

AniMove general R Reference Card

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Getting help

`help(topic)` documentation on `topic`
`?topic` short alternative to `help`
`help.search("topic")` search the help system
`apropos("topic")` the names of all objects in the search list matching the regular expression "topic"
`help.start()` start the HTML version of help
`methods(a)` e.g. `methods(summary)` gives all summary commands

Information about your data

`str(a)` display the internal structure of an R object
`summary(a)` gives a "summary" of `a`, usually a statistical summary but it is *generic* meaning it has different operations for different classes of `a`
`ls()` show objects in the search path; specify `pat="pat"` to search on a pattern
`dir()` show files in the current directory

Input and output

`source("script.R")` includes and executes `script.R` in this place
`read.table(f)` reads a file in table format and creates a data frame from it; the default separator `sep=""` is any whitespace; use `header=TRUE` to read the first line as a header of column names; use `as.is=TRUE` to prevent character vectors from being converted to factors; use `comment.char=""` to prevent "#" from being interpreted as a comment; use `skip=n` to skip `n` lines before reading data; see the help for options on row naming, NA treatment, and others
`read.csv(f,header=TRUE)` id. but with defaults set for reading comma-delimited files
`print(a, ...)` prints its arguments; generic, meaning it can have different methods for different objects
`write.table(x, file=f,row.names=TRUE, col.names=TRUE, sep=" ")` prints `x` after converting to a data frame; if `quote` is `TRUE`, character or factor columns are surrounded by quotes ("); `sep` is the field separator; `eol` is the end-of-line separator; `na` is the string for missing values; use `col.names=NA` to add a blank column header to get the column headers aligned correctly for spreadsheet input
`data(f)` loads specified data sets

For database interaction, see packages `RODBC`, `DBI`, `RMySQL`, `RPgSQL`, `ROracle`, for other file formats see `XML`, `hdf5`, `netCDF`

Data creation & removal

`c(...)` generic function to combine arguments with the default forming a vector; with `recursive=TRUE` descends through lists combining all elements into one vector
`from:to` generates a sequence; ":" has operator priority; `1:4 + 1` returns `2 3 4 5`
`seq(from,to)` generates a sequence `by=` specifies increment; `length=` specifies desired length
`seq(along=x)` generates `1, 2, ..., length(along)`; useful for for loops
`rep(x,times)` replicate `x` `times`; use `each=` to repeat "each" element of `x` `each` times; `rep(c(1,2,3),2)` is `1 2 3 1 2 3`; `rep(c(1,2,3),each=2)` is `1 1 2 2 3 3`
`data.frame(...)` create a data frame of the named or unnamed arguments; `data.frame(v=1:4,ch=c("a","B","c","d"),n=10)`; shorter vectors are recycled to the length of the longest
`list(...)` create a list of the named or unnamed arguments; `list(a=c(1,2),b="hi",c=3i)`;
`array(x,dim=)` array with data `x`; specify dimensions like `dim=c(3,4,2)`; elements of `x` recycle if `x` is not long enough
`matrix(x,nrow=,ncol=)` matrix; elements of `x` recycle
`factor(x,levels=)` encodes a vector `x` as a factor
`expand.grid()` a data frame from all combinations of the supplied vectors or factors
`cbind(df1, df2), rbind(df1,df2)` combine arguments by columns (rows) for data frames and the like
`rm(obj)` removes object
`rm(list = ls(all = TRUE))` removes all objects

Indexing your data

addressing vectors

<code>v[n]</code>	n^{th} element
<code>v[-n]</code>	all <i>but</i> the n^{th} element
<code>v[1:n]</code>	first <code>n</code> elements
<code>v[-(1:n)]</code>	elements from <code>n+1</code> to the end
<code>v[c(1,4,2)]</code>	specific elements
<code>v["name"]</code>	element named "name"
<code>v[x > 3]</code>	all elements greater than 3
<code>v[x > 3 & x < 5]</code>	all elements between 3 and 5
<code>v[x %in% c("a","and","the")]</code>	elements in the given set

addressing lists

<code>x[n]</code>	list with elements <code>n</code>
<code>x[[n]]</code>	n^{th} element of the list
<code>x[["name"]]</code>	element of the list named "name"
<code>x\$name</code>	id.

