CSM: An Improved Algorithm for Instance-based Reinforcement Learning

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Abstract

Instance-based approaches are effective ways to solve reinforcement learning problems. Utile Suffix Memory (USM) algorithm has shown decent results for distinguishing different states from instance chains and generating Q-value of actions of each state, but involving exponentially expanded state space and a number of redundant states. In this paper we propose a new state space compressed algorithm, called Compressed Suffix Memory (CSM) algorithm. CSM algorithm obtains heuristic information of environments by blind exploration, e.g. the path length of most solutions and goal frequencies, to improve efficiency and resist overfitting. We use Boltzmann sampling to balance between exploration and exploitation. Our experiments show that both the efficiency and the effect have been improved a lot by CSM algorithm compared with USM algorithm.

1 Introduction

Reinforcement learning is learning what to do—how to map situations to actions—so as to maximize a numerical reward signal in a provided environment [9]. In many reinforcement learning scenarios such as robotic exploration [8] and autonomous driving [2], the agent is only able to gain partial and noisy observations form environment, so POMDP (partially observable Markov decision process) model is wildly adopted. According to the observations, reward and the historical information, POMDPs provide a rich mathematical approach to solving sequential problems by calculating the Q-value of actions.

As the agent does not directly observe the underlying state, the generation of the state space is the key to POMDP-based reinforcement learning algorithms. Many instance based methods have been put forward, including Nearest Sequence Memory (NSM) algorithm [5] and Utile Suffix Memory (USM) algorithms [4]. USM algorithm presents the state space by tree-nodes in a suffix tree building from the instance chains, and is proved effective maximizing the Q-value of actions. However, the state space of USM

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algorithm exponentially expands during iteration and comprises many redundant states, which reduces the efficiency. Furthermore, because the ϵ -greedy policy of USM treats the second best and the worst the same, it may lead to overfitting.

In this paper, we propose a new algorithm, called Compressed Suffix Memory (CSM) algorithm, which optimizes the generation of a utile tree and decision process. First, the heuristic information is obtained by the agent during a blind exploration of the environment, e.g., l as the length of the longest non-repetitive observation sequence and p the probability of goal during this exploration. Second, the maximum depth of the suffix tree is limited to doubled l and the minimum instances required to trigger state splitting is deduced from p. Finally, after initializing the agent with a random policy, boltzmann sampling approach will be applied. Experiment has shown that both the efficiency and the effect have been greatly improved by CSM compared with USM.

The paper outline follows. We will briefly review the basics of reinforcement learning, POMDP problems and Utile Suffix Memory (USM) algorithm, in Section 2. Next we propose Compressed Suffix Memory (CSM) algorithm, which solves the weaknesses of USM by new means of utile tree generation, new exploration method and self correction mechanism, in Section 3. We measure the performance of CSM and see improvements comparing with USM, in Section 4. We close in Section 5, with a brief summary and possible means of improvement of CSM.

2 Background

2.1 Reinforcement Learning in Partially Observable Environment

Reinforcement learning is about how an agent learning to map states to actions and produce a maximized reward in a provided environment. In general, a reinforcement learning agent interacts with the environment over time. At each time step t, it determines its state s_t from a state space S, and chooses a best action a_t from an action space A

according to the policy π . The agent gets a instant reward r_t according to the reward function $R(s_t, a_t)$ and transfer to the next state s_{t+1} according to the transition probability $T(s_{t+1}|s_t, a_t)$. The reward is normally discounted with factor $\gamma \in (0, 1]$, and the accumulated reward at t_n is defined as $R_{t_n} = \sum_{t=0}^{t_n} \gamma^t r_t$. When a problem satisfies the Markov property, the problem can be formulated as a Markov decision process (MDP), which is defined by the 5-tuple (S, A, T, R, γ) .

However, in most cases, an agent cannot directly observe the states of the MDP model underlying the provided environment, but can only deduce a state by an observation. It is necessary to bring in partially observable Markov decision process (POMDP). It defines Ω as a set of observations and O as a set of conditional observation probabilities-mapping current state s_t and previous action a_{t-1} to the probability of current observation o_t . In that way, a POMDP can be defined by the 7-tuple $(S, A, T, R, \Omega, O, \gamma)$.

When the model is given, i.e., all elements of the 7-tuple are known, there are plenty of algorithms to calculate a best policy [7]. However, in model-free methods, an agent can learn with trail-and-error from experience directly and a policy can generated before grasping all information of a model [3]. An important way to implement model-free methods is to make an agent comprise some sort of internal memory [1, 4, 6] (see Figure 1). For example, the states of a model can be expressed by some nearest observations and internal states of an agent. After learning the state space, the agent can solve it by model-free methods, such as HQ-learning [10].

