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Tail Recursion

```
(define multiply
  (lambda ((a <number>) (b <integer>))
    (cond ((zero? b) 0)
          ((odd? b)
           (+ a (multiply (+ a a) (quotient b 2))))
          (else
           (multiply (+ a a) (quotient b 2))))))
```

Write a version of multiply which uses the same basic algorithm as above, but which is tail-recursive.

```
(define multiply-2
  (lambda ((a <number>) (b <integer>))
    (cond ((zero? b) 0)
          ((odd? b)
           (letrec ((iter
                     (lambda ((c <integer>) (result <number>))
                       (if (= c (quotient b 2))
                           result
                           (iter (quotient c 2) (+ result (* (quotient c 2) (+ a a)))))))
            (iter b a)))
          (else
           (letrec ((iter
                     (lambda ((c <integer>) (result <number>))
                       (if (= c (quotient b 2))
                           result
                           (iter (quotient c 2) (+ result (* (quotient c 2) (+ a a)))))))
            (iter b 0)))))
```