



# EE 3523 Final Project

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May 3, 2019

# INTRODUCTION



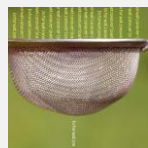
One of my songs was used for the signal to be filtered.



Analyzed a sample of 40 seconds from 00:28:00 to 01:08:00



2 Channel,  $F_s = 48\text{kHz}$ , 1920000 samples per channel.



Both L and R channels are filtered for each step of the project.

```
%Read in my song "ascend - bruno G*"
% "native" => samples are 24 bits stored as int32's
[samples, fs] = audioread("ascend_1604.wav", "double");
info = audioinfo("ascend_1604.wav");
```

```
%Get L and R Channels from WAV and make into row
%get 40 seconds of my song
sampleRate = info.SampleRate;
begin = 28; %start at second 28
duration = 40;
```

```
lchannel = samples( (sampleRate*begin) : ...
    (sampleRate*(begin+duration))-1 ,1) .';
```

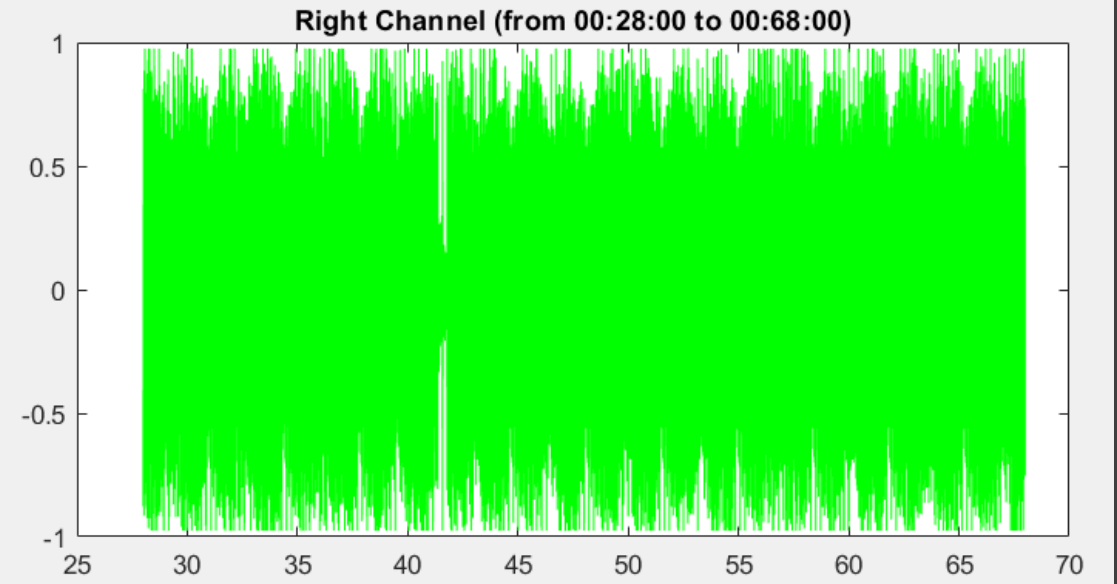
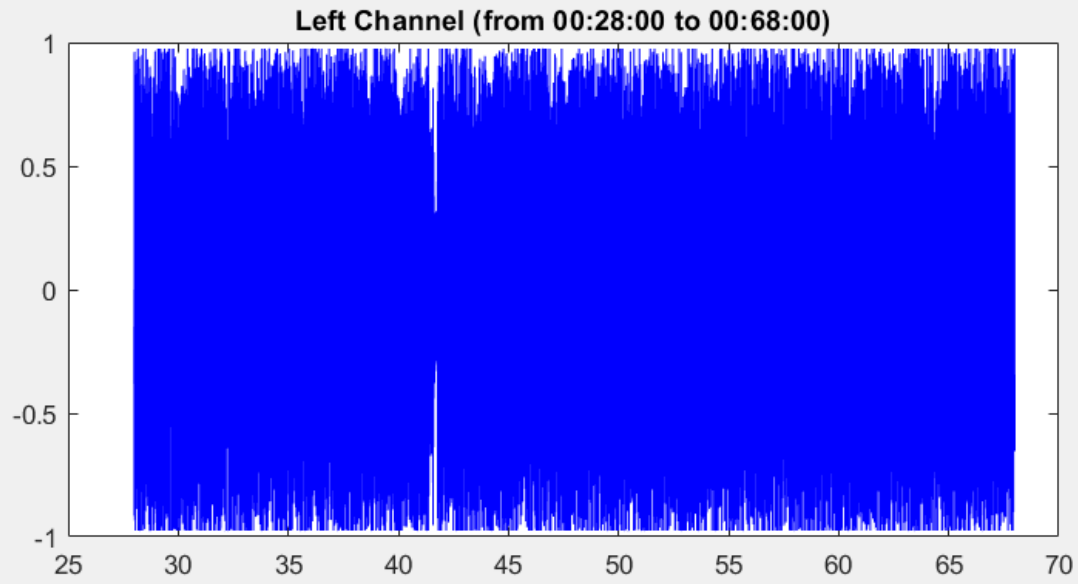
```
rchannel = samples( (48000*begin) : ...
    (sampleRate*(begin+duration))-1 ,2) .';
```

```
numSamples = length(lchannel);
```

```
%Assemble both channels into a track for playback
songSnippet = [ lchannel.' rchannel.'];
```

```
%play the audio tracks
%sound(songSnippet,sampleRate);
```

# 1. Code



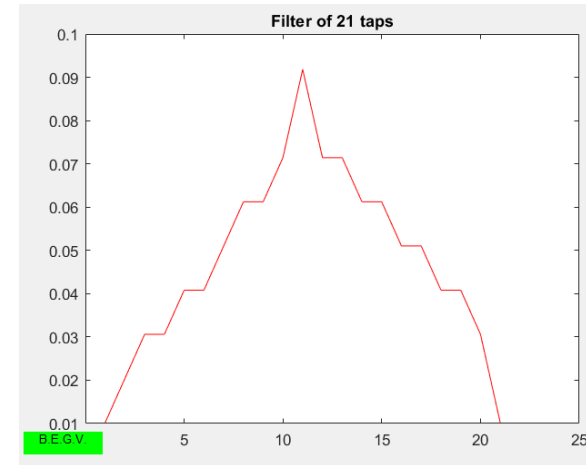
# 1. MATLAB Figures – raw data

# 1. Play the Song

```
%Assemble both channels into a track for playback  
songSnippet = [ lchannel.' rchannel.'];  
  
%play the audio tracks  
sound(songSnippet,sampleRate);
```