addressing matrices

<code>x[i,j]</code>	element at row <code>i</code> , column <code>j</code>
<code>x[i,]</code>	row <code>i</code>
<code>x[,j]</code>	column <code>j</code>
<code>x[,c(1,3)]</code>	columns 1 and 3
<code>x["name",]</code>	row named "name"

addressing data frames

similar functions as in the matrix indexing plus:

<code>df[["name"]]</code>	column named "name"
<code>df\$name</code>	column named "name"
<code>df[, "name"]</code>	column named "name"

Variable information

`is.na(x)`, `is.null(x)`, `is.array(x)`, `is.data.frame(x)`,
`is.numeric(x)`, `is.complex(x)`, `is.character(x)`, ...
test for type; for a complete list, use `methods(is)`
`length(x)` number of elements in `x`
`dim(x)` Retrieve or set the dimension of an object; `dim(x) <- c(3,2)`
`dimnames(x)` Retrieve or set the dimension names of an object
`nrow(x)` number of rows; `NROW(x)` is the same but treats a vector as a one-row matrix
`ncol(x)` and `NCOL(x)` id. for columns
`class(x)` get or set the class of `x`; `class(x) <- "myclass"`
`unclass(x)` remove the class attribute of `x`
`attr(x,which)` get or set the attribute `which` of `x`
`attributes(obj)` get or set the list of attributes of `obj`

Data selection and manipulation

`which.max(v)`, `which.min(v)` returns the index of the maximum (minimum) element of `v`

rev(v) reverses the elements of **v**
sort(v) sorts the elements of **v** in increasing order; to sort in decreasing order: **rev(sort(x))**
cut(x,breaks) divides **x** into intervals (factors); **breaks** is the number of cut intervals or a vector of cut points
match(x, y) returns a vector of the same length than **x** with the elements of **x** which are in **y** (**NA** otherwise)
which(x == a) returns a vector of the indices of **x** if the comparison operation is true (**TRUE**)
na.omit(x) suppresses the observations with missing data (**NA**)
na.fail(x) returns an error message if **x** contains at least one **NA**
unique(x) if **x** is a vector or a data frame, returns a similar object but with the duplicate elements suppressed
table(x) returns a table with the numbers of the differents values of **x** (typically for integers or factors)
subset(x, ...) returns a selection of **x** with respect to criteria (... , typically comparisons: **x\$V1 < 10**); if **x** is a data frame, the option **select** gives the variables to be kept or dropped using a minus sign
sample(x, size) resample randomly and without replacement **size** elements in the vector **x**, the option **replace = TRUE** allows to resample with replacement

Math

sin, cos, tan, asin, acos, atan, atan2, log, log10, exp
range(x) id. then **c(min(x), max(x))**
sum(x) sum of the elements of **x**
diff(x) lagged and iterated differences of vector **x**
prod(x) product of the elements of **x**
mean(x) mean of the elements of **x**
median(x) median of the elements of **x**
quantile(x, probs=) sample quantiles corresponding to the given probabilities (defaults to 0,.25,.5,.75,1)
weighted.mean(x, w) mean of **x** with weights **w**
rank(x) ranks of the elements of **x**
var(x) or **cov(x)** variance of the elements of **x** (calculated on $n-1$); if **x** is a matrix or a data frame, the variance-covariance matrix is calculated
sd(x) standard deviation of **x**
cor(x) correlation matrix of **x** if it is a matrix or a data frame (1 if **x** is a vector)
var(x, y) or **cov(x, y)** covariance between **x** and **y**, or between the columns of **x** and those of **y** if they are matrices or data frames
cor(x, y) linear correlation between **x** and **y**, or correlation matrix if they are matrices or data frames
round(x, n) rounds the elements of **x** to **n** decimals
log(v, base) computes the logarithm of **x** with base **base** **log10(v)** **base =10**
scale(x) if **x** is a matrix, centers and reduces the data; to center only use the option **center=FALSE**, to reduce only **scale=FALSE** (by default **center=TRUE**, **scale=TRUE**)

pmin(x,y,...) a vector which *i*th element is the minimum of **x[i]**, **y[i]**, ...
pmax(x,y,...) id. for the maximum
cumsum(v) a vector which *i*th element is the sum from **x[1]** to **x[i]**
cumprod(v) $f_i = \prod_{j=1..i} x_j = (x_1, x_1 \cdot x_2, \dots)$
cummin(v) $f_i = \min(x_1 \dots x_i)$
cummax(v) id. for the maximum
union(x,y), **intersect(x,y)**, **setdiff(x,y)**, **setequal(x,y)**, **is.element(el,set)** “set” functions
fft(v) Fast Fourier Transform **mvfft(x)** FFT of each column of a matrix
filter(x,filter) applies linear filtering to a univariate time series or to each series separately of a multivariate time series

