	0.0037	0.0036
-2.5	0.0062	0.0060	0.0059	0.0057	0.0055	0.0054	0.0052	0.0051	0.0049	0.0048
-2.4	0.0082	0.0080	0.0078	0.0075	0.0073	0.0071	0.0069	0.0068	0.0066	0.0064
-2.3	0.0107	0.0104	0.0102	0.0099	9600.0	0.0094	0.0091	0.0089	0.0087	0.0084
-2.2	0.0139	0.0136	0.0132	0.0129	0.0125	0.0122	0.0119	0.0116	0.0113	0.0110
-2.1	0.0179	0.0174	0.0170	0.0166	0.0162	0.0158	0.0154	0.0150	0.0146	0.0143
-2.0	0.0228	0.0222	0.0217	0.0212	0.0207	0.0202	0.0197	0.0192	0.0188	0.0183
-1.9	0.0287	0.0281	0.0274	0.0268	0.0262	0.0256	0.0250	0.0244	0.0239	0.0233
-1.8	0.0359	0.0351	0.0344	0.0336	0.0329	0.0322	0.0314	0.0307	0.0301	0.0294
-1.7	0.0446	0.0436	0.0427	0.0418	0.0409	0.0401	0.0392	0.0384	0.0375	0.0367
-1.6	0.0548	0.0537	0.0526	0.0516	0.0505	0.0495	0.0485	0.0475	0.0465	0.0455
-1.5	0.0668	0.0655	0.0643	0.0630	0.0618	9090.0	0.0594	0.0582	0.0571	0.0559
4.1-	0.0808	0.0793	0.0778	0.0764	0.0749	0.0735	0.0721	0.0708	0.0694	0.0681
1 .3	0.0968	0.0951	0.0934	0.0918	0.0901	0.0885	0.0869	0.0853	0.0838	0.0823
-1.2	0.1151	0.1131	0.1112	0.1093	0.1075	0.1056	0.1038	0.1020	0.1003	0.0985
1.1	0.1357	0.1335	0.1314	0.1292	0.1271	0.1251	0.1230	0.1210	0.1190	0.1170
-1.0	0.1587	0.1562	0.1539	0.1515	0.1492	0.1469	0.1446	0.1423	0.1401	0.1379
6.0	0.1841	0.1814	0.1788	0.1762	0.1736	0.1711	0.1685	0.1660	0.1635	0.1611
9.0	0.2119	0.2090	0.2061	0.2033	0.2005	0.1977	0.1949	0.1922	0.1894	0.1867
-0.7	0.2420	0.2388	0.2358	0.2327	0.2296	0.2266	0.2236	0.2206	0.2177	0.2148
9.0-	0.2743	0.2709	0.2676	0.2643	0.2611	0.2578	0.2546	0.2514	0.2482	0.2451
-0.5	0.3085	0.3050	0.3015	0.2981	0.2946	0.2912	0.2877	0.2843	0.2810	0.2776
-0.4 4	0.3446	0.3409	0.3372	0.3336	0.3300	0.3264	0.3228	0.3192	0.3156	0.3121
-0.3	0.3821	0.3783	0.3745	0.3707	0.3669	0.3632	0.3594	0.3557	0.3520	0.3483
-0.2	0.4207	0.4168	0.4129	0.4090	0.4052	0.4013	0.3974	0.3936	0.3897	0.3859
-0.1	0.4602	0.4562	0.4522	0.4483	0.4443	0.4404	0.4364	0.4325	0.4286	0.4247
0.0	0.5000	0.4960	0.4920	0.4880	0.4840	0.4801	0.4761	0.4721	0.4681	0.4641
										continued



The Cumulative Standardized Normal Distribution (Continued) Entry represents area under the cumulative standardized normal distribution from --- to Z

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Z	0.00	0.01	0.02	0.03	0.04	0.05	90.0	0.07	0.08	60.0	
0.0	0.5000	0.5040	0.5080	0.5120	0.5160	0.5199	0.5239	0.5279	0.5319	0.5359	
0.1	0.5398	0.5438	0.5478	0.5517	0.5557	0.5596	0.5636	0.5675	0.5714	0.5753	
0.2	0.5793	0.5832	0.5871	0.5910	0.5948	0.5987	0.6026	0.6064	0.6103	0.6141	