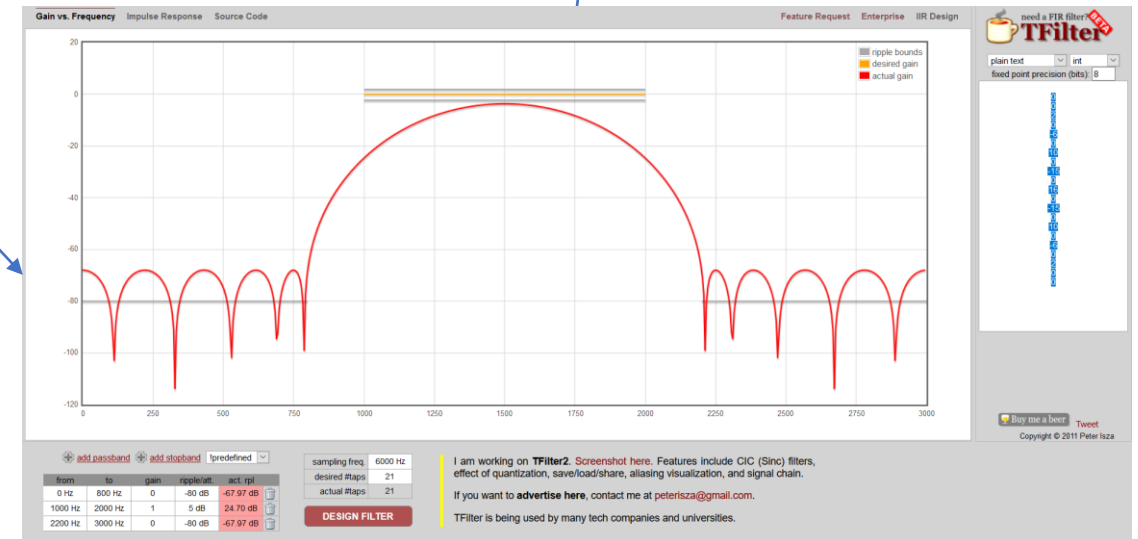
## 2. Filter the Signal

- Filter of 21 taps created given guidelines
- Normalized with  $k = \text{sum of } h(n)$
- \*other filters tested using online tap-filter generator
  - These are commented out



```
%Create Triangle Filter filter(11) is the center
filter = [1 2 3 3 4 4 5 6 6 7 7 9 7 7 6 6 5 5 4 4 3 1];
%{
filter = [-659 -1915 -2005 -358 1679 1089 -1853 -2807 ...
2077 10186 14235 10186 2077 -2807 -1853 1089 ...
1679 -358 -2005 -1915 -659];
%}
%filter = [3 -1 -3 -1 -7 2 25 -3 -44 1 53 1 -44 -3 25 2 -7 -1 -3 -1 3];
%BPF 1-2KHz
%filter = [0 0 2 0 -6 0 10 0 -15 0 16 0 -15 0 10 0 -6 0 2 0 0];

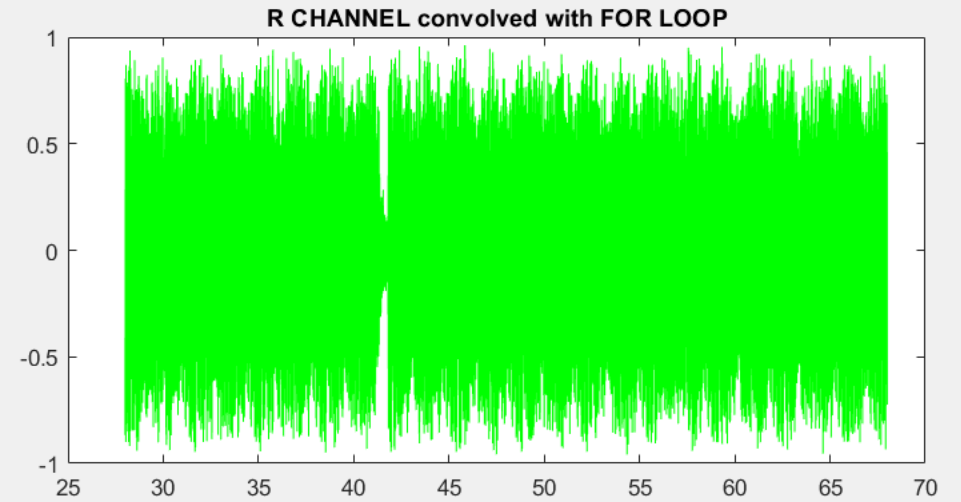
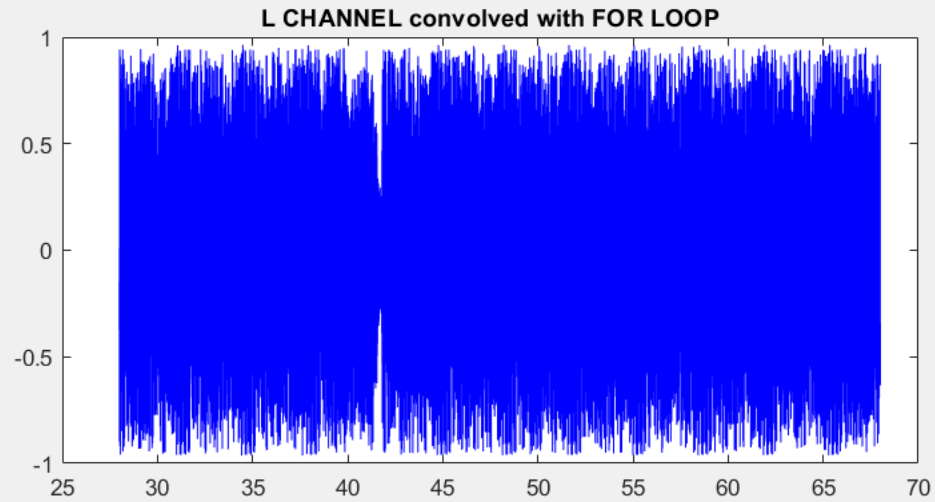
k = sum(filter); % normalize
filter = filter/k;
filterAxis = 1:length(filter);
```



## 2A. Calculate Direct Convolution

- First  $h(n)$  was mirrored
- Then for loop was generated to calculate the convolution
- Both L and R channels are convolved with the triangle filter

```
68 %LEFT channel
69 convLeft = lchannel;
70 convFilter = filter(length(filter) : -1 : 1); %mirror
71
72 for n=11:numSamples-10
73     p=lchannel(n-10:n+10);
74     convLeft(n)=sum(p.*convFilter);
75 end
76
77 %RIGHT channel
78 convRight = rchannel;
79
80 for n=11:numSamples-10
81     p=rchannel(n-10:n+10);
82     convRight(n)=sum(p.*convFilter);
83 end
```



B.E.G.V.