The internal memory of an agent can comprise instances that record what it has encountered at each time step. Nearest Sequence Memory (NSM) and Utile Suffix Memory (USM) algorithms are based on the instances.

2.2 Utile Suffix Memory Algorithm

The interaction between the agent implementing USM and the environment is described by *A*, *O*, *R*, which are finite set of actions, finite set of observations and a reward function. Like other instance based algorithms, USM records each of

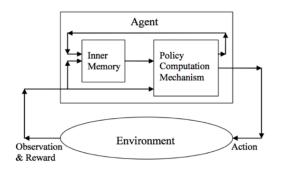


Figure 1: The agent model that has internal memory

its raw instances [4]. At each time step t, the agent executes action $a_t \in A$ to get a new instance, gets observation $o_{t+1} \in O$, and get a instant reward r_{t+1} according to R, which is determined by the environment. That new instance is formulated as

$$T_{t+1} = (T_t, a_t, o_{t+1}, r_{t+1}).$$
 (1)

 T_{t+1} is T_t 's successor and, similarly, T_{t-1} is T_t 's predecessor. Normally, in an environment with goals for agent to reach, chains of instances-from initial instance to instance reached goal-are built during the learning phase.

In order to find hidden states from those instances chains, USM creates a suffix tree, whose leaves present the state space and store clustered instances. Each node of the tree can thus be uniquely identified by the string of labels on the path from node to the root, and the string is called the node's suffix. An instance is always deposited into the nodes whose suffix matches its observation and action context, or suffix. That is, for an instance T_i , if its suffix $[..., o_{t-3}, a_{t-3}, o_{t-2}, a_{t-2}, o_{t-1}, a_{t-1}]$ matches the suffix of some node, it would be put into that node (see Figure 2). The set of instances that a node contains is written as I(s). The suffix tree leaf which instance T belongs to is written as L(T). It is inevitable that the action layer and the observation layer appears alternately when tree grows (see Figure 2).

Besides the general nodes, there is another type of node called "fringe" node [4]. The fringe nodes are actually the deepest layers of the suffix tree, however, we treated them the inner instance buckets of the leaves previously mentioned. Fringe nodes also contain instances according to the same suffix criterion used by non-fringe nodes. That is, if the suffix of a leaf is $[a_{t-2}, o_{t-1}, a_{t-1}]$, an 1-layer deeper fringe nodes of it will stores the instance that matches suffix $[o_{t-2}, a_{t-2}, o_{t-1}, a_{t-1}]$. The agent decides whether it should promote fringe nodes to leaves by Kolmogorov-Smirnov test, which determine the instances in the fringes and that of their parent are drawn the same distribution.

The steps of USM is as below:

1. The agent begins with a suffix tree that comprises a

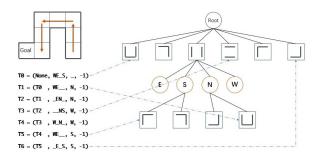


Figure 2: The agent navigates itself in a maze (probably not the first time), generates a sequence of instances, and builds a suffix tree. The action layer and the observation layer appears alternately.

- root node and an layer of observation nodes as leaves, i.e., the agent only acts according to its observation.
- 2. The agent chooses an action according to ϵ -greedy policy, executes it and generates an instance (see Equation 1).
- The agent insert the instance into the suffix tree. The instance is classified to leaves and fringes with the same suffix with that instance.
- 4. The agent triggers K-S test every *n* additions of instance. If the Q-value of fringes and their parent are from different distributions, the fringes will be promoted to leaves. The instance will always be added to fringes and leaves that have the same suffix with the instance. Q-value table will be updated after every addition of instance. Time step increases and algorithm jumps to step 2.

There are two obvious deficiencies of the USM algorithm. Firstly, in the USM algorithm, the number of states may exponentially increase as the number of steps grows, but many states are redundant, which correspond to the same state in the real environment. Thus, it will reduce the efficiency of the algorithm. Secondly, since the initial Q value of all leaves is initialized with 0, the ϵ -greedy policy may lead to overfitting. Because the ϵ -greedy policy of USM treats the second best and the worst the same, it drastically decrease the probability to explore other actions which may get higher reward. For example, we found that in the first few steps, the agent may get negative default return after choosing actions at some states, which decreases the probability of exploring those actions when at those states again.