0.3	0.6179	0.6217	0.6255	0.6293	0.6331	0.6368	0.6406	0.6443	0.6480	0.6517	
4.0	0.6554	0.6591	0.6628	0.6664	0.6700	0.6736	0.6772	0.6808	0.6844	0.6879	
0.5	0.6915	0.6950	0.6985	0.7019	0.7054	0.7088	0.7123	0.7157	0.7190	0.7224	
9.0	0.7257	0.7291	0.7324	0.7357	0.7389	0.7422	0.7454	0.7486	0.7518	0.7549	
0.7	0.7580	0.7612	0.7642	0.7673	0.7704	0.7734	0.7764	0.7794	0.7823	0.7852	
8.0	0.7881	0.7910	0.7939	0.7967	0.7995	0.8023	0.8051	0.8078	0.8106	0.8133	
6.0	0.8159	0.8186	0.8212	0.8238	0.8264	0.8289	0.8315	0.8340	0.8365	0.8389	
1.0	0.8413	0.8438	0.8461	0.8485	0.8508	0.8531	0.8554	0.8577	0.8599	0.8621	
1.1	0.8643	0.8665	0.8686	0.8708	0.8729	0.8749	0.8770	0.8790	0.8810	0.8830	
1.2	0.8849	0.8869	0.8888	0.8907	0.8925	0.8944	0.8962	0.8980	0.8997	0.9015	
1.3	0.9032	0.9049	9906.0	0.9082	0.9099	0.9115	0.9131	0.9147	0.9162	0.9177	
4.	0.9192	0.9207	0.9222	0.9236	0.9251	0.9265	0.9279	0.9292	0.9306	0.9319	
1.5	0.9332	0.9345	0.9357	0.9370	0.9382	0.9394	0.9406	0.9418	0.9429	0.9441	
1.6	0.9452	0.9463	0.9474	0.9484	0.9495	0.9505	0.9515	0.9525	0.9535	0.9545	
1.7	0.9554	0.9564	0.9573	0.9582	0.9591	0.9599	0.9608	0.9616	0.9625	0.9633	
6 .	0.9641	0.9649	0.9656	0.9664	0.9671	0.9678	0.9686	0.9693	0.9699	90.60	
1.9	0.9713	0.9719	0.9726	0.9732	0.9738	0.9744	0.9750	0.9756	0.9761	0.9767	
2.0	0.9772	0.9778	0.9783	0.9788	0.9793	0.9798	0.9803	0.9808	0.9812	0.9817	
2.1	0.9821	0.9826	0.9830	0.9834	0.9838	0.9842	0.9846	0.9850	0.9854	0.9857	
2.2	0.9861	0.9864	0.9868	0.9871	0.9875	0.9878	0.9881	0.9884	0.9887	0.9890	
2.3	0.9893	9686.0	0.9898	0.9901	0.9904	0.9906	0.9909	0.9911	0.9913	0.9916	
2.4	0.9918	0.9920	0.9922	0.9925	0.9927	0.9929	0.9931	0.9932	0.9934	0.9936	
2.5	0.9938	0.9940	0.9941	0.9943	0.9945	0.9946	0.9948	0.9949	0.9951	0.9952	
5.6	0.9953	0.9955	0.9956	0.9957	0.9959	0.9960	0.9961	0.9962	0.9963	0.9964	
2.7	0.9965	9966.0	0.9967	0.9968	0.9969	0.9970	0.9971	0.9972	0.9973	0.9974	
2.8	0.9974	0.9975	0.9976	0.9977	0.9977	0.9978	0.9979	0.9979	0.9980	0.9981	
5.9	0.9981	0.9982	0.9982	0.9983	0.9984	0.9984	0.9985	0.9985	0.9986	0.9986	
3.0	0.99865	0.99869	0.99874	0.99878	0.99882	0.99886	0.99889	0.99893	0.99897	0.99900	
3.1	0.99903	90666.0	0.99910	0.99913	0.99916	0.99918	0.99921	0.99924	0.99926	0.99929	
3.2	0.99931	0.99934	0.99936	0.99938	0.99940	0.99942	0.99944	0.99946	0.99948	0.99950	
3.3	0.99952	0.99953	0.99955	0.99957	0.99958	0.99960	0.99961	0.99962	0.99964	0.99965	
3.4	0.99966	0.99968	0.99969	0.99970	0.99971	0.99972	0.99973	0.99974	0.99975	92666.0	
3.5	0.99977	0.99978	0.99978	0.99979	0.99980	0.99981	0.99981	0.99982	0.99983	0.99983	