## 2A. MATLAB Figures

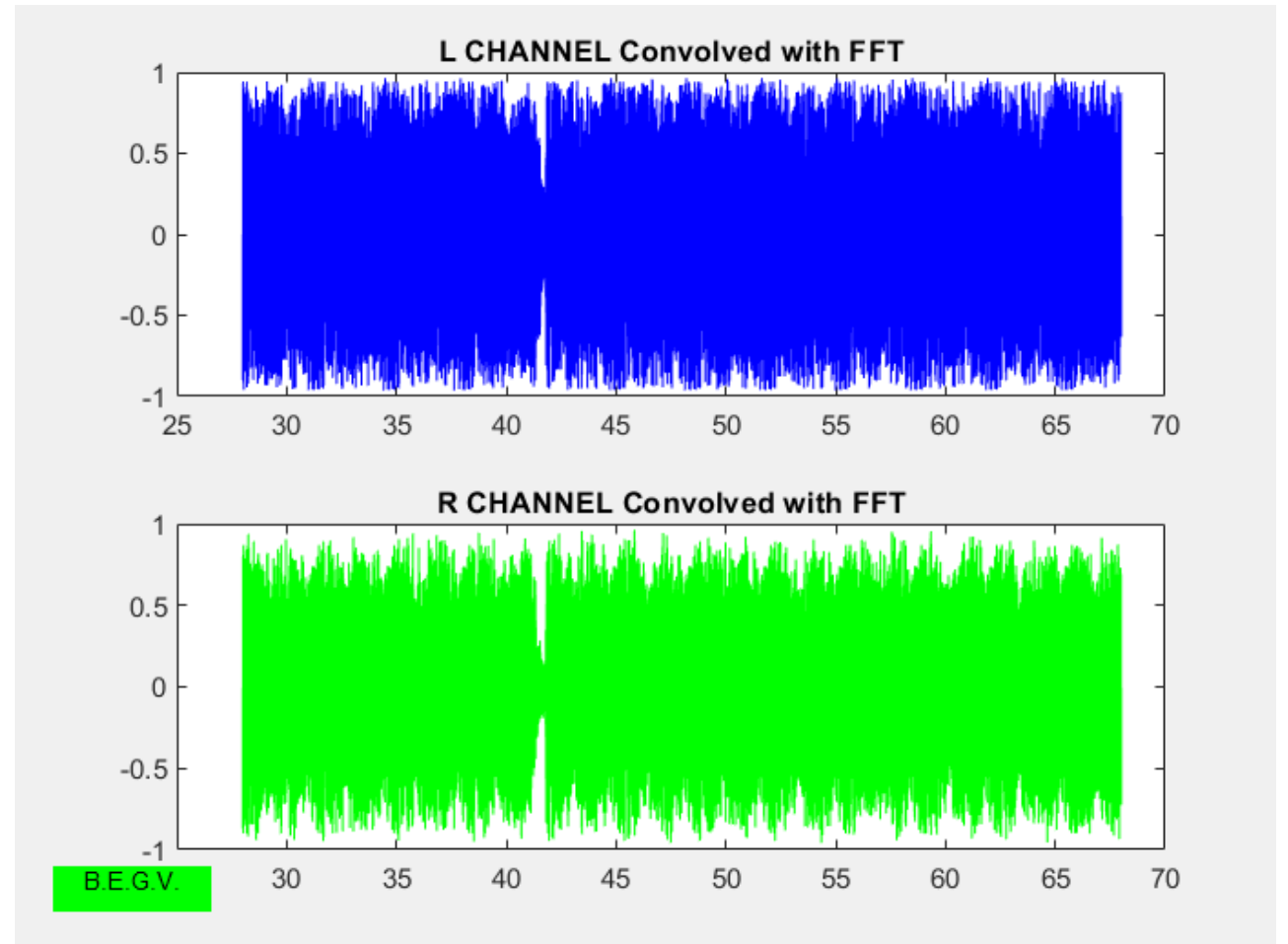


## 2A. Calculate Convolution with FFT

- This problem was confusing because part C asks to do FFT and IFFT for the convolution also.
- Steps:
  - Zero padding of L and R Channels with length of filter -1.
  - Zero padding filter with length of L channel or R channel.
  - Finding FFT's of L channel, R channel, and the triangle filter.
  - L channel \* filter = F[L channel] x F[filter]
  - R channel \* filter = F[R channel] x F[filter]
  - Inverse FFT of F[L channel] x F[filter]
  - Inverse FFT of F[R channel] x F[filter]

```
124 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%Convolution by FFT%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
125
126 %Setup FFT of L and R Channels, and Filter
127 - fft_l = fft( [ lchannel zeros(1, length(filter)-1) ] );
128 - fft_r = fft( [ rchannel zeros(1, length(filter)-1) ] );
129 %fft_f = fft([filter zeros(1, length(lchannel) - length(filter)) ]); %not
130 %needed, automatic padding
131 - fft_f = fft(filter, length(fft_l));
132
133 %Convolve in frequency domain
134 - convF_l = fft_l .* fft_f;
135 - convF_r = fft_r .* fft_f;
136
137 %Go back to time domain
138 - conv_l = ifft(convF_l);
139 - conv_r = ifft(convF_r);
140
141 %resize timeAxis to account for the added samples from convolution
142 - timeAxis = begin:(1/sampleRate):(begin+duration + (19/sampleRate));
143
```

## 2A. MATLAB Figures



## 2B-1. Overlap Add Convolution

- Both L and R channels were split into chunks of 10 sec each.
- Each channel has a 4 x (480000+20) matrix to store the 4 chunks
- 10 sec with 48000 sampling rate is 480000 samples

```
155 %%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%PART B-1%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
156
157 - tenSec = sampleRate*10; %constant
158 - chunks = 0: (tenSec): numSamples; %mark the bounds of each chunk
159 - chunks = chunks + 1;
160 - totChunks = length(chunks) - 1; %constant for total chunks
161
162 %set aside memory for overlap add method.
163 %this is a 4 row by 480000 + 20 zeros vector for each convolution
164 - chunkV_l = zeros(totChunks, tenSec + (length(filter)-1) );
165 - chunkV_r = chunkV_l;
166
167 %make loop to make a matrix to hold 10 second chunks
168 - for i=1:totChunks
169     %get the 10 sec chunks from song for each channel
170     L = lchannel(chunks(i):chunks(i+1)-1);
171     R = rchannel(chunks(i):chunks(i+1)-1);
172
173     %assign to the first ten seconds the fetched samples
174     chunkV_l(i,1:tenSec) = L;
175     chunkV_r(i,1:tenSec) = R;
176 - end
```

## 2B-1. Continued

- Once the chunks are in the matrices, it's time to take their FFT's
- The filter FFT is also recalculated with the length of one chunk (480020)

```
%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%%
```

```
%same as chunkV_r setup but for storing FFTs  
chunkV_r_fft = zeros(totChunks, length(chunkV_l(1,:)));  
chunkV_l_fft = chunkV_r_fft;
```

```
%get the frequency bins and store in another matrix
```

```
for i=1:totChunks  
    chunkV_l_fft(i,:) = fft(chunkV_l(i,:));  
    chunkV_r_fft(i,:) = fft(chunkV_r(i,:));  
end
```

```
%now resize the filter vector for each tensesec chunk
```

```
fft_f = fft(filter,length(chunkV_l_fft(1,:)));
```

chunkV_l	4x480020 double
chunkV_l_fft	4x480020 complex double
chunkV_r	4x480020 double
chunkV_r_fft	4x480020 complex double
fft_conv_l	1x1920020 double
fft_f	1x480020 complex double

## 2B.1 - Continued

- All FFT's have been calculated (L channel, R channel, filter),
- Now lets convolve each chunk with the filter
- After convolution, an inverse FFT is done on each resultant chunk for both channels.