Matrices

t(x) transpose
diag(x) diagonal
%% matrix multiplication and scalar product
solve(a,b) solves **a %% x = b** for **x**
solve(a) matrix inverse of **a**
rowsum(x) sum of rows for a matrix-like object; **rowSums(x)** is a faster version
colsum(x), **colSums(x)** id. for columns
rowMeans(x) fast version of row means **colMeans(x)** id. for columns

Advanced data processing

The apply family functions are very powerful and fast, they do replace a 'for loop' but are difficult to grasp.
apply(X,INDEX,FUN=) a vector or array or list of values obtained by applying a function **FUN** to margins (**INDEX**) of **X**
lapply(X,FUN) apply **FUN** to each element of the list **X**
tapply(X,INDEX,FUN=) apply **FUN** to each cell of a ragged array given by **X** with indexes **INDEX**
by(data,INDEX,FUN) apply **FUN** to data frame **data** subsetted by **INDEX**
merge(a,b) merge two data frames by common columns or row names
xtabs(a b,data=x) a contingency table from cross-classifying factors
aggregate(df,by,FUN) splits a data frame into subsets, computes summary statistics for each, and returns the result in a convenient form; **by** is a list of grouping elements, each as long as the variables in the data frame
stack(x, ...) transform data available as separate columns in a data frame or list into a single column
unstack(x, ...) inverse of **stack()**
cast(x, ...) reshapes a data frame between 'wide' format with repeated measurements in separate columns of the same record and 'long' format with the repeated measurements in separate records; use (direction="wide") or (direction="long")
melt(x, ...) melts an object into a form suitable for casting

Strings

paste(s1,s2, sep=" ") concatenate vectors after converting to character; **collapse=** is an optional string to separate “collapsed” results **paste0(s1,s2)** paste without separator (since R 2.15)
substr(s,start,stop) substrings in a character vector; can also assign, as **substr(s, start, stop) <- value**
strsplit(s,split) split **s** according to the substring **split**
grep(pattern,s) search **pattern** in **s**; see **?regex**
tolower(s), **toupper(s)** convert to lowercase (uppercase)
match(x,table) a vector of the positions of first matches for the elements of **x** among **table**
x %in% table id. but returns a logical vector

Dates and Times

All animal tracks come with a time stamp. The class **Date** has dates without times. **POSIXct** has dates and times, including time zones. Comparisons (e.g. **>**), **seq()**, and **difftime()** are useful. **Date** also allows **+** and **-**. **?DateTimeClasses** gives more information. See also package **chron**.

as.Date(s) and **as.POSIXct(s)** convert to the respective class; **format(dt)** converts to a string representation. The default string format is “2012-02-21”. These accept a second argument to specify a format for conversion. Some common formats are:

%a, **%A** Abbreviated and full weekday name.
%b, **%B** Abbreviated and full month name.
%d Day of the month (01–31).
%H Hours (00–23).
%I Hours (01–12).
%j Day of year (001–366).
%m Month (01–12).
%M Minute (00–59).
%p AM/PM indicator.
%S Second as decimal number (00–61).
%U Week (00–53); the first Sunday as day 1 of week 1.
%w Weekday (0–6, Sunday is 0).
%W Week (00–53); the first Monday as day 1 of week 1.
%y Year without century (00–99). Avoid it.
%Y Year with century.
%z (read only) Offset from Greenwich; -0800 is 8 hours west of.
%Z (read only) Time zone as a character string (empty if not available).

Where leading zeros are shown they will be used on output but are optional on input. See **?strftime**.