3 Compressed Suffix Memory Algorithm

In order to overcome the weaknesses of USM. We reconstructed the work flow of agent in maze environments. Firstly, we introduces the blind exploration. Exploration and exploitation is a key issue in reinforcement learning. Agent could first make a blind policy exploration of the environment, obtaining some heuristic experience, and apply it to following reinforcement learning. We found that the longest non-repetitive observations of the maze and the frequency of goals can decently presents the local complexity and the scale of the environment, respectively. The heuristic experience can be used to improve the algorithm:

1. The depth of the suffix tree could be constrained. We tried to locate the redundant states of USM and found a potential cause. The suffix tree may grow so deep that a leaf's suffix is longer than most paths from start to goal. By deducing the length of most paths from start to goal as *l* and limiting the suffix tree's depth to 2*l* can reduce the generation of less useful leaves. So we set *l* as the sum of longest horizontal edge and vertical edge found by the blind search, since in most situations, paths generated by the best policy are shorter than *l*.

- 2. Instances in tree node could be denser. Instead of doing K-S test every *n* instances added, which may lead to overfitting at some leaves, agent only triggers K-S test when leaves and their fringe nodes are holding enough instances. The minimum number *b* of instances to do K-S test is deduced from blind exploration, since *b* should vary with environment scale. In practice, we find the frequency of goals in blind exploration well describes the environment scale.
- 3. The ϵ -greedy approach can be improved. The main problem of ϵ -greedy approach is that it treats the second best and the worst the same, hence decreasing the probability to explore the second best action. We use boltzmann sampling to balance between exploration and exploitation, which assigns actions with similar Q value similar probabilities to encourage agent to explore or exploit them all, instead of only the best. The probability to choose an action a_i at leaf s with temperature t is

$$p(s, a_i) = e(s, a_i) / \sum_a e(s, a),$$
 (2)

which *e* is

$$e(s, a) = \exp((Q(s, a) - \max Q(s))/t) \tag{3}$$

The details and the pseudo code (see Algorithm 1) form of the CSM algorithm is as below.

- 1. The agent begins with a suffix tree that comprises a root node and an layer of observation nodes as leaves, i.e., the agent only acts according to its observation.
- 2. The agent randomly explores the environment for a number of times. The agent deduces the the effective path length *l* to goal and minimum number *b* of instances to do K-S test in that exploration. The maximum depth of the suffix tree is set to 2*l*.
- 3. The agent executes action and interacts with the environment at time step t. It records its learning history as an instance T_t (see Equation 1). For all s, no matter s is leaf or fringe, if the suffix of s matches the suffix of T_t . Their instance set are updated as:

$$I(s) \leftarrow I(s) \cup T_t.$$
 (4)

Let L(T) be the leaf which instance T belongs to. $L(T_t)$ is cached to agent memory.

4. For each instance added, the agent does one Bellman iteration with the leaves of of the states:

$$Q(s, a) \leftarrow R(s, a) + \gamma Pr(s'|s, a)U(s'). \tag{5}$$

Let I(s, a) be the subset of I(s) that contains all the instances that executed action a. U(s') is the utility of the state s', calculated as $U(s) = \max_{a \in A} Q(s, a)$. R(s, a) and Pr(s'|s, a) are the estimated immediate reward and the transition probability, respectively, that drawn from the instance chains:

$$R(s, a) = \frac{\sum_{T_i \in I(s, a)} r_i}{|I(s, a)|},$$
(6)

$$Pr(s'|s,a) = \frac{|\forall T_i \in I(s,a) \ s.t. \ L(T_{i+1} = s')|}{|I(s,a)|}.$$
 (7)

5. Agent perform Kolmogorov-Smirnov when $L(T_t)$ is not the same as $L(T_{t-1})$ and $L(T_t)$ holds enough instances (more than b). The expected discounted reward of instance T_i is written as $H(T_i)$, and is defined

$$H(T_i) = r_i + \gamma U(L(T_{i+1})) \tag{8}$$

Agent calculates every $Q(T_i)$ for instances of leaf and those of immediate fringe nodes, then determines whether they are from the same distribution. If they are not, those fringe nodes would be promoted as leaves.

6. Agent does Boltzmann sampling to choose the next action, i.e., with probability $p(s, a_i)$ the agent chooses a_i as a_{t+1} (see Equation 2). In practice, we encourage agent to do random exploration for n_r times, and then perform Boltzmann sampling method with descendant temperature. Time step increase to t + 1 and algorithm jumps to step 3.