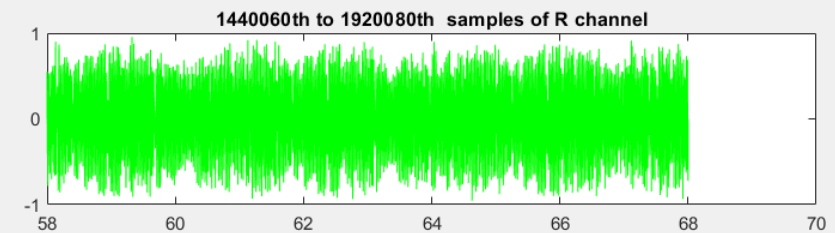
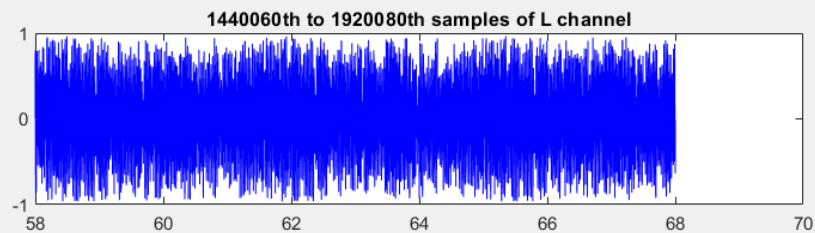
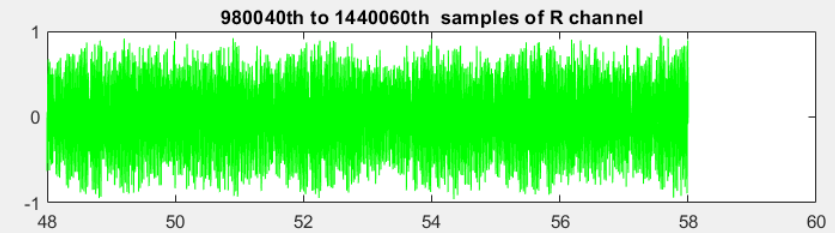
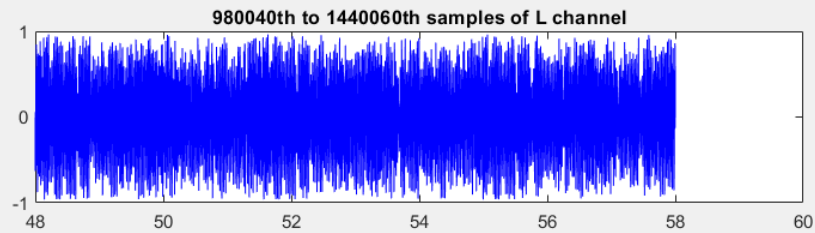
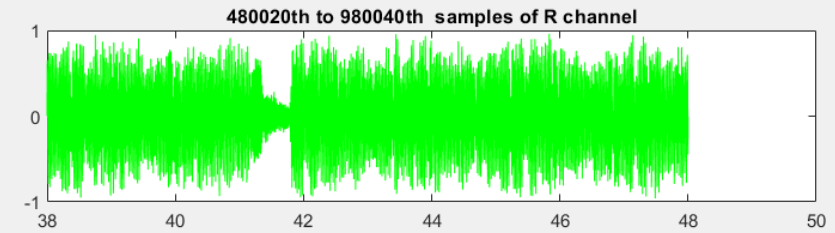
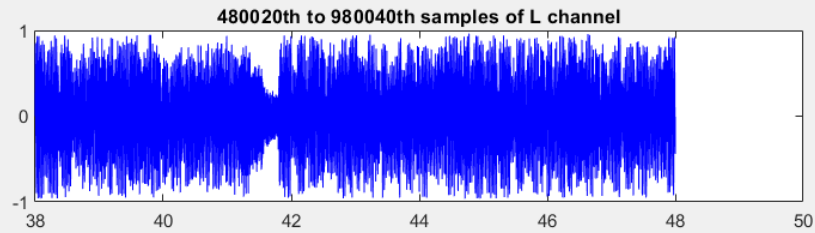
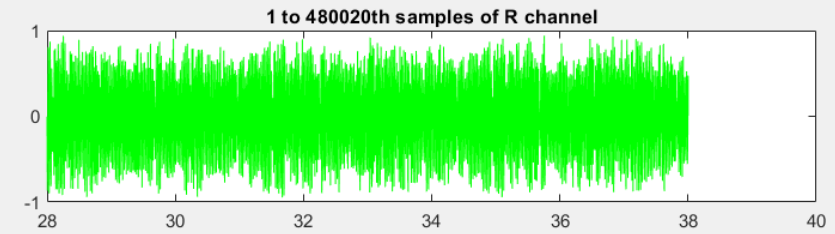
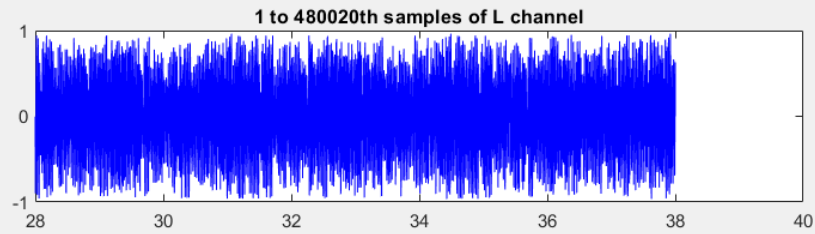
```
%now that both the filter and 10 sec chunk are the same size
%with zero padding, time to convolve!

%setup again matrices to store the convolutions
overlap_fft_l = zeros(totChunks, length(chunkV_l(1,:)));
overlap_fft_r = overlap_fft_l;

% F(signal)*F(filter) for each channel
for i=1:totChunks
    overlap_fft_l(i,:) = chunkV_l_fft(i,:) .* fft_f;
    overlap_fft_r(i,:) = chunkV_r_fft(i,:) .* fft_f;
end

%now time to go back to time domain to play the filtered song!
overlap_l = zeros(totChunks, length(chunkV_l(1,:)));
overlap_r = overlap_l;

%inverse fft for each chunk and store in l and r matrices
for i=1:totChunks
    overlap_l(i,:) = ifft( overlap_fft_l(i,:) );
    overlap_r(i,:) = ifft( overlap_fft_r(i,:) );
end
```