Plotting

Several plotting options exist in R to plot your results and these are constantly changing. Below you will find standard R plotting commands and further down more sophisticated options using e.g. ggplot2 functionality. Furthermore does R offer spatial data plotting options which can be found on the AniMove spatial cheat sheet.

plot(y) plot of the values of **y** (on the *y*-axis) ordered on the *x*-axis
plot(x, y) bivariate plot of **x** against **y**
hist(x) histogram of the frequencies of **x**
barplot(x) histogram of the values of **x**; use **horiz=FALSE** for horizontal bars
dotchart(x) if **x** is a data frame, plots a Cleveland dot plot (stacked plots line-by-line and column-by-column)
pie(x) circular pie-chart
boxplot(x) “box-and-whiskers” plot
sunflowerplot(x, y) id. than **plot()** but the points with similar coordinates are drawn as flowers which petal number represents the number of points
stripplot(x) plot of the values of **x** on a line (an alternative to **boxplot()** for small sample sizes)
coplot(x~y | z) bivariate plot of **x** and **y** for each value or interval of values of **z**
interaction.plot(f1, f2, y) if **f1** and **f2** are factors, plots the means of **y** (on the *y*-axis) with respect to the values of **f1** (on the *x*-axis) and of **f2** (different curves); the option **fun** allows to choose the summary statistic of **y** (by default **fun=mean**)
matplot(x,y) bivariate plot of the first column of **x** *vs.* the first one of **y**, the second one of **x** *vs.* the second one of **y**, etc.
fourfoldplot(x) visualizes, with quarters of circles, the association between two dichotomous variables for different populations (**x** must be an array with **dim=c(2, 2, k)**, or a matrix with **dim=c(2, 2)** if $k = 1$)
assocplot(x) Cohen–Friendly graph showing the deviations from independence of rows and columns in a two dimensional contingency table
mosaicplot(x) ‘mosaic’ graph of the residuals from a log-linear regression of a contingency table
pairs(x) if **x** is a matrix or a data frame, draws all possible bivariate plots between the columns of **x**
plot.ts(x) if **x** is an object of class “**ts**”, plot of **x** with respect to time, **x** may be multivariate but the series must have the same frequency and dates
ts.plot(x) id. but if **x** is multivariate the series may have different dates and must have the same frequency
qqnorm(x) quantiles of **x** with respect to the values expected under a normal law
qqplot(x, y) quantiles of **y** with respect to the quantiles of **x**
contour(x, y, z) contour plot (data are interpolated to draw the curves), **x** and **y** must be vectors and **z** must be a matrix so that **dim(z)=c(length(x), length(y))** (**x** and **y** may be omitted)

filled.contour(x, y, z) id. but the areas between the contours are coloured, and a legend of the colours is drawn as well
image(x, y, z) id. but with colours (actual data are plotted)
persp(x, y, z) id. but in perspective (actual data are plotted)
stars(x) if **x** is a matrix or a data frame, draws a graph with segments or a star where each row of **x** is represented by a star and the columns are the lengths of the segments
symbols(x, y, ...) draws, at the coordinates given by **x** and **y**, symbols (circles, squares, rectangles, stars, thermometres or “boxplots”) which sizes, colours ... are specified by supplementary arguments
termplot(mod.obj) plot of the (partial) effects of a regression model (**mod.obj**)

The following parameters are common to many plotting functions:
add=FALSE if **TRUE** superposes the plot on the previous one (if it exists)
axes=TRUE if **FALSE** does not draw the axes and the box
type="p" specifies the type of plot, “**p**”: points, “**l**”: lines, “**b**”: points connected by lines, “**o**”: id. but the lines are over the points, “**h**”: vertical lines, “**s**”: steps, the data are represented by the top of the vertical lines, “**S**”: id. but the data are represented by the bottom of the vertical lines
xlim=, ylim= specifies the lower and upper limits of the axes, for example with **xlim=c(1, 10)** or **xlim=range(x)**
xlab=, ylab= annotates the axes, must be variables of mode character
main= main title, must be a variable of mode character
sub= sub-title (written in a smaller font)