Experiment

Experiment Setup

We run algorithms with three well-known benchmarks: Tiger-Grid, Hallway and McCallum as well as a large Prim Maze generated by Prim algorithm randomly (see Figure 3). The characteristics of POMDP benchmarks are described below (see Table 1), where |S|, |A|, $|\Omega|$, r_d , r_p , r_q , denotes the number of states, the number of actions, the number of observations, default reward, penalty and goal, respectively. The |A| is 4 because the action of the agent normally includes: moving south, west, east and north. However, problems differ in some details.

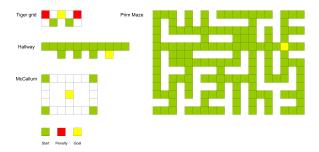


Figure 3: Benchmark mazes

In Tiger-Grid, the agents are initially assigned to one of two definite starting positions. The probability of each starting position is 0.5. The goal of the model is to make the agent reach the goal position as soon as possible. Once the agent reaches the goal position, it will be reset to two starting positions. Tiger-Grid's maze comprises two penalty positions where agent will receive a negative reward.

Algorithm 1 Compressed Suffix Algorithm

Input: iteration steps n, radom steps in iteration n_r **Output:** average discounted return E(r)

- 1: Initialize path length l, and minimum number b of instance required to do K-S test by blind exploration
- 2: Initialize temperature *t* as positive infinity
- 3: Initialize a suffix tree with depth limitation 2l
- 4: Initialize agent with random start position
- 5: **for** i = 0 to n **do**
- if $i > n_r$ then 6:
- t decreases from 0.5 to nearly 0 as i increases 7:
- end if 8:
- 9: Choose action a by boltzmann sampling and execute it (see Equation 2)
- 10: **while** not moved after executed a **do**
- Choose action a by boltzmann sampling with 11: higher t and execute it
- 12: end while
- Generate instance *T* according to the execution of *a* 13: just now
- Insert *T* into the suffix tree, and find the leaf node *s* 14: the instance belongs

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15:
            I(s) = I(s) \cup T_t
            Q(s, a) = R(s, a) + \gamma Pr(s'|s, a)U(s')
16:

\widetilde{R}(s, a) = \sum_{T_i \in I(s, a)} r_i / |I(s, a)| 

Pr(s'|s, a) = |\forall T_i \in I(s, a) \text{ s.t. } L(T_{i+1} = s')| / |I(s, a)|

17:
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- 18:
- 19: if |I(s)| > b then
- do K-S test between H(T)s of s and its fringe nodes, 20: get p_value p
- 21: if p < 0.1 then
- promote fringe nodes to leaves 22:
- 23: end if end if 24:
- 25: if agent at goal then
- 26: Initialize agent with random start position
- 27: end if
- 28: end for
- 29: Use boltzmann sampling at low temperature on Q(s, a)to produce average discounted reward ADR (see Equation 9)
- 30: return ADR

In Hallway, similar to Tiger-Grid problem but still different, agent will be reset randomly to a non-goal state. The Hallway does not include any penalty position. Furthermore, the hallway adds 4 landmarks as hint for agent to discover hidden states.

In McCallum, after reached the goal, the agent will be randomly reset at one of the 4 corners. There are 3 southnorth hallways, which are deliberately designed for agent to distinguish, since they are ambiguous.

In Prim Maze, which is randomly generated by Prim algorithm and mean to be big. |S| of Prim Maze is several times the *S* of others. When the agent arrives at the goal, Prim Maze will reset the agent to a random state in the maze.

We evaluate average discounted reward, ADR, in the exper-

Table 1: Benchmarks

problem	S	A	$ \Omega $	r_d	r_p	r_g
Tiger-Grid	9	4	7	-0.1	-4	32
Hallway	15	4	4	-0.1	-4	32
McCallum	23	4	9	-0.1	-4	32
Prim Maze	167	4	16	-0.1	-4	96

iment:

$$ADR = \frac{\sum_{i=0}^{n_{trails}} \sum_{j=0}^{n_{steps}} \gamma^{j} r^{j}}{n_{trails}},$$
 (9)

ADR is widely considered to be a good evaluation of the quality of a value function. The higher the ADR is, the more intelligent the agent is considered to be. We track the changing of ADR through time to determine whether CSM helps the agent to learn faster and better.