## 2B.1 – MATLAB Figures

# 2B.2 - Overlap New Signal from Chunks

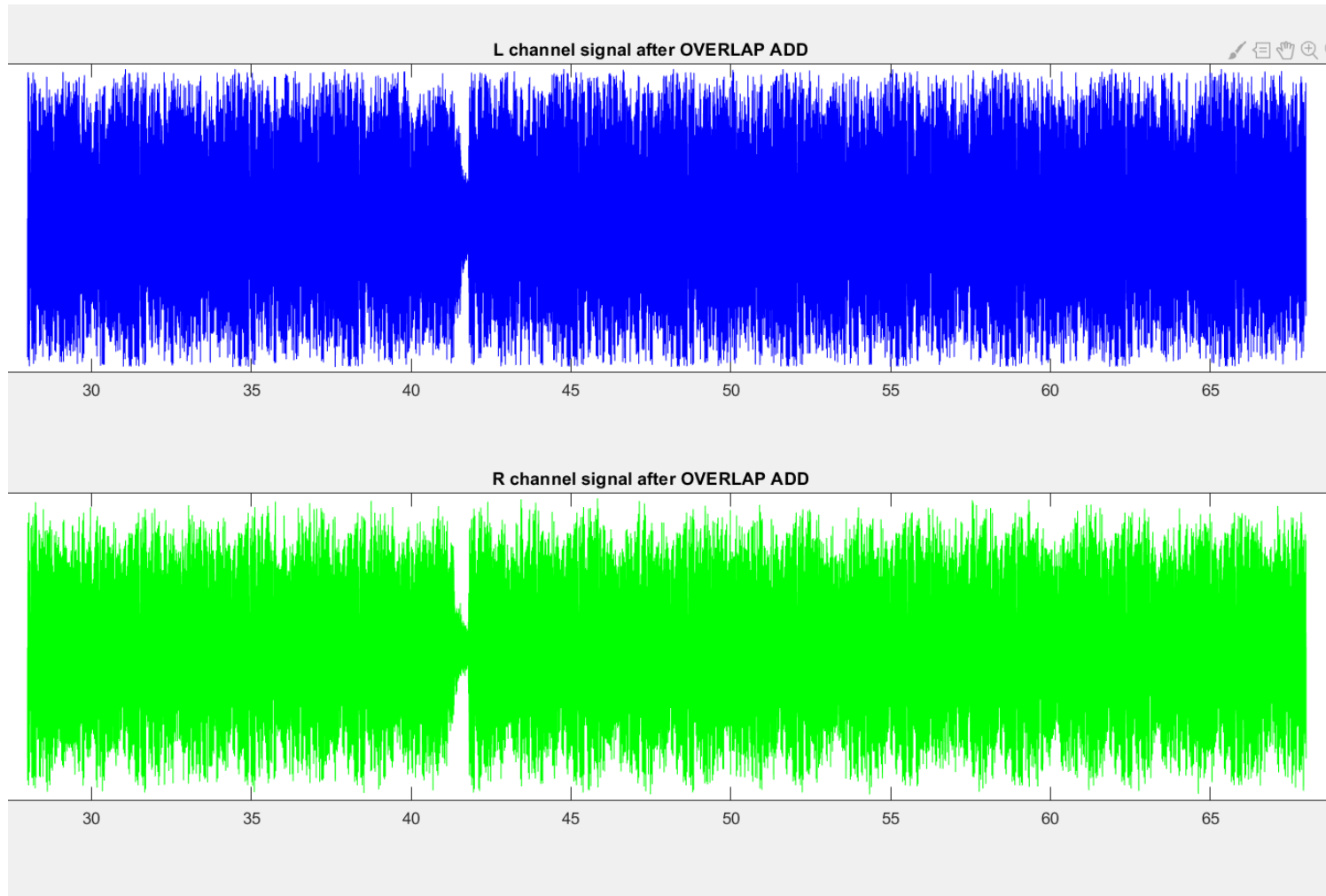
- Now that all FFTS are calculated, the next step is to overlap and add.
- Here, two vectors were created to store the final convolved signal in both L and R channels.
- The algorithm adds and overlaps to the vector chunk by chunk
- Total length is  $M + N - 1$  or 1920020

fft_conv_l	1x1920020 double
fft_conv_r	1x1920020 double

```
266 %setup final time domain vectors for each channel
267 - fft_conv_l = zeros(1, length(lchannel) + length(filter)-1);
268 - fft_conv_r = fft_conv_l;
269
270 - overlapLen = length(overlap_fft_l(1,:));
271
272 %now add and overlap
273 - for i=1:totChunks-1
274 -     if i==1
275 -         fft_conv_l(i:overlapLen) = overlap_l(i,:);
276 -         fft_conv_r(i:overlapLen) = overlap_r(i,:);
277 -     end
278
279 %here, each 10 sec chunk is being added and between 480000 and 480020,
280 %overlap is being added.
281 - fft_conv_l(i*tenSec:i*tenSec+overlapLen-1) = ...
282 -     fft_conv_l(i*tenSec:i*tenSec+overlapLen-1) ...
283 -     + overlap_l(i+1,:);
284
285 %do the same for the right channel
286 - fft_conv_r(i*tenSec:i*tenSec+overlapLen-1) = ...
287 -     fft_conv_r(i*tenSec:i*tenSec+overlapLen-1) ...
288 -     + overlap_r(i+1,:);
289 - end
290
```

## 2B.2 – MATLAB Figures

- Convolution is correct because there are no transients in the signal.





## 2B.2 Confirm with RMSR Error

- Here, the variables mean the following:
- "conv\_l" → FFT Convolution
- "fft\_conv\_l" → OVERLAP ADD METHOD

```
fx >> MSR error for Left Channel = 0.0000
MSR error for Right Channel = 0.0000
```

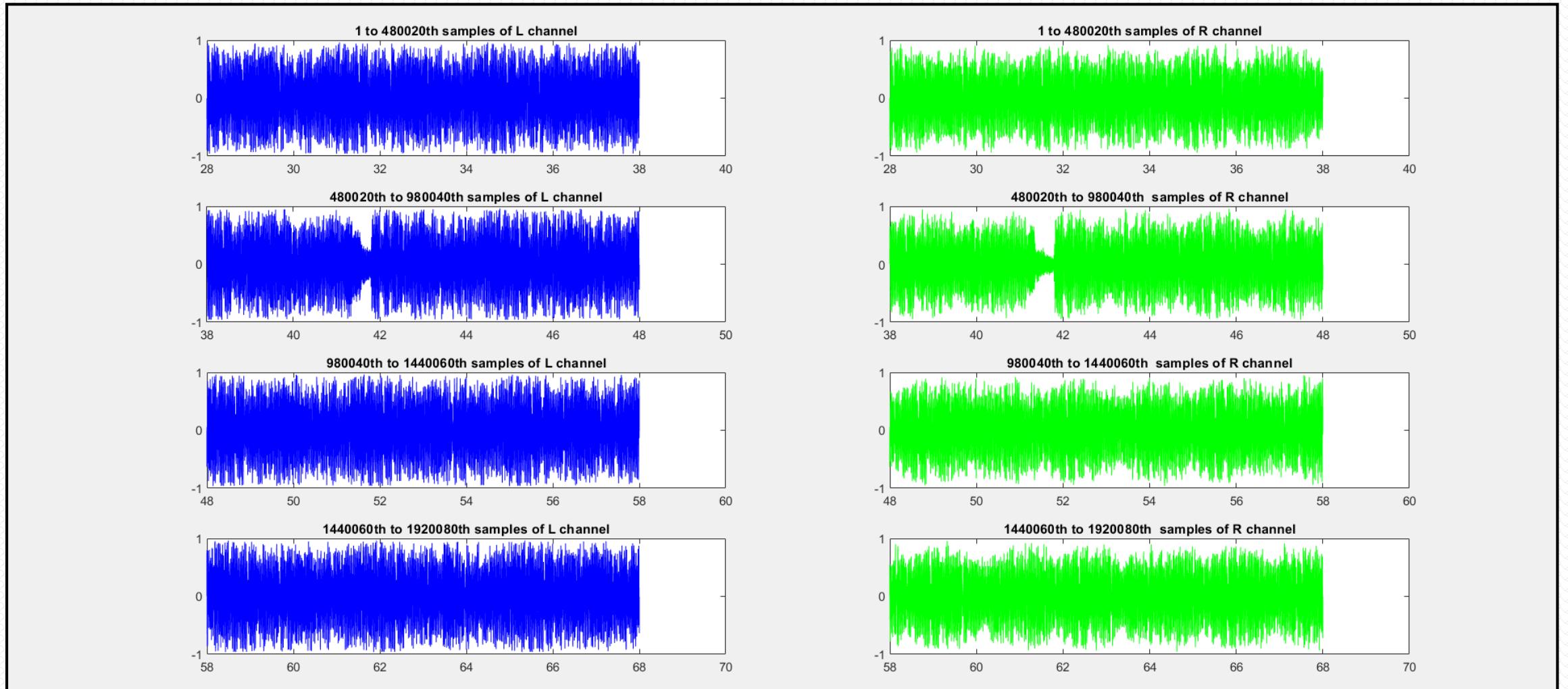
- VERY LOW RMSR!!!!

```
%calculate MSR error
MSR_L = sqrt(sum((conv_l - fft_conv_l).^2 )) / length(conv_l);
MSR_R = sqrt(sum((conv_r - fft_conv_r).^2 )) / length(conv_r);

fprintf(' MSR error for Left Channel = %6.4f \n',MSR_L);
fprintf(' MSR error for Right Channel = %6.4f \n',MSR_R);
```