3.6	0.99984	0.99985	0.99985	0.99986	0.99986	0.99987	0.99987	0.99988	0.99988	0.99989	
3.7	0.99989	0.99990	0.99990	0.99990	0.99991	0.99991	0.99992	0.99992	0.99992	0.99992	
3.8	0.99993	0.99993	0.99993	0.99994	0.99994	0.99994	0.99994	0.99995	0.99995	0.99995	
3.9	0.99995	0.99995	0.99996	0.99996	0.99996	0.99996	0.99996	96666.0	0.99997	0.99997	
4.0	0.999968329	329									
4.5	0.999996602	302									

Critical Values of t

			Upper-Tail Areas	se		
Degrees of Freedom	0.25	0.10	0.05	0.025	0.01	0.005
49	0.6795	1.2991	1.6766	2.0096	2.4049	2.6800
20	0.6794	1.2987	1.6759	2.0086	2.4033	2.6778
51	0.6793	1.2984	1.6753	2.0076	2.4017	2.6757
52	0.6792	1.2980	1.6747	2.0066	2.4002	2.6737
53	0.6791	1.2977	1.6741	2.0057	2.3988	2.6718
54	0.6791	1.2974	1.6736	2.0049	2.3974	2.6700
55	0.6790	1.2971	1.6730	2.0040	2.3961	2.6682
26	0.6789	1.2969	1.6725	2.0032	2.3948	2.6665
22	0.6788	1.2966	1.6720	2.0025	2.3936	2.6649
28	0.6787	1.2963	1.6716	2.0017	2.3924	2.6633
59	0.6787	1.2961	1.6711	2.0010	2.3912	2.6618
90	0.6786	1.2958	1.6706	2.0003	2.3901	2.6603
61	0.6785	1.2956	1.6702	1.9996	2.3890	2.6589
62	0.6785	1.2954	1.6698	1.9990	2.3880	2.6575
63	0.6784	1.2951	1.6694	1.9983	2.3870	2.6561
64	0.6783	1.2949	1.6690	1.9977	2.3860	2.6549
60	0.6783	1.2947	1.6686	1.9971	2.3851	2.6536
90	0.6782	1.2945	1.6683	1.9966	2.3842	2.6524
/0	0.0707	1 2043	1.007.9	1.9960	2.000.0	2.0312
00	0.0701	1.2941	1.0070	1.9933	2.3024	2.6301
69	0.6780	1 2028	1,6660	1.9949	2.2010	26470
2 7	0.0780	1 2036	1,6666	1 0030	2.3800	2,6469
- 6	0.6770	1 2024	1.0000	1.9939	2.3000	2.0469
73	0.6779	1.2934	1,6660	1.9933	2.3785	2,6440
2 7	0.0778	1 2031	1,6657	1,000	2,3778	26439
75	0.6778	1.2929	1.6654	1.9921	2.3771	2.6430
26	0.6777	1 2928	1 6652	1 9917	2 3764	2 6421
24	0.6777	1.2926	1.6649	1.9913	2.3758	2.6412
78	0.6776	1.2925	1.6646	1.9908	2.3751	2.6403
79	0.6776	1.2924	1.6644	1.9905	2.3745	2.6395
80	9/19/0	1.2922	1.6641	1.9901	2.3739	2.6387
81	0.6775	1.2921	1.6639	1.9897	2.3733	2.6379
82	0.6775	1.2920	1.6636	1.9893	2.3727	2.6371
83	0.6775	1.2918	1.6634	1.9890	2.3721	2.6364
84	0.6774	1.2917	1.6632	1.9886	2.3716	2.6356
82	0.6774	1.2916	1.6630	1.9883	2.3710	2.6349
98	0.6774	1.2915	1.6628	1.9879	2.3705	2.6342
87	0.6773	1.2914	1.6626	1.9876	2.3700	2.6335
8 8	0.6773	1.2912	1.6624	1.98/3	2.3695	2.6329
60	0.6773	1 2911	1.6620	1 9867	2.3690	2.0322
9 6	0.6772	1 2909	1 6618	1 9864	2.3680	2 6309
92	0.6772	1.2908	1.6616	1.9861	2.3676	2.6303
93	0.6771	1.2907	1.6614	1.9858	2.3671	2.6297
94	0.6771	1.2906	1.6612	1.9855	2.3667	2.6291