Our experiment uses a discount factor $\gamma=0.9$, an exploration probability $\epsilon=0.1$ for USM. The boundary value of the Kolmogorov-Smirnov test is p=0.1. We iterate the USM, CSM and random algorithm 2048 times, and set check points per 48 iteration. In each check point we test our model 256 times within 96 steps, i.e., $n_t rial$ is 256 (see Equation 9) in ADR calculation.

4.2 Experiment Results

The experiment results of CSM, USM and random algorithm are shown below (see Figure 4). It should be noted that even if $n_t rail$ -set to 256-seems large enough, the results of ADR may still fluctuate. Therefore, we record the (ADR, time) tuple in table below (see Table 2), when ADR first becomes satisfiable, rather than the maximum.

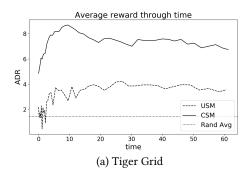
Table 2: Experiment Results

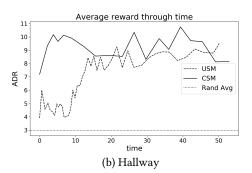
	satisfia	ble <i>ADR</i>	time taken		
problems	USM	CSM	USM	CSM	
Tiger-Grid	3.81	8.70	10.75	9.45	
Hallway	8.43	10.13	13.52	6.67	
McCallum	2.82	5.90	34.39	14.15	
Prim Maze	7.13	8.30	49.30	18.24	

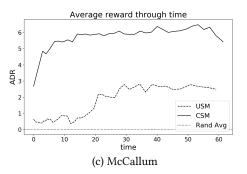
4.3 Experiment Results Analysis

In Tiger-Grid, CSM algorithm quickly reached a very high *ADR* in a short time after the start of the experiment. As the experiment progressed, the *ADR* of CSM algorithm converged to 7.5. In contrast, the *ADR* of USM algorithm fluctuated drastically in the early stage of the experiment, and became stable at around 4, which was only half of the CSM algorithm.

In Hallway, the *ADR* of both algorithms fluctuated violently, and converged to a similar value. However, when comparing time taken to reach those, CSM algorithm reached







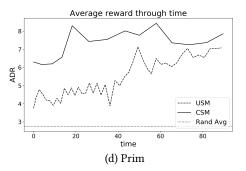


Figure 4: Performance of different agent on different benchmarks; y-axis is *ADR*, x-axis is runtime in seconds.

satisfiable *ADR* taken the half runtime of USM algorithm, i.e., the agent adopted CSM algorithm have learned twice as fast as agent adopted USM algorithm in Hallway.

In McCallum, similar to the performance in Tiger-Grid, CSM algorithm quickly reached a very high *ADR* in short

time after the start of the experiment. As the experiment progressed, the *ADR* of CSM algorithm was basically stable at 6. On the other hand, the *ADR* of USM algorithm have not significantly increased in the early stage. What's more, USM algorithm got a far less max *ADR* than CSM algorithm, which is only about 3. The figure indicated that in McCallum, CSM algorithm could find a better policy more quickly than USM algorithm.

In larger scale problems, such as the Prim Maze, CSM algorithm also performed faster and better than USM. From the experiment results, CSM algorithm achieved a satisfiable *ADR* about 8 in about 20 seconds. USM algorithm, meanwhile, only reached around 5. Even if in the mid-stage of the experiment, where the *ADR* of USM has experienced arapid growth, its time cost was almost three times that of CSM, and had a still lower *ADR*.

In addition, it can be seen from the experiment result that at the beginning of the experiment, although both algorithms have not gained experience through learning, CSM has obtained a higher *ADR* than USM. This can be explained in two ways:

- CSM algorithm uses the Boltzmann sampling method to choose action, the agent does not only perform the best action at the stage of exploitation, but other non-optimal actions, which resist overfitting at early stage.
- CSM rises the *temperature* of Boltzmann sampling when agent continously bumps into walls, which helps agent get out of that position. That ensures the efficiency of exploration.

It is for these two reasons that CSM algorithm is able to understand the environment better and discover the goal faster than USM algorithm, hence obtaining a higher *ADR*.

Overall, It can be seen that CSM algorithm helps agent to learn faster and better than USM algorithm

5 Conclusion

In this paper, the USM algorithm is described in detail, and the defects of USM algorithm are proposed. Based on the original algorithm, some suggestions for improvement are proposed. Then the CSM (Compressed Suffix Memory) algorithm is proposed. At the end of this paper, the content of the maze experiment is introduced to test the CSM algorithm, and compared with the results of the USM algorithm, it shows that the CSM algorithm does have some improvement effects.

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