# C – FFT Convolution

- This has been demonstrated in the previous slides so does not need further information



# Speed of Code

Elapsed time is 1.465537 seconds.  
Elapsed time is 0.482034 seconds.  
Elapsed time is 0.717119 seconds.  
Elapsed time is 0.070773 seconds.

1.465537 is for part A (direct calculation of convolution)

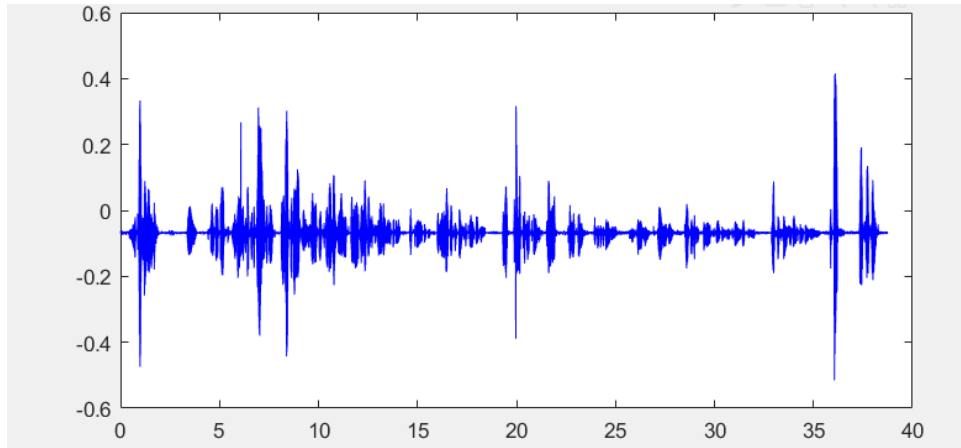
- 2 Channels of 1.92 Million samples each = 2.62 MSPS analyzed (double precision)

0.482034 is for part A (FFT convolution)

- Again 2 channels, plus same length filter (zero padded) = 5.76 Million samples = 11.949 GSPS!!!

0.717119 is for part B1 (FFT convolution of 8 chunks (4 per channel).

0.070773 is for part B2 (Custom overlap add algorithm)



Test RUN#2-  
Mike.wav  
signal

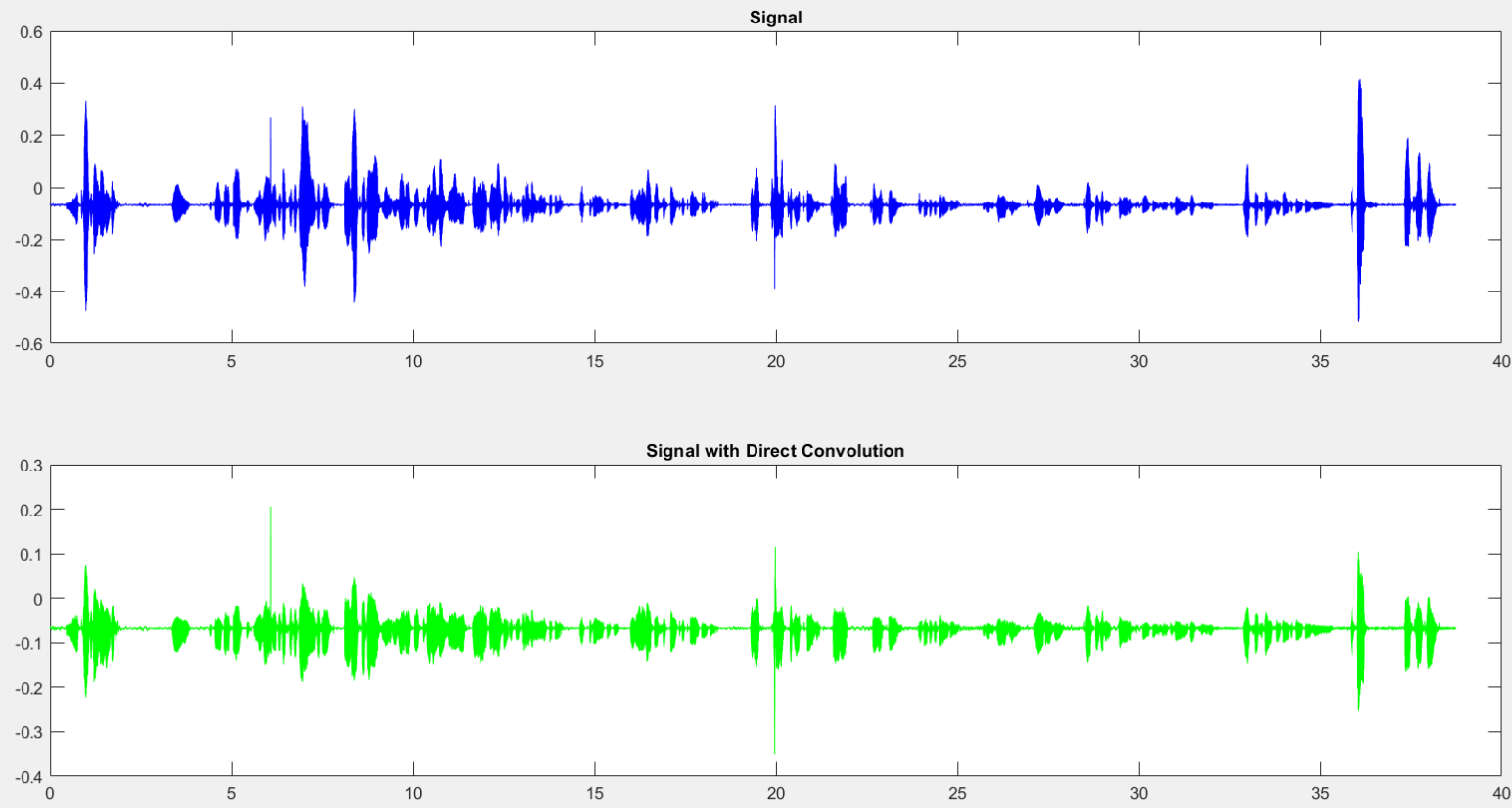
- Mike.wav signal was convolved with the following parameters:

```
%~~~~~CONFIG PARAMETERS~~~~~%  
  
duration = 40;      %how long should signal be (seconds)  
begin = 0;          %reference point to start (seconds)  
chunkSize = 10;     %how many seconds per chunk to do convolution  
filePath = "mike.wav"; %file path to .wav relative to home directory  
  
%~~~~~CONFIG PARAMETERS~~~~~%
```