Low-level plotting commands

points(x, y) adds points (the option **type=** can be used)
lines(x, y) id. but with lines
text(x, y, labels, ...) adds text given by **labels** at coordinates (**x,y**); a typical use is: **plot(x, y, type="n"); text(x, y, names)**
mtext(text, side=3, line=0, ...) adds text given by **text** in the margin specified by **side** (see **axis()** below); **line** specifies the line from the plotting area
segments(x0, y0, x1, y1) draws lines from points (**x0,y0**) to points (**x1,y1**)
arrows(x0, y0, x1, y1, angle= 30, code=2) id. with arrows at points (**x0,y0**) if **code=2**, at points (**x1,y1**) if **code=1**, or both if **code=3**; **angle** controls the angle from the shaft of the arrow to the edge of the arrow head
abline(a,b) draws a line of slope **b** and intercept **a**
abline(h=y) draws a horizontal line at ordinate **y** (vertical line: **=v**)
abline(lm.obj) draws the regression line given by **lm.obj**
rect(x1, y1, x2, y2) draws a rectangle which left, right, bottom, and top limits are **x1, x2, y1**, and **y2**, respectively

polygon(x, y) draws a polygon linking the points with coordinates given by **x** and **y**
legend(x, y, legend) adds the legend at the point (**x,y**) with the symbols given by **legend**
title() adds a title and optionally a sub-title
axis(side, vect) adds an axis at the bottom (**side=1**), on the left (**2**), at the top (**3**), or on the right (**4**); **vect** (optional) gives the abscissa (or ordinates) where tick-marks are drawn
locator(n, type="n", ...) returns the coordinates (*x,y*) after the user has clicked **n** times on the plot with the mouse; also draws symbols (**type="p"**) or lines (**type="l"**) with respect to optional graphic parameters (...); by default nothing is drawn (**type="n"**)

Graphical parameters

These can be set globally with **par(...)**; many can be passed as parameters to plotting commands.
adj controls text justification (0 left-justified, 0.5 centred, 1 right-justified)
bg specifies the colour of the background (ex. : **bg="red"**, **bg="blue"**, ... the list of the 657 available colours is displayed with **colors()**)
bty controls the type of box drawn around the plot, allowed values are: “**o**”, “**l**”, “**7**”, “**c**”, “**u**” ou “**]**” (the box looks like the corresponding character); if **bty="n"** the box is not drawn
cex a factor controlling the default size of texts and symbols; you can scale numbers on the axes, **cex.axis**, the axis labels, **cex.lab**, the title, **cex.main**, and the sub-title, **cex.sub**
col controls the color of symbols and lines; use color names: “**red**”, “**blue**” see **colors()** or as “**#RRGGBB**”; see **rgb()**, **hsv()**, **gray()**, and **rainbow()**; as for **cex** there are: **col.axis**, **col.lab**, **col.main**, **col.sub**
font an integer which controls the style of text (1: normal, 2: italics, 3: bold, 4: bold italics); as for **cex** there are: **font.axis**, **font.lab**, **font.main**, **font.sub**
las an integer which controls the orientation of the axis labels (0: parallel to the axes, 1: horizontal, 2: perpendicular to the axes, 3: vertical)
lty controls the type of lines, can be an integer or string (1: “**solid**”, 2: “**dashed**”, 3: “**dotted**”, 4: “**dotdash**”, 5: “**longdash**”, 6: “**twodash**”, or a string of up to eight characters (between “**0**” and “**9**”) which specifies alternatively the length, in points or pixels, of the drawn elements and the blanks, for example **lty="44"** will have the same effect than **lty=2**
lwd a numeric which controls the width of lines, default 1
mar a vector of 4 numeric values which control the space between the axes and the border of the graph of the form **c(bottom, left, top, right)**, the default values are **c(5.1, 4.1, 4.1, 2.1)**

`mfc` a vector of the form `c(nr,nc)` which partitions the graphic window as a matrix of `nr` lines and `nc` columns, the plots are then drawn in columns

`mfrow` id. but the plots are drawn by row

`pch` controls the type of symbol, either an integer between 1 and 25, or any single character within ""

1 ○ 2 △ 3 + 4 × 5 ◇ 6 ▽ 7 ☒ 8 ✱ 9 ⊕ 10 ⊗ 11 ⌘ 12 ▢ 13 ☒ 14 ☒ 15 ■
16 ● 17 ▲ 18 ◆ 19 ● 20 ● 21 ○ 22 □ 23 ◇ 24 △ 25 ▽ * . . . X X a a ? ?

`ps` size in points of texts and symbols as integer

`pty` a character which specifies the type of the plotting region, "s": square, "m": maximal

ggplot2

`ggplot2` comes with its own syntax which is different from normal R syntax. It takes quite a while to learn it but produces very fancy graphics.