92	0.6771	1.2905	1.6611	1.9853	2.3662	2.6286
96	0.6771	1.2904	1.6609	1.9850	2.3658	2.6280
97	0.6770	1.2903	1.6607	1.9847	2.3654	2.6275
88.0	0.6770	1.2902	1.6606	1.9845	2.3650	2.6269
99	0.6770	1.2902	1.6604	1.9842	2.3646	2.6264
1,00	0.6767	1 2893	1,6588	1 9818	2.3642	2,0239
120	0.6765	1 2886	1 6577	1 9799	2.3578	2,0213
8	0.6745	1.2816	1.6449	1.9600	2.3263	2.5758
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Degrees of			Upper-Tall Areas	as		
Freedom	0.25	0.10	0.05	0.025	0.01	0.005
- 0	1.0000	3.0777	6.3138	12.7062	31.8207	63.6574
V 6	0.8165	1.8850	2.9200	4.3027	0.9040	9.9248
0 4	0.7407	1 5332	2 1318	2 7764	3 7469	4 6041
2	0.7267	1.4759	2.0150	2.5706	3.3649	4.0322
9 9	0.7176	1.4398	1.9432	2.4469	3.1427	3.7074
7	0.7111	1.4149	1.8946	2.3646	2.9980	3.4995
8	0.7064	1.3968	1.8595	2.3060	2.8965	3.3554
6	0.7027	1.3830	1.8331	2.2622	2.8214	3.2498
10	0.6998	1.3722	1.8125	2.2281	2.7638	3.1693
Ξ:	0.6974	1.3634	1.7959	2.2010	2.7181	3.1058
7	0.6955	1.3562	1.7823	2.1788	2.6810	3.0545
20 5	0.6938	1.3502	1.7709	2.1604	2.6503	3.0123
<u>4</u> π	0.6924	13450	1 7531	2 1315	2,6245	2 0467
2 4	0.6912	1 3368	1 7450	2 1100	2.6023	2 0208
2 1	0.6892	1.3334	1 7396	2 1098	2.5669	
- 00	0.6884	1.3304	1.7341	2.1009	2.5524	2.8784
19	0.6876	1.3277	1.7291	2.0930	2.5395	
20	0.6870	1.3253	1.7247	2.0860	2.5280	2.8453
21	0.6864	1.3232	1.7207	2.0796	2.5177	2.8314
22	0.6858	1.3212	1.7171	2.0739	2.5083	2.8188
5 23	0.6853	1.3195	1.7139	2.0687	2.4999	2.8073
24	0.6848	1.31/8	1.7109	2.0639	2.4922	2.7969
0 0	0.0044	1.3163	1.7051	2.0595	2.4651	2.707
27	0.6840	1.3150	1.7033	2.0555	2.4786	2 7707
280	0.6834	13125	1 7011	2.0310	2 4671	2 7633
29	0.6830	1.3114	1,6991	2.0452	2.4620	2.7564
30	0.6828	1.3104	1.6973	2.0423	2.4573	2.7500
31	0.6825	1.3095	1.6955	2.0395	2.4528	2.7440
32	0.6822	1.3086	1.6939	2.0369	2.4487	2.7385
33	0.6820	1.3077	1.6924	2.0345	2.4448	2.7333
34	0.6818	1.3070	1.6909	2.0322	2.4411	2.7284
35	0.6816	1.3062	1.6896	2.0301	2.4377	2.7238
36	0.6814	1.3055	1.6883	2.0281	2.4345	2.7195
37	0.6812	1.3049	1.6871	2.0262	2.4314	2.7154
38	0.6810	1.3042	1.6860	2.0244	2.4286	2.7116
39	0.6808	1.3036	1.6849	2.0227	2.4258	2.7079
0 ;	0.6807	1.3031	1.6839	2.0211	2.4233	2.7045
- 4	0.0803	1.3025	1.0829	2.0195	2.4208	2.7012
7 4 7	0.6804	1.3020	1.6820	2.0161	2.4163	2 6951
2 4	0.6801	13011	1 6802	2 0154	24141	2 6923
45	0.6800	1.3006	1.6794	2.0141	2.4121	2.6896
46	0.6799	1.3002	1.6787	2.0129	2 4 102	2 6870
11					12.1.1	0.00.4
4/	0.6797	1.2998	1.6779	2.0117	2.4083	2.6846

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