PS: can change the Config parameters to display different convolutions

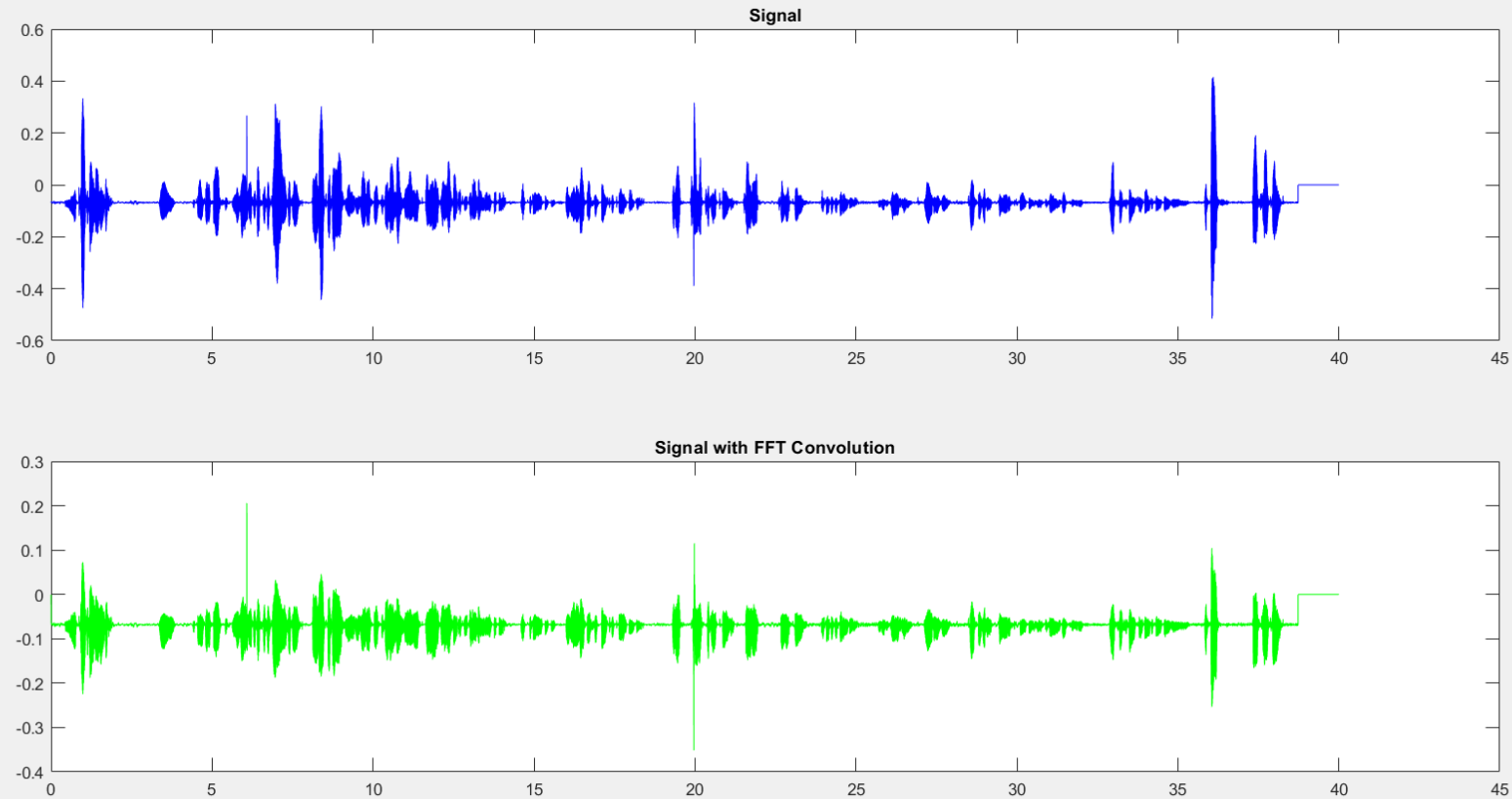
# 2A – Direct Convolution

- Basic for-loop method for this convolution



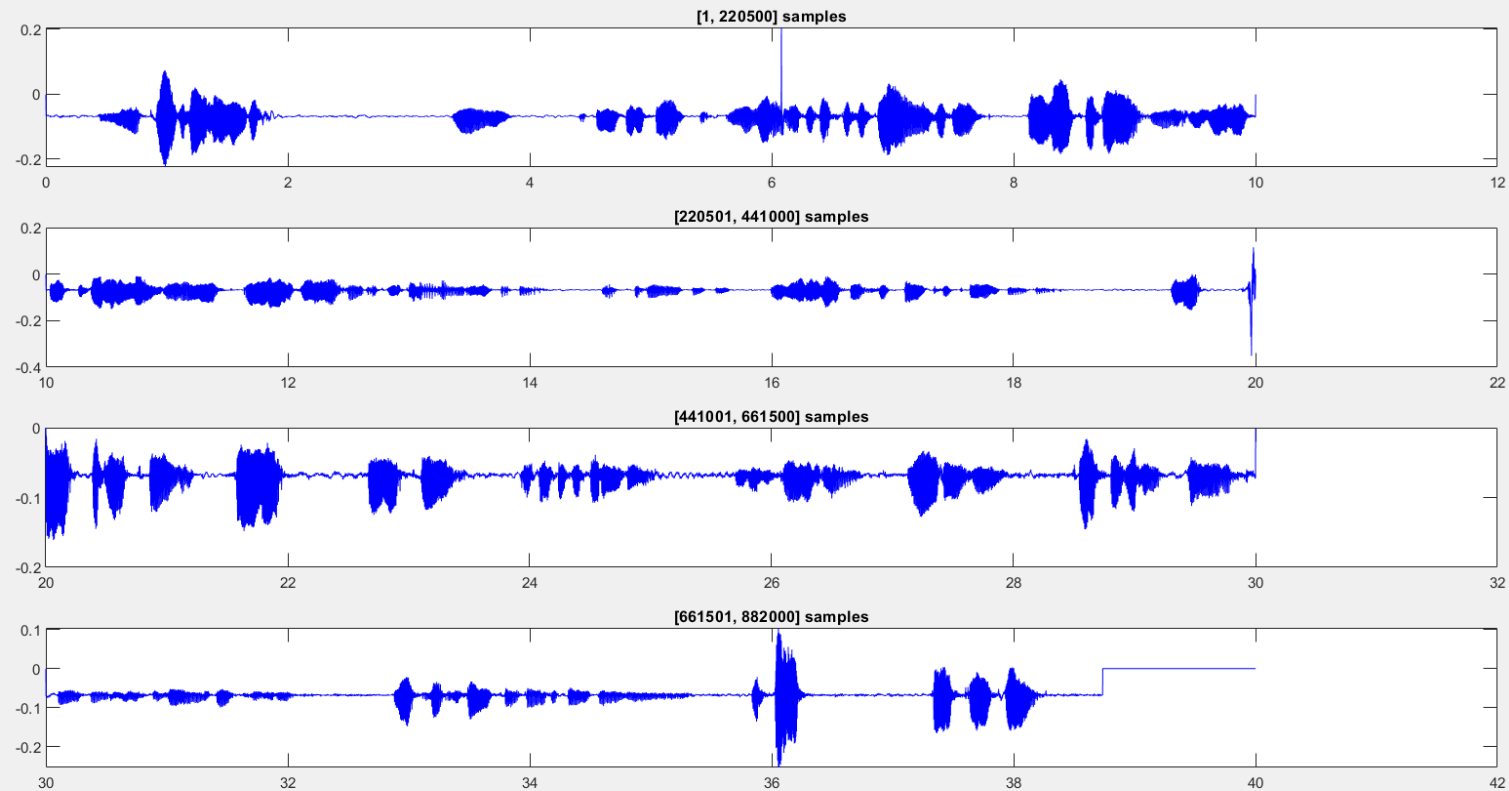
# 2A and C – FFT Convolution

- Used fft and ifft MATLAB functions



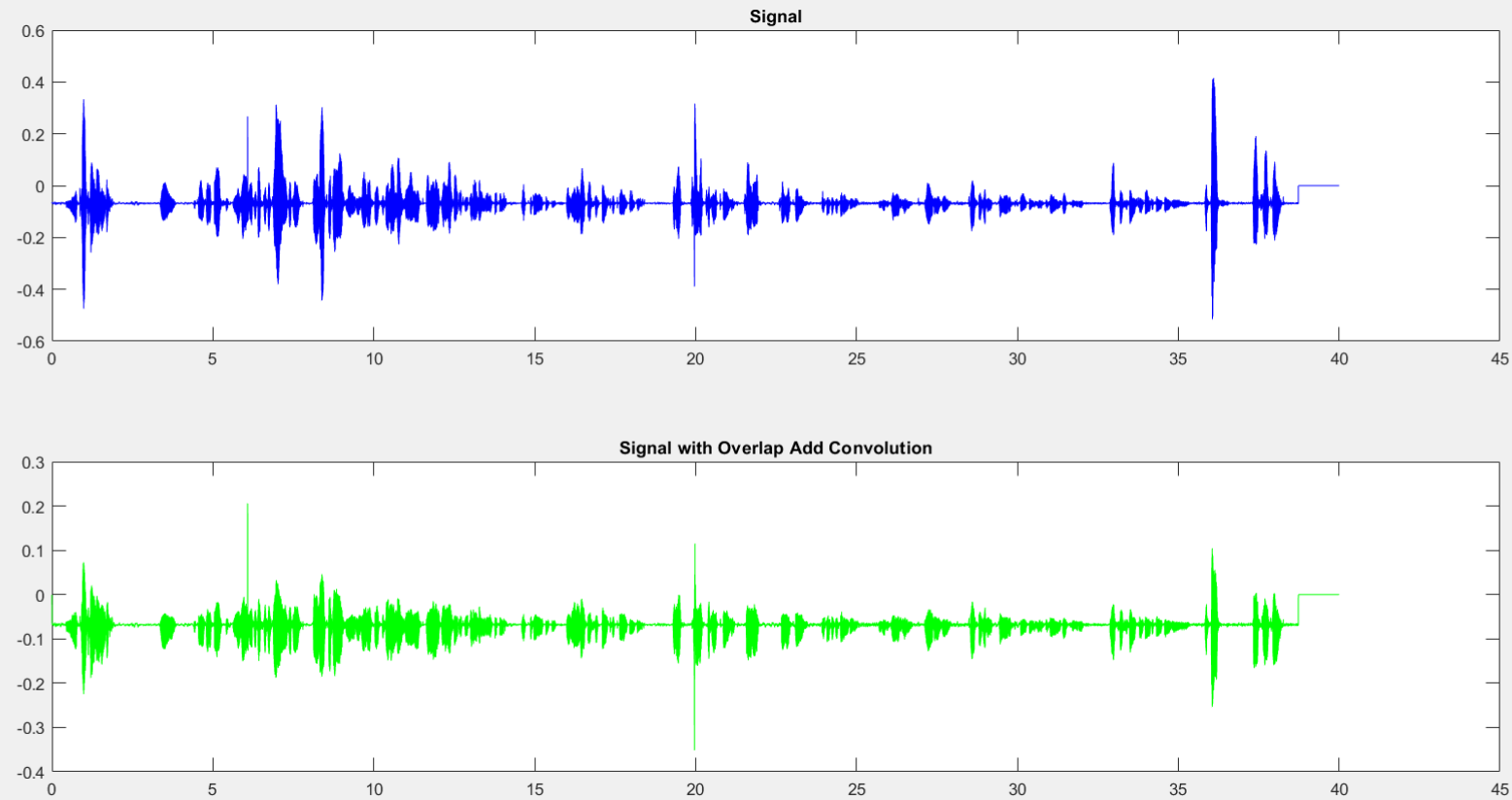
# 2B – Overlap-Add Convolution

- 4 chunks, with the last one being zero padded to fit a ten second chunk
- FFT and IFFT each 10 second chunk





## 2B – Overlapped Convolved Signal



# Conclusion - Performance

Direct Convolution

> Elapsed time is 0.673388 seconds.

FFT Convolution

> Elapsed time is 0.247151 seconds.

Overlap Add Convolution - Convolver each Chunk

> Elapsed time is 0.314171 seconds.

Overlap Add Convolution - Overlap and Add

> Elapsed time is 0.036498 seconds.

MSR error for Signal = 0.0000013919

- The figure on the left displays how many seconds each convolution took
- $MSR = 1.39 \times 10^{-6}$
- The bottom image displays the system specs which ran the code
  - Using an SSD for storage

[View basic information about your computer](#)

Windows edition

Windows 10 Home

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System

Processor: Intel(R) Core(TM) i5-7300HQ CPU @ 2.50GHz 2.50 GHz

Installed memory (RAM): 8.00 GB (7.87 GB usable)

System type: 64-bit Operating System, x64-based processor



# References

- Filter Design  
<http://t-filter.engineerjs.com/>
- Text on Figures  
<https://stackoverflow.com/questions/10525890/matlab-add-text-to-the-outside-of-figure>
- DSP Guide FFT Convolution  
<http://www.dspguide.com/ch18/2.htm>
- Class codes
- Dr. Grigoryan
  
- \*\*\*\*\*Can find all code on my [github.com/brunogracia](https://github.com/brunogracia)



**THANK YOU**