`qplot(x=vx, y=vy, data=df)` plots columns `df$vx` and `df$vy`

Lattice (Trellis) graphics

`xplot(y~x)` bivariate plots (with many functionalities)

`barchart(y~x)` histogram of the values of `y` with respect to those of `x`

`dotplot(y~x)` Cleveland dot plot (stacked plots line-by-line and column-by-column)

`densityplot(~x)` density functions plot

`histogram(~x)` histogram of the frequencies of `x`

`bwplot(y~x)` “box-and-whiskers” plot

`qqmath(~x)` quantiles of `x` with respect to the values expected under a theoretical distribution

`stripplot(y~x)` single dimension plot, `x` must be numeric, `y` may be a factor

`qq(y~x)` quantiles to compare two distributions, `x` must be numeric, `y` may be numeric, character, or factor but must have two ‘levels’

`splo` matrix of bivariate plots

`levelplot(z~x*y|g1*g2)` coloured plot of the values of `z` at the coordinates given by `x` and `y` (`x`, `y` and `z` are all of the same length)

`wireframe(z~x*y|g1*g2)` 3d surface plot

`cloud(z~x*y|g1*g2)` 3d scatter plot

Statistics, optimization and model fitting

`aov(formula)` analysis of variance model

`anova(fit,...)` analysis of variance (or deviance) tables for one or more fitted model objects

`lm(formula)` fit linear models; `formula` is typically of the form `response termA + termB + ...`; use `I(x*y)` + `I(x^2)` for terms made of nonlinear components

`glm(formula,family=)` fit generalized linear models, specified by giving a symbolic description of the linear predictor and a description of the error distribution; `family` is a description of the error distribution and link function to be used in the model; see `?family`

`nls(formula)` nonlinear least-squares estimates of the nonlinear model parameters

`glm()` generalized linear model

`gam()` generalized additive model

`kmeans()` kmeans clustering

`tree()` builds a decision tree

`rpart()` builds a decision tree

`randomForest()` random forest machine learning

`maxent()` Maximum Entropy model

`svm()` Support Vector Machines in the `e1071` package, but other packages provide SVM as well such as: `kernlab`, `klaR`, `svm-path`, `shogun`

`approx(x,y=)` linearly interpolate given data points; `x` can be an `xy` plotting structure

`spline(x,y=)` cubic spline interpolation

`loess(formula)` fit a polynomial surface using local fitting

`predict(fit,...)` predictions from `fit` based on input data

`coef(fit)` returns the estimated coefficients (sometimes with their standard-errors)

`residuals(fit)` returns the residuals

`deviance(fit)` returns the deviance

`fitted(fit)` returns the fitted values

`logLik(fit)` computes the logarithm of the likelihood and the number of parameters

`AIC(fit)` computes the Akaike information criterion or AIC

Distributions

`rnorm(n, mean=0, sd=1)` Gaussian (normal)

`rexp(n, rate=1)` exponential

`rgamma(n, shape, scale=1)` gamma

`rpois(n, lambda)` Poisson

`rt(n, df)` ‘Student’ (*t*)

`rchisq(n, df)` Pearson

`rbinom(n, size, prob)` binomial

`rlogis(n, location=0, scale=1)` logistic

`rnbinom(n, size, prob)` negative binomial

`runif(n, min=0, max=1)` uniform

`rwilcox(nn, m, n), rsignrank(nn, n)` Wilcoxon’s statistics

All these functions can be used by replacing the letter `r` with `d`, `p` or `q` to get, respectively, the probability density (`dfunc(x, ...)`), the cumulative probability density (`pfunc(x, ...)`), and the value of quantile (`qfunc(p, ...)`, with $0 < p < 1$).

Programming

`function(arglist)` `expr` function definition

`return(value)`

`if(cond) expr`

`if(cond) cons.expr else alt.expr`

`for(var in seq) expr`

`while(cond) expr`

`repeat expr`

`break`

`next`

Use braces `{ }` around statements

`ifelse(test, yes, no)` a value with the same shape as `test` filled with elements from either `yes` or `no`

Examples in this document use the variables `df` = data frame object, `v` = vector, `s` = string, `f` = filename as string

Credits

This R reference card is adapted to [AniMove](#) needs by Martin Wegmann, Benjamin Leutner and Mirjana Bevanda but based on the reference card by Jonas Stein, Tom Short and Emmanuel Paradis.

